# Cosmological implications of EW vacuum instability: constraints on the Higgs-curvature coupling from inflation

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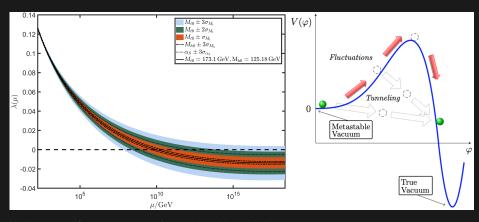
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## Introduction

Experimental values of SM particle masses  $m_h, m_t$  indicate that:

- $\bullet\,$  SM may be valid up to  $\mu_{\rm QG};$  early Universe consistent minimal model.
- currently in metastable EW vacuum  $\rightarrow$  constrain fundamental physics.





#### Introduction

• Decay expands at c with singularity within  $\rightarrow$  true vacuum bubbles:

$$d\langle \mathcal{N}
angle = \mathbf{\Gamma} d\mathcal{V} \Rightarrow \langle \mathcal{N}
angle = \int_{\mathrm{past}} d^4x \sqrt{-g} \mathbf{\Gamma}(x) \, .$$

• Universe still in metastable vacuum  $\rightarrow$  no bubbles in past light-cone:

$$P(\mathcal{N}=0) \propto e^{-\langle \mathcal{N} \rangle} \sim \mathcal{O}(1) \Rightarrow \langle \mathcal{N} \rangle \lesssim 1$$

• Low decay rate  $\Gamma$  today, but higher rates in the early Universe.

Vacuum bubbles expectation value (during inflation)

$$\left\langle \mathcal{N} \right\rangle = \frac{4\pi}{3} \int_0^{N_{\text{start}}} dN \left( \frac{a_{\text{inf}} \left( \eta_0 - \eta \left( N \right) \right)}{e^N} \right)^3 \frac{\Gamma(N)}{H(N)} \le 1$$

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#### Tree-level curvature corrections

- Classical solutions to the tunneling process from false to true vacuum.
- High H's during inflation, CdL $\rightarrow$ HM instanton with action difference

$$B_{\rm HM}(R) pprox rac{384 \pi^2 \Delta V_{\rm H}}{R^2}$$

where  $\Delta V_{
m H} = V_{
m H}(h_{
m bar}) - V_{
m H}(h_{
m fv})$ : barrier height ightarrow decay rate

$$\Gamma_{\rm HM}(R) pprox \left(rac{R}{12}
ight)^2 e^{-B_{\rm HM}(R)}$$

• Curvature effects enter at tree level via non-minimal coupling  $\xi$ :

$$V_{
m H}(h,\mu,R)=rac{\xi(\mu)}{2}Rh^2+rac{\lambda(\mu)}{4}h^4$$

Coleman (1977), Coleman and De Lucia (1980), Hawking and Moss (1987).

#### One-loop curvature corrections

• Minkowski terms to 3-loops, curvature corrections in dS at 1-loop:

$$V_{
m H}(h,\mu,R) = rac{\xi(\mu)}{2}Rh^2 + rac{\lambda(\mu)}{4}h^4 + rac{lpha(\mu)}{144}R^2 + \Delta V_{
m loops}(h,\mu,R) \,,$$

where the loop contribution can be parametrized as

$$\Delta V_{\text{loops}} = \frac{1}{64\pi^2} \sum_{i=1}^{31} \left\{ n_i \mathcal{M}_i^4 \left[ \log\left(\frac{|\mathcal{M}_i^2|}{\mu^2}\right) - d_i \right] + \frac{n_i' R^2}{144} \log\left(\frac{|\mathcal{M}_i^2|}{\mu^2}\right) \right\}$$

• RGI: choose  $\mu=\mu_*(h,R)$  such that  $\Delta V_{\rm loops}(h,\mu_*,R)=0$   $\rightarrow$ 

#### RGI effective Higgs potential

$$V_{\rm H}^{\rm RGI}(h,R) = \frac{\xi(\mu_*(h,R))}{2}Rh^2 + \frac{\lambda(\mu_*(h,R))}{4}h^4 + \frac{\alpha(\mu_*(h,R))}{144}R^2$$

Markkanen et al, "The 1-loop effective potential for the Standard Model in curved spacetime" 2018.

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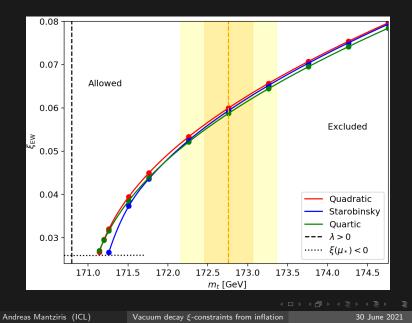
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- 1 Calculate  $\Delta V_{\rm H}$  and plug it in  $\Gamma$ .
- 2 Choose inflationary model by specifying  $V(\phi)$  for the inflaton.
- 3 Complete calculation of  $\langle \mathcal{N} \rangle$  imposing the condition  $\langle \mathcal{N} \rangle \leq 1$ .

$$\langle \mathcal{N} 
angle = rac{4\pi}{3} \int_{0}^{N_{\mathrm{start}}} dN \left( rac{a_{\mathrm{inf}} \left( \eta_{0} - \eta \left( N 
ight) 
ight)}{e^{N}} 
ight)^{3} rac{\Gamma(N)}{H(N)} \leq 1$$

4 Result: constraints on  $\xi \ge \xi_{\langle N \rangle = 1}$ .

#### Results: Bounds on $\xi$



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## Conclusions

Included 1-loop curv. corrections beyond dS  $\rightarrow$  most accurate constraints:

 $\xi$ -bounds for  $m_t \pm 2\sigma$  in each model (numerical errors< 1%)

Quadratic :  $\xi_{\rm EW} \ge 0.060^{+0.007}_{-0.008}$ , Quartic :  $\xi_{\rm EW} \ge 0.059^{+0.007}_{-0.008}$ , Starobinsky :  $\xi_{\rm EW} \ge 0.059^{+0.007}_{-0.009}$ ,

with the minimal assumption that inflation lasts N = 60 *e*-foldings.

that are  $V(\phi)$ -independent,  $N_{\text{start}}$ -independent and  $m_t$ -dependent.

Next step: consider Starobinsky Inflation ( $R^2$ -model):

$$S = \int d^4x \sqrt{-g_J} \left[ \frac{M_P^2}{2} \left( 1 - \frac{\xi h^2}{M_P^2} \right) R_J + \frac{1}{12\alpha^2} R_J^2 + \frac{1}{2} g_J^{\mu\nu} \partial_\mu h \partial_\nu h - \frac{\lambda}{4} h^4 \right]$$
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# Starobinsky $/R^2$ inflation

Due to the conformal transformation  $m_i^2 \to m_i^2 e^{-\sqrt{\frac{2}{3}}\frac{\phi}{M_P}}$ , meaning that the RG scale  $\mu_*$  will be different because  $\Delta V_{\text{loops}}$  will change.

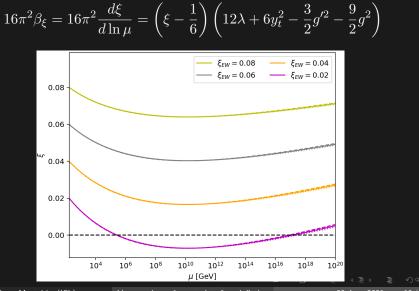
$$\mathcal{L} pprox rac{M_P^2}{2}R + rac{1}{2}\partial_\mu\phi\partial^\mu\phi + rac{1}{2}\partial_\mu\rho\partial^\mu
ho - U^{\mathrm{total}}(
ho, \phi, R)$$
  
h  $U^{\mathrm{total}} = V_{\mathrm{Star}} + m_{\mathrm{eff}}rac{
ho^2}{2} + \lambda_{\mathrm{eff}}rac{
ho^4}{4}$ , where  $\Xi = \xi - rac{1}{6}$  and

$$\begin{split} V_{\text{Star}} &= \frac{3\alpha^2 M_P^4}{4} \left( 1 - e^{-\sqrt{\frac{2}{3}}\frac{\phi}{M_P}} \right)^2,\\ m_{\text{eff}} &= \xi R + 3\alpha^2 M_P^2 \Xi \left( 1 - e^{-\sqrt{\frac{2}{3}}\frac{\phi}{M_P}} \right) e^{-\sqrt{\frac{2}{3}}\frac{\phi}{M_P}} + \frac{\Xi}{M_P^2} \partial_\mu \phi \partial^\mu \phi,\\ \lambda_{\text{eff}} &= \lambda + 3\alpha^2 \Xi^2 e^{-2\sqrt{\frac{2}{3}}\frac{\phi}{M_P}} + \frac{4\left(\xi R\right)_{\text{eff}}}{\Xi^{-2}M_P^2} + \frac{4\Xi^3}{M_P^4} \partial_\mu \phi \partial^\mu \phi. \end{split}$$

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## Additional slides - Running of non-minimal coupling $\xi$

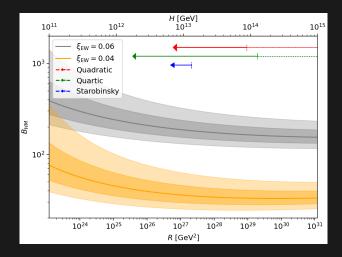


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## Additional slides - Curvature effects on the bounce action



Shaded areas:  $1\sigma$ ,  $2\sigma$  deviation from the central  $m_t$ ; a heavier top quark decreases the value of  $B_{\rm HM}$  and vice versa. Solid red, blue and green arrows: last 60 *e*-foldings in quadratic, Starobinsky and quartic inflation.

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#### Additional slides - Numerical solution

Solve the system of coupled differential equations

$$\frac{d^2\phi}{dN^2} = \frac{V(\phi)^2}{M_P^2 H^2} \left(\frac{d\phi}{dN} - M_P^2 \frac{V'(\phi)}{V(\phi)}\right)$$
$$\frac{d\tilde{\eta}}{dN} = -\tilde{\eta}(N) - \frac{1}{a_{\inf}H(N)}$$
$$\frac{d\langle \mathcal{N} \rangle}{dN} = \gamma(N) = \frac{4\pi}{3} \left[a_{\inf} \left(\frac{3.21e^{-N}}{a_0 H_0} - \tilde{\eta}(N)\right)\right]^3 \frac{\Gamma(N)}{H(N)}$$

where  $\tilde{\eta}=e^{-N}\eta$  and  $\eta:$  conformal time and we set the end of inflation at

$$\frac{\ddot{a}}{a}\Big|_{\phi=\phi_{\rm inf}} = H^2 \left[1 - \frac{1}{2M_P^2} \left(\frac{d\phi}{dN}\right)^2\right]\Big|_{\phi=\phi_{\rm inf}} = 0$$

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# Additional Slides - Inflationary Models

• Quadratic inflation, where  $m = 1.4 \times 10^{13}$  GeV, with

$$V(\phi) = \frac{1}{2}m^2\phi^2$$

• Quartic inflation, where  $\lambda = 1.4 \times 10^{-13}$ , with

$$V(\phi)=rac{1}{4}\lambda\phi^4$$

• Starobinsky inflation (Starobinsky-like power-law model), where  $\alpha = 1.1 \times 10^{-5}$ , with

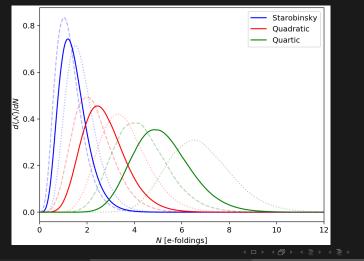
$$V(\phi) = \frac{3}{4} \alpha^2 M_P^4 \left( 1 - e^{-\sqrt{\frac{2}{3}} \frac{\phi}{M_P}} \right)^2$$

Quadratic and quartic models are simple but not realistic; Starobinsky inflation complies with data and can link different inflationary models.

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## Additional Slides - Results: Bubble nucleation time

- If bubbles form at  $N < 1 \rightarrow$  bounds maybe unreliable due to  $B_{\rm HM}^{\rm dS}$ .
- If bubbles form at  $N \gg 60 \rightarrow$  bounds would depend on early times.



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# Additional Slides - Results: Significance of the total duration of inflation

- Inflation can last for many orders of magnitude longer than 60 *e*-folds.
- $\bullet\,$  We study early time behavior by splitting the  $\langle {\cal N} \rangle {\text -integral}$

$$\langle \mathcal{N} \rangle (N_{\mathrm{start}}) = \langle \mathcal{N} \rangle (60) + \int_{60}^{N_{\mathrm{start}}} rac{d\mathcal{V}}{dN} \Gamma(N) \, dN \; ,$$

where we set  $\langle \mathcal{N} \rangle(60) = 1$  and slow roll applies to the 2nd term.

•  $B_{
m HM}pprox$  constant at early times, so that

$$\langle \mathcal{N} \rangle (N_{\text{start}}) \approx 1 + \frac{4\pi e^{-B_{\text{HM}}}}{3} N_{\text{start}} \,.$$

• Contributing if  $N_{\rm start}\gtrsim e^{B_{\rm HM}}\sim 10^{60}\gg 60\,e$ -folds but not infinite.