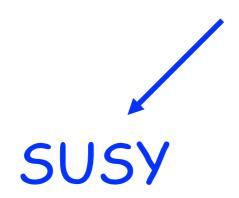
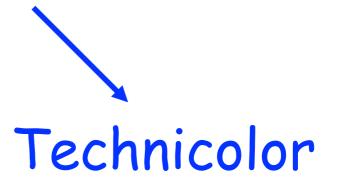
Monopoles, Anomalies, and Electroweak Symmetry Breaking

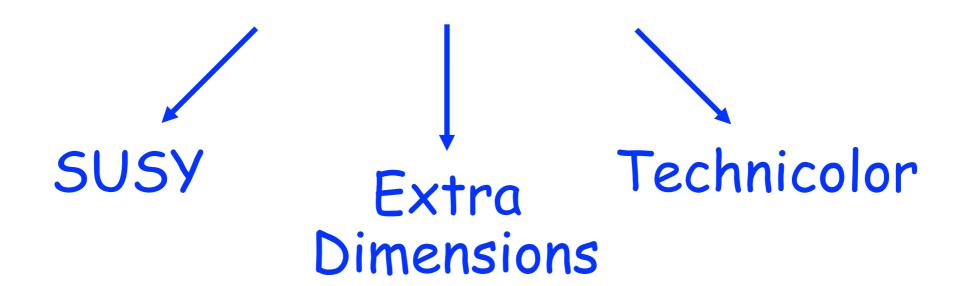
John Terning with Csaba Csaki, Yuri Shirman in progress

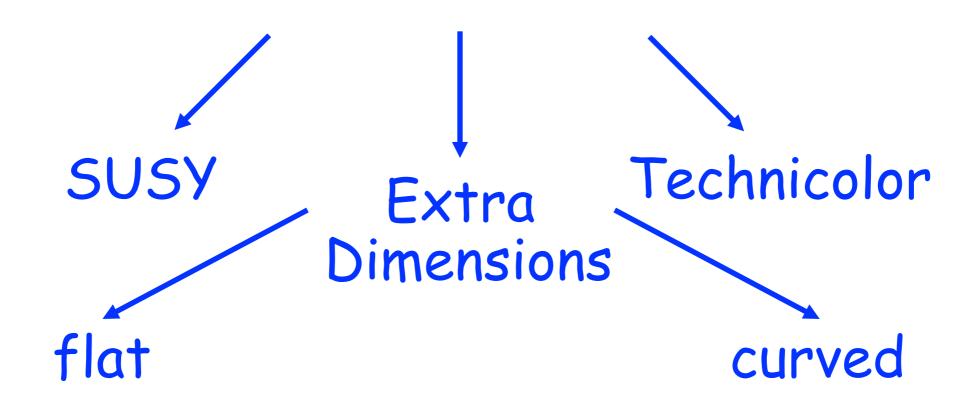
Outline

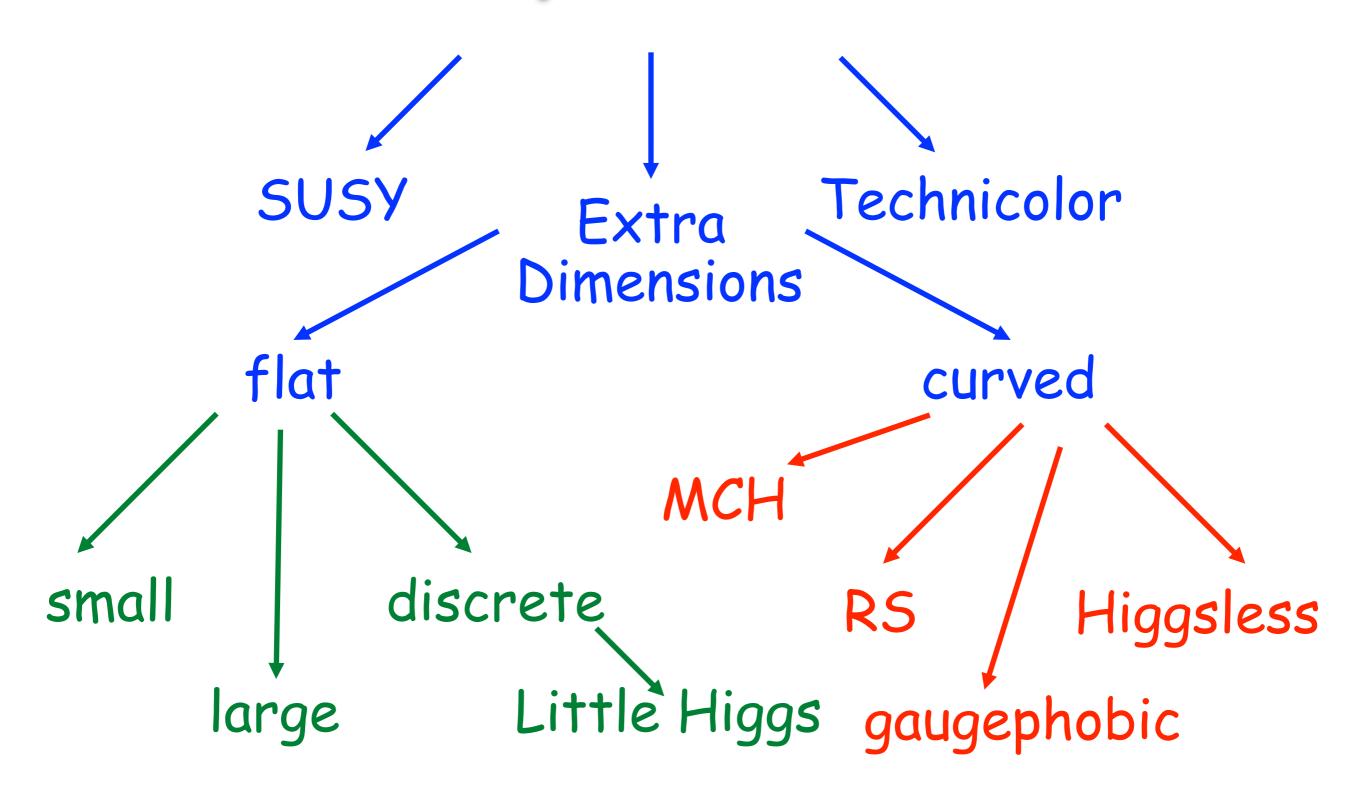
- Motivation
- A Brief History of Monopoles
- * Anomalies
- * Models
- * LHC
- Conclusions



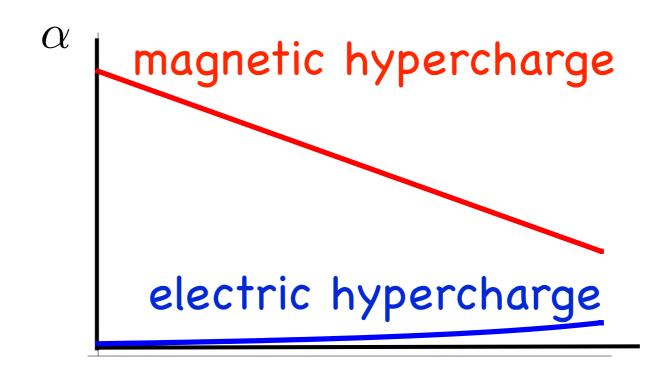








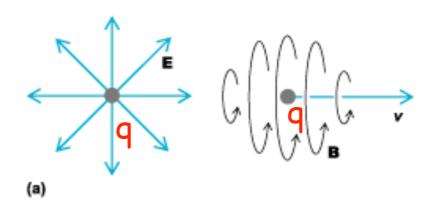
The Vision Thing

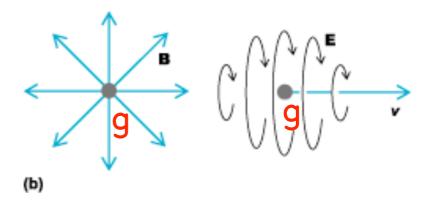


 $$\ln \mu$$ consistent theory of massless dyons? chiral symmetry breaking -> EWSB?

J.J. Thomson



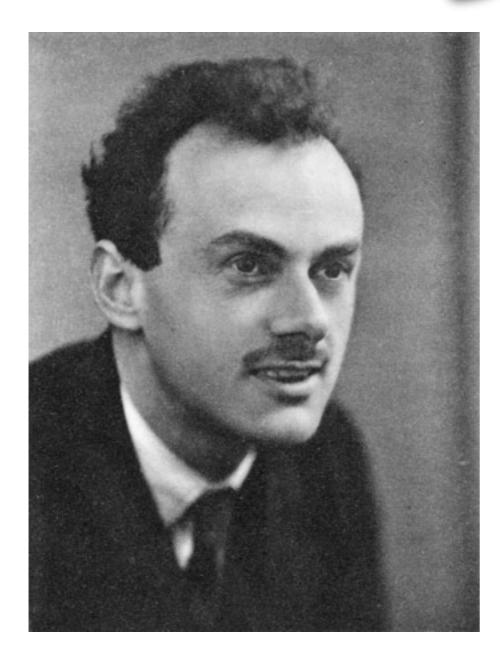




$$J = q g$$

Philos. Mag. 8 (1904) 331

Dirac

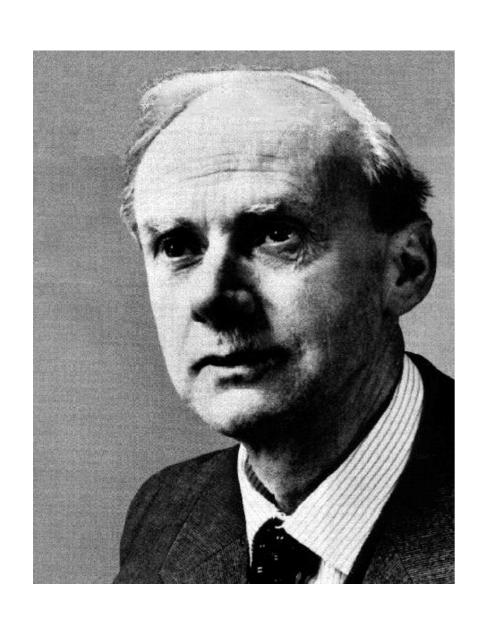


$$q = \frac{n}{2}$$

charge quantization

Proc. Roy. Soc. Lond. A133 (1931) 60

Dirac



non-local action?

$$F_{\mu\nu} = \partial_{\mu}A_{\nu} - \partial_{\nu}A_{\mu} + {}^*G_{\mu\nu}$$

$$G_{\mu\nu}(x) = 4\pi (n \cdot \partial)^{-1} [n_{\mu} *j_{\nu}(x) - n_{\nu} *j_{\mu}(x)]$$

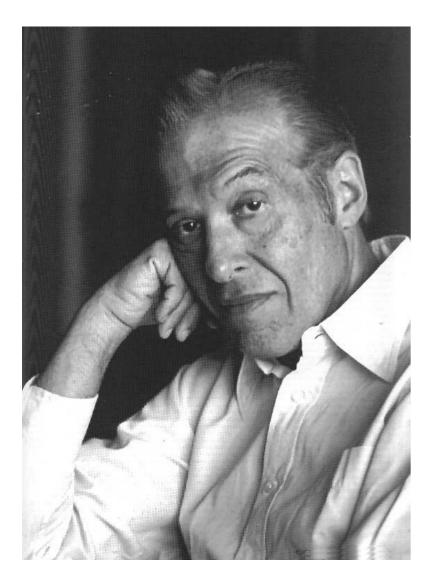
$$= \int (dy) [f_{\mu}(x - y) *j_{\nu}(y) - f_{\nu}(x - y) *j_{\mu}(y)]$$

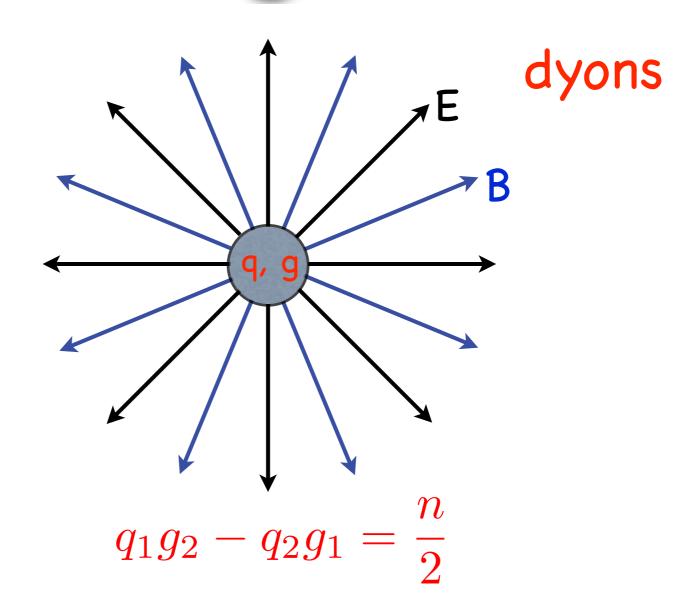
$$\partial_{\mu} f^{\mu}(x) = 4\pi \delta(x)$$

$$f^{\mu}(x) = 4\pi n^{\mu} (n \cdot \partial)^{-1} \delta(x)$$

Phys. Rev. 74 (1948) 817

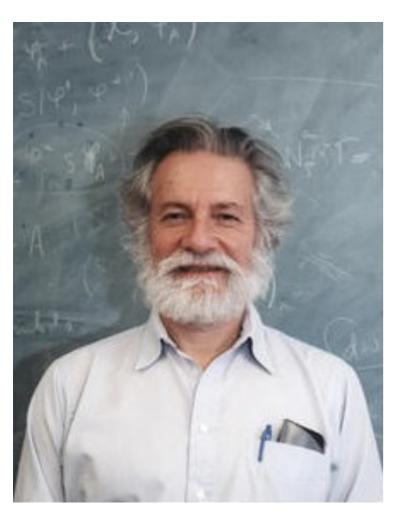
Schwinger





Science 165 (1969) 757

Zwanziger



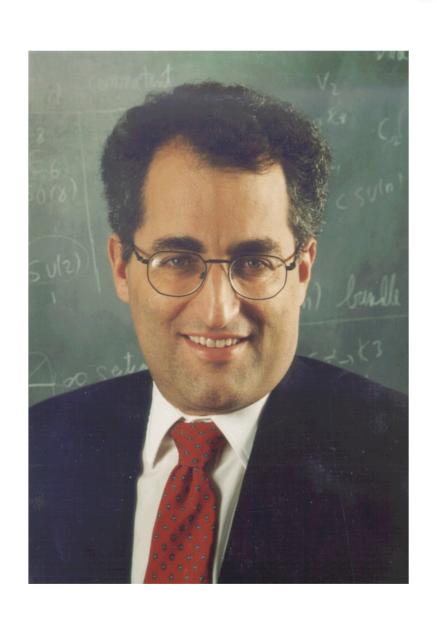
non-Lorentz invariant, local action?

$$\mathcal{L} = -\frac{1}{2n^2e^2} \left\{ \left[n \cdot (\partial \wedge A) \right] \cdot \left[n \cdot^* (\partial \wedge B) \right] - \left[n \cdot (\partial \wedge B) \right] \cdot \left[n \cdot^* (\partial \wedge A) \right] + \left[n \cdot (\partial \wedge A) \right]^2 + \left[n \cdot (\partial \wedge B) \right]^2 \right\} - J \cdot A - \frac{4\pi}{e^2} K \cdot B.$$

$$F = \frac{1}{n^2} \left(\left\{ n \wedge \left[n \cdot (\partial \wedge A) \right] \right\} - * \left\{ n \wedge \left[n \cdot (\partial \wedge B) \right] \right\} \right)$$

Phys. Rev. D3 (1971) 880

Witten



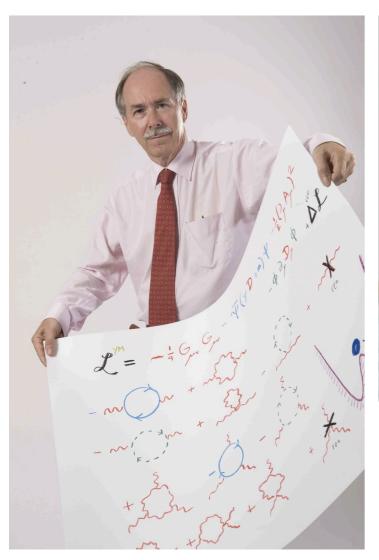
effective charge shifted

$$\mathcal{L}_{\text{free}} = -\frac{1}{4e^2} F^{\mu\nu} F_{\mu\nu} - \frac{\theta}{32\pi^2} F^{\mu\nu} * F_{\mu\nu}$$

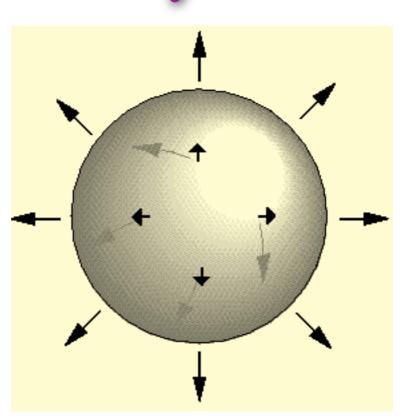
$$q_{\text{eff},j} = q_j + g_j \frac{\theta}{2\pi}$$

Phys. Lett. B86 (1979) 283

't Hooft-Polyakov



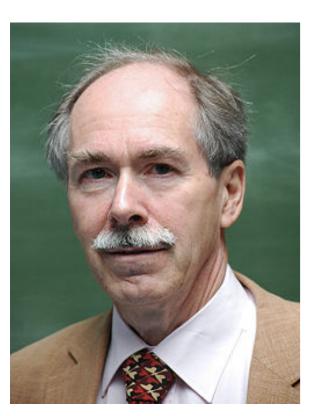




topological monopoles

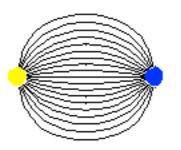
Nucl. Phys., B79 1974, 276 JETP Lett., 20 1974, 194

't Hooft-Mandelstam





magnetic condensate confines electric charge

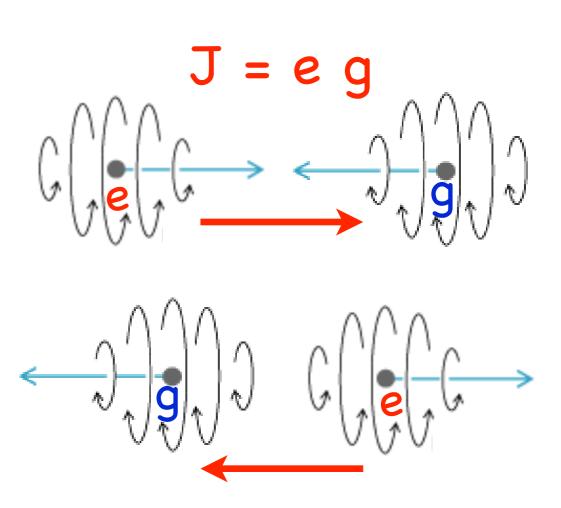


High Energy Physics Ed. Zichichi, (1976) 1225 Phys. Rept. 23 (1976) 245

Rubakov-Callan







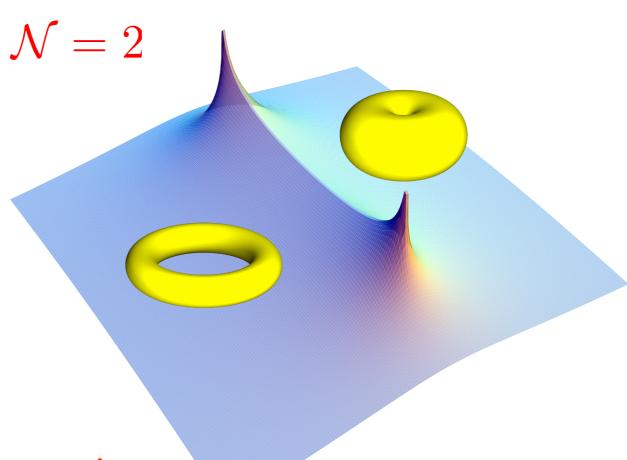
new unsuppressed contact interactions!

JETP Lett. 33 (1981) 644 Phys. Rev. D25 (1982) 2141

Seiberg-Witten



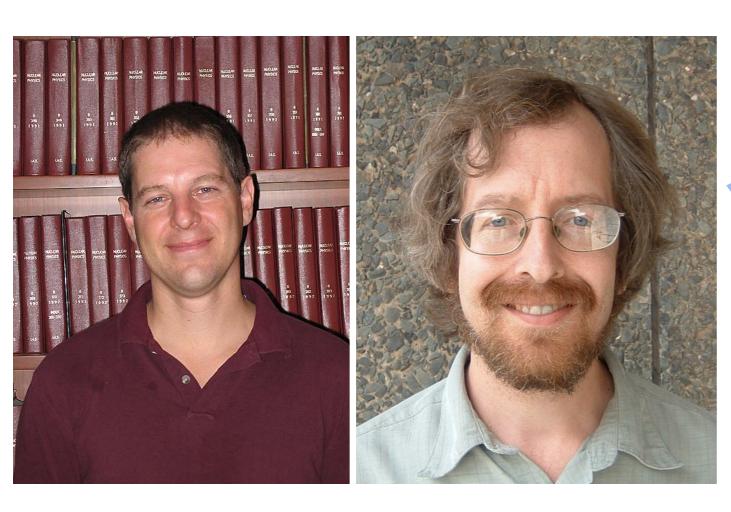


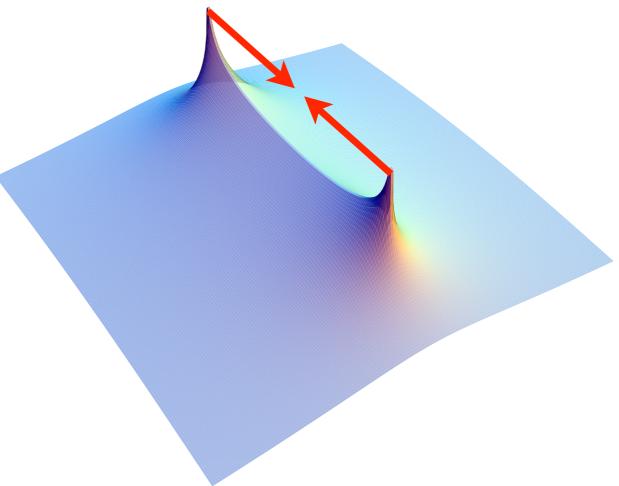


massless fermionic monopoles

hep-th/9407087

Argyres-Douglas





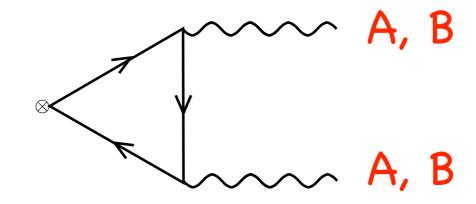
CFT with massless electric and magnetic charges hep-th/9505062

Toy Model

is this anomaly free?

Anomalies

$$\mathcal{L} = -\frac{1}{2n^2e^2} \left\{ \left[n \cdot (\partial \wedge A) \right] \cdot \left[n \cdot^* (\partial \wedge B) \right] - \left[n \cdot (\partial \wedge B) \right] \cdot \left[n \cdot^* (\partial \wedge A) \right] + \left[n \cdot (\partial \wedge A) \right]^2 + \left[n \cdot (\partial \wedge B) \right]^2 \right\} - J \cdot A - \frac{4\pi}{e^2} K \cdot B.$$



E-M Duality

$$\vec{E} \rightarrow \vec{B}$$
 $\vec{B} \rightarrow -\vec{E}$

$$*F^{\mu\nu} = \frac{1}{2} \epsilon^{\mu\nu\alpha\beta} F_{\alpha\beta}$$
$$F^{\mu\nu} \to *F^{\mu\nu}$$

Shift Symmetry

$$\mathcal{L}_{\text{free}} = -\frac{1}{4e^2} F^{\mu\nu} F_{\mu\nu} - \frac{\theta}{32\pi^2} F^{\mu\nu} * F_{\mu\nu}$$

$$\theta \to \theta + 2\pi$$

$$\tau \equiv \frac{\theta}{2\pi} + \frac{4\pi i}{e^2}$$

E-M Duality

$$\mathcal{L}_{\text{free}} = -\text{Im}\,\frac{\tau}{32\pi}\left(F^{\mu\nu} + i^*F^{\mu\nu}\right)^2$$

$$\mathcal{L}_c = \frac{1}{4\pi} \int d^4 B_\mu \partial_\nu * F^{\mu\nu}$$

$$\tilde{\mathcal{L}} = \operatorname{Im} \frac{1}{32\pi\tau} \left(\tilde{F}^{\mu\nu} + i^* \tilde{F}^{\mu\nu} \right)^2$$

$$\tilde{F}_{\mu\nu} = \partial_{\mu}B_{\nu} - \partial_{\nu}B_{\mu}$$

SL(2,Z)

$$au\equiv rac{ heta}{2\pi}+rac{4\pi i}{e^2} \qquad S: au o -rac{1}{ au} \qquad T: au o au+1$$

$$au'=rac{a au+b}{c au+d} \qquad K^\mu o aK'^\mu+cJ'^\mu \ , \quad J^\mu o bK'^\mu+dJ'^\mu$$

$$K^{\mu} \rightarrow aK'^{\mu} + cJ'^{\mu}$$
, $J^{\mu} \rightarrow bK'^{\mu} + dJ'^{\mu}$
$$ad - bc = 1$$

not a symmetry

ß from SL(2,Z)

$$\frac{d\tau}{d\log\mu} = \beta$$

$$\begin{pmatrix} a & -b \\ -c & d \end{pmatrix} \begin{pmatrix} q \\ g \end{pmatrix} = \begin{pmatrix} n \\ 0 \end{pmatrix} \qquad n = \gcd(q, g)$$

$$c = g/n, d = q/n$$
 $aq - bg = n$

$$\frac{d\tau'}{d\log\mu} = i\frac{n^2}{16\pi^2}$$

$$\frac{d\tau}{d\log\mu} = \frac{i}{16\pi^2}(q+g\tau)^2$$

ß from SL(2,Z)

$$\frac{d\tau}{d\log\mu} = \frac{i}{16\pi^2}(q+g\tau)^2$$

$$\beta_{e} = \mu \frac{de}{d\mu} = \frac{e^{3}}{12\pi^{2}} \sum_{j} \left[\left(q_{j} + \frac{\theta}{2\pi} g_{j} \right)^{2} - g_{j}^{2} \frac{16\pi^{2}}{e^{4}} \right]$$

$$\beta_{\theta} = \mu \frac{d\theta}{d\mu} = -\frac{16\pi}{3} \sum_{j} \left[q_{j}g_{j} + \frac{\theta}{2\pi} g_{j}^{2} \right]$$

Argyres, Douglas hep-th/9505062

SL(2,Z)

$$\frac{\operatorname{Im}(\tau)}{4\pi} \,\partial_{\mu} \left(F^{\mu\nu} + i * F^{\mu\nu} \right) = J^{\nu} + \tau K^{\nu}$$

$$K^{\mu} \to aK'^{\mu} + cJ'^{\mu}, J^{\mu} \to bK'^{\mu} + dJ'^{\mu}$$

 $(F^{\mu\nu} + i^*F^{\mu\nu}) \to \frac{1}{c\tau^* + d} (F'^{\mu\nu} + i^*F'^{\mu\nu})$

$$\frac{\text{Im}(\tau')}{4\pi} \,\partial_{\nu} \left(F'^{\mu\nu} + i * F'^{\mu\nu} \right) = J'^{\mu} + \tau' K'^{\mu}$$

Zwanziger Generalized

$$\mathcal{L} = -\operatorname{Im} \frac{\tau}{8\pi n^2} \left\{ \left[n \cdot \partial \wedge (A+iB) \right] \cdot \left[n \cdot \partial \wedge (A-iB) \right] \right\}$$
$$-\operatorname{Re} \frac{\tau}{8\pi n^2} \left\{ \left[n \cdot \partial \wedge (A+iB) \right] \cdot \left[n \cdot^* \partial \wedge (A-iB) \right] \right\}$$
$$+\operatorname{Re} \left[\left(A-iB \right) \cdot \left(J+\tau K \right) \right]$$

$$F = \frac{1}{n^2} \left(\left\{ n \wedge \left[n \cdot (\partial \wedge A) \right] \right\} - * \left\{ n \wedge \left[n \cdot (\partial \wedge B) \right] \right\} \right)$$

$$(A+iB) \to \frac{1}{c\tau^* + d} (A' + iB')$$

Axial Anomaly from SL(2,Z)

$$(q,g) \to (n,0)$$

$$\partial_{\mu} j_A^{\mu}(x) = \frac{n^2}{16\pi^2} F'^{\mu\nu} * F'_{\mu\nu}$$

$$= \frac{n^2}{32\pi^2} \operatorname{Im} (F'^{\mu\nu} + i * F'^{\mu\nu})^2$$

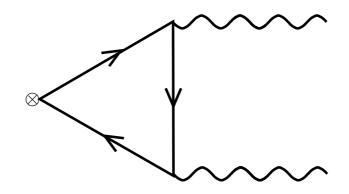
Axial Anomaly

$$\partial_{\mu} j_{A}^{\mu}(x) = \frac{n^{2}}{32\pi^{2}} \operatorname{Im} (c\tau^{*} + d)^{2} (F^{\mu\nu} + i^{*}F^{\mu\nu})^{2}$$

$$= \frac{1}{16\pi^{2}} \operatorname{Re} (q + \tau^{*}g)^{2} F^{\mu\nu} * F_{\mu\nu} + \frac{1}{16\pi^{2}} \operatorname{Im} (q + \tau^{*}g)^{2} F^{\mu\nu} F_{\mu\nu}$$

$$= \frac{1}{16\pi^{2}} \left\{ \left[\left(q + \frac{\theta}{2\pi} g \right)^{2} - g^{2} \frac{16\pi^{2}}{e^{4}} \right] F^{\mu\nu} * F_{\mu\nu} + \left[qg + \frac{\theta}{2\pi} g^{2} \right] F^{\mu\nu} F_{\mu\nu} \right\}$$

Axial Anomaly



$$\partial_{\mu} j_A^{\mu}(x) = \frac{1}{16\pi^2} \left\{ \left[q^2 - g^2 \frac{16\pi^2}{e^4} \right] F^{\mu\nu} * F_{\mu\nu} + qg F^{\mu\nu} F_{\mu\nu} \right\}$$

$SU(N)^2U(1)$ Anomaly

$$\mathcal{L}_{\text{anom}} = c \Omega G^{a\mu\nu} * G^a_{\mu\nu}$$

$$\Omega = \Omega_A + i\,\Omega_B$$

$$\Omega \to \frac{1}{c\tau^* + d} \; \Omega'$$

$SU(N)^2U(1)$ Anomaly

$$\mathcal{L}_{anom} = \frac{n \operatorname{Tr} T^{a}(r) T^{a}(r)}{16\pi^{2}} \Omega'_{A} G^{a\mu\nu} * G^{a}_{\mu\nu}
= \frac{n \operatorname{Tr} T^{a}(r) T^{a}(r)}{16\pi^{2}} \operatorname{Re} \Omega' G^{a\mu\nu} * G^{a}_{\mu\nu}
= \frac{n T(r)}{16\pi^{2}} \operatorname{Re} (c\tau^{*} + d) \Omega G^{a\mu\nu} * G^{a}_{\mu\nu}
= \frac{T(r)}{16\pi^{2}} \left[\left(q + \frac{\theta}{2\pi} g \right) \Omega_{A} + g \frac{4\pi}{e^{2}} \Omega_{B} \right] G^{a\mu\nu} * G^{a}_{\mu\nu}$$

U(1)³ Anomaly

$$\mathcal{L}_{\text{anom}} = \frac{n^3}{16\pi^2} \, \Omega'_A \, F'^{\mu\nu} \, {}^*F'_{\mu\nu} = \frac{n^3}{32\pi^2} \, \text{Re} \left[\Omega' \right] \, \text{Im} \left[\left(F'^{\mu\nu} + i \, {}^*F'_{\mu\nu} \right)^2 \right]$$

$$= \frac{n^3}{32\pi^2} \, \text{Re} \left[\left(c\tau^* + d \right) \Omega \right] \, \text{Im} \left[\left(c\tau^* + d \right)^2 \, \left(F^{\mu\nu} + i \, {}^*F_{\mu\nu} \right)^2 \right]$$

$$= \frac{1}{16\pi^2} \, \left[\left(q + \frac{\theta}{2\pi} g \right)^3 - \left(q + \frac{\theta}{2\pi} g \right) \frac{16\pi^2}{e^4} g^2 \right] \, \Omega_A \, F^{\mu\nu} \, {}^*F_{\mu\nu}$$

$$- \frac{1}{16\pi^2} \, \left[- \left(q + \frac{\theta}{2\pi} g \right)^2 \frac{4\pi}{e^2} g + \frac{64\pi^3}{e^6} g^3 \right] \, \Omega_B \, F^{\mu\nu} \, {}^*F_{\mu\nu}$$

$$- \frac{1}{8\pi^2} \, \left[\left(q + \frac{\theta}{2\pi} g \right)^2 \frac{4\pi}{e^2} g \, \Omega_A + \left(q + \frac{\theta}{2\pi} g \right) \frac{16\pi^2}{e^4} g^2 \, \Omega_B \right] \, F^{\mu\nu} \, F_{\mu\nu}$$

U(1)³ Anomaly

$$\sum_{j} q_{j}^{3} = 0$$

$$\sum_{j} q_{j} g_{j}^{2} = 0$$

$$\sum_{j} q_{j}^{2} g_{j} = 0$$

$$\sum_{j} g_{j}^{3} = 0$$

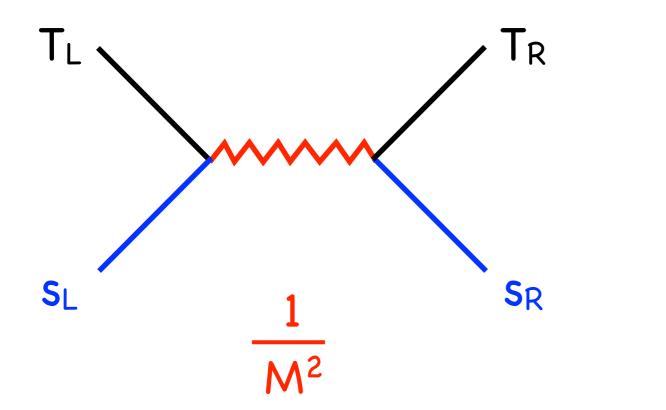
Toy Model

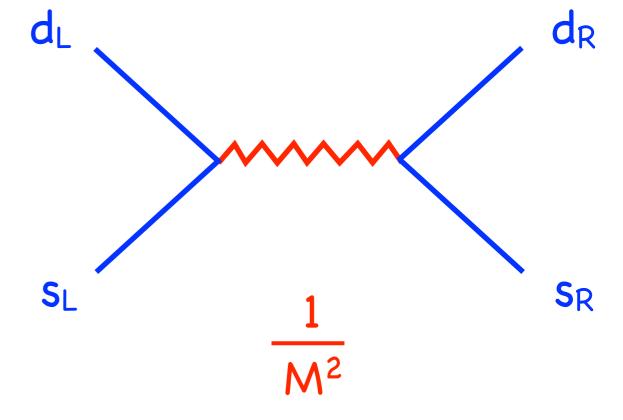
$$\sum_{j} q_{j}^{3} = 0 \; , \quad \sum_{j} g_{j}^{3} = 0 \; , \quad \sum_{j} g_{j}^{2} q_{j} = 0 \; , \quad \sum_{j} q_{j}^{2} g_{j} = 0 \; , \quad \sum_{j} q_{j} = 0 \; , \quad \sum_{j} q_{j} = 0 \; , \quad \sum_{j} q_{j} = 0 \; , \quad \sum_{j} \operatorname{Tr} T_{r_{j}}^{a} T_{r_{j}}^{b} q_{j} = 0 \; , \quad \sum_{j} \operatorname{Tr} T_{r_{j}}^{a} T_{r_{j}}^{b} q_{j} = 0 \; , \quad \sum_{j} \operatorname{Tr} T_{r_{j}}^{a} T_{r_{j}}^{b} q_{j} = 0 \; , \quad \sum_{j} \operatorname{Tr} T_{r_{j}}^{a} T_{r_{j}}^{b} q_{j} = 0 \; , \quad \sum_{j} \operatorname{Tr} T_{r_{j}}^{a} T_{r_{j}}^{b} q_{j} = 0 \; , \quad \sum_{j} \operatorname{Tr} T_{r_{j}}^{a} T_{r_{j}}^{b} q_{j} = 0 \; , \quad \sum_{j} \operatorname{Tr} T_{r_{j}}^{a} T_{r_{j}}^{b} q_{j} = 0 \; , \quad \sum_{j} \operatorname{Tr} T_{r_{j}}^{a} T_{r_{j}}^{b} q_{j} = 0 \; , \quad \sum_{j} \operatorname{Tr} T_{r_{j}}^{a} T_{r_{j}}^{b} q_{j} = 0 \; , \quad \sum_{j} \operatorname{Tr} T_{r_{j}}^{a} T_{r_{j}}^{b} q_{j} = 0 \; , \quad \sum_{j} \operatorname{Tr} T_{r_{j}}^{a} T_{r_{j}}^{b} q_{j} = 0 \; , \quad \sum_{j} \operatorname{Tr} T_{r_{j}}^{a} T_{r_{j}}^{b} q_{j} = 0 \; , \quad \sum_{j} \operatorname{Tr} T_{r_{j}}^{a} T_{r_{j}}^{b} q_{j} = 0 \; , \quad \sum_{j} \operatorname{Tr} T_{r_{j}}^{a} T_{r_{j}}^{b} q_{j} = 0 \; , \quad \sum_{j} \operatorname{Tr} T_{r_{j}}^{a} T_{r_{j}}^{b} q_{j} = 0 \; , \quad \sum_{j} \operatorname{Tr} T_{r_{j}}^{a} T_{r_{j}}^{b} q_{j} = 0 \; , \quad \sum_{j} \operatorname{Tr} T_{r_{j}}^{a} T_{r_{j}}^{b} q_{j} = 0 \; , \quad \sum_{j} \operatorname{Tr} T_{r_{j}}^{a} T_{r_{j}}^{b} q_{j} = 0 \; , \quad \sum_{j} \operatorname{Tr} T_{r_{j}}^{a} T_{r_{j}}^{b} q_{j} = 0 \; , \quad \sum_{j} \operatorname{Tr} T_{r_{j}}^{a} T_{r_{j}}^{b} T_{r_{j}}^{b} q_{j} = 0 \; , \quad \sum_{j} \operatorname{Tr} T_{r_{j}}^{a} T_{r_{j}}^{b} T_{r_{j}}^{b} q_{j} = 0 \; , \quad \sum_{j} \operatorname{Tr} T_{r_{j}}^{a} T_{r_{j}}^{b} T_$$

Dynamics

Quark Masses

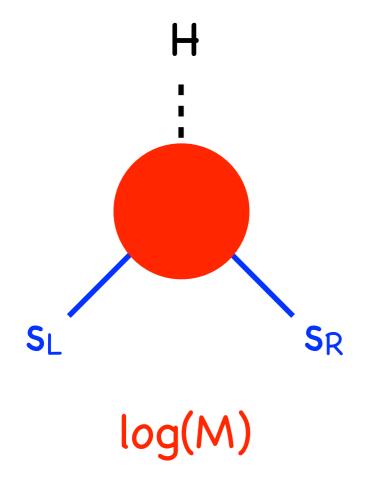
technicolor: fail

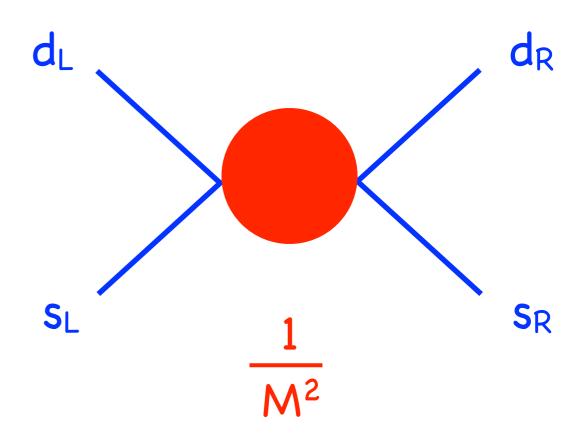




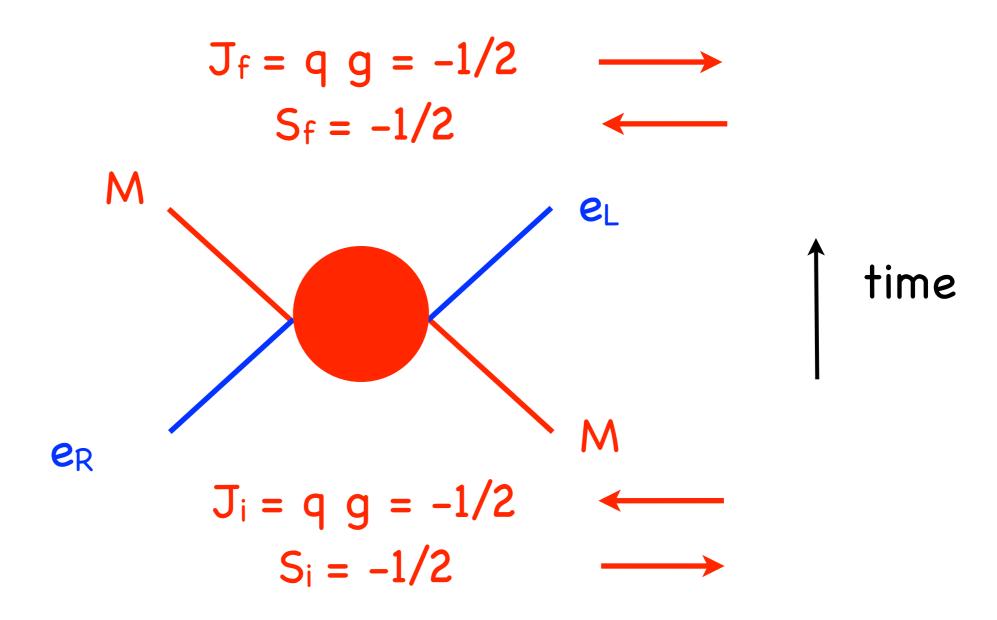
Quark Masses

Standard Model





Callan-Rubakov



New dimension 4, four particle operator

$$J_{f} = q g = 1/2$$

$$S_{f} = -1$$

$$U_{R}$$

$$\uparrow_{L}$$

$$\uparrow_{R}$$

$$U_{L}$$

$$J_{i} = q g = 2$$

$$S_{i} = 1$$

$$\uparrow_{R}$$

$$\downarrow_{L}$$

$$\downarrow_{R}$$

$$J_{f} = q g = 1/2$$

$$S_{f} = -1$$

$$U_{R}$$

$$\uparrow_{L}$$

$$\uparrow_{R}$$

$$U_{L}$$

$$J_{i} = q g = 2$$

$$S_{i} = 1$$

$$fail!$$

$$J_f = q g = 2$$

$$S_f = 0$$

$$U_R \qquad \uparrow_R$$

$$\uparrow_L \qquad \downarrow_U_L$$

$$J_i = q g = 1/2$$

$$S_i = 0$$

$$\uparrow_L \qquad \downarrow_U$$

$$J_f = q g = 2$$

$$S_f = 0$$

$$U_R \qquad \uparrow_R$$

$$\downarrow \qquad \qquad \uparrow_L \qquad \qquad \downarrow_L$$

$$J_i = q g = 1/2$$

$$S_i = 0$$

$$fail!$$

non-Abelian magnetic charge

$$Q = T^3 + Y$$

$$Q_m = T_m^3 + Y_m$$

explicit examples known in GUT models

EWSB is forced to align with the monopole charge

non-Abelian magnetic charge

$$Q = T^3 + Y$$

$$e^{2\pi iQ} = e^{2\pi iT^3} e^{2\pi iY}$$

$$= \operatorname{diag}(e^{i\frac{1}{2}2\pi}, e^{-i\frac{1}{2}2\pi})$$

$$= Z$$

$$(SU(2)_L \times U(1)_Y)/Z_2$$

The Model

 $(SU(3)_c \times SU(2)_L \times U(1)_Y)/Z_6$

| | $SU(3)_c$ | $U(1)_{em}:q$ | $U(1)_{em}:g$ | $U(1)_Y:q$ | $U(1)_Y:g$ |
|------------------|-----------|----------------|---------------|-------------------|------------|
| $\overline{U_L}$ | d | $\frac{2}{3}$ | 1 | $\frac{1}{6}$ | 1 |
| D_L | d | $-\frac{1}{3}$ | 1 | $\frac{1}{6}$ | 1 |
| N_L | 1 | 0 | -3 | $-\frac{1}{2}$ | -3 |
| E_L | 1 | -1 | -3 | $-\frac{1}{2}$ | -3 |
| U_R | d | $\frac{2}{3}$ | 1 | $\frac{2}{3}^{2}$ | 1 |
| D_R | d | $-\frac{3}{1}$ | 1 | $-\frac{3}{1}$ | 1 |
| N_R | 1 | 0 | -3 | 0 | -3 |
| E_{R} | 1 | -1 | -3 | 1 | -3 |

$$\alpha_m = \frac{1}{4\alpha} \approx 32$$

$$J_f = \frac{1}{3} + \frac{2}{3} \cdot 1$$

$$S_f = +1$$

$$U_L \qquad t_R$$

$$\downarrow \qquad \qquad \downarrow \qquad \qquad \uparrow$$

$$t_L \qquad \qquad \downarrow \qquad \qquad \downarrow$$

$$J_i = \frac{1}{3} + \left(\frac{1}{2} + \frac{1}{6}\right) \cdot 1$$

$$S_i = -1$$

$$J_f = \frac{1}{3} + \frac{2}{3} \cdot 1$$

$$S_f = +1$$

$$U_L \qquad \dagger_R$$

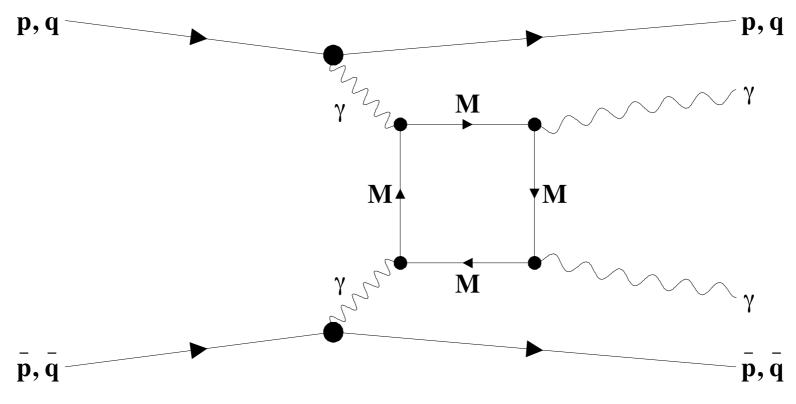
$$\uparrow_L \qquad \downarrow \qquad \downarrow_R$$

$$J_i = \frac{1}{3} + \left(\frac{1}{2} + \frac{1}{6}\right) \cdot 1$$

$$S_i = -1$$

$$hooray!$$

Phenomenology

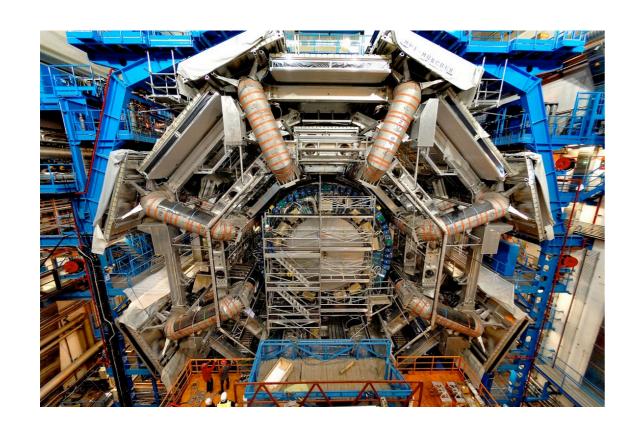


uncontrolled perturbation theory

Ginzburg, Schiller hep-th/9802310

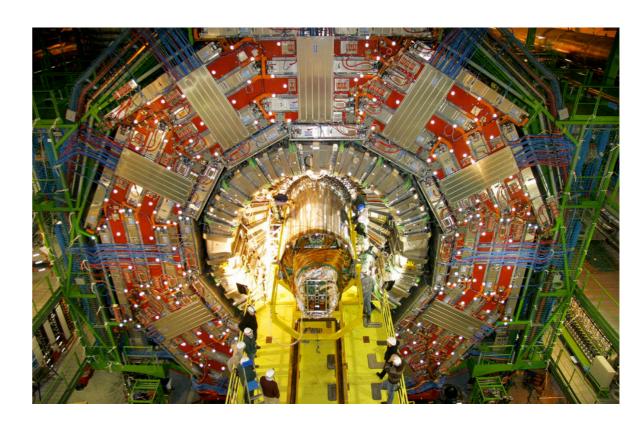


pair production, unconfined, highly ionizing



ATLAS has a trigger for monopoles





CMS does not



Conclusions

Monopoles are still fascinating after all these years

Anomalies for monopoles can be easily calculated

monopoles can break EWS and give the top quark a large mass

the LHC could be very exciting