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# Cours LISA : Modèle de Performance

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# Plan

**I/ Objectifs et structure du modèle de performance**

**II/ Rappels sur la mesure**

**III/ Quelques bruits en détails**

**IV/ Limitations**

# The Consortium LISA Performance Model

## GOAL

Link between science specifications in the Science Requirement Document and the instruments noises and parameters values.

- Bottom Up : **Current Best Estimate [CBE]** -> Capture the physics and our best understanding of the instrument.
- Top Down approach: **Allocation** -> Capture our level of confidence.

## The Consortium LISA Performance Model

- **Frequency domain model of the LISA constellation** as Amplitude Spectrum Density
- **Hierarchical model** : from strain sensitivity to sub-system noises & parameters

# Objectif du modèle de performance

## Sous-systèmes Environnement

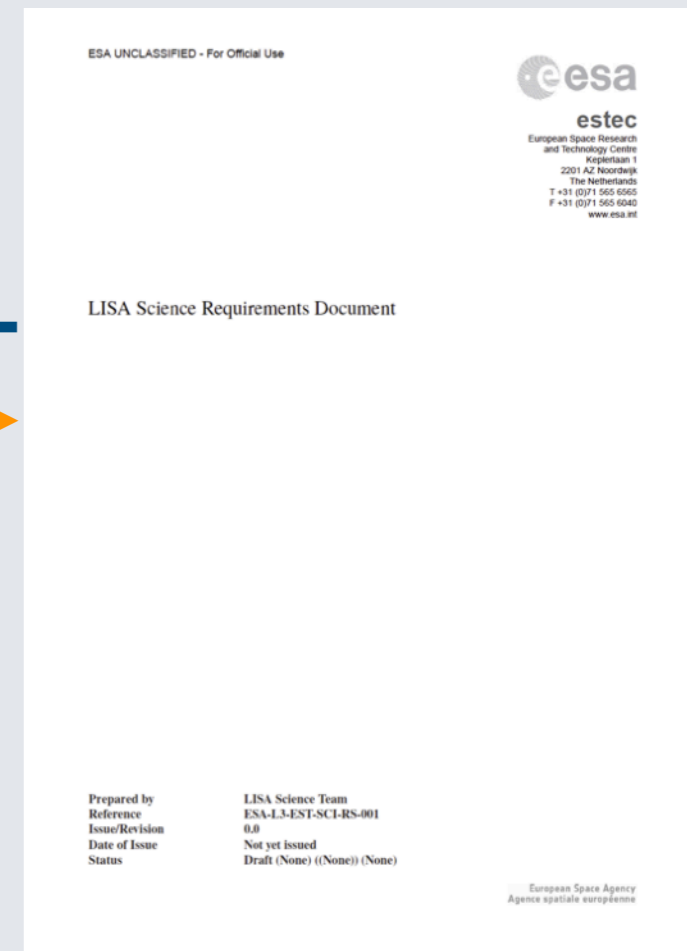
- Stabilité température
- Stabilité plateforme
- Type de matériaux
- Bruit de la photodiode
- etc...

**CBE : Current Best Estimate**

Modèle quasi-analytique de l'instrument

**Allocation**

## Requirements Scientifiques





October 2020      **Release 1.4 beta - New models/No allocation**

- Stray light main contributors in all IFO's
- SC & MOSA angular jitters coupling to the TM force noise due to SC gravitational imbalance

November 2020      **Data Format & Model sent to primes for interfacing with the performance model**

December 2020      **New « TDI » Performance Model Release (2.0)**

- New TDI 2.0 top level representation
- OMS noises & Test Mass acceleration in TDI variables
- New long arm Tilt-To-Lenght coupling with calibration & drift
- New Laser residuals & Clock residuals and calibration analytical models

January 2020      **Update Release 2.0 with « Consortium » allocation tree**



**Produce « primes » version(s) of the Performance Model**

Spring 2021      **New performance Model Release (2.1)**

- TDI consolidation
- TDI XY
- DWS & Phasemeter
- ... [TBD]

# Structure

## INPUTS

Multiple versions  
Nominal/Cold/Hot

*Constants*

*Parameters*

*Noise Sources*

*Transfer Functions*

## MODELS

LISA  
Performance  
Model  
*[Sum square  
Linear Sum  
Math Formula]*

- Derived Parameters
- Derived Noises
- Derived Transfer Functions
- Reference Noises

## PRODUCTS

- Performance Tree
- Noise Power Spectrum Density
  - CBE breakdown
  - Allocation vs CBE

# Structure: Test Mass IFO Electronic Noise

## INPUTS

```

'Noises' :
  • TMI equivalent input current noise density of the electronics
    description : Equivalent input current noise density of the electronics
    type : Source Noise
    varname : s_I_seg_el_tmi

'Parameters' :
  • lambda = 1.064e-06 [[m]]
    description : Laser wavelength
    documentation :

  • N_pd_TM = 4.0 [[]]
    description : Number of photoreceivers for the TM IFO
    documentation :

  • N_seg_TM = 4.0 [[]]
    description : Number of segments per photoreceiver in the TM IFO
    documentation :

  • eta_car = 0.81 [[]]
    description : RX power in main carrier signal
    documentation :

  • R_pd = 0.69 [[A W^(-1)]]
    description : Responsivity of InGaAs
    documentation :

  • HE_loc = 0.82 [[]]
    description : Heterodyne Efficiency in a Local IFO
    documentation :

  • P_LO_TM = 5e-06 [[W]]
    description : Local Oscillator power at the photo-receiver input
    documentation : [Optical Power budget, LISA-UKOB-INST-RP-001]

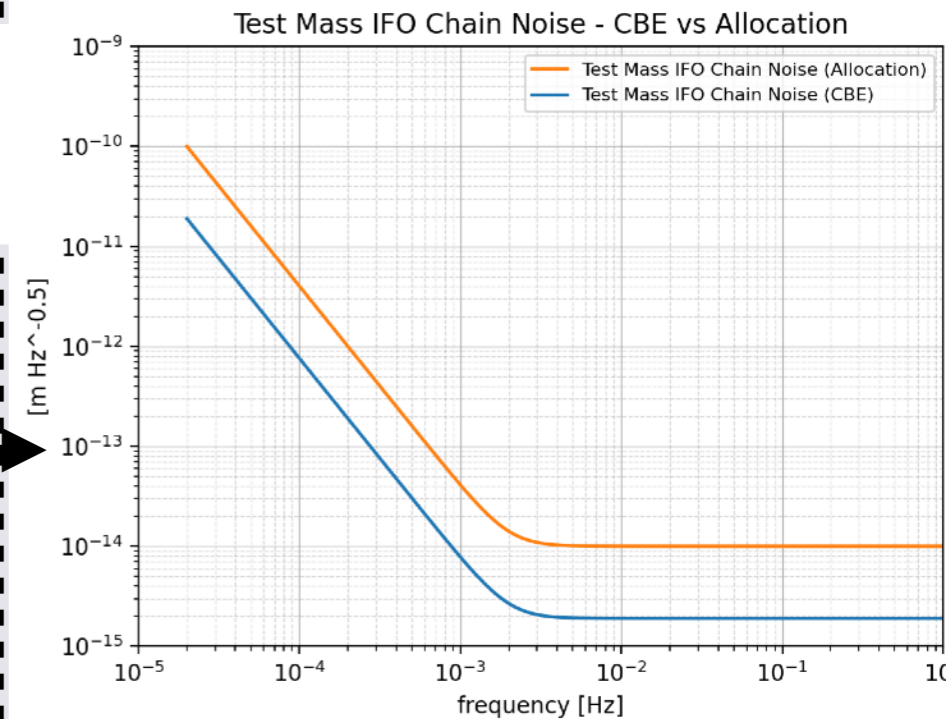
  • P_TX_TM = 0.001 [[W]]
    description : TX-beam fraction impinging at the photo-receiver input
    documentation : [Optical Power budget, LISA-UKOB-INST-RP-001]
  
```

## MODEL

Derived Noise

$$\tilde{S}_{\text{TMI,Chain}} = \frac{\lambda}{2\pi} \frac{\tilde{S}_{I_{\text{seg,el}}} \sqrt{N_{\text{Seg,Loc}} \cdot N_{\text{PD,Loc}}}}{R_{\text{PD}} \epsilon_{\text{Carr}} \sqrt{2\eta_{\text{het,Loc}} P_{\text{LO,TM}} P_{\text{TX,TM}}}}$$

## PRODUCTS



# Structure: Long Arm Waveplates Thermoelastic

## INPUTS

'Noises' :

- **OB Temperature Stability** [K<sup>2</sup> Hz<sup>-1</sup>]  
*description* : This applies to the entire OB basep: optical path.  
*type* : Source Noise  
*varname* : S\_T\_OB

'constants' :

- **FOM\_Qtz** =  [[K<sup>(-1)</sup>]]  
*description* : Thermal OPD change of Crystal Quartz

'Parameters' :

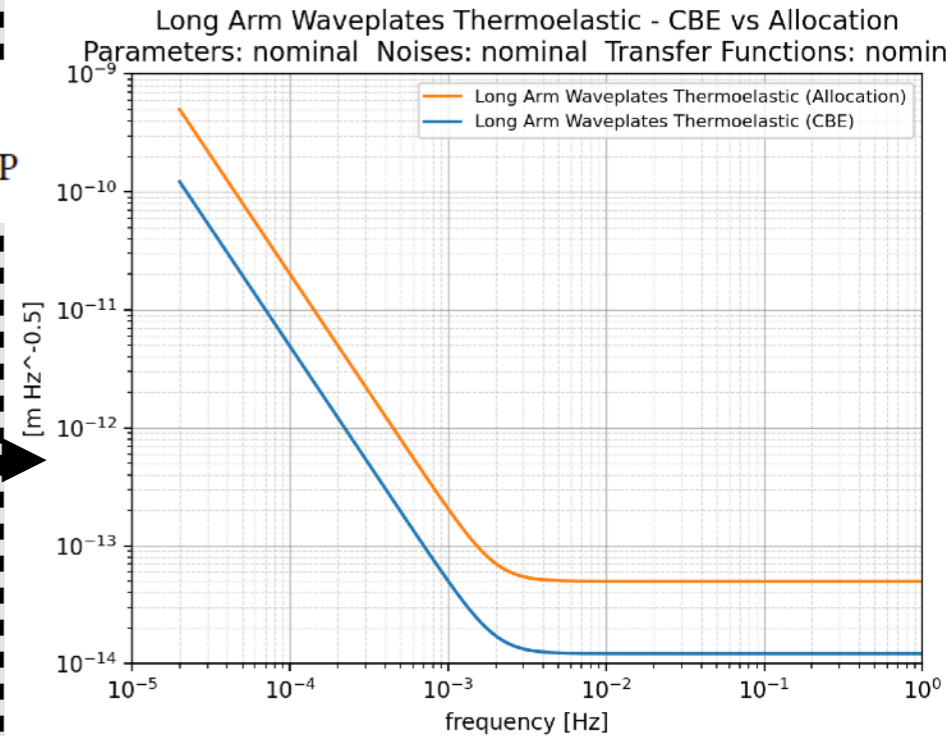
- **D\_wp** =  [[m]]  
*description* : Thickness of a waveplate  
*documentation* :
- **N\_WP\_LA** =  []  
*description* : Number of differential transmission arm interferometer.  
*documentation* :

## MODEL

Derived Noise

$$\tilde{S}_{\text{Therm,LA,WP}} = \text{FOM}_{\text{Qtz}} \cdot \tilde{S}_{\text{TOB}} \cdot N_{\text{WP,LA}} \cdot D_{\text{WP}}$$

## PRODUCTS



# INPUTS

# MODEL

# PRODUCTS

Matlab

Python or  
Matlab Reader

Multiple versions  
Nominal/Cold/Hot

*Constants*

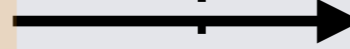
*Parameters*

*Noise Sources*

*Transfer Functions*



LISA  
Performance  
Model



- Performance Tree
- Noise Power Spectrum Density
  - CBE breakdown
  - Allocation vs CBE

- Derived Parameters
- Derived Noises
- Derived Transfer Functions
- Reference Noises

Model w/o  
values

Model with  
values

22 Matlab  
Generator  
Scripts

200 NSDF  
files (xml)

4 csv files

png -plots  
png- graphs  
DataFile



Technical Note



# Parameters - CSV files

LISA\_PerfModel\_Parameters

name	description	unit	documentation	allocation	nominal	cold	hot
lambda	Laser wavelength	[m]		1.064E-06	1.064E-06	1.064E-06	
L_arm	Arm Length	[m]		2500000000	2500000000	2500000000	
D_tel	Telescope Diameter (clear aperture)	[m]		0.300000000000000000	0.300000000000000000	0.300000000000000000	0
P_L	Laser Power from MOPA	[W]		2	2	2	
R12	Vector from TM1 to Tm2	[m]		0.420000000000000000	0.420000000000000000	0.420000000000000000	0
L_MSS	Effective length of MSS	[m]	[LISA-ADSF-INS	0.300000000000000000	0.300000000000000000	0.300000000000000000	0
R_pd	Responsivity of InGaAs	[A W <sup>(-1)</sup> ]		0.690000000000000000	0.690000000000000000	0.690000000000000000	0
D_pd	QPD Diameter	[m]		0.001	0.001	0.001	
TMsize	TestMass size	[m]		0.046000000000000000	0.046000000000000000	0.046000000000000000	0.0
TMmass	TestMass mass	[kg]		1.930000000000000000	1.930000000000000000	1.930000000000000000	
VacuumPressure	Vacuum Enclosure Pressure	[Pa]		1E-06	1E-06	1E-06	
T_GRS	GRS Temperature	[K]		293	293	293	
alphanoise	Noise amplification factor	[]		13	13	13	
DCX_DX_GRS1	Cx to TM derivative with respect to x for GRS1	[F m <sup>(-1)</sup> ]		2.91385358345786E-10	2.91385358345786E-10	2.91385358345786E-10	2.9
DCXH_DX_GRS1	Cx to EH derivative with respect to x for GRS1	[F m <sup>(-1)</sup> ]		-6.96752395467991E-11	-6.96752395467991E-11	-6.96752395467991E-11	-6.9
CEL_GRS1	Total TM to electrodes capacitance for GRS1	[F]		1.53958921869247E-11	1.53958921869247E-11	1.53958921869247E-11	1.5
CTOT	Total TM capacitance	[F]		3.42E-11	3.42E-11	3.42E-11	
D2CTOT_DX2_GRS1	Total TM to ground capacitance second derivative with respect to x <sup>2</sup> for C	[F m <sup>(-2)</sup> ]		1.36515242625754E-06	1.36515242625754E-06	1.36515242625754E-06	1.3
R_star	Electrodes Effective Armlength between x-face electrodes	[m]		0.033000000000000000	0.033000000000000000	0.033000000000000000	0.0
eta_car	RX power in main carrier signal	[]		0.810000000000000000	0.810000000000000000	0.810000000000000000	0
HE_la	Heterodyne Efficiency in the Long Arm IFO	[]		0.75	0.75	0.75	
HE_loc	Heterodyne Efficiency in a Local IFO	[]		0.820000000000000000	0.820000000000000000	0.820000000000000000	0
eta_fibre	Optical efficiency of the OB feed fibres (insertion loss of 0.3 dB)	[]		0.933000000000000000	0.933000000000000000	0.933000000000000000	0
eta_fios	Optical efficiency of the OB FIOS (loss at FIOS PBS + output polariser	[]		0.956938384000000000	0.956938384000000000	0.956938384000000000	0
eta_OB_TX	Optical Efficiency of the OB TX Path	[]		0.941417218	0.941417218	0.941417218	
eta_Tel_TX	Optical Efficiency of the Telescope TX Path	[]		0.947152849000000000	0.947152849000000000	0.947152849000000000	0
alpha_fact	Optimum transmission factor for gaussian beam through two apertures.	[]		0.40726436345010700	0.40726436345010700	0.40726436345010700	0
eta_Tel_RX	Optical Efficiency of the Telescope RX Path	[]		0.813666809000000000	0.813666809000000000	0.813666809000000000	0
eta_OB_RX	Optical Efficiency of the OB RX Path up to Long Arm QPDs	[]		0.779871202000000000	0.779871202000000000	0.779871202000000000	0

# Parameters - CSV files

LISA\_PerfModel\_Parameters

<b>D_ob</b>	Characteristic scale of the OB for path stability	[m]		1	1
<b>D_ob_grs</b>	Dimension between GRS and OB	[m]		0.25	0.25
<b>D_path</b>	Possible path mismatch error on OB	[m]		1	1
<b>D_comp_tol</b>	Tolerance on the thickness of a Beam Splitter	[m]		0.0001	0.0001
<b>D_mir</b>	One Mirror Thickness	[m]		0.008	0.008
<b>D_win</b>	Thickness of the Optical Window on the GRS	[m]		0.00635	0.00635
<b>D_wp</b>	Thickness of a waveplate	[m]		0.001	0.001
<b>D_paam</b>	Offset from PAAM mount to reference mirror	[m]		0.007	0.007
<b>C_RX</b>	Total Rx TTL Coupling Factor	[m rad <sup>(-1)</sup> ]		0.005	0.005
<b>C_TX</b>	Total Tx TTL Coupling Factor	[m rad <sup>(-1)</sup> ]		0.004	0.004
<b>C_TM</b>	Total TM TTL Coupling Factor	[m rad <sup>(-1)</sup> ]		4E-05	4E-05
<b>TTL_Cal</b>	TTL Calibration Accuracy	[]		1	1
<b>los</b>	Alignment tolerance between TM Normal and RX Direction	[rad]		7E-05	7E-05
<b>CTE_MSS_OBTel</b>	Coefficient of thermal expansion of the MSS averaged over the structural material	[K <sup>(-1)</sup> ]		9E-06	9E-06
<b>dx_sc_pp</b>	Residual SC Translation Per Axis. Infer from LPF o1 measurement	[m]		1E-08	1E-08
<b>dL</b>	Expected Ranging Bias	m		1	0.1
<b>L_dot</b>	Average SC speed	m s <sup>(-1)</sup>		8	8
<b>kF</b>	Anti-aliasing filter property	Hz <sup>(-2)</sup>	This is an approximation shape at	3.38.*f.^2	3.38.*f.^2
<b>fhet</b>	Maximal beatnote frequency	Hz		25000000	25000000
<b>fmod</b>	Modulation frequency	Hz		2400000000	2400000000
<b>P_incidentTM</b>	laser power incident on the TM	W		0.001	0.001
<b>T_OB</b>	Optical Bench Temperature	K		293	293
<b>D_hole</b>	laser hole diameter on the EH +X face	m		0.006	0.006
<b>epsilon</b>	TM reflectivity			1	1
<b>dg_dT_mean</b>	Electro-Housing mean temperature fluctuation coupling coefficient to differential	m s <sup>(-2)</sup> K <sup>(-1)</sup>	Measured at the end of LPF missile	1E-12	1E-12
<b>dg_dDT</b>	Electro-Housing temperature gradient fluctuation coupling coefficient to differential	m s <sup>(-2)</sup> K <sup>(-1)</sup>		2E-11	2E-11
<b>omegasquarexx</b>	Test Mass x-axis stiffness	s <sup>(-2)</sup>		-8E-07	-8E-07
<b>omegasquareGRSxx</b>	Test Mass x-axis stiffness due to GRS	s <sup>(-2)</sup>		-7E-07	-7E-07
<b>omegaxsquare</b>	TestMass y to x cross-stiffness	s <sup>(-2)</sup>		-6E-08	-6E-08
<b>omegaxzsquare</b>	TestMass z to x cross-stiffness	s <sup>(-2)</sup>		-6E-08	-6E-08
<b>omegaxphisquare</b>	TestMass phi to x cross-stiffness	m/s <sup>(2)</sup>		-1.012E-09	-1.012E-09
<b>omegaxetasquare</b>	TestMass eta to x cross-stiffness	m/s <sup>(2)</sup>		-4.6E-10	-4.6E-10
<b>omegaxthetasquare</b>	TestMass theta to x cross-stiffness	m/s <sup>(2)</sup>		-4.6E-10	-4.6E-10

# Noise Sources - CSV files

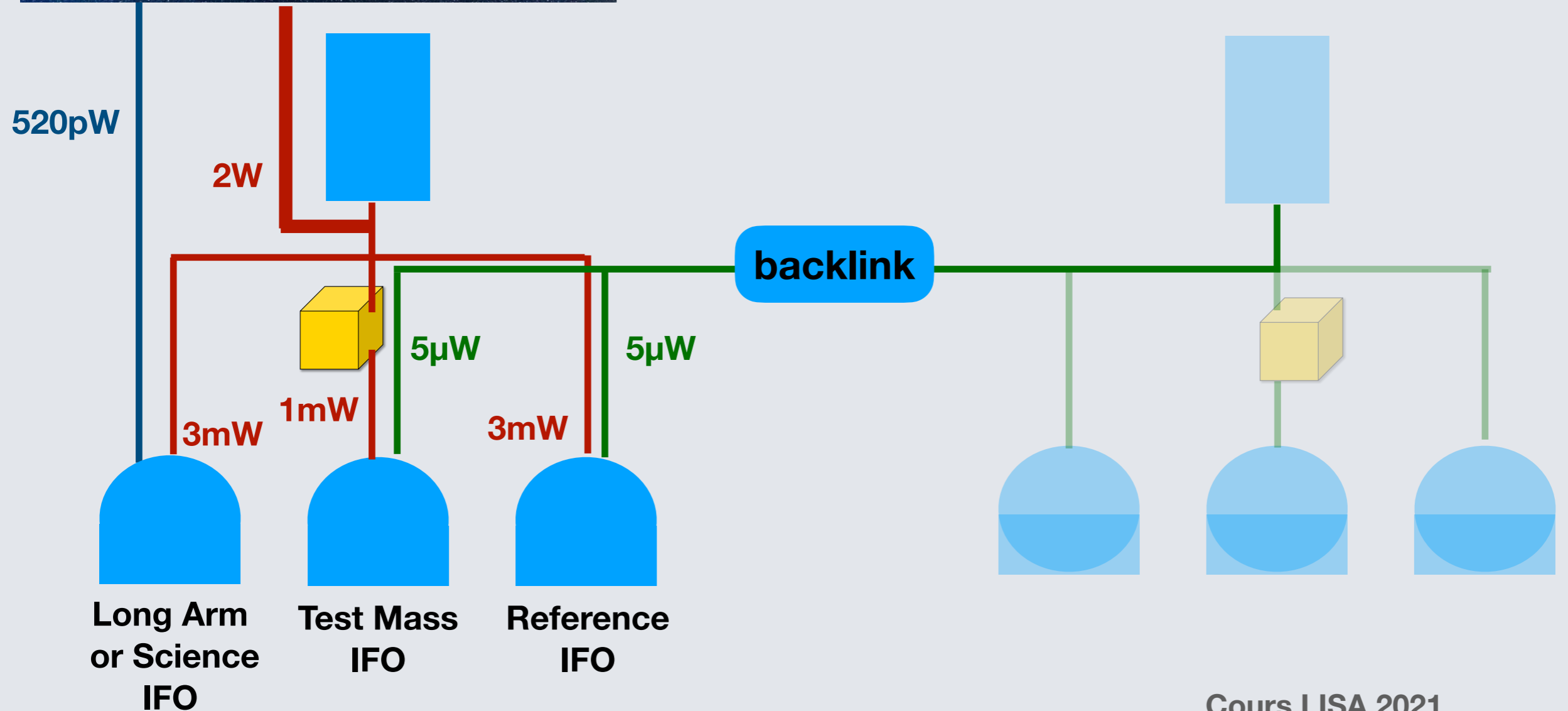
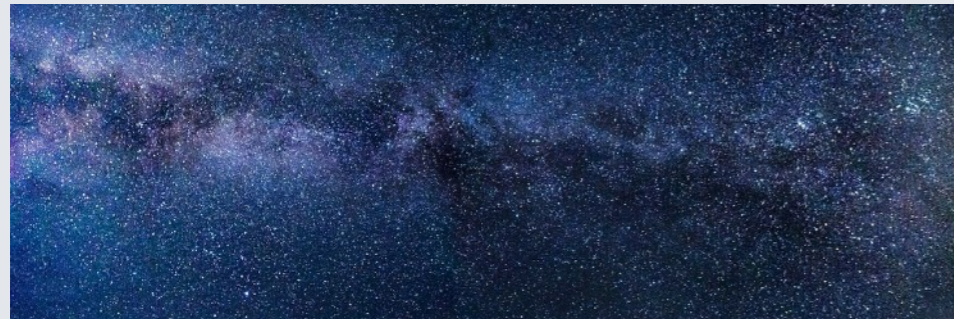
LISA\_PerfModel\_NoiseInputs

name	type	varname	description	documentation	unit	allocation
<b>TMI equivalent input current noise density of the electrode</b>	Source Noise	s_l_seg_el_tmi	Equivalent input current noise	Value from GSFC measurements	A Hz <sup>-0.5</sup>	$3.5E-12 \cdot \sqrt{1+(2E-3/f)^4}$
<b>LA equivalent input current noise density of the electrode</b>	Source Noise	s_l_seg_el_LA	Equivalent input current noise	Value from GSFC measurements	A Hz <sup>-0.5</sup>	$3.5E-12 \cdot \sqrt{1+(2E-3/f)^4}$
<b>Long Arm PMS</b>	Source Noise	longArmPmsNoise	Apparent displacement noise	Currently these are both top	m Hz <sup>-0.5</sup>	$2E-12 \cdot \sqrt{1+(2E-3/f)^4}$
<b>Test Mass IFO PMS</b>	Source Noise	tmiPmsNoise	Apparent displacement noise	For now these are both top	m Hz <sup>-0.5</sup>	$1E-12 \cdot \sqrt{1+(2E-3/f)^4}$
<b>Laser Frequency Stability</b>	Source Noise	laserFreqStab	The required laser frequency stability	SCI-F ESA ESA-LISA-EST-I	Hz Hz <sup>-0.5</sup>	$30 \cdot \sqrt{1+(2E-3/f)^4}$
<b>Reference PMS</b>	Source Noise	refPmsNoise	Apparent displacement noise	For now these are both top	m Hz <sup>-0.5</sup>	$1E-12 \cdot \sqrt{1+(2E-3/f)^4}$
<b>REF equivalent input current noise density of the electrode</b>	Source Noise	s_l_seg_el_ref	Equivalent input current noise	Value from GSFC measurements	A Hz <sup>-0.5</sup>	$3.5E-12 \cdot \sqrt{1+(2E-3/f)^4}$
<b>MSS Temperature Stability</b>	Source Noise	S_T_MSS	This applies to the element	This applies to the elements	K <sup>2</sup> Hz <sup>-1</sup>	$(10e-6)^2 \cdot (1+(2e-3/f)^4)$
<b>OB Temperature Stability</b>	Source Noise	S_T_OB	This applies to the element	Technically we could allow	K <sup>2</sup> Hz <sup>-1</sup>	$(10e-6)^2 \cdot (1+(2e-3/f)^4)$
<b>Telescope Temperature Stability</b>	Source Noise	S_T_Tel	This applies to the entire telescope.		K <sup>2</sup> Hz <sup>-1</sup>	$(10e-6)^2 \cdot (1+(2e-3/f)^4)$
<b>Test Mass temperature stability</b>	Source Noise	S_T_TM	Required stability of the test mass	Since this effects only the C	K <sup>2</sup> Hz <sup>-1</sup>	$(0.25E-6)^2 \cdot (1+(2E-3/f)^4)$
<b>OW temperature stability</b>	Source Noise	S_T_OW	This applies to the OWS	Note that this could be merged	K <sup>2</sup> Hz <sup>-1</sup>	$(10e-6)^2 \cdot (1+(2e-3/f)^4)$
<b>Fibre Temperature Stability</b>	Source Noise	S_T_fibre	Expected fibre temperature stability	eLISA-AEI-PRDS-2019-04-	K <sup>2</sup> Hz <sup>-1</sup>	$(1.4e-3)^2 \cdot (1+(2e-3/f)^4)$
<b>Unmodelled Local Oscillator TTL</b>	Source Noise	thermoRefTTL	Allow for in-band thermal jitter of the local oscillator		m Hz <sup>-0.5</sup>	$0.1e-12 \cdot \sqrt{1+(2E-3/f)^4}$
<b>mean temperature fluctuations of the GRS head</b>	Source Noise	S_T_GRS	Assumed levels of mean temperature fluctuations	Currently an allocation only	K <sup>2</sup> Hz <sup>-1</sup>	$(43e-6)^2 \cdot (100e-6/f)^7 + (5e-6)^2$
<b>temperature difference fluctuations across the Electrode</b>	Source Noise	S_DT_EH	Assumed levels of temperature difference fluctuations	Currently an allocation only	K <sup>2</sup> Hz <sup>-1</sup>	$(1e-5)^2 \cdot (1e-4/f)^4 + (5e-6)^2$
<b>mean temperature fluctuations as seen by the TM through the GRS</b>	Source Noise	S_T_TM_VIEW	Assumed levels of mean temperature fluctuations	Currently an allocation only	K <sup>2</sup> Hz <sup>-1</sup>	$(1e-3)^2 \cdot (1e-4/f)^3 + (5e-6)^2$
<b>Test Mass DWS Noise</b>	Source Noise	s_DWS_Loc	Local or Test Mass Drift	Currently an allocation only	rad Hz <sup>-0.5</sup>	$5E-9 \cdot \sqrt{1+(0.7E-3/f)^4}$
<b>Jitter y TM wrt MOSA</b>	Source Noise	Sy_tm	TestMass Jitter along y with respect to MOSA		m <sup>2</sup> Hz <sup>-1</sup>	$(5e-9)^2 \cdot (1 + (1e-3/f)) \cdot (1 + (f/8e-3)^4) / (1 + (f/8e-3)^4)$
<b>Jitter z TM wrt MOSA</b>	Source Noise	Sz_tm	TestMass Jitter along z	Currently an allocation only	m <sup>2</sup> Hz <sup>-1</sup>	$(5e-9)^2 \cdot (1 + (1e-3/f)) \cdot (1 + (f/8e-3)^4) / (1 + (f/8e-3)^4)$
<b>Jitter x TM wrt MOSA</b>	Source Noise	Sx_tm	TestMass Jitter along x	Currently an allocation only	m <sup>2</sup> Hz <sup>-1</sup>	$(0.95e-9)^2 \cdot (1 + (2e-4/f)^2) \cdot (1 + (f/8e-3)^4) / (1 + (f/8e-3)^4)$
<b>Jitter x TM wrt GRS</b>	Source Noise	S_x_GRS	GRS-OB baseline drift	Currently an allocation only	m <sup>2</sup> Hz <sup>-1</sup>	$(0.3e-9)^2 \cdot (1 + (1.5e-3/f)^2)$
<b>Jitter phi TM wrt MOSA</b>	Source Noise	S_phi_grs	Tm phi angular jitter	Currently an allocation only	rad <sup>2</sup> Hz <sup>-1</sup>	$(10e-9)^2 \cdot (1 + (5e-4/f)^4 + (2e-3/f)^2)$
<b>Jitter eta TM wrt MOSA</b>	Source Noise	S_eta_grs	TM eta angular jitter	Currently an allocation only	rad <sup>2</sup> Hz <sup>-1</sup>	$(10e-9)^2 \cdot (1 + (5e-4/f)^4 + (2e-3/f)^2)$
<b>Jitter theta TM wrt MOSA</b>	Source Noise	S_theta_grs	TestMass Jitter along theta	Currently an allocation only	rad <sup>2</sup> Hz <sup>-1</sup>	$(200e-9)^2 \cdot (1 + (1e-3/f))$
<b>Jitter angular S/C wrt IS.</b>	Source Noise	SCang_SC_IS	Residual SC angular jitter	Currently an allocation only	rad Hz <sup>-0.5</sup>	$10E-9 \cdot \sqrt{1+(0.8E-3/f)^4}$
<b>Jitter phi MOSA wrt IS.</b>	Source Noise	MOSA_phi_IS	Residual MOSA jitter	Currently an allocation only	rad Hz <sup>-0.5</sup>	$10E-9 \cdot \sqrt{1+(0.8E-3/f)^4}$
<b>Jitter eta MOSA wrt IS.</b>	Source Noise	MOSA_eta_IS	Residual MOSA jitter	Currently an allocation only	rad Hz <sup>-0.5</sup>	$1E-9 \cdot \sqrt{1+(0.8E-3/f)^4}$
<b>Jitter phi MOSA wrt S/C</b>	Source Noise	sphi_MOSA_SC	Residual MOSA Jitter	Currently an allocation only	rad Hz <sup>-0.5</sup>	$10E-9 \cdot \sqrt{1+(0.8E-3/f)^4}$
<b>Jitter Uncontrolled MOSA wrt S/C</b>	Source Noise	su_MOSA_SC	Residual uncontrolled MOSA jitter	Currently an allocation only	rad Hz <sup>-0.5</sup>	$10E-9 \cdot \sqrt{1+(0.5E-3/f)^4}$



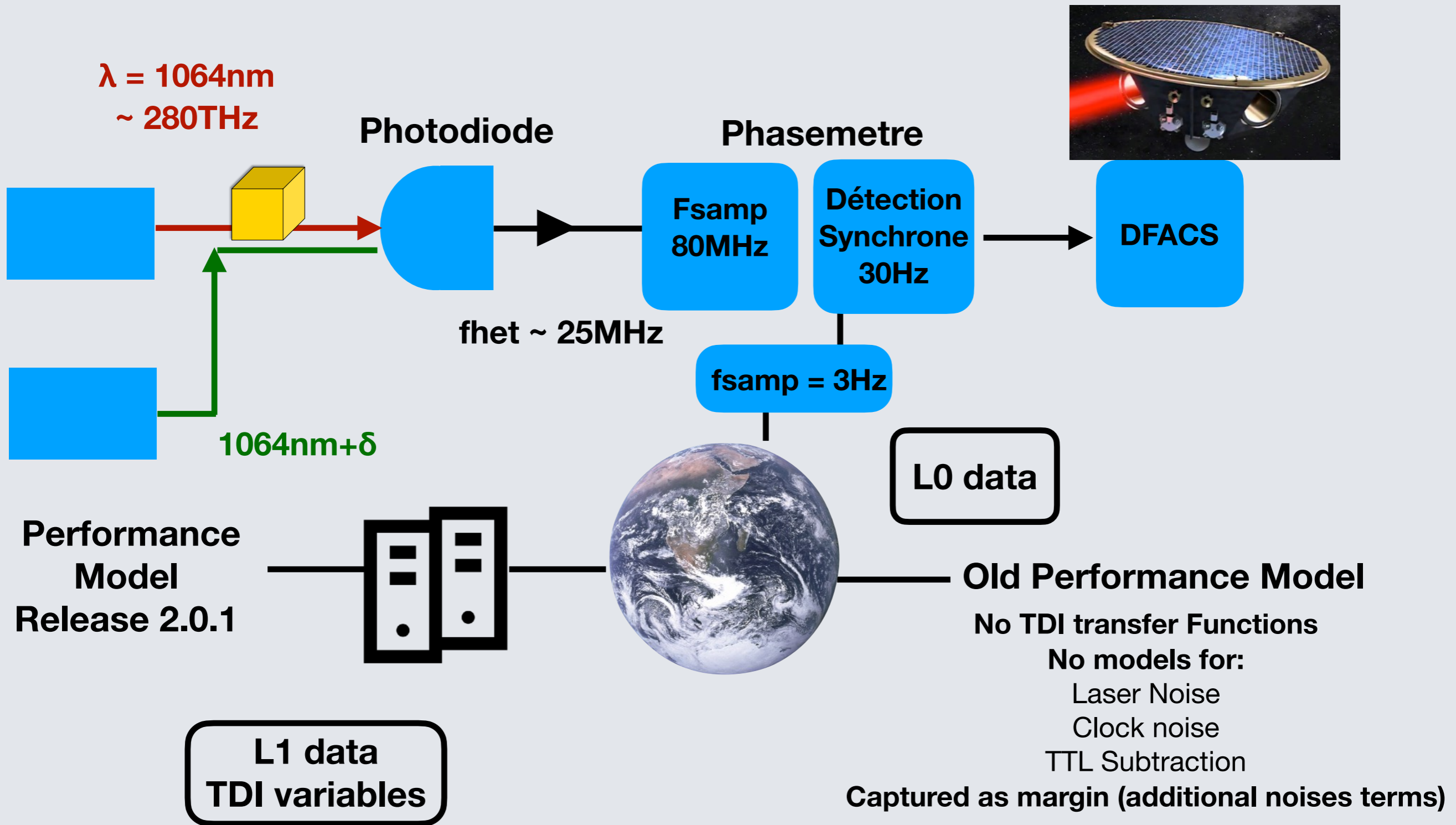
## **II/ Rappels sur la mesure**

# Mesures Généralités



- Reconstruire une mesure Test Mass/Test Mass, on combine les trois interféromètres.
- On considère les MOSA identiques dans le modèle de perf

# Fréquences

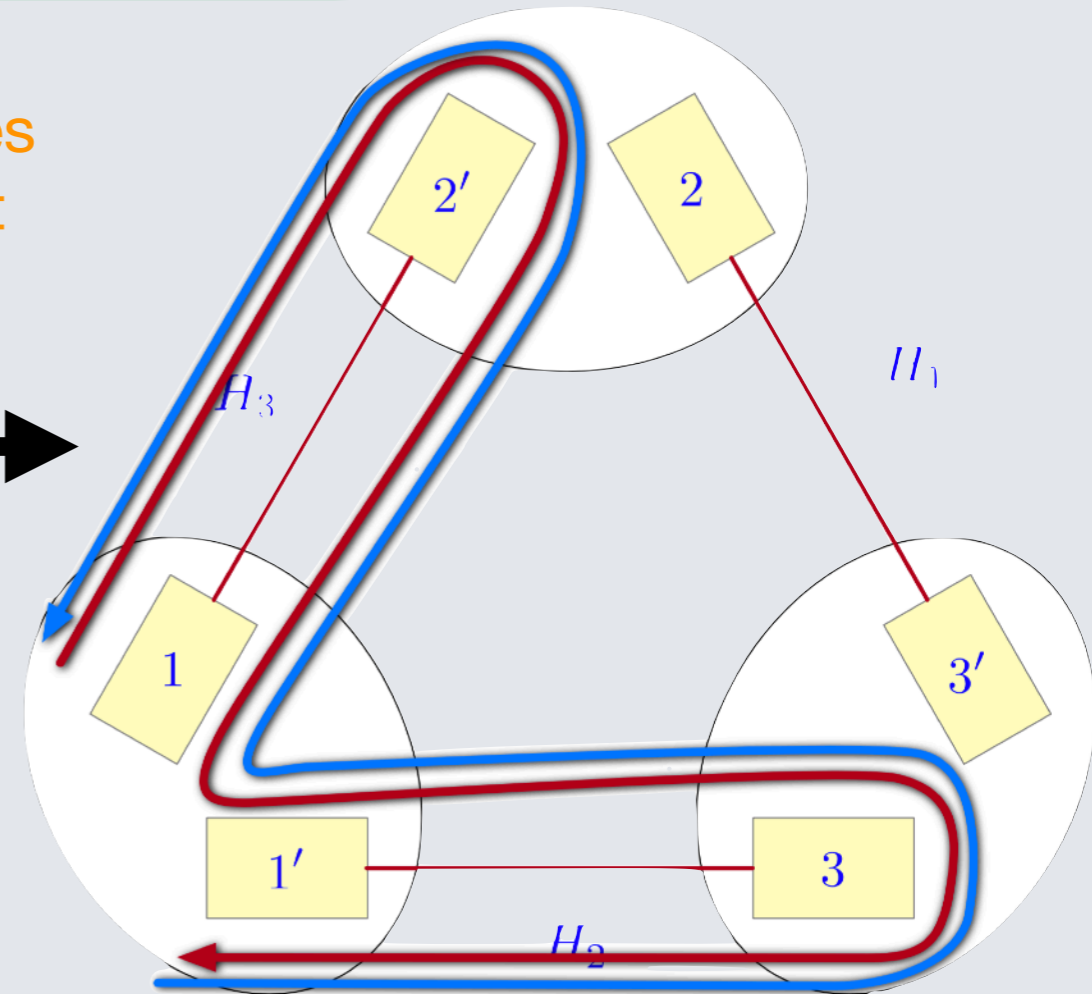


# Time Delay Interferometry

Combinaison d'une mesure long bras et des mesures test masse et référence des bancs 1 et 3. Equivalent mesure test mass/test mass

$$X_{1.5} = \eta'_1 + \mathcal{D}_{2'}\eta_3 + \mathcal{D}_{2'}\mathcal{D}_2\eta_1 + \mathcal{D}_{2'}\mathcal{D}_2\mathcal{D}_3\eta'_2 - \eta_1 - \mathcal{D}_3\eta'_2 - \mathcal{D}_3\mathcal{D}_{3'}\eta'_1 - \mathcal{D}_3\mathcal{D}_{3'}\mathcal{D}_{2'}\eta_3$$

**opérateurs de retard**



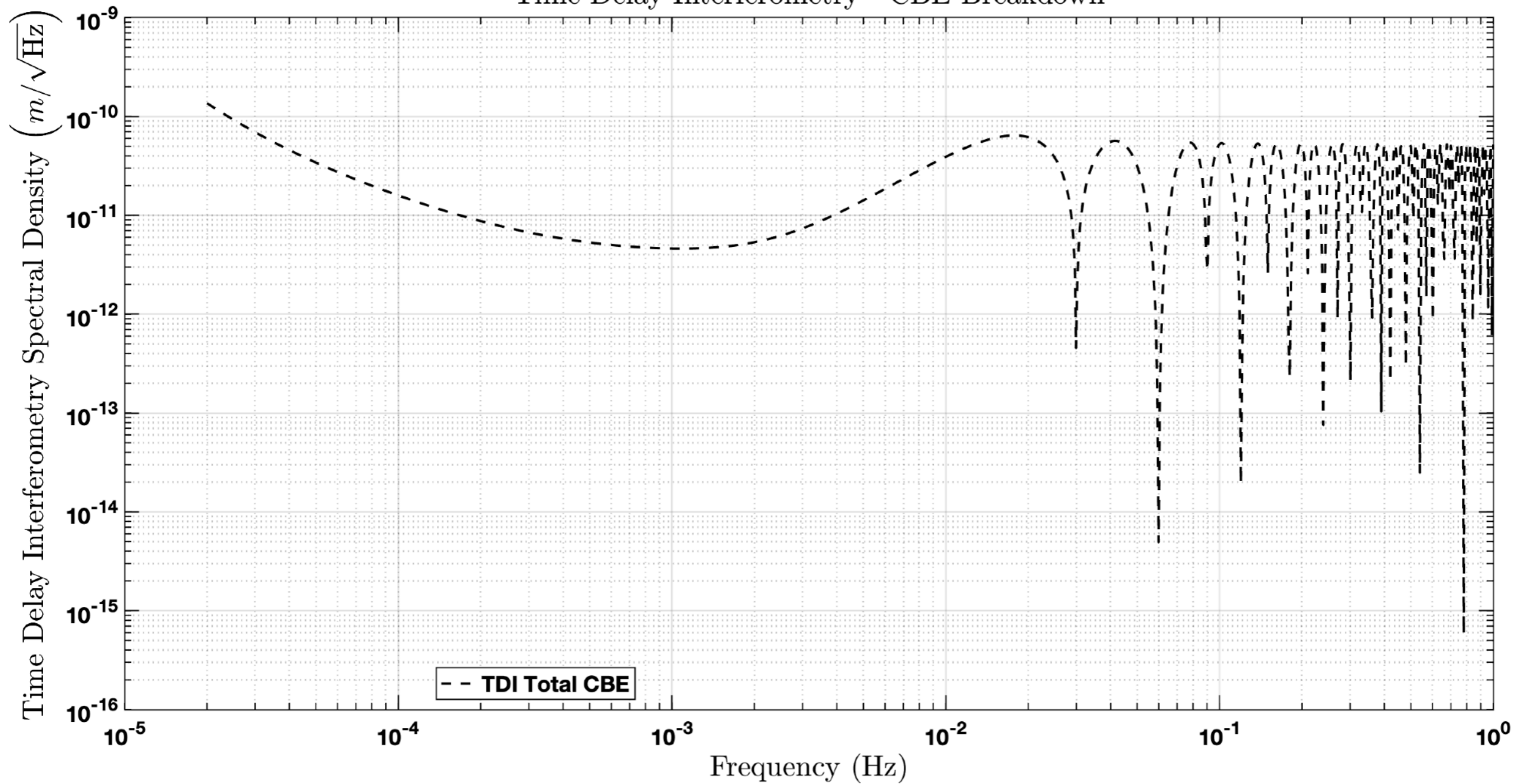
$$PSD_{X_{1.5}} = 16 \sin^2(\omega L) (S_N) + (3 + \cos(2\omega L)) (S_\delta)$$

**Displacement noise**

**Acceleration Noise**

# Budget De Bruit

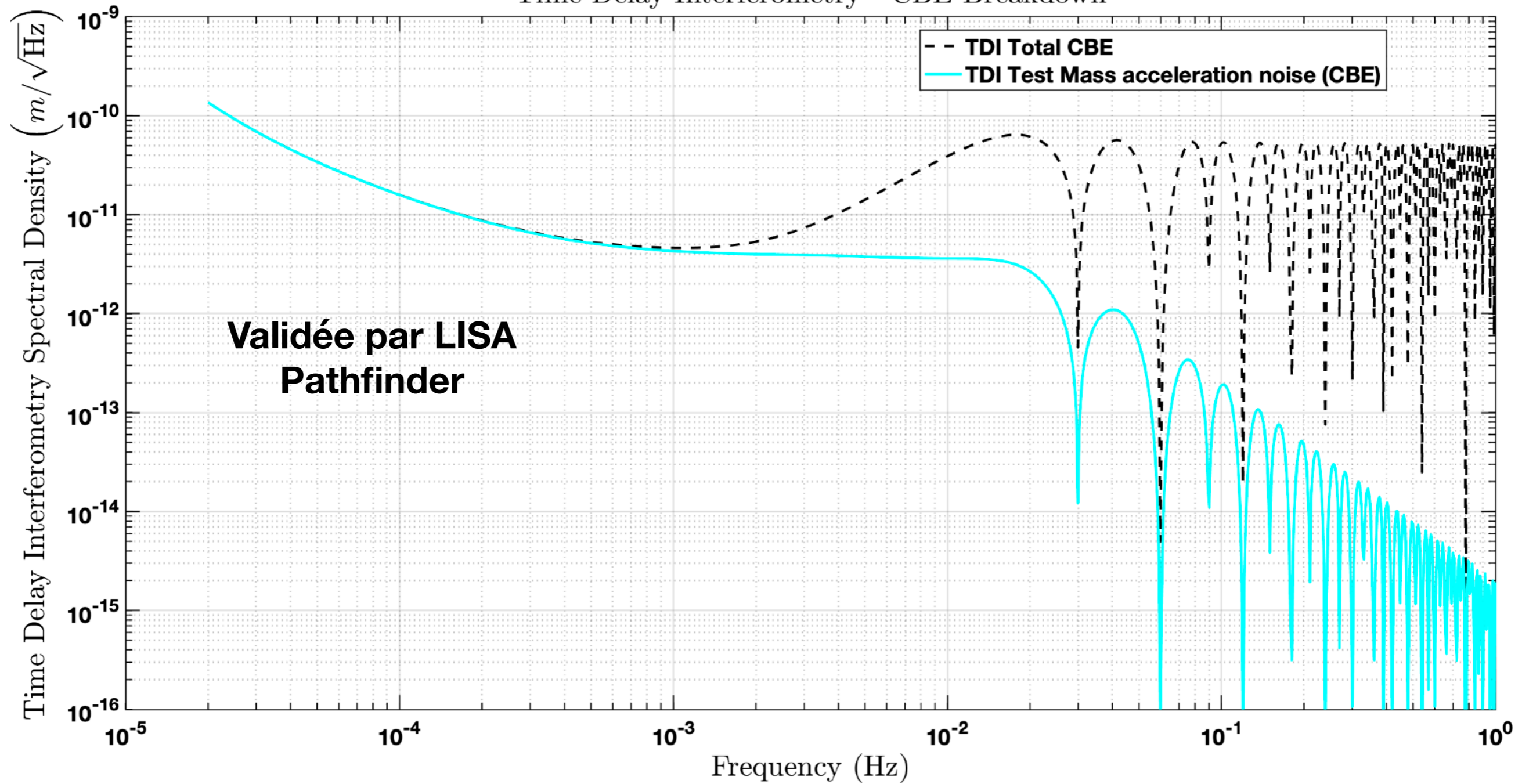
Time Delay Interferometry - CBE Breakdown





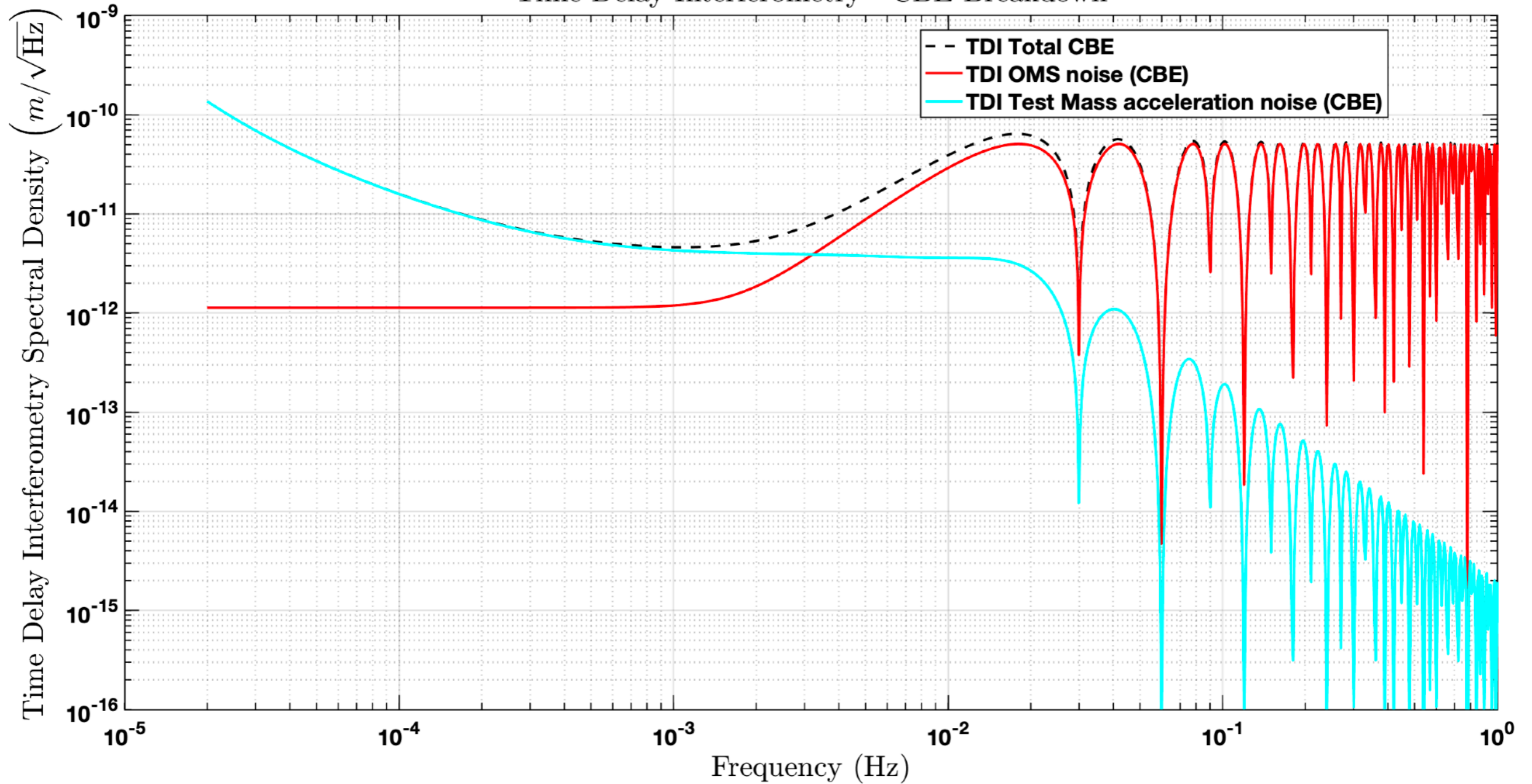
# Budget De Bruit

Time Delay Interferometry - CBE Breakdown

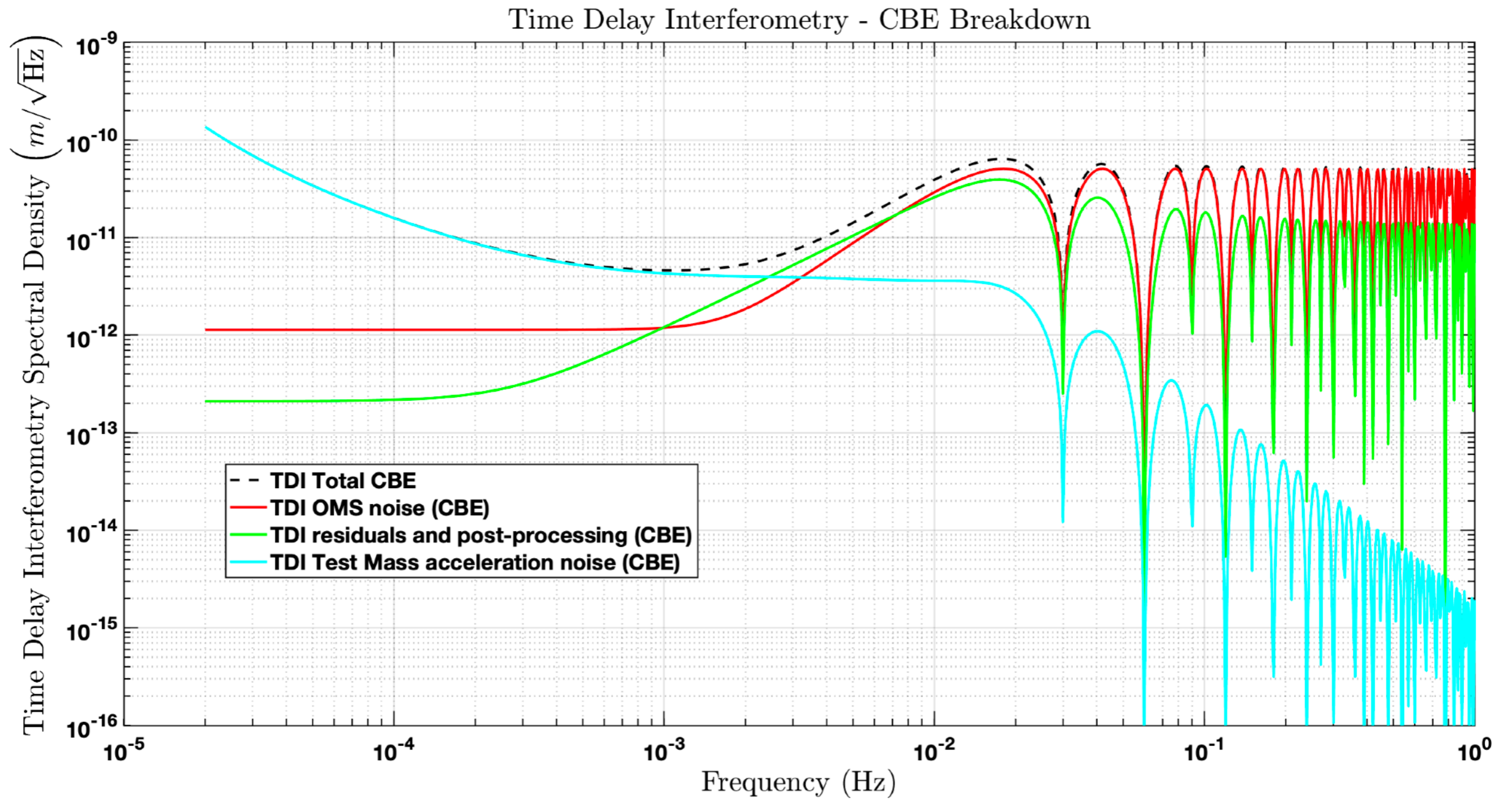


# Budget DE BRUIT

Time Delay Interferometry - CBE Breakdown



# Budget De Bruit





## **III/ Quelques Bruits**

## Optical Metrology System

- Shot Noise
- Backlink stray light
- Telescope Thermo-mechanical noise

# OMS : Shot Noise

- Plus importante source de bruit OMS  $\sim 5\text{pm}/\sqrt{\text{Hz}}$
- Limite « dur » par design - telescope/optique

Bruit en phase [rad/ $\sqrt{\text{Hz}}$ ]  
LISA band (20 $\mu\text{Hz}$  - 1Hz)

Bruit à la fréquence hétérodyne [/ $\sqrt{\text{Hz}}$ ]

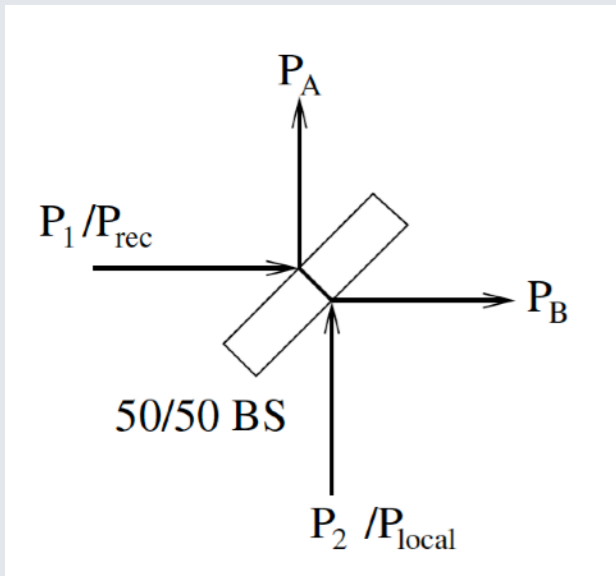
$$\tilde{\varphi} = \frac{1}{C/N_0} = \frac{\tilde{x}}{x_{\text{signal,rms}}},$$

Amplitude de la porteuse à la fréquence hétérodyne  
 $f_{\text{het}}$  (25MHz)

Dérivation des bruits OMS: électronique, RIN, shot noise, phasemètre.

# OMS : Shot Noise

Signal Scientifique



$$P_{A/B} = \frac{1}{2} \left( \overbrace{P_1 + P_2}^{\text{average}} \pm \underbrace{2 \sqrt{\eta_{\text{het}} P_1 P_2}}_{\text{amplitude}} \underbrace{\sin(2\pi f_{\text{het}} t + \varphi)}_{\text{time dependence}} \right)$$

AC term (heterodyne beat note)

**P1 = 3mW**  
**P2 = 520pW**

Heterodyne efficiency

$$P_{sig,rms} = \frac{P_{sig}}{\sqrt{2}} = \sqrt{2} \sqrt{\eta_{\text{het}} P_1 P_2}$$

$$I_{sig,rms} = R_{pd} P_{sig,rms}$$

$R_{pd}$

Responsivity of InGaAs

# OMS : Shot Noise

$$\tilde{I}_{shot} = \sqrt{2q_e R_{pd}(P_1 + P_2)}$$

$$I_{sig,rms} = R_{pd} \sqrt{2} \sqrt{\eta_{het} P_1 P_2}$$

$$\tilde{\phi}_{tot,shot} = \frac{\sqrt{q_e(P_1 + P_2)}}{\sqrt{R_{pd} \eta_{het} P_1 P_2}}$$

**Conversion factor:  
phase to displacement**

$$\tilde{s}_{LA,shot} = \frac{\lambda \sqrt{q_e(P_{Rec} + P_{TX,LA})}}{2\pi \epsilon_{Carr} \sqrt{R_{PD} \eta_{het,LA} P_{Rec} P_{TX,LA}}}$$

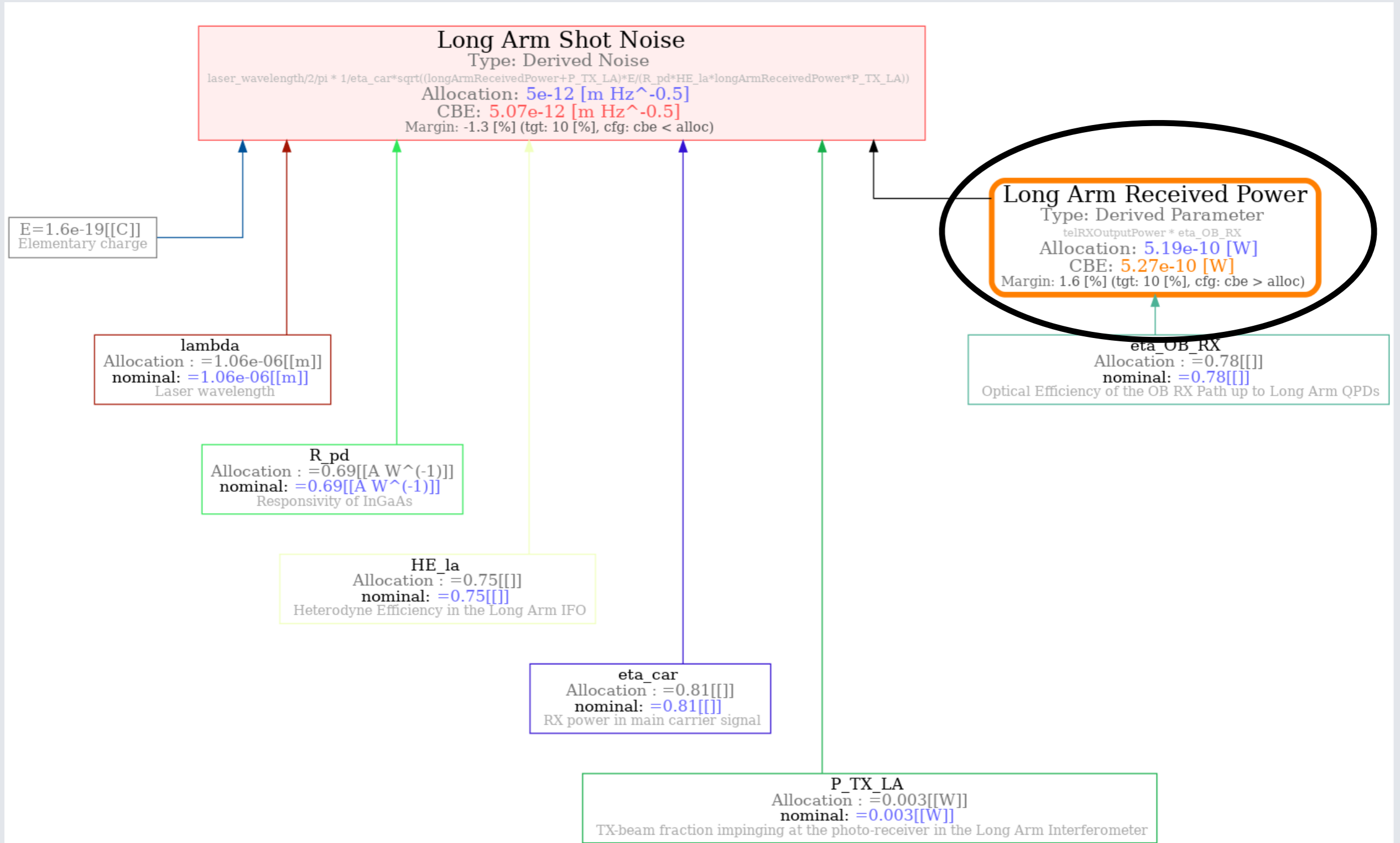
500pW

3mW

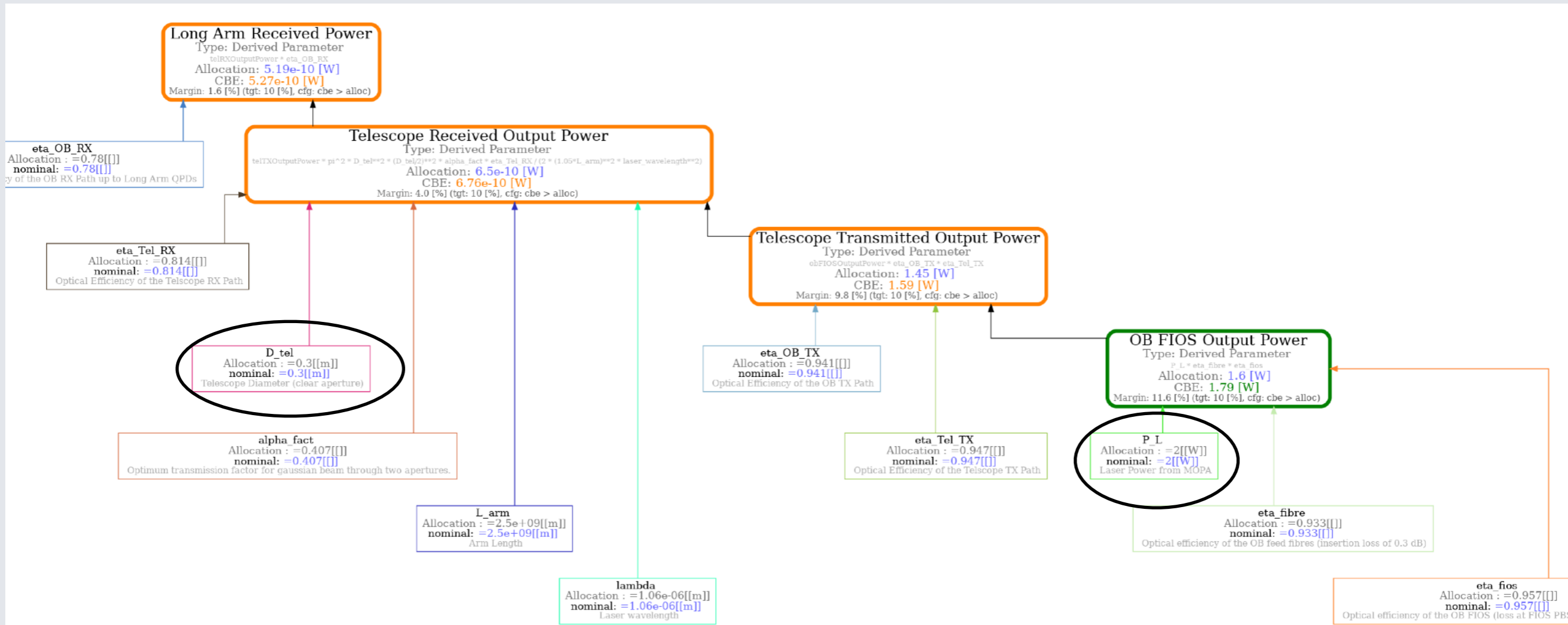
**Shot noise in the  
performance model:  
5pm/√Hz**

**Carrier Efficiency:  
0.8**

# OMS : Shot Noise

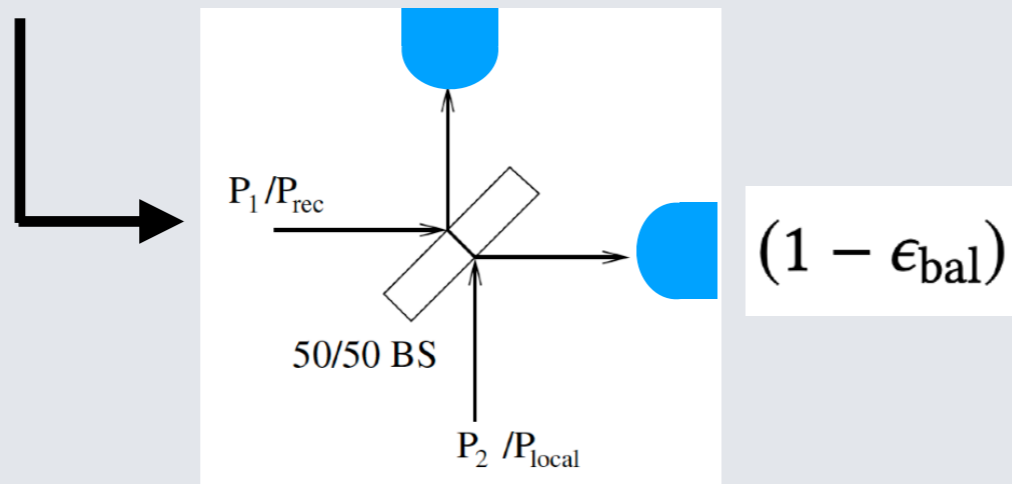
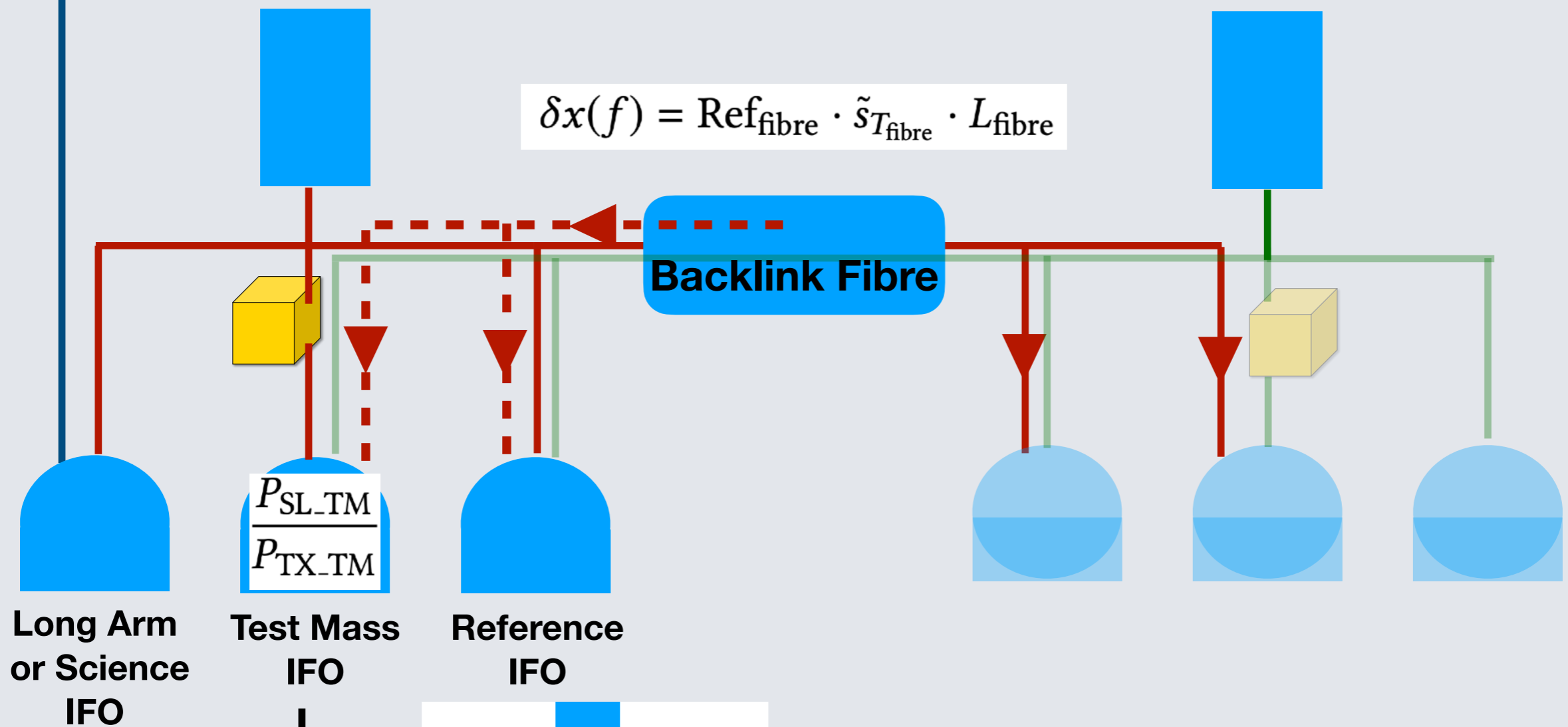
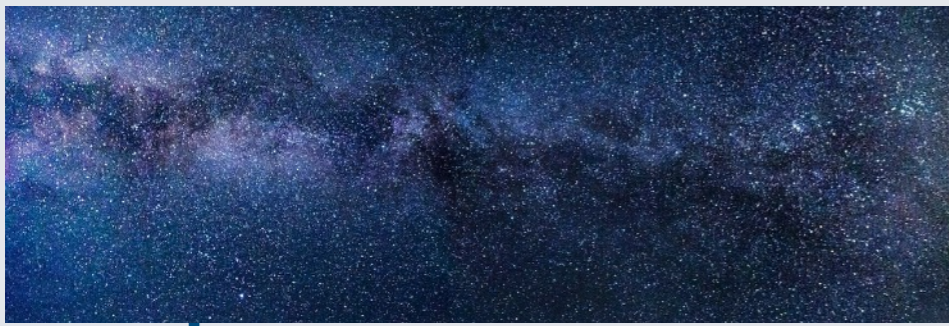


# OMS : Shot Noise



[15] Ewan Fitzsimons. OMS Optical Power Budget. Technical Report LISA-UKOB-INST-RP-001 ,V1.2, UKATC and UGL, 05 2019.

# OMS : Backlink Straylight





# OMS : Backlink Straylight

- LISA-APC-INST-TN-005\_i1.2\_StrayLightToPhase
- LISA-AEI-PRDS-RP-001\_v1\_PRDS\_Fibre\_Irradiation\_Test\_Report
- LISA-AEI-PRDS-TN1-2109
- Optical Power Budget, LISA-UKOB-INST-RP-001

$$\delta x(f) = \text{Ref}_{\text{fibre}} \cdot \tilde{s}_{T_{\text{fibre}}} \cdot L_{\text{fibre}} \cdot$$

OPD noise/kelvin/  
fibre length.  
Measure AEI

Stabilité en température  
de la fibre 1.4mk/sqrt(Hz)

$$\tilde{s}_{\text{TMI, Stray, PRDS}} = \sqrt{\epsilon_{\text{pol, Rayl}} \epsilon_{\text{mod, Rayl}} \frac{P_{\text{SL\_TM}}}{P_{\text{TX\_TM}}} \delta x(f) (1 - \epsilon_{\text{bal}})},$$

Educated  
Guess

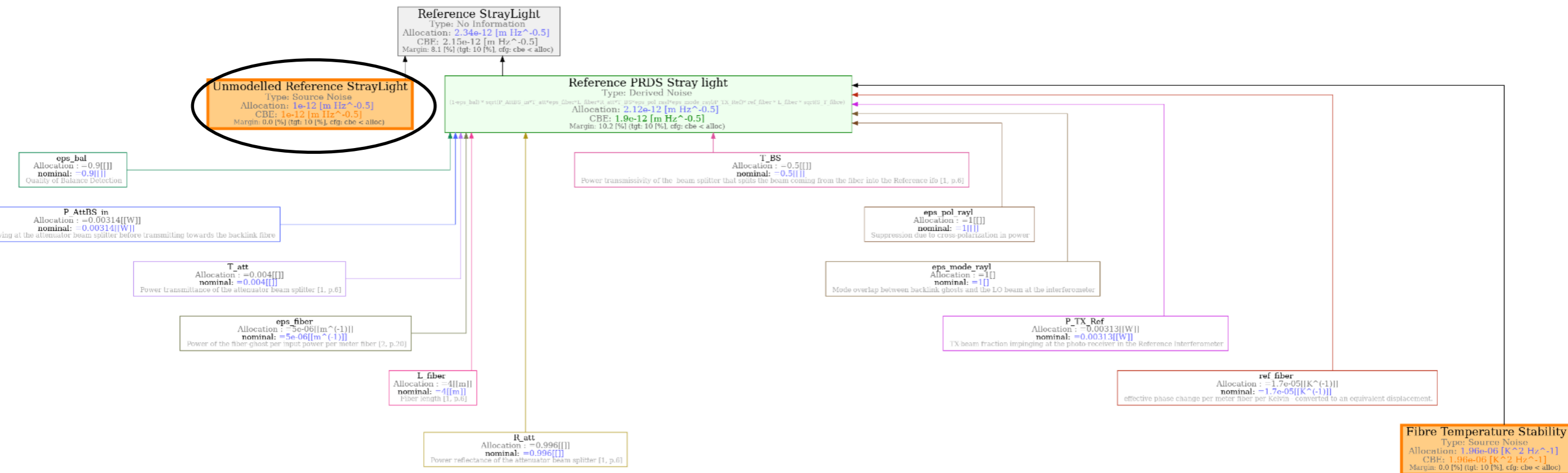
Optical  
bench design

Optical  
Components  
uncertainties = 0.9

- Same contribution in reference IFO
- Dominant source of noise for Test Mass IFO: 3.4 pm/sqrt(Hz) and reference IFO: 2 pm/sqrt(Hz)

# OMS : Backlink Straylight

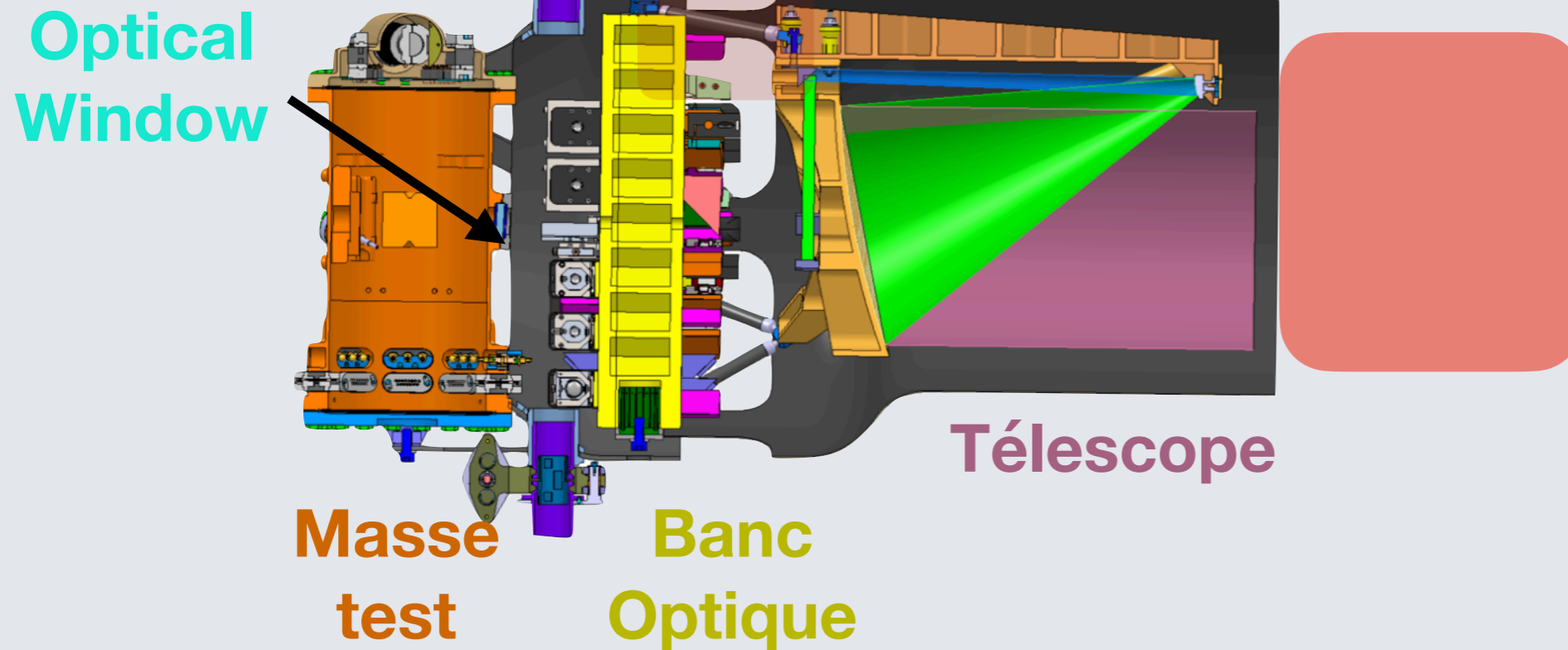
## Source de straylight non modelisées: 1pm/sqrt(Hz)



- LISA-APC-INST-TN-005\_i1.2\_StrayLightToPhase
- LISA-AEI-PRDS-RP-001\_v1\_PRDS\_Fibre\_Irradiation\_Test\_Report
- LISA-AEI-PRDS-TN1-2109
- Optical Power Budget, LISA-UKOB-INST-RP-001

# OMS : Thermal Noises

On définit une température pour chacun des sous-système



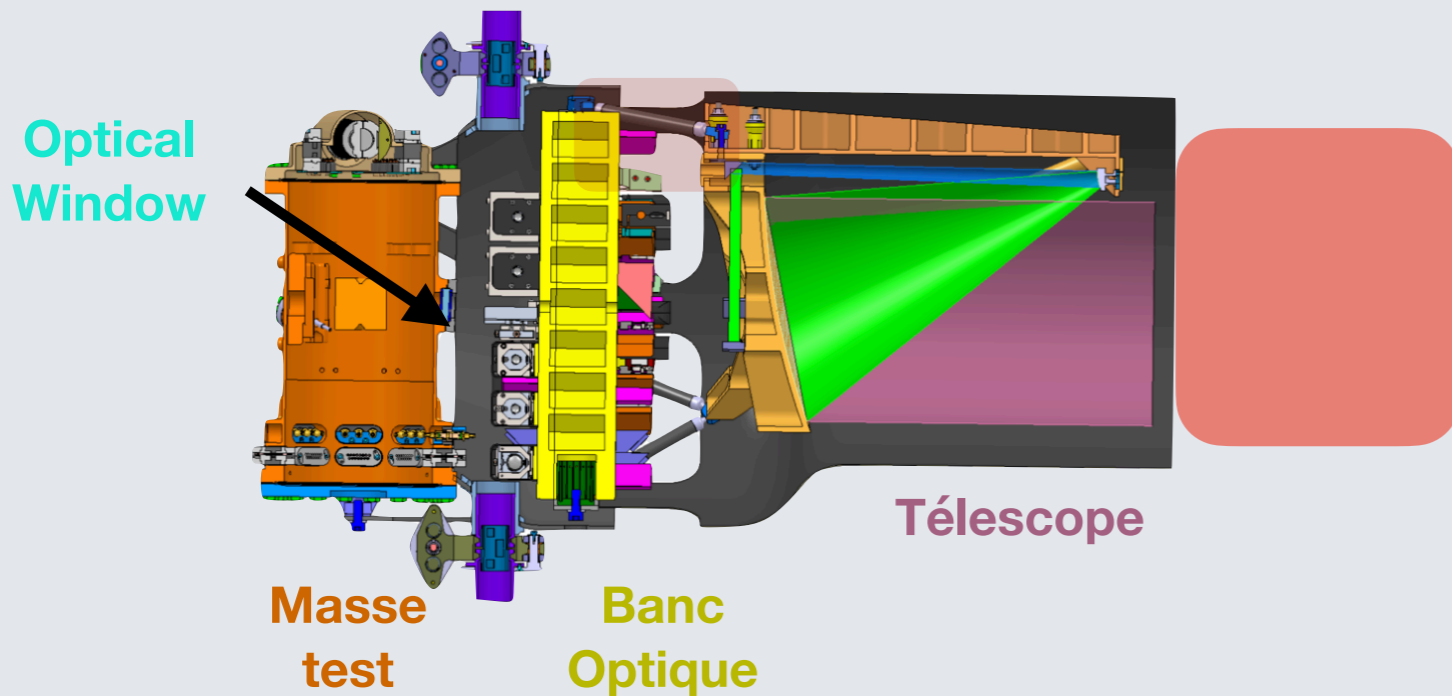
Taille caractéristique du banc optique

$$\tilde{S}_{\text{Therm,OB}} = \alpha_{\text{cte,Zer}} \cdot \tilde{S}_{T_{\text{OB}}} \cdot D_{\text{OB}}$$

Coefficient d'expansion thermique du zerodur

Stabilité thermique du banc optique ~ 10uK/sqrt(Hz) [Primes]

# OMS : Thermal Noises



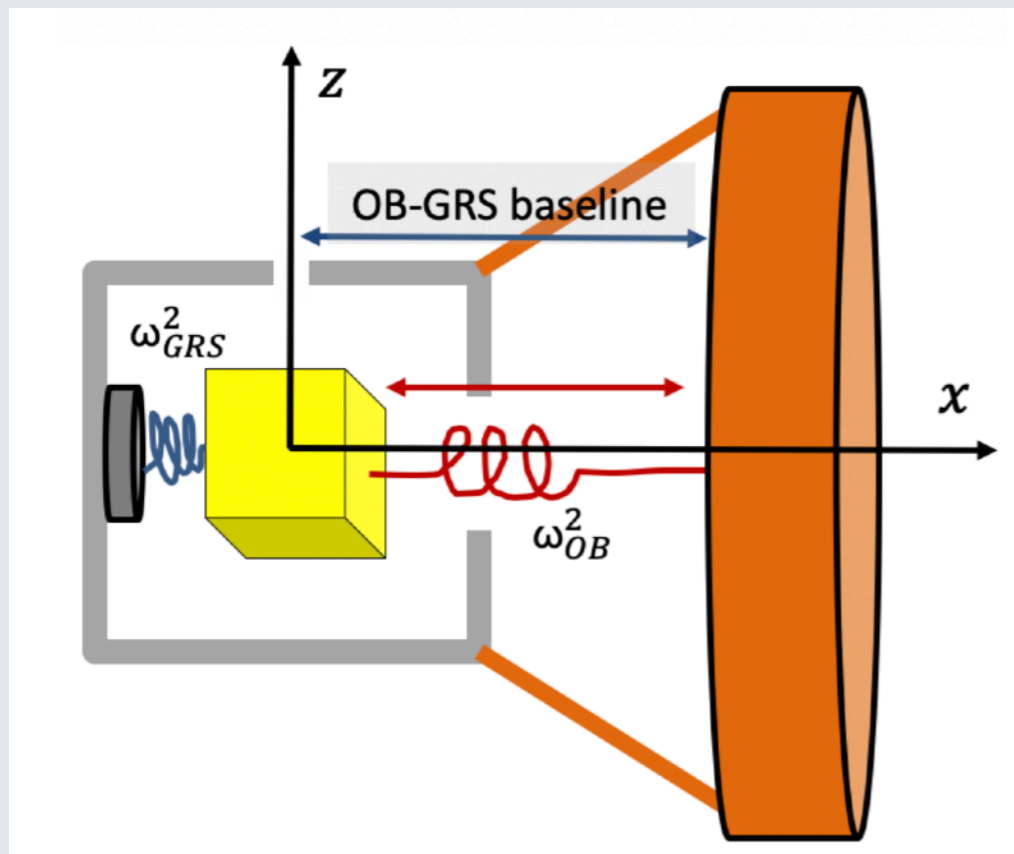
- PAAM Piston
- OB Baseplate Thermoelastic
- Long Arm Waveplates
- Test Mass Waveplates
- Mirror Thermoelastic
- Component Thermoelastic
- Long Arm Telescope contribution
- GRS Optical Window Thermoelastic
- Test Mass Thermoelastic

- Impact of correlation not known
- Each contribution is summed up linearly
- What matters for the OMS is the mHz temperature stability
- $10\mu\text{K}/\sqrt{\text{Hz}}$  is the limitation of the sensor in LPF.
- We might have some margin (cf: telescope dimension study)
- Inputs from the prime are expected during the phase A extension.

## Reference Gravitationnelle

- Stiffness coupling noise
- Thermal Force noise
- Actuation crosstalk

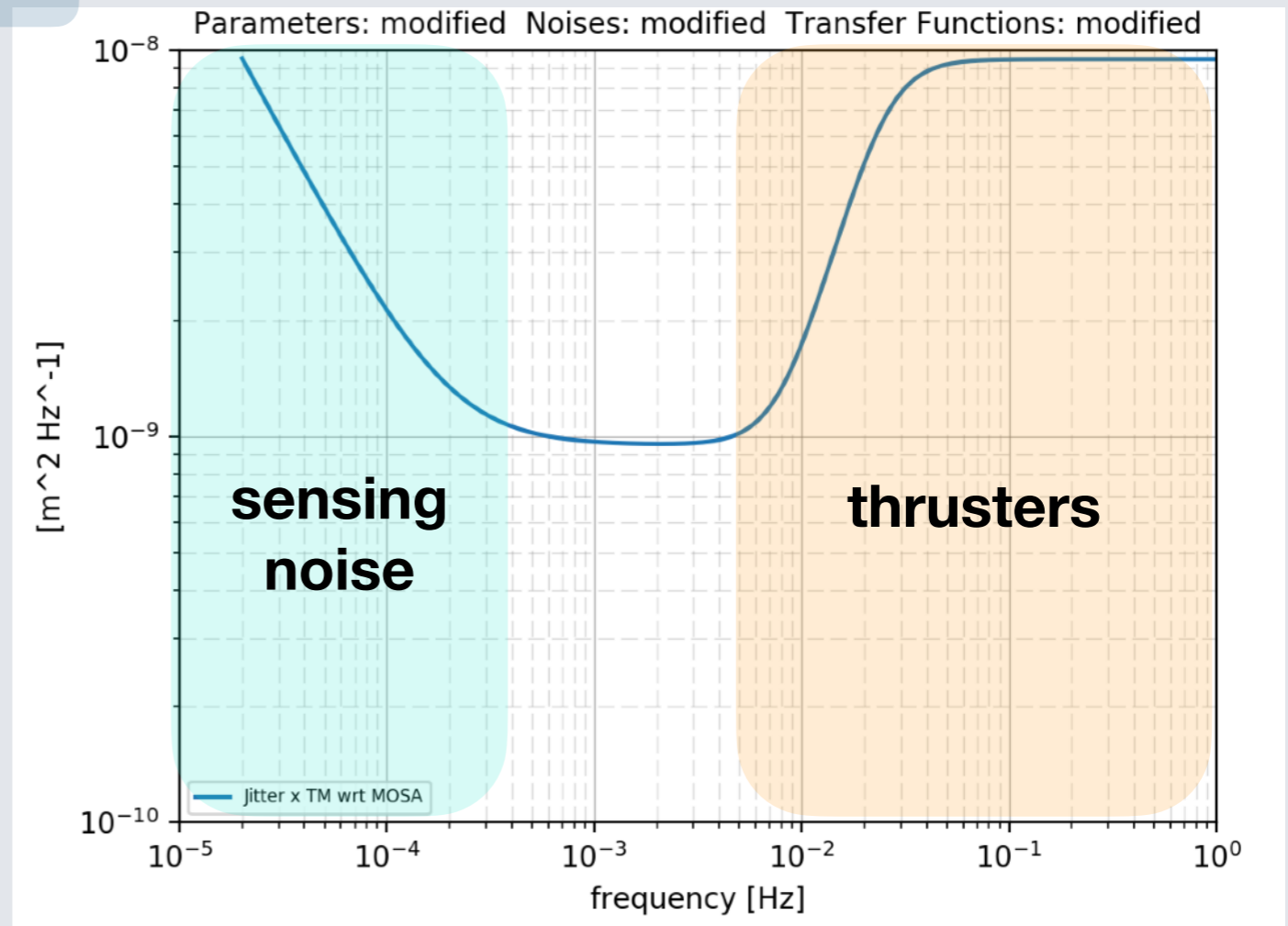
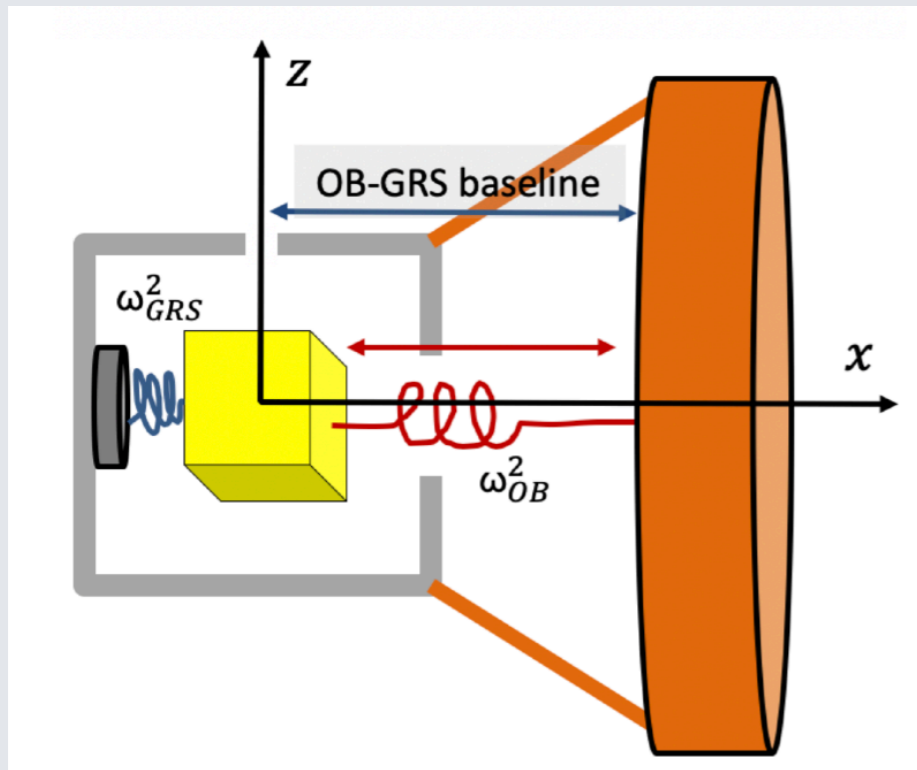
# GRS : Stiffness Coupling



- **La masse test est dans un champ gravitationnel et électrique non uniforme**
- **Tout déplacement relatif à la masse test entraîne un couplage avec ces champs.**

- **Valable sur tous les autres axes.**
- **Dominant à basse fréquence.**

# GRS : Stiffness Coupling



**Bruit  
accélération  
de la masse  
test**

**Stiffness  
coefficient**

**Stabilité de la  
plateforme en X  
Axe Drag Free**

**Déformation  
thermo-mécanique  
entre OB et le GRS**

$$\delta g_x = -\omega_{xx, TOT}^2 \times (\delta x_{TM} - \delta x_{OB}) - (\omega_{xx, TOT}^2 - \omega_{xx, OB}^2) \times (\delta x_{OB} - \delta x_{GRS}),$$

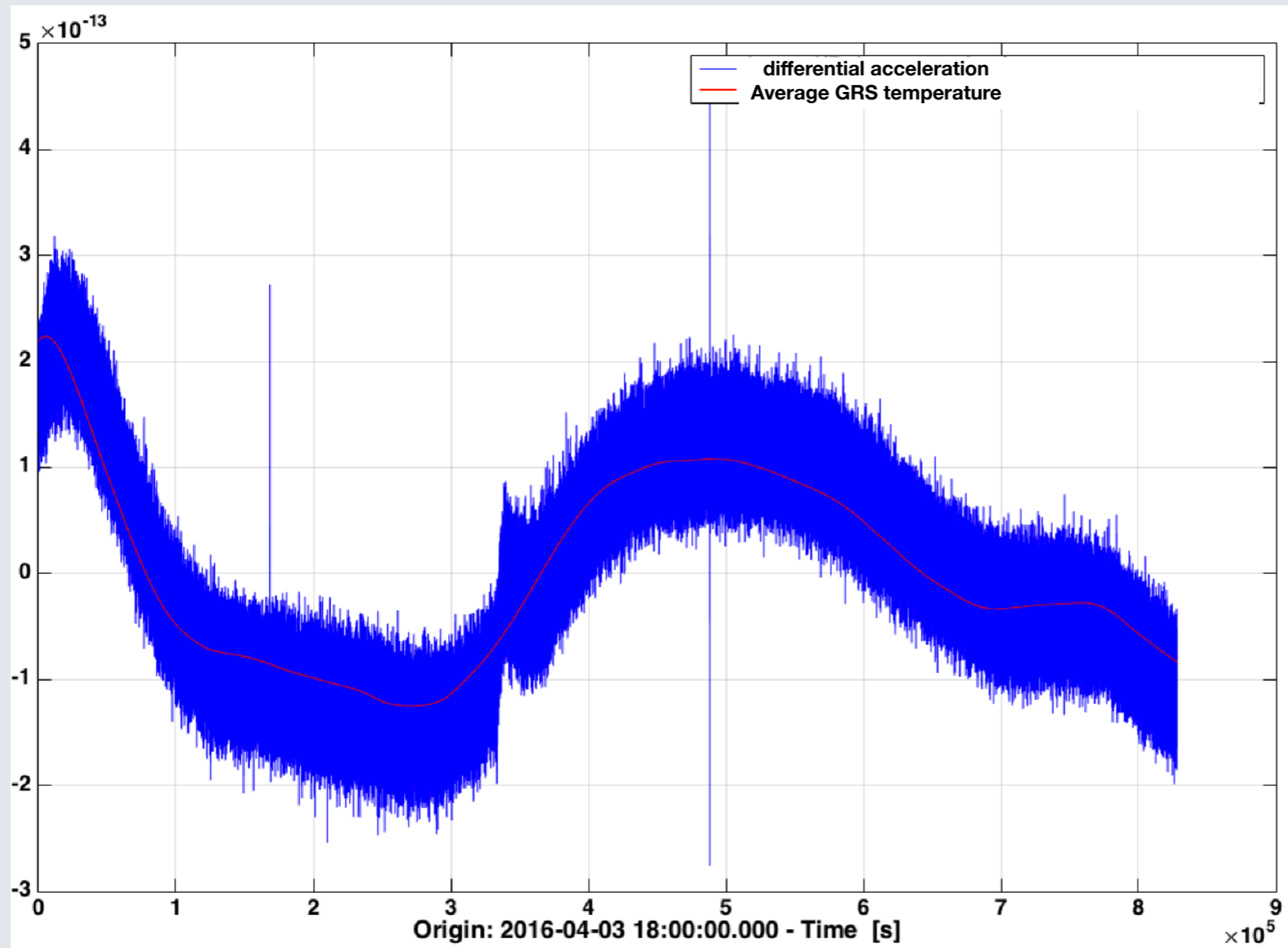
**[Gravitational  
balancing]**

**[DFACS design &  
sensing noise]**

**[MSS design and  
temperature stability]**

# EH/GRS average temperature force noise

During LPF : correlation between the GRS average temperature and the differential acceleration between two test masses.





# EH/GRS average temperature force noise

Model for the LISA

Acceleration  
noise on a TM

$$S_g^{TGRS} \approx \left| \frac{\partial g_x}{\partial T_{GRS}} \right| S_{TGRS}$$

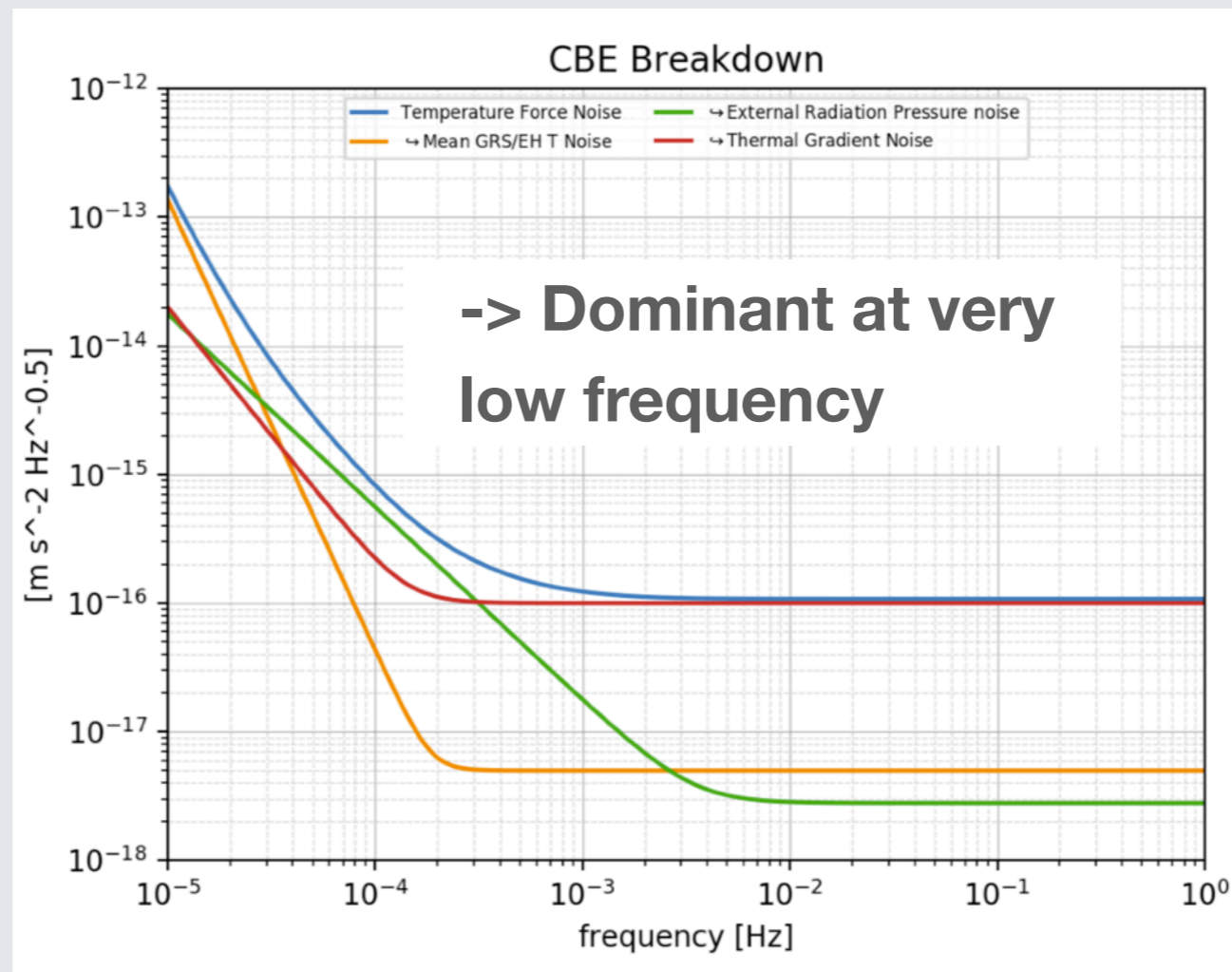
Average GRS  
temperature

Measured  
during LPF

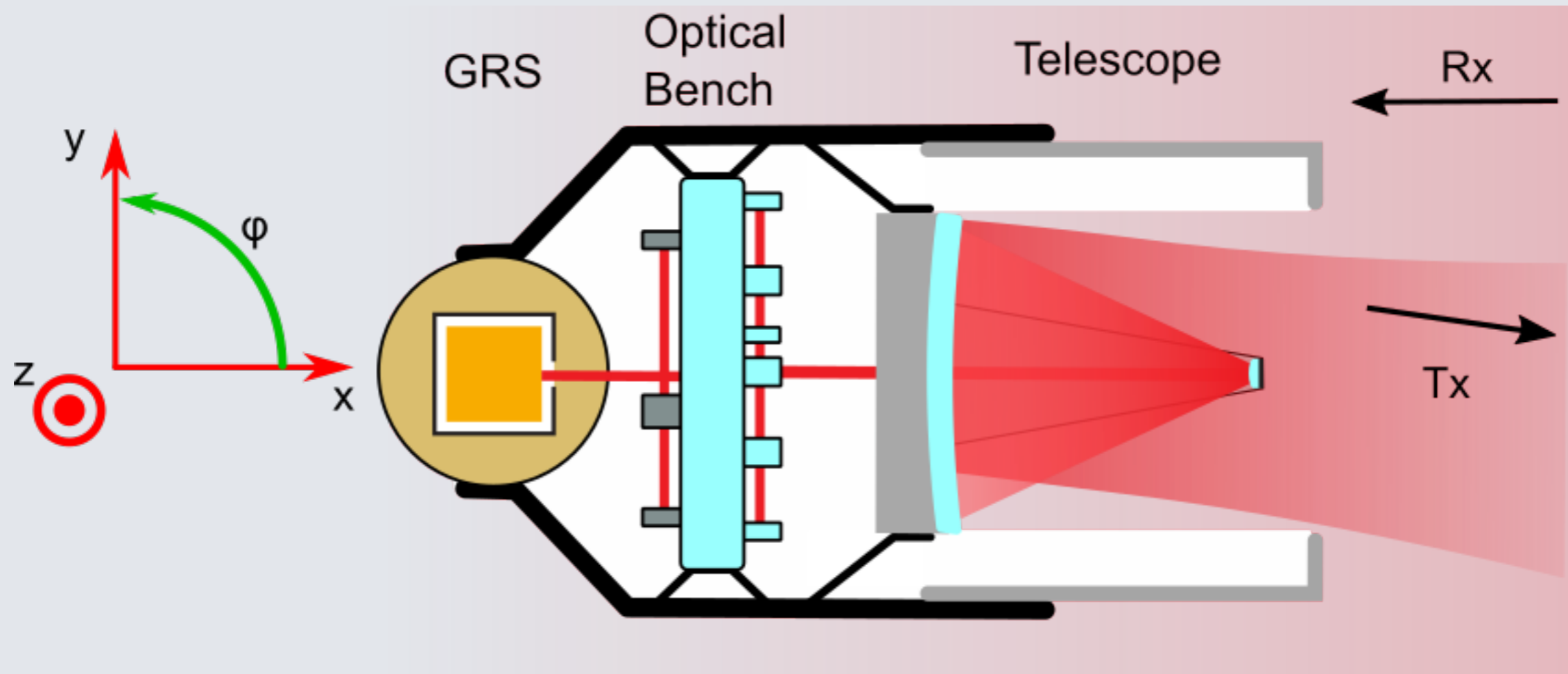
Physical explanation

associated most likely with asymmetric outgassing sources, in and immediately around the EH in view of the TM through the laser holes,

Contribution to the  
LISA budget noise



# GRS : Actuation Crosstalk



**X axis is drag free - Spacecraft follow Test Mass -> Thrusters**

**Phi axis is suspension - Test Mass Follow Spacecraft -> Electrostatic actuators**

# GRS : Actuation Crosstalk

Accélération de la masse test sur X

Coefficient crosstalk

$$S_g = \beta_{ACT_{\phi x}}^2 S_{\gamma\phi c}$$

Bruit torque en Phi appliquée par les actuateurs électrostatiques

Bras de levier

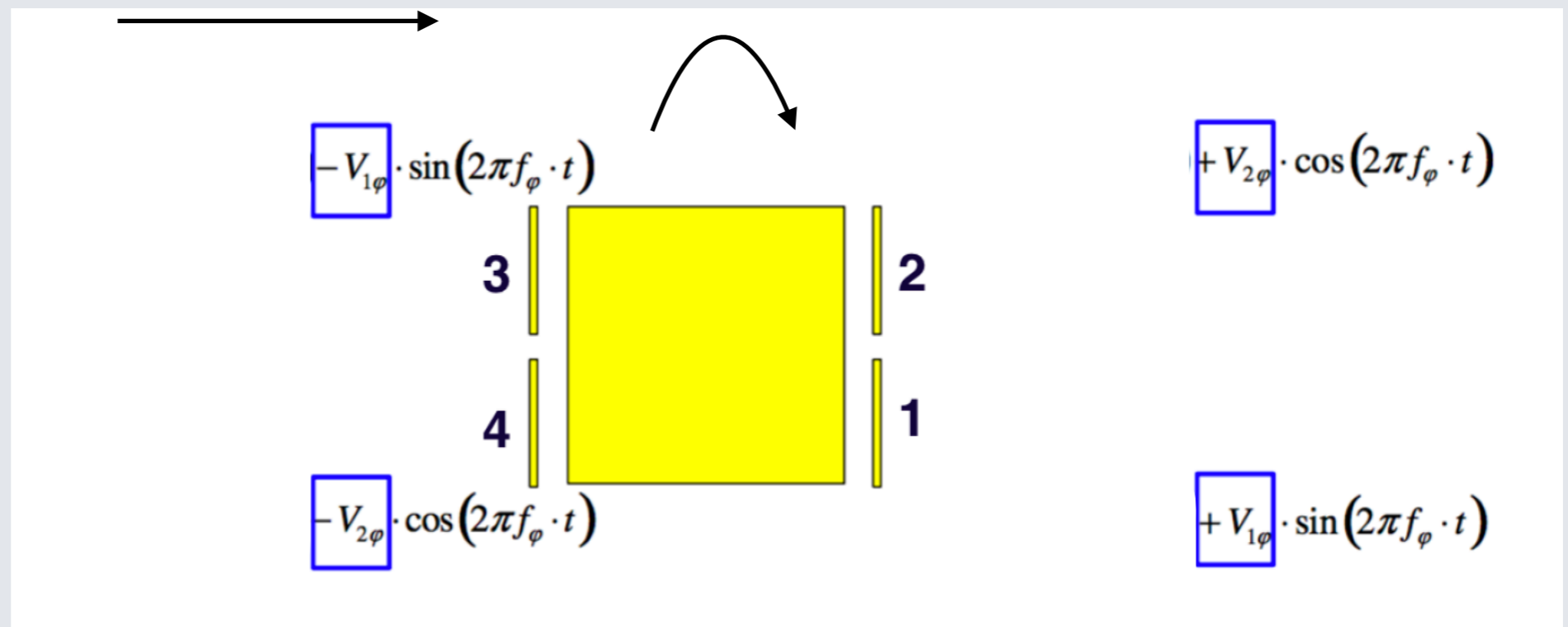
$$\beta_{ACT_{\phi x}} \approx R_{\phi}^* \delta$$

Voltage gain imbalance : 0.5%

$$S_{\gamma\phi c} \approx |T_{TM\phi}(\omega)|^2 \left[ \omega^4 S_{SC/IS}^{\phi} + S_{\gamma\phi INT} \right]$$

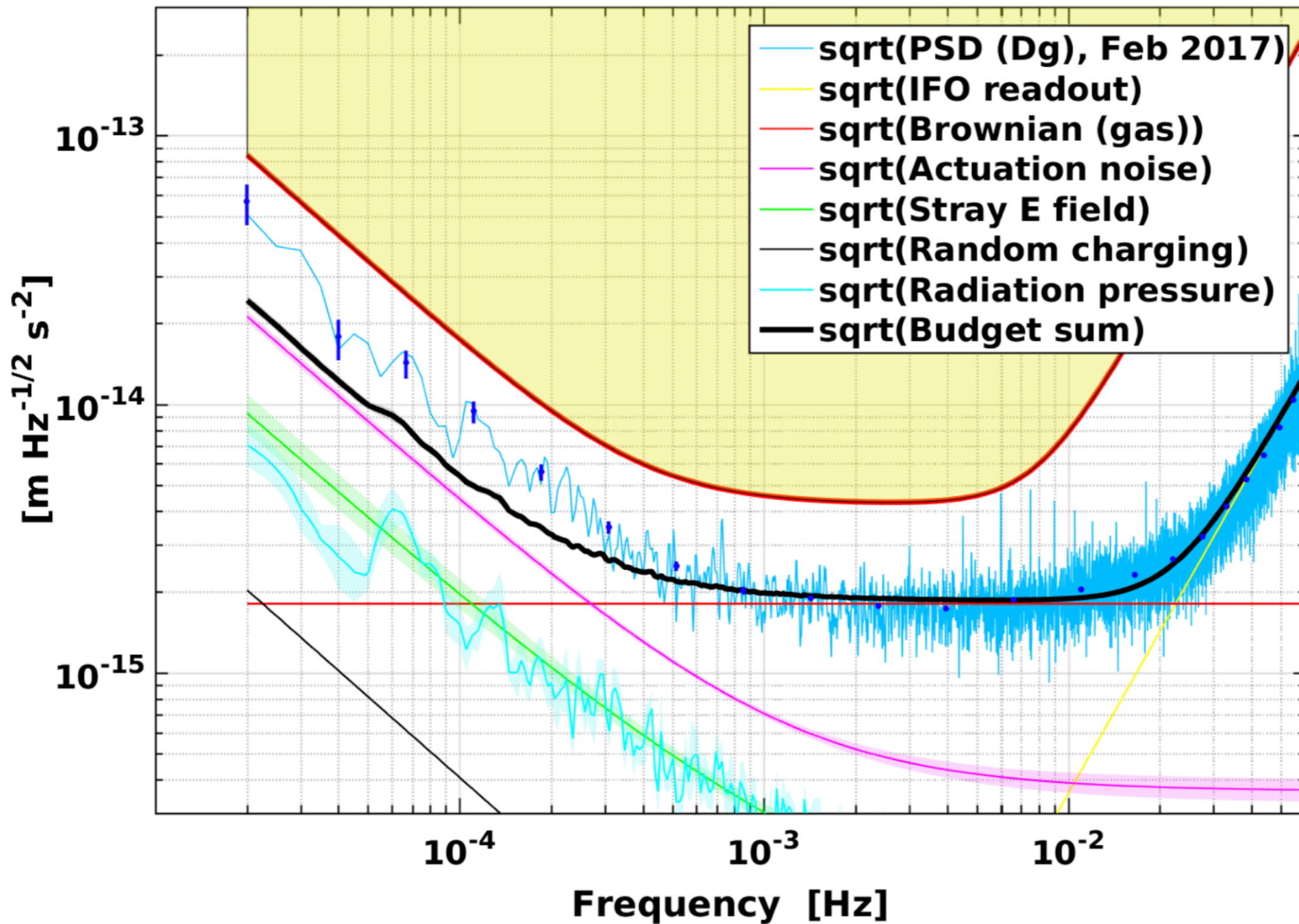
Xaxis

Phi



Force ~ V<sup>2</sup>

# Mystery noise and LPF

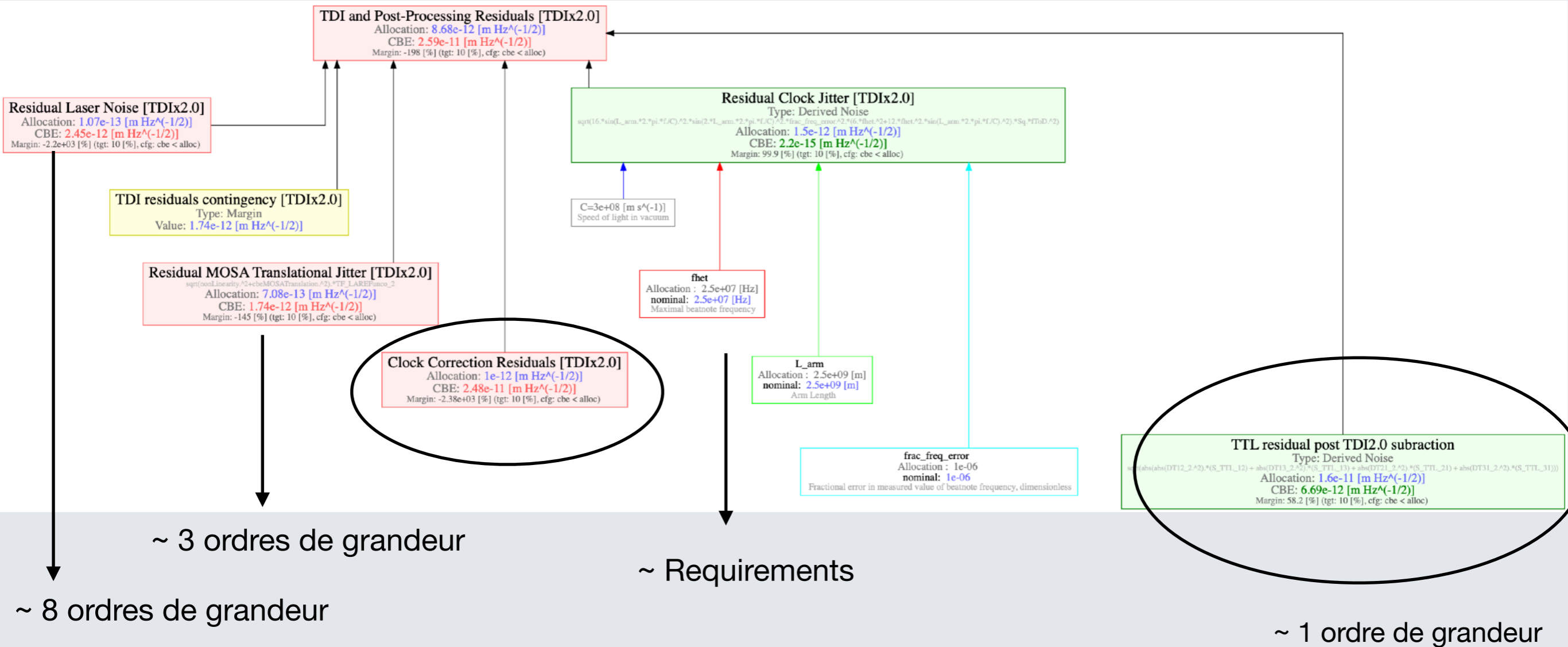


## TDI residuals & Post Processing

- Modulation noise
- Tilt-To-Length coupling

# TDI and Post processing residuals

- Concernent tous les bruits réduits ou ajoutés au sol
- Les bruits réduits dépassent largement les specs





# TDI : Clock Modulation

- Rappel : le signal est digitalisé à 80MHz par une horloge entachée d'une erreur  $\delta t$
- On va « imprimer » l'erreur d'horloge sur des sidebands à 2GHz et le transférer au S/C distant
- Le signal d'horloge est dominant sur les sidebands -> mesure indépendante.

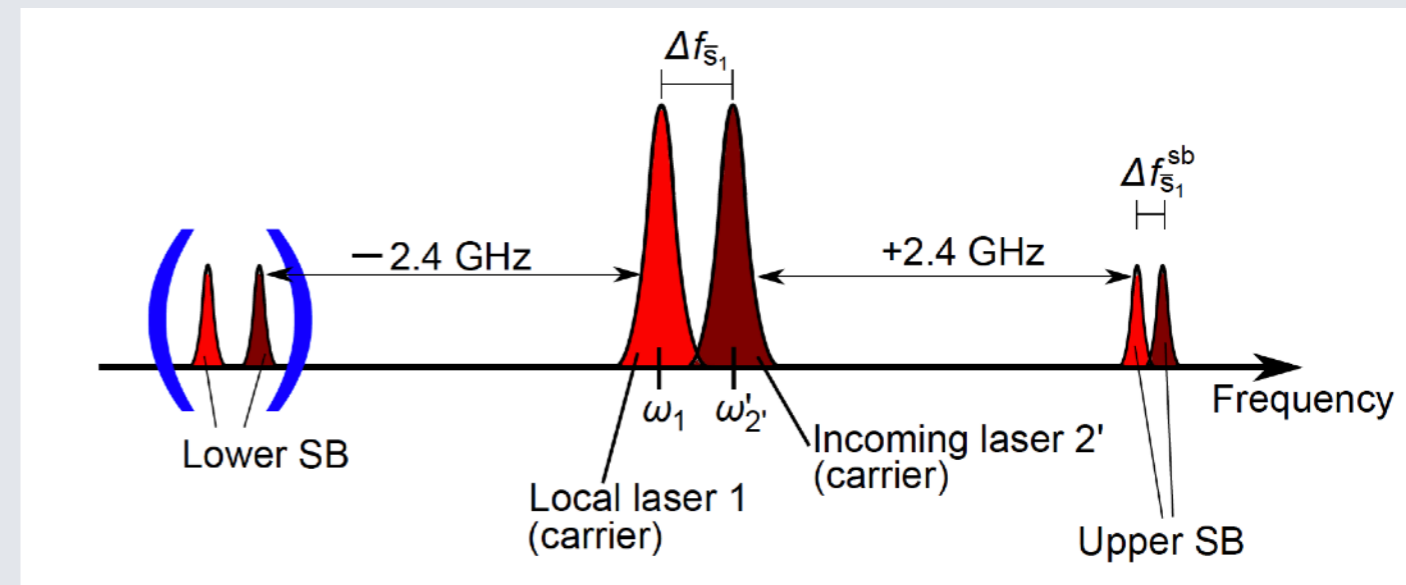
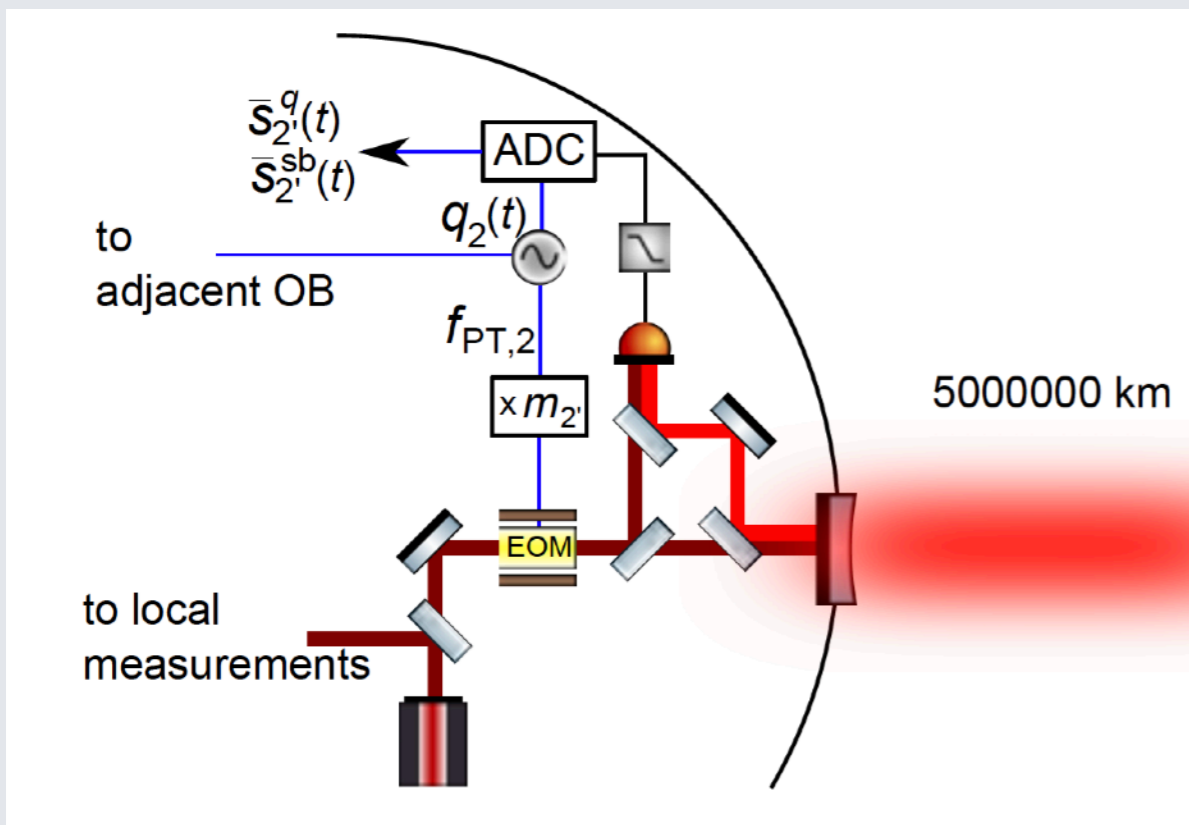
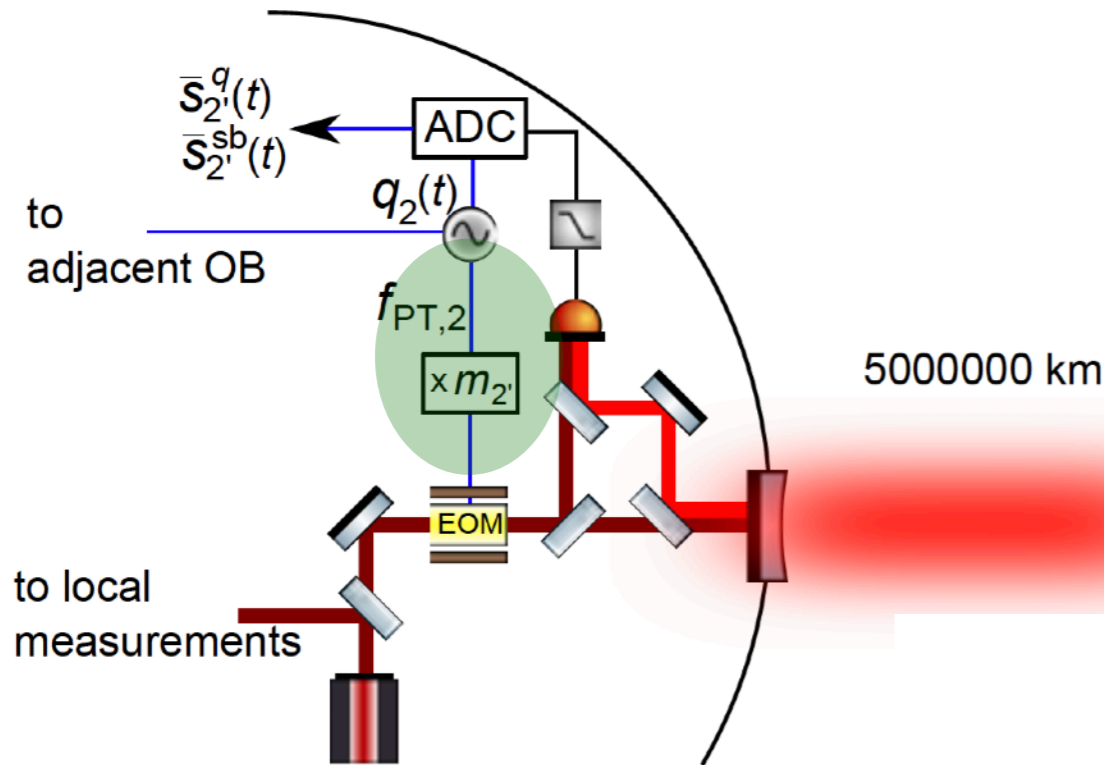


image: Time-Delay Interferometry Simulations for the Laser Interferometer Space Antenna.  
Phd thesis. M.otto



# TDI : Clock Modulation

- Chaque IFO va produire un canal de mesure supplémentaire : bande latérale.
- Ce dernier va être soustrait à la mesure principale.



## Beatnote Frequency

$$S_q^{\text{modulation-error}} \approx \left[ 6v_{\text{BN}}^2 + 12v_{\text{BN}}^2 \sin(\omega L)^2 \right] \tilde{s}_M^2 C_{XX}$$

- Mesure : These S. Barke (AEI)

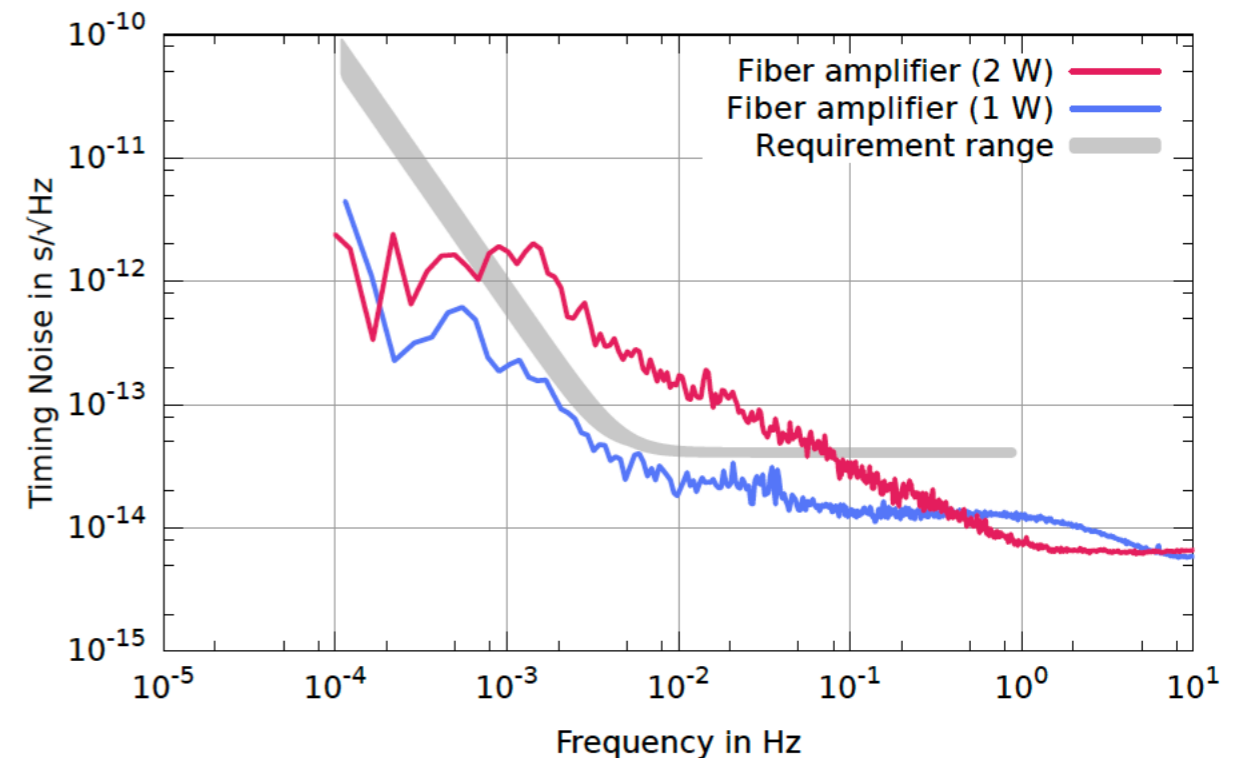
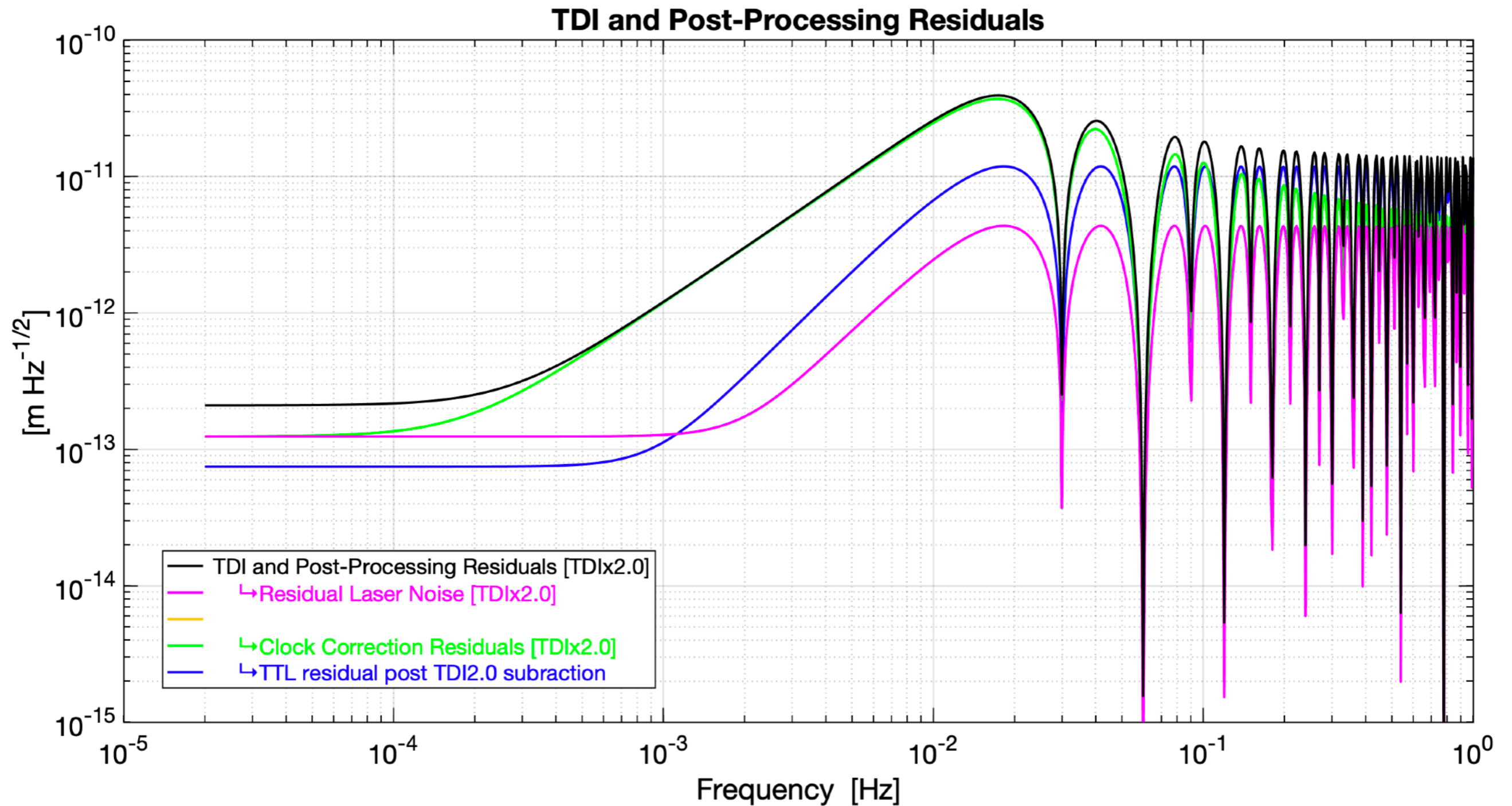


Figure 5.13: Timing jitter of an Ytterbium-doped fiber amplifier measured at 2 GHz modulation frequency for 1 and 2 W output power. The requirements are met for a power of 1 W but clearly violated for an output power of 2 W [66].

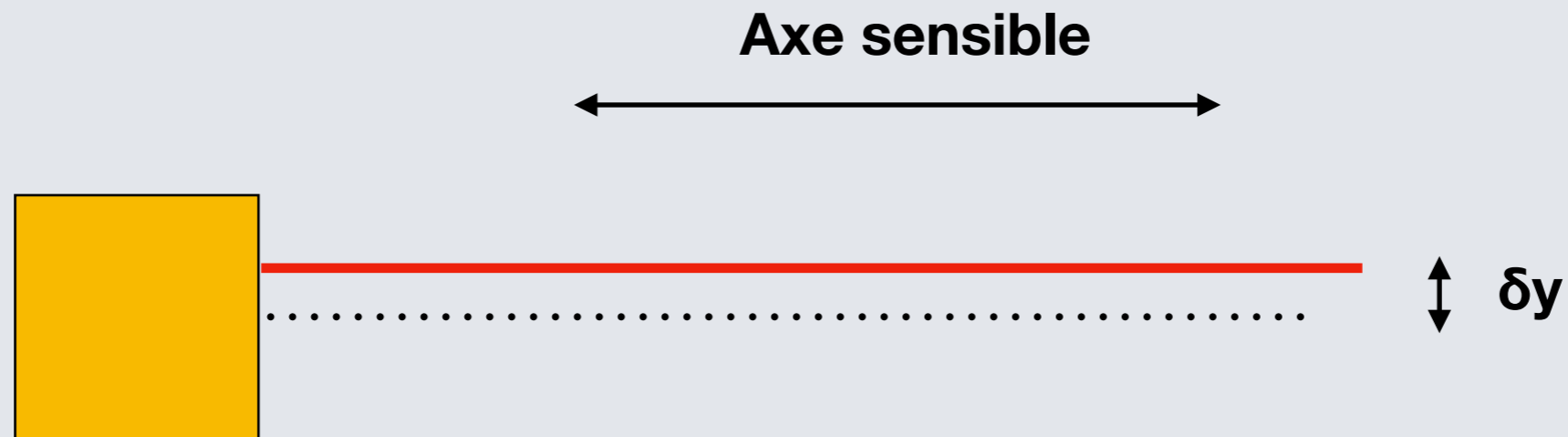
# TDI : Clock Modulation



## TDI residuals: TTL

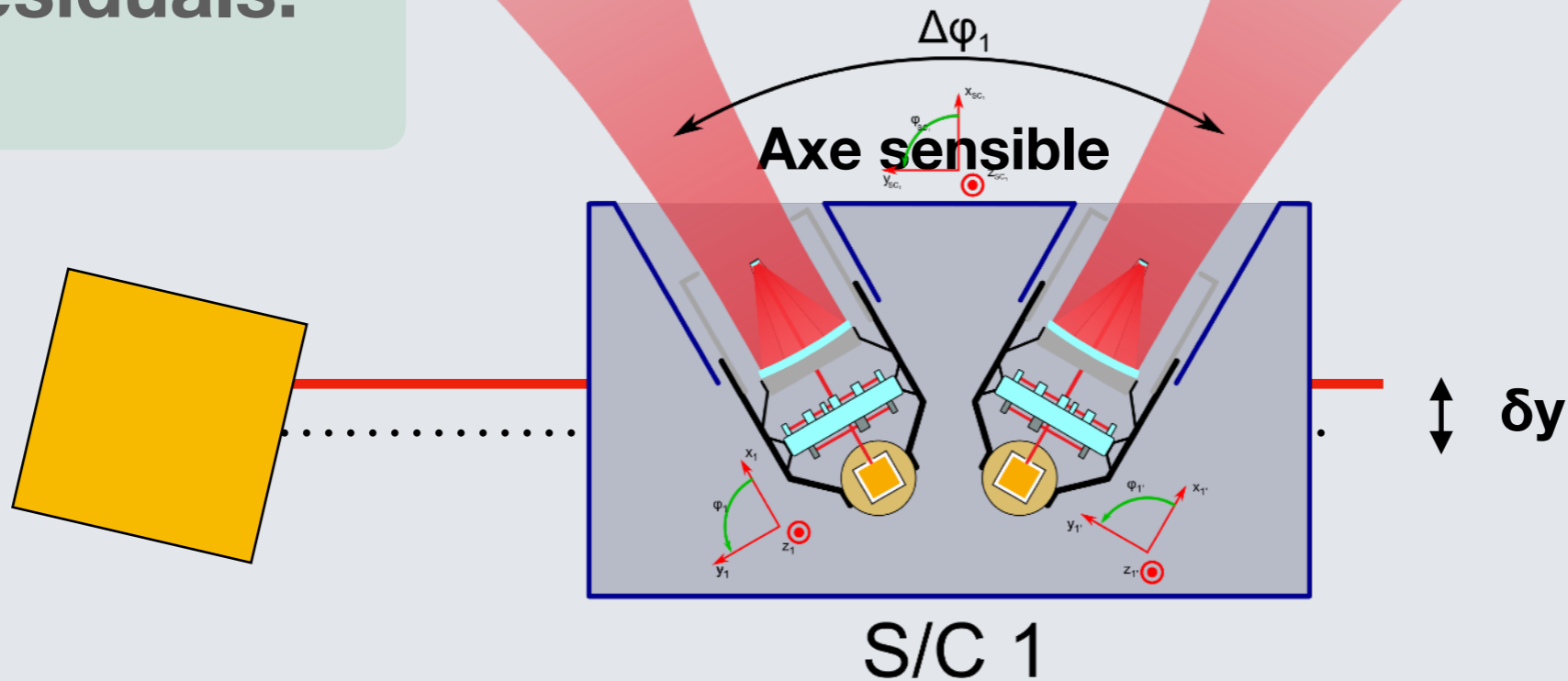
TTL is any effect which couples a rotation of the system to a measured pathlength

- Coupling driven entirely by misalignment and imperfections in the OMS



- **Split interférométrie - chaque interféromètre contribuera au TTL**
- **Beam Alignment mechanism - Calibration au sol**
- **Calibration en Vol.**

**TDI residuals:  
TTL**



Dans le modèle de performance on ne modélise pas les TTL mais leur couplage avec la mesure.

Principe de mesure par interféromètre et par degré de liberté:

$$[\text{Noise}] = [\text{TTL coupling factor}] \times [\text{Angular Jitter}]$$

**Coefficients  
TTL effectifs**

**Bruits des  
DWS**

**Magnification  
du Telescope  
et de l'OB**

$$S_{x, \text{TTLRes}}$$

$$+ S_{\text{jitter/IS}} \cdot (\delta C_{\text{TTL/IS}}^2 + C_{\text{TTLdrift/IS}}^2),$$

**Jitters angulaires  
correlations**

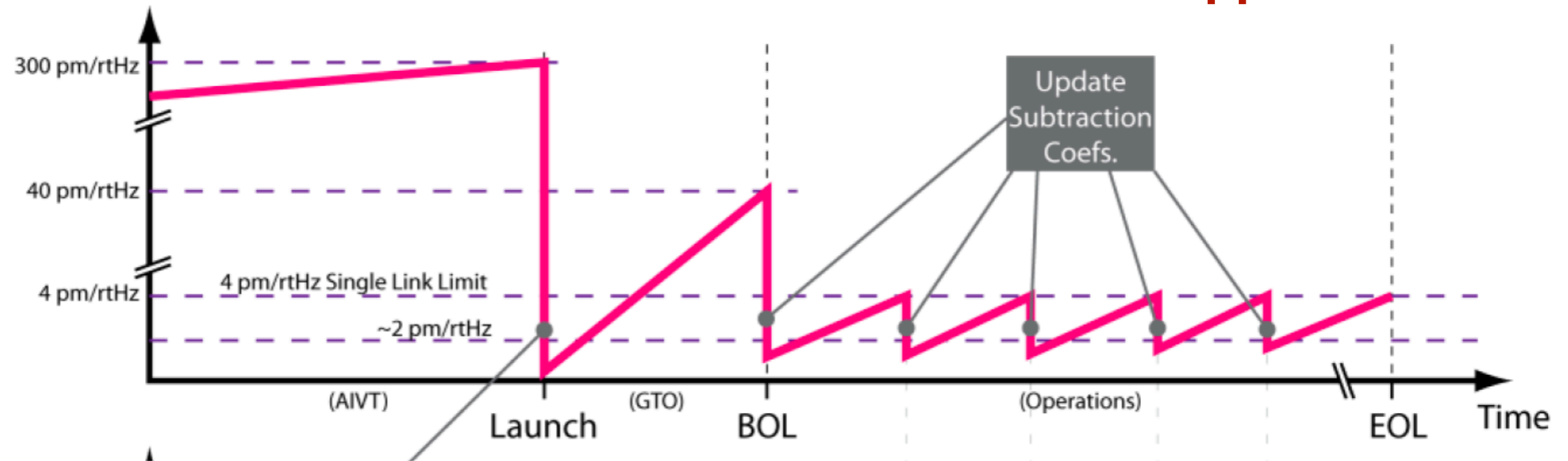
**Résidus  
calibration**

**Drift des  
alignements**

# TTL calibration scenario

All numbers are approximate.

Single Link  
Noise After  
Corrections



Beaucoup de contraintes importantes interdépendante :

- Bruit des DWS
- Alignement sol
- Calibration sol
- Calibration vol
- Stabilité de la plateforme

# TTL Effective coefficient decomposition

**Table 2:** Total budget for TTL in the RX Path.

Contributor	TTL per DOF (External) [mm/rad]	Correlates with Telescope	Limiting Requirement
Relative alignment between OB and Telescope nominal	4.02	Y	$\delta y, \delta z = \pm 30 \mu\text{m}$ alignment tolerance at OB/Telescope interface
Telescope pupil knowledge error	4.02	Y	$\delta y, \delta z = \pm 30 \mu\text{m}$ uncertainty at the internal (small) pupil
Telescope internal-external axis tolerance	1	Y	$\delta y, \delta z = \pm 1 \text{ mm}$ tolerance on the axis-axis separation of the telescope
Pupil shear	0.2	Y	$\delta y, \delta z = \pm 0.2 \text{ mm}$ max offset of the external pupil for any FOV position
Longitudinal-Lateral cross coupling	0.5		$\Delta x = \pm 3 \text{ mm}$ longitudinal alignment tolerance between the OB and Telescope nominal pupils, $\delta \eta, \delta \phi = 10 \mu\text{rad}$ boresighting of the telescope
Telescope geometric	0.55		Inherent property of the telescope
Imaging system residual	1.7		Inherent property of the imaging
LO lateral alignment	0.59		$\delta y, \delta z = \pm 30 \mu\text{m}$ alignment tolerance at recombiner
LO waist matching	0.1		$\delta x = \pm 1.5 \text{ m}$ tolerance of positioning the waist to the entrance pupil of the imaging system
QPD lateral	1.96		$\delta y, \delta z = \pm 10 \mu\text{m}$ alignment tolerance
QPD longitudinal	0.08		$\delta x = \pm 2 \text{ mm}$ alignment tolerance
Wavefront Error	0.8		$\lambda/20$ RMS total WFE
Other Terms	0.5		To be evaluated
Margin	1		
<i>RX Aperture Stop</i>	<i>0</i>		<i>This is our compensator, so we exclude its alignment from the total budget.</i>
<b>Total (RSS),  C<sub>RX</sub> </b>	<b>6.55</b>		

**Reference:**  
**LISA-UKOB-INST-TN-004 LISA**  
**Optical Alignment Analysis**

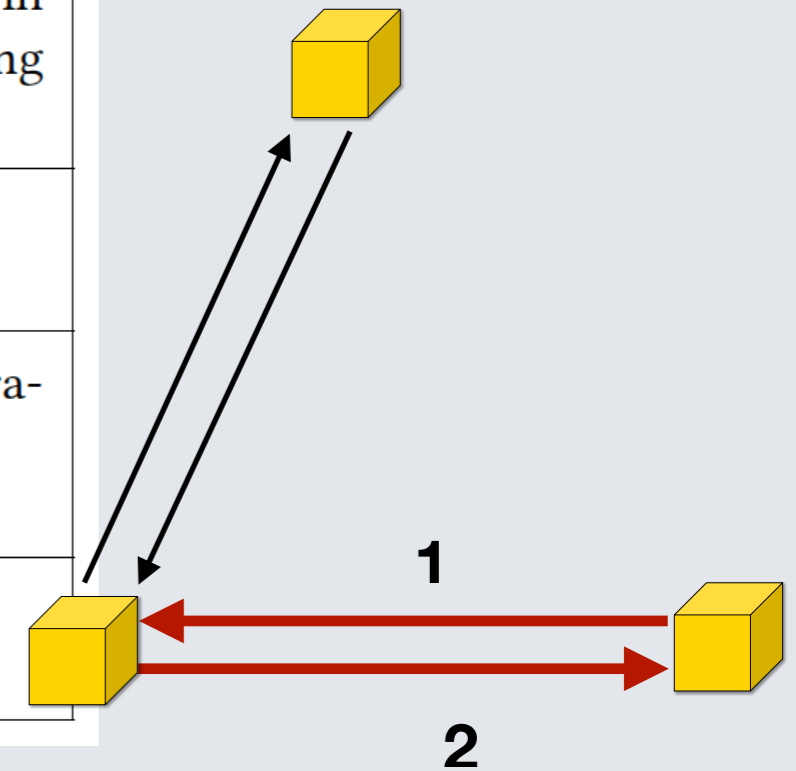
# TDI Transfer Functions



# TDI Transfer Functions

$$C_{XX}(\omega) = 16 \sin^2\left(\omega \frac{L}{c}\right) \sin^2\left(2\omega \frac{L}{c}\right)$$

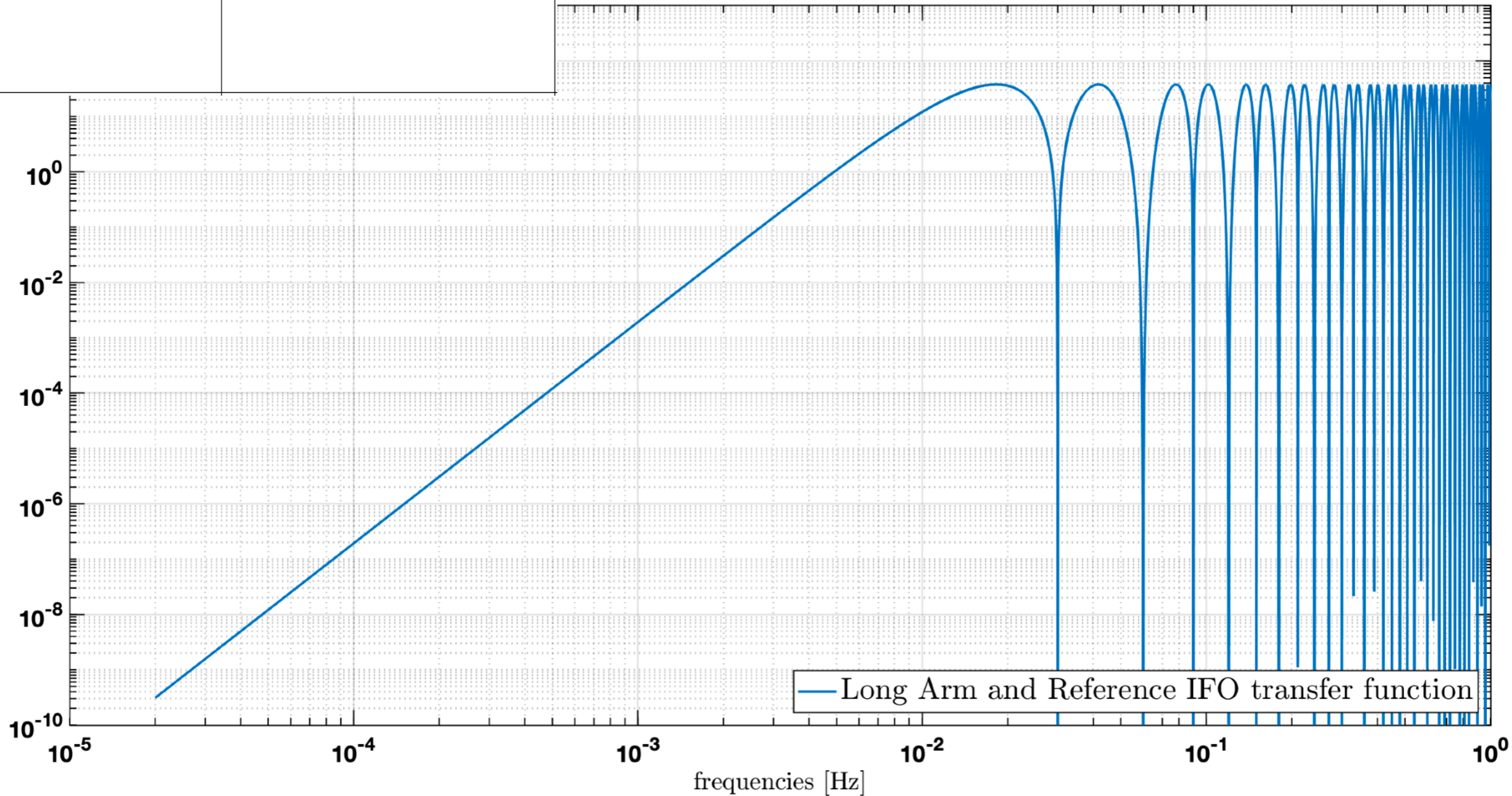
Categories of TDI transfer function	XX 2.0	XY 2.0	Example noises in current Performance Model
Uncorrelated long-arm (science) and reference IFO	$4 C_{XX}(\omega)$ ~ 4 à basse fréquence	$C_{XY}(\omega)$	Long-arm noise, Reference noise, Thermal-mechanical noise, OMS unallocated contingency, Unmodelled noises in TDI and post-processing residuals
Uncorrelated test-mass IFO	$C_{XX}(\omega) (3 + \cos(2\omega \frac{L}{c}))$	$C_{XY}(\omega)$	Test-mass IFO noises
Uncorrelated test-mass acceleration	$4 C_{XX}(\omega) (3 + \cos(2\omega \frac{L}{c}))$ <b>Le mouvement de la masse test est mesuré deux fois.</b>	$4 C_{XY}(\omega)$	Single test-mass acceleration noise
Fully-correlated telescope	$4 C_{XX}(\omega) (3 + \cos(2\omega \frac{L}{c}))$	...	Not yet implemented



# TDI Transfer Functions

Categories of TDI transfer function	XX 2.0
Uncorrelated long-arm (science) and reference IFO	$4 C_{XX}(\omega)$

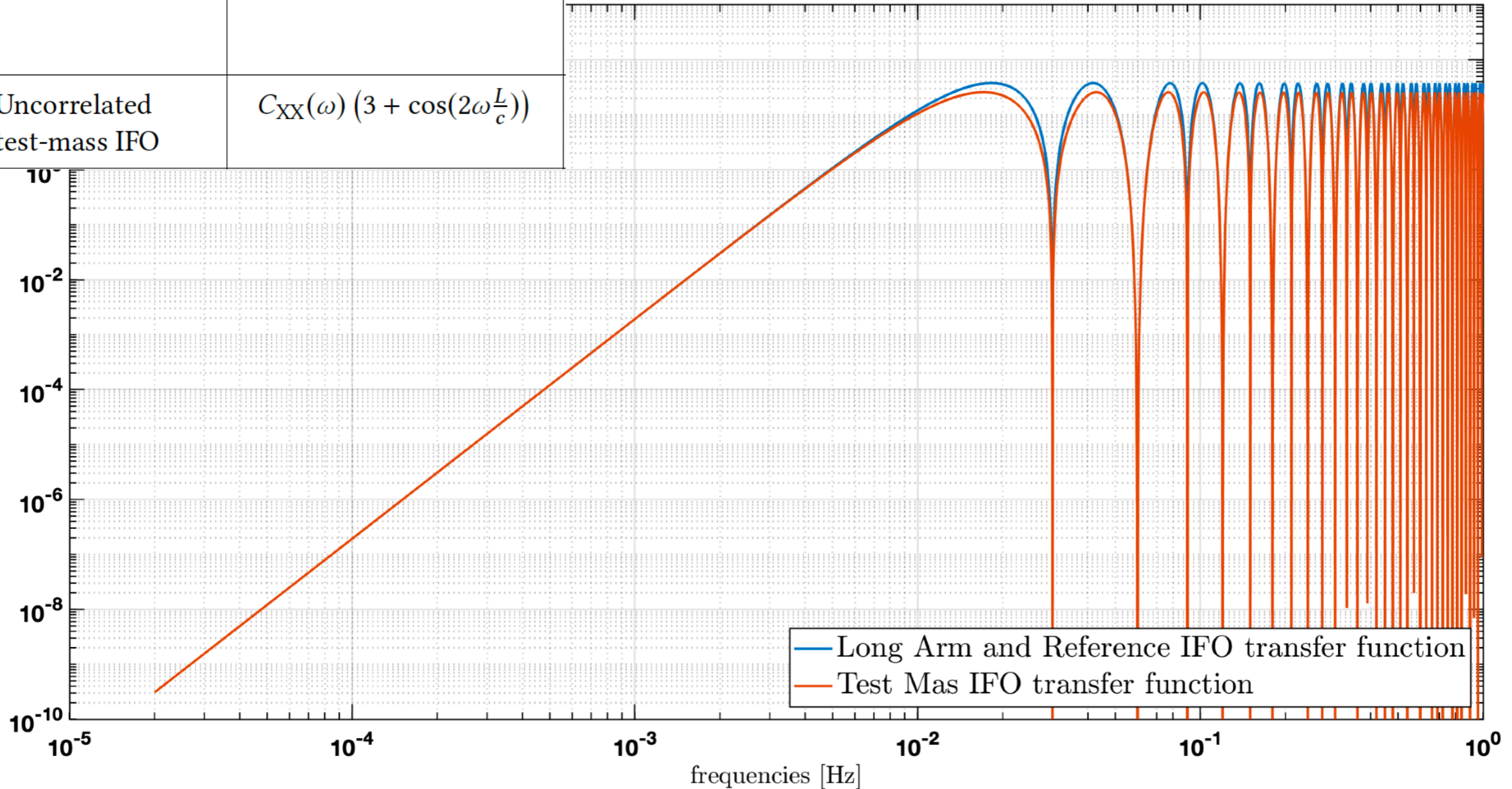
Transfer functions used in the Performance Model



# TDI Transfer Functions

Categories of TDI transfer function	XX 2.0
Uncorrelated long-arm (science) and reference IFO	$4 C_{XX}(\omega)$
Uncorrelated test-mass IFO	$C_{XX}(\omega) (3 + \cos(2\omega \frac{L}{c}))$

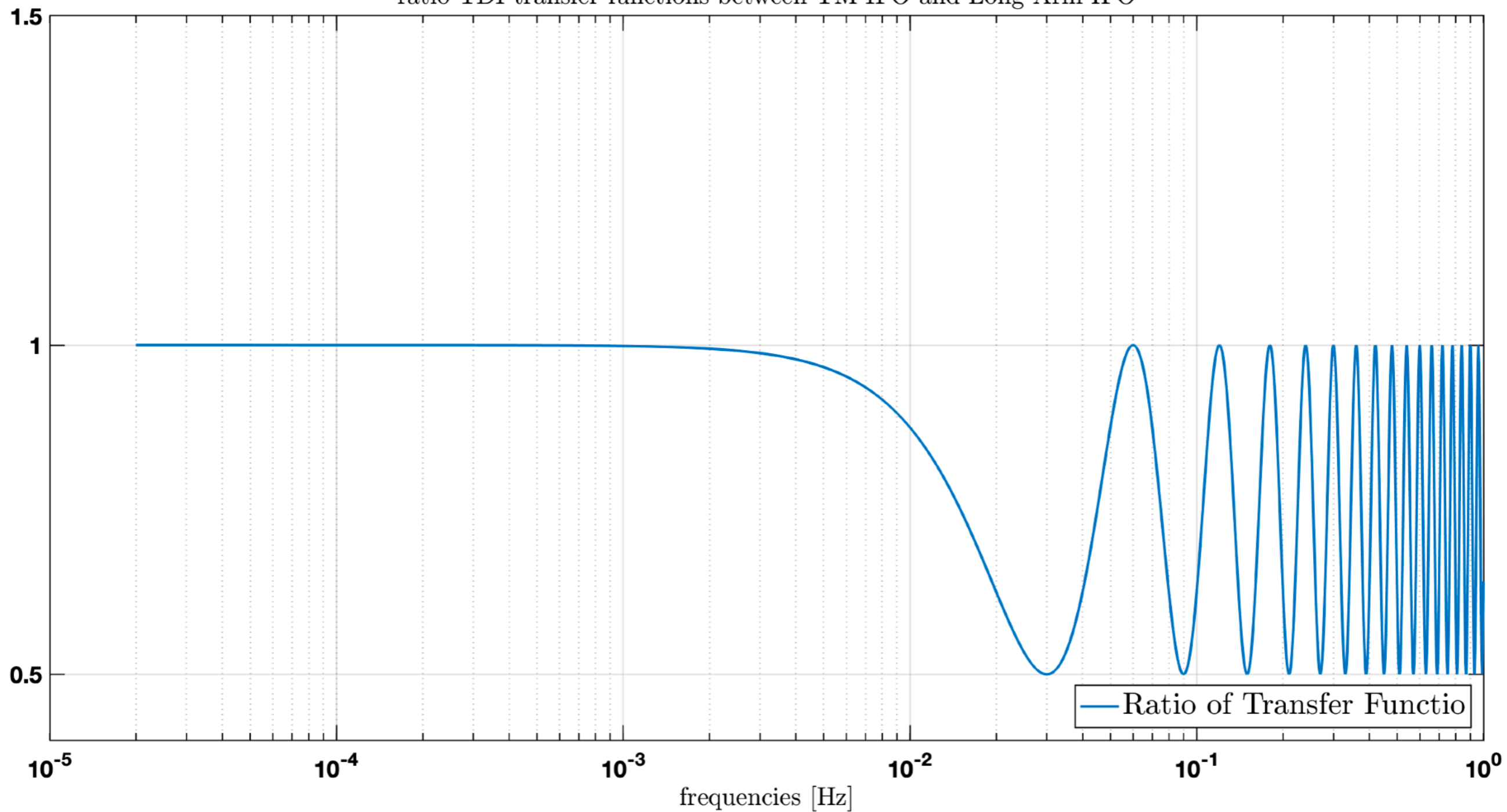
Transfer functions used in the Performance Model





# TDI Transfer Functions

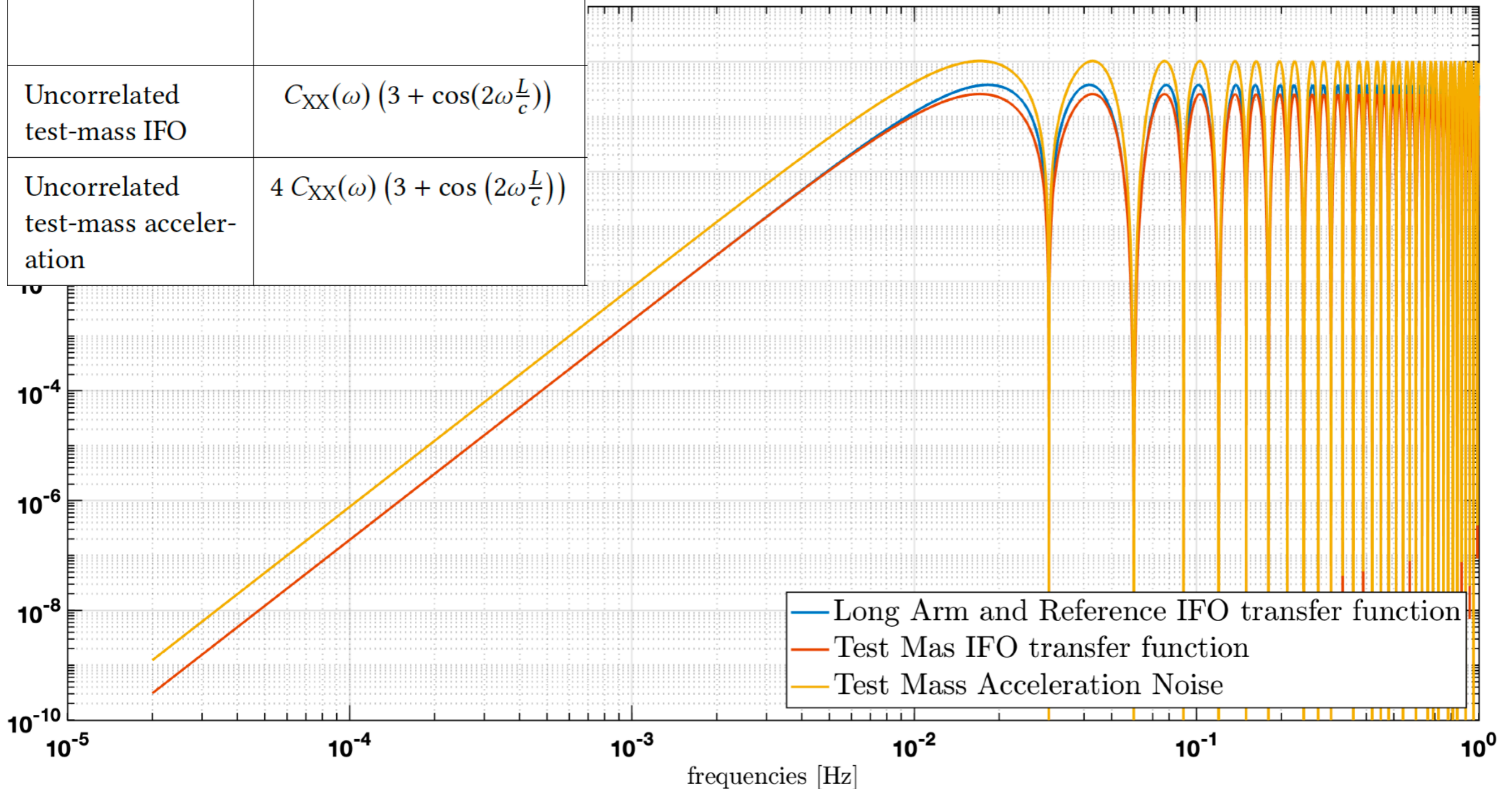
ratio TDI transfer functions between TM IFO and Long Arm IFO



# TDI Transfer Functions

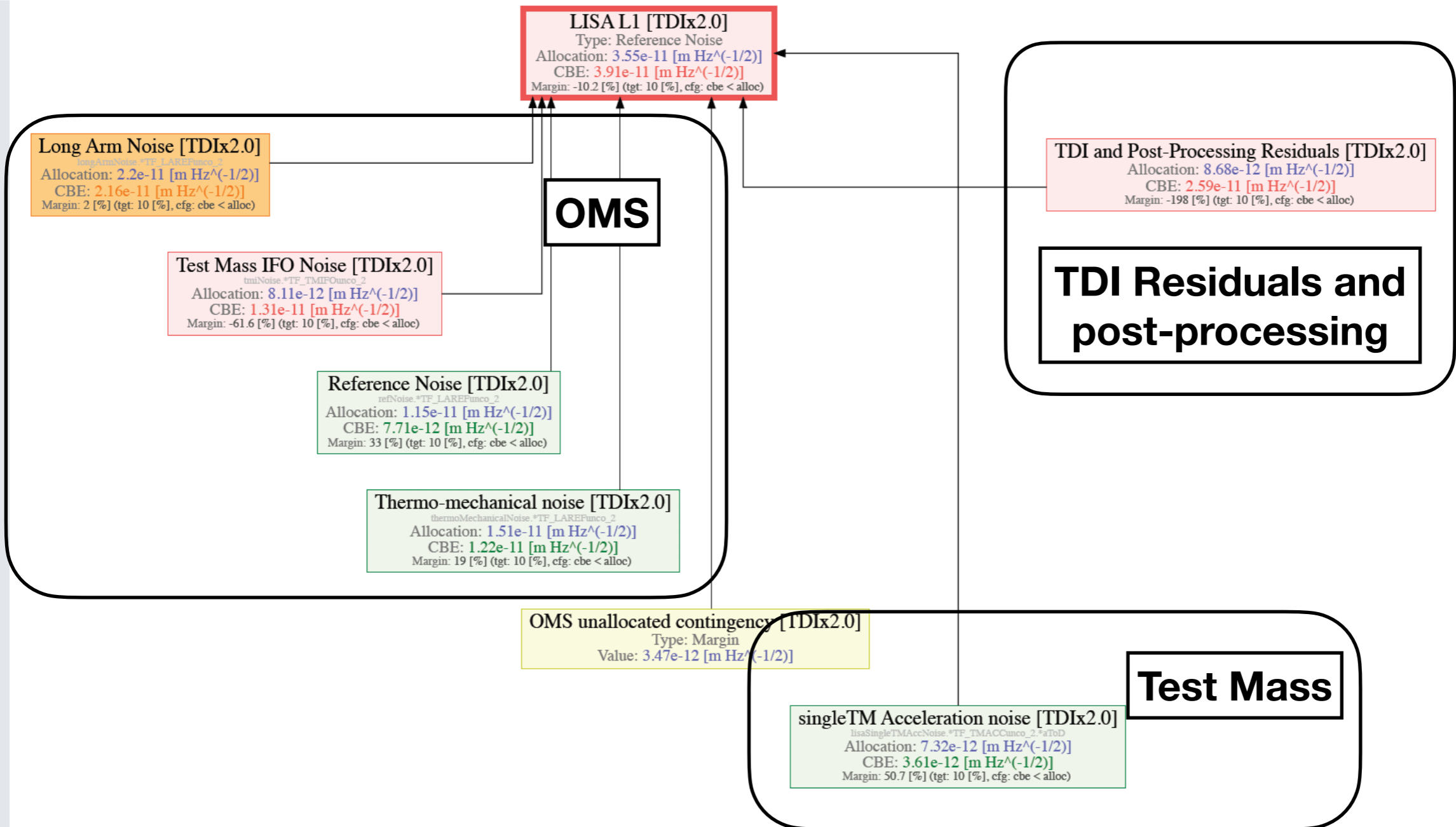
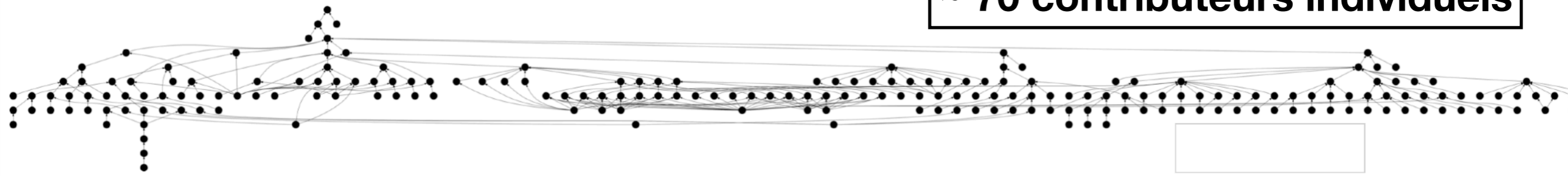
Categories of TDI transfer function	XX 2.0
Uncorrelated long-arm (science) and reference IFO	$4 C_{XX}(\omega)$
Uncorrelated test-mass IFO	$C_{XX}(\omega) (3 + \cos(2\omega \frac{L}{c}))$
Uncorrelated test-mass acceleration	$4 C_{XX}(\omega) (3 + \cos(2\omega \frac{L}{c}))$

Transfer functions used in the Performance Model

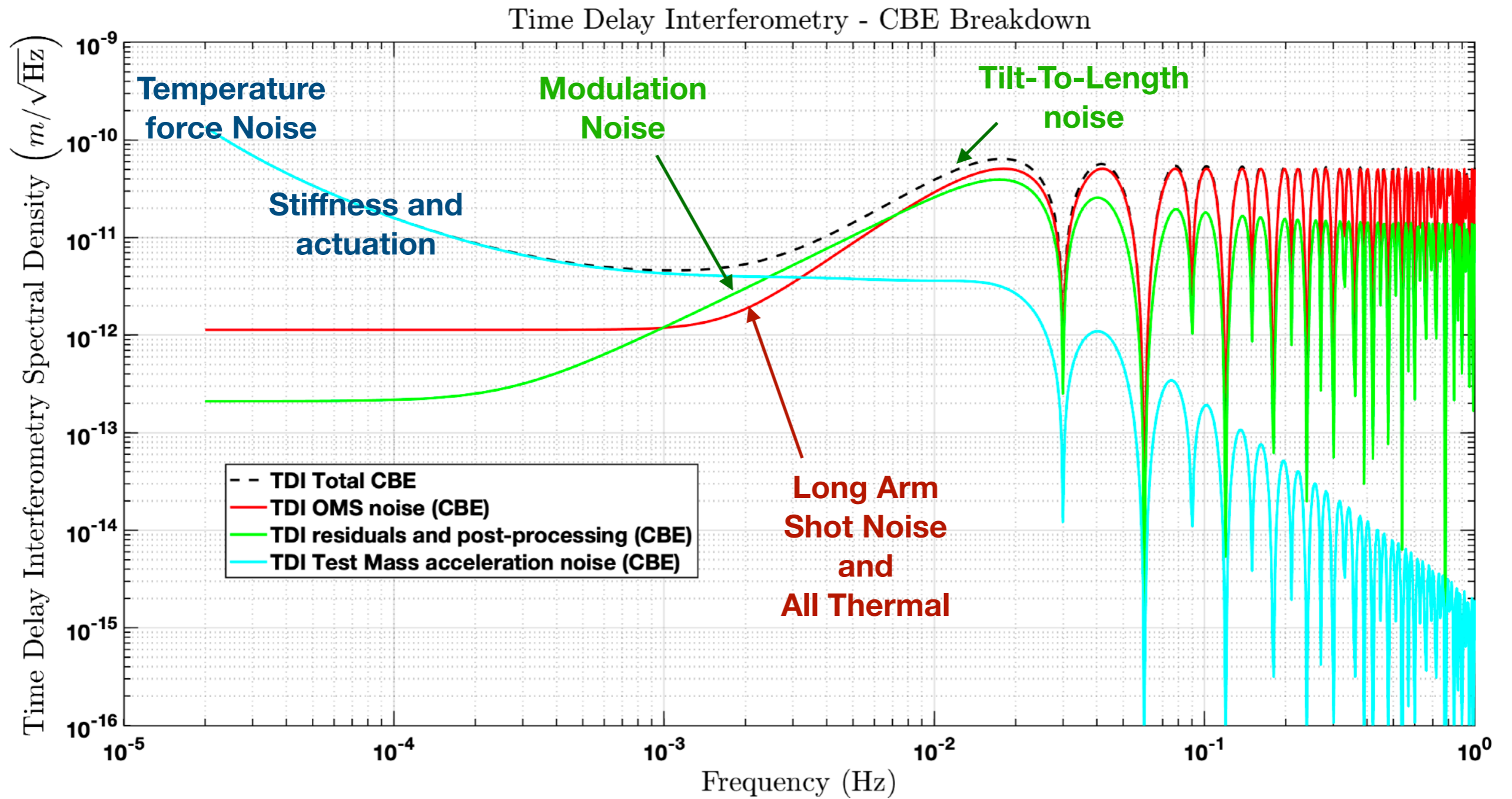


# Combiner les sources de bruits

~ 70 contributeurs individuels



# Budget De Bruit

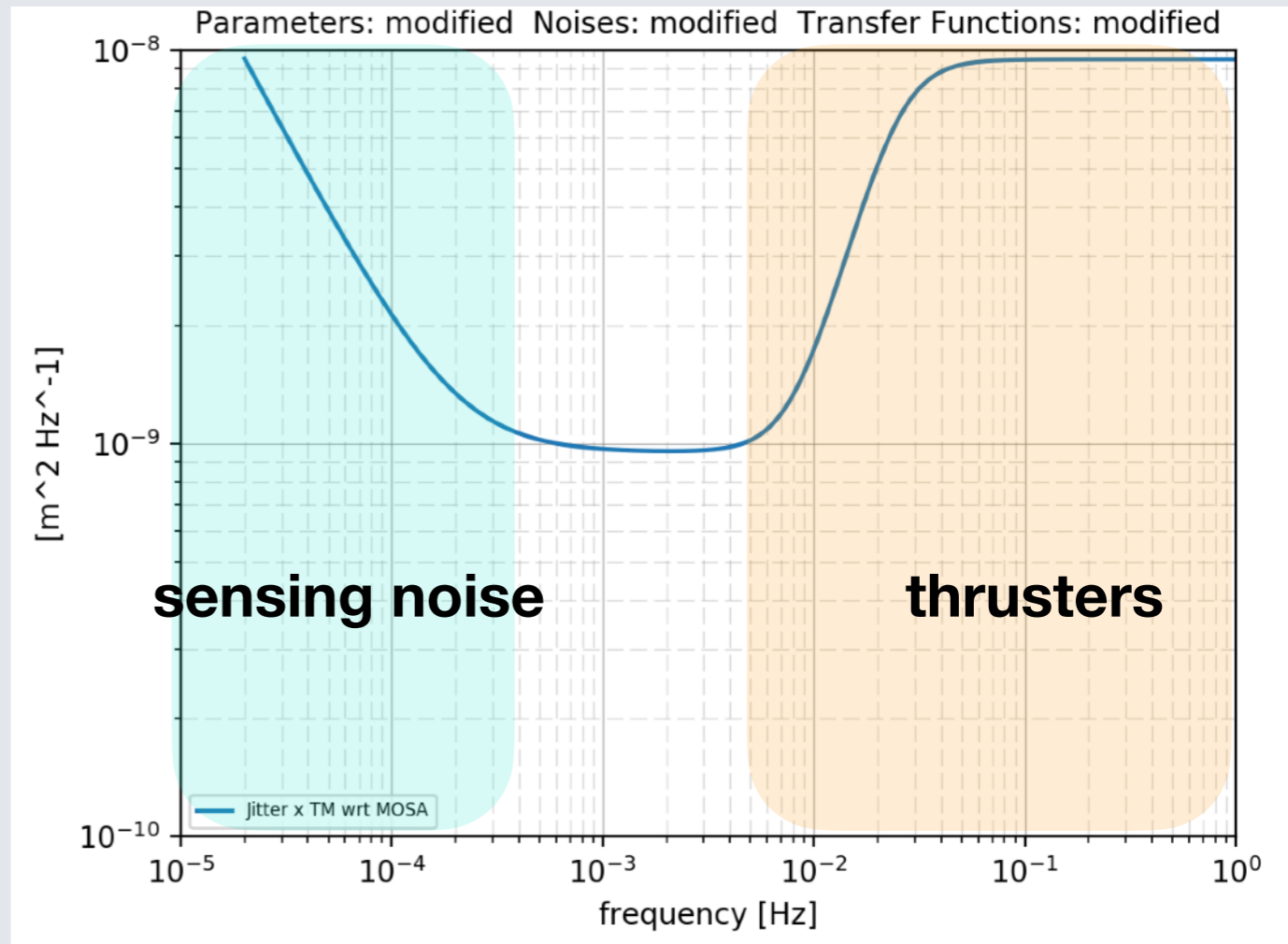
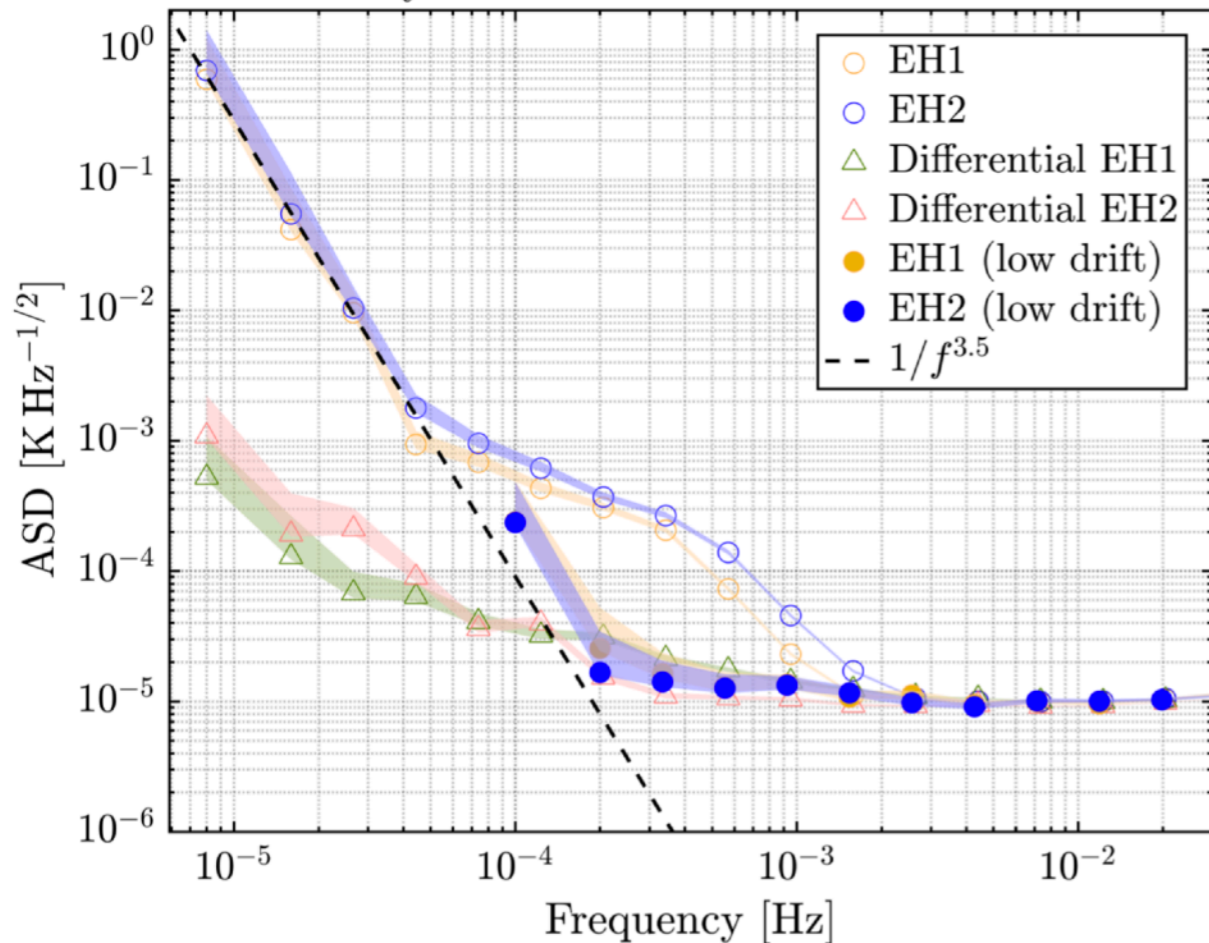




## **IV/ Limitations**

# Thermal and Platform stability : correlations

February run: from 2017-02-14 to 2017-02-27

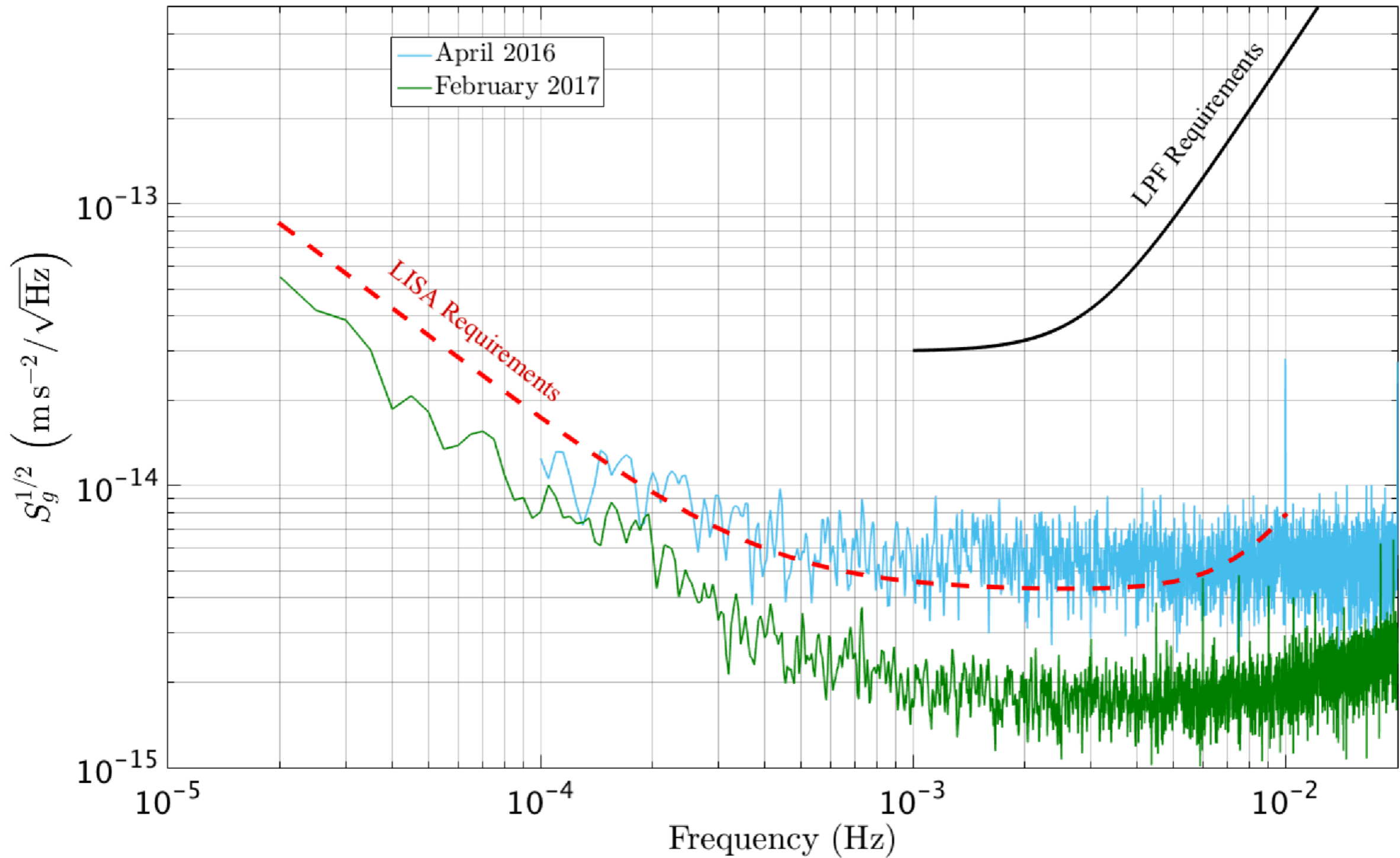


- Héritage Pathfinder limité au GRS
- Design LISA différent

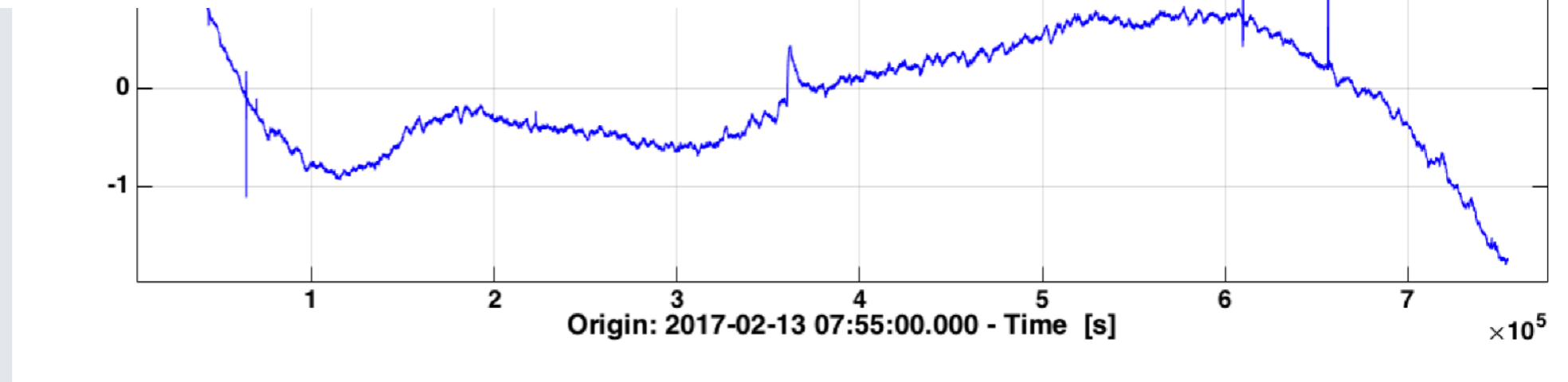
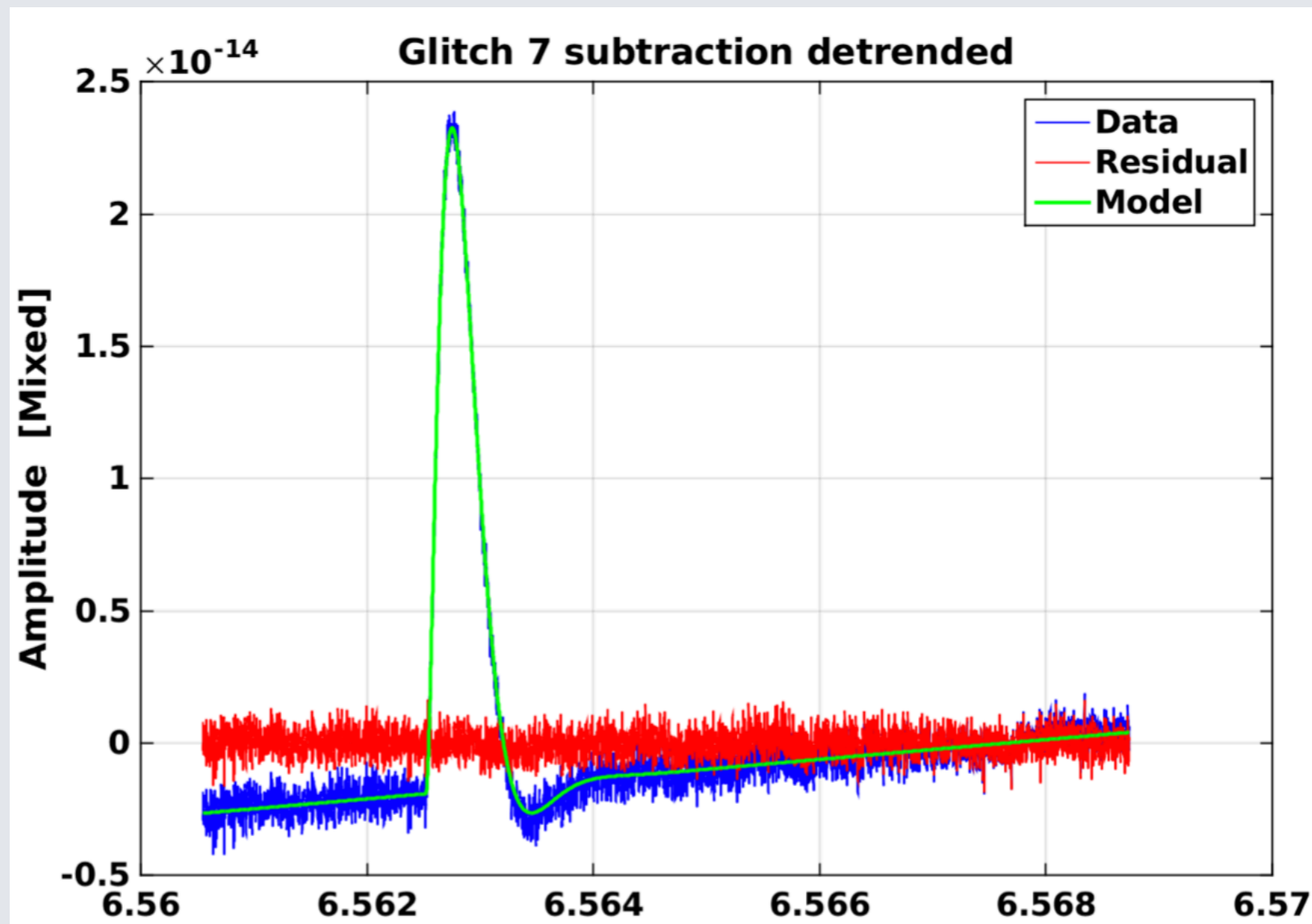
- Héritage Pathfinder sur l'axe sensible
- Jitters angulaires différents.

# Non stationarity

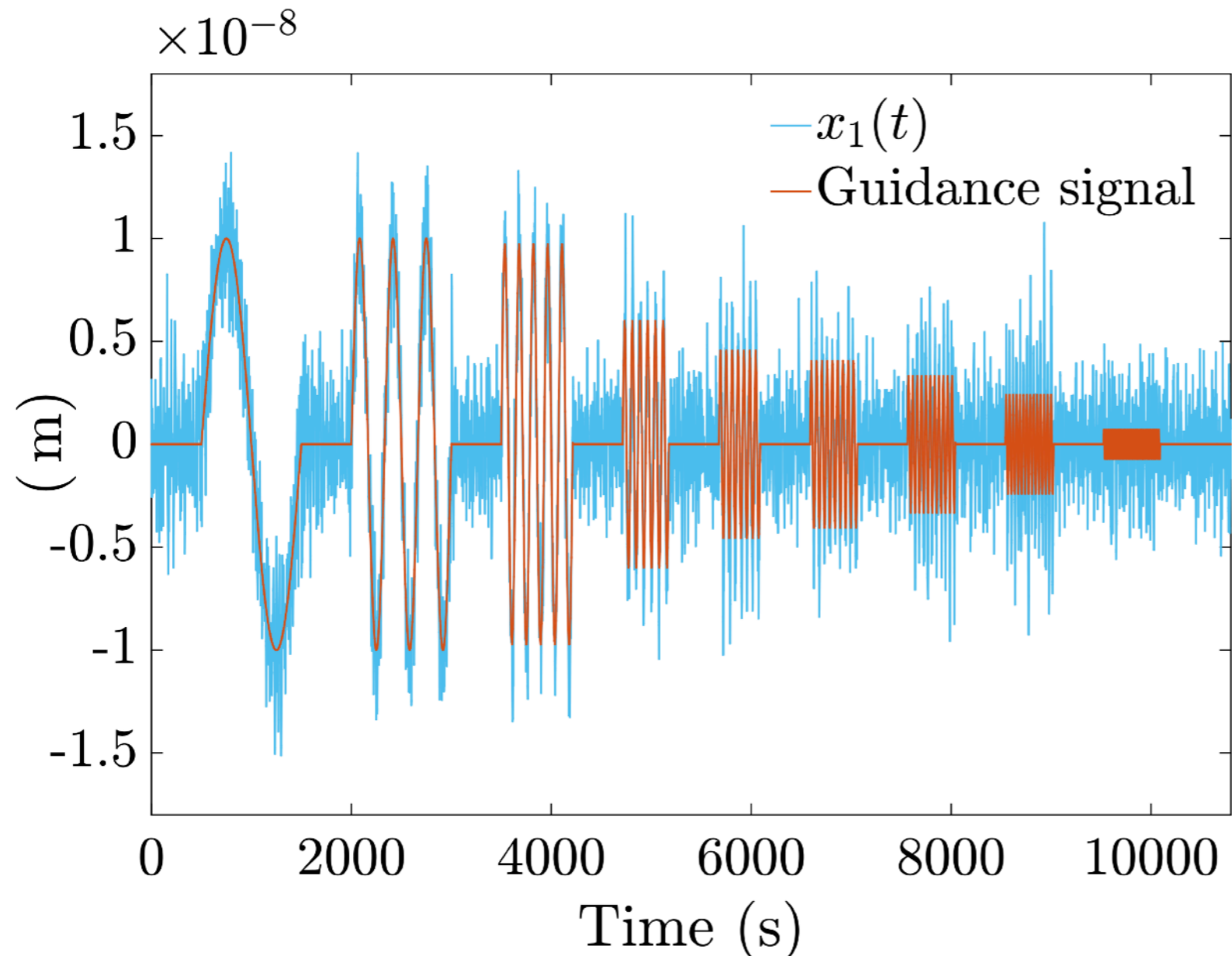
LISA Pathfinder deltaG



# Glitches



# Calibration



- Clock Noise / TTL / Stiffness ?
- Du fait de la présence du bruit laser - TDI indispensable (simulation)

## Missing noises

- Modélisation du Phasemètre
- Modélisation des DWS.
- Résidu du mouvement du SC sur l'axe sensible.
- Interpolation - Laser
- Armlength Stochastic
- Sidebands coupling because of clock calibration.
- Modelling of the Anti Aliasing filter in the performance model.
- Long Arm Line Of Sight alignment.

**Merci**

**Acces au data pack de la release 2.0.1 (Technical Note+  
release Note + Changelog):**

<https://atrium.in2p3.fr/87d2870c-5aef-4f4d-8a60-9a3afc4fe62f>

**Site web pour produire plots et récupérés les  
données de WebNSDF :**

<https://perf-lisa.in2p3.fr/>

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