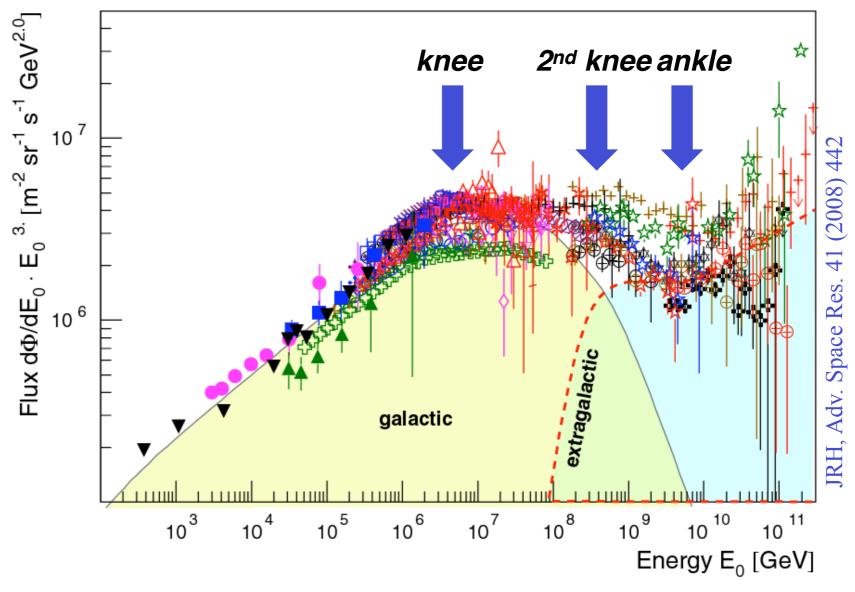
Paris
7-11 December 2020



Models for the knee in the energy spectrum of cosmic rays



Jörg R. Hörandel

RU Nijmegen, Nikhef, VU Brussel

http://particle.astro.ru.nl

A Matthews Heitler Model – mass resolution in EAS measurements

depth of shower maximum

$$X_{max}^{A} = X_{max}^{p} - X_{0}lnA$$
 radiation length X₀=36.7 g/cm²

typical uncertainty

$$\Delta X_{max} \approx 20 \text{ g/cm}^2$$

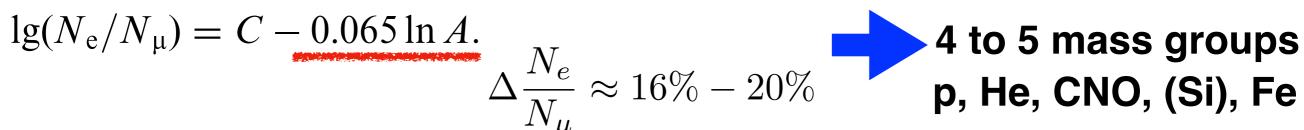
expected mass resolution



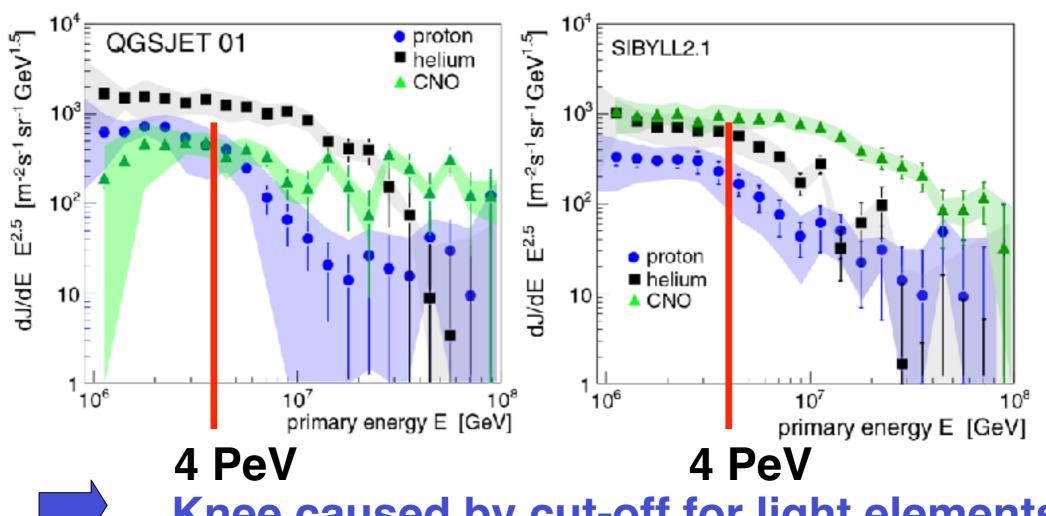
electron-muon ratio

$$\lg(N_{\rm e}/N_{\rm \mu}) = C - 0.065 \ln A.$$

$$\Delta \frac{N_e}{N_\mu} \approx 16\% - 20\%$$



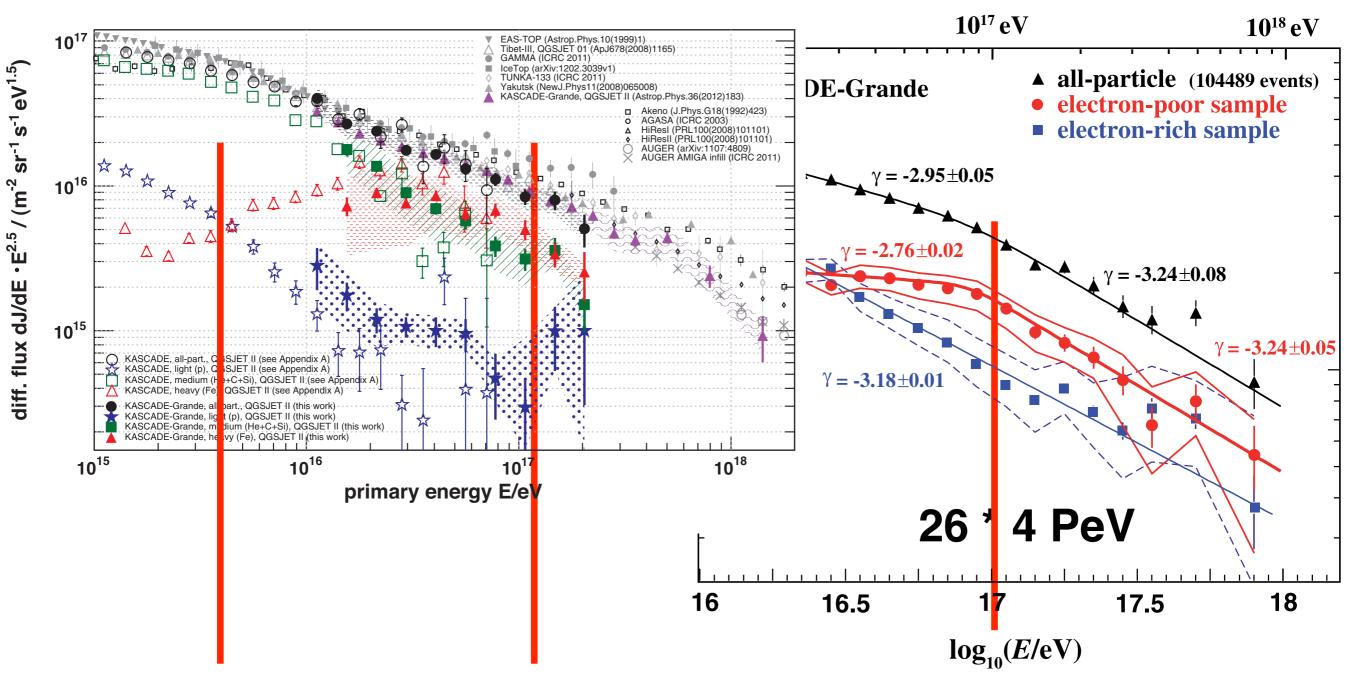
KASCADE: Energy spectra for elemental groups



Knee caused by cut-off for light elements

Astrophysical interpretation limited by description of interactions in the atmosphere

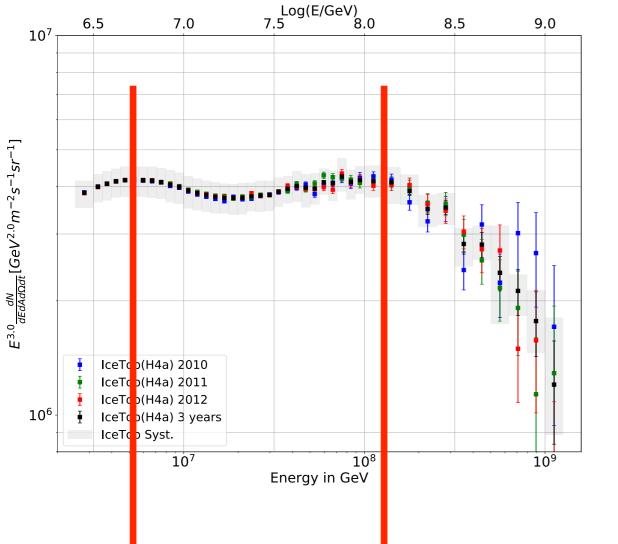
KASCADE-Grande



knee 4 PeV 26 * 4 PeV

W.D. Apel et al., PRL 107 (2011) 171104 W.D. Apel et al., Astropart. Phys 47 (2013) 54

Ice Cube - Ice Top



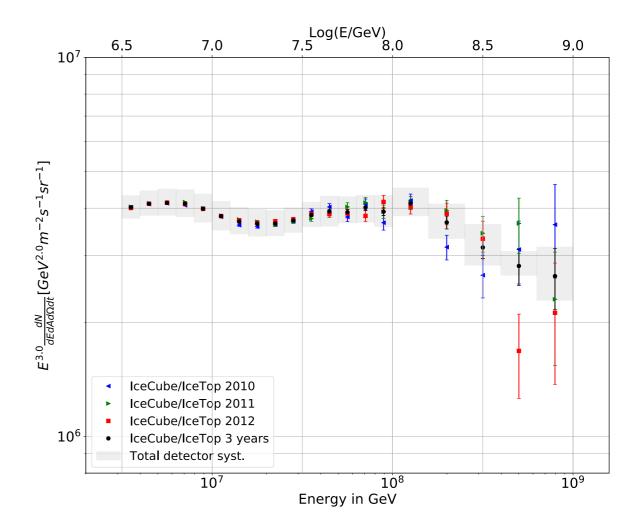


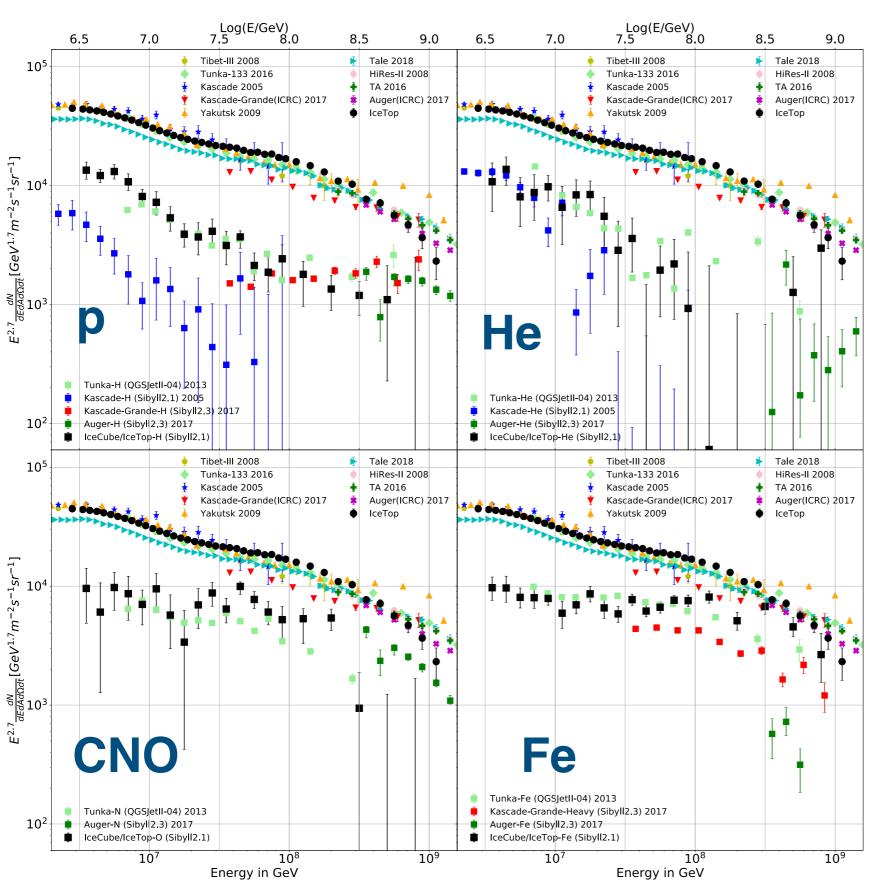
FIG. 9. All-particle energy spectrum from the IceTop-alone FIG. 12. All-particle energy spectrum from the coincident analysis from each of the three years, and the three years together.

~5 PeV ~26*5 PeV Ice Top only

analysis from each of the three years analyzed individually compared to the combined result. The gray band represents the total detector uncertainty from both the IceTop and InIce arrays, as discussed in Section IVB.

combined

Ice Cube - Ice Top



TALE (TA low-energy extension) ICRC 2017

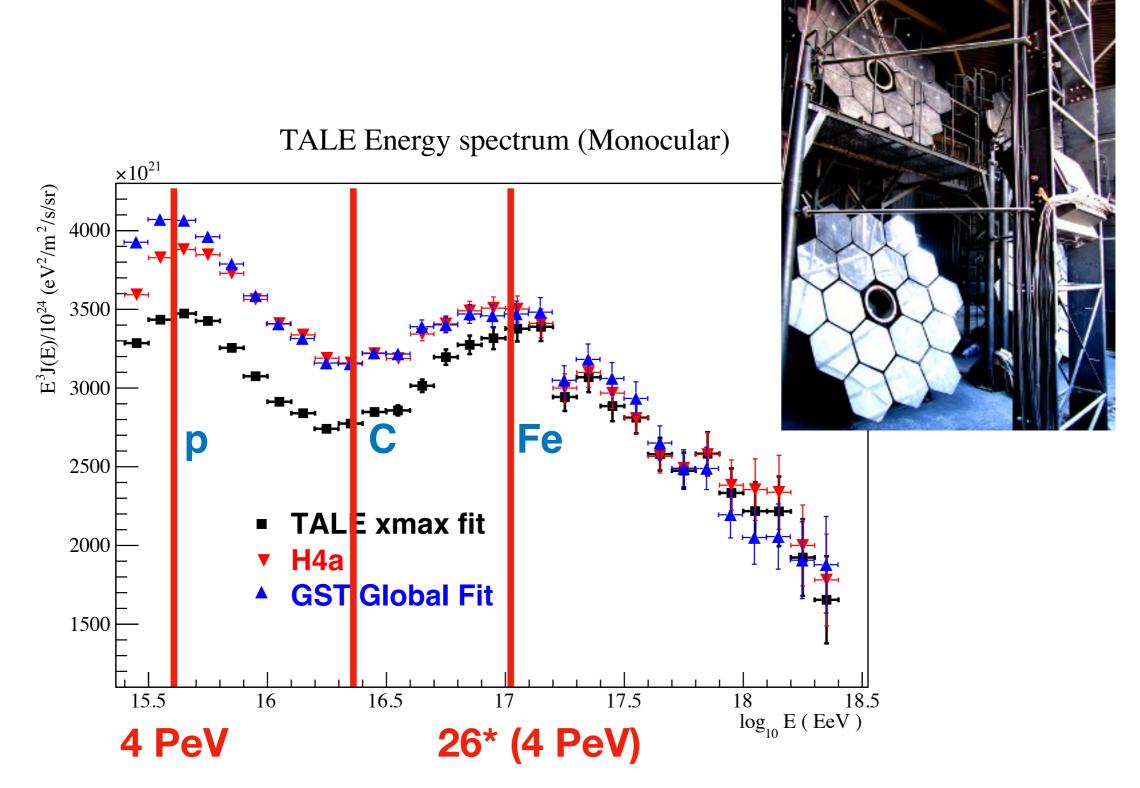
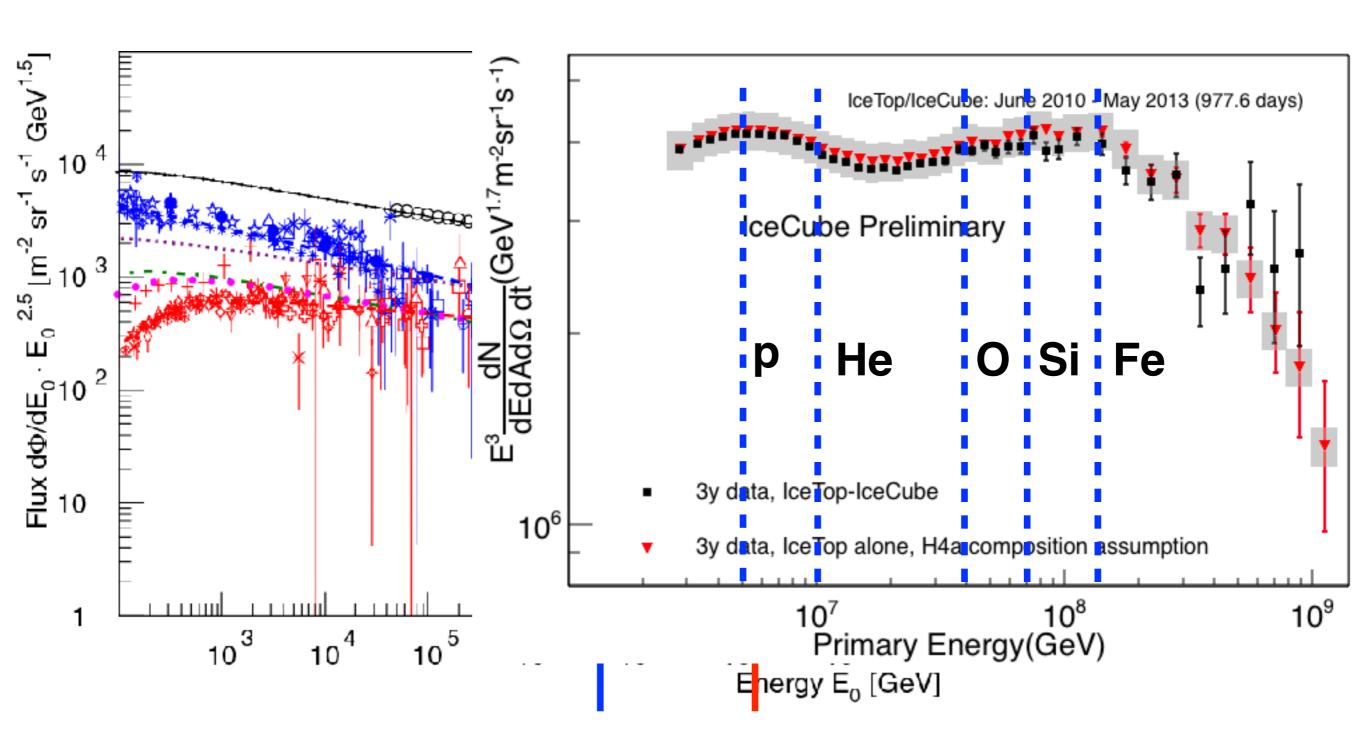
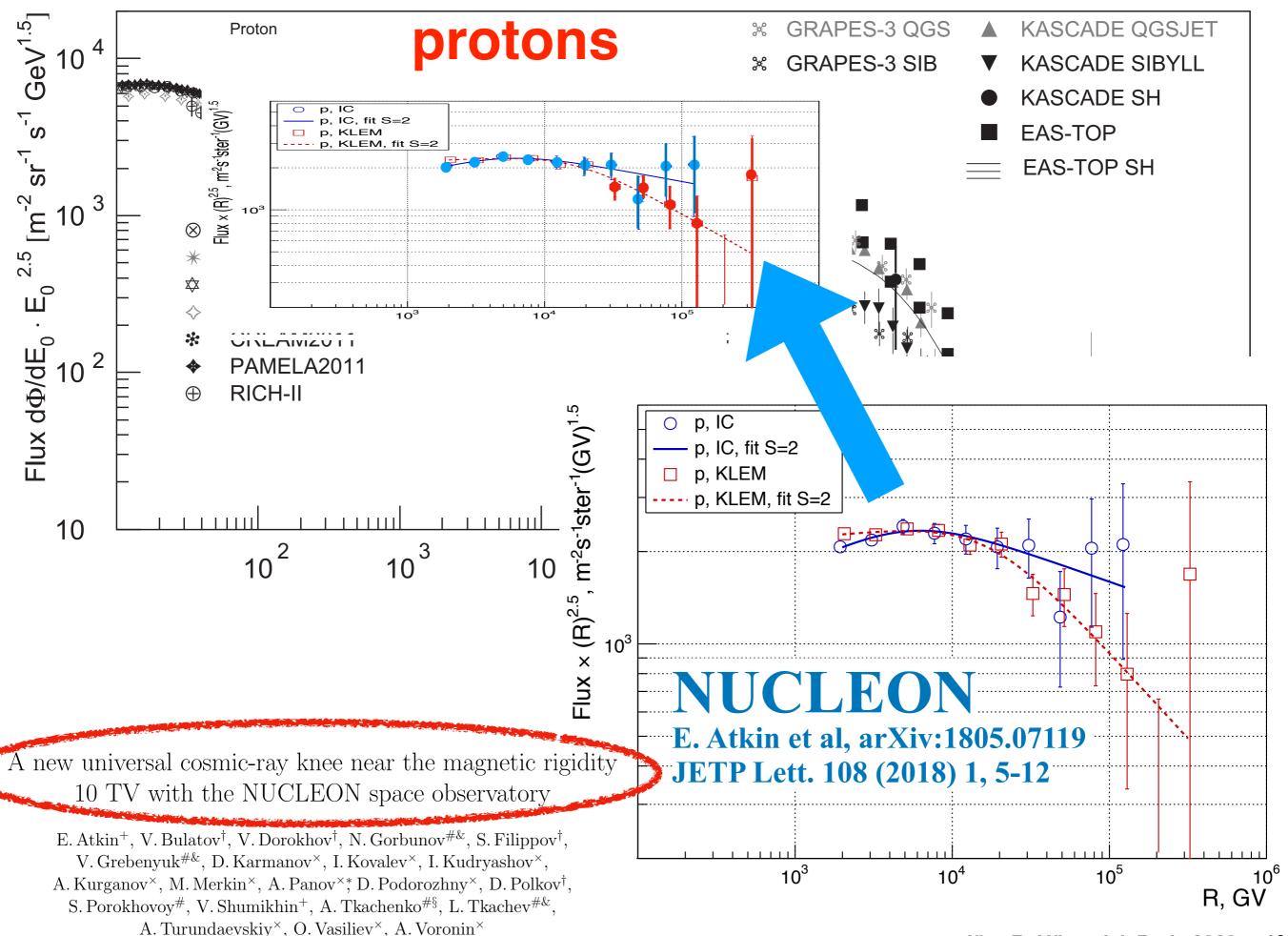


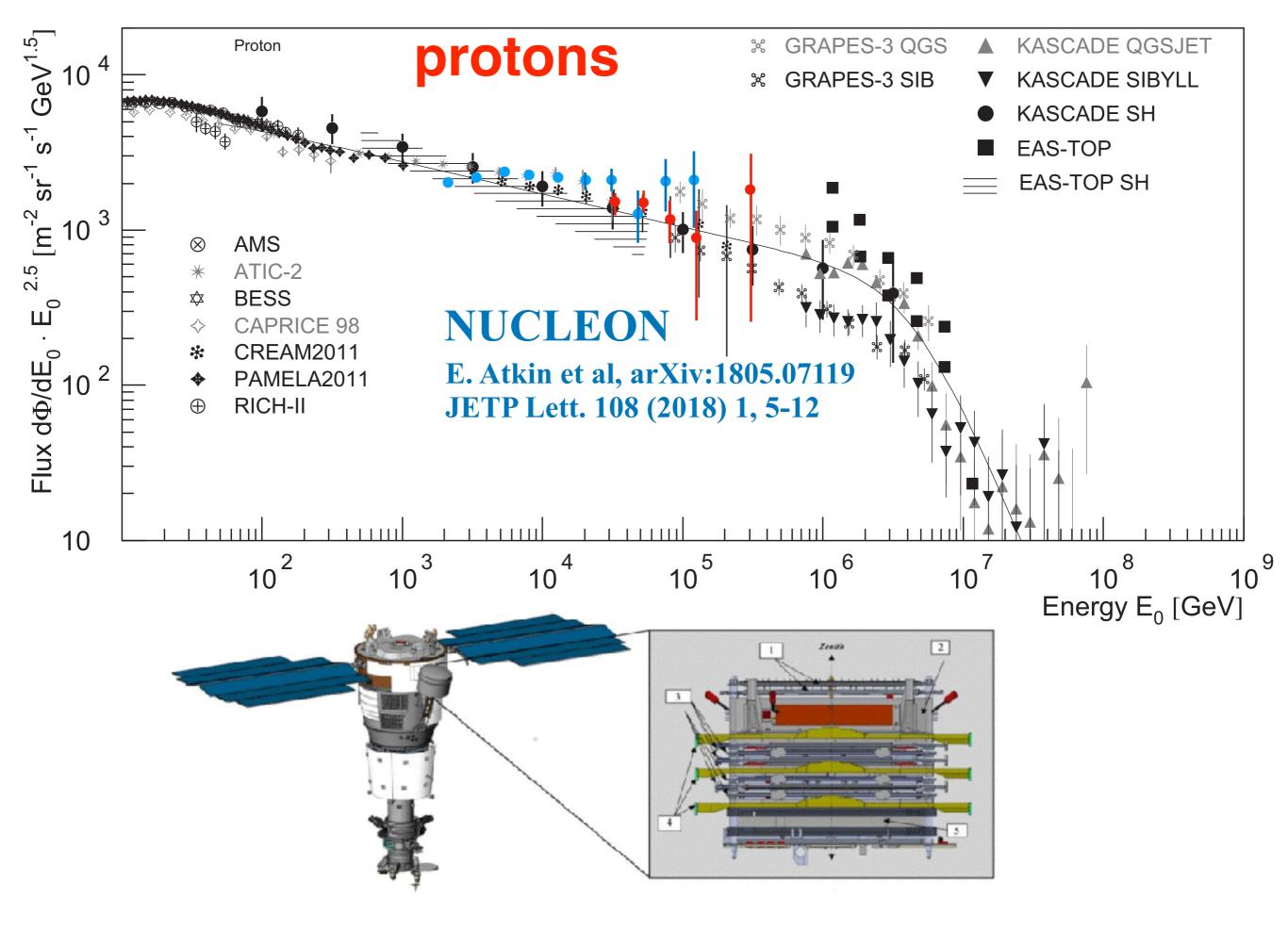
Figure 3: TALE Cosmic rays energy spectrum measured with TALE. The result is based on a QGSJet II-3 hadronic model assumption. A mixed primary composition given by the H4a, and "global fit" models, as well as a TALE derived mix was used in the calculations.

Cosmic-ray energy spectrum









Observation of a knee in the Cosmic Ray p+He energy spectrum below 1 PeV by ARGO-YBJ

A. D'Amone, I. De Mitri, A. Surdo*

Dipartimento di Matematica e Fisica "E. De Giorgi" - Università del Salento and Istituto Nazionale di Fisica Nucleare (INFN) - Sezione di Lecce Via per Arnesano, I-73100, Lecce, Italy E-mail: surdo@le.infn.it

for the ARGO-YBJ Collaboration

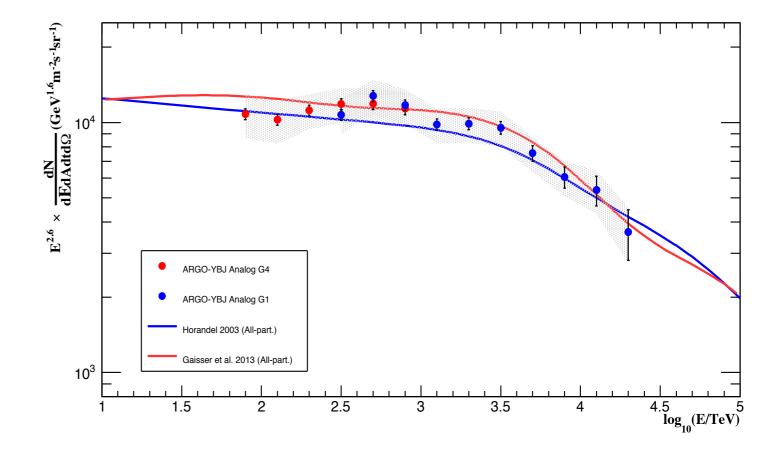


Figure 4: The all-particle energy spectrum of primary CRs resulting from this work. The parametrizations provided by [4] and [23] are shown for comparison.

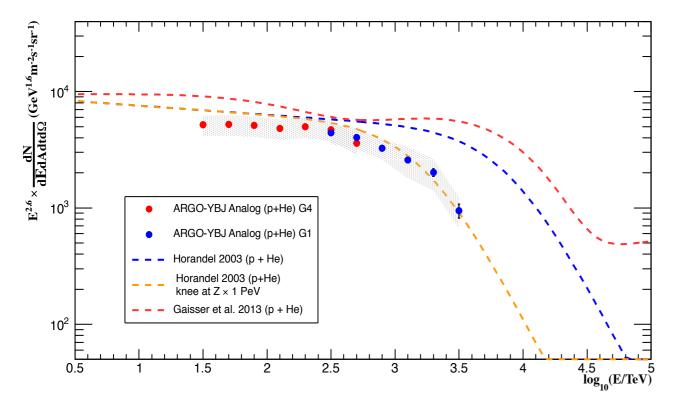


Figure 6: Light (i.e. p+He) component energy spectrum of primary CRs as measured in the analysis of ARGO-YBJ analog data (see text).

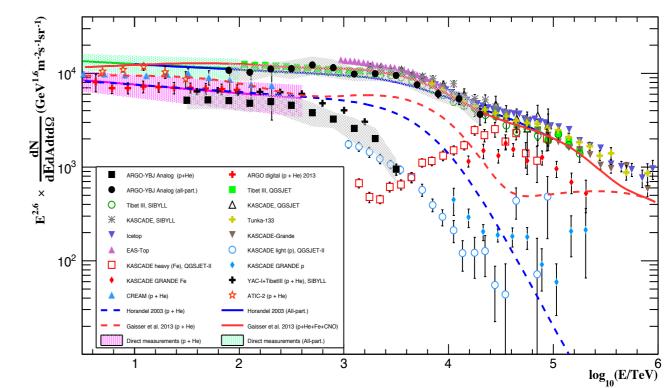


Figure 7: All-particle and light-component energy spectra of primary CRs as measured in this work, compared to several other experimental results.

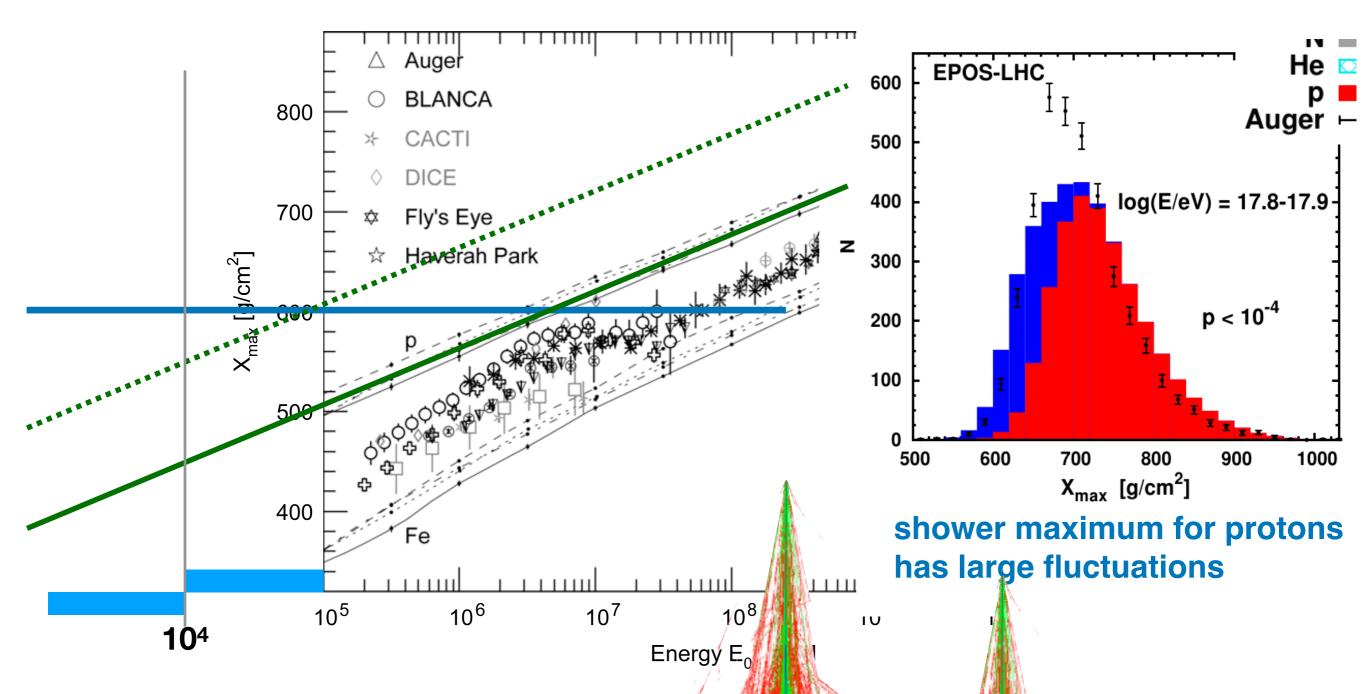
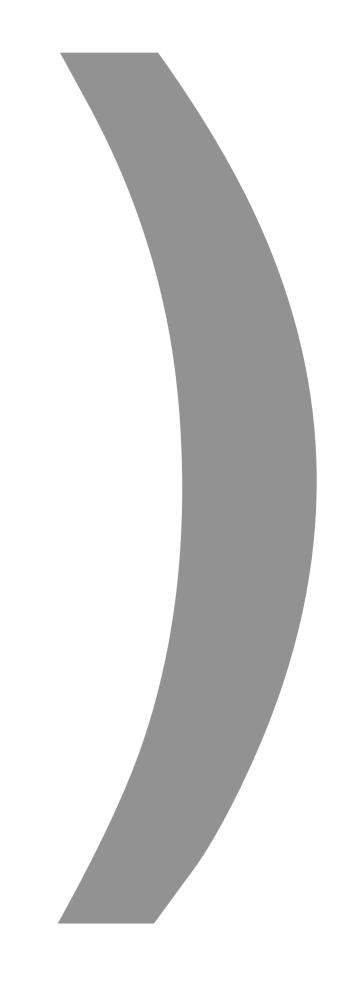


Fig. 13. Average depth of the shower maximum X_{max} as function of primary energy Ely's Eye [307], Haverah Park [308], HEGRA [174], HiRes/MIA [228], HiRes [309], We The lines indicate simulations for proton and iron induced showers using the COKS (---), SIBYLL 2.1 (...), and EPOS 1.6 (----).

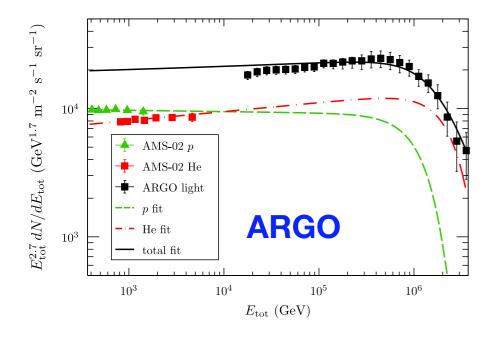
ined by Auger [30] ANCA [173], CACTI [306], DICE [182], [310], SPASE/VI [311], Tunka-25 [176], Yakutsk [312]. ion model QGSJET 01 (—), QGSJET II-3

ARGO at 4300 m.a.s.l $= 606 \text{ g/cm}^2$

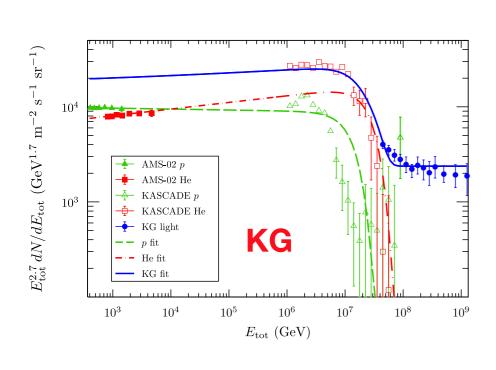
some remarks

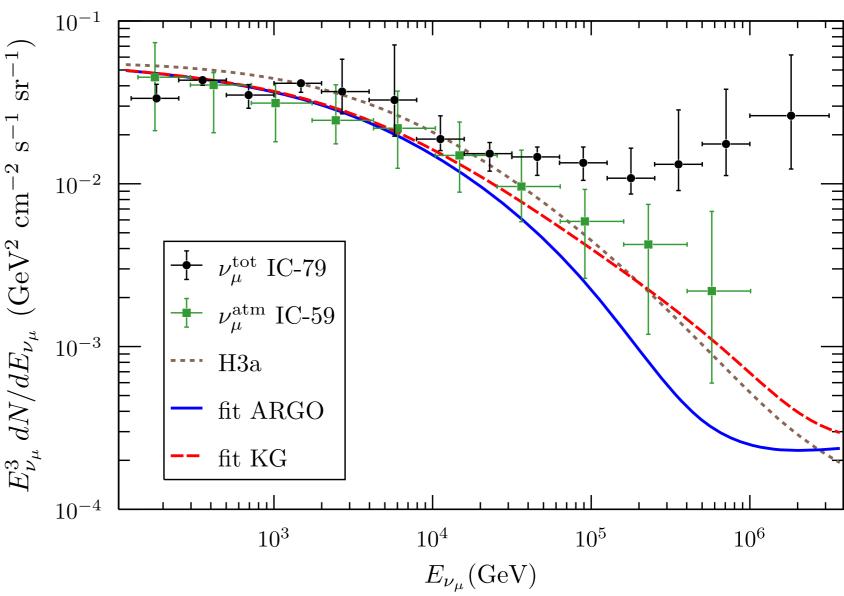


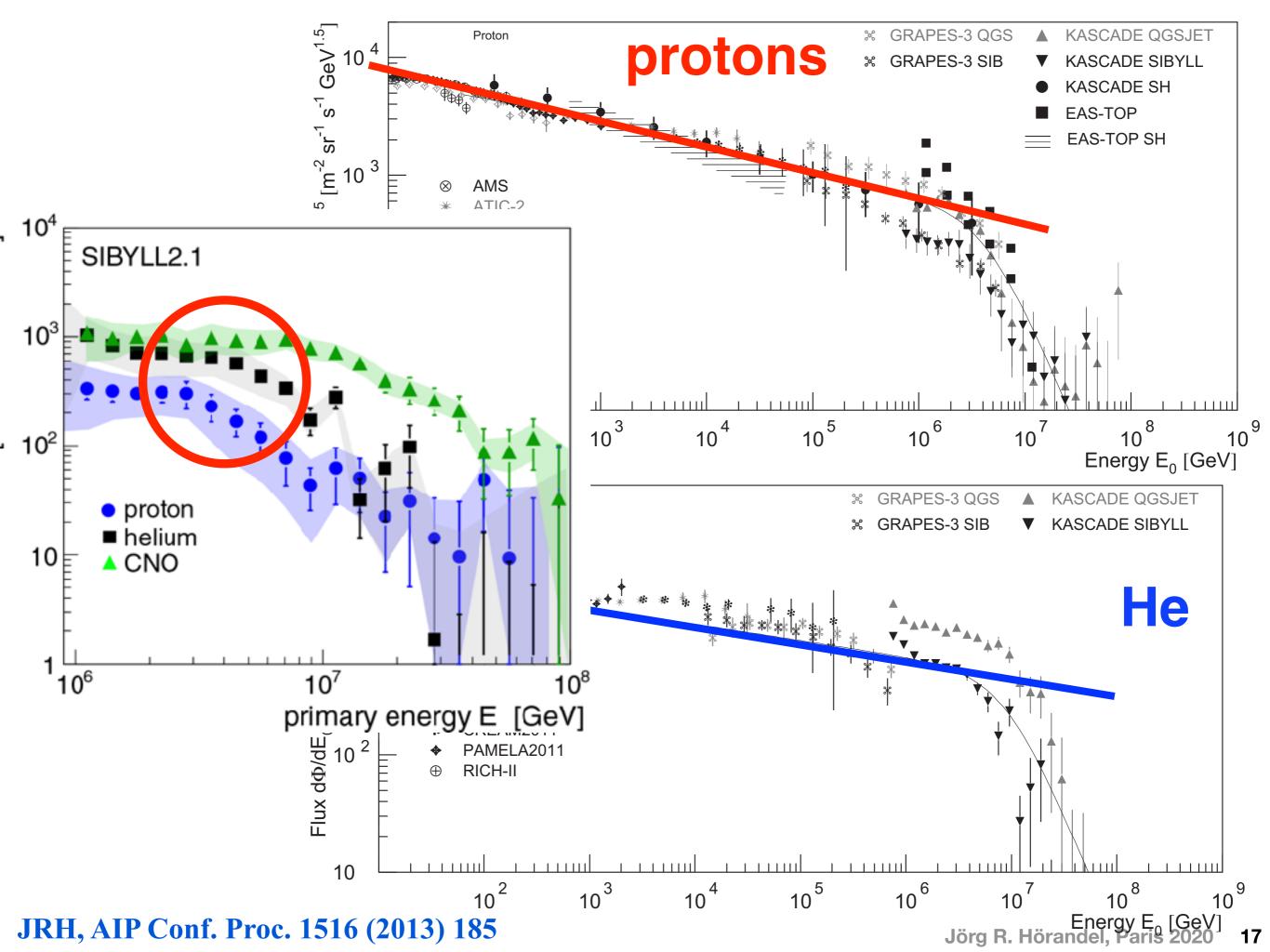
Atmospheric neutrinos and the knee of the cosmic ray spectrum



take ARGO + KASCADE-Grande measurements to predict neutrino flux







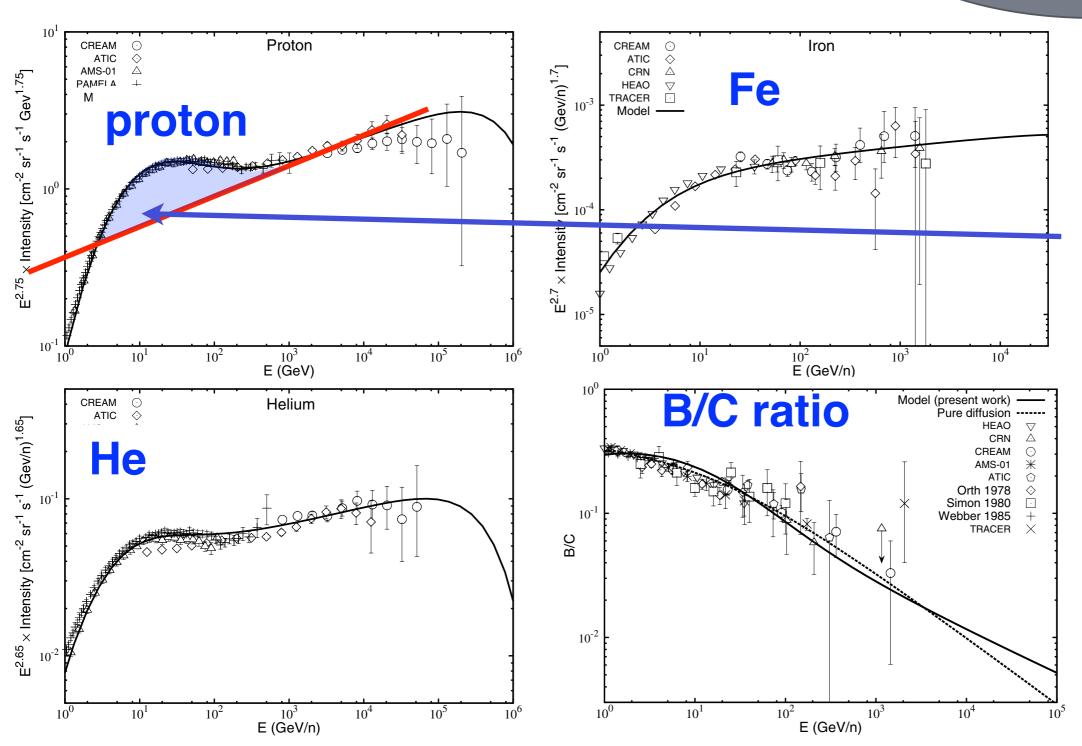
Astronomy Astrophysics

Source Matter Galaxy B=5uG π,B,Li,...

CR

GeV-TeV cosmic-ray spectral anomaly as due to reacceleration by weak shocks in the Galaxy*

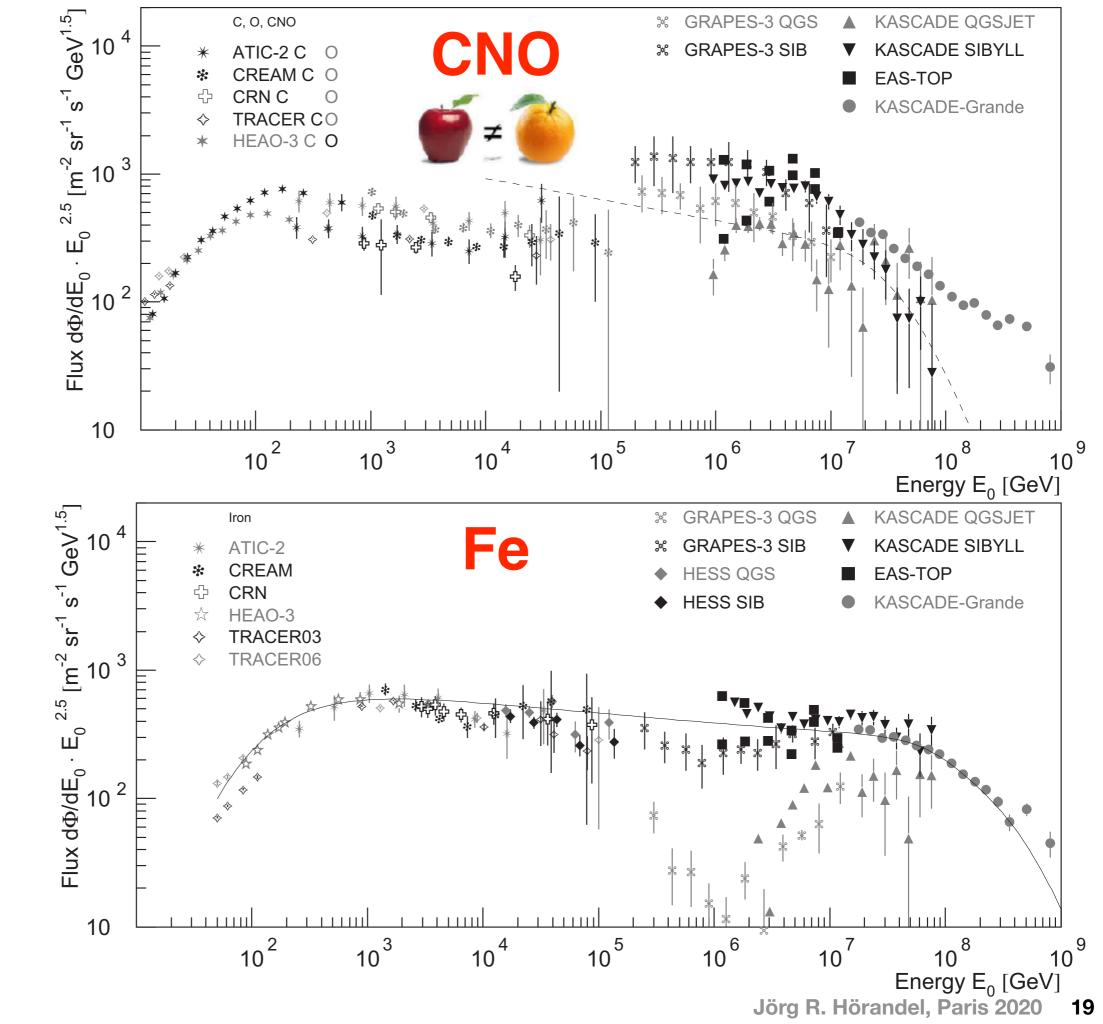
Satyendra Thoudam and Jörg R. Hörandel



bump due to reaccelertion by weak shocks in the Galaxy

Disk





Origin of the knee? JRH, Astropart. Phys. 21 (2004) 241 (updated)

.. in SNR

.. in SNR + radio galaxies

.. in oblique shocks

.. in variety of SNR

Single source model

Reacceleration in galactic wind

Leakage from Galaxy

Minimum pathlength model

Anomalous diffusion model

Hall diffusion model

Diffusion in turbulent magnetic fields

Diffusion and drift

γ-ray bursts

Cannonball model Acceleration in GRB + diffusion Acceleration in GRB E_{max} ~A

Interaction with background particles

Diffusion model + photo-disintegration references and uv photons)

Photo-disintegration (optical and uv photons)

Particle risysics in atmosphere

Gravitons, SUSY

Berezhko & Ksenofontov

Stanev ...

Kobayakawa ..

Sveshnikova

Erlykin & Wolfendale

Völk & Zirakashvili



Lagutin ..

Ptuskin .., Kalmykov .

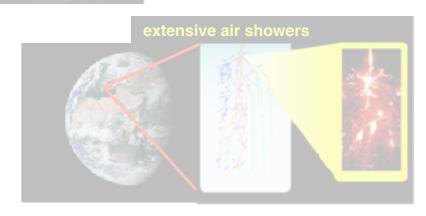
Ogio & Kakimoto

Roulet ...



Plaga Wick ..

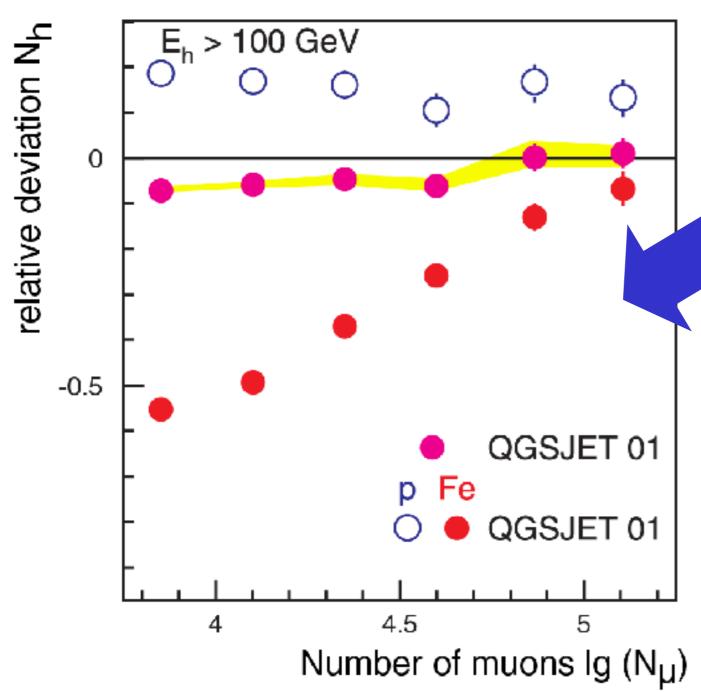
Dova .. Candia ..



Test of hadronic interaction models

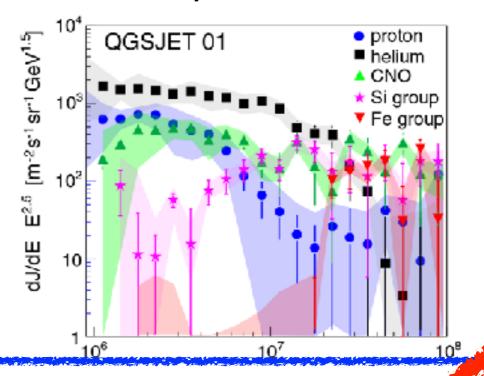
QGSJET 01

Number of hadrons vs. number of muons



inconsistencies on 10% level

N_e - N_μ analysis



in literature:

ideas that knee is caused from new interactions in atmosphere -> energy is carried away by "invisible channes"





Electron, muon and hadron size spectra of EAS in the "knee" region R. Glasstetter^a and J.R. Hörandel^a for the KASCADE Collaboration*

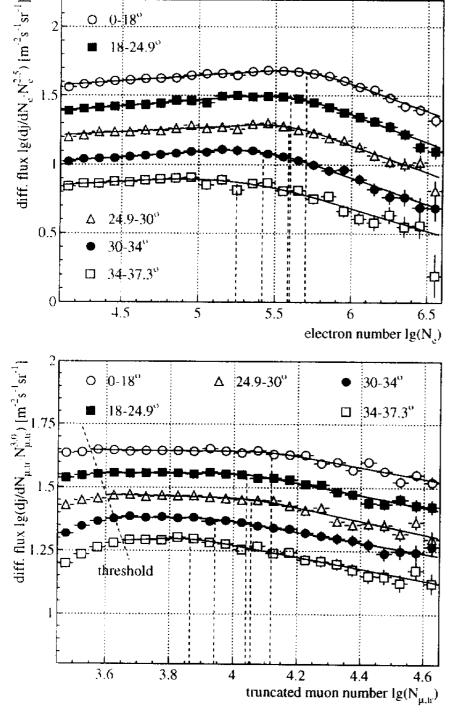


Figure 1. Electromagnetic (top) and muonic (bottom) shower size spectra for different zenith angle bins.

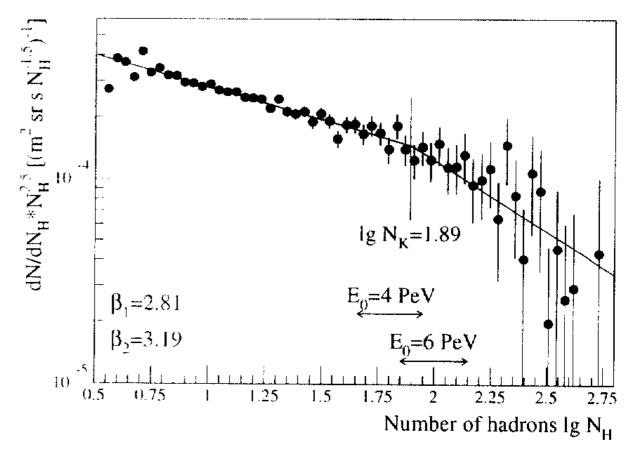


Figure 3. Hadronic shower size spectrum.

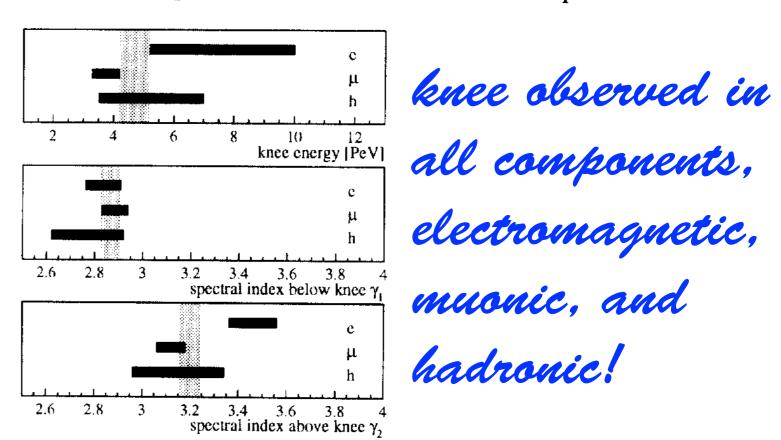
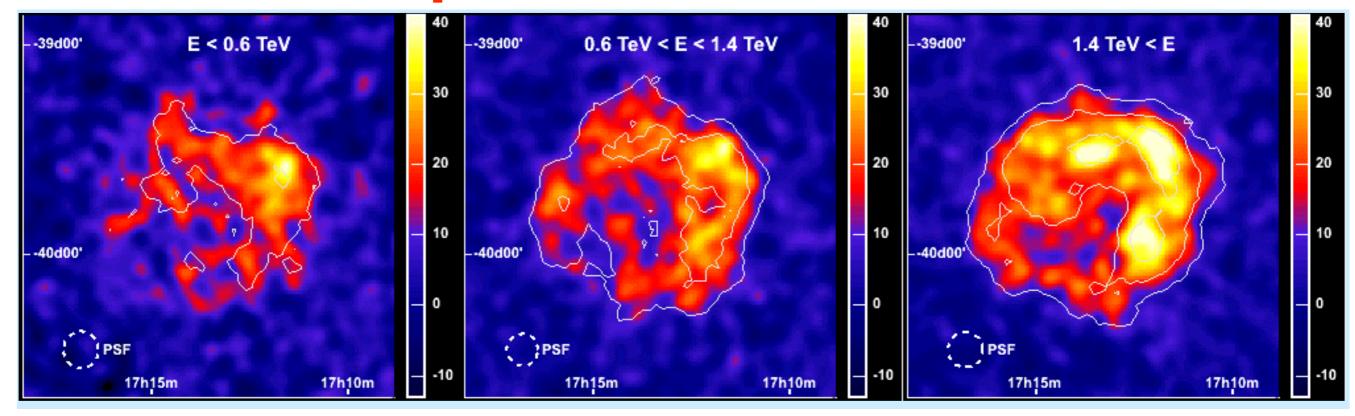
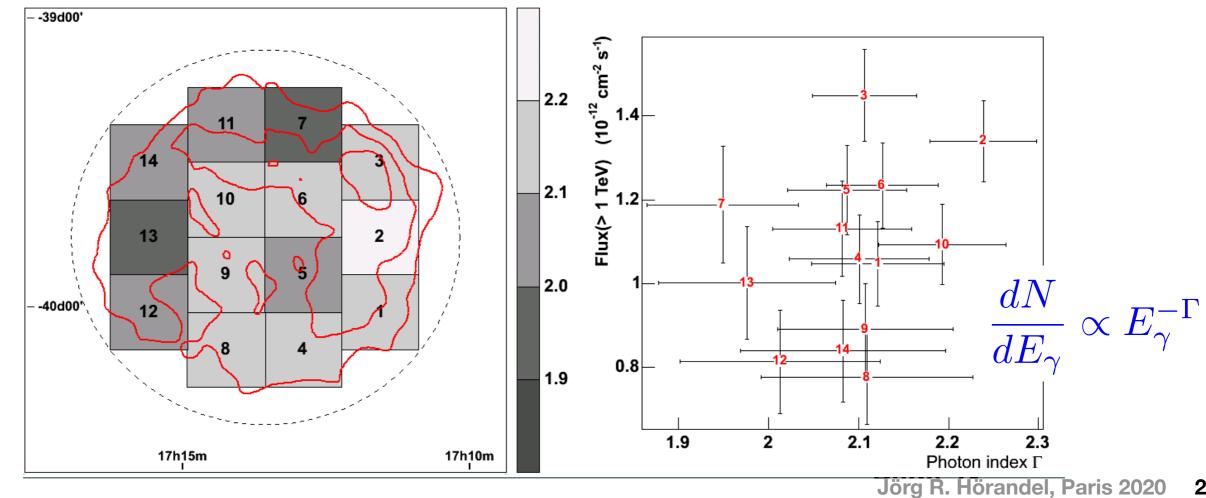


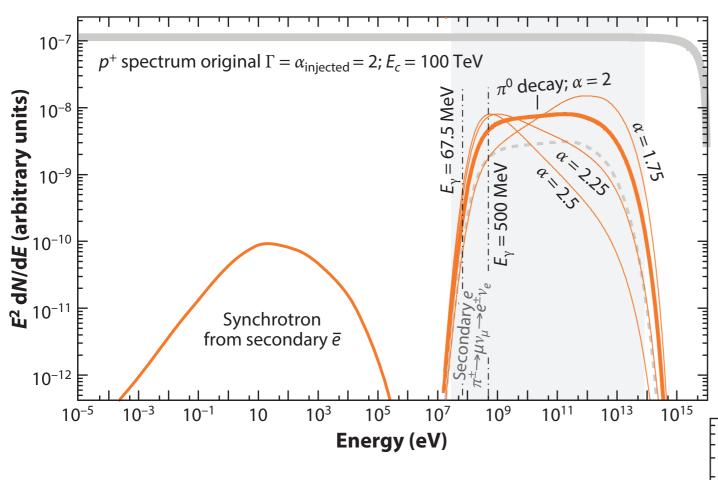
Figure 4. Knee position and spectral indices.

H.E.S.S. supernova remnant RXJ 1713





Acceleration of cosmic rays at SNR



Figure

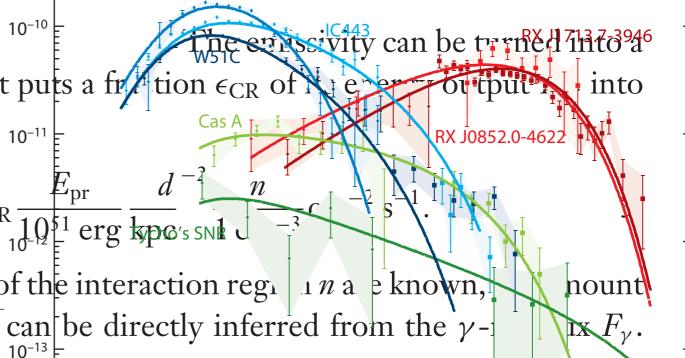
Spectral energy distribution of accelerated protons (power-law index $\alpha_{\rm injected} = 2.0$ and cutoff at 100 TeV) and γ -rays resulting from inelastic collisions with interstellar material. The dominant emission into photons occurs via the decay $\pi^0 \to \gamma \gamma$ (solid orange curves). The γ -ray spectrum follows the parent protons' spectrum rather closely in the midenergy range and in the high-energy cutoff region. For all proton indices, the low-energy turnover is a characteristic feature of the pion-decay emission. Also shown is the spectrum of electrons resulting from the inelastic proton–proton interactions via the decay chain $\pi^{\pm} \to \mu + \nu_{\mu} \to e^{\pm}\nu_{e}$ (dashed gray curve). For the synchrotron emission from these so-called secondary electrons, a source with age $t_{\rm age} = 1,000$ years and $B = 30~\mu{\rm G}$ have been assumed. The shaded gray region shows the sensitive range of current γ -ray detectors (Fermi-LAT, imaging atmospheric Cherenkov detectors).

flux at Earth by an astrophysical accelerator that puts a fraction ϵ_{CR} of the acceleration of protons:

of protons:
$$F_{\gamma}(>100\,\mathrm{MeV}) = 4.4 \times 10^{-7} \epsilon_{\mathrm{SQR}}^{\mathrm{SQR}} \frac{E_{\mathrm{pr}}}{10^{-11}} \frac{d}{\mathrm{kpc}' \mathrm{s}\,\mathrm{SNR}}$$

In other words, if the distance d and the density of the interaction regular n and n are known,

Typical years spectra for several of the most prominant superneval remarks (SNRs) Young Sixes (<1,000 years) are shown in grean. These typically show smaller γ -ray fluxes but rather hard spectra in the GeV and TeV bands. The older (but still referred to as young) shell-type SNRs RX J1713.7-3946 and RX J0852.0-4622 (Vela Junior) of ages \sim 2,000 years are shown in shades of red. These show very hard spectra in the GeV band (Γ = 1.5) and a peak in the TeV band with an exponential cutoff beyond 10 TeV. The middle-aged SNRs (\sim 20,000 years) interacting with molecular clouds (W44, W51C, and IC443) are shown in blue. Also shown are hadronic fits to the data (*solid lines*).



10¹¹

Photon energy (eV)

10¹⁰

W44

10⁸

10⁹

10¹³

10¹²

10¹⁴

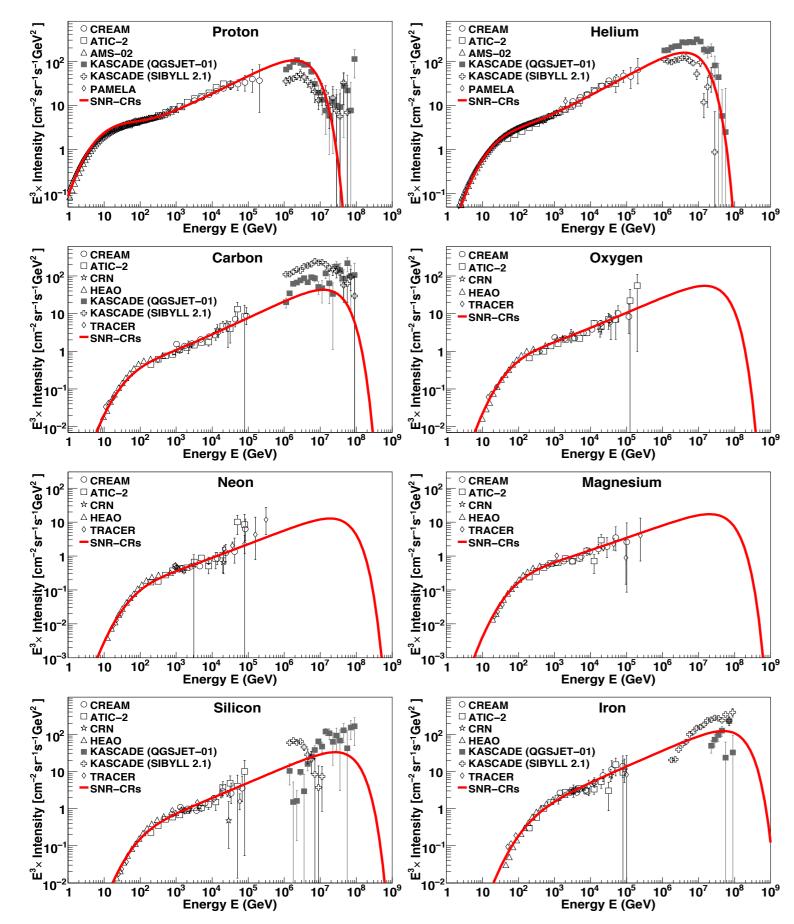


Fig. 1. Energy spectra for different cosmic-ray elements. Solid line: Model prediction for the SNR-CRs. Data: CREAM (Ahn et al. 2009; Yoon et al. 2011), ATIC-2 (Panov et al. 2007), AMS-02 (Aguilar et al. 2015a,b), PAMELA (Adriani et al. 2011), CRN (Müller et al. 1991; Swordy et al. 1990), HEAO (Engelmann et al. 1990), TRACER (Obermeier et al. 2011), and KASCADE (Antoni et al. 2005). Cosmic-ray source parameters (q, f) used in the calculation are given in Table 1. For the other model parameters (D_0, a, η, s) , see text for details.

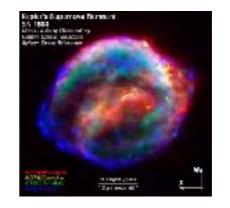
Contribution of (regular) SNR-CR

$$E_c = Z \cdot 4.5 \ 10^6 \ \mathrm{GeV}$$

$$Q(p) = AQ_0(Ap)^{-q} \exp\left(-\frac{Ap}{Zp_c}\right),$$

Table 1. Source spectral indices, q, and energy injected per supernova, f, for the different species of cosmic rays used in the calculation of the SNR-CRs spectra shown in Figures 1 and 2.

Particle type	q	$f (\times 10^{49} \text{ ergs})$
Proton	2.24	6.95
Helium	2.21	0.79
Carbon	2.21	2.42×10^{-2}
Oxygen	2.25	2.52×10^{-2}
Neon	2.25	3.78×10^{-3}
Magnesium	2.29	5.17×10^{-3}
Silicon	2.25	5.01×10^{-3}
Iron	2.25	4.95×10^{-3}



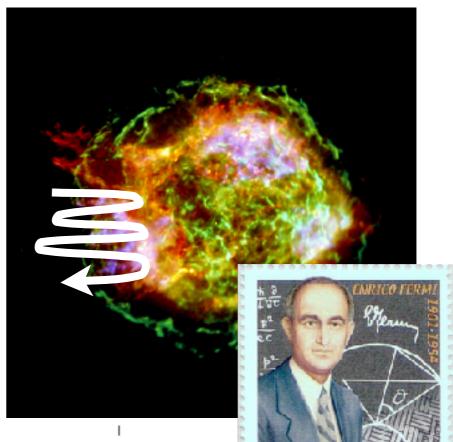
Mt. Fuji $^{2.5}\,[{ m m}^{-2}\,{ m sr}^{-1}\,{ m s}^{-1}\,{ m GeV}^{1.5}]$ Proton ♦ HEGRA . Mt. Chacaltava KASCADE SH RICH-II **JACEE** Smith $^{2.5}\,\mathrm{[m^{-2}\,sr^{-1}\,s^{-1}\,GeV^{1.5}]}$ Helium RUNJOB JACEE Smith SOKOL C, O, CNO CNO ATIC C ATIC O RUNJOB CRN C TRACER O Berezhko - · - · · Kobayakawa $^{2.5}\,[\mathrm{m^{\text{-}2}\,sr^{\text{-}1}\,s^{\text{-}1}\,GeV^{\text{1}.5}}]$ Iron GRAPES-3 SIB CRN RUNJOB Harevama □ JACEE Flux $d\Phi/dE_0 \cdot E_0$ 102 10⁷ Energy E₀ [GeV]

maximum energy

 $E_{max} \propto B \cdot Z$

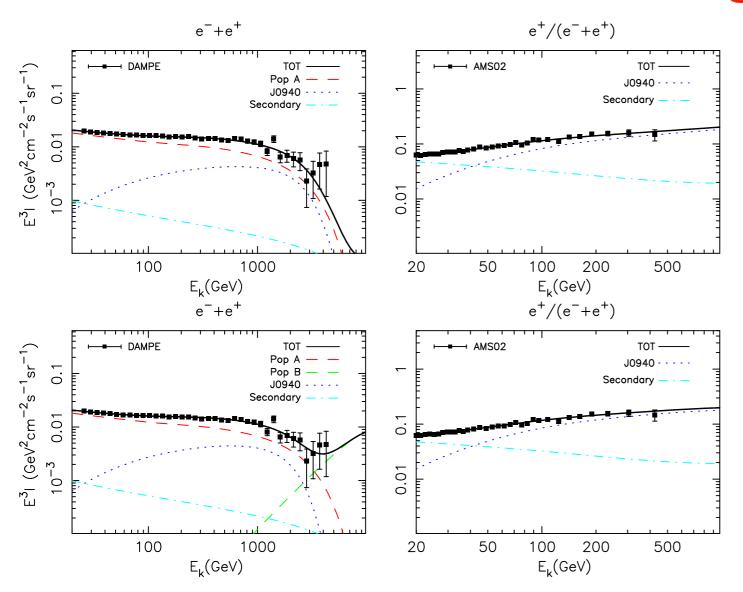


 $E_{max} \approx Z \cdot 100 \text{ TeV} \dots Z \cdot 5 \text{ PeV}$



- Berezhko
- Kobayakawa
- Stanev
 - Sveshnikova
 - **Poly Gonato**

Explanation of the knee-like feature in the DAMPE cosmic e- + e+ energy spectrum



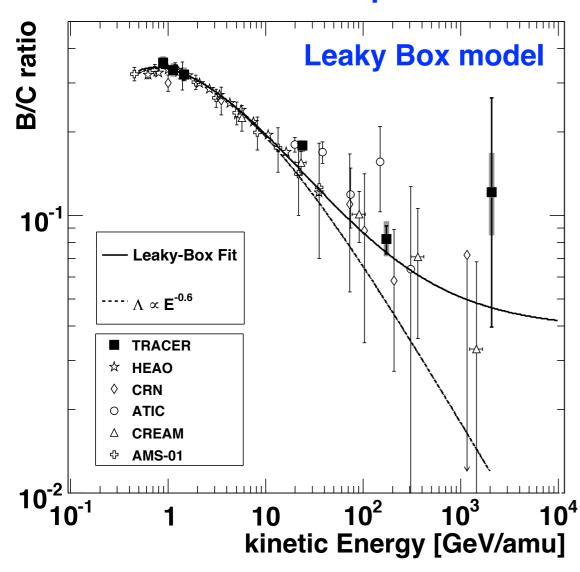
acceleration of electrons in SNR+ radiative cooling

(+maybe contribution from single SNR)

FIG. 1. Results of the fitting to the DAMPE $e^- + e^+$ and AMS-02 $e^+/(e^- + e^+)$ data, with PSR J0940-5428 as the single positron source in the high energy region. Left panels: the electron plus positron spectrum. Right panels: the positron fraction. The results in the bottom panels include the population B of SNRs, while the results in the top panels do not. In the legends, 'TOT' stands for the total $e^- + e^+$ flux (or $e^+/(e^- + e^+)$) of all the sources, the population A of SNRs are abbreviated to 'Pop A', the population B are abbreviated to 'Pop B', while 'J0940' stands for PSR J0940-5428.

Pathlength of cosmic rays in Galaxy

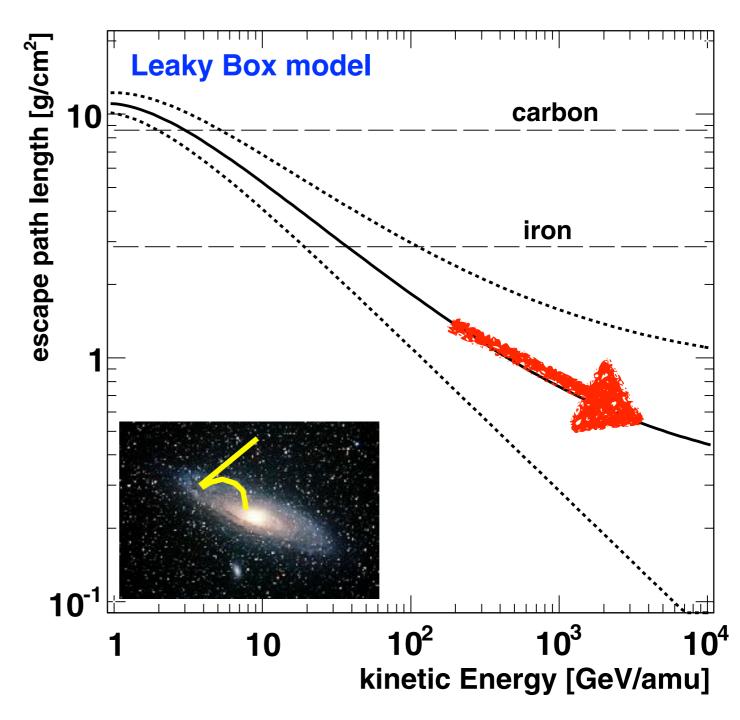
TRACER balloon experiment



Escape Path Length:

$$\Lambda_{esc}(E) = CE^{-\delta} + \Lambda_0$$

- ► Propagation index: $\delta = 0.64 \pm 0.02$.
- ► Residual path length: $\Lambda_0 = 0.7 \pm 0.2 \text{ g/cm}^2$.



$$\Lambda(R) = \frac{26.7\beta}{(\beta R)^{\delta} + (0.714 \cdot \beta R)^{-1.4}} + \Lambda_0 \text{ g/cm}^2,$$



Astroparticle Physics 27 (2007) 119-126



www.elsevier.com/locate/astropart

example of knee due to propagation/leakage from Galaxy

Propagation of super-high-energy cosmic rays in the Galaxy

Jörg R. Hörandel a,*, Nikolai N. Kalmykov b, Aleksei V. Timokhin c

The steady-state diffusion equation for the cosmic-ray density N(r) is (neglecting nuclear interactions and energy losses)

$$-\nabla_i D_{ij}(r) \nabla_j N(r) = Q(r). \tag{1}$$

Q(r) is the cosmic-ray source term and $D_{ij}(r)$ the diffusion tensor.

Under the assumption of azimuthal symmetry and taking into account the predominance of the toroidal component of the magnetic field, Eq. (1) is presented in cylindrical coordinates as

$$\left[-\frac{1}{r} \frac{\partial}{\partial r} r D_{\perp} \frac{\partial}{\partial r} - \frac{\partial}{\partial z} D_{\perp} \frac{\partial}{\partial z} - \frac{\partial}{\partial z} D_{A} \frac{\partial}{\partial r} + \frac{1}{r} \frac{\partial}{\partial r} r D_{A} \frac{\partial}{\partial z} \right] N(r, z) = Q(r, z), \tag{2}$$

where N(r,z) is the cosmic-ray density averaged over the large-scale fluctuations with a characteristic scale $L \sim 100$ pc [3]. $D_{\perp} \propto E^m$ is the diffusion coefficient, where m is much less than one ($m \approx 0.2$), and $D_A \propto E$ the Hall diffusion coefficient. The influence of Hall diffusion becomes predominant at high energies (>10¹⁵ eV). The sharp

The magnetic field of the Galaxy consists of a large-scale regular and a chaotic, irregular component $\vec{B} = \vec{B}_{\text{reg}} + \vec{B}_{\text{irr}}$. A purely azimuthal magnetic field was assumed for the regular field

$$B_z = 0$$
, $B_r = 0$, $B_{\phi} = 1 \,\mu\text{G} \exp\left(-\frac{z^2}{z_0^2} - \frac{r^2}{r_0^2}\right)$,

where $z_0 = 5$ kpc and $r_0 = 10$ kpc are constants [3].

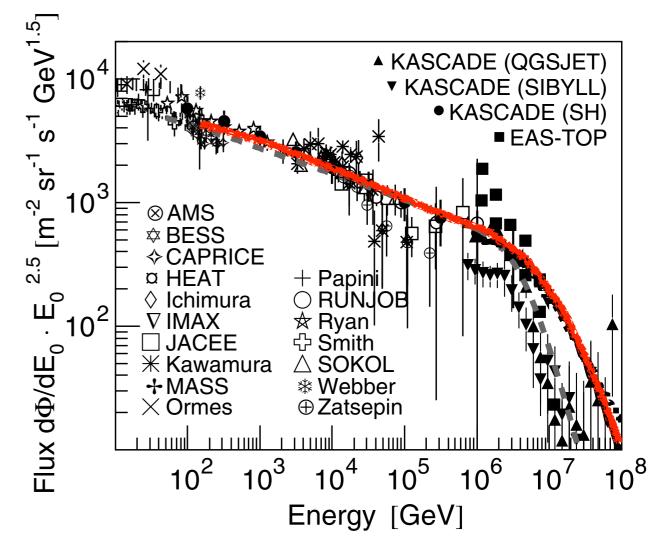


Fig. 7. Proton flux as obtained from various measurements, for references see [28], compared to the spectra shown in Fig. 6 (black lines) and the *polygonato* model [26] (grey, dashed line).

Cosmic-Ray Transport between the Knee and the Ankle with CRPropa

Lukas Merten*a, Julia Tjusa, Chad Bustardb, and Ellen G. Zweibelbc

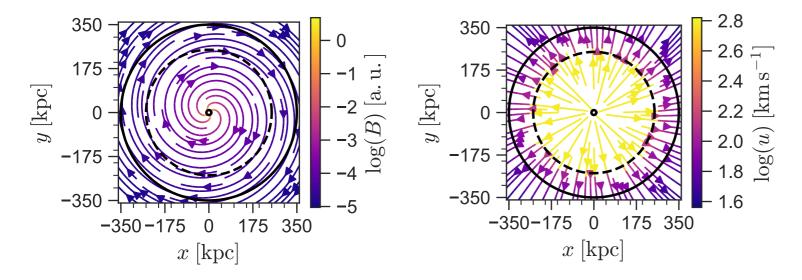


Figure 1: Face on view of the magnetic field and the Galactic wind in the Galactic plane. The inner solid circle is the observer sphere and the outer solid circle is the free escape boundary. The shock position is marked by the dashed circle.

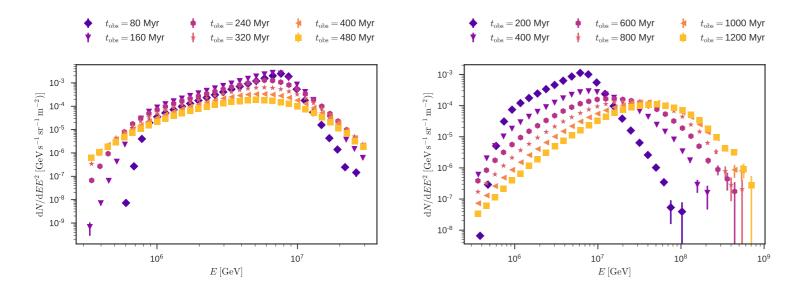
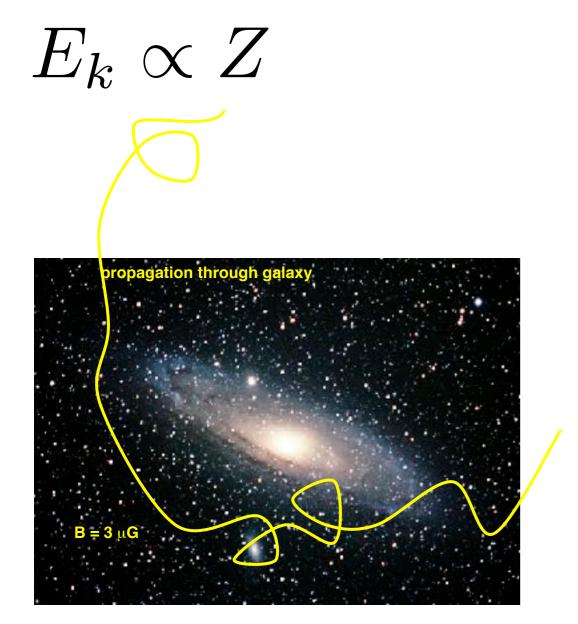


Figure 2: Energy spectrum at the spherical observer sphere $r_{\rm obs} = 10$ kpc. Left including perpendicular diffusion $\epsilon = 0.1$ and right pure parallel diffusion.

In this work an innovative technique—based on stochastic differential equations—to solve the transport equation is explained.

The ansatz of propagating independent phase-space elements (or pseudo-particles) allows for easy parallelization which makes it attractive for modern large-scale computing architectures. It combines the numerical framework of the single particle propagation with the advantage of ensemble averaged description of the transport equation. Making it an ideal tool to describe the transition between Galactic and extra-galactic cosmic-rays.

leakage from Galaxy



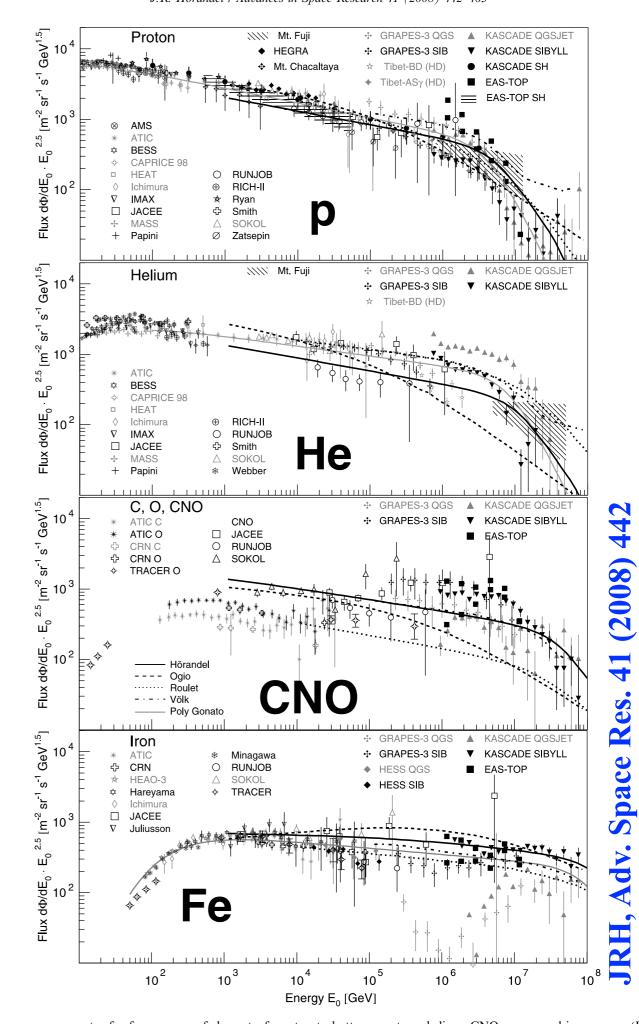
---- Hörandel

--- Ogio

······ Roulet

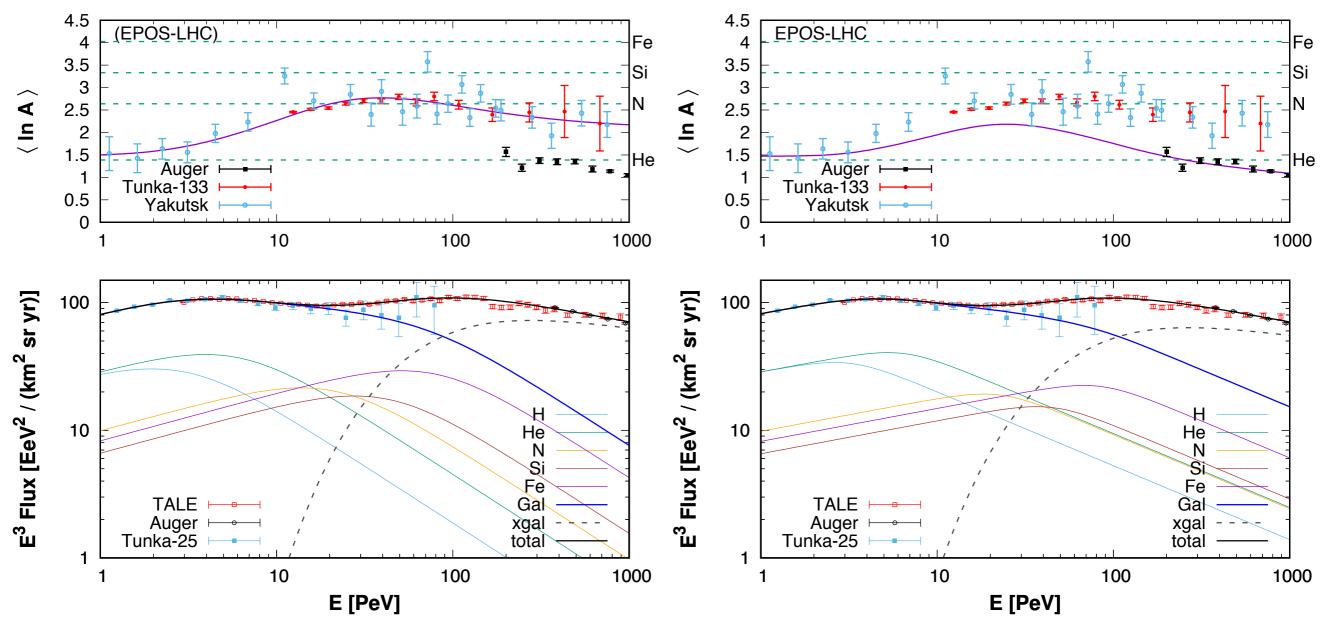
- · - · · Völk

——— Poly Gonato



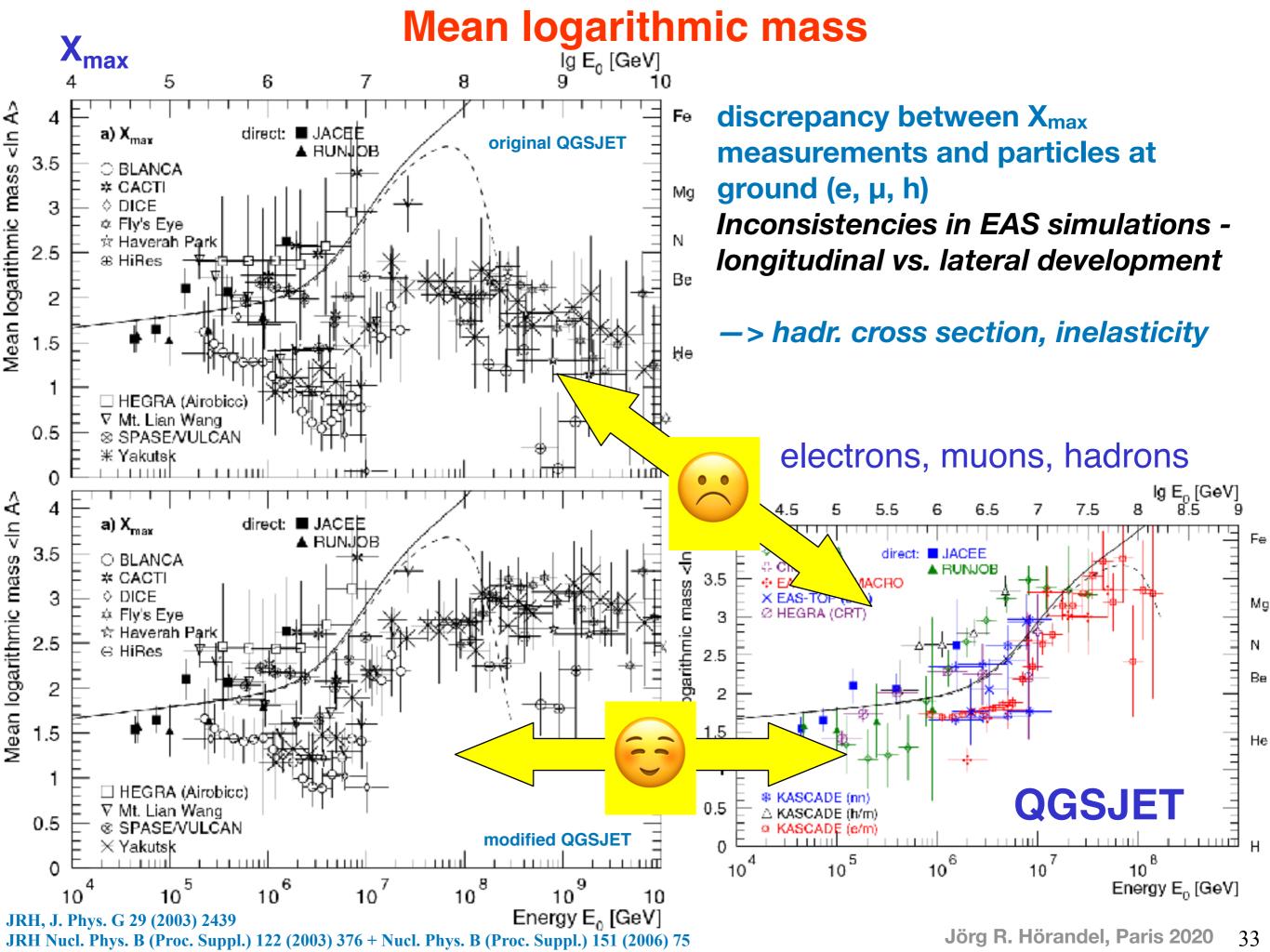
A scenario for the Galactic cosmic rays between the knee and the second-knee

fit using X_{max} data from TALE, Tunka, Yakutsk, Auger



knee at E_k ~3 PeV * Z -> Fe knee at 80 PeV

extragalactic component dominant >100 PeV



Contribution of (regular) SNR-CR to all-particle spectrum

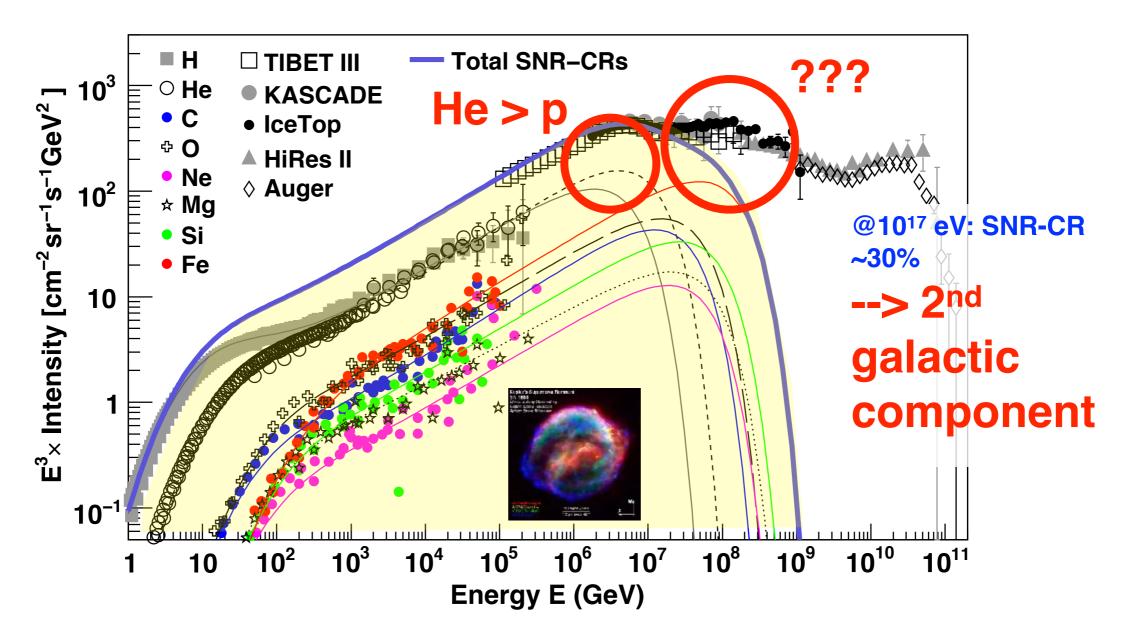
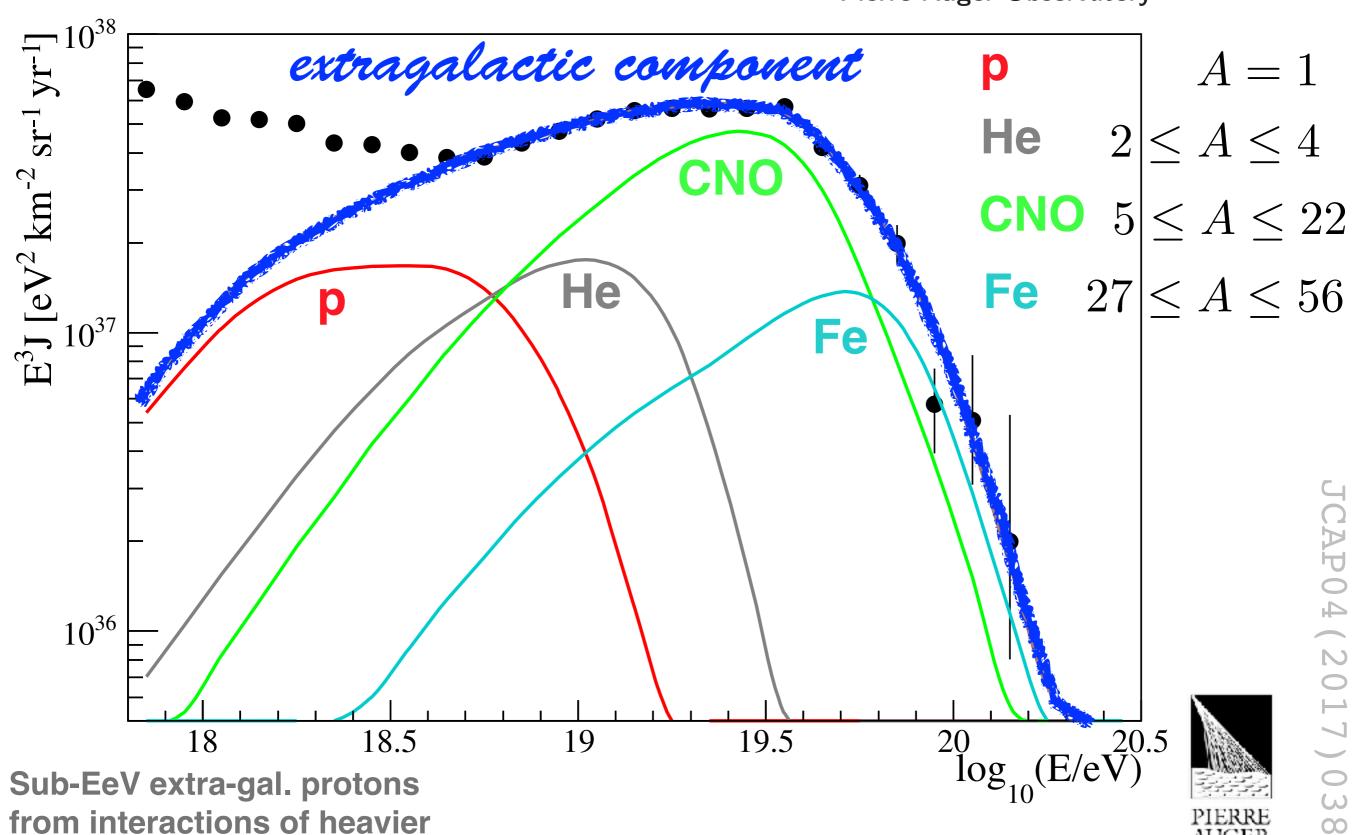


Fig. 2. Contribution of SNR-CRs to the all-particle cosmic-ray spectrum. The thin lines represent spectra for the individual elements, and the thick-solid line represents the total contribution. The calculation assumes an exponential cut-off energy for protons at $E_c = 4.5 \times 10^6$ GeV. Other model parameters, and the low-energy data are the same as in Figure 1. Error bars are shown only for the proton and helium data. High-energy data: KASCADE (Antoni et al. 2005), IceTop (Aartsen et al. 2013), Tibet III (Amenomori et al. 2008), the Pierre Auger Observatory (Schulz et al. 2013), and HiRes II (Abbasi et al. 2009).

~8% of mechanical power of SN --> CRs

Combined fit of spectrum and composition data as measured by the **Pierre Auger Observatory**



nuclei

S. Thoudam et al., A&A 595 (2016) A33

C/He=0.1

all-particle spectra including 2nd galactic component

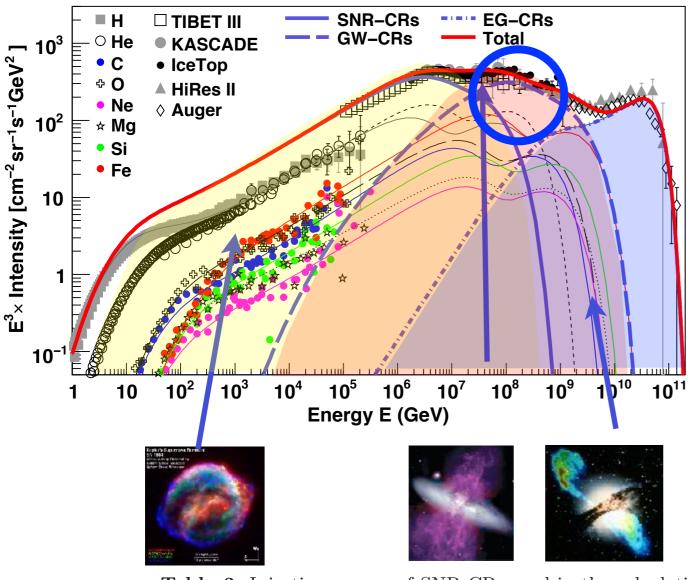
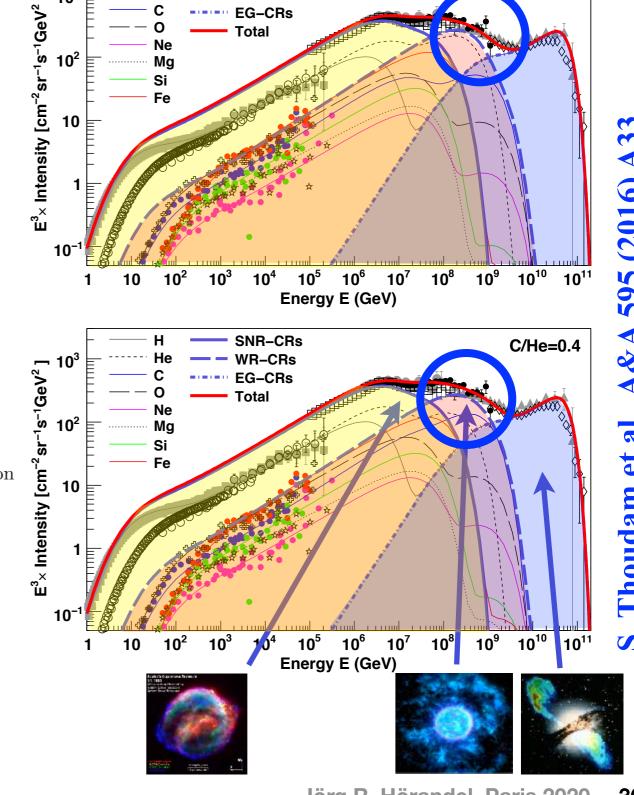


Table 3. Injection energy of SNR-CRs used in the calculation of all-particle spectrum in the WR-CR model (Figure 6).

Particle type	C/He = 0.1	C/He = 0.4
	$f(\times 10^{49} \text{ ergs})$	$f(\times 10^{49} \text{ ergs})$
Proton	8.11	8.11
Helium	0.67	0.78
Carbon	2.11×10^{-2}	0.73×10^{-2}
Oxygen	2.94×10^{-2}	2.94×10^{-2}
Neon	4.41×10^{-3}	4.41×10^{-3}
Magnesium	6.03×10^{-3}	6.03×10^{-3}
Silicon	5.84×10^{-3}	5.84×10^{-3}
Iron	5.77×10^{-3}	5.77×10^{-3}



SNR-CRs

WR-CRs

EG-CRs

Total

Paris
7-11 December 2020





Models for the knee in the energy spectrum of cosmic rays

- knee in all-particle spectrum at ~4.5 PeV caused by fall-off of light elements (p, He)
- experimental (world) data indicate rigidity-dependent fall-off of individual elements
 - (in particular unfolding by KASCADE[-Grande] and IceCube/Top)
- spectrum above knee is superposition of individual spectra (elemental knees)
 - -> fine structure in all-particle spectrum
 - -> end of galactic CR component
- astrophysical origin of knee: combination of maximum energy attained in sources (Supernovae) (Hillas criterion) and leakage from Galaxy
- 2nd galactic component at ~10¹⁷ eV?
- extra-galactic origin >10¹⁸ eV