

Higgs boson mass and production cross-section measurement at FCC-ee

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On behalf of the FCC Collaboration

IRN Terascale meeting LPC-Clermont

November 23rd 2021



Université
de Paris



FUTURE
CIRCULAR
COLLIDER

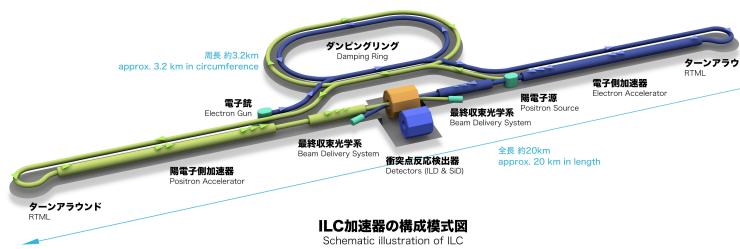
- Overview of FCC
- Recoil mass technique
- Event selection
- Signal and background modelling
- Systematics

Future Colliders

□ Future Linear Colliders:

1. International Linear Collider (ILC)

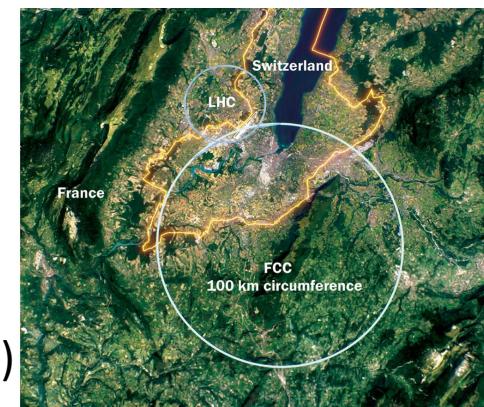
- 1) e^+e^- at 250GeV, 500 GeV and 1 TeV
- 2) 30-50 km



□ Future Circular Colliders:

1. The Future Circular Collider (FCC)

- 1) FCC-ee: e^+e^- at $\sim 91\text{-}365$ GeV, as first-generation Z, Higgs and top factory at high luminosities
- 2) FCC-hh: $p - p$ at 100 TeV as natural continuation of LHC at energy frontier
- 3) Circumference ~ 90 km (LHC: ~ 27 KM)



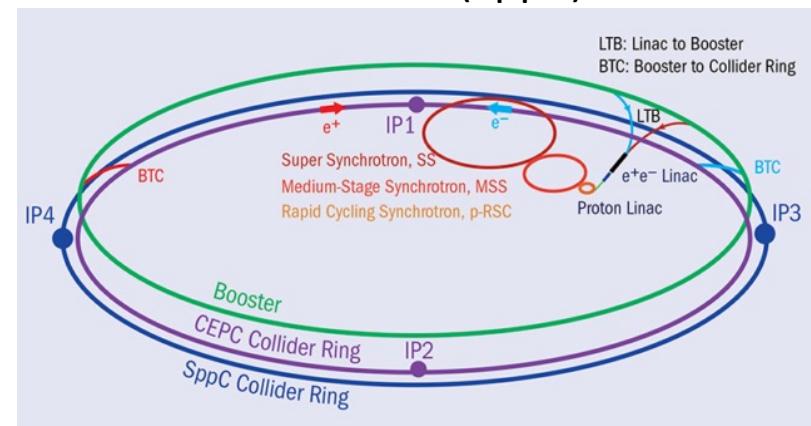
2. The Compact Linear Collider (CLIC)

- 1) e^+e^- at 380 GeV, 1.5 TeV and 3 TeV
- 2) 11-50 km

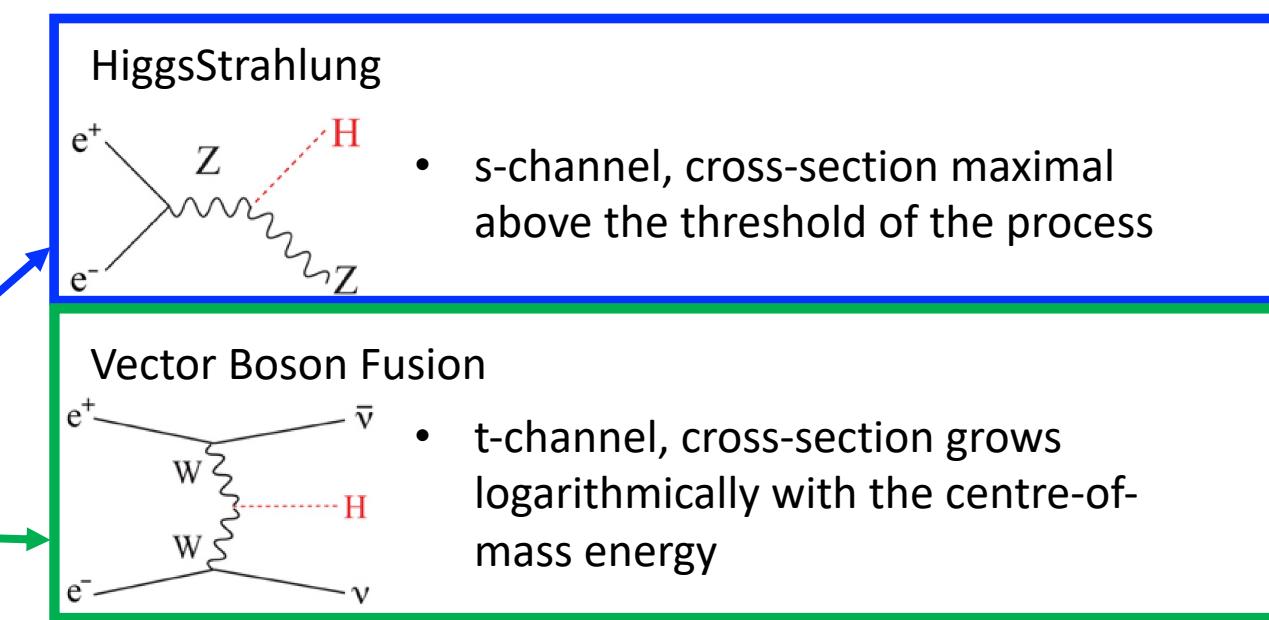
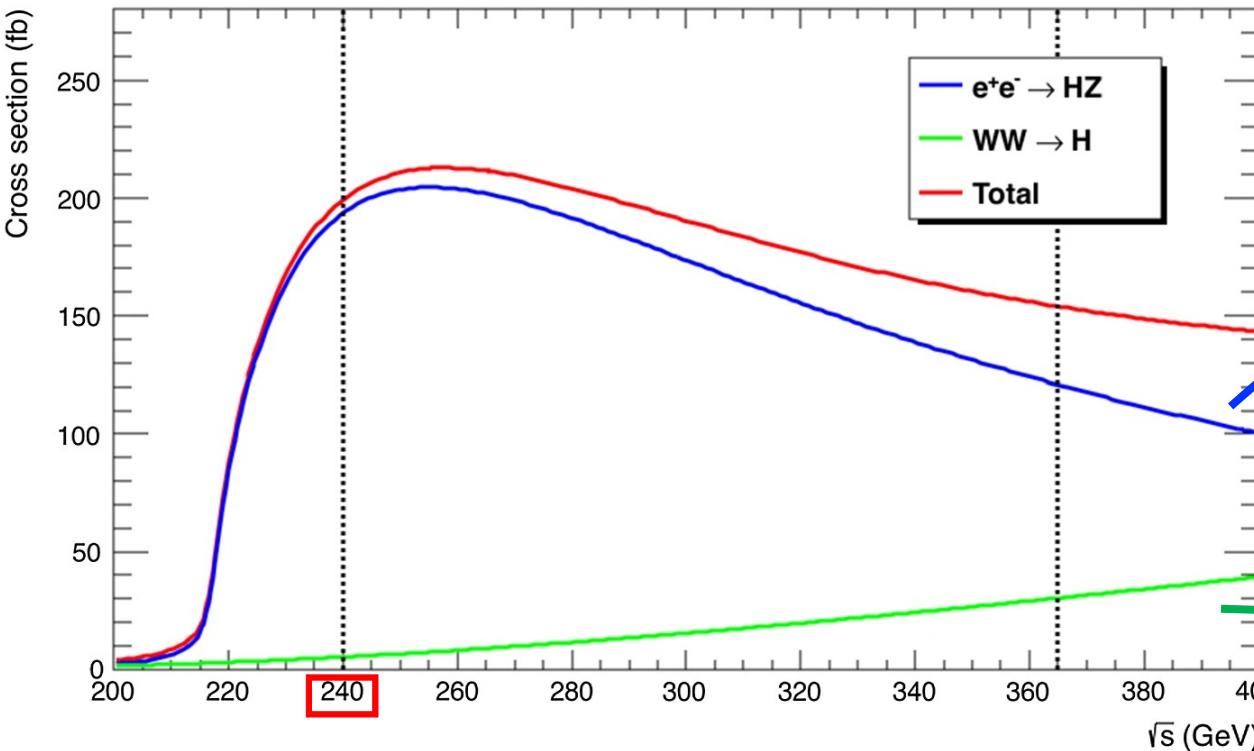


2. Circular Electron Positron Collider (CEPC)

- 1) e^+e^- with similar parameters as FCC-ee
- 2) Super Proton-Proton Collider (SppC)



Higgs production at Future Circular Collider (FCC)



FCC-ee as a Higgs factory

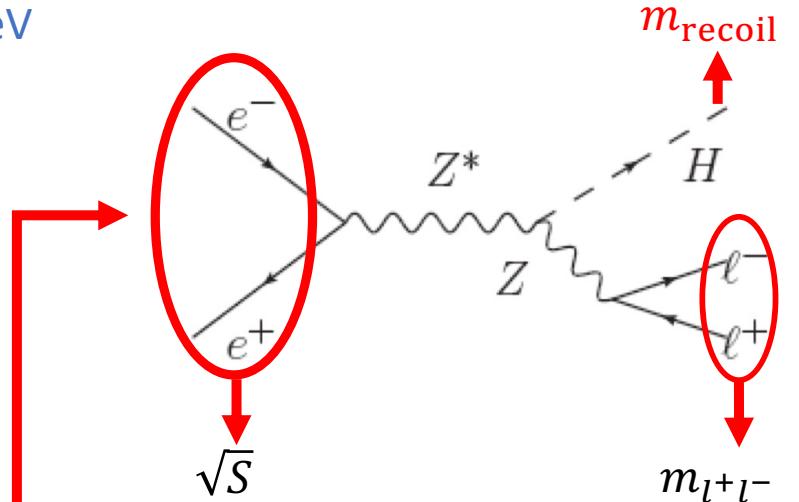
➤ Total Cross-section is maximal at $\sqrt{s} \sim 260$ GeV

➤ For the Higgsstrahlung ($e^+e^- \rightarrow ZH$):

1. ZH optimal event rate is at $\sqrt{s} \sim 240$ GeV : $\sigma \sim 200$ fb $\sim 10^6$ events (@ $L = 5 ab^{-1}$)
2. With data at $\sqrt{s} \sim 365$ GeV, 1.8×10^5 ZH and 0.45×10^5 WW-fusions (~30%) (@ $L = 1.5 ab^{-1}$)
(useful for measuring self-coupling and Γ_H precisely)

➤ Goal: precise measurements of ZH cross section (per mille) and Higgs mass \sim MeV

- Current best result: $m_H = 125.38 \pm 0.14 (\pm 0.12)$ GeV @CMS
- The σ_{ZH} accuracy could reach 0.5%
- determine g_{HZZ} and Higgs width (Γ_H)
- Electron Yukawa coupling measurement via s-channel
- $e^+e^- \rightarrow H$ @ $\sqrt{s} = m_H$ ($\Gamma_H = 4.2$ MeV) (details on [arXiv:2107.02686](#))
- Trilinear Higgs-self coupling (details on [arXiv:1809.10041](#))



➤ Signal: $e^+e^- \rightarrow ZH \rightarrow l\bar{l} + X$

ZH is the dominant Higgs production process @ 240 GeV e^+e^- machine

➤ M_{recoil} from the Z production without measuring the Higgs production final state

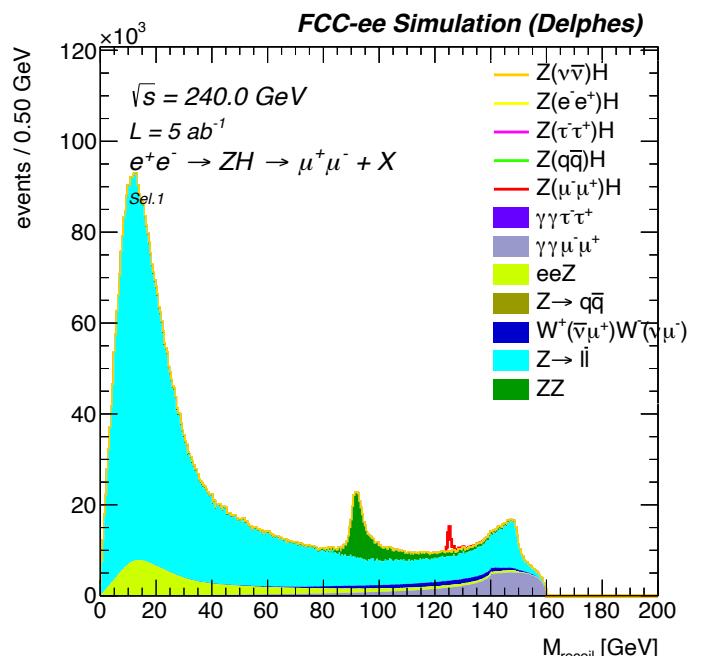
$$m_{\text{recoil}}^2 = (\sqrt{s} - E_{l\bar{l}})^2 - p_{l\bar{l}}^2 = s - 2E_{l\bar{l}}\sqrt{s} + m_{l\bar{l}}^2$$

➤ Sensitive to the precise knowledge of the centre-of-mass energy (\sqrt{s})

and Initial Stat Radiation(ISR)

➤ Model-independent study

➤ WW, ZZ and $Z/\gamma \rightarrow l\bar{l}$ Backgrounds @ 240 GeV



Signal, Background and Selections

Monte-Carlo campaign (“Spring2021”):

- $\sqrt{s} = 240 \text{ GeV}$
- Luminosity: $L = 5 \text{ ab}^{-1}$
- Initial Stat Radiation (ISR) and Final Stat Radiation (FSR) on
- Beam Energy Spread (BES) sets to $0.165\% = \pm 198 \text{ MeV}$
- IDEA detector; detector response modelled with Delphes

• Signals:

1. $Z(\mu^+\mu^-)H$ (Whizard)
2. $Z(\tau^+\tau^-)H$ (Whizard)
3. $Z(q\bar{q})H$ (Whizard)
4. $Z(\nu\bar{\nu})H$ (Whizard)
5. $Z(e^+e^-)H$ (Whizard)

• Backgrounds:

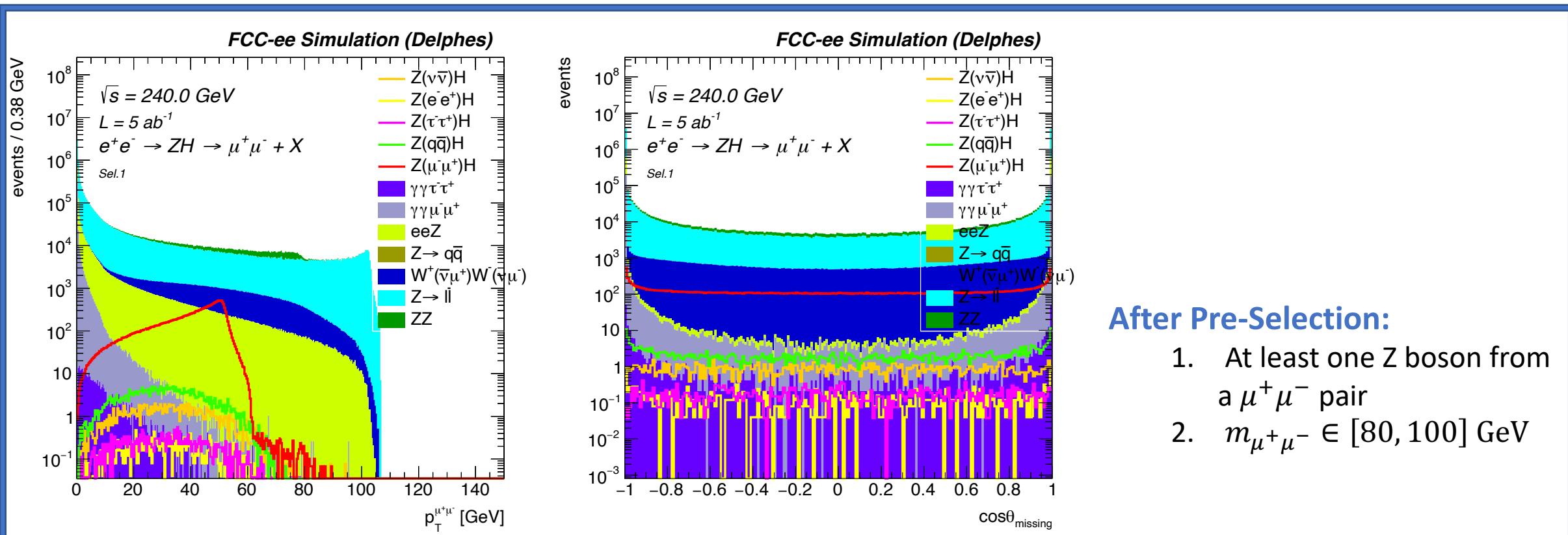
1. $ZZ(\text{inclusive}),$ (Pythia)
2. $W^+(\nu\mu^+)W^-(\bar{\nu}\mu^-),$ (Pythia)
3. $Z \rightarrow l^+l^-,$ (Pythia)
4. $Z \rightarrow q\bar{q},$ (Pythia)
5. $eeZ,$ (Whizard)
6. $\gamma\gamma \rightarrow \mu^+\mu^-$, (Whizard)
7. $\gamma\gamma \rightarrow \tau^+\tau^-$ (Whizard)

	mumuH	WW_mumu	ZZ(inclusive)	Zll
$\sigma \cdot L$	33822	1289600	6794950	68893500
NEVENTS	10^6	10^7	10^7	$0.99 \cdot 10^7$
NEVENTS/$\sigma \cdot L$	29.57	7.75	1.47	0.14

Event Selection

Event-Selection:

1. At least one Z boson from a $\mu^+\mu^-$ pair
2. $m_{\mu^+\mu^-} \in [86, 96]$ GeV → focus on Z resonance space
3. $M_{\text{recoil}} \in [120, 140]$ GeV → Signal exhibits sharp peak around ~ 125 GeV,
4. $p_T^{\mu^+\mu^-} \in [20, 70]$ GeV → Signal mainly within this region, Low $p_T^{\mu^+\mu^-}$ cuts back-to-back events ($Z/\gamma^* \rightarrow ll$)
5. $|\cos \theta_{\text{missing}}| < 0.98$ → Polar angle of missing momentum, reduce $\gamma\gamma$ processes. ISR emitted approximately collinear with the incoming beams escapes detection in the beam pipe



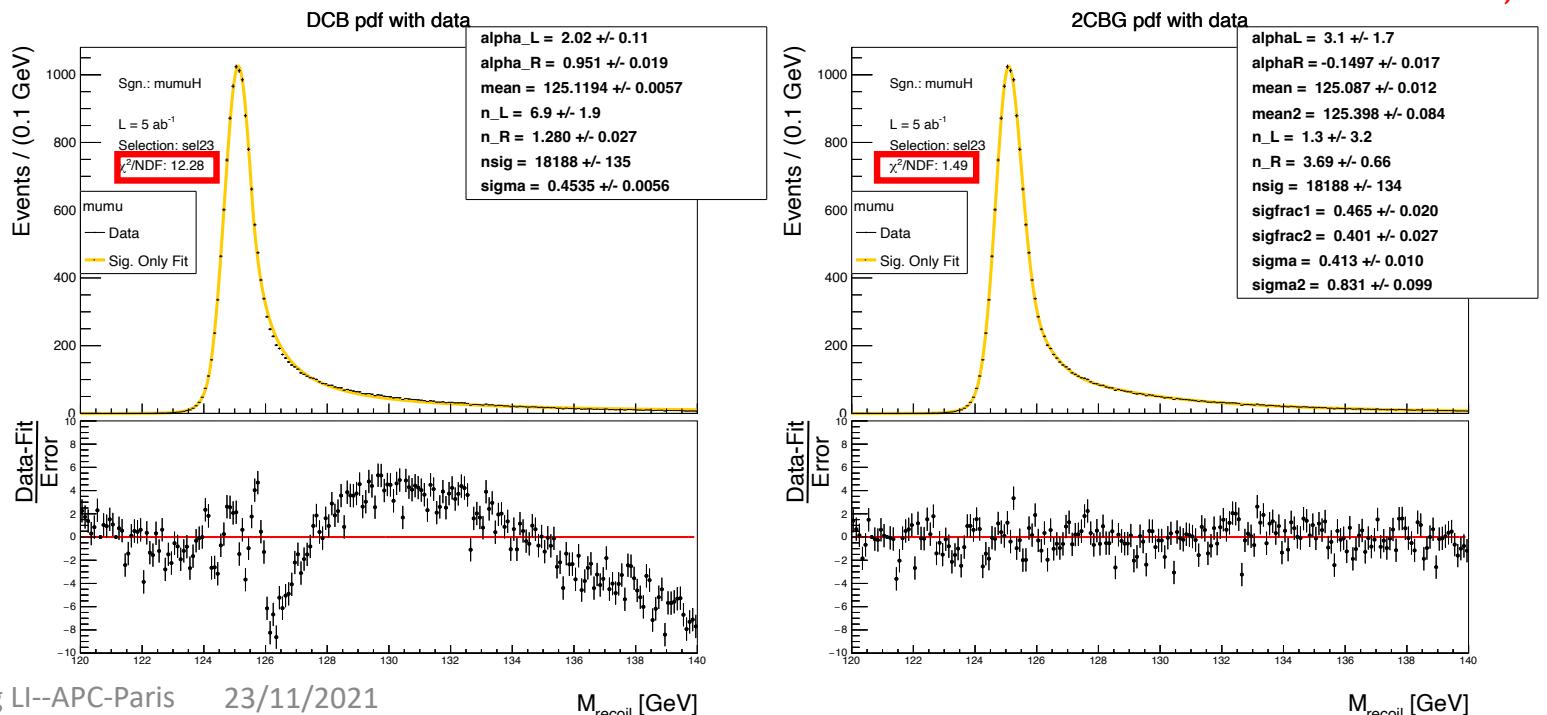
After Pre-Selection:

1. At least one Z boson from a $\mu^+\mu^-$ pair
2. $m_{\mu^+\mu^-} \in [80, 100]$ GeV

Signal Modelling

Customized p.d.f. 2CBG:

- Two **crystal-ball functions** (left and right), sharing mean and width
- Added Gaussian to cope with the high tails
- Gaussian suppressed in norm ($\text{sigfrac1} + \text{sigfrac2} > 0.8$)
- In total 10 “free” parameters (+1 normalization)
- $\text{pdf}(M_{\text{recoil}}) = \text{sigfrac1} \cdot CB(M_{\text{recoil}}; \mu, \sigma, \alpha_L, n_L)$
 $+ \text{sigfrac2} \cdot CB(M_{\text{recoil}}; \mu, \sigma, \alpha_R, n_R)$
 $+ (1 - \text{sigfrac1} - \text{sigfrac2}) \cdot \text{Gauss}(M_{\text{recoil}}; \mu_2, \sigma_2)$

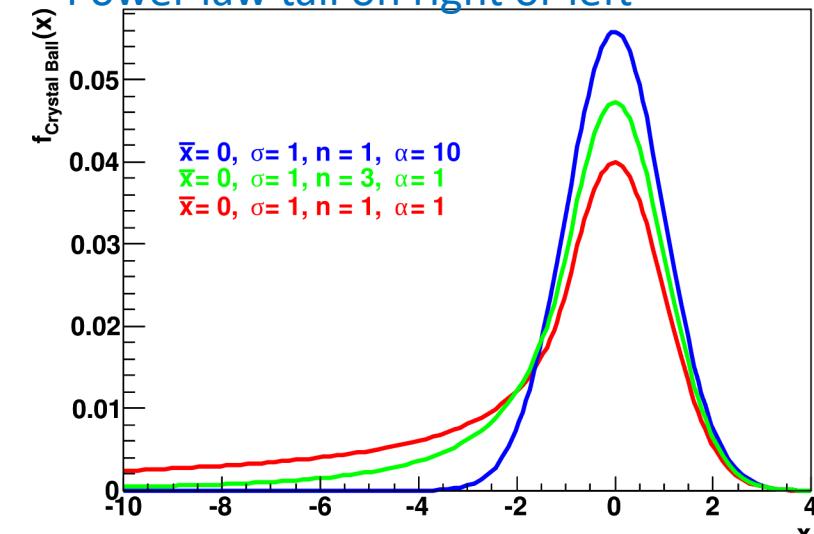


Crystal-Ball function:

$$f(x; \alpha, n, \bar{x}, \sigma) = N \cdot \begin{cases} \exp(-\frac{(x-\bar{x})^2}{2\sigma^2}), & \text{for } \frac{x-\bar{x}}{\sigma} > -\alpha \\ A \cdot (B - \frac{x-\bar{x}}{\sigma})^{-n}, & \text{for } \frac{x-\bar{x}}{\sigma} \leq -\alpha \end{cases}$$

Gaussian Core

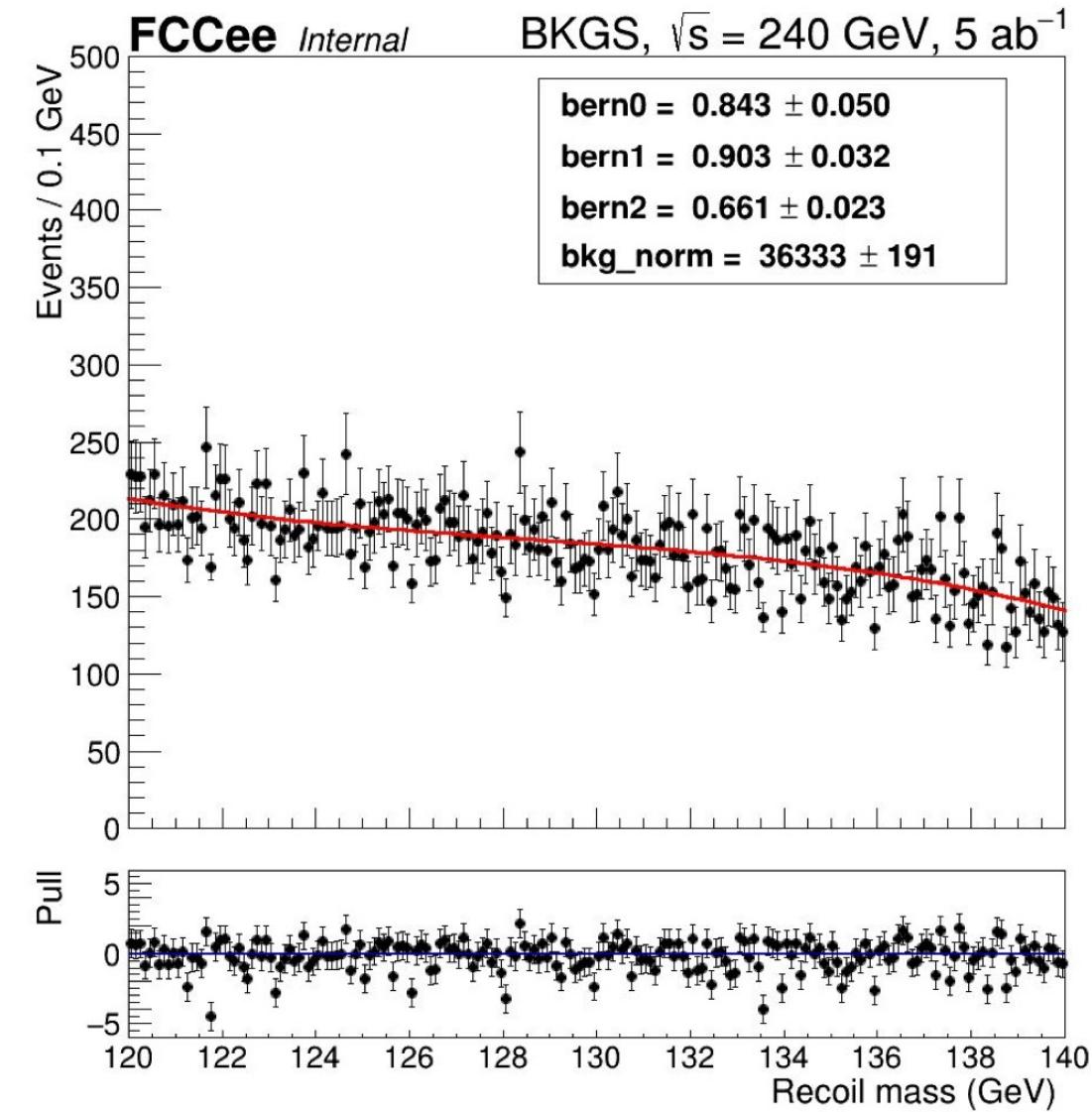
Power law tail on right or left



Background modelling

Statistical treatment of backgrounds:

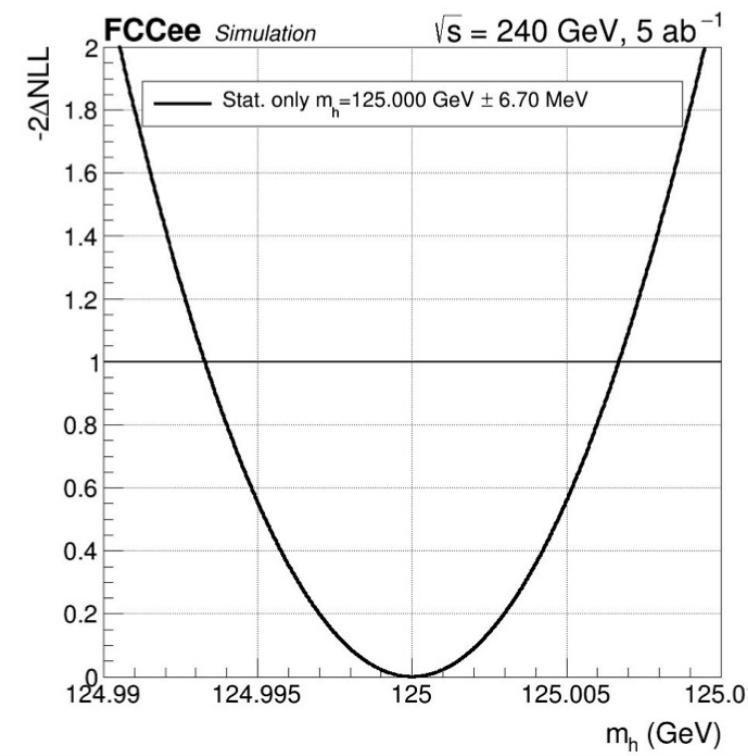
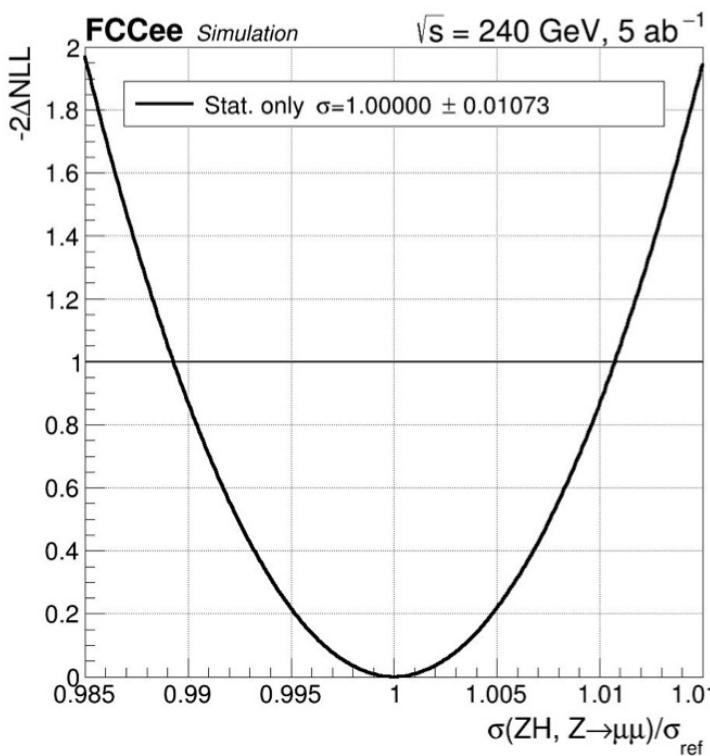
- All backgrounds are merged
- Smoothly falling background modelled as **third-order polynomial fit**
- Keep polynomial coefficients constant, but keep total normalization floating
- Sufficient sample statistics for all backgrounds ($\sim 4x$ expected at 5 /ab), except for $Z/\gamma^* \rightarrow ll$ where slightly more MC is necessary



Statistical Analysis

Statistical analysis performed using Combine, the CMS statistical framework developed in context of Higgs analyses (*)

- Signal and background analytical shapes are fitted to pseudo-data Asimov dataset (= randomized with mean=signal+background)
 - Injected 125.0 GeV signal with cross-section of 0.0067656 pb (ref)
 - Free parameters: signal norm, background norm and mH floating
- Likelihood scans to extract cross-sections and Higgs mass with robust uncertainties
- First, w/o accounting for experimental uncertainties → **stat-only result**



Stat-only uncertainties:
→ Cross-section: ~ 1.1 %
→ Higgs mass: 6.70 MeV

(*) The ATLAS, CMS Collaborations, and LHC Higgs Combination Group. Procedure for the LHC Higgs boson search combination in Summer 2011. Technical Report CMS-NOTE-2011-005. ATL-PHYS-PUB-2011-11, CERN, Geneva, Aug 2011

Systematic uncertainties

Study of systematic uncertainties to assess the impact on the Higgs mass and cross-section measurement

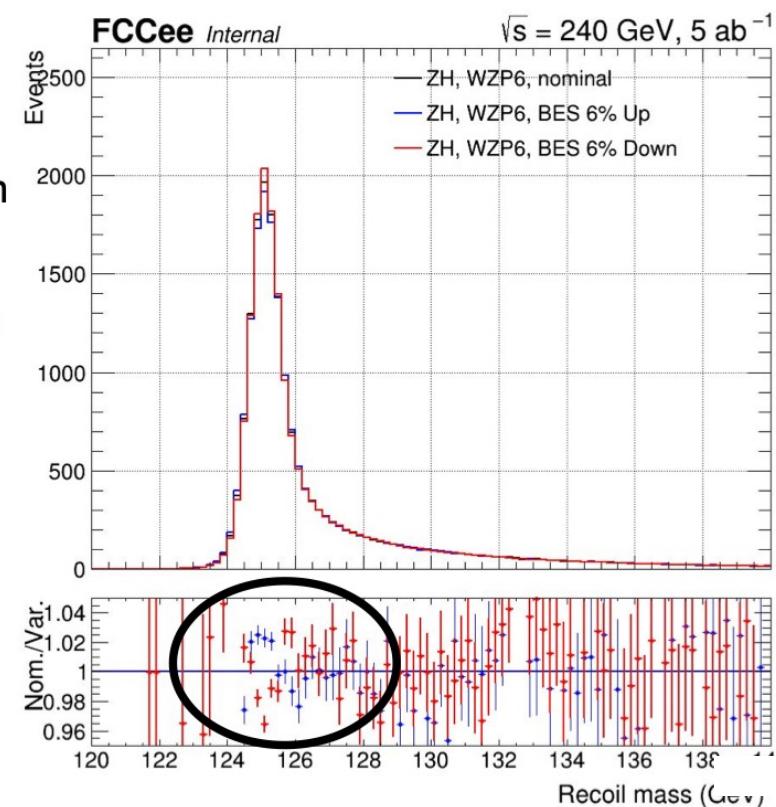
- Uncertainties directly alter the recoil distribution shape and/or normalization
- Can be constrained with data, depending on source of uncertainty
- Considered uncertainties: BES, ISR, center-of-mass, muon momentum scale

1) Beam energy spread uncertainty (nominal BES: $\pm 0.165\% = \pm 198$ MeV)

- Uncertainty driven by accelerator instrumentation: bunch length measurement up to 0.3 mm accuracy or better → **6% BES uncertainty**
- Data-driven BES constraining possible $ee \rightarrow ff(\gamma)$; e.g. longitudinal momentum imbalance of dimuon spectrum and/or Bhabha during fill → **estimated to be 1% BES uncertainty**

Generated perturbed signal samples @ 125.0 GeV with:

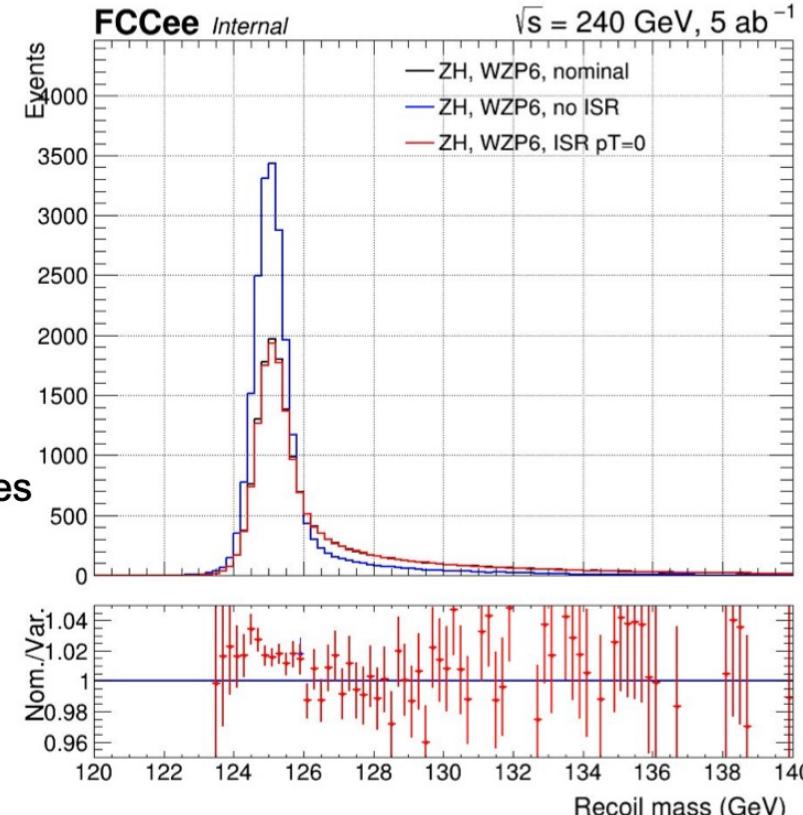
- 6% BES variation: 2-3 % shape effect observed at mass peak
- 1% BES variation: negligible variation ~ within statistical uncertainty



Systematic uncertainties

2) Initial State Radiation: ISR has impact on shape and normalization (xsec)

- ISR treatment in Whizard using structure function approach: photon p_T spectrum
 - either strict collinear approximation ($p_T = 0$)
 - or ad-hoc implementation of a physical spectrum (default sample)
- Generated perturbed sample in the strict collinear approximation
 - rather drastic → **very conservative estimation of ISR uncertainty !**
- Benchmarking against KKMC at Z-peak and/or Sherpa to obtain more realistic uncertainties for ISR treatment
- Can be constrained directly using data-driven techniques (including BES)



3) Center-of-mass: +/- 2 MeV

- \sqrt{s} parameter in the recoil mass definition → uncertainty induces ~ linear shift the recoil distribution
- Precision estimated to be 2 MeV at 240 GeV using radiative return events $Z \rightarrow ll$ or $Z \rightarrow qq$

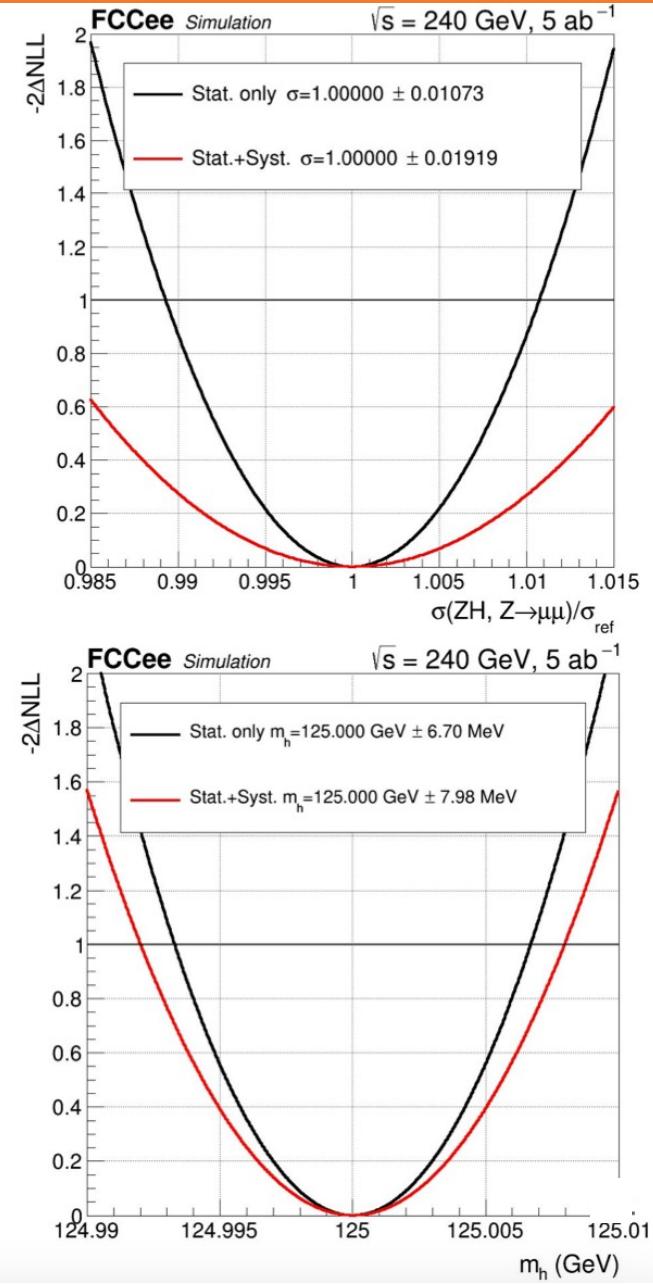
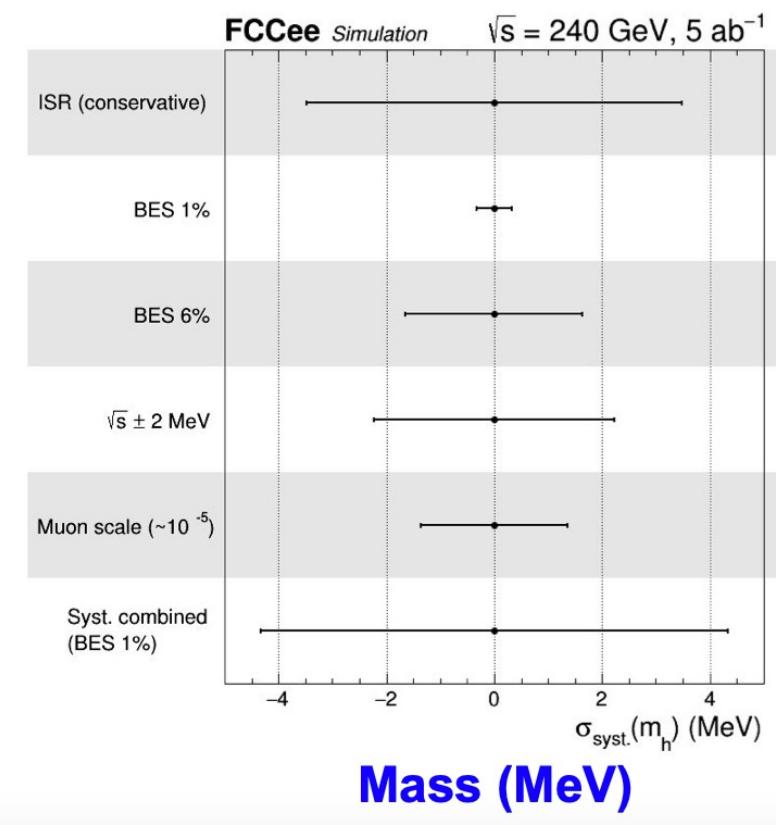
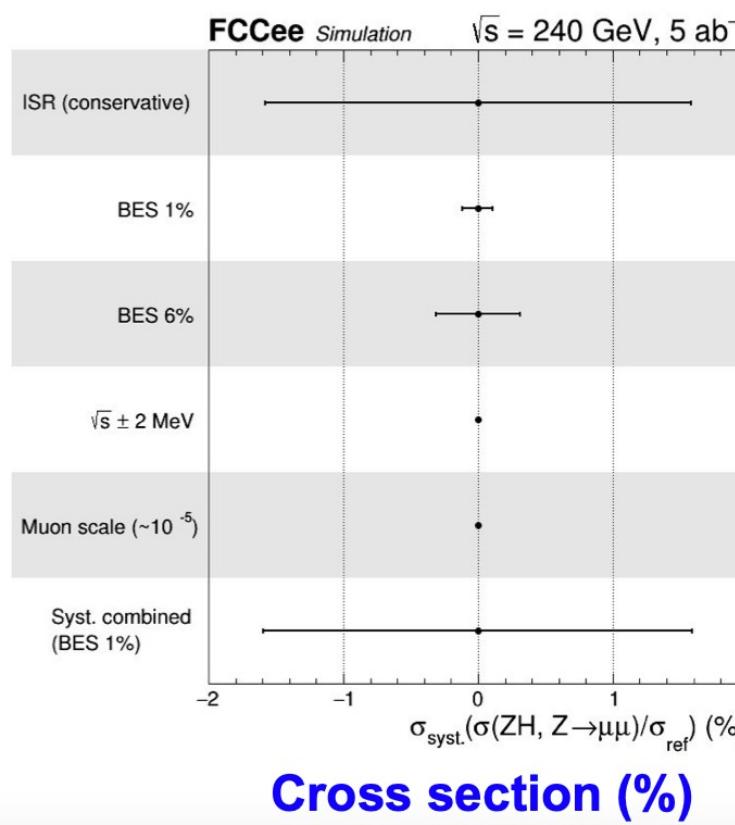
4) Muon momentum scale: relative scale uncertainty variation of 1e-5

- Directly affects $m(\mu\mu)$, hence shift in recoil mass
- Statistical potential to measure muon scale ~ 1e-6, but limited to yield 1e-5 uncertainty

Systematic uncertainties

Systematic variations included in likelihood as Gaussian constraint terms

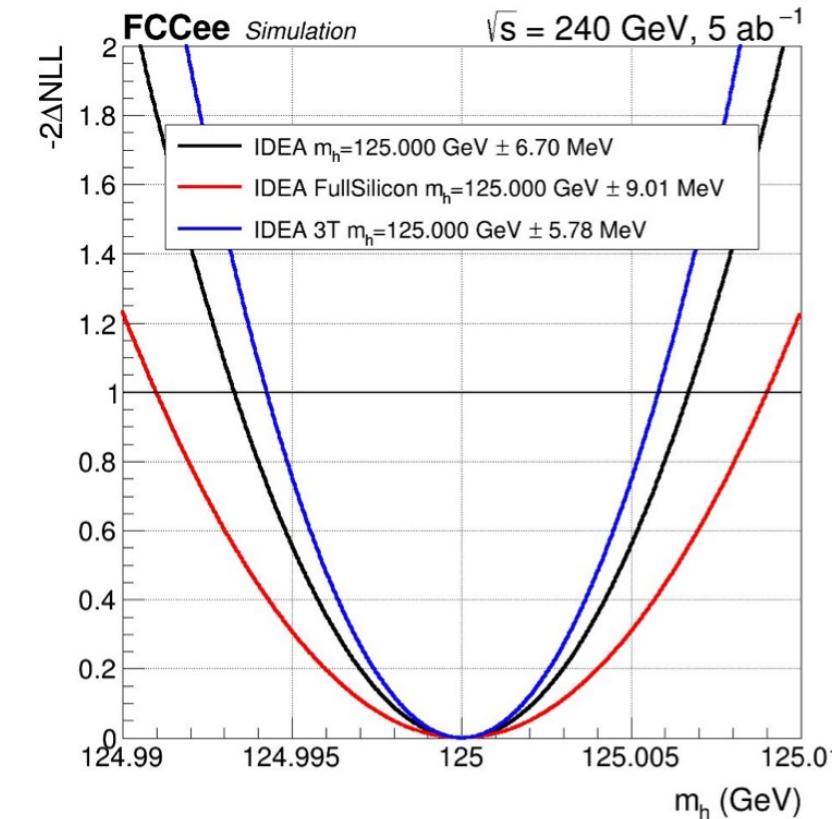
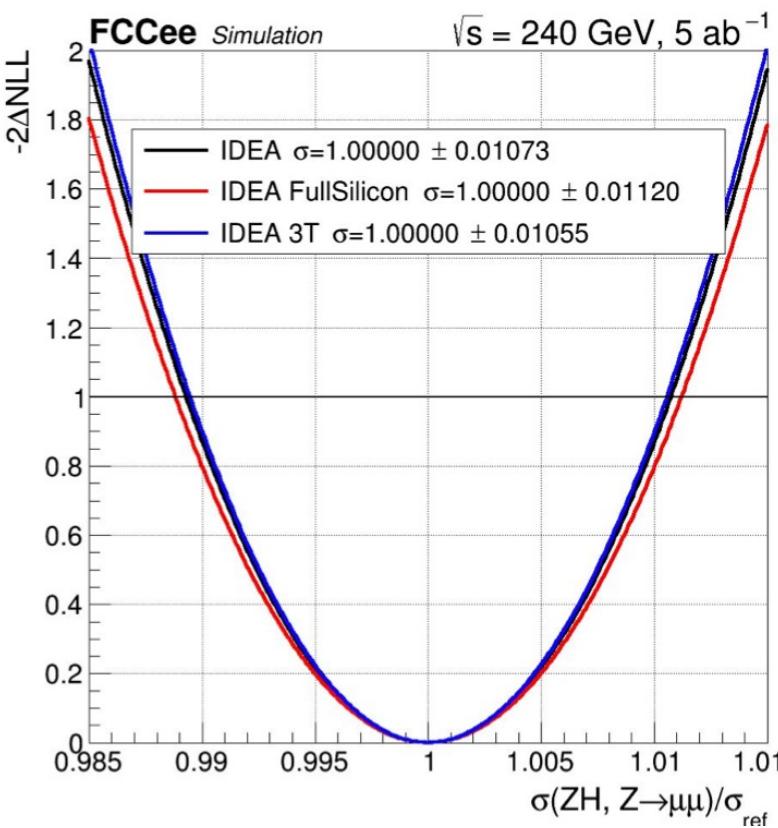
- Inclusion of all systematics: $\Delta m_H = 7.98 \text{ MeV}$ and $\Delta\sigma = 1.92 \%$
- Breakdown of uncertainties: vary systematics one by one, extract $\sigma_{\text{syst}}^2 = \sigma_{\text{tot}}^2 - \sigma_{\text{stat}}^2$
- ISR dominant (but conservatively estimated), muon scale/ \sqrt{s} accounts for $\sim 2 \text{ MeV}$ on Δm_H
- Impact on cross-section limited, except ISR



IDEA detector configurations

Different IDEA detector configurations studied:

- Magnetic field increased from 2T to 3T → expected better momentum resolution
- FullSilicon tracker instead of drift chamber → degraded resolution due to enhanced multiple scattering, especially at low p_T and in the range relevant for this analysis
- Effect on mass scales with resolution, impact on cross-section uncertainty limited



Stat-only results

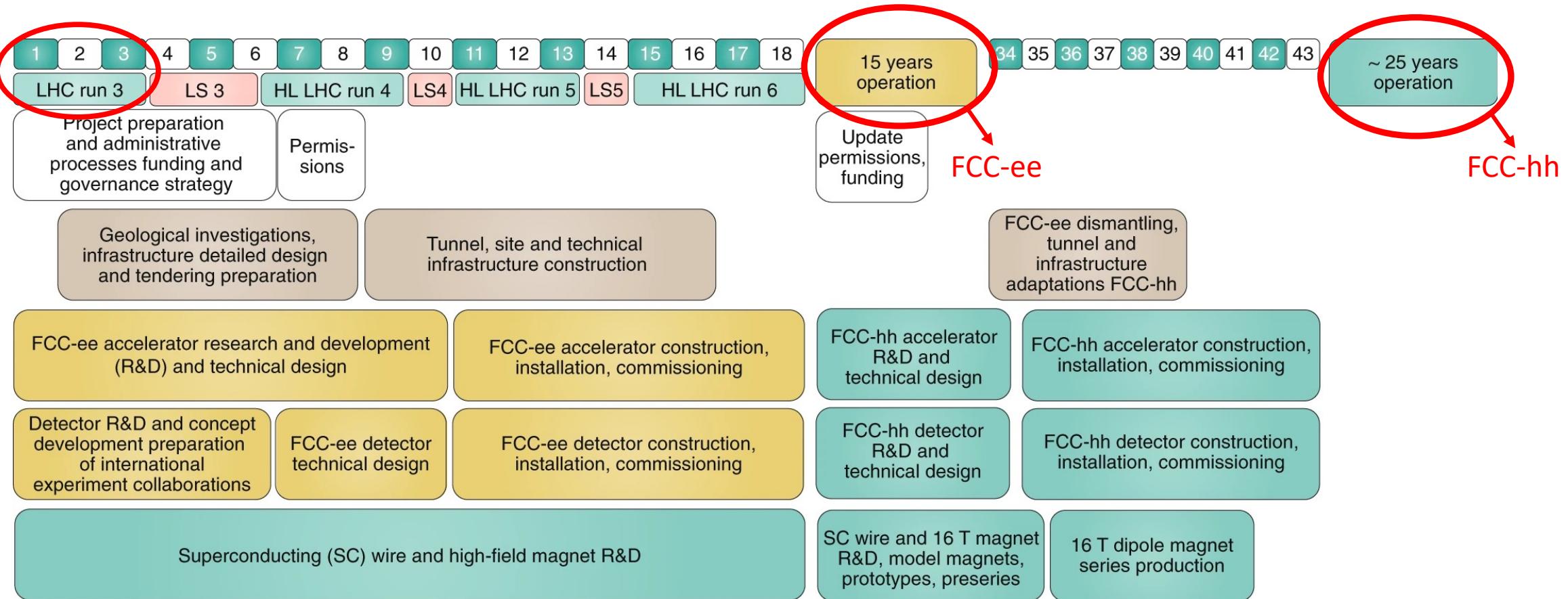
IDEA	Δm_H (MeV)	$\Delta\sigma$ (%)
Nominal	6.70	1.07
FullSilicon	9.01	1.12
3T	5.78	1.06

❖ Conclusion:

- In the Higgs measurements at the e^+e^- colliders, the “ZH recoil mass” method will improve the uncertainty of m_H to a few MeV level (and the Higgs boson width $\Gamma = 4.1$ MeV in the SM, could also be measured)
- Measure the HZZ coupling as a “candle” for other Higgs studies
- Optimized event selection to reject main backgrounds
- Signal modelling with customized p.d.f.
- Statistical analysis yields Higgs mass uncertainty 6.7MeV, cross-section 1.1% (stat-only)
- Inclusion of systematic uncertainties results into 8.0 MeV / 1.9% respectively, where ISR dominant but conservatively estimated

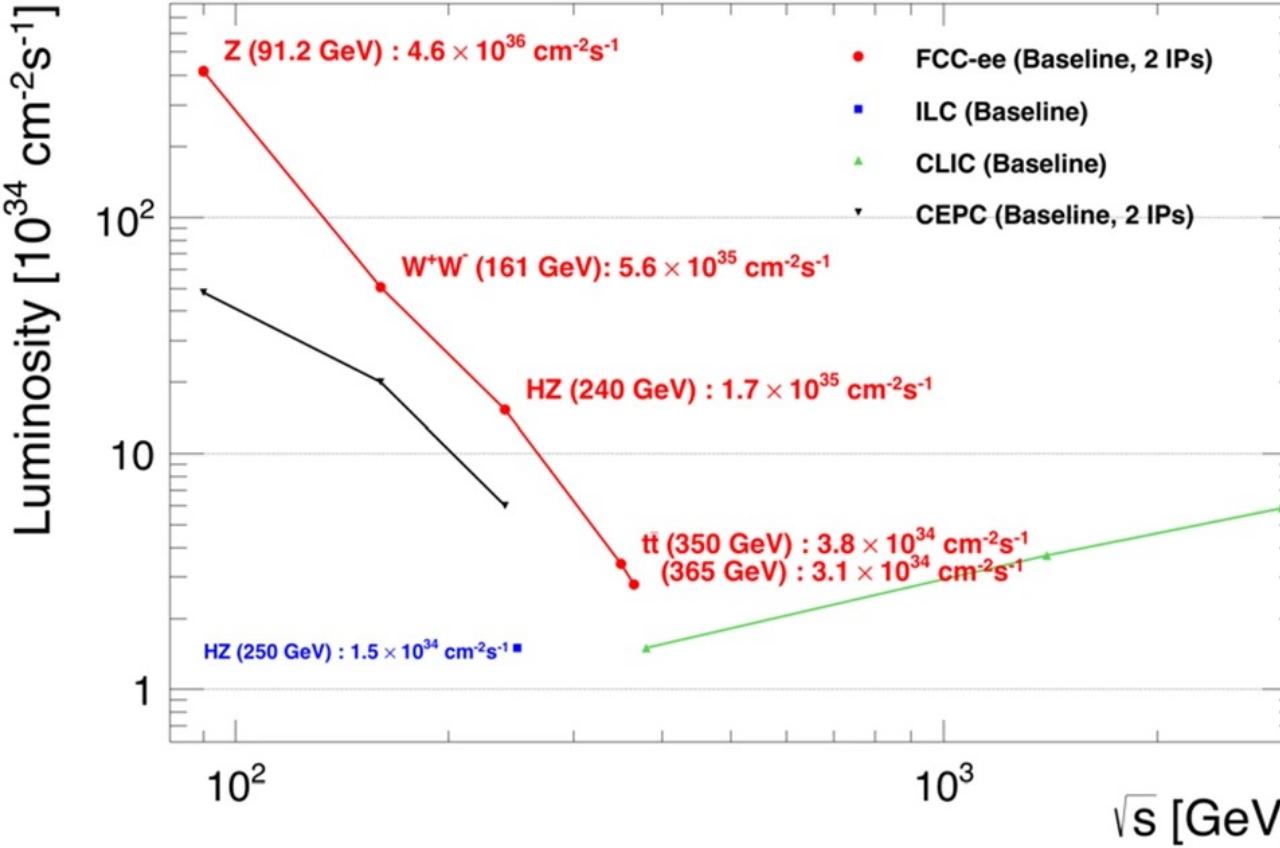
Backup

FCC integrated program



1. On the 18 years of preparation
 - 1) Feasibility study (5 year)
 - 2) then civil constructions
 - 3) then machine and detectors construction
2. 15 years of FCC-ee on different energy points
3. ~10 years to change the magnets between, and change the detectors
4. 25 years of FCC-hh

FCC-ee Luminosities



FCC Physics Opportunities

➤ 4 baseline working points

- Z pole @ 91.2 MeV
- W^+W^- threshold @ 161 GeV
- ZH threshold @ 240 GeV
- $t\bar{t}$ threshold @ 365 GeV

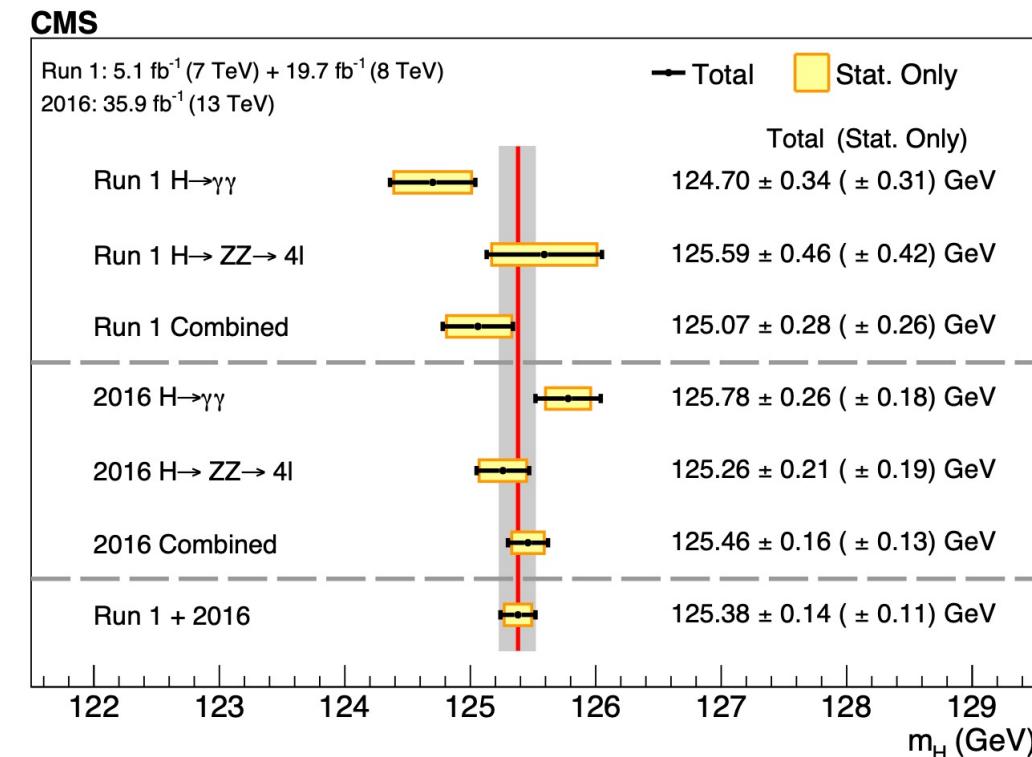
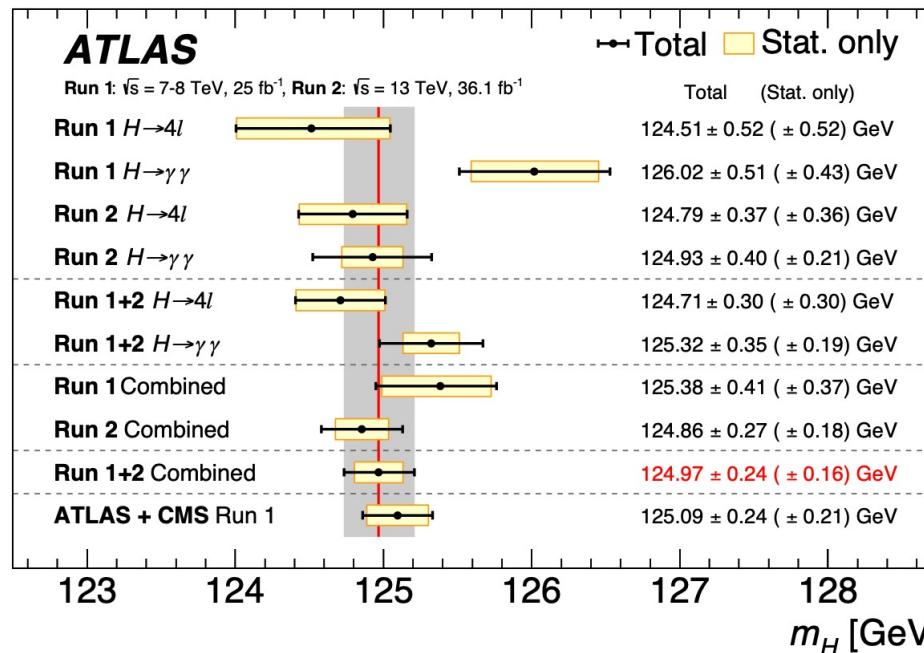
Phase	Run duration (years)	Centre-of-mass energies (GeV)	Integrated luminosity (ab^{-1})	Event statistics
FCC-ee-Z	4	88–95	150	3×10^{12} visible Z decays
FCC-ee-W	2	158–162	12	10^8 WW events
FCC-ee-H	3	240	5	10^6 ZH events
FCC-ee-tt(1)	1	340–350	0.2	$t\bar{t}$ threshold scan
FCC-ee-tt(2)	4	365	1.5	10^6 $t\bar{t}$ events

Where are we?

- Last ATLAS public m_H combined result includes 36 fb^{-1} Run 2 + Run 1 data

$$m_H = 124.97 \pm 0.24 (\pm 0.16) \text{ GeV}$$

[Stefano's talk at ATLAS WEEK](#)



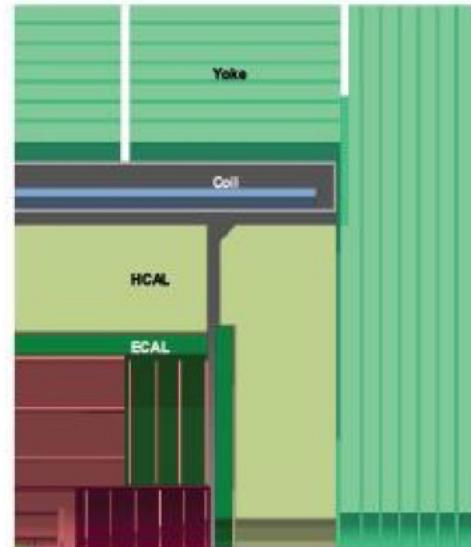
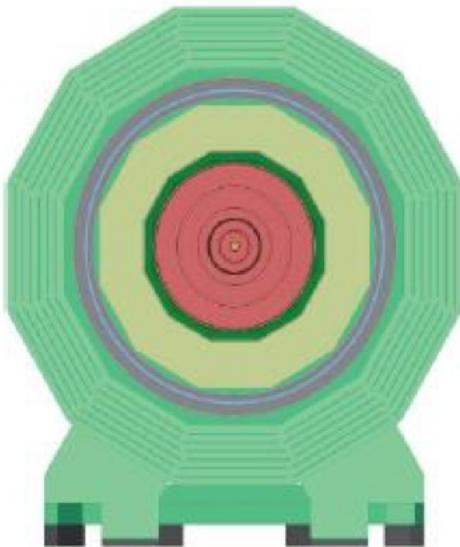
- Current LHC most precise measurement is from CMS

$$m_H = 125.38 \pm 0.14 (\pm 0.12) \text{ GeV}$$

FCC-ee is expected to reach $\sim \text{MeV}$ uncertainty

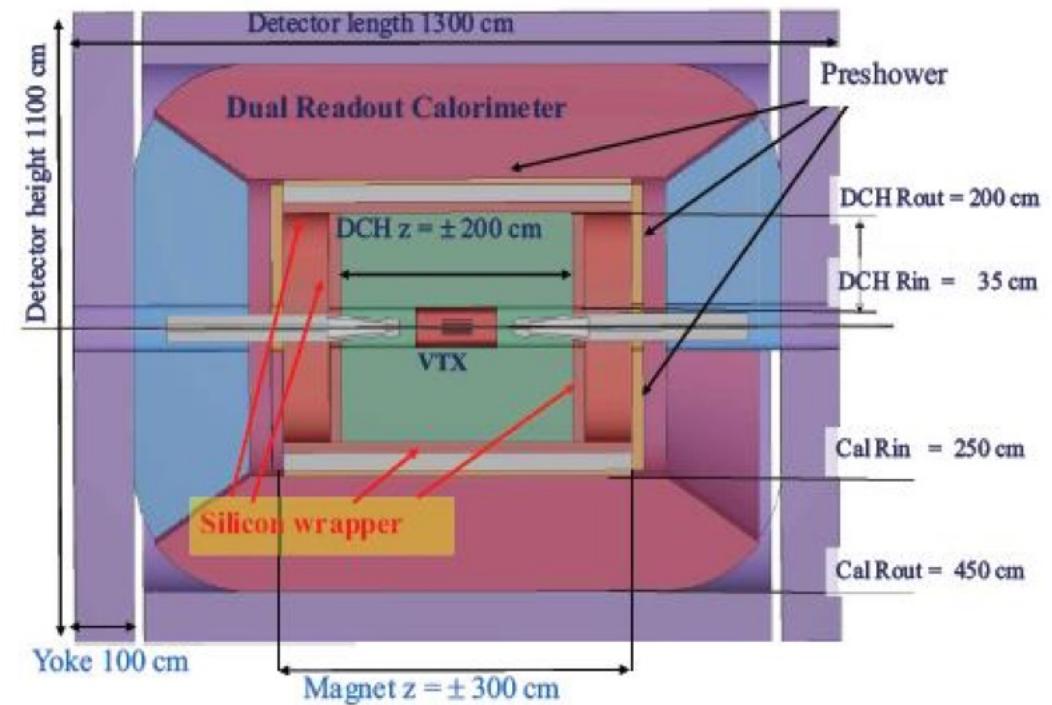
Detectors under study

CLD



- conceptually extended from the CLIC detector design
 - full silicon tracker
 - 2T magnetic field
 - high granular silicon-tungsten ECAL
 - high granular scintillator-steel HCAL
 - instrumented steel-yoke with RPC for muon detection

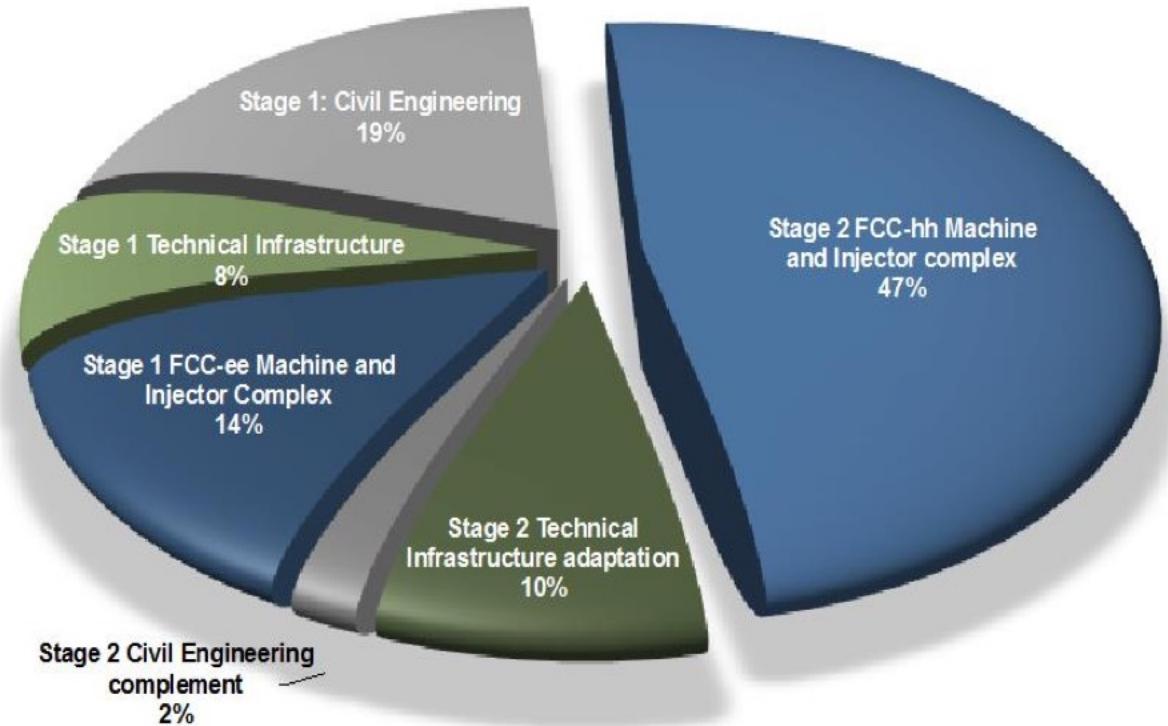
IDEA



- explicitly designed for FCC-ee/CepC
 - silicon vertex
 - low X_0 drift chamber
 - drift-chamber silicon wrapper
 - MPGD/magnet coil/lead preshower
 - dual-readout calorimeter: lead-scintillating/cerenkov fibers
 - μ Rwell for muon detection

Detectors under study

Domain	Cost in MCHF
Stage 1 - Civil Engineering	5,400
Stage 1 - Technical Infrastructure	2,200
Stage 1 - FCC-ee Machine and Injector Complex	4,000
Stage 2 - Civil Engineering complement	600
Stage 2 - Technical Infrastructure adaptation	2,800
Stage 2 - FCC-hh Machine and Injector complex	13,600
TOTAL construction cost for integral FCC project	28,600



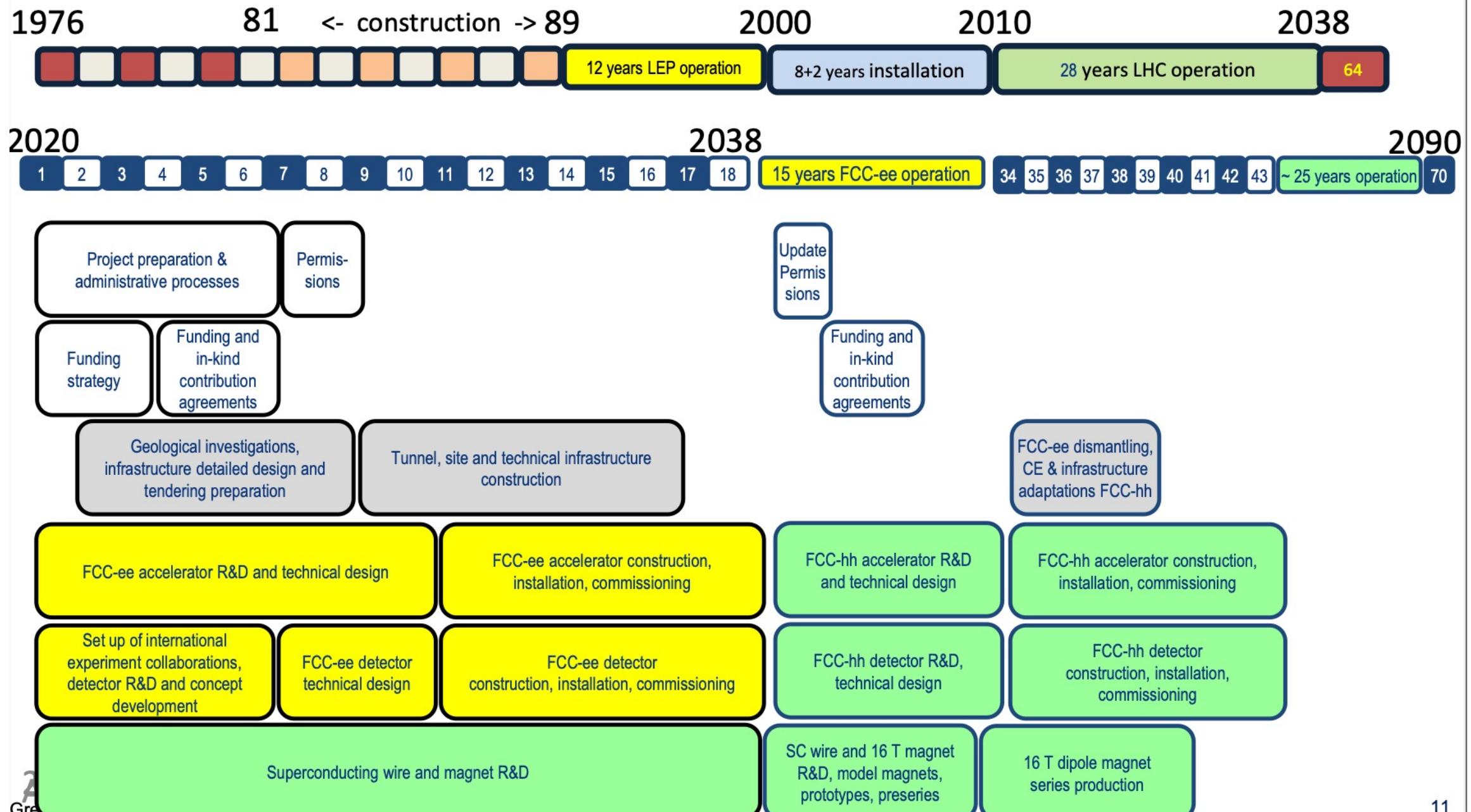
Total construction cost FCC-ee (Z, W, H) amounts to 10.5 BCHF + 1.1 BCHF (tt).

- Associated to a total project duration of ~20 years (2025 – 2045)

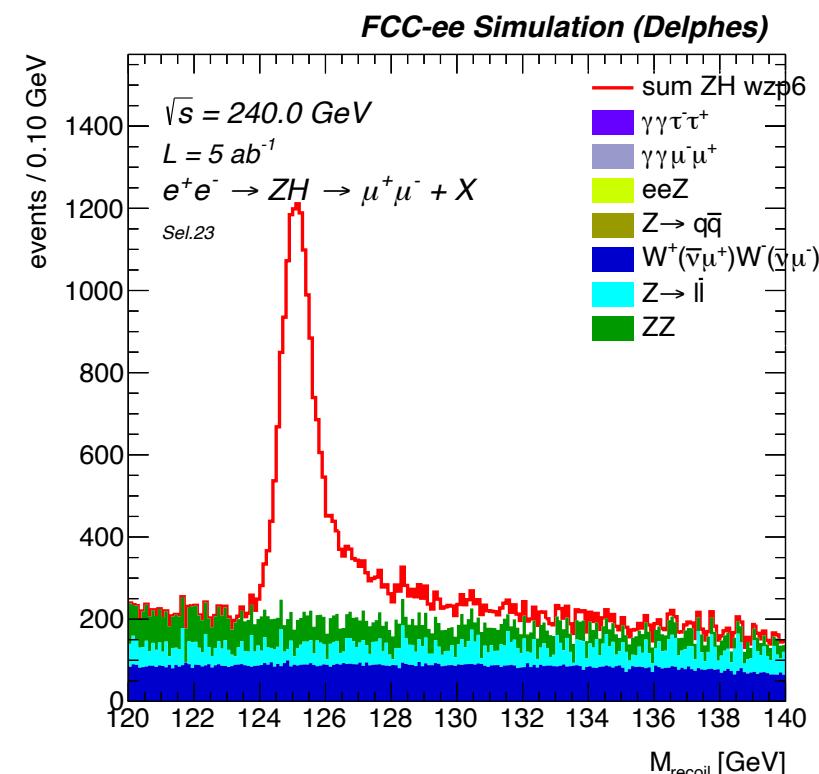
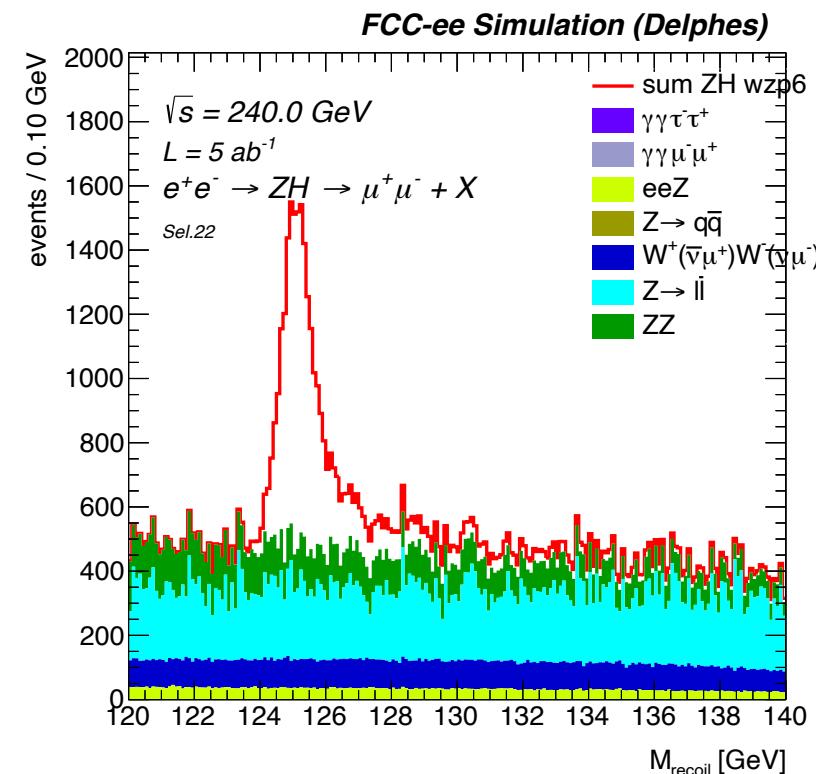
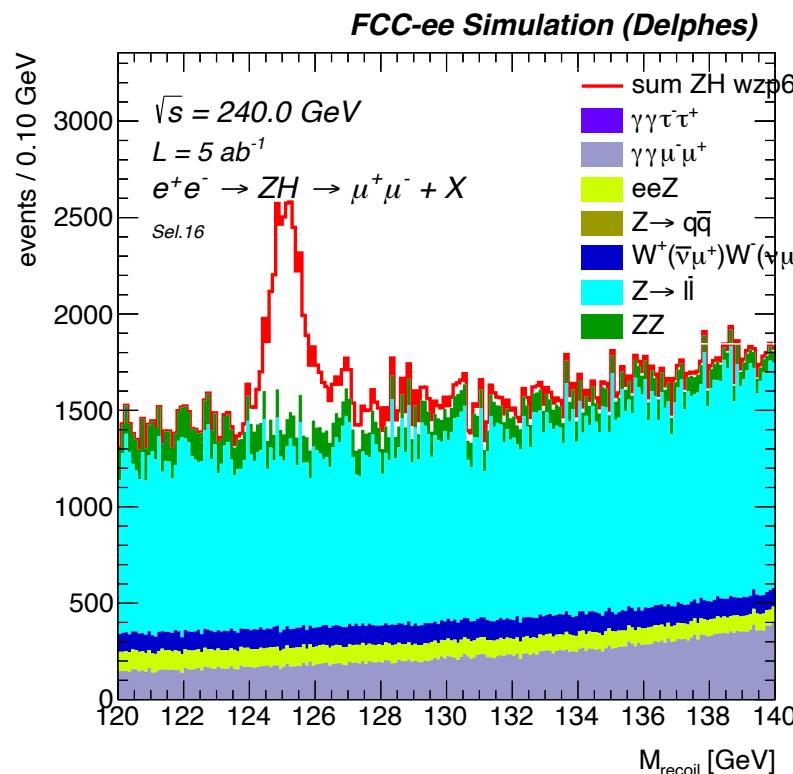
Total construction cost for subsequent FCC-hh amounts to 17 BCHF.

- Associated to a total project duration of ~25 years (2035 – 2060) (FCC-hh stand alone 25 BCHF)

FCC timeline with LEP-LHC



Evaluation of M_{recoil} distribution



APC-0-Selection:

1. At least one Z boson from a $\mu^+\mu^-$ pair
2. $m_{\mu^+\mu^-} \in [86, 96] \text{ GeV}$
3. $M_{recoil} \in [120, 140] \text{ GeV}$

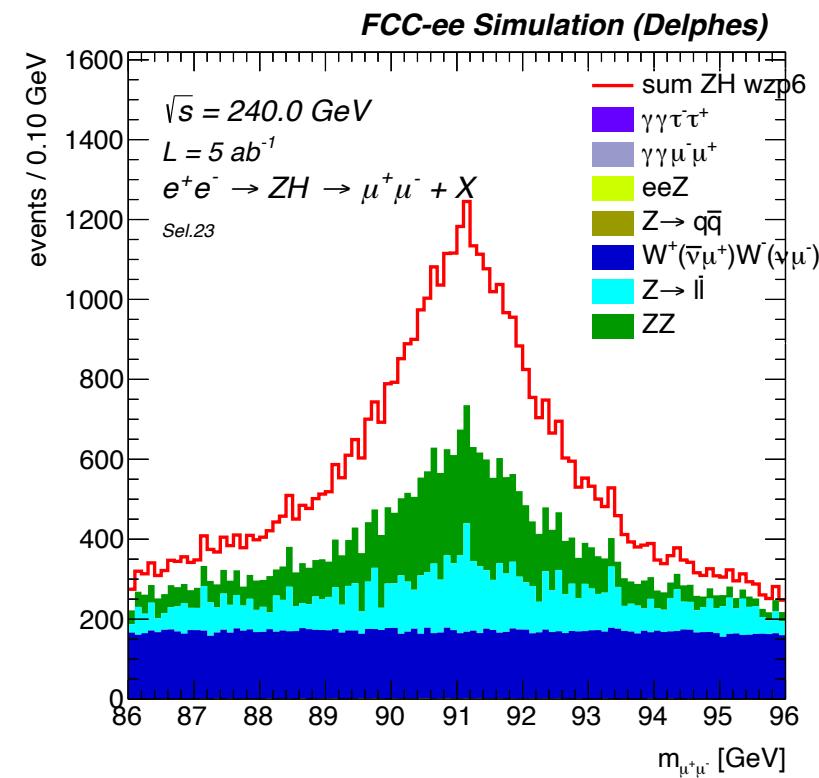
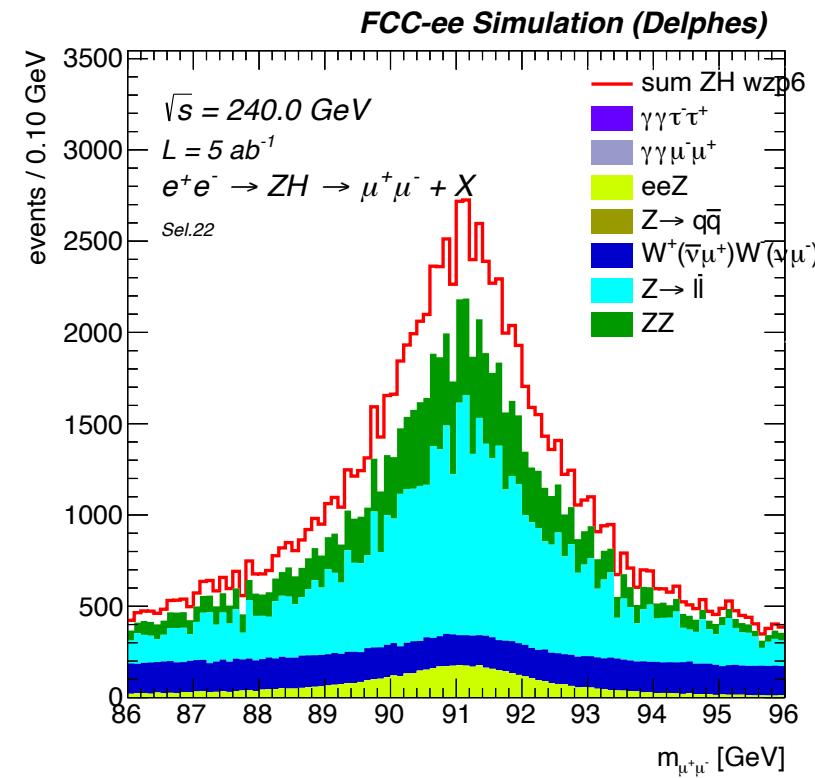
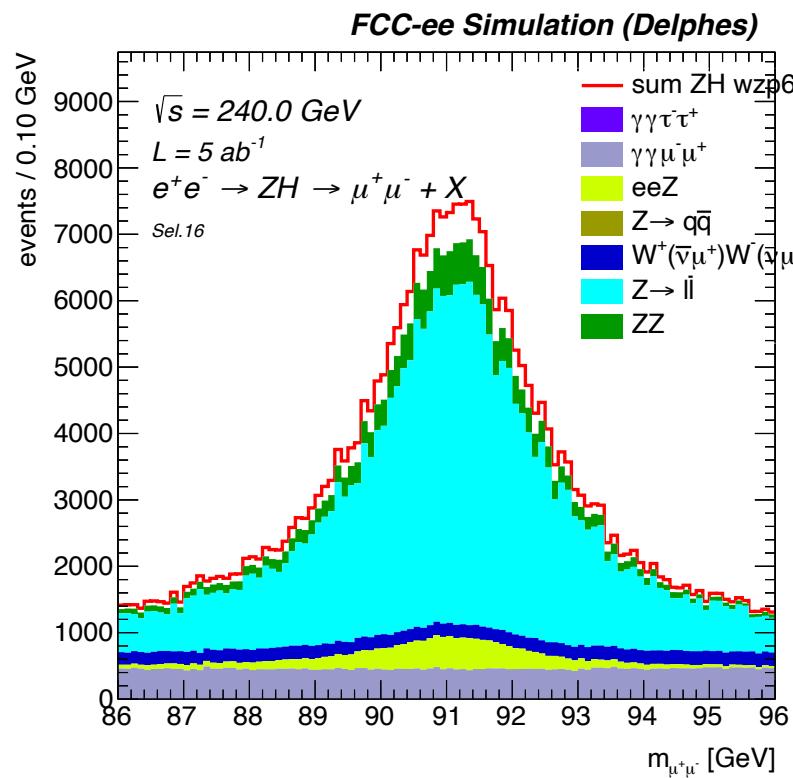
APC-1-Selection:

1. At least one Z boson from a $\mu^+\mu^-$ pair
2. $m_{\mu^+\mu^-} \in [86, 96] \text{ GeV}$
3. $M_{recoil} \in [120, 140] \text{ GeV}$
4. $p_T^{\mu^+\mu^-} \in [20, 70] \text{ GeV}$

APC-2-Selection:

1. At least one Z boson from a $\mu^+\mu^-$ pair
2. $m_{\mu^+\mu^-} \in [86, 96] \text{ GeV}$
3. $M_{recoil} \in [120, 140] \text{ GeV}$
4. $p_T^{\mu^+\mu^-} \in [20, 70] \text{ GeV}$
5. $|\cos \theta_{missing}| < 0.98$

Evaluation of $m_{\mu^+\mu^-}$ distribution



APC-0-Selection:

1. At least one Z boson from a $\mu^+\mu^-$ pair
2. $m_{\mu^+\mu^-} \in [86, 96] \text{ GeV}$
3. $M_{\text{recoil}} \in [120, 140] \text{ GeV}$

APC-1-Selection:

1. At least one Z boson from a $\mu^+\mu^-$ pair
2. $m_{\mu^+\mu^-} \in [86, 96] \text{ GeV}$
3. $M_{\text{recoil}} \in [120, 140] \text{ GeV}$
4. $p_T^{\mu^+\mu^-} \in [20, 70] \text{ GeV}$

APC-2-Selection:

1. At least one Z boson from a $\mu^+\mu^-$ pair
2. $m_{\mu^+\mu^-} \in [86, 96] \text{ GeV}$
3. $M_{\text{recoil}} \in [120, 140] \text{ GeV}$
4. $p_T^{\mu^+\mu^-} \in [20, 70] \text{ GeV}$
5. $|\cos \theta_{\text{missing}}| < 0.98$

Expected value of the coupling constant

$$\sigma_{ZH} \times \mathcal{B}(H \rightarrow X\bar{X}) \propto \frac{g_{HZZ}^2 \times g_{HXX}^2}{\Gamma_H} \quad \text{and} \quad \sigma_{H\nu_e\bar{\nu}_e} \times \mathcal{B}(H \rightarrow X\bar{X}) \propto \frac{g_{HWW}^2 \times g_{HXX}^2}{\Gamma_H},$$

- The σ_{ZH} accuracy could reach 0.5%

[arXiv:2106.15438](https://arxiv.org/abs/2106.15438)

- Obtaining the ZH cross section, one can determine g_{HZZ} and Higgs width (Γ_H)

- g_{HZZ} , g_{HWW} , g_{Hgg} and $g_{H\tau\tau}$ are expected to reach per mille precision

\sqrt{s}	240 GeV		365 GeV	
Integrated luminosity	5 ab^{-1}		1.5 ab^{-1}	
$\delta(\sigma\mathcal{B})/\sigma\mathcal{B}$ (%)	ZH	$\nu_e\bar{\nu}_e$	H	$\nu_e\bar{\nu}_e$
H \rightarrow any	± 0.5		± 0.9	
H $\rightarrow b\bar{b}$	± 0.3	± 3.1	± 0.5	± 0.9
H $\rightarrow c\bar{c}$	± 2.2		± 6.5	± 10
H $\rightarrow gg$	± 1.9		± 3.5	± 4.5
H $\rightarrow W^+W^-$	± 1.2		± 2.6	± 3.0
H $\rightarrow ZZ$	± 4.4		± 12	± 10
H $\rightarrow \tau^+\tau^-$	± 0.9		± 1.8	± 8
H $\rightarrow \gamma\gamma$	± 9.0		± 18	± 22
H $\rightarrow \mu^+\mu^-$	± 19		± 40	
H \rightarrow invisible	< 0.3		< 0.6	

Coupling	Precision (%) (κ framework / EFT)
g_{HZZ}	0.17 / 0.26
g_{HWW}	0.41 / 0.27
g_{Hbb}	0.64 / 0.56
g_{Hcc}	1.3 / 1.2
g_{Hgg}	0.89 / 0.82
$g_{H\tau\tau}$	0.66 / 0.57
$g_{H\mu\mu}$	3.9 / 3.8
$g_{H\gamma\gamma}$	1.3 / 1.2
$g_{HZ\gamma}$	10. / 9.3
g_{Htt}	3.1 / 3.1
Γ_H	1.1

Number of events, error and number of entries

Sample	Pre-Selection			APC-2-Selection			#Entries
	#Events	Error	#Entries	#Events	Error		
$Z(\mu^+\mu^-)H$	24178.8	28.6	714893	18181.1	24.8	537560	
$Z(\tau^+\tau^-)H$	32.7	1.1	873	12.4	0.7	330	
$Z(q\bar{q})H$	425.5	5.4	6179	171.5	3.4	2491	
Total Signal	24637.0	35.1	721945	18365.0	28.9	540381	
$W^+(\nu\mu^+)W^-(\bar{\nu}\mu^-)$	133530.9	131.2	1035444	16927.3	46.7	131260	
ZZ(inclusive)	315780.4	463.2	464728	11219.8	87.3	16512	
$Z \rightarrow l\bar{l}$	7846308.6	7389.3	1127515	9471.1	256.7	1361	
Total Main Bkgs.	8295619.8	7983.8	2627687	37618.2	390.8	149133	
$\gamma\gamma\mu\mu$	384090.8	315.2	1484600	4.7	1.1	18	
$\gamma\gamma\tau\tau$	304.3	8.0	1456	6.3	1.1	30	
eeZ	793603.7	286.8	7654357	24.0	1.6	231	
$Z \rightarrow q\bar{q}$	0.0	0.0	0	0.0	0.0	0	
$Z(\nu\bar{\nu})H$	173.8	3.7	2257	69.3	2.3	900	
$Z(e^+e^-)H$	23.4	1.0	587	9.3	0.6	234	
Additional Bkgs	1178195.9	614.7	9143257	113.5	6.7	1413	

➤ Final-Selection

- At least one Z boson from a $\mu^+\mu^-$ pair.
- $m_{\mu^+\mu^-} \in [86, 96] \text{ GeV}$
- $p_T^{\mu^+\mu^-} \in [20, 70] \text{ GeV}$
- $|\cos \theta_{missing}| < 0.98$
- $M_{\text{recoil}} \in [120, 140] \text{ GeV}$

Compared to Pre-Selection,
Final-Selection keeps $\sim 75\%$ signals
but rejects

➤ Main background:

- $\sim 87\% WW$
- $\sim 96\% ZZ$
- $\sim 99.88\% Z \rightarrow l\bar{l}$

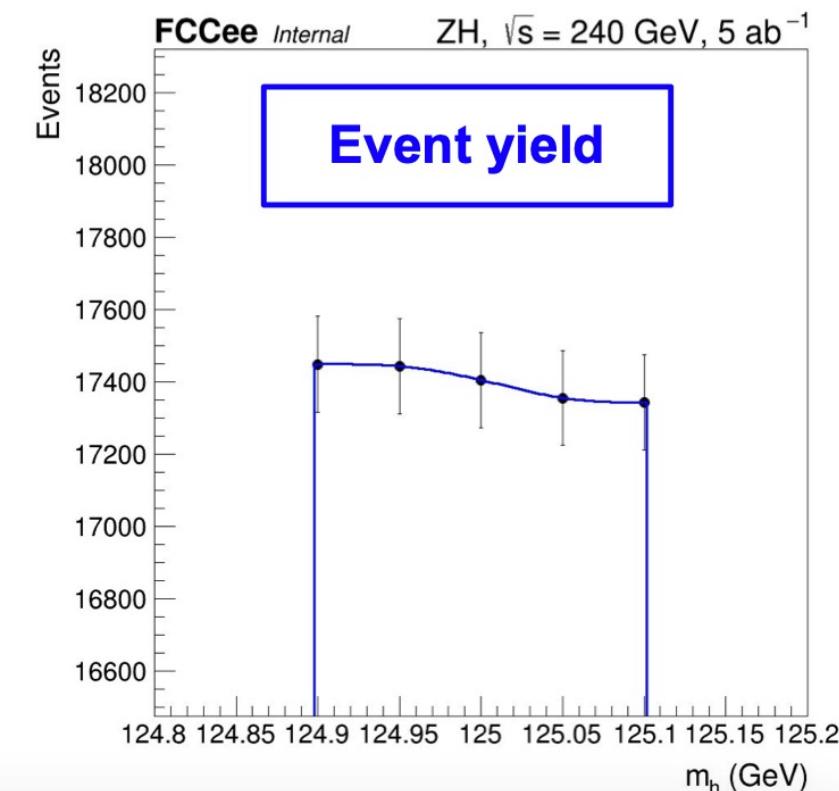
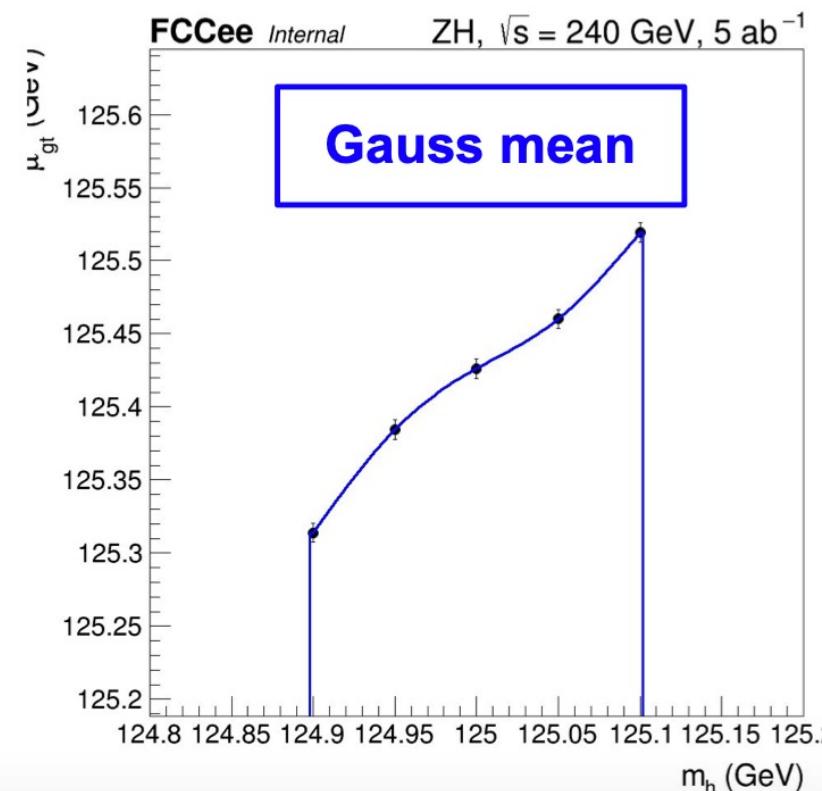
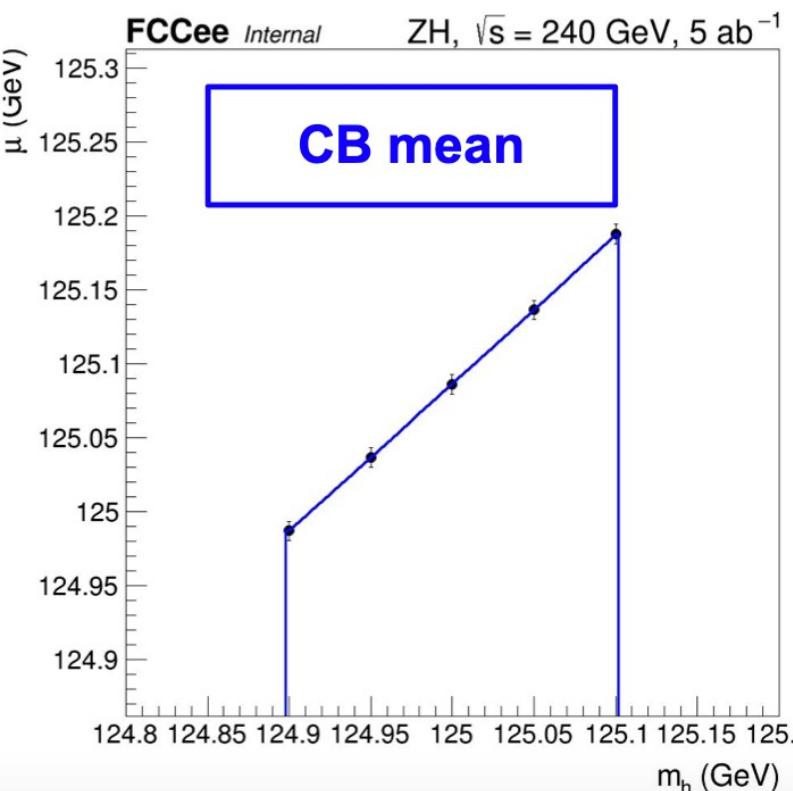
➤ Additional background

- $\sim 99.99\% \gamma\gamma\mu\mu$,
- $\sim 99.93\% eeZ$

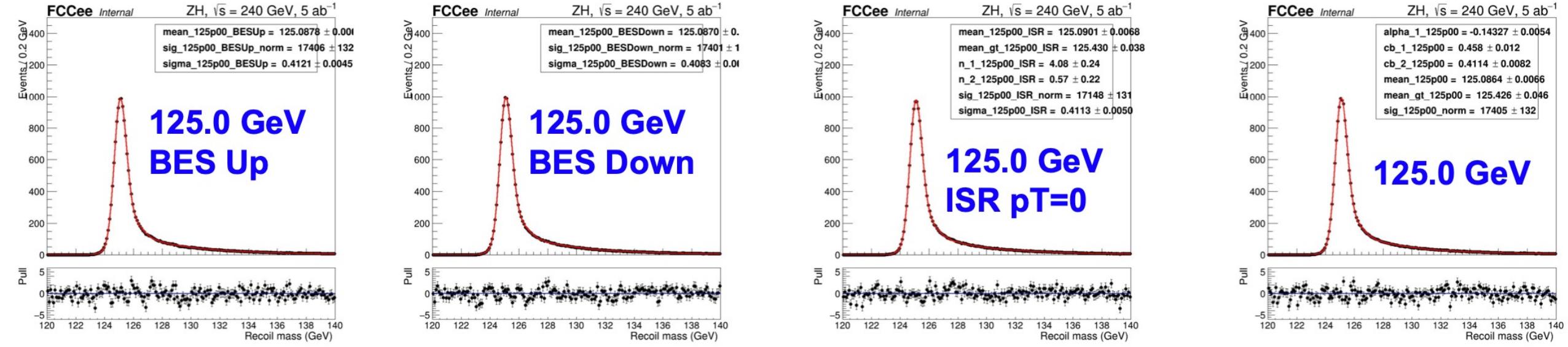
Fitting model and parameter settings

How does the signal shape change as function of (true) Higgs mass m_h ?

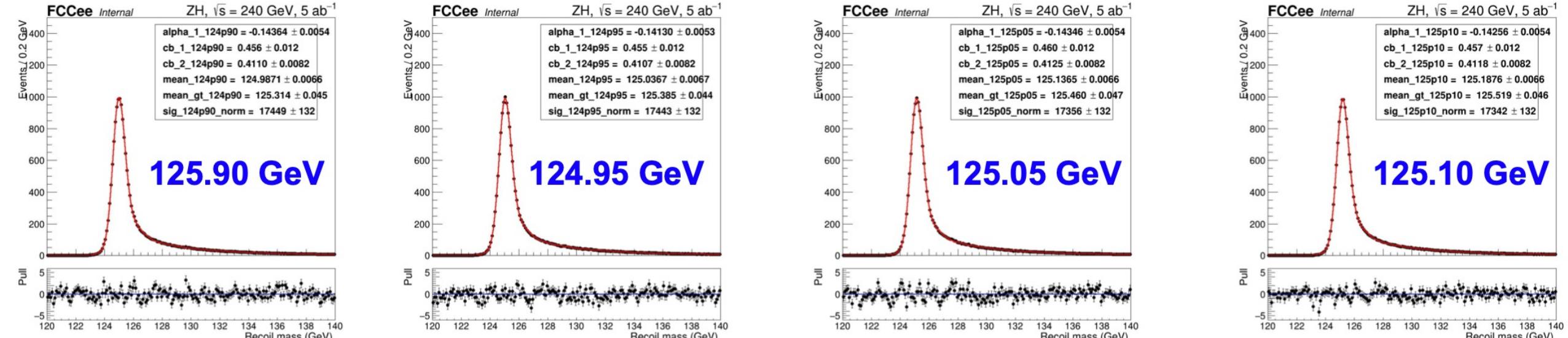
- Generated extra samples around 125 GeV: 124.9, 124.95, 125.05, 125.1 GeV
- Found only significant dependency on the mean (both CB and Gauss) and yields
 - Dependency as function of m_h described using Spline
- Other parameters set as constant (best-fit parameters @ 125.0 GeV, see backup for all fits)



Signal fits with 2CBG

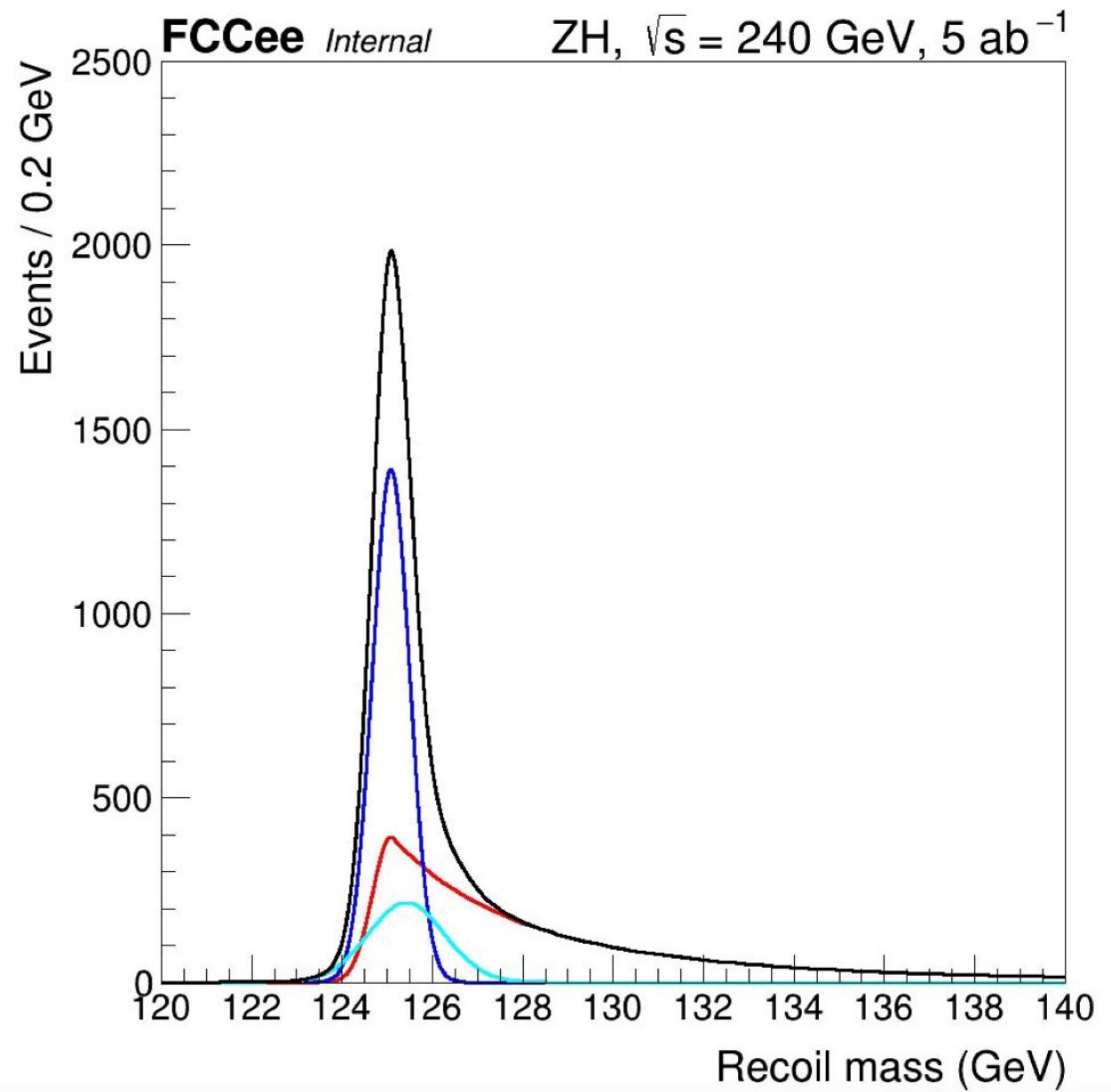


No bias in fits observed



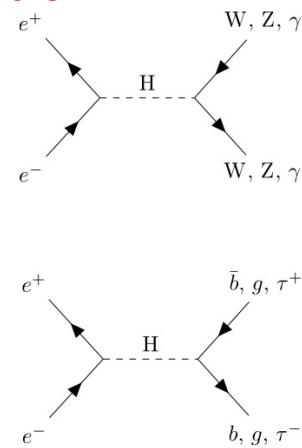
Decomposition of 2CBG

Signal PDF	1.000
CB1	0.4580
CB2	0.4114
Gauss	0.1306

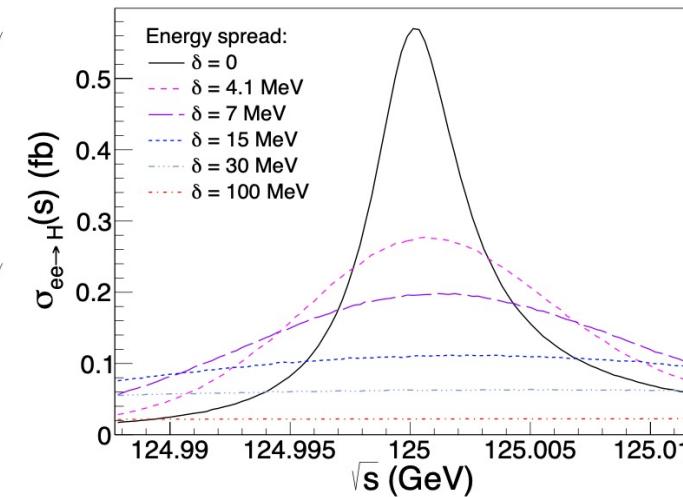
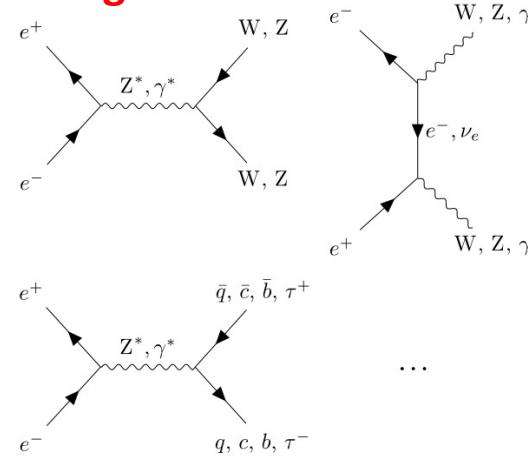


The electron Yukawa coupling via resonant s-channel $e^+e^- \rightarrow H$ production

Signals



Backgrounds:



[arXiv:2107.02686](https://arxiv.org/abs/2107.02686)

$$\sigma_{ee \rightarrow H} = \frac{4\pi \Gamma_H \Gamma(H \rightarrow e^+e^-)}{(s - m_H^2)^2 + m_H^2 \Gamma_H^2},$$

- Yukawa couplings have been measured so far only for t, b and τ (μ, c after HL-LHC)
- Higgs decay to e^+e^- is unobservable: $BR(H \rightarrow e^+e^-) \propto m_e^2 \approx 5 \times 10^{-9}$
- Peak cross-section: $\sigma_{ee \rightarrow H} = 1.64 \text{ fb}$ ($m_H = 125 \text{ GeV}, \Gamma_H = 4.2 \text{ MeV}$)

Challenges:

- Centre-of-mass energy at Higgs pole (Accurate knowledge of Higgs mass (~MeV)) → (feasible at FCC-ee with recoil method)
- ISR and beam-energy spread (~MeV but still deliver large L_{int}) → If $(\delta_{\sqrt{s}}, L_{int}) = (4.1 \text{ MeV}, 10 \text{ ab}^{-1})$
then $\sigma_{e^+e^- \rightarrow H} = 0.28 \text{ fb}$
- Existence of multiple backgrounds

Fundamental Physics motivations:

- Electron Yukawa coupling is measurable
- New particle that is quasi-degenerate with Higgs boson mass?

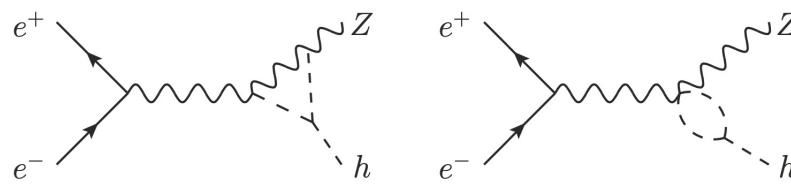
$H \rightarrow gg$	$H \rightarrow WW^* \rightarrow \ell\nu 2j; 2\ell 2\nu; 4j$	$H \rightarrow ZZ^* \rightarrow 2j 2\nu; 2\ell 2j; 2\ell 2\nu$	$H \rightarrow b\bar{b}$	$H \rightarrow \tau_{had}\tau_{had}; c\bar{c}; \gamma\gamma$	Combined
1.1σ	$(0.53 \otimes 0.34 \otimes 0.13)\sigma$	$(0.32 \otimes 0.18 \otimes 0.05)\sigma$	0.13σ	$< 0.02\sigma$	1.3σ

Its feasibility study is still on going

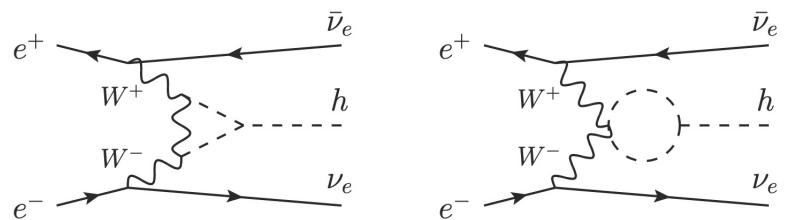
Trilinear Higgs Self-coupling

Trilinear coupling:

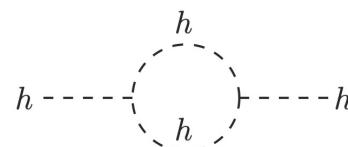
□ Higgs strahlung: $e^+e^- \rightarrow ZH$



□ WW-fusion: $e^+e^- \rightarrow \nu\bar{\nu}_e H$



□ Higgs self-energy



$$\kappa_\lambda \equiv \frac{\lambda_3}{\lambda_3^{\text{SM}}}, \quad \lambda_3^{\text{SM}} = \frac{m_h^2}{2v^2}.$$

$$\Sigma_{\text{NLO}} = Z_H \Sigma_{\text{LO}} (1 + \kappa_\lambda C_1)$$

- Including all the FCC-ee running, a model-independent precision of $\pm 42\%$ can be achieved on k_λ reduced to $\pm 34\%$ in combination with HL-LHC, and to $\pm 12\%$ when only k_λ is allowed to vary
- FCC-hh has the potential to reach a precision of $\sim 3\text{-}5\%$ of λ_3 from di-Higgs production, in combination with the precise Higgs decay branching ratio measurements from the FCC-ee
- With four IPs, the first 5σ demonstration of the Higgs self-coupling is within reach in 15 years at FCC-ee

