

# Higgs Theory

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Conveners:

(TH) Fabrizio Caola, Stephen Jones

# Outline

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## Overview

Truly impressive progress since last meeting

Pushing more channels one “N” higher

Increasingly, differential & fiducial predictions produced at high-orders

Very important progress understanding mixed EW-QCD, quark mass effects

## Selected Examples

$ggH$ : Fully differential + fiducial cross-section @ N<sup>3</sup>LO QCD, mixed QCD-EW, top-quark mass effects @ NNLO QCD

VBF: Les Houches 2019 study, non-factorisable contributions

$WH$  @ NNLO QCD with bottom-quark mass effects,  $WHj$  @ NNLO QCD

$b\bar{b}H$  @ N<sup>3</sup>LO QCD with 4FS/5FS matching

$Hb\bar{b}$  QCD + EW corrections

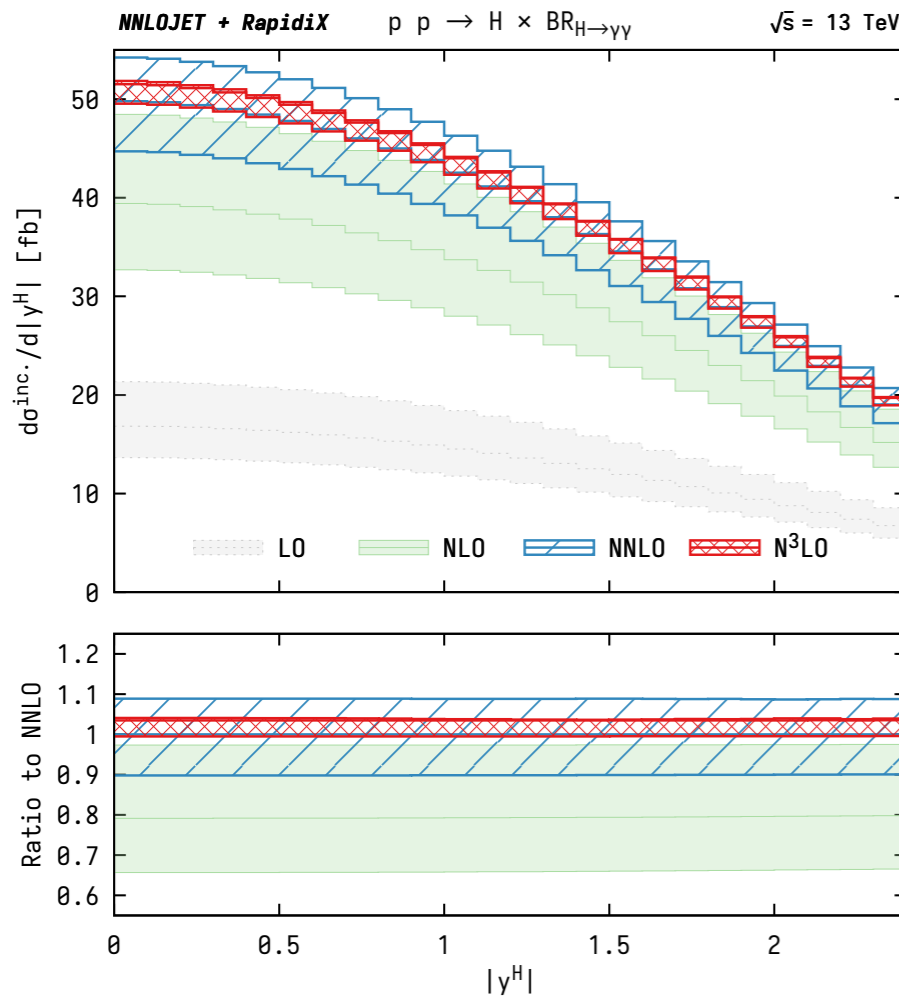
$t\bar{t}H$  off-diagonal channels @ NNLO QCD,  $tHj$  QCD + EW corrections

Progress in global EFT fits

**I had to make a very unfair selection and I skip several very interesting and important topics, please feel free to bring them up during questions/discussion!**

# ggF: N<sup>3</sup>LO Differential (Part 1)

## Inclusive

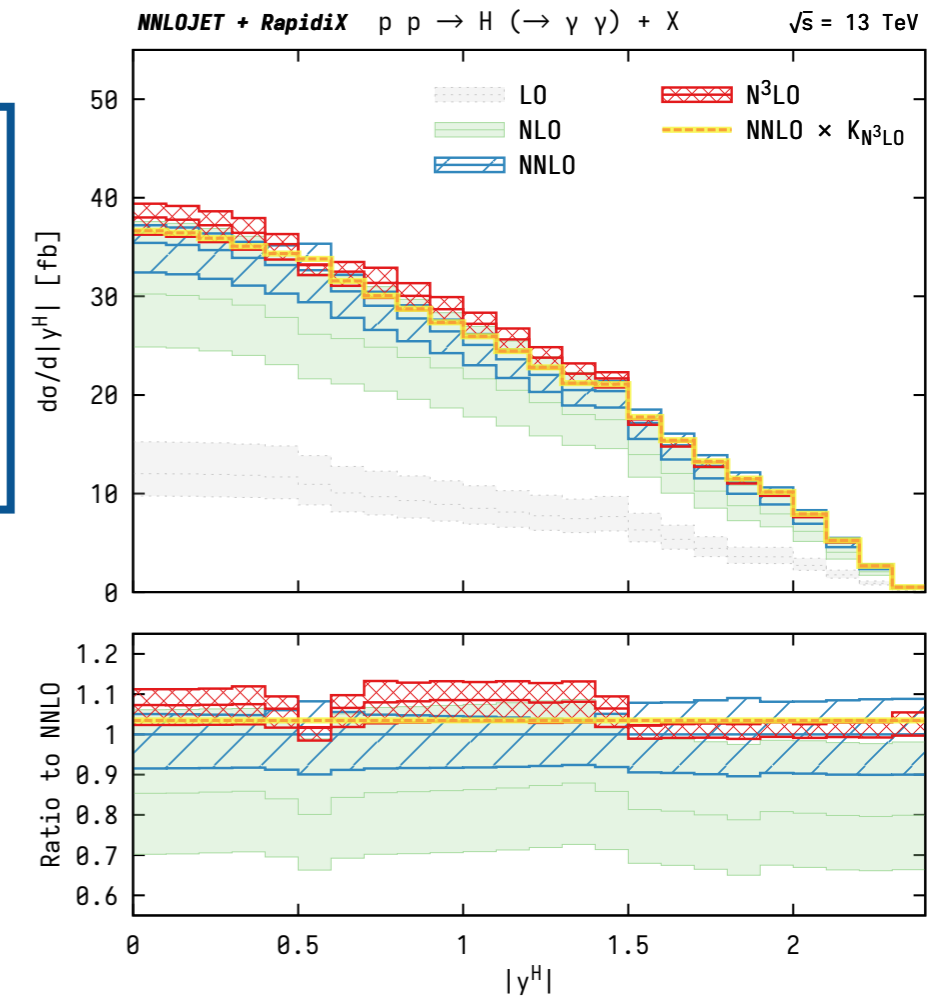


## ATLAS cuts

$p_T^{\gamma_1} > 0.35 m_{\gamma\gamma}$   
 $p_T^{\gamma_2} > 0.25 m_{\gamma\gamma}$   
 $|y^\gamma| < 2.37$   
 $1.37 < |y^\gamma| < 1.52$  (reject)  
 $\Delta R < 0.2$



## Fully Differential



Chen, Gehrmann, Glover, Huss, Mistlberger, Pelloni 21

Used projection-to-born method, presented:  $y^H, y^{\gamma_1}, \Delta y^{\gamma_1\gamma_2}$

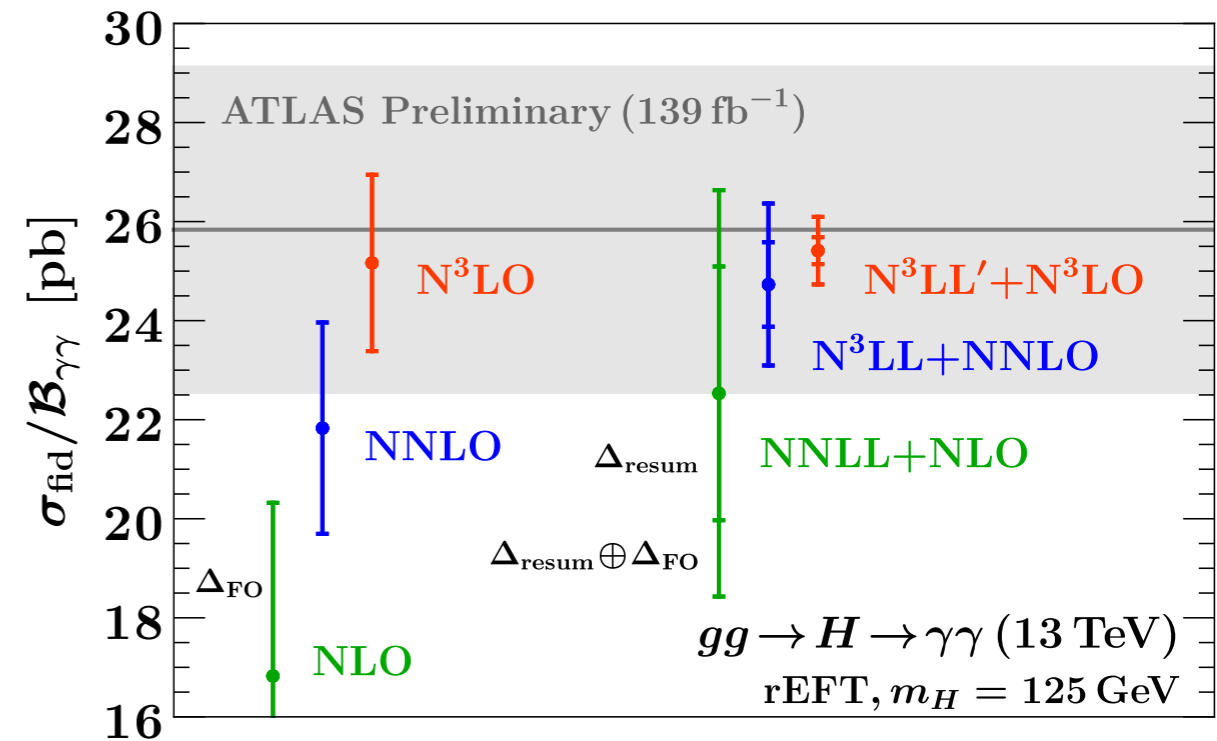
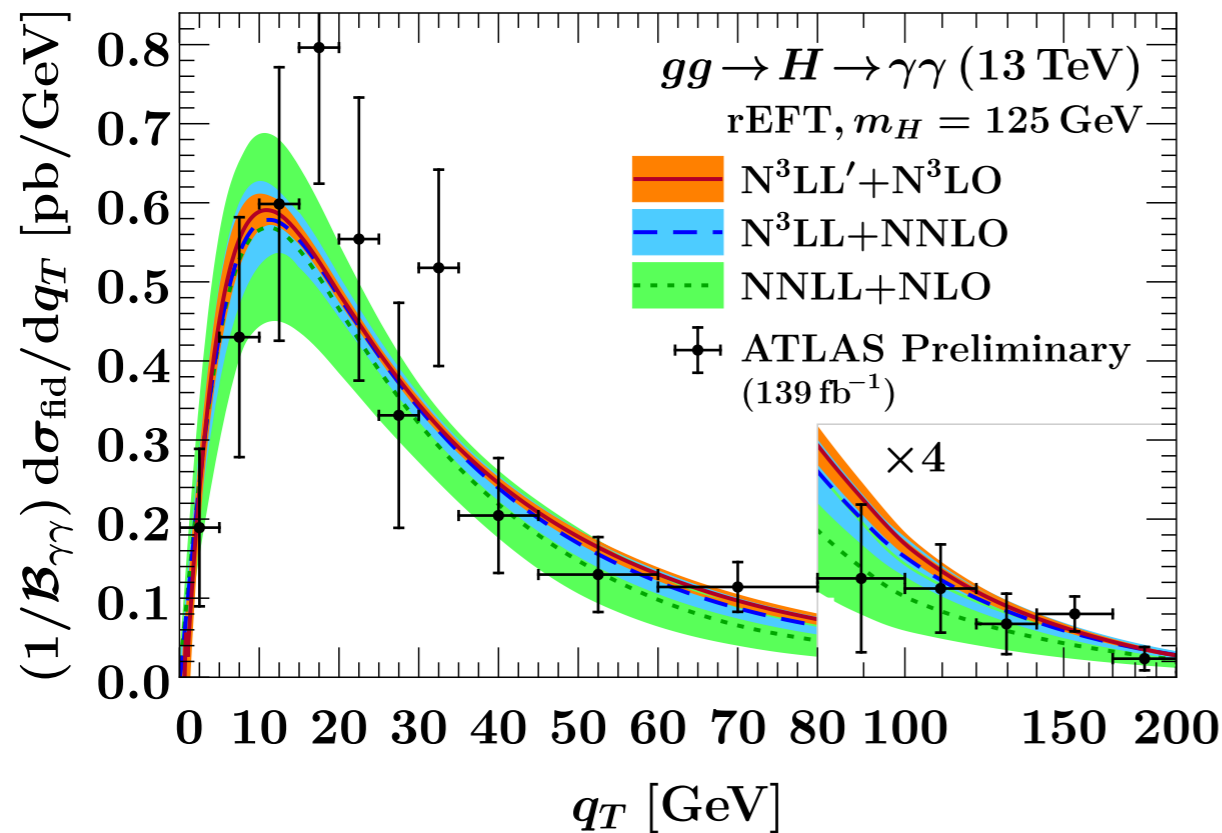
Perturbative expansion looks reasonable (reduced uncertainties, stable)

**Inclusive: remarkably flat K-factor (as expected)**

**Differential: naïve rescaling fails for  $|y^H| < 1.5$ , IR sensitivity @  $|y^H| \sim 0.5$**

# ggF: N<sup>3</sup>LO Differential (Part 2)

## With Fiducial Cuts



Billis, Dehnadi, Ebert, Michel, Tackmann 21

**Resummed large fiducial power corrections induced by fiducial cuts (even in  $\sigma_{\text{fid}}$ )**

$$\sigma_{\text{fid}} = 57.69 (1 \pm 2.7\%_{\text{pert}} \pm 2.1\%_{\text{BR}} \pm 3.2\%_{\text{PDF}+\alpha_s} \pm 2\%_{\text{EW}} \pm 2\%_{t,b,c}) \text{ fb}$$

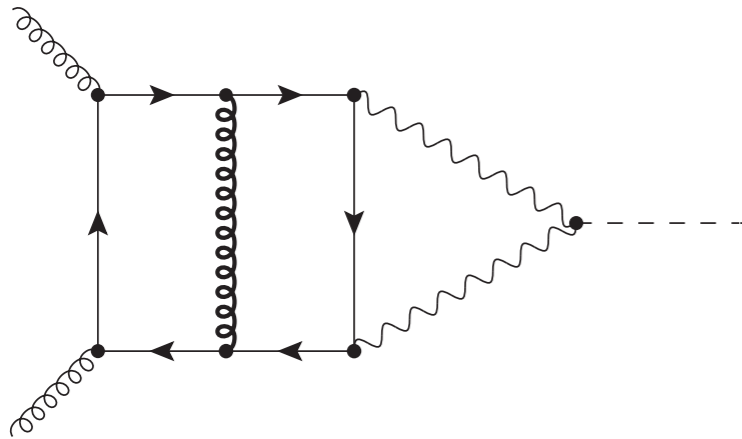
## Future:

Include fiducial power corrections also in  $y^H$ ,  $\Delta y^{\gamma_1\gamma_2}$ ? (J. Michel talk @ LHCP2021)

Explore different fiducial cuts which suppress these effects?



# ggF: Mixed QCD-EW Corrections

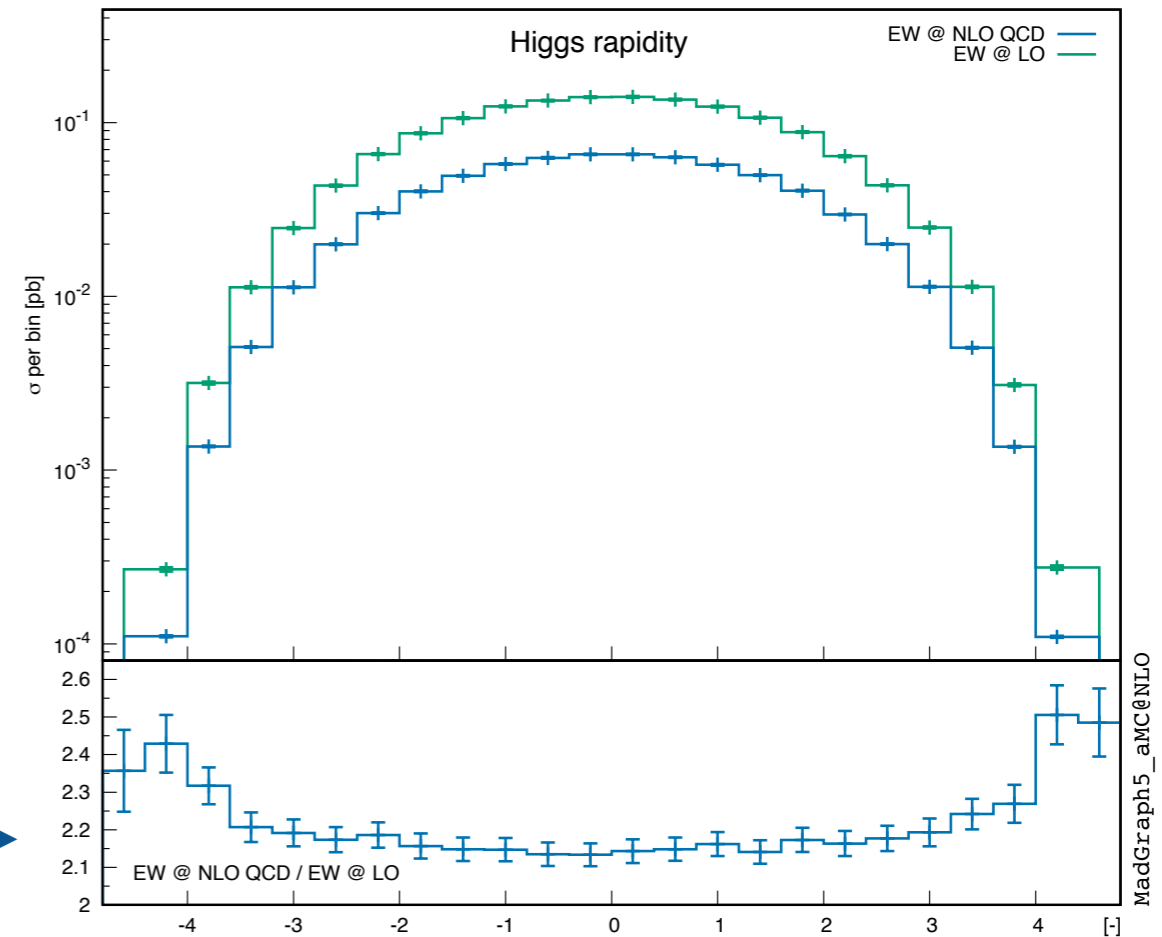


## Challenging computations

Bonetti, Melnikov, Tancredi 17

Bonetti, Panzer, Smirnov, Tancredi 20

Dominant light-quark contributions computed, rather flat K-factor (at least for rapidity distribution)



Becchetti, Bonciani, Del Duca, Hirschi, Moriello, Schweitzer 20

Increases  $\sigma_{\text{tot}}$  by +5.1 % , reduces residual uncertainty  $\delta(\text{EW}) \sim 0.6 \%$

Favouring factorisation of EW corrections:  $\sigma = \sigma_{\text{LO}} (1 + \delta_{\text{QCD}}) \times (1 + \delta_{\text{EWK}})$

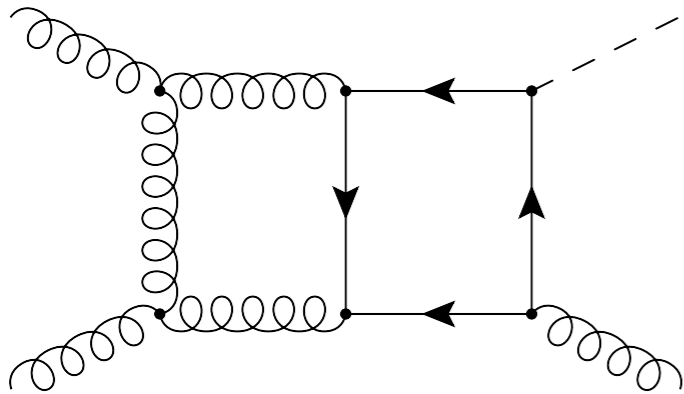
Compatible with previous estimates e.g. Bonetti, et al. 18; Anastasiou et al. 18, Anastasiou, et al. 08

## Future:

Corrections at large  $p_T$ ? Without heavy top-quark approximation?

LO and NLO quark-induced EW contribution

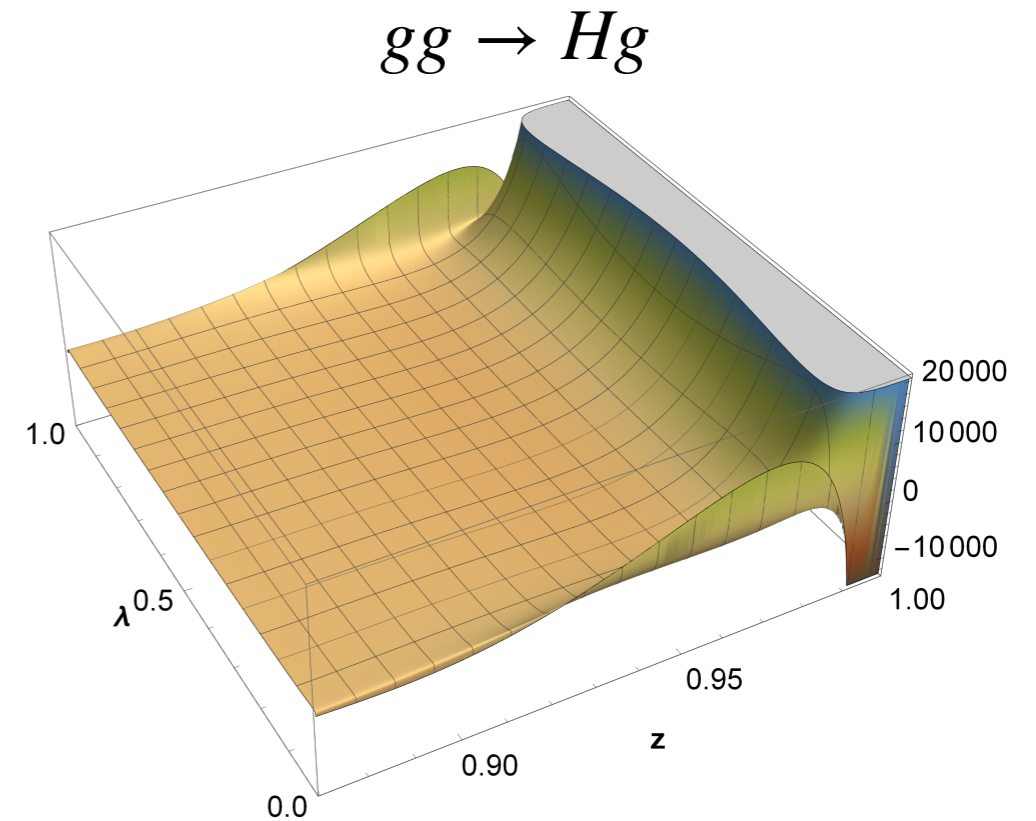
# ggF: NNLO with full top-quark mass



H+1jet @ 2-loop & H @ 3-loop  
using numerical solution of  
differential equations

Czakon, Niggetiedt 20;

Czakon, Harlander, Klappert, Niggetiedt 21



Czakon, Harlander, Klappert, Niggetiedt 21

Decreases  $\sigma_{\text{tot}}$  by  $-0.26\%$

Intricate interplay between mass effects:  $gg$  ( $+0.62\%$ ),  $qg$  ( $-16\%$ ),  $qq$  ( $-15\%$ )

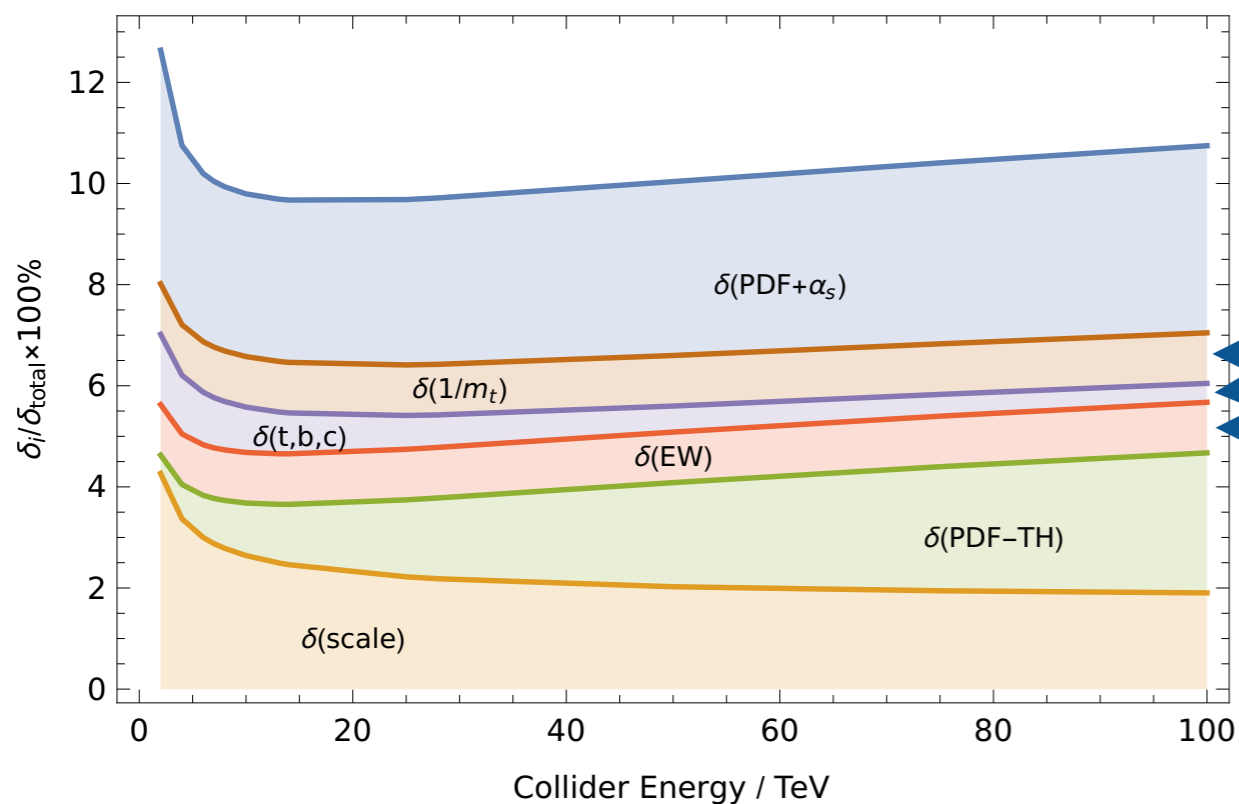
Complete NNLO results obtained using STRIPPER framework

## Future:

Use technology to include light quark mass effects (large logs/need to resum?)

Impact on differential distributions/ fiducial cross sections

# ggF: Taking Stock



Progress is steadily beating down sources of TH uncertainty

Czakon, Harlander, Klappert, Niggetiedt 21

Becchetti, Bonciani, Del

Duca, Hirschi, Moriello, Schweitzer 20; + Bonetti,

Panzer, Smirnov, Tancredi, Melnikov, ...

iHixs2: Dulat, Lazopoulos, Mistlberger 18

Also exposing new sources of uncertainty/ areas where we can do better:

Fiducial power corrections (covered previously)

Next-to-leading power corrections @ threshold

Beneke, Garny, Jaskiewicz, Szafron, Vernazza, Wang 19;

van Beekveld, Laenen, Sinninghe Damsté, Vernazza 21;

## The precision era mantra:

TH: Do we miss sources of uncertainty? (PDF MHOU, Schemes, NLP, ...)

EXP: Do we use the most accurate results? (PS validation, Match/ Merge)

Elephant in the room PDF (+PDF TH) uncertainties

# VBF: LH2019 Study

Extensive study of VBF (started at LH2019) published!

Buckley, Chen, Cruz-Martinez, Ferrario Ravasio, Gehrmann, Glover, Höche, Huss, Huston, Lindert, Plätzer, Schönherr 21

Input from NNLOjet, POWHEG, Herwig, Sherpa

**Important work getting a handle on this:**

NLOPS vs NNLO

Detailed PS comparisons

Additive/Multiplicative matching

Jet-radius dependence

High- $p_{T,H}$  region

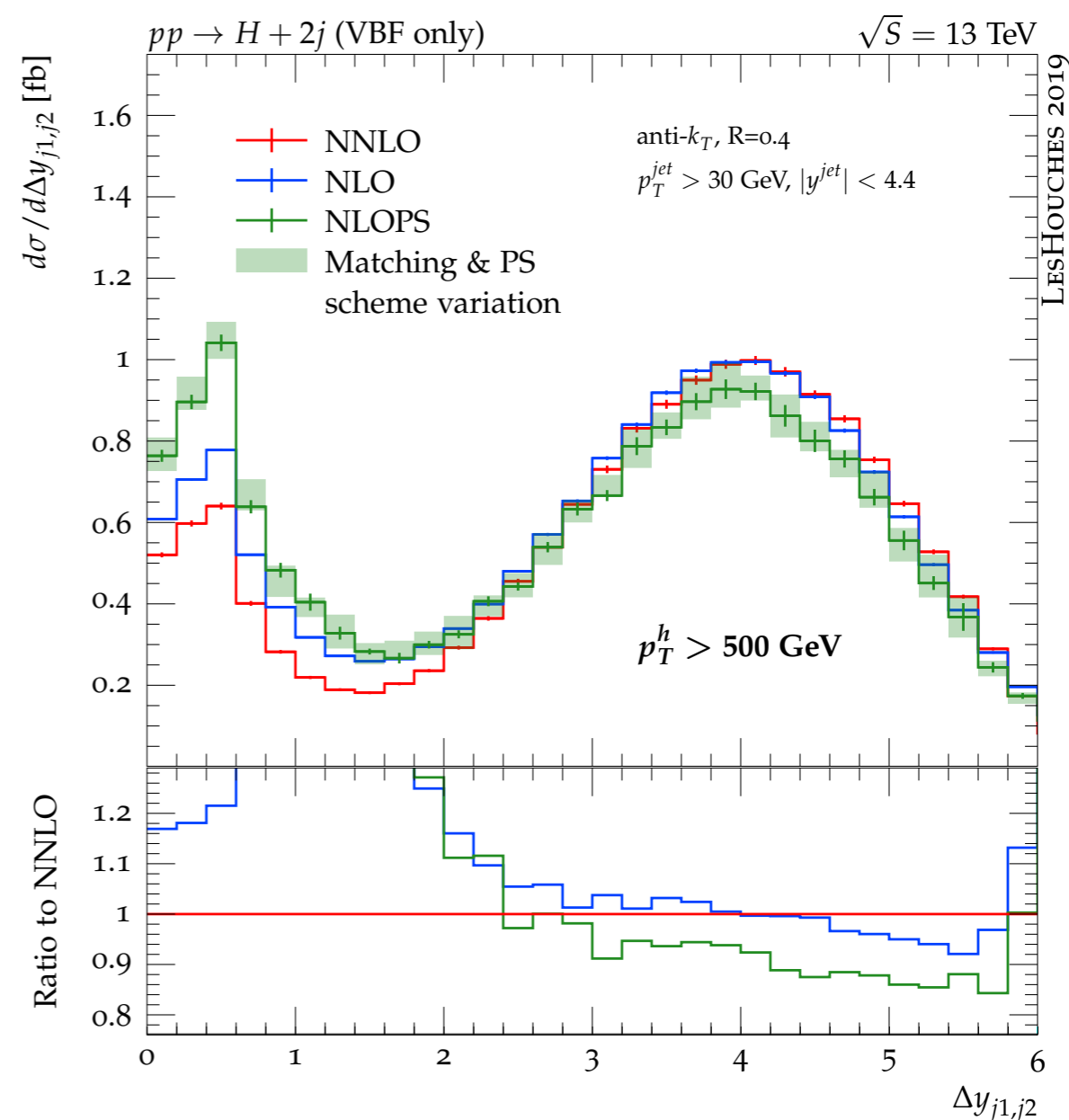
**Many Lessons:**

At large  $p_{T,H}$  disentangling VH/VBF more difficult

Mostly(!) reasonable NNLO vs NLOPS

EW  $H + 2 \text{ jet} \approx \text{VBF} + \text{VH}$

...



# VBF ( $H \rightarrow ZZ$ ): NLO QCD + EW

Process  $pp \rightarrow e^+e^-\mu^+\mu^-jj + X$  at  $\mathcal{O}(\alpha^7)$  and  $\mathcal{O}(\alpha_s\alpha^6)$

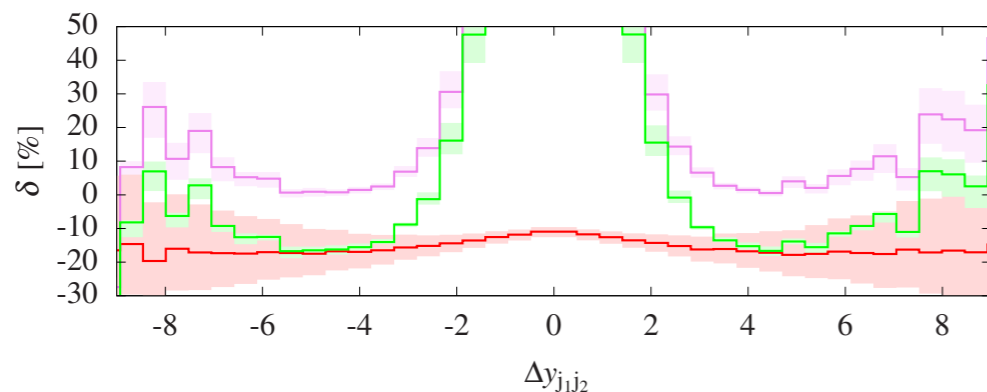
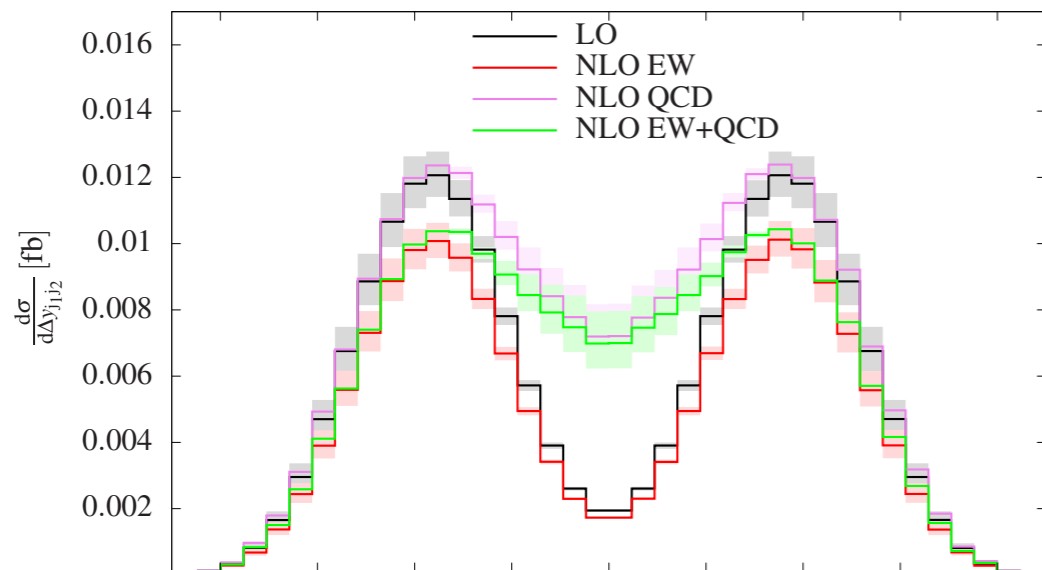
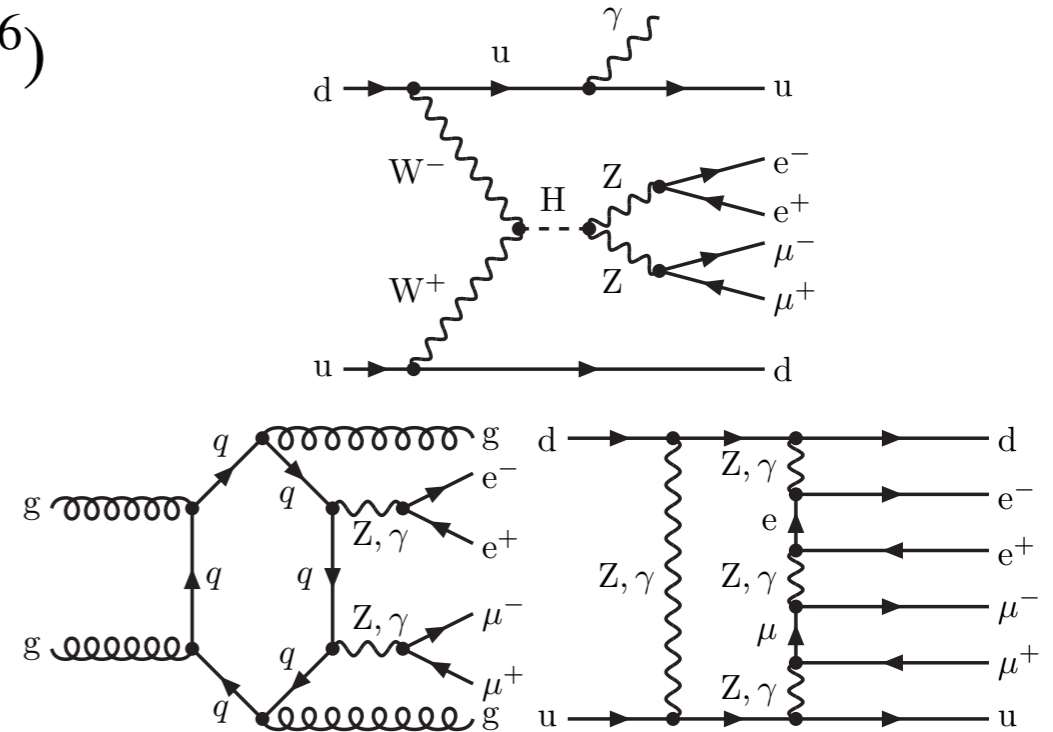
Denner, Franken, Pellen, Schmidt 20

Includes all off-shell, non-resonant & interf. effects

Decreases  $\sigma_{\text{fid}}$  by  $-16\%$ , mostly due to EW

Sudakov logs:  $\ln^2(Q^2/M_W^2)$ ,  $\ln(Q^2/M_W^2)$

EW corrections can reach  $-40\%$  at high energy



## Lessons:

Authors advocate proper inclusion of tri-boson contributions, not subtracting from signal

Care when using MC relying on VBS to extrapolate inclusive measurements

# VBF $HH$ : Non-factorisable contribution

VBF Approximation/structure function approach:  
neglect the (colour suppressed) exchange of  
particles between the quark lines

Non-factorisable contributions recently studied  
using the eikonal approximation

Liu, Melnikov, Penin 19

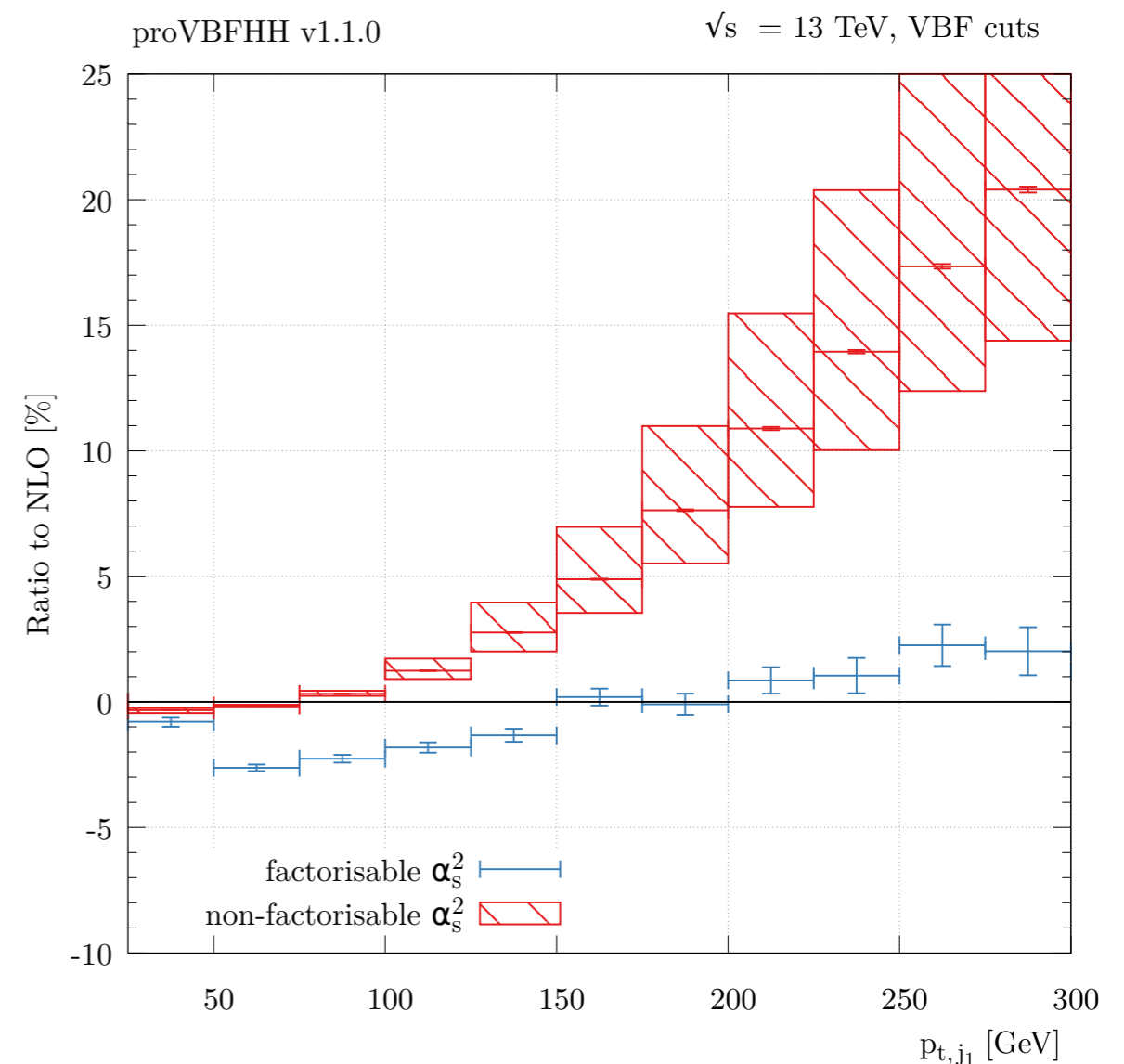
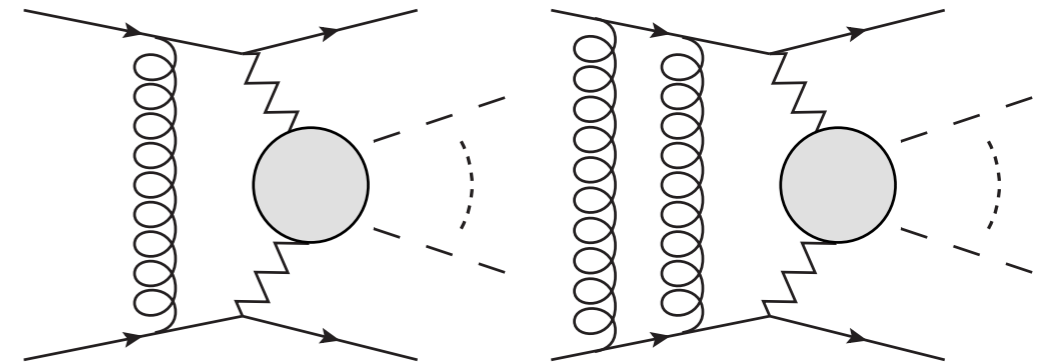
Dreyer, Karlberg, Tancredi 20

**H - Small corrections, but shape can differ  
from structure function approximation**

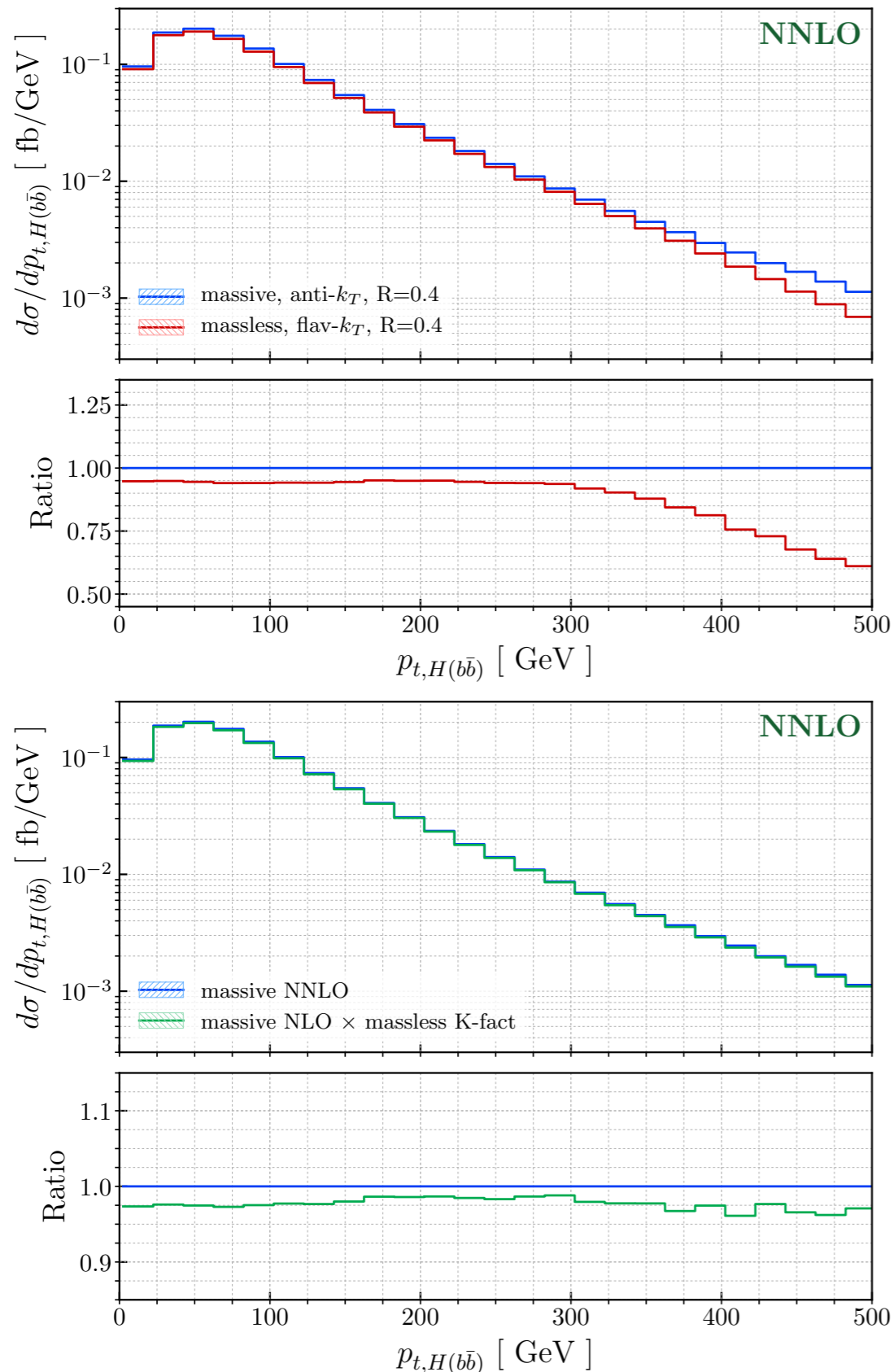
**HH - Delicate cancellations between  
diagrams spoiled, giving rise to a large  
corrections**

$$d\sigma_{HH,nf}^{NNLO} \sim \tilde{\alpha}_s^2 \left[ \left(1 - \frac{\pi^2}{3}\right) (d\sigma_{TT}^{LO} + d\sigma_{TB}^{LO}) + \left(\frac{5}{4} - \frac{\pi^2}{3}\right) d\sigma_{BB}^{LO} \right].$$

(As pointed out by authors) Eikonal  
approximation not trustworthy for too high  $p_{t,j}$



# VH: NNLO WH with b mass effects



$WH$  production with  $H \rightarrow b\bar{b}$  now known at NNLO QCD including bottom mass effects  
Behring, Bizon, Caola, Melnikov, Röntsch 20

Allows application of realistic jet algorithms for  $b$  jets (important for TH vs EXP)

Including  $b$  mass increases  $\sigma_{\text{tot}}$  by +6.3 %  
(+7.7 % for boosted  $\sigma_{\text{fid}}$ )

Rescaling massive NLO works for some distributions ( e.g.  $p_{t,H(b\bar{b})}$  but not  $m_{H(b\bar{b})}$  )

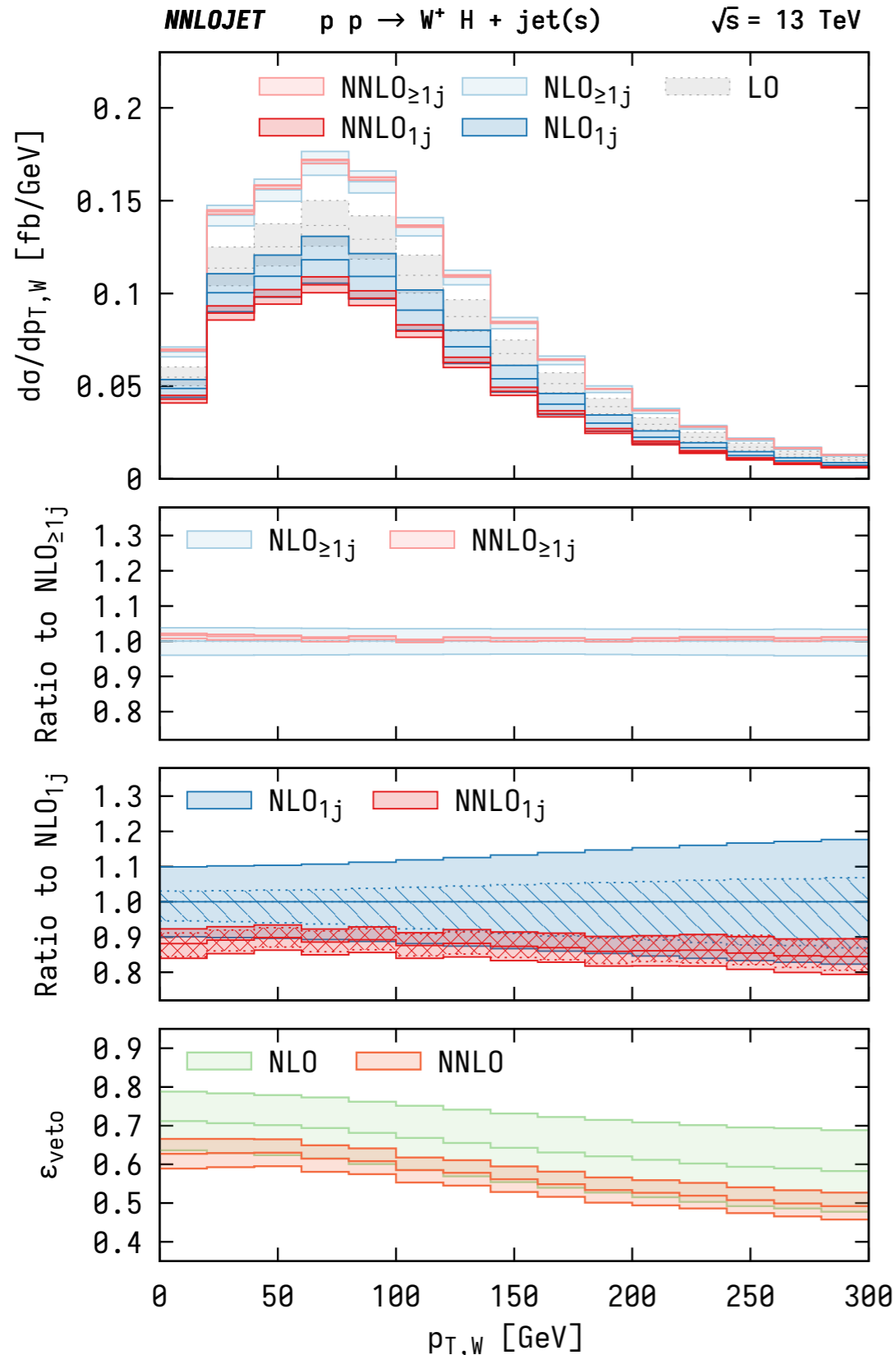
**New paper today:**

Anomalous couplings in  $WH$  and  $ZH$  @ NNLO QCD with massive  $b$  quarks

Bizon, Caola, Melnikov, Röntsch 21



# VHj: NNLO WH + jet(s)



NNLO QCD including Drell-Yan type and top-loop induced contributions

Gauld, Gehrmann-De Ridder, Glover, Huss, Majer 20

Flat K-factors  $\sim 1$  for inclusive jet production

Corrections  $\mathcal{O}(-10\%)$  for exclusive jet production (residual TH uncertainty  $\mathcal{O}(5\%)$ )

NLO/NNLO predictions consistent only when **uncorrelated** prescription for evaluating TH uncertainty is used

$$\sigma_{1j} \equiv \sigma_{\geq 1j} - \sigma_{\geq 2j}, \quad \Delta_{1j}^2 = \Delta_{\geq 1j}^2 + \Delta_{\geq 2j}^2$$

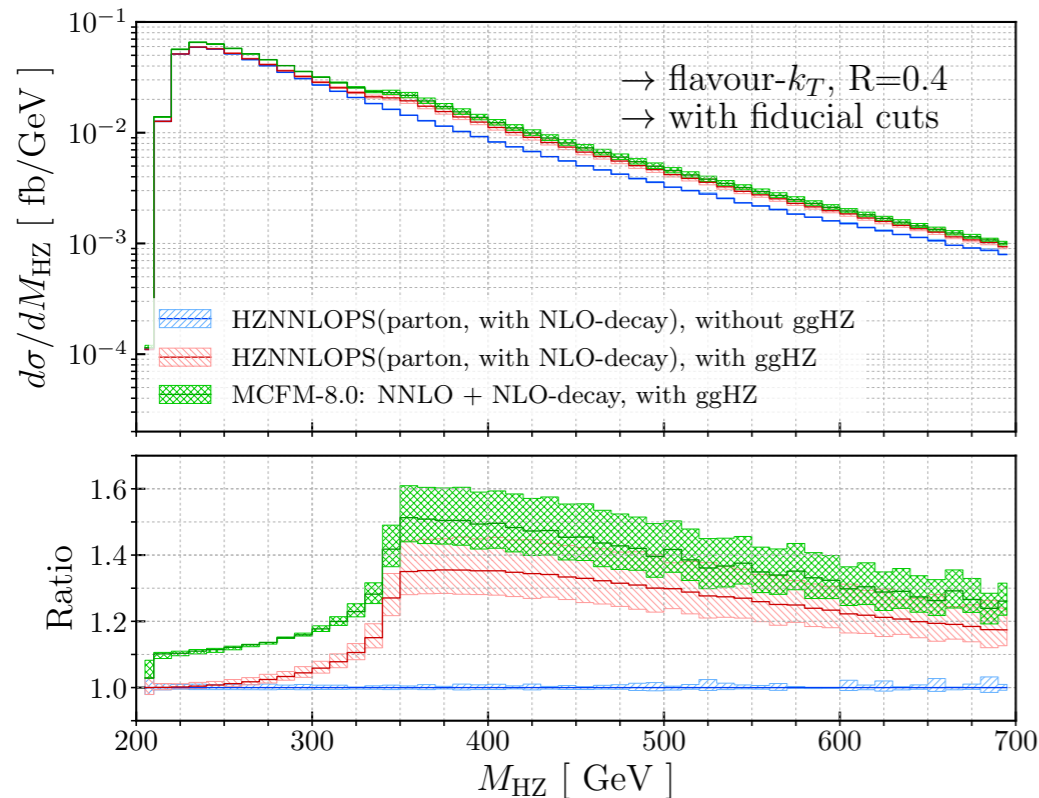
Stewart, Tackmann 11

**Future:**

What should we be doing with b-jets in general? Want a procedure close to EXP but which we can handle theoretically (correct treatment of  $g \rightarrow b\bar{b}$ )

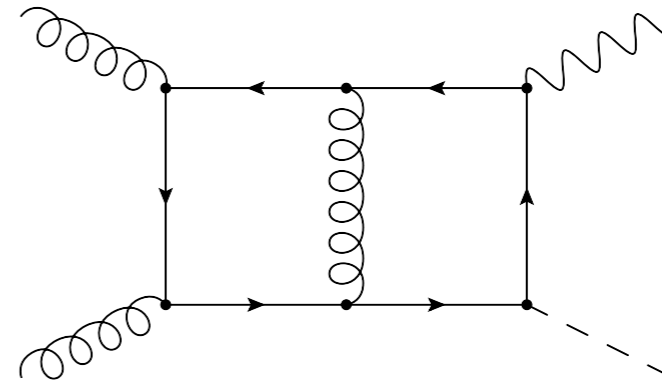


# ZH/ZZ/WW: Gluon fusion virtuals



Astill, Bizon, Re, Zanderighi 18

Sizeable impact of  $gg \rightarrow ZH$  above top-quark threshold, desirable to have to NLO



TH progress: virtuals complete

Davies, Mishima, Steinhauser 20;

Chen, Heinrich, Jones, Kerner, Klappert, Schlenk 20;

Virtuals complete also for  $gg \rightarrow WW$  and  $gg \rightarrow ZZ$

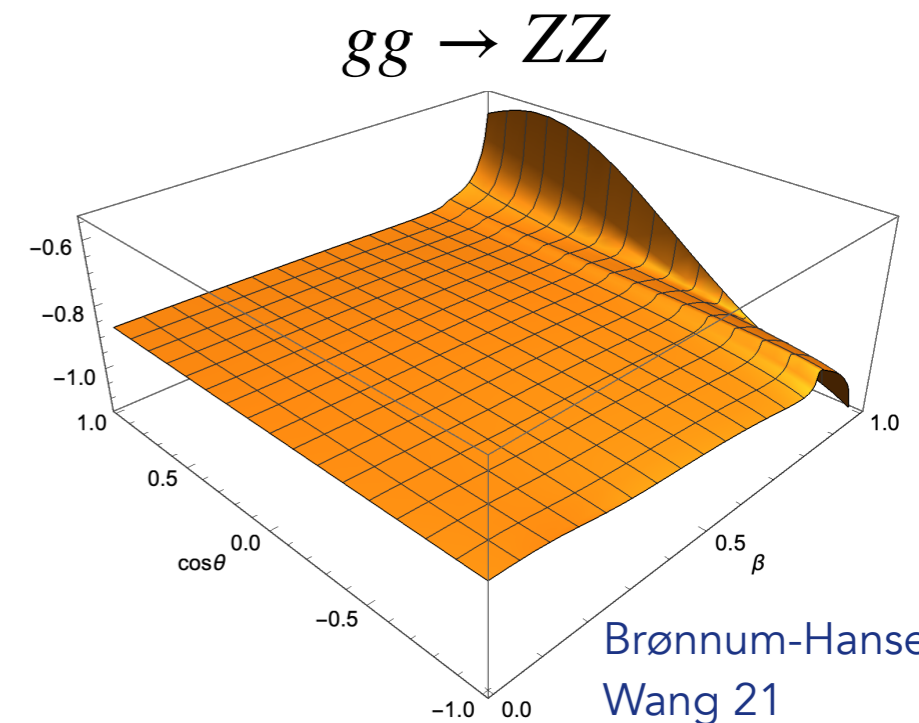
Davies, Mishima, Steinhauser, Wellmann 20; Brønnum-Hansen, Wang 20, 21;

Agarwal, Jones, von Manteuffel 20;

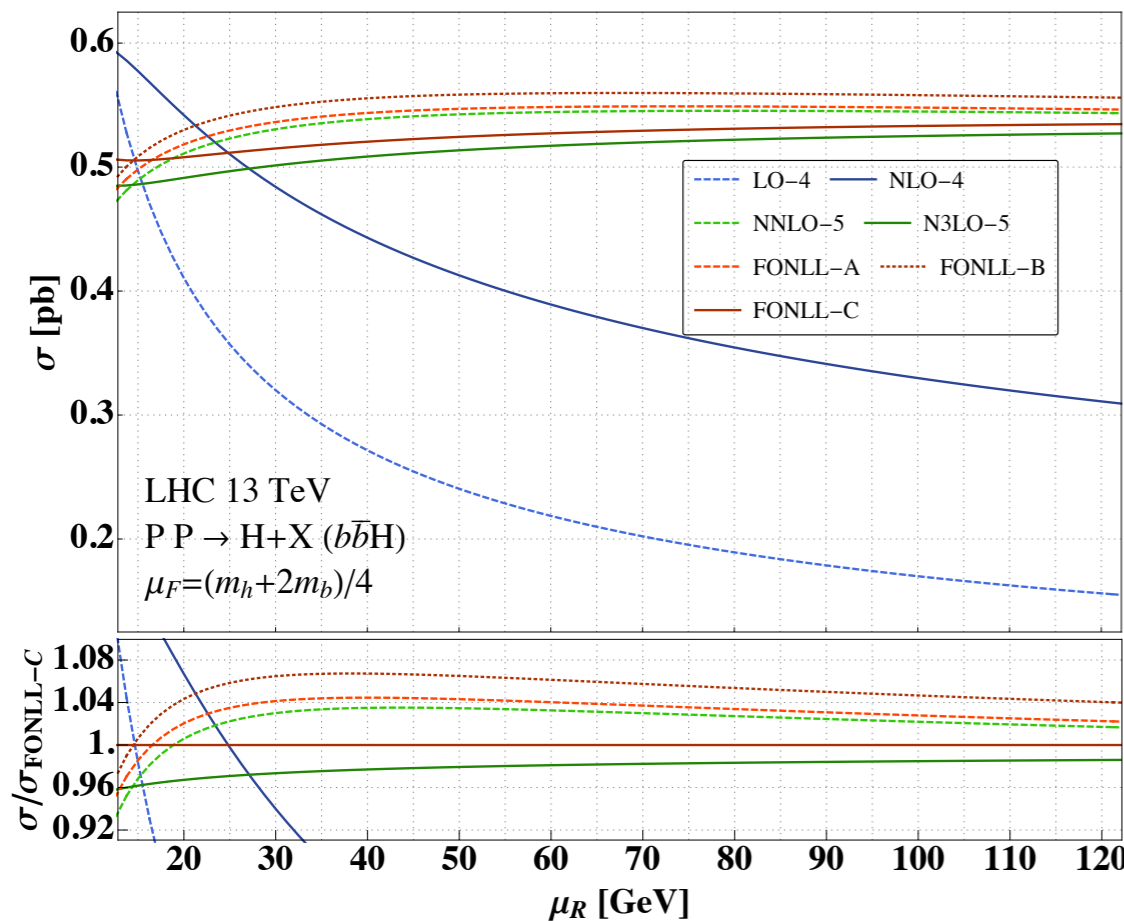
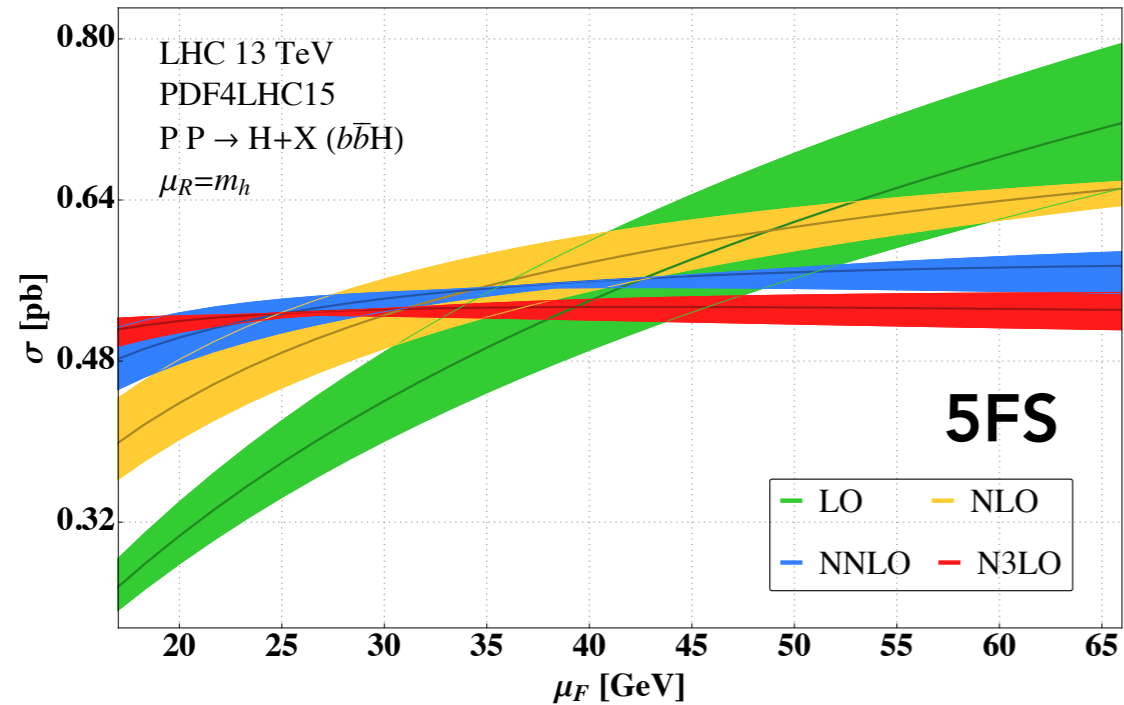
## Future:

Interesting to see impact of these corrections above/around top-quark

Must not forget mass-scheme uncertainty



# $b\bar{b} \rightarrow H$ : N<sup>3</sup>LO QCD



N<sup>3</sup>LO QCD corrections to  $b\bar{b} \rightarrow H$

Duhr, Dulat, Hirschi, Mistlberger 20

Supports choice of a rather small value for  $\mu_F$

Examined 3 matching procedures for 4FS/5FS

$$\sigma^{\text{matched}} = \sigma^{(4)} + \sigma^{(5)} - \sigma^{(4-5)}$$

**FONLL-A:** All ingredients  $\mathcal{O}(\alpha_s^2)$

NNLO 5FS matched to LO 4FS

**FONLL-B:** All ingredients  $\mathcal{O}(\alpha_s^3)$  except parts of  $\sigma^{(5)}$  with a b-quark in the initial state, kept to  $\mathcal{O}(\alpha_s^2)$

Retains NLO accuracy of 4FS

**FONLL-C:** All ingredients  $\mathcal{O}(\alpha_s^3)$

N<sup>3</sup>LO 5FS matched to NLO 4FS

Matching increases  $\sigma_{\text{tot}}$  by +2%

New  $b$ -initiated channels give a **large negative** contribution

**Questions:** Anything general to learn about 4FS/5FS from this?

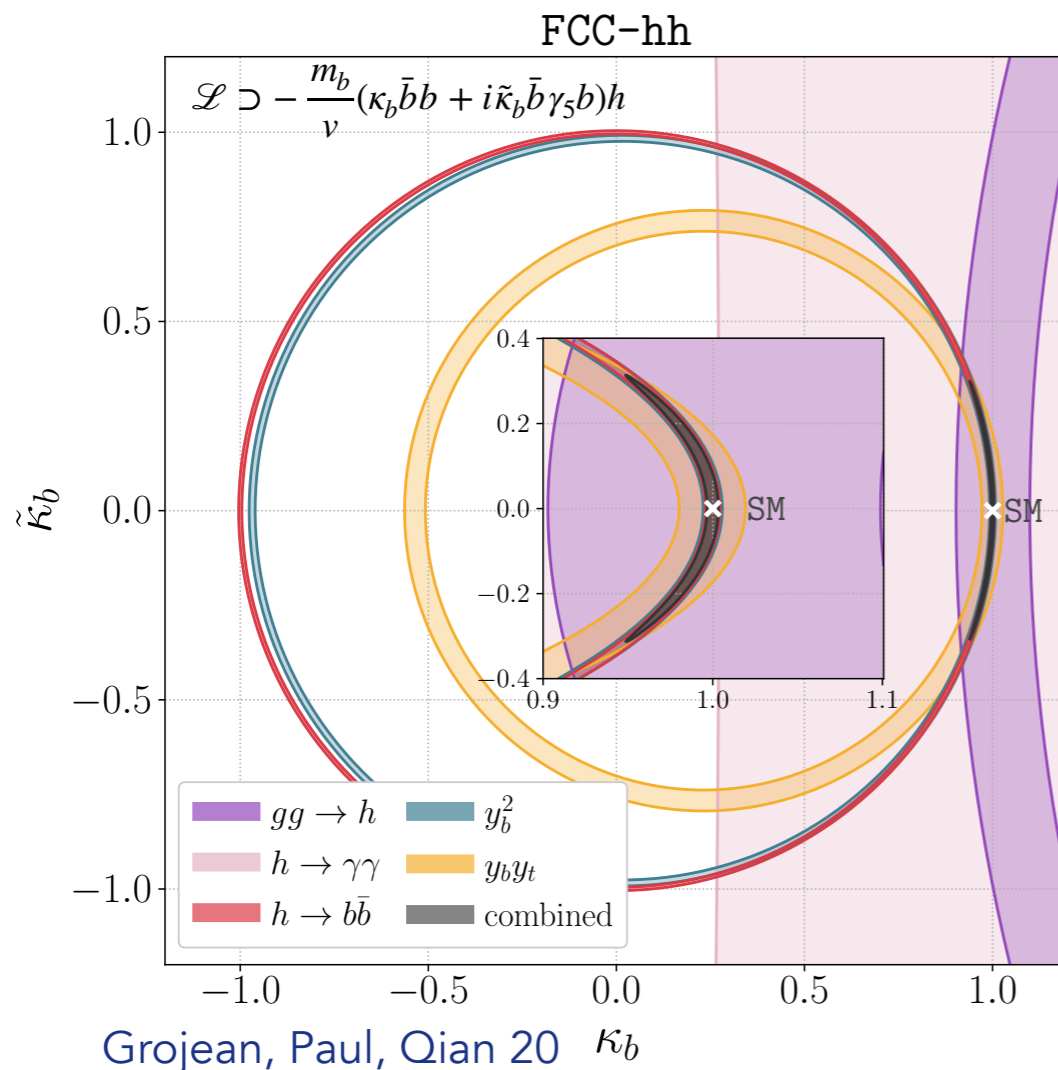
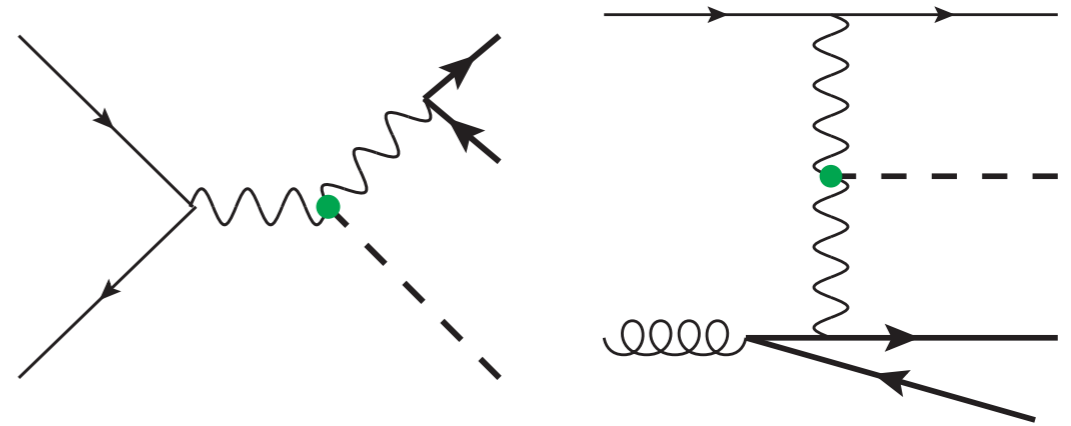
# RIP $Hb\bar{b}$ ?

$Hb\bar{b}$  studied accounting for all 1-loop and real-emission corrections of QCD and EW origin

$\mathcal{O}(\alpha_s^m \alpha^{n+1})$  with  $m + n = 2, 3$

**Challenging** to extract genuine  $y_b^2$  signal due to huge  $ZH$ , VBF backgrounds (even differentially)

Pagani, Shao, Zaro 20



But BDTs can still separate the hidden signal?

Grojean, Paul, Qian 20

Authors applied a variety of techniques: interpretable machine learning, kinematic shapes, Shapley values,...

Still @ HL-LHC  $h \rightarrow b\bar{b}$ ,  $gg \rightarrow h$  very constraining  
@ FCC-hh  $Hb\bar{b}$  improves bounds on phase by 15 %

**Future:**

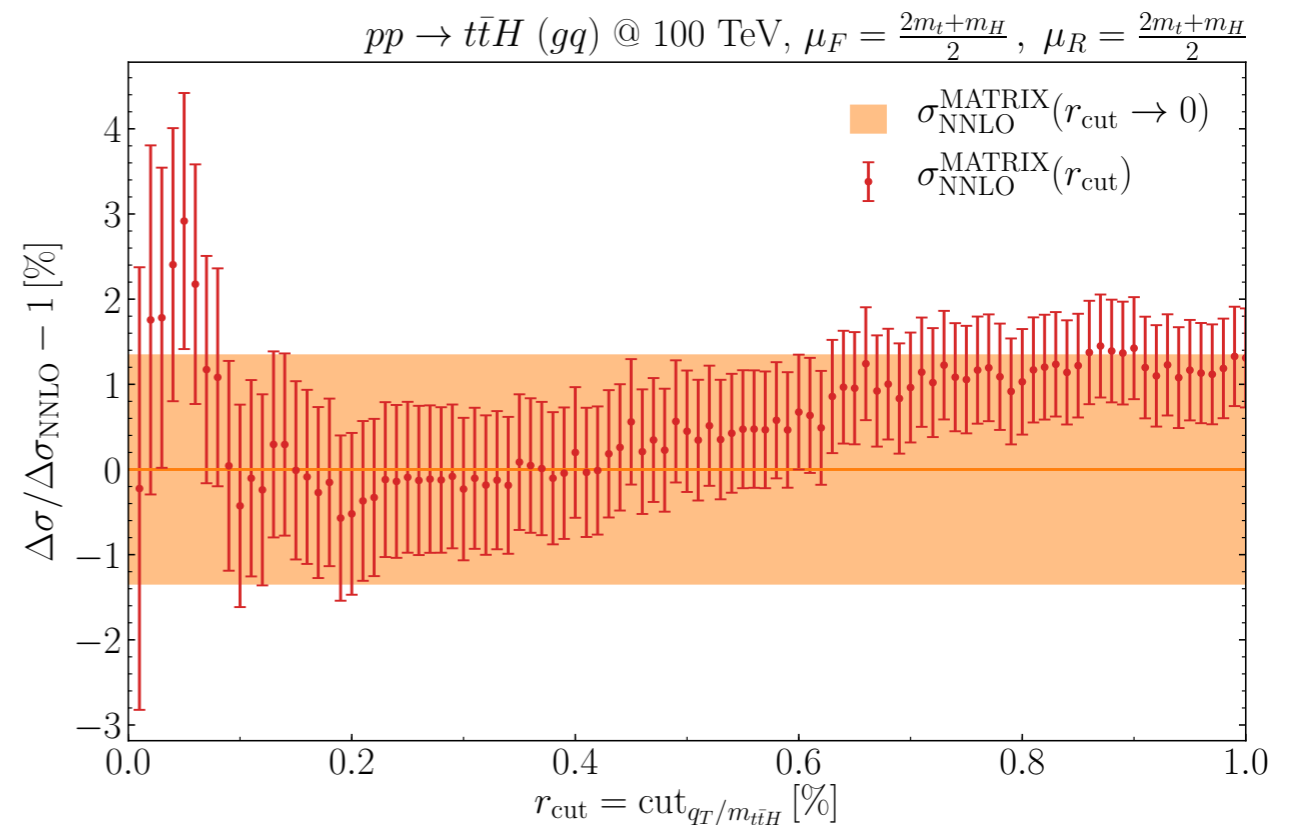
Clearly a challenging measurement

A good testing ground for separating S/B

# $t\bar{t}H$ : NNLO QCD Off-Diagonal Contributions

$ab \rightarrow t\bar{t}H + X$ , off-diagonal contributions  
 $(qg, qq, qq', q\bar{q}' \ (q \neq q'))$  obtained @ NNLO  
 Catani, Fabre, Grazzini, Kallweit 21

**Fully differential** results obtained using the  $q_T$  subtraction method, can be applied generally to  $Q\bar{Q}F$  (where  $F$  is a colourless final state system)



$\sigma$ [fb]	13 TeV	100 TeV
LO	394.987(3)	28228.2(2)
NLO (MADGRAPH5_AMC@NLO)	499.76(4)	36948(3)
NLO (MATRIX)	499.73(1)	36947(1)
NLO ( $q_T$ )	499.79(4)	36947(3)
$\mathcal{O}(\alpha_S^4)_{qg}$	-0.796(27)	214.7(2.9)
$\mathcal{O}(\alpha_S^4)_{q(\bar{q})q'}$	0.62694(82)	95.307(56)

No big surprises,  $\mathcal{O}(\alpha_s^4)$  contribution of off-diagonal channels found to contribute at few per mille level

## Future:

Clearly, interesting to see the impact of diagonal channels @ NNLO

**New paper today:** Higgs-boson production in top-quark fragmentation, can obtain top-quark/Higgs boson mass dependence from massless calculations

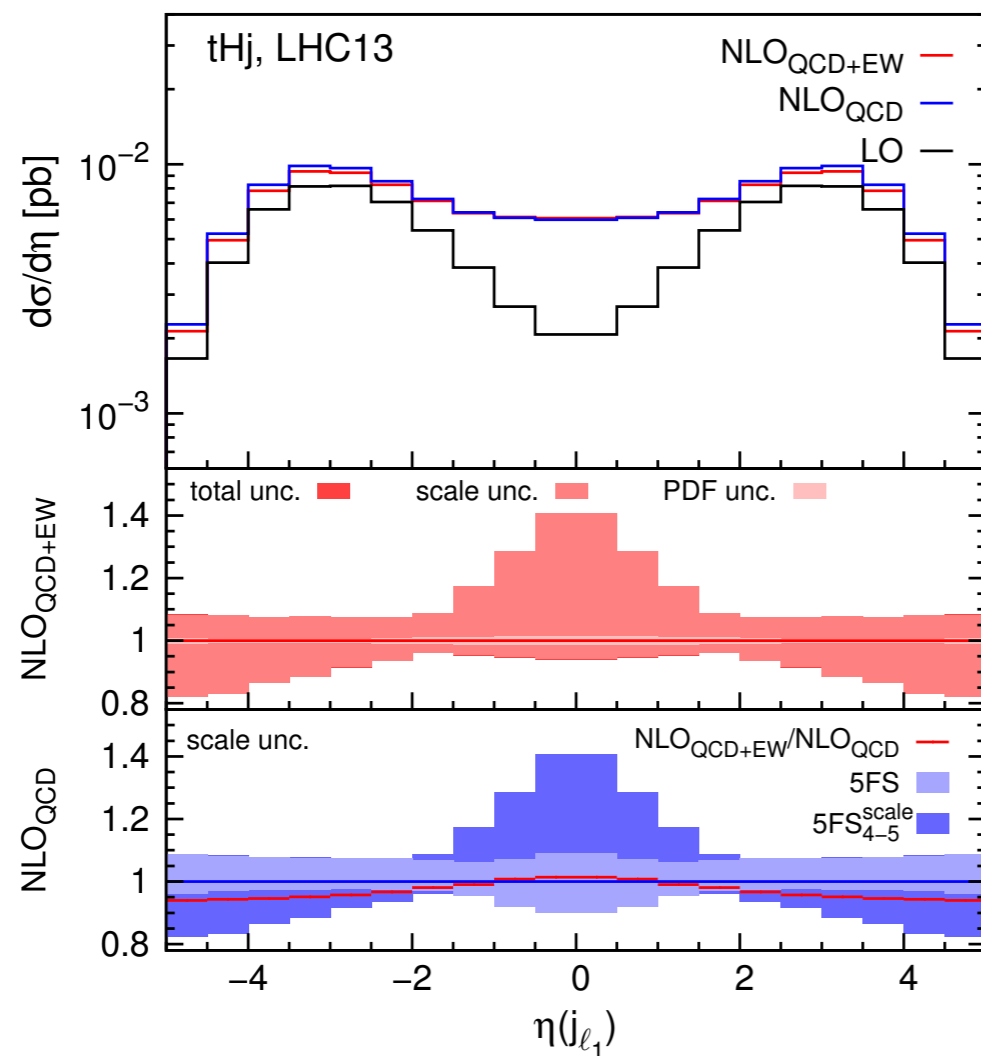
Brancaccio, Czakon, Generet, Krämer 21

# $tHj$ and $tZj$ : NLO QCD+EW predictions

$tHj$  and  $tZj$  computed at NLO QCD+EW accuracy in 5FS, “matching” to 4FS proposed

Pagani, Tsirikos, Vryonidou 20

NLO EW corrections found to be within NLO QCD theory uncertainties only if 4FS/5FS uncertainty taken into account ( $5FS_{4-5}^{scale}$ )



Accuracy	Channel	FS	$tHj$	
NLO <sub>QCD</sub>	$t$ -ch.	4FS	68.1(1) <sup>+2.7(+4.0%)</sup> <sub>-4.5(-6.6%)</sub>	+0.4(+0.5%) -0.4(-0.5%)
		5FS	71.3(1) <sup>+5.2(+7.2%)</sup> <sub>-1.7(-2.4%)</sub>	+0.3(+0.5%) -0.3(-0.5%)
		$5FS_{4-5}^{scale}$	71.3(1) <sup>+5.2(+7.2%)</sup> <sub>-7.7(-10.9%)</sub>	+0.3(+0.5%) -0.3(-0.5%)
NLO <sub>QCD</sub>	$t$ -ch., $s$ -ch., $tW_h$	5FS	85.1(2) <sup>+5.4(+6.4%)</sup> <sub>-2.3(-2.7%)</sub>	+0.5(+0.6%) -0.5(-0.6%)
		$5FS_{4-5}^{scale}$	85.1(2) <sup>+6.2(+7.2%)</sup> <sub>-9.2(-10.9%)</sub>	+0.5(+0.6%) -0.5(-0.6%)
NLO <sub>QCD+EW</sub>	$t$ -ch., $s$ -ch., $tW_h$	5FS	82.2(2) <sup>+5.6(+6.8%)</sup> <sub>-2.4(-2.9%)</sub>	+0.5(+0.6%) -0.5(-0.6%)
		$5FS_{4-5}^{scale}$	82.2(2) <sup>+5.9(+7.2%)</sup> <sub>-8.9(-10.9%)</sub>	+0.5(+0.6%) -0.5(-0.6%)

EW corrections reduce  $\sigma_{tot}$  by  $-3.4\%$ , also slightly alter shape

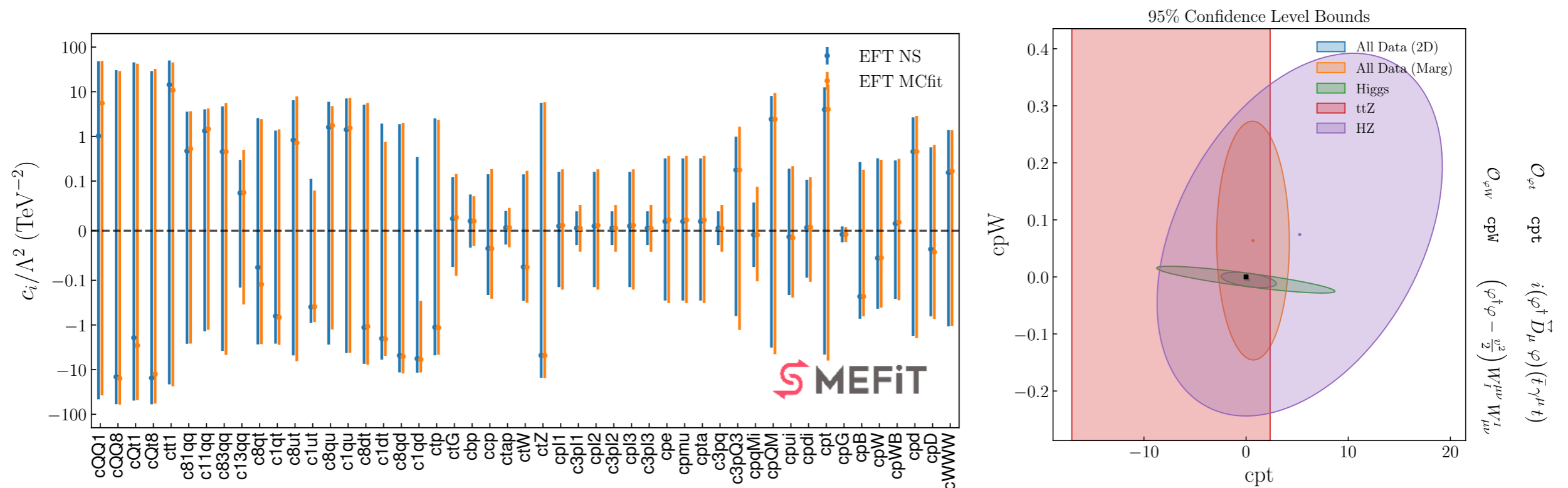
**Note:** Separation of  $t$ -channel,  $s$ -channel or  $tW$  production modes not properly defined at NLO EW accuracy, estimation of FS uncertainty not trivial

# EFT: top+higgs global fits

Significant advances in global EFT fits to Higgs, diboson, top and EW data,  
Also accounting for linear and quadratic corrections in the  $1/\Lambda^2$  expansion

Several mature codes now publicly available e.g. SMEFIT, Fitmaker

Ellis, Madigan, Mimasu, Sanz, You 20; Ethier, Maltoni, Mantani, Nocera, Rojo, Slade, Vryonidou, Zhang 21



NLO QCD corrections to EFT cross-sections automated and an have non-trivial impact on fit (best-fit, CL intervals)

## Future:

Data from high- $p_T$  VBS, Z-production in VBF, DY, multi-jet?  
Flavour data from LHCb, Belle...

Low energy e.g. neutrino data, electric dipole moment...

Develop "statistically optimal" observables for EFT



# Conclusion

## Strange times, strange location, strange talk...

Really incredible progress has been made since the last LH:

- Wish-list has been thoroughly attacked from all sides
- Many interesting topics have (re-)emerged (fiducial cuts and IR sensitivity, QCD-EW corrections,  $b$ -jets, 4FS/5FS, non-factorisable contributions to VBF)
- Much, much, more... (please bring them up during the discussion!)

Very hard to capture the spirit of Les Houches in a Zoom talk

**This year we will miss the mountains, but hopefully not the discussion...**

process	known	desired
$pp \rightarrow H$	$N^3\text{LO}_{\text{HTL}}$ (incl.) $N^{(1,1)}\text{LO}_{\text{QCD} \otimes \text{EW}}^{(\text{HTL})}$ $\text{NNLO}_{\text{HTL}} \otimes \text{NLO}_{\text{QCD}}$	$N^3\text{LO}_{\text{HTL}}$ (partial results available) $\text{NNLO}_{\text{QCD}}$
$pp \rightarrow H + j$	$\text{NNLO}_{\text{HTL}}$ $\text{NLO}_{\text{QCD}}$	$\text{NNLO}_{\text{HTL}} \otimes \text{NLO}_{\text{QCD}} + \text{NLO}_{\text{EW}}$
$pp \rightarrow H + 2j$	$\text{NLO}_{\text{HTL}} \otimes \text{LO}_{\text{QCD}}$ $N^3\text{LO}_{\text{QCD}}^{(\text{VBF}^*)}$ (incl.) $\text{NNLO}_{\text{QCD}}^{(\text{VBF}^*)}$ $\text{NLO}_{\text{EW}}^{(\text{VBF})}$	$\text{NNLO}_{\text{HTL}} \otimes \text{NLO}_{\text{QCD}} + \text{NLO}_{\text{EW}}$ $\text{NNLO}_{\text{QCD}}^{(\text{VBF})} + \text{NLO}_{\text{EW}}^{(\text{VBF})}$
$pp \rightarrow H + 3j$	$\text{NLO}_{\text{HTL}}$ $\text{NLO}_{\text{QCD}}^{(\text{VBF})}$	$\text{NLO}_{\text{QCD}} + \text{NLO}_{\text{EW}}$
$pp \rightarrow H + V$	$\text{NNLO}_{\text{QCD}} + \text{NLO}_{\text{EW}}$	$\text{NLO}_{gg \rightarrow HZ}^{(t,b)}$
$pp \rightarrow HH$	$N^3\text{LO}_{\text{HTL}} \otimes \text{NLO}_{\text{QCD}}$	$\text{NLO}_{\text{EW}}$
$pp \rightarrow H + t\bar{t}$	$\text{NLO}_{\text{QCD}} + \text{NLO}_{\text{EW}}$	$\text{NNLO}_{\text{QCD}}$
$pp \rightarrow H + t/\bar{t}$	$\text{NLO}_{\text{QCD}}$	$\text{NLO}_{\text{QCD}} + \text{NLO}_{\text{EW}}$

[LH2019 Wishlist](#)





**Thank you for listening!**