

# Electroweak top-pair production in the presence of $Z'$ and $W'$ bosons at NLO QCD+PS

**I. Schienbein**

**Univ. Grenoble Alpes/LPSC Grenoble**

based on:

R. Bonciani, T. Jezo, M. Klasen, D. Lamprea, F. Lyonnet, IS, arXiv: 1511.08185  
M. Altakach, T. Jezo, M. Klasen, J.-N. Lang, IS, arXiv: 2012.14855

# Introduction and Overview

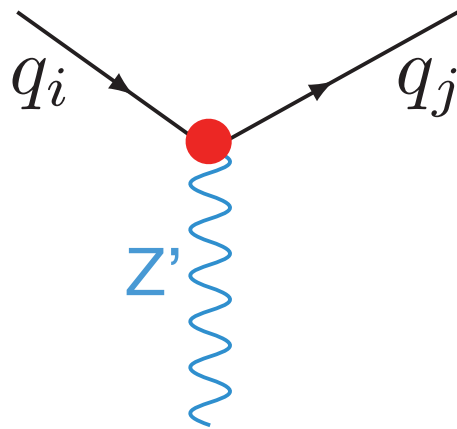
# Motivation

- New heavy spin-1 resonances ( $Z', W'$ ) are predicted in a variety of models, in particular in models with an extended gauge symmetry
- In many cases, the  $Z'$  can decay leptonically and the **strongest constraints come from searches with leptonic final states**
- Nevertheless, **final states with top quarks** are very interesting:
  - The heavy top quark may play a special role w.r.t. to **EW** and BSM physics which couples preferentially to the **third generation** or not to leptons
  - Even for models with couplings to leptons, the addition of **top quark observables** is important to **distinguish** between different BSM scenarios [PRD86(2012)035005]

# PBZ<sub>p</sub> calculation

- In 2015 we performed a calculation of NLO QCD corrections to EW top-pair production at the LHC in the presence of a  $Z'$  boson [arXiv: 1511.08185]

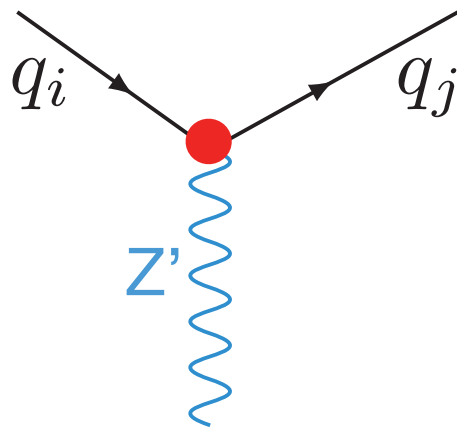
- $Z'$  boson with general, flavour diagonal couplings to SM fermions



- Results implemented in the POWHEG BOX framework
- SM ( $\gamma, Z$ ) and new physics ( $Z'$ ) interference effects taken into account
- QED singularities consistently treated

# New PBZ<sub>p</sub> calculation

- We have performed a complete **re-calculation** [arXiv:2012.14855]
- Amplitudes generated using the **Recola2** package [arXiv:1705.06053]
- New code can deal with general **Z'** and **W'** couplings to SM fermions



- The calculation now includes **t-channel W** and **W'** contributions
- As before, **POWHEG** implementation: **NLO+PS** matched calculation
- As before, all **interference terms** included; **QED singularities** treated

# New PBZ<sub>p</sub> calculation

- New calculation much more involved
- Many more diagrams
- Different amplitude generation
- Different technical details (e.g.,  $\gamma_5$  treatment)
- **Full agreement** with **old PBZ<sub>p</sub>** if reduced to old setup

# Top-pair hadroproduction

# Top-quark pair production

The partonic top-quark pair production cross section at NLO:

$$\sigma_{ab}(\mu_r) = \sigma_{2;0}(\alpha_S^2) + \sigma_{0;2}(\alpha^2) + \sigma_{3;0}(\alpha_S^3) + \sigma_{2;1}(\alpha_S^2\alpha) + \sigma_{1;2}(\alpha_S\alpha^2) + \sigma_{0;3}(\alpha^3)$$

- $\sigma_{2;0}$ : SM QCD background
- $\sigma_{3;0}$ : NLO QCD corrections to the SM background

- NLO known since the late 80ths
- NLO predictions for heavy quark correlations
- Spin correlations between t and tbar
- NNLO calculation completed

Nason, Dawson, Ellis '88/'89  
Beenakker, Kuif, van Neerven, Smith '89  
Bojak, Stratmann '03: polarized case

Mangano, Nason, Ridolfi '92

Bernreuther, Brandenburg, Si, Uwer, '01/'04

Czakon, Mitov '13:  $\sigma_{\text{tot}}$   
Czakon, Mitov '14: distributions



# Top-quark pair production

The partonic top-quark pair production cross section at NLO:

$$\sigma_{ab}(\mu_r) = \sigma_{2;0}(\alpha_S^2) + \sigma_{0;2}(\alpha^2) + \sigma_{3;0}(\alpha_S^3) + \sigma_{2;1}(\alpha_S^2\alpha) + \sigma_{1;2}(\alpha_S\alpha^2) + \sigma_{0;3}(\alpha^3)$$

- $\sigma_{2;0}$ : SM QCD background
- $\sigma_{3;0}$ : NLO QCD corrections to the SM background

- $\sigma_{2;1}$ : EW corrections to the QCD background

- Gauge invariant subset, no QCDxEW interferences from box diagrams
- Beenakker,Denner,Hollik,Mertig,Sack,Wackerroth '94  
Kao,Wackerroth '00: 2HDM

- Rest of EW corrections including Z-gluon interferences and corrections from real and virtual photons

Kühn,Scharf,Uwer, '06  
Moretti,Nolten,Ross '06  
Bernreuther,Fuecker,Si '06  
Hollik,Kollar '08

# Top-quark pair production

The partonic top-quark pair production cross section at NLO:

$$\sigma_{ab}(\mu_r) = \sigma_{2;0}(\alpha_S^2) + \sigma_{0;2}(\alpha^2) + \sigma_{3;0}(\alpha_S^3) + \sigma_{2;1}(\alpha_S^2\alpha) + \sigma_{1;2}(\alpha_S\alpha^2) + \sigma_{0;3}(\alpha^3)$$

## Existing calculations including a Z' boson:

- Factorized approach (no SMxZ', no qg-channel with Z'), purely vector or axial vector or left or right couplings Gao, C.S. Li, B.H. Li, Yuan, Zhu '10
- no SMxZ', includes: qg-channel, top-decay in NWA with spin correlations, Z' contribution to  $\sigma_{2;1}$  (broad resonances) Caola, Melnikov, Schulze '13

- **Our calculation:** includes: SMxZ' interferences, general couplings, QED contribution, POWHEG implementation, top-decay, no Z' contribution to  $\sigma_{2;1}$

- $\sigma_{0;2}$ : EW top-quark pair production arXiv:1511.08185, arXiv:2012.14855

- $\sigma_{1;2}$ : NLO QCD corrections to EW top-quark pair production

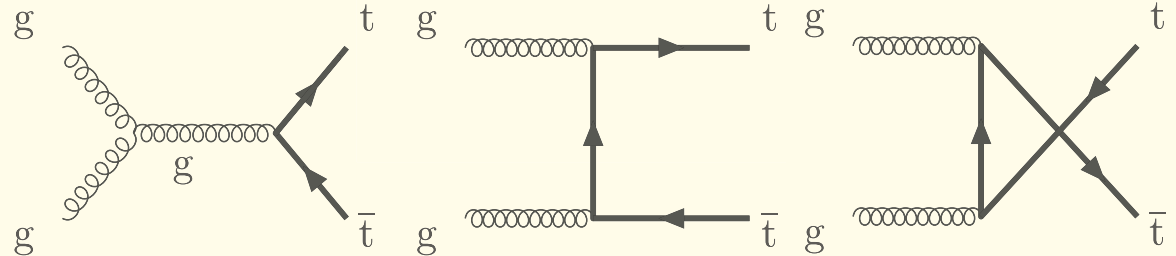
- $\sigma_{0;3}$ : neglected

# LO subprocesses: $\sigma_{2;0}$ and $\sigma_{0;2}$

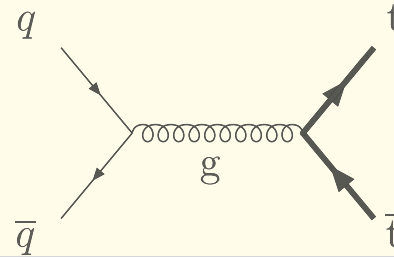
- $\hat{\sigma}^{\text{LO}} = \hat{\sigma}_S^{\text{LO}}(\alpha_S^2) + \hat{\sigma}_W^{\text{LO}}(\alpha_W^2)$

- SM

- ▶  $gg, \mathcal{O}(\alpha_S^2)$ :

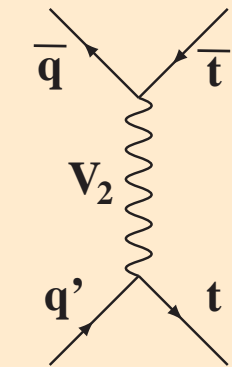
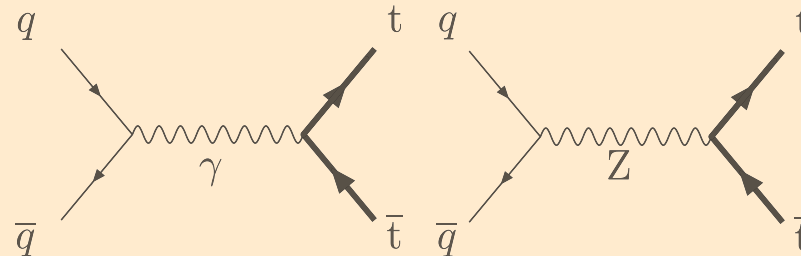


- ▶  $q\bar{q}, \mathcal{O}(\alpha_S^2)$ :



$\sigma_{2;0}$

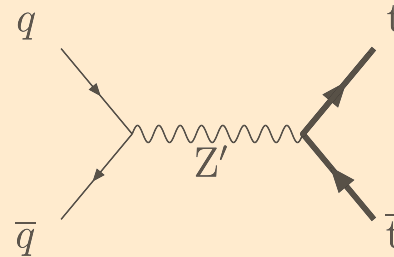
- ▶  $q\bar{q}, \mathcal{O}(\alpha_W^2)$ :



$\sigma_{0;2}$

- beyond SM

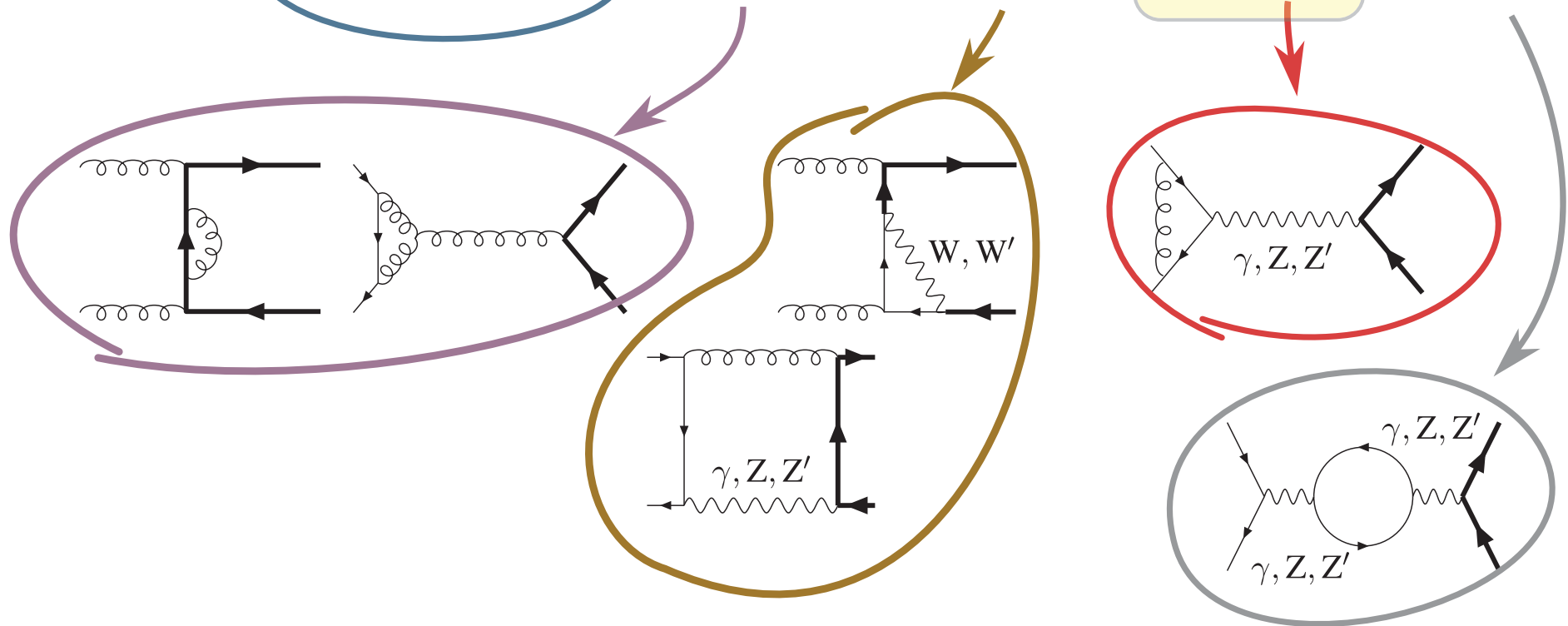
- ▶  $q\bar{q}, \mathcal{O}(\alpha_W^2)$ :



# NLO virtual

LO

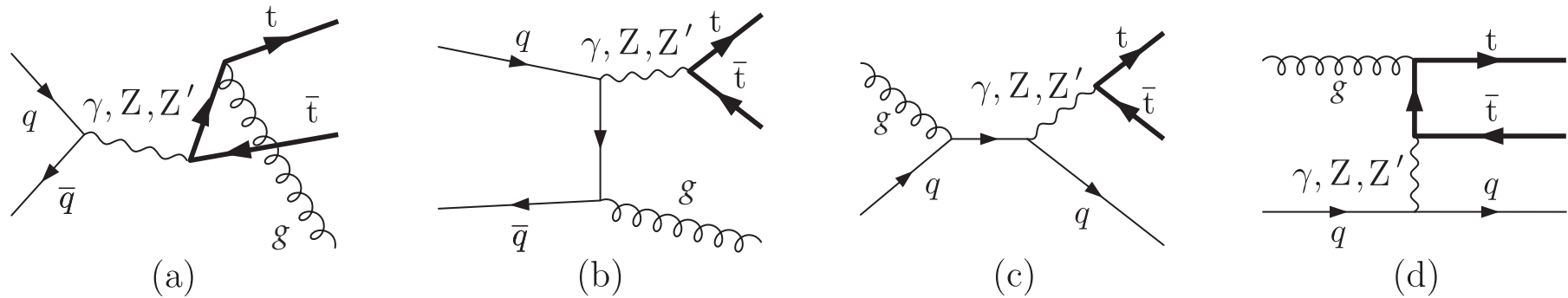
$$\bullet \hat{\sigma}^{\text{NLO}} = \hat{\sigma}(\alpha_S^2) + \hat{\sigma}(\alpha_W^2) + \hat{\sigma}(\alpha_S^3) + \hat{\sigma}(\alpha_S^2\alpha_W) + \hat{\sigma}(\alpha_S\alpha_W^2) + \hat{\sigma}(\alpha_W^3)$$



•  $\mathcal{O}(\alpha_S^3)$  not affected by the presence of  $Z'$

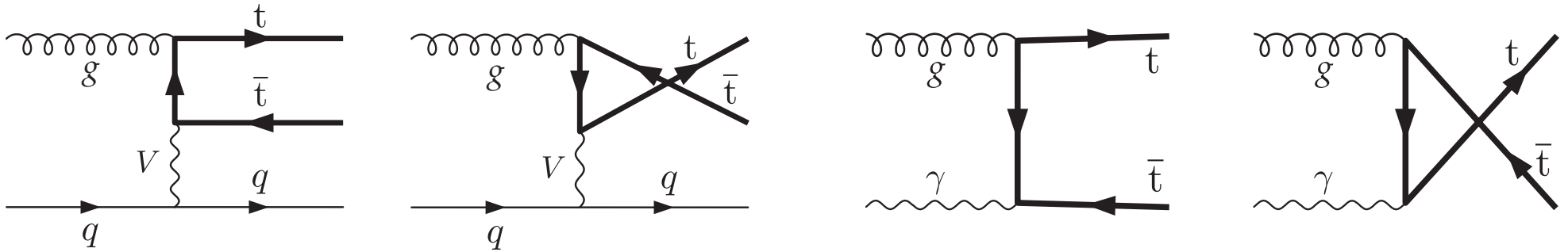
• we calculate  $\mathcal{O}(\alpha_S\alpha_W^2)$

# NLO real corrections



- interferences of real and real diagrams
- new channel as compared to tree-level and 1-loop diagrams
- no loops, no UV divergences
- IR divergences, after integration over 1 particle phase space
  - ▶ soft (S) divergences: radiation of a soft gluon (a), (b)
  - ▶ initial state collinear (ISC) divergences: (b), (d)
  - ▶ no final state collinear (FSC) divergences

# QED contribution



- The  $gq$ -channel has an initial state C-div. associated to a photon propagator
- For the mass factorization procedure need to introduce a **photon PDF** and have to include **photon-initiated subprocesses**
- Counting the photon PDF as  $\mathcal{O}(\alpha)$  the LO  $g\gamma$ -channel contributes to  $\sigma_{1;2}(\alpha_s \alpha^2)$
- This channel turns out to be **numerically important**

# Models

# Sequential SM (SSM)

- A toy model where  $Z'$  ( $W'$ ) have the same couplings to fermions as the SM  $Z$  ( $W$ )
- The width of  $Z'$  ( $W'$ ) increases proportionally to its mass
- It is a widely used benchmark model in which **LHC** data are analysed
- Most stringent limits:
  - **Leptonic final states:**
    - $M_{Z'} \geq 5.15$  TeV assuming  $\Gamma/M_{Z'} = 3\%$  [CMS-PAS-EXO-19-019]
  - **Hadronic final states:**
    - $M_{Z'} \geq 2.7$  TeV assuming  $\Gamma/M_{Z'} = 3\%$  [arXiv:1910.08447]
- Input parameter:  $M_{Z'}$  ( $M_{W'}$ )



# Leptophobic Topcolor model (TC) [arXiv:1112.4928]

- **New strong dynamics** with  $SU(3)_2$  symmetry coupling preferentially to the third generation while the original  $SU(3)_1$  gauge group couples only to the **1st** and **2nd** generation; breaking  $SU(3)_1 \times SU(3)_2 \rightarrow SU(3)_C$
- Formation of top quark condensate generates large top mass
- To block the formation of a bottom quark condensate an **additional**  $U(1)_2$  symmetry with associated  $Z'$  is introduced;  $U(1)_1 \times U(1)_2 \rightarrow U(1)_Y$
- $Z'$  couples only to **1st** and **3rd** generation; no significant coupling to leptons
- The **TC** model is frequently studied in **ATLAS** & **CMS** searches
- Most stringent limits:
  - $M_{Z'} \geq 6.65$  TeV (5.25 TeV, 3.8 TeV) for  $\Gamma/M_{Z'} = 30\%$  (10%, 1%) [arXiv:1810.05905v2]

# Leptophobic Topcolor model

- **Three parameters** (in addition to  $M_{Z'}$ ):
  - Ratio of the two  $U(1)$  coupling constants:  $\cot \Theta_H$
  - $f_1$ : relative strength of the  $Z'$ -coupling to right-handed up-type quarks w.r.t. to the left-handed up-type quarks
  - $f_2$ : same for down-type quarks
- $\cot \Theta_H$  should be large to enhance the condensation of top quarks but no bottom quarks
- The **LO cross sections** are usually computed using
  - a fixed small  $Z'$  width (which fixes  $\cot \Theta_H$ ):  $\Gamma_{Z'} = 1.2\% M_{Z'}$
  - $f_1=1, f_2=0$  (maximizes the fraction of  $Z'$  bosons decaying into top pairs)

# Third Family Hypercharge Model [arXiv:1809.01158]

- A minimal extension of the **SM** by an anomaly-free, spontaneously-broken  $U(1)_F$  gauge symmetry
- Explains the neutral current B anomaly measurements and the heaviness of the third family fermions
- $Z'$  with **flavour non-diagonal** couplings; now possible in PBZp
- Most stringent limits:
  - $M_{Z'} \geq 1.2 \text{ TeV}^*$  [arXiv:1904.10954]
- Input parameters:
  - $M_{Z'}$
  - The  $U(1)_F$  gauge coupling:  $g_F$
  - The mixing angle between **second** and **third generation**:  $\theta_{sb}$

# Numerical Results

- Events in **LHE** format using new-**PBZp** with stable on-shell **top quark**
- **Generation** cut on the **top pair** invariant mass:
  - $M_{t\bar{t}} \geq 0.75M_Z$
  - Applied at the **Born** phase space level
  - More statistics in the interesting regions
- **PYTHIA 8.2** to decay the **top quark** leptonically and to shower the events
- **Rivet** to impose the following **acceptance** cuts:
  - $\geq 2$  charged leptons,  $\geq 2$  neutrinos,  $\geq 2$  b-jets
  - $R = 0.5$  (**anti- $k_T$** ),  $p_T > 25$  GeV,  $|\eta| < 2.5$

# Setup and Input

- $\sqrt{s} = \{14 \text{ TeV}, 27 \text{ TeV}, 50 \text{ TeV}, 100 \text{ TeV}\}$
- $M_{Z'} = \{2000 \text{ GeV}, \dots, 8000 \text{ GeV}\}$
- $M_{\text{top}} = 172.5 \text{ GeV}$
- **PDF** choice: NNPDF31\_nlo\_as\_0118\_luxqed
- $\mu_R^2 = \mu_F^2 = \hat{s}$

# Effect of cuts

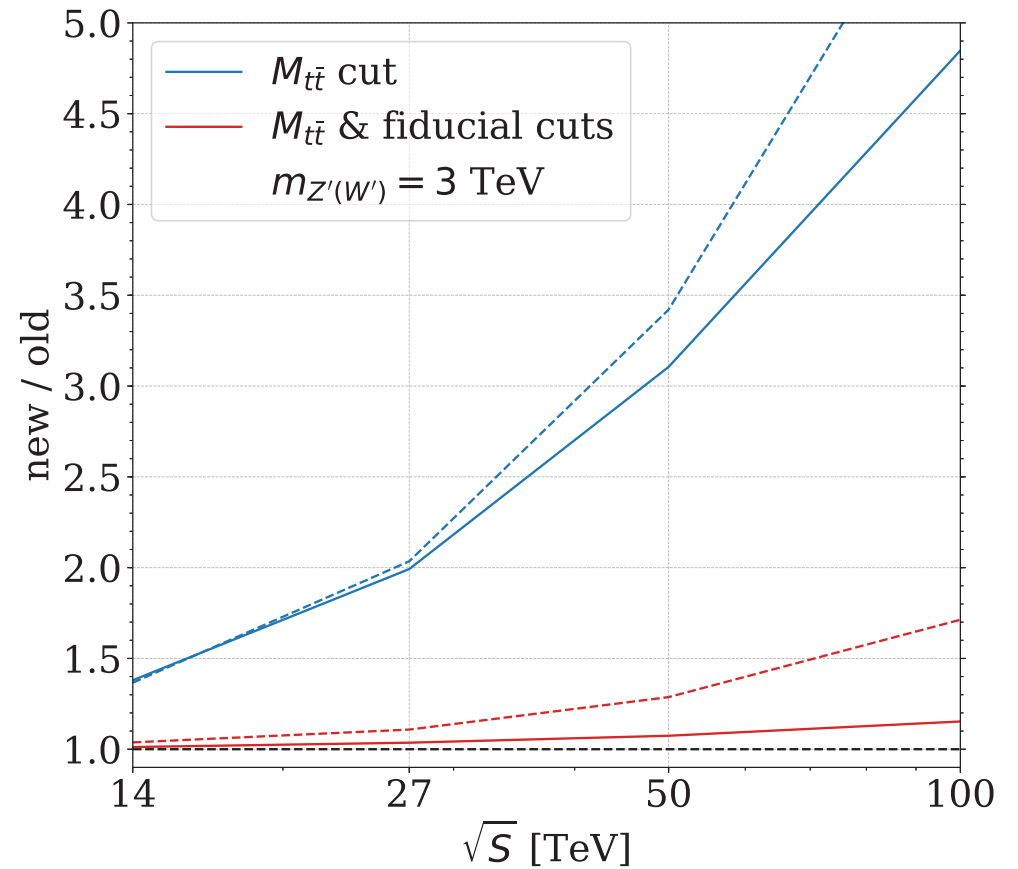
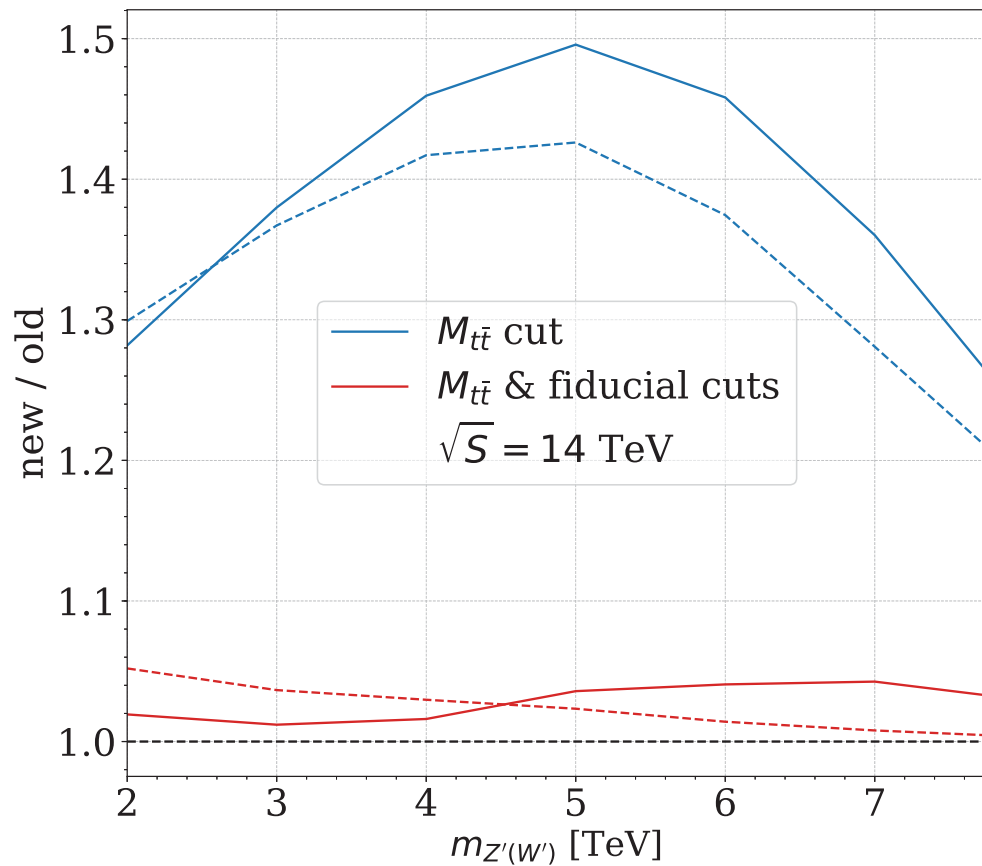
**Table 1:** Total cross sections in LO for top-pair production at  $\mathcal{O}(\alpha_s\alpha)$  and  $\mathcal{O}(\alpha^2)$  in the SM and SSM at  $\sqrt{S} = 14$  TeV. The  $Z'$ -boson mass is set to 5 TeV. For all the predictions in this table we use NLO  $\alpha_S$  and NLO PDFs.

Contribution	no cuts [fb]	$m_{t\bar{t}}$ cut [fb]	Further reduction in %
			$m_{t\bar{t}}$ & fiducial cuts [%]
$\gamma g + g\gamma \rightarrow t\bar{t}, \mathcal{O}(\alpha\alpha_s)$	3700	0.0327	41.6
$q\bar{q}' \rightarrow W \rightarrow t\bar{t}, \mathcal{O}(\alpha^2) + \text{interf.}$	3220	0.0573	3.7
$q\bar{q} \rightarrow g/W \rightarrow t\bar{t}, \mathcal{O}(\alpha\alpha_s)$	-1680	0.000703	37.4
$q\bar{q} \rightarrow \gamma/Z \rightarrow t\bar{t}, \mathcal{O}(\alpha^2)$	510	0.00614	74.9
$q\bar{q} \rightarrow Z' \rightarrow t\bar{t}, \mathcal{O}(\alpha^2)$	0.210	0.114	77.4
$q\bar{q}' \rightarrow W' \rightarrow t\bar{t}, \mathcal{O}(\alpha^2) + \text{interf.}$	0.0025	–	–

SM

Signal

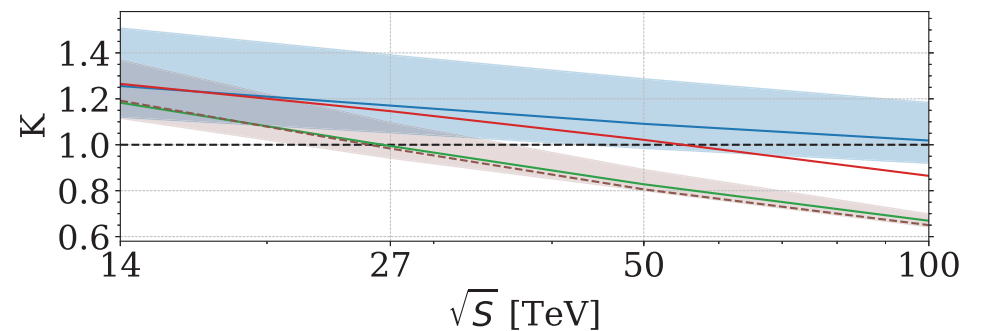
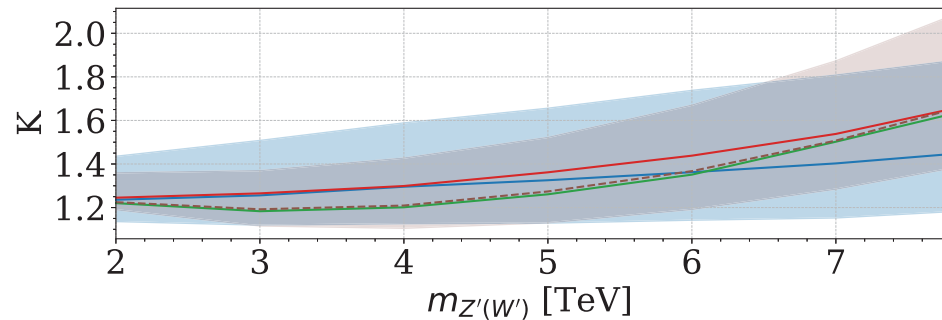
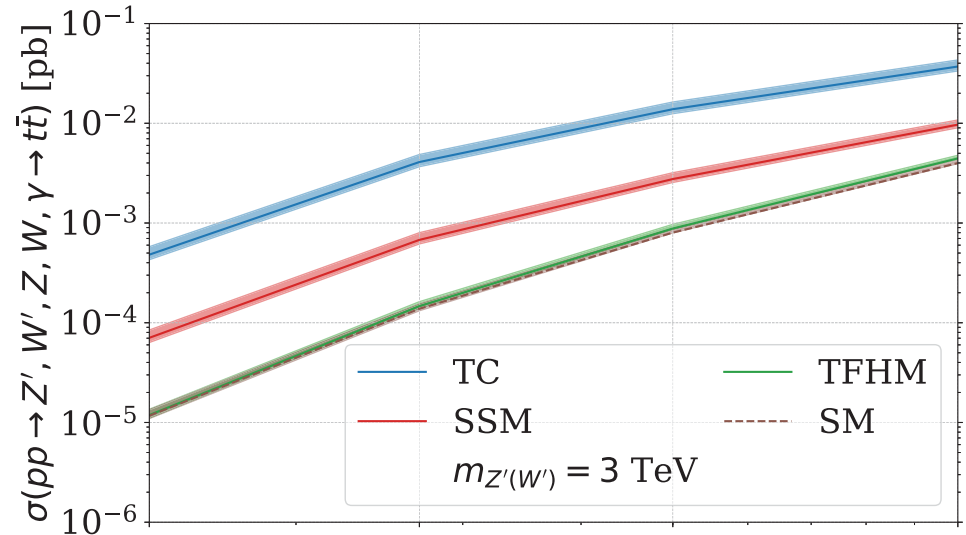
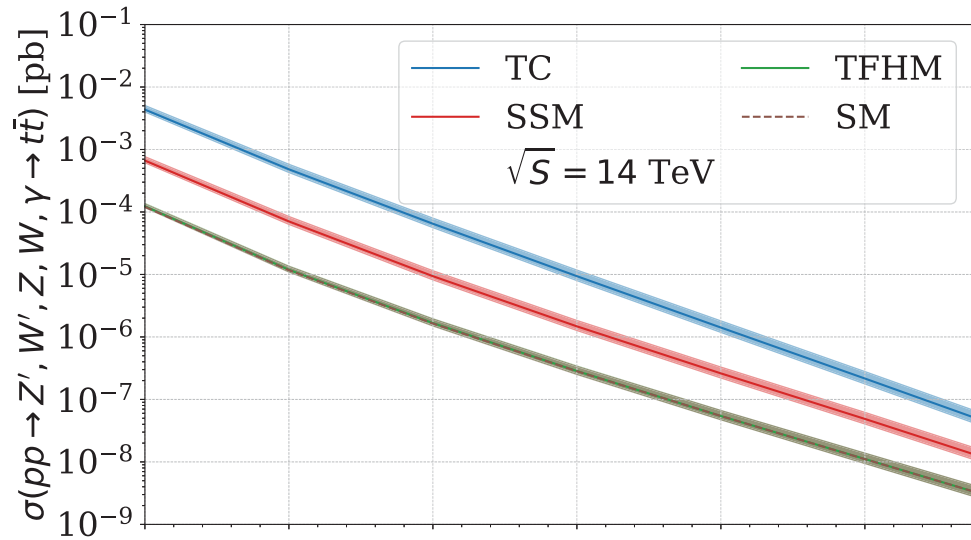
# New PBZ<sub>p</sub> vs Old PBZ<sub>p</sub>



- **Dashed: LO+PS ; Solid: NLO+PS**
- **Fiducial cuts important to effectively suppress new contributions**
- **At 100 TeV, the ratio still exceeds 1.5 at LO+PS**



# Fiducial cross sections for EW Top pair production at NLO+PS



- At LHC14: K-factor **increases** with  $Z'$ -mass; whereas cross section drops
- As function of energy: K-factor drops; cross section increases
- Predictions for TFHM can barely be distinguished from SM; At 100 TeV,  $K=1.13$

# Conclusions

- **New PBZp code available: NLO+PS**
- **New t-channel** contributions in PBZp small **after** fiducial cuts
- **K-factors and cross sections can be calculated with PBZp depending on the model, chosen parameters and cuts.**
- **TFHM not accessible in top-pair production at LHC14**  
**Accessible at FCC100? Requires more detailed study**
- **More dedicated studies for FCC-hh possible** for models with extra gauge bosons: integrated cross sections, invariant mass distributions, transverse momentum and rapidity distributions
- **New PBZp has been implemented in CONTUR**  
**in collaboration with Jon Butterworth (ATLAS)**

**Backup slides**

# Total cross sections for $M_{Z'} = 3 \text{ TeV}$

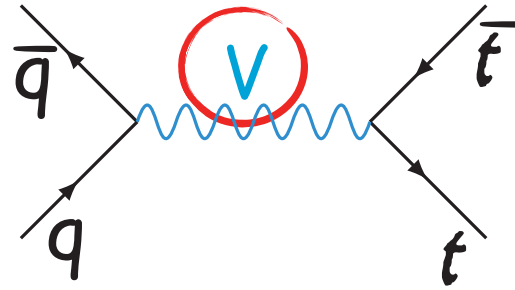
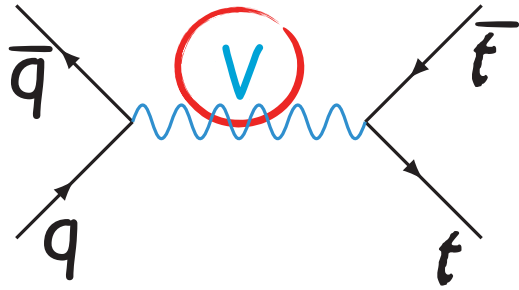
For LO uses the NNPDF23\_lo\_as0119\_qed PDF set

Order	Processes	Model	$\sigma$ [pb]	$\sigma$ [pb] ( $m_{t\bar{t}} > \frac{3}{4}m_{Z'}$ )
cut reduces bgd by more than three orders of mag.	$gg \rightarrow t\bar{t}$		473.93(7)	0.15202(2)
	$gg + qg \rightarrow t\bar{t} + q$		1261.0(2)	0.45255(7)
	LO $\gamma g + g\gamma \rightarrow t\bar{t}$		4.8701(8)	0.0049727(6)
	LO $\gamma g + g\gamma \rightarrow t\bar{t}$ (NLO $\alpha_s$ and PDFs)		5.1891(8)	0.004661(6)
cut reduces signal by only about 10%; still signal only 3% to 8% of QCD background → additional cuts needed	LO $q\bar{q} \rightarrow \gamma/Z \rightarrow t\bar{t}$	SM	0.36620(7)	0.00017135(3)
	$\rightarrow \gamma/Z \rightarrow t\bar{t}$	SM	0.5794(1)	0.00017174(5)
	$+ qg \rightarrow \gamma/Z + q \rightarrow t\bar{t} + q$	SM	4.176(2)	0.001250(6)
	$\rightarrow Z' \rightarrow t\bar{t}$	SSM	0.0050385(8)	0.0044848(7)
	$\rightarrow \gamma/Z/Z' \rightarrow t\bar{t}$	SSM	0.35892(7)	0.0043464(7)
	$\rightarrow \gamma/Z/Z' \rightarrow t\bar{t}$	SSM	0.5676(1)	0.005155(3)
NLO $q\bar{q} + qg \rightarrow \gamma/Z/Z' + q \rightarrow t\bar{t} + q$	SSM	4.172(2)	0.007456(9)	
LO $q\bar{q} \rightarrow Z' \rightarrow t\bar{t}$	TC	0.012175(2)	0.011647(2)	
LO $q\bar{q} \rightarrow \gamma/Z/Z' \rightarrow t\bar{t}$	TC	0.38647(7)	0.011984(2)	
NLO $q\bar{q} \rightarrow \gamma/Z/Z' \rightarrow t\bar{t}$	TC	0.6081(2)	0.01468(1)	
NLO $q\bar{q} + qg \rightarrow \gamma/Z/Z' + q \rightarrow t\bar{t} + q$	TC	4.202(2)	0.01002(1)	

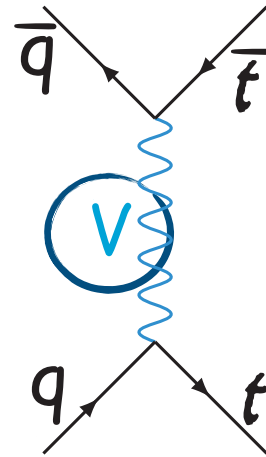
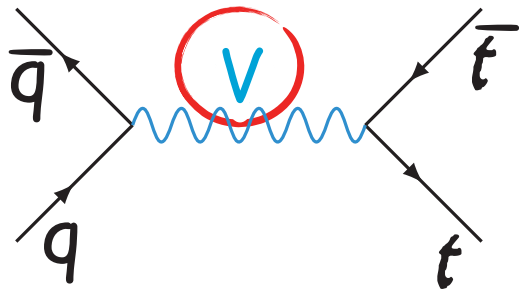
# Subprocesses (5 FNS)

Born (0QCD4EW0BSM)

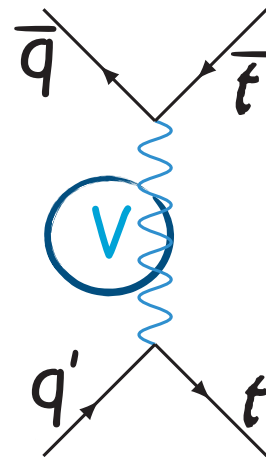
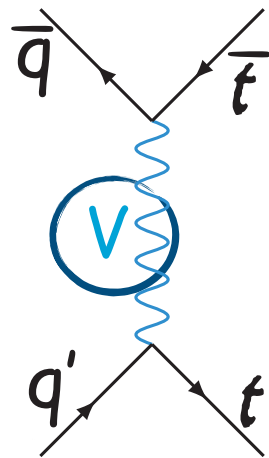
$\gamma, Z$



$\gamma, Z$



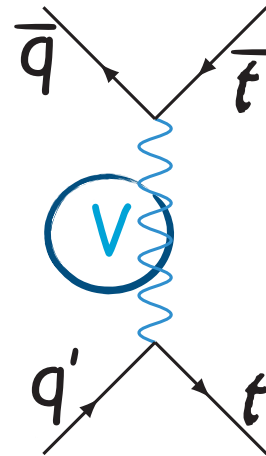
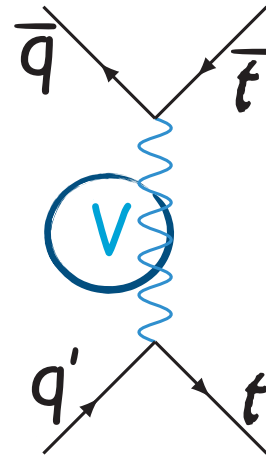
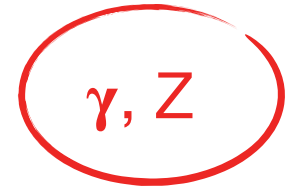
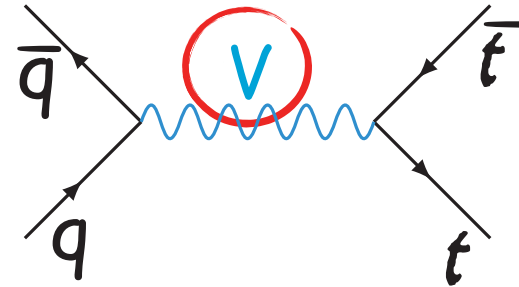
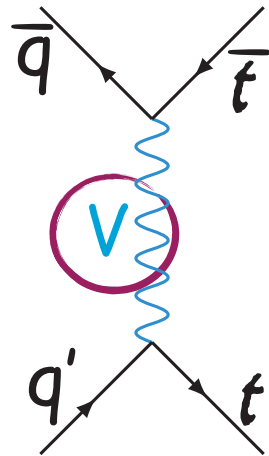
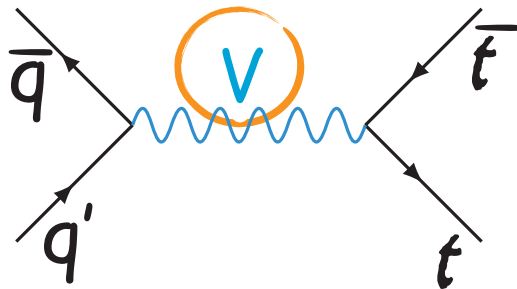
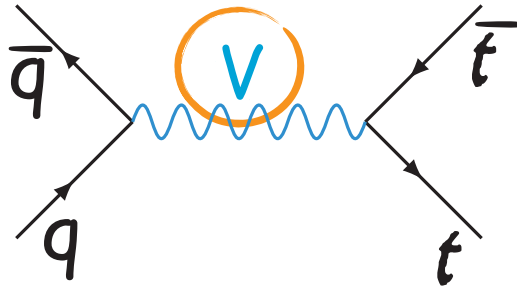
$W$



$W$

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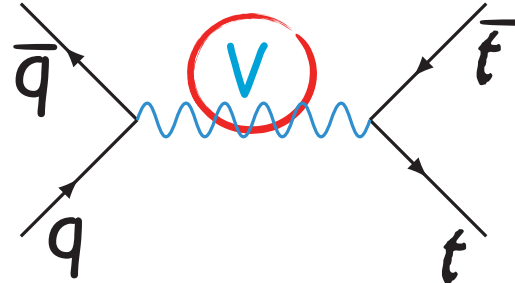
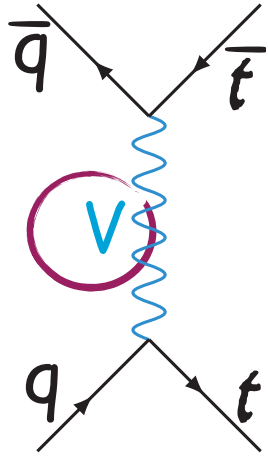
Born (0QCD4EW2BSM)



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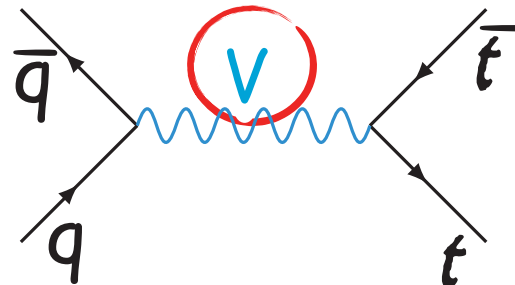
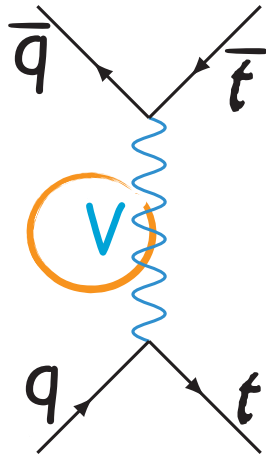
Born (0QCD4EW2BSM)

$W'$



$\gamma, Z$

$Z'$

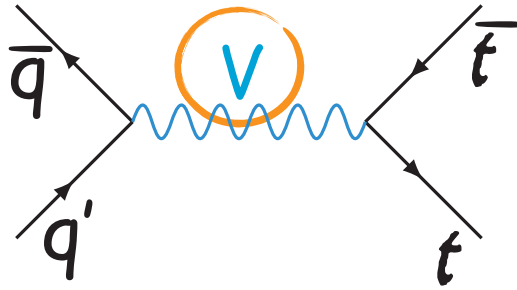


$\gamma, Z$

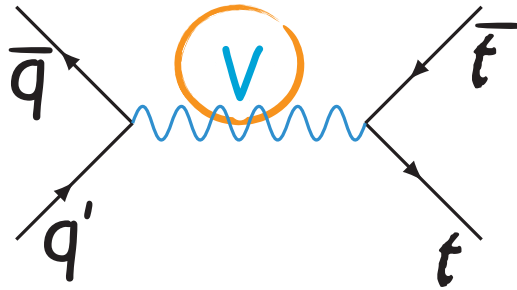
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Born (0QCD4EW4BSM)

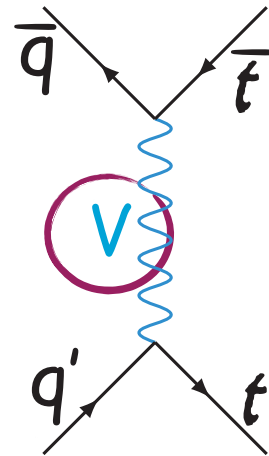
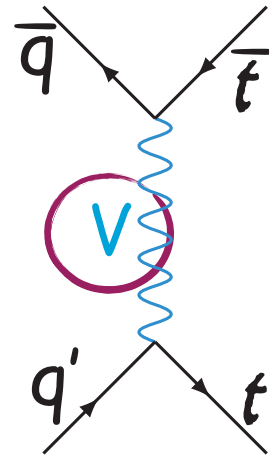
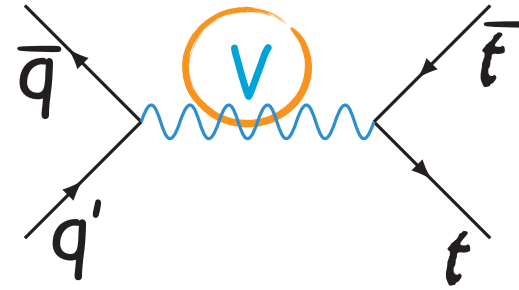
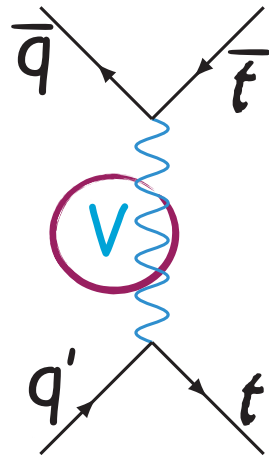
Z'



Z'



W'



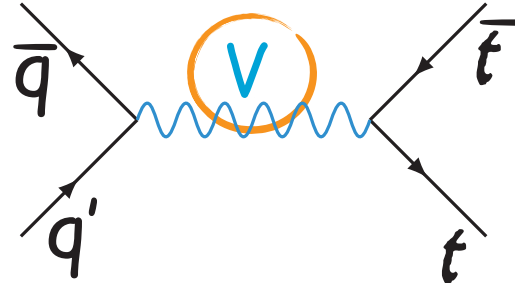
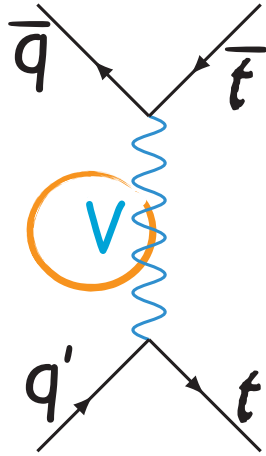
W'



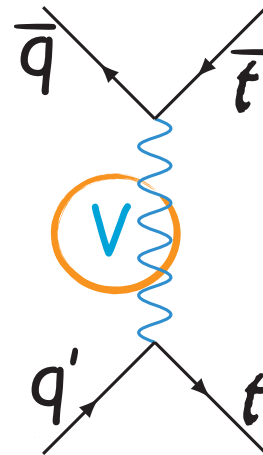
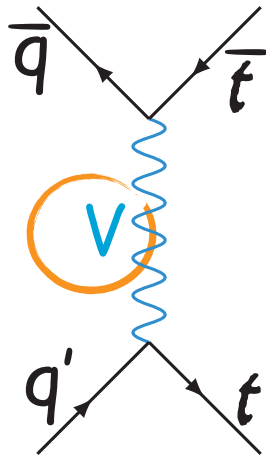
# Subprocesses (5 FNS)

Born (0QCD4EW4BSM)

Z'

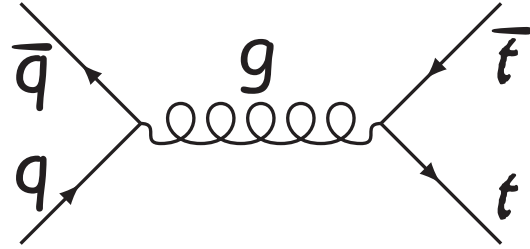


Z'

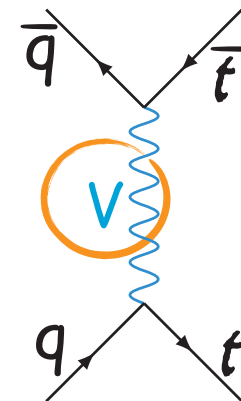
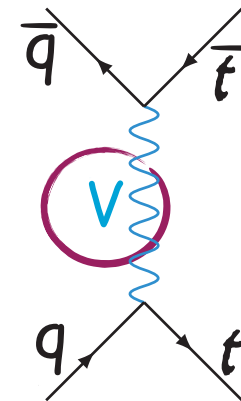
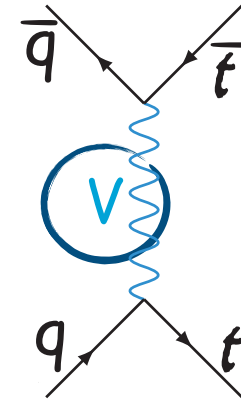
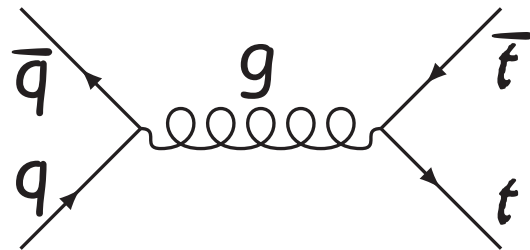
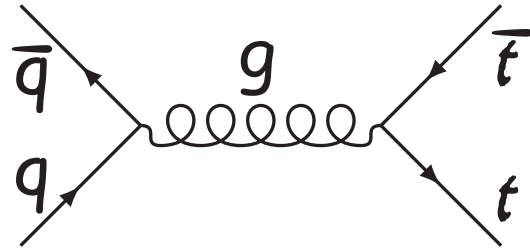


# Subprocesses (5 FNS)

Born (2QCD2EW0BSM):



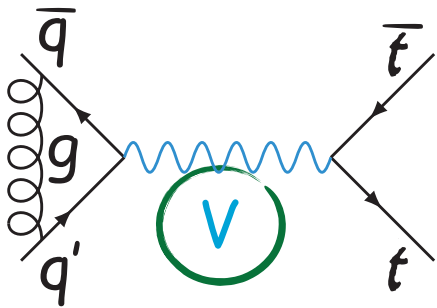
Born (2QCD2EW2BSM):



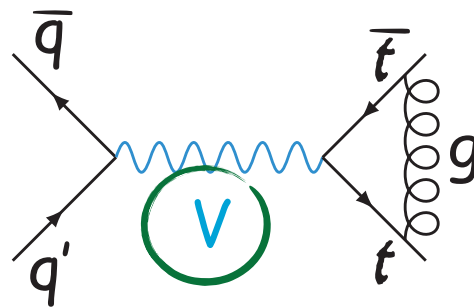
# Subprocesses (5 FNS)

Virtual

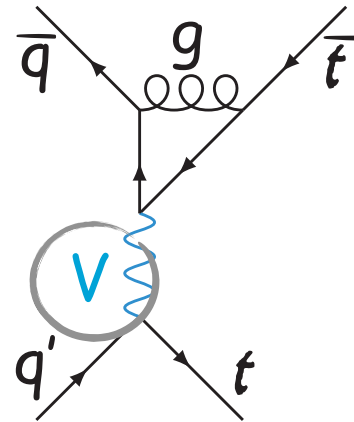
$\gamma, Z, Z'$



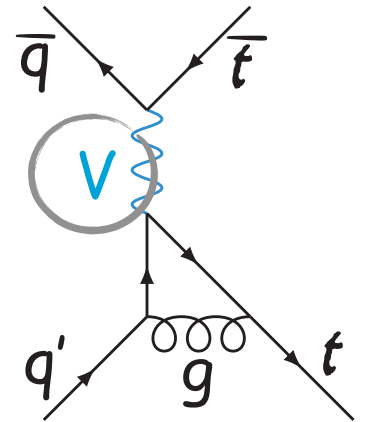
(a)



(b)



(c)



(d)

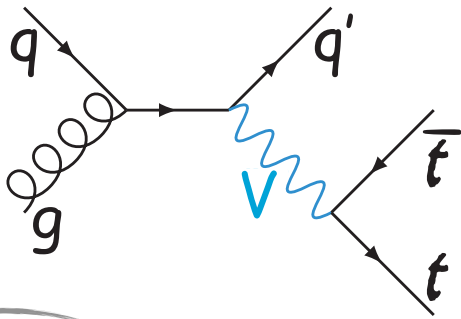
$Z', W', W$

# Subprocesses (5 FNS)

$$q' + \bar{q} \rightarrow t + \bar{t} + g$$

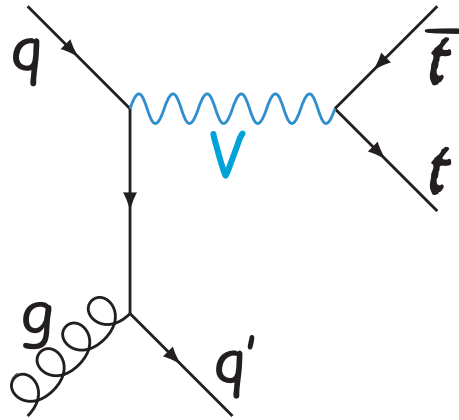
# Subprocesses (5 FNS)

$$g + q \rightarrow t + \bar{t} + q'$$

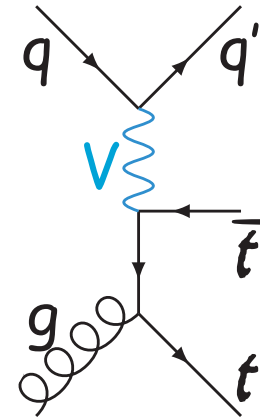


$W, W', Z'$

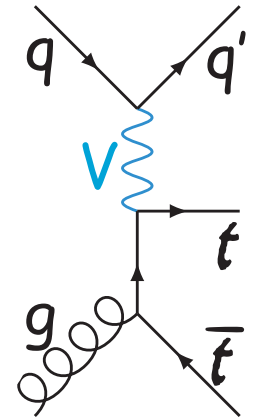
(a)



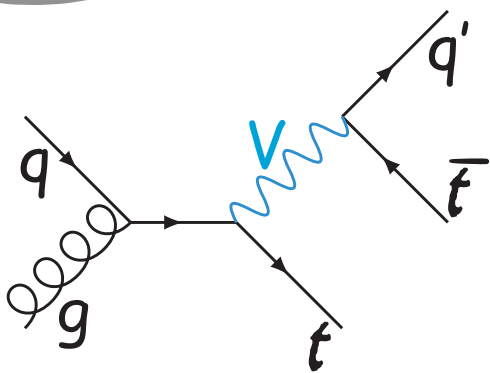
(b)



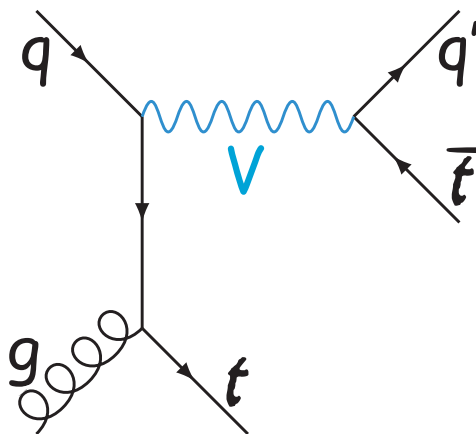
(c)



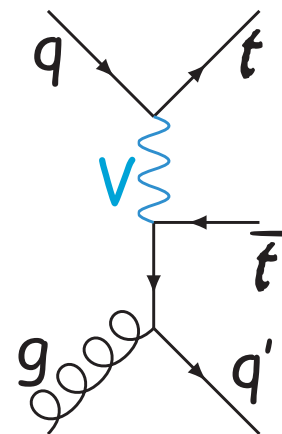
(d)



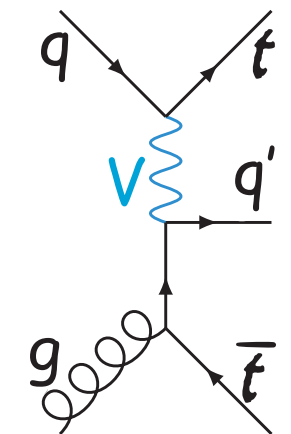
(e)



(f)



(g)



(h)