# B-physics and viable NP(LQ) scenarios 

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## Workshop FCC-France (May 2020)

based on works done with
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## Turn of the 21st century CKM




Impressively - TL UT and LP UT agree to less than I0\%
CPV phase is non-zero but too small to accommodate the observes BAU
[Experiment - high precision era! Lattices huge improvement!]
Only tensions in Vub and Vcb (inclusive Vs. exclusive) but all in all, CKM is very unitary! 2008, Nobel Prize

## Impressive progress in LQCD



## Impressive progress in LQCD



## Or else... NP searches

## Strategy:

fix $\mathrm{V}_{\text {ij }}$ from tree level processes, then look for NP in FCNC


$$
\mathcal{B}\left(B_{s} \rightarrow \mu^{+} \mu^{-}\right)_{\text {theo. }}=3.34\left({ }_{-25}^{+13}\right) \times 10^{-9} \quad \mathcal{B}\left(B_{s} \rightarrow \mu^{+} \mu^{-}\right)_{\mathrm{LHCb}+\mathrm{CMS}}=2.9(7) \times 10^{-9}
$$

| $C_{i j}$ | 1 | $V_{t i} V_{t j}^{*}$ |
| :---: | :---: | :---: |
| $B_{s} \rightarrow \mu^{+} \mu^{-}$ | $>10 \mathrm{TeV}$ | $>2.5 \mathrm{TeV}$ |
| $K \rightarrow \pi \nu \bar{\nu}$ | $>100 \mathrm{TeV}$ | $>1.8 \mathrm{TeV}$ |

$$
O=\frac{1}{\Lambda^{2}} C_{i j} \bar{Q}_{i} \gamma^{\mu} Q_{j} H^{\dagger} D_{\mu} H
$$

Strategy:
fix $\mathrm{V}_{\mathrm{ij}}$ by tree level processes, then look for NP in FCNC


$$
O=\frac{1}{\Lambda^{2}} C_{i j}^{\prime} \bar{Q}_{i} \gamma^{\mu} Q_{j} \bar{Q}_{i} \gamma_{\mu} Q_{j}
$$

| $C_{i j}^{\prime}$ | 1 | $\left\|V_{t i} V_{t j}^{*}\right\|^{2}$ |
| :---: | :---: | :---: |
| $K^{0}-\bar{K}^{0}$ | $>2 \times 10^{4} \mathrm{TeV}$ | $>8 \mathrm{TeV}$ |
| $B^{0}-\bar{B}^{0}$ | $>0.5 \times 10^{4} \mathrm{TeV}$ | $>5 \mathrm{TeV}$ |
| $B_{s}^{0}-\bar{B}_{s}^{0}$ | $>0.1 \times 10^{4} \mathrm{TeV}$ | $>5 \mathrm{TeV}$ |

## Flavor puzzle

| $C_{i j}$ | 1 | $V_{t i} V_{t j}^{*}$ |
| :---: | :---: | :---: |
| $B_{s} \rightarrow \mu^{+} \mu^{-}$ | $>10 \mathrm{TeV}$ | $>2.5 \mathrm{TeV}$ |
| $K \rightarrow \pi \nu \bar{\nu}$ | $>100 \mathrm{TeV}$ | $>1.8 \mathrm{TeV}$ |

- For natural C~O(1), NP scale is huge
- Need lots of fine tuning to reduce NP scale to $\mathrm{O}(1 \mathrm{TeV})$ as needed to mend the hierarchy problem
- Way out: NP is (almost) aligned with the SM
- MFV

| $C_{i j}^{\prime}$ | 1 | $\left\|V_{t i} V_{t j}^{*}\right\|^{2}$ |
| :---: | :---: | :---: |
| $K^{0}-\bar{K}^{0}$ | $>2 \times 10^{4} \mathrm{TeV}$ | $>8 \mathrm{TeV}$ |
| $B^{0}-\bar{B}^{0}$ | $>0.5 \times 10^{4} \mathrm{TeV}$ | $>5 \mathrm{TeV}$ |
| $B_{s}^{0}-\bar{B}_{s}^{0}$ | $>0.1 \times 10^{4} \mathrm{TeV}$ | $>5 \mathrm{TeV}$ |

## 2012-202X : LFUV was and still is exciting

$$
R_{D^{(*)}}=\frac{\mathcal{B}\left(B \rightarrow D^{(*)} \tau \bar{\nu}\right)}{\mathcal{B}\left(B \rightarrow D^{(*)} \ell \bar{\nu}\right)_{\ell \in(e, \mu)} \quad \& \quad R_{D^{(*)}}^{\exp }>R_{D^{(*)}}^{\mathrm{SM}}, ~} \quad
$$

$$
R_{K^{(*)}}=\left.\frac{\mathcal{B}\left(B \rightarrow K^{(*)} \mu \mu\right)}{\mathcal{B}\left(B \rightarrow K^{(*)} e e\right)}\right|_{q^{2} \in\left[q_{\min }^{2}, q_{\max }^{2}\right]} \& \quad R_{K^{(*)}}^{\exp }<R_{K^{(*)}}^{\mathrm{SM}}
$$

Also corroborated by LHCb through $R_{J / \psi}^{\exp }>R_{J / \psi}^{\mathrm{SM}}, R_{p K}^{\exp }>R_{p K}^{\mathrm{SM}}$

$$
\begin{array}{ll}
R_{D^{(*)}}^{\exp }>R_{D^{(*)}}^{\mathrm{SM}} & \Rightarrow \quad \Lambda_{\mathrm{NP}} \lesssim 3 \mathrm{TeV} \\
R_{K^{(*)}}^{\exp }<R_{K^{(*)}}^{\mathrm{SM}} \quad \Rightarrow \quad \Lambda_{\mathrm{NP}} \lesssim 30 \mathrm{TeV} \quad \text { Di Luzio et al. } 2017
\end{array}
$$

## After Moriond EW 2019

$$
R_{D^{(*)}}=\frac{\mathcal{B}\left(B \rightarrow D^{(*)} \tau \bar{\nu}\right)}{\mathcal{B}\left(B \rightarrow D^{(*)} \ell \bar{\nu}\right)}
$$



- NEW [Belle]: $R_{D}=0.31(4)$, $R_{D^{*}}=0.28(2)$.
- $R_{\left.D^{*}\right)}$ discrepancy w.r.t. SM predictions decreases from $3.8 \sigma$ to $3.1 \sigma$.
- Large disagreement between BaBar and Belle results.
$\Rightarrow$ Unclear exp. situation!

After Moriond EW 2019




- NEW [LHCb]:

$$
\left[R_{K}^{\text {new }}\right]_{\text {avg }}=0.85(6)
$$

- Discrepancy between Run 1 and Run $2[\approx 2 \sigma]$ :

$$
\begin{aligned}
& {\left[R_{K}^{\text {new }}\right]_{\text {run } 1}=0.71(8)} \\
& {\left[R_{K}^{\text {new }}\right]_{\text {run 2 }}=0.92(8)}
\end{aligned}
$$

## EFT - exclusive $b \rightarrow c \ell \nu$

$$
\begin{aligned}
\mathcal{L}_{\mathrm{eff}} & =-2 \sqrt{2} G_{F} V_{c b}\left[\left(1+g_{V_{L}}\right)\left(\bar{c}_{L} \gamma_{\mu} b_{L}\right)\left(\bar{\ell}_{L} \gamma^{\mu} \nu_{L}\right)+g_{V_{R}}\left(\bar{c}_{R} \gamma_{\mu} b_{R}\right)\left(\bar{\ell}_{L} \gamma^{\mu} \nu_{L}\right)\right. \\
& \left.+g_{S_{R}}\left(\bar{c}_{L} b_{R}\right)\left(\bar{\ell}_{R} \nu_{L}\right)+g_{S_{L}}\left(\bar{c}_{R} b_{L}\right)\left(\bar{\ell}_{R} \nu_{L}\right)+g_{T}\left(\bar{c}_{R} \sigma_{\mu \nu} b_{L}\right)\left(\bar{\ell}_{R} \sigma^{\mu \nu} \nu_{L}\right)\right]+ \text { h.c. }
\end{aligned}
$$

- $S U(3)_{c} \times S U(2)_{L} \times U(1)_{Y}$ gauge invariance:
$\Rightarrow g_{V_{R}}$ is LFU at dimension $6\left(W \bar{c}_{R} b_{R}\right.$ vertex).
$\Rightarrow$ Four coefficients left: $g_{V_{L}}, g_{S_{L}}, g_{S_{R}}$ and $g_{T}$.
- Several viable solutions to $R_{D^{(*)}}$ :
[Freytsis et al. 2015]
- e.g. $g_{V_{L}} \in(0.04,0.11)$, but not only!


## Which coupling? Situation after Moriond EW 2019



Updates of Freytsis et al. '15 Angelescu et al. '18

Which Lorentz structure to pick?
Observables from angular distribution of $B \rightarrow D^{*}(D \pi) \ell \nu$ can help


MILC-Fermilab 1912.05886

## What $L Q$ scenario for $R_{D}$ and $R_{D^{*}}$ ?

| Model | $g_{\text {eff }}^{b \rightarrow c \tau \bar{\nu}}\left(\mu=m_{\Delta}\right)$ | $R_{D^{(*)}}$ |
| :---: | :---: | :---: |
| $S_{1}=(\overline{3}, 1,1 / 3)$ | $g_{V_{L}}, g_{S_{L}}=-4 g_{T}$ | $\checkmark$ |
| $R_{2}=(3,2,7 / 6)$ | $g_{S_{L}}=4 g_{T}$ | $\checkmark$ |
| $S_{3}=(\overline{3}, 3,1 / 3)$ | $g_{V_{L}}$ | $\times$ |
| $\ldots$ | $\ldots$ | $\ldots$ |
| $U_{1}=(3,1,2 / 3)$ | $g_{V_{L}}, g_{S_{R}}$ | $\checkmark$ |
| $U_{3}=(3,3,2 / 3)$ | $g_{V_{L}}$ | $\times$ |
| $\ldots$ | $\ldots$ | $\ldots$ |

Viable models for $\underline{R_{D^{(*)}}}$ :

- $U_{1}\left(g_{V_{L}}\right), S_{1}\left(g_{V_{L}}\right.$ and $\left.g_{S_{L}}=-4 g_{T}\right)$, and $R_{2}\left(g_{S_{L}}=4 g_{T} \in \mathbb{C}\right)$
- Some models are excluded by other flavor constraints: $B \rightarrow K \nu \bar{\nu}, \Delta m_{B_{s}} \ldots$
- Possibility to distinguish them by using other $b \rightarrow c \not \nu \nu$ observables!


## EFT - exclusive $b \rightarrow$ sll

$$
\mathcal{H}_{\text {eff }}=-\frac{4 G_{F}}{\sqrt{2}} V_{t b} V_{t s}^{*}\left[\sum_{i=1}^{6} C_{i}(\mu) \mathcal{O}_{i}(\mu)+\sum_{i=7,8,9,10, P, S, \ldots}\left(C_{i}(\mu) \mathcal{O}_{i}+C_{i}^{\prime}(\mu) \mathcal{O}_{i}^{\prime}\right)\right]+\text { h.c. }
$$

$$
\begin{array}{ll}
\mathcal{O}_{9}^{(\prime)}=\left(\bar{s} \gamma_{\mu} P_{L(R)} b\right)\left(\bar{\ell} \gamma^{\mu} \ell\right) & \mathcal{O}_{10}^{(\prime)}=\left(\bar{s} \gamma_{\mu} P_{L(R)} b\right)\left(\bar{\ell} \gamma^{\mu} \gamma^{5} \ell\right) \\
\mathcal{O}_{S}^{(\prime)}=\left(\bar{s} P_{R(L)} b\right)(\overline{\ell \ell}) & \mathcal{O}_{P}^{(\prime)}=\left(\bar{s} P_{R(L)} b\right)\left(\bar{\ell} \gamma_{5} \ell\right) \\
\mathcal{O}_{7}^{(\prime)}=m_{b}\left(\bar{s} \sigma_{\mu \nu} P_{R(L)} b\right) F^{\mu \nu} & \\
\hline
\end{array}
$$

$$
\mathcal{B}\left(B_{s} \rightarrow \mu \mu\right)^{\exp }=\left(3.0 \pm 0.6_{-0.2}^{+0.3}\right) \times 10^{-9}
$$

Fit to clean quantities: $\mathcal{B}\left(B_{s} \rightarrow \mu \mu\right)$ and $R_{K^{(*)}}$


- Only vector (axial) coefficients can accommodate data.
- $C_{9,10}^{\prime}$ disfavored by $R_{K^{*}}^{\exp }<R_{K^{*}}^{\mathrm{SM}}$
- $C_{9}=-C_{10}$ allowed - consistent with a left-handed $S U(2)_{L}$ invariant operator!


## What LQ scenario for $R_{k}$ and $R_{k}$ ?



$$
\mathcal{L}=x_{L}^{i j} \bar{Q}_{i} \gamma_{\mu} U_{1}^{\mu} L_{j}+x_{R}^{i j} \bar{d}_{R i} \gamma_{\mu} U_{1}^{\mu} \ell_{R j}+\text { h.c. },
$$

Assumptions:

$$
x_{L}=\left(\begin{array}{ccc}
0 & 0 & 0 \\
0 & x_{L}^{s \mu} & x_{L}^{s \tau} \\
0 & x_{L}^{b \mu} & x_{L}^{b \tau}
\end{array}\right), \quad \quad x_{R} \approx 0 .
$$

$$
\begin{aligned}
\bullet b & \rightarrow c \tau \bar{\nu}: \\
g_{V_{L}} & =\frac{v^{2}}{2 m_{U_{1}}^{2}}\left(x_{L}^{b \tau}\right)^{*}\left(x_{L}^{b \tau}+\frac{V_{c s}}{V_{c b}} x_{L}^{s \tau}\right) \neq 0
\end{aligned}
$$

- $b \rightarrow s \mu \mu$ :

$$
x_{L}=\left(\begin{array}{ccc}
0 & 0 & 0 \\
0 & x_{L}^{s \mu} & x_{L}^{s \tau} \\
0 & x_{L}^{b \mu} & x_{L}^{b \tau}
\end{array}\right)
$$

$C_{9}^{\mu \mu}=-C_{10}^{\mu \mu} \propto-\frac{\pi v^{2}}{m_{U_{1}}^{2}}\left(x_{L}^{b \mu}\right)^{*} x_{L}^{s \mu} \neq 0$

- Other observables: $\tau \rightarrow \mu \phi, B \rightarrow \tau \bar{\nu}, D_{(s)} \rightarrow \mu \bar{\nu}, D_{s} \rightarrow \tau \bar{\nu}$, $K \rightarrow \mu \bar{\nu} / K \rightarrow e \bar{\nu}, \tau \rightarrow K \bar{\nu}$ and $B \rightarrow D^{(*)} \mu \bar{\nu} / B \rightarrow D^{(*)} e \bar{\nu}$.
- LQ pair-production via QCD:

- Di-lepton tails at high-pT:


Angelescu et al '18, Faroughy et al '15
[CMS-PAS-EXO-17-003]

$$
m_{U_{1}} \gtrsim 1.5 \mathrm{TeV}
$$

[assuming $\left.\mathcal{B}\left(U_{1} \rightarrow b \tau\right) \approx 0.5\right]$
[ATLAS. 1707.02424,1709.07242]




$$
\mathcal{B}(B \rightarrow K \mu \tau) \gtrsim \text { few } \times 10^{-7}
$$

UV completion:

- Pati-Salam group, $\mathcal{G}_{\mathrm{PS}}=S U(4) \times S U(2)_{L} \times S U(2)_{R}$, contains $U_{1}=(3,1,2 / 3)$.
- Viable extensions of $\mathcal{G}_{\mathrm{PS}}$ at the TeV scale have been proposed: $\Rightarrow U_{1}+Z^{\prime}+g^{\prime}$ [+new fermions].


## Back to SLQ's

| Model | $R_{D^{(*)}}$ | $R_{K^{(*)}}$ | $R_{D^{(*)}} \& R_{K^{(*)}}$ |
| :---: | :---: | :---: | :---: |
| $S_{1}=(\overline{3}, 1,1 / 3)$ | $\checkmark$ | $x$ | $x$ |
| $R_{2}=(3,2,7 / 6)$ | $\checkmark$ | $\checkmark^{*}$ | $x$ |
| $S_{3}=(\overline{3}, 3,1 / 3)$ | $x$ | $\checkmark$ | $x$ |
| $U_{1}=(3,1,2 / 3)$ | $\checkmark$ | $\checkmark$ | $\checkmark$ |
| $U_{3}=(3,3,2 / 3)$ | $x$ | $\checkmark$ | $x$ |


| Observable |
| :---: |
| $b \rightarrow s \mu \mu$ |
| $b \rightarrow c \tau \nu$ |
| $\mathcal{B}(\tau \rightarrow \mu \phi)$ |
| $\mathcal{B}(B \rightarrow \tau \nu)$ |
| $\mathcal{B}\left(D_{s} \rightarrow \mu \nu\right)$ |
| $\mathcal{B}\left(D_{s} \rightarrow \tau \nu\right)$ |
| $r_{K}^{e / \mu}$ |
| $r_{K}^{\tau / \mu}$ |
| $R_{D}^{\mu / e}$ |

## $Z \rightarrow \ell \ell$ and $Z \rightarrow \nu \nu$

Arnan, D.B., Mescia, Sumensari '19 [arXiv:1901.06315]


$$
\delta \mathcal{L}_{\text {eff }}^{Z}=\frac{g}{\cos \theta_{W}} \sum_{f, i, j} \bar{f}_{i} \gamma^{\mu}\left[g_{f_{L}}^{i j} P_{L}+g_{f_{R}}^{i j} P_{R}\right] f_{j} Z_{\mu}
$$

$$
g_{f_{L(R)}}^{i j}=\delta_{i j} g_{f_{L(R)}}^{\mathrm{SM}}+\delta g_{f_{L(R)}}^{i j}: \quad \begin{aligned}
& g_{f_{L}}^{\mathrm{SM}}=I_{3}^{f}-Q^{f} \sin ^{2} \theta_{W} \\
& g_{f_{R}}^{\mathrm{SM}}=-Q^{f} \sin ^{2} \theta_{W}
\end{aligned}
$$

$$
\begin{aligned}
& g_{V}^{e, \exp }=-0.03817(47) \\
& g_{V}^{\mu, \exp }=-0.0367(23) \\
& g_{V}^{\tau, \exp }=-0.0366(10)
\end{aligned}
$$

$$
g_{A}^{e, \exp }=-0.50111(35)
$$

$$
\begin{aligned}
g_{A}^{\mu, \exp } & =-0.50120(54) \\
g_{A}^{\tau, \exp } & =-0.50204(64)
\end{aligned}
$$

Not in Phys.Rep. by Dorsner et al '16

$$
\delta \mathcal{L}_{\mathrm{eff}}^{Z}=\frac{g}{\cos \theta_{W}} \sum_{f, i, j} \bar{f}_{i} \gamma^{\mu}\left[g_{f_{L}}^{i j} P_{L}+g_{f_{R}}^{i j} P_{R}\right] f_{j} Z_{\mu}
$$

$$
g_{f_{L(R)}}^{i j}=\delta_{i j} g_{f_{L(R)}}^{\mathrm{SM}}+\delta g_{f_{L(R)}}^{i j}
$$

$$
\begin{aligned}
& g_{f_{L}^{\mathrm{SM}}}=I_{3}^{f}-Q^{f} \sin ^{2} \theta_{W} \\
& g_{f_{R}}^{\mathrm{SM}}=-Q^{f} \sin ^{2} \theta_{W}
\end{aligned}
$$




LLA: $\mathcal{O}\left(x_{t} \log x_{t}\right), \mathcal{O}\left(x_{Z} \log x_{Z}\right)$

$$
x_{j}=m_{j}^{2} / m_{\Delta}^{2}
$$

Feruglio et al. '17 and '18
Full: most significant $\mathcal{O}\left(x_{Z} \log x_{t}\right)$

$$
\mathcal{L}_{R_{2}}=y_{R}^{i j} \bar{Q}_{i} \ell_{R j} R_{2}-y_{L}^{i j} \bar{u}_{R i} R_{2} i \tau_{2} L_{j}+\text { h.c. }
$$

$C_{9}^{k l}=C_{10}^{k l} \stackrel{\text { tree }}{=}-\frac{\pi v^{2}}{2 V_{t b} V_{t s}^{*} \alpha_{\mathrm{em}}} \frac{y_{R}^{s l}\left(y_{R}^{b k}\right)^{*}}{m_{R_{2}}^{2}}$.
$C_{9}^{k l}=-C_{10}^{k l} \stackrel{\text { loop }}{=} \sum_{u, u^{\prime} \in\{u, c, t\}} \frac{V_{u b} V_{u^{\prime} s}^{*}}{V_{t b} V_{t s}^{*}} y_{L}^{u^{\prime} k}\left(y_{L}^{u l}\right)^{*} \mathcal{F}\left(x_{u}, x_{u^{\prime}}\right)$

$$
y_{L}=\left(\begin{array}{ccc}
0 & 0 & 0 \\
0 & y_{L}^{c \mu} & 0 \\
0 & y_{L}^{t \mu} & 0
\end{array}\right), \quad \quad y_{R}=0
$$




## Accommodating all of them $-\mathrm{R}_{\mathrm{D}}, \mathrm{R}_{\mathrm{D}^{*}}, \mathrm{R}_{\mathrm{K}}, \mathrm{R}_{\mathrm{k}^{*}}$

| Model | $R_{D^{(*)}}$ | $R_{K^{(*)}}$ | $R_{D^{(*)}} \& R_{K^{(*)}}$ |
| :---: | :---: | :---: | :---: |
| $S_{1}=(\overline{3}, 1,1 / 3)$ | $\checkmark$ | $x$ | $x$ |
| $R_{2}=(3,2,7 / 6)$ | $\checkmark$ | $\checkmark^{*}$ | $x$ |
| $S_{3}=(\overline{3}, 3,1 / 3)$ | $x$ | $\checkmark$ | $x$ |
| $U_{1}=(3,1,2 / 3)$ | $\checkmark$ | $\checkmark$ | $\checkmark$ |
| $U_{3}=(3,3,2 / 3)$ | $x$ | $\checkmark$ | $x$ |

- Two scalar LQs can also do the job (no extra parameters):
$\Rightarrow S_{1}$ and $S_{3}$ [Crivellin et al. '17, Marzocca. '18], $R_{2}$ and $S_{3} \quad$ D.B. et al '18


## $\mathrm{S}_{3} \& \mathrm{R}_{2}$ Model

D.B., Dorsner, Fajfer, Faroughy, Kosnik, Sumensari '18 [arXiv:1806.05689]

- In flavor basis

$$
\begin{array}{r}
\mathcal{L} \supset y_{R}^{i j} \bar{Q}_{i} \ell_{R j} R_{2}+y_{L}^{i j} \bar{u}_{R i} L_{j} \widetilde{R}_{2}^{\dagger}+y^{i j} \bar{Q}_{i}^{C} i \tau_{2}\left(\tau_{k} S_{3}^{k}\right) L_{j}+\text { h.c. } \\
R_{2}=(3,2,7 / 6), S_{3}=(\overline{3}, 3,1 / 3)
\end{array}
$$

- In mass-eigenstates basis

$$
\begin{aligned}
\mathcal{L} \supset & \left(V_{\mathrm{CKM}} y_{R} E_{R}^{\dagger}\right)^{i j} \bar{u}_{L i}^{\prime} \ell_{R j}^{\prime} R_{2}^{(5 / 3)}+\left(y_{R} E_{R}^{\dagger}\right)^{i j} \bar{d}_{L i}^{\prime} \ell_{R j}^{\prime} R_{2}^{(2 / 3)} \\
& +\left(U_{R} y_{L} U_{\mathrm{PMNS}}\right)^{i j} \bar{u}_{R i}^{\prime} \nu_{L j}^{\prime} R_{2}^{(2 / 3)}-\left(U_{R} y_{L}\right)^{i j} \bar{u}_{R i}^{\prime} \ell_{L j}^{\prime} R_{2}^{(5 / 3)} \\
& -\left(y U_{\mathrm{PMNS}}\right)^{i j} \bar{d}_{L i}^{\prime C} \nu_{L j}^{\prime} S_{3}^{(1 / 3)}-\sqrt{2} y^{i j} \bar{d}_{L i}^{\prime C} \ell_{L j}^{\prime} S_{3}^{(4 / 3)} \\
+ & \sqrt{2}\left(V_{\mathrm{CKM}}^{*} y U_{\mathrm{PMNS}}\right)_{i j} \bar{u}_{L i}^{\prime C} \nu_{L j}^{\prime} S_{3}^{(-2 / 3)}-\left(V_{\mathrm{CKM}}^{*} y\right)_{i j} \bar{u}_{L i}^{\prime C} \ell_{L j}^{\prime} S_{3}^{(1 / 3)}+\text { h.c. }
\end{aligned}
$$

and assume

$$
\underline{y_{R}=y_{R}^{T}} \quad y=-y_{L}
$$

$y_{R} E_{R}^{\dagger}=\left(\begin{array}{ccc}0 & 0 & 0 \\ 0 & 0 & 0 \\ 0 & 0 & y_{R}^{b \tau}\end{array}\right), U_{R} y_{L}=\left(\begin{array}{ccc}0 & 0 & 0 \\ 0 & y_{L}^{c \mu} & y_{L}^{c \tau} \\ 0 & 0 & 0\end{array}\right), U_{R}=\left(\begin{array}{ccc}1 & 0 & 0 \\ 0 & \cos \theta & -\sin \theta \\ 0 & \sin \theta & \cos \theta\end{array}\right)$

Parameters: $m_{R_{2}}, m_{S_{3}}, y_{R}^{b \tau}, y_{L}^{c \mu}, y_{L}^{c \tau}$ and $\theta$

Effective Lagrangian at $\mu \approx m_{\mathrm{LQ}}$ :

- $b \rightarrow c \tau \bar{\nu}$ :

NB. $\Lambda_{\mathrm{NP}} / g_{\mathrm{NP}} \approx 1 \mathrm{TeV}$

$$
\propto \frac{y_{L}^{c \tau} y_{R}^{b \tau *}}{m_{R_{2}}^{2}}\left[\left(\bar{c}_{R} b_{L}\right)\left(\bar{\tau}_{R} \nu_{L}\right)+\frac{1}{4}\left(\bar{c}_{R} \sigma_{\mu \nu} b_{L}\right)\left(\bar{\tau}_{R} \sigma^{\mu \nu} \nu_{L}\right)\right]+\ldots
$$

- $b \rightarrow s \mu \mu$ :

NB. $\Lambda_{\mathrm{NP}} / g_{\mathrm{NP}} \approx 30 \mathrm{TeV}$

$$
\propto \sin 2 \theta \frac{\left|y_{L}^{c \mu}\right|^{2}}{m_{S_{3}}^{2}}\left(\bar{s}_{L} \gamma^{\mu} b_{L}\right)\left(\bar{\mu}_{L} \gamma_{\mu} \mu_{L}\right)
$$

- $\Delta m_{B_{s}}$ :

$$
\propto \sin ^{2} 2 \theta \frac{\left[\left(y_{L}^{c \mu}\right)^{2}+\left(y_{L}^{c \tau}\right)^{2}\right]^{2}}{m_{S_{3}}^{2}}\left(\bar{s}_{L} \gamma^{\mu} b_{L}\right)^{2}
$$

$\Rightarrow$ Suppression mechanism of $b \rightarrow s \mu \mu$ wrt $b \rightarrow c \tau \bar{\nu}$ for $\operatorname{small} \sin 2 \theta$.
$\Rightarrow$ Phenomenology suggests $\theta \approx \pi / 2$ and $y_{R}^{b \tau}$ complex


Bounds should be less stringent when considering propagating LQ!


## Simple and viable $S U(5)$ GUT

- Choice of Yukawas was biased by $S U(5)$ GUT aspirations
- Scalars: $R_{2} \in \underline{\mathbf{4 5}}, \underline{\mathbf{5 0}}, S_{3} \in \underline{45}$. SM matter fields in $\mathbf{5}_{i}$ and $\mathbf{1 0}_{i}$
- Operators $\mathbf{1 0}_{i} \mathbf{1 0}_{j} \underline{\mathbf{4 5}}$ forbidden to prevent proton decay [Dorsner et al 2017]
- Available operators

$$
\begin{aligned}
\mathbf{1 0}_{i} \mathbf{5}_{j} \underline{\mathbf{4 5}:} & y_{2}^{R L} \bar{u}_{R}^{i} R_{2}^{a} \varepsilon^{a b} L_{L}^{j, b}, \quad y_{3 i j}^{L L}{\overline{Q^{C}}}_{L}^{i, a} \varepsilon^{a b}\left(\tau^{k} S_{3}^{k}\right)^{b c} L_{L}^{j, c} \\
\mathbf{1 0}_{i} \mathbf{1 0}_{j} \underline{\mathbf{5 0}:} & y_{2}^{L R}{ }_{i j} \bar{e}_{R}^{i} R_{2}^{a *} Q_{L}^{j, a}
\end{aligned}
$$

- While breaking $S U(5)$ down to SM the two $R_{2}$ 's mix - one can be light and the other (very) heavy. Thus our initial Lagrangian!
- The Yukawas determined from flavor physics observables at low energy remain perturbative ( $\lesssim \sqrt{4 \pi}$ ) up to the GUT scale, using one-loop running


## Summary and perspectives

- Flavor anomalies are still there but the experimental situation unclear. Needs clarification from Belle-II!
- Many questions could be answered if we had exp. info on $b \rightarrow s \tau \tau$ modes, eg. $B \rightarrow K^{(*)} \tau \tau$. Improving $\mathcal{B}\left(B \rightarrow K^{(*)} \tau \mu\right)$ - very helpful to model builders.

Belle-II and FCC

- (Even partial) angular distributions of $B_{(s)} \rightarrow D_{(s)}^{(*)} \tau \nu_{\tau}, B_{c} \rightarrow J / \psi \tau \nu_{\tau}$ and $\Lambda_{b} \rightarrow \Lambda_{c}^{(*)} \tau \nu_{\tau}$ could help discriminating among various NP scenarios.

LHCb and Belle II but FCC

- Viable single mediator explanations to $R_{K^{(*)}}$ and/or $R_{D^{(*)}}$ (and friends). Only the vector $U_{1}$ is viable. Two scalar LQs can do the job too.
- Many scenarios with upper and lower bounds for $\mathcal{B}(Z \rightarrow \tau \mu)$. Can someone measure $\mathcal{B}(Z \rightarrow \tau \tau)$ and $\mathcal{B}\left(W \rightarrow \tau \nu_{\tau}\right)$ ?

