

Publishing Statistical Models

— getting the most out of particle physics experiments —

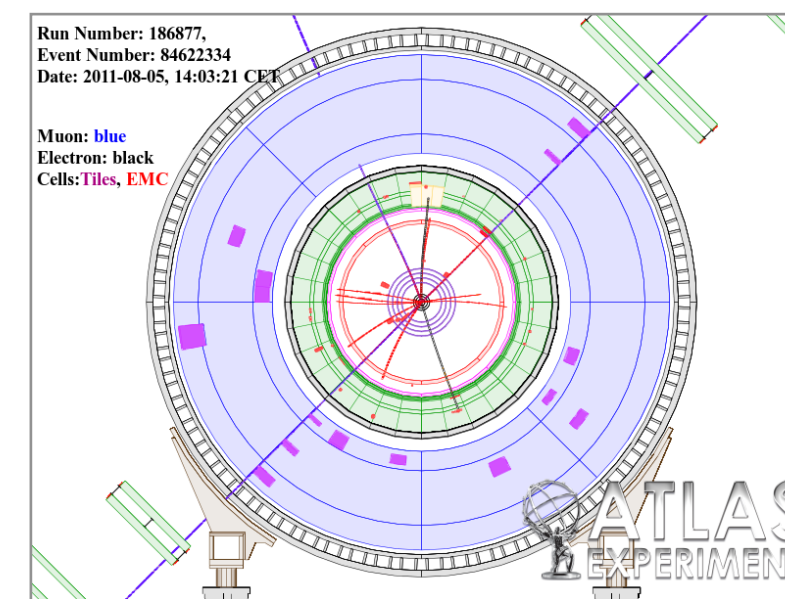
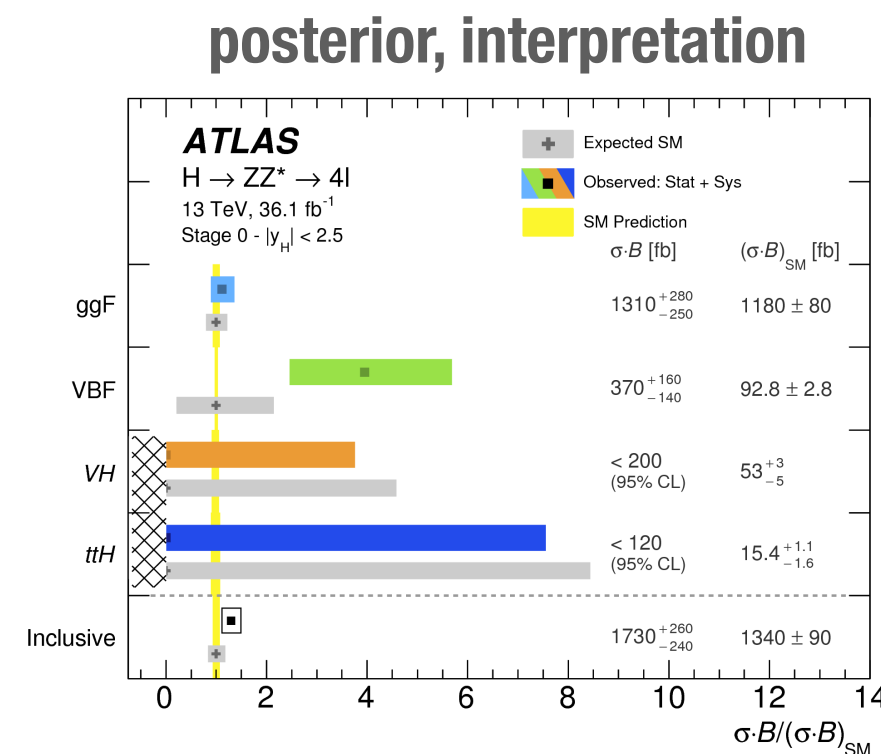
Sabine Kraml

LPSC Grenoble

Introduction

In particle physics experiments, the statistical nature of the data is typically quantified by ascribing to it a probability, as specified by a **statistical model** $p(\text{data}|\text{theory})$

$$p(\text{theory}|\text{data}) = \frac{p(\text{data}|\text{theory})}{p(\text{data})} p(\text{theory})$$



prior

$$\mathcal{L} = -\frac{1}{4} F_{\mu\nu} F^{\mu\nu} + i\bar{\psi}\not{D}\psi + h.c. + \bar{\psi}_i y_{ij} \psi_j \phi + h.c. + \frac{1}{2} \partial_\mu \phi^2 - V(\phi)$$

Introduction

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Primary measurements

Parameters of interest (POIs)

$$p(x, y | \mu, \theta) = p(x | \mu, \theta) p(y | \theta)$$

auxiliary data

nuisance parameters

Probability density of the auxiliary data

The values y are often estimates of corresponding nuisance parameters, and their probability may be, e.g., a Gaussian with a specified standard deviation

The diagram illustrates the components of a statistical model. At the top, 'Primary measurements' and 'Parameters of interest (POIs)' are labeled. Arrows point from these labels to the variables x and μ in the joint probability density function $p(x, y | \mu, \theta)$. Below the equation, 'auxiliary data' and 'nuisance parameters' are labeled, with arrows pointing to the variables y and θ respectively. To the right of the equation, a text box explains that y represents the probability density of the auxiliary data, often being estimates of nuisance parameters like a Gaussian with a specified standard deviation.

Describes the probabilistic dependence of the *observable* data on the parameters of interest and the nuisance parameters.

When observed data are entered into the stat. model, this becomes the **likelihood** function.

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Describes the probabilistic dependence and the nuisance parameters.

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Essential information for analysis preservation and reuse

In recent years, **a lot of progress** has been made regarding presentation of results, reinterpretation efforts, Open Data, etc.

Publication of the full statistical models is a logical next step to maximise the shelf life and the scientific return of exp. analyses; **technical solutions exist** to make this feasible.

Publishing statistical models: Getting the most out of particle physics experiments

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September 9, 2021

Abstract

The statistical models used to derive the results of experimental analyses are of incredible scientific value and are essential information for analysis preservation and reuse. In this paper, we make the scientific case for systematically publishing the full statistical models and discuss the technical developments that make this practical. By means of a variety of physics cases — including parton distribution functions, Higgs boson measurements, effective field theory interpretations, direct searches for new physics, heavy flavor physics, direct dark matter detection, world averages, and beyond the Standard Model global fits — we illustrate how detailed information on the statistical modelling can enhance the short- and long-term impact of experimental results.

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white paper, arXiv:2109.04981

A 20+ year journey

- **2000 First PHYSTAT workshop [CERN 2000-005]**

Unanimous [agreement](#) that particle physicists should [publish likelihood](#) functions, given their fundamental importance in extracting quantitative results from experimental data.

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Recommendation 3b: When feasible, [provide](#) a mathematical description of the final [likelihood function](#) in which experimental data and parameters are clearly distinguished, [...].

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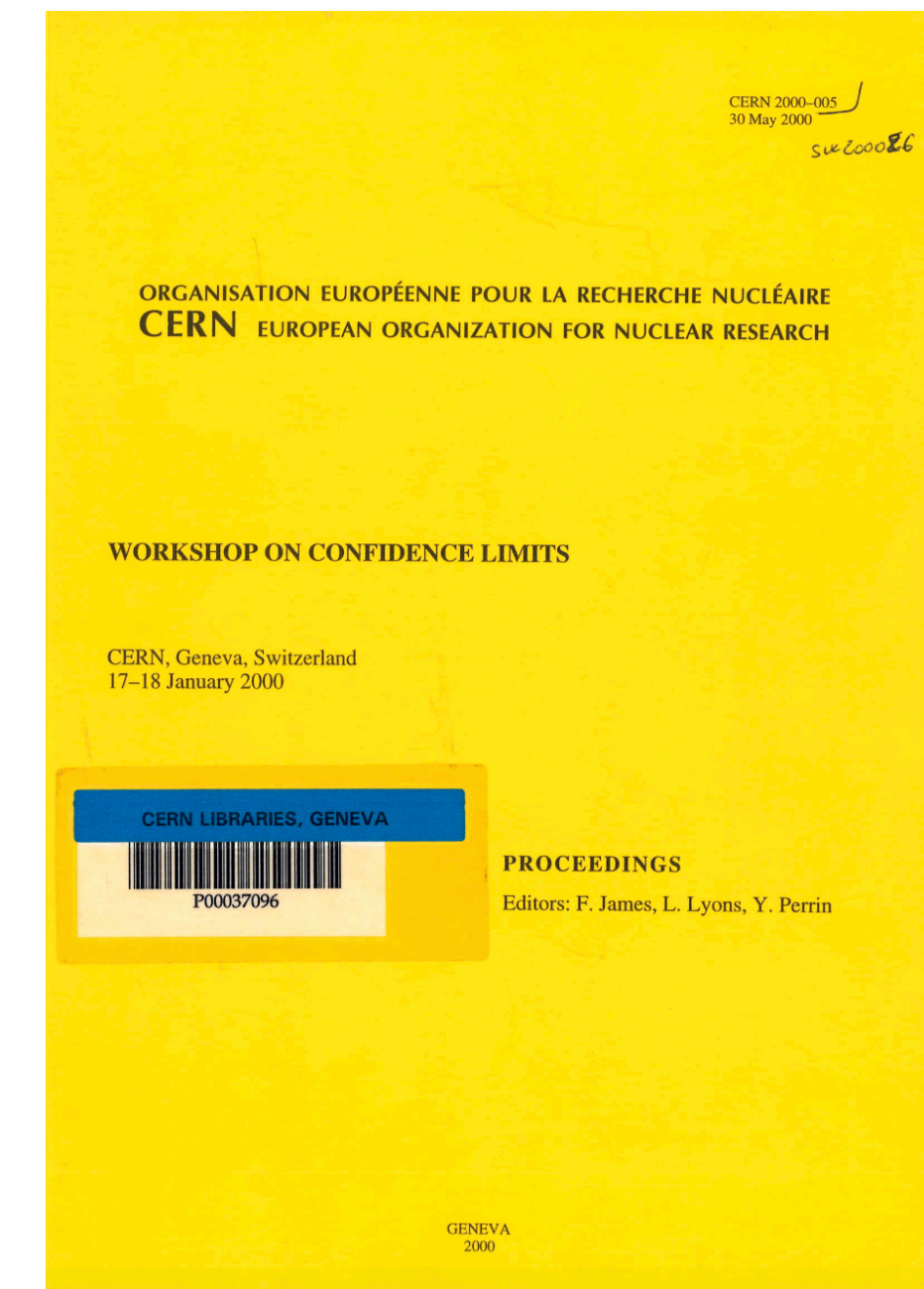
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ATLAS PUB Note
ATL-PHYS-PUB-2019-029
21st October 2019



Reproducing searches for new physics with the ATLAS experiment through publication of full statistical likelihoods

The ATLAS Collaboration

The ATLAS Collaboration is starting to publicly provide likelihoods associated with statistical fits used in searches for new physics on HEPData. These likelihoods adhere to a specification first defined by the HistFactory p.d.f. template. This note introduces a JSON schema that fully describes the HistFactory statistical model and is sufficient to reproduce key results from published ATLAS analyses. This is per-se independent of its implementation in ROOT and it can be used to run statistical analysis outside of the ROOT and RooStats/RooFit framework. The first of these likelihoods published on HEPData is from a search for bottom-squark pair production. Using two independent implementations of the model, one in ROOT and one in pure Python, the limits on the bottom-squark mass are reproduced, underscoring the implementation independence and long-term viability of the archived data.



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New open release allows theorists to explore LHC data in a new way

The ATLAS collaboration releases full analysis likelihoods, a first for an LHC experiment

CERN News

9 JANUARY, 2020 | By Katarina Anthony

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ATLAS releases 'full orchestra' of analysis instruments

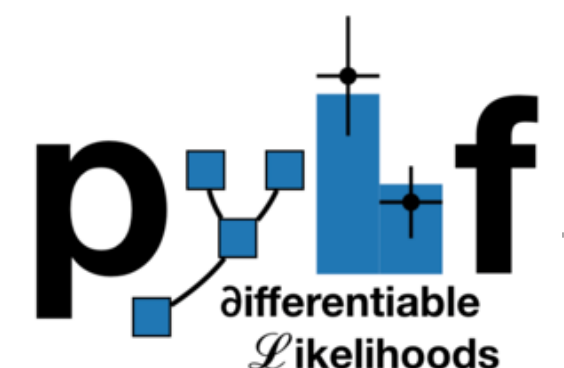
01/14/21 | By Stephanie Melchor

The ATLAS collaboration has begun to publish likelihood functions, information that will allow researchers to better understand and use their experiment's data in future analyses.

Symmetry magazine

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ATLAS releases ‘full analysis’

SCIENTIFIC PRACTICE | MEETING REPORT

LHC reinterpreters think long-term

28 April 2021

CERN Courier

ATLAS PUB Note
ATL-PHYS-PUB-2019-029
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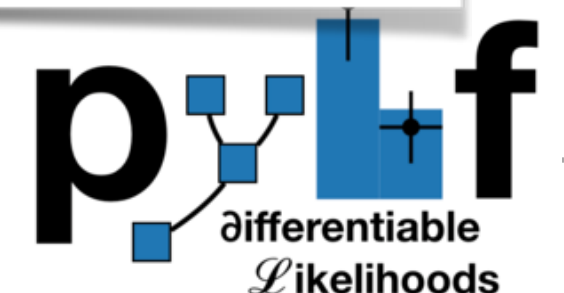
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Summary magazine

ing searches for new physics with the publication of full
ods

likelihoods associated with statistical



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Why it matters

w/o proper statistical model, a Gaussian approximation is forced onto the reuse of experimental results

$$\chi^2(\mu) = \frac{1}{N_{\text{dat}}} \sum_{ij=1}^{N_{\text{dat}}} \left(\mathcal{O}_i^{(\text{th})}(\mu) - \mathcal{O}_i^{(\text{exp})} \right) (\text{cov}^{-1})_{ij} \left(\mathcal{O}_j^{(\text{th})}(\mu) - \mathcal{O}_j^{(\text{exp})} \right)$$

Issues:

- Often lack of information on correlations
- Non-positive-definite cov. matrices on HEPData
- Lack of breakdown of correlated systematic sources
- Systematic uncertainties might not be Gaussian
- Different naming for systematic sources complicates combining processes
- Correlations between processes often not available

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Severely affects many areas:

- Parton distribution functions
- Effective field theory fits
- Higgs physics
- Heavy flavour physics
- Limits on new particles
- Global averages
- BSM Global fits
- DM constraints
-
-

Examples discussed in [arXiv:2109.04981](https://arxiv.org/abs/2109.04981)

Some examples

from the white paper and the hands-on workshop Nov 8-12

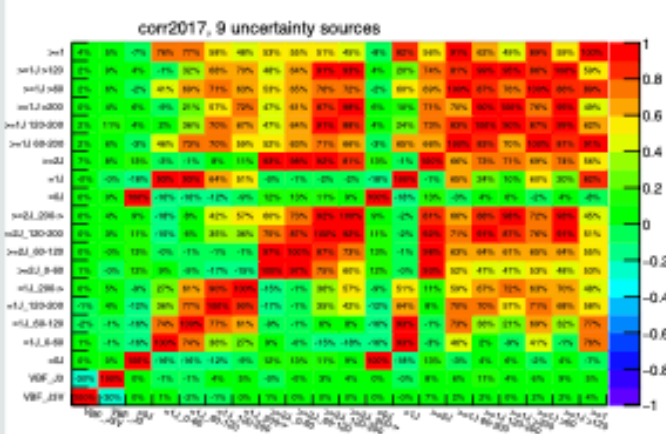
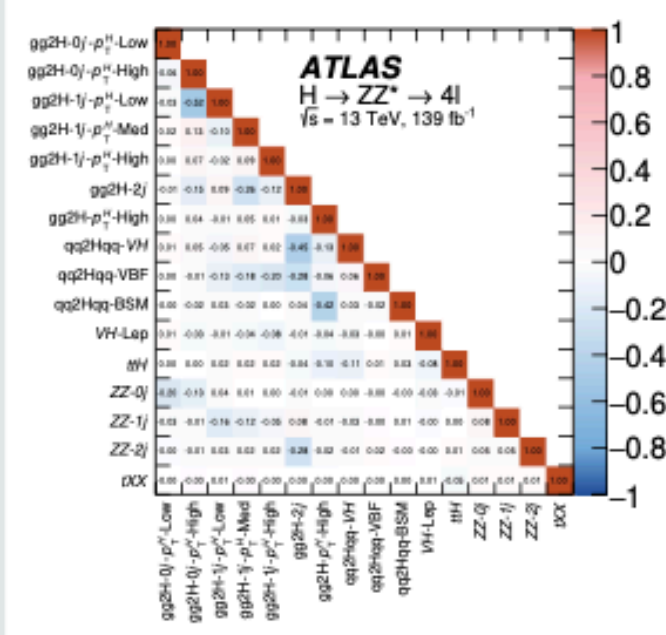
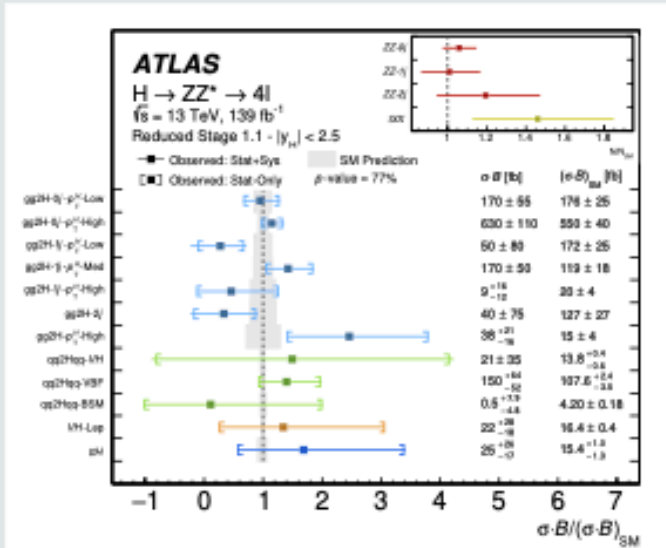
see [paper](#) and [Indico](#) for more

Higgs Measurements — Limitations of Reconstructed LLHs

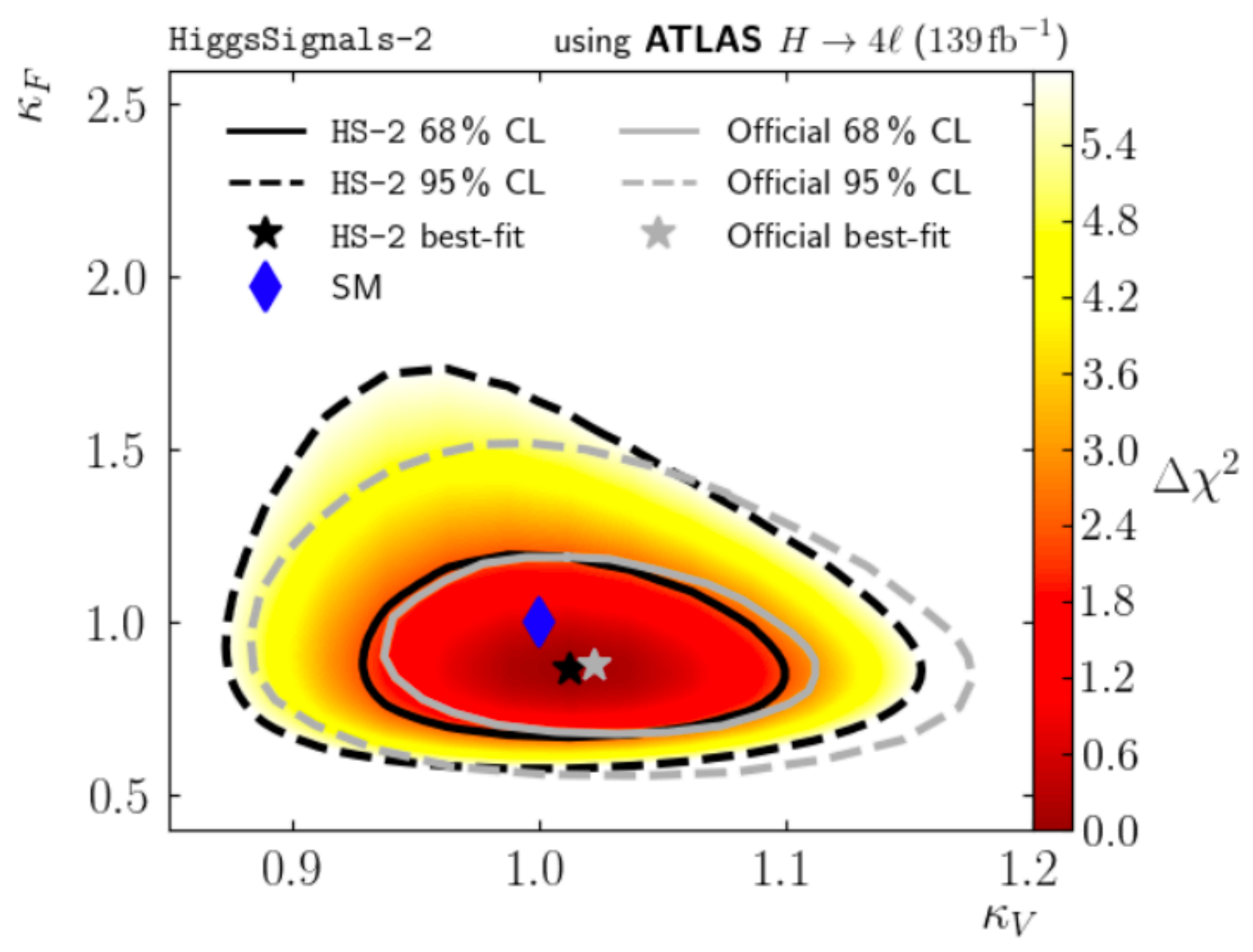
Example: ATLAS $H \rightarrow ZZ \rightarrow 4\ell$ [ATLAS 2004.03447]

HiggsSignals implementation

- measurements (12-bin STXS)
- experimental correlations
- theory correlations [2017 Scheme]



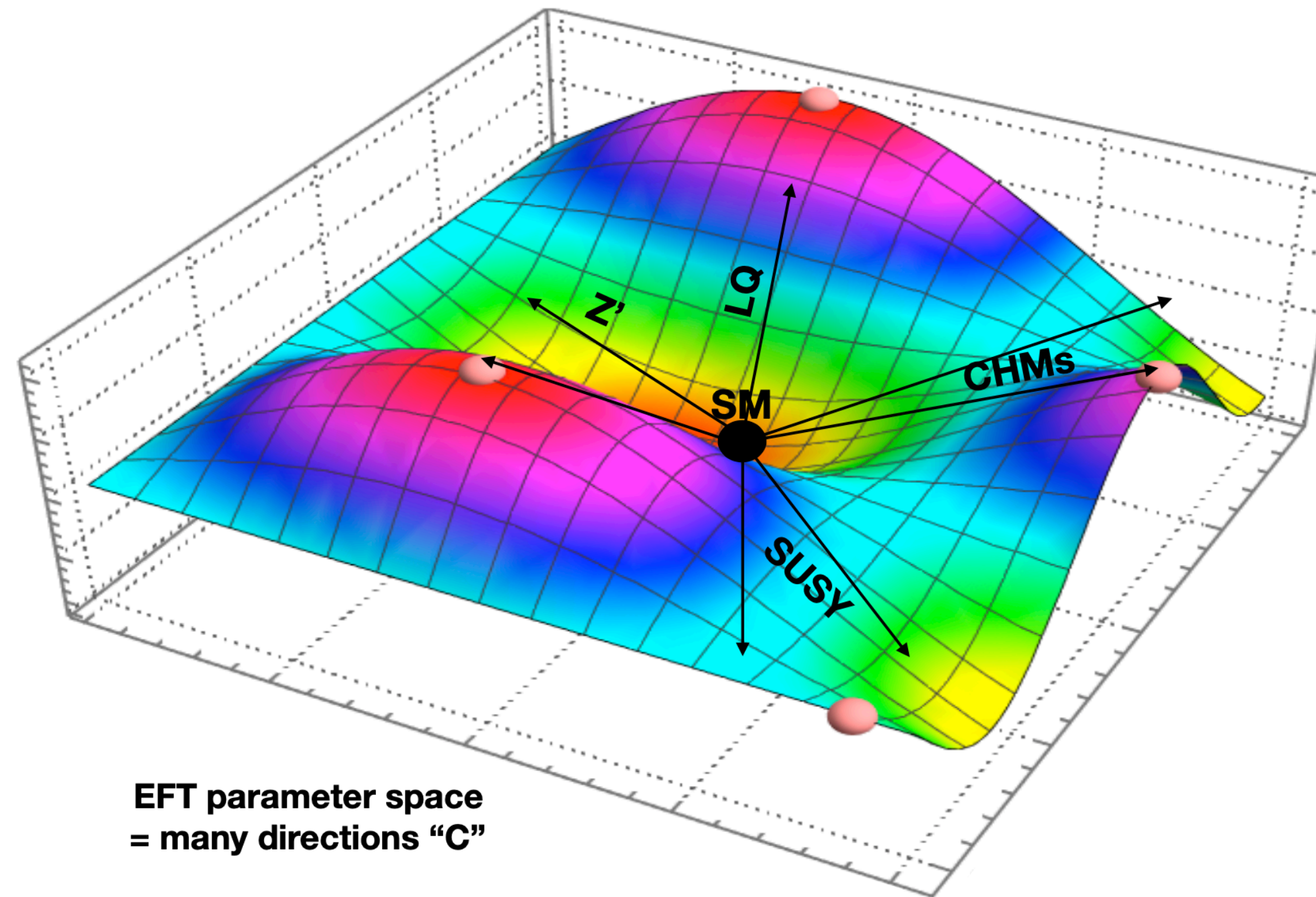
Performance of HiggsSignals compared to official κ -fit.



Jonas Wittbrodt

Publication of Statistical Models
Hands-on workshop 8-12 Nov 2021
<https://indico.cern.ch/event/1088121/>

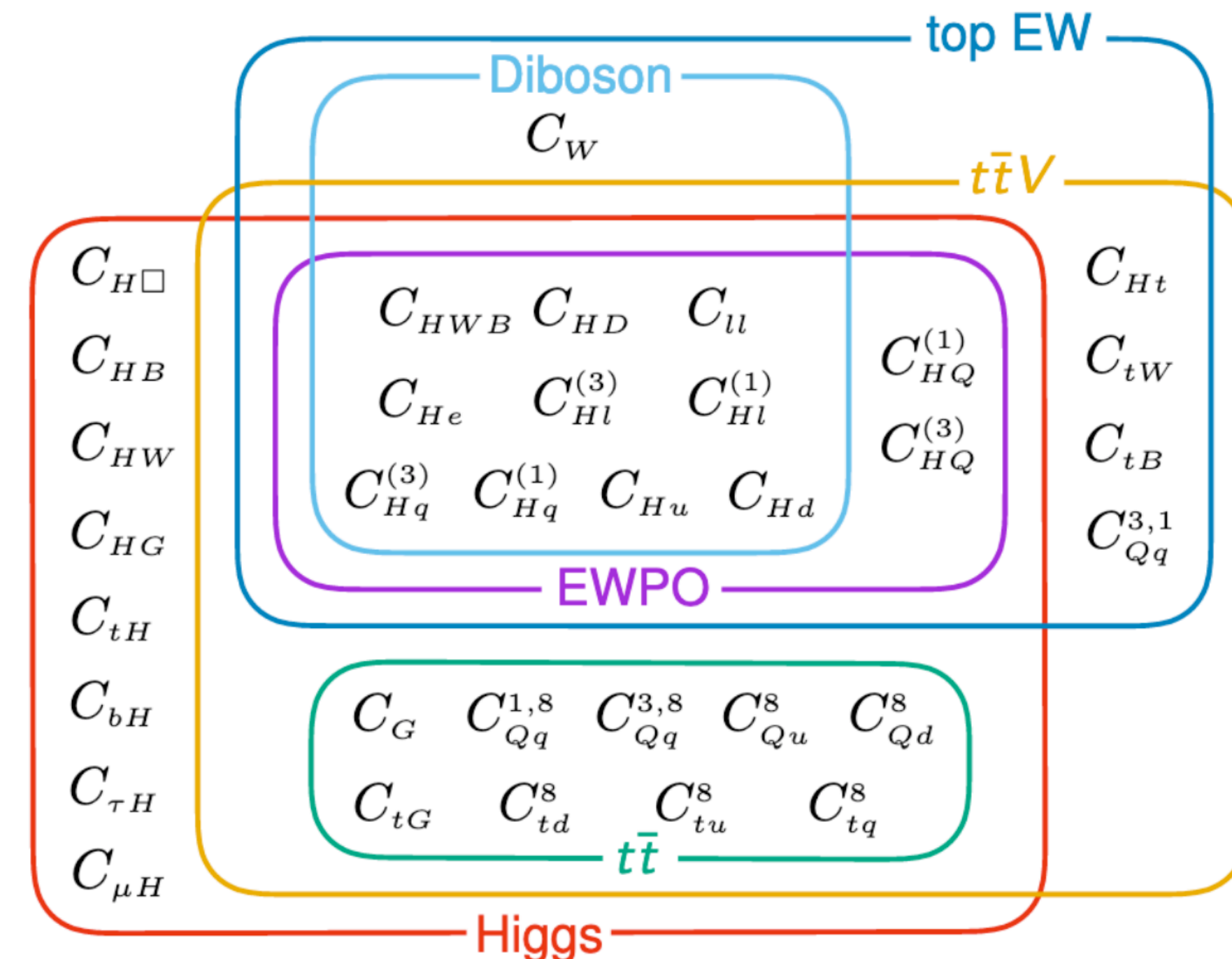
EFT approach



EFT fits involve Higgs, top, diboson, etc. data
Need to choose which observables to use, to **avoid double-counting**
Choices are **neither straightforward nor unique**

Veronica Sanz on EFT fits

Combination is important: each operator affects many observables beyond the LHC group separation

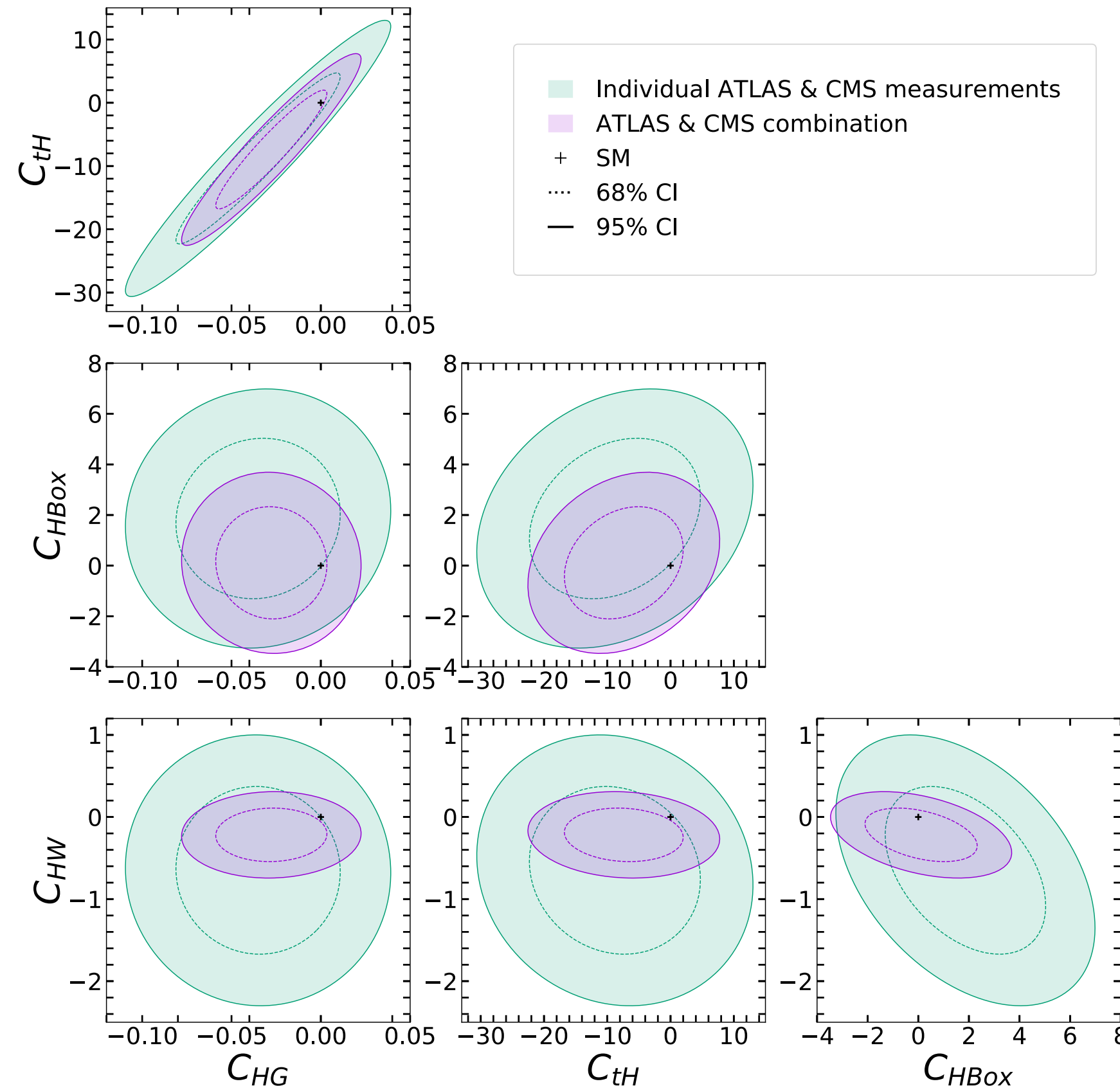


Ellis, Madigan, Mimasu, VS and You
JHEP(21), 2012.02779

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Veronica Sanz on EFT fits

Simple exercise for the white paper:
just Higgs, compare single vs combined experimental results



When considering many observables at once:
With a fixed set of cuts we can compute how the EFT coefficients correlate among different observables but lack information on how all these measurements correlate, even within each experiment (lumi, pdfs, jet resolution, ...)

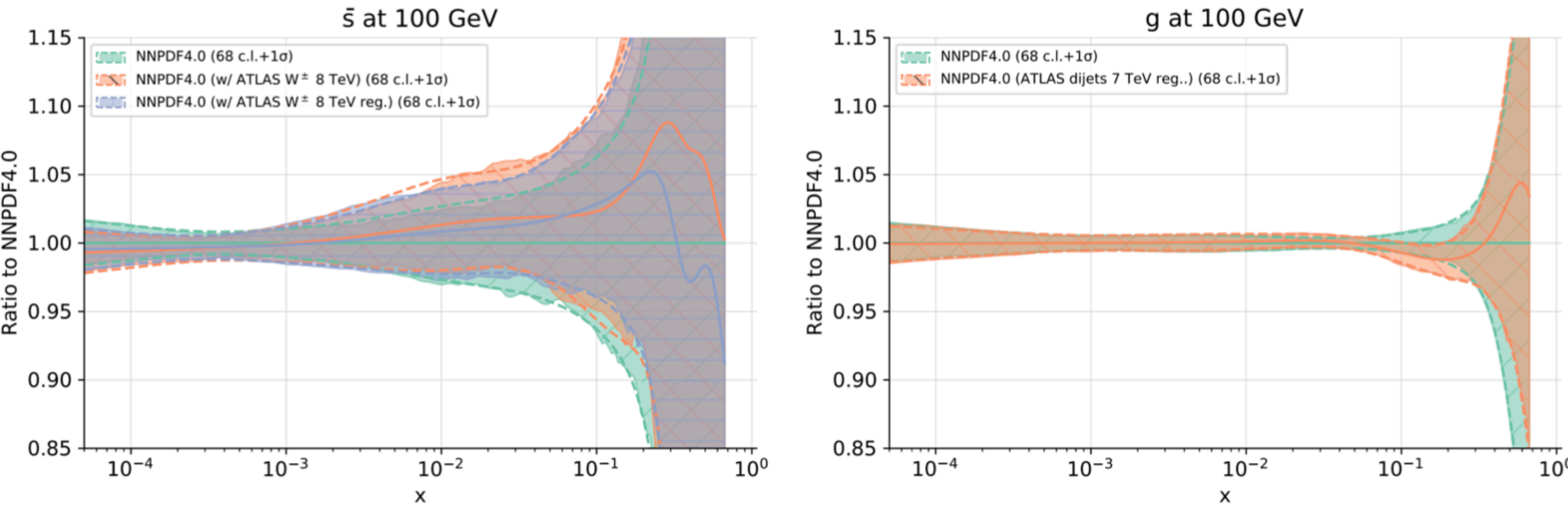
Signal and **backgrounds** can both be affected by EFT effects, and background composition changes within the differential distribution whereas typical analyses assume BSM affects signal only.

“It is clear that with more information we would be able to push further these studies; aim is to find a **robust deviation**, which may not have a clear equivalent in one distribution/ individual channel.”

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ill-defined covariance matrices

One particularly worrisome consequence of the **lack of open likelihoods** is that results may become very sensitive to **small variations of the official correlation model**



Assess impact in fit by transforming the original covariance matrix into a matrix with the **same eigenvectors** but with **clipped eigenvalues** below some cut-off: **stable PDFs** with much lower χ^2

Dataset	N_{dat}	Z_{orig}	χ^2_{orig}	χ^2_{reg}
ATLAS W, Z 7 TeV CC ($\mathcal{L} = 4.6 \text{ fb}^{-1}$)	46	9.01	1.89	0.93
ATLAS W 8 TeV (*)	22	11.28	3.50	1.15
CMS dijets 7 TeV	54	4.70	1.81	1.73
ATLAS dijets 7 TeV	90	9.93	2.14	0.92
CMS 3D dijets 8 TeV (*)	122	4.47	1.50	0.92

minimal modification of correlation model, large impact in fit quality, PDFs stable

Juan Rojo on PDF fits

Key component of predictions for particle, nuclear, and astro-particle experiments.

Address fundamental questions in QCD.

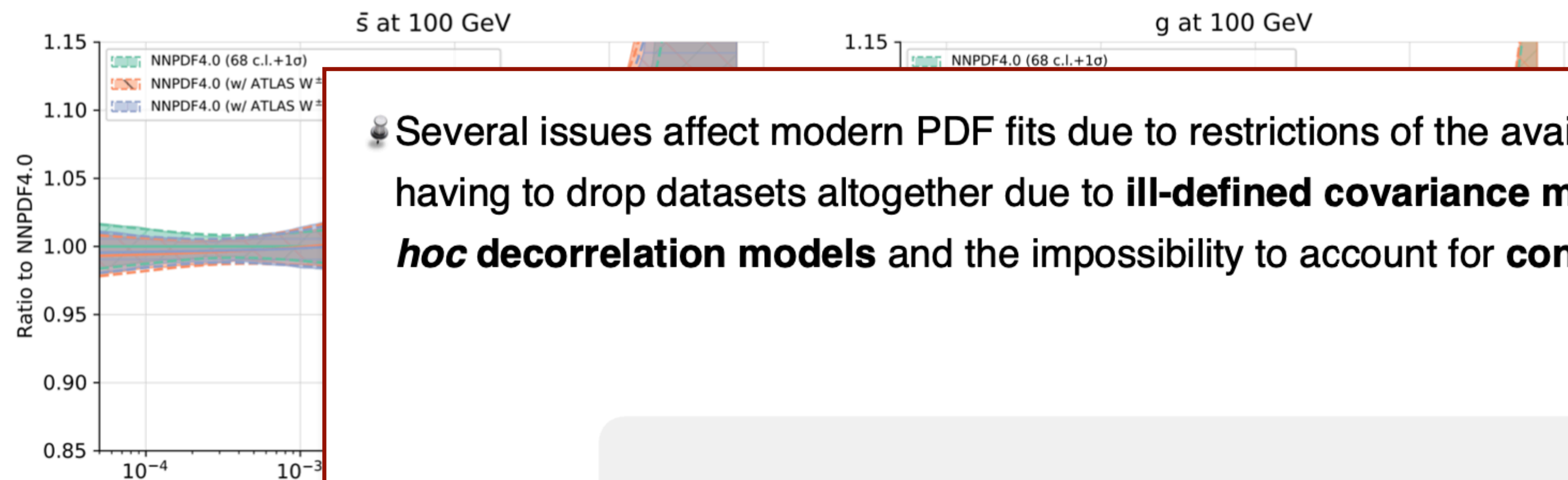
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Key component of predictions for particle, particle

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Several issues affect modern PDF fits due to restrictions of the available information, from having to drop datasets altogether due to **ill-defined covariance matrices** to implementing **ad-hoc decorrelation models** and the impossibility to account for **constraints from search data**

PDF interpretations of the HL-LHC data may become seriously hampered, or even impossible altogether, unless **experiments release their full statistical models**

Assess impact of eigenvectors

Dataset

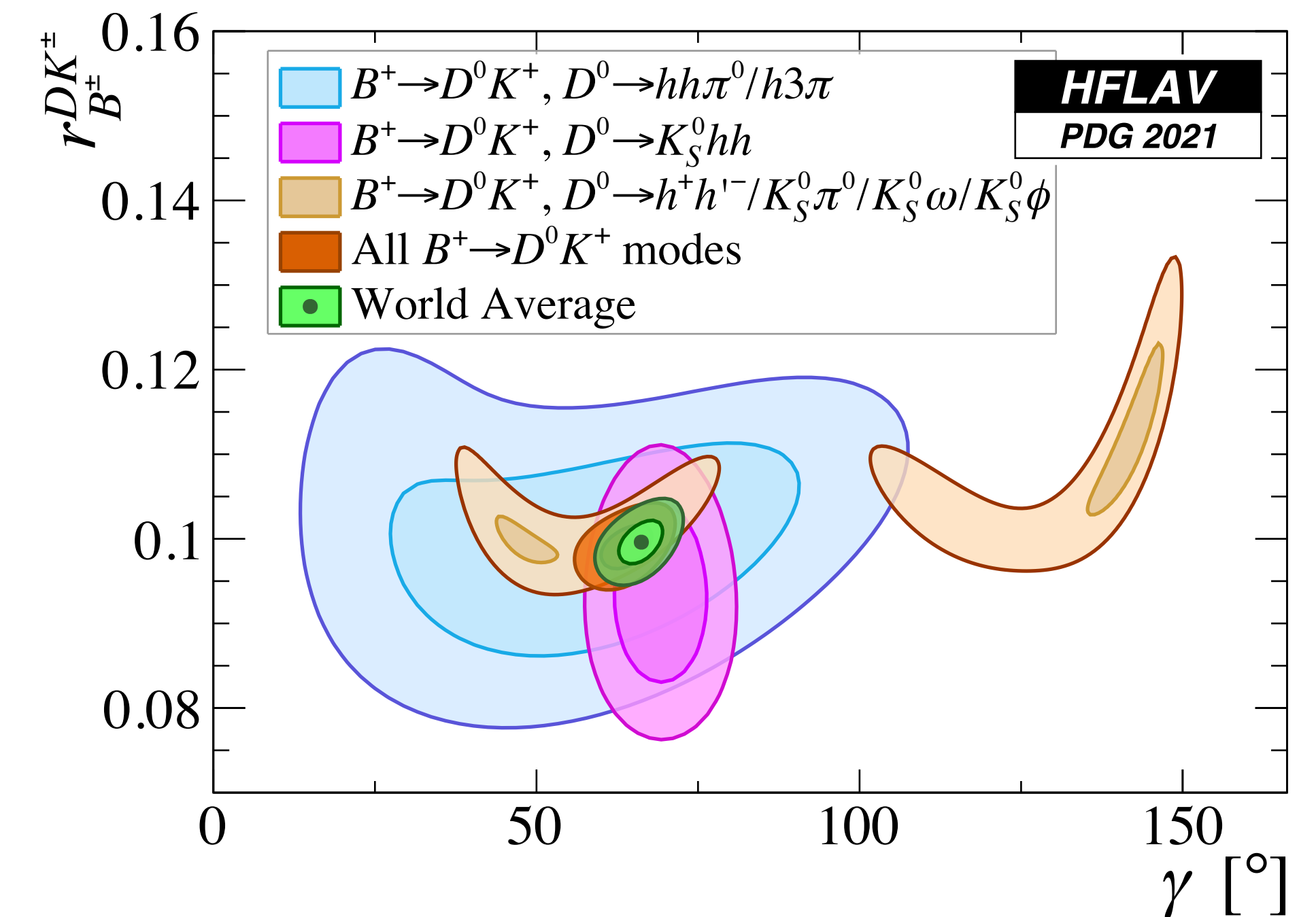
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Averages of measurements

done by, e.g., the Particle Data Group (PDG) or the Heavy Flavor Averaging Group (HFLAV)

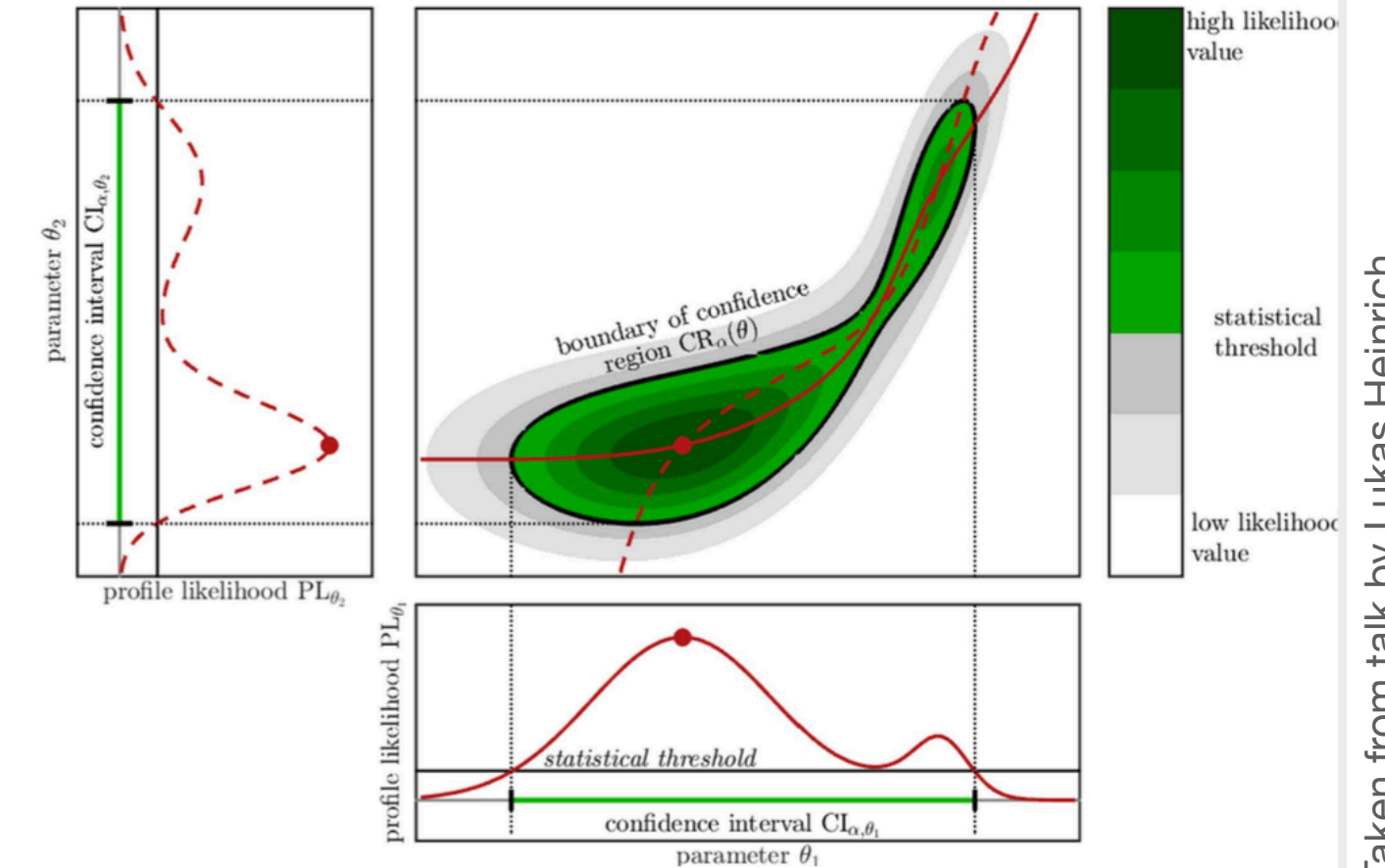
- Likelihood is reasonably well defined if a central value with symmetric uncertainties is quoted. In case of asymmetric uncertainties, assumptions have to be made about the shape of the likelihood function.
- If a limit on the parameter is published the situation is even worse. The likelihood function of the measurement is largely undefined.
- Correlations
 - between measurements by different collaborations
 - between measurements by the same collaboration with different methods or datasetsmust be known if correct averages are to be produced. This information is often not or only partly available.



Ways forward

(Profile) likelihoods: very useful but not sufficient

- In the likelihood, the **data is baked in**
 - cannot evaluate likelihood on new data
 - cannot sample from the model (pseudo-data, toy MC)
- In profile likelihoods, **nuisance parameter are fixed**
 - cannot statistically combine profile likelihoods targeting parameters of interest if they share nuisances
 - cannot update constraint terms (auxiliary measurements)
- Reparametrization in terms of different parameters of interest is not always possible
 - parametrization in terms of quantities such as masses, cross sections, widths, branching fractions, etc., is often more useful than a parametrization in terms of theory-model (Lagrangian) parameters
 - risk of introducing dependencies which can result in a loss of information



Taken from talk by Lukas Heinrich

Publish the full statistical model

Lots of advantages:

ideally in a serialized (written to a file) format that is both human-readable and machine-readable
with a declarative specification that provides a mathematical definition of the model.

- no loss of information
- full set of systematics
- full structure apparent
- long-term preservation and reuse
- simplified approaches still possible but developed / carried out in public

→ tool for better (re)interpretation
→ basis for sound combinations

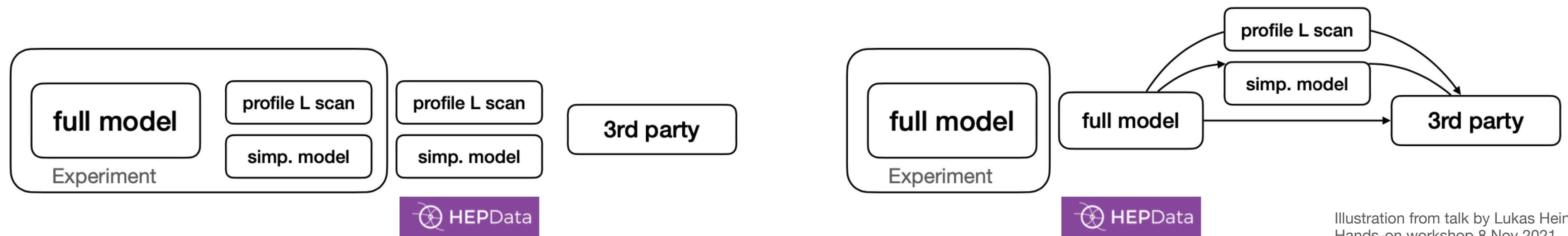


Illustration from talk by Lukas Heinrich
Hands-on workshop 8 Nov 2021

ATLAS took the leap^d

ATL-PHYS-PUB-2019-029

... and started to publish plain-text serialisation of HistFactory workspaces in JSON format

- Provides background estimates, **changes under systematic variations**, and observed data counts at the same fidelity as used in the experiment.

	Description	Modification	Constraint Term c_χ	Input
constrained	Uncorrelated Shape	$\kappa_{scb}(\gamma_b) = \gamma_b$	$\prod_b \text{Pois}(r_b = \sigma_b^{-2} \rho_b = \sigma_b^{-2} \gamma_b)$	σ_b
	Correlated Shape	$\Delta_{scb}(\alpha) = f_p(\alpha \Delta_{scb, \alpha=-1}, \Delta_{scb, \alpha=1})$	$\text{Gaus}(a = 0 \alpha, \sigma = 1)$	$\Delta_{scb, \alpha=\pm 1}$
	Normalisation Unc.	$\kappa_{scb}(\alpha) = g_p(\alpha \kappa_{scb, \alpha=-1}, \kappa_{scb, \alpha=1})$	$\text{Gaus}(a = 0 \alpha, \sigma = 1)$	$\kappa_{scb, \alpha=\pm 1}$
	MC Stat. Uncertainty	$\kappa_{scb}(\gamma_b) = \gamma_b$	$\prod_b \text{Gaus}(a_{\gamma_b} = 1 \gamma_b, \delta_b)$	$\delta_b^2 = \sum_s \delta_{sb}^2$
	Luminosity	$\kappa_{scb}(\lambda) = \lambda$	$\text{Gaus}(l = \lambda_0 \lambda, \sigma_\lambda)$	$\lambda_0, \sigma_\lambda$
free	Normalisation	$\kappa_{scb}(\mu_b) = \mu_b$		
	Data-driven Shape	$\kappa_{scb}(\gamma_b) = \gamma_b$		

Rate modifications defined in HistFactory for bin b , sample s , channel c .

- Usage: RooFit, **pyhf**
- Target: long-term data/analysis preservation, reinterpretation purposes



Resources

gz File

Archive of full likelihoods in the HistFactory JSON format described in ATL-PHYS-PUB-2019-029. Provided are 3 statistical models labeled RegionA, RegionB and RegionC respectively each in their own sub-directory. For each model the background-only model is found in the file named 'BkgOnly.json'. For each model a set of patches for various signal points is provided.

Download

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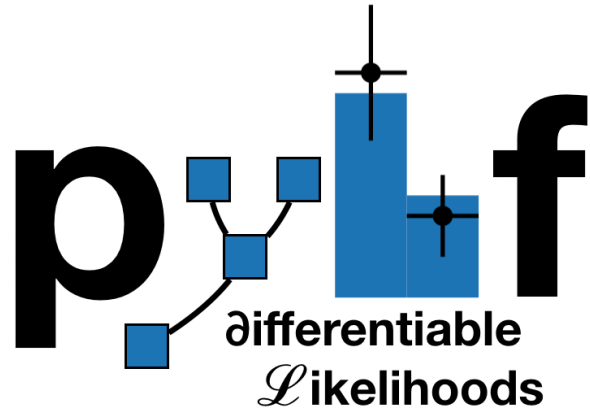
Rate modifications defined in HistFactory for bin b , sample s , channel c .

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Likelihood available

Search for charginos and neutralinos in all-hadronic final states	SUSY	Accepted by PRD	17-AUG-21	13	139 fb ⁻¹
4-top xsec measurement	TOPQ	Accepted by JHEP	22-JUN-21	13	139 fb ⁻¹
Search for gluinos, stops and electroweakinos in RPV models in final states with 1L and many jets	SUSY	Accepted by EPJC	17-JUN-21	13	139 fb ⁻¹
Search for charginos and neutralinos in final states with 3L and MET	SUSY	Accepted by EPJC	03-JUN-21	13	139 fb ⁻¹
Measurement of ttZ cross sections in Run 2	TOPQ	Eur. Phys. J. C 81 (2021) 737	23-MAR-21	13	139 fb ⁻¹
Search for third-generation scalar leptoquarks decaying to a top quark and a tau lepton	EXOT	JHEP 06 (2021) 179	27-JAN-21	13	139 fb ⁻¹
Search for squarks and gluinos in final states 1L, jets and MET	SUSY	Eur. Phys. J. C 81 (2021) 600	05-JAN-21	13	139 fb ⁻¹
Search for charginos and neutralinos in RPV models in final states with 3L (or more)	SUSY	Phys. Rev. D 103, (2021) 112003	20-NOV-20	13	139 fb ⁻¹
Search for displaced leptons	SUSY	Phys. Rev. Lett. 127 (2021) 051802	13-NOV-20	13	139 fb ⁻¹
Search for squarks and gluinos in final states with 0L, jets and MET	SUSY	JHEP 02 (2021) 143	27-OCT-20	13	139 fb ⁻¹
Measurement of the ttbar production cross-section in the lepton+jets channel at 13 TeV	TOPQ	Phys. Lett. B 810 (2020) 135797	24-JUN-20	13	139 fb ⁻¹
Stop pair, long-lived; displaced vertex and displaced muon	SUSY	Phys. Rev. D 102 (2020) 032006	26-MAR-20	13	136 fb ⁻¹
Chargino-neutralino pair; 3 leptons, weak-scale mass splittings	SUSY	Phys. Rev. D 101 (2020) 072001	18-DEC-19	13	139 fb ⁻¹
Chargino-neutralino pair, slepton pair; soft leptons	SUSY	Phys. Rev. D 101 (2020) 052005	28-NOV-19	13	139 fb ⁻¹
Staus; taus	SUSY	Phys. Rev. D 101 (2020) 032009	15-NOV-19	13	139 fb ⁻¹
Chargino-neutralino pair; Higgs boson in final state, 2 b-jets and 1 lepton	SUSY	Eur. Phys. J. C 80 (2020) 691	19-SEP-19	13	139 fb ⁻¹
Stop pair, sbottom pair, gluino pair; two same-sign leptons or three leptons	SUSY	JHEP 06 (2020) 46	18-SEP-19	13	139 fb ⁻¹
Sbottm; b-jets	SUSY	JHEP 12 (2019) 060	08-AUG-19	13	139 fb ⁻¹

Usage in BSM tools



reinterpretation becomes JSON patching

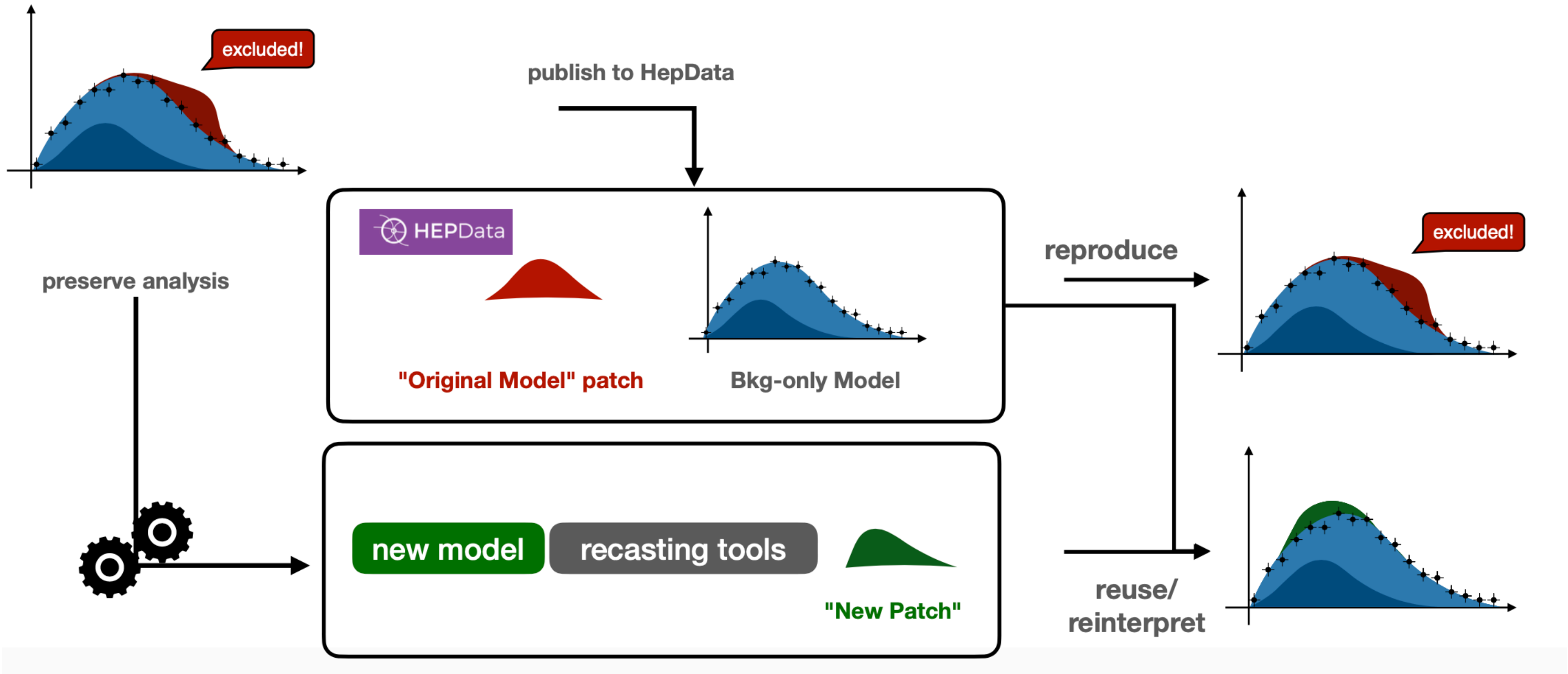


Illustration from talk by Lukas Heinrich
Hands-on workshop 8 Nov 2021

Usage in BSM tools

reinterpretation becomes JSON patching

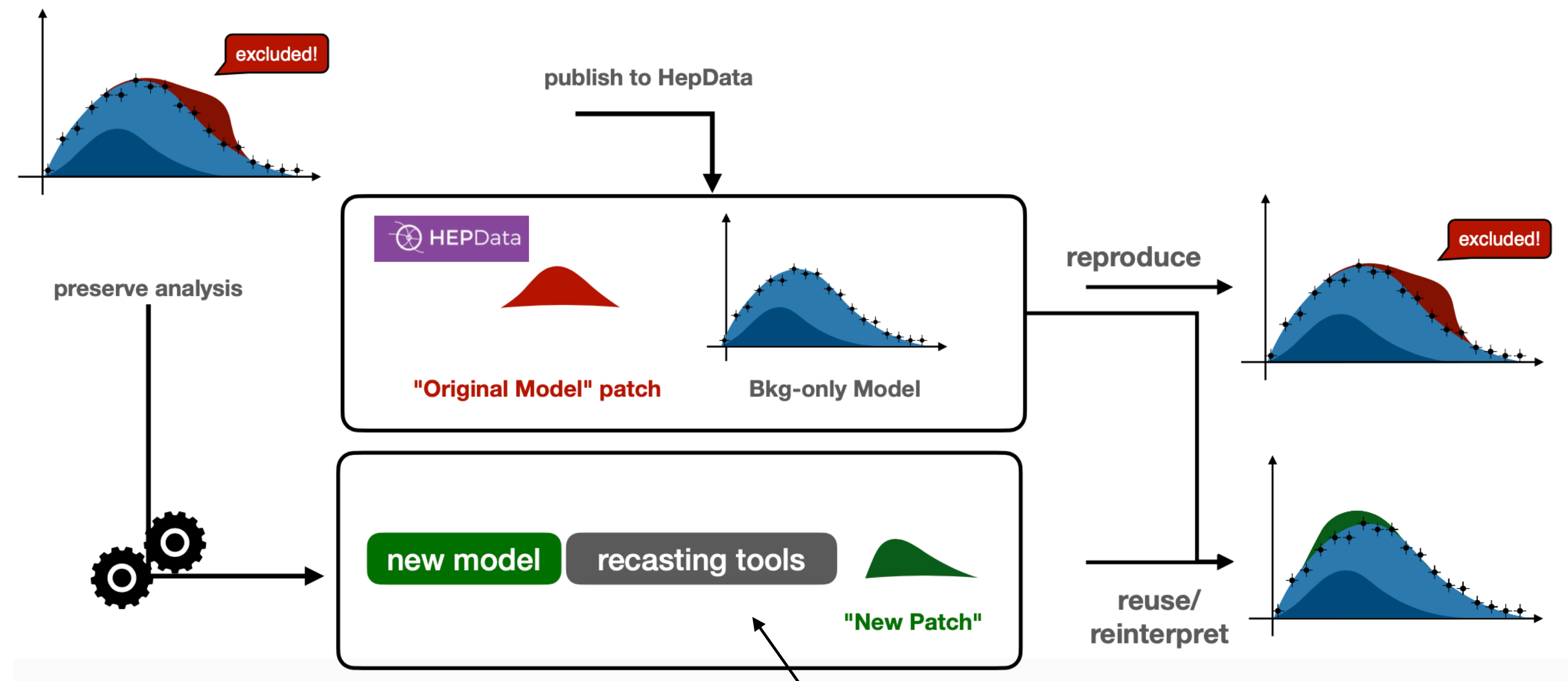


Illustration from talk by Lukas Heinrich
Hands-on workshop 8 Nov 2021



Interfaced to pyhf since SModelS v1.2.4 (now v2.1)
G. Alguero, SK, W. Waltenberger, [arXiv:2009.01809](https://arxiv.org/abs/2009.01809)

Usage in BSM tools

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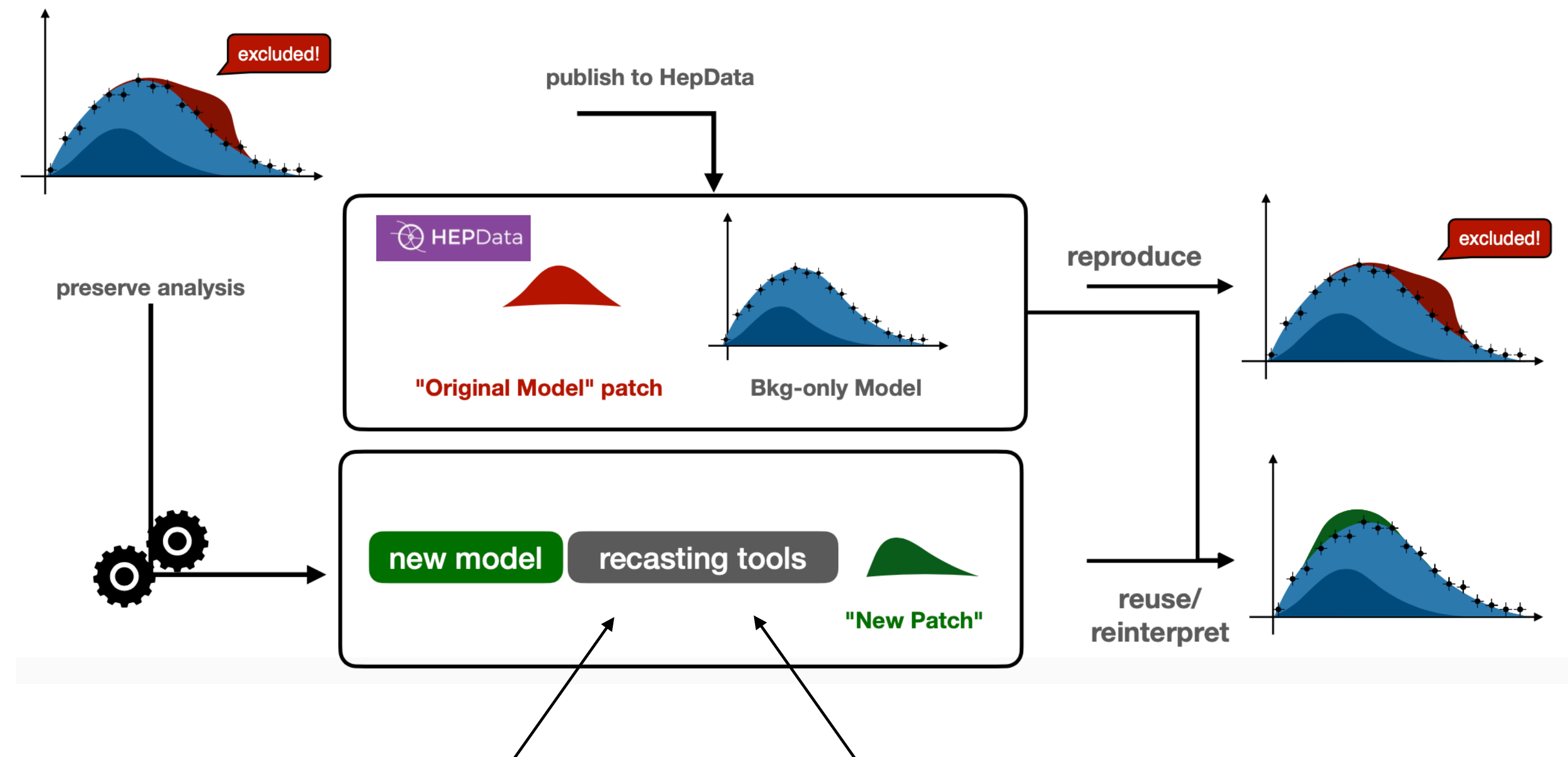


Illustration from talk by Lukas Heinrich
Hands-on workshop 8 Nov 2021

G. Alguero, J. Araz, B. Fuks, SK,
Functionality available v1.9 onward, paper in progress

MAD Analysis 5

SModelS

Interfaced to pyhf since SModelS v1.2.4 (now v2.1)
G. Alguero, SK, W. Waltenberger, [arXiv:2009.01809](https://arxiv.org/abs/2009.01809)

ATLAS Run 2 results in SModelS 2.1.0 database

ID	Short Description	\mathcal{L} [fb ⁻¹]	UL _{obs}	UL _{exp}	EM	comb.
ATLAS-SUSY-2015-01 [62]	2 <i>b</i> -jets	3.2	✓			
ATLAS-SUSY-2015-02 [63]	1 ℓ stop	3.2	✓		✓	
ATLAS-SUSY-2015-06 [64]	0 ℓ + 2–6 jets	3.2			✓	
ATLAS-SUSY-2015-09 [65]	jets + 2 SS or $\geq 3\ell$	3.2	✓			
ATLAS-SUSY-2016-06 [66]	disappearing tracks	36.1			✓	
ATLAS-SUSY-2016-07 [67]	0 ℓ + jets	36.1	✓		✓	
ATLAS-SUSY-2016-08 [68]	displaced vertices	32.8	✓			
ATLAS-SUSY-2016-14 [69]	2 SS or 3 ℓ 's + jets	36.1	✓			
ATLAS-SUSY-2016-15 [70]	0 ℓ stop	36.1	✓			
ATLAS-SUSY-2016-16 [71]	1 ℓ stop	36.1	✓		✓	
ATLAS-SUSY-2016-17 [72]	2 OS leptons	36.1	✓			
ATLAS-SUSY-2016-19 [73]	2 <i>b</i> -jets + τ 's	36.1	✓			
ATLAS-SUSY-2016-24 [74]	2–3 ℓ 's, EWino	36.1	✓		✓	
ATLAS-SUSY-2016-26 [75]	≥ 2 <i>c</i> -jets	36.1	✓			
ATLAS-SUSY-2016-27 [76]	jets + γ	36.1	✓		✓	
ATLAS-SUSY-2016-28 [77]	2 <i>b</i> -jets	36.1	✓			
ATLAS-SUSY-2016-32 [44]	HSCP	31.6	✓	✓	✓	
ATLAS-SUSY-2016-33 [78]	2 OSSF ℓ 's	36.1	✓			
ATLAS-SUSY-2017-01 [79]	$WH(bb)$, EWino	36.1	✓			
ATLAS-SUSY-2017-02 [80]	0 ℓ + jets	36.1	✓	✓		
ATLAS-SUSY-2017-03 [21]	multi- ℓ EWino	36.1	✓		✓	
ATLAS-SUSY-2018-04 [81]	2 hadronic taus	139.0	✓		✓	JSON
ATLAS-SUSY-2018-06 [22]	3 leptons, EWino	139.0	✓	✓	✓	
ATLAS-SUSY-2018-10 [17]	1 ℓ + jets	139.0	✓		✓	
ATLAS-SUSY-2018-12 [19]	0 ℓ + jets	139.0	✓	✓	✓	
ATLAS-SUSY-2018-14 [15]	displaced leptons	139.0			✓	JSON
ATLAS-SUSY-2018-22 [18]	multi-jets	139.0	✓		✓	
ATLAS-SUSY-2018-23 [20]	$WH(\gamma\gamma)$, EWino	139.0	✓	✓		
ATLAS-SUSY-2018-31 [82]	2 <i>b</i> + 2 <i>H</i> (<i>bb</i>)	139.0	✓		✓	JSON
ATLAS-SUSY-2018-32 [59]	2 OS leptons	139.0	✓			
ATLAS-SUSY-2019-08 [60]	1 ℓ + <i>H</i> (<i>bb</i>), EWino	139.0	✓		✓	JSON



Efficiency maps for 17 analyses,
 10 with full Run 2 luminosity
 4 with full likelihoods
 (more to come)



gz File

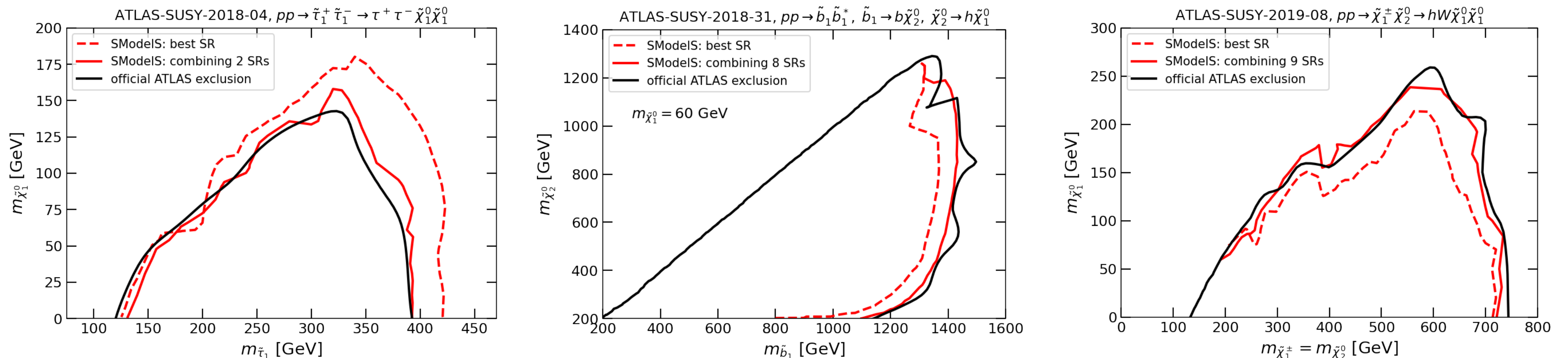
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Download



ATLAS' bkg-only models in SModelS

NB the signal patches also provided by ATLAS turn out to be highly useful for extracting $A \times \varepsilon$ maps needed by SModelS

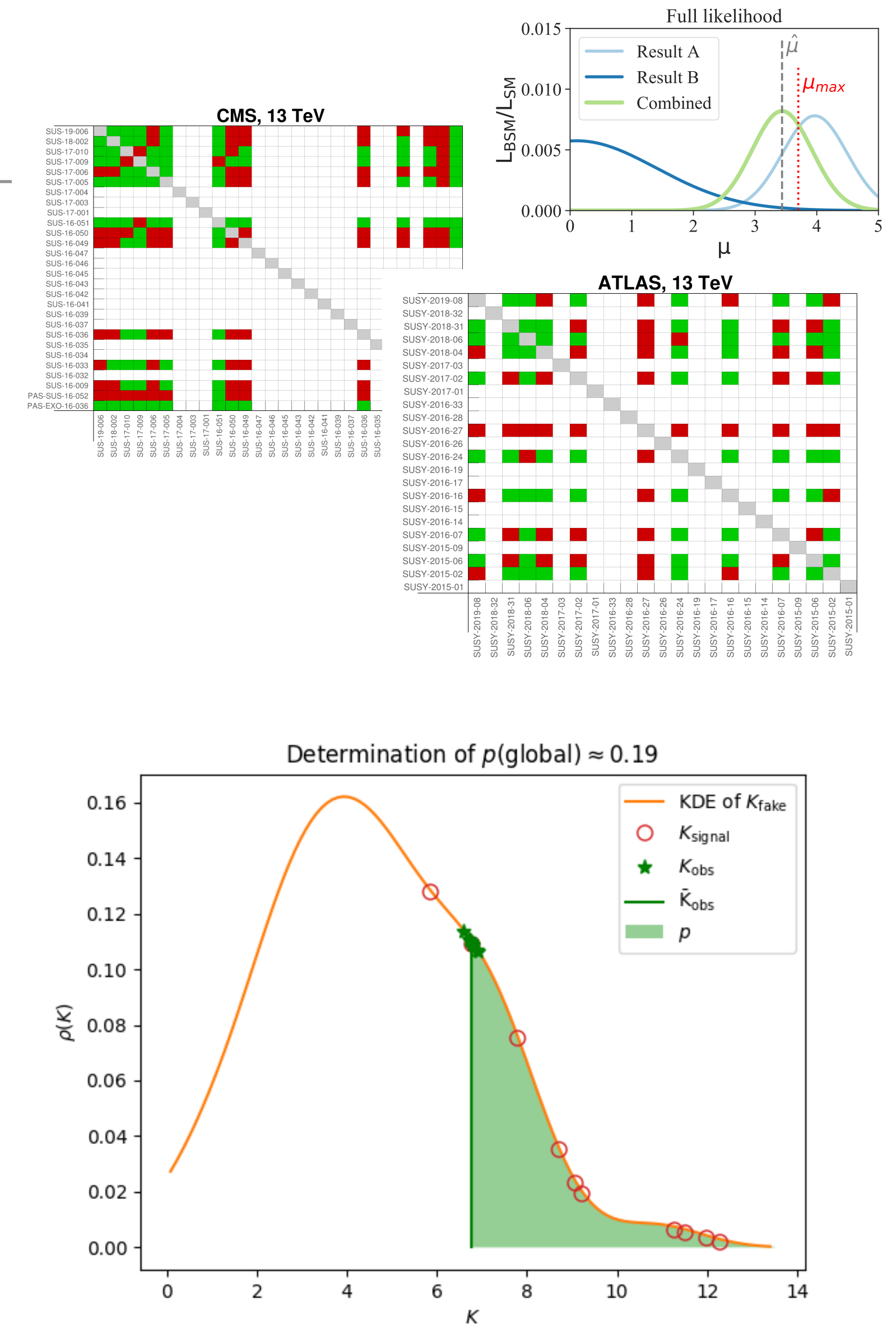


Statistical combination of signal regions is important → much better agreement with official limits

For signal region combination within a given analysis, a simplified likelihood would be sufficient and much faster.
However, eventually we want to do more than that (next slide)

Looking for dispersed signals

- In 2012.12246: prototype **statistical learning algorithm** to
 - identify potential dispersed signals in the LHC data
 - fit “proto-models” (new particles, decay modes, signal strengths) to them while remaining compatible with the entirety of LHC results in the SModelS database
- Based on simplified model results
 - exploits SModelS functionality and database
- Construct a **global likelihood** as product of likelihoods of approximately uncorrelated analyses
- To **determine a global p-value for the SM**, we produce “fake” SModelS databases **by sampling background models** (i.e. setting $\langle \# \text{observed} \rangle = \# \text{expected}$, sampled within BG uncertainties)



Could also be applied to look for consistent small deviations in SM measurements, EFT interpretation, etc. Correct statistical modelling is crucial

Conclusions

- The available details on the statistical model may heavily affect the **short- and long-term impacts** of any measurement.
- Use cases are a clear **call to action**.

An immediate action that can be taken by the community:

- (i) publish all the associated RooWorkspaces or
- (ii) for binned statistical models based on the HistFactory specification, publish the models in the pyhf JSON format.

- If adopted, will lead to more and higher-quality, science. Huge impact.

4 Physics examples, use cases

arXiv:2109.04981

- 4.1 Parton distribution functions
- 4.2 Higgs boson measurements and EFT interpretations
 - 4.2.1 Theorists' perspective
 - 4.2.2 Perspective from “official” experimental combinations
 - 4.2.3 An example of likelihood publishing for Higgs boson characterization
- 4.3 Direct searches for new physics
 - 4.3.1 Supersymmetry and exotics searches
 - 4.3.2 Searches for additional Higgs bosons
 - 4.3.3 Going further: combination of analyses, global p-value, etc.
- 4.4 Heavy flavor physics
 - 4.4.1 Rare decays and Lepton Flavor Universality Violation ratios
 - 4.4.2 Form factor and V_{ub} , V_{cb} determinations
 - 4.4.3 Future global EFT fits for $b \rightarrow c \tau \bar{\nu}_\tau$
 - 4.4.4 DNNLikelihood example: global EFT fits for $b \rightarrow s$ transitions
- 4.5 Dark matter direct detection
 - 4.5.1 CRESST-III public results
 - 4.5.2 XENON1T S2-only data
 - 4.5.3 Example combination
- 4.6 World averages
- 4.7 BSM global fits

Longer-term developments are certainly needed to enhance, streamline, and facilitate the use of published statistical models. However, the publication of the currently available statistical models would already be a watershed development in the field, one we hope the community is ready to embrace.

From the white paper summary

An immediate action that can be taken by the community:

- (i) publish all the associated RooWorkspaces or
- (ii) for binned statistical models based on the HistFactory specification, publish the models in the pyhf JSON format.

This would provide the impetus for the development of tools to make the use of the published models user-friendly, efficient, and effective.

Longer-term developments are certainly needed to enhance, streamline, and facilitate the use of published statistical models. However, the publication of the currently available statistical models would already be a watershed development in the field, one we hope the community is ready to embrace.

Challenges and outstanding issues; cf. white paper sect. 5

- ▶ Systematic naming conventions for (nuisance) parameters
→ facilitate combinations
- ▶ Serialisation of statistical models beyond HistFactory
→ e.g., CMS Combine tool
- ▶ Strategies and public tools for pruning, simplification and/or partial profiling of the full model when runtime is an issue
→ model surveys, global fits
- ▶ Systematic use in theory community; extension of fitting procedures and tools that currently assume Gaussian error sources
→ e.g. PDF, EFT fits
- ▶ Errors on errors
- ▶ ...

Exciting developments ahead

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