ALPs and WISPs – Illuminating Hidden Worlds

Light Shining Through a Wall Axion Like & Any Light Particle Searches WISP Search in Lab. Experiments

K. Ehret – ALPS Collaboration, DESY XLVth Rencontres de Moriond - EW La Thuile, March 12th, 2010

Outline

Illuminating Hidden Worlds

Particle Physics at Lowest Energies

- Axions a Brief Introduction
- ALPs and WISPs
- Direct WISP Search:
 - Experimental Challenges Small Signals
 - □ Setups Light Shining Through a Wall
- ALPS Experiment at DESY
- Preliminary Results ALPS I
- Steps Towards Astrophysical Bounds

Conclusions

see also talk by Malcolm Fairbairn



Reminder: QCD Axion

Experiments show that QCD conserves C·P!

- \Box size of C•P violation in QCD described by angle Θ
- □ Missing electric dipole moment of neutron: Θ < 10⁻⁹
- CP Conservation explained by Axion
 - additional U(1) chiral symmetry (Peccei-Quinn, 1977) predicts a new particle
 - Wilczek and Weinberg noticed 1978 oscillation of Θ constitutes an axion-field
 - name introduced by Wilczek Axion "cleans" QCD (like the detergent)
 - □ Axion: very light & couples very weakly
- Axion remains not only as
 - □ a solution to the CP conservation of QCD,
 - □ but also as a candidate for Dark Matter.





Dark Matter could be Axions!



H. Baer, presentation at 5th Patras Workshop on Axions, WIMPs and WISPs, 2009

A QCD axion in the mass region of 10⁻⁵ to 10⁻⁴ eV would be a "perfect" cold Dark Matter candidate

The axion was not invented to solve the Dark Matter problem!

There could be axion even if they are not Dark Matter!

Many hints from astrophysics to new physics in the sub-eV region (cf. Malcolm Fairbairn's talk)

new physics @ low energy frontier

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From Axions to ALPs and WISPs

String Theory tells: There might be much more than a QCD axion.

Axions and ALPs, hidden sector photons, mini-charged particles occur naturally in string-theory motivated extensions of the Standard Model

WISPs: Weakly Interacting Sub-eV Particles

- Scalar or pseudoscalar particles: "axion-like particles" ALPs exploit the Primakoff effect
- Neutral vectorbosons: "hidden sector photons" HP mixing with "ordinary" photons.

□ Minicharged particles (MCP, about 10⁻⁶ e): "loop effects".



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Is there new Physics at low Energies?

Experiments with intense laser beams providing very high photon number fluxes or extremely good control of beam properties.

Indirect WISP search: search for polarization effects



Recent worldwide interest and activities triggered and inspired by the (non confirmed) **PVLAS observation** – change of laser light polarization in magnetic field

A. Ringwald "Particle Interpretations of the PVLAS Data" arXiv:0704.3195

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Direct WISP Search – Light Shining Through a Wall (LSW)

 γ^*

LSW: search for "invisible" ALPs (& other WISPs) in lab experiments

- cross-check of indirect searches,
- determination of properties of new particles
- access to WISPs not detectable in indirect searches



$$P_{\gamma \to \phi \to \gamma} = P_{\gamma \to \phi}(B_1, l_1, q_1) P_{\phi \to \gamma}(B_2, l_2, q_2)$$

 $P_{\gamma \to \phi}(B, l, q) = \frac{g^2}{4} B^2 L^2 \frac{\sin^2(qL/2)}{(qL/2)^2}$

$$q = \frac{m_{\phi}^2}{2E_{\gamma}} \qquad P_{\gamma \to \phi \to \gamma} \sim g^4$$



Okun 1982, Skivie 1983, Ansel'm 1985, Van Bibber et al. 1987

Low conversion probability <10⁻²³:

- high photon fluxes (intensive laser)
- strong magnetic field (for ALP)
- very sensitive detector (SPC)

Limits on ALPs



Mainly from Astrophysics (lifetime of Stars, MBR), BFRT, ...

Some WISP parameter regions only accessible in lab exp.

Theory starts to develop predictions for WISPs to be confirmed be experiment!



 $M_{MSN} \sim \alpha \ / \ (\pi g) \ \cdot \ O(1)$

In the "hidden sector" models the existing limits probe messenger masses at TeV to PeV scales!



World-wide activities in this research field

Experiment	Reference	$\Delta \theta$	ψ	LSW
ALPS (DESY/D) "Axion-Like Particle Search"	arXiv:0905.4159	×	×	~
BFRT (BNL-Fermilab-Rochester-Trieste)	Phys.Rev. D47 (1993)	~	~	~
BMV (LULI/F) Biréfringence Magnétique du Vide"	Phys.Rev.Lett. 99 (2007) Phys.Rev.D 78 (2009)	×	~	~
GammeV (Fermilab/USA) Gamma to meV particle search"	Phys.Rev.Lett. 100 (2008) Phys.Rev.Lett. 102 (2009)	×	×	~
LIPSS (Jefferson Lab/USA) 'Light Pseudoscalar or Scalar particle Search"	Phys.Rev.Lett. 101 (2008) arXiv:0810.4189	×	×	~
OSQAR (CERN/CH) Optical Search for QED vacuum magnetic birefrin- ence, Axions and photon Regeneration"	Phys.Rev.D 78 (2008)	×	×	~
PVLAS (INFN/I) Polarizzazione del Vuoto con LASer"	Phys.Rev.Lett. 96 (2006) Erratum-ibid. 99 (2007) Phys.Rev.D 77 (2008)	~	r	(••)
Q&A (Hsinchu/Taiwan) QED & Axion"	Mod.Phys. A22 (2007)	~	×	×

0 1 1 1

M. Ahlers, presentation at the 5th Patras Workshop on Axions, WIMPs and WISPs, 2009

LIPSS@JLab

prelim results



BFRT - finished in 1993

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ALPS @ DESY Hamburg



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ALPS @ DESY

January 2007: Letter of Intent published -> ALPS approved May 2007: dedicated funding for ALPS, decision for green 532 nm laser Phase 0: study of systematic, stability, alignment and sensitivity 2008: set-up off an optical cavity commissioning run – demonstrating the feasibility of resonant laser power build-up in ALPS (NIM A doi:10.1016/j.nima.2009.10.102) Collaboration with gravitational wave community essential 2009: upgrade of system (resonant SHG, cavity in vacuum, detector)

physics data run with vacuum and gas

Collaboration

- DESY
- Hamburger Sternwarte (Observatory)
- Laser Zentrum Hannover
- Max Planck Institute for Gravitational Physics (Albert Einstein Institute)



ALPS Experiment at DESY

Axion Like Particle Search



photon regeneration experiment using a HERA Dipole Magnet >axion like particles ALP



ALPS Experiment at DESY

Any Light Particle Search



photon regeneration experiment using a HERA Dipole Magnet

- ➤axion like particles ALP
- massive hidden sector photons HP
- minicharged particles MCP



ALPS Experiment at DESY

Laser

Magnet B1 = B2 = 5.16 T

Detector



- \Box Primary and secondary γ have same properties
- □ Rate of re-converted photons (for ALP) ~ (B·I)⁴
- only one magnet can be used ->experimental challenge:
 - mirror and absorber in the middle of the magnet
 - no direct access possible



Setup: Beam Tube, Mirror & Detector

two beam tubes – one from each side: removable & vacuum tight (10⁻⁷ mbar)

- 1. laser tube (generation side):
 - windows on both sides
 - adjustable mirror in middle
- 2. detector tube (regeneration part):
 - removable wall on inner side
 - open for alignment purpose
 - window on outer side



precise remote mirror steering inside magnet (@ 5 Tesla and vacuum) adopted piezo based squiggle motors



high sensitivity, low noise **CCD camera** PI - **PIXIS:1024BL**

- •liquid cooling circulator at -70°
- •13 µm square pixel, 1024 * 1024
- •eff 95 % at 532 nm
- •dark current 0.001 e-/pixel/sec
- •low readout noise: 3.8 e-/pixel
- •beam spot focused on 3*3 pixel
- •stability after removal < 10 μm
- •reference beam optional guided to camera





Setup: Laser System

- > power & time structure (pulsed): Nγ
- > polarization: 0+ and 0- ALP
- > experimental constraints: very good beam properties
- eLIGO Laser System: narrow linewidth master-oscillator power amplifier system:
 - 1064 nm
 - provides 35 W CW
 - high frequency stability (1 MHz / min)

resonant second harmonic generation

- with resonant cavity around nonlinear crystal to maximize output
- output: up to 4,6 W high quality 532 nm green laser light

optical Fabry Perot resonator (cavity) in generation part (laser tube)

- coherent superposition enlarges light field between mirrors
- power buildup PB=Pcirc/Pin
- single-mode emitting cw laser needed!



Optical Resonator - Cavity

- Phase of light must reproduce itself aftereach roundtrip
 - cavity length must be stable in time length
 - changes of pm degrade PB
- Stabilization onto resonance
 - use sign change of phase
 - Pound-Drever-Hall readout scheme
- Power buildup governed by
 - internal losses (esp. windows)
 - ALPS cavity completly inside vacuum
 - mirror transmission
- Locking of cavity by adjusting frequency of IR 1064nm laser
 - adopting IR laser MOPA (with piezo)
 - Length noise 500 times larger than laser frequency noise!
 - cavity locked on fundamental mode







Power buildup inside cavity. Transmission of second mirror is 300ppm





Resonant Photon Generation



Successful and stable operation of a resonant cavity in the generation part! & resonant second harmonic generation Achieved a power build up of 300

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Resonant Photon Generation





95 % confidence level – method of Feldman

detection probability $< 1 / 10^{24}$

>

and Cousins

2009 Data Analysis, Selection and Sensitivity

- ✤ around 50h of beam time recorded several 100h of dark frames
- looking for enhancement in "signal" region (defined by beam spot) compared to dark frames.
- check for cosmics or other spurious activity remove about 10% of data frames from analysis
- the analysis is performed for each pixel a 11.11 grid
- test the CCD and the data analysis with a photon beam of extremely low intensity around 10 mHz







0.580

 6.599 ± 0.735

0.6012 ± 0.3325

3.66



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Entries Mean



Signal-Dark

ALPS: Preliminary Results for the Vacuum Data

> ALPS is the most sensitive experiment for WISP searches in the laboratory. For axion-like particles, ALPS probes physics at the "multi-10-TeV scale"!





A new Method to extend the Mass Range

> The coherent phenomena probed at ALPS induce regions of insensitivity.

$$P = \left(\frac{g^2}{4} B^2 L^2 \frac{\sin^2(qL/2)}{(qL/2)^2}\right)^2$$

with $q = p_{\gamma} - p_{\phi}$, L = length of B field



- > They originate from $q \cdot L = (p_{\gamma} p_{\Phi}) \cdot L = 2m \cdot \pi$
- > Idea: change photon momentum p_{γ} by a small amount of gas: $p_{\gamma (gas)} = p_{\gamma} \cdot \sqrt{1+2(n-1)}$, where *n* denotes the refraction index.
- > We apply this approach by taking data with a pressure of 0.18 mb of Argon in the laser and detector beam tubes.



Preliminary Results for the Argon Data

> Gaps in sensitivity for axion-like particles are closed!



ALPS is now in the forefront of lab experiments searching for WISPs



Outlook

> The world-wide activities in this research field are strengthening, but there is still a way to go!



- Increase sensitivity for lower couplings
- > Laser (power + optical cavity)
- Magnet (field strength + length)
- > Detector sensitivity
- Measurement time / statistics

 will not really help: g~t^{-1/8}
 Factor 2 if one measures one year (256 days) instead of one day!

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Prospects of direct WISP Searches - Towards lower Couplings

Laser (flux of incoming photons) in tight magnet bore:

✤ AL	.PS at present:	3 W 532 nm (enhanced LIGO), cavity with power built up of 300	1 kW
✤ AL	.PS II:	100 W 532/1064 nm (advanced LIGO), cavity with power built up of 1000	100 kW
OS	SQAR proposal:	1kW 1064 nm (Nd-YAG), cavity with power built up of 10.000	10,000 kW
Mag	net (interaction	probability):	
✤ A	LPS at present:	$\frac{1}{2} + \frac{1}{2}$ HERA dipole,	
		B = 5 T, I = 4.2 m	21 Tm
♦ C	SQAR proposal:	1+1 LHC, dipoles	
		B = 9.7 T, I = 14.3 m	140 Tm
♦ L	arger scale exp:	6 + 6 Tevatron dipoles	180 Tm
		6 + 6 HERA dipoles	280 Tm
		2 + 2 LHC dipoles	300 Tm
		4 + 4 LHC dipoles	600 Tm
••• ••	dreams"		





Prospects of direct WISP Searches - Towards lower Couplings

Detector sensitivity:

- •ALPS at present: PIXIS 1024B few mHz
- •"kind-of-limit": radioactivity, CR in 20·20 μm² signal region at ALPS about 0.02 mHz
 - may be reached e.g. with TES (single photon counting)
 - or with heterodyne detection scheme

Reach relative to ALPS in 2009 (g=10⁻⁷GeV⁻¹):

- > Laser (power + optical cavity):100
- > Magnet (field strength + length):15
- > Detector sensitivity: 200

Physics:

$$g = 2 \cdot (BI)^{-1} \cdot (P_{\gamma \to \phi \to \gamma})^{-4}$$

= g_{ALPS} · (15)⁻¹·(100·200)⁻⁴

$$= g_{ALPS} / 200$$

≈ 5·10⁻¹⁰GeV⁻¹



 $m_{\phi}[eV]$



A possible Scenario for ALPS II

> Still a way to go!





A possible Scenario for ALPS I

> Invest into more powerful magnets.





A possible Scenario for ALPS II

> Increase laser power from 1 kW to 150 kW, add single photon detector.





Prospects of direct WISP Searches - Towards lower Couplings

Ingenuity in addition to "brute force":

"Resonantly enhanced Axion-Photon Regeneration"

P. Sikivie, D.B. Tanner, Karl van Bibber. Phys.Rev.Lett.98:172002,2007.

(also <u>F. Hoogeveen</u>, <u>T. Ziegenhagen</u>, DESY-90-165, Nucl.Phys.B358)



Implementation of a second cavity in the regeneration part of the experiment to enhance the conversion probability WISP \rightarrow photon

Increase power output by finesse of cavity: 10⁴ seems to be possible.

There are different ideas and proposals under discussion



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A possible Scenario for ALPS II

> Include a second resonator in the detector tube behind the wall.





A possible Scenario for ALPS I

- it looks feasible to build a lab experiment which reaches a sensitivity beyond the actual limits coming from astrophysics (within a few years)
- > at that time: new results from lab-experiments, astrophysics and LHC





Conclusions

- Growing worldwide interest and effort in low energy particle physics theory and experiment.
- WISP searches in the laboratory are complementary to astrophysics experiments.
- LSW experiments: direct WISP search
- ALPS success based on a close collaboration of particle physicists (theory and experiment), laser physicists from the gravitational wave detector community and an "accelerator" lab
- ALPS has set up an optical resonant in the generation part of the LSW experiment power buildup of 300 achieved
- ALPS provides the most stringent laboratory constraints on WISPs
- Based on this experience, future large scale LSW experiments are feasible which surpasses present day limits from astrophysics – ALPS II
- Finding the QCD axion remains a challenging target.



Outlook

- WISP search in the lab is complementary to High Energy activities and astrophysics – probe of models (String theory motivated) – potential to make significant contributions
- > hopefully there are many discoveries in the next years which helps to solve open questions of particle physics

Next (6th) Patras Workshop: Zurich

Juli 5 – July 9, 2010 Annual Workshop on Axions, WIMPs and WISP



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Backup Slides



Resonantly enhanced Axion-Photon Regeneration

There are different ideas and proposals



"Detailed design of a resonantly-enhanced axionphoton regeneration experiment" G. Mueller, P. Sikivie, D. B. Tanner and K. v.Bibber 10.1103/PhysRevD.80.072004

Use two lasers with offset in frequency to allow for a heterodyne detection scheme.



Setup under consideration for ALPS II

- IR 1064 nm for WISP production
- SHG 532nm for locking of 2. cavity
- single photon detector e.g. TES



Laser System

Laser - γ parameters:

- Energy of photons determines ϕ mass reach
- Power & time structure (pulsed): N γ
- Polarization: 0+ and 0- ALP
- experimental constraints: very good beam properties

Avoid diffractive losses

> small aperture in beam tube

=> σ < 12 mm

> propagation of beam inside laser tube

Focus Spot Size

- secondary photons focused on small spot (detector)
- > same properties as laser beam
- focus spot size comparable to pixel size of digital cameras

 $\sigma_{
m m}$

$$\sigma(z) = \sigma_0 \cdot \sqrt{\frac{z^2 \cdot \lambda \cdot M^2}{\pi \cdot \sigma_0^2 / 4}}$$
$$M^2 = \sigma_0 \cdot \Theta \cdot \frac{\pi}{\lambda}$$

focus spot size.

$$_{\rm in} = \frac{\lambda \cdot f \cdot M^2}{\pi \cdot \sigma}$$



Without Magnets: Searching for hidden Photons





Only laboratory experiments searching for massive hidden sector photons might close the gap in the meV mass region! Same laser and detector technology, but no magnets needed. Only long straight vacuum

tubes!



Search for massive Photons

"Light shining through a wall" without external fields:

(like neutrino oscillations).

Principle of an experiment:

$$\gamma \xrightarrow{\phi} \xrightarrow{\phi} \xrightarrow{\phi} \gamma$$

$$length L_1 \qquad length L_2$$

$$P_{reconv.} = 16\chi^4 \cdot [sin(qL_1/2) \cdot sin(qL_2/2)]^2$$

Experimental requirements very similar to searches for axion-likes, but:

- no magnetic field,
- UHV conditions.
- (kinetic mixing)



Indirect WISP Search Experiments

> PVLAS at Leagnaro, Italy

- high finesse Fabry-Perot cavity
- upgrade plans
- also direct search plans
- > Q&A in Taiwan
 - ongoing
 - sensitivity comparable to PVLAS
- > BMV at Toulouse (France)
 - starting, test of QED prediction of ellipticity
 - also direct search experiments
- > OSQAR at CERN (using two LHC dipoles)
 - starting, test of QED prediction
 - also direct search experiments



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LSW Experiments

Experiment	Lasersystem	Magnet	
ALPS@DESY	532 nm, cw Optical Resonator	HERA sc Dipol B=5,2T, I=9m	2mHZ CCD
BFRT@Brookhaven	Optical delay line	2* 4,4m 3,7T	Finished in 1993 limits on existence of WISPs
BMV@Toulouse	6·10 ²³ photons, 1060 nm, 82 pulses	4.4 + 4.4 Tm 0,37m – 12,3T pulsed	0.5 Hz ongoing, limits published
GammeV@FNAL	6·10 ²³ photons, 532 nm, 5Hz pulses	Tevatron Magnet 6m - 5T	0.01 mHz PM - ongoing, limits published - most sensitive limits on WISPs until 2009
LIPSS@JLab	6·10 ²⁵ photons, 935 nm, pulsed FEL	1.8 + 1.8 Tm 2* 1,77T, 1m	1 mHz ongoing, preliminary results
OSQAR@CERN	488+514 nm , cw 18 W Argon Laser	136 + 136 Tm LHC Magnet 9,5T 14,3m	1 mHz ? ongoing, preliminary results



Experimental Setup: Beam Tubes – Mirror Holders



Cavity=34W AR window Vacuum tube AR window Vacuum tube 9 m 9 m

magnet beam pipe is bent
clear aperture only 18 mm ☺
just one magnet - mirror in middle
-> exp. challenge and constrain on beam quality of laser

two beam tubes – one from each side: removable & vacuum tight (10⁻⁷ mbar)

- 1. laser tube (generation side):
 - windows on both sides
 - adjustable mirror in middle
- 2. detector tube (regeneration part):
 - removable wall on inner side
 - open for alignment purpose
 - window on outer side



precise remote mirror steering inside magnet (@ 5 Tesla) custom made motor based on piezo actuators for high finesse cavity in vacuum squiggle motors



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Detector – CCD Camera

- > **Detector**: high sensitivity, low noise
- ➤aiming for single photon detection
- initially SBIG ST-402
- > now: PRINCETON INSTRUMENTS PIXIS:1024BL
 - liquid cooling circulator at -70°
 - CCD47-10 AIMO Back Illuminated CCD sensor
 - 13 μm square pixel, 1024 * 1024
 - eff 95 % at 532 nm
 - dark current 0.001 e-/pixel/sec
 - Iow readout noise: 3.8 e-/pixel







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Data Analysis - Classification of Data

Compare signal of data and background (dark) frames

- observable: difference in mean of many 'signal' to mean 'background'
- looking for enhancement in the "signal" pixel



Categories, Signals and Backgrounds

8 groups of frames to analyze, 4 Signals, 4 Backgr.

conversion from ADU to photons:

- gain [ADU / p.e.]
- quantum efficiency [p.e. / γ]
- beam spot eff. / stability
- laser power, optical losses
- Data 1h camera frames
- Signal region defined by beam spot



Data Sets used for the 2009 Results

around 50h of beam time – 45h with magnet in operation and several 100h of dark frames

Data	binning	Signal pixel	frames	selected	
Dark Frame Series 090828-090907		(151,193) with reference beam	136	122	93%
Dark Frame Singles 090904-090907	X: 3;1022;3;340 Y: 1;1020;3;340		17	16	94%
Laser-on-hor-Magnet-on 090827			9	9	100%
Laser-on-vert-Magnet-on 090907			2	2	100%
Laser-on-vert-Magnet-off 090907			1	1	100%
Dark Frame Series Shutter closed 091023-091027		2;3;340 (133,195) 4;3;341 without reference beam	80	65	81%
Dark Frame Series Shutter open 091027-091030	X: 3;1022;3;340		45	34	76%
Laser-on-hor-Magnet-on 091030			5	5	100%
Laser-on-hor-Magnet-on-0.18mb 091028-091029	1. 2,1024,3,341		10	8	80%
Laser-on-vert-Magnet-on-0.18mb 091026-091027			9	8	89%
Low Intensity Test 090918		(147,165) without reference beam	4	4	100%
Dark Frame Series 090919-090921	X: 1;1023;3;341		59	47	80%
Laser-on-hor-Magnet-on 090922	Y: 1;1023;3;341		2	2	100%
Laser-on-vert-Magnet-on 090922			6	6	100%



limits

- > 95 % confidence level method of Feldman and Cousins
- > exclusion limit 95% C.L.
- > Laser Power > 1kW
- > sensitivity

Polarization	n-1	Р(γ→Θ→γ) (95%CL)
horizontal	0	2.3·10 ⁻²⁵
vertical	0	3.0·10 ⁻²⁵
hor.+vert.	0	1.0·10 ⁻²⁵

Polarization	n-1	Р(γ→Θ→γ) (95%CL)
horizontal	5.0·10- ⁸	1.1·10 ⁻²⁴
vertical	5.0·10 ⁻⁸	3.1·10 ⁻²⁴
hor.+vert.	5.0·10 ⁻⁸	1.8·10 ⁻²⁴



Detectors for future LSW Experiments

- Choice of detector depends on details of the setup (esp. locking of regeneration cavity):
- > potential "background-free" single photon counter (also 1064 nm): Transition Edge Sensor @ 100 mK, Nanowire Photon Counter @ few K



A. Engel (UZH), http://www.physik.uzh. ch/groups/schilling/resc h/Detektoren.pdf

Heterodyne detection: mix two signals and search for a Fourier component signals (used by gravitational wave community)

$$S = |E_{SO}e^{i(\omega_1 t + \phi)} + E_{LO}e^{i\omega_2 t}|^2$$
$$= E_{LO}^2 + 2E_{LO}E_{SO}\cos(\Omega t + \phi)$$

