



# Test of lepton universality and searches for lepton flavor violation



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(on behalf of **BABAR Collaboration**)

Rencontres de Moriond 2010 – EW session  
La Thuile 6<sup>th</sup>-13<sup>th</sup> March 2010

# Outline

- ✓ New results from **BABAR** on:

**NEW!  
(LaThuile)**

- ✓ Lepton Universality test in  $\Upsilon(1S)$  decays

[arXiv:1002.4358](https://arxiv.org/abs/1002.4358) (sub.PRL)

- ✓ Searches for Lepton Flavor Violation:

- ✓ in  $\tau \rightarrow e\gamma, \mu\gamma$  decays

PRL 104, 021802 (2010)  
[arXiv:0908.2381]

**NEW!!!**

- ✓ in  $\tau \rightarrow 3$  charged leptons decays

[arXiv:1002.4550](https://arxiv.org/abs/1002.4550)(sub.PRD-RC)

**NEW!  
(LaThuile)**

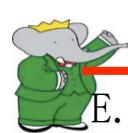
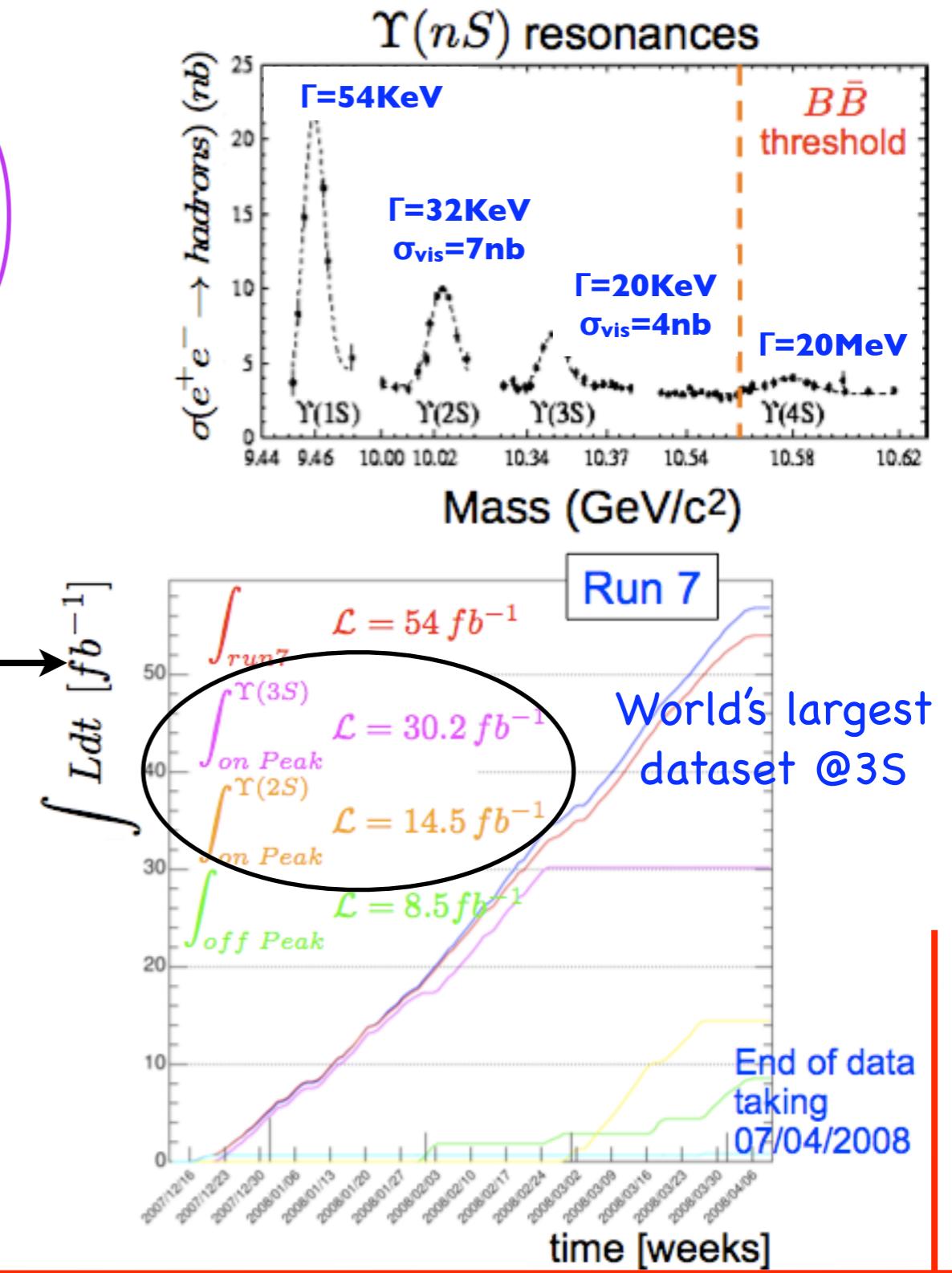
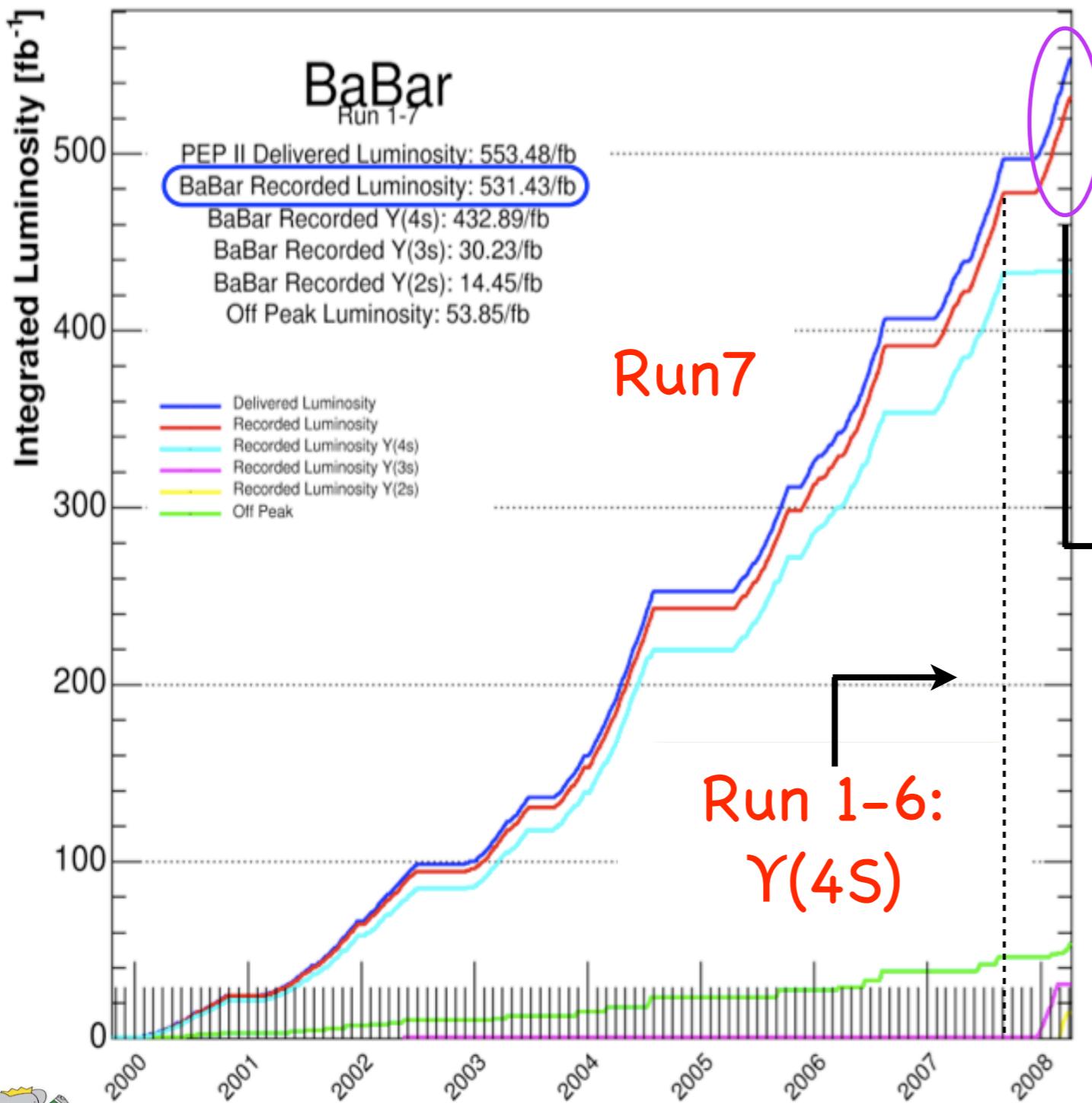
- ✓ in  $\Upsilon(3,2S) \rightarrow e^\pm \tau^\mp, \mu^\pm \tau^\mp$  decays

[arXiv:1001.1883](https://arxiv.org/abs/1001.1883) (sub.PRL)



# BABAR data samples

- ✓ PEP-II asymmetric energy  $e^+e^-$ -collider operating at the  $\Upsilon$  resonances
- ✓ BABAR recorded luminosity



# Lepton Universality Test

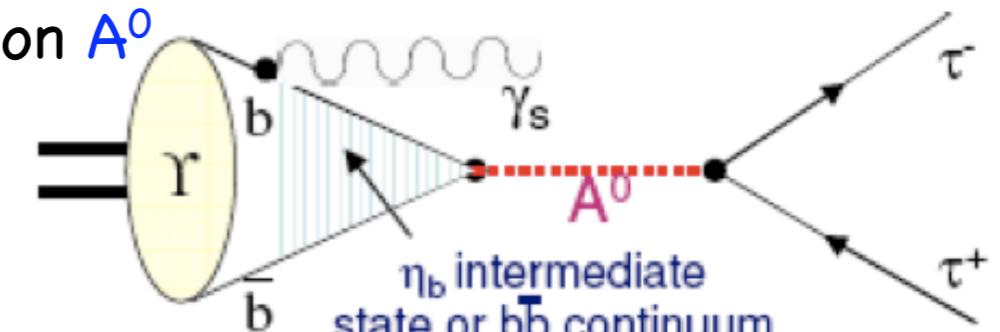
## 1. Theory

[arXiv:1002.4358](https://arxiv.org/abs/1002.4358) (sub. PRL)

- ✓ In the SM couplings between gauge bosons and leptons are independent of lepton flavor
- ✓ SM expectation for  $R_{ll'} = BR(\Upsilon(1S) \rightarrow l^+l^-)/BR(\Upsilon(1S) \rightarrow l'^+l'^-)$  is  $\sim 1$  (except for small lepton-mass effects,  $R_{\tau\mu} \sim 0.992$ )
- ✓ NMSSM: deviations of  $R_{ll'}$  from SM expectation are possible in the hypothesis of existence of a light pseudo-scalar Higgs boson  $A^0$
- ✓  $A^0$  may mediate the decay chain of the  $\Upsilon(1S)$ :

$$\Upsilon(1S) \rightarrow A^0 \gamma, A^0 \rightarrow l^+l^- \quad (1)$$

$$\Upsilon(1S) \rightarrow \eta_b(1S) \gamma, \eta_b(1S) \rightarrow A^0 \rightarrow l^+l^- \quad (2)$$



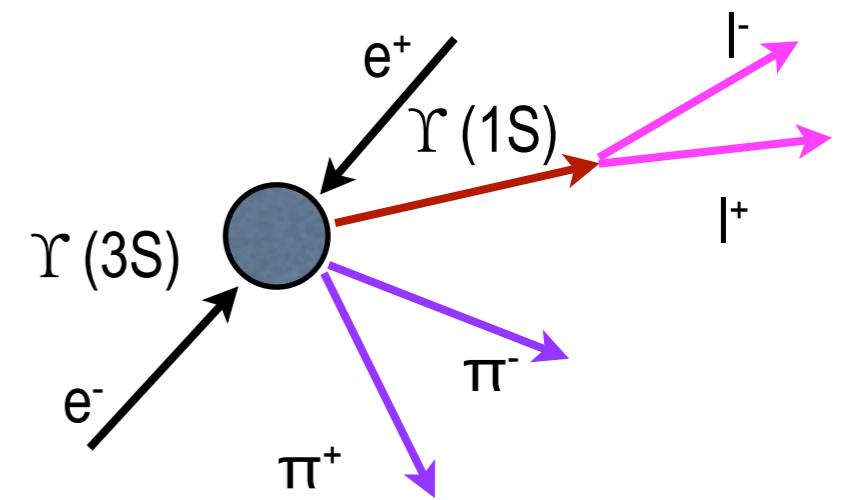
Int.J.Mod.Phys.A19, 2183 (2004);  
PL B653, 67 (2007);  
JHEP 0901, 061 (2009)

- ✓ If the photon is undetected, the lepton pair would be ascribed to the  $\Upsilon(1S)$
- ✓ It can result in a deviation of  $R_{ll'}$  from SM expectation (lepton universality breaking)  $\rightarrow$  NP effect
- ✓ Effect more evident when one of the leptons is a  $\tau$  (up to 4%)  $\rightarrow R_{\tau\mu}$



## 2. Strategy

- ✓  $28 \text{ fb}^{-1}$  of data collected at  $\Upsilon(3S)$  CM energy  $\rightarrow \sim 122 \cdot 10^6 \Upsilon(3S)$
- ✓ Tag  $\Upsilon(1S)$  exploiting  $\Upsilon(3S) \rightarrow \Upsilon(1S)\pi^+\pi^-$ ,  $\Upsilon(1S) \rightarrow \tau^+\tau^-$  and  $\mu^+\mu^-$  events:
  - ✓  $\text{BF}(\Upsilon(3S) \rightarrow \Upsilon(1S)\pi^+\pi^-) \sim 5\%$
  - ✓ select  $\tau$  1-prong decays
  - ✓ 4-charged tracks final state topology
- ✓ Any number of extra photons allowed
- ✓ Separate selections for  $\Upsilon(1S) \rightarrow \tau^+\tau^-$  and  $\mu^+\mu^-$  events
- ✓ Bkg:  $q\bar{q}$  events,  $\tau$ -pairs, QED events,  $\Upsilon(1S)$  generic decays
- ✓ A multivariate analysis approach in  $\tau^+\tau^-$  channel
- ✓ Signal extraction efficiencies (estimated on MC simulations):



$\epsilon_{\mu\mu} \sim 45\%$   
 $\epsilon_{\tau\tau} \sim 17\%$



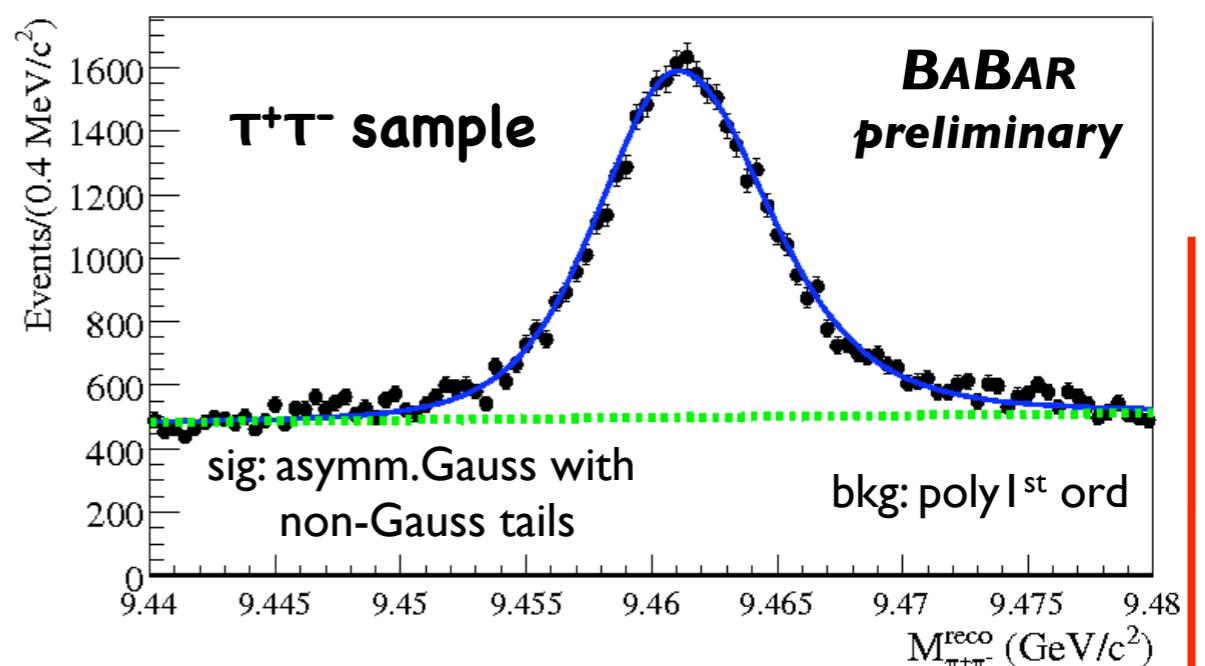
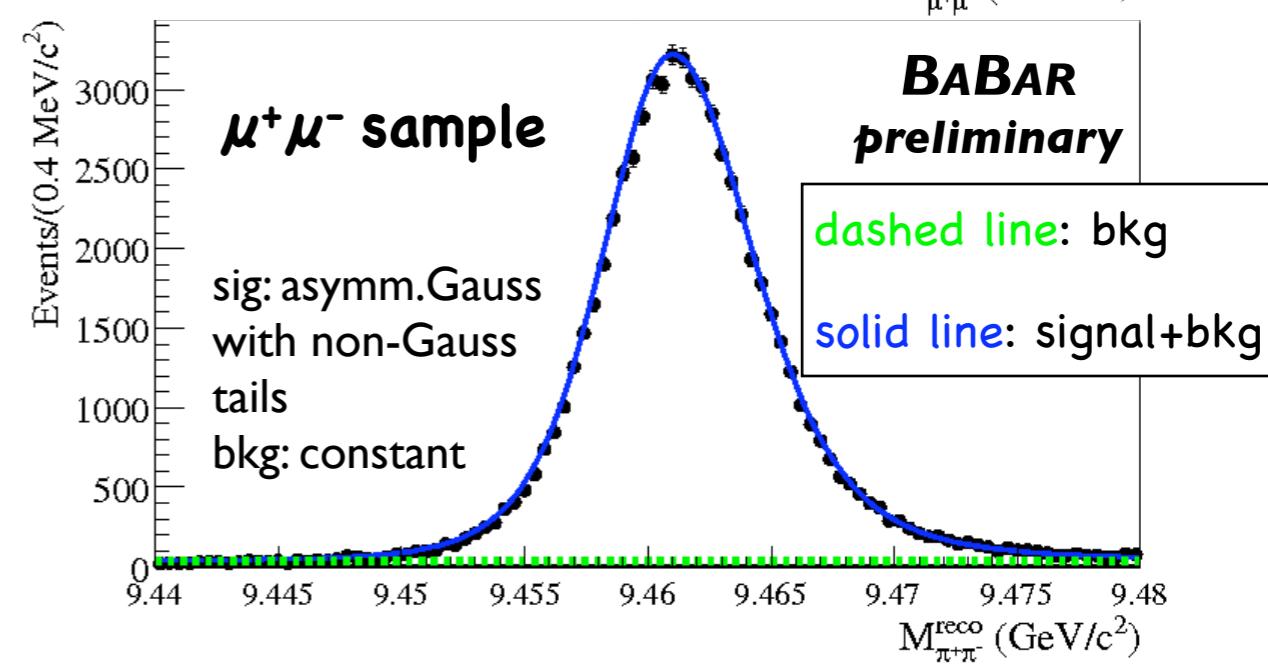
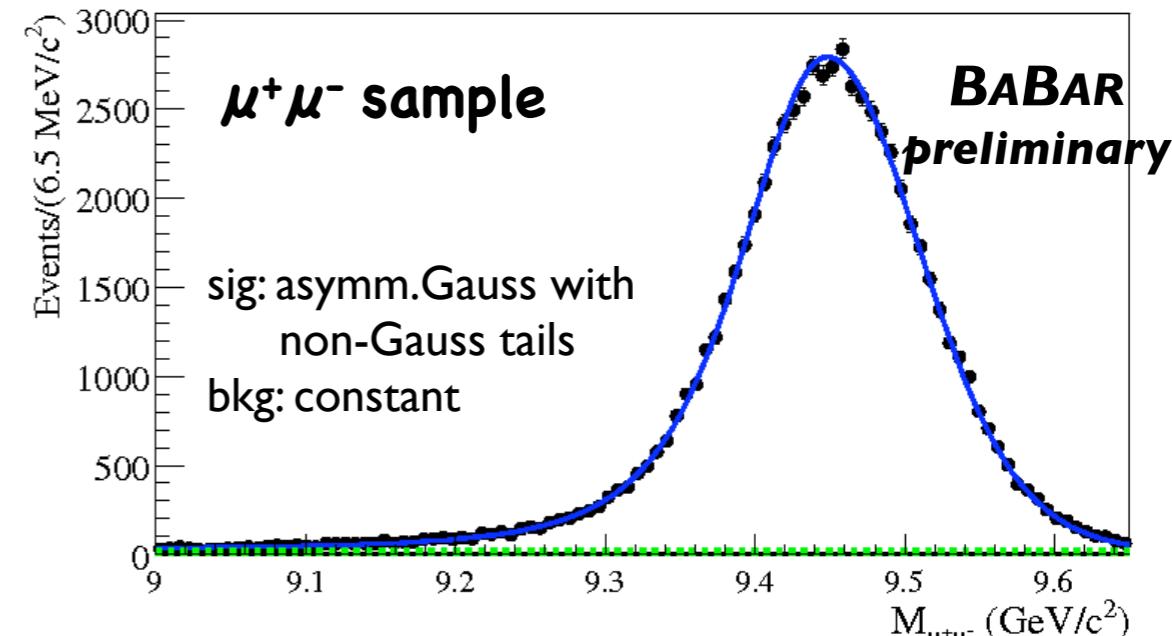
### 3. Signal extraction

- ✓ Extended and unbinned maximum-likelihood fit:
- ✓ in  $\mu^+\mu^-$  channel a 2-dim likelihood based on  $M_{\pi^+\pi^-}^{\text{reco}}$  and  $M_{\mu^+\mu^-}$
- ✓ in  $\tau^+\tau^-$  channel a 1-dim likelihood based on  $M_{\pi^+\pi^-}^{\text{reco}}$

$M_{\mu^+\mu^-}$  invariant  $\mu^+\mu^-$  mass

$$M_{\pi^+\pi^-}^{\text{reco}} = \sqrt{s + M_{\pi^+\pi^-}^2 - 2 \cdot \sqrt{s} \cdot \sqrt{M_{\pi^+\pi^-}^2 + p_{\pi^+\pi^-}^{*2}}}$$

- ✓ PDFs chosen from a data sub-sample (~1/10 of the total), then discarded
- ✓ Fit performed simultaneously to the 2 datasets
- ✓  $R_{\tau\mu}$  returned



### 3. Results

- ✓ Correction for known differences between data and simulation efficiencies
- ✓ Systematic uncertainty contributions (up to 2.2%):
  - ✓ event selection efficiency
  - ✓  $\mu$  identification
  - ✓ trigger efficiency
  - ✓ imperfect knowledge of signal and bkg shapes
  - ✓ peaking background yield

**$R_{\tau\mu}(\Upsilon(1S)) : 1.005 \pm 0.013 \text{ (stat.)} \pm 0.022 \text{ (syst.)}$**

**BABAR**  
**preliminary**

#### 1. Significant improvement in precision

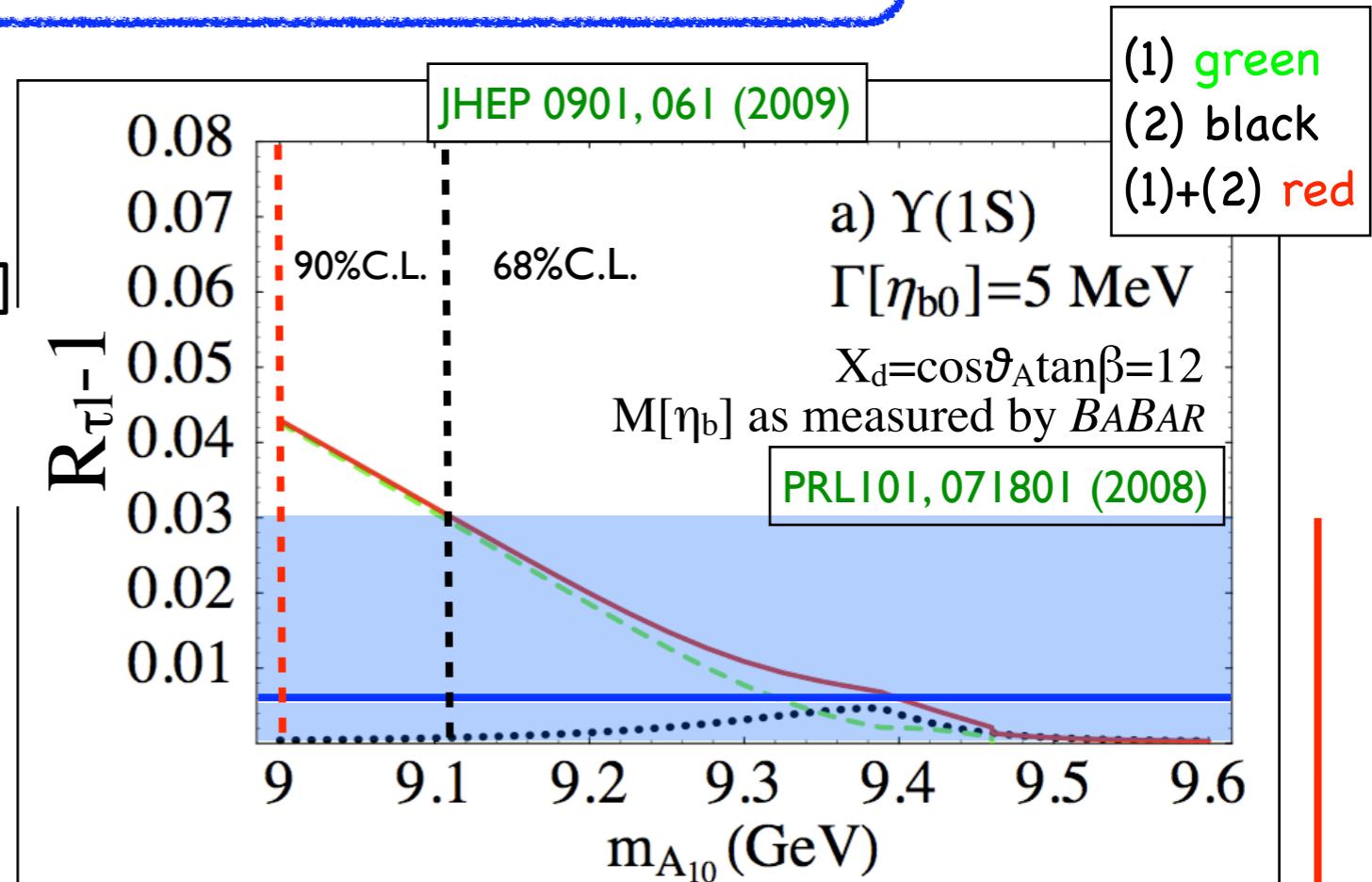
[Previous best result by CLEO:

$$R_{\tau\mu}(\Upsilon(1S)) : 1.02 \pm 0.02 \text{ (stat.)} \pm 0.05 \text{ (syst.)}$$

PRL98, 052002 (2007)

#### 2. No significant deviations w.r.t. SM expectations ( $R_{\tau\mu}(\Upsilon(1S)) \sim 0.992$ )

#### 3. Excluded $m(A^0) < 9 \text{ GeV}/c^2$ @90% C.L.



# Searches for charged LFV

## Theory

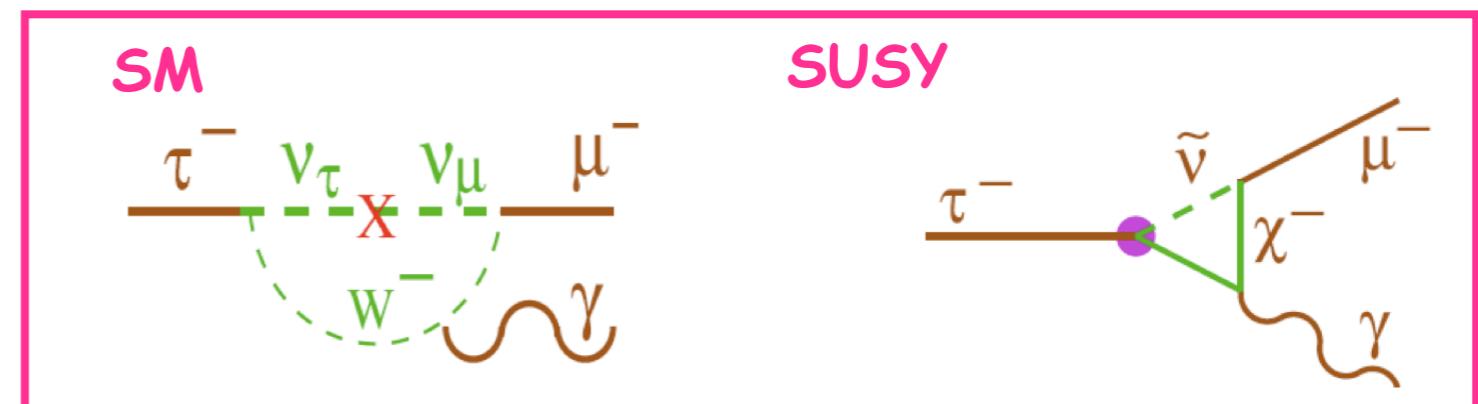
- ✓ In the SM with  $\nu$ -masses oscillation LFV can occur
- ✓ Never observed in processes involving **charged** LFV (tree-level contribution suppressed by  $(\Delta m_\nu^2/M_W^2)^2 \lesssim 10^{-48}$  to undetectable levels)
- ✓ Enhancements close to experimental sensitivity ( $\text{BR} \sim \mathcal{O}(10^{-8})$ ) in many extensions of the SM
- ✓ Search for charged LFV in:



# Searches for charged LFV

## Theory

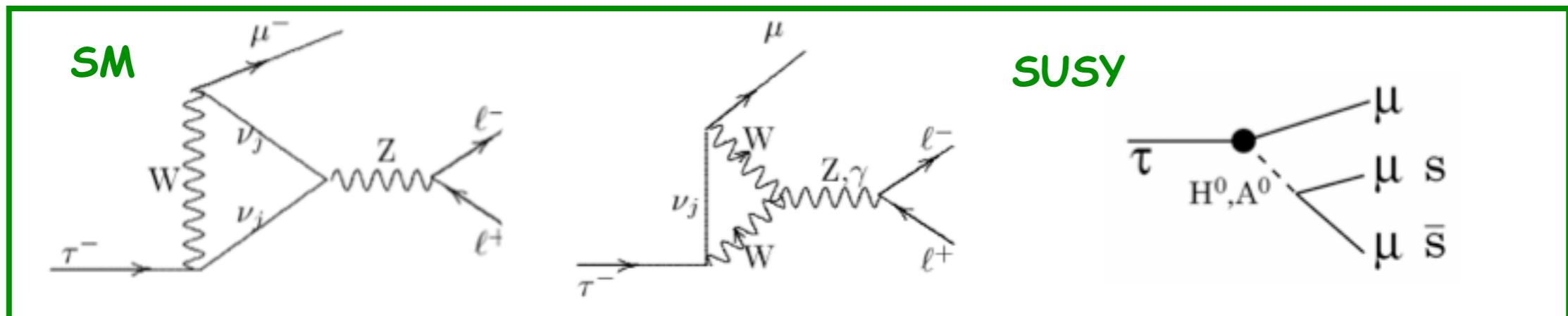
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  - ✓  $\tau \rightarrow l \gamma$  decays:



# Searches for charged LFV

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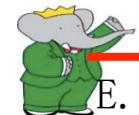
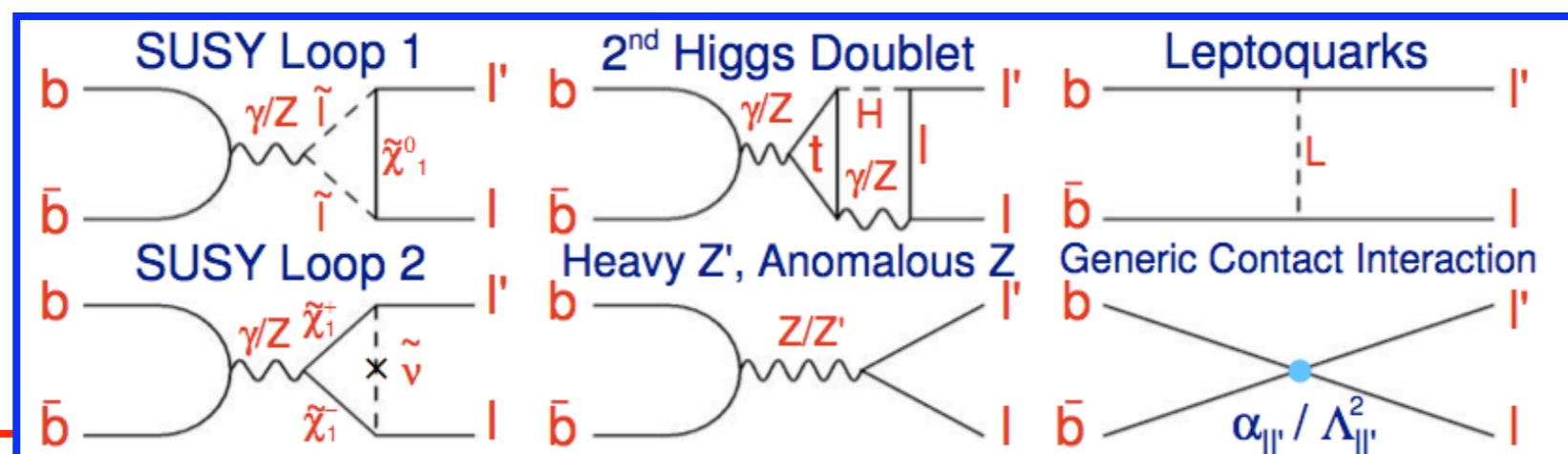
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  - ✓  $\tau \rightarrow l \gamma$  decays
  - ✓  $\tau \rightarrow 3l$  decays:



# Searches for charged LFV

## Theory

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- ✓ Search for charged LFV in:
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  - ✓  $\tau \rightarrow 3l$  decays
  - ✓  $\gamma \rightarrow ll'$  decays:

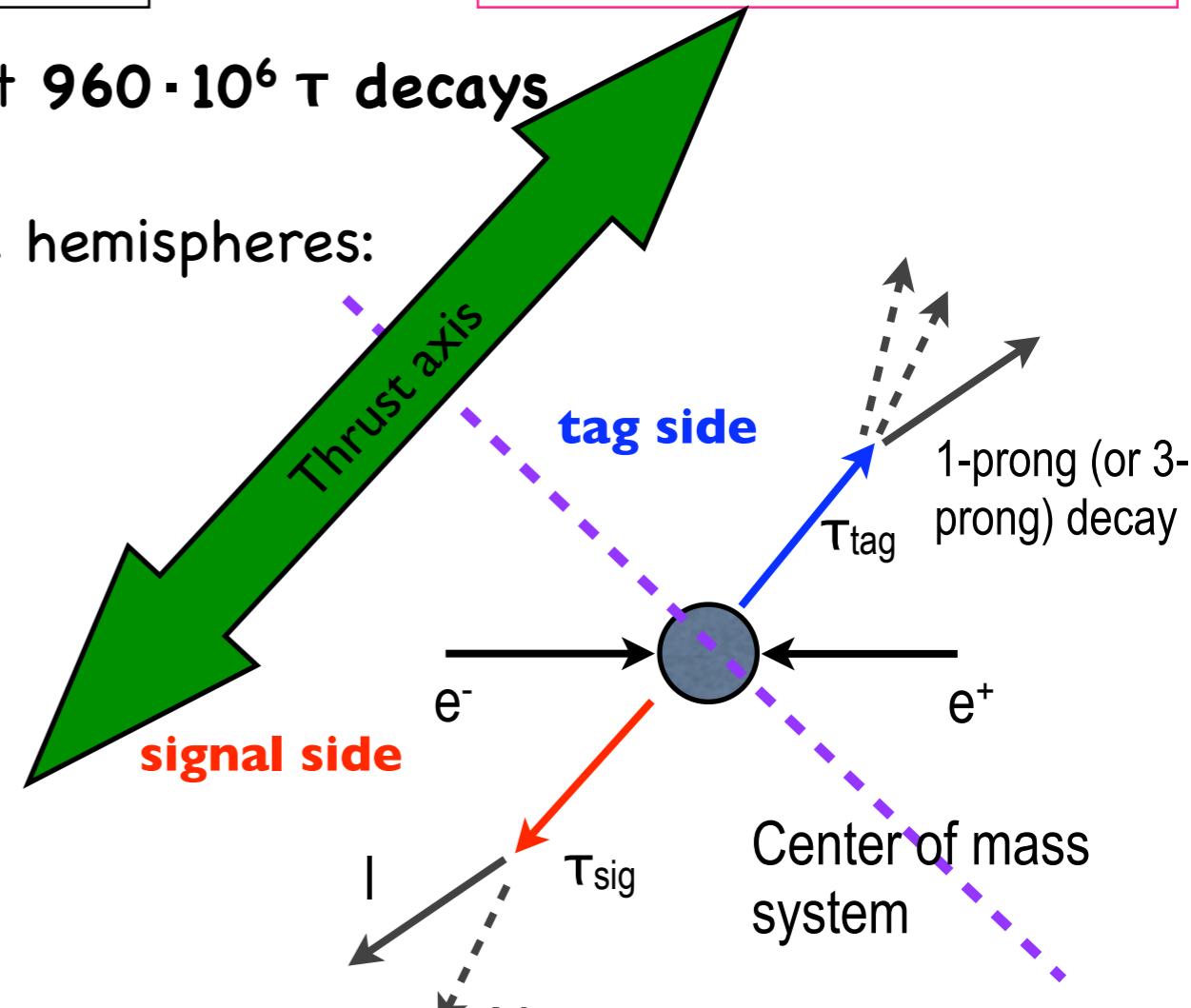


# LFV in $\tau^\pm \rightarrow e^\pm / \mu^\pm \gamma$

$\sigma(e^+e^- \rightarrow b\bar{b}) @ Y(4S) \sim 1.05 \text{ nb}$   
 $\sigma(e^+e^- \rightarrow \tau^+\tau^-) @ Y(4S) \sim 0.92 \text{ nb}$   
 $\text{BR}(Y(3,2S) \rightarrow \tau^+\tau^-) \sim 2\%$

## 1. Strategy

- ✓ BABAR is a  $\tau$ -factory as well: a total of about  $960 \cdot 10^6 \tau$  decays
- ✓ Reconstructed events  $e^+e^- \rightarrow \tau^+\tau^-$ , divided in 2 hemispheres:
- ✓ **SIGNAL side**: -  $l^\pm\gamma$  pair:  $M(l^\pm\gamma) \sim M_\tau$   
 $E(l^\pm\gamma)_{CM} \sim \sqrt{s}/2$   
- only 1  $\gamma$  with  $E(\gamma)_{CM} > 1 \text{ GeV}$   
- 1 track with  $p_{CM} < 0.77\sqrt{s}/2$   
identified as an  $e$  or a  $\mu$   
-  $\gamma$  and  $l$  back-to-back in  $\tau$ -rest frame  
 $\rightarrow$  boosted:  $\cos\theta_{\gamma l} < 0.786$
- ✓ **TAG side** (expected to contain a SM  $\tau$ -decay):  $\tau \rightarrow 1$  or 3 charged tracks
  - $e$ -tag,  $\mu$ -tag,  $\pi$ -tag, 3h-tag
  - different selections (neural networks approach) for each tag
- ✓ Backgrounds:  $\tau$ -pairs (irreducible),  $e^+e^-\gamma/\mu^+\mu^-\gamma$ , hadronic  $\tau$  decays with  $\pi$  mis-id



## 2. Results

- ✓ Signal extraction:  $\Delta E = E(l\gamma)_{CM} - \sqrt{s}/2$
- and  $m_{EC}$  (beam energy-constrained  $\tau$  mass)
- ✓ Signal reconstruction efficiency: 4% (6%) for  $\tau \rightarrow e\gamma$  ( $\tau \rightarrow \mu\gamma$ ) final states
- ✓ Fraction of expected bkg from fits to the Fit Box
- ✓ Number of events in the  $2\sigma$  signal ellipses compatible with bkg expectations
- ✓ Systematic errors: tracking, PID and trigger and bkg filters efficiencies; track momentum and photon energy and resolution in the signal side
- ✓ **Upper limits @ 90%C.L.:**

$$\mathcal{B} (\tau^\pm \rightarrow e^\pm \gamma) < 3.3 \times 10^{-8}$$

$$\mathcal{B} (\tau^\pm \rightarrow \mu^\pm \gamma) < 4.4 \times 10^{-8}$$

**Previous:**

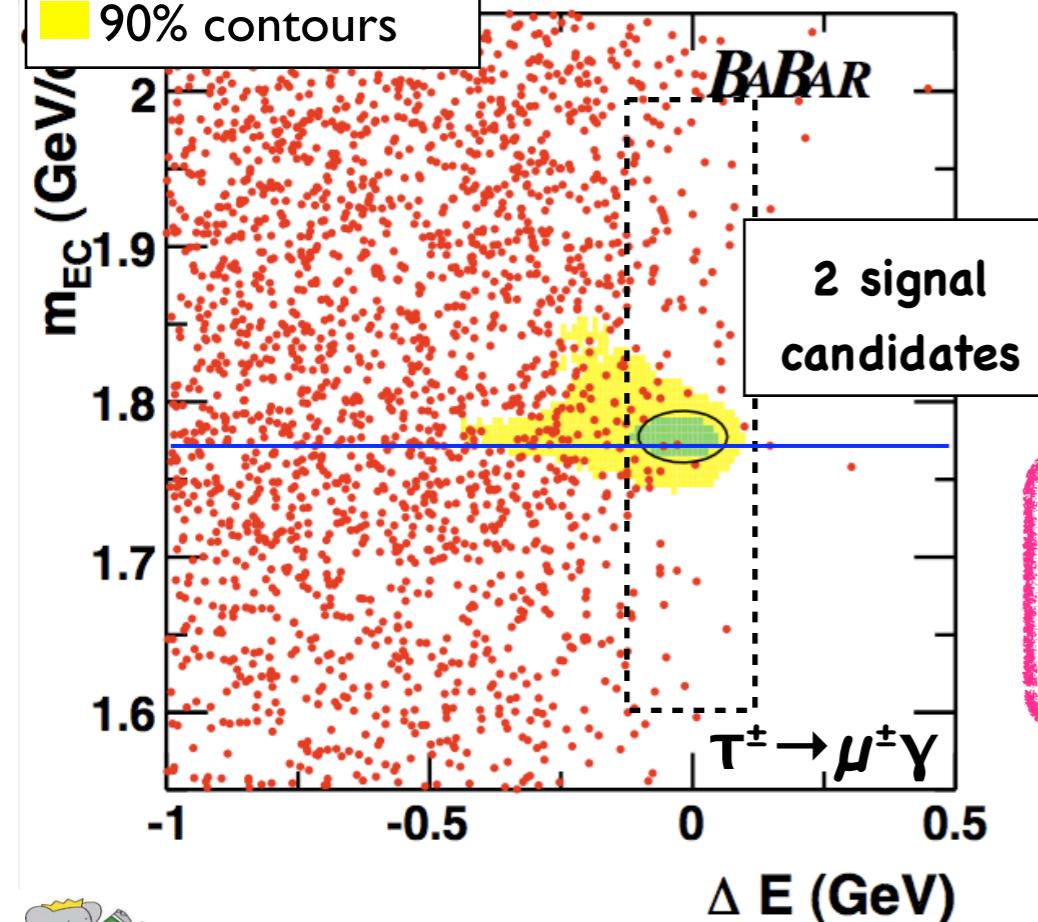
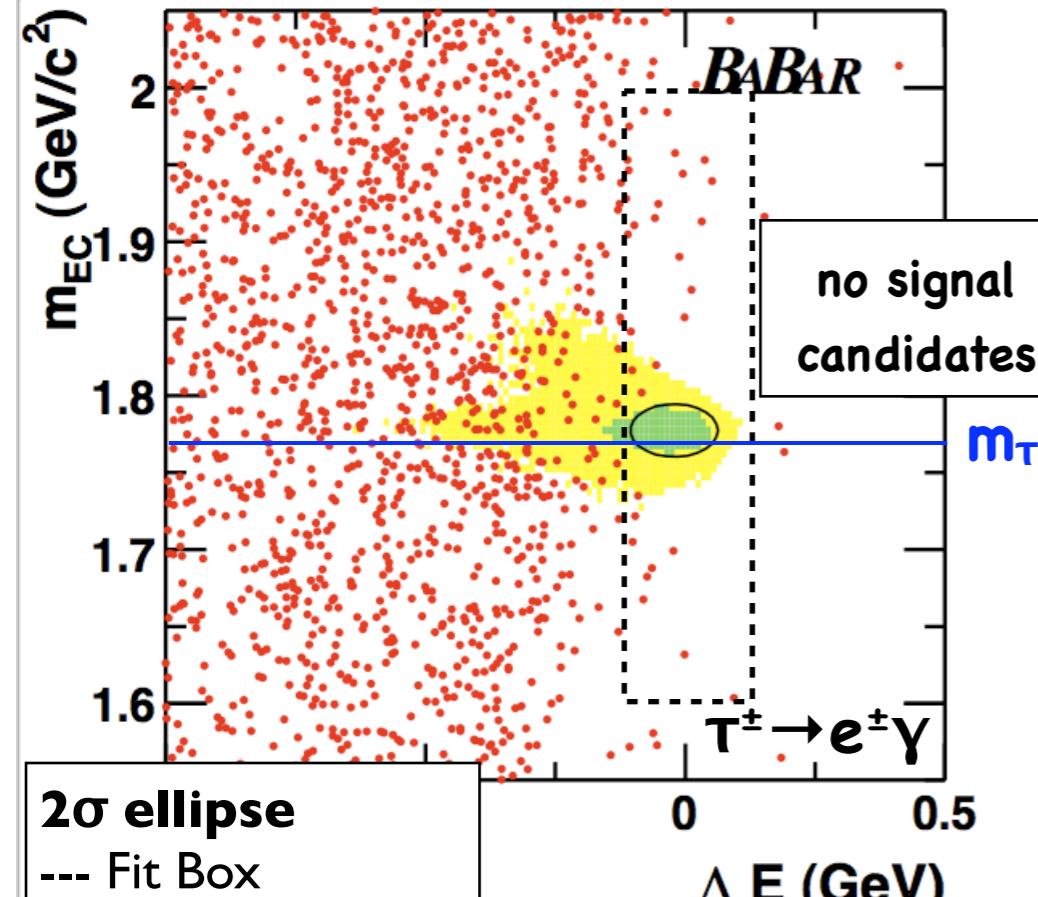
$$1.1 \times 10^{-7} \text{ (BABAR)}$$

PRL96, 041801 (2006)

$$4.5 \times 10^{-8} \text{ (Belle)}$$

PL B666, 16 (2008)

The most stringent limits on LFV in these decays



# LFV in $\tau^- \rightarrow 3$ charged leptons

arXiv:1002.4550 (sub. PRD-RC)

## 1. Strategy

✓ Run 1-6 data ( $\Upsilon(4S)$ )  $\rightarrow 430 \cdot 10^6 \tau$ -pairs

✓ 6 channels studied:

$\tau^- \rightarrow e^- e^+ e^-$   
 $\tau^- \rightarrow \mu^- e^+ e^-$   
 $\tau^- \rightarrow e^- \mu^+ e^-$   
 $\tau^- \rightarrow \mu^- \mu^+ e^-$   
 $\tau^- \rightarrow \mu^- e^+ \mu^-$   
 $\tau^- \rightarrow \mu^- \mu^+ \mu^-$

✓ 4 charged tracks and zero net charge

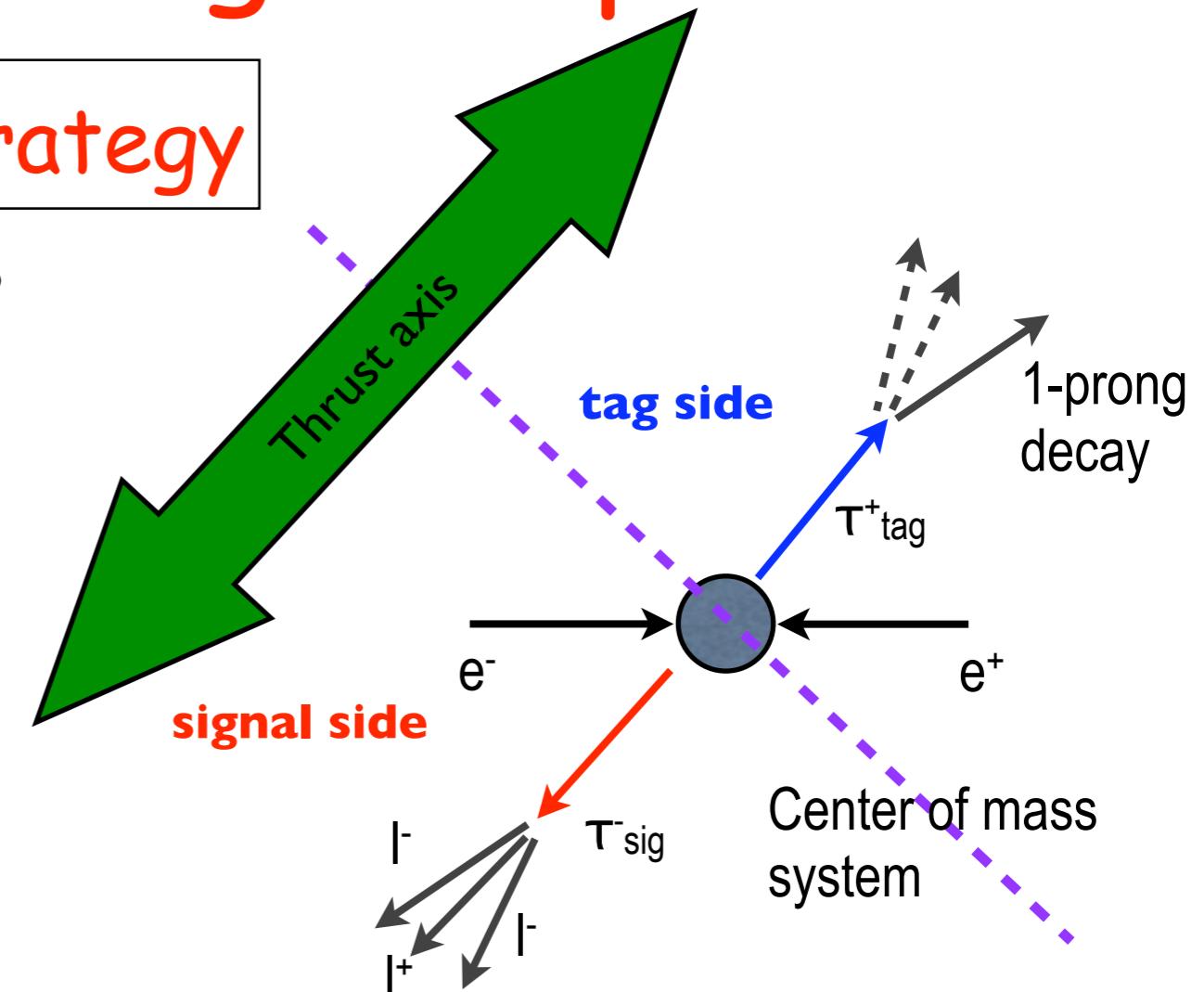
✓ **SIGNAL**: 3 charged particles, identified as  $e$  or  $\mu$ , with  $M(3l) \sim M_\tau$  and  $E(3l)_{CM} \sim \sqrt{s}/2$

✓ **TAG**:  $\tau \rightarrow 1$  prong decays

✓ PID used in suppressing backgrounds:

- $q\bar{q}$  events
- QED events (Bhabha and  $\mu^+ \mu^-$  pairs)
- SM  $\tau^+ \tau^-$  decays

✓ Further selection criteria, partially common to all the channels, partially channel-dependent



## 2. Results

- ✓ Expected selection efficiencies:  
6-13% depending on the channel considered

- ✓ Signal extraction:  $\Delta E = E(3l)_{CM} - \sqrt{s}/2$   
and  $\Delta M_{EC} = M_{EC} - m_\tau$

- ✓ Systematic uncertainties due to PID (dominant), tracking efficiency, errors in bkg estimation

### Upper limits @ 90%C.L.:

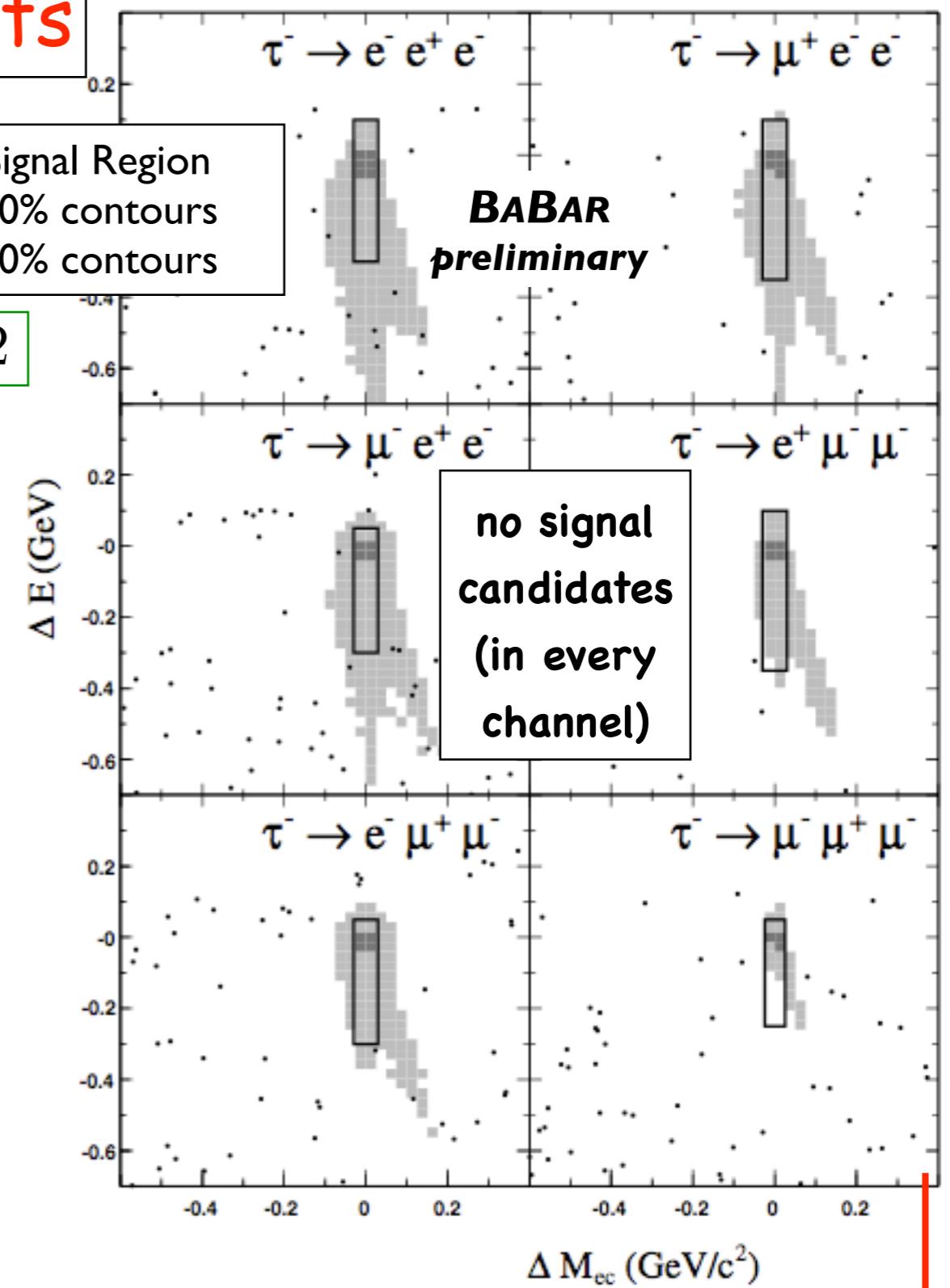
Channel	UL@90%C.L. ( $\cdot 10^{-8}$ )	
	BABAR	Belle
$e^-e^+e^-$	2,9	2,7
$\mu^-e^+e^-$	2,2	1,8
$e^-\mu^+e^-$	1,8	1,5
$\mu^-\mu^+e^-$	3,2	2,7
$\mu^-e^+\mu^-$	2,6	1,7
$\mu^-\mu^+\mu^-$	3,3	2,1
$\tau$ -pairs ( $\cdot 10^6$ )	430	719

✓ Significant improvement wrt previous BABAR result

PRL95, 251803 (2007)

✓ Competitive with Belle result, even with a smaller statistics

arXiv:1001.3221 (sub.PLB)



[Resolution different among channels (worst in e channels); radiative losses, tracking resolution.]



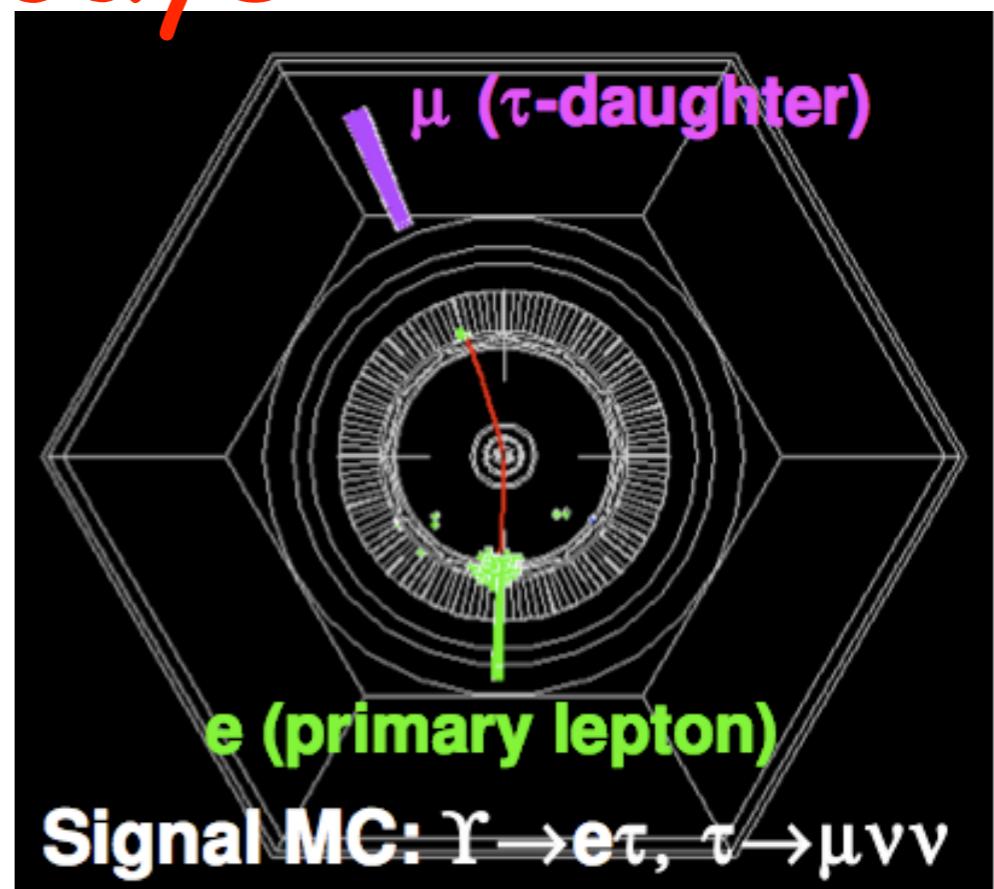
# LFV in $\Upsilon$ decays

[arXiv:1001.1883](https://arxiv.org/abs/1001.1883) (sub.PRL)

## 1. Strategy

- ✓ Search for  $\Upsilon(nS) \rightarrow l^\pm \tau^\mp$  with  $n=2,3$  and  $l=e,\mu$
- ✓  $27 \text{ fb}^{-1}$  of data collected at  $\Upsilon(3S)$  CM energy  
 $\rightarrow \sim 117 \cdot 10^6 \Upsilon(3S)$
- ✓  $14 \text{ fb}^{-1}$  of data collected at  $\Upsilon(2S)$  CM energy  
 $\rightarrow \sim 99 \cdot 10^6 \Upsilon(2S)$
- ✓ Signature:
  - 1 primary lepton ( $e$  or  $\mu$ )
  - 1  $\tau$  detected through a leptonic ( $\mu$  or  $e$ ) or hadronic ( $\pi^\pm + \pi^0$ ) decay

Process	$\tau$ decay	Channel
$\Upsilon(3,2S) \rightarrow e\tau$	$\tau \rightarrow \mu\nu\nu$	leptonic $e\tau$
$\Upsilon(3,2S) \rightarrow e\tau$	$\tau \rightarrow \pi^\pm \pi^0 \nu / \pi^\pm \pi^0 \pi^0 \nu$	hadronic $e\tau$
$\Upsilon(3,2S) \rightarrow \mu\tau$	$\tau \rightarrow e\nu\nu$	leptonic $\mu\tau$
$\Upsilon(3,2S) \rightarrow \mu\tau$	$\tau \rightarrow \pi^\pm \pi^0 \nu / \pi^\pm \pi^0 \pi^0 \nu$	hadronic $\mu\tau$



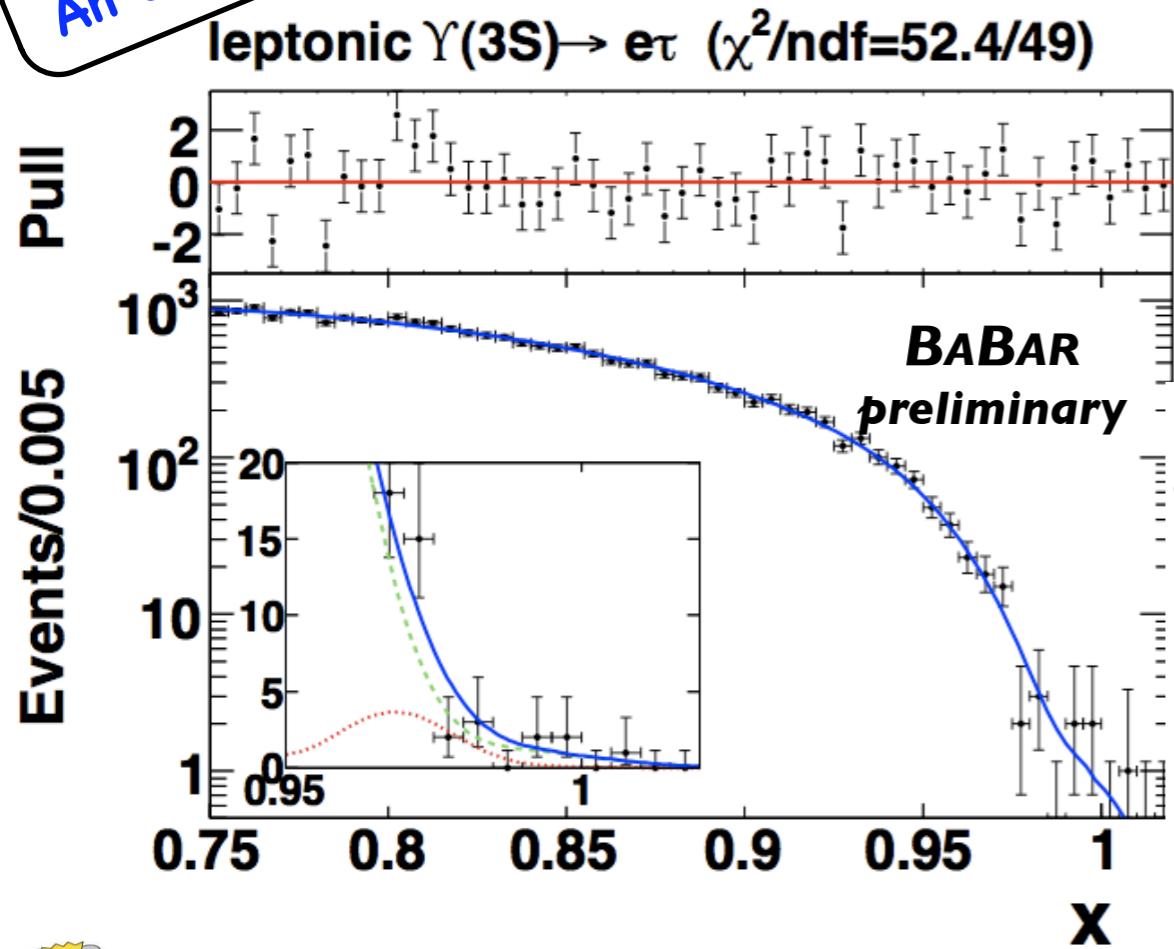
- ✓ Background events:
  - Bhabha and  $\mu$ -pair (and mis-ID)
  - $\tau$ -pair
  - multiple  $\pi$  and additional  $\gamma$
- ✓ Selection partially common to the 4 channels, partially channel-specific (PID,  $\tau$ -daughter kinematics)



## 2. Signal extraction and results

- ✓ Discriminating variable:  $x = \text{primary lepton momentum}/\text{beam energy}$
- ✓ Unbinned extended maximum-likelihood fit
- ✓ PDFs chosen for:
  - signal (peaks at  $x=x_{\text{MAX}} \sim 0.97$ ) → from extracted signal yields, BR calculated
  - $\tau$ -pair bkg (smooth, endpoint at  $x_{\text{MAX}}$ )
  - Bhabha/ $\mu$ -pair bkg (peaks at  $x \sim 1$ )
  - hadron bkg (smooth, endpoint at  $x_{\text{MAX}}$ )

An example of fit:

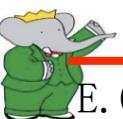


$$\mathcal{B} = N_{\text{SIG}} / (\epsilon_{\text{SIG}} \times N_{\Upsilon(nS)})$$

Systematics uncertainties (mainly from PDF shapes) and corrections applied

PRL101, 201601 (2008)

	$\mathcal{B} (10^{-6})$	$\text{UL} (10^{-6})$	Improvement factor
$\mathcal{B}(\Upsilon(2S) \rightarrow e^\pm \tau^\mp)$	$0.6^{+1.5+0.5}_{-1.4-0.6}$	< 3.2	first!
$\mathcal{B}(\Upsilon(2S) \rightarrow \mu^\pm \tau^\mp)$	$0.2^{+1.5+1.0}_{-1.3-1.2}$	< 3.3	5.5
$\mathcal{B}(\Upsilon(3S) \rightarrow e^\pm \tau^\mp)$	$1.8^{+1.7+0.8}_{-1.4-0.7}$	< 4.2	first!
$\mathcal{B}(\Upsilon(3S) \rightarrow \mu^\pm \tau^\mp)$	$-0.8^{+1.5+1.4}_{-1.5-1.3}$	< 3.1	3.7



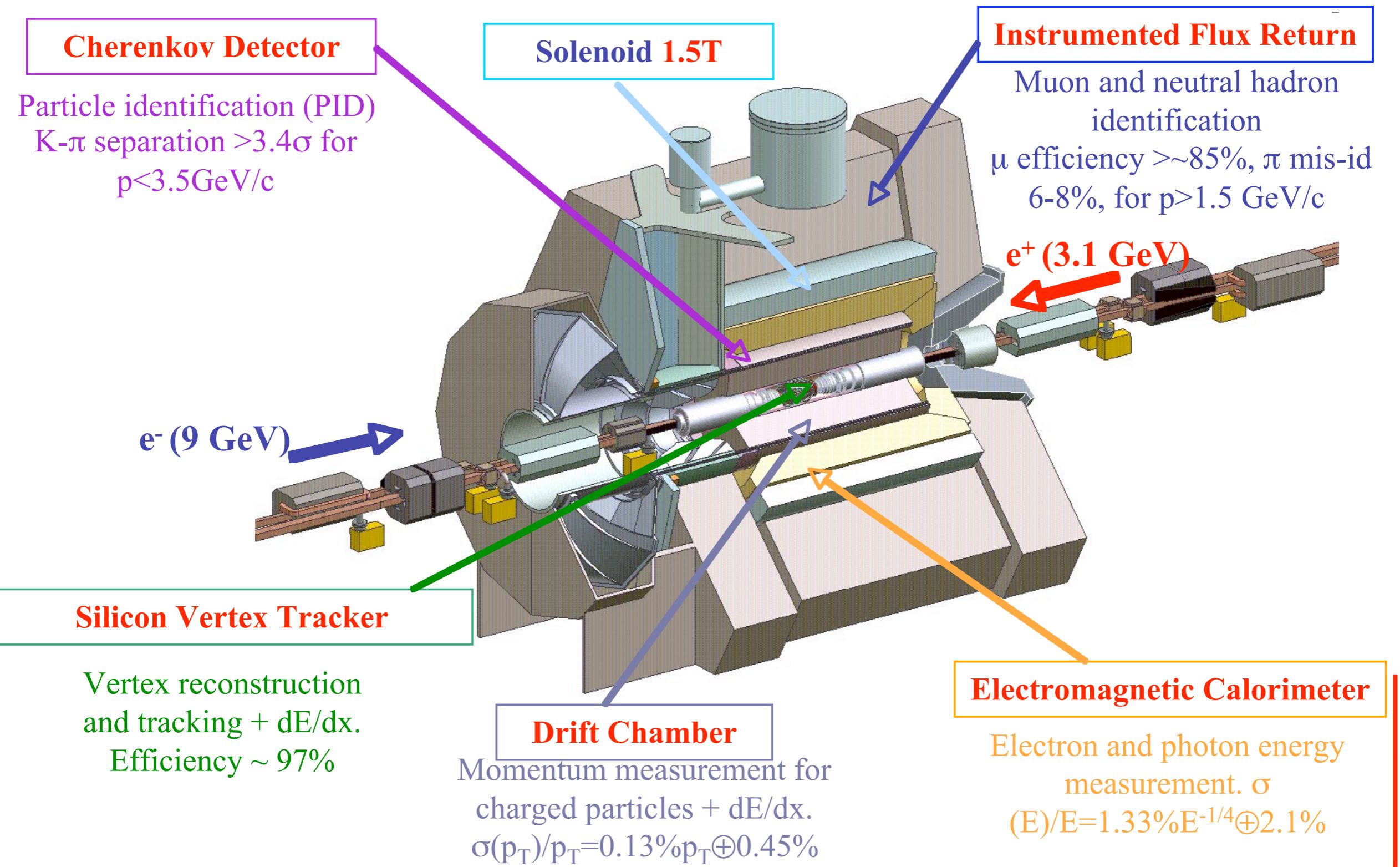
# Conclusions

- ✓ BABAR data are a rich harvest for several important and different precision tests on the SM and beyond
- ✓ Now finalizing most of the analyses using the full dataset at  $\Upsilon(4S)$  energy
- ✓  $\Upsilon(3S)$  and  $\Upsilon(2S)$  datasets give important results too
- ✓ Recent results on:
  - ✓ Lepton Universality in  $\Upsilon(1S)$  decays
  - ✓ LFV searches in  $\tau$  and  $\Upsilon$  decays
- ✓ BABAR results are now able to dialogue with theoretical limits and able (or near) to exclude some foreseen parameters' space regions for several models



**BACKUP SLIDES**

# The BABAR detector



# Lepton Universality Test

- ✓ Likelihood written as:

$$\mathcal{L}_{ext} = \mathcal{L}_{ext}^\mu \cdot \mathcal{L}_{ext}^\tau, \quad \mathcal{L}_{ext}^i = \frac{e^{-N'_i}(N'_i)^{N_i}}{N_i!} \prod_{k=1}^{N_i} \mathcal{P}_k^i$$

$$\mathcal{P}_k^\mu \equiv \frac{N_{sig\mu}}{N'_\mu} \mathcal{P}_k^\mu(M_{\pi^+\pi^-}^{reco}) \cdot \mathcal{P}_k^\mu(M_{\mu^+\mu^-}) + \frac{N_{bkg\mu}}{N'_\mu} \mathcal{P}_k^{bkg\mu}(M_{\pi^+\pi^-}^{reco}) \cdot \mathcal{P}_k^{bkg\mu}(M_{\mu^+\mu^-})$$

$$\mathcal{P}_k^\tau \equiv \frac{\epsilon_{\tau\tau}}{\epsilon_{\mu\mu}} \frac{N_{sig\mu}}{N'_\tau} R_{\tau\mu} \mathcal{P}_k^\tau(M_{\pi^+\pi^-}^{reco}) + \frac{N_{bkg\tau}}{N'_\tau} \mathcal{P}_k^{bkg\tau}(M_{\pi^+\pi^-}^{reco})$$

- ✓ Asymmetric Gaussian with non-Gaussian tails functional form:

$$\mathcal{F}(x) = \exp \left\{ - \frac{(x - \mu)^2}{2\sigma^2(L, R) + \alpha(L, R)(x - \mu)^2} \right\}$$

- ✓ Summary of systematic uncertainties:

	$\mu^+\mu^-$	$\tau^+\tau^-$
event selection	1.2%	
PID	1.2%	—
Trigger	0.18%	0.10%
BGF	negl.	negl.
PDFs parameters	1.1%	
Bkg PDF	0.22%	
Agreement $\mu^+\mu^-$ vs. $\tau^+\tau^-$ in <i>MassPiPiReco</i>	0.6%	
Peaking bkg	—	0.4%
MC statistics	0.08%	0.09%
<b>TOTAL</b>	<b>2.2%</b>	
<i>Corrections to efficiency:</i>		
PID	1.023	—
Trigger	—	1.020
<i>Corrections to signal yield:</i>		
Peaking bkg	—	0.996



# LFV in $\tau$ decays

- ✓ NP models for  $\tau \rightarrow e/\mu\gamma$  and  $\tau \rightarrow lll$  decays:

		$\tau \rightarrow \mu\gamma$	$\tau \rightarrow lll$
<b>SM + <math>v</math> mixing</b>	Lee Shrock, PRD 16 (1977) 1444 Cheng Li, PRD 45 (1980) 1908	UNDETECTABLE	UNDETECTABLE
<b>SUSY Higgs</b>	Dedes Ellis Raidal, PLB 549 (2002) 159 Brignole Rossi, PLB 566 (2003) 517	$10^{-10}$	$10^{-7}$
<b>SM + heavy Maj. <math>v_R</math></b>	Cvetic Dib Kim Kim, PRD 66 (2002) 034008	$10^{-9}$	$10^{-10}$
<b>Non-universal <math>Z'</math></b>	Yue Zhang Liu, PLB 547 (2002) 252	$10^{-9}$	$10^{-8}$
<b>SUSY SO(10)</b>	Masiero Vempati Vives, NPB 649 (2003) 189 Fukuyama Kikuchi Okada, PRD 68 (2003) 033012	$10^{-8}$	$10^{-10}$
<b>mSUGRA + SeeSaw</b>	Ellis Gomez Leontaris Lola Nanopoulos, EPJ C14 (2002) 319 Ellis Hisano Raidal Shimizu, PRD 66 (2003) 115013	$10^{-7}$	$10^{-9}$



✓ Systematics for  $\tau \rightarrow e/\mu\gamma$  decays:

Systematic Influence on the Signal Efficiency	$\tau^\pm \rightarrow e^\pm\gamma$	$\tau^\pm \rightarrow \mu^\pm\gamma$
(i) Trigger and BGFilter efficiency	1.3	1.0
(ii) Tracking reconstruction efficiency	0.4	0.4
(iii) Neutral cluster reconstruction efficiency	1.8	1.8
(iv) PID error associated with electron/muon selectors	2.3	2.7
(v) Modeling of the variables entering the NN	2.7	1.8
(vi) Signal Track and photon energy scale & resolution: vary $(\Delta E, m_{EC})$ mean, rms independently	6.4	6.2
(viii) Beam energy scale and spread: anti-correlated $(\Delta E, m_{EC})$ shift $(\pm 2, \mp .8)$ MeV	0.7	0.7
(viii) Normalization uncertainty	0.7	0.7
(ix) Model dependence	0.1	0.2
Total	7.7	7.4
Total (without signal box variation)	4.3	4.0

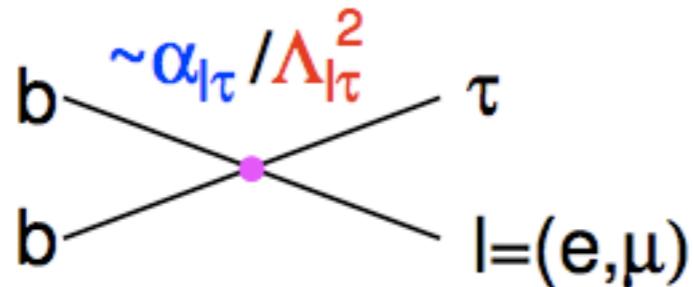
Table 15: Relative Systematic errors (%) associated with the signal efficiency.



# LFV in $\Upsilon$ decays

- ✓ NP constraint using effective field theory:

CLFV  $\Upsilon$  decays:  $b\bar{b}l\tau$  contact interaction with NP coupling constant and mass scale



$$\frac{\alpha_{l\tau}^2}{\Lambda_{l\tau}^4} = \frac{\text{BF}(\Upsilon(3S) \rightarrow l\tau)}{\text{BF}(\Upsilon(3S) \rightarrow ll)} \frac{2q_b \alpha^2}{(M_{\Upsilon(nS)})^4} \quad l = (e, \mu)$$

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$$\alpha_{e\tau} = 1 \rightarrow \Lambda_{e\tau} > 1.6 \text{ TeV}$$

(previously 1.4 TeV)

