

# $B \rightarrow K^* \mu^+ \mu^-$ : hadronic effects or new physics

**Siavash Neshatpour**

Lyon University, IP2I

[Based on Phys. Rev. D 102, 055001 \(2020\)](#)

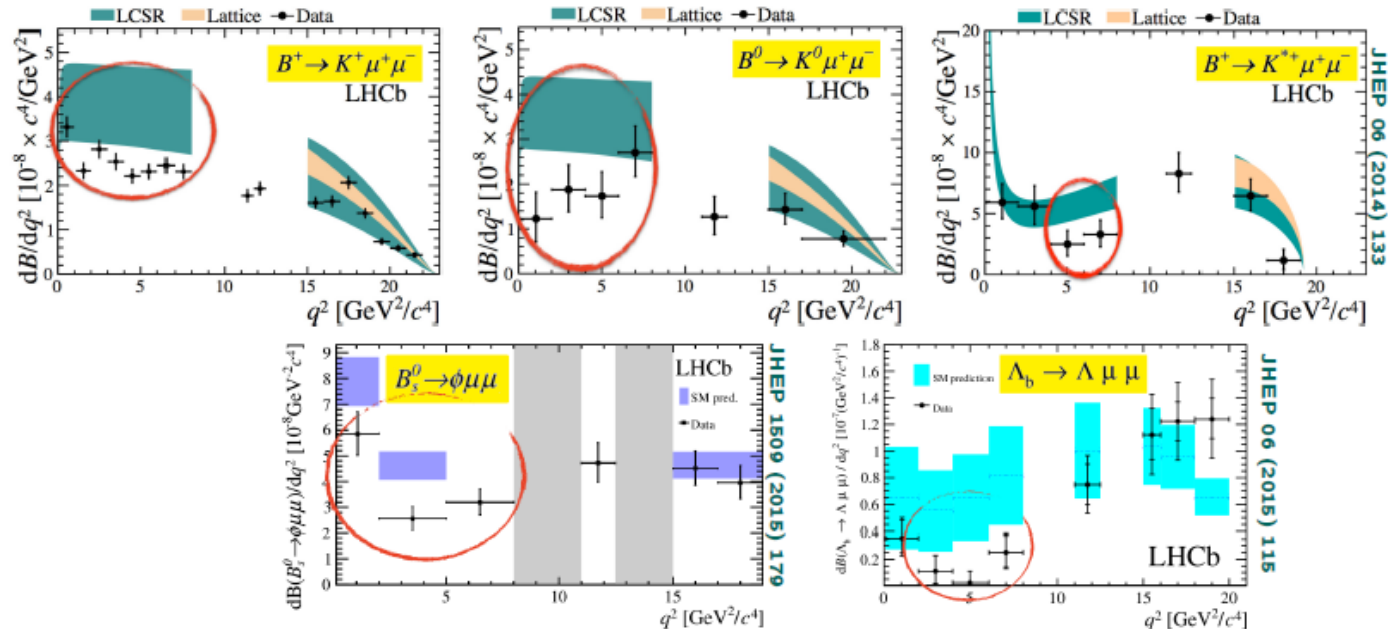
In collaboration with T. Hurth, N. Mahmoudi

GDR-InF annual workshop

Several deviations (“anomalies”) with respect to the SM predictions in  $b \rightarrow s \ell \ell$  measurements

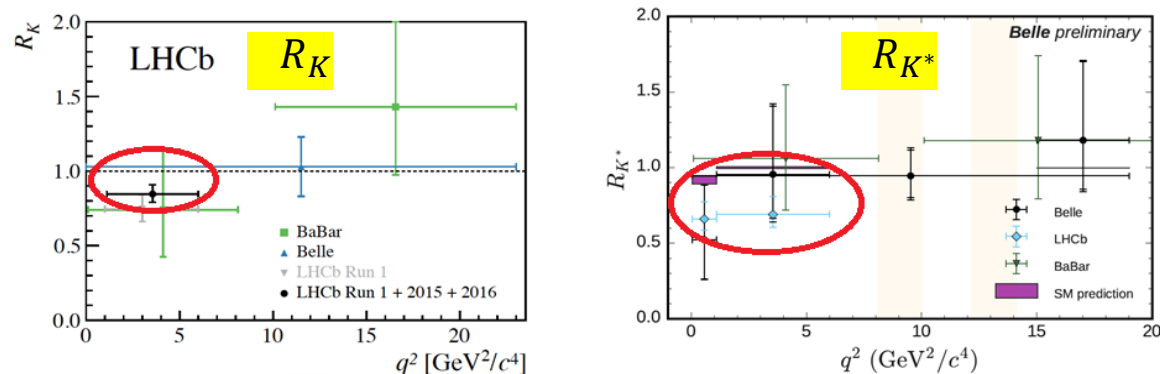
## ○ Branching fractions:

- $B \rightarrow K \mu^+ \mu^-$
- $B \rightarrow K^* \mu^+ \mu^-$
- $B_s \rightarrow \phi \mu^+ \mu^-$
- $\Lambda_b \rightarrow \Lambda \mu^+ \mu^-$



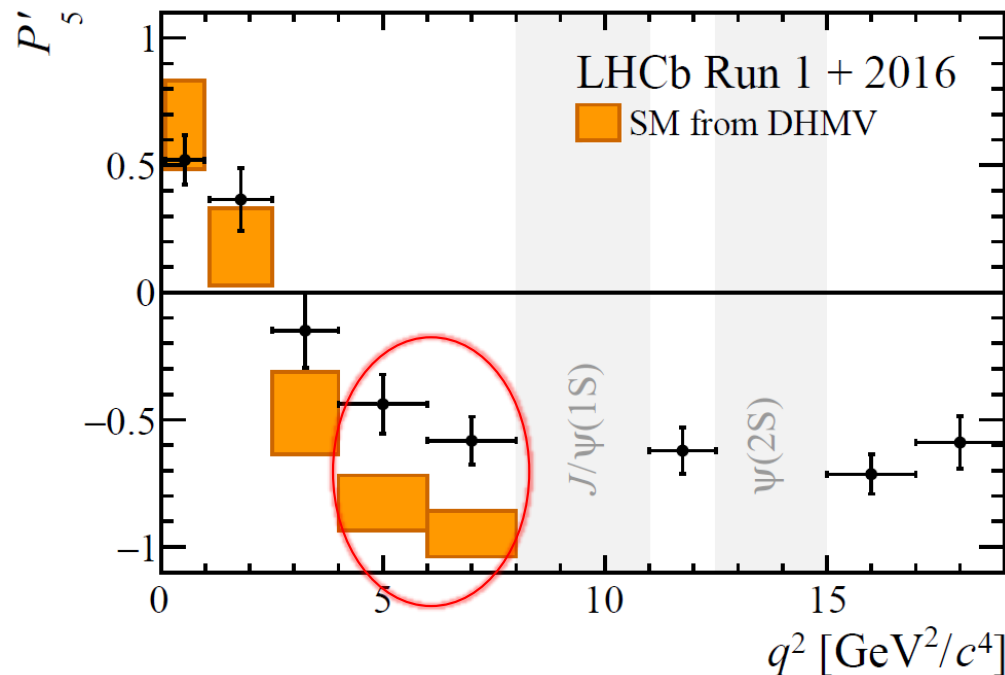
## ○ Lepton flavour violating ratios:

- $R_K$
- $R_{K^*}$



Several deviations (“anomalies”) with respect to the SM predictions in  $b \rightarrow s \ell \ell$  measurements

- Long standing anomaly in the  $B \rightarrow K^* \mu^+ \mu^-$  angular observable  $P'_5 / S_5$  ( $= P'_5 \times \sqrt{F_L(1 - F_L)}$ )
  - 2013 LHCb ( $1 \text{ fb}^{-1}$ )
  - 2016 LHCb ( $3 \text{ fb}^{-1}$ )
  - 2020 LHCb ( $4.7 \text{ fb}^{-1}$ )



[E. Smith CERN Seminar '20  
LHCb 2003.04831]

- $2.5\sigma$  &  $2.9\sigma$  local tension in  $P'_5$  with the respect SM predictions (DHMV)
- deviations in other angular observables/bins

Effective Hamiltonian for  $b \rightarrow s \ell^+ \ell^-$  transitions:  $\mathcal{H}_{\text{eff}} = \mathcal{H}_{\text{eff}}^{\text{had}} + \mathcal{H}_{\text{eff}}^{\text{sl}}$

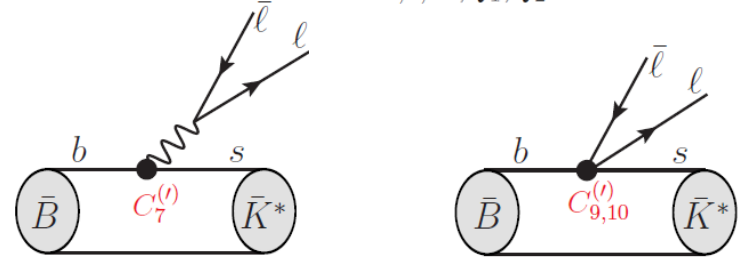
$$\mathcal{H}_{\text{eff}}^{\text{had}} = -\frac{4G_F}{\sqrt{2}} V_{tb} V_{ts}^* \left[ \sum_{i=1\dots 6} C_i(\mu) O_i(\mu) + C_8(\mu) O_8(\mu) \right]$$

$$\mathcal{H}_{\text{eff}}^{\text{sl}} = -\frac{4G_F}{\sqrt{2}} V_{tb} V_{ts}^* \left[ \sum_{i=7,9,10,Q_1,Q_2} C_i^{(\ell)}(\mu) O_i^{(\ell)}(\mu) \right]$$

Effective Hamiltonian for  $b \rightarrow s \ell^+ \ell^-$  transitions:  $\mathcal{H}_{\text{eff}} = \mathcal{H}_{\text{eff}}^{\text{had}} + \mathcal{H}_{\text{eff}}^{\text{sl}}$

$$\mathcal{H}_{\text{eff}}^{\text{had}} = -\frac{4G_F}{\sqrt{2}} V_{tb} V_{ts}^* \left[ \sum_{i=1 \dots 6} C_i(\mu) O_i(\mu) + C_8(\mu) O_8(\mu) \right]$$

$$\mathcal{H}_{\text{eff}}^{\text{sl}} = -\frac{4G_F}{\sqrt{2}} V_{tb} V_{ts}^* \left[ \sum_{i=7,9,10,Q_1,Q_2} C_i^{(\ell)}(\mu) O_i^{(\ell)}(\mu) \right]$$



factorisable contributions:

7 independent form factors  $\tilde{V}_{\pm,0}, \tilde{T}_{\pm,0}, \tilde{S}$

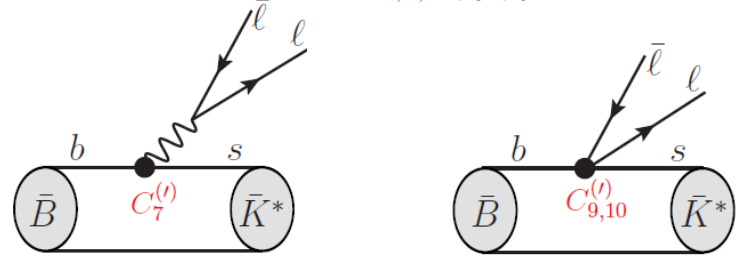
[Khodjamirian et al. '10, Bharucha et al. '15, Gubernari et al. '18]

## Theory framework: exclusive mode $B \rightarrow K^* \ell^+ \ell^-$

Effective Hamiltonian for  $b \rightarrow s \ell^+ \ell^-$  transitions:  $\mathcal{H}_{\text{eff}} = \mathcal{H}_{\text{eff}}^{\text{had}} + \mathcal{H}_{\text{eff}}^{\text{sl}}$

$$\mathcal{H}_{\text{eff}}^{\text{had}} = -\frac{4G_F}{\sqrt{2}} V_{tb} V_{ts}^* \left[ \sum_{i=1 \dots 6} C_i(\mu) O_i(\mu) + C_8(\mu) O_8(\mu) \right]$$

$$\mathcal{H}_{\text{eff}}^{\text{sl}} = -\frac{4G_F}{\sqrt{2}} V_{tb} V_{ts}^* \left[ \sum_{i=7,9,10,Q_1,Q_2} C_i^{(\prime)}(\mu) O_i^{(\prime)}(\mu) \right]$$



factorisable contributions:

7 independent form factors  $\tilde{V}_{\pm,0}, \tilde{T}_{\pm,0}, \tilde{S}$

[Khodjamirian et al. '10, Bharucha et al. '15, Gubernari et al. '18]

Helicity amplitudes:

$$H_V(\lambda) = -i N' \left\{ (C_9 - C_9') \tilde{V}_\lambda(q^2) + \frac{m_B^2}{q^2} \left[ \frac{2 \hat{m}_b}{m_B} (C_7^{\text{eff}} - C_7') \tilde{T}_\lambda(q^2) \right] \right\}$$

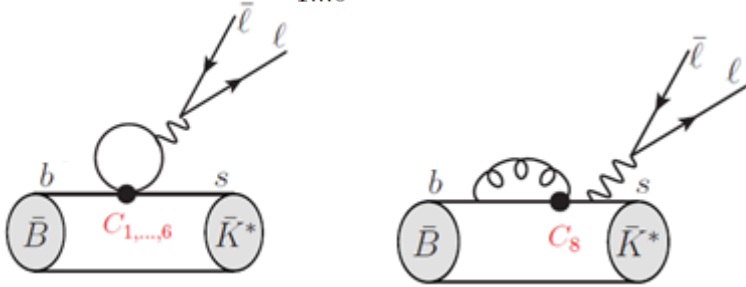
$$H_A(\lambda) = -i N' (C_{10} - C_{10}') \tilde{V}_\lambda(q^2)$$

$$H_P = i N' \left\{ \frac{2 m_\ell \hat{m}_b}{q^2} (C_{10} - C_{10}') \left( 1 + \frac{m_s}{m_b} \right) \tilde{S}(q^2) \right\}$$

# Theory framework: exclusive mode $B \rightarrow K^* \ell^+ \ell^-$

Effective Hamiltonian for  $b \rightarrow s \ell^+ \ell^-$  transitions:  $\mathcal{H}_{\text{eff}} = \mathcal{H}_{\text{eff}}^{\text{had}} + \mathcal{H}_{\text{eff}}^{\text{sl}}$

$$\mathcal{H}_{\text{eff}}^{\text{had}} = -\frac{4G_F}{\sqrt{2}} V_{tb} V_{ts}^* \left[ \sum_{i=1 \dots 6} C_i(\mu) O_i(\mu) + C_8(\mu) O_8(\mu) \right]$$



non-local effects: in general “naïve”  
factorization not applicable

$$\frac{e^2}{q^2} \epsilon_\mu L_V^\mu \left[ \underbrace{Y(q^2) \tilde{V}_\lambda}_{\text{fact., perturbative}} + \underbrace{\text{LO in } \mathcal{O}\left(\frac{\Lambda}{m_b}, \frac{\Lambda}{E_{K^*}}\right)}_{\text{non-fact., QCDf}} + \underbrace{h_\lambda(q^2)}_{\text{power corrections,}} \right]$$

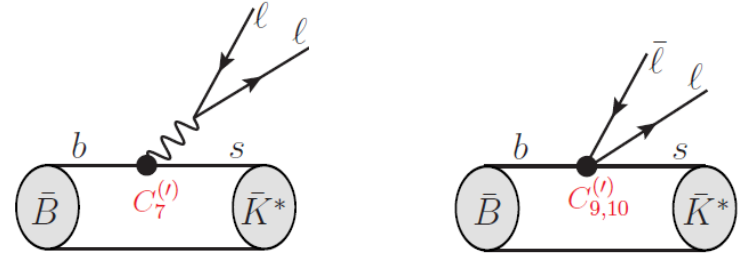
Helicity amplitudes:

$$H_V(\lambda) = -i N' \left\{ (C_9^{\text{eff}} - C_9') \tilde{V}_\lambda(q^2) + \frac{m_B^2}{q^2} \left[ \frac{2 \hat{m}_b}{m_B} (C_7^{\text{eff}} - C_7') \tilde{T}_\lambda(q^2) - 16 \pi^2 \mathcal{N}_\lambda(q^2) \right] \right\}$$

$$H_A(\lambda) = -i N' (C_{10} - C_{10}') \tilde{V}_\lambda(q^2)$$

$$H_P = i N' \left\{ \frac{2 m_\ell \hat{m}_b}{q^2} (C_{10} - C_{10}') \left( 1 + \frac{m_s}{m_b} \right) \tilde{S}(q^2) \right\}$$

$$\mathcal{H}_{\text{eff}}^{\text{sl}} = -\frac{4G_F}{\sqrt{2}} V_{tb} V_{ts}^* \left[ \sum_{i=7,9,10, Q_1, Q_2} C_i^{(\ell)}(\mu) O_i^{(\ell)}(\mu) \right]$$



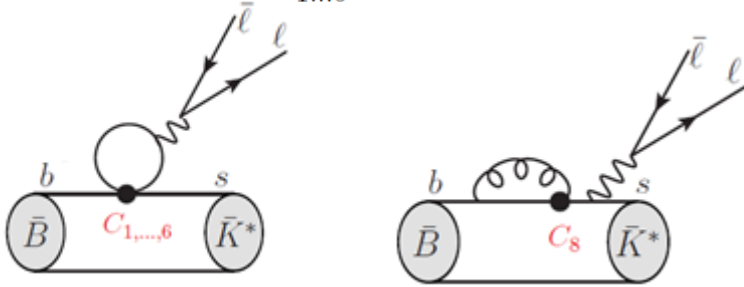
factorisable contributions:  
7 independent form factors  $\tilde{V}_{\pm,0}, \tilde{T}_{\pm,0}, \tilde{S}$

[Khodjamirian et al. '10, Bharucha et al. '15, Gubernari et al. '18]

❖ To distinguish hadronic effects from NP in  $C_{7,9}$   
good control over hadronic contributions needed

Effective Hamiltonian for  $b \rightarrow s \ell^+ \ell^-$  transitions:  $\mathcal{H}_{\text{eff}} = \mathcal{H}_{\text{eff}}^{\text{had}} + \mathcal{H}_{\text{eff}}^{\text{sl}}$

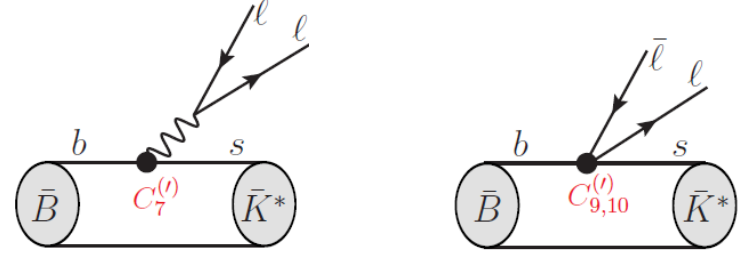
$$\mathcal{H}_{\text{eff}}^{\text{had}} = -\frac{4G_F}{\sqrt{2}} V_{tb} V_{ts}^* \left[ \sum_{i=1 \dots 6} C_i(\mu) O_i(\mu) + C_8(\mu) O_8(\mu) \right]$$



non-local effects: in general “naïve”  
factorization not applicable

$$\frac{e^2}{q^2} \epsilon_\mu L_V^\mu \left[ \underbrace{Y(q^2) \tilde{V}_\lambda}_{\text{fact., perturbative}} + \underbrace{\text{LO in } \mathcal{O}\left(\frac{\Lambda}{m_b}, \frac{\Lambda}{E_{K^*}}\right)}_{\text{non-fact., QCDf}} + \underbrace{h_\lambda(q^2)}_{\text{power corrections,}} \right]$$

$$\mathcal{H}_{\text{eff}}^{\text{sl}} = -\frac{4G_F}{\sqrt{2}} V_{tb} V_{ts}^* \left[ \sum_{i=7,9,10,Q_1,Q_2} C_i^{(\ell)}(\mu) O_i^{(\ell)}(\mu) \right]$$



factorisable contributions:  
7 independent form factors  $\tilde{V}_{\pm,0}, \tilde{T}_{\pm,0}, \tilde{S}$

[Khodjamirian et al. '10, Bharucha et al. '15, Gubernari et al. '18]

Calculated for low  $q^2$  at LO in QCD factorisation [Beneke et al. '01 & '04], but higher powers are unknown

- partial calculation with LCSR and dispersion relations [Khodjamirian et al. 1006.4945]
- recent progress exploiting analyticity of amplitudes [Bobeth et al. 1707.07305] & ongoing work by van Dyk et al.

See talk by M. Bordone

Power corrections often “guesstimated”

- Significance of tensions in  $B \rightarrow K^* \mu^+ \mu^-$  angular observables depends on the choice of “guesstimate” made for the size of the power corrections ( $h_\lambda$ )



## NP effect vs. hadronic contributions

Instead of making assumptions on the size of the power corrections  $h_\lambda$ , they can be parameterised by a general ansatz (compatible with the analyticity structure): [Jäger, Camalich, 1412.3183], [Ciuchini et al. 1512.07157]

$$h_{\pm,[0]} = \left[ \sqrt{q^2} \times \right] \left( h_{\pm,[0]}^{(0)} + q^2 h_{\pm,[0]}^{(1)} + q^4 h_{\pm,[0]}^{(2)} \right)$$

⇒ NP effects in  $C_9$  are embedded in the hadronic contributions [A. Arbey, T. Hurth, F. Mahmoudi, SN, 1806.02791]

Due to the embedding, fits to NP and hadronic contributions can be compared with the Wilks' test

## NP effect vs. hadronic contributions

Instead of making assumptions on the size of the power corrections  $h_\lambda$ , they can be parameterised by a general ansatz (compatible with the analyticity structure): [Jäger, Camalich, 1412.3183], [Ciuchini et al. 1512.07157]

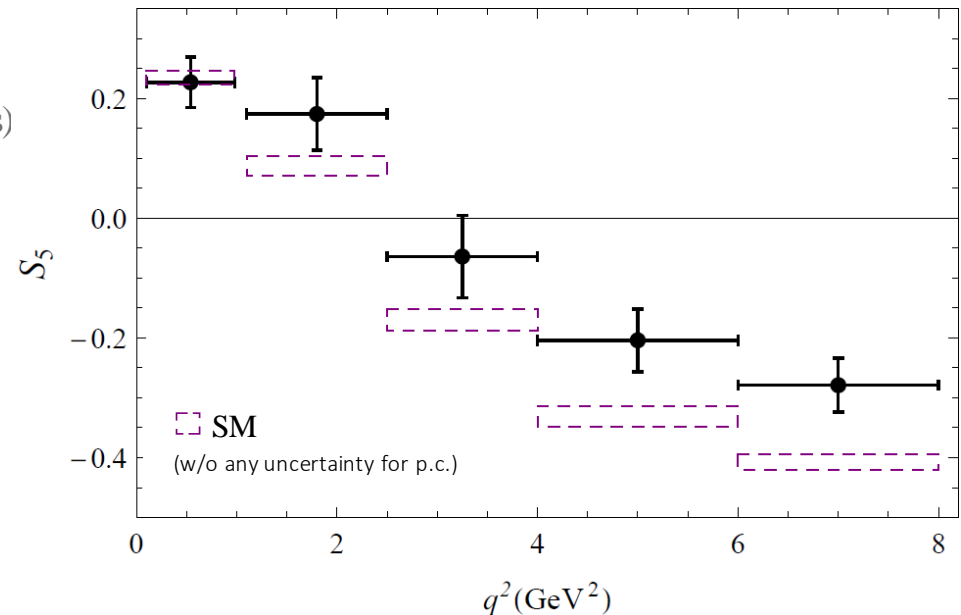
$$h_{\pm,[0]} = \left[ \sqrt{q^2} \times \right] \left( h_{\pm,[0]}^{(0)} + q^2 h_{\pm,[0]}^{(1)} + q^4 h_{\pm,[0]}^{(2)} \right)$$

⇒ NP effects in  $C_9$  are embedded in the hadronic contributions [A. Arbey, T. Hurth, F. Mahmoudi, SN, 1806.02791]

Due to the embedding, fits to NP and hadronic contributions can be compared with the Wilks' test

- Fit to
- Wilson coefficient  $\delta C_9^{\text{NP}}$
  - Hadronic quantities  $h_{+,-,0}^{(0,1,2)}$  (18 parameters)

**$B \rightarrow K^* \mu^+ \mu^-$  observables (low  $q^2$ )  
and  $\text{BR}(B \rightarrow K^* \gamma)$**



## NP effect vs. hadronic contributions

Instead of making assumptions on the size of the power corrections  $h_\lambda$ , they can be parameterised by a general ansatz (compatible with the analyticity structure): [Jäger, Camalich, 1412.3183], [Ciuchini et al. 1512.07157]

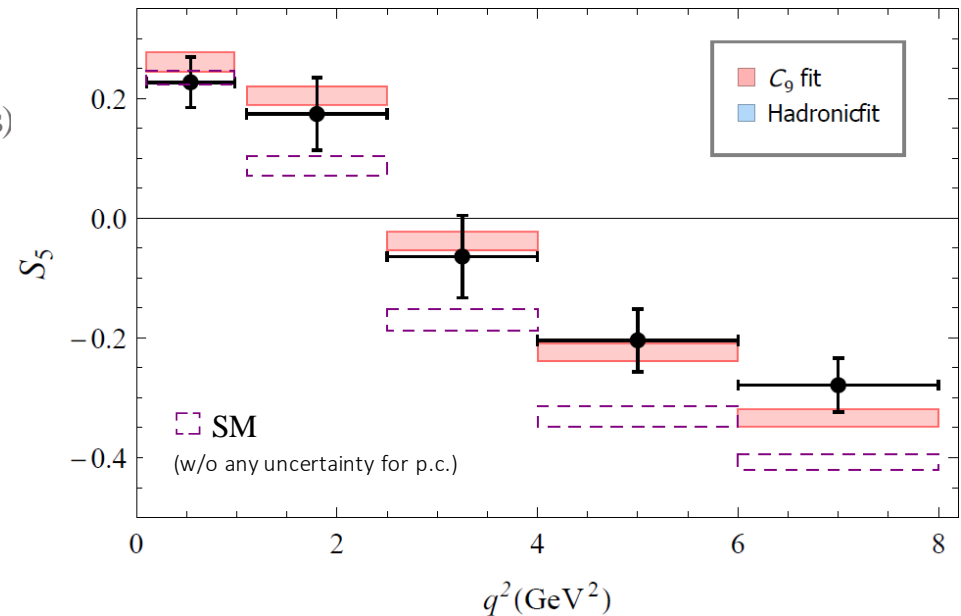
$$h_{\pm,[0]} = \left[ \sqrt{q^2} \times \right] \left( h_{\pm,[0]}^{(0)} + q^2 h_{\pm,[0]}^{(1)} + q^4 h_{\pm,[0]}^{(2)} \right)$$

⇒ NP effects in  $C_9$  are embedded in the hadronic contributions [A. Arbey, T. Hurth, F. Mahmoudi, SN, 1806.02791]

Due to the embedding, fits to NP and hadronic contributions can be compared with the Wilks' test

- Fit to
- Wilson coefficient  $\delta C_9^{\text{NP}}$
  - Hadronic quantities  $h_{+,-,0}^{(0,1,2)}$  (18 parameters)

$B \rightarrow K^* \mu^+ \mu^-$ observables (low $q^2$ ) and $\text{BR}(B \rightarrow K^* \gamma)$		
	Real $\delta C_9$ (1)	Hadronic fit (18)
Plain SM	$6.0\sigma$	$4.7\sigma$



➤ Fit to  $\delta C_9$  improves description of the data with  $6\sigma$  compared to the SM (w/o any uncertainty for p.c.)

## NP effect vs. hadronic contributions

Instead of making assumptions on the size of the power corrections  $h_\lambda$ , they can be parameterised by a general ansatz (compatible with the analyticity structure): [Jäger, Camalich, 1412.3183], [Ciuchini et al. 1512.07157]

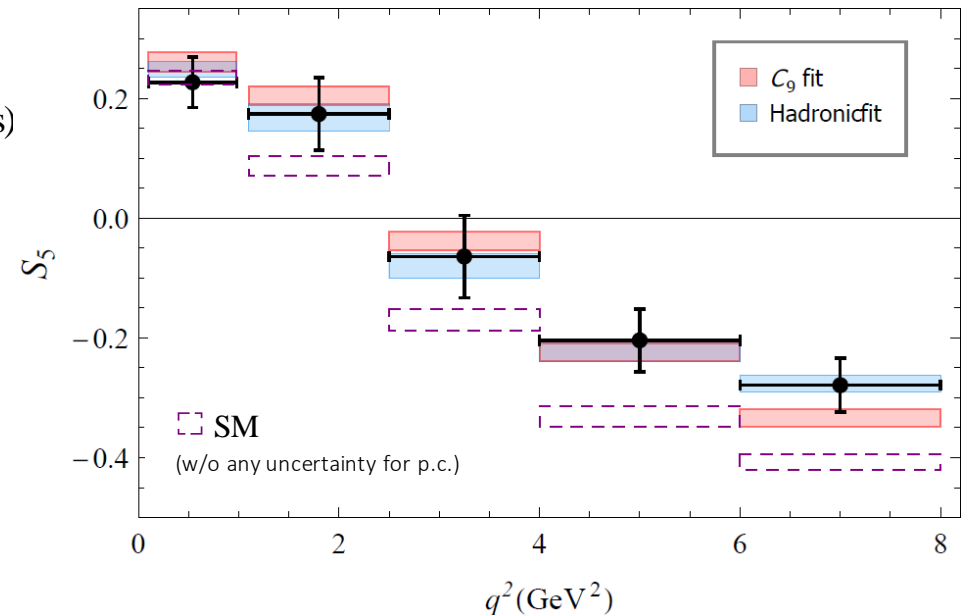
$$h_{\pm,[0]} = \left[ \sqrt{q^2} \times \right] \left( h_{\pm,[0]}^{(0)} + q^2 h_{\pm,[0]}^{(1)} + q^4 h_{\pm,[0]}^{(2)} \right)$$

⇒ NP effects in  $C_9$  are embedded in the hadronic contributions [A. Arbey, T. Hurth, F. Mahmoudi, SN, 1806.02791]

Due to the embedding, fits to NP and hadronic contributions can be compared with the Wilks' test

- Fit to
- Wilson coefficient  $\delta C_9^{\text{NP}}$
  - Hadronic quantities  $h_{+,-,0}^{(0,1,2)}$  (18 parameters)

$B \rightarrow K^* \mu^+ \mu^-$ observables (low $q^2$ ) and $\text{BR}(B \rightarrow K^* \gamma)$		
	Real $\delta C_9$ (1)	Hadronic fit (18)
Plain SM	$6.0\sigma$	$4.7\sigma$



- Fit to  $\delta C_9$  improves description of the data with  $6\sigma$  compared to the SM (w/o any uncertainty for p.c.)
- Hadronic fit also describes the data well

## NP effect vs. hadronic contributions

Instead of making assumptions on the size of the power corrections  $h_\lambda$ , they can be parameterised by a general ansatz (compatible with the analyticity structure): [Jäger, Camalich, 1412.3183], [Ciuchini et al. 1512.07157]

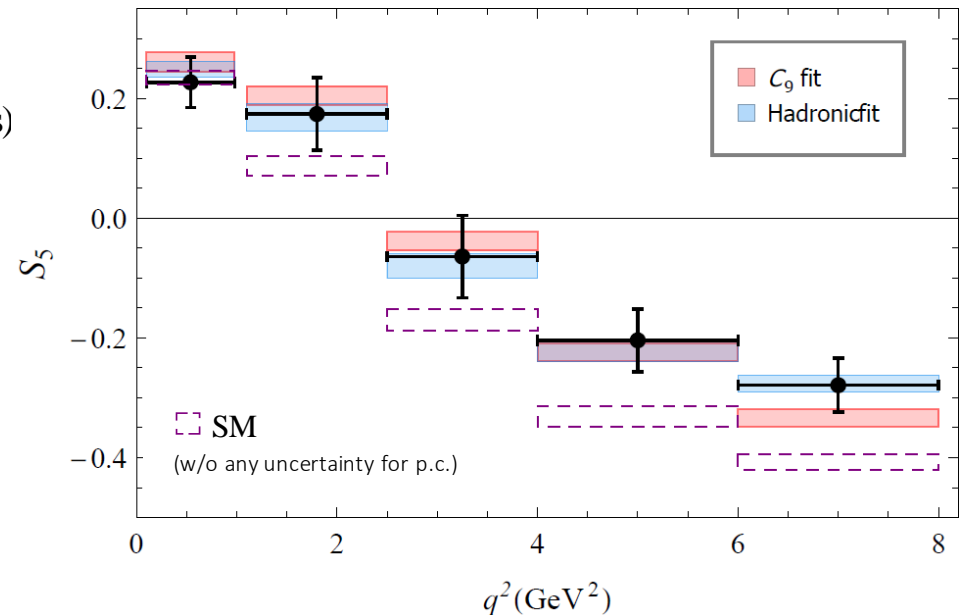
$$h_{\pm,[0]} = \left[ \sqrt{q^2} \times \right] \left( h_{\pm,[0]}^{(0)} + q^2 h_{\pm,[0]}^{(1)} + q^4 h_{\pm,[0]}^{(2)} \right)$$

⇒ NP effects in  $C_9$  are embedded in the hadronic contributions [A. Arbey, T. Hurth, F. Mahmoudi, SN, 1806.02791]

Due to the embedding, fits to NP and hadronic contributions can be compared with the Wilks' test

- Fit to
- Wilson coefficient  $\delta C_9^{\text{NP}}$
  - Hadronic quantities  $h_{+,-,0}^{(0,1,2)}$  (18 parameters)

$B \rightarrow K^* \mu^+ \mu^-$ observables (low $q^2$ ) and $\text{BR}(B \rightarrow K^* \gamma)$		
	Real $\delta C_9$ (1)	Hadronic fit (18)
Plain SM	$6.0\sigma$	$4.7\sigma$
Real $\delta C_9$	--	$1.5\sigma$



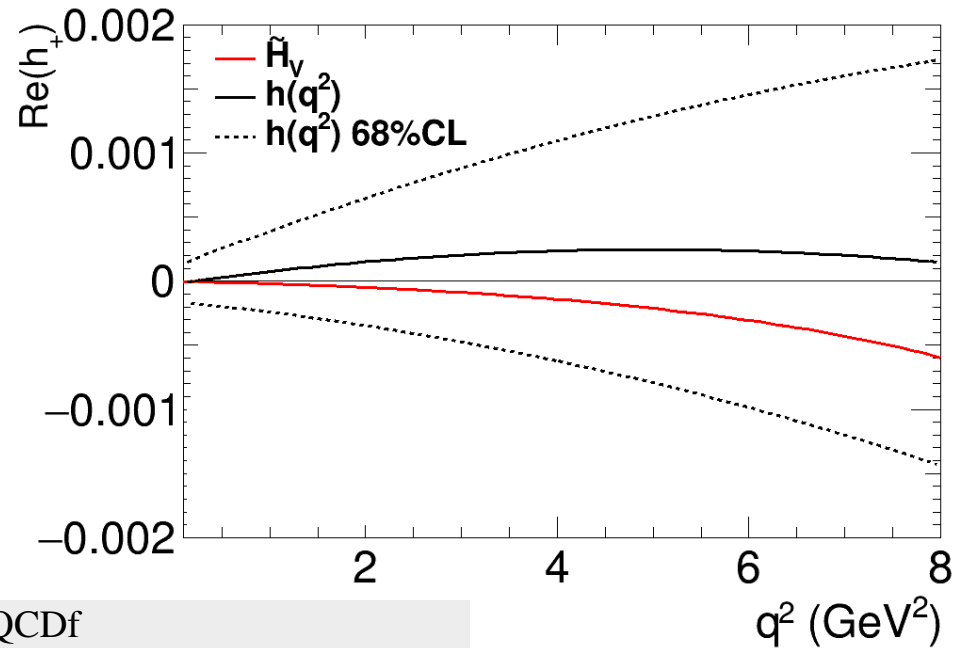
- Fit to  $\delta C_9$  improves description of the data with  $6\sigma$  compared to the SM (w/o any uncertainty for p.c.)
- Hadronic fit also describes the data well
- Adding 17 more parameters compared to the NP in  $C_9$  doesn't significantly improve the fit ( $\sim 1.5\sigma$ )

The hadronic fit includes 18 free parameters

$B \rightarrow K^* \bar{\mu}\mu/\gamma$ observables ( $\chi^2_{\text{SM}} = 85.15$ , $\chi^2_{\text{min}} = 25.96$ ; $\text{Pull}_{\text{SM}} = 4.7\sigma$ )		
	Real	Imaginary
$h_+^{(0)}$	$(-2.37 \pm 13.50) \times 10^{-5}$	$(7.86 \pm 13.79) \times 10^{-5}$
$h_+^{(1)}$	$(1.09 \pm 1.81) \times 10^{-4}$	$(1.58 \pm 1.69) \times 10^{-4}$
$h_+^{(2)}$	$(-1.10 \pm 2.66) \times 10^{-5}$	$(-2.45 \pm 2.51) \times 10^{-5}$
$h_-^{(0)}$	$(1.43 \pm 12.85) \times 10^{-5}$	$(-2.34 \pm 3.09) \times 10^{-4}$
$h_-^{(1)}$	$(-3.99 \pm 8.11) \times 10^{-5}$	$(1.44 \pm 2.82) \times 10^{-4}$
$h_-^{(2)}$	$(2.04 \pm 1.16) \times 10^{-5}$	$(-3.25 \pm 3.98) \times 10^{-5}$
$h_0^{(0)}$	$(2.38 \pm 2.43) \times 10^{-4}$	$(5.10 \pm 3.18) \times 10^{-4}$
$h_0^{(1)}$	$(1.40 \pm 1.98) \times 10^{-4}$	$(-1.66 \pm 2.41) \times 10^{-4}$
$h_0^{(2)}$	$(-1.57 \pm 2.43) \times 10^{-5}$	$(3.04 \pm 29.87) \times 10^{-6}$

The hadronic fit includes 18 free parameters

$B \rightarrow K^* \bar{\mu}\mu/\gamma$ observables ( $\chi^2_{\text{SM}} = 85.15$ , $\chi^2_{\text{min}} = 25.96$ ; $\text{Pull}_{\text{SM}} = 4.7\sigma$ )		
	Real	Imaginary
$h_+^{(0)}$	$(-2.37 \pm 13.50) \times 10^{-5}$	$(7.86 \pm 13.79) \times 10^{-5}$
$h_+^{(1)}$	$(1.09 \pm 1.81) \times 10^{-4}$	$(1.58 \pm 1.69) \times 10^{-4}$
$h_+^{(2)}$	$(-1.10 \pm 2.66) \times 10^{-5}$	$(-2.45 \pm 2.51) \times 10^{-5}$
$h_-^{(0)}$	$(1.43 \pm 12.85) \times 10^{-5}$	$(-2.34 \pm 3.09) \times 10^{-4}$
$h_-^{(1)}$	$(-3.99 \pm 8.11) \times 10^{-5}$	$(1.44 \pm 2.82) \times 10^{-4}$
$h_-^{(2)}$	$(2.04 \pm 1.16) \times 10^{-5}$	$(-3.25 \pm 3.98) \times 10^{-5}$
$h_0^{(0)}$	$(2.38 \pm 2.43) \times 10^{-4}$	$(5.10 \pm 3.18) \times 10^{-4}$
$h_0^{(1)}$	$(1.40 \pm 1.98) \times 10^{-4}$	$(-1.66 \pm 2.41) \times 10^{-4}$
$h_0^{(2)}$	$(-1.57 \pm 2.43) \times 10^{-5}$	$(3.04 \pm 29.87) \times 10^{-6}$



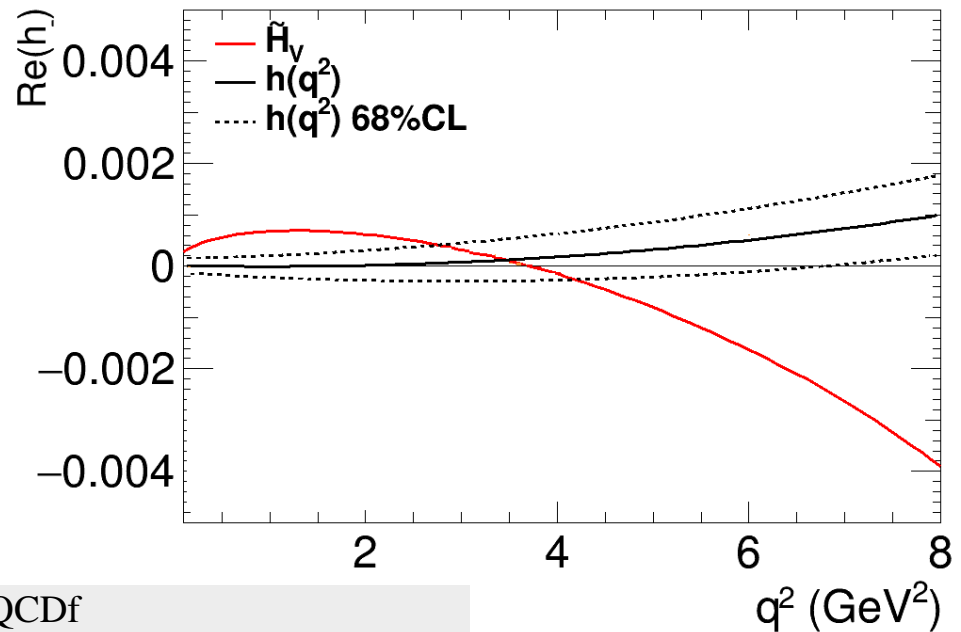
Red line: LO QCDf  
Solid black line:  $h_\lambda$   
Dashed black line: 68% C.L. region of  $h_\lambda$  fit

➤  $h_\lambda$  compatible with zero at  $1\sigma$  level

→ too many free parameters to get strongly constrained with current data

The hadronic fit includes 18 free parameters

$B \rightarrow K^* \bar{\mu}\mu/\gamma$ observables ( $\chi^2_{\text{SM}} = 85.15$ , $\chi^2_{\text{min}} = 25.96$ ; $\text{Pull}_{\text{SM}} = 4.7\sigma$ )		
	Real	Imaginary
$h_+^{(0)}$	$(-2.37 \pm 13.50) \times 10^{-5}$	$(7.86 \pm 13.79) \times 10^{-5}$
$h_+^{(1)}$	$(1.09 \pm 1.81) \times 10^{-4}$	$(1.58 \pm 1.69) \times 10^{-4}$
$h_+^{(2)}$	$(-1.10 \pm 2.66) \times 10^{-5}$	$(-2.45 \pm 2.51) \times 10^{-5}$
$h_-^{(0)}$	$(1.43 \pm 12.85) \times 10^{-5}$	$(-2.34 \pm 3.09) \times 10^{-4}$
$h_-^{(1)}$	$(-3.99 \pm 8.11) \times 10^{-5}$	$(1.44 \pm 2.82) \times 10^{-4}$
$h_-^{(2)}$	$(2.04 \pm 1.16) \times 10^{-5}$	$(-3.25 \pm 3.98) \times 10^{-5}$
$h_0^{(0)}$	$(2.38 \pm 2.43) \times 10^{-4}$	$(5.10 \pm 3.18) \times 10^{-4}$
$h_0^{(1)}$	$(1.40 \pm 1.98) \times 10^{-4}$	$(-1.66 \pm 2.41) \times 10^{-4}$
$h_0^{(2)}$	$(-1.57 \pm 2.43) \times 10^{-5}$	$(3.04 \pm 29.87) \times 10^{-6}$



Red line: LO QCDf  
Solid black line:  $h_\lambda$   
Dashed black line: 68% C.L. region of  $h_\lambda$  fit

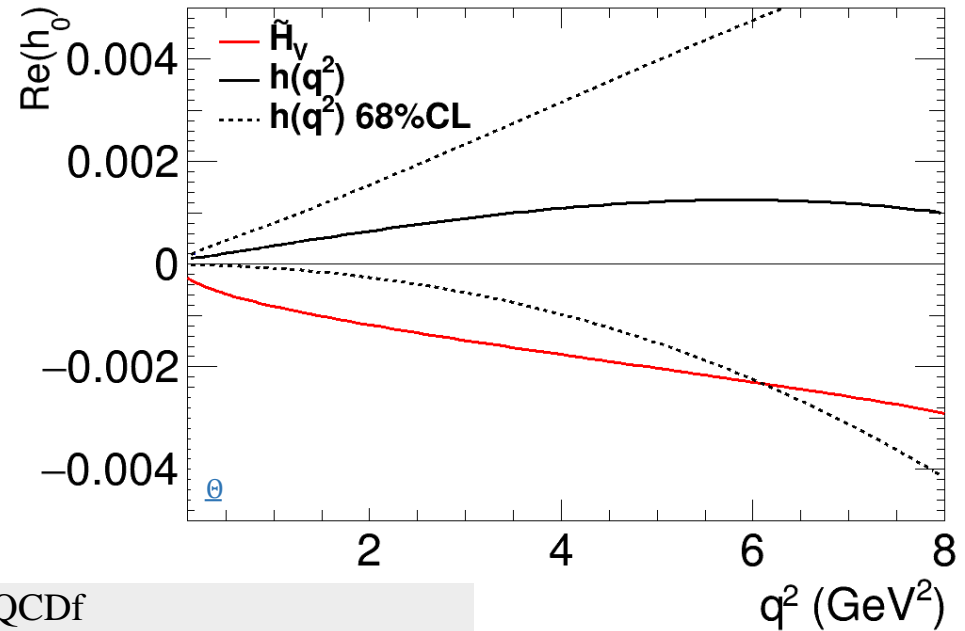
➤  $h_\lambda$  compatible with zero at  $1\sigma$  level

➔ too many free parameters to get strongly constrained with current data



The hadronic fit includes 18 free parameters

$B \rightarrow K^* \bar{\mu}\mu/\gamma$ observables ( $\chi^2_{\text{SM}} = 85.15$ , $\chi^2_{\text{min}} = 25.96$ ; $\text{Pull}_{\text{SM}} = 4.7\sigma$ )		
	Real	Imaginary
$h_+^{(0)}$	$(-2.37 \pm 13.50) \times 10^{-5}$	$(7.86 \pm 13.79) \times 10^{-5}$
$h_+^{(1)}$	$(1.09 \pm 1.81) \times 10^{-4}$	$(1.58 \pm 1.69) \times 10^{-4}$
$h_+^{(2)}$	$(-1.10 \pm 2.66) \times 10^{-5}$	$(-2.45 \pm 2.51) \times 10^{-5}$
$h_-^{(0)}$	$(1.43 \pm 12.85) \times 10^{-5}$	$(-2.34 \pm 3.09) \times 10^{-4}$
$h_-^{(1)}$	$(-3.99 \pm 8.11) \times 10^{-5}$	$(1.44 \pm 2.82) \times 10^{-4}$
$h_-^{(2)}$	$(2.04 \pm 1.16) \times 10^{-5}$	$(-3.25 \pm 3.98) \times 10^{-5}$
$h_0^{(0)}$	$(2.38 \pm 2.43) \times 10^{-4}$	$(5.10 \pm 3.18) \times 10^{-4}$
$h_0^{(1)}$	$(1.40 \pm 1.98) \times 10^{-4}$	$(-1.66 \pm 2.41) \times 10^{-4}$
$h_0^{(2)}$	$(-1.57 \pm 2.43) \times 10^{-5}$	$(3.04 \pm 29.87) \times 10^{-6}$



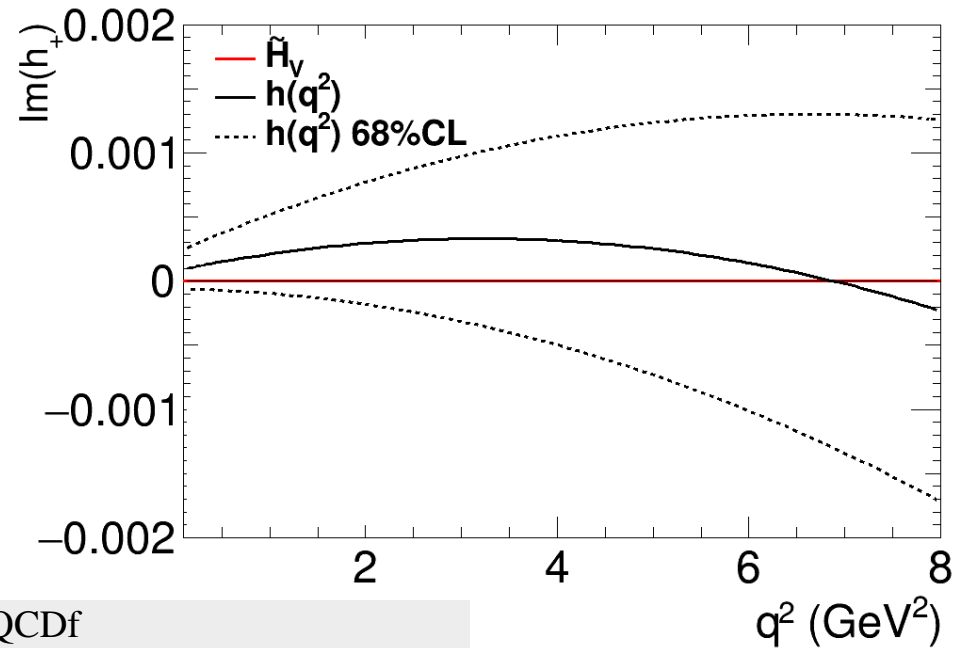
Red line: LO QCDf  
Solid black line:  $h_\lambda$   
Dashed black line: 68% C.L. region of  $h_\lambda$  fit

➤  $h_\lambda$  compatible with zero at  $1\sigma$  level

→ too many free parameters to get strongly constrained with current data

The hadronic fit includes 18 free parameters

$B \rightarrow K^* \bar{\mu}\mu/\gamma$ observables		
$(\chi^2_{\text{SM}} = 85.15, \chi^2_{\text{min}} = 25.96; \text{Pull}_{\text{SM}} = 4.7\sigma)$		
	Real	Imaginary
$h_+^{(0)}$	$(-2.37 \pm 13.50) \times 10^{-5}$	$(7.86 \pm 13.79) \times 10^{-5}$
$h_+^{(1)}$	$(1.09 \pm 1.81) \times 10^{-4}$	$(1.58 \pm 1.69) \times 10^{-4}$
$h_+^{(2)}$	$(-1.10 \pm 2.66) \times 10^{-5}$	$(-2.45 \pm 2.51) \times 10^{-5}$
$h_-^{(0)}$	$(1.43 \pm 12.85) \times 10^{-5}$	$(-2.34 \pm 3.09) \times 10^{-4}$
$h_-^{(1)}$	$(-3.99 \pm 8.11) \times 10^{-5}$	$(1.44 \pm 2.82) \times 10^{-4}$
$h_-^{(2)}$	$(2.04 \pm 1.16) \times 10^{-5}$	$(-3.25 \pm 3.98) \times 10^{-5}$
$h_0^{(0)}$	$(2.38 \pm 2.43) \times 10^{-4}$	$(5.10 \pm 3.18) \times 10^{-4}$
$h_0^{(1)}$	$(1.40 \pm 1.98) \times 10^{-4}$	$(-1.66 \pm 2.41) \times 10^{-4}$
$h_0^{(2)}$	$(-1.57 \pm 2.43) \times 10^{-5}$	$(3.04 \pm 29.87) \times 10^{-6}$



Red line: LO QCDf

Solid black line:  $h_\lambda$

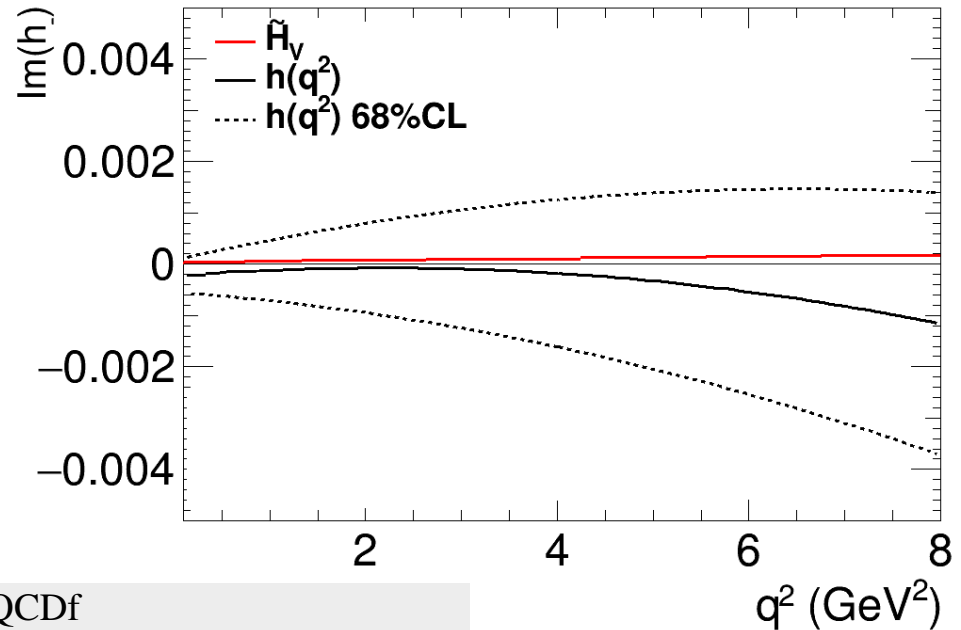
Dashed black line: 68% C.L. region of  $h_\lambda$  fit

➤  $h_\lambda$  compatible with zero at  $1\sigma$  level

➔ too many free parameters to get strongly constrained with current data

The hadronic fit includes 18 free parameters

$B \rightarrow K^* \bar{\mu}\mu/\gamma$ observables ( $\chi^2_{\text{SM}} = 85.15$ , $\chi^2_{\text{min}} = 25.96$ ; $\text{Pull}_{\text{SM}} = 4.7\sigma$ )		
	Real	Imaginary
$h_+^{(0)}$	$(-2.37 \pm 13.50) \times 10^{-5}$	$(7.86 \pm 13.79) \times 10^{-5}$
$h_+^{(1)}$	$(1.09 \pm 1.81) \times 10^{-4}$	$(1.58 \pm 1.69) \times 10^{-4}$
$h_+^{(2)}$	$(-1.10 \pm 2.66) \times 10^{-5}$	$(-2.45 \pm 2.51) \times 10^{-5}$
$h_-^{(0)}$	$(1.43 \pm 12.85) \times 10^{-5}$	$(-2.34 \pm 3.09) \times 10^{-4}$
$h_-^{(1)}$	$(-3.99 \pm 8.11) \times 10^{-5}$	$(1.44 \pm 2.82) \times 10^{-4}$
$h_-^{(2)}$	$(2.04 \pm 1.16) \times 10^{-5}$	$(-3.25 \pm 3.98) \times 10^{-5}$
$h_0^{(0)}$	$(2.38 \pm 2.43) \times 10^{-4}$	$(5.10 \pm 3.18) \times 10^{-4}$
$h_0^{(1)}$	$(1.40 \pm 1.98) \times 10^{-4}$	$(-1.66 \pm 2.41) \times 10^{-4}$
$h_0^{(2)}$	$(-1.57 \pm 2.43) \times 10^{-5}$	$(3.04 \pm 29.87) \times 10^{-6}$



Red line: LO QCDf

Solid black line:  $h_\lambda$

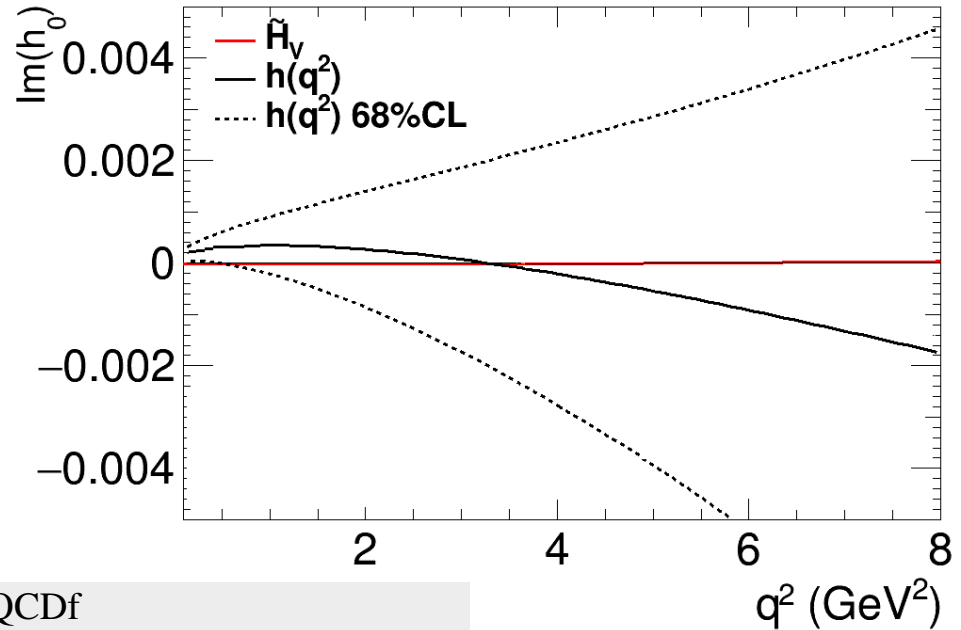
Dashed black line: 68% C.L. region of  $h_\lambda$  fit

➤  $h_\lambda$  compatible with zero at  $1\sigma$  level

➔ too many free parameters to get strongly constrained with current data

The hadronic fit includes 18 free parameters

$B \rightarrow K^* \bar{\mu}\mu/\gamma$ observables ( $\chi^2_{\text{SM}} = 85.15$ , $\chi^2_{\text{min}} = 25.96$ ; $\text{Pull}_{\text{SM}} = 4.7\sigma$ )		
	Real	Imaginary
$h_+^{(0)}$	$(-2.37 \pm 13.50) \times 10^{-5}$	$(7.86 \pm 13.79) \times 10^{-5}$
$h_+^{(1)}$	$(1.09 \pm 1.81) \times 10^{-4}$	$(1.58 \pm 1.69) \times 10^{-4}$
$h_+^{(2)}$	$(-1.10 \pm 2.66) \times 10^{-5}$	$(-2.45 \pm 2.51) \times 10^{-5}$
$h_-^{(0)}$	$(1.43 \pm 12.85) \times 10^{-5}$	$(-2.34 \pm 3.09) \times 10^{-4}$
$h_-^{(1)}$	$(-3.99 \pm 8.11) \times 10^{-5}$	$(1.44 \pm 2.82) \times 10^{-4}$
$h_-^{(2)}$	$(2.04 \pm 1.16) \times 10^{-5}$	$(-3.25 \pm 3.98) \times 10^{-5}$
$h_0^{(0)}$	$(2.38 \pm 2.43) \times 10^{-4}$	$(5.10 \pm 3.18) \times 10^{-4}$
$h_0^{(1)}$	$(1.40 \pm 1.98) \times 10^{-4}$	$(-1.66 \pm 2.41) \times 10^{-4}$
$h_0^{(2)}$	$(-1.57 \pm 2.43) \times 10^{-5}$	$(3.04 \pm 29.87) \times 10^{-6}$



Red line: LO QCDf

Solid black line:  $h_\lambda$

Dashed black line: 68% C.L. region of  $h_\lambda$  fit

➤  $h_\lambda$  compatible with zero at  $1\sigma$  level

→ too many free parameters to get strongly constrained with current data

A (minimal) description of hadronic contributions with fewer free parameters

$$h_\lambda(q^2) = -\frac{\tilde{V}_\lambda(q^2)}{16\pi^2} \frac{q^2}{m_B^2} \Delta C_9^{\lambda, \text{PC}} \quad \begin{array}{l} \text{for each helicity } (\lambda = +, -, 0) \text{ a different } \Delta C_9^{\text{PC}} \\ \rightarrow \text{three real (six complex) parameters} \end{array}$$

- If NP in  $C_9$  is the favoured scenario, the three different fitted helicities should give the same value  
⇒ Can work as a null test for NP

A (minimal) description of hadronic contributions with fewer free parameters

$$h_\lambda(q^2) = -\frac{\tilde{V}_\lambda(q^2)}{16\pi^2} \frac{q^2}{m_B^2} \Delta C_9^{\lambda, \text{PC}}$$

for each helicity ( $\lambda = +, -, 0$ ) a different  $\Delta C_9^{\text{PC}}$   
 $\rightarrow$  three real (six complex) parameters

- If NP in  $C_9$  is the favoured scenario, the three different fitted helicities should give the same value  
 $\Rightarrow$  Can work as a null test for NP

$B \rightarrow K^* \bar{\mu}\mu/\gamma$ observables ( $\chi_{\text{SM}}^2 = 85.15$ , $\chi_{\text{min}}^2 = 39.40$ ; $\text{Pull}_{\text{SM}} = 5.5\sigma$ )	
	best fit value
$\Delta C_9^{+, \text{PC}}$	$(3.39 \pm 6.44) + i(-14.98 \pm 8.40)$
$\Delta C_9^{-, \text{PC}}$	$(-1.02 \pm 0.22) + i(-0.68 \pm 0.79)$
$\Delta C_9^{0, \text{PC}}$	$(-0.83 \pm 0.53) + i(-0.89 \pm 0.69)$

Fitted parameters not the same for different helicities  
 but in agreement with each other within  $1\sigma$

A (minimal) description of hadronic contributions with fewer free parameters

$$h_\lambda(q^2) = -\frac{\tilde{V}_\lambda(q^2)}{16\pi^2} \frac{q^2}{m_B^2} \Delta C_9^{\lambda, \text{PC}} \quad \text{for each helicity } (\lambda = +, -, 0) \text{ a different } \Delta C_9^{\text{PC}} \\ \rightarrow \text{three real (six complex) parameters}$$

- If NP in  $C_9$  is the favoured scenario, the three different fitted helicities should give the same value  
⇒ Can work as a null test for NP

$B \rightarrow K^* \bar{\mu} \mu / \gamma$ observables ( $\chi_{\text{SM}}^2 = 85.15$ , $\chi_{\text{min}}^2 = 39.40$ ; $\text{Pull}_{\text{SM}} = 5.5\sigma$ )	
	best fit value
$\Delta C_9^{+, \text{PC}}$	$(3.39 \pm 6.44) + i(-14.98 \pm 8.40)$
$\Delta C_9^{-, \text{PC}}$	$(-1.02 \pm 0.22) + i(-0.68 \pm 0.79)$
$\Delta C_9^{0, \text{PC}}$	$(-0.83 \pm 0.53) + i(-0.89 \pm 0.69)$

Fitted parameters not the same for different helicities  
but in agreement with each other within  $1\sigma$

Fit to only $\text{BR}(B \rightarrow K^* \gamma)$ and $B \rightarrow K^* \mu^+ \mu^-$ observables (low $q^2$ )		
	Real $\delta C_9$ (1)	Hadronic fit; Complex $\Delta C_9^{\lambda, \text{PC}}$ (6)
Plain SM (0)	(6.0 $\sigma$ )	(5.5 $\sigma$ )
Real $\delta C_9$ (1)	--	(1.8 $\sigma$ )

- Adding the hadronic parameters improve the fit with less than  $2\sigma$  significance

Strong indication that the NP interpretation is a valid option, although the situation remains inconclusive

# Future prospects



LHCb projections for  $B \rightarrow K^* \mu^+ \mu^-$  with 14, 50 and 300  $\text{fb}^{-1}$  luminosity

Keeping present central values, the three benchmark points don't give acceptable fits ( $p$ -value  $\approx 0$ )

We assume two extreme scenarios, adjusting the experimental data such that

- ❑ Central value of fit to  $C_9$  remains the same
- ❑ Central values of the hadronic fit remain the same

LHCb projections for  $B \rightarrow K^* \mu^+ \mu^-$  with 14, 50 and 300  $\text{fb}^{-1}$  luminosity

Keeping present central values, the three benchmark points don't give acceptable fits ( $p$ -value  $\approx 0$ )

We assume two extreme scenarios, adjusting the experimental data such that

- ☒ Central value of fit to  $C_9$  remains the same
- ☐ Central values of the hadronic fit remain the same

Central value of fit to $C_9$ remains the same						
	14 fb <sup>-1</sup> (Syst.)		50 fb <sup>-1</sup> (Syst./4)		300 fb <sup>-1</sup> (Syst./4)	
	Real $\delta C_9$	Hadronic fit $h_\lambda$	Real $\delta C_9$	Hadronic fit $h_\lambda$	Real $\delta C_9$	Hadronic fit $h_\lambda$
Plain SM	8.1 $\sigma$	5.1 $\sigma$	15.1 $\sigma$	12.9 $\sigma$	21.4 $\sigma$	19.6 $\sigma$

- Very good fits for  $C_9$  by construction

LHCb projections for  $B \rightarrow K^* \mu^+ \mu^-$  with 14, 50 and 300  $\text{fb}^{-1}$  luminosity

Keeping present central values, the three benchmark points don't give acceptable fits ( $p$ -value  $\approx 0$ )

We assume two extreme scenarios, adjusting the experimental data such that

- ❑ Central value of fit to  $C_9$  remains the same
- ❑ Central values of the hadronic fit remain the same

Central value of fit to $C_9$ remains the same						
	14 $\text{fb}^{-1}$ (Syst.)		50 $\text{fb}^{-1}$ (Syst./4)		300 $\text{fb}^{-1}$ (Syst./4)	
	Real $\delta C_9$	Hadronic fit $h_\lambda$	Real $\delta C_9$	Hadronic fit $h_\lambda$	Real $\delta C_9$	Hadronic fit $h_\lambda$
Plain SM	8.1 $\sigma$	5.1 $\sigma$	15.1 $\sigma$	12.9 $\sigma$	21.4 $\sigma$	19.6 $\sigma$

- Very good fits for  $C_9$  by construction
- Good hadronic fits for all three benchmark points of this scenario, but no improvement compared to  $C_9$
- Uncertainties of most of the parameters of the hadronic fit become very large for higher luminosities indicating most of the 18 parameters are not needed to describe the data

LHCb projections for  $B \rightarrow K^* \mu^+ \mu^-$  with 14, 50 and 300  $\text{fb}^{-1}$  luminosity

Keeping present central values, the three benchmark points don't give acceptable fits ( $p$ -value  $\approx 0$ )

We assume two extreme scenarios, adjusting the experimental data such that

- ☐ Central value of fit to  $C_9$  remains the same
- ☐ Central values of the hadronic fit remain the same

Central values of the hadronic fit is always the same						
	14 $\text{fb}^{-1}$ (Syst.)		50 $\text{fb}^{-1}$ (Syst./4)		300 $\text{fb}^{-1}$ (Syst./4)	
	Real $\delta C_9$	Hadronic fit $h_\lambda$	Real $\delta C_9$	Hadronic fit $h_\lambda$	Real $\delta C_9$	Hadronic fit $h_\lambda$
Plain SM	$7.9\sigma$	$7.9\sigma$	$14.6\sigma$	$22.5\sigma$	$18.9\sigma$	$41.8\sigma$

LHCb projections for  $B \rightarrow K^* \mu^+ \mu^-$  with 14, 50 and 300  $\text{fb}^{-1}$  luminosity

Keeping present central values, the three benchmark points don't give acceptable fits ( $p\text{-value} \approx 0$ )

We assume two extreme scenarios, adjusting the experimental data such that

- ☐ Central value of fit to  $C_9$  remains the same
 ☐ Central values of the hadronic fit remain the same

Central values of the hadronic fit is always the same						
	14 $\text{fb}^{-1}$ (Syst.)		50 $\text{fb}^{-1}$ (Syst./4)		300 $\text{fb}^{-1}$ (Syst./4)	
	Real $\delta C_9$	Hadronic fit $h_\lambda$	Real $\delta C_9$	Hadronic fit $h_\lambda$	Real $\delta C_9$	Hadronic fit $h_\lambda$
Plain SM	7.9 $\sigma$	7.9 $\sigma$	14.6 $\sigma$	22.5 $\sigma$	18.9 $\sigma$	41.8 $\sigma$
Real $\delta C_9$	--	4.0 $\sigma$	--	17.5 $\sigma$	--	37.4 $\sigma$

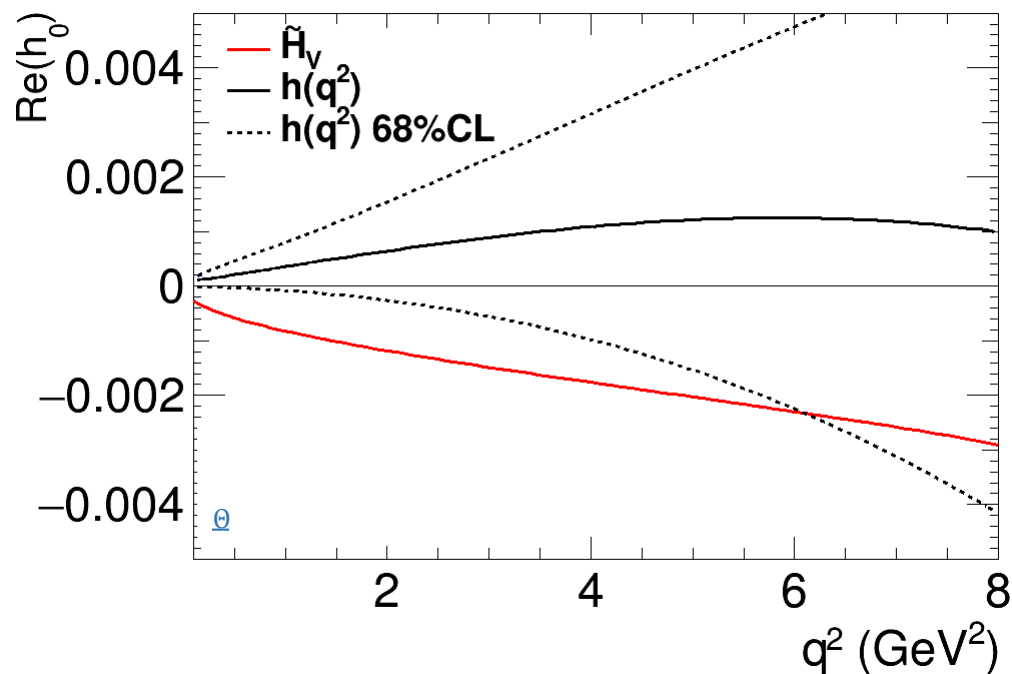
- Hadronic fit, gives an improvement with 4 $\sigma$  significance compared to fit to  $C_9$  after Run 2 (14  $\text{fb}^{-1}$ ) but situation still remains inconclusive
- After first LHCb upgrade (50  $\text{fb}^{-1}$ ) conclusive judgment is possible

LHCb projections for  $B \rightarrow K^* \mu^+ \mu^-$  with 14, 50 and 300  $\text{fb}^{-1}$  luminosity

Keeping present central values, the three benchmark points don't give acceptable fits ( $p$ -value  $\approx 0$ )

We assume two extreme scenarios, adjusting the experimental data such that

- ☐ Central value of fit to  $C_9$  remains the same
- ☐ Central values of the hadronic fit remain the same



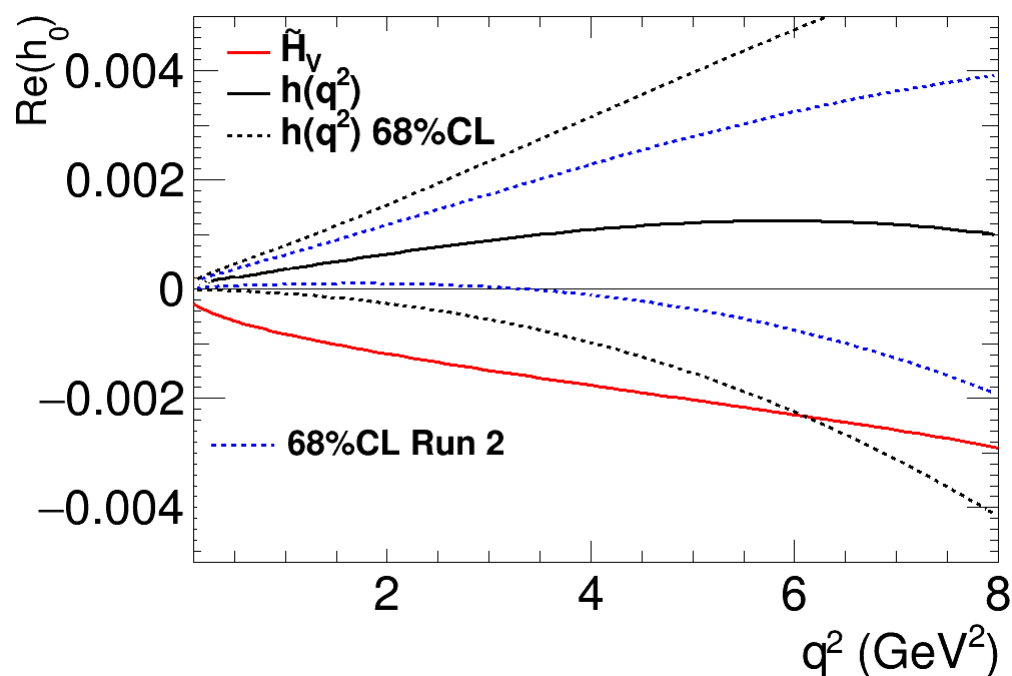
- Hadronic fit, gives an improvement with  $4\sigma$  significance compared to fit to  $C_9$  after Run 2 ( $14 \text{ fb}^{-1}$ ) but situation still remains inconclusive
- After first LHCb upgrade ( $50 \text{ fb}^{-1}$ ) conclusive judgment is possible

LHCb projections for  $B \rightarrow K^* \mu^+ \mu^-$  with 14, 50 and 300  $\text{fb}^{-1}$  luminosity

Keeping present central values, the three benchmark points don't give acceptable fits ( $p$ -value  $\approx 0$ )

We assume two extreme scenarios, adjusting the experimental data such that

- Central value of fit to  $C_9$  remains the same
- Central values of the hadronic fit remain the same



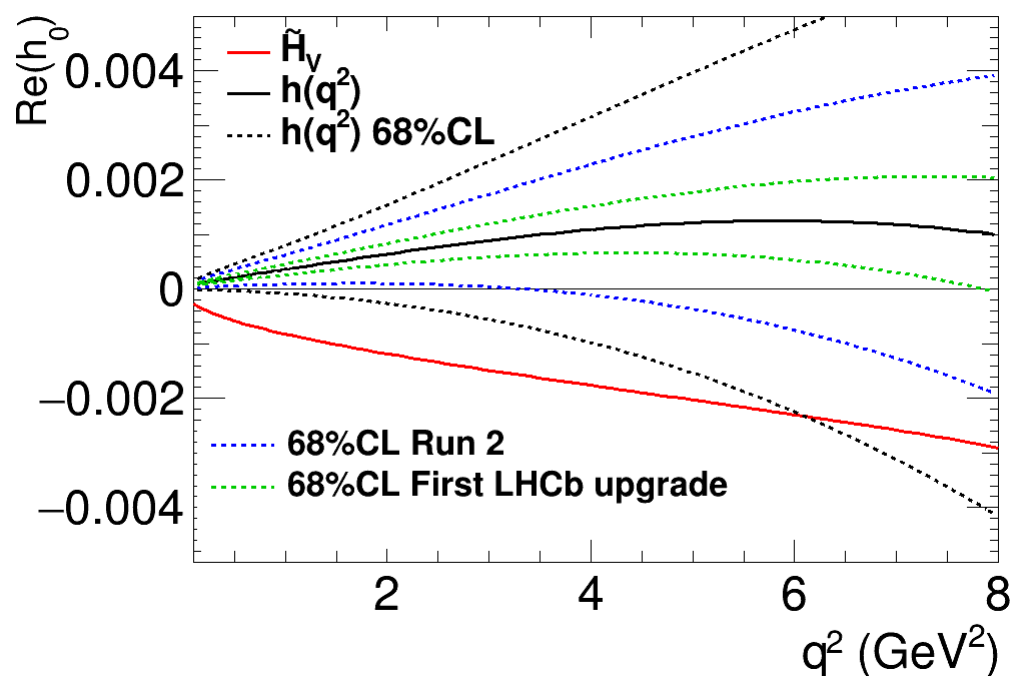
- Hadronic fit, gives an improvement with  $4\sigma$  significance compared to fit to  $C_9$  after Run 2 ( $14 \text{ fb}^{-1}$ ) but situation still remains inconclusive
- After first LHCb upgrade ( $50 \text{ fb}^{-1}$ ) conclusive judgment is possible

LHCb projections for  $B \rightarrow K^* \mu^+ \mu^-$  with 14, 50 and 300  $\text{fb}^{-1}$  luminosity

Keeping present central values, the three benchmark points don't give acceptable fits ( $p$ -value  $\approx 0$ )

We assume two extreme scenarios, adjusting the experimental data such that

- Central value of fit to  $C_9$  remains the same
- Central values of the hadronic fit remain the same



- Hadronic fit, gives an improvement with  $4\sigma$  significance compared to fit to  $C_9$  after Run 2 ( $14 \text{ fb}^{-1}$ ) but situation still remains inconclusive
- After first LHCb upgrade ( $50 \text{ fb}^{-1}$ ) conclusive judgment is possible
  - ↪ fitted parameters no longer consistent with zero at  $1\sigma$  level

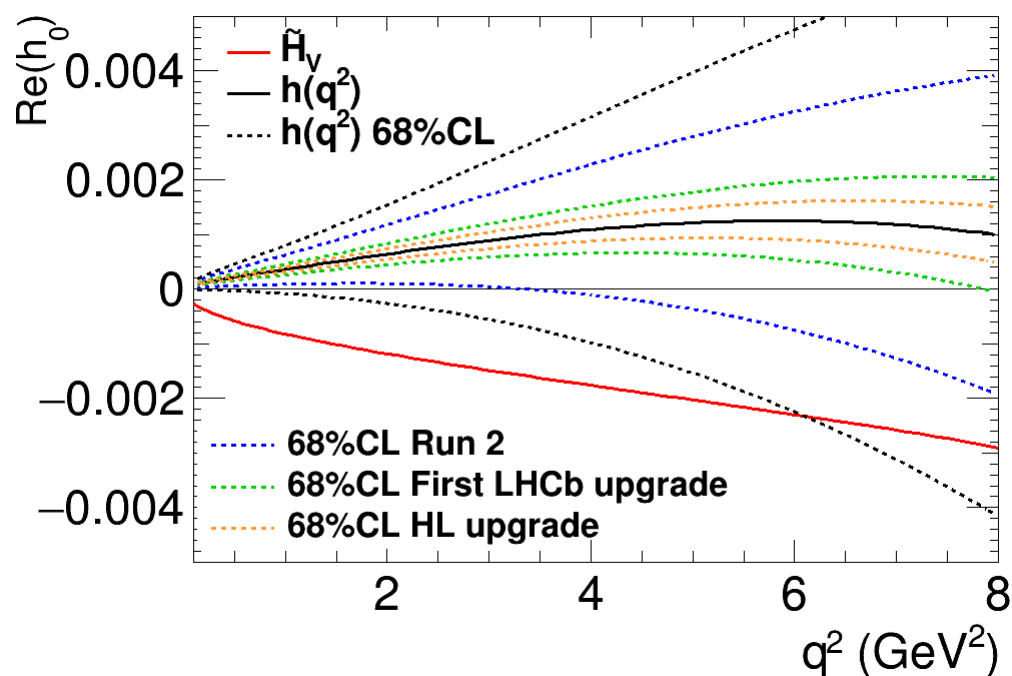


LHCb projections for  $B \rightarrow K^* \mu^+ \mu^-$  with 14, 50 and 300  $\text{fb}^{-1}$  luminosity

Keeping present central values, the three benchmark points don't give acceptable fits ( $p\text{-value} \approx 0$ )

We assume two extreme scenarios, adjusting the experimental data such that

- Central value of fit to  $C_9$  remains the same
- Central values of the hadronic fit remain the same



- Hadronic fit, gives an improvement with  $4\sigma$  significance compared to fit to  $C_9$  after Run 2 ( $14 \text{ fb}^{-1}$ ) but situation still remains inconclusive
- After first LHCb upgrade ( $50 \text{ fb}^{-1}$ ) conclusive judgment is possible
  - ↪ fitted parameters no longer consistent with zero at  $1\sigma$  level

# Global analysis of $b \rightarrow s\ell^+\ell^-$ observables

Considering all the relevant data on  $b \rightarrow s$  transitions

(117 observables)

- $R_K, R_{K^*}$
- $\text{BR}(B_{s,d} \rightarrow \mu^+ \mu^-)$
- $\text{BR}(B_s \rightarrow e^+ e^-)$
- $\text{BR}(B \rightarrow X_s \mu^+ \mu^-)$
- $\text{BR}(B \rightarrow X_s e^+ e^-)$
- $\text{BR}(B \rightarrow K^* e^+ e^-)$
- $\text{BR}(B \rightarrow K^{*+} \mu^+ \mu^-)$
- $B_s \rightarrow \phi \mu^+ \mu^-$ : BR, ang. obs.
- $B^{0(+)} \rightarrow K^{0(+)} \mu^+ \mu^-$ : BR, ang. obs.
- $B \rightarrow K^{*0} \mu^+ \mu^-$ : BR, ang. obs.
- $\Lambda_b \rightarrow \Lambda \mu^+ \mu^-$ : BR, ang. obs.

# Global analysis of $b \rightarrow s$ transitions: one-operator fit

Considering all the relevant data on  $b \rightarrow s$  transitions

(117 observables)

- $R_K, R_{K^*}$
- $\text{BR}(B_{s,d} \rightarrow \mu^+ \mu^-)$
- $\text{BR}(B_s \rightarrow e^+ e^-)$
- $\text{BR}(B \rightarrow X_s \mu^+ \mu^-)$
- $\text{BR}(B \rightarrow X_s e^+ e^-)$
- $\text{BR}(B \rightarrow K^* e^+ e^-)$
- $\text{BR}(B \rightarrow K^{*+} \mu^+ \mu^-)$
- $B_s \rightarrow \phi \mu^+ \mu^-$ : BR, ang. obs.
- $B^{0(+)} \rightarrow K^{0(+)} \mu^+ \mu^-$ : BR, ang. obs.
- $B \rightarrow K^{*0} \mu^+ \mu^-$ : BR, ang. obs.
- $\Lambda_b \rightarrow \Lambda \mu^+ \mu^-$ : BR, ang. obs.

All observables ( $\chi^2_{\text{SM}} = 157.3$ )			
	b.f. value	$\chi^2_{\text{min}}$	Pull <sub>SM</sub>
$\delta C_9$	$-0.94 \pm 0.14$	126.8	$5.5\sigma$
$\delta C_9^\mu$	$-0.93 \pm 0.13$	115.2	$6.5\sigma$
$\delta C_9^e$	$0.84 \pm 0.26$	145.5	$3.4\sigma$
$\delta C_{10}$	$0.20 \pm 0.22$	156.4	$0.9\sigma$
$\delta C_{10}^\mu$	$0.51 \pm 0.17$	146.4	$3.3\sigma$
$\delta C_{10}^e$	$-0.78 \pm 0.23$	144.3	$3.6\sigma$
$\delta C_{\text{LL}}^\mu$	$-0.53 \pm 0.10$	125.4	$5.6\sigma$
$\delta C_{\text{LL}}^e$	$0.43 \pm 0.13$	144.8	$3.5\sigma$

**Computations performed using  
SuperIso public program**  
(assuming 10% error for p.c.)

## Global analysis of $b \rightarrow s$ transitions: one-operator fit

Considering all the relevant data on  $b \rightarrow s$  transitions

(117 observables)

- $R_K, R_{K^*}$
- $\text{BR}(B_{s,d} \rightarrow \mu^+ \mu^-)$
- $\text{BR}(B_s \rightarrow e^+ e^-)$
- $\text{BR}(B \rightarrow X_s \mu^+ \mu^-)$
- $\text{BR}(B \rightarrow X_s e^+ e^-)$
- $\text{BR}(B \rightarrow K^* e^+ e^-)$
- $\text{BR}(B \rightarrow K^{*+} \mu^+ \mu^-)$
- $B_s \rightarrow \phi \mu^+ \mu^-$ : BR, ang. obs.
- $B^{0(+)} \rightarrow K^{0(+)} \mu^+ \mu^-$ : BR, ang. obs.
- $B \rightarrow K^{*0} \mu^+ \mu^-$ : BR, ang. obs.
- $\Lambda_b \rightarrow \Lambda \mu^+ \mu^-$ : BR, ang. obs.

All observables ( $\chi^2_{\text{SM}} = 157.3$ )			
	b.f. value	$\chi^2_{\text{min}}$	Pull <sub>SM</sub>
$\delta C_9$	$-0.94 \pm 0.14$	126.8	$5.5\sigma$
$\delta C_9^\mu$	$-0.93 \pm 0.13$	115.2	$6.5\sigma$
$\delta C_9^e$	$0.84 \pm 0.26$	145.5	$3.4\sigma$
$\delta C_{10}$	$0.20 \pm 0.22$	156.4	$0.9\sigma$
$\delta C_{10}^\mu$	$0.51 \pm 0.17$	146.4	$3.3\sigma$
$\delta C_{10}^e$	$-0.78 \pm 0.23$	144.3	$3.6\sigma$
$\delta C_{\text{LL}}^\mu$	$-0.53 \pm 0.10$	125.4	$5.6\sigma$
$\delta C_{\text{LL}}^e$	$0.43 \pm 0.13$	144.8	$3.5\sigma$

**Computations performed using  
SuperIso public program**  
(assuming 10% error for p.c.)

➤ Most favoured scenario is  $\delta C_9^\mu$  followed by  $\delta C_{\text{LL}}^\mu$  ( $\delta C_9^\mu = -\delta C_{10}^\mu$ ), same hierarchy as pre 2020 LHCb

Considering all the relevant data on  $b \rightarrow s$  transitions

(117 observables)

- $R_K, R_{K^*}$
- $\text{BR}(B_{s,d} \rightarrow \mu^+ \mu^-)$
- $\text{BR}(B_s \rightarrow e^+ e^-)$
- $\text{BR}(B \rightarrow X_s \mu^+ \mu^-)$
- $\text{BR}(B \rightarrow X_s e^+ e^-)$
- $\text{BR}(B \rightarrow K^* e^+ e^-)$
- $\text{BR}(B \rightarrow K^{*+} \mu^+ \mu^-)$
- $B_s \rightarrow \phi \mu^+ \mu^-$ : BR, ang. obs.
- $B^{0(+)} \rightarrow K^{0(+)} \mu^+ \mu^-$ : BR, ang. obs.
- $B \rightarrow K^{*0} \mu^+ \mu^-$ : BR, ang. obs.
- $\Lambda_b \rightarrow \Lambda \mu^+ \mu^-$ : BR, ang. obs.

All observables ( $\chi^2_{\text{SM}} = 157.3$ )			
	b.f. value	$\chi^2_{\text{min}}$	Pull <sub>SM</sub>
$\delta C_9$	$-0.94 \pm 0.14$	126.8	$5.5\sigma$
$\delta C_9^\mu$	$-0.93 \pm 0.13$	115.2	$6.5\sigma$
$\delta C_9^e$	$0.84 \pm 0.26$	145.5	$3.4\sigma$
$\delta C_{10}$	$0.20 \pm 0.22$	156.4	$0.9\sigma$
$\delta C_{10}^\mu$	$0.51 \pm 0.17$	146.4	$3.3\sigma$
$\delta C_{10}^e$	$-0.78 \pm 0.23$	144.3	$3.6\sigma$
$\delta C_{\text{LL}}^\mu$	$-0.53 \pm 0.10$	125.4	$5.6\sigma$
$\delta C_{\text{LL}}^e$	$0.43 \pm 0.13$	144.8	$3.5\sigma$

**Computations performed using  
SuperIso public program**  
(assuming 10% error for p.c.)

- Most favoured scenario is  $\delta C_9^\mu$  followed by  $\delta C_{\text{LL}}^\mu$  ( $\delta C_9^\mu = -\delta C_{10}^\mu$ ), same hierarchy as pre 2020 LHCb
- Significance have increased by  $\sim 1\sigma$  for the most prominent scenarios compared to 2019

## Global analysis of $b \rightarrow s$ transitions: one-operator fit

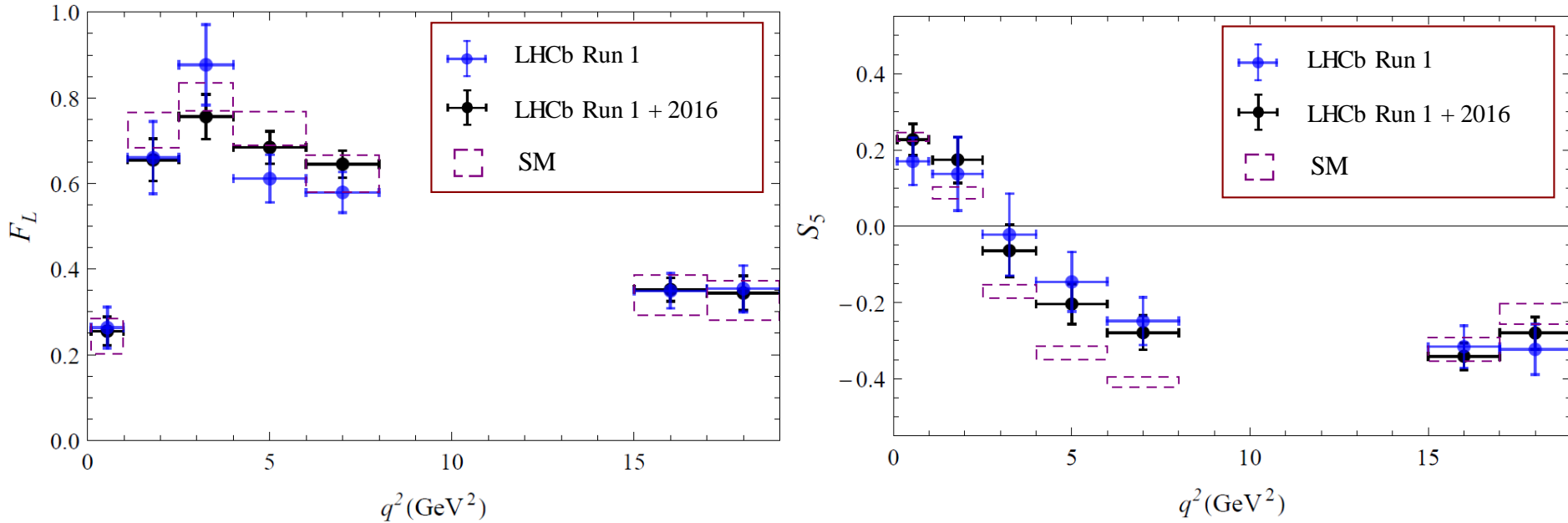
Fit to  $B \rightarrow K^* \mu^+ \mu^-$  angular observables: Run 1 ( $3 \text{ fb}^{-1}$ ) compared to Run 1 + 2016 ( $4.7 \text{ fb}^{-1}$ )

$B \rightarrow K^* \mu^+ \mu^-$ angular observables			
	$\chi_{\text{SM}}^2$	$\chi_{\text{min}}^2(\delta C_9)$	$\text{Pull}_{\text{SM}}(\delta C_9)$
Run 1	57.25	43.08	$4.0\sigma$
Run 1 + 2016	81.07	52.27	$5.4\sigma$

- Most favoured scenario is  $\delta C_9^\mu$  followed by  $\delta C_{\text{LL}}^\mu$  ( $\delta C_9^\mu = -\delta C_{10}^\mu$ ), same hierarchy as pre 2020 LHCb
- Significance have increased by  $\sim 1\sigma$  for the most prominent scenarios compared to 2019
- Change in significance mainly due to the recent LHCb analysis of the  $B \rightarrow K^* \mu^+ \mu^-$  angular observables with  $4.7 \text{ fb}^{-1}$  ( $\rightarrow$  larger  $\chi_{\text{SM}}^2$ )

## Global analysis of $b \rightarrow s$ transitions: one-operator fit

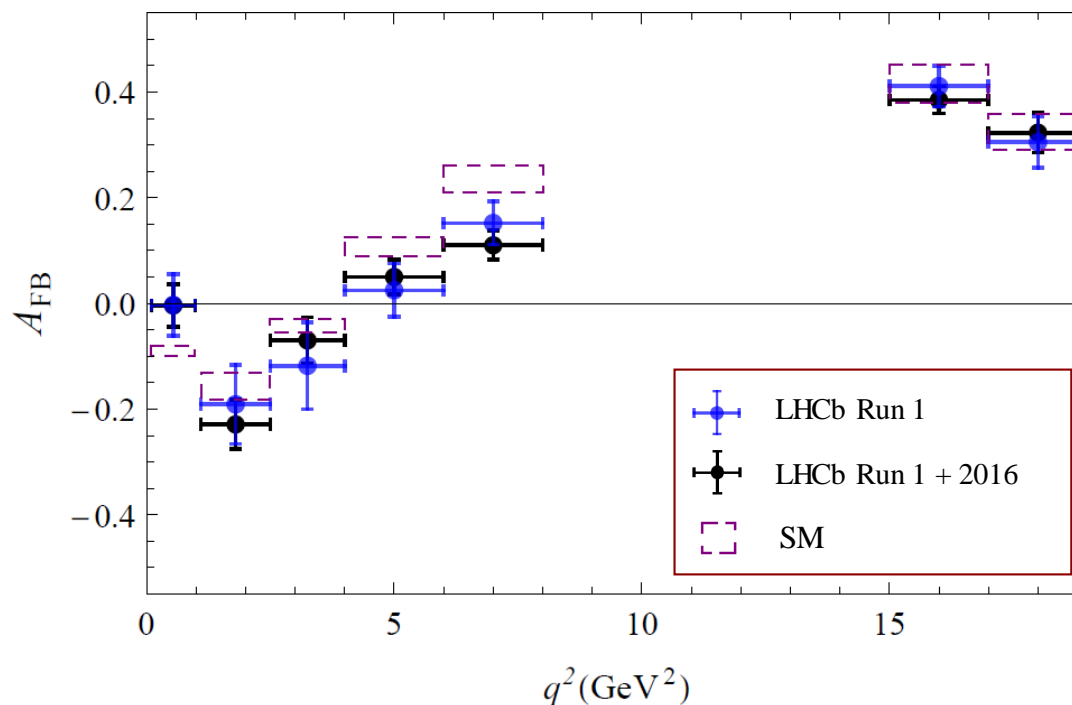
Fit to  $B \rightarrow K^* \mu^+ \mu^-$  angular observables: Run 1 ( $3 \text{ fb}^{-1}$ ) compared to Run 1 + 2016 ( $4.7 \text{ fb}^{-1}$ )



- Most favoured scenario is  $\delta C_9^\mu$  followed by  $\delta C_{\text{LL}}^\mu$  ( $\delta C_9^\mu = -\delta C_{10}^\mu$ ), same hierarchy as pre 2020 LHCb
- Significance have increased by  $\sim 1\sigma$  for the most prominent scenarios compared to 2019
- Change in significance mainly due to the recent LHCb analysis of the  $B \rightarrow K^* \mu^+ \mu^-$  angular observables with  $4.7 \text{ fb}^{-1}$  ( $\rightarrow$  larger  $\chi_{\text{SM}}^2$ )
  - ↪ smaller experimental uncertainties

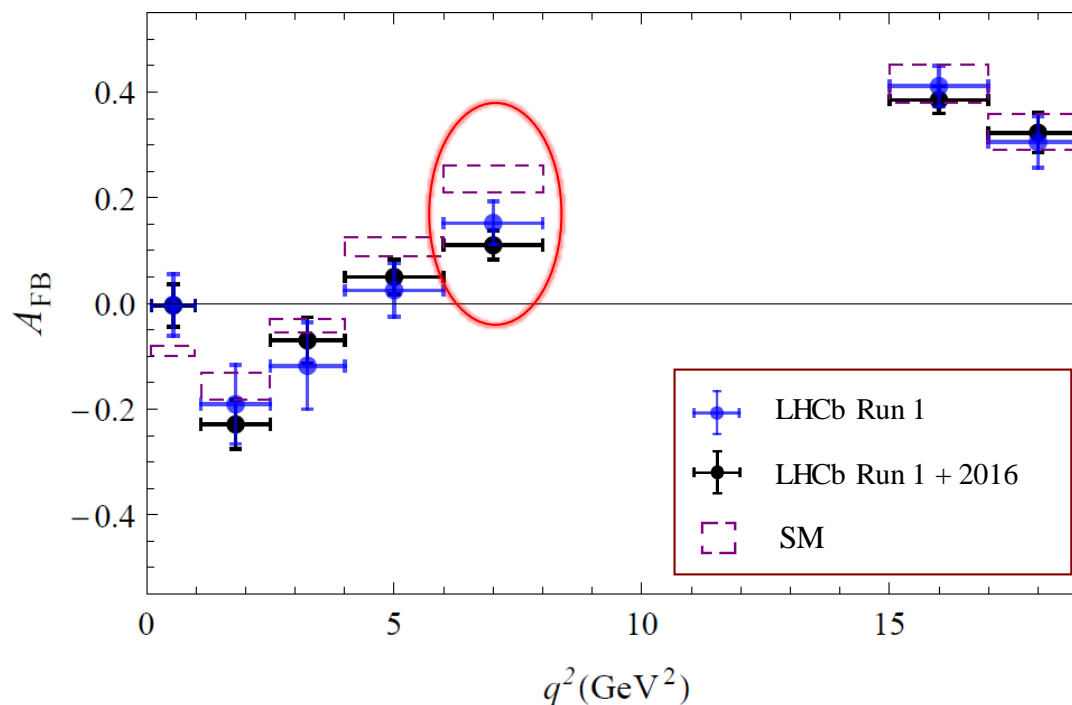


Fit to  $B \rightarrow K^* \mu^+ \mu^-$  angular observables: Run 1 ( $3 \text{ fb}^{-1}$ ) compared to Run 1 + 2016 ( $4.7 \text{ fb}^{-1}$ )



- Most favoured scenario is  $\delta C_9^\mu$  followed by  $\delta C_{LL}^\mu$  ( $\delta C_9^\mu = -\delta C_{10}^\mu$ ), same hierarchy as pre 2020 LHCb
- Significance have increased by  $\sim 1\sigma$  for the most prominent scenarios compared to 2019
- Change in significance mainly due to the recent LHCb analysis of the  $B \rightarrow K^* \mu^+ \mu^-$  angular observables with  $4.7 \text{ fb}^{-1}$  ( $\rightarrow$  larger  $\chi_{SM}^2$ )
  - ↪ smaller experimental uncertainties
  - ↪ further tensions

Fit to  $B \rightarrow K^* \mu^+ \mu^-$  angular observables: Run 1 ( $3 \text{ fb}^{-1}$ ) compared to Run 1 + 2016 ( $4.7 \text{ fb}^{-1}$ )



- Most favoured scenario is  $\delta C_9^\mu$  followed by  $\delta C_{LL}^\mu$  ( $\delta C_9^\mu = -\delta C_{10}^\mu$ ), same hierarchy as pre 2020 LHCb
- Significance have increased by  $\sim 1\sigma$  for the most prominent scenarios compared to 2019
- Change in significance mainly due to the recent LHCb analysis of the  $B \rightarrow K^* \mu^+ \mu^-$  angular observables with  $4.7 \text{ fb}^{-1}$  ( $\rightarrow$  larger  $\chi_{SM}^2$ )
  - ↪ smaller experimental uncertainties
  - ↪ further tensions

## Global analysis of $b \rightarrow s$ transitions: multi-dimensional fit

Using all the relevant data on  $b \rightarrow s$  transitions

**Multi-dimensional fit:**  $C_7, C_8, C_9^\ell, C_{10}^\ell, C_S^\ell, C_P^\ell +$  primed coefficients (20 d.o.f.)

All observables with $\chi_{\text{SM}}^2 = 157.28$ $(\chi_{\text{min}}^2 = 100.34; \text{Pull}_{\text{SM}} = 4.3\sigma)$			
$\delta C_7$ $0.05 \pm 0.03$		$\delta C_8$ $-0.71 \pm 0.43$	
$\delta C_7'$ $-0.01 \pm 0.02$		$\delta C_8'$ $-0.09 \pm 0.86$	
$\delta C_9^\mu$ $-1.11 \pm 0.19$	$\delta C_9^e$ $-6.69 \pm 1.37$	$\delta C_{10}^\mu$ $0.08 \pm 0.25$	$\delta C_{10}^e$ $3.97 \pm 4.99$
$\delta C_9'^\mu$ $0.18 \pm 0.35$	$\delta C_9'^e$ $1.84 \pm 1.75$	$\delta C_{10}'^\mu$ $-0.13 \pm 0.21$	$\delta C_{10}'^e$ $0.05 \pm 5.01$
$C_{Q_1}^\mu$ $-0.07 \pm 0.12$	$C_{Q_1}^e$ $-1.52 \pm 0.98$	$C_{Q_2}^\mu$ $-0.10 \pm 0.14$	$C_{Q_2}^e$ $-4.36 \pm 1.46$
$C_{Q_1}'^\mu$ $0.05 \pm 0.12$	$C_{Q_1}'^e$ $-1.40 \pm 1.56$	$C_{Q_2}'^\mu$ $-0.17 \pm 0.15$	$C_{Q_2}'^e$ $-4.33 \pm 2.33$

- Significance of the fit has increased by  $\sim 1\sigma$  compared to our 2019 fit
- Several Wilson coefficients in the electron sector were previously undetermined in the 20-dimension fit now all WC are constrained (some still weakly) ← updated upper bound on  $B_s \rightarrow e^+ e^-$  [LHCb 2003.03999]

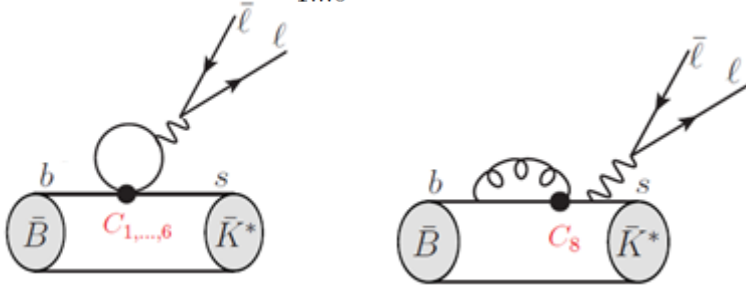
- ❑ Significance of tensions depend on assumptions for power corrections
- ❑ Statistical comparison favours NP, however situation remains inconclusive
- ❑ Future data (after the first LHC upgrade) can give strong indications whether NP better describe the anomalies or hadronic contributions
- ❑ Most favoured NP scenario still  $C_9^\mu$  followed by  $C_{LL}^\mu$  – no change compared to pre-2020
- ❑ Increase of  $\sim 1\sigma$  for the favoured NP scenarios

*Thank you!*

*Backup*

Effective Hamiltonian for  $b \rightarrow s \ell^+ \ell^-$  transitions:  $\mathcal{H}_{\text{eff}} = \mathcal{H}_{\text{eff}}^{\text{had}} + \mathcal{H}_{\text{eff}}^{\text{sl}}$

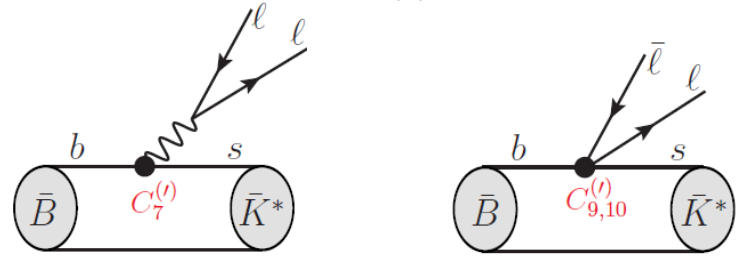
$$\mathcal{H}_{\text{eff}}^{\text{had}} = -\frac{4G_F}{\sqrt{2}} V_{tb} V_{ts}^* \left[ \sum_{i=1 \dots 6} C_i(\mu) O_i(\mu) + C_8(\mu) O_8(\mu) \right]$$



non-local effects: in general “naïve”  
factorization not applicable

$$\frac{e^2}{q^2} \epsilon_\mu L_V^\mu \left[ \underbrace{Y(q^2) \tilde{V}_\lambda}_{\text{fact., perturbative}} + \underbrace{\text{LO in } \mathcal{O}\left(\frac{\Lambda}{m_b}, \frac{\Lambda}{E_{K^*}}\right)}_{\text{non-fact., QCDf}} + \underbrace{h_\lambda(q^2)}_{\text{power corrections,}} \right]$$

$$\mathcal{H}_{\text{eff}}^{\text{sl}} = -\frac{4G_F}{\sqrt{2}} V_{tb} V_{ts}^* \left[ \sum_{i=7,9,10,Q_1,Q_2} C_i^{(\ell)}(\mu) O_i^{(\ell)}(\mu) \right]$$



factorisable contributions:  
7 independent form factors  $\tilde{V}_{\pm,0}, \tilde{T}_{\pm,0}, \tilde{S}$

[Khodjamirian et al. '10, Bharucha et al. '15, Gubernari et al. '18]

Helicity amplitudes:

$$H_V(\lambda) = -i N' \left\{ (C_9^{\text{eff}} - C_9') \tilde{V}_\lambda(q^2) + \frac{m_B^2}{q^2} \left[ \frac{2 \hat{m}_b}{m_B} (C_7^{\text{eff}} - C_7') \tilde{T}_\lambda(q^2) - 16\pi^2 \mathcal{N}_\lambda(q^2) \right] \right\}$$

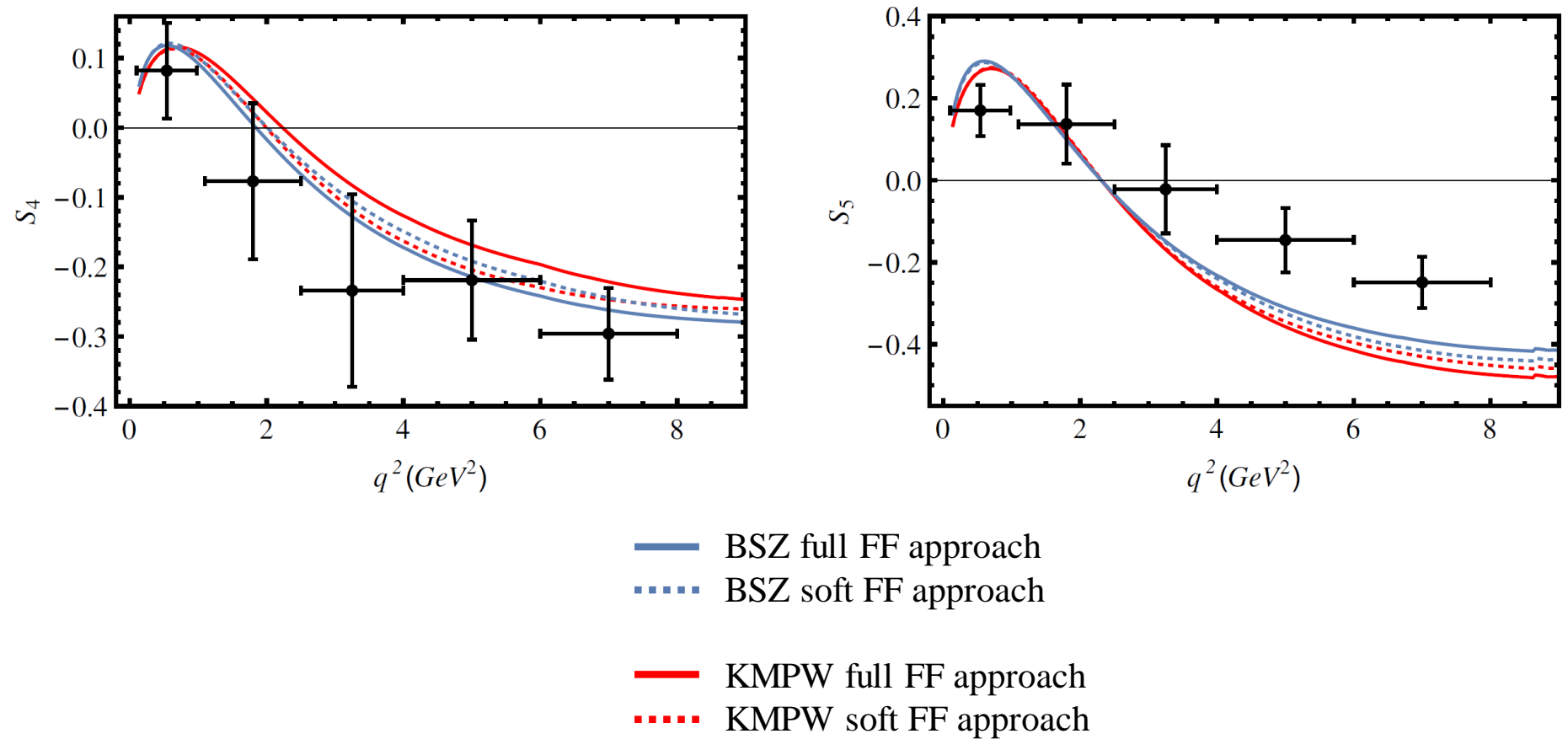
$$h_{\pm,[0]} = \left[ \sqrt{q^2} \times \right] \left( h_{\pm,[0]}^{(0)} + q^2 h_{\pm,[0]}^{(1)} + q^4 h_{\pm,[0]}^{(2)} \right)$$

$$\delta H_V^{\text{PC}}(\lambda = \pm) = i N' \frac{m_B^2}{q^2} 16\pi^2 h_{\pm}(q^2) = i N' \frac{m_B^2}{q^2} 16\pi^2 \left[ h_{\pm}^{(0)} + q^2 h_{\pm}^{(1)} + q^4 h_{\pm}^{(2)} \right]$$

$$\delta H_V^{\text{PC}}(\lambda = 0) = i N' \frac{m_B^2}{q^2} 16\pi^2 h_0(q^2) = i N' \frac{m_B^2}{q^2} 16\pi^2 \left[ \sqrt{q^2} \left( h_0^{(0)} + q^2 h_0^{(1)} + q^4 h_0^{(2)} \right) \right]$$

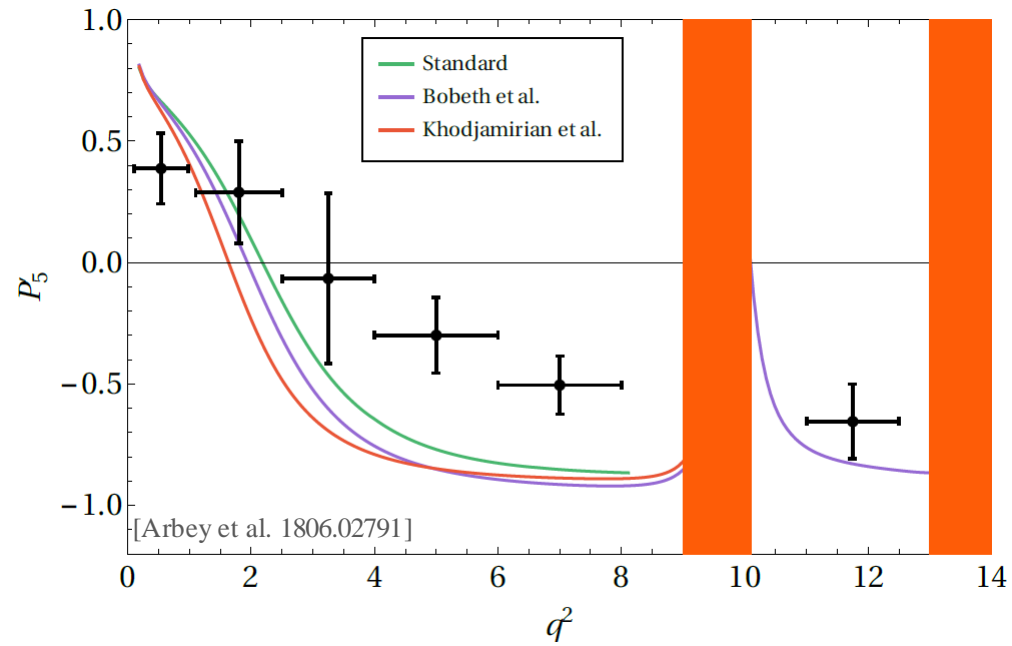
$B \rightarrow K^* \bar{\mu}\mu/\gamma$ observables; low $q^2$ bins up to 8 GeV <sup>2</sup>								
nr. of free parameters	1 $\left(\begin{smallmatrix} \text{Real} \\ \delta C_9 \end{smallmatrix}\right)$	2 $\left(\begin{smallmatrix} \text{Real} \\ \delta C_7, \delta C_9 \end{smallmatrix}\right)$	2 $\left(\begin{smallmatrix} \text{Comp.} \\ \delta C_9 \end{smallmatrix}\right)$	4 $\left(\begin{smallmatrix} \text{Comp.} \\ \delta C_7, \delta C_9 \end{smallmatrix}\right)$	3 $\left(\begin{smallmatrix} \text{Real} \\ \Delta C_9^{\lambda, \text{PC}} \end{smallmatrix}\right)$	6 $\left(\begin{smallmatrix} \text{Comp.} \\ \Delta C_9^{\lambda, \text{PC}} \end{smallmatrix}\right)$	9 $\left(\begin{smallmatrix} \text{Real} \\ h_{+,-,0}^{(0,1,2)} \end{smallmatrix}\right)$	18 $\left(\begin{smallmatrix} \text{Comp.} \\ h_{+,-,0}^{(0,1,2)} \end{smallmatrix}\right)$
0 (plain SM)	6.0 $\sigma$	5.6 $\sigma$	5.8 $\sigma$	5.4 $\sigma$	5.4 $\sigma$	5.5 $\sigma$	5.0 $\sigma$	4.7 $\sigma$
1 (Real $\delta C_9$ )	—	0.5 $\sigma$	1.5 $\sigma$	1.2 $\sigma$	0.6 $\sigma$	1.8 $\sigma$	1.1 $\sigma$	1.5 $\sigma$
2 (Real $\delta C_7, \delta C_9$ )	—	—	—	1.4 $\sigma$	—	—	1.3 $\sigma$	1.6 $\sigma$
2 (Comp. $\delta C_9$ )	—	—	—	0.8 $\sigma$	—	1.7 $\sigma$	—	1.4 $\sigma$
4 (Comp. $\delta C_7, \delta C_9$ )	—	—	—	—	—	—	—	1.5 $\sigma$
3 (Real $\Delta C_9^{\lambda, \text{PC}}$ )	—	—	—	—	—	2.2 $\sigma$	1.4 $\sigma$	1.7 $\sigma$
6 (Comp. $\Delta C_9^{\lambda, \text{PC}}$ )	—	—	—	—	—	—	—	0.1 $\sigma$
9 (Real $h_{+,-,0}^{(0,1,2)}$ )	—	—	—	—	—	—	—	1.5 $\sigma$

## Impact of choice of form factors (BSZ vs KMPW) and approach (full FF , soft FF)

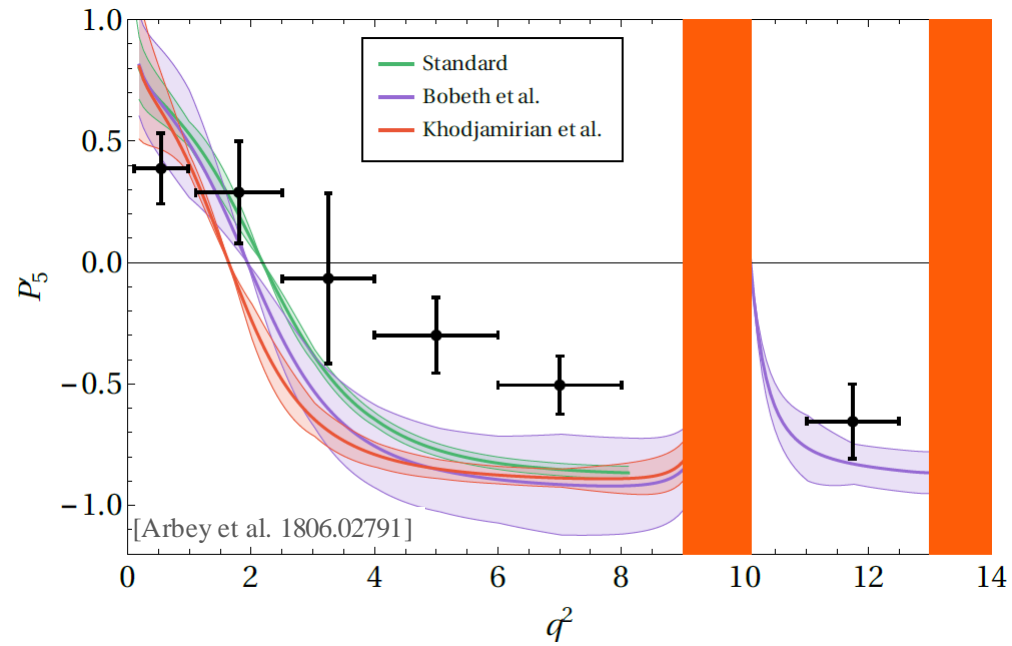




## Impact of power corrections



## Impact of power corrections



## Impact of power corrections

