

Dynamics of critical fluctuations in heavy-ion collisions

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Supervisors

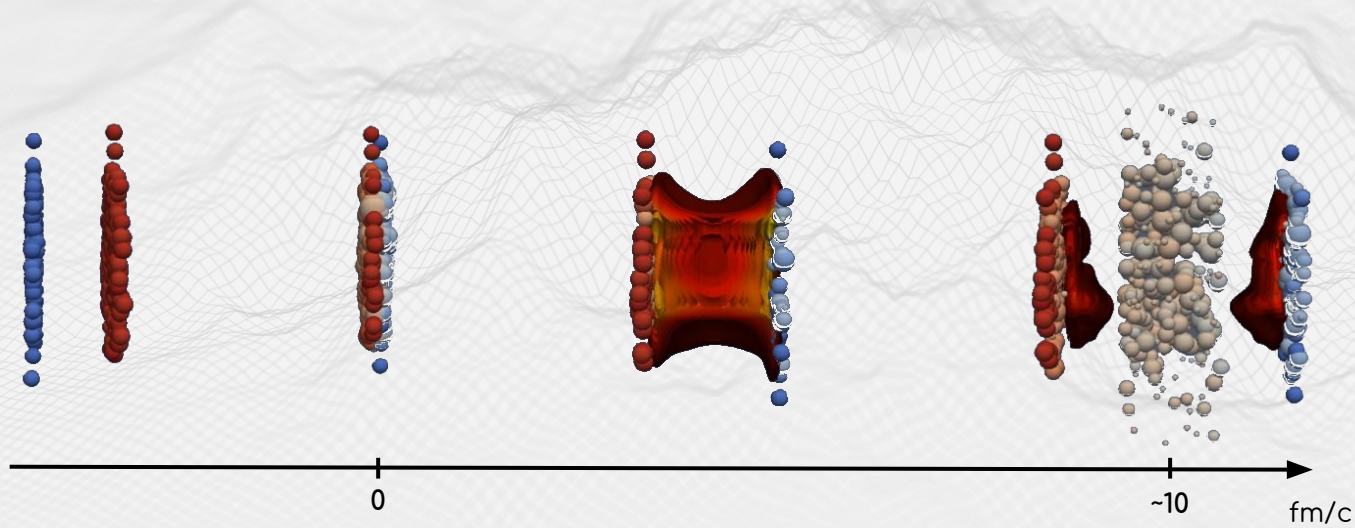
Taklit Sami (director)

Marlene Nahrgang

Marcus Bluhm

Deconfined state of strongly interacting matter : The quark-gluon plasma.

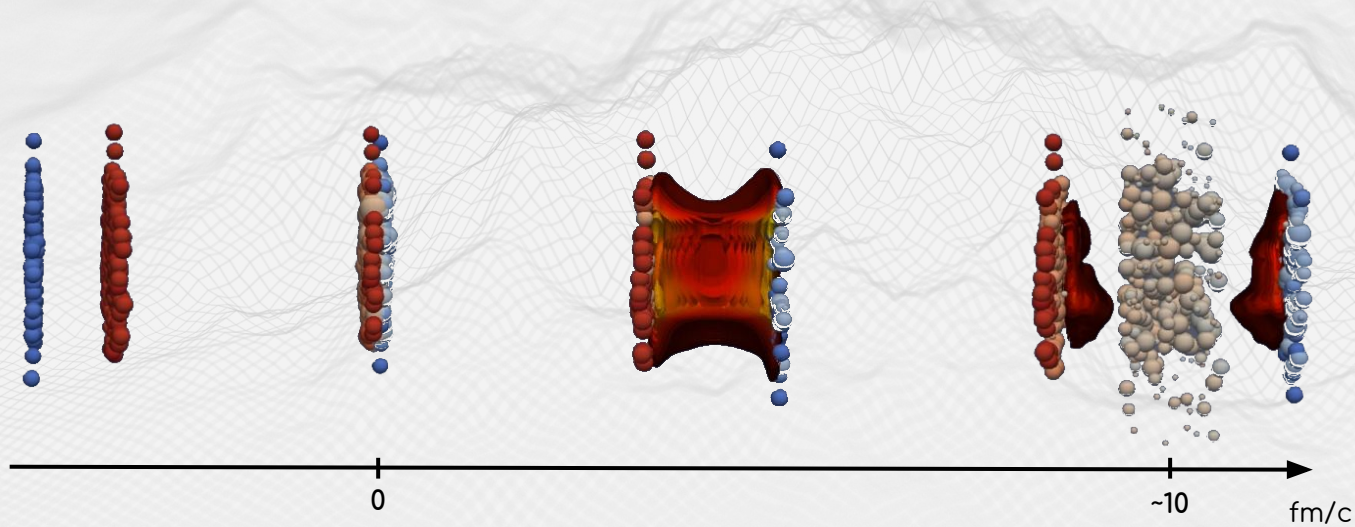
Experimentally studied in heavy-ion collision.



MADAI collaboration, Hannah Petersen and Jonah Bernhard

Deconfined state of strongly interacting matter : The quark-gluon plasma.

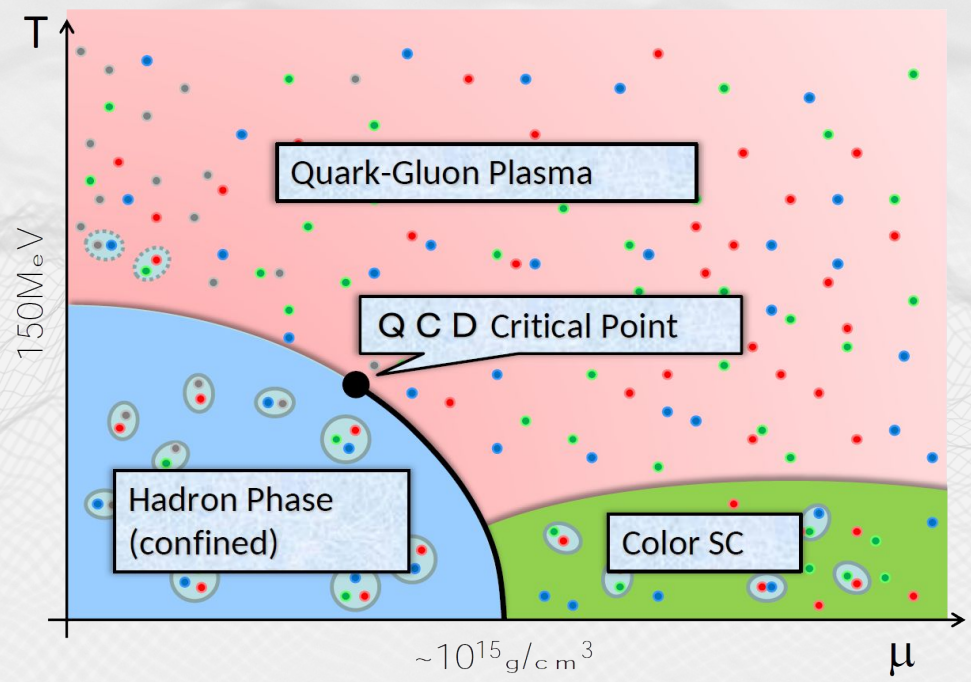
Experimentally studied in heavy-ion collision.



MADAI collaboration, Hannah Petersen and Jonah Bernhard

What are the thermodynamic properties of the strongly interacting matter ?

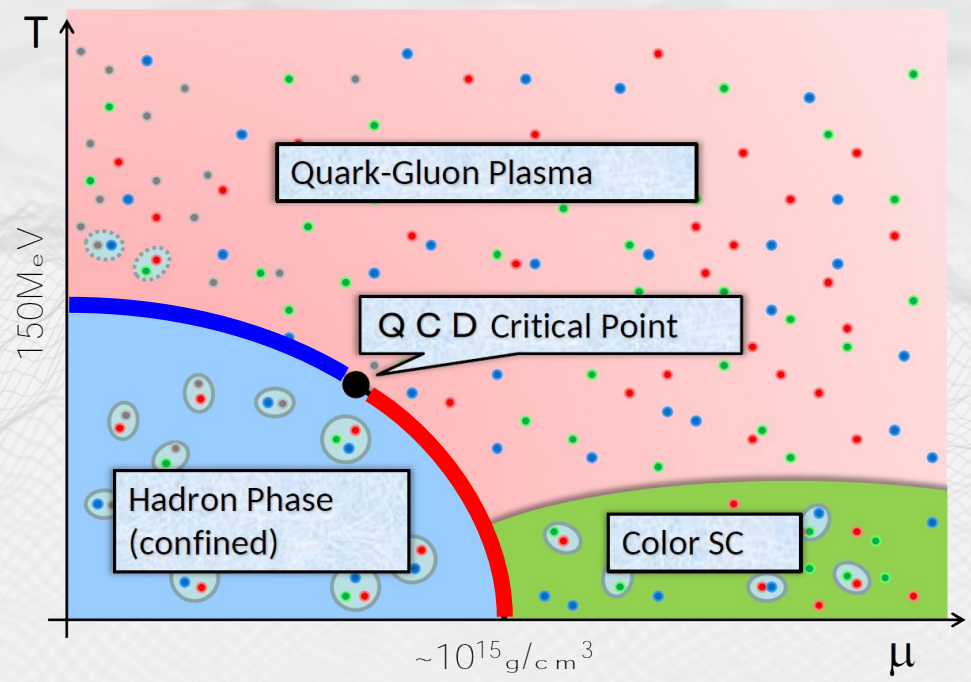
The QCD phase diagram



The QCD phase diagram

Crossover phase transition

1st order phase transition



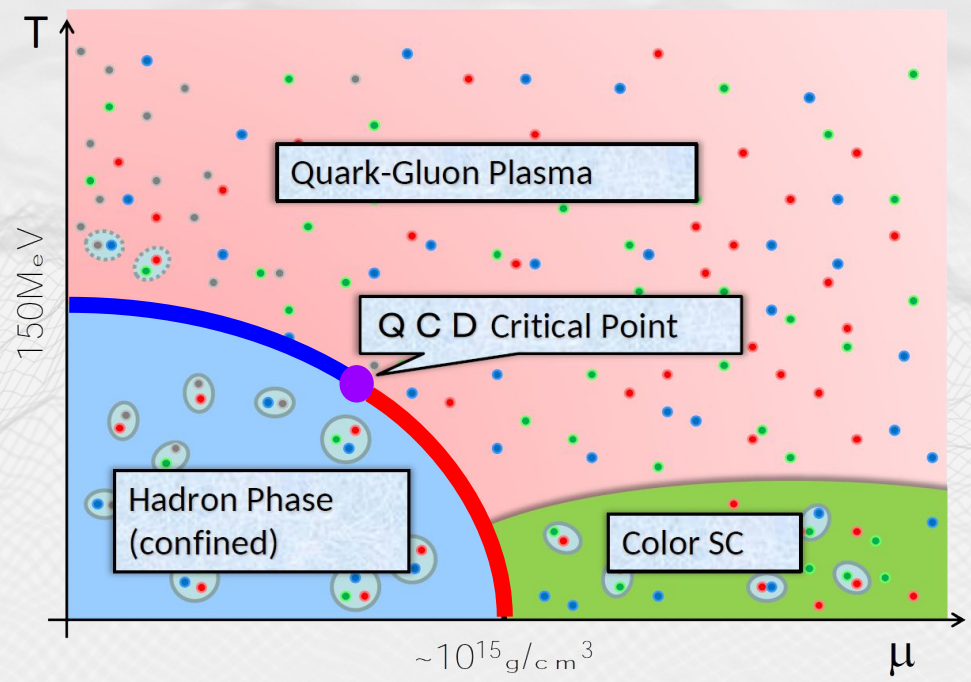
Introduction

The QCD phase diagram

Crossover phase transition

Critical point

1st order phase transition



Is there a **critical point** in the QCD phase diagram ?

Introduction

Thermodynamic of QCD matter ?

Is there a critical point ?

Introduction

Criticality: **Extraordinary effects.**

- Huge net-baryon density fluctuations
- Infinite correlation length ξ
- Infinite susceptibility
- Universal behavior



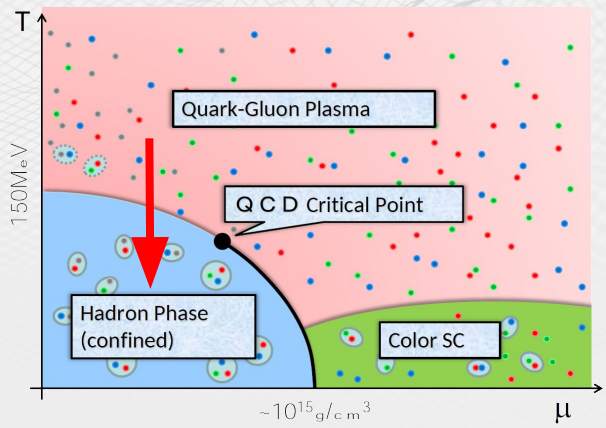
$$\sigma^2 \sim \xi^2$$

$$S \sim \xi^{4.5}$$

$$\kappa \sim \xi^7$$

M. A. Stephanov, 2008

Dynamics: **Rapid expansion and quick temperature decrease**



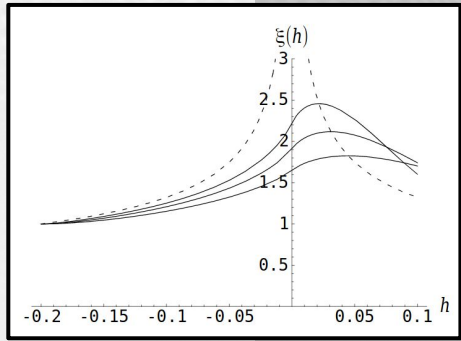
→ Critical slowing down



$$\tau_{relax} \propto \xi^z$$

Hohenberg, Halperin, Rev. Mod. Phys. 49, 435; 1977

→ Non-equilibrium effects



Berdnikov, Rajagopal, MIT-CTP, 1999

Introduction

Thermodynamic of QCD matter ?

Is there a critical point ?

Extraordinary critical effects

Rapid expansion and temperature decrease

Introduction

$$\sigma^2 \sim \xi^2$$

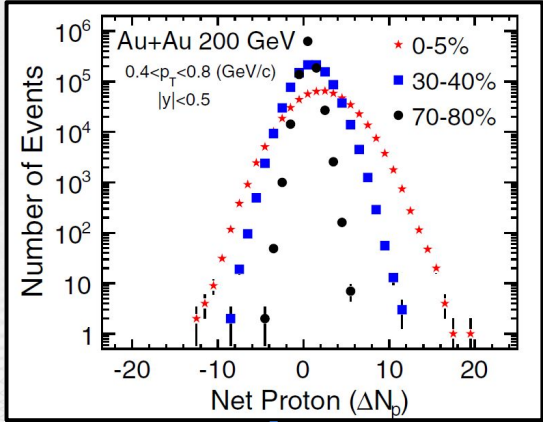
$$S \sim \xi^{4.5}$$

$$\kappa \sim \xi^7$$

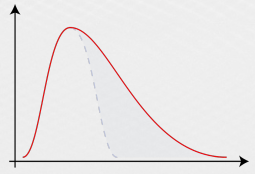
Introduction

- Thermodynamic of QCD matter ?
- Is there a critical point ?
- Extraordinary critical effects
- Rapid expansion and temperature decrease

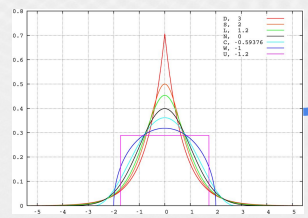
The fluctuations observables can be measured **experimentally**



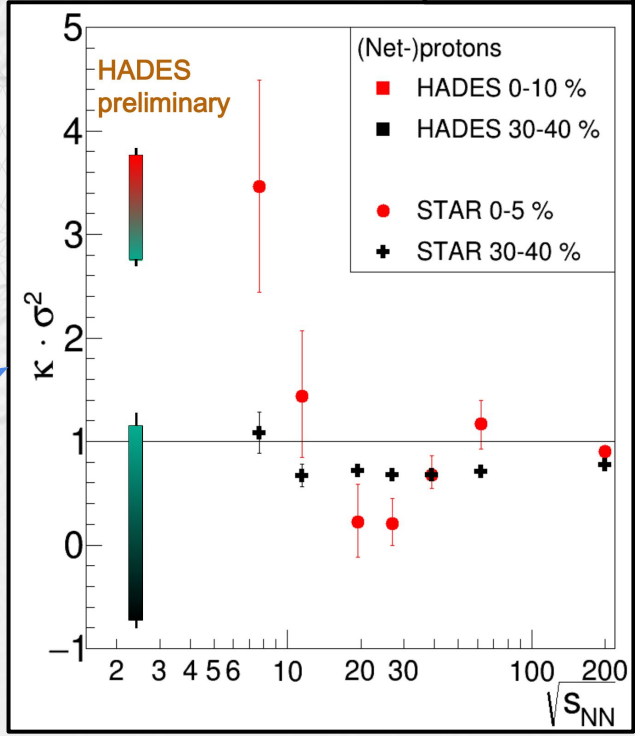
STAR Collab. ~2010



Skewness



Kurtosis



Introduction

Our work :

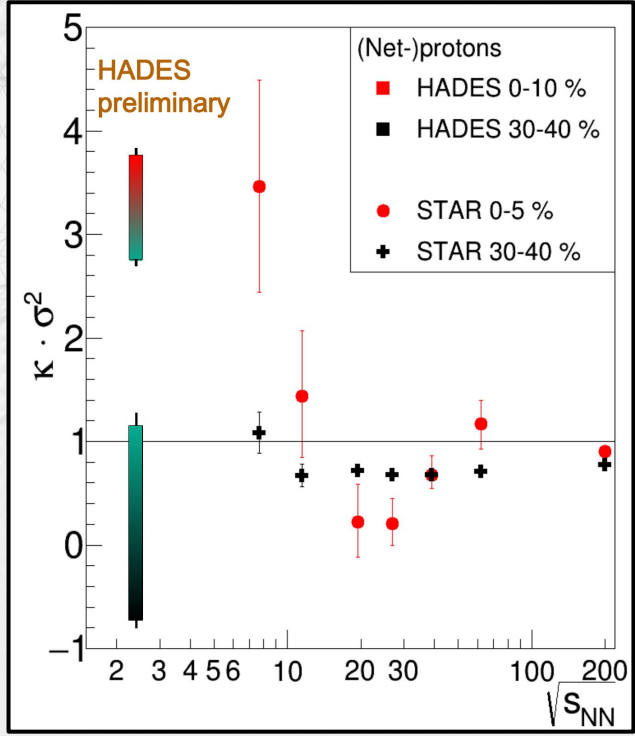
Study the **direct** impact of the **dynamics** on the **critical fluctuations** of the net-baryon density and compute fluctuations related observables

Our goals :

Interpret **experimental** results on the fluctuations observables

Are they a sign of the QCD **critical point** ?

Suggest sensible observables for **experimental** measurement



Introduction

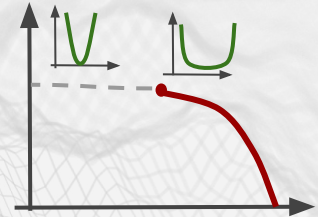
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Interplay of the dynamical and critical effects impact on the fluctuations ?

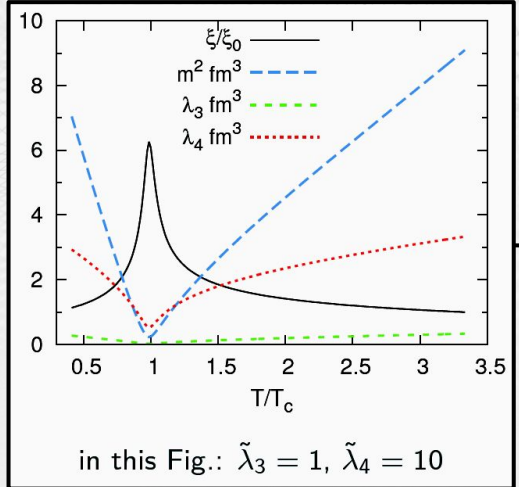
Model for criticality

Ginzburg-Landau free energy functional

$$F(T, \delta n_B) = T \int \left[\frac{m^2(T)}{2 n_c^2} \delta n_B^2 + \frac{K}{2 n_c^2} (\nabla \delta n_B)^2 + \frac{\lambda_3(T)}{2 n_c^3} \delta n_B^3 + \frac{\lambda_4(T)}{2 n_c^4} \delta n_B^4 + \frac{\lambda_6}{2 n_c^6} \delta n_B^6 \right] d\vec{x}$$



Temperature parametrization : correlation length given by a mapping from 3D Ising model to the QCD phase diagram



$T_c = 0.15 \text{ GeV}$

Relation with the correlation length

$$\begin{aligned} m^2 &= 1/(\xi_0 \xi^2) \\ K &= \tilde{K}/\xi_0 \\ \lambda_3 &= n_c \tilde{\lambda}_3 (\xi/\xi_0)^{-3/2} \\ \lambda_4 &= n_c \tilde{\lambda}_4 (\xi/\xi_0)^{-1} \\ \lambda_6 &= n_c \tilde{\lambda}_6 \end{aligned}$$

M. Tsypin PRL73 (1994); PRB55 (1997)

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Interplay of the dynamical and critical effects impact on the fluctuations ?

Model for criticality

- Ginzburg-Landau free energy functional
- Correlation length from 3D Ising
- Temperature parametrization with the correlation length

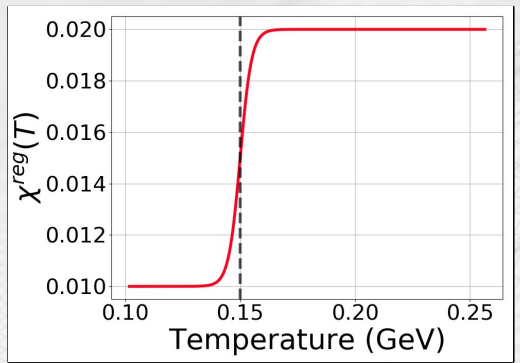
Non critical contributions

Introduction

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Interplay of the dynamical and critical effects impact on the fluctuations ?

Parametrization of the susceptibility far from the critical point



$$X(T) = \frac{\chi_2^{B, latt}(T)}{s} T^3 \longrightarrow \begin{aligned} X(T_i) &= 0.02 \text{ fm}^{-4} \\ X(T_f) &= 0.01 \text{ fm}^{-4} \end{aligned}$$

Asakawa, Heinz, Müller PhysRevLett.85.2072

$$\chi(T) = \frac{n_c^2}{m^2(T)} \longrightarrow m_{eff}^2(T)$$

Model for criticality

- Ginzburg-Landau free energy functional
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Non-critical contributions

Lattice susceptibilities

Higher order couplings

In the hadron gas : $\frac{\chi_4^{B, latt}(T)}{\chi_2^{B, latt}(T)} = 1$

In the QGP : $\frac{\chi_4^{B, latt}(T)}{\chi_2^{B, latt}(T)} = \frac{2}{3\pi^2}$

$$\longrightarrow \begin{aligned} X_4(T_i) &= 0.02 \text{ fm}^{-4} \\ X_4(T_f) &= 0.001 \text{ fm}^{-4} \end{aligned} \longrightarrow \lambda_{4, eff}(T)$$

M. Sakaida, M. Asakawa, H. Fujii, and M. Kitazawa Phys. Rev. C 95, 064905

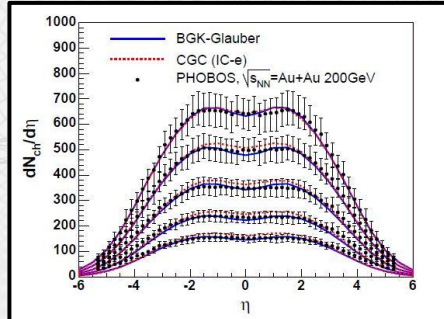
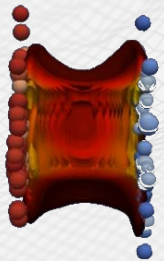
Stochastic diffusion equation :

$$\frac{\partial}{\partial t} \delta n_B = D \frac{\partial^2}{\partial x^2} \left\{ \frac{\delta F}{\delta n_B} \right\} + \frac{\partial}{\partial x} \xi$$

- Ginzburg-landau
- Intrinsic white gaussian noise

$$\langle \xi(x_1, t_1) \xi(x_2, t_2) \rangle = 2 \kappa T \delta(x_1 - x_2) \delta(t_1 - t_2)$$

D : diffusion coefficient κ : mobility coefficient



B. B. Back et al. Phys. Rev. Lett. 91, 052303

Milne coordinates

$$\tau = \sqrt{t^2 - x^2}$$

$$y = \frac{1}{2} \ln \left(\frac{t+z}{t-z} \right)$$

$$\frac{\partial}{\partial \tau} \delta n_B(\tau, y) = D(\tau) \frac{\partial^2}{\partial y^2} \left\{ \frac{\delta F}{\delta n_B} \right\}(\tau, y) + \frac{\partial}{\partial y} \xi(\tau, y)$$

M.Kitazawa, M.Nahrgang, M.Bluhm, N.Touroux, GP, Nuclear Physics A 1005 (2021) 121797 (proceeding Quark Matter 2019)

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Interplay of the dynamical and critical effects impact on the fluctuations ?

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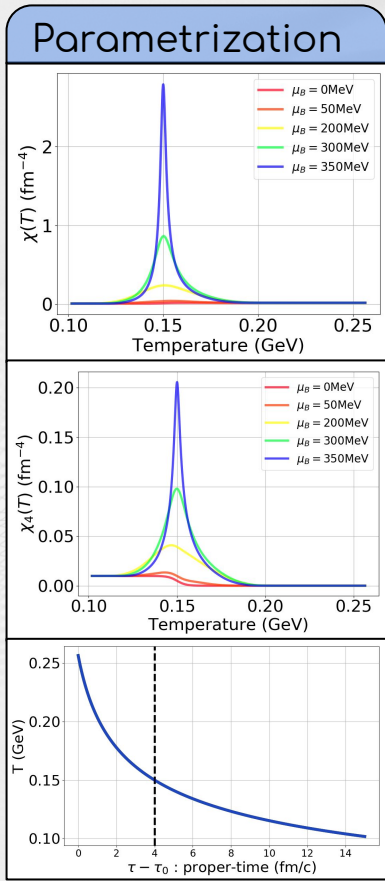
Non-critical contributions

Lattice susceptibilities

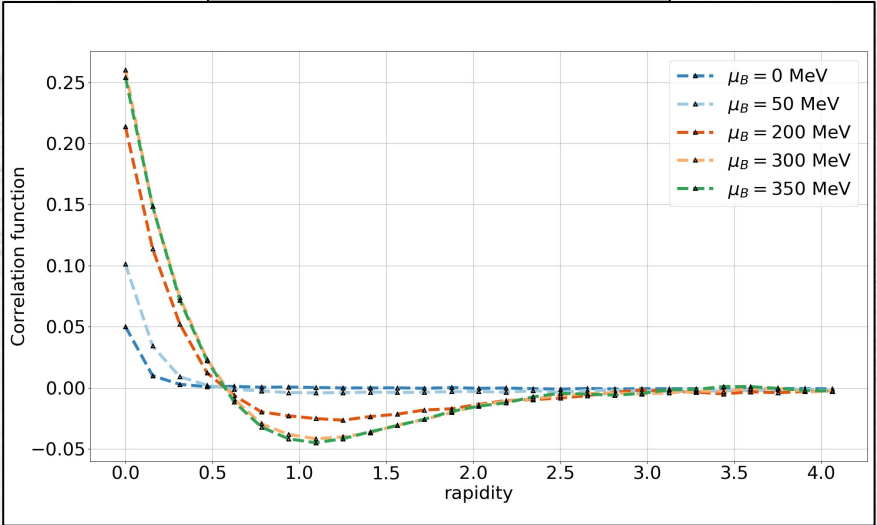
Dynamics

- Diffusion equation
- Intrinsic noise
- Milne coordinates

Selected results : Correlation function



$T = 145$ MeV



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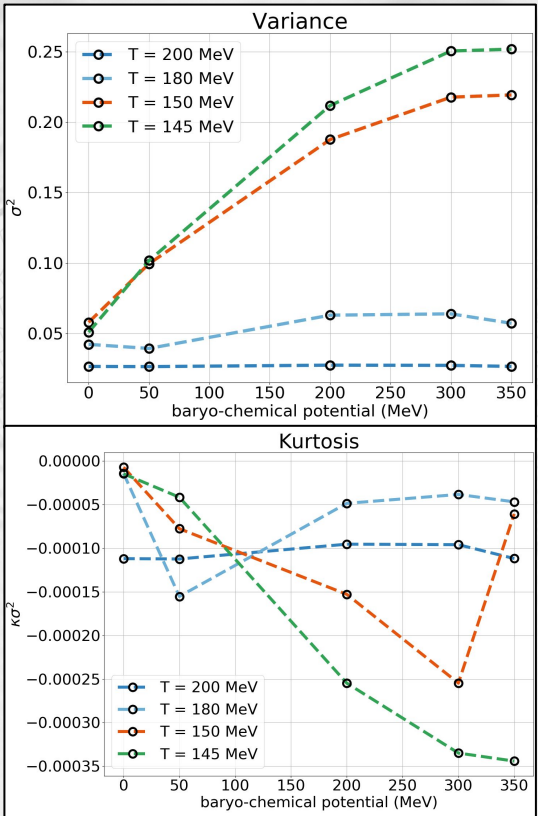
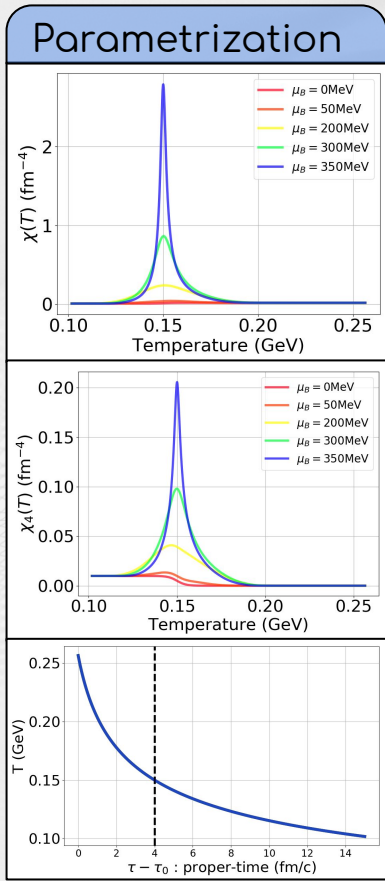
Dynamics

- Diffusion equation
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Selected results

Correlation function

Selected results : Variance and kurtosis



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Selected results

- Correlation function
- Variance & Kurtosis

Conclusion

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Thank you for your attention !