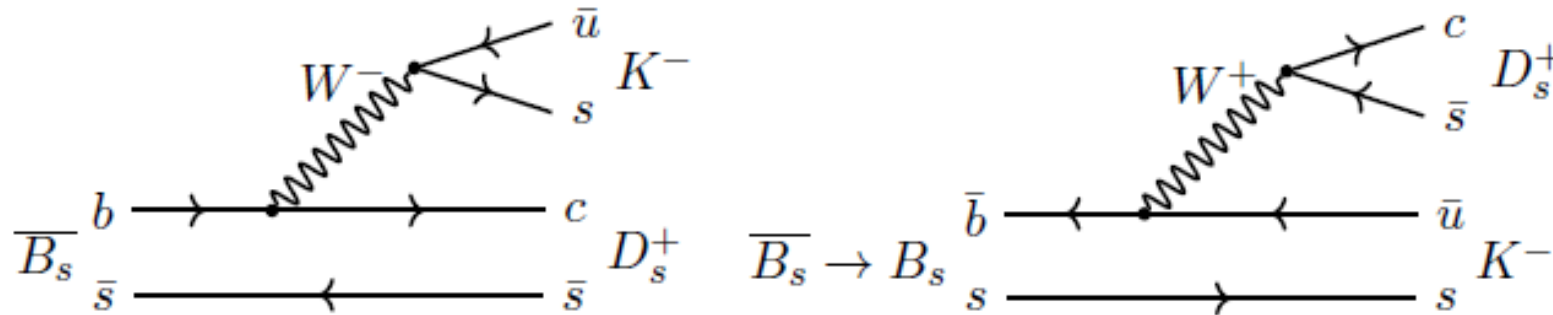


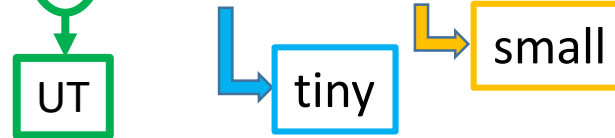
# Study of $B_s \rightarrow D_s K$ at FCC-ee and constraints on detector

R. Aleksan  
20/1/2021



$$\phi_{CKM} = \alpha_s - \beta_s = \gamma + \gamma_{ds} - 2\beta_s$$

Motivations



- Study of CP violation :
  - Sensitivity on  $UT_{CKM}$  angle  $\gamma$  ( ... and mixing parameter  $\frac{\Delta m}{\Gamma}$  )
- Study of CP detector resolutions :
  - Tracking
  - Calorimetry
  - PId

**Time dependent  $B_s$  decay**

$$\Gamma(B_s \rightarrow f) = |\langle f|B_s \rangle|^2 \times e^{-\Gamma t} \left\{ [1 - \omega(1 - \rho^2)] \cos^2 \frac{\Delta mt}{2} + [\rho^2 + \omega(1 - \rho^2)] \sin^2 \frac{\Delta mt}{2} - (1 - 2\omega)\rho \sin \phi_{CP}^+ \sin \Delta mt \right\}$$

$$\Gamma(\overline{B}_s \rightarrow f) = |\langle f|B_s \rangle|^2 \times e^{-\Gamma t} \left\{ [\rho^2 + \omega(1 - \rho^2)] \cos^2 \frac{\Delta mt}{2} + [1 - \omega(1 - \rho^2)] \sin^2 \frac{\Delta mt}{2} + (1 - 2\omega)\rho \sin \phi_{CP}^+ \sin \Delta mt \right\}$$

$$\Gamma(B_s \rightarrow \overline{f}) = |\langle f|B_s \rangle|^2 \times e^{-\Gamma t} \left\{ [\rho^2 + \omega(1 - \rho^2)] \cos^2 \frac{\Delta mt}{2} + [1 - \omega(1 - \rho^2)] \sin^2 \frac{\Delta mt}{2} - (1 - 2\omega)\rho \sin \phi_{CP}^- \sin \Delta mt \right\}$$

$$\Gamma(\overline{B}_s \rightarrow \overline{f}) = |\langle f|B_s \rangle|^2 \times e^{-\Gamma t} \left\{ [1 - \omega(1 - \rho^2)] \cos^2 \frac{\Delta mt}{2} + [\rho^2 + \omega(1 - \rho^2)] \sin^2 \frac{\Delta mt}{2} + (1 - 2\omega)\rho \sin \phi_{CP}^- \sin \Delta mt \right\}$$

**Note:  $\Delta\Gamma_s$  neglected**

$$\sin^2 \phi_{CKM} = \frac{1}{2} \times \left\{ 1 + \sin \phi_{CP}^+ \sin \phi_{CP}^- \pm \sqrt{(1 - \sin^2 \phi_{CP}^+)(1 - \sin^2 \phi_{CP}^-)} \right\}$$

$$\rho = \frac{A(B_s \rightarrow D_s^+ K^-)}{A(\overline{B}_s \rightarrow D_s^+ K^-)} \approx 0.7$$

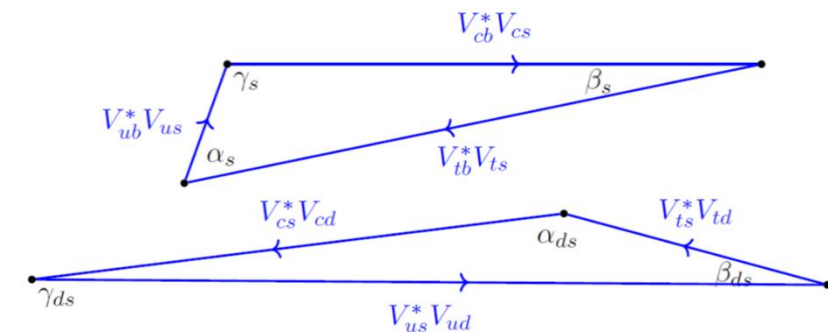
$$\rho(D_s^+ \pi^-) = 0$$

 $\omega = \text{wrong tagging}$ 

	LEP	BaBar	LHCb
$\epsilon(1 - 2\omega)^2$	25-30%	30%	6%

$$\phi_{CP}^\pm = \phi_{CKM} \pm \delta_s$$

$$\phi_{CKM} = \gamma + \gamma_{ds} - 2\beta_s$$



$$\gamma_{ds} \approx 0.04^\circ$$

$$\beta_s \approx 1^\circ (B_s \rightarrow J/\psi \phi)$$

**2-fold ambiguity**

## Expected number of events

$E_{\text{cm}} = 91.2 \text{ GeV}$ and $\int L = 150 \text{ ab}^{-1}$			
$\sigma(e^+e^- \rightarrow Z)$ nb	number of Z	$f(Z \rightarrow \overline{B}_s)$	Number of produced $\overline{B}_s$
$\sim 42.9$	$\sim 6.4 \cdot 10^{12}$	0.0159	$\sim 1 \cdot 10^{11}$
$\overline{B}_s$ decay Mode	Decay Mode	Final State	Number of $\overline{B}_s$ decays
nonCP eigenstates			
$D_s^+ \pi^-$	$D_s^+ \rightarrow \phi \pi$	$K^+ K^- \pi^+ \pi^-$	$\sim 6.9 \cdot 10^6$
$D_s^+ \pi^-$	$D_s^+ \rightarrow \phi \rho$	$K^+ K^- \pi^+ \pi^- \pi^0$	$\sim 12.9 \cdot 10^6$
$D_s^+ K^-$	$D_s^+ \rightarrow \phi \pi$	$K^+ K^- \pi^+ K^-$	$\sim 5.2 \cdot 10^5$
$D_s^+ K^-$	$D_s^+ \rightarrow \phi \rho$	$K^+ K^- \pi^+ K^- \pi^0$	$\sim 9.8 \cdot 10^5$
$D^0 \phi$	$D^0 \rightarrow K \pi$	$K^- \pi^+ K^+ K^-$	$\sim 6.1 \cdot 10^4$
$D^0 \phi$	$D^0 \rightarrow K \rho$	$K^- \pi^+ K^+ K^- \pi^0$	$\sim 1.7 \cdot 10^5$
CP eigenstates			
$J/\psi \phi$	$J/\psi \rightarrow \mu^+ \mu^-$	$\mu^+ \mu^- K^+ K^-$	$\sim 3.2 \cdot 10^6$
$\phi \phi$	$\phi \rightarrow K^+ K^-$	$K^+ K^- K^+ K^-$	$\sim 4.8 \cdot 10^5$

(To be x 2 for  $B_s$ )

# Detector response is parametrized

Acceptance :

$$|\cos \theta| < 0.95$$

Track  $p_T$  resolution :

$$\frac{\sigma(p_T)}{p_T^2} = 2. \times 10^{-5} \oplus \frac{1.2 \times 10^{-3}}{p_T \sin \theta}$$

Track  $\phi, \theta$  resolution :

$$\sigma(\phi, \theta) \mu\text{rad} = 18 \oplus \frac{1.5 \times 10^3}{p_T \sqrt[3]{\sin \theta}}$$

Vertex resolution :

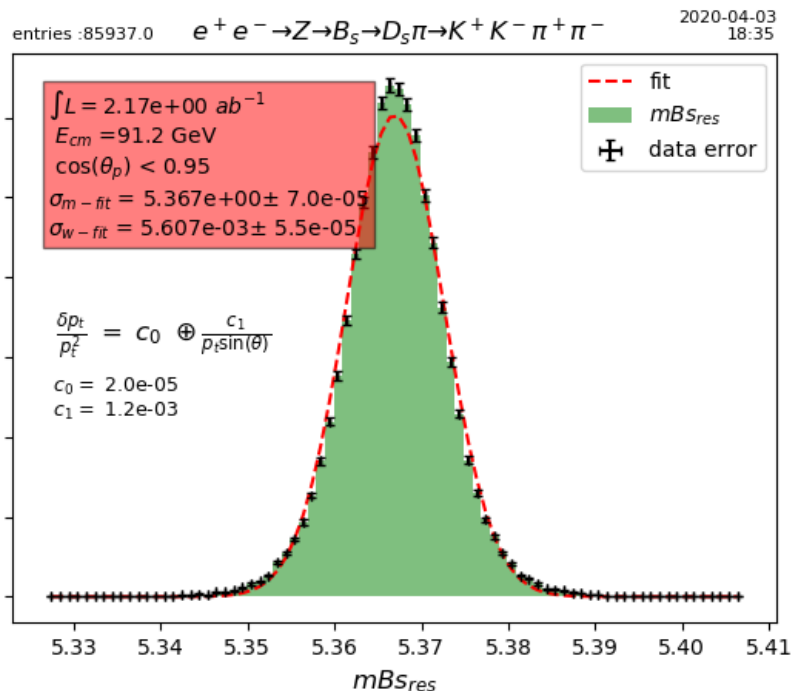
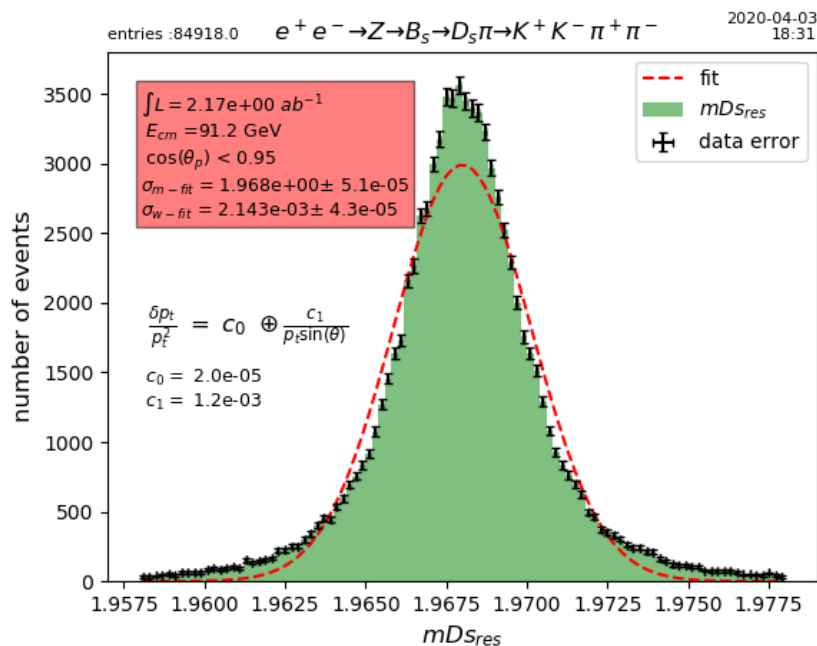
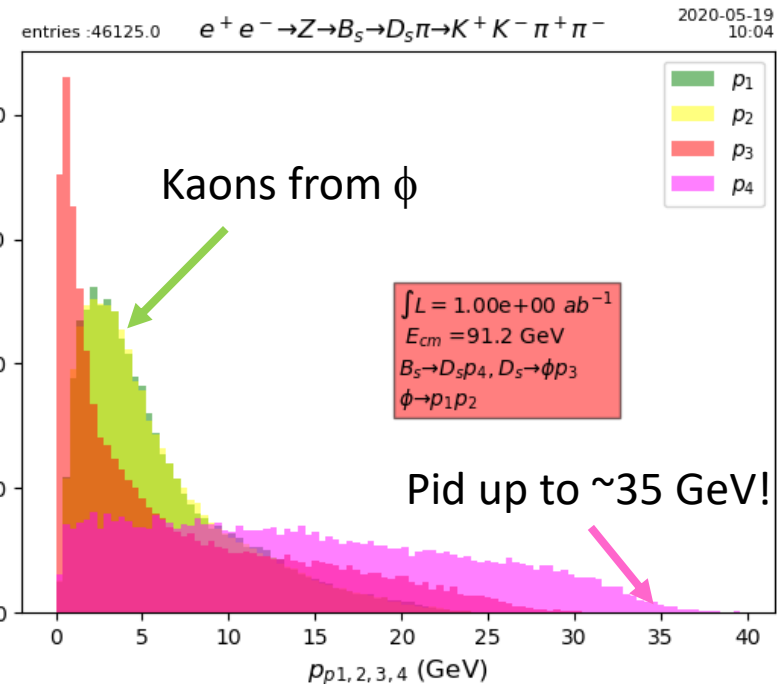
$$\sigma(d_{\text{Im}}) \mu\text{m} = 1.8 \oplus \frac{5.4 \times 10^1}{p_T \sqrt{\sin \theta}}$$

Vertex resolution :

$$\langle \sigma(d_{\text{Im}}) \rangle \simeq 10 \mu\text{m} \text{ (Bachelor } \pi/K)$$

Calorimeter resolution :

$$\frac{\sigma(E)}{E} = \frac{5 \times 10^{-2}}{\sqrt{E}} \oplus 5 \times 10^{-3}$$



Charged final state only

	unit	value
acceptance	%	86
$\sigma(m_{D_s})$	MeV	$\sim 2.1$
$\sigma(m_{B_s})$	MeV	$\sim 5.6$

To be compared to

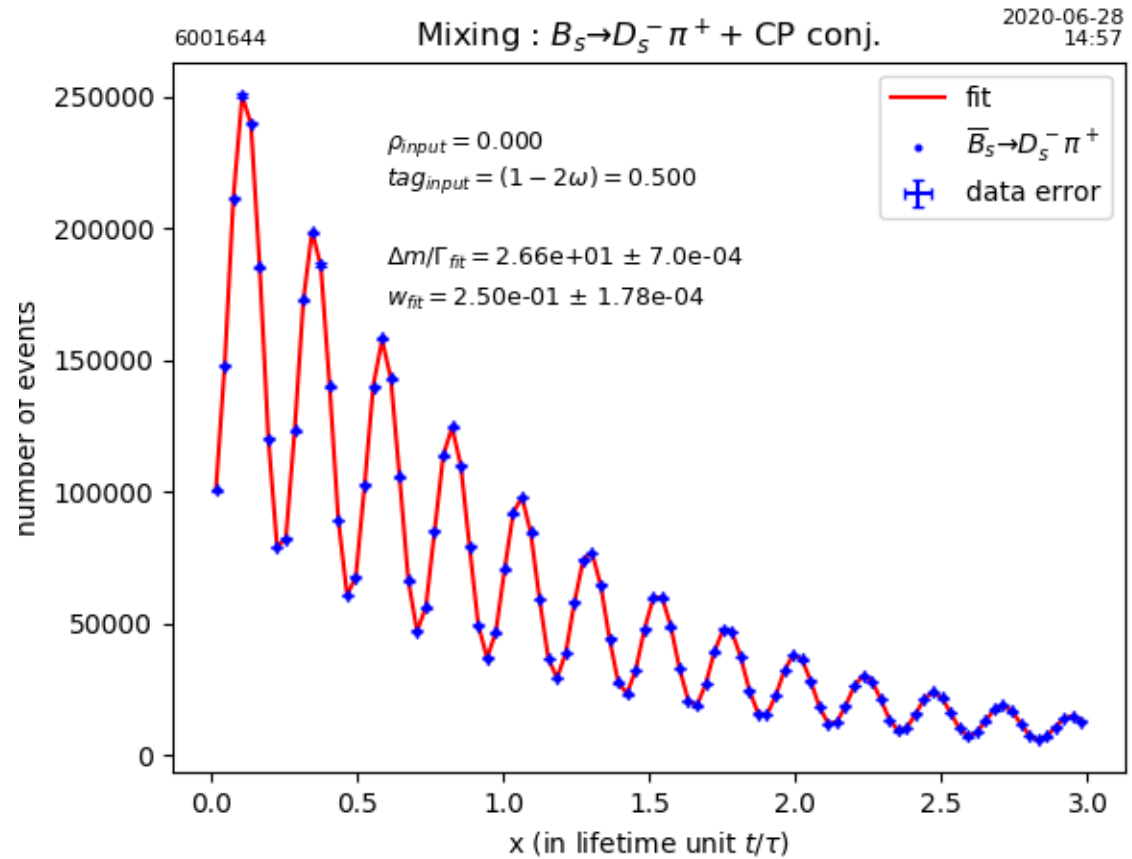
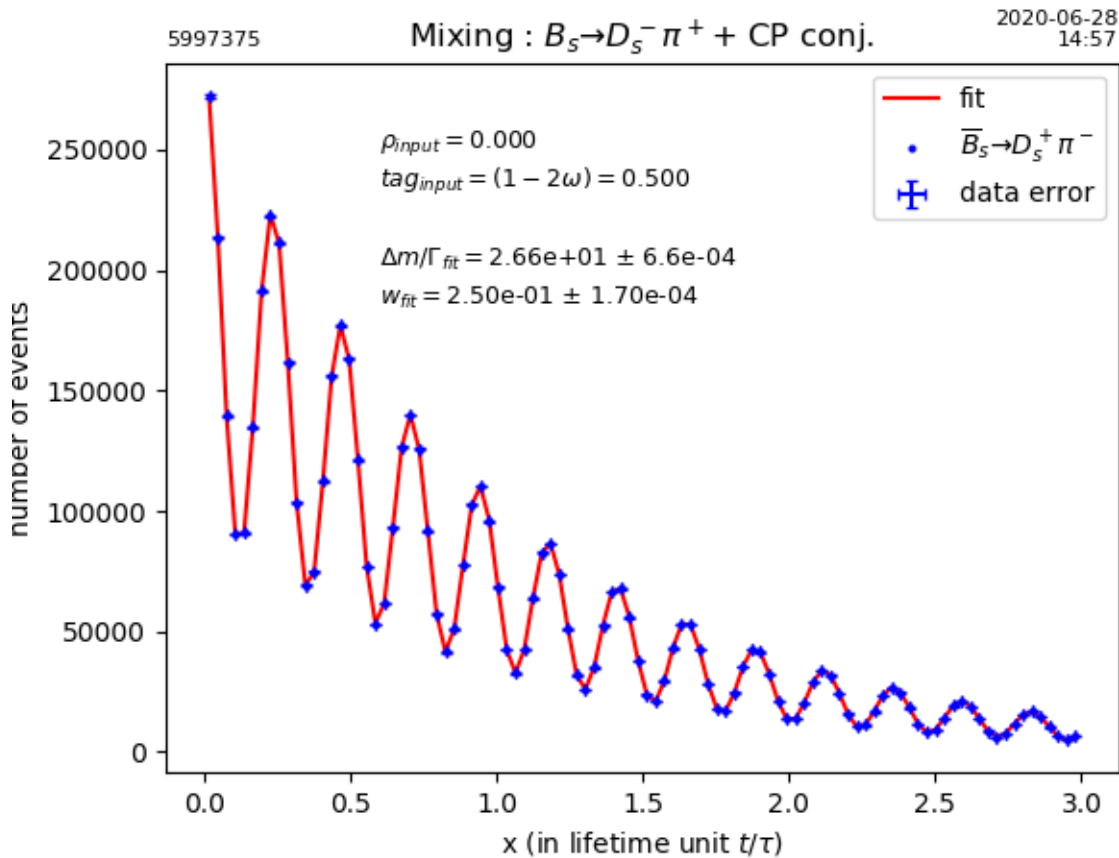
$$\sigma(m_{B_s})_{\text{LHCb}} \approx 17 \text{ MeV}$$

# B<sub>s</sub> Mixing Measurement with B<sub>s</sub> → D<sub>s</sub>π

Mean B flight distance ≈ 3000 μm

Flight distance resolution < 20 μm (negligible) ⇒ full simulation and vertex fit would be useful (cf E.Perez)

Background mainly combinatorics (very small)



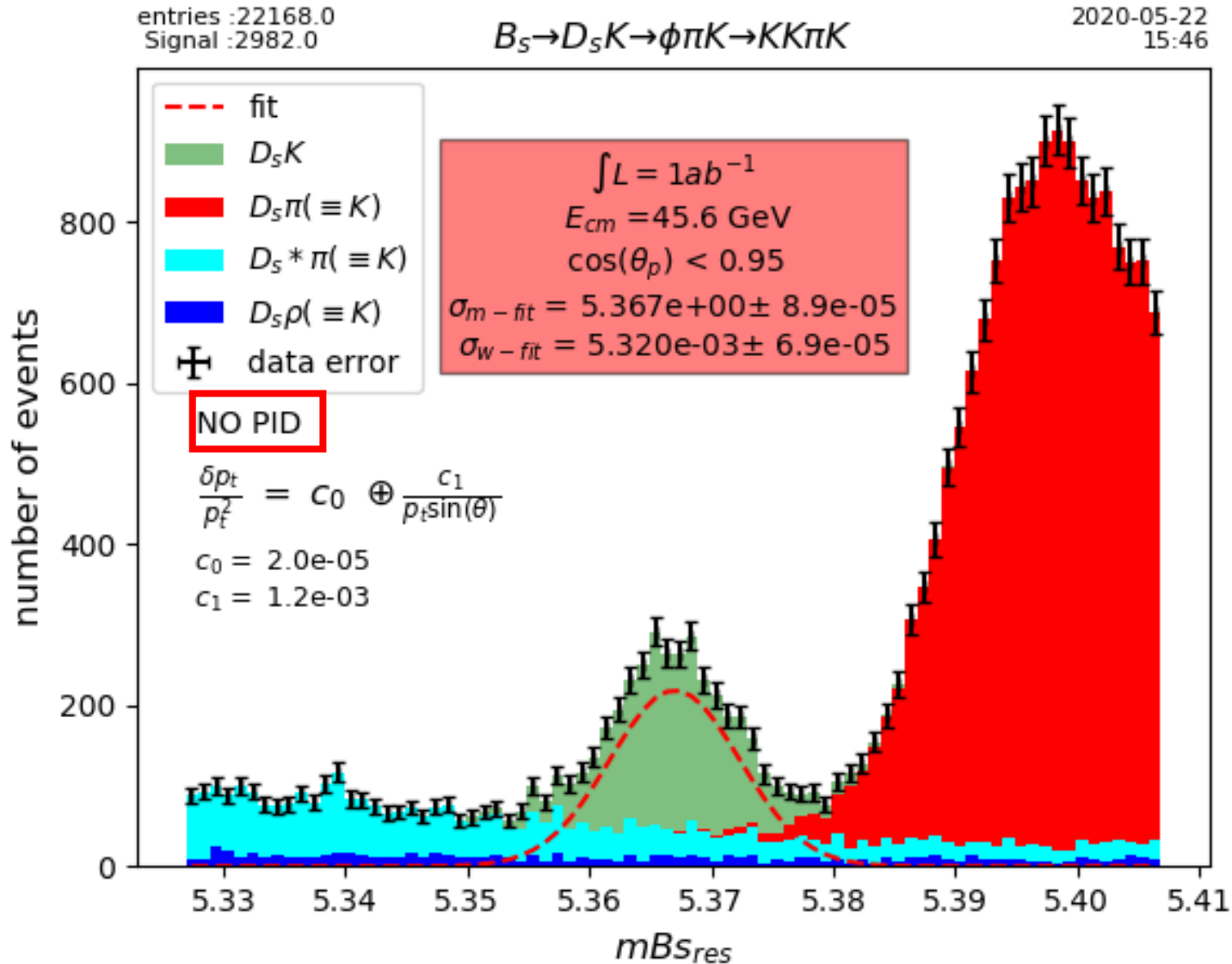
Result 1 :

$$\delta(\Delta m_{B_s})_{stat} \approx (5 \times 10^{-4}) 10^{12} \hbar s^{-1} [PDG: (2.1 \times 10^{-2}) 10^{12} \hbar s^{-1}]$$

$$\delta(\omega)_{stat} = 1.4 \times 10^{-4}$$

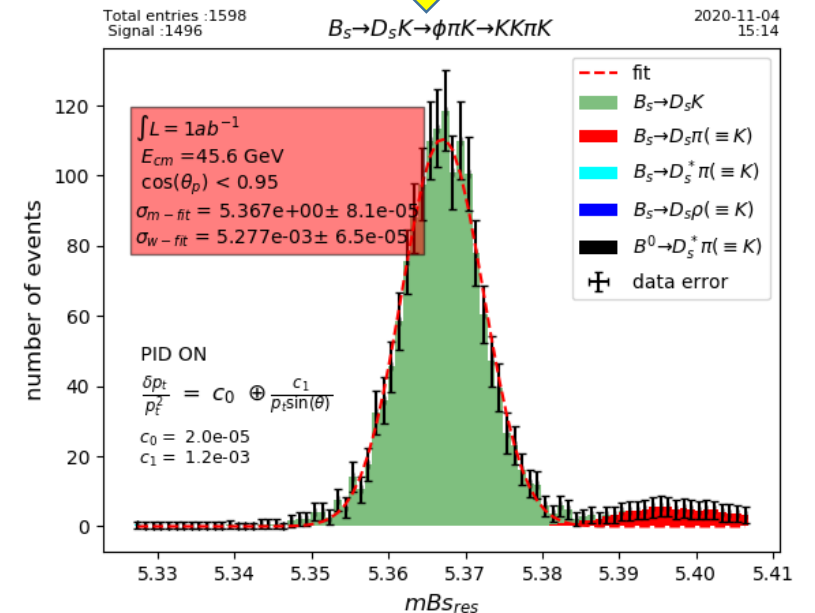
Wrong tagging measured very precisely

# Measurement of CP violation with $B_s \rightarrow D_s K$



Result 2 :

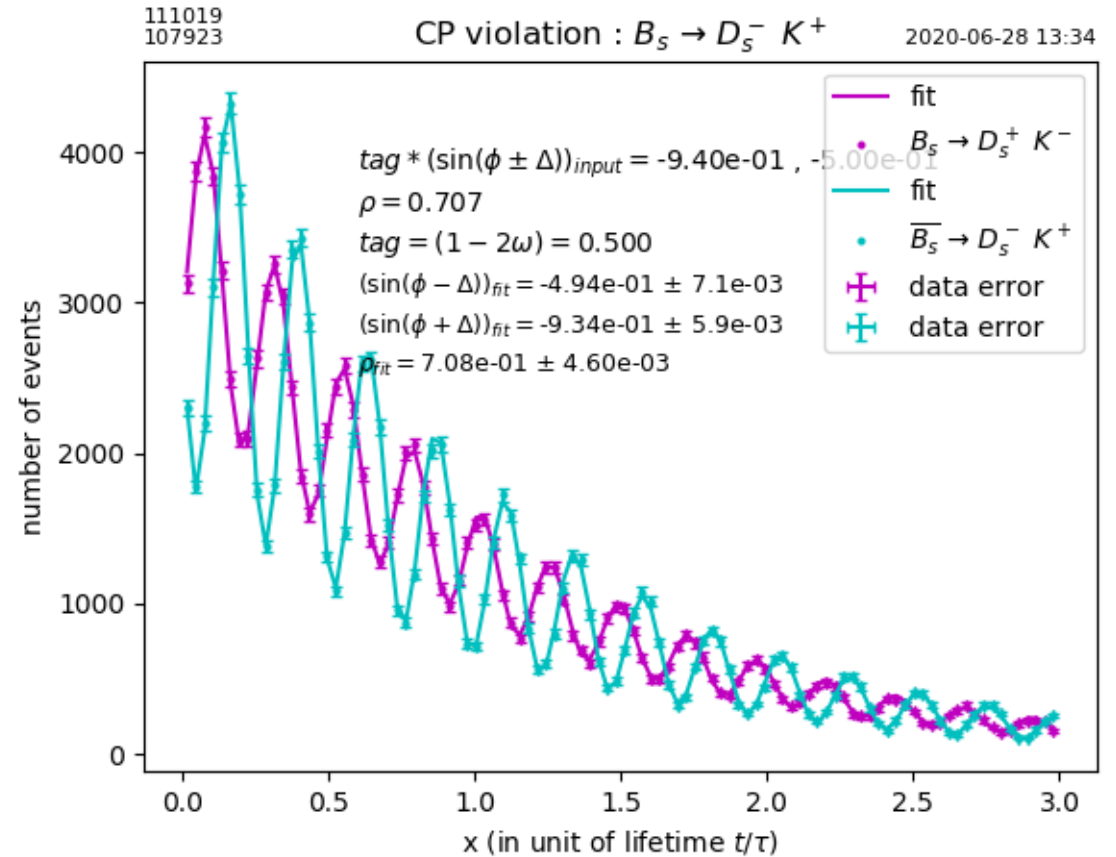
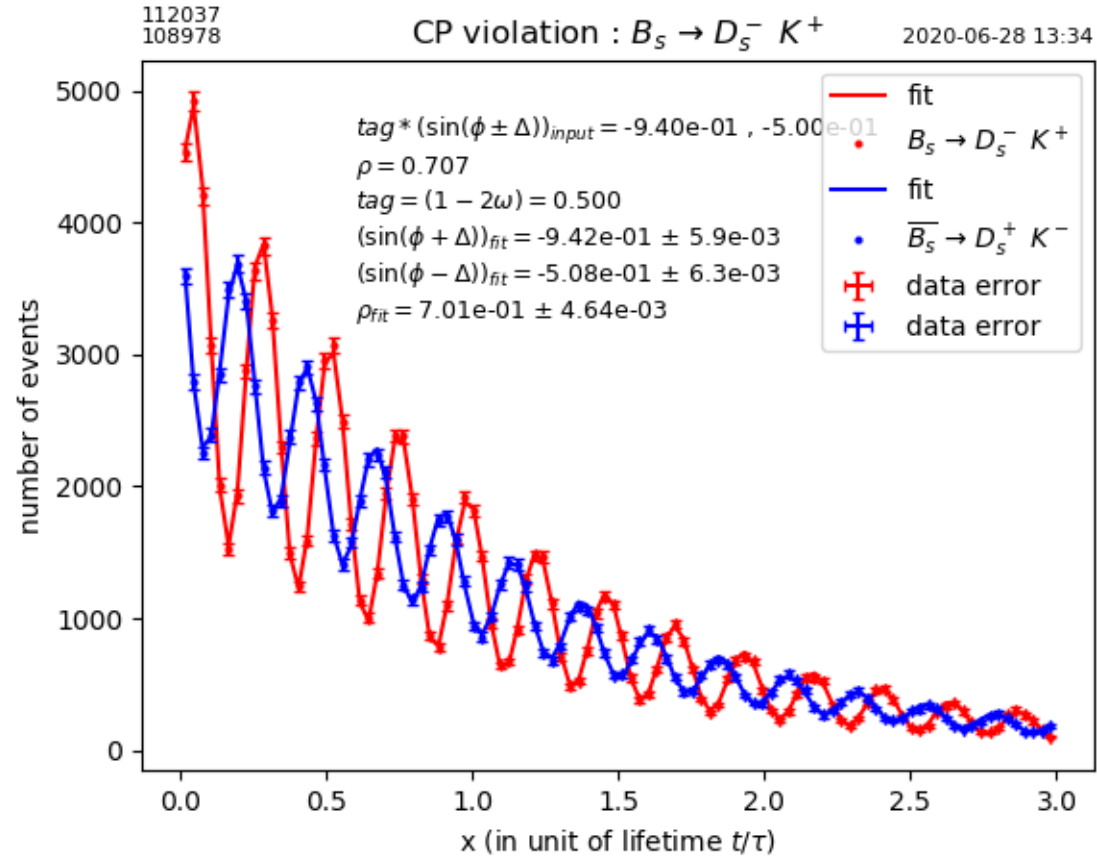
- Tracking resolution **crucial** to reduce background
- Combinatoric background to be added (but expected to be relatively small)
- A modest PID (ToF + dE/dx) enough (see presentation later this afternoon)



# Measurement of CP violation with $B_s \rightarrow D_s K$

$$\int L dt = 150 \text{ ab}^{-1}$$

PDG:  $\gamma = (71.1^{+4.6}_{-5.3})^\circ$



Result 3 :

$$\delta(\rho) \approx 3.2 \times 10^{-3} (stat.)$$

$$\delta(\sin^2 \phi_{CKM}) \approx \delta(\sin^2 \gamma) \approx 5 \times 10^{-3} (stat.) \cong \delta(\gamma) \approx 0.4^\circ (stat.)$$

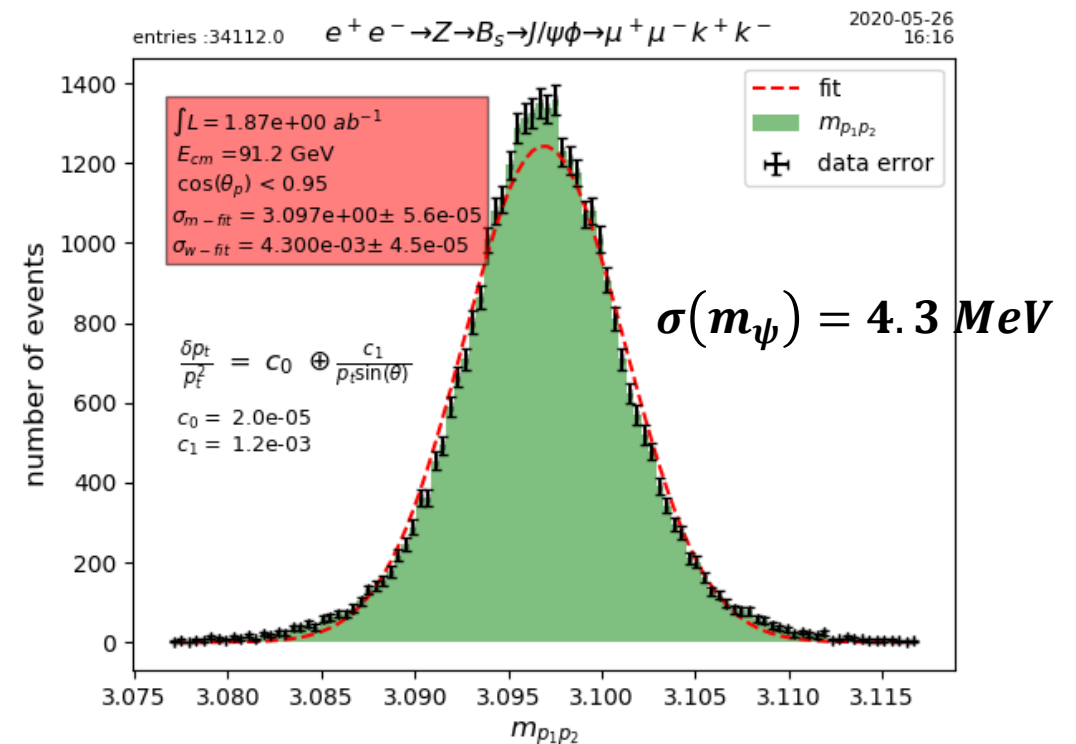
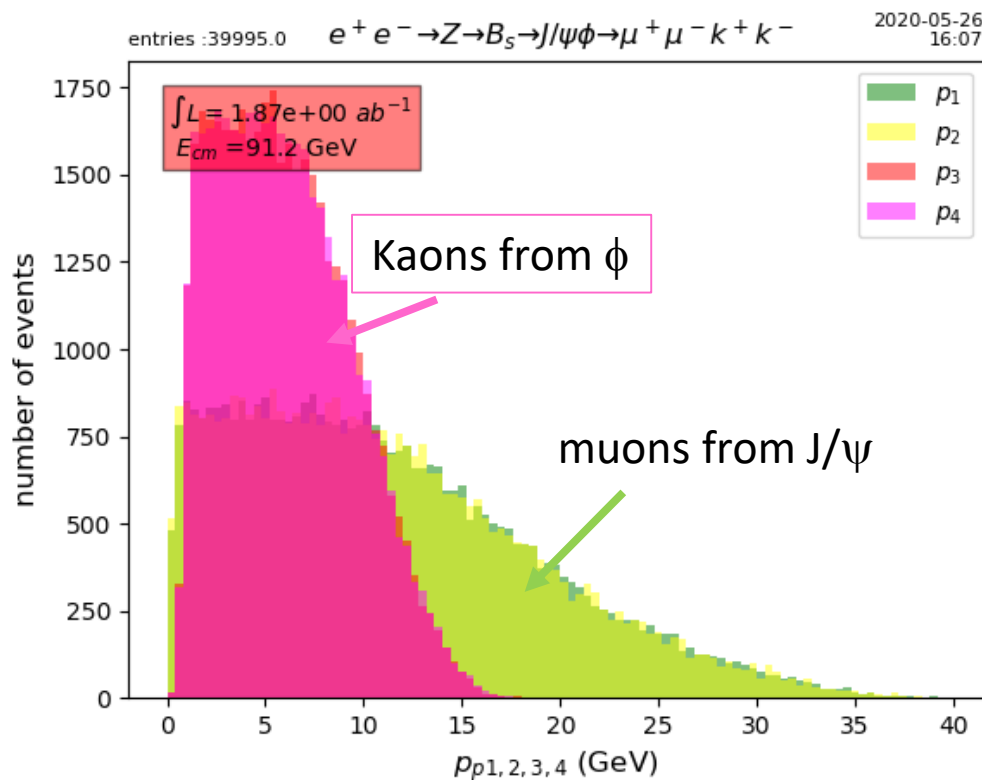
Potential statistical gain of factor 4-5 with  $D_s^\pm \rightarrow K^{*0} K^\pm, \phi \rho^\pm, \dots$  but background needs to be studied (see later)+  
 Additional potential gain (another factor  $\sim 2$ ) with  $B_s \rightarrow D_s^{*\pm} K^\mp, D_s^\pm K^{*\mp}, D_s^{*\pm} K^{*\mp}$ , most modes including  $\gamma(s)$

# Measurement of CP violation with $B_s \rightarrow J/\psi\phi \rightarrow \mu^+\mu^-K^+K^-$

With  $B_s \rightarrow D_s K$  :  $\delta(\phi_{CKM}) = \delta(\gamma + \gamma_{ds} - 2\beta_s) \lesssim 0.4^\circ$  (stat.)

To take advantage of the full sensitivity , measurement of  $\beta_s$  needed

With  $B_s \rightarrow J/\psi\phi$   $\phi_{CKM} = 2\beta_s \approx 2^\circ$



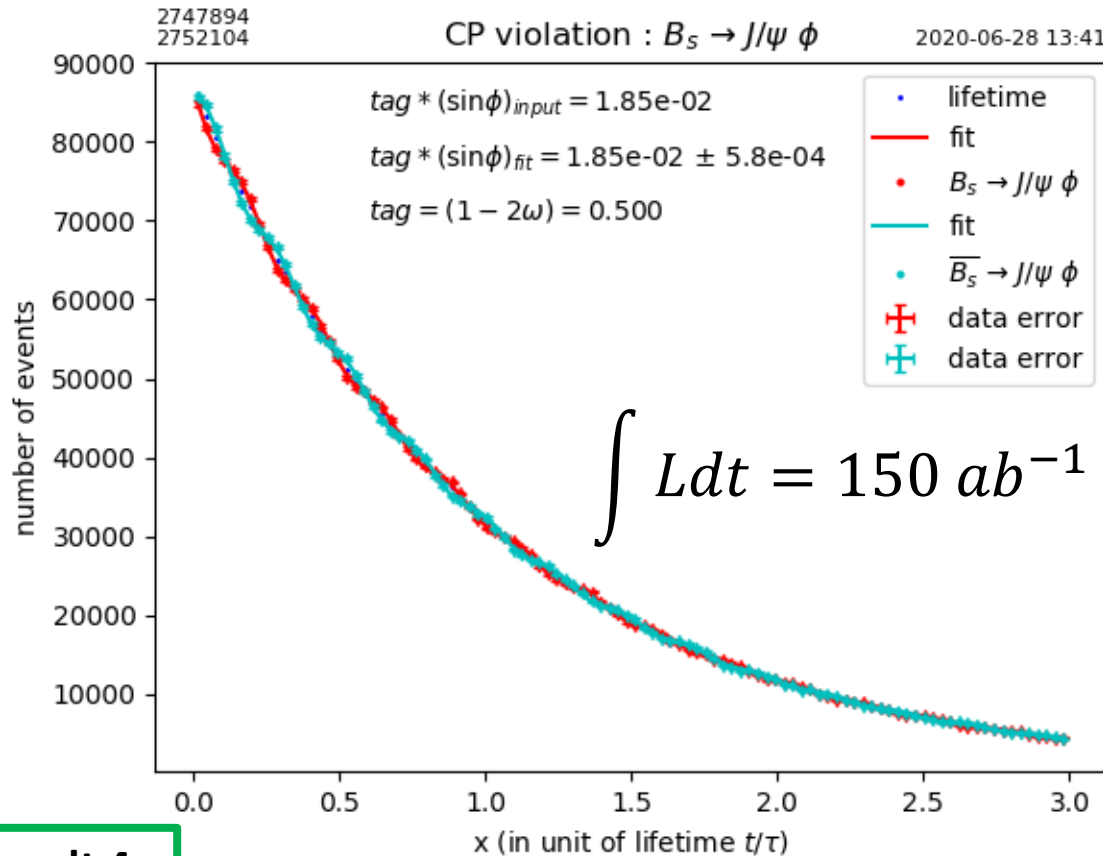


# Measurement of CP violation with $B_s \rightarrow J/\psi\phi \rightarrow \mu^+\mu^-K^+K^-$

CKM:  $\beta_s \approx 1^\circ$

PDG:  $\beta_s = (0.60 \pm 0.89)^\circ$

With  $\Gamma_L/\Gamma = 1$



However for  $B_s \rightarrow J/\psi\phi$

PDG		
$f_L = \Gamma_L/\Gamma$	$0.527 \pm 0.008$	CP = +
$f_{\parallel} = \Gamma_{\parallel}/\Gamma$	$0.228 \pm 0.007$	CP = +
$f_{\perp} = \Gamma_{\perp}/\Gamma$	$0.245 \pm 0.004$	CP = -

In HQS,  $\Gamma_{\parallel} = \Gamma_{\perp} \Leftrightarrow \mathcal{A}^{mix} = \mathcal{A}_L^{mix}$

Angular analysis required (tbd) :  $\Gamma_L/\Gamma \neq 1$   
 Otherwise additional  $\sin\Phi$  term amplitude reduction by factor  $\sim(1 - 2f_{\perp})$

Reduced sensitivity by factor  $\sim 2$  (can be partly compensated using  $J/\psi \rightarrow e^+ e^-$ )

Result 4 :

$$\delta(\sin\phi_{CKM}) = \delta(\sin 2\beta_s) \approx 1.2 \times 10^{-3} \cong \delta(\beta_s) \approx 3.5^\circ \times 10^{-2} (stat.)$$

# Inclusion of neutrals for $B_S \rightarrow D_S K$ reconstruction

e.g. could potentially increase statistics (x 3) by adding  $D_S^\pm \rightarrow \phi \rho^\pm$   $\frac{D_S^\pm \rightarrow \phi \rho^\pm}{D_S^\pm \rightarrow \phi \pi^\pm} \approx 1.9$

More generally many physics topics (such as flavor physics) would benefit by using neutrals

⇒ Significant advantage compared to LHCb ⇒ constraint on calorimeter and PId

With very good calorimeter resolution (Xtal type)

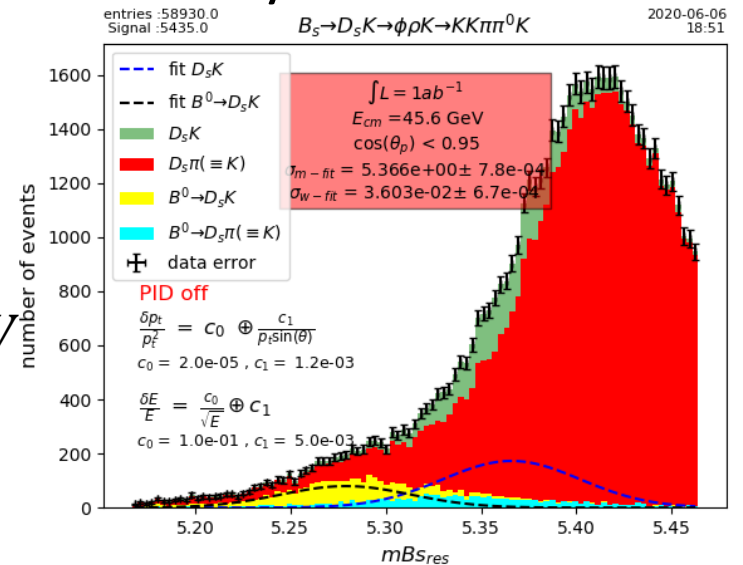
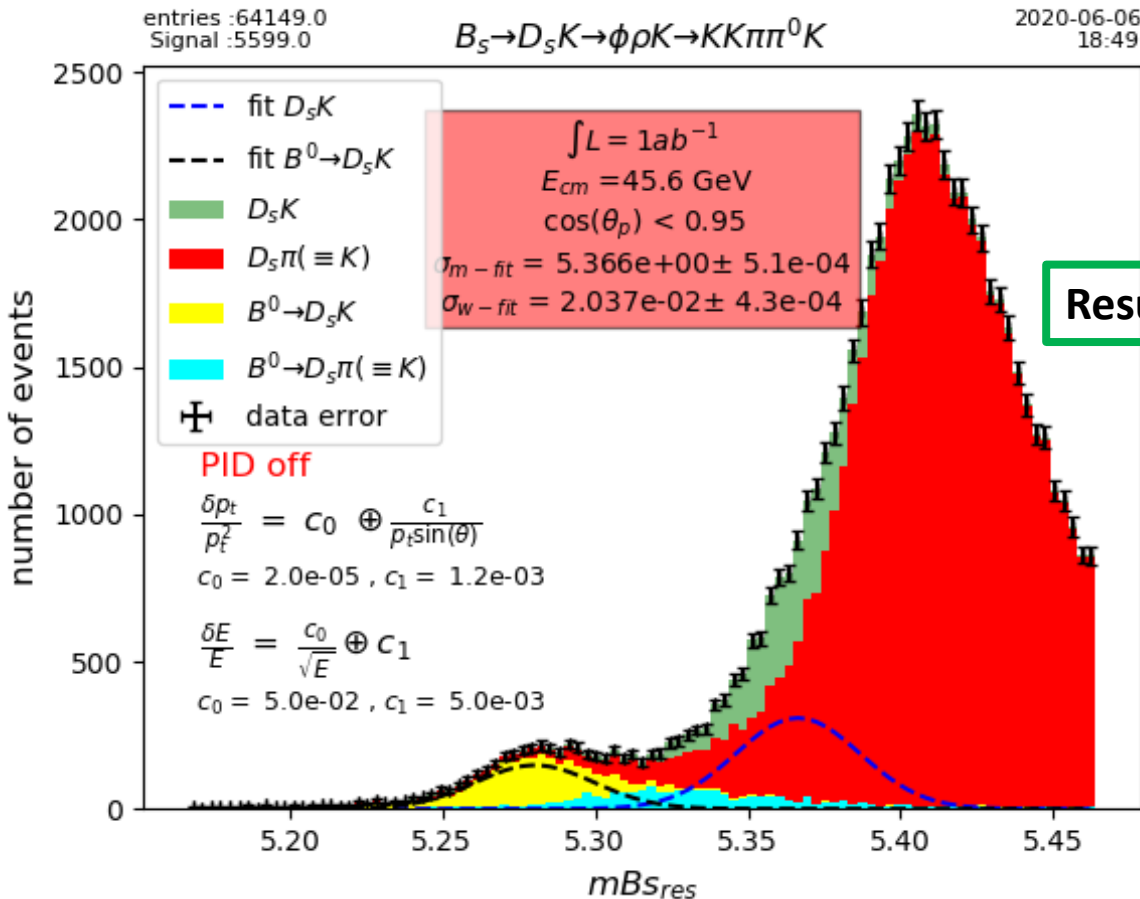
$$\sigma(D_S^\pm(\phi\pi^\pm)K^\mp) \approx 5.6\text{MeV} \rightarrow \sigma(D_S^\pm(\phi\rho^\pm)K^\mp) \approx 20\text{MeV}$$

⇒ Background  $D_S^\pm(\phi\rho^\pm)\pi^\mp$  huge

**Result 6 :** ⇒ Excellent PId mandatory

Much worse with LAr type Cal.

$$\sigma(D_S^\pm(\phi\rho^\pm)K^\mp) \approx 36.\text{MeV}$$

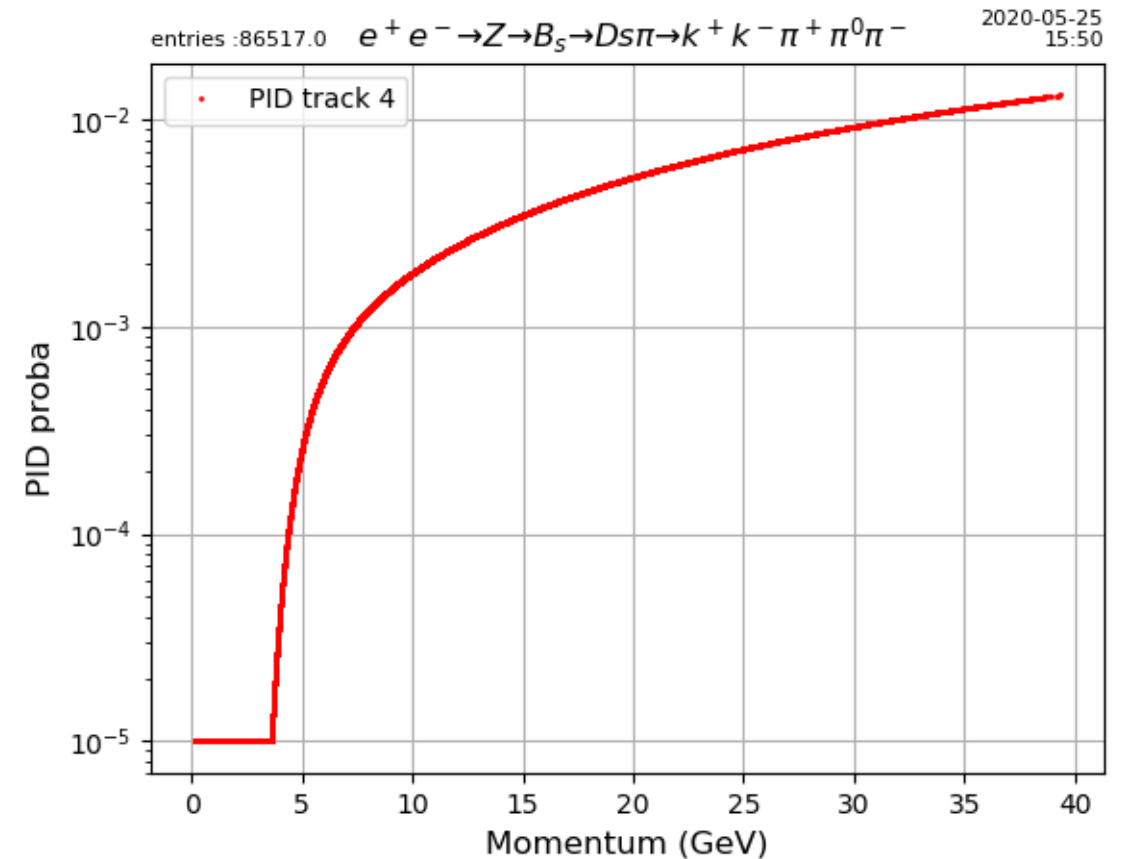
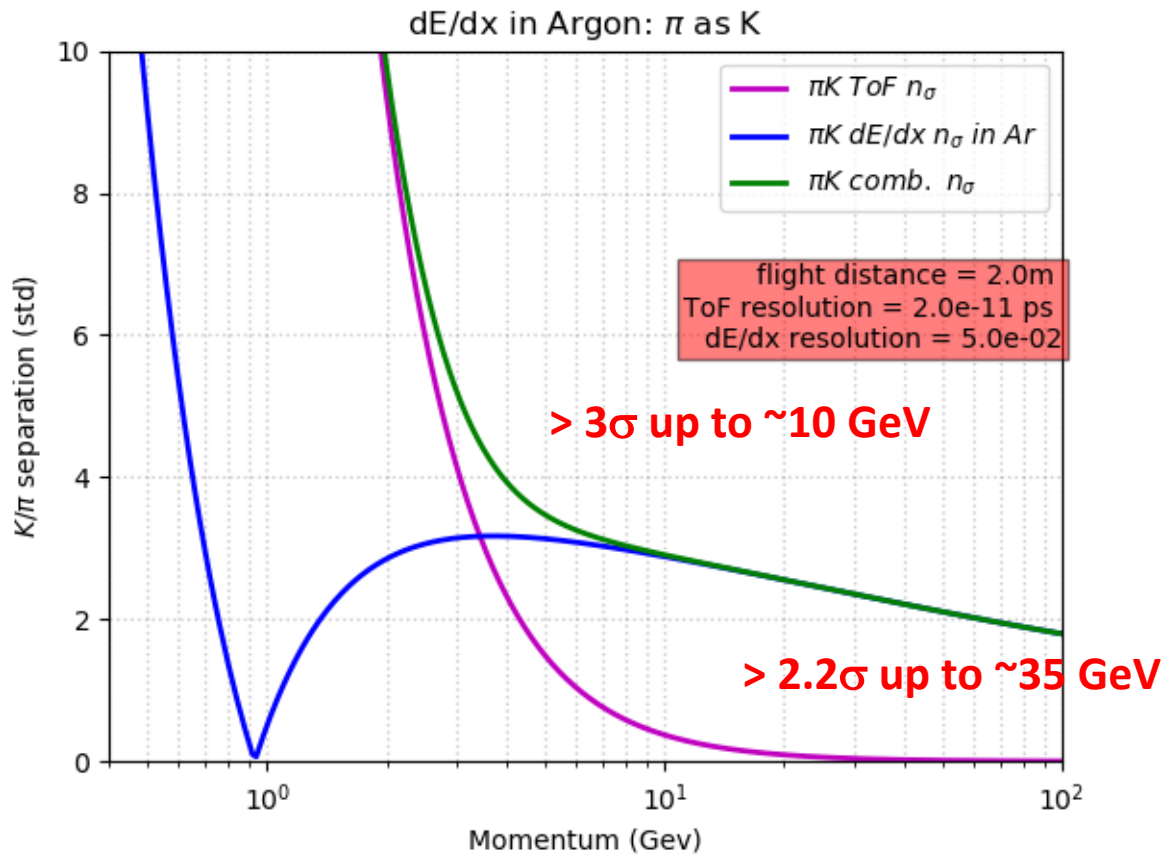


# Inclusion of « standard and modest » PID (dE/dx and ToF)

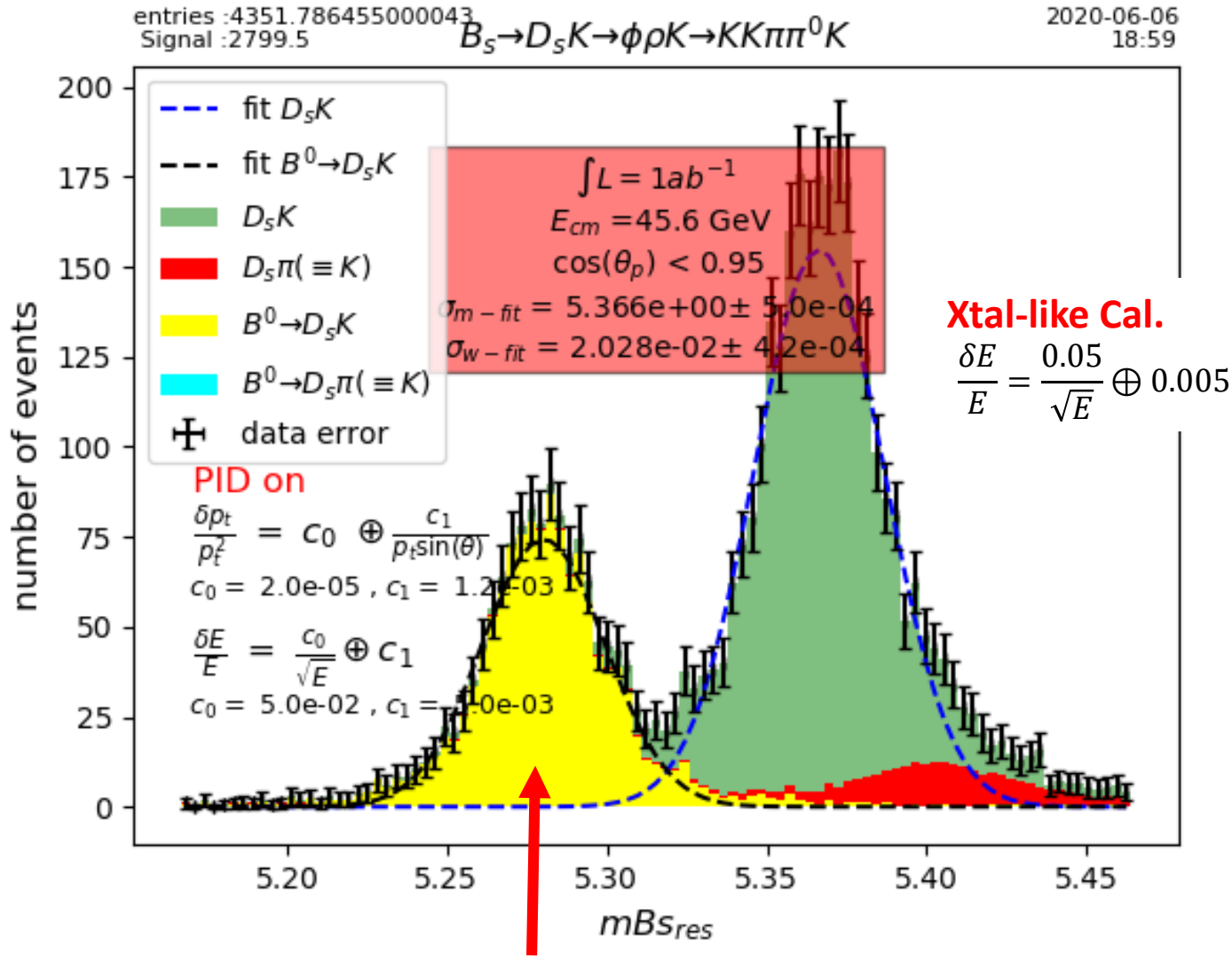
Somewhat conservative PID

- Resolution  $\sigma\left(\frac{dE}{dx}\right) = 5\%$
- Resolution  $\sigma(ToF) = 20\text{ps}$  ( $\cong 6\text{mm}$ )
- ToF Detector location : 2m from IP

Probability of  $\pi$  misidentification as K with  $\varepsilon(K)=50\%$



# Effect of dE/dx and ToF

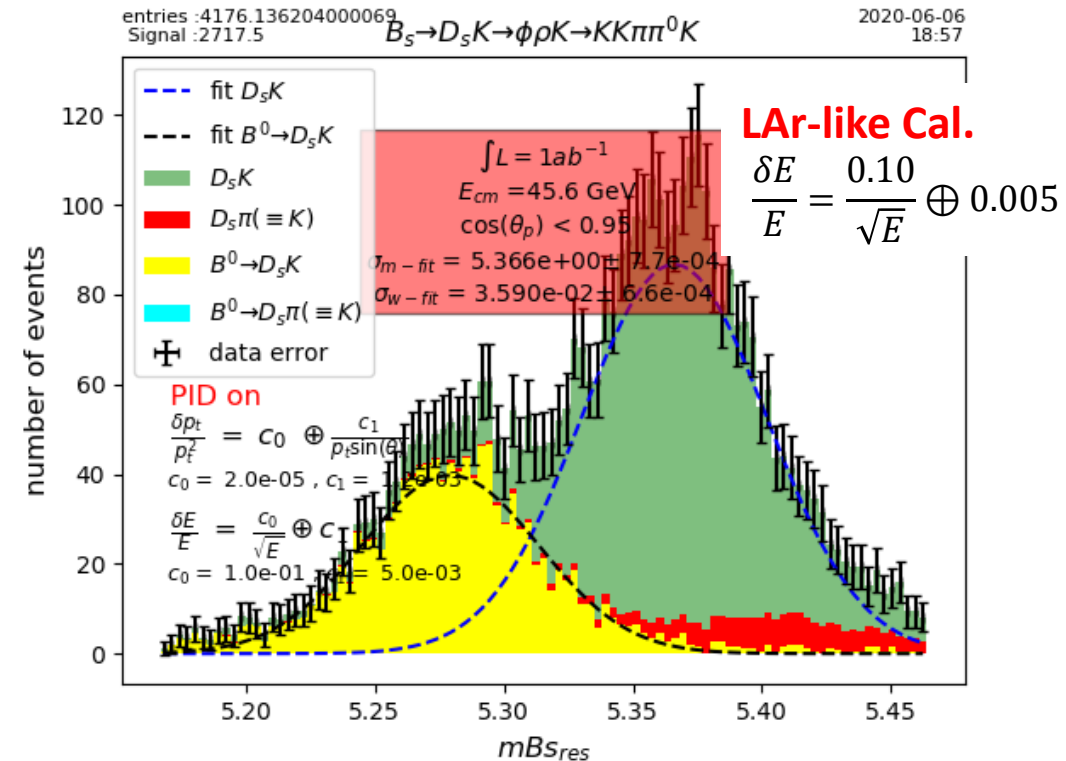


« Irreducible bkg », only mass resolution can beat it

**Result 7 : Excellent calorimetry (Xtal like) is also mandatory**

Other backgrounds have to be added  
dE/dx + simple ToF probably not enough unless

- beyond state-of-the-art is achieved for dE/dx and ToF
- or addition of a dedicated PID system

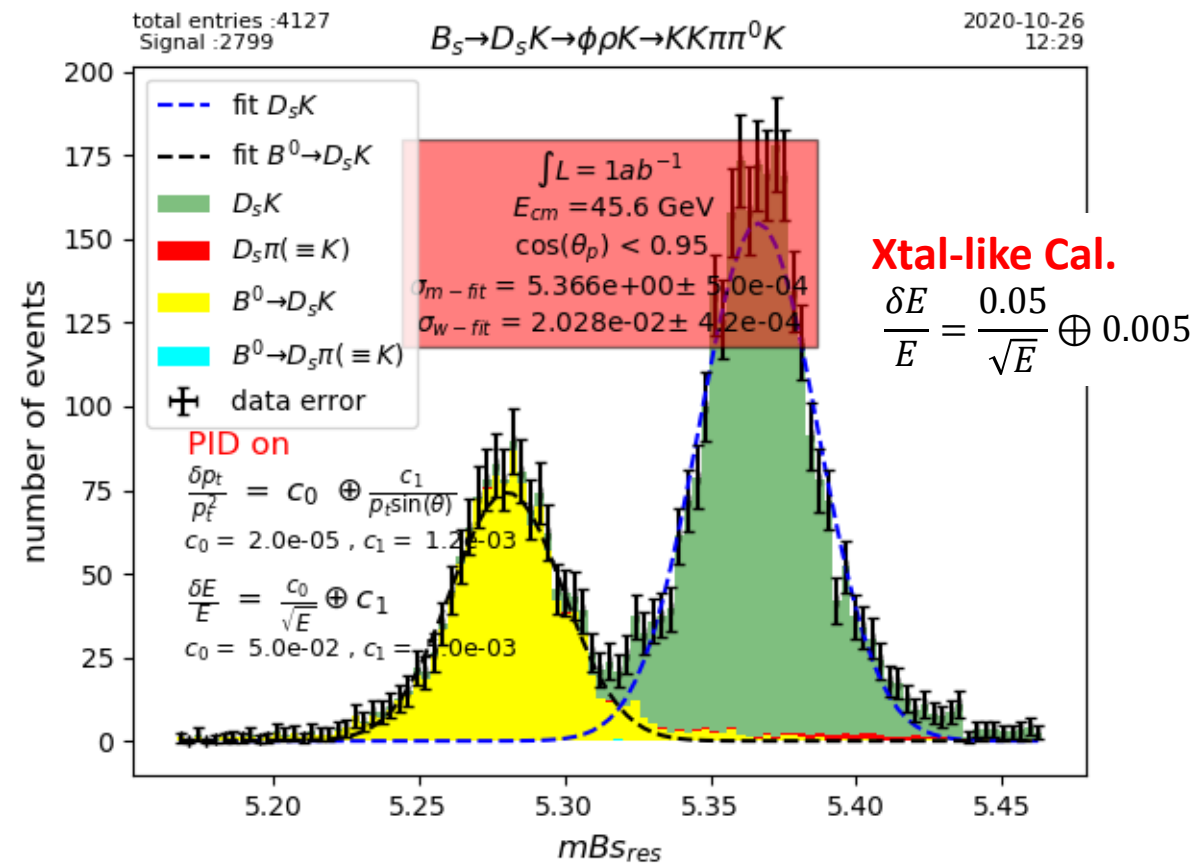
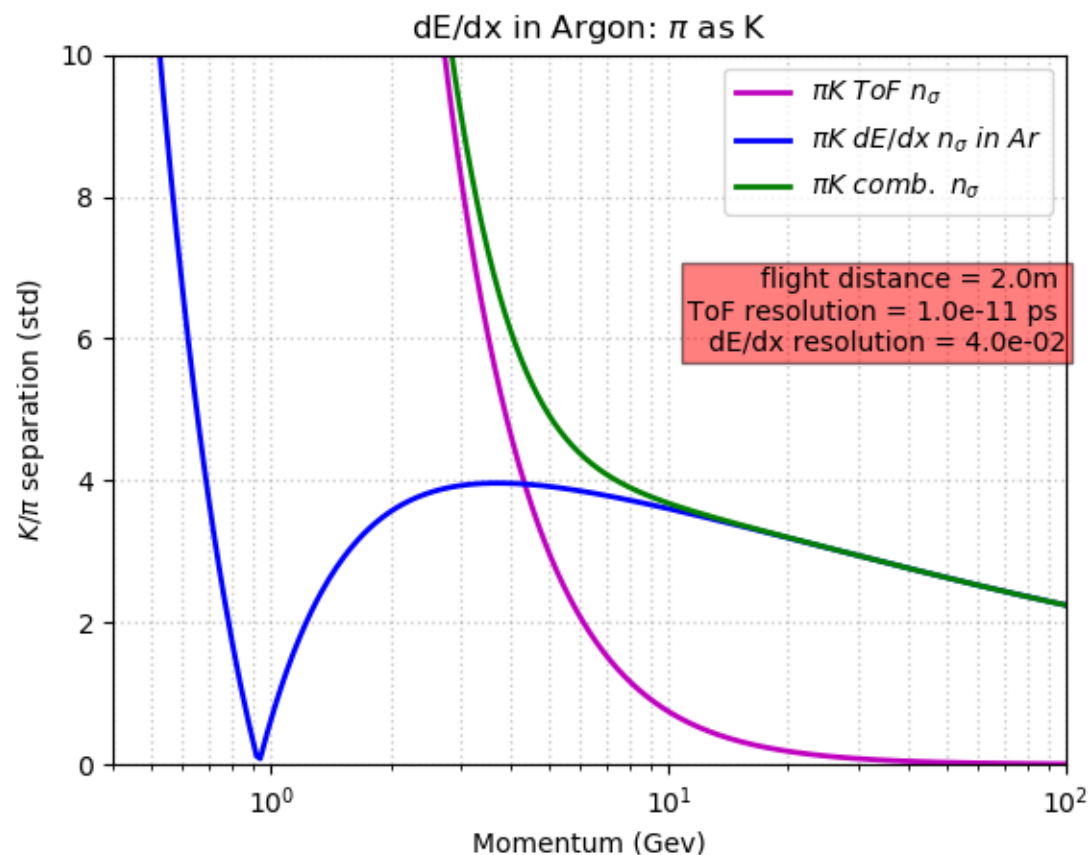


# Inclusion of « improved » dE/dx and ToF

Resolution  $\sigma\left(\frac{dE}{dx}\right) = 4\%$

Resolution  $\sigma(ToF) = 10\text{ps} (\cong 3\text{mm})$

Detector location : 2m from IP



## Conclusions

$B_s \rightarrow D_s K$  (as well as  $B_s \rightarrow J/\psi \phi$ ,  $B_s \rightarrow \phi \phi$ ) are excellent showcases for

- Studying sensitivity on CP violation (measurement of CKM angle  $\gamma$ ,  $\beta_s$ )
- Excellent for search of BSM physics, in particular with  $B_s \rightarrow \phi \phi$
- Determining constraints on detector



$\delta(\gamma) \lesssim 0.4^\circ$  (stat.),  $\delta(\beta_s) \lesssim 3.4^\circ \times 10^{-2}$  (stat.) achievable

with only 1  
decay mode !!!

More than 1 order of magnitude improvement compared to present PDG errors

However this requires



**Excellent tracking and vertexing resolution**,  $\frac{\sigma(p_T)}{p_T^2} \leq 2. \times 10^{-5} \oplus \frac{1.2 \times 10^{-3}}{p_T \sin \theta}$



**Excellent calorimetry resolution**, ideally  $\frac{\sigma(E)}{E} \lesssim \frac{5 \times 10^{-2}}{\sqrt{E}} \oplus 5 \times 10^{-3}$

Allows to use  
many other  
decay mode !!!

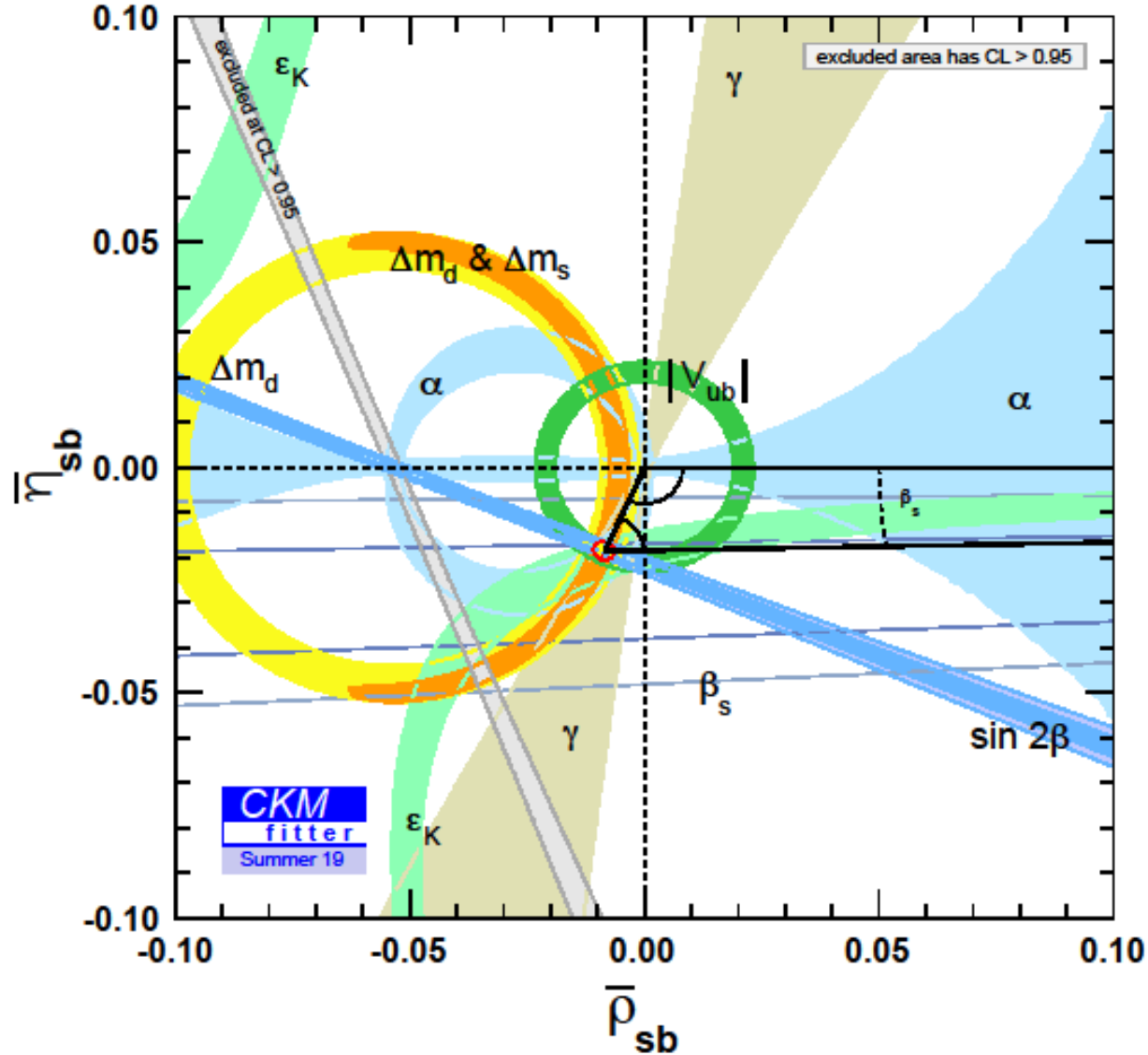


**AND Excellent PID resolution**

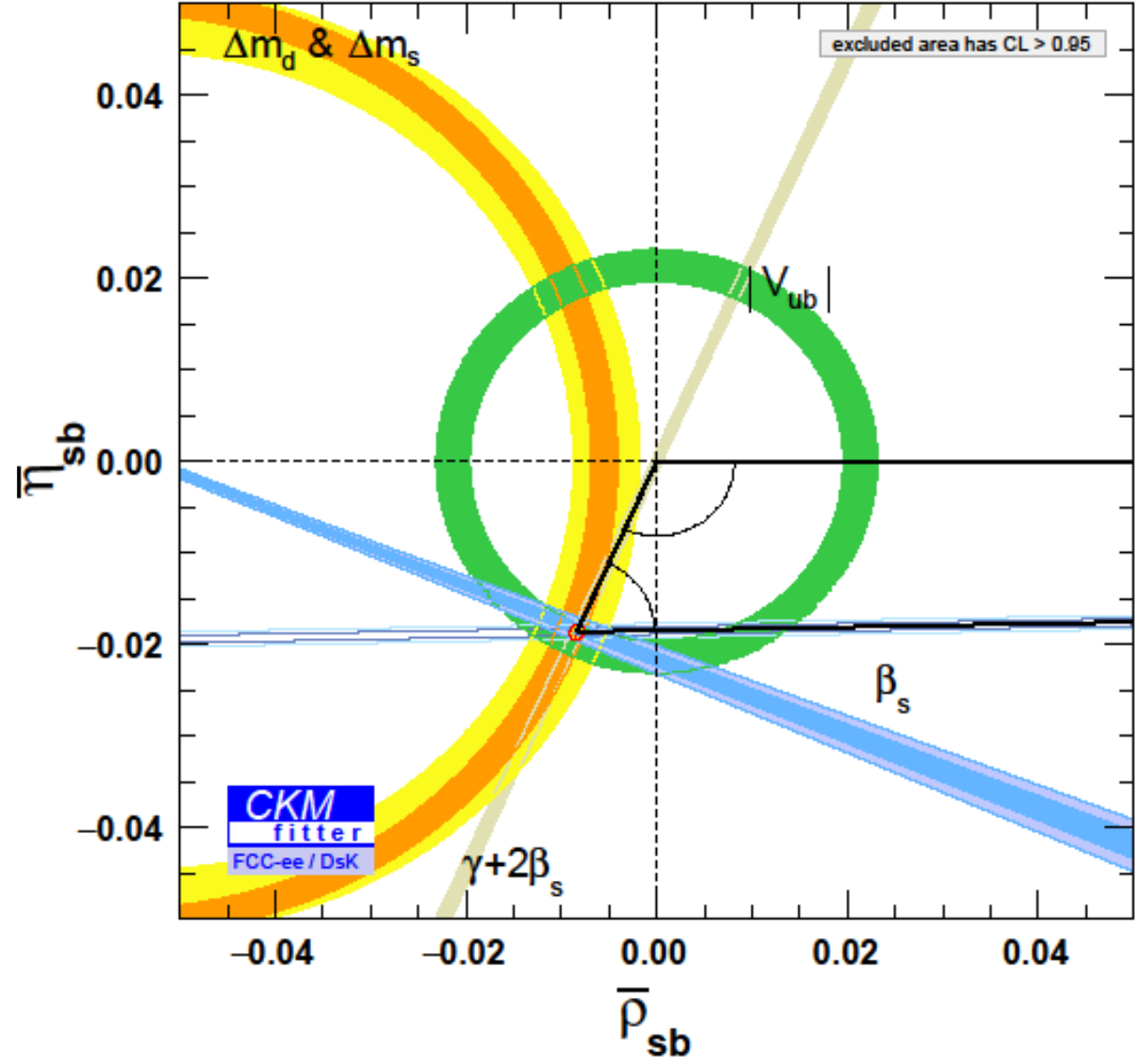
$> 3 \sigma$   $K/\pi$  separation up to 25 GeV (covers also K tagging),  
Ideally up to 35 GeV

A full simulation would be useful to refine further analysis, in particular for vertexing

Present situation



Foreseen situation with FCCee  
(Note the different scale)



# Backup Slides



In SM , only few other possible diagrams with same CKM element as tree diagram

- ⇒ well defined CKM angle measured
- ⇒ no direct CP violation expected

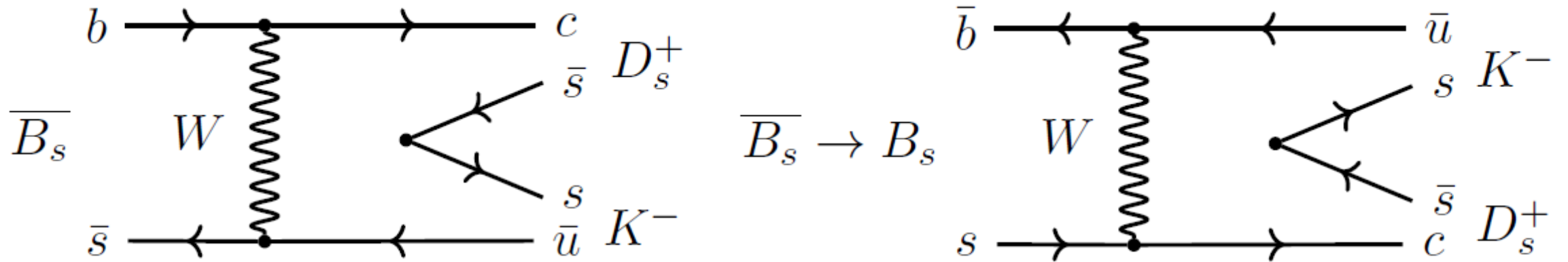


Figure 5: Exchange (sub-dominant) diagrams for  $\bar{B}_s \rightarrow D_s^+ K^-$

# Simulated detector configuration

*Silicon vertex and tracking detector*

2020-10-01 14:56

**B = 3.8T**

<i>layer</i>	<i>r (cm)</i>	<i><math>\delta</math> (<math>\mu\text{m}</math>)</i>	<i>x0</i>
1	1.60e+00	3.00e+00	1.50e-03
2	1.80e+00	6.00e+00	1.50e-03
3	3.70e+00	4.00e+00	1.50e-03
4	3.90e+00	4.00e+00	1.50e-03
5	5.80e+00	4.00e+00	1.50e-03
6	6.00e+00	4.00e+00	1.50e-03
7	1.53e+01	7.00e+00	6.50e-03
8	3.00e+01	7.00e+00	6.50e-03

*Silicon outer detector*

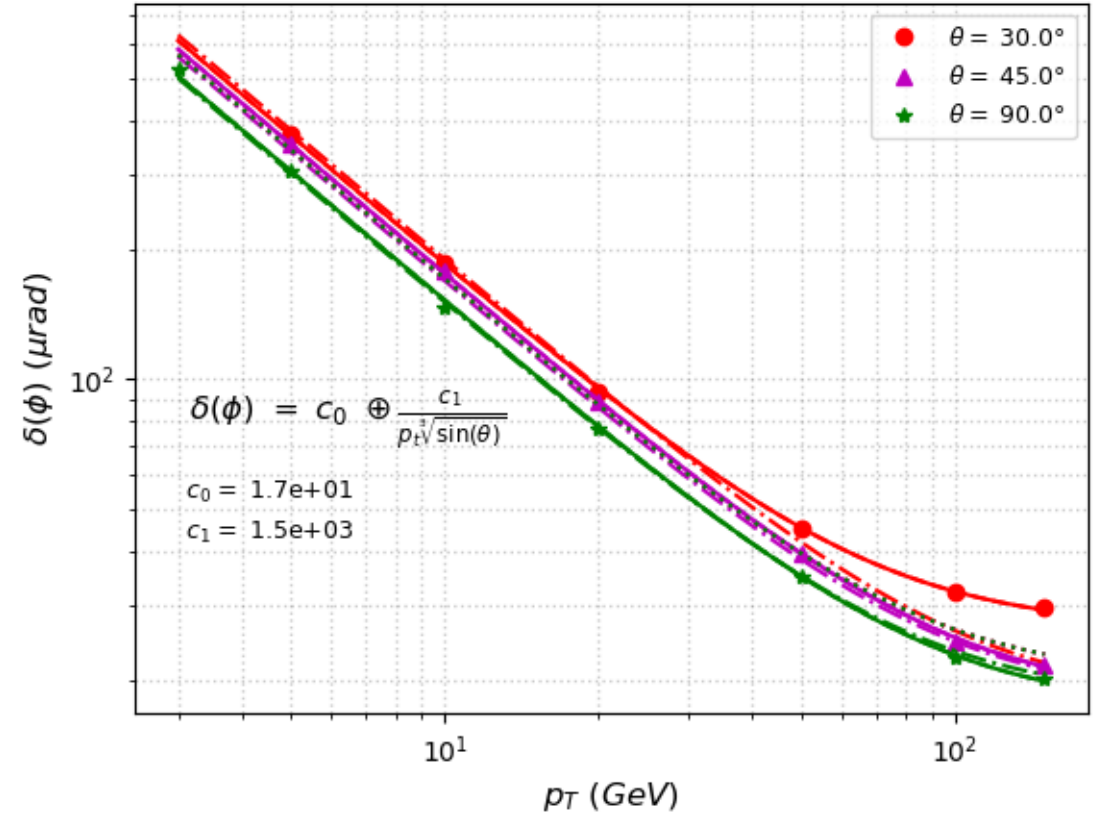
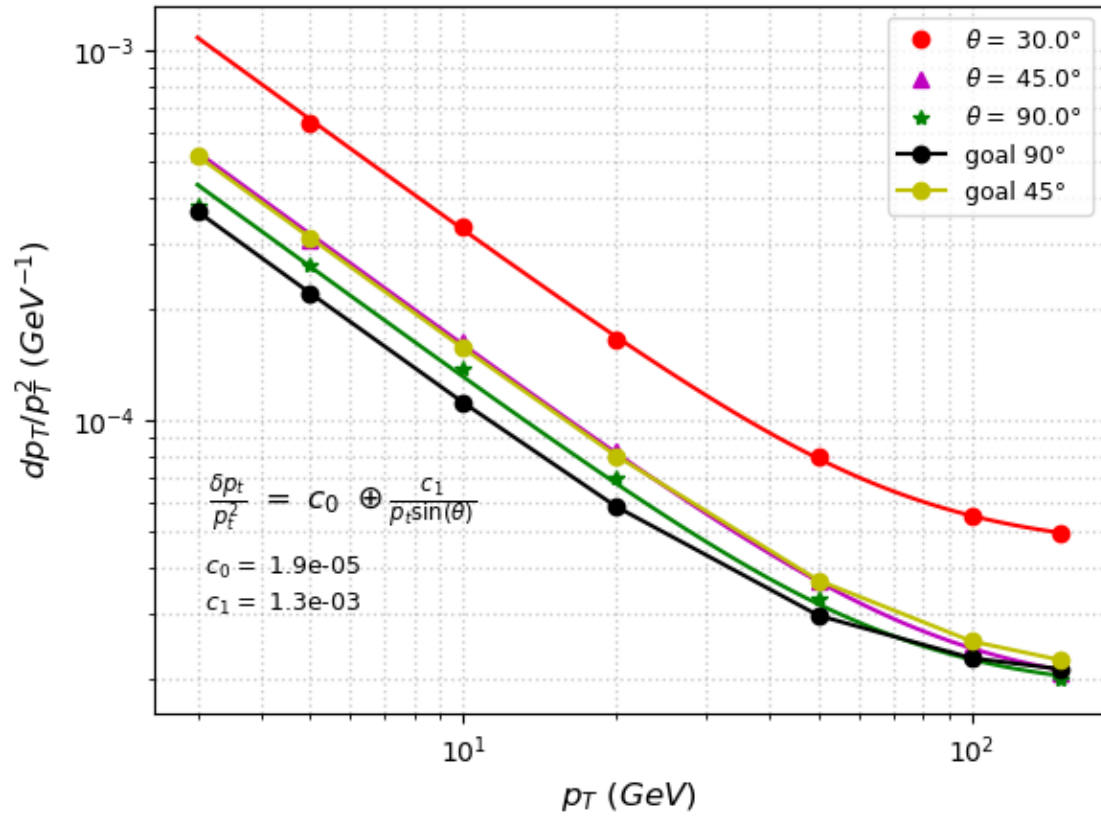
<i>layer</i>	<i>r (cm)</i>	<i><math>\delta</math> (<math>\mu\text{m}</math>)</i>	<i>x0</i>
1	1.81e+02	7.00e+00	1.00e-02

*TPC detector*

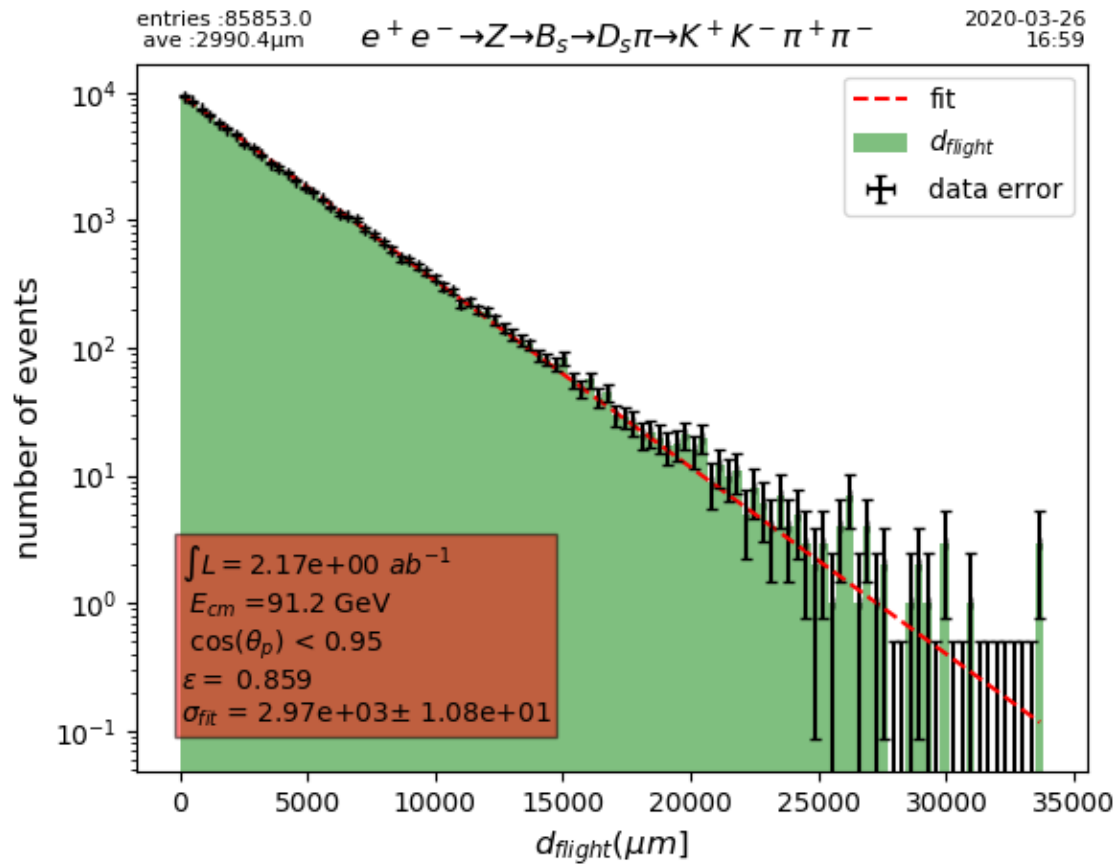
<i>layer</i>	<i>r (cm)</i>	<i><math>\delta</math> (<math>\mu\text{m}</math>)</i>	<i>x0</i>
1	4.00e+01	1.00e+02	5.95e-05
...	4.07e+01	1.00e+02	5.95e-05
200	1.80e+02	1.00e+02	5.95e-05

# Detector resolutions

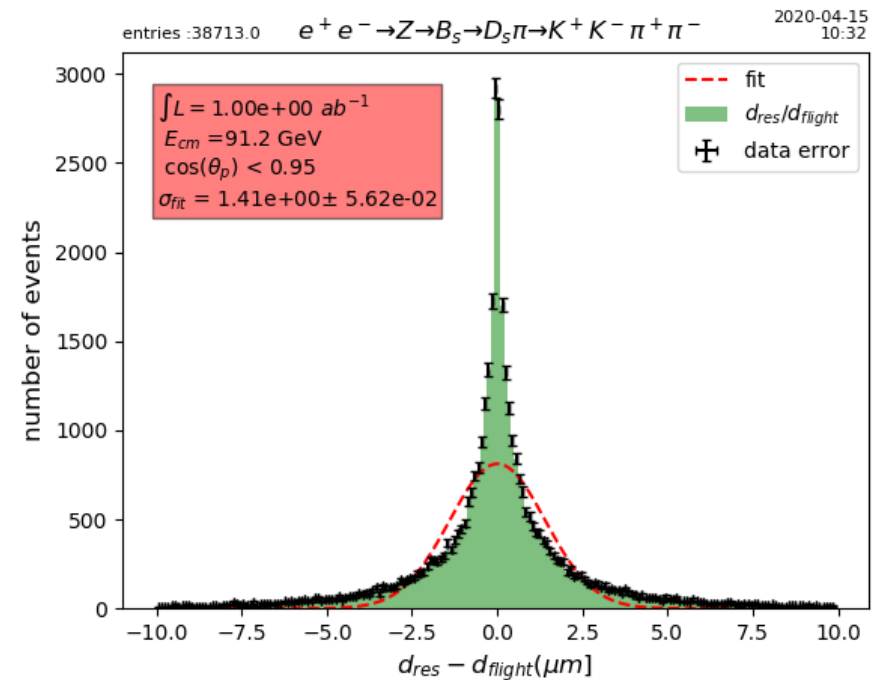
ILD type detector (6 vertex Si layers + 2 Inner Si layers + TPC + 1 outer Si layer)



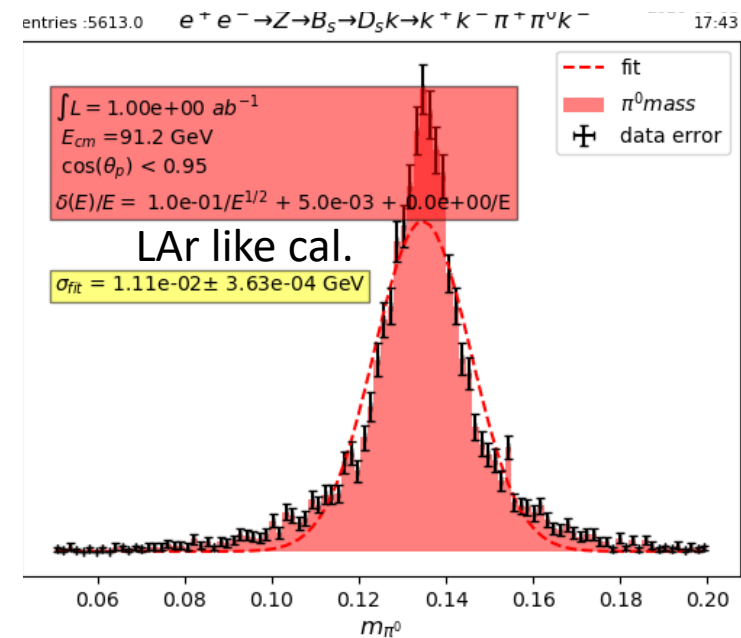
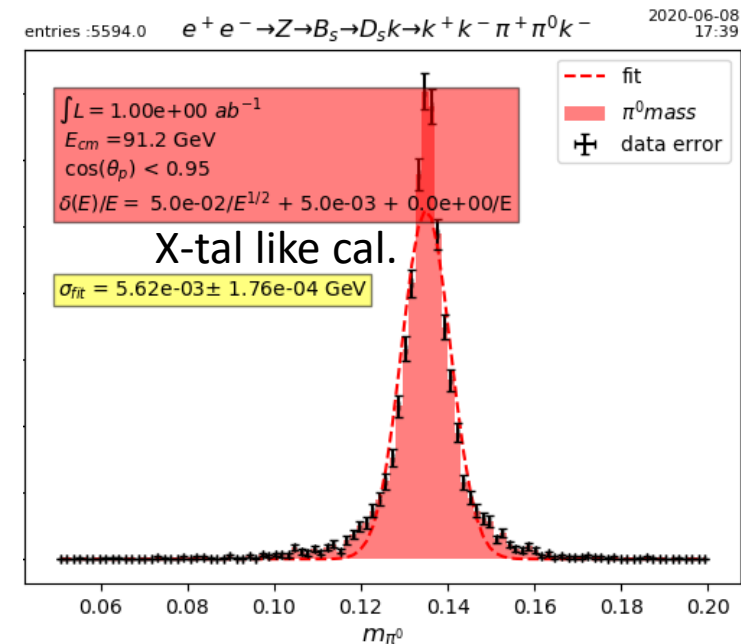
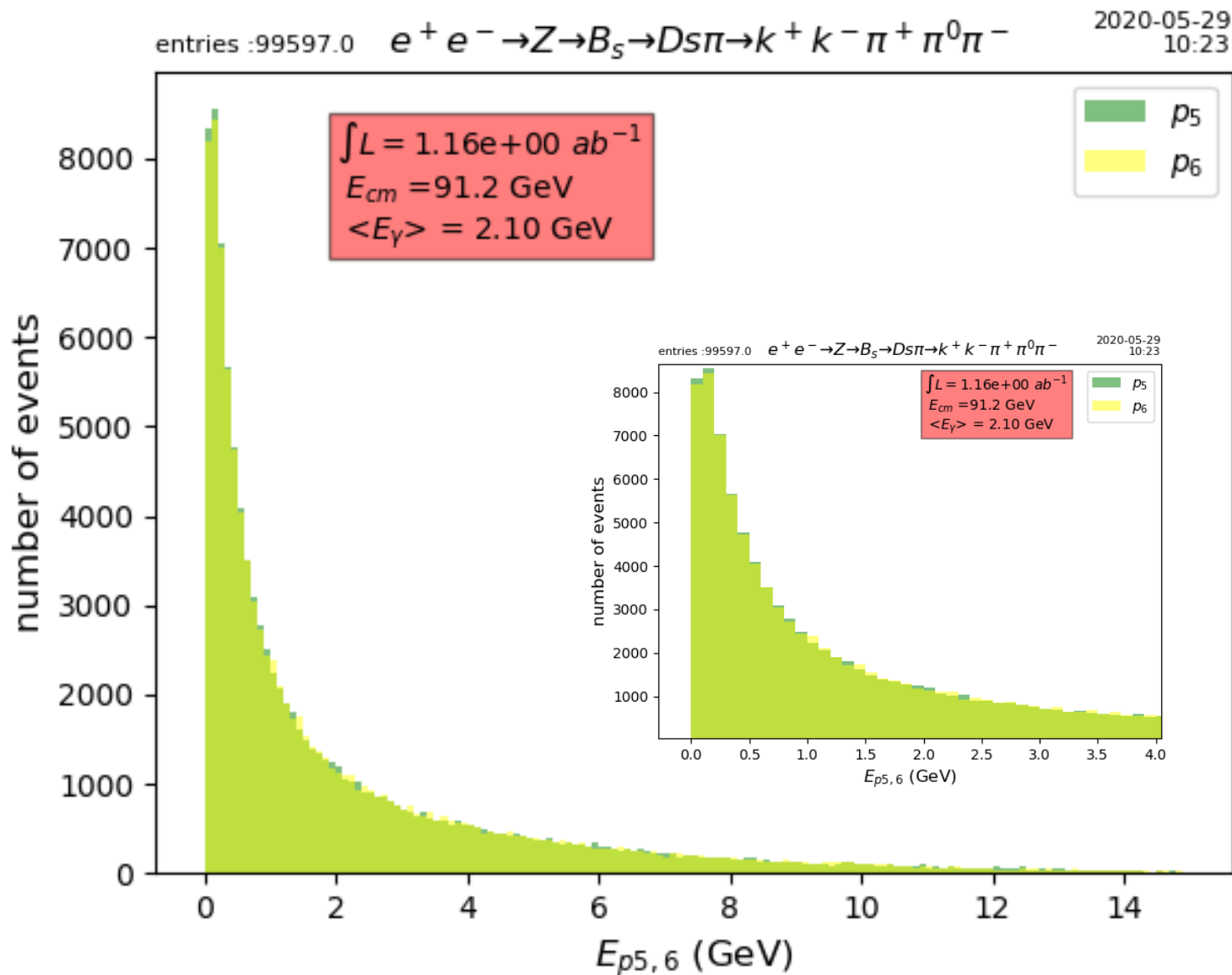
$\langle \text{B flight distance} \rangle \approx 3000 \mu\text{m}$



B Flight distance error due to error on B momentum measurement

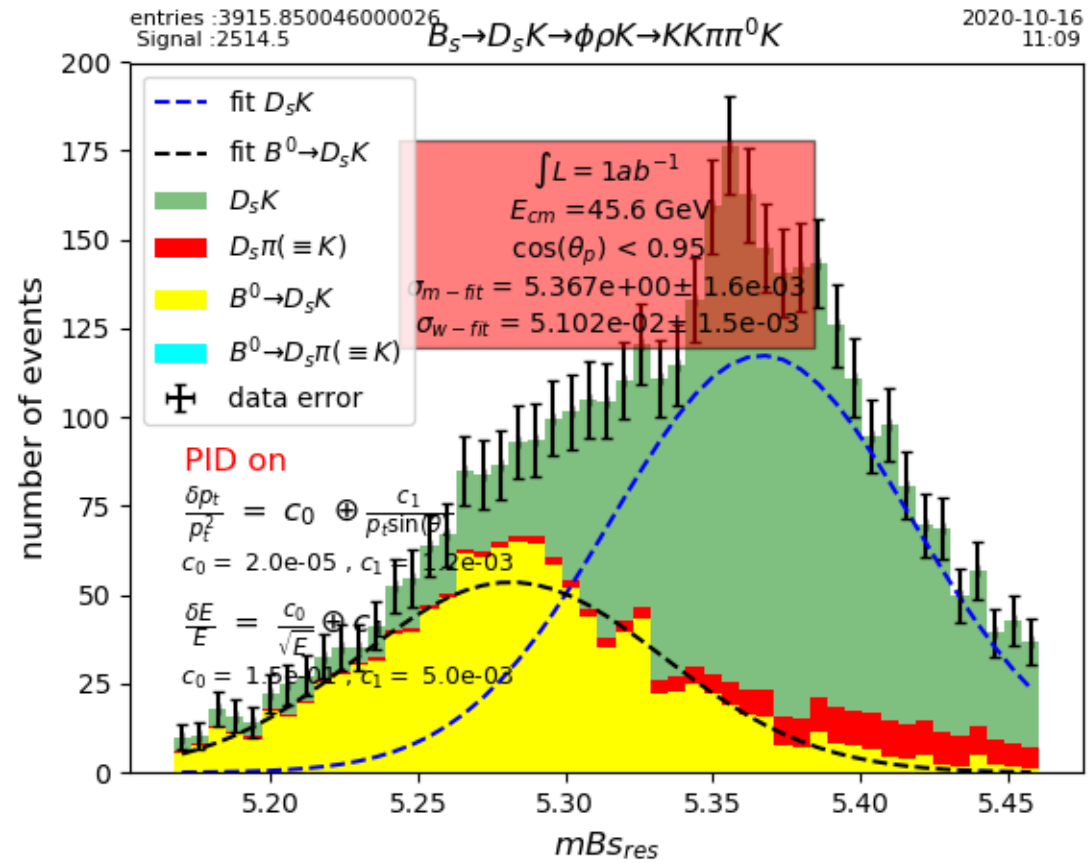
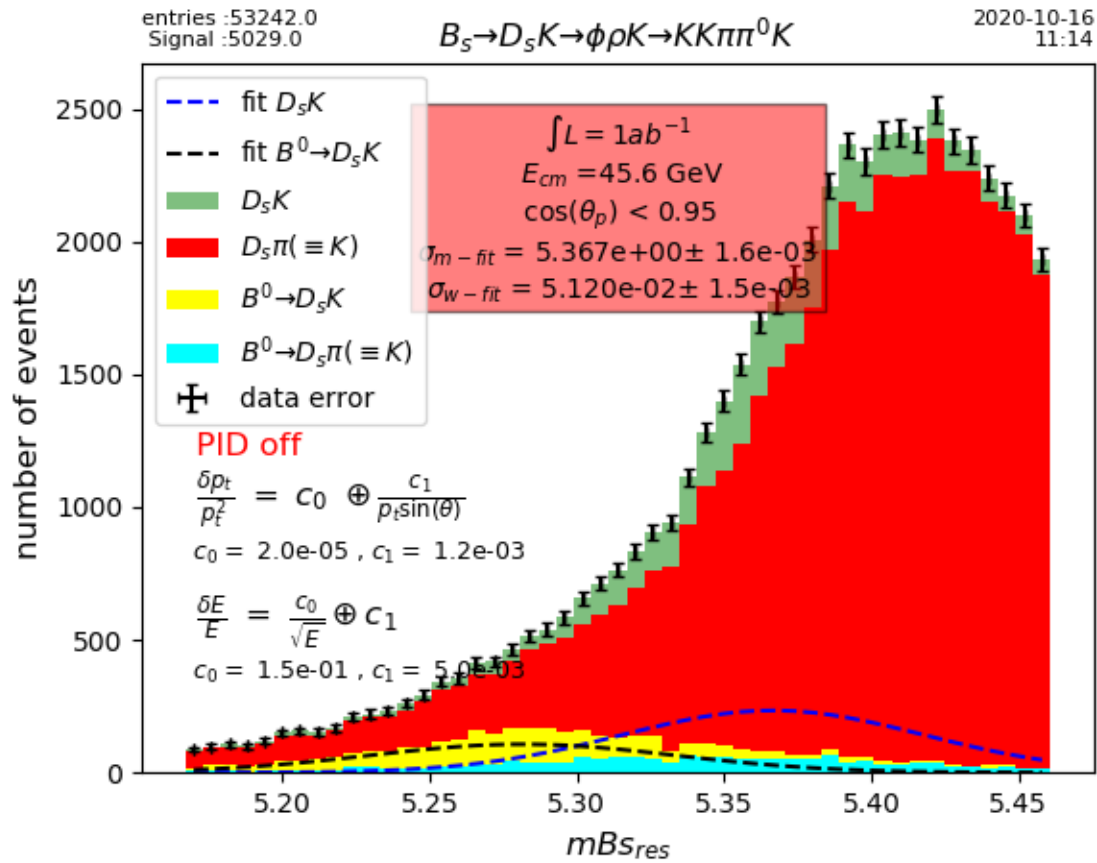


# Energy spectrum of $\gamma$ from $D_s^- \rightarrow \phi \rho^- \rightarrow (K^+ K^-)_\phi (\pi^- \pi^0)_\rho$



# Inclusion of neutrals for $B_s \rightarrow D_s K$ reconstruction

Assuming HGCal like calorimeter with  $\frac{\delta E}{E} = \frac{0.15}{\sqrt{E}} \oplus 0.005$



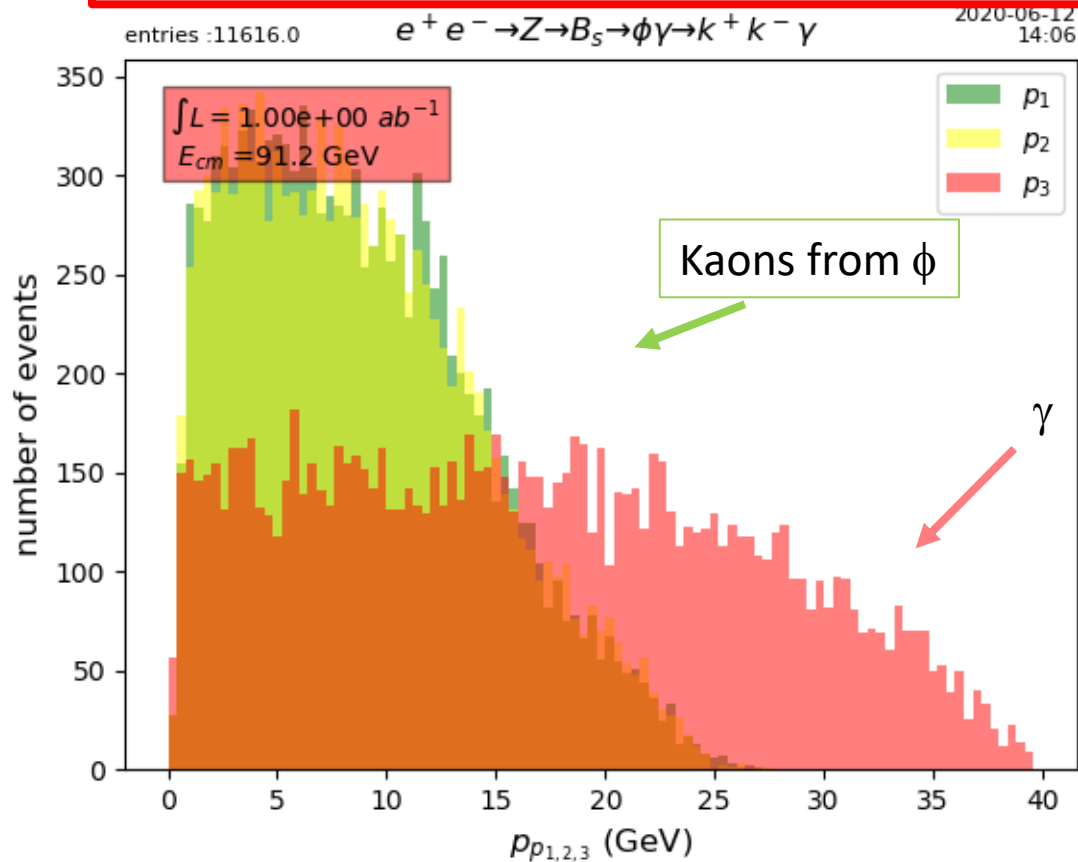
Xtal type to HGCal Type :  $\sigma(D_s^\pm(\phi\rho^\pm)K^\mp) \approx 20\text{MeV} \rightarrow 51\text{MeV}$

# Study of CP violation with $B_s \rightarrow \phi\gamma$

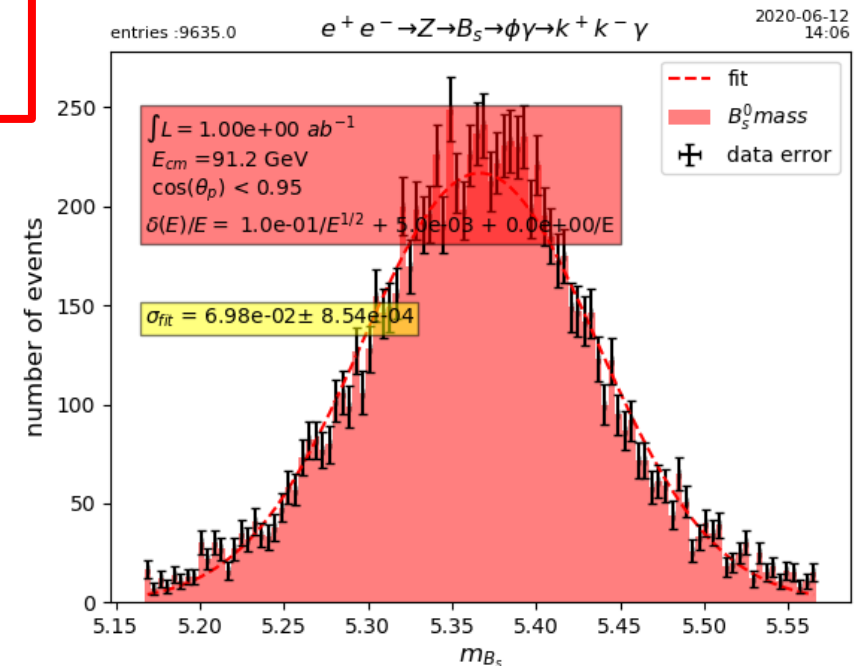
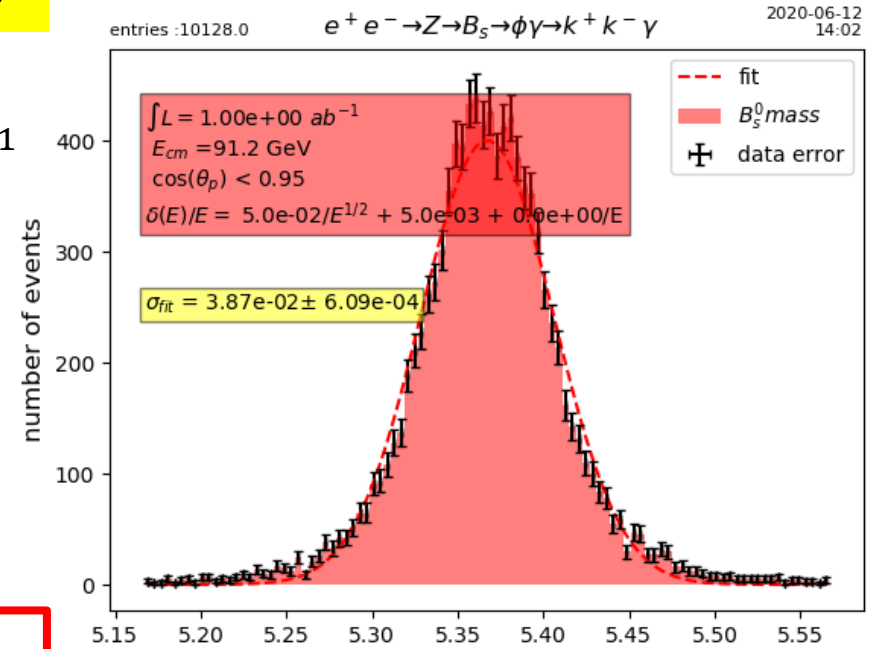
Same as  $B_s \rightarrow \phi\phi$   $\phi_{CKM} \approx 0^\circ$   $Br(B_s \rightarrow \phi\gamma) = 3.4 \times 10^{-5}$   
 $\Rightarrow$  Very good for probing BSM  $\cong 1.7 \times 10^6$  events with  $150 ab^{-1}$

2 main issues requiring dedicated study

- Study of background as mass resolution is poor
  - $\sigma(m_{B_s}) \approx 39 MeV$  with Xtal like calo.
  - $\sigma(m_{B_s}) \approx 70 MeV$  with Lar like calo.
- Study of vertex resolution as  $\phi$  is strongly boosted ( $\sigma > 400\mu m!$ )



PID needed to reject  $B^0 \rightarrow K^{*0}\gamma$  where  $\pi$  from  $K^{*0}$  is used as K

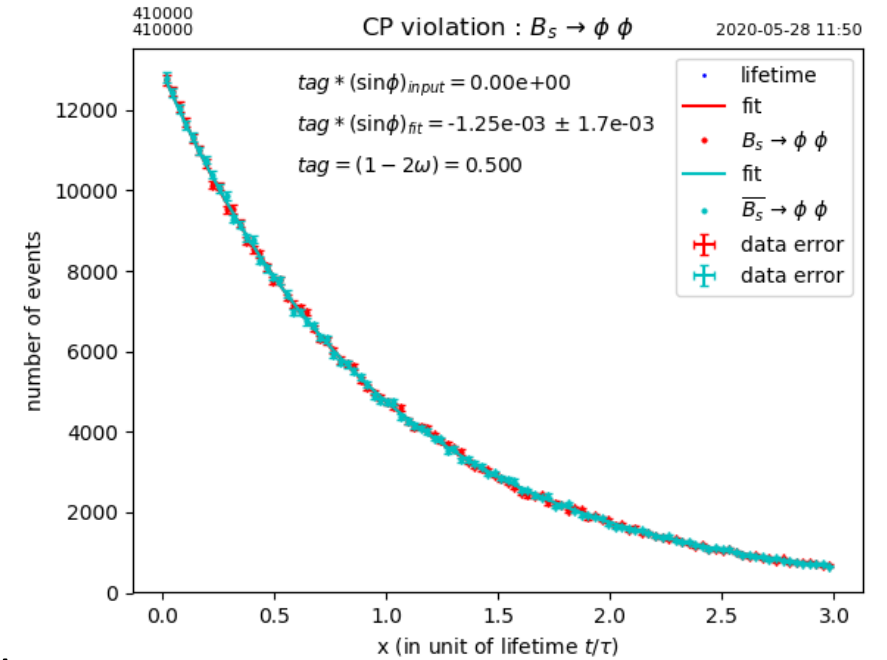
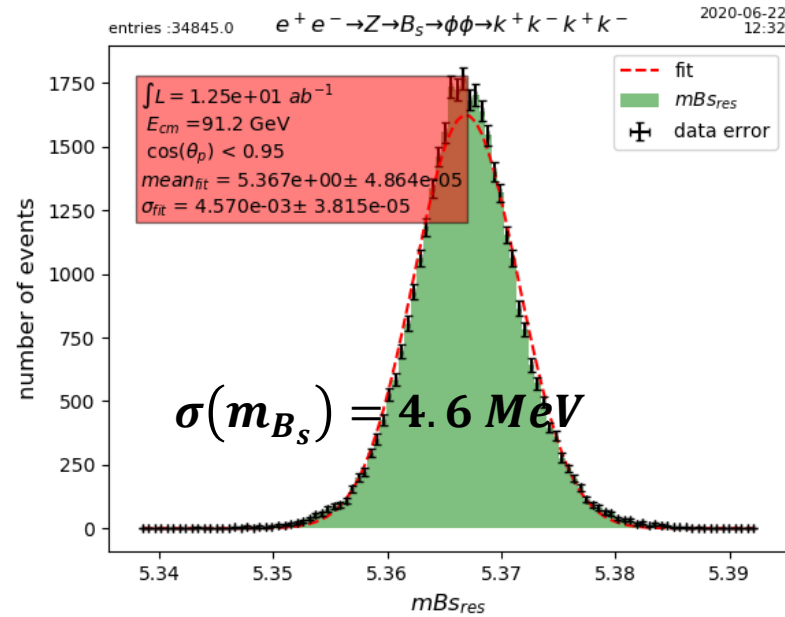
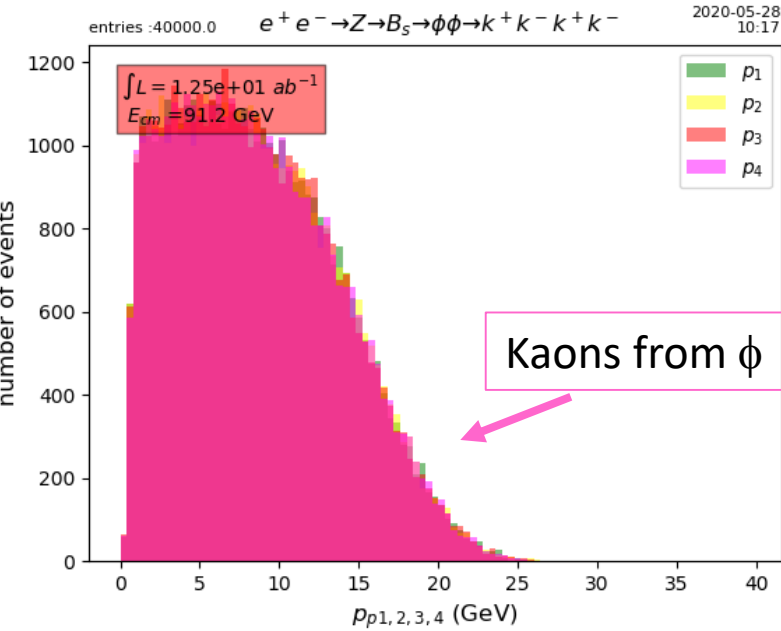


# (Digression) Study of CP violation with $B_s \rightarrow \phi\phi \rightarrow K^+K^-K^+K^-$

With  $B_s \rightarrow \phi\phi$

$\phi_{CKM} \approx 0.5^\circ$  ( $u, c, t$  quarks)  
 $\phi_{CKM} = 0^\circ$  ( $t$  quark only)

$\Rightarrow$  Very good for probing BSM



PDG		
$f_L = \Gamma_L/\Gamma$	$0.378 \pm 0.013$	CP=+
$f_{  } = \Gamma_{  }/\Gamma$	$0.330 \pm 0.016$	CP=+
$f_{\perp} = \Gamma_{\perp}/\Gamma$	$0.292 \pm 0.009$	CP=-

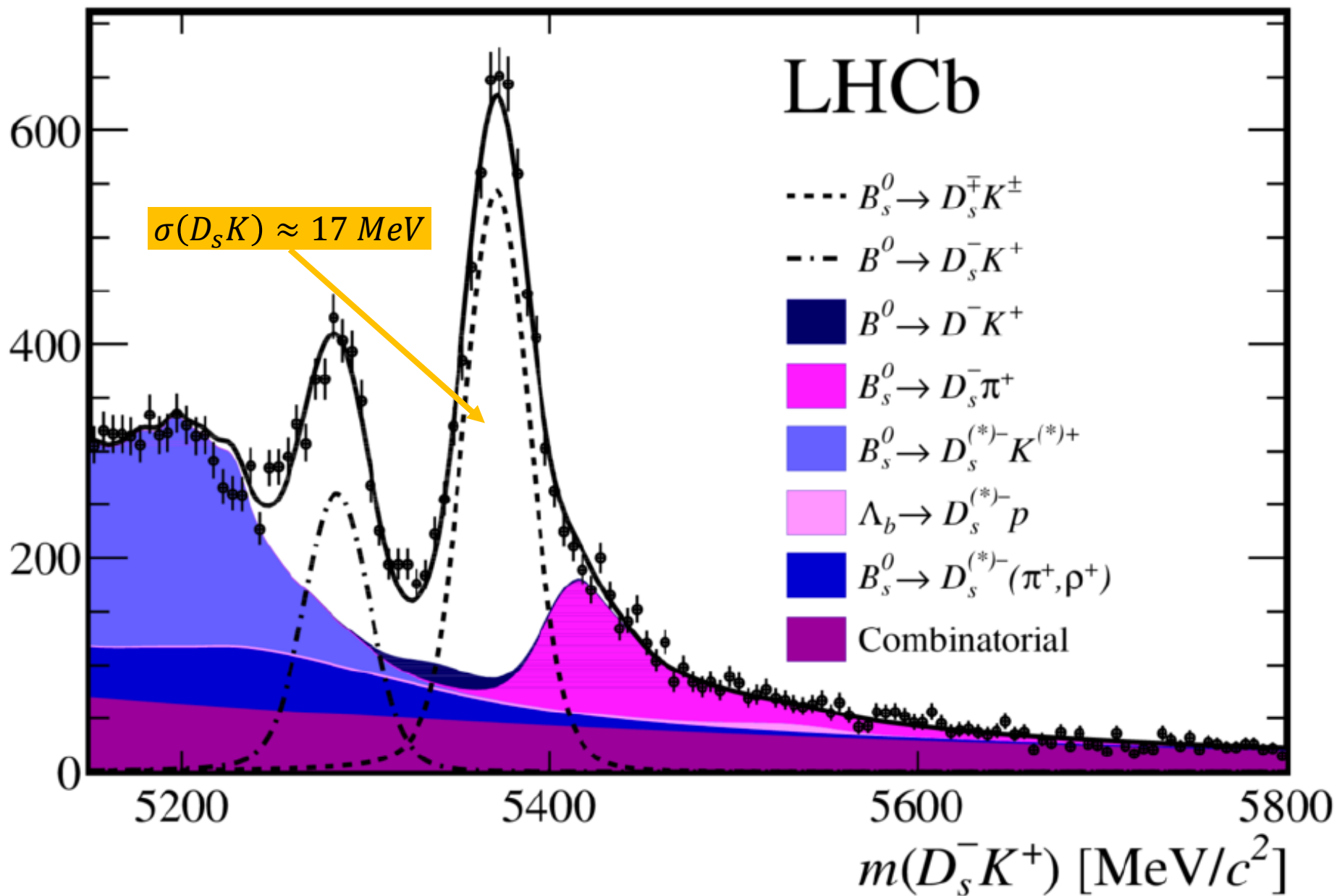
Angular analysis required (tbd)

Otherwise reduced sensitivity by factor  $\frac{1}{1-2f_{\perp}} \approx 2.4$

**Result 5 :**  $\delta(\sin\phi_{CKM}) \approx 3.4 \times 10^{-3} \cong \delta(\phi_{CKM}) \approx 0.2^\circ$  (stat.)



Candidates / (5 MeV/c<sup>2</sup>)



[LHCb, JHEP 05 (2015) 019]