

# Yang-Mills and QCD correlation functions from the Curci-Ferrari model at two-loop order

Nahuel Barrios

Advisors: Marcela Peláez and Urko Reinosa

Rencontres de Physique des Particules - April 8, 2021

[N. Barrios, M. Peláez, U. Reinosa, and N. Wschebor. PRD (2020)]  
[N. Barrios, J. Gracey, M. Peláez and U.Reinosa - arXiv]



# Outline

- 1 The Curci-Ferrari model in Landau gauge
- 2 Two-loop ghost-antighost-gluon vertex in YM theory
- 3 Two-loop propagators in QCD
- 4 Conclusions and outlook

# Motivation

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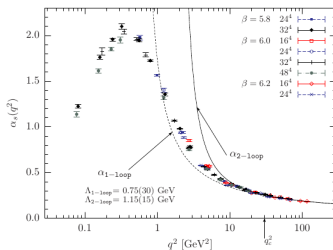
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  - UV: asymptotic freedom  $\implies$  perturbation theory.

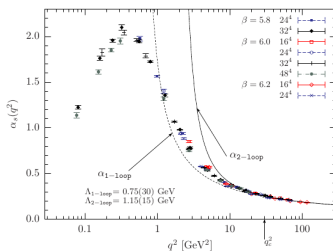


[Sternbeck, Schiller, Bogolubsky (2006)]

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IR: Landau pole!

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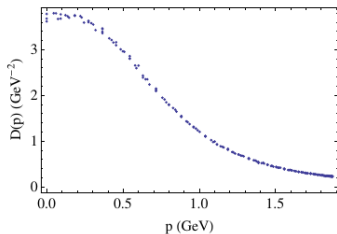
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- 2 Modify FP action (Gribov copies).
  - ▶ Gribov-Zwanziger formalism
  - ▶ Curci-Ferrari model

## Curci-Ferrari model in Landau gauge (quenched approximation)

$$L = \frac{1}{4}(F_{\mu\nu}^a)^2 + \partial_\mu \bar{c}^a (D_\mu c)^a + ih^a \partial_\mu A_\mu^a + \frac{m^2}{2}(A_\mu^a)^2$$

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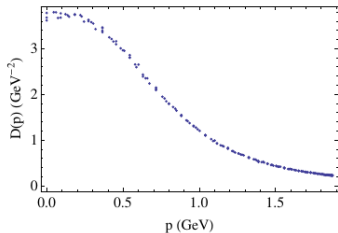
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[A. Cucchieri, A. Maas and T. Mendes (2008)]

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- In the UV limit we recover standard FP action
- CF has the same symmetries than FP, except BRST
- Renormalizable

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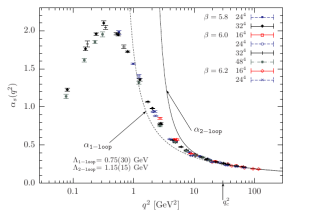
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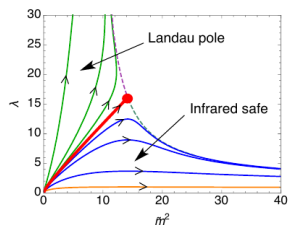
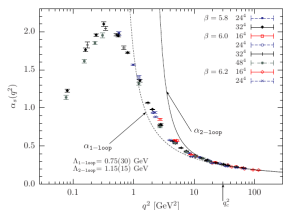
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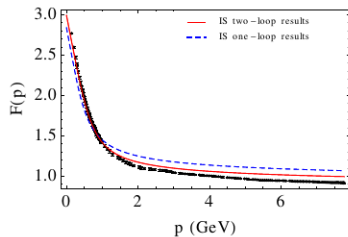
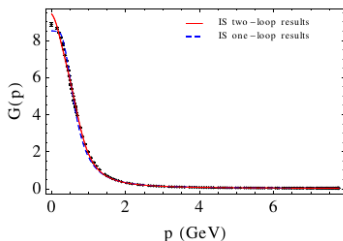


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**Infrared safe scheme**

# Two-point functions - SU(3) YM

- Two- and three- point correlation functions



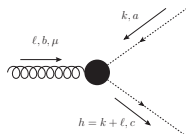
[Lattice data from: A.G. Duarte, O. Oliveira and P. J. Silva (2018)]

[Tissier, Wschebor (2011)]

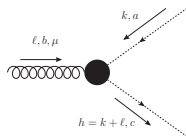
[Gracey, Peláez, Reinoso, Tissier (2019)]

- From these fits we can extract  $\lambda(\mu)$  and  $m(\mu)$  and make predictions:
  - ▶ at non-zero temperature
  - ▶ we will focus on zero temperature in this talk

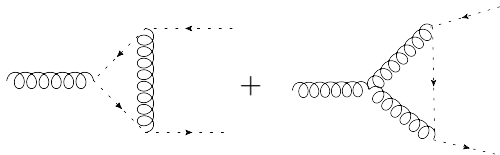
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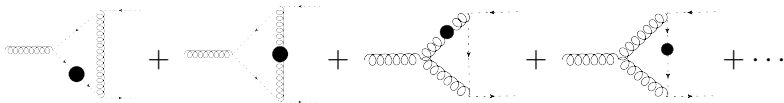


1-loop diagrams:

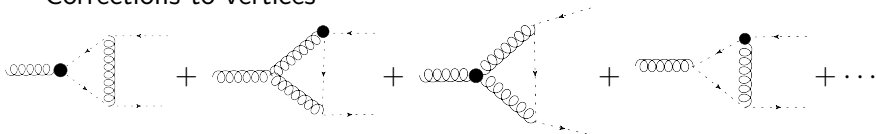


2-loop diagrams:

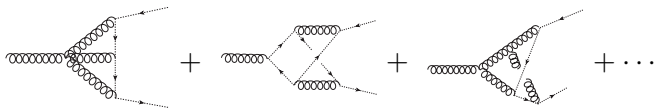
- Corrections to propagators



- Corrections to vertices



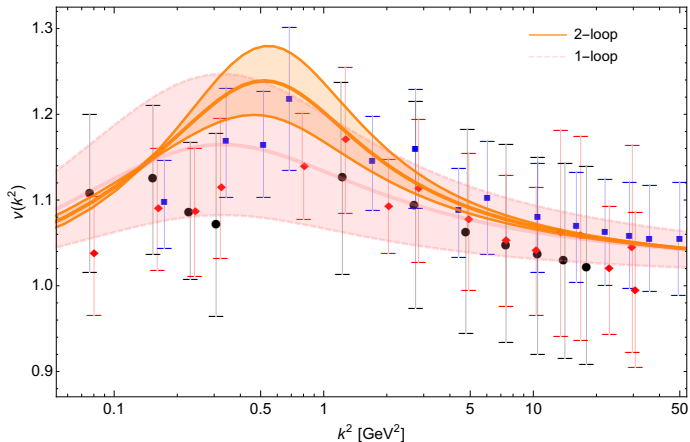
- Two-loop genuine



Non-planar diagrams (vanished thanks to Jacobi identity)

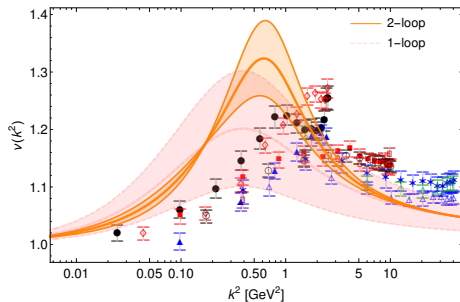


# SU(3) YM prediction - ghost-gluon vertex - vanishing gluon momentum



[Lattice data from Sternbeck *et al.* (2006)]

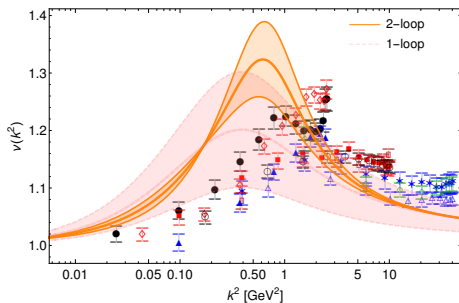
# SU(2) YM - ghost-gluon vertex - vanishing gluon momentum



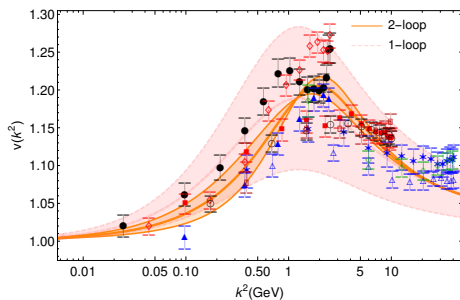
Prediction

[Lattice data from A. Maas (2020)]

# SU(2) YM - ghost-gluon vertex - vanishing gluon momentum




Prediction




Fit

[Lattice data from A. Maas (2020)]

Two-loop QCD propagators from the CF model.  $N_f=2$ 


 $F(k)$


 $D(k)$



$$S(k) = Z(k) \frac{i\not{k} + \mathbb{1} M(k)}{k^2 + M^2(k)}$$

37 2-loop diagrams, 6 1-loop diagrams in total.

[M. Peláez, M. Tissier and N. Wschebor (2014)]

[R. Williams, C. S. Fischer and W. Heupel (2015)]

[A. Cyrol, M. Mitter, J. Pawłowski and N. Strodthoff (2017)]

[A. C. Aguilar, J. C. Cardona, M. N. Ferreira and J. Papavassiliou (2018)]

[F. Gao, J. Papavassiliou and J. Pawłowski (2021)]

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- coupling is up to 3 times larger than in YM sector in the IR
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We compared with two sets of lattice data:  $M_\pi = 426$  MeV and  $M_\pi=150$  MeV.

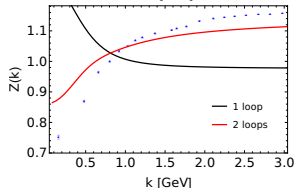
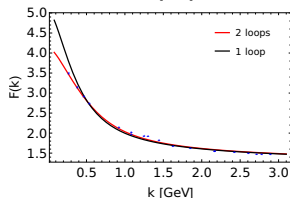
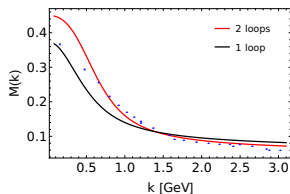
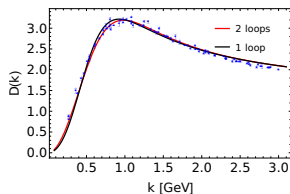
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Two fits:

- Minimizing  $\chi^2 \equiv \frac{1}{4} (\chi_F^2 + \chi_D^2 + \chi_Z^2 + \chi_M^2)$
- Minimizing  $\tilde{\chi}^2 \equiv \frac{1}{3} (\chi_F^2 + \chi_D^2 + \chi_Z^2)$

Results  $M_\pi=426$  MeVMinimizing  $\chi$ 

[Lattice data from A. Sternbeck, K. Maltman, M. Muller-Preussker, L. von Smekal (2012) and O. Oliveira, P.J. Silva, J. I. Skullerud, A. Sternbeck (2019)]



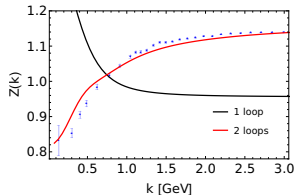
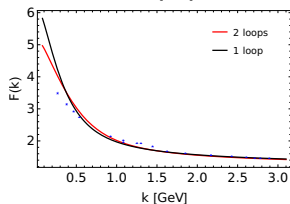
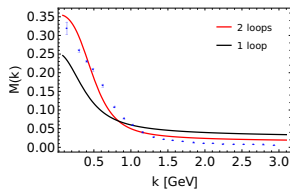
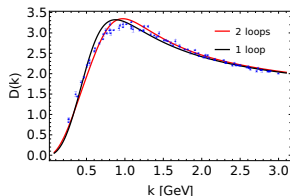
Error table for  $\chi$ 

order	$\lambda_0$	$m_0$	$M_0$	$\chi_F(\%)$	$\chi_D(\%)$	$\chi_Z(\%)$	$\chi_M(\%)$
1-loop	0.39	430	140	3.3	5.3	19.3	16.1
2-loop	0.32	390	160	2.4	3.7	5.3	9.0

masses in MeV.

Error table for  $\tilde{\chi}$ 

order	$\chi_F(\%)$	$\chi_D(\%)$	$\chi_Z(\%)$
1-loop	5.5	3.9	16.1
2-loop	2.5	3.7	3.0

Results  $M_\pi=150$  MeVMinimizing  $\chi$ 

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order	$\lambda_0$	$m_0$	$M_0$	$\chi_F(\%)$	$\chi_D(\%)$	$\chi_Z(\%)$	$\chi_M(\%)$
1-loop	0.41	400	60	6.3	6.1	20.6	27.3
2-loop	0.36	360	50	5.6	5.1	1.9	12.7

Error table for  $\tilde{\chi}$ 

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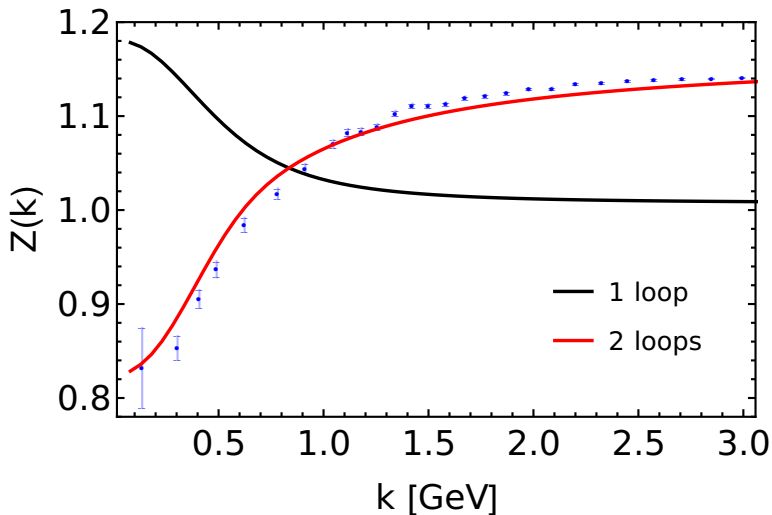
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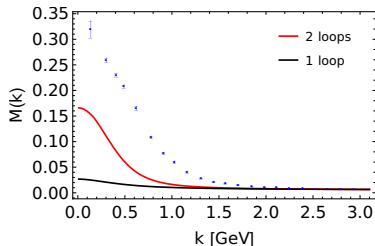
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Error comparison

$M_\pi$	$\chi_{2-loop}(\%)$	$\tilde{\chi}_{2-loop}(\%)$
150	7.5	2.5
426	5.6	3.1

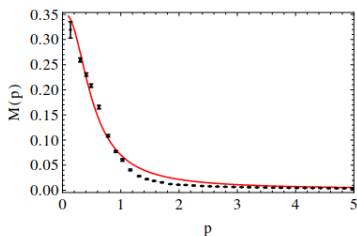
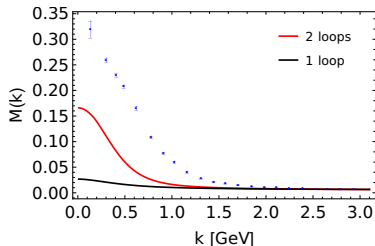
Results  $Z - M_\pi = 150 \text{ MeV} - \tilde{\chi}$ 

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- SBCS can be captured in the CF model via the RI expansion: expansion in powers of gauge coupling and  $\frac{1}{N}$  [M. Peláez, U. Reinosa, J. Serra, M. Tissier, N. Wschebor (2017), (2021)]

# Conclusions and outlook

- Ghost-antighost-gluon is very well reproduced in  $SU(3)$  YM theory via the CF model at two-loop order.
- For  $SU(2)$  the results are not as good as  $SU(3)$ , although they represent an improvement with respect to the one-loop evaluation.
- QCD  $F(k)$  and  $D(k)$  are well captured by a perturbative expansion within the CF model.
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