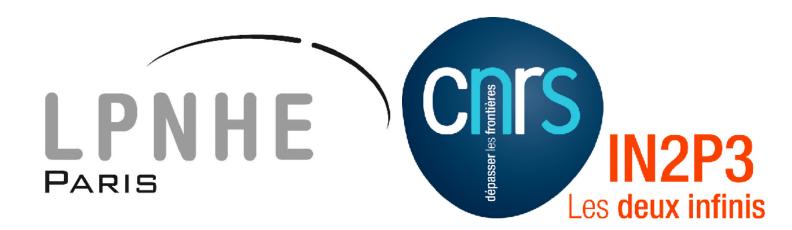


### **Clock and GNSS performances** LPNHE Neutrino group Discussion SYRTE-LPNHE — March 17th 2021







### Quantify time stability

Signal y(t) (usually discrete measurements  $y_i = y(t_i)$ ) How to compute stability?

$$S_{y}(\omega) = \frac{|\tilde{y}(\omega)|^{2}}{T}$$

$$\sigma_{\text{Allan}}(n) = \sqrt{\frac{1}{2\left(\frac{N}{n}-1\right)} \sum_{l=1}^{\frac{N}{n}-1}}$$

→ Frequency domain: **power spectral density (PSD)**  $\left|\int_0^T y(t) \exp(i\omega t) dt\right|^2$  $\rightarrow$  Time domain: Allan variance (AV)  $\left(y_{l+1}^{(n)} - y_{l}^{(n)}\right)^{2} \text{ with } y_{l}^{(n)} = \frac{1}{n} \sum_{i=1}^{n} y_{ln+i}$ (1,5)Many variations around this formula like **modified AV**:

$$\sigma_{\text{Mod}}(\tau) = \sqrt{\frac{1}{2n^2(N-2n+1)}} \sum_{j=1}^{N-2n+1} \left(\sum_{i=j}^{j+n-1} y_{i+n}^{(n)} - y_i^{(n)}\right)^2_{(3,5)}}$$

**Hyper-Kamiokande** 



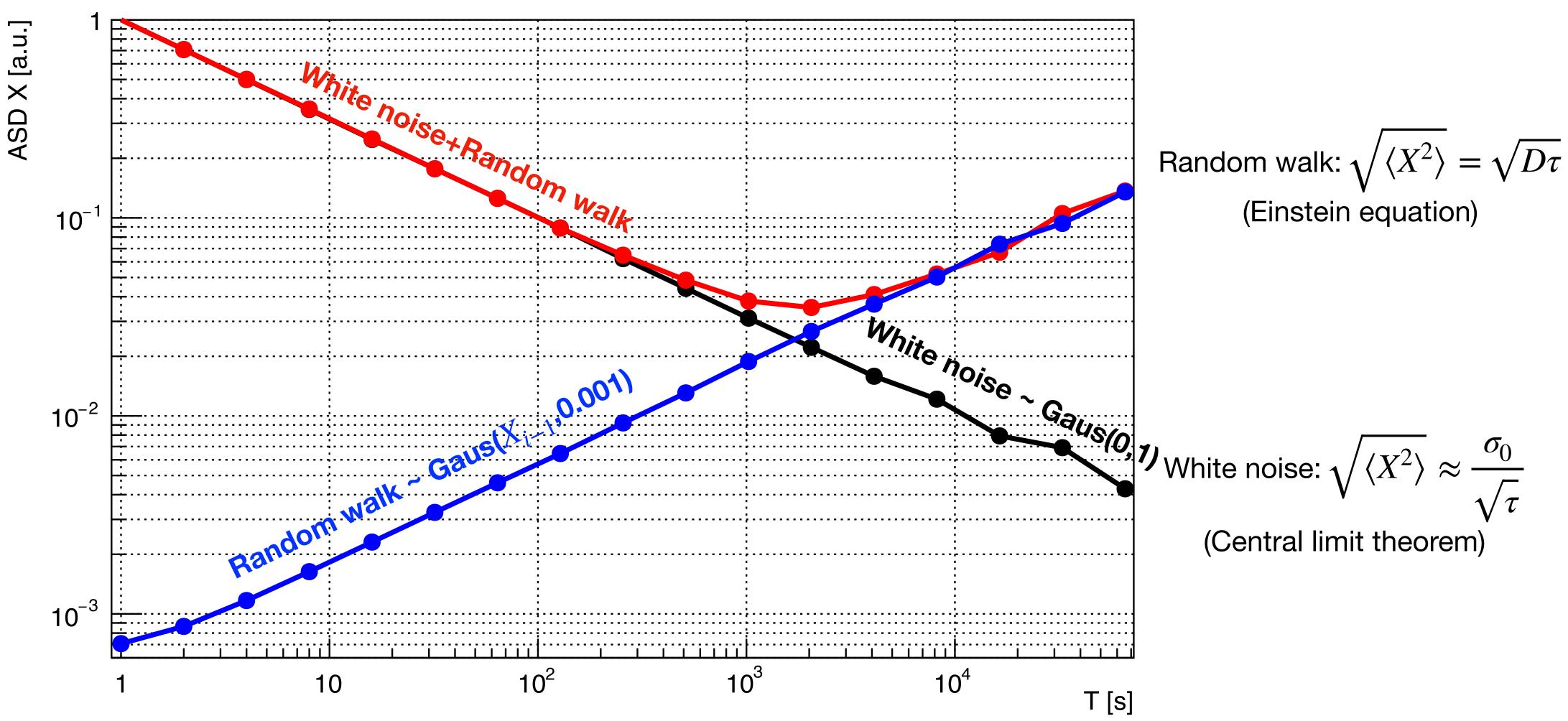






### Generating data and ASD

#### Allan Standard Deviation













## Short-term stability: jitter definition LPNHE

### Jitter: fluctuations on both amplitude, frequency and phase

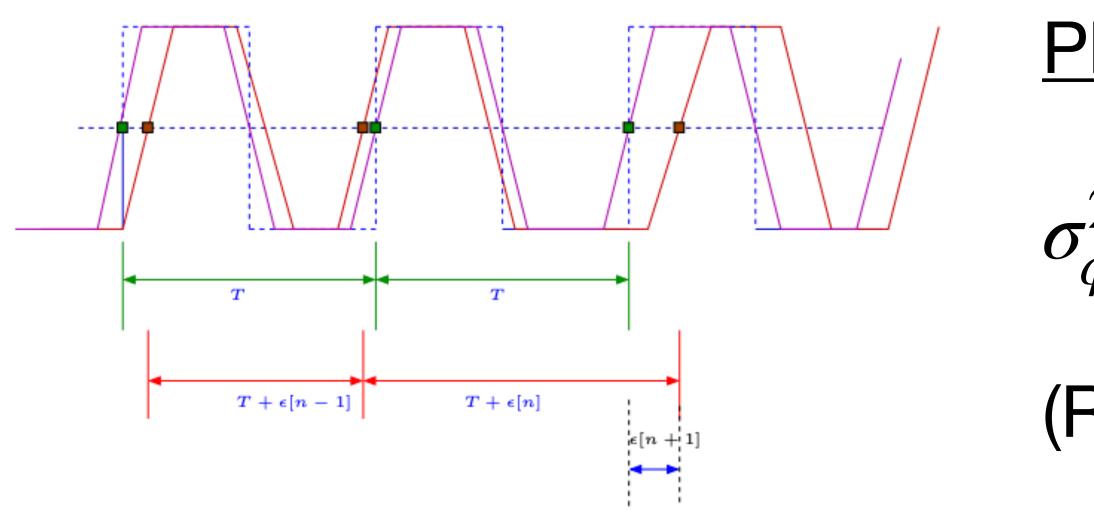


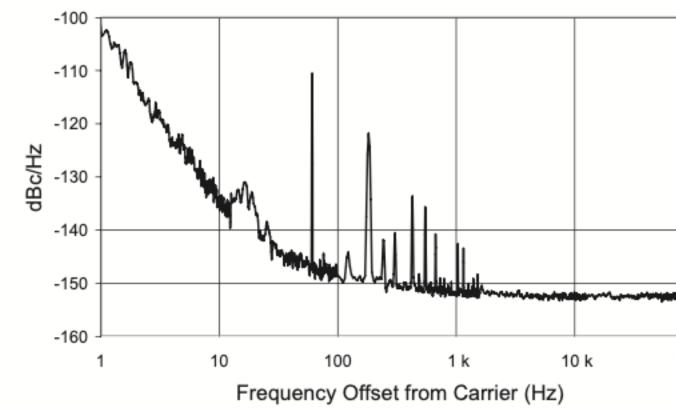
Figure 8. Sampling Clock Jitter: The time duration (period) between successive triggers vary as a result of the phase noise. Ideal clocks preserve constant period T, whereas, practical clocks vary the value randomly, leding to jitter

 $2\pi f_0$  $2\pi f_0$ Not quite the same as  $AV \rightarrow is$  there a known relation? https://documents.epfl.ch/users/p/pu/pulikkoo/private/report\_pn\_jitter\_oscillator\_ratna.pdf Discussion SYRTE-LPNHE — March 17th 2021



PRS10 Single Side Band Phase Noise

 $\sin \pi \tau f$ 



### Phase noise:

 $\sigma_{\phi}$ 

$$a_{b}^{2}(\tau) = \left\langle \bar{\phi}^{2} \right\rangle = \frac{1}{\tau^{2}} \left\langle \left[ \int_{t_{k}-\tau}^{t_{k}} \phi(t) dt \right]^{2} \right\rangle$$

r  $\infty$ 

D(J)

(RMS phase) jitter (@1 s):



100 k





### **Clock recommendations**

- 1- Microsemi 5071A → 70-80 k€
- 2- OSA 3235B → 50 k€
- 3- PHM1008 → 55 k€
- 4- Cold Rb clock → >100 k€

Off-the-shelf systems:

- 5- SRS FS725  $\rightarrow$  3 k€
- 6- SRS PRS10  $\rightarrow$  1.5 k€



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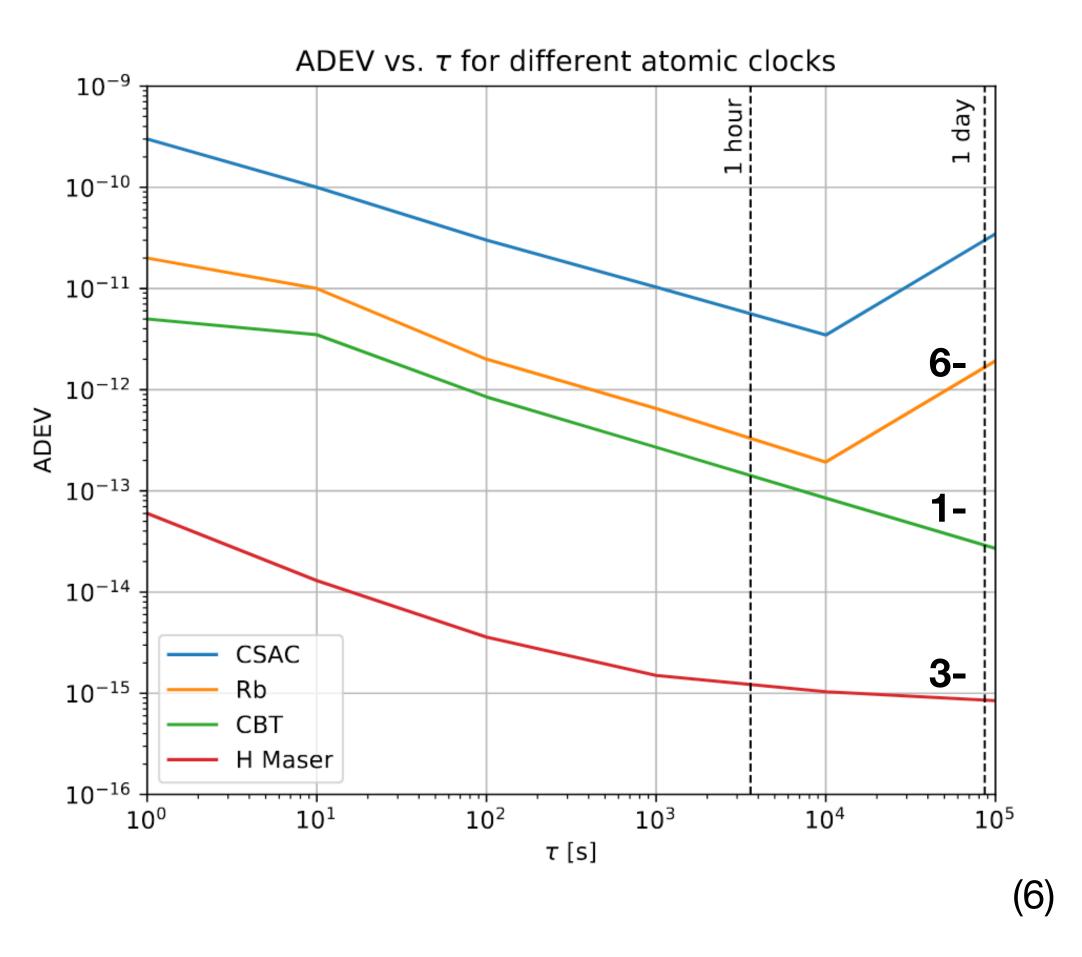


### Email from Michel with useful clock recommandations and price tags





### **Clocks performances from litterature LPNHE**



Active Hydrogen Maser.



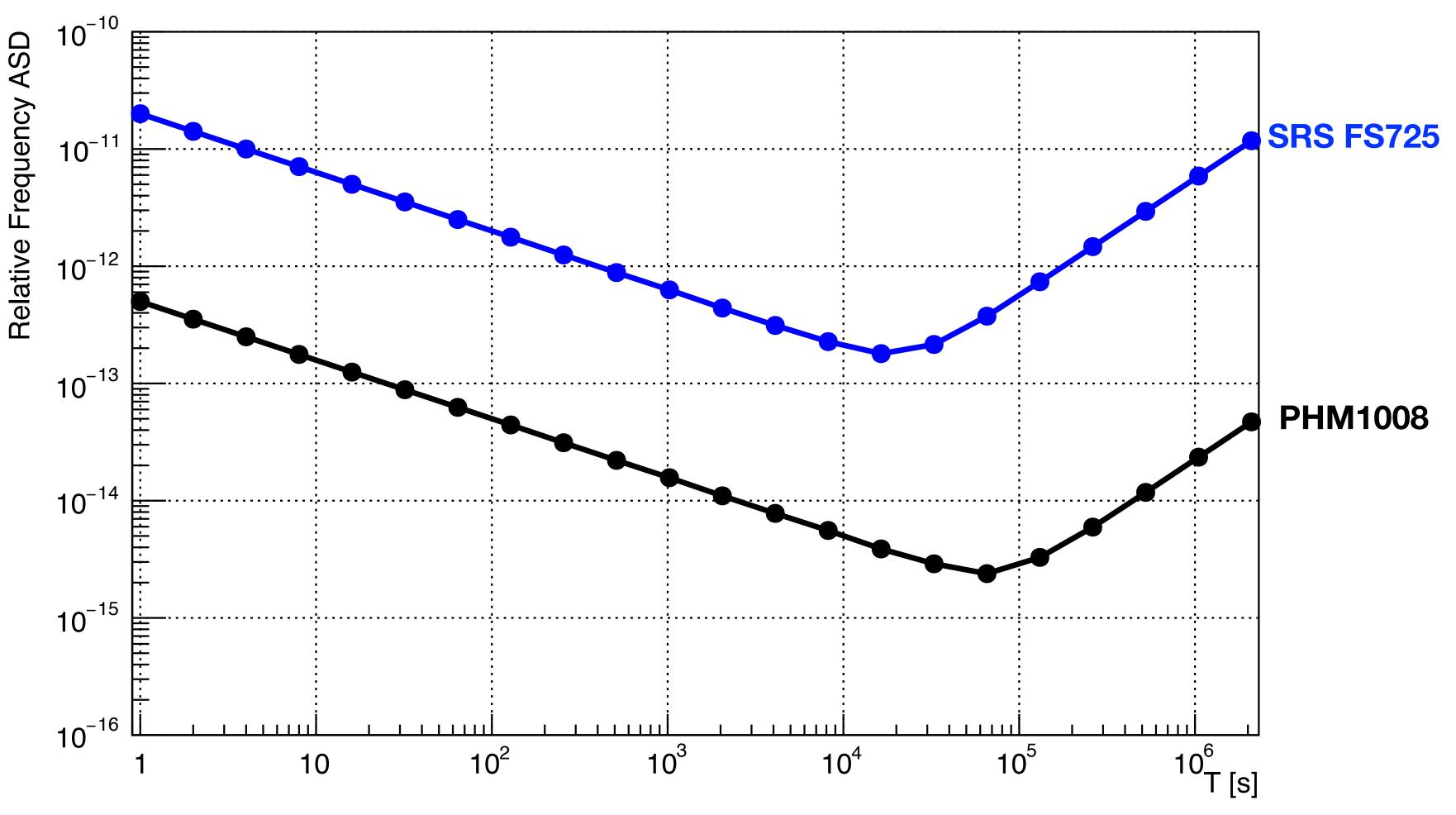
Fig. 2. Comparison of ADEV for different frequency standard technologies. The curves shown from top to bottom are the Microchip CSAC, SRS PRS10 Rb frequency standard, Microchip 5071A Cesium Beam Tube, and Vremya













### Reproducing data sheets



#### Allan Standard Deviation





- Jitter@1sec ("wander"):
- Standard oscilloscope (Tektronic MSO Series 5?)
- Phase noise analyzer (Integrated PSD/jitter)

Long-term ASD:

- Is this useful or should we just trust specs? - How are the parameters (frequencies?) computed? - Are these oscilloscopes/analyzers stable enough > 1day? - Use a more stable clock as comparison?
- Impact of temperature and humidity drifts on clock?
- Maintenance?



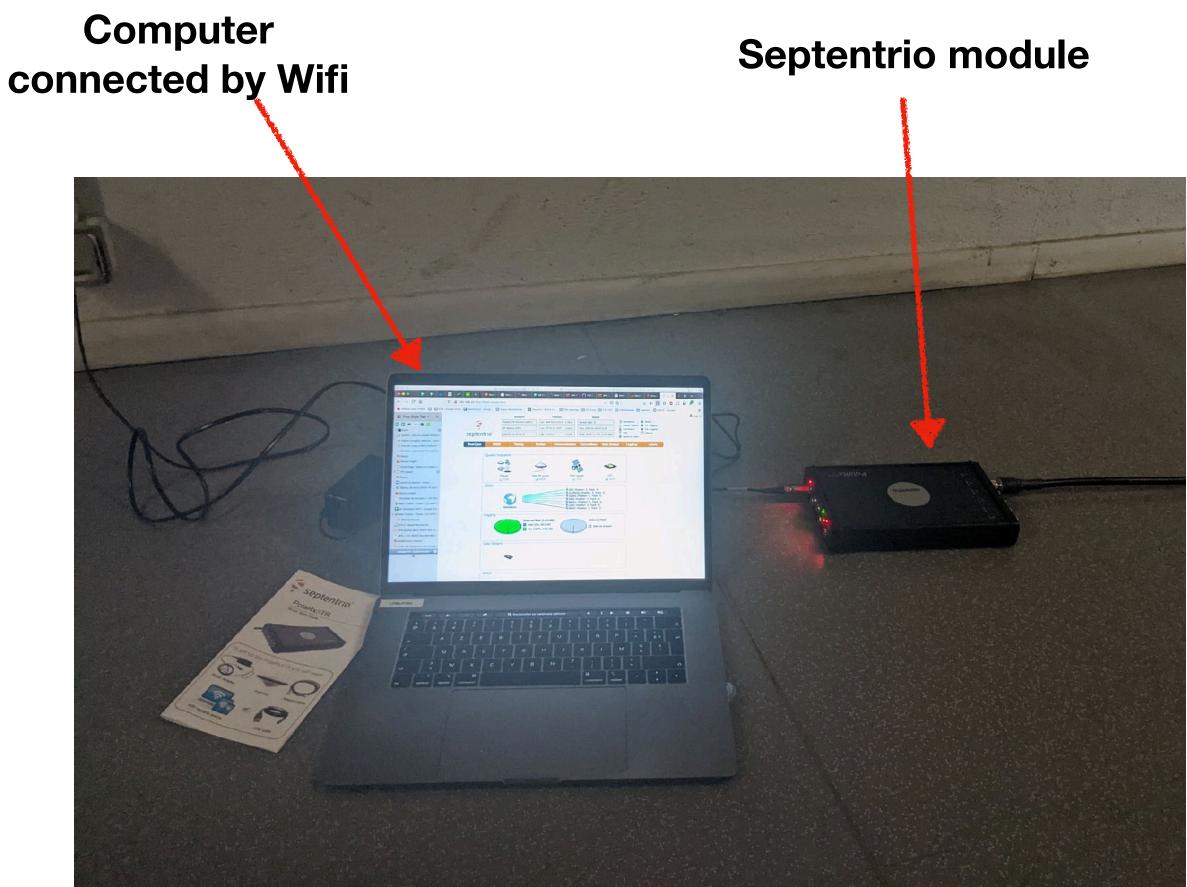
### **REGISTE How to measure time stability of clocks? LPNHE**







### First test of GNSS antenna

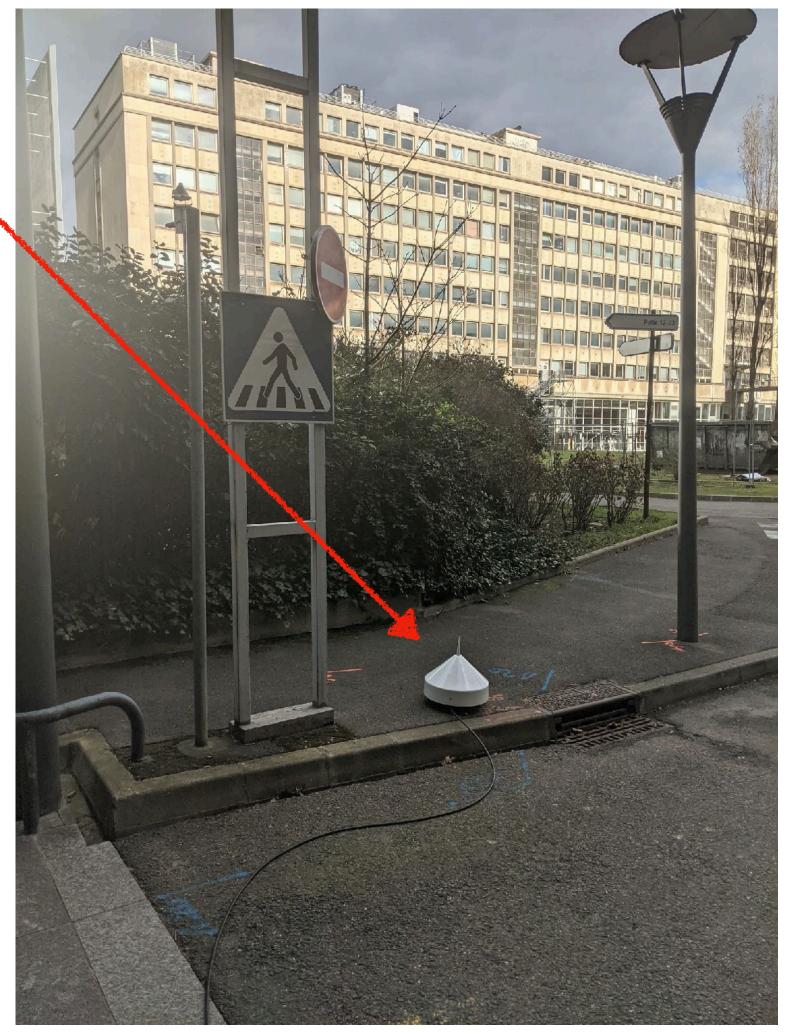




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Antenna



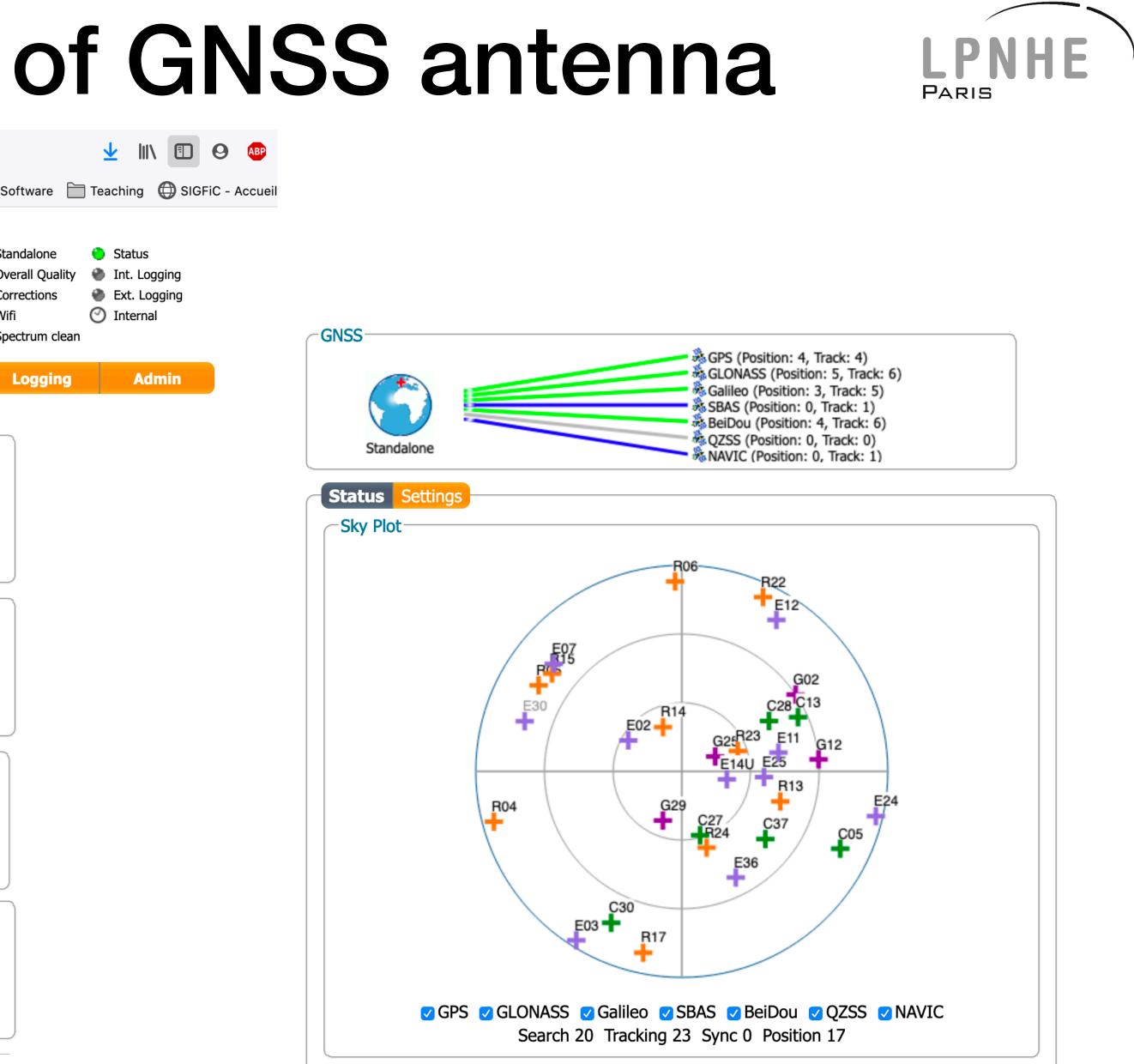
#### Friday February 26th



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☑			Neutrine IN2D2	Ev 🛅 T2K meetin		••• 🕑 🏠
Google Drive Séminaires - C		Receiver PolaRx5TR-3222543 (SE IP Address (Eth): Uptime: 0d 00:08:19		Position           50'53.9518"         2.780m           '24.1595"         4.101m	gs         CC-100IS           Status           Tracked Sats: 21           Time: 2021-02-26 14           Temp: 38.00 °C — V	4:51:21
Overview		Timing licators Dverall 7/10	Station Main RF power 10/10	GPS ( GLON Galilee SBAS BeiDo QZSS	Corrections signals 7/10 Position: 4, Track: 4) ASS (Position: 4, Track o (Position: 3, Track: 0) U (Position: 0, Track: 0) U (Position: 5, Track: 0) U (Position: 0, Track: 0) C (Position: 0, Track: 0)	ck: 5) 5) ) 6)
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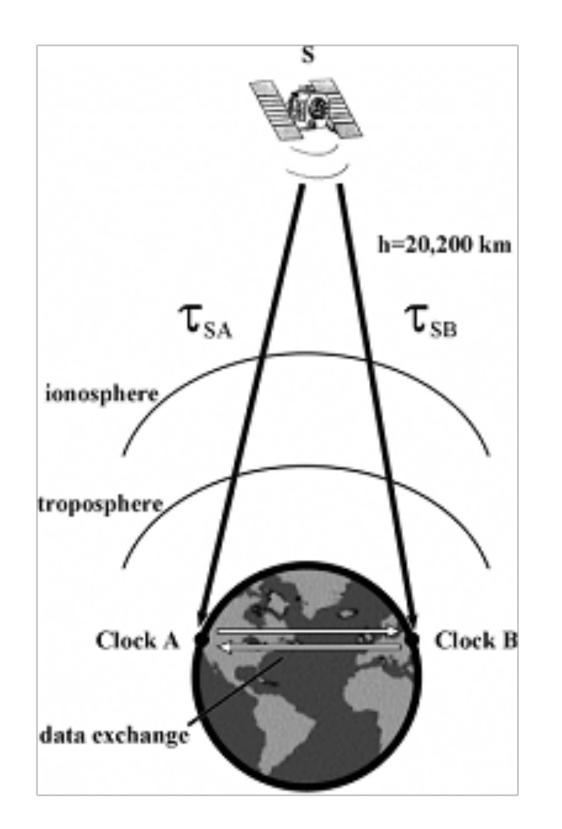
#### It works (but only outside...)!





#### **GPS frequency stability and time uncertainty** LPNI Paris

#### Technique

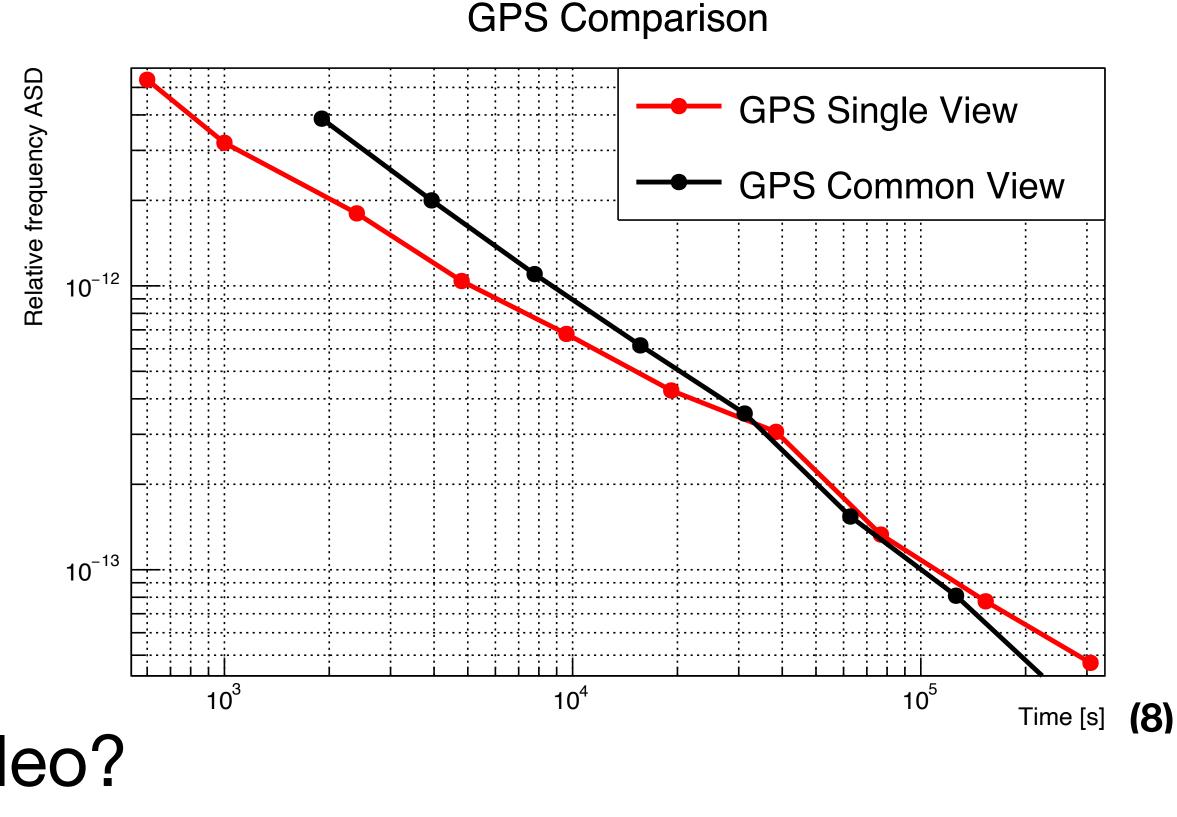


**One-Way** Common View Melting pot Carrier-Phase

Not quite  $1/\sqrt{T}$  dependence...? Old paper: how about now? Galileo?



Timing Uncertainty, 24 h, 2σ	Frequency Uncertainty, 24 h, 2σ
< 20 ns	< 2 x 10 <sup>-13</sup>
≈ 10 ns	≈ 1 x 10 <sup>-13</sup>
< 5 ns	< 5 x 10 <sup>-14</sup>
< 500 <u>ps</u>	< 5 x 10 <sup>-15</sup>



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Η	Ε	

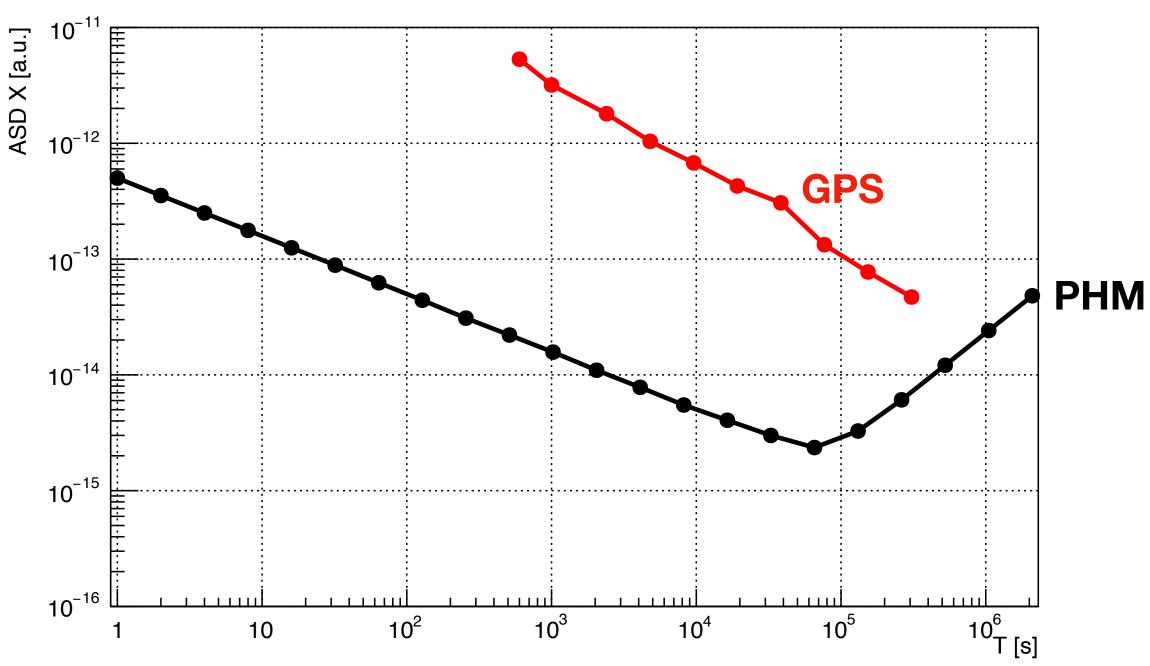


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## Locking clock PPS on GPS

Allan Standard Deviation

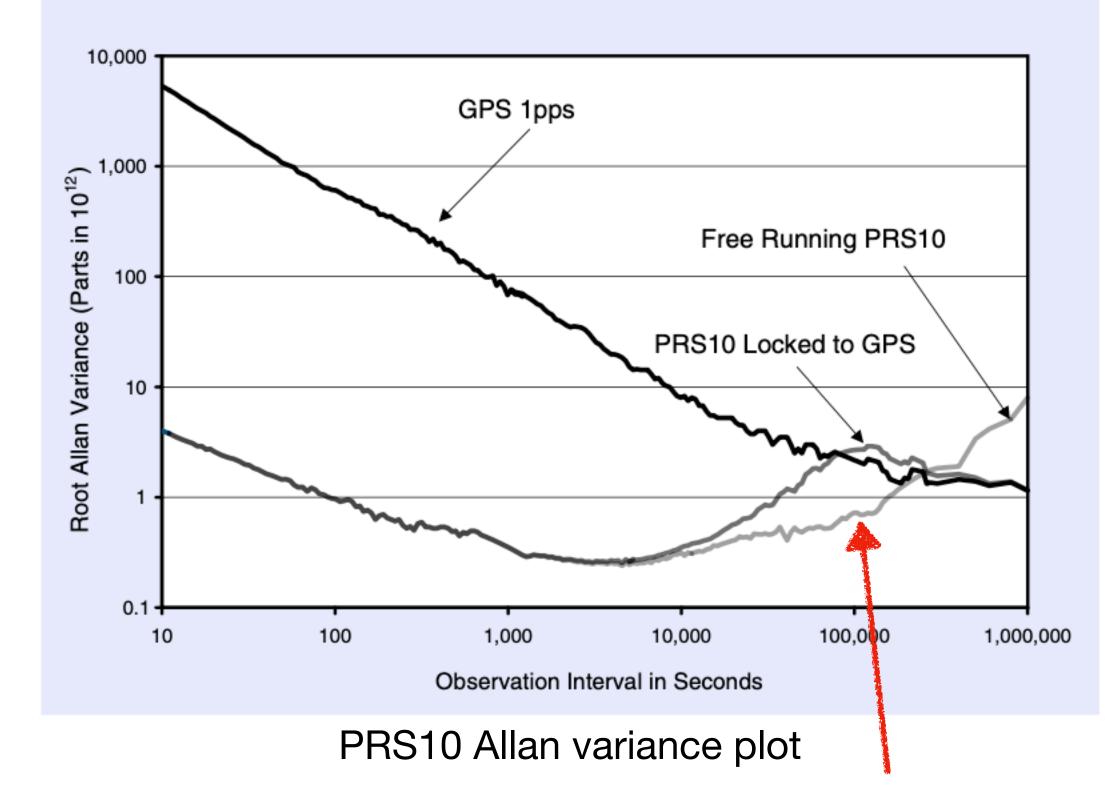


What configuration is recommended?



Discussion SYRTE-LPNHE — March 17th 2021





Locking doesn't seem to be the best of both  $\rightarrow$  why?

# Is 1pps locking automatically done in the GNSS antenna control box?





- Install and test software interfaces
- $\rightarrow$  Backend API necessary/available?
- Install antenna on Jussieu roof (in the coming months)
- Test long-term stability of GNSS 1pps with and without atomic clock
- $\rightarrow$  what equipment?
- Test locking method
- Calibrate cables and antenna at SYRTE



### GNSS: what's next?







- (1) Statistics of Atomic Frequency Standards, D. W. Allan, Proceedings of the IEEE, 54 2 221-230, Feb. 1966, doi: 10.1109/PROC.1966.4634.
- (2) Characterization of frequency stability, J. A. Barnes, A. R. Chi, et al., IEEE Trans. Instrum. Meas. IM-20 **2** 105 (1971).
- (3) Long-range time transfer with optical fiber links and cross comparisons with satellite-based methods, N. Kaur, PhD thesis 2019.
- (4) T4Science pH Maser 1008 Specifications sheet
- (5) Handbook of Frequency Stability Analysis, W.J. Riley, <u>here</u>
- (6) A Review of Contemporary Atomic Frequency Standards, B.L. Schmittberger, D.R. Scherer, arXiv:2004.09987
- Lombardi, L.M. Nelson, A.N. Novick, V.S. Zhang Cal Lab 8. 26-33 satellite techniques, F. Riedel et al 2020 Metrologia 57 045005
- (7) cRb-Clock Preliminary Data sheet, SpectraDynamics, <u>here</u> (8) Time and Frequency Measurements Using the Global Positioning System, M.A. (9) Direct comparisons of European primary and secondary frequency standards via
- Hyper-Kamiokande

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### Biblio



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### Backup

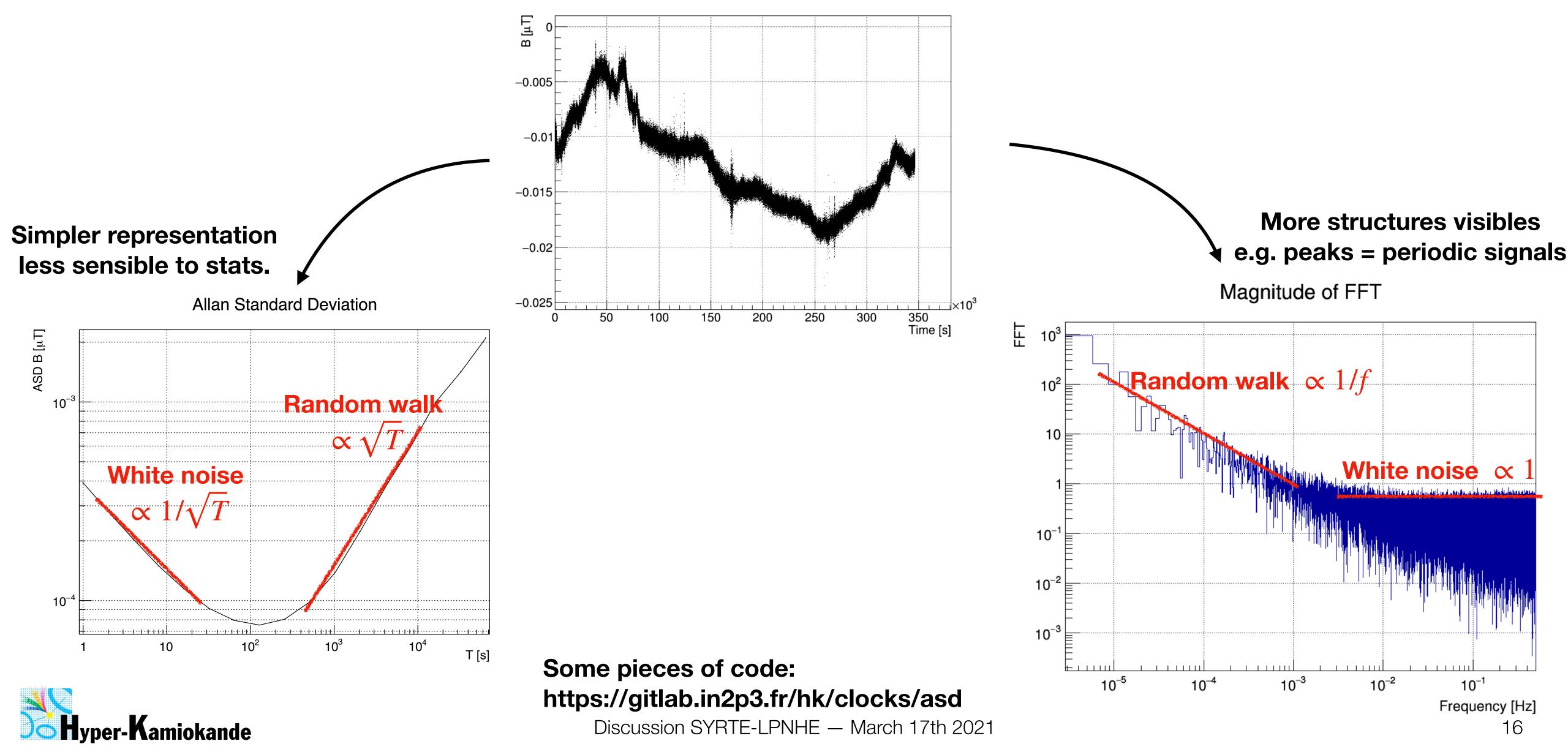








## Visualizing things





Data



## **Relation between PSD and AV**

(via Parseval-Plancherel theorem), we have:

$$\sigma_{\text{Allan}}\left(n\right) = \frac{2}{\pi n\tau}.$$

(Averaging over all noise frequency scales gives time stability)





- Similarly to the usual variance is related to the Discrete Fourier transform
  - $\frac{2}{\tau n\tau} \int_{0}^{\infty} \mathrm{d}u S_{y} \left(\frac{u}{\pi n\tau}\right) \frac{\sin^{4} u}{u^{2}} \int_{0}^{\infty} \frac{\mathrm{d}u}{u^{2}} \int_$



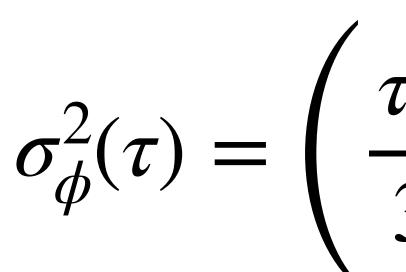




# SCIENCES SORBONNE UNIVERSITÉ Why phase noise instead of frequency noise? LPNHE

phase differences defined by the up-front (or down-front) instead of looking at the instantaneous period/frequency of the signal.

Relations between frequency and phase:





- For comparing two clocks (especially digital clocks), easier to look at
  - $S_{\dot{\omega}}(\omega) = \omega^2 S_{\phi}(\omega)$

 $\sigma_{\phi}^{2}(\tau) = \left(\frac{\tau^{2}}{3}\right) \cdot \operatorname{Mod} \sigma_{\phi}^{2}(\tau)$ <sup>(5)</sup>







### White Rabbit architecture

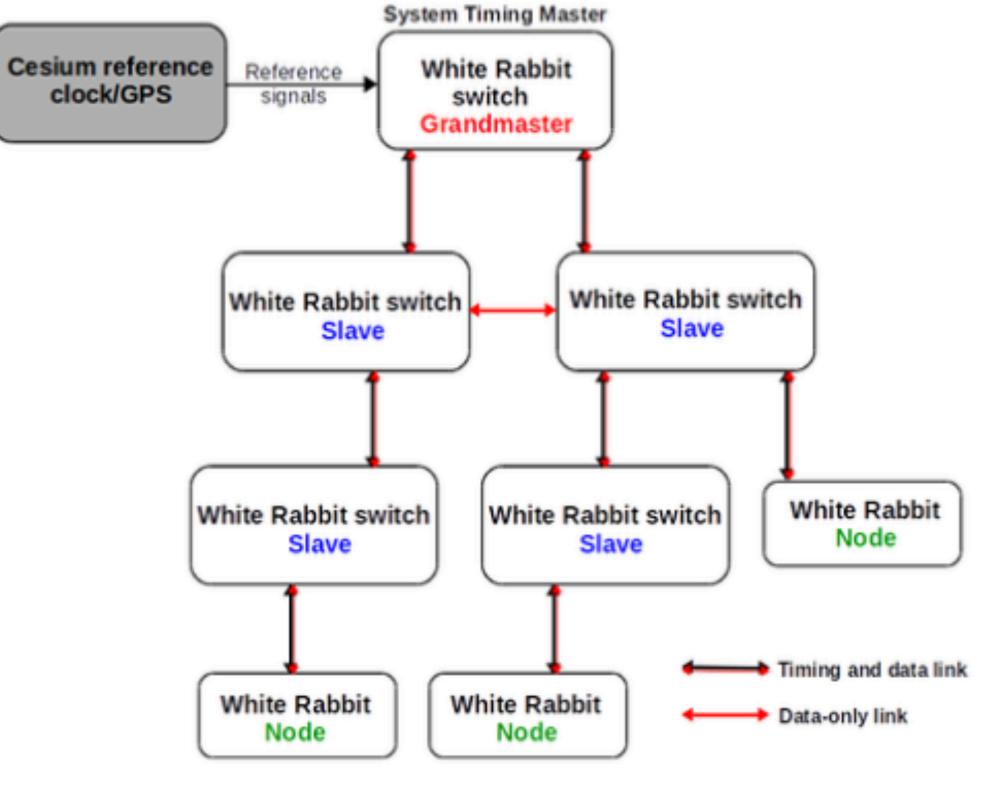


FIGURE 2.5: A typical White Rabbit Network [42]. (3)







