

Lattice QCD and New Physics

Federico Mescia

ECM & ICC,
Universitat de Barcelona

- *Outline*

① Flavour Physics and New Physics:

➡ High Precision calculations: Lattice QCD

② Opportunity of new physics and Lattice QCD

➡ Charged Current modes: $K \rightarrow \pi l \nu$, $K \rightarrow \mu \nu$, $B \rightarrow \tau \nu$, $B \rightarrow D \tau \nu$: *H⁺, right-handed current ...*

➡ Flavour Changing Neutral Current observables: ΔM_s , ε_K ,
 $B \rightarrow K^* \mu \mu$: *H⁰, gluino ...*

Flavour Physics and New Physics

Next Discovery in Flavour Physics mostly driven by the modes

①

CP asym. in
 $B_s \rightarrow \psi \phi$.
 $\beta_s^{SM} \approx 0$

LHCb

yesterday-talk by P. Jenny

②

$B_s \rightarrow \mu \mu$

③

$K \rightarrow \pi \nu \nu$

NA62-JPARC

tomorrow-talk by C. Smith

④

$K_{\mu 2}/K_{e 2}$

➡ *to large extent, hadronic uncertainties is not a big issue for these modes!!:*

➡ *However, discriminating potentially New Physics effects will involve a much larger set of flavour-changing processes =>*

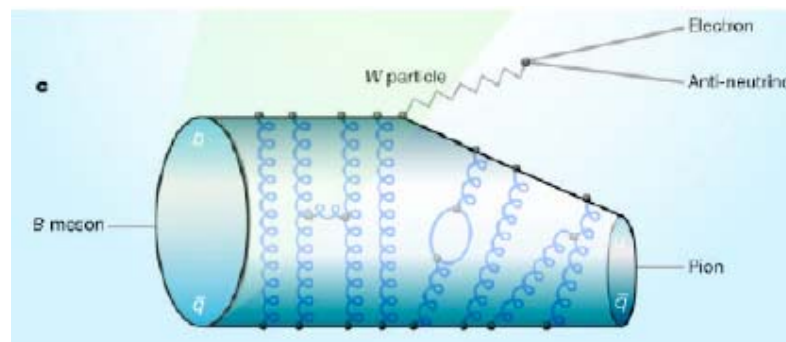
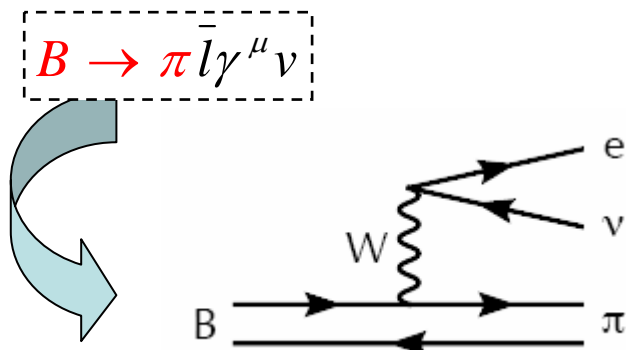
$B \rightarrow \tau \nu$, $B \rightarrow D \tau \nu$, $B \rightarrow \pi(\rho) l \nu$, ΔM_s , ε_K , $B \rightarrow K^* \mu \mu$

➡ **BIG ISSUE:** *keeping under good control hadronic uncertainties*

LATTICE QCD

Flavour Physics and New Physics: Lattice QCD

In order to interpret the experimental results in quark sector, *must include effects of confining quarks into hadrons* \Leftrightarrow *Non-Perturbative regime*



$$\text{Amplitude} = C_w \times \langle B | \bar{b} \gamma^\mu u | \pi \rangle \bar{l} \gamma^\mu \nu$$

Hard modes: $\alpha(m_b) \sim \text{weak}$:

➡ effective theories: OPE, HQET

Soft modes: $\alpha(m_\rho) \sim \text{strong!}$

➡ Matrix elements: **Lattice QCD** ☹️

➡ **Matrix elements can be computed on Lattice QCD** in an accurate and controllable manner, thanks the systematic character of Lattice simulations

➡ **NOW true thanks to tremendous progress in the present years!**

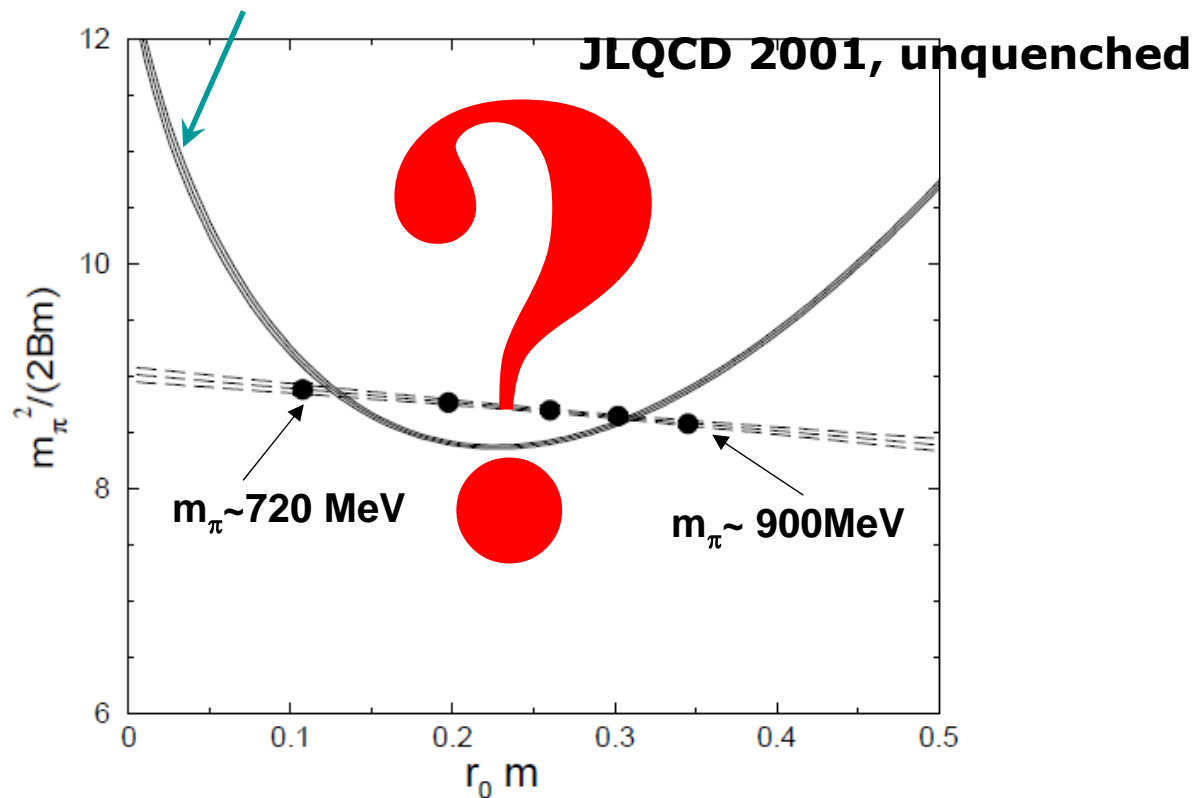


Chiral Regime of QCD

A problem with (old) lattice simulations:
Heavy pion mass!

Chiral regime of QCD

$$m_\pi^2 = M^2 \left[1 + \frac{M^2}{32\pi^2 F^2} \log(M^2/\Lambda_3^2) + \dots \right], \quad M^2 = 2Bm$$

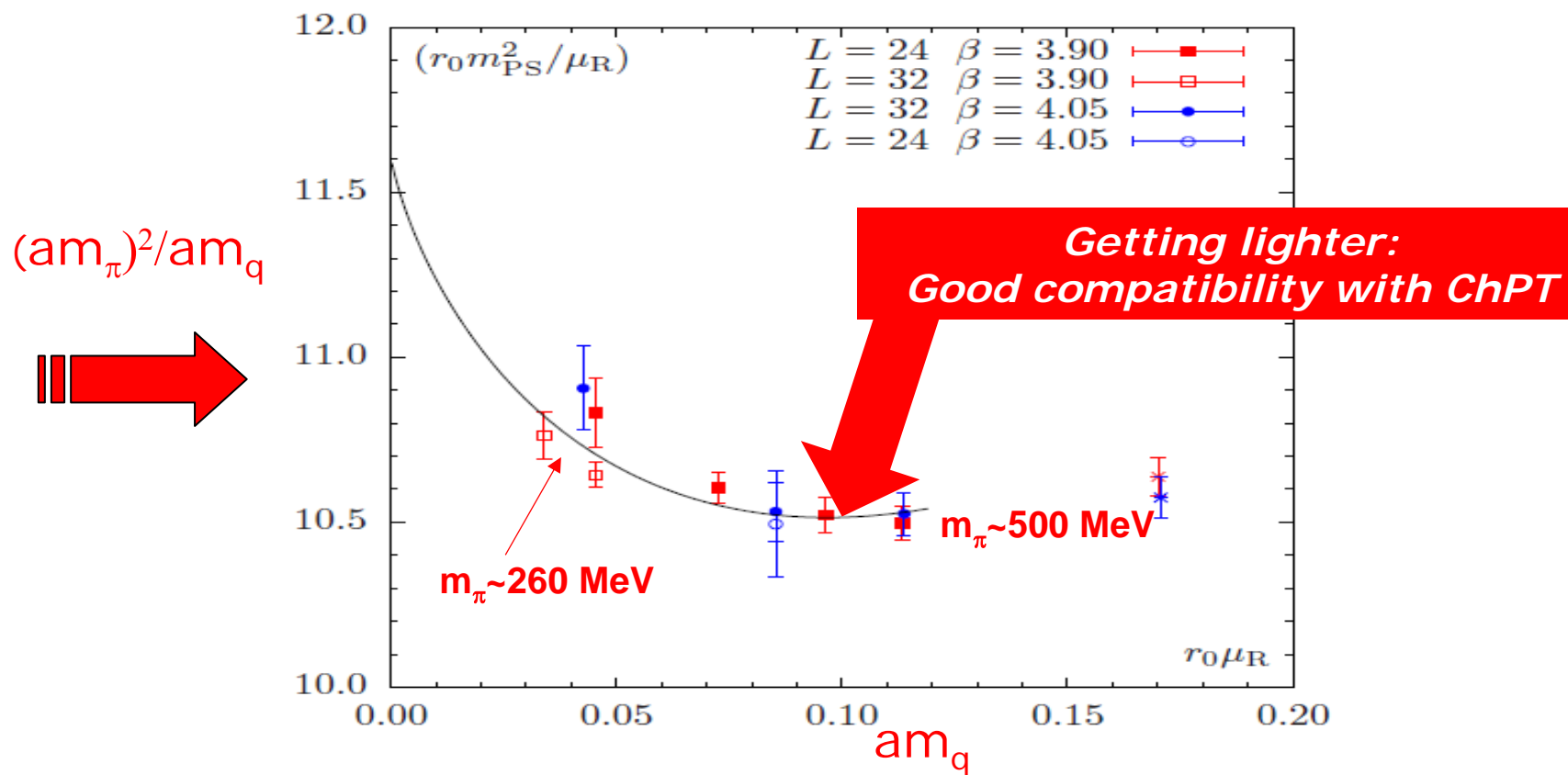


Incompatibility with ChPT?

Chiral Regime of QCD

No more problems with (new) lattice simulations:
Good compatibility with ChPT

$$m_\pi^2 = M^2 \left[1 + \frac{M^2}{32\pi^2 F^2} \log(M^2/\Lambda_3^2) + \dots \right], \quad M^2 = 2Bm$$



ETMC arXiv:0803.0224

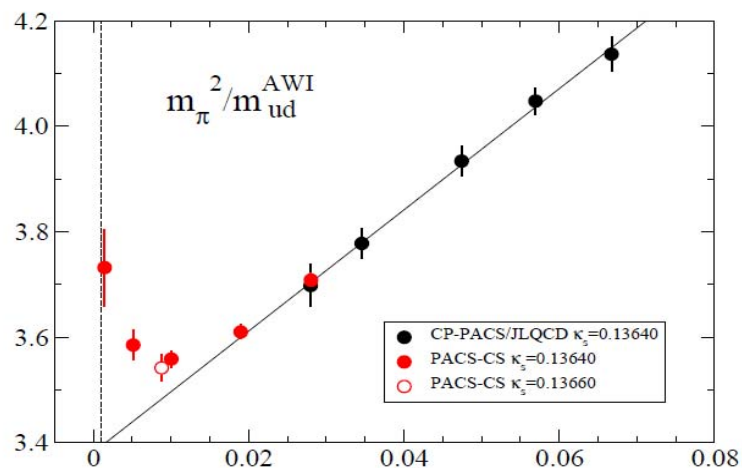
2008, unquenched, Wilson-like fermions

Similar plots by other collaborations (using QCD actions from first principle)

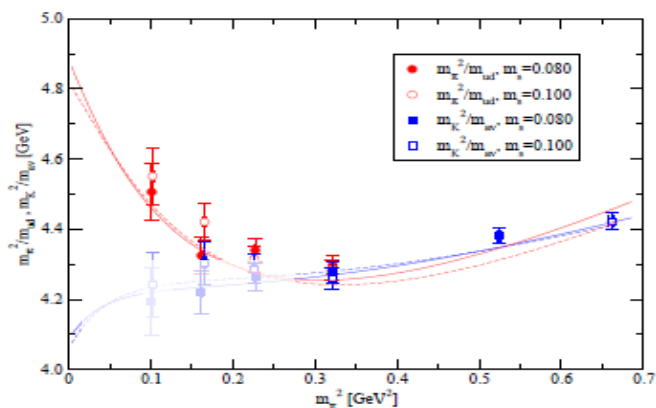
Chiral regime of QCD

$$(\mathbf{am}_\pi)^2/\mathbf{am}_q$$

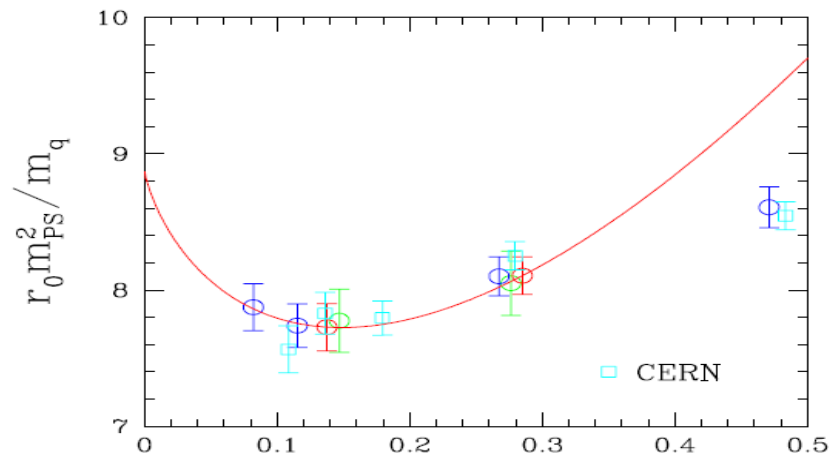
Hints of chiral Logs



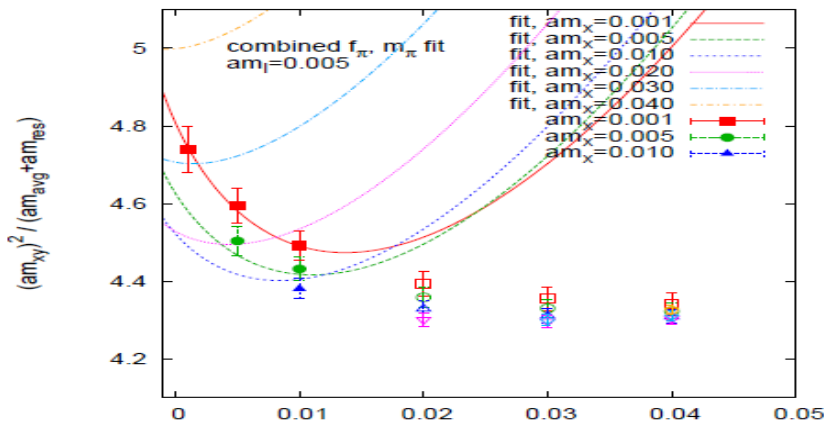
PACS-CS'08, $N_F=2+1$, Clover:
 $a=0.09$ fm, $M_\pi=156$ MeV, $L M_\pi \sim 2.3!!$



JLQCD/TWQCD'08, $N_F=2+1$, Overlap:
 $a=0.11$ fm, $M_\pi=300$ MeV, $L M_\pi \sim 2.6!!$



QCDSF'08, $N_F=2$, Clover:
 $a=0.07$ fm, $M_\pi=313$ MeV, $L M_\pi \sim 4$



RBC/UKQCD'06, $N_F=2+1$, DWF
 $a=0.114$ fm, $M_\pi=310$, $L M_\pi \sim 3-4$

What about phenomenology?

★ Up to now, only a few observables available from first principle QCD action (2006 - on)

⇒ **Wilson-like & Domain-Wall fermions**

■ some observables are still in the “quenched approximation” (1974-2002);

● most unquenched estimates are from staggered fermions (**MILC: 2002 – on**)

😊 **First realistic QCD study => MILC opened up unquenched era!!**

😞 *but unsatisfactory in high-precision era!:*

⇒ *staggered ansatz: $\det[D_{NF=1}] \cong \det[D_{stag}]^{1/4}$ to eliminate spurious “tastes”:*

⇒ *non-local theory! Shamir, Bernard, Golterman, Sharpe, Creutz '04-'08*

⇒ **QCD when lattice spacing goes 0?**

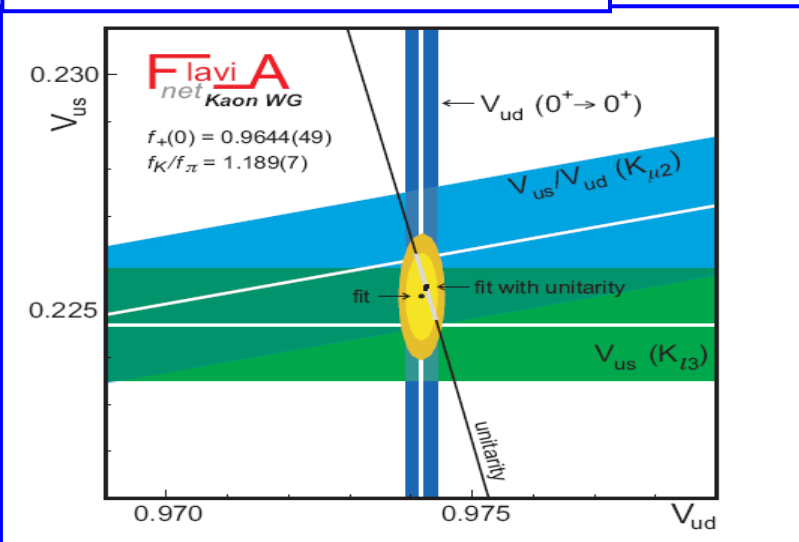
⇒ **at finite a , significant lattice artefacts: to subtract by complicated fit**

😞 *Phenomenological safe lattice data still need some time but progress already visible!*



2010: Lattice QCD in Flavour Physics

$$|V_{ud}|^2 + |V_{us}|^2 + |V_{ub}|^2 = 1$$



$K \rightarrow l\nu$: exp. err 0.2%



lattice err. on f_K/f_π :

2-3% (2006) \rightarrow 0.7% (2010)

$K \rightarrow \pi l\nu$: exp. err 0.2%



lattice err. on $f_+(0)$:

0.9% (2006) \rightarrow 0.5% (2010)

$B \rightarrow D(D^*) l\nu$: exp. err 1.5%



lattice err. on $F(1)$ & $G(1)$:

5% (2006) \rightarrow 2.5% (2010)



Simulation from first-principle action.

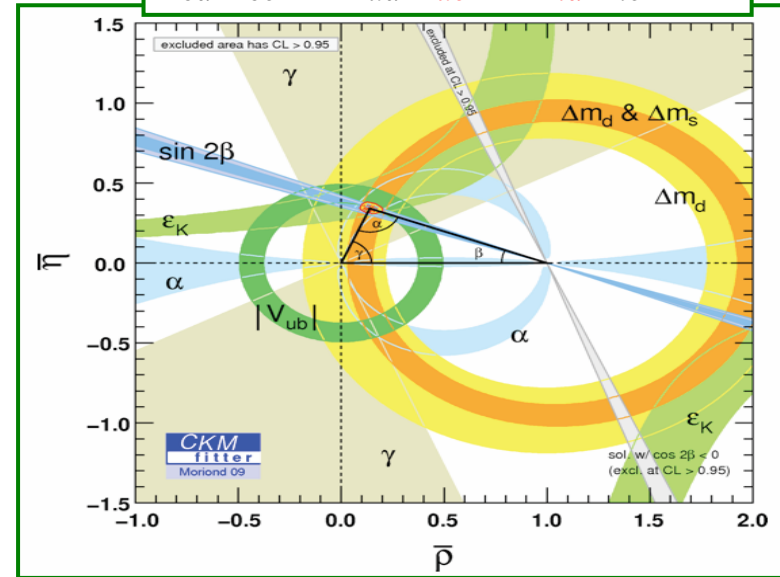


Quenched simulation.



Staggered fermions

$$V_{cd} V_{cb}^* + V_{ud} V_{ub}^* + V_{td} V_{tb}^* = 0$$



ϵ_K : $K^0-\bar{K}^0$ mixing

exp. err 0.5%

lattice err. on B_K :

11% (2006) \rightarrow 5% (2010)

ΔM_d : $B_d^0-B_d^0$ mixing

exp. err 1%

lattice err. on $f_{B_d}\sqrt{B_{B_d}}$:

13% (2006) \rightarrow 6%? (2010)

ΔM_s : $B_s^0-B_s^0$ mixing

exp. err 0.7%

lattice err. on $f_{B_s}\sqrt{B_{B_s}}$:

13% (2006) \rightarrow 6%? (2010)

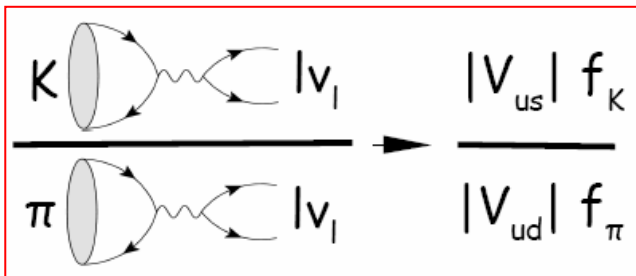
$B \rightarrow \pi(\rho) l\nu$:

exp. err 10%

lattice err. on $f_+(q^2)$:

11% (2007)!

f_K/f_π : an example of Modern lattice measure



Hadronic uncertainties from

$$\langle 0 | \bar{s} \gamma^\mu \gamma_5 u | K \rangle = p^\mu f_K$$

$$\langle 0 | \bar{d} \gamma^\mu \gamma_5 u | \pi \rangle = p^\mu f_\pi$$

f_K/f_π : lattice enters high precision era

❖ No Competition from non-Lattice approaches:

$$f_K/f_\pi = 1 + (m_K^2 - m_\pi^2) \times \text{unknown-coef.}$$

f_K/f_π

Lattice systematic under control!

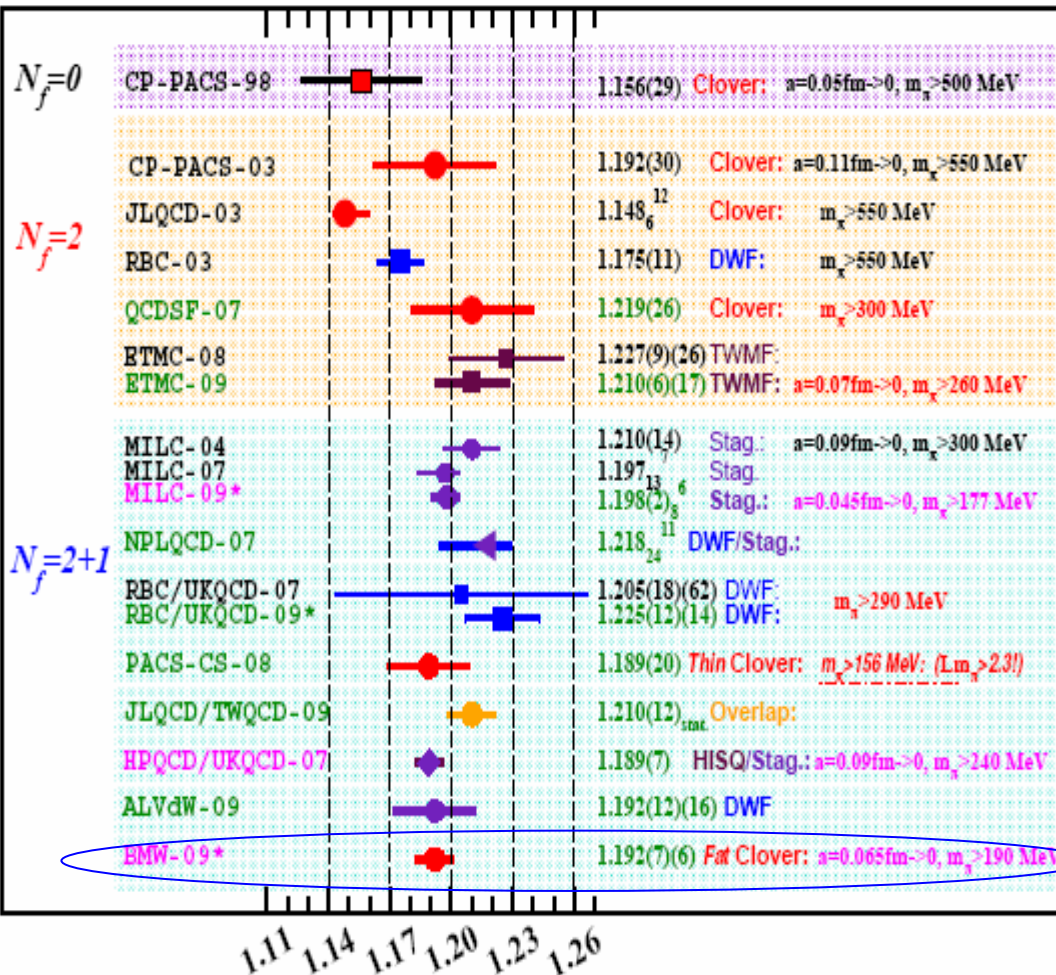
- ❑ Independent determinations (Wilson-like, Domain Wall, Stag.);
- ❑ Many lattice spacings (Continuum Limit reached);
- ❑ Light $m_\pi \sim 190$ MeV;
- ❑ Finite size effects under control.

$$f_K/f_\pi = 1.192 \pm 0.009 \text{ [0.75%];}$$

postdiction?

$$f_K/f_\pi - 1 = 0.192 \pm 0.009 \text{ [5%]}$$

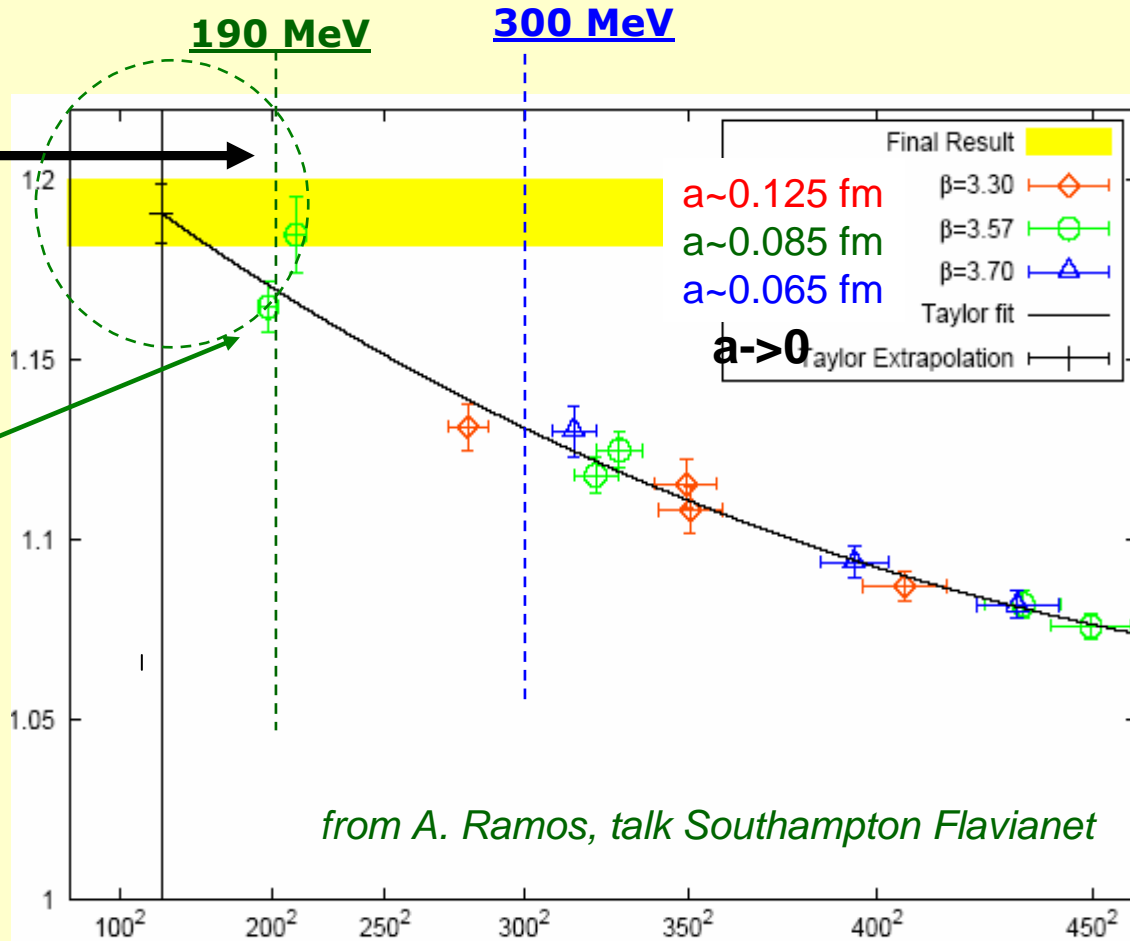
good prospects to improve $f_K/f_\pi - 1$ to 1% accuracy?



f_K/f_π - Evaluations

- getting very close to the physical point; **190 MeV**

The final result extrapolated at the physical pion is only 2% above the lightest point simulated!



- **BMW result: $N_F=2+1$, Clover, $a=0.06 \rightarrow 0$, $m_\pi \geq 190$ MeV, $L m_\pi \sim 4$**
 $f_K/f_\pi = 1.192(7) (6) \Rightarrow \sigma_{\text{rel}} \sim 0.75\%$ ($\delta_{SU(3)} \sim 5\%$)

Beyond SM from K_{l2} and K_{l3}

Not-trivial SM test

$$\left(|V_{ud}|^2 + |V_{us}|^2 + \cancel{|V_{ub}|^2} \right) \neq 1$$

CKM Unitarity breaking

$$G_{CKM}^2 \equiv G_F^2 \times \left(|V_{ud}|^2 + |V_{us}|^2 \right) \neq 1 \times G_F^2$$

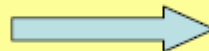
Gauge Universality Breaking

covered by Martin Gonzalez-Alonso on Wed

➤ appealing BSM possibilities

▪ **MSSM**

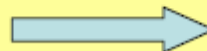
Hou - Isidori & Paradisi,



constrain on scalar densities

▪ **a Higgsless model**

Bernard, Oertel, Passemar & Stern



constraint on right-handed currents

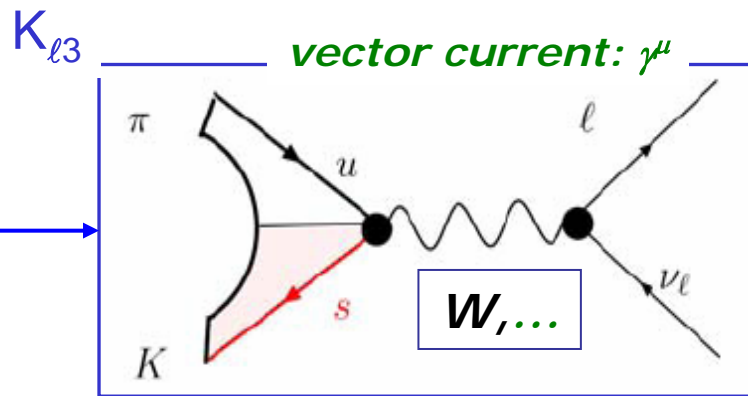
$$B(K \rightarrow \mu\nu) / B(K \rightarrow \pi l\nu)$$

Higgsless Model: resonances => $SM + (\bar{s}\gamma_R^\mu u)(\bar{\ell}\gamma_L^\mu \nu)$

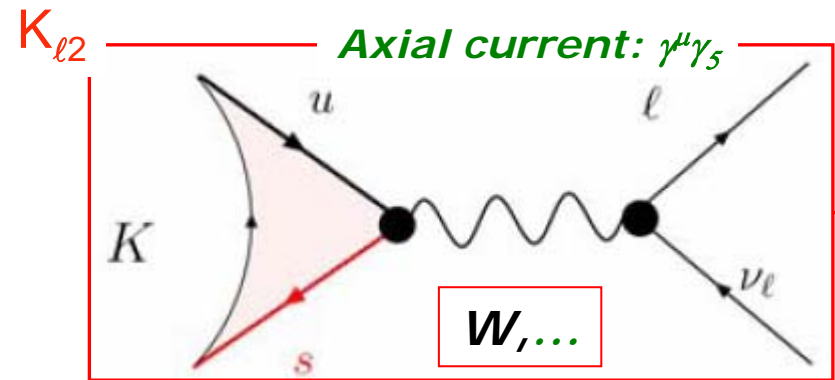
Bernard, Hirn, Oertel, Passemar & Stern

- “Higgs-Goldstone field” to give mass to W and Z ;
- no elementary Higgs particle => higher order operators (composite, partial, no Higgs)

=> Effects from right-handed currents compatible to EWPT



K_{I3} : RHC =>
 $|V_{us}|^{KI3} \rightarrow |V_{us}|^{KI3} (1 + \varepsilon^{RH})$



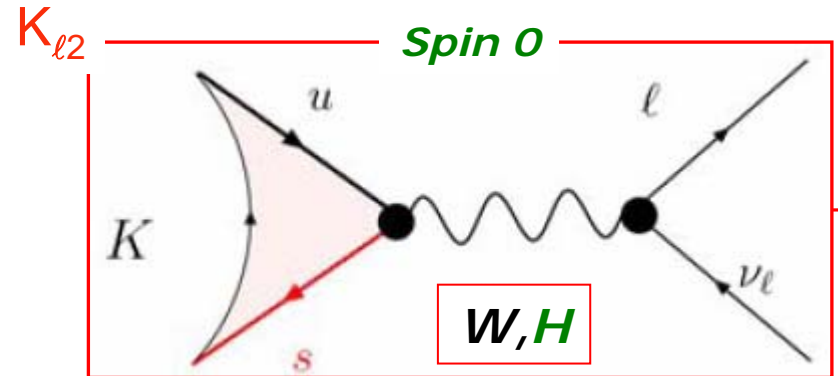
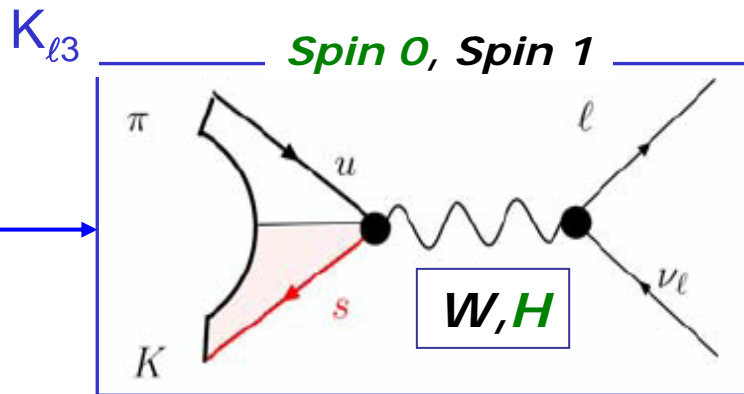
K_{I2} : RHC =>
 $|V_{us}|^{KI2} \rightarrow |V_{us}|^{KI2} (1 - \varepsilon^{RH})$

$1 - 2\varepsilon^{RH} = 1.004(6)$

Collider Signature:
 W' , Strong dynamics@TeV

2HDM, Susy: Charged Higgs =>

$$SM + (\bar{s}_R u_L)(\bar{\ell} \nu_L)$$



K_{l3} : Higgs effects => $f_0(q^2) \rightarrow f_0(q^2)(1 + g^H q^2/m_H^2)$

- to test g^H => calculate slope and curvature of $f_0(q^2)$!

$|V_{us}|^{Kl3}$ is NP free as soon as we use $f_0(q^2)$ from data

K_{l2} : Higgs effects => $|V_{us}|^{Kl2} \rightarrow |V_{us}|^{Kl2} (1 + g^H m_K^2/m_H^2)$

- to test g^H => f_K from theory: f_K/f_π better determined

constrain on scalar densities

Hadronic uncertainties => estimate this ratio from the same simulation!

$$\frac{B(K \rightarrow \mu\nu)}{B(\pi \rightarrow \mu\nu)} \times \frac{B(n \rightarrow pl\nu)}{B(K \rightarrow \pi l\nu)} = \left(\frac{f_K}{f_\pi} \frac{1}{f_+(0)} \right)^2 \times \left(1 + g^H \frac{m_K^2}{m_{H^+}^2} \right)^2 \quad (\text{known f.s.})$$

similarly search on H^+ from

$$B^\pm \rightarrow \tau^\pm \nu$$

$$Br(B \rightarrow \tau\nu) \propto |V_{ub}|^2 f_B^2 m_B m_\tau^2 \times \left(1 + g^H \frac{m_B^2}{m_{H^+}^2} \right)^2$$

● hadronic uncertainty in f_B :
~15% accuracy from Lattice

Best for indirect H^+ searches
but only feasible at ● SuperB

$$B^\pm \rightarrow D \tau^\pm \nu$$

$$\frac{d\Gamma(B \rightarrow D\tau\nu)}{dq^2} \propto |V_{cb}|^2 \rho_V(q^2) \times \left(\left| 1 - \frac{m_\tau^2}{m_B^2} \right| \left| 1 + g^H \frac{q^2}{m_{H^+}^2} \right| \rho_S(q^2) \right)^2$$

2. hadronic uncertainty in ρ_V , ●
 ρ_S ■

Only scalar component sensitivity to H^+ but opportunity for Lhcb

but different theoretical and experimental prospects

■ Quenched simulation.

● Staggered fermions

constrain on scalar densities

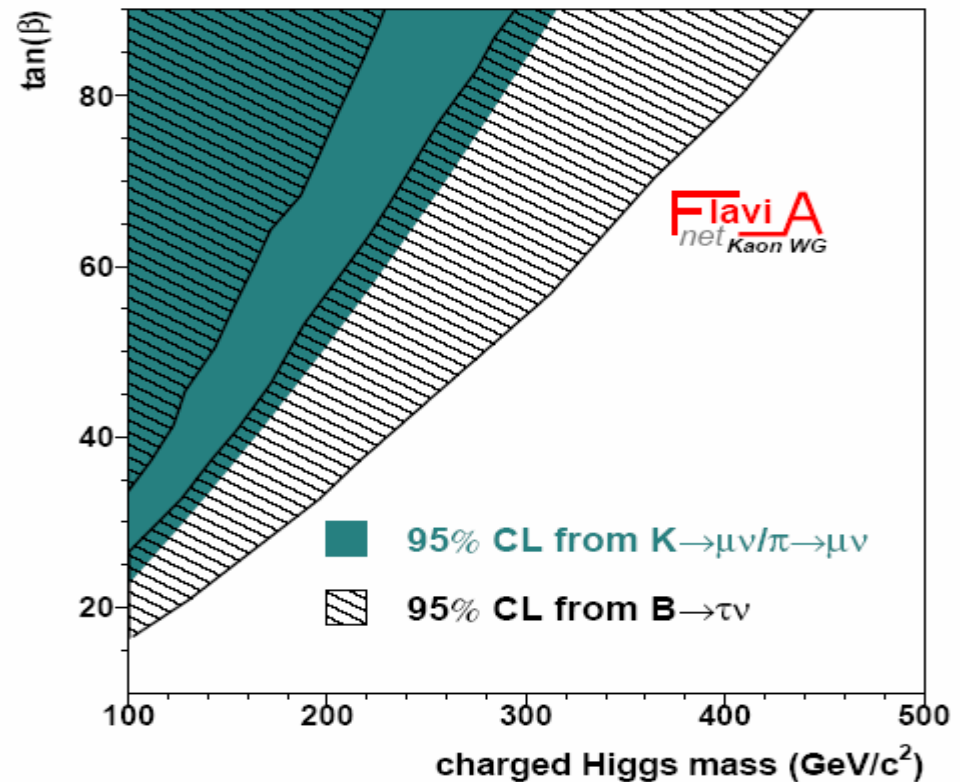
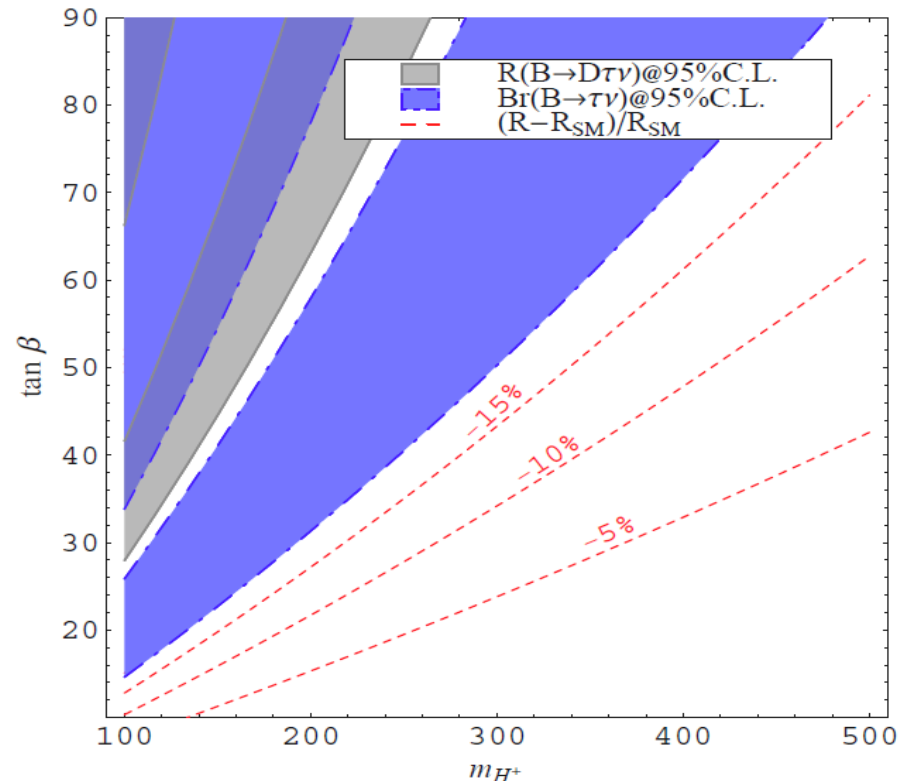
$$\underline{B^\pm \rightarrow D \tau^\pm \nu}$$

$$\underline{B^\pm \rightarrow \tau^\pm \nu}$$

$$\frac{B(K \rightarrow \mu \nu)}{B(\pi \rightarrow \mu \nu)} \times \frac{B(n \rightarrow p l \nu)}{B(K \rightarrow \pi l \nu)}$$

Example MFV@large $\tan\beta$

$$g^H = -\tan\beta^2 / (1 + \varepsilon_0 \tan\beta)$$



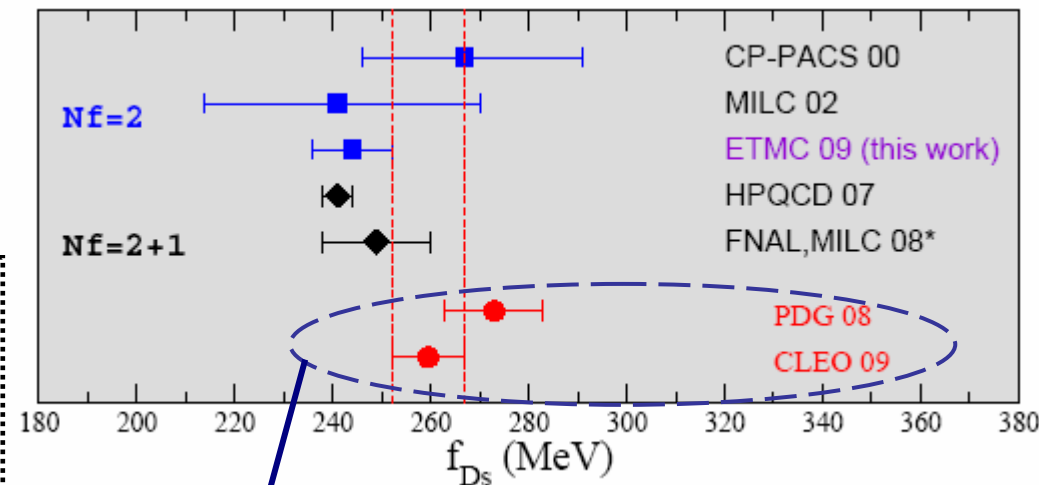
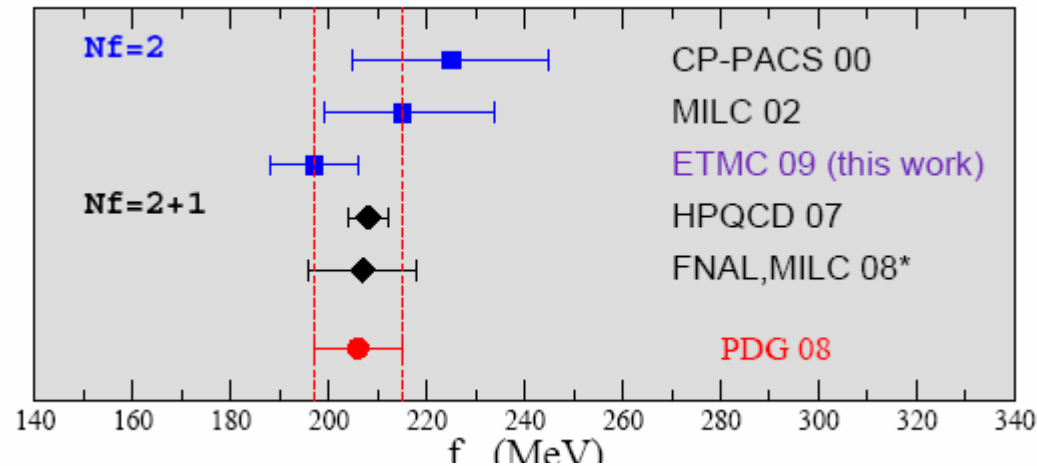
Kamenik & F.M '08:
Nierste, Trine, Westhoff '08

2008 f_{D_s} puzzle: 3-4 σ deviation with experiments

f_D and f_{D_s} recently measured at CLEO, BaBar and Belle with good accuracy! (assuming CKM unitarity)

Valuable cross check of Lattice QCD.

Overall consistency of lattice results;
But still only a few uncorrelated lattice simulations.
Mind discretization error from charm mass



f_{D_s} "puzzle" weakened by CLEO-c 2009 accurate measurement

$\Delta F=2$ observables:

ε_K , ΔM_d and ΔM_s

□ Important role for the SM Unitarity Triangle analysis:

❖ **strong constraints for non-minimal flavour models:**

➔ **MSSM** -> generic down squarks insertion [Gabbiani et al. 1994]

➔ **Little Higgs** [A. Buras et al. 2004]

*Lattice role and New Physics
Opportunities!*

$\Delta F=2$ constraints in Minimal Flavour Violation (MFV)

EFT: D'Ambrosio, Giudice, Isidori & Strumia '02

$$\mathcal{L}_{\text{eff}}^{\text{MFV}} = \sum_i \frac{\delta C_i}{\Lambda^2} \mathcal{O}_i^{(6)}$$

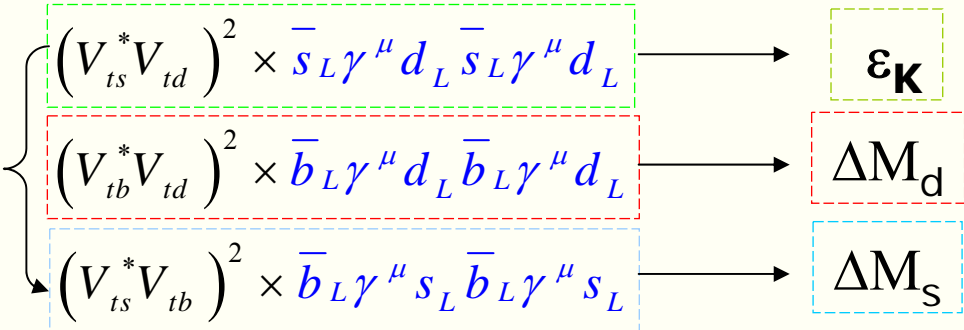
flavour violation mediated by Yukawa beyond SM too!!

\mathcal{O} basis invariant under $\text{SU}(3)_{\text{Q}} \times \text{SU}(3)_{\text{U}_R} \times \text{SU}(3)_{\text{D}_R}$

• Due to the large top $Y, Y_U Y_U^+ \propto y_t^2 \sim O(1)$

$$1) \quad \mathcal{O}_{SM}^{(6)} = \bar{Q}_L Y_U Y_U^+ \gamma^\mu Q_L \cdot \bar{Q}_L Y_U Y_U^+ \gamma^\mu Q_L$$

1 Higgs doublet, SM basis complete -> CMFV

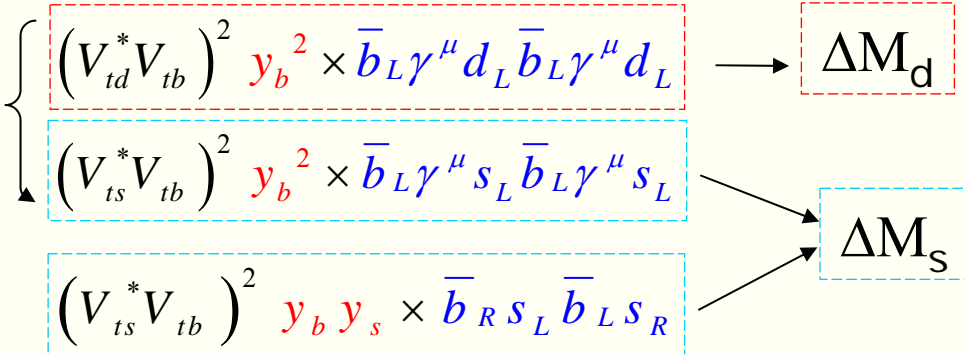


Buras, Gambino, Gorbahn, Jager, L. Silvestrini '00

• Adding Higgs doublets, $Y_D \propto m_b / m_t \frac{\langle H_U \rangle}{\langle H_D \rangle} \sim O(1)$ ($\tan\beta$ enhancement of down-type YDs)

$$2) \quad \left(\bar{Q}_L Y_D Y_D^+ Y_U Y_U^+ \gamma^\mu Q_L \right)^2$$

$$3) \quad \bar{D}_R Y_D^+ Y_U Y_U^+ Q_L \cdot \bar{Q}_L Y_U Y_U^+ Y_D D_R$$



A few extra $\mathcal{O}^{(6)}_s$ in a clear pattern between $s \rightarrow d$ & $b \rightarrow d$, $b \rightarrow s$ transitions
Improved Lattice calculation needed to discriminate this MFV pattern!

$\Delta F=2$ constraints in MFV and Lattice QCD

□ Up to now, unquenched results only for SM operators:

$$\bar{s}_L \gamma^\mu d_L \bar{s}_L \gamma^\mu d_L \propto B_K \rightarrow \sigma_{rel} \sim 5\%,$$

★ Simulation from first-principle action:
RBC-UKQCD $N_f=2+1$ Domain Wall f.:
No continuum limit?? $M_\pi \geq 330$ MeV
➤ *Need further calculation on the Lattice!*

$$\bar{b}_L \gamma^\mu s_L \bar{b}_L \gamma^\mu s_L \propto B_s f_{Bs}^2 \rightarrow \sigma_{rel} \sim 16\%.$$

● Simulation from staggered fermions?

$$\bar{b}_L \gamma^\mu d_L \bar{b}_L \gamma^\mu d_L \propto B_d f_{Bd}^2 \rightarrow \sigma_{rel} \sim 16\%$$

➤ *Need further calculation on the Lattice!*
➤ *At current lattice spacing, $m_b \cdot a \sim 1$,
b quark cannot be directly simulated*

□ Up to now, only fix a lower bound from the scale of New Physics

UTfit 0707.0636

$$\Lambda \geq 5.5 \text{ TeV}$$

$$\Lambda \geq 0.5 \text{ TeV}$$

loop-suppr.

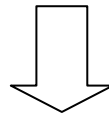
ϵ_K	ΔM_d	ΔM_s
	$\sin(2\beta)$	$\sin(2\beta_s)$

□ a 2.2σ tension in $\beta_s = \phi_s$ from CDF/D0? => lower bound from Bs system!
=> awaiting LHCb!

$$\Delta F=1 \ b \rightarrow s \text{ transitions:}$$

$$B \rightarrow K^* \mu^+ \mu^- \dots$$

Lattice role, LHCb and New Physics Opportunities!



Experiment	BaBar [8]	Belle [7]	CDF [9]
$\text{BR}(B \rightarrow K^* \mu^+ \mu^-) \times 10^7$	$11.1 \pm 1.9 \pm 0.7$	$10.8^{+1.0}_{-1.0} \pm 0.9$	$8.1 \pm 3.0 \pm 1.0$
Number of $B\bar{B}$ events	384×10^6	657×10^6	—

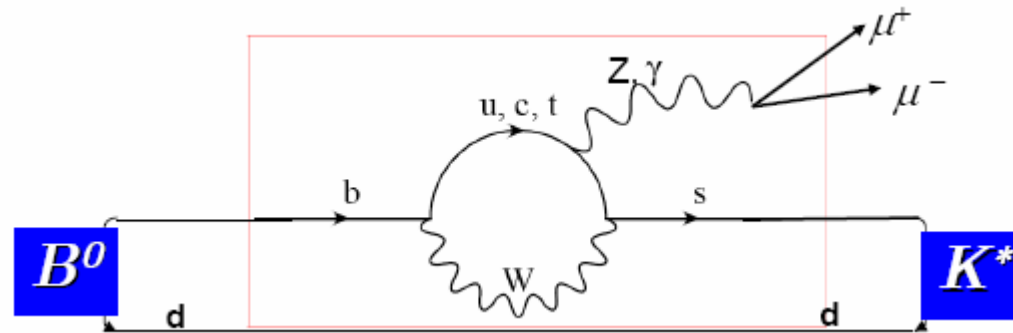
still small statistics -> ~230 events -> the rarest decay!



-> ~7500 events at LHCb for $B \rightarrow K^* \mu^+ \mu^-$

$B \rightarrow K^* \mu^+ \mu^-$ modes

1. Flavour Changing Neutral Current $b \rightarrow s$ processes \rightarrow rare process



\Rightarrow Exploiting the decay $K^* \rightarrow K\pi$, LHCb will access to a plethora of new observables:

$$\bar{B}^0 \rightarrow \bar{K}^{*0} (\rightarrow K^- \pi^+) \mu^+ \mu^-$$

$$\frac{d^4 \Gamma_{\bar{B}_d}}{ds d\theta_l d\theta_K d\phi} \propto \mathbf{l}_1 + \mathbf{l}_2 \cos 2\theta_l + \mathbf{l}_3 \sin^2 \theta_l \cos 2\phi + \mathbf{l}_4 \sin 2\theta_l \cos \phi + \mathbf{l}_5 \sin \theta_l \cos \phi + \mathbf{l}_6 \cos \theta_l + \mathbf{l}_7 \sin \theta_l \sin \phi + \mathbf{l}_8 \sin 2\theta_l \sin \phi + \mathbf{l}_9 \sin^2 \theta_l \sin 2\phi.$$

\Rightarrow correlations among angular coefficients is dependent on New Physics modes and allows to discriminate among different New Physics Models.

Egede, Hurth, Matias, Ramon, Reece '08;

Altmannshofer, Ball, Bharucha, Buras, Straub Wick '08;

$$A(B \rightarrow K^* \mu \mu) = \langle K^* | H_{\text{eff}} | B \rangle = \begin{cases} C_7 \times \bar{b} \sigma^{\mu\nu} s F_{\mu\nu} \\ C_9 \times \bar{b} \gamma_L^\mu s \bar{l} \gamma^\mu l + C_{10} \times \bar{b} \gamma_L^\mu s \bar{l} \gamma^\mu \gamma_5 l \\ C_S \times \bar{b}_L s_R \bar{l} l \end{cases}$$

➤ Matrix elements \Leftrightarrow 7 form factors

Lattice QCD

$$\begin{aligned} \langle K^*(p_{K^*}) | \bar{s} \gamma_\mu P_{L,R} b | B(p) \rangle &= i \epsilon_{\mu\nu\alpha\beta} \epsilon^{\nu*} p^\alpha q^\beta \frac{V(q^2)}{m_B + m_{K^*}} \mp \\ &\mp \frac{1}{2} \left\{ \epsilon_\mu^* (m_B + m_{K^*}) A_1(q^2) - (\epsilon^* \cdot q) (2p - q)_\mu \frac{A_2(q^2)}{m_B + m_{K^*}} - \right. \\ &\quad \left. - \frac{2m_{K^*}}{q^2} (\epsilon^* \cdot q) [A_3(q^2) - A_0(q^2)] q_\mu \right\}, \end{aligned}$$

$$\begin{aligned} \langle K^*(p_{K^*}) | \bar{s} i \sigma_{\mu\nu} q^\nu P_{R,L} b | B(p) \rangle &= -i \epsilon_{\mu\nu\alpha\beta} \epsilon^{\nu*} p^\alpha q^\beta T_1(q^2) \pm \\ &\pm \frac{1}{2} \left\{ [\epsilon_\mu^* (m_B^2 - m_{K^*}^2) - (\epsilon^* \cdot q) (2p - q)_\mu] T_2(q^2) + \right. \\ &\quad \left. + (\epsilon^* \cdot q) \left[q_\mu - \frac{q^2}{m_B^2 - m_{K^*}^2} (2p - q)_\mu \right] T_3(q^2) \right\}. \end{aligned}$$

❖ Up to now, only T_1 on the Lattice but quenched (Becirevic, Lubicz, Mescia '06)

$A_{FB}(B_d \rightarrow K^* l^+ l^-)$, already plays a special role:

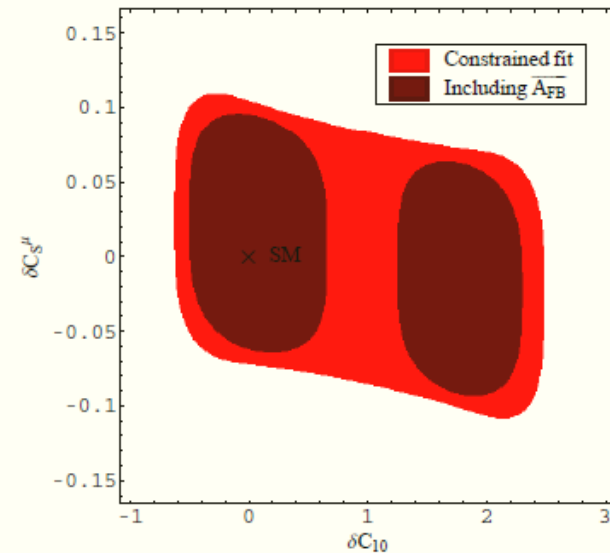
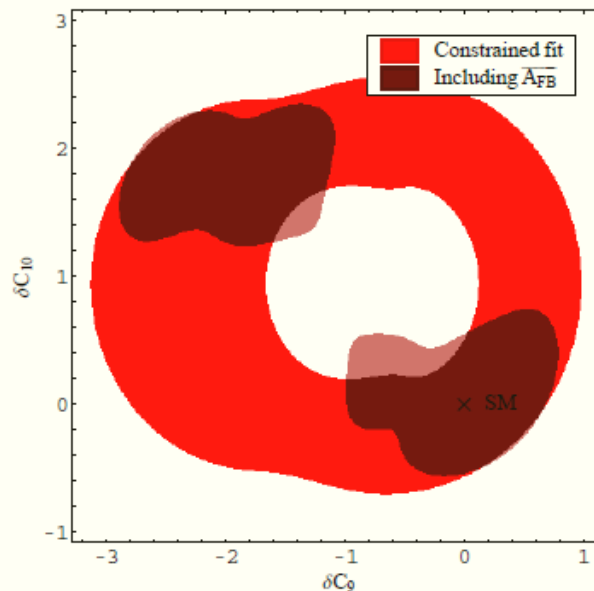
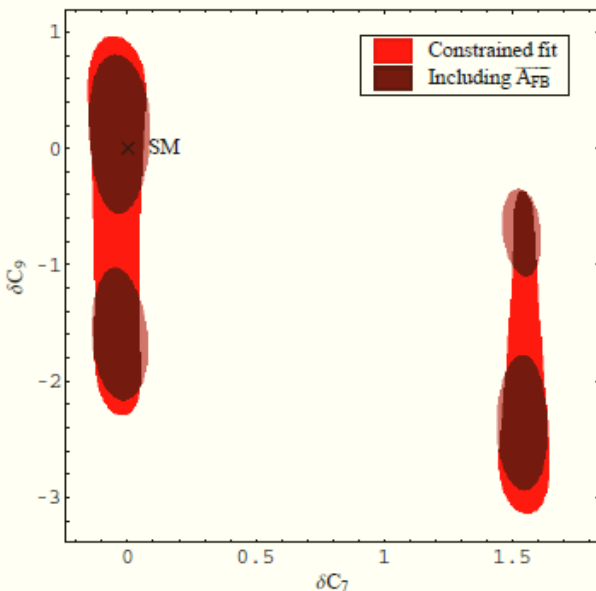
- ❖ very large experimental error;
- ❖ Golden modes for LHCb

➔ **Necessary to improve lattice form factors!**

$A_{FB}(B_d \rightarrow K^* l^+ l^-)$: 2 bins

exp (large): Babar+Belle '09

$[q^2 < 6.25 \text{ GeV}^2]$	$0.24^{+0.19}_{-0.24}$	-0.01 ± 0.02
$[q^2 > 10.24 \text{ GeV}^2]$	$0.76^{+0.53}_{-0.34}$	0.20 ± 0.08



Model-independent Analysis in MFV!

FCNC constraints from $Br(B_d \rightarrow X_s \gamma)$, $Br(B_d \rightarrow X_s l^+ l^-)$, $Br(B_d \rightarrow \mu^+ \mu^-)$, ΔM_s

Hurth, Isidori, Kamenik, F.M '08

Summarising:

➡ Evidence of New Physics in the Flavour physics mainly

①

$$\text{CPV in } B_s \rightarrow \psi\phi \\ \beta_s^{SM} \approx 0$$

②

$$B_s \rightarrow \mu\mu$$

③

$$K \rightarrow \pi \nu\nu$$

④

$$K_{\mu 2}/K_{e 2}$$

LHCb

yesterday-talk by P. Jenny

NA62-JPARC

tomorrow-talk by C. Smith

➡ then, discriminating among New Physics Models will involve deeper investigations:

$$B \rightarrow \tau \nu, B \rightarrow D \tau \nu, B \rightarrow \pi(\rho) l \nu, \Delta M_s, \varepsilon_K, B \rightarrow K^* \mu \mu$$

➡ Challenge is keeping under good control hadronic uncertainties

LATTICE QCD

Conclusions:

LATTICE QCD -> tremendous progress in recent years:

➡ reliable unquenched simulations with pions close to the physical point => $m_\pi = 156 \text{ MeV}$ (PACS-CS), $m_\pi = 190 \text{ MeV}$ (BMW)

➡ f_K/f_π paradigm of present lattice progress!

➡ many other calculations should be come soon at the same precision!

In particular, for B-physics observables => LHCb

Still a long work for 1%-precision in B-physics, according New Physics expectation (MFV).

① discretization errors: $a * m_B \ll 1$

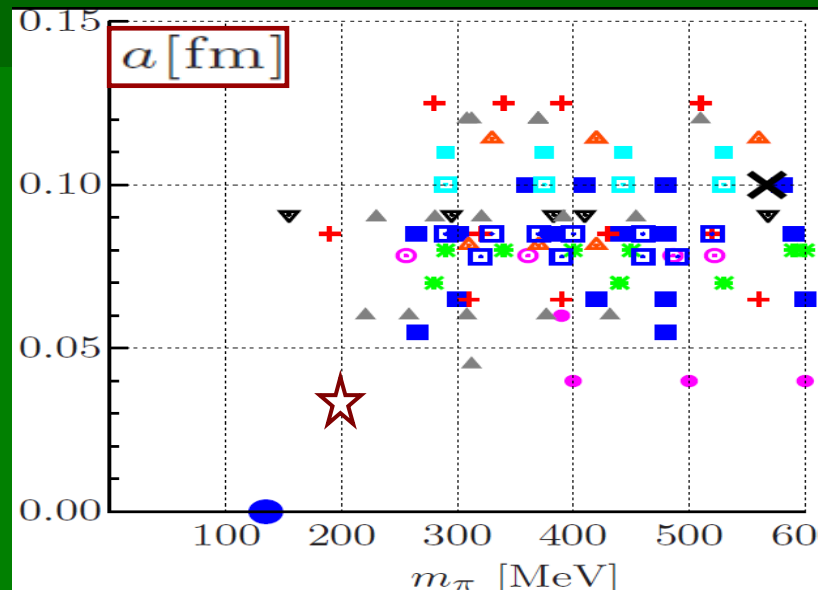
=> $a \sim 0.033 \text{ fm}$ (6 GeV): ($a \geq 0.07 \text{ fm}$)

② finite volume effects: $L * m_\pi \gg 1$

=> $L \geq 4.5 \text{ fm}$ ($L \leq 3 \text{ fm}$)

③ chiral regime: $200 \leq m_\pi \leq 300 \text{ MeV}$

V. Lubicz Super-B report.

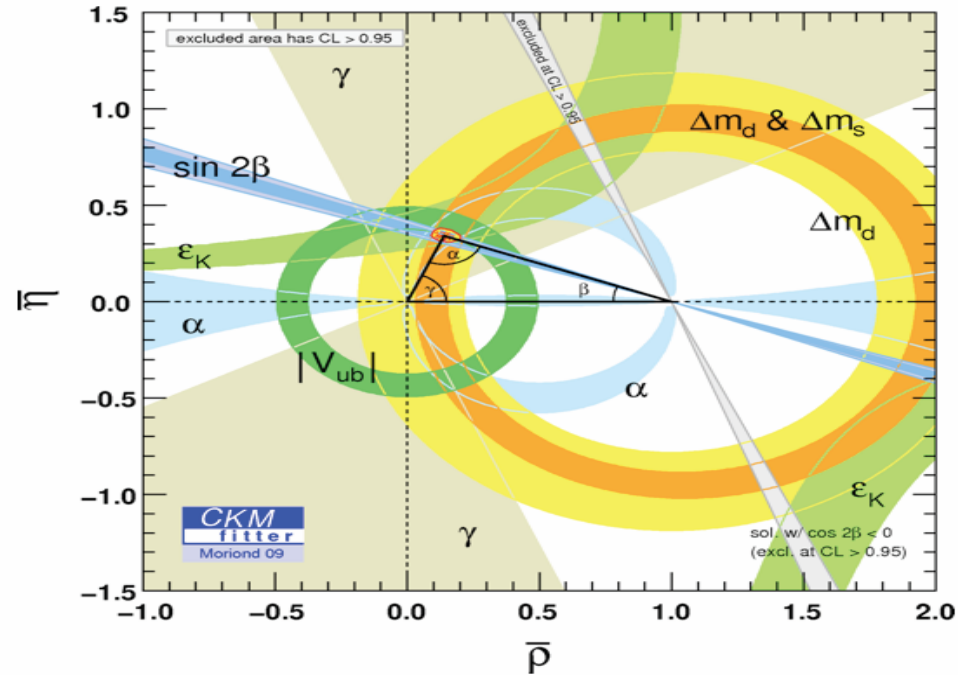
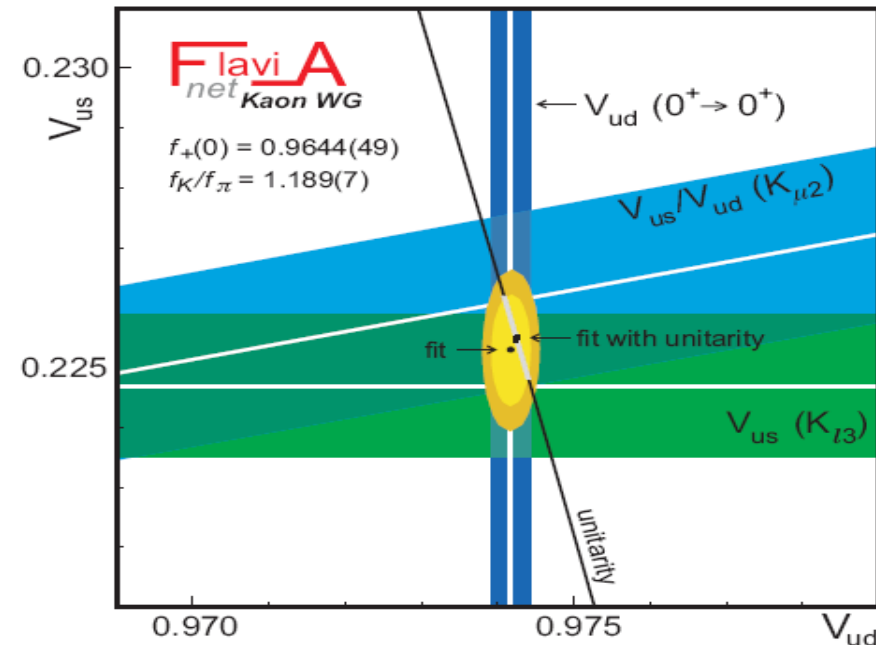


courtesy of G. Herdoiza

Flavour Physics Tests

$$|V_{ud}|^2 + |V_{us}|^2 + |V_{ub}|^2 = 0.9995(7)$$

$$V_{cd}V_{cb}^* + V_{ud}V_{ub}^* + V_{td}V_{tb}^* = 0$$



- Universality test of Quark-Lepton weak gauge coupling: **rel. error~0.7%**

On Wednesday: talk by M. Gonzalez-Alonso
“New Physics bounds on CKM unitarity”

- Unitarity triangle: CP violation on the Standard Model:

rel. error on $\rho \sim 17\%$ $\eta \sim 5\%$

see talks by P. Urquijo and O. Long

➤ **Constraining V_{us} , ρ , η as precisely as possible from as many independent modes as possible in order to search for New Physics!**

GOOD NEWS!

Precision Lattice Era

$$Z_{\text{QCD}} = \int \mathcal{D}A_\mu e^{-S_g} \prod_q \det(\mathcal{D} + m_q^{\text{sea}})$$

Recent outstanding achievements:

- Wilson: *CERN-TOV.'05*,
- Twisted-mass: *ETMC'07*,
- “Clover”: *BMW'08*,
- Clover: *PACS-CS'08*,
- Overlap: *JLQCD/TW'08*,

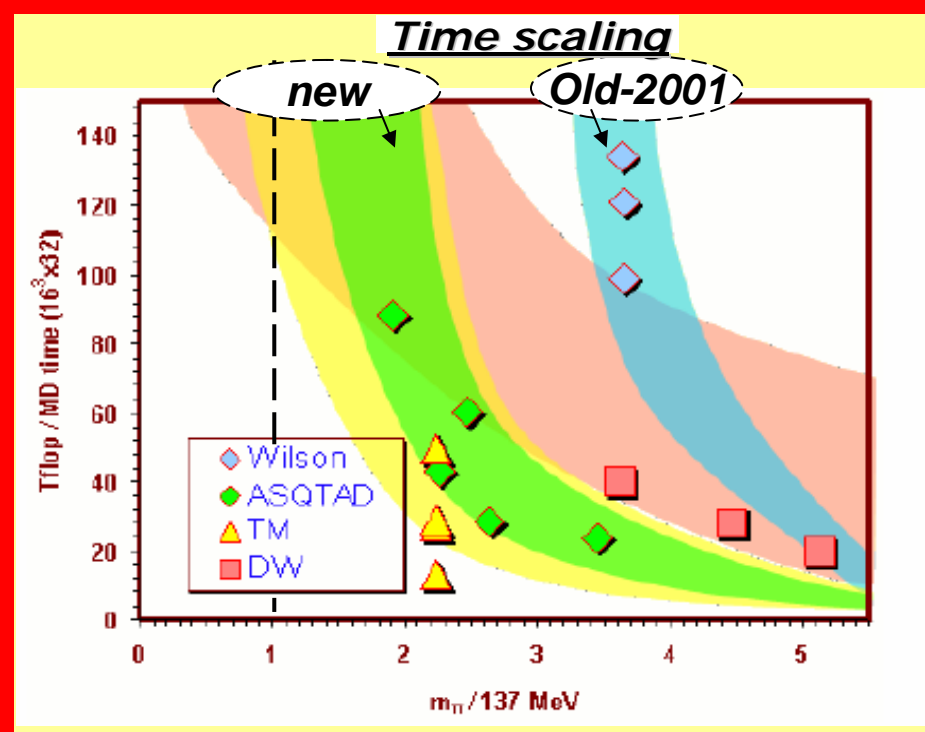
- Domain Wall: *RBC-'06*,
- Staggered: *MILC-2002*,

$m_\pi \sim 280$ MeV
 $m_\pi \sim 280 \rightarrow 250$ MeV
 $m_\pi \sim 190$ MEV
 $m_\pi \sim 156$ MEV
 $m_\pi \sim 290$ MEV

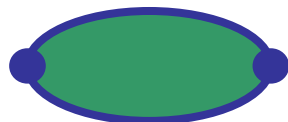
$m_\pi \sim 330$ MEV
 $m_\pi \sim 280$ MeV

$(N_F=2)$
 $(N_F=2 \rightarrow N_F=2+1+1)$
 $(N_F=2+1)$
 $(N_F=2+1)$
 $(N_F=2 \text{ \& } 2+1)$

$(N_F=2+1)$
 $(N_F=2+1)$??



QUENCHED QCD
 $N_F=0$ $m_q^{\text{sea}} \rightarrow \infty$



$N_F=2+1$
 $(m_u+m_d) + m_s$ $m_c^{\text{sea}} \rightarrow \infty$



❖ CPV signals in the B_s sector:

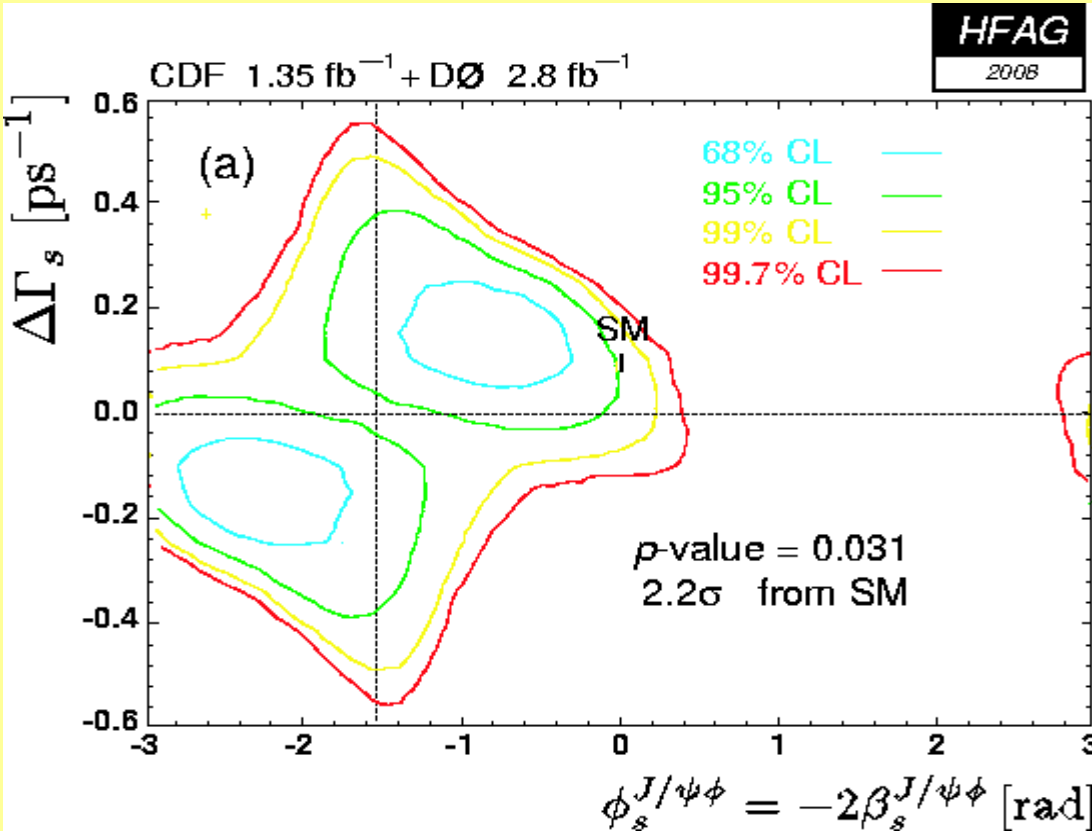
$\beta_s^{MFV} \approx \beta_s^{SM}$



$B_s^- \rightarrow \psi \phi$
 t -dependent CP asymmetries

LHCb

Tevatron



Key observable to kill MFV
2.2σ deviation!

$\phi_s = -2\beta_s$

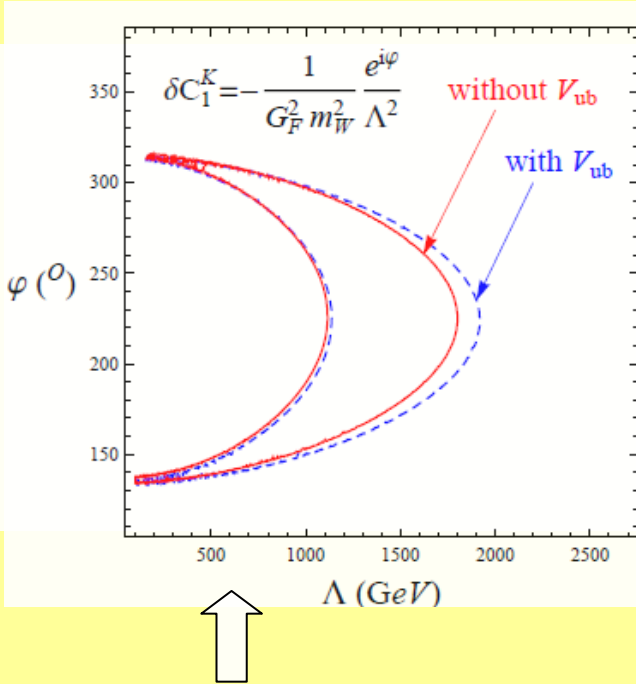
tensions on $\Delta F=2$ observables \Rightarrow upper limit for Λ_{new} ?!

ϵ_K

$$\epsilon_K \propto B_K^* C_{SM} + \frac{\text{Im} A_0}{\text{Re} A_0} = 0.92(2) * B_K^* C_{SM}$$

1. RBC '07-'08; Aubin et al '09 \rightarrow 5%

2. Buras & Guadagnoli 08, 09



68% C.L.

	Operator	Λ (TeV)
K mixing	$O_1^{(K)}$	< 1.9
	$O_4^{(K)}$	< 24
B_s mixing	$O_1^{(d)}$ & $O_1^{(s)}$	$\begin{cases} 1.0 \div 1.4 & \text{no } V_{ub} \\ 1.1 \div 2.0 & \text{with } V_{ub} \end{cases}$

**Lunghi & Soni 09
(Gaussian analysis!!)**

$$\delta \mathcal{H}_{\text{eff}} = - \frac{(V_{tq} V_{tq'}^*)^2}{16 \pi^2} \frac{e^{i \varphi}}{\Lambda^2} O_i$$

ϕ_s

$$B_s \rightarrow \psi \phi$$

t-dependent CP asymmetries

D0 and CDF data: $\phi_s = -0.76^{+0.37}_{-0.33}$
 or $\phi_s = -2.37^{+0.33}_{-0.37}$