# Hybrid Potential Simulations of Enzyme Catalysis

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General Introduction

- Hybrid QC/MM Potentials
- Applications

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## Simple Chemical Reactions

#### $CI^{-} + CH_{3}CI$ $\leftarrow$ $CICH_{3} + CI^{-}$



## Quantum Chemistry

Schrödinger Equation:



## Quantum Chemical Methods

- Ab Initio:
  - Density functional theory (DFT)
  - Molecular orbital (MO) methods; e.g. Hartree-Fock (HF)
     Precise but slow.
- Semi-Empirical:
  - MO-based; e.g. AM1, MNDO, PM3
  - Faster but more approximate.



# Reaction coordinate: $R_1 - R_2$

# Energy profile in vacuum.









## **Complex Chemical Reactions**

Two problems linked to size:

- Calculation of the potential energy:
  - Quantum chemical methods too expensive.
- Exploring the potential energy surface: Sampling of relevant conformations.

#### Hybrid Potentials

A combination of methods that treat different parts of a system at varying levels of precision.

First QC/MM potentials conceived to study enzyme reactions:

A. Warshel and M. Levitt. Theoretical Studies of Enzymatic Reactions: Dielectric Electrostatic and Steric Stabilization of the Carbonium Ion in the Reaction of Lysozyme. J. Mol. Biol. 103, 227-249 (1976).



# An Enzyme Example



## QC/MM Methods I

#### QC Potentials:

- Ab initio DFT and HF Gaussian basis functions.
- Various semi-empirical methods.

#### MM Potentials:

• AMBER, CHARMM, OPLS-AA, UFF force fields.

#### Boundary:

- Periodic boundary conditions.
- Truncated systems.

## QC/MM Methods II

QC/MM Non-bonding Interactions:

- Electrostatic full QC (e<sup>-</sup> and n<sup>+</sup>)/MM (point charge).
- Lennard-Jones.

QC/MM Covalent Interactions:



## QC/MM Methods III

• Solve Hartree-Fock or Kohn-Sham equations to self-consistency each time an energy is calculated.

 $\hat{H}_{\rm Eff}\Psi = E\Psi$ 

- Use the energy and forces for:
  - Geometry optimization
  - Reaction path location
  - Molecular dynamics simulation
  - Free-energy determination

# fDynamo

- M. J. Field. A Practical Introduction to the Simulation of Molecular Systems. Cambridge University Press, Cambridge, 1999.
- M. J. Field, M. Albe, C. Bret, F. Proustde Martin and A. Thomas. The Dynamo Library for Molecular Simulations using Hybrid Quantum Mechanical and Molecular Mechanical Potentials. J. Comput. Chem. 21, 1088-1100 (2000).



## fDynamo Characteristics

- Fortran 90/95.
- A library of modules not a program.
- A variety of simulation approaches, including:
  - QC, MM and QC/MM potentials.
  - Geometry optimization.
  - Saddle point and reaction path finding.
  - Normal mode analysis.
  - MC and MD simulations.
  - Free-energy calculations.
- Serial and coarse-grained parallel versions.

## Beyond fDynamo

Limitations of Fortran 90/95 include:

- Absence of many of the capabilities of modern computer languages (e.g. objects and inability to interact with the operating system).
- Lack of good open-source compilers.

Replacement approaches considered included C, C++, Eiffel, Fortran 2000, Java, Objective C, Python and Ruby.

## pDynamo Characteristics

- Python/C:
  - Python for the majority of operations .
  - C for speed.
- A series of Python packages.
- Object-oriented structure.
- Equivalent functionality to fDynamo and more:
  - Arbitrary crystal symmetry.
  - Coupling to external programs (e.g. ORCA).
  - DFT methods.
  - More external file formats, ...

# pDynamo

- M. J. Field. A Practical Introduction to the Simulation of Molecular Systems. Cambridge University Press, Cambridge, 2007 (2nd edition).
- M. J. Field. The pDynamo Library for Molecular Simulations using Hybrid Quantum Mechanical and Molecular Mechanical Potentials. J. Chem. Theo. Comput. 4, 1151-1161 (2008).

The library is available at:

http://www.pdynamo.org

#### MARTIN J. FIELD

#### A Practical Introduction to the Simulation of Molecular Systems



## Applications to Enzymes I

- Acetyl-coenzyme A synthase (Amara et al., JACS '05).
- AIRase (Proust et al., JACS '00).
- Aldehyde dehydrogenase (Wymore et al., CBI '03).
- cAMP-dependent protein kinase (Díaz and Field, JACS '04).
- Chorismate mutase from *B. subtilis* (Martí *et al.*, JACS '01, Crehuet and Field, JPC '07).
- Fluorescent Proteins (Adam *et al.*, PNAS '08; Lelimousin *et al.*, Biochem. '09, JACS '10).
- HG(X)PRTase (Thomas et al., JACS '02, '06; Crehuet et al., JMGM '05).
- Hydrogenase from D. gigas (Amara et al., JACS '99; Galván et al., Proteins, '08).
- Influenza neuraminidase (Thomas et al., JACS '99).
- PBPs (Oliva et al., Proteins '03).
- PFOR (Amara et al., Angew. Chem. Intl. Ed. '07).

## Applications to Enzymes II

- Hydrogenase from *D. gigas* (Amara *et al.*, JACS '99):
  - DFT/MM hybrid potential.
- Influenza neuraminidase (Thomas et al., JACS '99):
  - QC/MM path-integral free-energy simulations.
- AIRase (Proust *et al.*, JACS '00):
  - Ab initio corrections to the semi-empirical QC/MM energies.
- Chorismate mutase from *B. subtilis* (Crehuet and Field, JPC '07):
  - TPS simulations.

#### Application to HGXPRTase I

 Malaria causes one million deaths per year in Africa alone.

• The causative agent, the protozoan *Plasmodium falciparum*, cannot synthesize purine nucleotides but scavenges its host's purine bases.



- Hypoxanthine-guanine-xanthine-phosphoribosyl-transferase (HGXPRTase) is a possible target for anti-malarial drugs.
- Human HGPRTase has a much reduced affinity for xanthine.

#### Application to HGXPRTase II

A. Thomas and M. J. Field (JACS '02)
R. Crehuet, A. Thomas and M. J. Field (JMGM '05)
A. Thomas and M. J. Field (JACS '06)



#### Application to HGXPRTase III



#### Application to HGXPRTase IV

#### S<sub>N</sub>1 mechanism:

• Favoured by KIE measurements.

#### S<sub>N</sub>2 mechanism:

• X-ray crystallographic structure.



Immucillin HP transition state analog.

And what type of  $S_N 1$  or  $S_N 2$ ?  $A_N D_N$ ,  $D_N A_N$ , ...

#### Application to HGXPRTase V



## Application to HGXPRTase VI



#### Application to HGXPRTase VII

A range of simulation approaches are necessary:

- Local approaches:
  - Critical point determination.
  - Reaction paths.
- Global approaches:
  - Molecular dynamics.
  - Free-energy calculations.

#### Nudged-Elastic-Band Method

Method due to H. Jónsson and co-workers.



## Nudged-Elastic-Band II



#### Nudged-Elastic-Band III

#### Reaction Coordinate Variables

#### Temperature-Dependent Path







## Free Energies

Thermodynamic average of a property  $\chi$ :

$$\langle \chi \rangle = \int \chi(\Gamma) \rho(\Gamma) d\Gamma$$

Potential of mean force:

$$\mathcal{W}(s) \propto -k_{\rm B}T \ln \int \exp(-\mathcal{V}(\Gamma,s)/k_{\rm B}T) d\Gamma$$

#### Application to HGXPRTase VIII



### Application to HGXPRTase IX



#### Application to HGXPRTase X



Stepwise pathway favoured with a barrier of ~  $80 \text{ kJ} \text{ mol}^{-1}$ .

### Application to HGXPRTase XI



 Comparison to the human enzyme — HGPRTase.

 Comparison of hypoxanthine and xanthine.

Pf – blue ; human – magenta

## Application to HGXPRTase XII

- Overall mechanisms and energetics very similar.
- Proton transfer barriers higher in human enzyme.
- "Significant" differences in transition state structures:

Distances (Å)	TS Pf	TS Human
C1'N9	2.56 ± 0.08	1.82 ± 0.01
C1'O2A	1.80 ± 0.22	2.29 ± 0.08

#### Perspectives - HG(X)PRTase

- Preferred mechanism:
  - Proton transfer
  - Glycosyl transfer
- Agreement with experimental data barrier heights, KIEs.
- Ligand binding affinities.

### Proton Transfer Pathways in Hydrogenase I

I. Galván *et al.*, Proteins, '08 I. Galván and M. J. Field, J. Comput. Chem., '08



 $H_2 \Leftrightarrow 2H^+ + 2e^-$ 

- Ni-Fe hydrogenase (A. Volbeda et al., Nat. '95).
- Molecular channels (Y. Montet et al., Nat. Struct. Biol. '97).
- Proton channels or pathways?

## Proton Transfer Pathways in Hydrogenase II

Strategy:

- Hypothesize possible pathways from X-ray structures.
- Identify individual proton transfer events.
- Evaluate partial NEB pathways.
- Piece together full profiles.

#### Proton Transfer Pathways in Hydrogenase III



 $\Delta E^{\ddagger} \sim 40 \text{ kJ mol}^{-1}$ 

 $\Delta E^{\ddagger} \sim 150 \text{ kJ mol}^{-1}$ 

# Fluorescent Proteins I

Mickael Lelimousin (in collaboration with Virgile Adam, Dominique Bourgeois and Antoine Royant).

Irreversible transition between green and red emitting states in photoconvertible FPs.





## Fluorescent Proteins II



• Excited state NEB pathway calculations using a CI method.



## Fluorescent Proteins III



Analysis and identification of factors important for photoconversion.