CI methods for nuclear structure and reactions

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Atelier Physique Théorique des deux infinis

CI calculations: broad spectrum of applications



- define effective interaction
- $\mathscr{H}_{eff}\Psi_{eff} = E\Psi_{eff}$
- build and diagonalize energy matrix

Nuclear forces and nuclear structure

- Shell evolution: from stability to dripline
- Isospin symmetry breaking
- Emergence of quadrupole collectivity, superdeformation
- Vibrational modes
- Dipole resonances
- Symmetries



- β decay
- ββ decay
- e capture 🛛 👄

Particle capture reactions

 \Leftrightarrow

 \Leftrightarrow

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- Neutron-capture rates <
- Proton-capture rates

supernovae

fundamental interactions

nucleosynthesis

nature of neutrino

- \iff r-process
- ⇔ rp-process
- ⇔ novae



CI (LSSM) calculations: giant computations $H_{eff}|\Psi_{eff}\rangle = E|\Psi_{eff}\rangle$ $|\Psi_{eff}\rangle = \sum C_{act}|\Phi_{act}\rangle$ Ballon (30 km)Pile de CD avec un an de données du LHC (~ 20 km)

1 nucleu:

Concorde

(15 km)

Mont Blanc

stat

(4.8 km)

$$\begin{split} |\Phi_{ph}\rangle &= \phi_{\alpha_1}(\vec{r}_1)\phi_{\alpha_2}(\vec{r}_2)...\phi_{\alpha_n}(\vec{r}_n) \\ E &= \sum_{pp'hh'} C^*_{p'h'} \langle \Phi_{p'h'} | H_{eff} | \Phi_{ph} \rangle C_{ph} \end{split}$$

CORE

Exponential growth of basis dimensions: $D \sim \begin{pmatrix} d_{\pi} \\ p \end{pmatrix} \cdot \begin{pmatrix} d_{v} \\ n \end{pmatrix}$ In *pf* shell : ⁵⁶Ni 1,087,455,228 In *pf-sdg* space : ⁷⁸Ni 210.046.691.518

- Actual limits in giant diagonalizations: 0.2 10¹² (¹¹⁴Sn)
- Largest matrices up to now: ~ 10¹⁴ non-zero matrix elements
- More than 1,000,000 CD-ROM's to store a single matrix !
- Can not be stored on hard disk: computed on the fly
- Strasbourg LSSM codes: ANTOINE and NATHAN

Structure and decay of exotic nuclei

Nowadays, LSSM calculations in extended model spaces comprising a few oscillator shells reshell structure evolution and sudden onset of deformation in very neutron-rich nuclei

Accurate description and deep insight into nuclear structure

repavement for ab-initio methods

- Construction of fully microscopic interactions for valence-space calculations (Okubo-Lee-Suzuki transformation) as a path towards regions where no experimental data available
- Development of numerical techniques and state-of-the-art computations
- Search for additionnal guidelines and shortcuts using symmetry based approaches



Shape Coexistence in ⁷⁸Ni as the Portal to the Fifth Island of Inversion F. Nowski, A. Poves, E. Caurier, and B. Bourthong Pirvs, Rev. Lett. 7272501 (2016) - Dublined 27 December 2016

Kamila Sieja

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Effective interactions in the sd shell





⁷⁸Ni revealed as a doubly magic stronghold against nuclear deformation



BSM: New opportunities for nuclear structure studies

Synergies between Large Scale Shell Model & Projected Generator Coordinate Method

- Application to studies of: -Octupole shapes -N=Z nuclei -Heavy and superheavy nuclei $-\beta\beta$ decay
- -r-process nucleosynthesis
 - Technical aspects with Taurus/DFSM codes
 - Optimal selection of GCM states
 - Center of mass decoupling
 - Ab-initio interactions

Collaboration with Universidad Autonoma Madrid & IRN ASTRANUCAP





B. Bounthong, IPHC, PhD Thesis (2016) D. Dao, IPHC, Post-Doc (2021)

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Triax. proj. + GCM:

Strongly deformed 8p8h structure



D. Dao, IPHC, Post-Doc (2021)

Isospin symmetry breaking

Accurate description of isospin violation and associated phenomena through development of Isospin Non Conserving hamiltonians in extended valence spaces:

 $((sd), (pf), (s_{1/2}d_{3/2}f_{7/2}p_{3/2})$ and beyond

 $\beta - p$ and $\beta - p\gamma$ decay studies and extraction of isospin mixing in the IAS

- Development of Isospin Non Conserving hamiltonians in the (sd - pf) valence space and numerous applications
- Improvement of MED and TED description within a band
- Interpretation for b and c coefficients staggering
- Support to forthcoming experimental studies

$$M(\alpha,T) = a(\alpha,T) + b(\alpha,T)T_{Z} + c(\alpha,T)T_{Z}^{2}$$

JT T=3/2

$$r_{\frac{13/2}{11-3/2}} r_{\frac{11}{11-3/2}}$$

-3 -4



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Nadezda Smirnova

Isospin-symmetry breaking: exotic nuclei, fundamental interactions and astrophysics (2017-2022) IN2P3/CENBG/IPHC/GANIL





PHYSICAL REVIEW C 95, 054301 (2017)



⁴⁸Mn: S_{exp} = 2.7(9).10⁻³,
$$\alpha_{exp}$$
 = 1.4(5)%

$0^+ \rightarrow 0^+ \beta$ -decay: a test of fundamental interactions

Large scale calculations for all emitters below A \leq 40 including nuclei in the vicinity of ^{40}Ca

Use of Isospin Non Conserving hamiltonians and Woods-Saxon wave functions for untruncated *sd* and *pf* calculations

New approach of radii determination without closure approximation

Use of new effective interactions developped in Strasbourg

- Lanczos Structure Function Method for δ_C
- New (*sd* − *pf*) interaction
- Effective Fermi Operator
- HF wave functions
- New emitters such as ⁵⁸Zn

Nadezda Smirnova

-Isospin-symmetry breaking: exotic nuclei, fundamental interactions and astrophysics (2017-2022) IN2P3/CENBG/IPHC/GANIL

$$\mathscr{F}t = (1+\delta_R)(1+\delta_{NS}-\delta_C)ft$$
$$= \frac{K}{M_{F0}^2 G_F^2 |V_{ud}|^2(1+\Delta_R)}$$



L. Xayavong, CENBG, PhD Thesis (2016) L. Xayavong and N. Smirnova, PRC97 (2018) 024324; PROC. NTSE2018.

$\beta\beta$ -decay and nature of neutrino

11 citations

Reliable nuclear matrix elements needed to plan and fully exploit impressive experiments looking for neutrinoless double-beta decay

$$[T_{1/2}^{0\nu}(0^+ \rightarrow 0^+)]^{-1} = G_{0\nu}|M^{0\nu}|^2 \langle m_{\nu}^{\beta\beta} \rangle^2$$



PRL Editors' Suggestion

Search for Neutrinoless Quadruple- β Decay of $^{150}\mathrm{Nd}$ with the NEMO-3 Detector

R. Amold et al. (NEMO-3 Collaboration) Phys. Rev. Lett. 119, 041801 (2017) - Published 24 July 2017

The calculation of the neutrinoless double- β decay matrix element within the realistic shell model

L. Coraggio,¹ A. Gargano,¹ N. Itaco,^{2,1} R. Mancino,^{2,1} and F. Nowacki^{3,4,2}

Talk of F. Nowacki later in this session

Input for reaction codes and benchmark of many-body

methods

Statistical treatment of the γ deexcitation strength function recomputations of thousands states and transitions needed

M1 and E1 treated on the same footing (application possible to any multipolarity)

Improved description of the radiative widths and CI-guided developments of fully-microscopic QRPA models

- Microscopic nuclear structure input for reaction codes (TALYS)
- Reliable predictions of reactions rates for nucleosynthesis

Kamila Sieja

Gamma Strength

(2017-2019) IN2P3/IPHC

collaboration CEA-DAM and University of Brussels





S. Goriely, S. Hilaire, S. Péru, KS, Phys. Rev. C98(2018)014327

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Reaction rates and nucleosynthesis

Proton capture reaction rates for rp process (X-ray bursts) or novae

-Resonance energies (with Isospin bre-aking)

-Widths with respect to proton and γ emission

-Several reactions in the sd shell

-pf shell nuclei around 40 Ca

-Thomas-Ehrman shift in sd shell

 $-(\alpha,\gamma),(\alpha,p),(p,\alpha)$ capture/emission modeling

 $-^{22}Mg(\alpha,p)^{25}AI$ and other reactions



Neutron capture reaction rates for rprocess

-CI calculations as benchmark for other methods

-Input for reaction studies: spectra, spectroscopic factors, decay widths

-Systematic evaluation of direct capture rates

-Tests of Hauser-Feshbach model in neutron-rich nuclei

-Resonant capture much more difficult to treat on the neutron-rich side



Talk of M. Oertel in the afternoon session

Summary

- High predictive power, accurate and detailed information (structure near and far from stability, nuclear and electroweak processes)
- Success and robustness of the approach encourage further developments and applications
- Simultaneous description of multiple low-energy phenonema but need of dedicated local studies
- Intense support for future experimental programs and developments (but manpower insufficient ...)
- Existing cross fertilizing collaborations in several domains: ab-initio studies, isospin symmetry breaking, astrophysics, ββ decay ... and others to develop !