

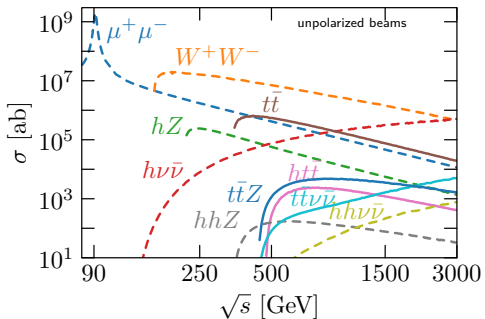
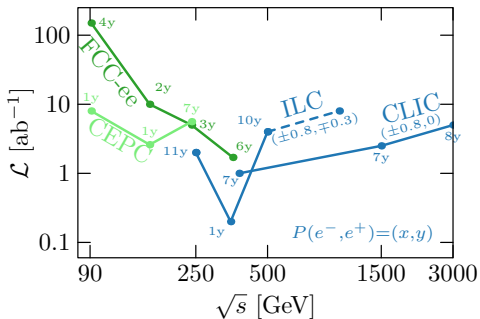
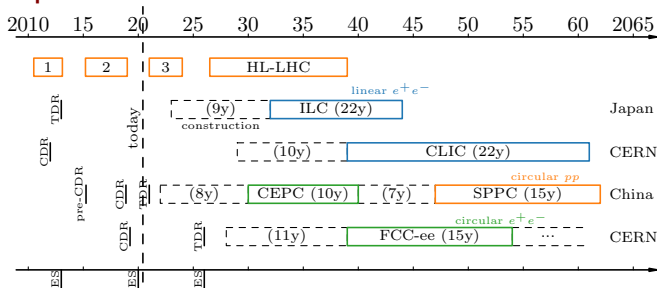
# Top-quark precision at lepton colliders

Gauthier Durieux  
(Technion)

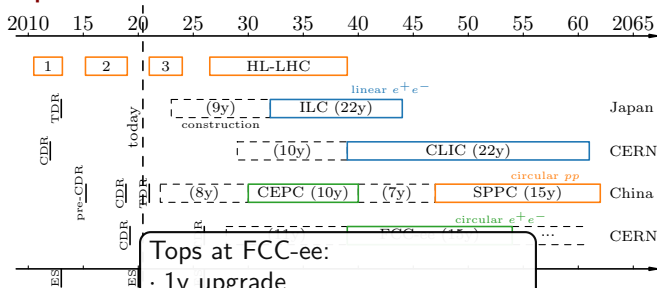
FCC France workshop  
15 May 2020



# Tops at lepton colliders

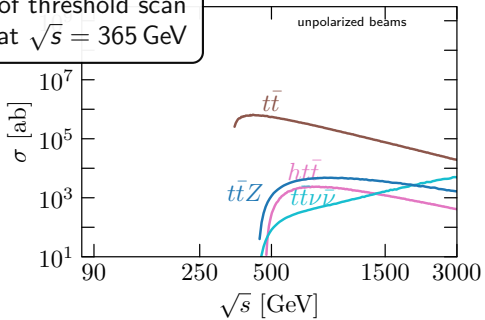
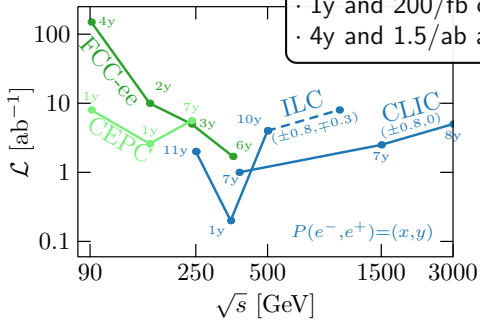


# Tops at lepton colliders



**Tops at FCC-ee:**

- 1y upgrade
- 1y and 200/fb of threshold scan
- 4y and 1.5/ab at  $\sqrt{s} = 365$  GeV

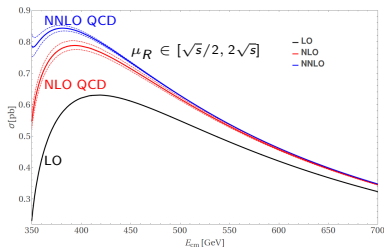


# Continuum $t\bar{t}$ production

## ► NNLO QCD, differential, stable tops

[Gao, Zhu '14]

[Chen, Dekkers, Heisler, Bernreuther, Si '16]



- $\sigma$  peaked at about 380 GeV
- fall-off as  $1/s$
- large corrections near threshold
- (enhanced for a left-handed beam)

## ► NLO EW, stable tops

[Beenakker, van der Marck, Hollik '91]

[Fleischer, Leike, Riemann, Werthenbach '93]

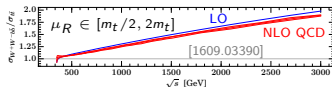
[Hahn, Hollik, Lorca, Riemann, Werthenbach '93]

## ► NLO QCD, unstable tops

[Liebler, Moortgat-Pick, Papanastasiou '15]

[Chokoufé, Kilian, Lindert, Pozzorini, Reuter, Weiss '16]

- single-top increases linearly with  $\sqrt{s}$
- $\sim 5\%$  off-shell effects at  $\sqrt{s} = 365$  GeV

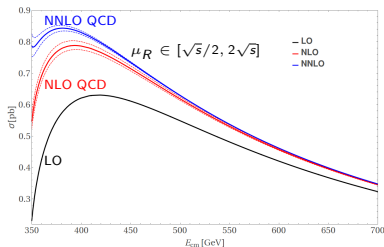


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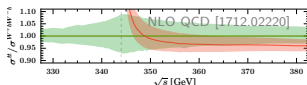
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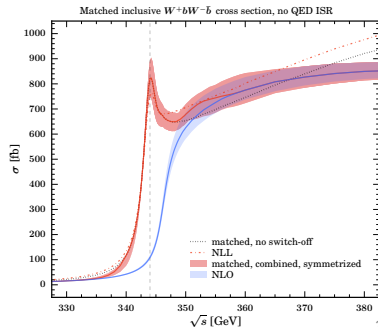
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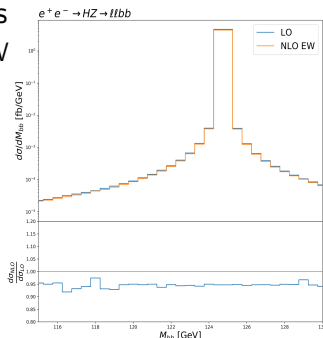
# Tools

getting ee-ready

- ▶ UFO support for BSM (almost complete)
- ▶ automated NLO QCD (FKS, resonance aware) [v3.0.0 $\alpha$  from March 3, 2020]
- ▶ Powheg matching to Pythia8 shower
- ▶ ee-ISR & beamstrahlung, also for polarized beams
- ▶ matched NLO  $e^+e^- \rightarrow bW^+\bar{b}W^-$  to threshold NLL [1712.02220]



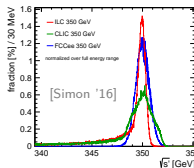
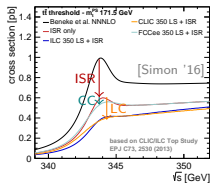
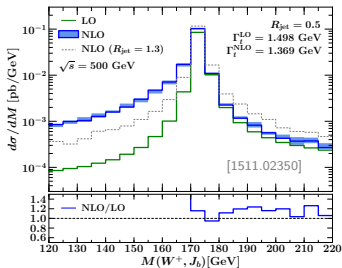
- ▶ UFO support for BSM
- ▶ automated NLO QCD and EW (CS subtraction)
- ▶ mc@nlo matching to parton shower
- ▶ YFS resummation of soft&collinear photons
  - to be matched to matrix element for NLO EW
  - no ISR/FSR interference yet
- ▶ Beamstrahlung being implemented
- ▶ Underlying events (e.g.  $\gamma\gamma$ ) planned





# MadGraph

- ▶ full UFO support for BSM (also at NLO)
- ▶ automated NLO QCD and EW (FKS, resonance aware)
- ▶ mc@nlo matching to parton shower
- ▶ ee-ISR
  - implemented for unpolarized beams [not released]
  - validated against Whizard in  $e^+e^- \rightarrow t\bar{t}$
- ▶ beamsstrahlung
  - implemented using parametrizations fitted to GuineaPig
  - no beam energy spread, so far
  - validation ongoing
- ▶ NLO+NLL electron PDF [Frixiene @ FCC workshop]
  - computed for unpolarized beams
  - only missing piece to be implemented for NLO EW



# Top EFT at NLO QCD

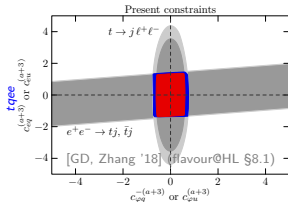
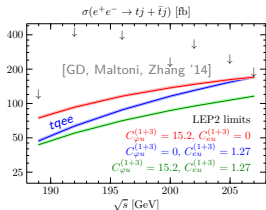
## LHC TOP WG standards

[dim6top UFO] [1802.07237]

avoid confusions, facilitate comparisons and combinations

### ► flavour violating [Zhang '14] [Degrande, Maltoni, Wang, Zhang '14] [GD, Maltoni, Zhang '14]

- UFO updated to LHC TOP WG standards [to appear] [TopFCNC UFO]
- automated NLO for four-fermion  $tqll$  operators [to appear]



### ► flavour conserving

- four-quark operators (with evanescent operators) [to appear]
- all-sector implementation [to appear] [SMEFtAtNLO UFO]

[Degrande, GD, Maltoni, Mimasu, Vryonidou, Zhang]

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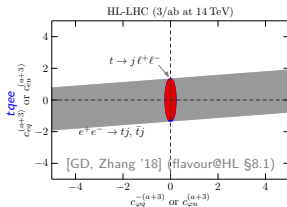
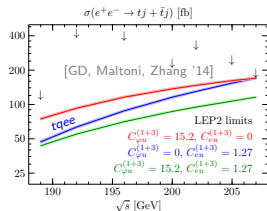
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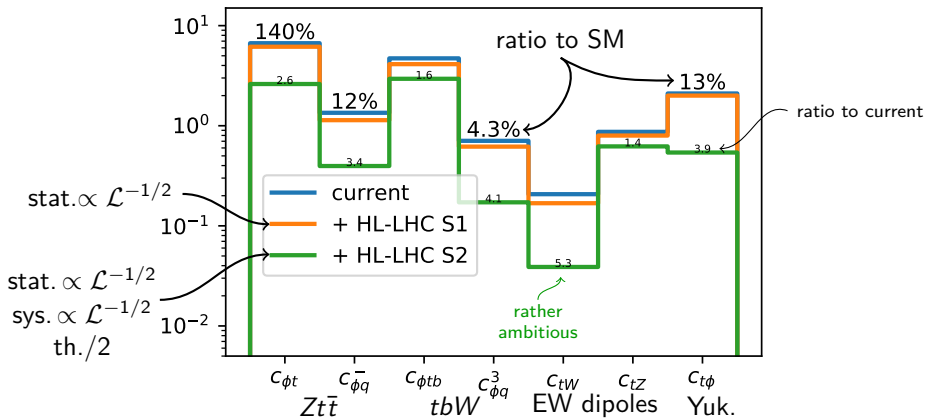
[Degrande, GD, Maltoni, Mimasu, Vryonidou, Zhang]

# Electroweak couplings

precise, global and robust

# LHC prospects

[projections from 1907.10619]  
 [TOP WG EFT conventions]

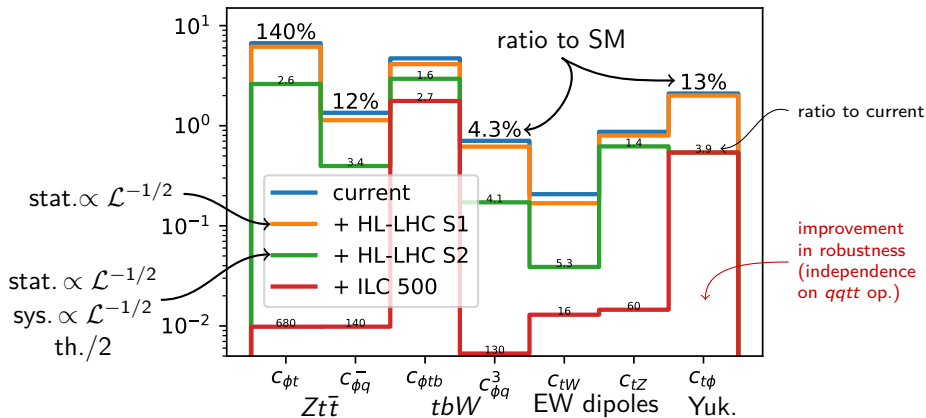


→ sys. and th. limited reach

→  $\sim 10\%$  level precision

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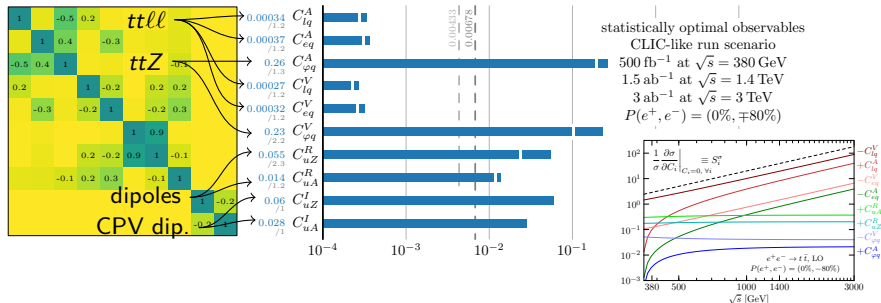
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# Global $e^+e^- \rightarrow t\bar{t}$ EFT analysis

[GD, Perelló, Vos, Zhang '18]

[see also Janot '15]

Two centre of mass energies are required to constrain all ten d.o.f. accessible linearly in resonant  $e^+e^- \rightarrow t\bar{t} \rightarrow bW^+ \bar{b}W^-$ .



statistically optimal observables

resonant  $e^+e^- \rightarrow t\bar{t} \rightarrow bW^+ \bar{b}W^-$   
 $m_b/m_t \rightarrow 0$ , analytical LO observable def.

effective stat. efficiencies determined with full sim.  
 in semi-leptonic final state

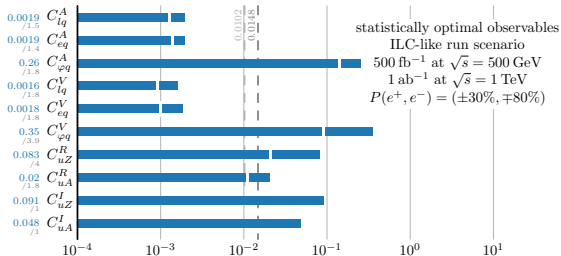
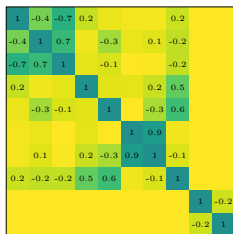
- in TeV<sup>-2</sup>,  $\Delta\chi^2 = 1$
- white marks: individual constraints
- /xx: global/individual ratios

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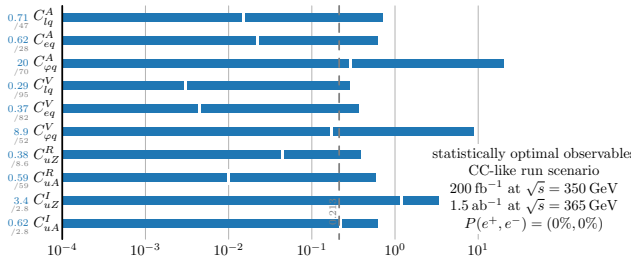
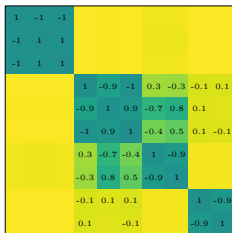


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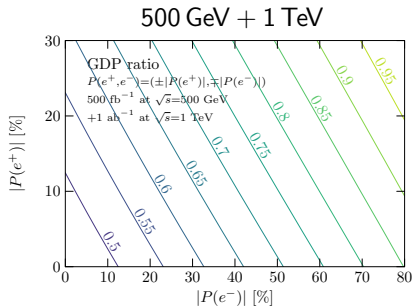


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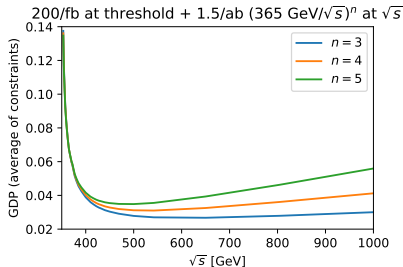
10% polarization costs  $\sim 5\%$  of GDP

w.r.t.  $P(e^+, e^-) = (\pm 30\%, \mp 80\%)$ :

- $P(e^+)$  compensated by 140% lumi
- $P(e^+, e^-)$  // by 460% lumi

$GDP \equiv [\det \text{cov}(C_i, C_j)]^{1/n}$   
 'global determinant parameter'  
 geometrical average of constraints  
 ratios are operator-basis independent

[GD, Grojean, Gu, Wang '17]

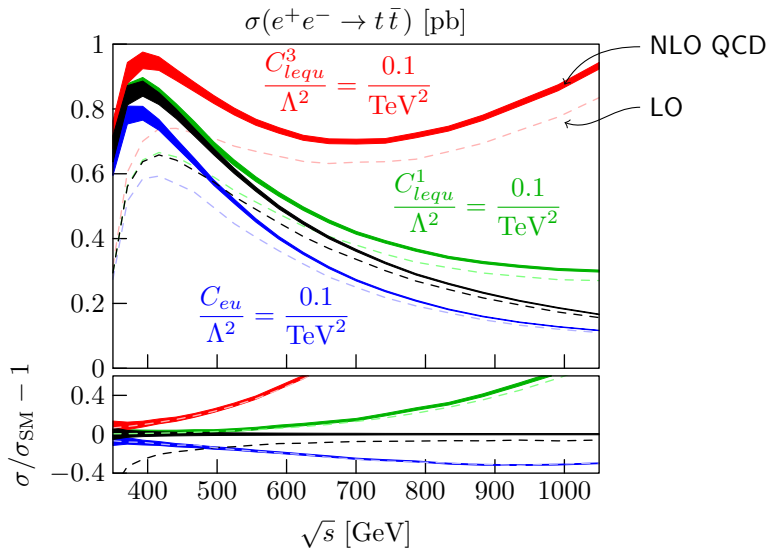


$\sqrt{s}$  lever arm disentangles  $2f/4f$

# NLO QCD for $t\bar{t}l\bar{l}$ and CPV dipole operators

In passing:

[GD, Perelló, Vos, Zhang '18]



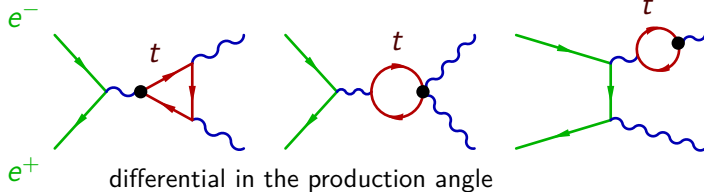
# Top/Higgs interplay

at one-loop

# Top electroweak loops

- At the  $Z$  pole
- In diboson production

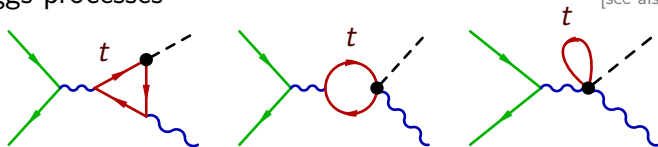
[Zhang, Greiner, Willenbrock '12]



[GD, Gu, Vrionidou, Zhang '18]

- In Higgs processes

[Vrionidou, Zhang, '18]  
[see also Boselli et al '18]



- Higgsstrahlung and  $W$ -fusion through reweighing in MG5/AMC@NLO
- Higgs decays

(excluding four-fermion operators, no top loop included in  $e^+e^- \rightarrow t\bar{t}$ )

# Top electroweak loops

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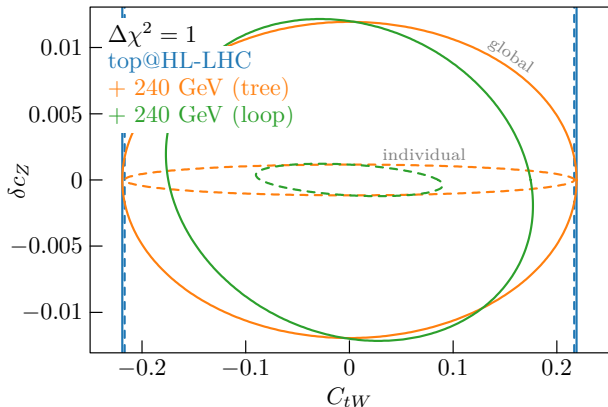
$e^-$

$e^+$

- In Higgs

• Higgs

• Higgs decays



- extra parameter space covered thanks to loop sensitivity
- room for improvement between glo. and ind. constraints

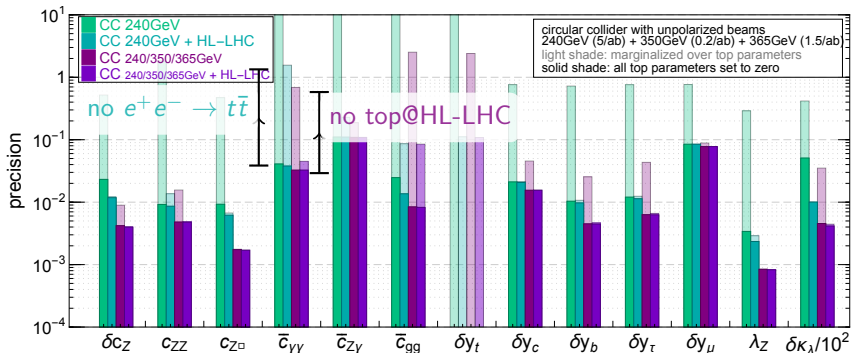
[GD, Gu, Vrionidou, Zhang '18]

(excluding four-fermion operators, no top loop included in  $e^+e^- \rightarrow t\bar{t}$ )

# Contamination in Higgs operators

[GD, Gu, Vriouidou, Zhang '18]

light shades: 12 Higgs op. floated + 6 top op. floated  
 dark shades: 12 Higgs op. floated + 6 top op.  $\rightarrow 0$



Uncertainties on the top have a big effect on the Higgs

- Higgsstr. run: insufficient
- Higgsstr. run  $\oplus e^+e^- \rightarrow t\bar{t}$ : large  $y_t$  contaminations in various coefficients
- Higgsstr. run  $\oplus$  top@HL-LHC: large top contaminations in  $\bar{c}_{\gamma\gamma,gg,Z\gamma,ZZ}$
- Higgsstr. run  $\oplus e^+e^- \rightarrow t\bar{t} \oplus$  top@HL-LHC: top contam. in  $\bar{c}_{gg}$  only

# Top-quark precision at lepton colliders

The top quark so far escaped the scrutiny of lepton colliders.

Such machines offer a unique opportunity  
for precise and robust determination  
of the top electroweak couplings and mass.

Knowing top-quark couplings precisely is indispensable  
for the Higgs precision program.

Tools are getting *ee*-ready!



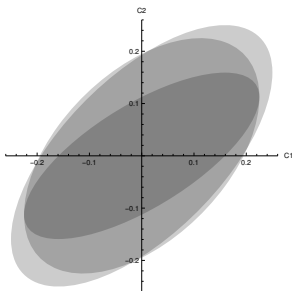
Backup

# Statistically optimal observables

minimize the one-sigma ellipsoid in EFT parameter space

(*joint efficient* set of estimators, saturating the Cramér-Rao bound:  $V^{-1} = I$ , like MEM)

For small  $C_i$ , with a phase-space distribution  $\sigma(\Phi) = \sigma_0(\Phi) + \sum_i C_i \sigma_i(\Phi)$ ,  
the stat. opt. obs. are the average values of  $O_i(\Phi) = n \sigma_i(\Phi) / \sigma_0(\Phi)$ .



e.g.  $\sigma(\phi) = 1 + \cos(\phi) + C_1 \sin(\phi) + C_2 \sin(2\phi)$

1. asymmetries:  $O_i \sim \text{sign}\{\sin(i\phi)\}$

2. moments:  $O_i \sim \sin(i\phi)$

3. statistically optimal:  $O_i \sim \frac{\sin(i\phi)}{1 + \cos \phi}$

$\Rightarrow$  area ratios 1.9 : 1.7 : 1

Previous applications in  $e^+e^- \rightarrow t\bar{t}$ , on different distributions:

[Grzadkowski, Hioki '00]

[Janot '15]

[Khiem et al '15]