

# Progress on Electroweak studies at FCC-ee

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2<sup>nd</sup> FCC-France Workshop  
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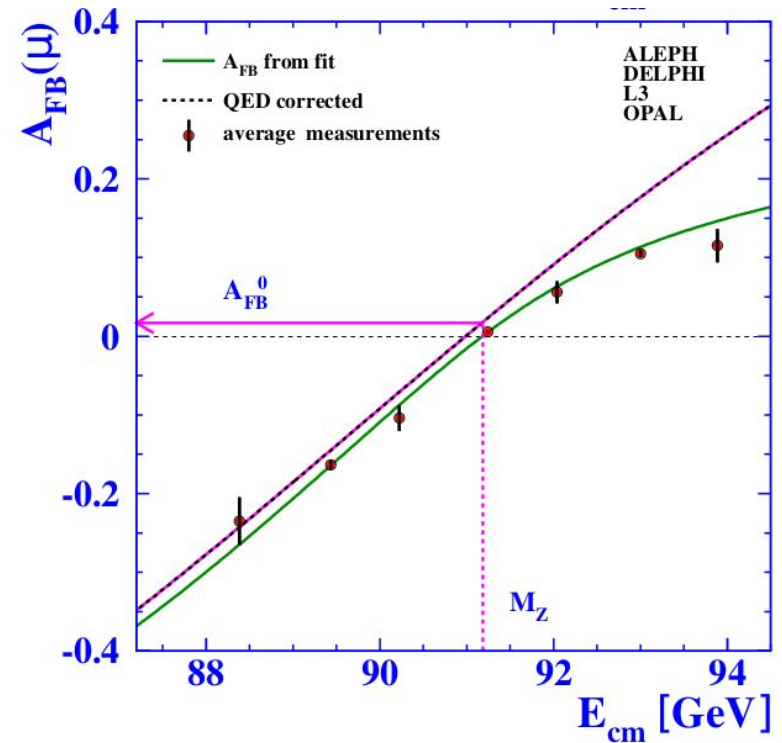
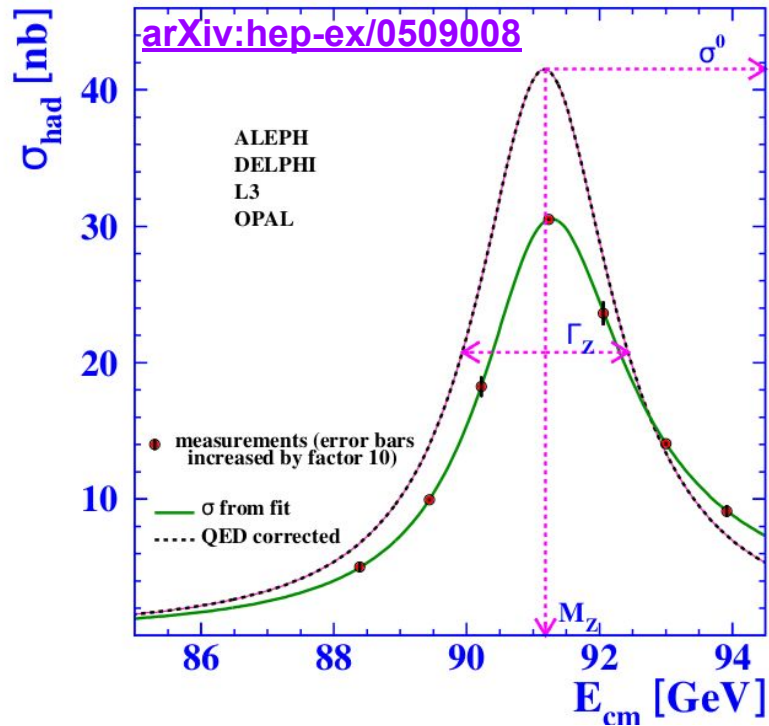
**Ciemat** Centro de Investigaciones  
Energéticas, Medioambientales  
y Tecnológicas



# Outline

- Focus on a few recent progress/prospects:
  - $A_{\text{FB}}(b)$
  - Some prospects in the HF sector (Rb, charm sector)
  - $ee \rightarrow \gamma\gamma$  channel
- Introduction and other <per-mille physics studies already discussed by Lucia (a few slides in backup just for completeness)

# Some Tera-Z key points



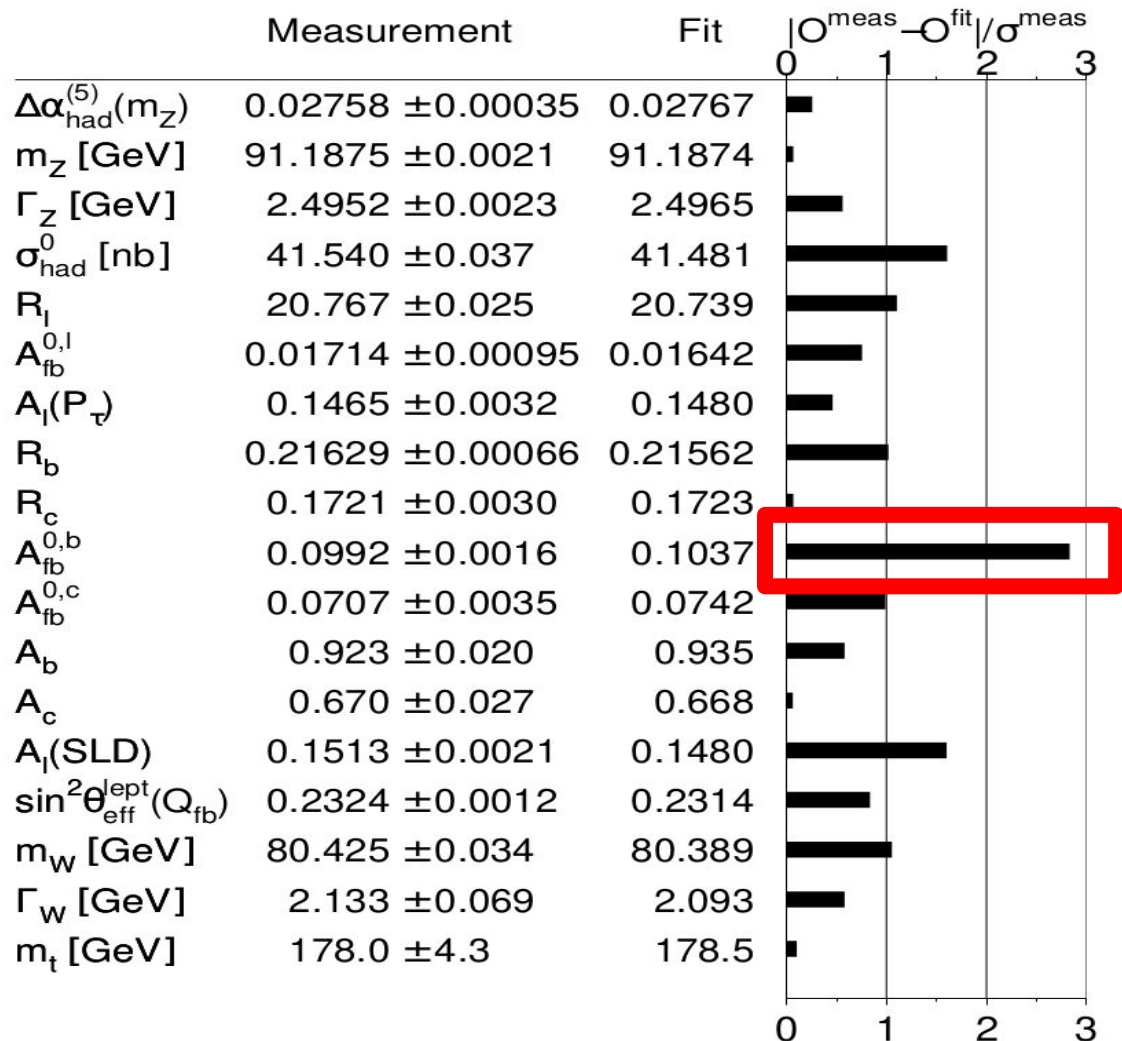
- Expected precisions in a nutshell:
  - $\approx 10^{-4}$  on cross sections (aimed luminosity uncertainty); possibility to reduce it by an order of magnitude using the measured  $\sigma(ee \rightarrow \gamma\gamma)$  as reference
  - $\approx 10^{-6}$  statistical uncertainties ( $\approx 1/\sqrt{N}$ ) on relative measurements like forward-backward charge asymmetries
  - Ultimate uncertainties typically dominated by systematics; precious value of "Tera" Z samples to study / constrain many of those uncertainties

# Present status of $A_{FB}(Q)$

- Electroweak measurement presenting the largest deviations in the global SM fit ([final LEPWWG paper \(2005\)](#))

$$A_{FB}(Q) = \frac{\sigma_F^Q - \sigma_B^Q}{\sigma_F^Q + \sigma_B^Q}$$

- New physics explanations require a substantial modification of Zbb right-hand couplings ([arxiv:0610173](#))



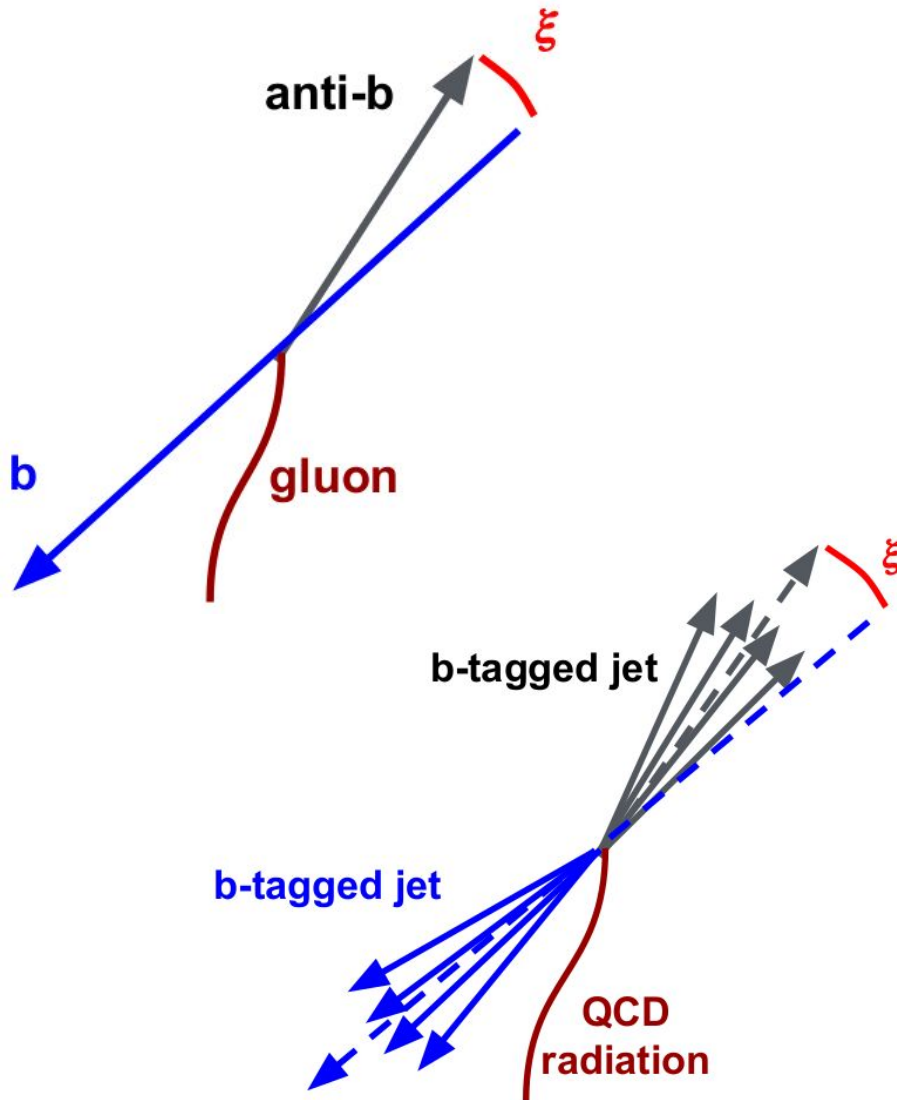
# Present status of $A_{FB}(Q)$

- QCD corrections are the dominant source of correlated systematics between measurements
- Measurement ([LEPEWWG reference](#)):  
 $0.0992$   
 $\pm 0.0015$  (stat.)  
 $\pm 0.0007$  (syst.)
- 1/2 syst. uncertainty using today's knowledge ([arXiv:2011.00530](#))
- Aiming for a  $\approx \pm 0.0001$  precision measurement at FCC-ee: one order of magnitude improvement !!**

Source	$R_b^0$ [ $10^{-3}$ ]	$R_c^0$ [ $10^{-3}$ ]	$A_{FB}^{0,b}$ [ $10^{-3}$ ]	$A_{FB}^{0,c}$ [ $10^{-3}$ ]	$\mathcal{A}_b$ [ $10^{-2}$ ]	$\mathcal{A}_c$ [ $10^{-2}$ ]
statistics	0.44	2.4	1.5	3.0	1.5	2.2
internal systematics	0.28	1.2	0.6	1.4	1.2	1.5
QCD effects	0.18	0	0.4	0.1	0.3	0.2
$B(D \rightarrow \text{neut.})$	0.14	0.3	0	0	0	0
D decay multiplicity	0.13	0.6	0	0.2	0	0
B decay multiplicity	0.11	0.1	0	0.2	0	0
$B(D^+ \rightarrow K^- \pi^+ \pi^+)$	0.09	0.2	0	0.1	0	0
$B(D_s \rightarrow \phi \pi^+)$	0.02	0.5	0	0.1	0	0
$B(\Lambda_c \rightarrow p K^- \pi^+)$	0.05	0.5	0	0.1	0	0
D lifetimes	0.07	0.6	0	0.2	0	0
B decays	0	0	0.1	0.4	0	0.1
decay models	0	0.1	0.1	0.5	0.1	0.1
non incl. mixing	0	0.1	0.1	0.4	0	0
gluon splitting	0.23	0.9	0.1	0.2	0.1	0.1
c fragmentation	0.11	0.3	0.1	0.1	0.1	0.1
light quarks	0.07	0.1	0	0	0	0
beam polarisation	0	0	0	0	0.5	0.3
total correlated	0.42	1.5	0.4	0.9	0.6	0.4
total error	0.66	3.0	1.6	3.5	2.0	2.7

# $A_{FB}(b/c)$

[arXiv:2010.08604](https://arxiv.org/abs/2010.08604)



- New developments for  $A_{FB}(b/c)$ : QCD corrections and uncertainties can be reduced significantly using acollinearity ( $\xi$ ) cuts  $\Rightarrow$  not a limiting factor anymore to reach the  $\lesssim 0.1\%$  precision level
- Further improvements expected from better heavy flavor tagging capabilities and a more accurate measurement of the heavy quark flight direction
- **Performing a realistic measurement with more sophisticated b/c tagging techniques  $\rightarrow$  define detector requirements**
- Note that all these measurements can be done with exclusive decays. Certainly for the charm case. For instance, a Tera-Z facility will provide  $\approx 10^8$   $B^+$  exclusive decays

# Reduction of QCD uncertainties

- Detailed table of central values and uncertainties:

**stat. unc. for  $7 \times 10^7$   
 $Z \rightarrow b\bar{b}$  events**

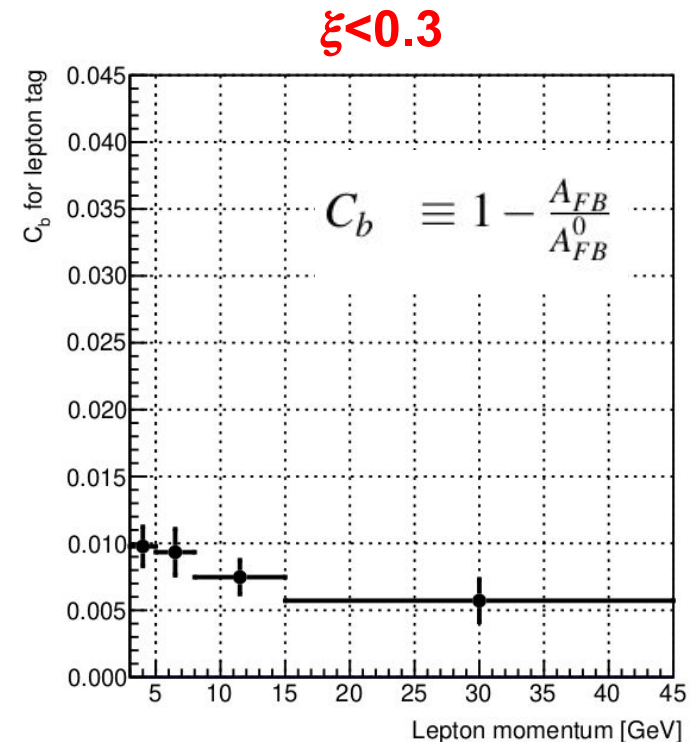
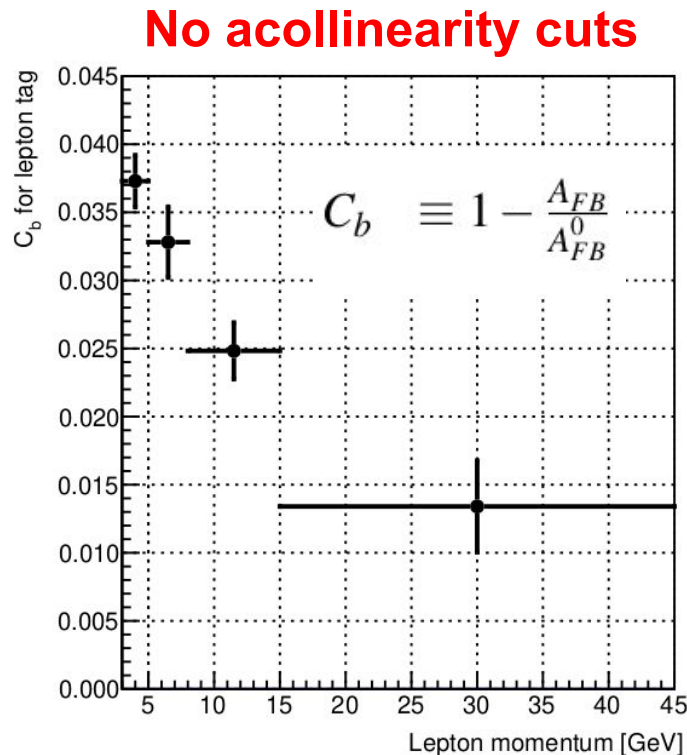
$\xi_0$ cut	Measured $A_{FB}$	$\Delta A_{FB}(\text{stat})$	$\Delta A_{FB}(\text{tune})$	$\Delta A_{FB}(\text{theo. QCD corr})$
No cut	$0.0998 \pm 0.0004$	0.00008	0.00014	0.00033
1.50	$0.1003 \pm 0.0003$	0.00011	0.00014	0.00023
1.00	$0.1011 \pm 0.0002$	0.00011	0.00010	0.00016
0.50	$0.1023 \pm 0.0002$	0.00011	0.00010	0.00007
0.30	$0.1030 \pm 0.0002$	0.00011	0.00010	0.00003
0.20	$0.1033 \pm 0.0001$	0.00011	0.00005	0.00002
0.10	$0.1035 \pm 0.0002$	0.00016	0.00005	0.00001

Table 9: Central values and components of the uncertainty in the measurement of the  $A_{FB}$  asymmetry with  $7 \times 10^7 e^+e^- \rightarrow b\bar{b}(g)$  events at the Z pole, for different  $\xi < \xi_0$  cuts at the reconstructed level.

**$\lesssim 0.1\%$  relative systematic  
uncertainties for  $\xi \lesssim 0.3$**

# ... also in semi-leptonic decays

- Evaluating the QCD corrections as a function of the momentum in semi-leptonic b decays, now with acollinearity cuts (generator level):



- Significant reduction (note:  $p_l > 3$  GeV cut in preselection)
- Full realistic analysis still to be done



# $R_b, R_c$

$$R_b = \frac{\Gamma_{b\bar{b}}}{\Gamma_{had}}, \quad R_c = \frac{\Gamma_{c\bar{c}}}{\Gamma_{had}}$$

- Measured at LEP/SLC very precisely using single and double-tag event fractions for the b case:



No Bckgd, no hemisphere correlations  $\Rightarrow R_b = \frac{f_{single}^2}{f_{double}}$

$$f_{single} = R_b \epsilon_b + R_c \epsilon_c + (1 - R_b - R_c) \epsilon_{uds}$$

**Real life:**

$$f_{double} = c_b R_b \epsilon_b^2 + c_c R_c \epsilon_c^2 + c_{uds} (1 - R_b - R_c) \epsilon_{uds}^2$$

$$c_b = c_c = c_{uds} = 1 \text{ if no hemisphere correlations}$$

# Present status of $R_b$ , $R_c$

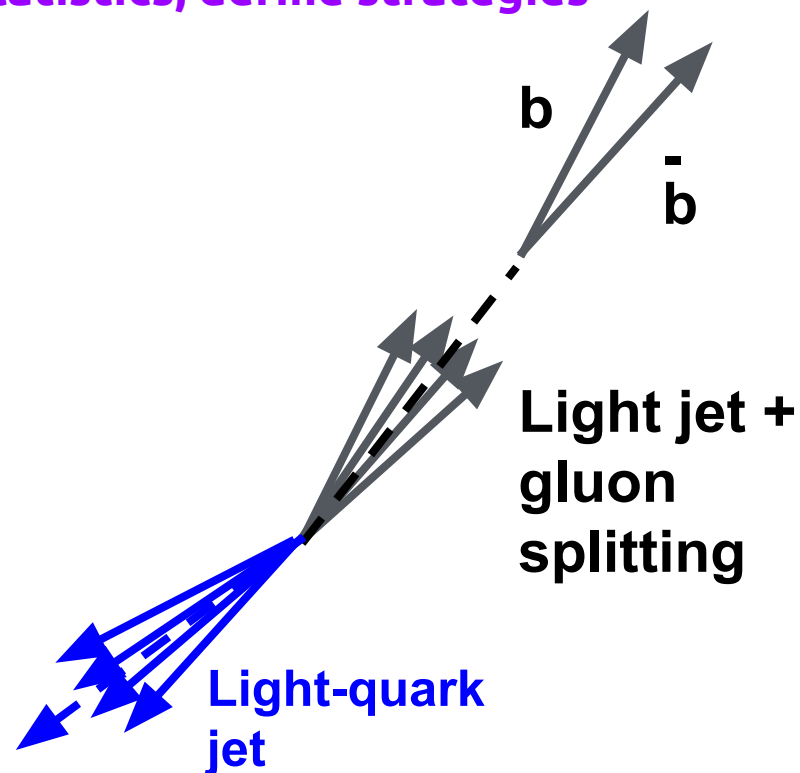
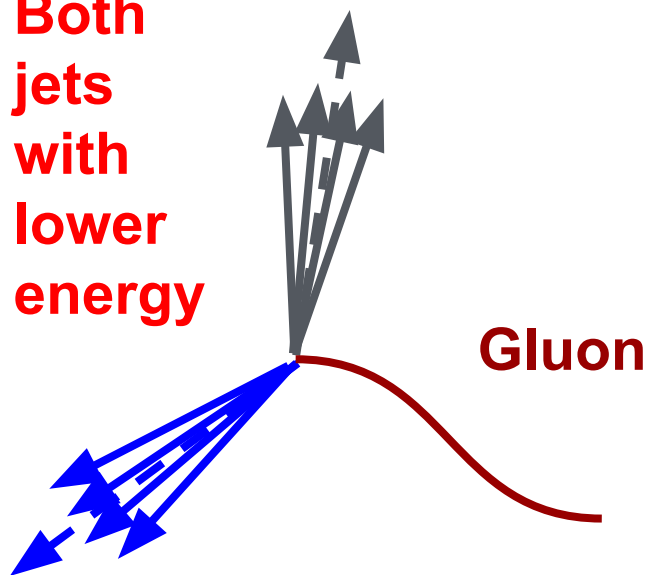
- Hemisphere correlation effects (QCD) and gluon splitting are large sources of correlated uncertainty among experiments
- LEPEWWG result:  
 $R_b = 0.21629 \pm 0.00066$
- Aiming for a  $\lesssim 3 \times 10^{-4}$  precision measurement on  $R_b$  at FCC-ee: one order of magnitude improvement
- $R_c$  to be re-studied for a Tera-Z factory via exclusive / inclusive single+double-tag methods (SLD way, not LEP main way)

Source	$R_b^0$ [ $10^{-3}$ ]	$R_c^0$ [ $10^{-3}$ ]	$A_{\text{FB}}^{0,b}$ [ $10^{-3}$ ]	$A_{\text{FB}}^{0,c}$ [ $10^{-3}$ ]	$\mathcal{A}_b$ [ $10^{-2}$ ]	$\mathcal{A}_c$ [ $10^{-2}$ ]
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# $R_b, R_c$

- Important elements of the study:
  - Improvement of the b (and c) purity → better detectors
  - Reduction of hemisphere correlations and syst. uncertainties:
    - Common vertex correlations (smaller in future detectors)
    - QCD effects (reduction with acollinearity cuts like in  $A_{FB}(Q)$  ?)
    - Gluon splitting → huge available statistics, define strategies

Both jets with lower energy



# Interest of the $e^+e^- \rightarrow \gamma\gamma$ at FCC-ee

- Process minimally affected by theoretical uncertainties:
    - Hadronic corrections only appear at the  $10^{-5}$  level ([arXiv:1906.08056](https://arxiv.org/abs/1906.08056))
  - Measurable at “relatively” high polar angles with respect to the beam:
    - $1/\sqrt{N}=1.3e-5$  for  $|\cos \theta|<0.95$ ,
    - $1/\sqrt{N}=2.0e-5$  for  $|\cos \theta|<0.7$
- ( $\sqrt{s}=91.2$  GeV, assuming LO cross section and 100% acceptance)

$\sqrt{s}$ (GeV)	$\sigma_{\Delta\alpha}^{\text{NNLO}}_{\text{lep+top}}/\sigma_{LO}$	$\sigma_{\Delta\alpha}^{\text{NNLO}}_{\text{had}}/\sigma_{LO}$	$\delta\sigma_{\text{had}}/\sigma_{LO}$
91	0.096%	0.085%	$3.7 \cdot 10^{-6}$
160	0.108%	0.098%	$3.8 \cdot 10^{-6}$
240	0.115%	0.108%	$3.9 \cdot 10^{-6}$
365	0.119%	0.120%	$4.0 \cdot 10^{-6}$

[arXiv:1906.08056](https://arxiv.org/abs/1906.08056)

Table 3: Relative contribution of the NNLO leptonic(+top) and hadronic vacuum polarization correction to the cross section in setup [b] and for four FCC-ee c.m. energies. In the last column, the uncertainty due to the hadronic contribution is shown.

- Hopefully not much sensitive to new physics.
  - **Can we quantify a bit more the potential of this channel ?**

# New physics deviations in $e^+e^- \rightarrow \gamma\gamma$

- If we stop at the  $s^2/\Lambda^4$  order (justified with large statistics and well below the true scale of physics, which is guaranteed in  $e^+e^-$  collisions):

$$\left( \frac{d\sigma}{d\cos\theta} \right)_{SM+new} = \left( \frac{d\sigma}{d\cos\theta} \right)_{SM} \left[ 1 + \frac{c_8 s^2}{8\pi\alpha\Lambda^4} \sin^2\theta \right]$$

- **This is the only possible “leading” behavior of new physics deviations in  $e^+e^- \rightarrow \gamma\gamma$ . It largely simplifies the task of measuring/excluding new physics effects if we want to use this process as luminosity reference**
- Physical examples (actually all, according to the previous statement, but just in case...):
  - Excited electrons (exchanged in t-channel), large extra-dimension effects (graviton exchange in s-channel)

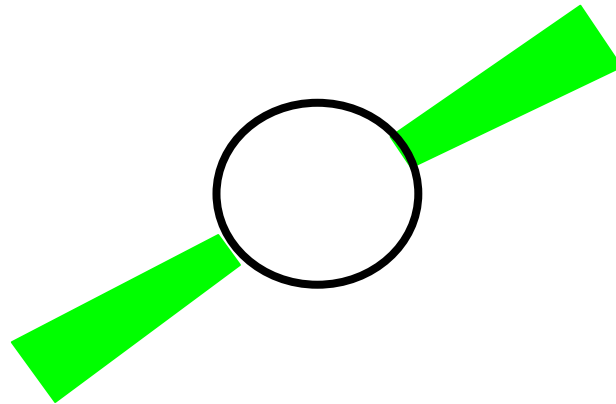
# Likelihood shape fit with $|\cos\theta| < 0.95$

Collider option	$\sqrt{s}$ [TeV]	$L$ [ab $^{-1}$ ]	$\Delta\lambda$ [TeV $^{-4}$ ]	$\Delta\sigma_{NP}/\sigma_{SM}$	$\Lambda_{\pm}$ limit [TeV]	$\Lambda$ limit [TeV]
FCC-ee	0.09	150.0	1.2	$1.9 \times 10^{-5}$	0.8	1.4
FCC-ee	0.16	10.0	$8.9 \times 10^{-1}$	$1.3 \times 10^{-4}$	0.9	1.6
FCC-ee	0.24	5.0	$3.7 \times 10^{-1}$	$2.8 \times 10^{-4}$	1.1	2.0
FCC-ee	0.35	1.5	$2.2 \times 10^{-1}$	$7.5 \times 10^{-4}$	1.2	2.2
ILC	0.25	2.0	$5.2 \times 10^{-1}$	$4.6 \times 10^{-4}$	1.0	1.8
ILC	0.50	4.0	$4.6 \times 10^{-2}$	$6.5 \times 10^{-4}$	1.8	3.3
CLIC	0.38	1.0	$2.1 \times 10^{-1}$	$9.9 \times 10^{-4}$	1.2	2.3
CLIC	1.50	1.5	$2.8 \times 10^{-3}$	$3.3 \times 10^{-3}$	3.7	6.7
CLIC	3.00	5.0	$1.9 \times 10^{-4}$	$3.5 \times 10^{-3}$	7.2	13.0

- Reaching the ultimate FCC-ee limit at the Z requires  $<10^{-4}$  precision in acceptance, but one can decouple SM rate and new physics effects
  - a simultaneous fit to both the measured SM rate and  $\lambda$  can be envisaged

# Some thoughts on systematics control

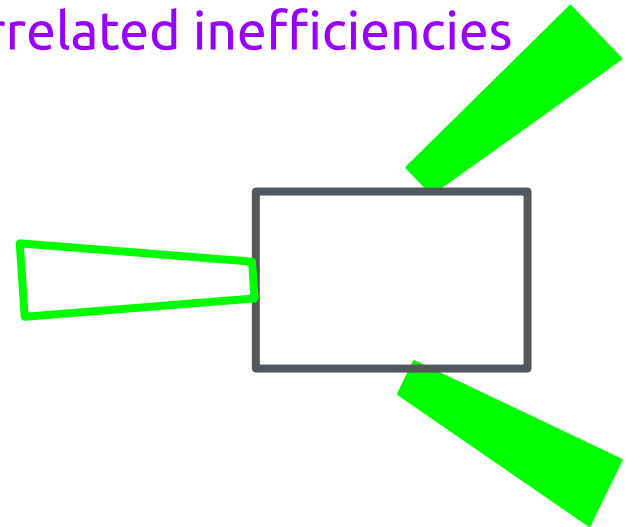
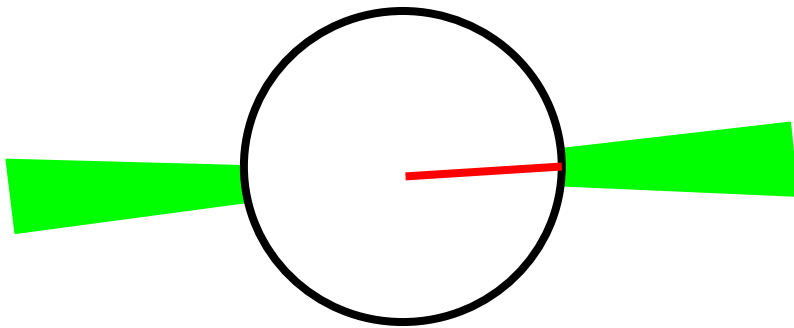
- Mostly based on past LEP2 experience:
  - Use relatively soft em-shape criteria to keep selection systematics under control
  - Use (loose) acollinearity cuts to reduce the size of radiative corrections (LEP2 studies). This also rejects additional high-energy (ISR) photons in the beam pipe



- Compact detector is a must. Minimize barrel-endcap gaps or just eliminate that region in analysis in a limit case
- Edge effects and precise measurement of the fiducial region also important (like in the  $\mu\mu$  case, I guess)

# Some thoughts on systematics control

- Accounting for percent effects:
  - Control sample: events with 1 good photon with zero track activity and another “loosely tagged” photon: stronger acollinearity cuts and electromagnetic energy
    - Measure/correct photon conversion probability and fermion-pair FSR on loosely tagged photons
    - Measure/correct electron identification acceptance on loosely tagged photons with zero track activity
    - Maybe a good idea to measure everything in a kind of global fit
  - Use acolinear  $\gamma\gamma$  (or  $ee$ ) events (hard photon in the beam pipe) to look for unaccounted back-to-back correlated inefficiencies



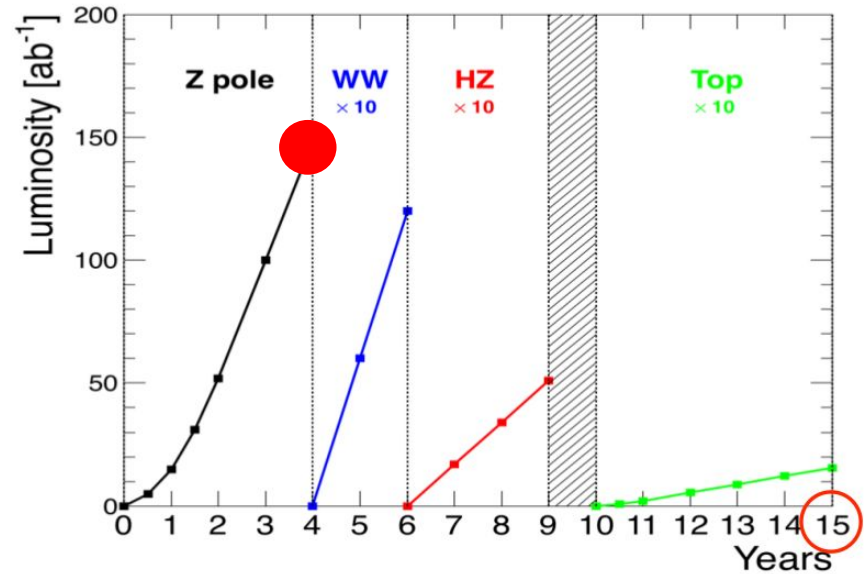
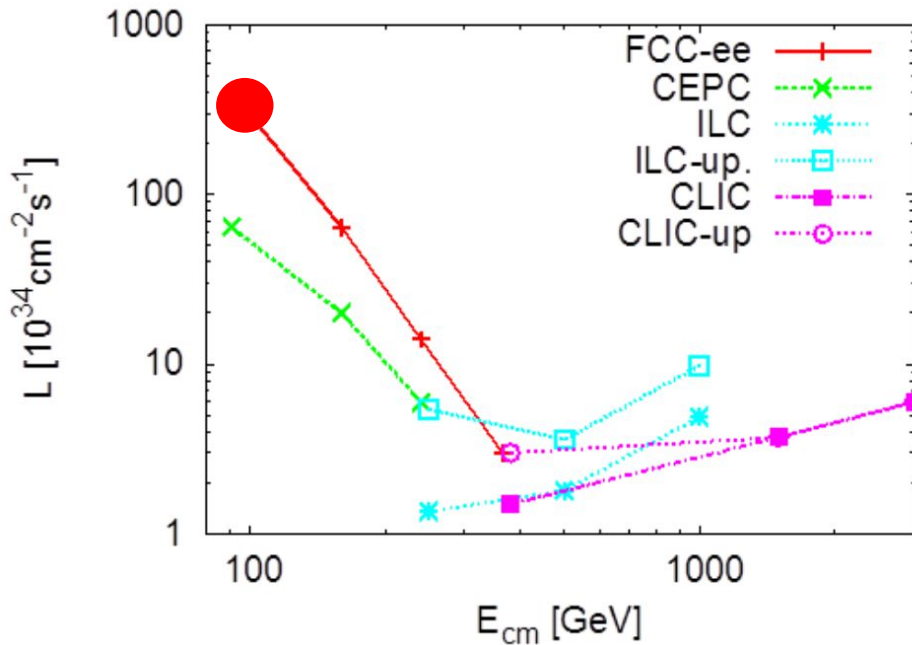


# Summary/outlook

- **Advancing in the EW front:**
  - ppm precision measurements: fine-tuning simulations and experimental techniques to keep systematics under control
  - $b/c/\tau$  front: significant step beyond LEP status/precision, refining experimental strategies to reduce systematics to a minimum
  - $ee \rightarrow \gamma\gamma$ :  $\approx 10^{-5}$  precision measurement in acceptance/efficiency/backgrounds possible, independently of new physics deviations  $\Rightarrow$  luminosity measurement beyond  $10^{-4}$  precision feasible
- **Significant amount of work ahead, but prospects are exciting !!**

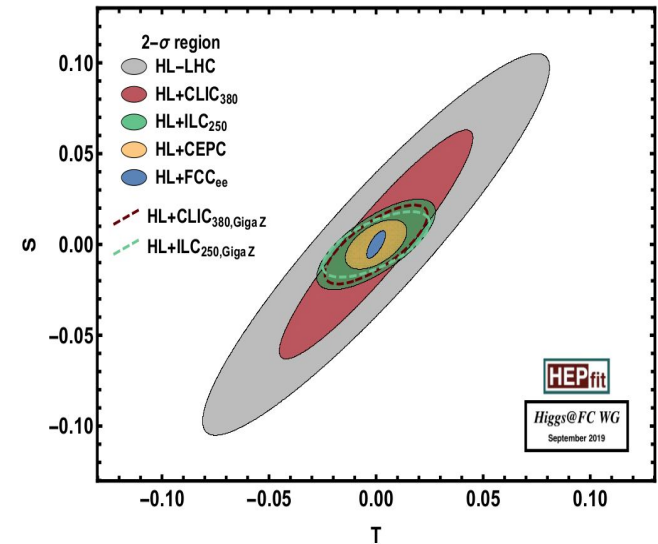
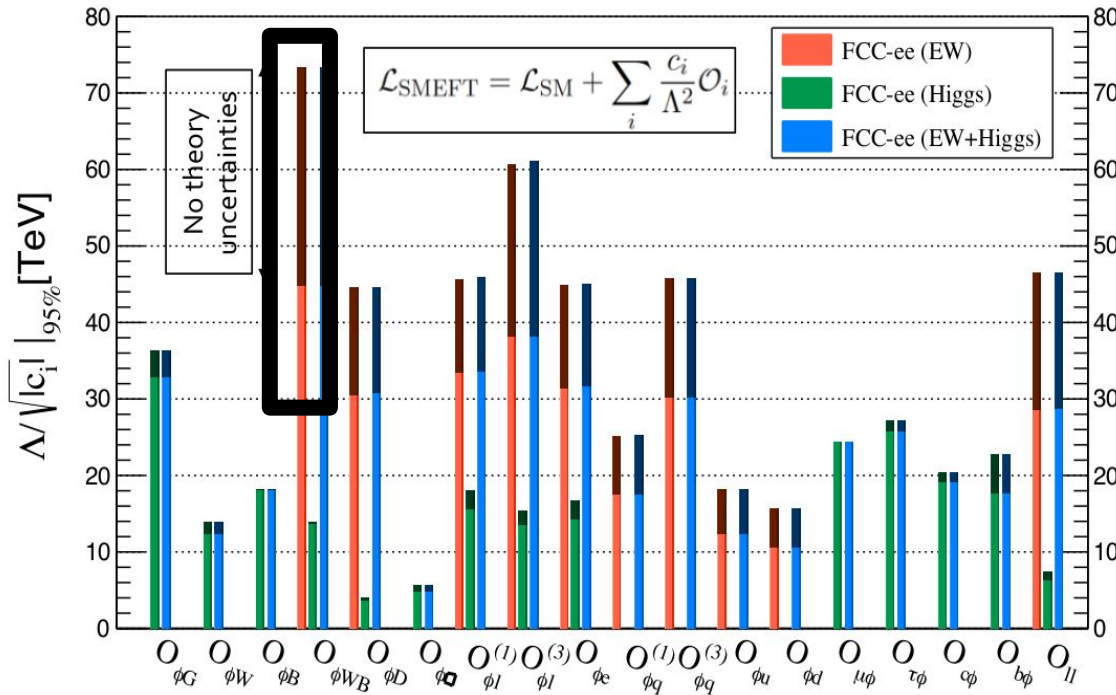
**Backup**

# FCC-ee context

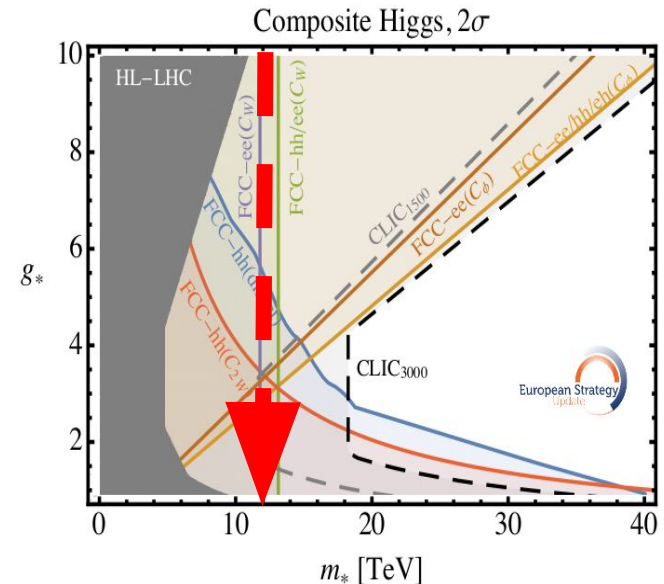


- FCC-ee:  $150 \text{ ab}^{-1}$ ,  $5 \times 10^{12}$  Z decays in  $\approx 4$  years of running at the Z pole
- Extraordinary  $\sqrt{s}$  precision: 100 keV at the Z, 300 keV at WW threshold  $\rightarrow$  exquisite control of beam uncertainties (average, width, systematics)
- Aiming for up to  $\approx 100$  times better precision than LEP/SLD on several electroweak precision observables (EWPO)
- **Current challenges: reduce uncertainties, establish theory / detector / machine requirements to reach the ultimate precision**

# Physics potential of Tera-Z



- Efficiently probing the 10-TeV scale for universal new-physics effects (Higgs compositeness, ...) with just a few years of EW running at the FCC-ee:
  - Strong constraints on the S parameter ( $O_{\phi_{WB}}$ ,  $O_W + O_B$  in SILH, ...)
  - Also on the T parameter (violations of custodial symmetry)

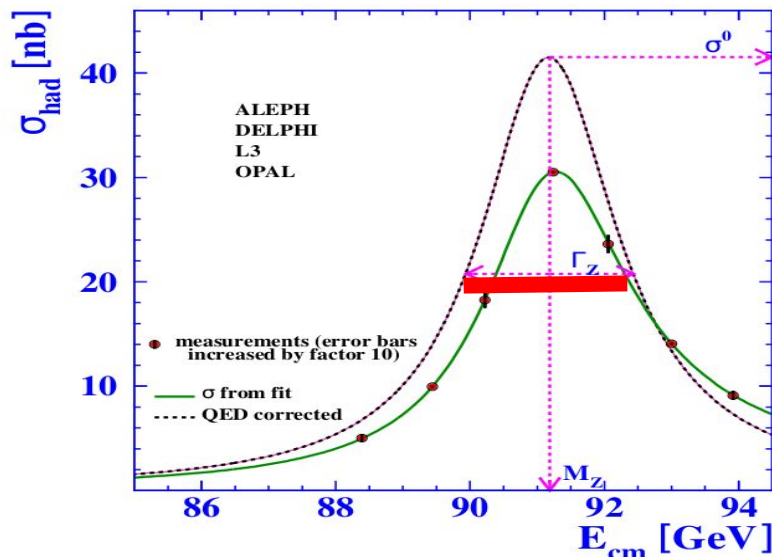


# Summary table

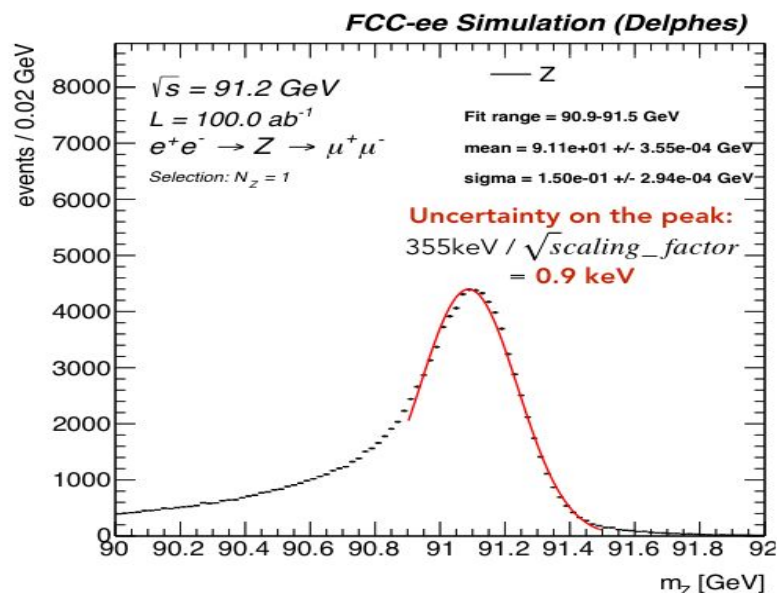
Observable	present value $\pm$ error	FCC-ee <b>Stat.</b>	FCC-ee Syst.	Comment and leading exp. error
$m_Z$ (keV)	$91186700 \pm 2200$	<b>4</b>	100	From Z line shape scan Beam energy calibration
$\Gamma_Z$ (keV)	$2495200 \pm 2300$	<b>4</b>	25	From Z line shape scan Beam energy calibration
$R_\ell^Z (\times 10^3)$	$20767 \pm 25$	<b>0.06</b>	0.2-1	ratio of hadrons to leptons <b>acceptance for leptons</b>
$\alpha_s(m_Z^2) (\times 10^4)$	$1196 \pm 30$	<b>0.1</b>	0.4-1.6	from $R_\ell^Z$ above
$R_b (\times 10^6)$	$216290 \pm 660$	<b>0.3</b>	<60	ratio of bb to hadrons stat. extrapol. from SLD
$\sigma_{\text{had}}^0 (\times 10^3)$ (nb)	$41541 \pm 37$	<b>0.1</b>	4	peak hadronic cross section luminosity measurement
$N_\nu (\times 10^3)$	$2996 \pm 7$	<b>0.005</b>	1	Z peak cross sections Luminosity measurement
$\sin^2 \theta_W^{\text{eff}} (\times 10^6)$	$231480 \pm 160$	<b>3</b>	1	from $A_{\text{FB}}^{\mu\mu}$ at Z peak Beam energy calibration
$1/\alpha_{\text{QED}}(m_Z^2) (\times 10^3)$	$128952 \pm 14$	<b>3</b>	small	from $A_{\text{FB}}^{\mu\mu}$ off peak QED&EW errors dominate

- $\approx$  two orders of magnitude improvement expected for  $\Gamma_Z, R_\ell, \alpha_s, \sin^2 \theta_W^{\text{eff}}$

# Examples: $\Gamma_Z$ , $\sin^2\theta_W^{\text{eff}}$



- Total Z width  $\rightarrow$  basically coming from the visible width of the lineshape
- $\sin^2\theta_W^{\text{eff}}$  effective:  $g_V/g_A$  coupling ratio  $\rightarrow$  forward-backward charge asymmetries (most precise in  $\mu\mu$  in final state)
- **3 energy points ( $\approx 88, 91.2, 94$  GeV)**



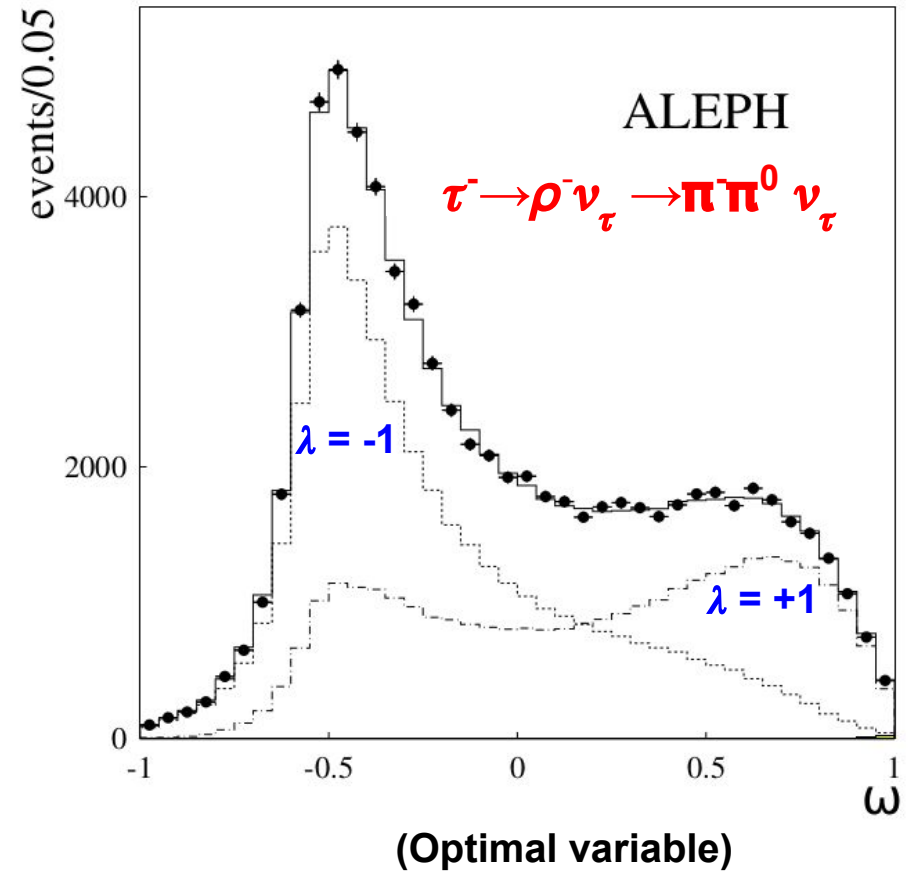
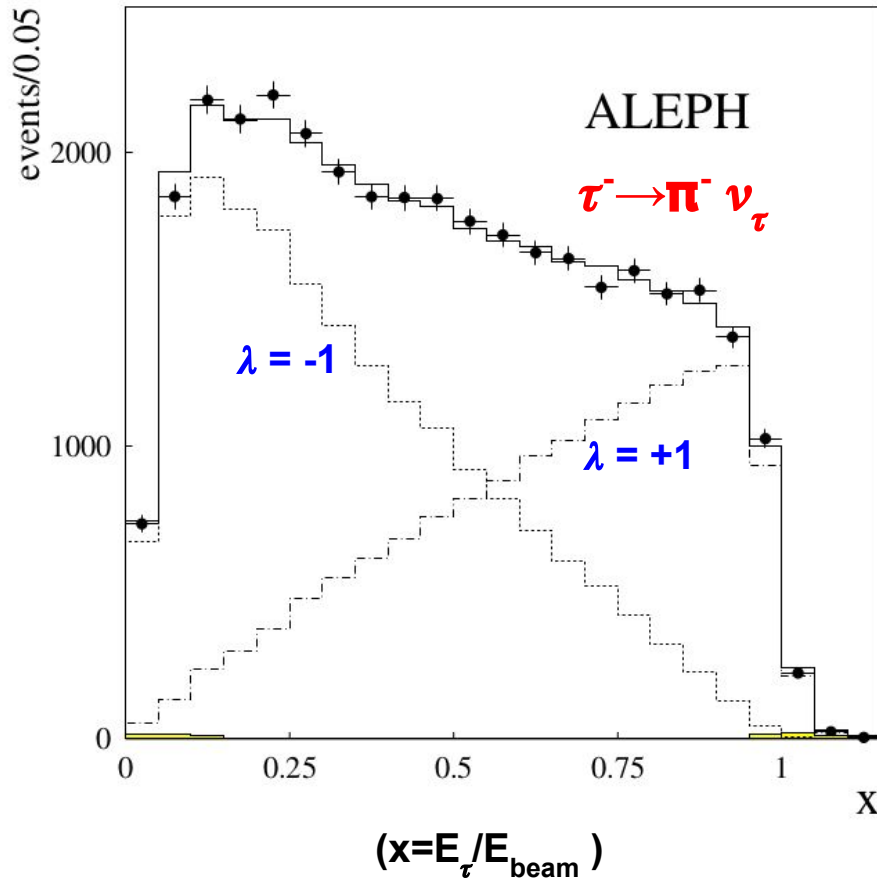
- Development of utilities/generators to study in much more detail point-to-point energy uncertainties, momentum-scale effects, ... , taking into account beam-energy spread, ISR, eventually initial-final state interference effects (E. Leogrande, E. Perez, P. Janot, ...)

# HF-EW summary table

Observable	present value $\pm$ error	FCC-ee <b>Stat.</b>	FCC-ee Syst.	Comment and leading exp. error
$A_{\text{FB},0}^b (\times 10^4)$	$992 \pm 16$	<b>0.02</b>	1-3	b-quark asymmetry at Z pole from jet charge
$A_{\text{FB}}^{\text{pol},\tau} (\times 10^4)$	$1498 \pm 49$	<b>0.15</b>	$< 2$	$\tau$ polarization asymmetry $\tau$ decay physics
$R_b (\times 10^6)$	$216290 \pm 660$	<b>0.3</b>	$< 60$	ratio of bb to hadrons stat. extrapol. from SLD

- **Objective: get  $\geq 20$  times better than current precision**

# Analysis at LEP



- Cross-talk between  $\tau$  decay channels and the precise understanding of the helicity shape are main items to study to reduce systematics:
  - $\approx 11\%$   $\tau$  background from other decay channels in these plots
  - the tiny yellow shaded area is the non- $\tau$  background



# $A_\tau$ to do: optimize channel separation

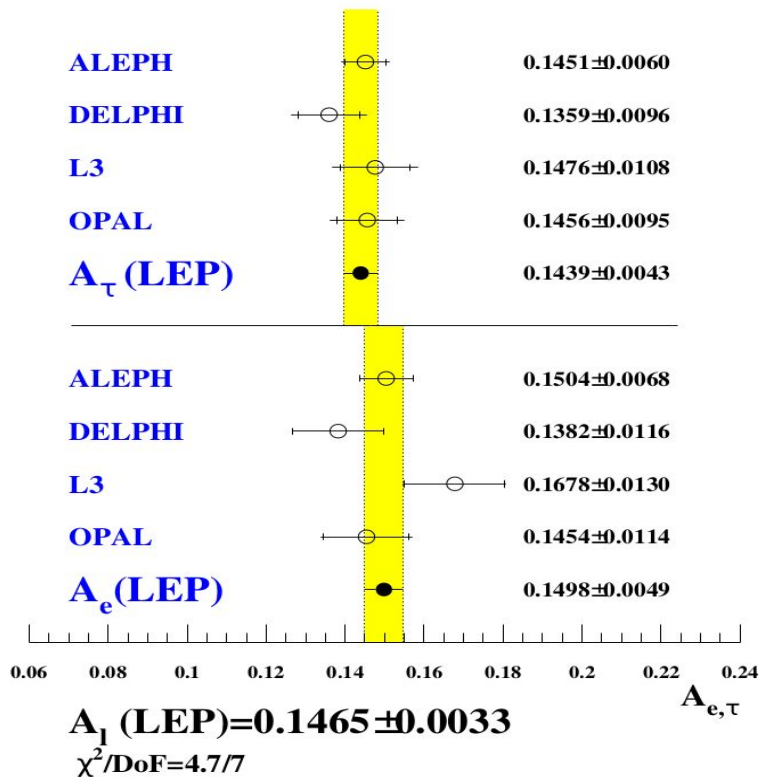
Table 2: Summary of the systematic uncertainties (%) on  $A_\tau$  and  $A_e$  in the single- $\tau$  analysis.

Source	$A_\tau$							ALEPH
	$h$	$\rho$	$3h$	$h2\pi^0$	$e$	$\mu$	Incl. $h$	
selection	-	0.01	-	-	0.14	0.02	0.08	
tracking	0.06	-	0.22	-	-	0.10	-	
ECAL scale	0.15	0.11	0.21	1.10	0.47	-	-	
PID	0.15	0.06	0.04	0.01	0.07	0.07	0.18	
misid.	0.05	-	-	-	0.08	0.03	0.05	
photon	0.22	0.24	0.37	0.22	-	-	-	
non- $\tau$ back.	0.19	0.08	0.05	0.18	0.54	0.67	0.15	
$\tau$ BR	0.09	0.04	0.10	0.26	0.03	0.03	0.78	
modelling	-	-	0.70	0.70	-	-	0.09	
MC stat	0.30	0.26	0.49	0.63	0.61	0.63	0.26	
TOTAL	0.49	0.38	1.00	1.52	0.96	0.93	0.87	

- **ALEPH was the best detector for this: large tracking volume for separation, large magnetic field for bending, high granularity for  $\pi^0 \rightarrow \gamma\gamma$  identification**
- **Photon separation /  $\pi^0$  identification was still the dominant systematics**

# $A_e$ is slightly different...

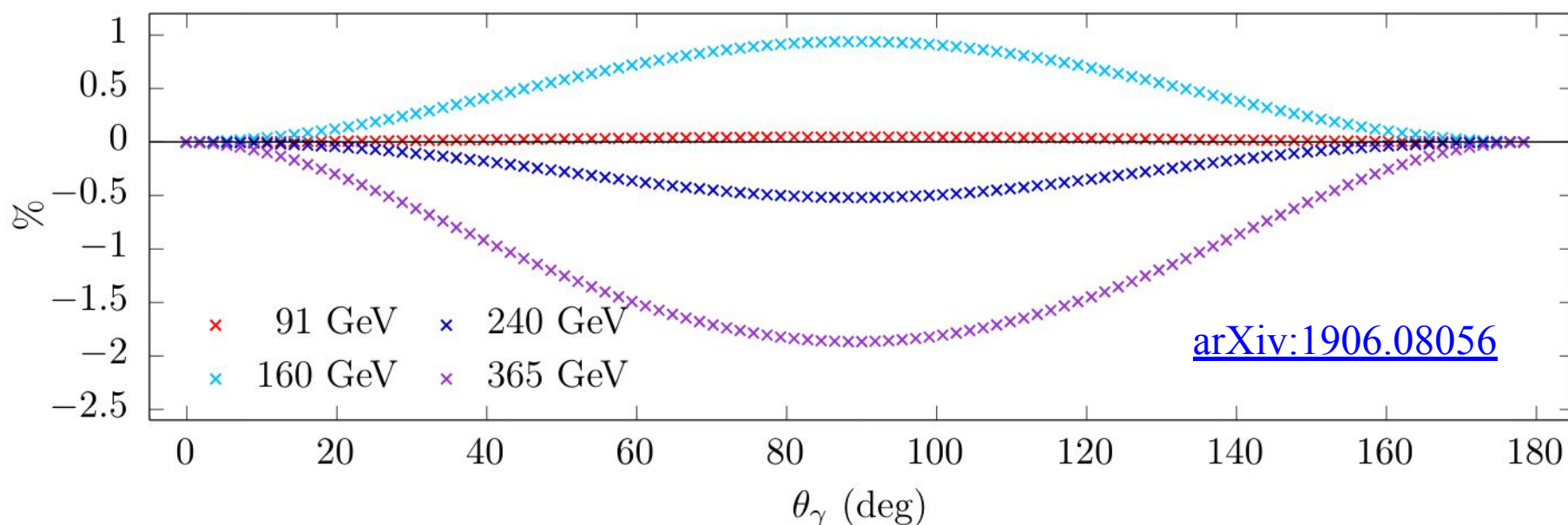
Experiment	$A_\tau$	$A_e$
ALEPH	$0.1451 \pm 0.0052 \pm 0.0029$	$0.1504 \pm 0.0068 \pm 0.0008$
DELPHI	$0.1359 \pm 0.0079 \pm 0.0055$	$0.1382 \pm 0.0116 \pm 0.0005$
L3	$0.1476 \pm 0.0088 \pm 0.0062$	$0.1678 \pm 0.0127 \pm 0.0030$
OPAL	$0.1456 \pm 0.0076 \pm 0.0057$	$0.1454 \pm 0.0108 \pm 0.0036$
LEP	$0.1439 \pm 0.0035 \pm 0.0026$	$0.1498 \pm 0.0048 \pm 0.0009$



- Note that  $A_e$  ( $\equiv -P_\tau^{\text{FB}}$ ) is much less affected by systematic uncertainties, because forward-backward asymmetry measurements are largely independent of (charge symmetric) acceptance uncertainties

# By-products

- Do QED radiative corrections include anyway terms equivalent to SM deviations of this  $\sin^2\theta$  type ?



Relative contribution of the weak NLO corrections to the  $ee \rightarrow \gamma\gamma$  cross section (which approximately follows a  $\sin^2\theta_\gamma$  dependence)

# Some thoughts on systematics control

- These ideas could be tested on realistic simulations, of course, but several of them could be just tested at the generator level (to be done)
  - Generator level:
    - $\gamma^* \rightarrow$  fermion-pair contributions
    - Rates of collinear vs acollinear photons
  - Simulation level:
    - Rate of conversion effects (much smaller for pixel+TPC ?)
    - Homogeneity of calorimeter, back-to-back effects, holes, ...
- We will be hardly able to conclude on an optimal polar angle cut before time is due. Typically, problems related with acceptance, electromagnetic identification or the presence of additional tracks / photons are more disturbing at the large  $|\cos\theta|$  edges, while the sensitivity loss by going more central is not so big.
- Not clear whether detailed simulations will offer much more than approximate simulations to conclude whether  $10^{-5}$  precisions (or  $\approx 10^{-4}$  precision in a local  $\cos(\theta)$  region) are reachable/realistic...