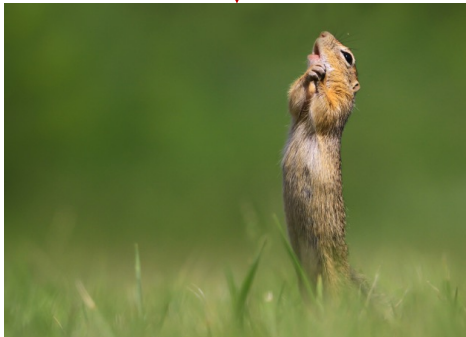


# Quantum Software Engineering (QSE) in intelligent robotic cognitive control Quantum Computational Intelligence Supremacy and Quantum Control

Perspective of collaboration development between JINR and IN2P3 in the next decades

1. Definition and structure of QSE
2. Quantum computational intelligence toolkit
3. Quantum Software Engineering in JINR projects

Measurement result of  
quantum computing



**Sergey V. Ulyanov**  
**Laboratory of Information Technologies**  
**Joint Institute for Nuclear Research**

18 May 2021

Superposition



## Prof. Sergey V. Ulyanov : 略歴

氏名 Sergei Victorovich Ulyanov

生年月日 1946年12月15日

国籍 ロシア

[1974] Ph.D

“Statistical analysis of seismic excitation on dynamical systems  
with random time-dependent parameters”

[1992] State Dr. of Physics and Mathematical Sciences (IFTP)

“Physical models of control objects and robust intelligent control –  
relativistic, quantum and thermodynamics-information aspects”

### 経歴

1965 Moscow State Technical University (Bauman Technical College)

1971 (自動制御システム) 入学 同上 卒業 (кафедра П -1: Системы управления)

1965 ~ 75 **Research Engineer and Senior Manager**

Central Institute of Building Construction, Ministry of Building Construction

1975 ~ 83 **Chief of Laboratory**

Central Institute of Biomedical Engineering, Ministry of Biomedical Engineering

1983 ~ 92 **Professor, Chief** of Department of Quantum and Relativistic Control Systems

Institute of Physical -Technical Problems, Soviet Academy of Sciences

1992 ~ 94 **Professor, Chief** of Artificial Intelligence Robotic Laboratory

Institute for Problems in Mechanics, Russian Academy of Science

1994 ~ 97 教授

電気通信大学 機械制御工学科

1997 ~ 2007 ヤマハ発動機(株) 研究開発センター

1999 ~ 2018 同社 YMENV R&D Office in Crema (Italy)



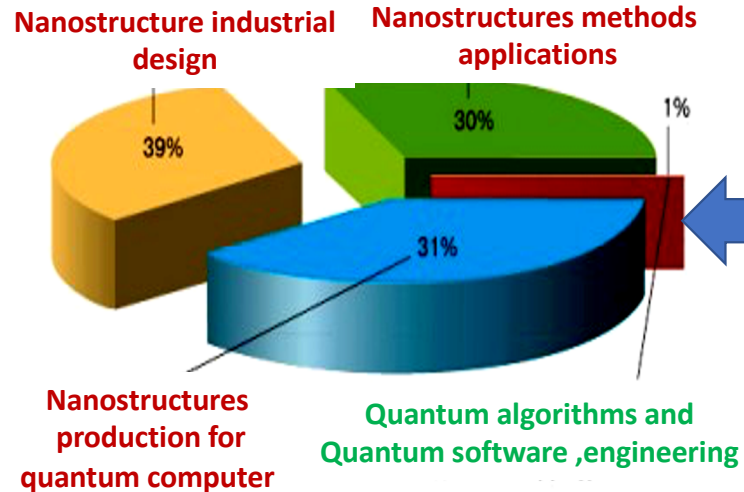
# 1. Definition and structure of QSE



**Software Engineering (SE)** (Friedrich L. Bauer):  
The establishment and use of sound engineering principles in order to obtain economically software that is reliable and works efficiently on real machines

Jianjun Zhao (2020), Quantum Software Engineering Landscapes and Horizons <https://arxiv.org/pdf/2007.07047.pdf>

**Quantum software engineering (QSE)** is the use of sound engineering principles for the development, operation, and maintenance of quantum software and the associated document to obtain economically quantum software that is reliable and works efficiently on quantum computers.



In this definition, we would like to highlight *three important issues in QSE*.

*First*, it is important to apply the "sound engineering principles" to quantum software development.

*Second*, the quantum software should be built "economically."

*Finally*, the quantum software should be "reliable" and needs to work "efficiently" on quantum computers.

Quantum software engineering can be regarded as a branch of systems engineering, which involves the development of large and complex quantum software systems.

V.V. Korenkov, A.G. Reshetnikov, S.V. Ulyanov, Quantum software engineering Pt 3: Quantum supremacy modelling. – M.: Kurs, 2021.

# A Quantum Software lifecycle

Quantum Software Requirements Analysis

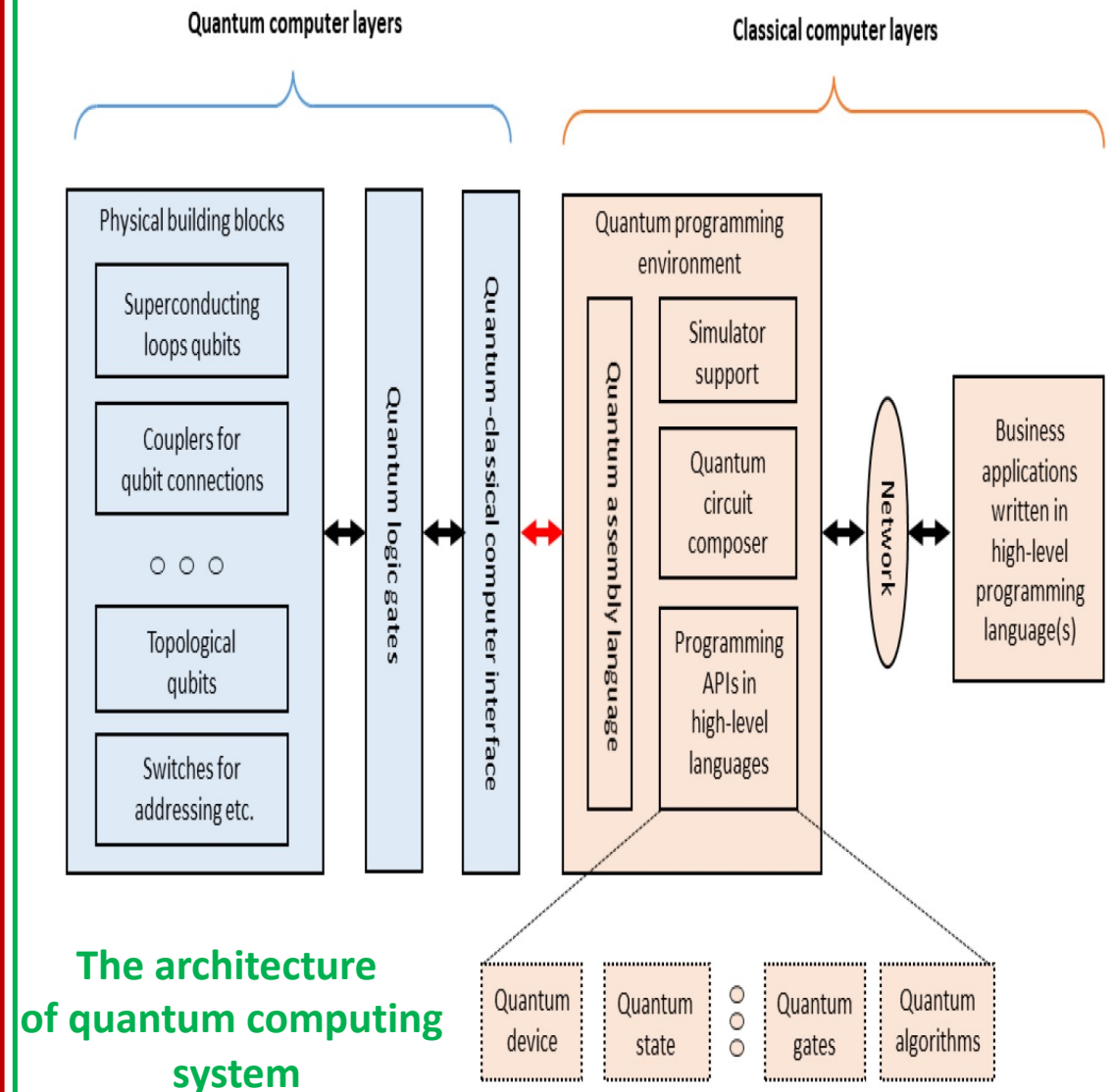
Quantum Software Design

Quantum Software Implementation

Quantum Software Testing

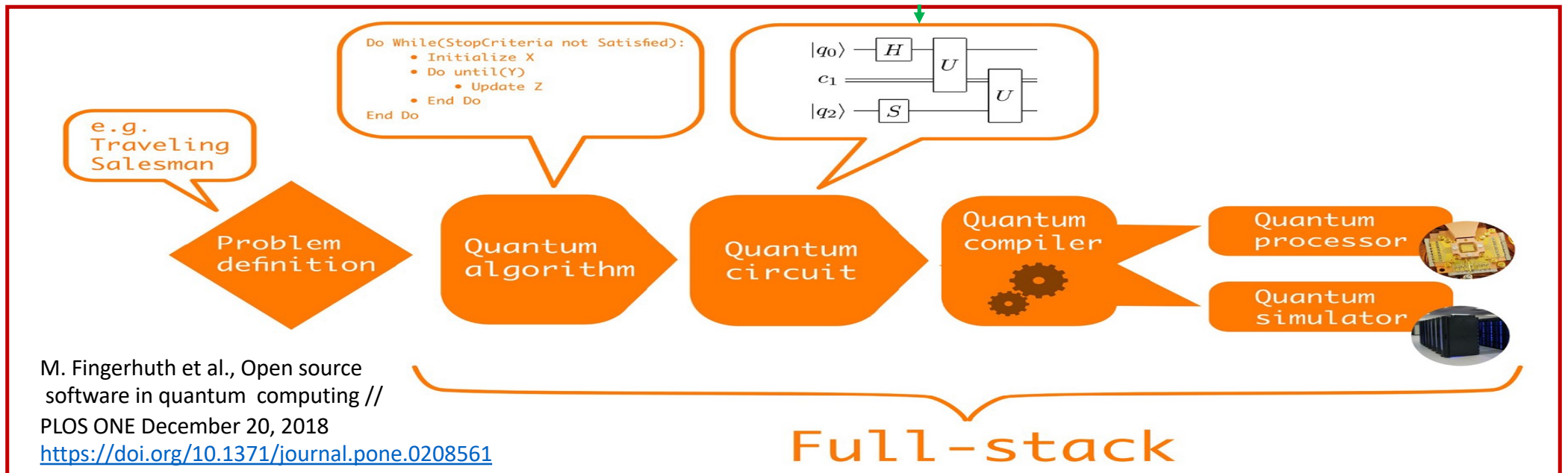
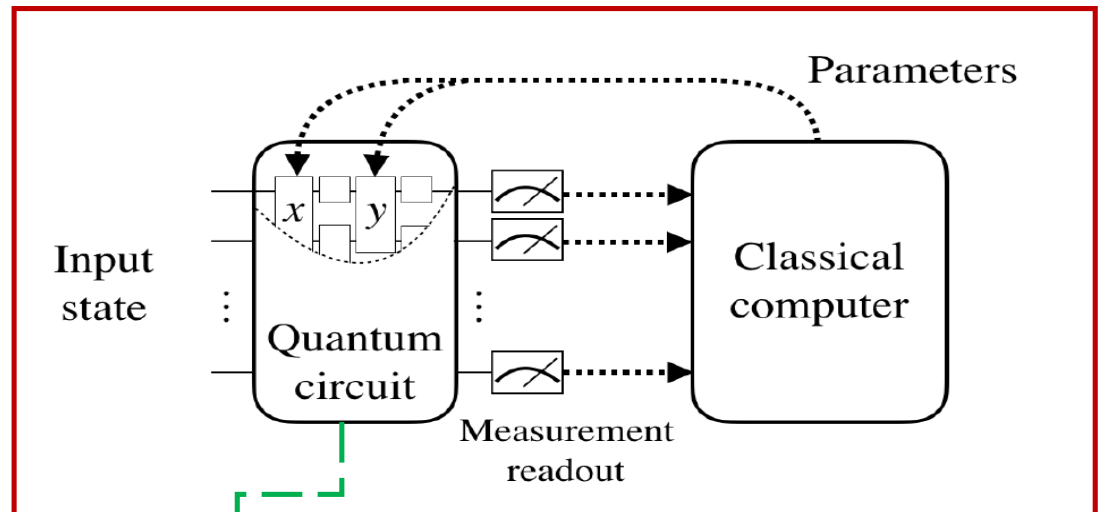
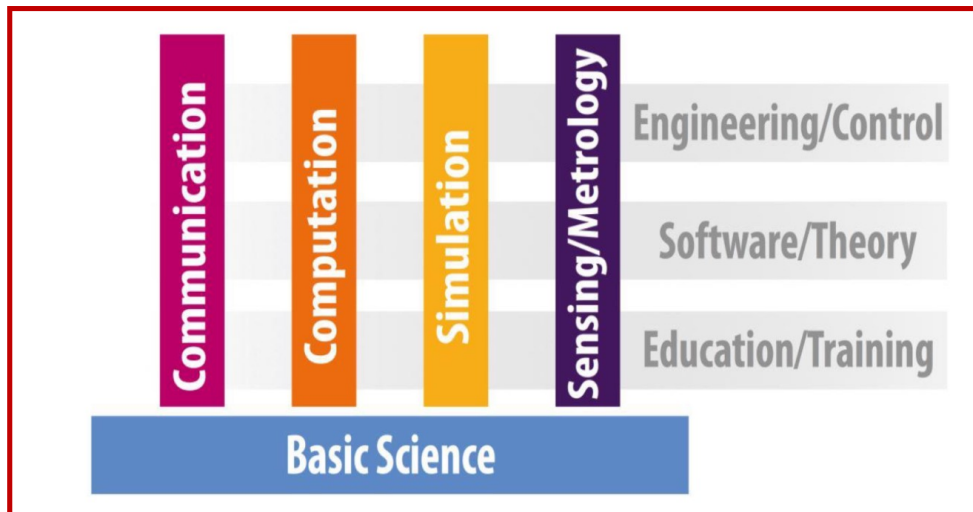
Quantum Software Maintenance

*QSE embraces the coexistence of classical and quantum computing, and advocates the use of reengineering techniques to integrate new quantum algorithms with the existing classical Information systems. Reverse engineering techniques are also needed to parse and abstract quantum program information that is to be integrated into classical programs*



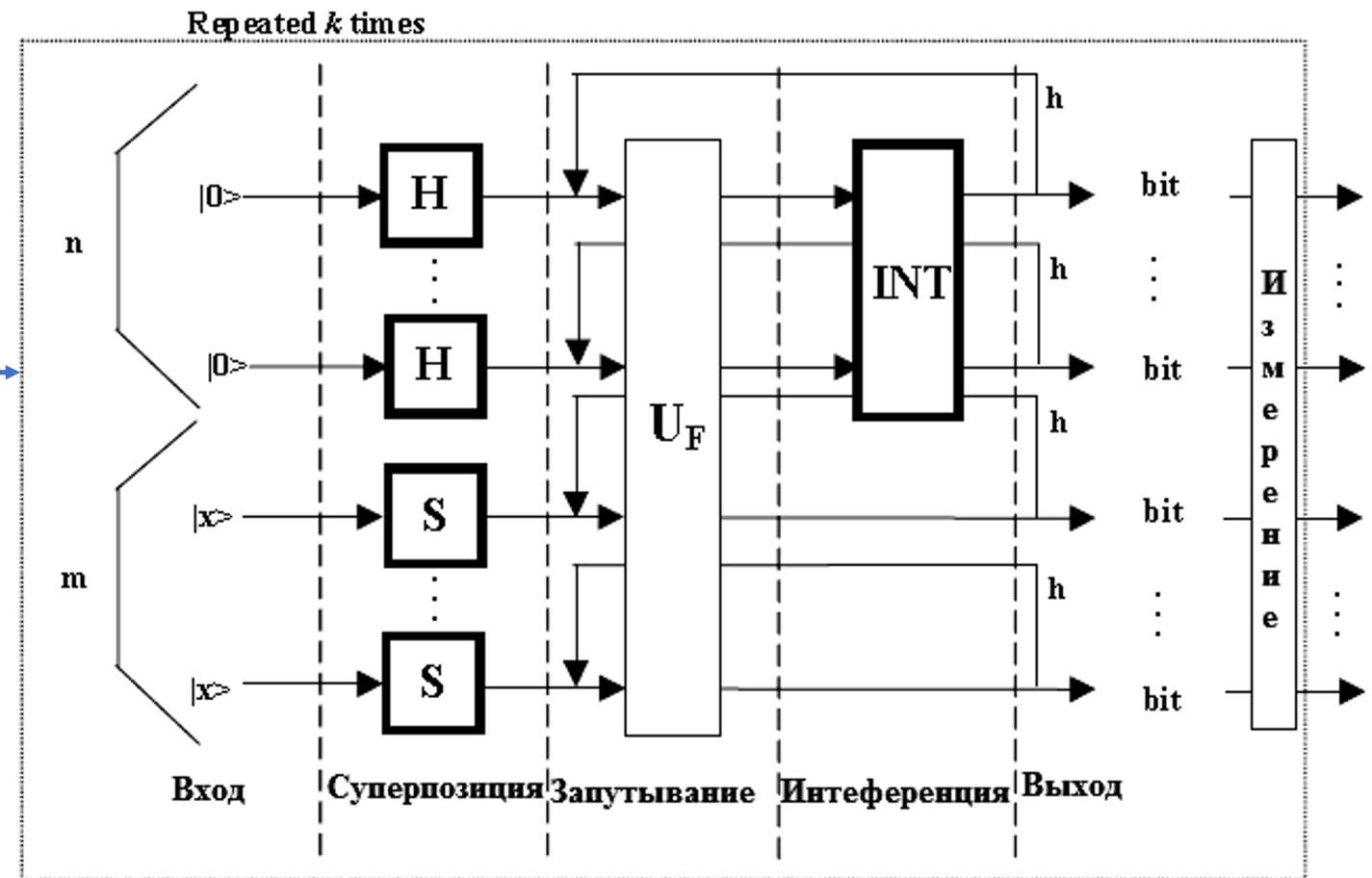


## 2. Quantum computational intelligence toolkit



Quantum algorithmic gate-based computing

V.V. Korenkov, A.G. Reshetnikov,  
S.V. Ulyanov, Quantum software  
engineering. – M.: Kurs, 2021



$$КАЯ = \left[ \left( Int \otimes^n I \right) \cdot U_F \right]^{h+1} \cdot \left[ {}^n H \otimes {}^m S \right]$$

# Quantum massive parallel computing

Quantum KB optimizer

SCO

Answer

QC output

QAG design

Classical input

Problem

General  
structure  
of  
quantum  
algorithm

$$|\psi_{fin}\rangle = [(\text{Interference})(\text{Quantum oracle})](\text{Superposition})|\psi_{initial}\rangle$$

Qualitative  
properties  
of function

Quantum Fourier  
transformation

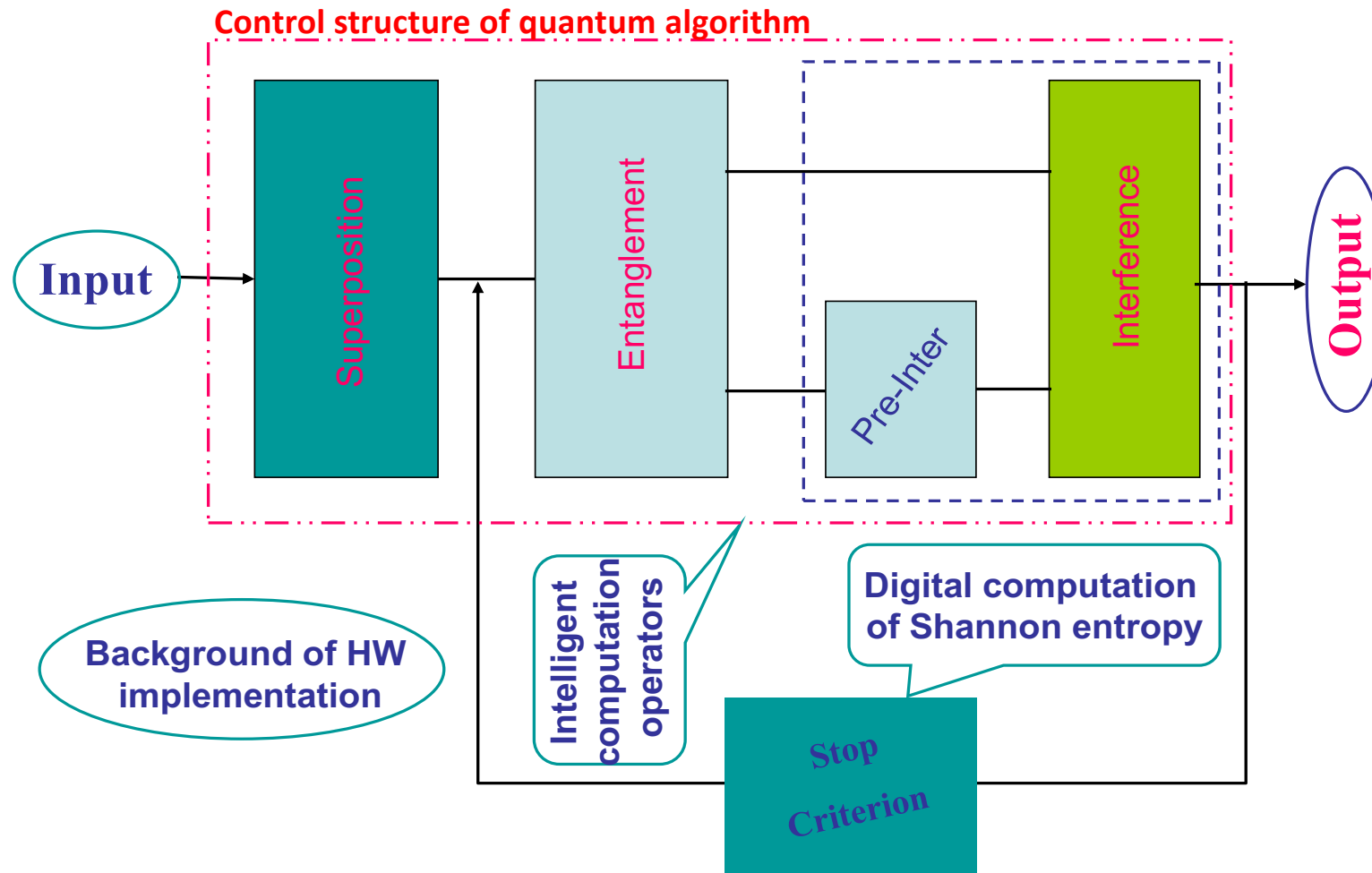
Problem oriented  
operator

Hadamard  
transformation

Coding of  
function  
properties

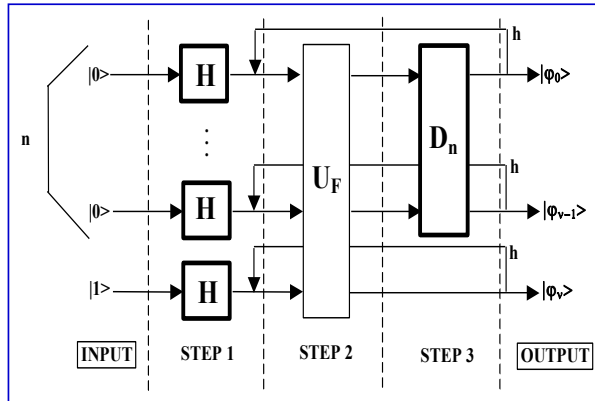
Qualitative properties  
of function

Quantum oracle as black box

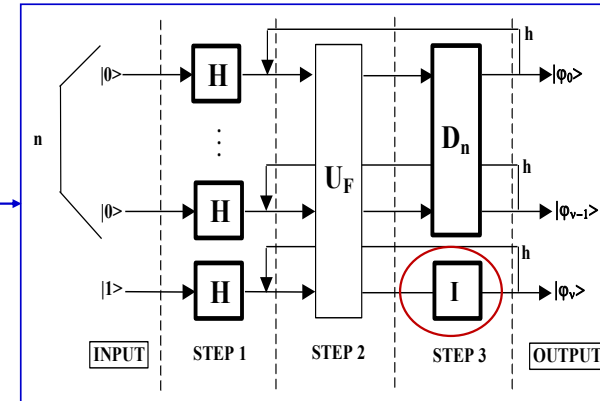


**a**

## Quantum algorithm gate



## Gate correction

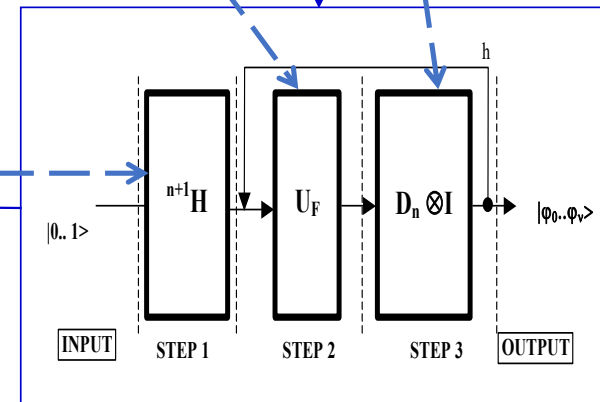
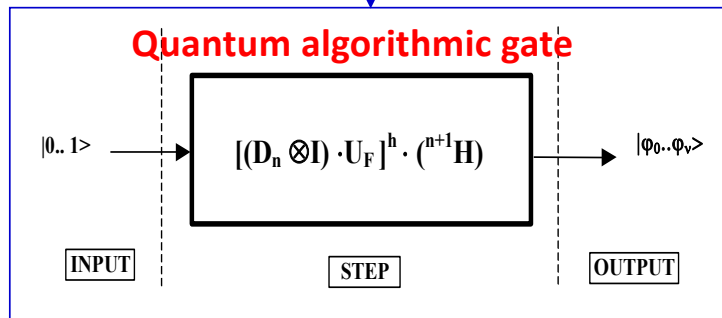


## Quantum oracle

## Diffusion matrix

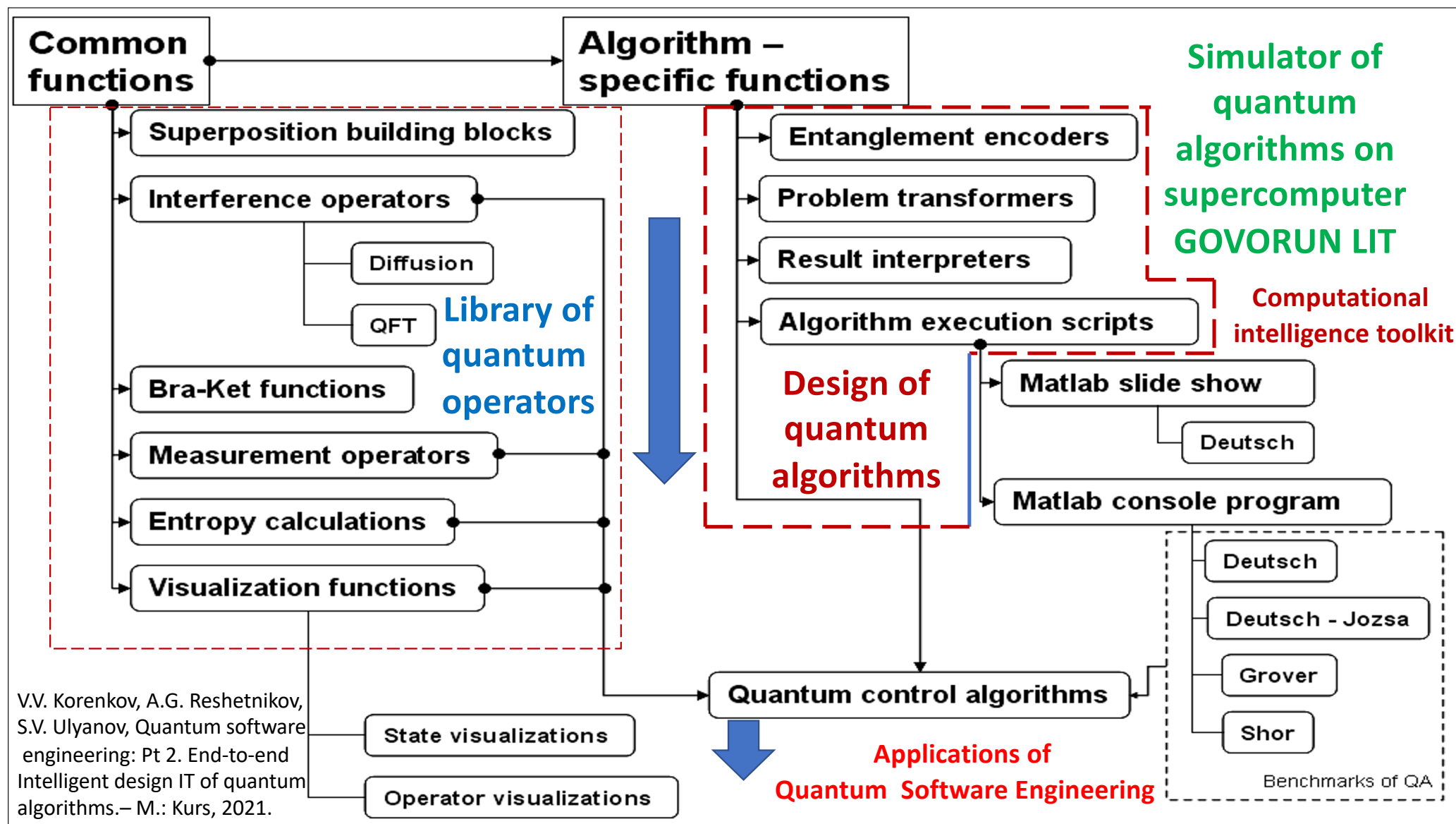
## Superposition

## Quantum algorithmic gate



## Quantum operation convolution



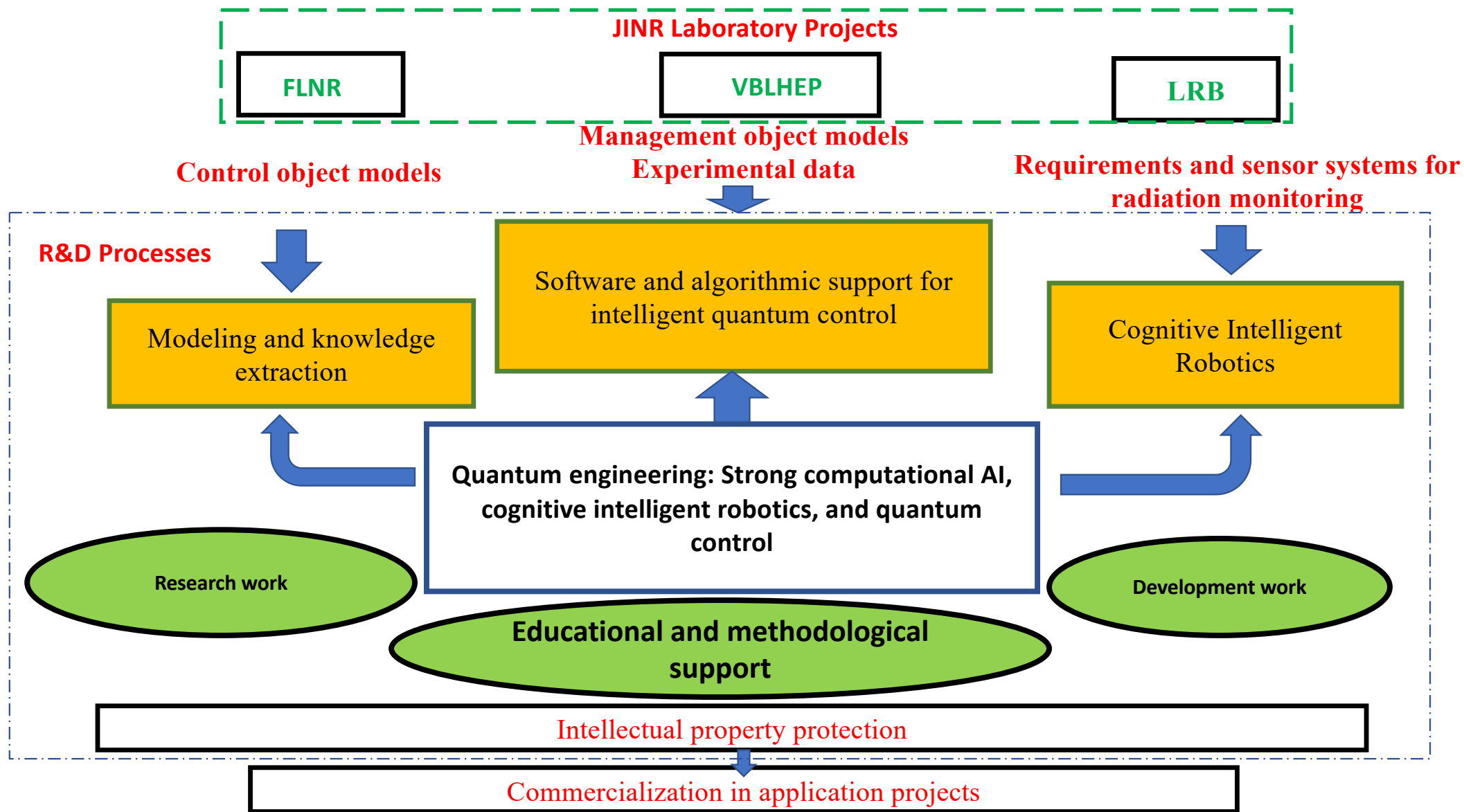


### 3. Quantum Engineering LIT: JINR projects examples

Quantum computing in quantum robust control design

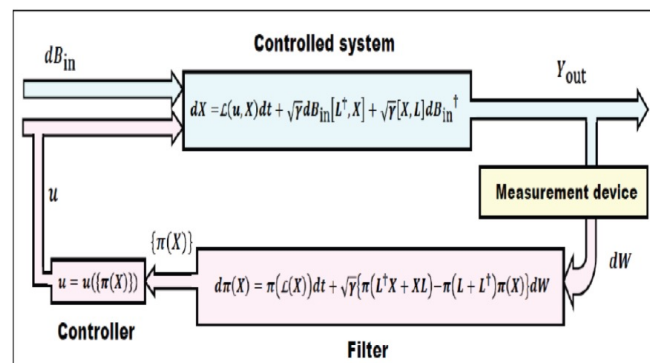
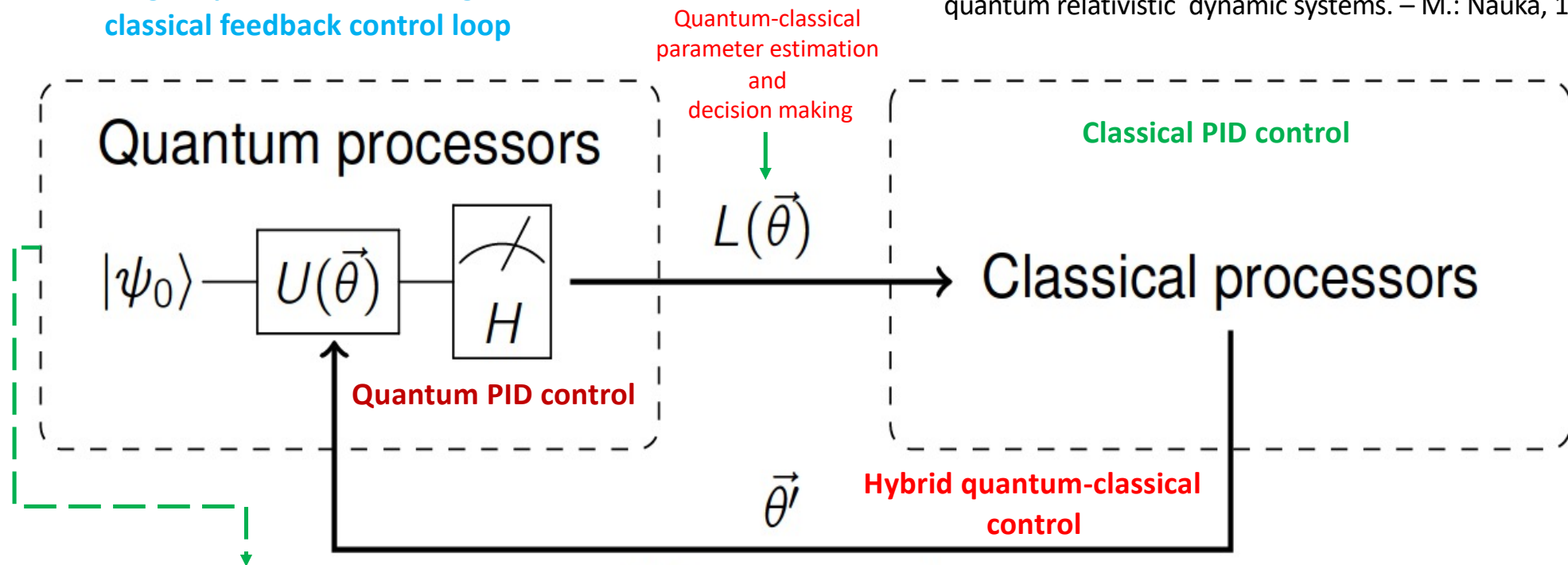
- *Control of nitrogen consumption in superconducting-coil electromagnet*
- *Control of high frequency station*
- *Intelligent robotics control*

Quantum algorithms approach in the search structure of super-heavy elements



## Embedding of quantum control algorithm in classical feedback control loop

B.N. Petrov, I.I. Goldenblat, S.V. Ulyanov, Control problems of quantum relativistic dynamic systems. – M.: Nauka, 1982.

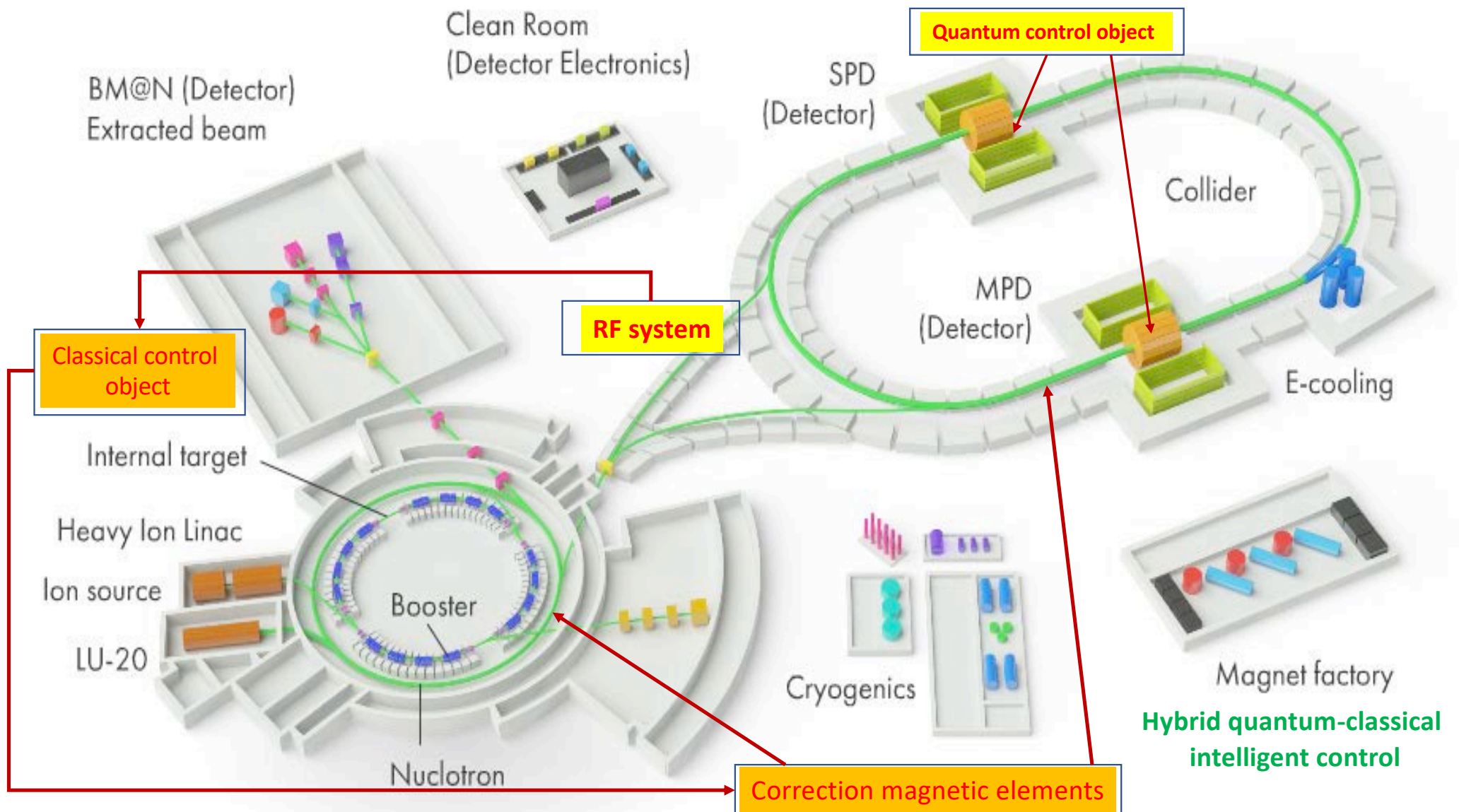


update parameters

*Models of quantum feedback control*

*Intelligent quantum feedback control:*

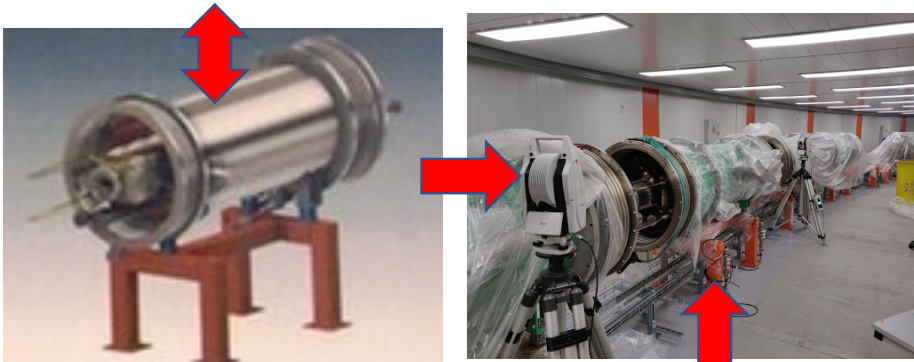
S.V. Ulyanov, Quantum relativistic informatics: Unconventional logic of physical rigor and mathematical correctness of control object models. - LAP Acad. Publ., Germ.2014



# Physical features of the control object and the physical process

## Features of an autonomous object

- Non-standard heat intakes
- Eddy currents in the core (heat the core)
- The dependence of the quality of the magnetic field on the quality of cooling
- Flashing of the wall and uneven cooling in the connecting nodes



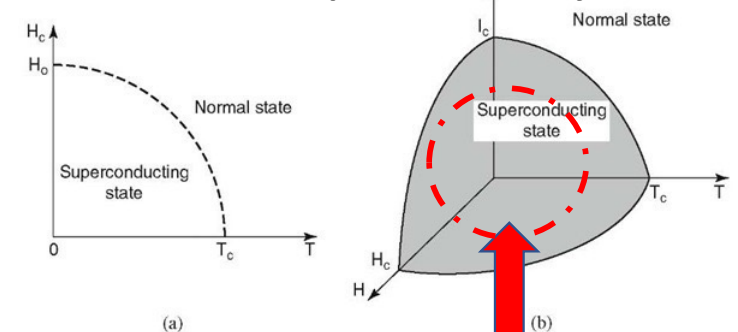
## Features of the group of magnetic elements

- Different eddy currents in the core
- Minor differences in magnets elements

**The principle of intelligent control:** Compensation of the indeterminate and inaccurate parameters of the magnetic element existing in a real object through the use of soft and quantum computing technologies

The control task is to maintain the state of superconductivity

## The state of superconductivity



The point of equilibrium in space and the permissible range of changes in current, temperature, and magnetic field



# Intelligent robotic quantum control

## Intelligent robotics based on quantum fuzzy inference

- Structure of self-organized intelligent control system
- Robotic redundant 7 DoF manipulator
- Autonomous and swarm robots with information exchange (video)

Robust Intelligent Control  
in Unpredicted Control Situations  
Relative to Quantum Knowledge:  
KB Self-organization Phenomena  
based on Quantum Fuzzy Inference

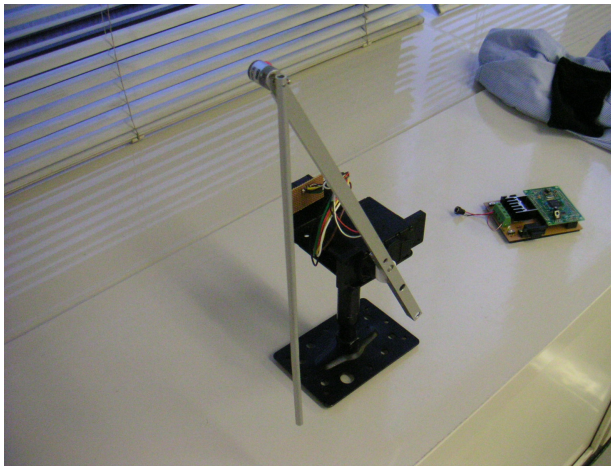
- Examples of simulation and benchmarks  
demo  
(cart – pole dynamic system)

# Inverted Pendulum

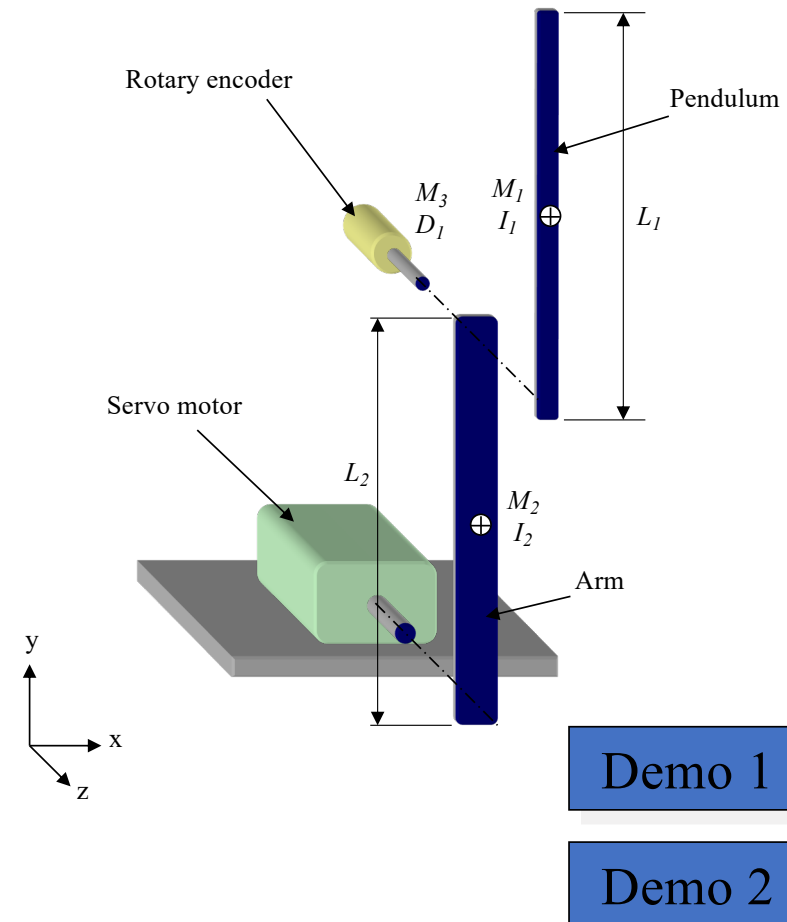
**Intelligent control of the pendulum based on the  
physical measurements**

**Without The knowledge of his mathematical model**

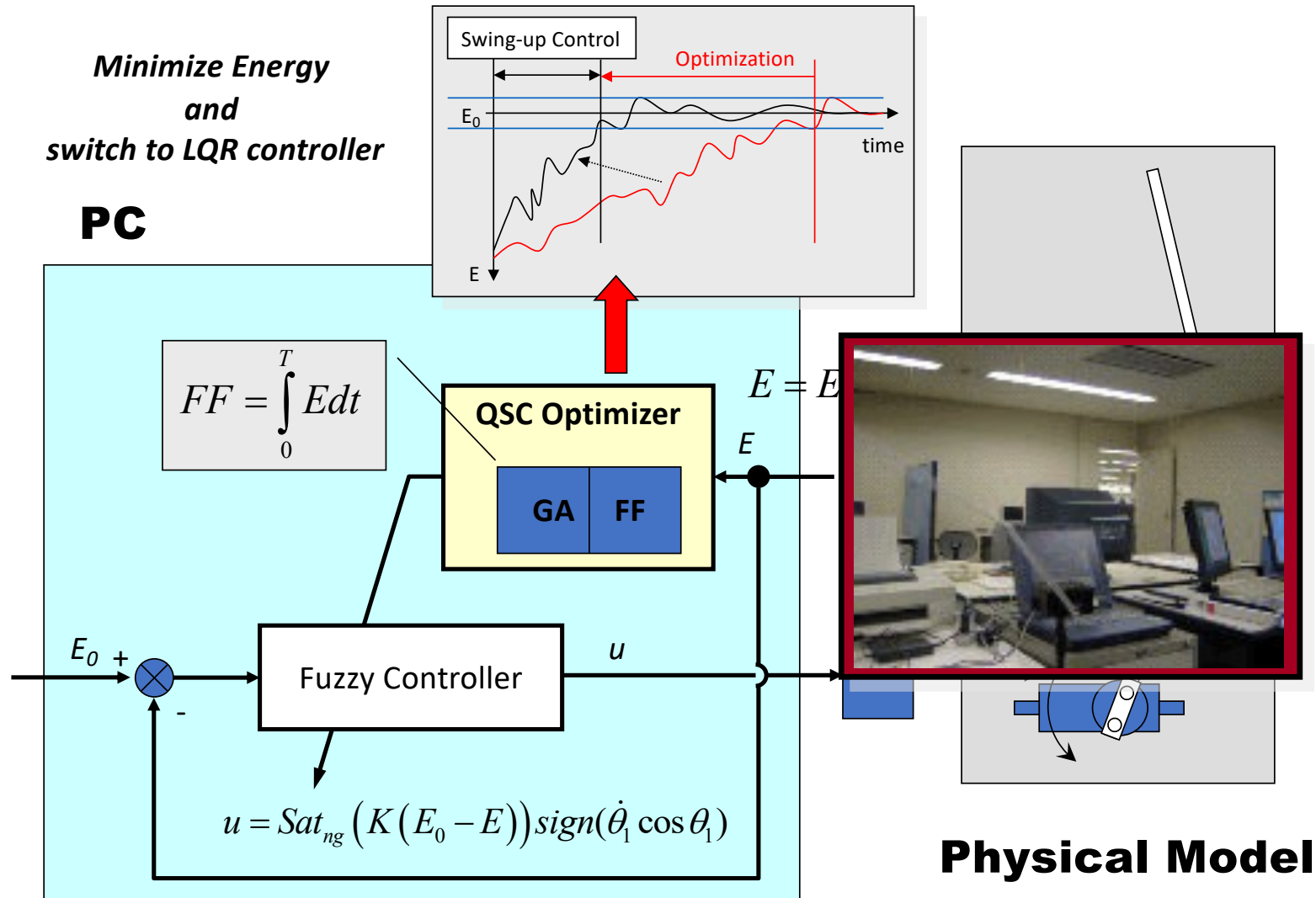
# Inverted pendulum hardware model



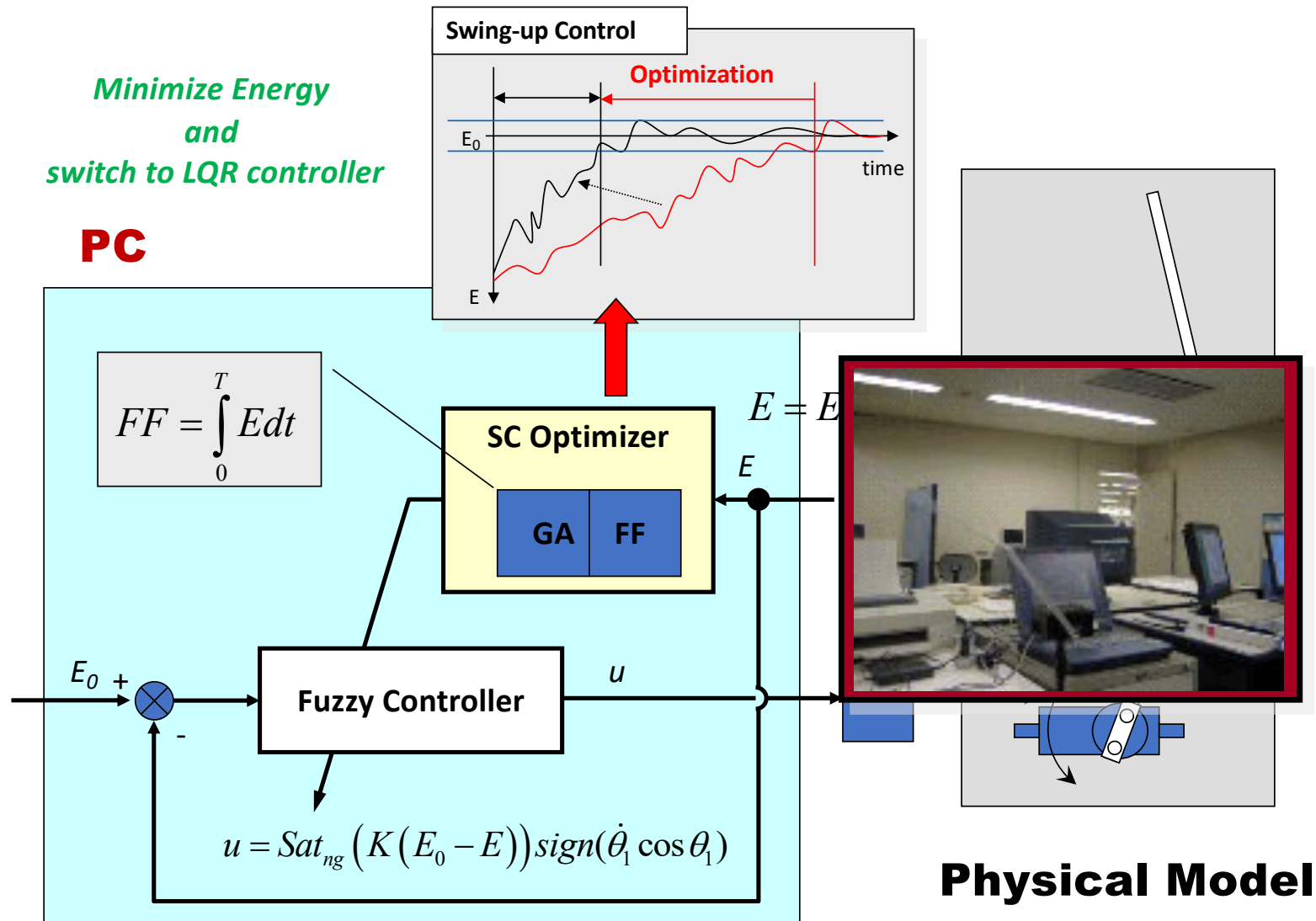
Pendulum	length	$L_1$	0.29	m
	mass	$M_1$	1.23E-2	kg
	momentum inertia	$I_1$	8.62E-5	kgm <sup>2</sup>
Arm	length	$L_2$	0.23	m
	mass	$M_2$	1.12E-2	kg
	momentum inertia	$I_2$	4.93E-5	kgm <sup>2</sup>
Rotary encoder	mass	$M_3$	1.00E-2	kg
	damping	$D_1$	5.00E-5	Ns/m



# Direct Swing-Up Optimization by QSCOptimizer



# Direct Swing-Up Optimization by SCOptimizer





100 frames sample

FC

QFC

QPID

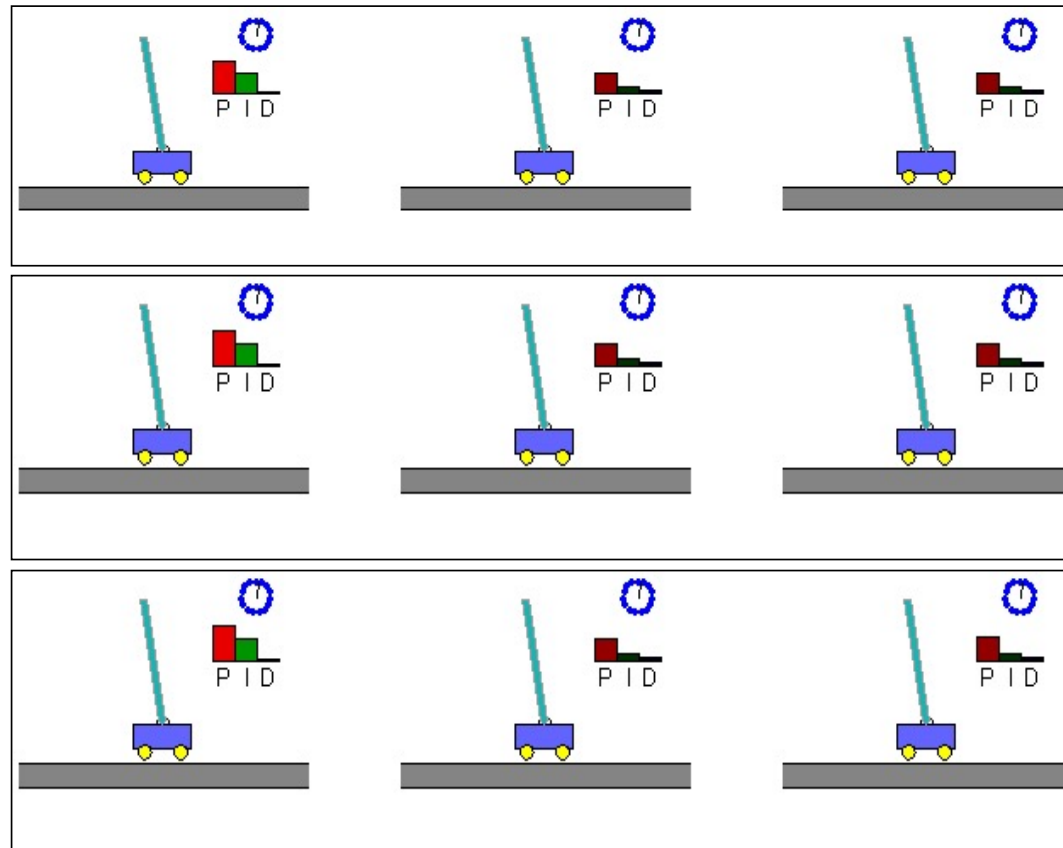
S3



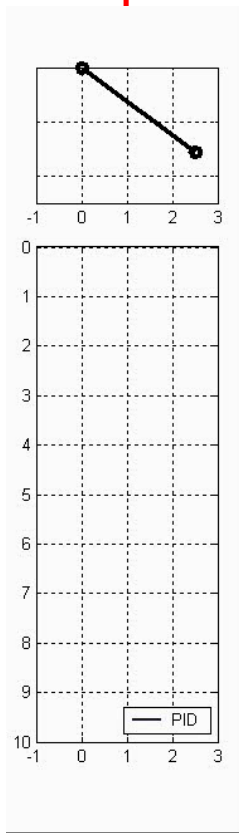
S4



S5

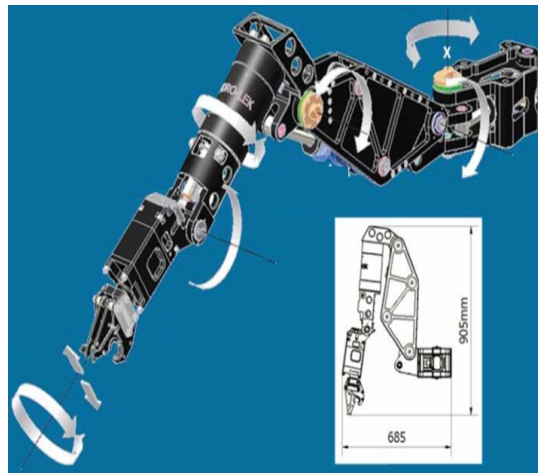
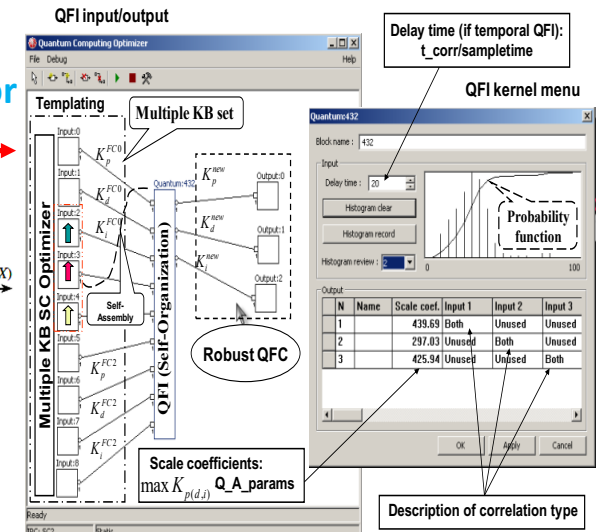
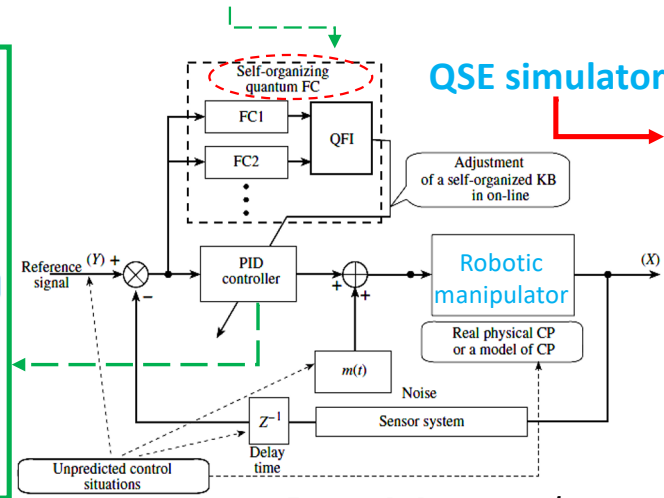
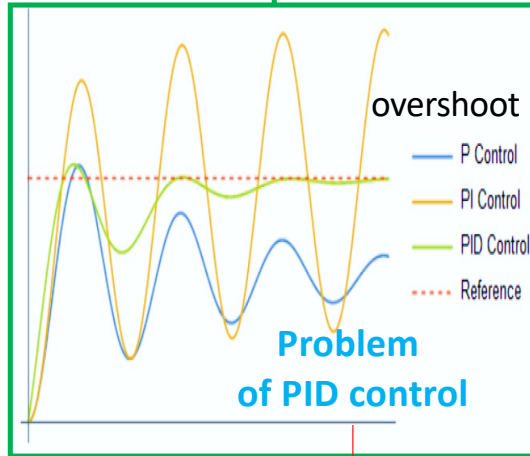


## Video



Robust control of pendulum under random excitation

## Structure of self-organized intelligent control system

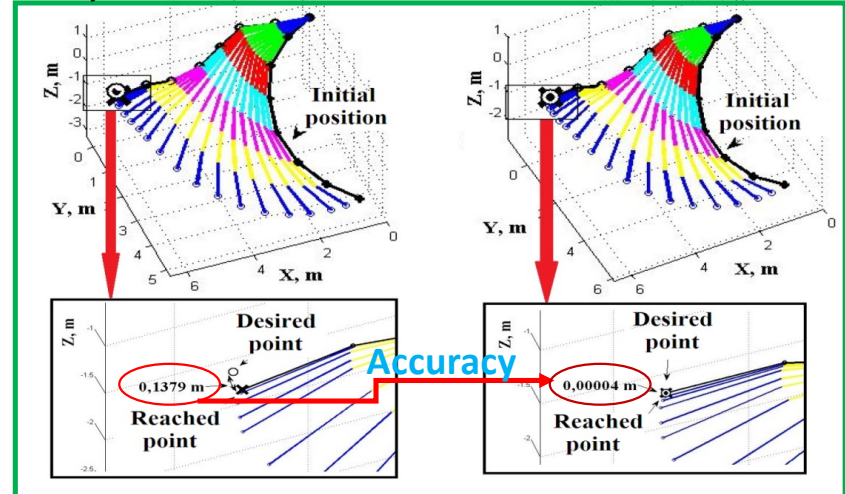


**QSE supremacy  
In robotics control**

Intractable  
conventional  
control  
problem

7 degree of  
freedom  
redundant  
manipulator

## Fuzzy PID control



Quantum  
PID  
control

V.V. Korenkov; A.G. Reshetnikov; S.V. Ulyanov, Quantum Software Engineering Supremacy in Intelligent Robotics // Published in: 2020 International Scientific and Technical Conference Modern Computer Network Technologies (MoNeTeC)

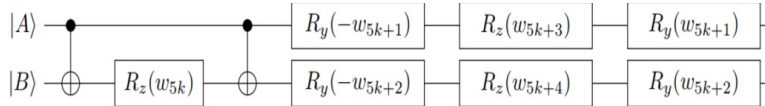
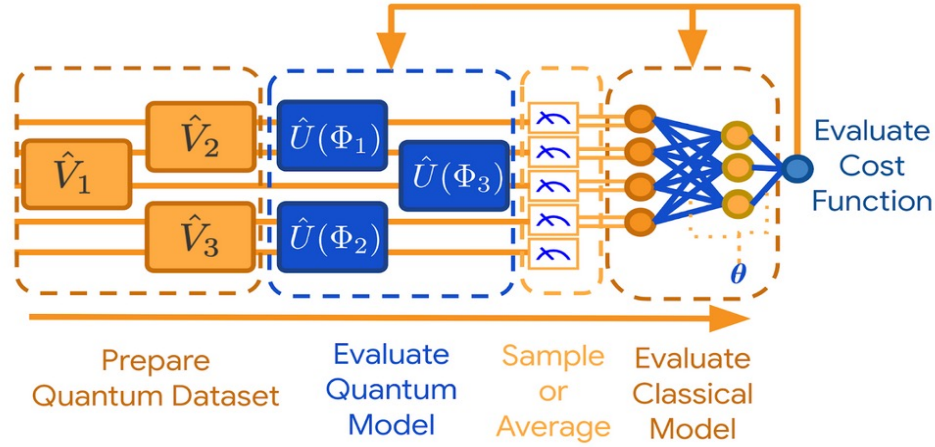


# Quantum intelligent control

- Quantum deep learning
- Quantum control of relativistic physical objects

## Deep Quantum Learning

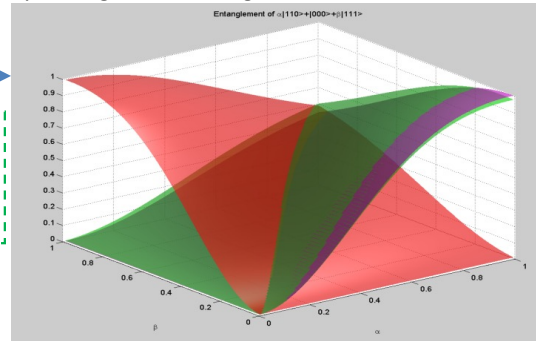
Evaluate Gradients & Update Parameters



This is the quantum circuit for the gate decomposition of a single time chunk of the entanglement witness.

The 2 qubit operations are CNOT gates,  $R$  is a rotation about a designated axis on the Bloch sphere, and the  $w$  values are functions of the system parameters  $K$ .

Figure shows entanglement of  $|\psi\rangle = \alpha|110\rangle + \beta|111\rangle + |000\rangle$  as a function of both  $\alpha$  and  $\beta$ , and compared with the three-way “tangle” agreement is quite good. The red surface shows the pairwise entanglement between qubits A and B, the green; 3-way entanglement among A, B, and C; the magenta is the (analytically calculated) 3-tangle.



J.E. Steck, E. C. Behrman, and N. Thompson,  
Machine Learning applied to Programming  
Quantum Computers // Conference paper, 2019.  
<https://www.researchgate.net/publication/330199278>

## Lagrangian quantum deep learning

The density matrix,  $\rho$ , of a quantum system as a function of time obeys the Schrödinger equation

$$\frac{d\rho}{dt} = \frac{1}{i\hbar} [H, \rho]$$

and has the formal solution as  $\rho = \exp(iLt) \rho(t_0)$ . The time evolution equation for the density matrix maps the initial state  $\rho(t_0)$  (input data for the quantum computer) to the final state  $\rho(t_f)$  (output calculated result). Parameters in the system Hamiltonian  $H$  are physical interactions and fields in quantum hardware and can be adjusted experimentally as functions of time. “Programming” this quantum computer involves finding the parameters using machine learning that yield the desired computation. Thus, we can train the system to evolve in time initial (input) to target final (output) states; yielding a quantum system that accurately approximates a chosen function, such as: logic gates, benchmark classification problems, or, since the time evolution is quantum mechanical, a quantum function like entanglement.

The learning rule for the quantum system based on dynamic backpropagation is derived as follows. Given an input (initial density matrix),  $\rho_0$ , and a target output,  $d$  (a “training pair”), we develop a weight update rule based on gradient descent to adjust the system parameters, i.e., train the system “weights”, to reduce the squared error between the target,  $d$ , and the output, Output. While minimizing the squared error, the system’s density matrix,  $\rho(t)$ , is constrained to satisfy the Schrödinger equation for all time in the interval  $(t_0, t_f)$ . We define a Lagrangian,  $L$ , to be minimized, as

$$L = \frac{1}{2} [d - \langle O(t_f) \rangle]^2 + \int_{t_0}^{t_f} \lambda^+(t) \left( \frac{\partial \rho}{\partial t} + \frac{i}{\hbar} [H, \rho] \right) \gamma(t) dt$$

where the Lagrange multiplier vectors are  $\lambda(t)$  and  $\gamma(t)$  (row and column, respectively), and  $O$  is an output measure (or some function of a measure), which is chosen for the particular problem under consideration. As an example, for our entanglement witness application, we defined the output as:

$$\langle O(t_f) \rangle = \text{tr}[\rho(t_f)O] = \sum_i p_i \langle \psi_i(t_f) | O | \psi_i(t_f) \rangle$$

where  $\text{tr}$  stands for the trace of the matrix, and where the density matrix is represented in terms of the chosen basis as

$\rho = \sum_i p_i |\psi_i\rangle \langle \psi_i|$ . We take the first variation of  $L$  with respect to  $\rho$ , set it equal to zero, then integrate by parts to give the following equation which can be used to calculate the vector elements of the Lagrange multipliers (“error deltas” in neural network terminology) that will be used in the learning rule:

$$\gamma_i \frac{\partial \gamma_j}{\partial t} + \frac{\partial \lambda_i}{\partial t} \gamma_j - \frac{i}{\hbar} \sum_k \lambda_k H_{ki} \gamma_j + \frac{i}{\hbar} \sum_k \lambda_i H_{jk} \gamma_k = 0$$

which is solved backward in time, with the boundary conditions at the final time  $t_f$  given by

$$-\left[ d - \langle O(t_f) \rangle \right] O_{ji} + \lambda_i(t_f) \gamma_j(t_f) = 0.$$

The gradient descent rule to minimize  $L$  with respect to  $w$  is  $w_{\text{new}} = w_{\text{old}} - \eta \frac{\partial L}{\partial w}$  or each “weight” parameter  $w$ , where  $\eta$  is the learning rate, and where the derivative is given by

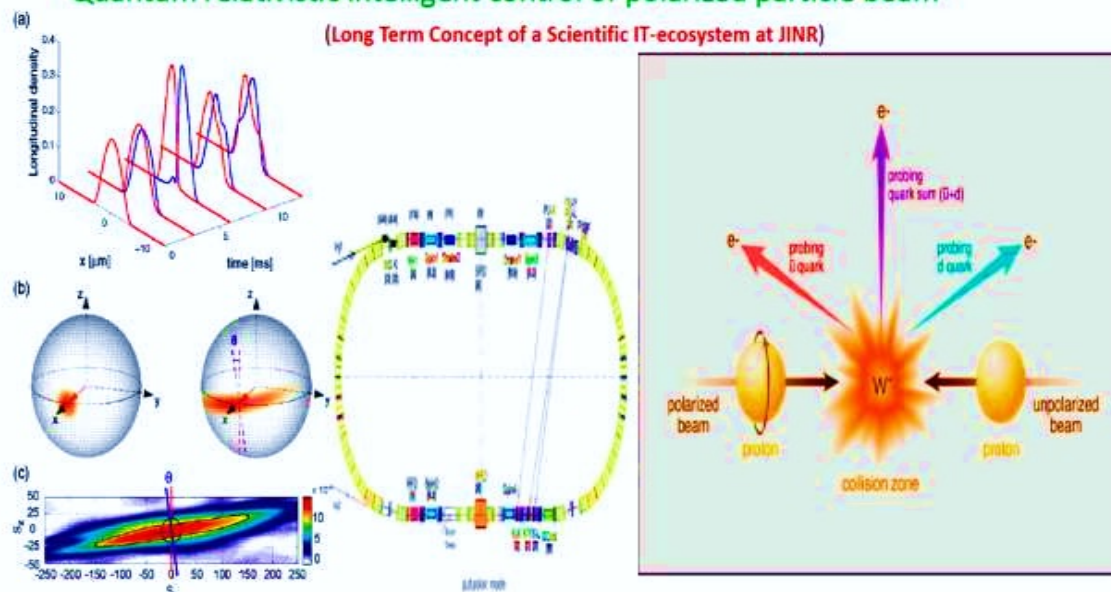
$$\frac{\partial L}{\partial w} = \frac{i}{\hbar} \int_0^{t_f} \lambda^+(t) \left[ \frac{\partial H}{\partial w}, \rho \right] \gamma(t) dt = \frac{i}{\hbar} \int_0^{t_f} \sum_{ijk} \left( \lambda_i(t) \frac{\partial H}{\partial w} \rho_{kj} \gamma_j - \lambda_i(t) \rho_{ik} \frac{\partial H_{kj}}{\partial w} \gamma_j \right) dt$$

The above technique, since it uses the density matrix, is applicable to any state of the quantum system, pure or mixed.



## Quantum relativistic intelligent control of polarized particle beam

(Long Term Concept of a Scientific IT-ecosystem at JINR)



The dynamics of interaction of a relativistic ensemble of particles with an electromagnetic field obeys the laws of quantum relativistic mechanics, and the laws of control theory require the predominance of the number of controlled degrees of freedom of the control system over the number of possible degrees of freedom of the controlled object

Given a time-varying quantum control system,

$$\frac{\partial \xi(x, t)}{\partial t} = [H_0(t, x) \otimes \mathcal{I}_e + \mathcal{I}_e \otimes H_e(t, x) + H_{SB}(t, x) + u_i(t) H_i(t, x) \otimes \mathcal{I}_e] \xi(t, x)$$

Free Hamiltonian  
of the system

**Dirac  
equations**

Tensor product for  
combined system

Hamiltonian describing  
the environment

Interaction Hamiltonian  
between the system and  
the environment

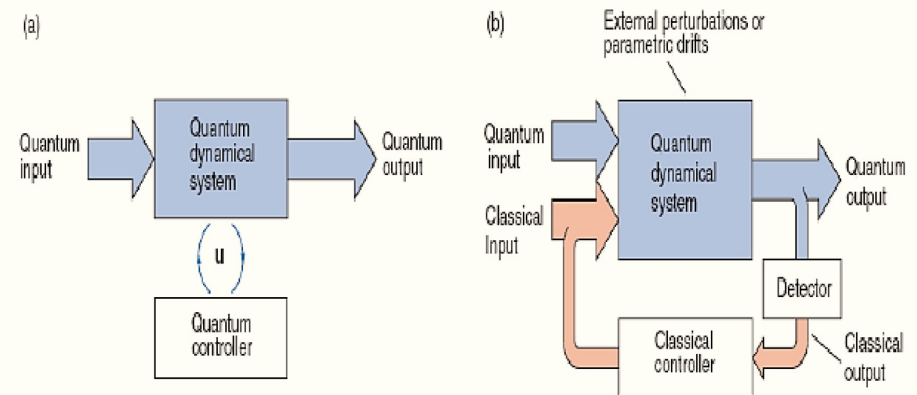
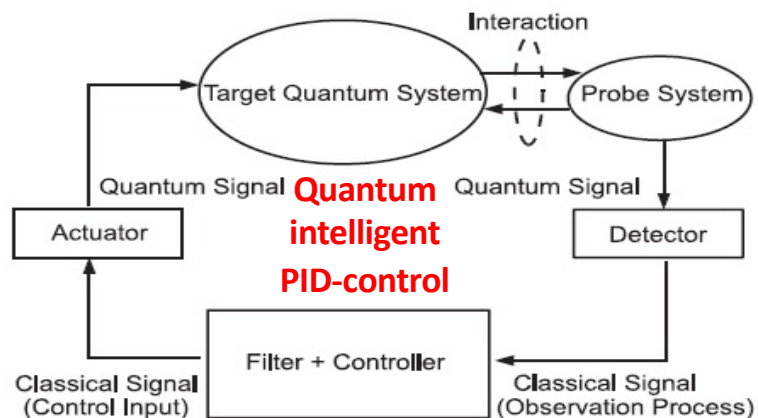
State of the  
Quantum  
system

Controls

Semiclassical Control  
Hamiltonians

**Quantum  
non-demolition  
feedback control  
of quantum object**

**Quantum  
relativistic  
Informatics  
toolkit**

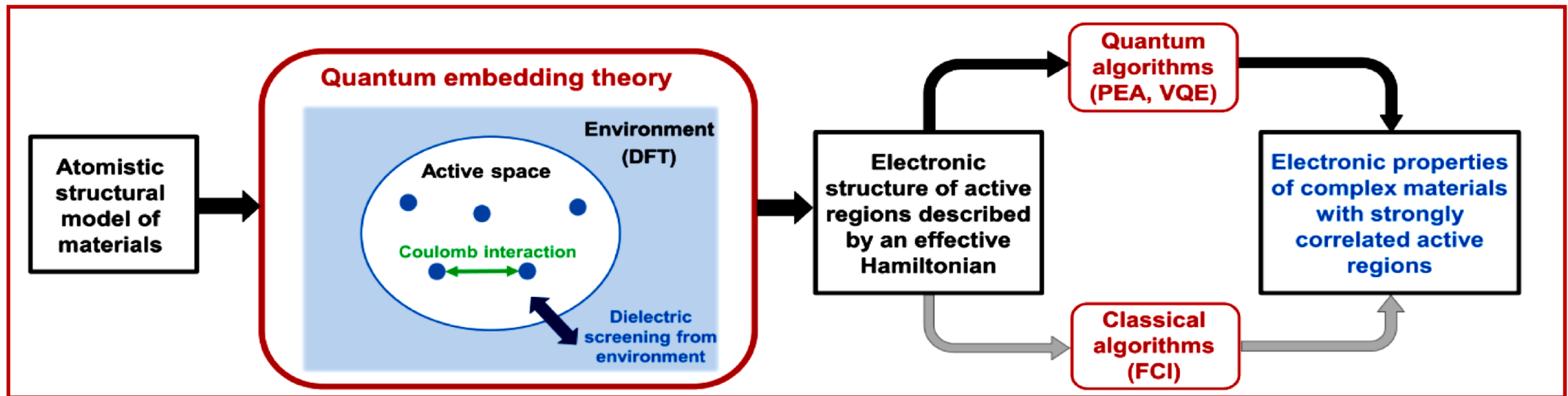




# Quantum simulation of super-heavy elements of Mendeleev's table:

## Quantum gate based approach

*General strategy for quantum simulations of materials using quantum embedding*



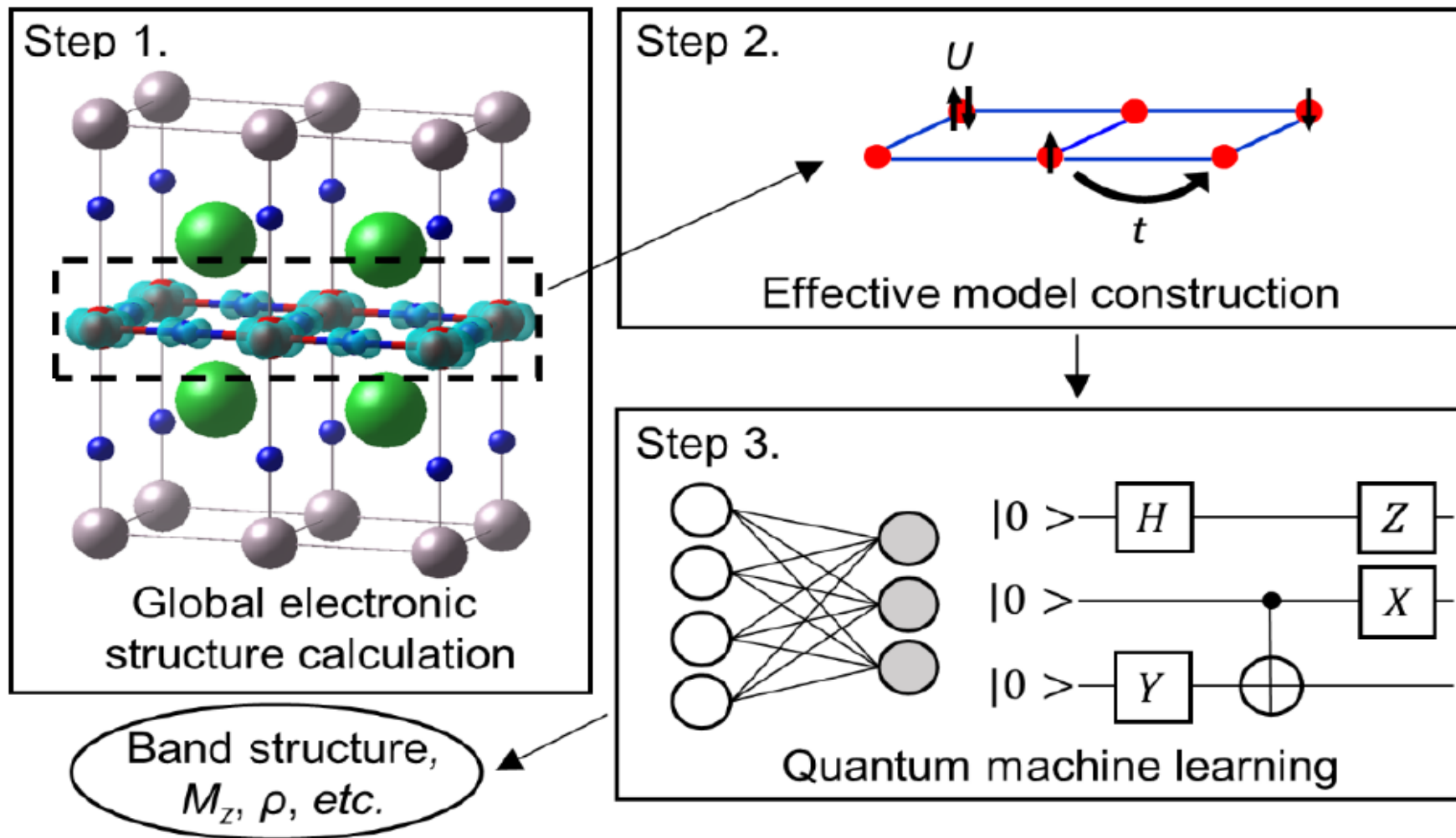
## Quantum simulator

Example of effective application in quantum chemistry

# Quantum simulator

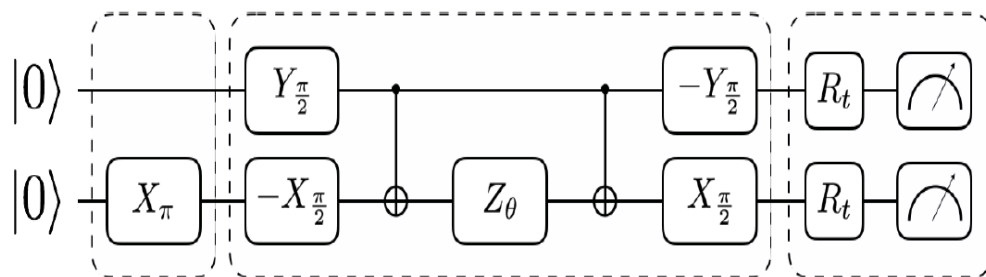
**Example of effective application in quantum chemistry**

## Workflow for calculation of materials properties using quantum algorithm for many-body problems of inorganic systems



The quantum circuit used in VQE to estimate the ground state energy for molecular hydrogen in the minimal basis

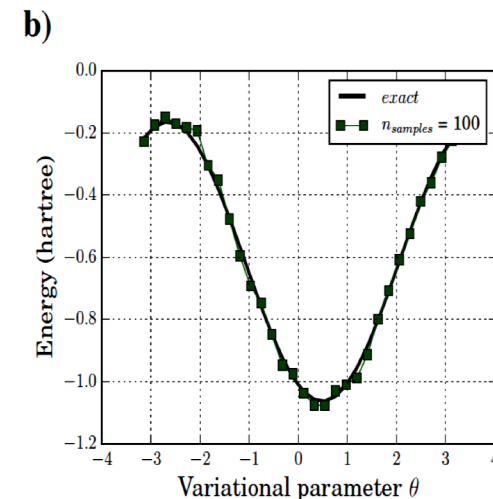
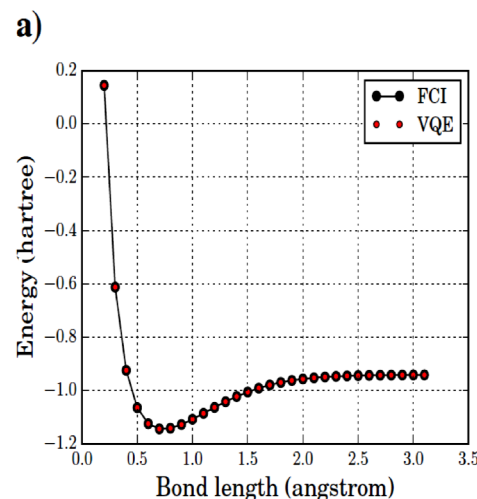
VQE simulation results for molecular hydrogen in the minimal basis (STO-6G)



1. Prepare Hartree-Fock (mean-field) reference state.

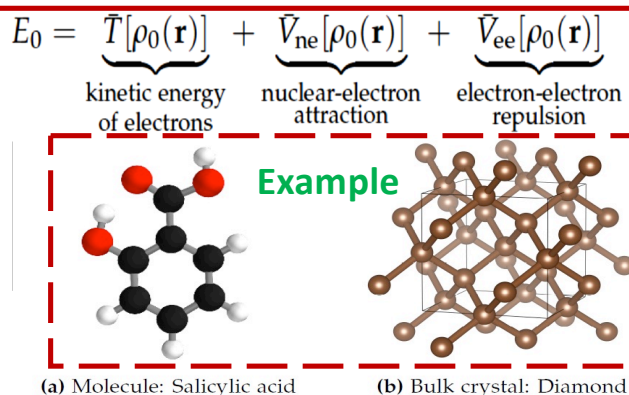
2. Implement unitary coupled-cluster (UCC) ansatz.

3. Apply necessary post-rotations for energy estimation.



$$\hat{H} = \underbrace{-\sum_i \frac{1}{2m_e} \nabla_i^2}_{\text{kinetic energy of electrons}} - \underbrace{\sum_k \frac{1}{2M_k} \nabla_k^2}_{\text{kinetic energy of nuclei}} - \underbrace{\sum_i \sum_k \frac{Z_k}{d_{ik}}}_{\text{electron-nuclear attraction}} + \underbrace{\sum_{i<j} \frac{1}{d_{ij}}}_{\text{electron-electron repulsion}} + \underbrace{\sum_{k<l} \frac{Z_k Z_l}{d_{kl}}}_{\text{nuclear-nuclear repulsion}}$$

The quantum-mechanical Hamiltonian operator of charged particles (electrons and nuclei) interact among each other



$$\bar{E}[\rho(\mathbf{r})] = \underbrace{\bar{T}_{\text{ni}}[\rho_0(\mathbf{r})]}_{\text{kinetic energy of non-interacting electrons}} + \underbrace{\bar{V}_{\text{ne}}[\rho_0(\mathbf{r})]}_{\text{nuclear-electron attraction}} + \underbrace{\bar{V}_{\text{ee}}[\rho_0(\mathbf{r})]}_{\text{classic electron repulsion}} + \underbrace{\Delta \bar{T}[\rho_0(\mathbf{r})]}_{\text{interaction correction of kinetic energy}} + \underbrace{\Delta \bar{V}_{\text{ee}}[\rho_0(\mathbf{r})]}_{\text{non-classical electron repulsion}},$$

Definition of the energy functional as a system of non-interacting electrons

Thank You  
for your attention