

# Neutrino Physics Introduction

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## Neutrino Physics Post-1998

1998: evidence for neutrino mass from SuperK  $(V_{\mu} \rightarrow V_{\tau})$ 

first solid evidence of beyond the Standard Model Physics

Massive Neutrinos

- 2002: evidence for neutrino mass from SNO ( $V_e \rightarrow V_{\mu,\tau}$ )
- 2003: KamLand confirmed Large Mixing Angle solution to solar V problem
- 2011: hints for non-zero  $\theta_{13}$  from T2K, MINOS, and Double Chooz
- 2012: evidences of non-zero  $\theta_{13}$  from Daya Bay and RENO

for some parameters: discovery phase into precision phase; and yet, many great discoveries to come

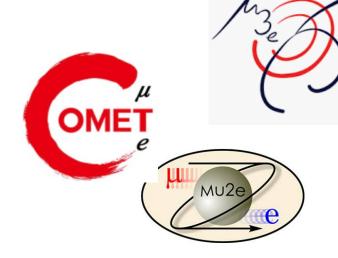
#### Neutrino Oscillation $\Rightarrow$ Massive Neutrinos

- Neutrino Masses are non-degenerate (at least two are non-zero)
  - mass eigenstates ≠ weak eigenstates
- Accidental symmetries in SM
  - Broken lepton flavor numbers:  $L_e$ ,  $L_\mu$ ,  $L_\tau$
  - Processes cross family lines in lepton sector now possible
    - As a result
      - neutrino oscillation
      - lepton flavor violation decays?





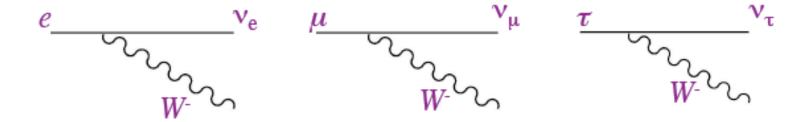






## What if Neutrinos Have Mass?

- Similar to the quark sector, there can be a mismatch between mass eigenstates and weak eigenstates
- weak interactions eigenstates:  $V_e$ ,  $V_{\mu}$ ,  $V_{\tau}$



- mass eigenstates: V<sub>1</sub>, V<sub>2</sub>, V<sub>3</sub>
- Pontecorvo-Maki-Nakagawa-Sakata (PMNS) Matrix

Maki, Nakagawa, Sakata, 1962; Pontecorvo, 1967

$$\begin{pmatrix} \boldsymbol{v}_e \\ \boldsymbol{v}_{\mu} \\ \boldsymbol{v}_{\tau} \end{pmatrix} = \begin{pmatrix} \boldsymbol{U}_{e1} & \boldsymbol{U}_{e2} & \boldsymbol{U}_{e3} \\ \boldsymbol{U}_{\mu 1} & \boldsymbol{U}_{\mu 2} & \boldsymbol{U}_{\mu 3} \\ \boldsymbol{U}_{\tau 1} & \boldsymbol{U}_{\tau 2} & \boldsymbol{U}_{\tau 3} \end{pmatrix} \begin{pmatrix} \boldsymbol{v}_1 \\ \boldsymbol{v}_2 \\ \boldsymbol{v}_3 \end{pmatrix}$$
 3 mixing angles 
$$\boldsymbol{U}_{\text{pMNS}} = \boldsymbol{V}_{e,L}^{\dagger} \boldsymbol{V}_{\nu,L}$$
 3 mixing angles 
$$\boldsymbol{U}_{\text{phase(s) for Dirac (Majorana)}}$$
 Dirac (Majorana)

$$U_{_{\mathsf{PMNS}}} = V_{e,L}^\dagger V_{
u,L}$$

Dirac (Majorana) neutrinos

## Leptonic Mixing Matrix

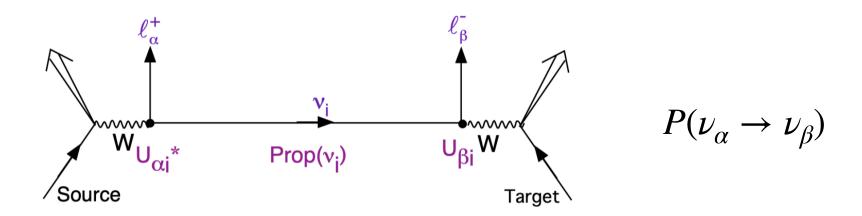
Pontecorvo-Maki-Nakagawa-Sakata (PMNS) Matrix

$$U_{\text{PMNS}} = \begin{bmatrix} 1 & 0 & 0 \\ 0 & c_{a} & s_{a} \\ 0 & -s_{a} & c_{a} \end{bmatrix} \begin{bmatrix} c_{\chi} & 0 & s_{\chi}e^{-i\delta} \\ o & 1 & 0 \\ -s_{\chi}e^{i\delta} & 0 & c_{\chi} \end{bmatrix} \begin{bmatrix} c_{S} & s_{S} & 0 \\ -s_{S} & c_{S} & 0 \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} 1 & O & 0 \\ 0 & e^{i\left(\frac{1}{2}\phi_{12}\right)} & 0 \\ 0 & e^{i\left(\frac{1}{2}\phi_{13} + \delta\right)} \end{bmatrix}$$
atm
reactor
solar
Majorana phases

- three mixing angles:  $c_a,\ c_s,\ c_x$
- three CP phases (if Majorana):  $\delta$ ,  $\phi_{12}$ ,  $\phi_{13}$ 
  - 1 CP phase (if Dirac):  $\delta$
- Oscillation experiments: sensitive only to  $\delta$

#### Neutrino Oscillation: Macroscopic Quantum Mechanics

- production: neutrinos of a definite flavor produced by weak interaction
- propagation: neutrinos evolve according to their masses
- detection: neutrinos of a different flavor composition detected



$$P[\nu_{\mu} \rightarrow \nu_{e}] = \sin^{2} 2\theta \sin^{2} \left[ 1.27 \Delta m_{32}^{2} \left( \frac{(\text{eV})^{2}}{c^{2}} \right) \frac{L(\text{km})}{E(\text{GeV})} \right]$$

## Classes of Experiments

#### Oscillation Experiments:

Atmospheric, solar, reactor, accelerator neutrinos

- mass ordering, CP phases,
   precision measurements
- Searches for BSM physics

#### Weak Decay Kinematics:

- Absolute mass scale
- Precision cosmology

#### Neutrino cross sections, $CE\nu NS$ :

- Interpretation of data
- BSM

#### Neutrinoless Double Beta Decay:

- Majorana vs Dirac

#### Astrophysical Neutrinos:

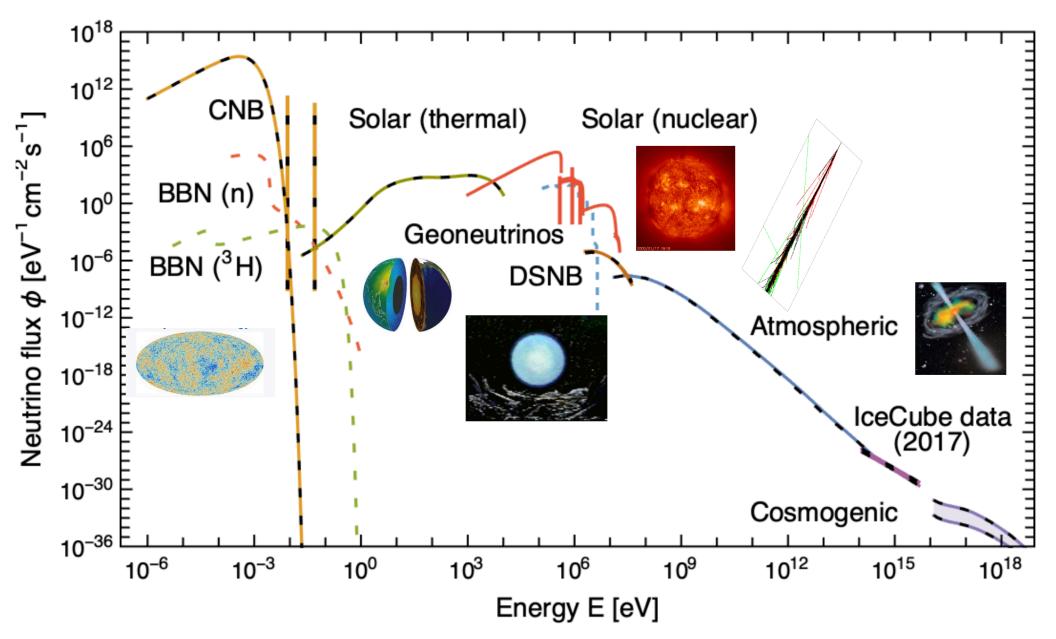
SN, GRBs, AGNs, mergers

Possible BSM physics

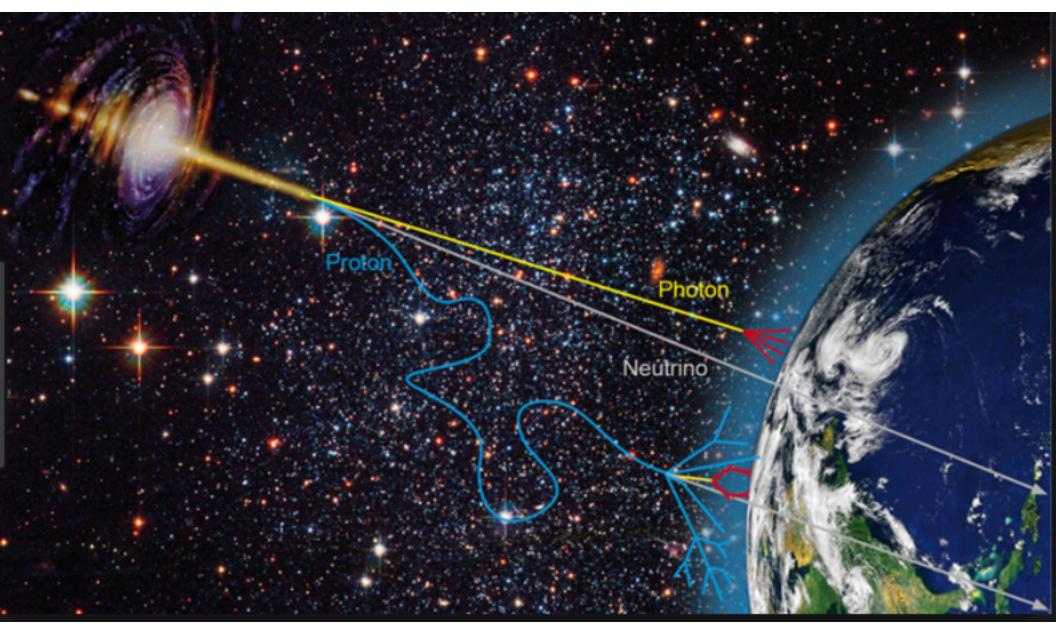
#### Grand Unified Neutrino Spectrum at Earth

Edoardo Vitagliano, Irene Tamborra, Georg Raffelt. Oct 25, 2019. 54 pp. MPP-2019-205

e-Print: arXiv:1910.11878 [astro-ph.HE] I PDF



[Slide Curtesy: Kate Scholberg, Snowmass CSS 2022]



[Photo credit: Astroparticle Physics - DESY]

Neutrinos as messengers

IceCube: Talk by Juan Pablo Yanez

## Where Do We Stand?

• Latest 3 neutrino global analysis:

Gonzalez-Garcia, Maltoni, Schwetz (NuFIT), 2111.03086

		Normal Ordering (Best Fit)		Inverted Ordering ( $\Delta \chi^2 = 7.0$ )	
		bfp $\pm 1\sigma$	$3\sigma$ range	bfp $\pm 1\sigma$	$3\sigma$ range
with SK atmospheric data	$\sin^2 \theta_{12}$	$0.304^{+0.012}_{-0.012}$	$0.269 \rightarrow 0.343$	$0.304^{+0.013}_{-0.012}$	$0.269 \rightarrow 0.343$
	$\theta_{12}/^{\circ}$	$33.45^{+0.77}_{-0.75}$	$31.27 \rightarrow 35.87$	$33.45^{+0.78}_{-0.75}$	$31.27 \rightarrow 35.87$
	$\sin^2 \theta_{23}$	$0.450^{+0.019}_{-0.016}$	$0.408 \rightarrow 0.603$	$0.570^{+0.016}_{-0.022}$	$0.410 \rightarrow 0.613$
	$\theta_{23}/^{\circ}$	$42.1_{-0.9}^{+1.1}$	$39.7 \rightarrow 50.9$	$49.0_{-1.3}^{+0.9}$	$39.8 \rightarrow 51.6$
	$\sin^2 \theta_{13}$	$0.02246^{+0.00062}_{-0.00062}$	$0.02060 \rightarrow 0.02435$	$0.02241^{+0.00074}_{-0.00062}$	$0.02055 \rightarrow 0.02457$
	$\theta_{13}/^{\circ}$	$8.62^{+0.12}_{-0.12}$	$8.25 \rightarrow 8.98$	$8.61^{+0.14}_{-0.12}$	$8.24 \rightarrow 9.02$
	$\delta_{\mathrm{CP}}/^{\circ}$	$230^{+36}_{-25}$	$144 \rightarrow 350$	$278^{+22}_{-30}$	$194 \rightarrow 345$
	$\frac{\Delta m_{21}^2}{10^{-5} \text{ eV}^2}$	$7.42^{+0.21}_{-0.20}$	$6.82 \rightarrow 8.04$	$7.42^{+0.21}_{-0.20}$	$6.82 \rightarrow 8.04$
	$\frac{\Delta m_{3\ell}^2}{10^{-3}~\text{eV}^2}$	$+2.510^{+0.027}_{-0.027}000000000000000000000000000000000000$	$+2.430 \rightarrow +2.593$	$-2.490^{+0.026}_{-0.028}$	$-2.574 \rightarrow -2.410$

- ⇒ hints of  $\theta_{23}$  ≠  $\pi/4$
- ightharpoonup expectation of Dirac CP phase  $\delta$
- → slight preference for normal mass ordering

## Neutrino Mass Measurements

- search for absolute mass scale:
  - ullet end point kinematic of tritium beta decays  $\operatorname{Tritium} o He^3 + e^- + \overline{
    u}_e$

$$m_{\mathcal{V}_e} < 2.2 \text{ eV } (95\% \text{ CL})$$
 Mainz  $m_{\mathcal{V}_{\mu}} < 170 \text{ keV}$   $m_{\mathcal{V}_{\tau}} < 15.5 \text{ MeV}$ 

KATRIN: current limit  $\sim 0.8~\text{eV}$  Future sensitivity  $\sim 0.2~\text{eV}$ 

Other ideas: Project 8, ECHO, Holmes

• neutrinoless double beta decay

current bound: 
$$|\langle m \rangle| \equiv \left| \sum_{i=1,2,3} m_i U_{ie}^2 \right| <$$
 (0.061-0.165) eV (Kamland-Zen, 2016)

• Cosmology  $\Sigma(m_{\nu_i}) < 0.12 \text{ eV}$ 

 $N_{eff}$  = 2.99  $\pm$  0.17 [Planck 2018]  $\Rightarrow$  fully thermalized sterile neutrino disfavored

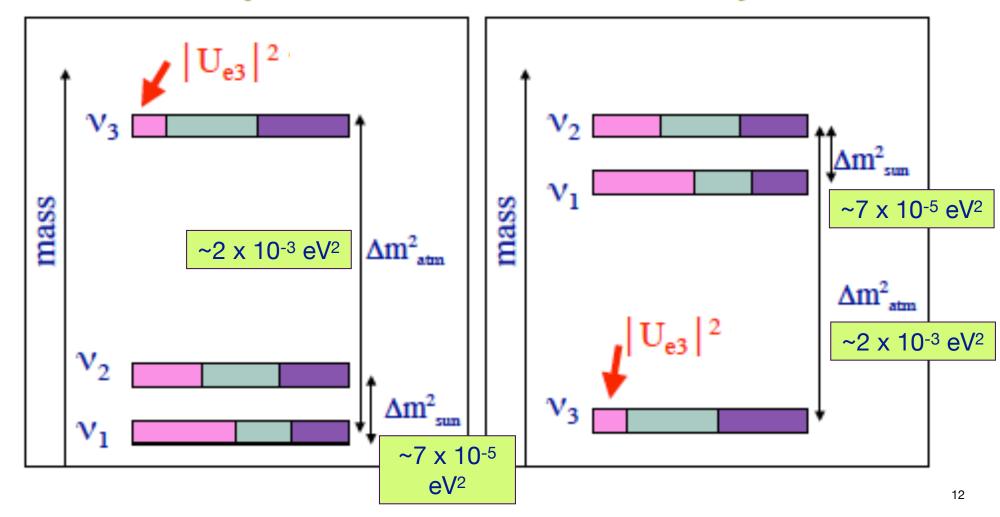
## How are masses ordered?



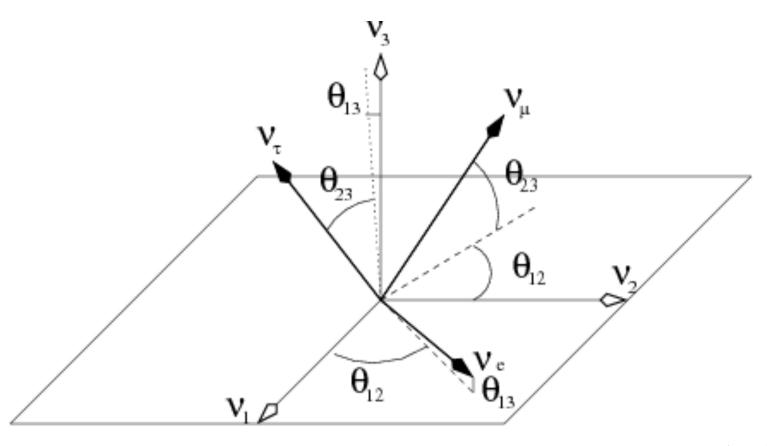
#### The known knowns:

#### normal hierarchy:

#### inverted hierarchy:



## The Known Knowns



NuFIT (2022)

 $[\Theta^{lep}_{23} \sim 42^{\circ}]$ 

 $[\Theta^{\text{lep}}_{12} \sim 33^{\circ}]$ 

 $[\Theta^{lep}_{13} \sim 9^{\circ}]$ 

## Open Questions - Neutrino Properties



- © CP violation in lepton sector?
- $^{\odot}$  Mass ordering: sign of ( $\Delta m_{13}^2$ )?
- Precision:  $\theta_{23} > \pi/4$ ,  $\theta_{23} < \pi/4$ ,  $\theta_{23} = \pi/4$ ?

#### CP Violation in Neutrino Oscillation

- With leptonic Dirac CP phase  $\delta \neq 0 \Rightarrow$  leptonic CP violation
- Predict different transition probabilities for neutrinos and antineutrinos

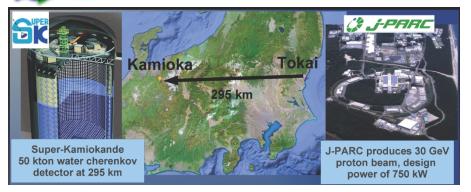
$$P(\nu_{\alpha} \to \nu_{\beta}) \neq P(\overline{\nu_{\alpha}} \to \overline{\nu_{\beta}})$$

 One of the major scientific goals at current and planned neutrino experiments

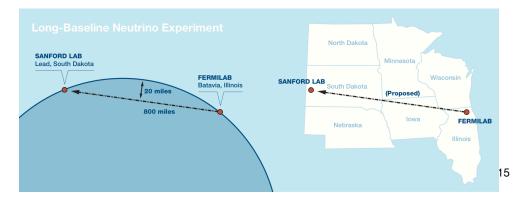




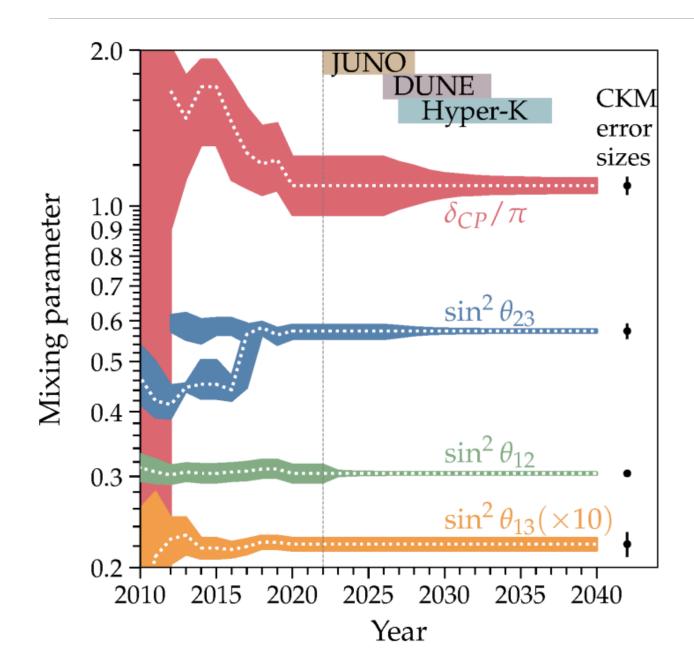
#### Hyper-Kamiokande



#### **DUNE**



## Experimental Precision: Oscillation Parameters



**NoVA: Talk by Ashley Back** 

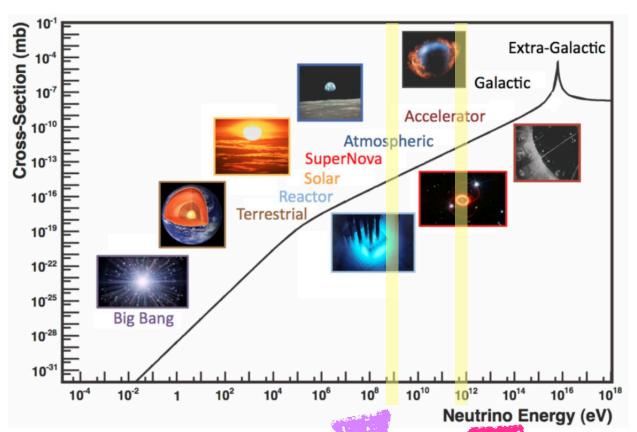
T2K: Talk by Alexander Izmaylov

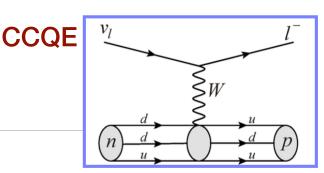
**DUNE: Talk by Pip Hamilton** 

Hyper-K: Talk by Stephane Zsoldos

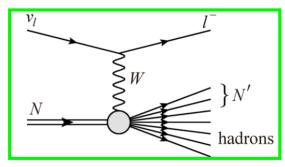
JUNO: Talk by Giuseppe Andronico

## Neutrino Interactions





CC DIS





MicroBooNE: Talk by Melissa Uchida

@GeV: Needed to understand oscillation data



SND@CERN: Talk by Albert De Roeck

(TeV) Neutrinos at LHC

# Some Anomalies are more anomalous than others.

## Neutrino Anomalies

# Neutrinos Travel Faster Than Light, According to One Experiment

Others doubt the mind-boggling claim, which would overturn Einstein's theory of special relativity

22 SEP 2011 · BY ADRIAN CHO (Science)



Common origin of superluminal neutrinos and DAMA annual modulation Multiple Lorentz Groups - A Toy Model for Superluminal Muon Neutrinos domain v Superluminal neutring ight, According Superluminal Neutrinos in the Minimal Standard Model Extension Experiment Cthers doubt the m awould overturn Einstein's theory of special relativ

Superluminal Neutrinos without Revolution Tachyonic neutrinos and the neutrino mas

Common origin

Multipl

## Once Again, Physicists Debunk Faster-Than-Light **Neutrinos**

Five different groups agree that the elusive particles obey Einstein's speed limit after all

8 JUN 2012 · BY ADRIAN CHO (Science)

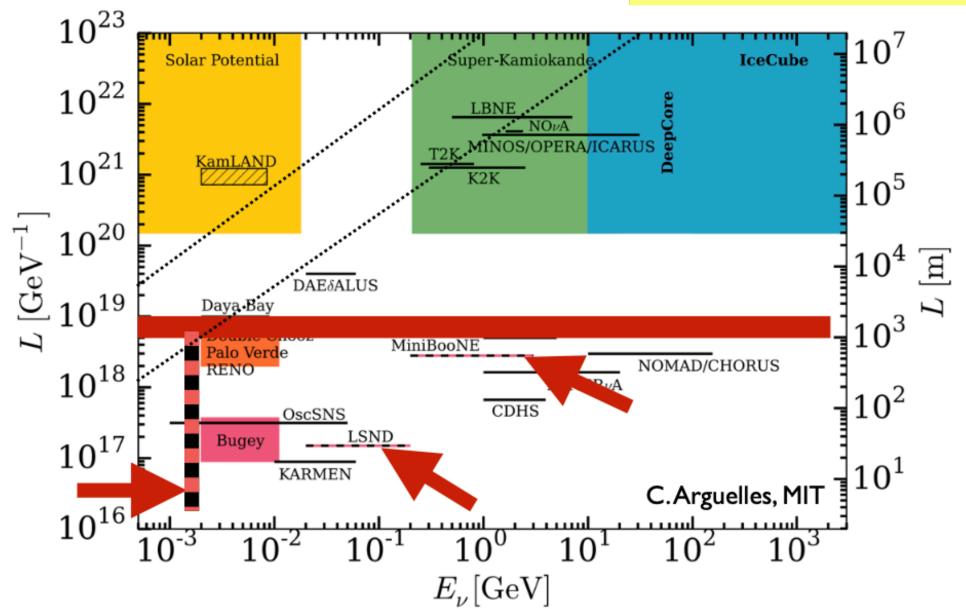
Superluminal Neutrinos in the Minimal Standard Model Extension Ctners doubt the m Einstein's theory of special

Superluminal Neutrinos Without Revolution Tachyonic neutrinos and the neutrino mas

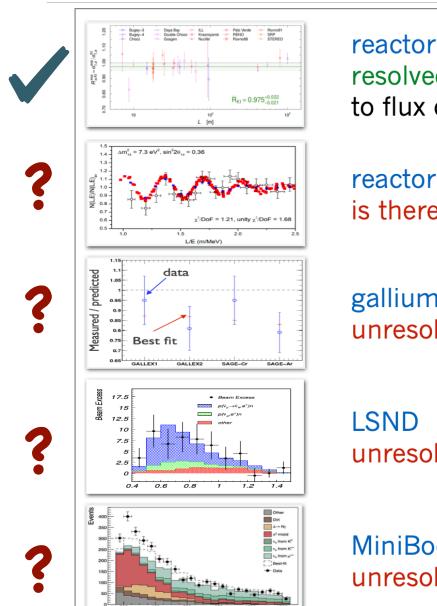


## Neutrino Anomalies

Measurements at < km disagree with state-of-the-art neutrino predictions



## Neutrino Anomalies



reactor flux anomaly resolved with new input data to flux calculation

reactor spectra is there really an anomaly?

gallium anomaly unresolved, recently reinforced

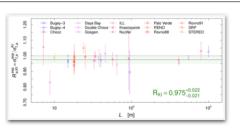
unresolved

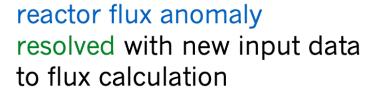
MiniBooNE unresolved

[Slide Curtesy: Joachim Kopp @ Neutrino 2022]

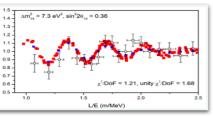
## Are there sterile neutrinos?







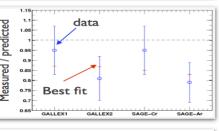




reactor spectra

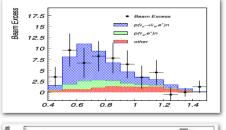
is there really an anomaly?





gallium anomaly unresolved, recently reinforced





#### LSND unresolved



[Slide Curtesy: Joachim Kopp @ Neutrino 20221

#### New neutrino mass states (eV)?



#### Sterile neutrinos

**DANSS: Talk by Eduard** Samigullin

MicroBooNE: Talk by Melissa Uchida

IceCube: Talk by Juan **Pablo Yanez** 

(NoVA: Talk by Ashley Back)



## Are Neutrinos their Own Antiparticles?

Two-neutrino double- $\beta$  decay



#### Maria Goeppert-Mayer, 1935

LN conserved

$$(A,Z) \rightarrow (A,Z+2) + e^- + e^- + \overline{\nu}_e + \overline{\nu}_e$$

First observed in 1987



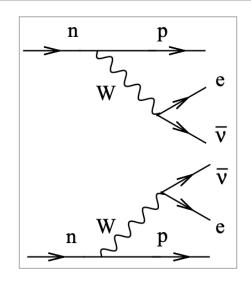
#### Neutrinoless double- $\beta$ decay

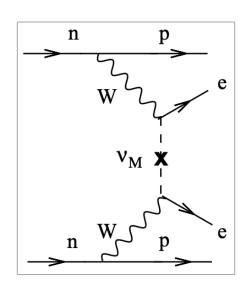
Wendell Furry, 1939

$$\Delta L = 2$$
  $(A, Z) \to (A, Z + 2) + e^{-} + e^{-}$ 

Required massive Majorana neutrinos;

Not yet observed



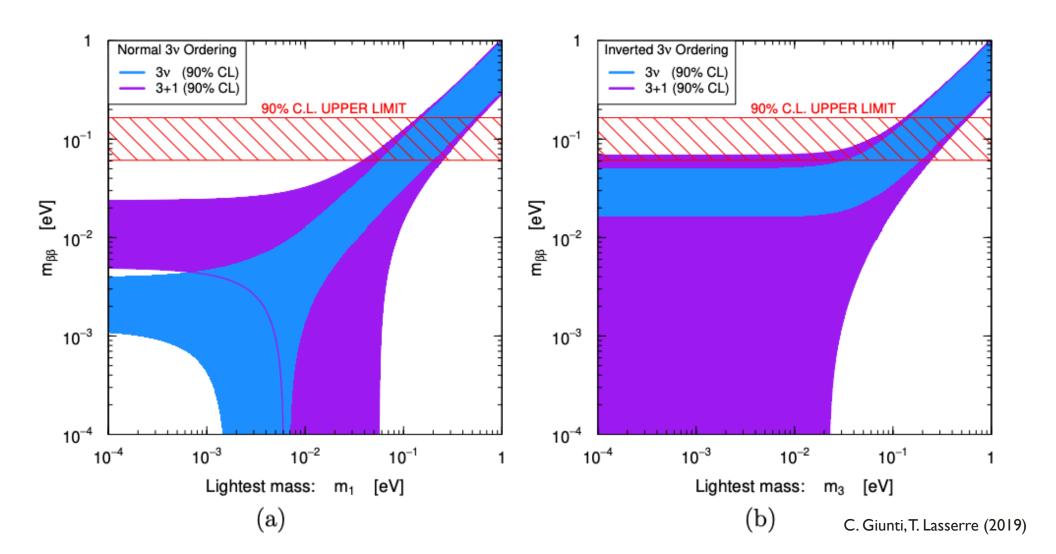


## $|m_{etaeta}| = \left|\sum_{k=1}^4 U_{ek}^2 m_k ight|$

## Neutrinoless Double Beta Decay

#### $3\nu$ : IO fully covered by 2035

#### $4\nu$ : NO can be probed



## Open Questions - Neutrino Properties



- Majorana vs Dirac?
- CP violation in lepton sector?
- Absolute mass scale of neutrinos?
- $^{\odot}$  Mass ordering: sign of  $(\Delta m_{13}^2)$ ?
- Sterile neutrino(s)?
- Precision:  $\theta_{23} > \pi/4$ ,  $\theta_{23} < \pi/4$ ,  $\theta_{23} = \pi/4$ ?
- Additional Neutrino Interactions?

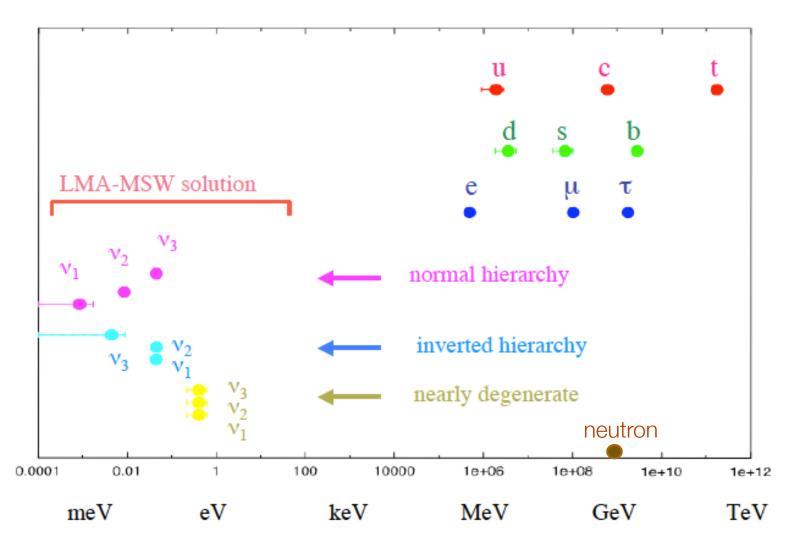
a suite of current and upcoming experiments to address these puzzles To understand some of these properties

⇒ BSM Physics

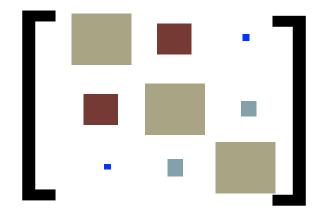


Smallness of neutrino mass:

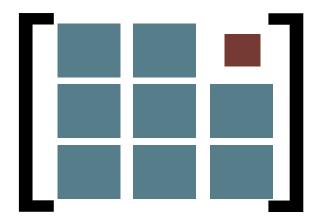
$$m_V \ll m_{e, u, d}$$



#### Flavor structure:

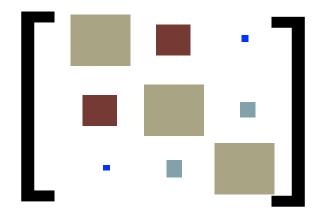


quark mixing

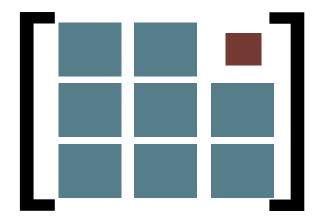


leptonic mixing

#### Flavor structure:



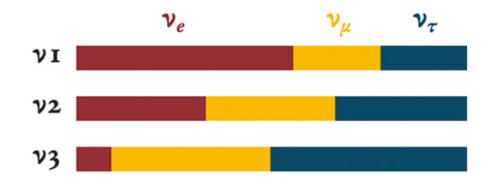
quark mixing



leptonic mixing

weak interaction eigenstates



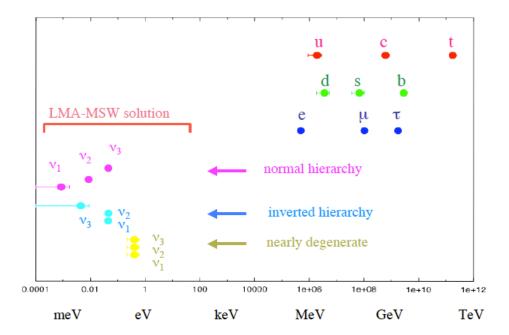


mass eigenstates



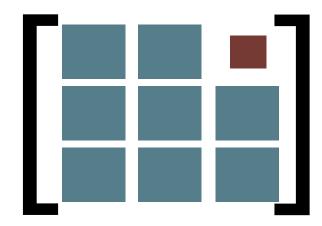
Smallness of neutrino mass:

$$m_V \ll m_{e, u, d}$$

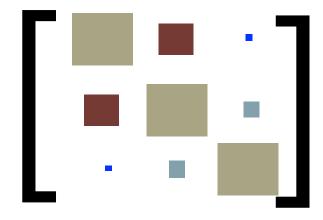


Fermion mass and hierarchy problem → Many free parameters in the Yukawa sector of SM

#### Flavor structure:



#### leptonic mixing



quark mixing

## Why Should We Care?

- Understanding a wealth of data, fundamentally
- SM flavor sector: no understanding of significant fraction (22/28) of SM parameters; (c.f. SM gauge sector)
- Neutrinos as window into BSM physics
  - neutrino mass generation unknown (suppression mechanism, scale)
  - Uniqueness of neutrino masses → connections w/ NP frameworks
- Neutrinos affords opportunities for new explorations
  - New Tools
  - May address other puzzles in particle physics
    - Window into early Universe
  - UV connection e.g. modular symmetries: Talk by Michael Ratz

e.g. stability of Dark Matter: Talk by Ricardo Cepedello

#### Smallness of neutrino masses

What is the operator for neutrino mass generation?

- Majorana vs Dirac
- scale of the operator
- suppression mechanism

## Neutrino Mass beyond the SM

• SM: effective low energy theory

$$\mathcal{L} = \mathcal{L}_{ ext{SM}} + \boxed{rac{\mathcal{O}_{5D}}{M} + rac{\mathcal{O}_{6D}}{M^2} + ...}$$
 new physics effects

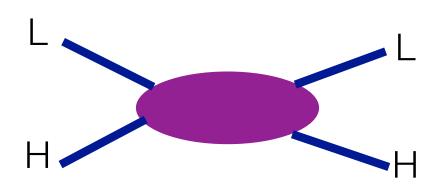
• only one dim-5 operator: most sensitive to high scale physics

$$rac{\lambda_{ij}}{M}HHL_iL_j \quad \Rightarrow \quad m_
u = \lambda_{ij}rac{v^2}{M}$$
 Weinberg, 1979

- m<sub>v</sub> ~  $(\Delta m^2_{atm})^{1/2}$  ~ 0.1 eV with v ~ 100 GeV,  $\lambda$  ~ O(1)  $\Rightarrow$  M ~ 10<sup>14</sup> GeV
- Lepton number violation  $\Delta L = 2 \Rightarrow Majorana$  fermions

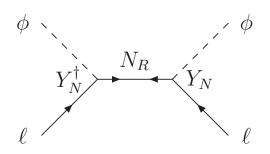


## Neutrino Mass beyond the SM



3 possible portals

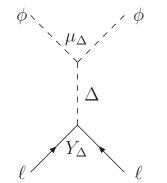
#### Type-I seesaw



 $N_R$ : SU(3)<sub>c</sub> x SU(2)<sub>w</sub> x U(1)<sub>Y</sub> ~(1,1,0)

Minkowski, 1977; Yanagida, 1979; Glashow, 1979; Gell-mann, Ramond, Slansky,1979; Mohapatra, Senjanovic, 1979;

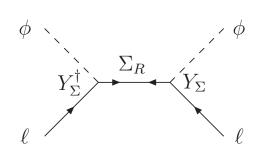
#### Type-II seesaw



 $\Delta$ : SU(3)<sub>c</sub> x SU(2)<sub>w</sub> x U(1)<sub>Y</sub> ~(1,3,2)

Lazarides, 1980; Mohapatra, Senjanovic, 1980

#### Type-III seesaw



$$\Sigma = (\Sigma^+, \Sigma^0, \Sigma^-)$$

 $\Sigma_R$ : SU(3)<sub>c</sub> x SU(2)<sub>w</sub> x U(1)<sub>Y</sub> ~(1,3,0)

Foot, Lew, He, Joshi, 1989; Ma, 1998

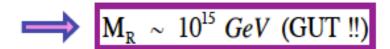
### Why are neutrinos light? (Type-I) Seesaw Mechanism

Adding the right-handed neutrinos:

$$(v_L \quad v_R) \begin{pmatrix} 0 & m_D \\ m_D & M_R \end{pmatrix} \begin{pmatrix} v_L \\ v_R \end{pmatrix}$$

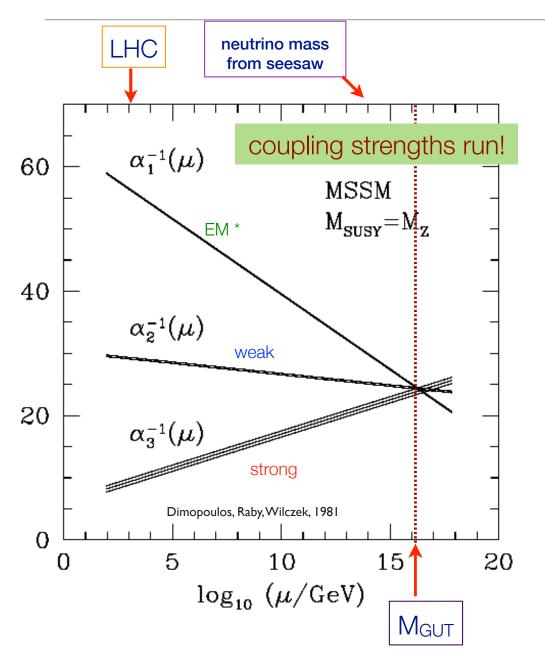
$$m_{m v} \sim m_{light} \sim rac{m_D^2}{M_R} << m_D$$
  $m_{heavy} \sim M_R$ 

For 
$$m_{V_3} \sim \sqrt{\Delta m_{atm}^2}$$
If  $m_D \sim m_t \sim 180 \; GeV$ 





#### Grand Unification Naturally Accommodates Seesaw

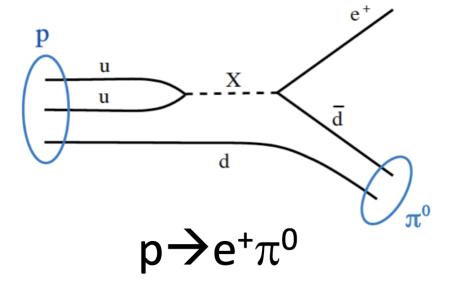


- $^{\odot}$  origin of the heavy scale  $\Rightarrow$  U(1)<sub>B-L</sub>
- exotic mediators ⇒ predicted in many GUT theories, e.g. SO(10)

```
16 = (3, 2, 1/6) \sim \begin{cases} u & u & u \\ d & d & d \end{cases}
+ (3^*, 1, -2/3) \sim (u^c & u^c & u^c)
+ (3^*, 1, 1/3) \sim (d^c & d^c & d^c)
+ (1, 2, -1/2) \sim \begin{cases} v \\ e \end{cases}
+ (1, 1, 1) \sim e^c
+ (1, 1, 0) \sim v^c
```

GUT predicts proton decay

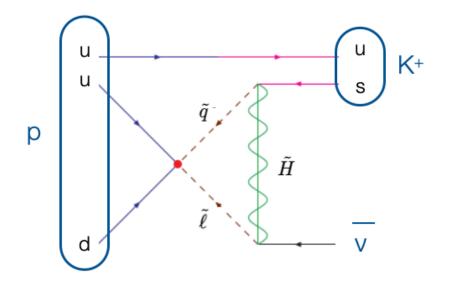
$$\Delta(B-L)=0$$



X: exotic heavy force carriers

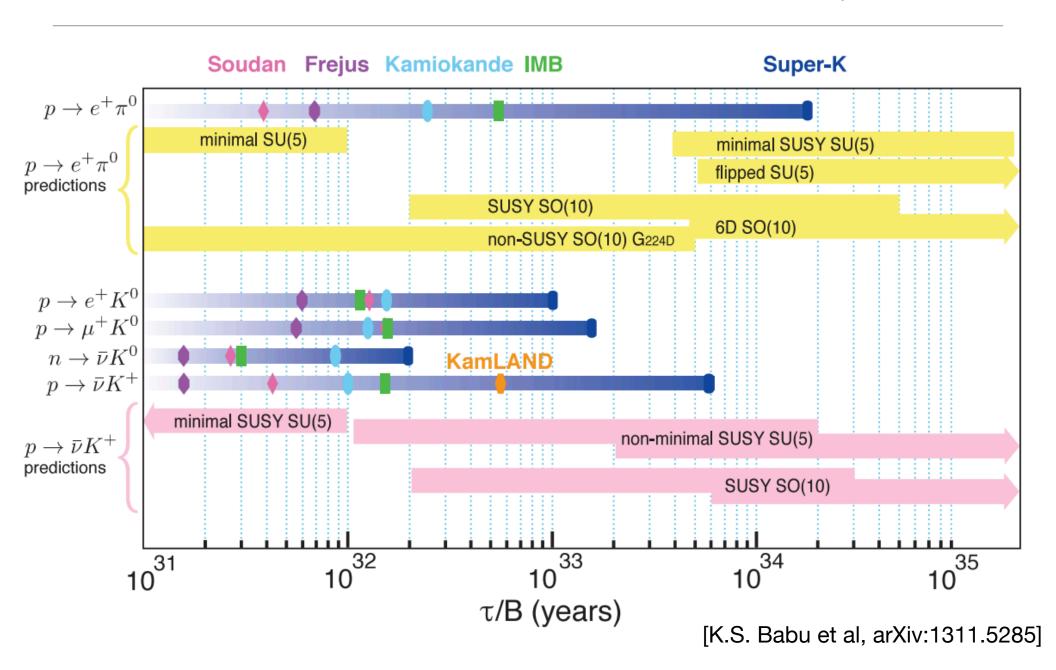
$$au_p \propto M_X^4$$

SUSY GUTs: additional contributions mediated by superpartners



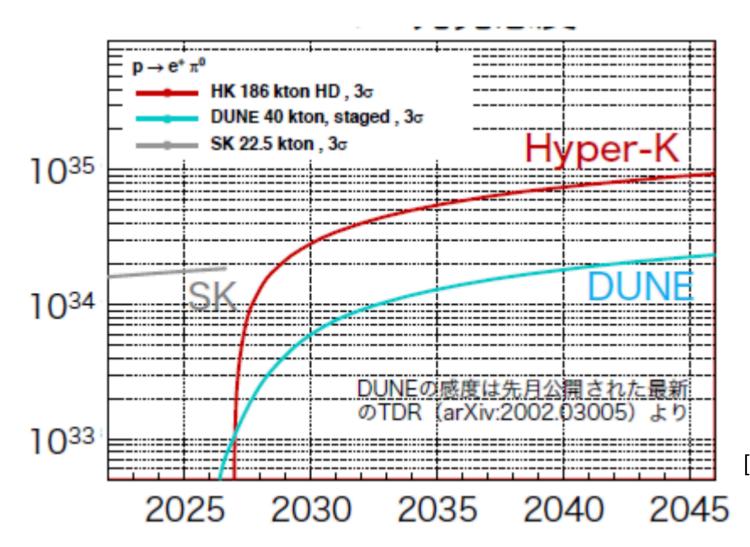
 $ilde{H}$ : color-triplet Higgsinos

$$au_p \propto M_{ ilde{H}}^2$$



3σ discovery potential

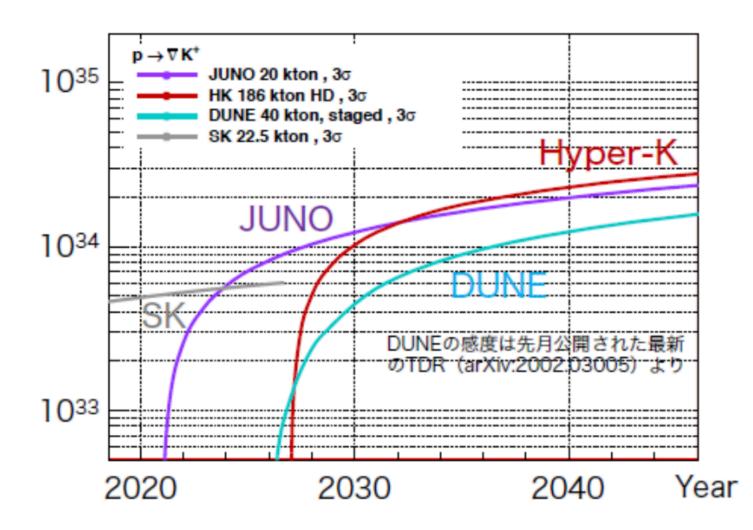
 $p \rightarrow e^+ \pi^0$ 



[M. Miura @ ICISE 2021]

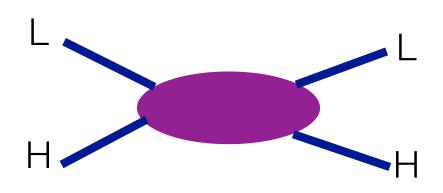
#### 3σ discovery potential

$$p \rightarrow v K^+$$



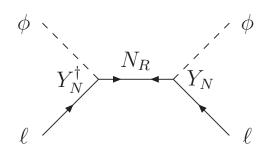
[M. Miura @ ICISE 2021]

## Neutrino Mass beyond the SM



3 possible portals

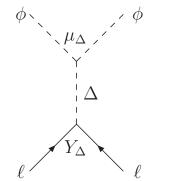
#### Type-I seesaw



 $N_R$ : SU(3)<sub>c</sub> x SU(2)<sub>w</sub> x U(1)<sub>Y</sub> ~(1,1,0)

Minkowski, 1977; Yanagida, 1979; Glashow, 1979; Gell-mann, Ramond, Slansky,1979; Mohapatra, Senjanovic, 1979;

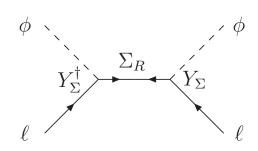
#### Type-II seesaw



 $\Delta$ : SU(3)<sub>c</sub> x SU(2)<sub>w</sub> x U(1)<sub>Y</sub> ~(1,3,2)

Lazarides, 1980; Mohapatra, Senjanovic, 1980

#### Type-III seesaw



$$\Sigma = (\Sigma^+, \Sigma^0, \Sigma^-)$$

 $\Sigma_R$ : SU(3)<sub>c</sub> x SU(2)<sub>w</sub> x U(1)<sub>Y</sub> ~(1,3,0)

Foot, Lew, He, Joshi, 1989; Ma, 1998

#### Low Scale Seesaws

 $m_{v} \sim (\Delta m^{2}_{atm})^{1/2} \sim 0.1$  eV with  $v \sim 100$  GeV,  $\lambda \sim 10^{-6}$   $\Rightarrow M \sim 10^{2}$  GeV

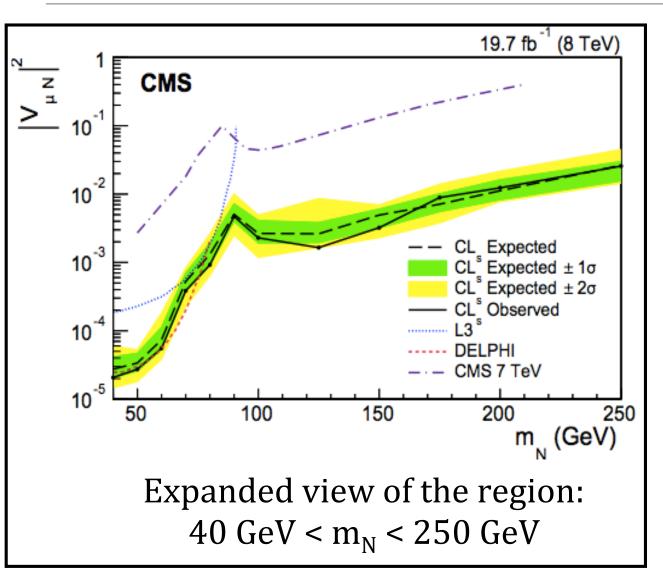
#### New particles:

- · Type I seesaw: generally decouple from collider experiments
- Type II seesaw:  $\Delta^{++} 
  ightarrow e^+ e^+$  ,  $\mu^+ \mu^+$  ,  $au^+ au^+$
- Type III seesaw: observable displaced vertex, dark matter candidate
- · inverse seesaw: non-unitarity effects
- radiative mass generation: model dependent singly/doubly charged
   SU(2) singlet, even colored scalars in loops, dark matter candidate

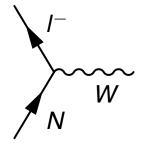
#### New interactions:

- LR symmetric model: W<sub>R</sub>
- R parity violation:  $\tan^2 \theta_{\rm atm} \simeq \frac{BR(\tilde{\chi}_1^0 \to \mu^\pm W^\mp)}{BR(\tilde{\chi}_1^0 \to \tau^\pm W^\mp)}$

#### Cautions!!! Is it really the v<sub>R</sub> in Type I seesaw?



RH neutrino production thru active-sterile mixing:



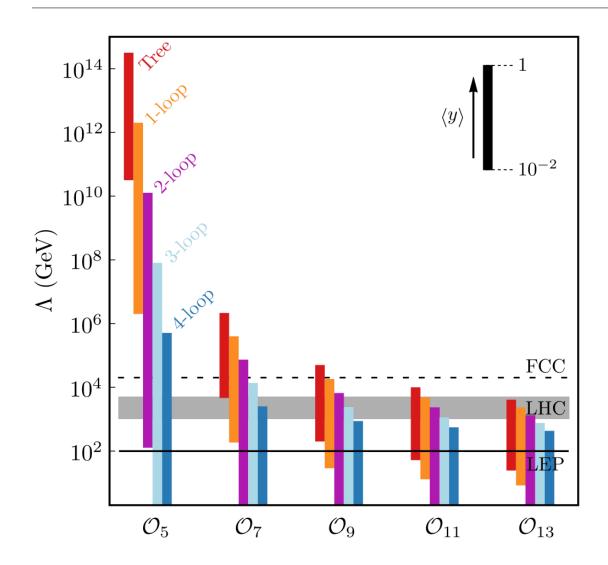
$$\propto V = \frac{m_D}{M_B} \sim \frac{10^{-4} \text{ GeV}}{100 \text{ GeV}} = 10^{-6}$$

RH neutrino relevant for v mass generation

$$|V_{\mu N}|^2 = 10^{-12}$$

unless extremely fine-tuned

#### Higher Dimensional Neutrino Masses

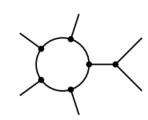


$$m_
u \propto \epsilon \cdot \left(rac{1}{16\pi^2}
ight)^n \cdot \left(rac{v}{\Lambda}
ight)^{d-5} \cdot rac{v^2}{\Lambda}$$

Babu, Leung (2001); de Gouvea, Jenkins (2007); .....

e.g. at dim-7, 1-loop

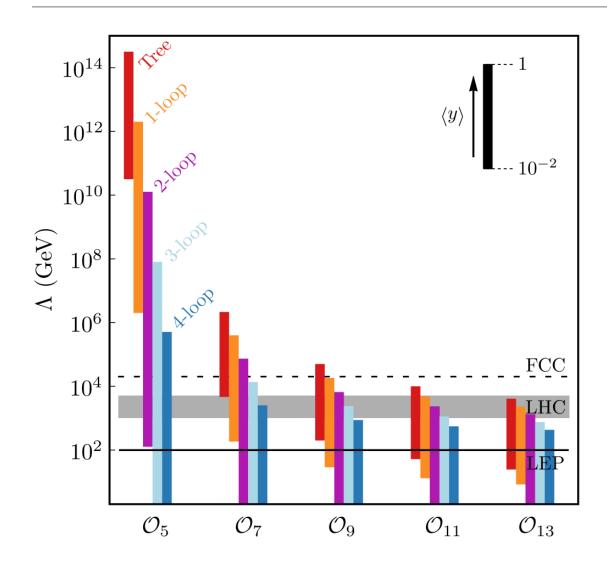
$$O_1' = LLHH(H^{\dagger}H)$$



For an excellent review on Radiative Neutrino Mass Generation: Cai, Herrero-García, Schmidt, Vincente, Volkas, 1706.08524

Anamiati, Castillo-Felisola, Fonseca, Helo, Hirsch (2019)

#### Higher Dimensional Neutrino Masses

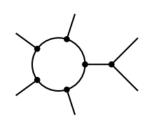


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## Need a lot of work to have realistic mixing

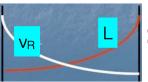
# What if neutrinos are Dirac?

#### Small Masses - Dirac Neutrinos

Randall-Sundrum warped extra dimensions

$$\psi_{(0)} \sim e^{(1/2-c)ky}$$

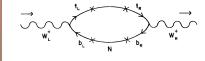




SM (us)

Grossman, Neubert (2000); Huber, Shafi (2001)

#### Radiative Mass Generation



Cheng, Li (1978); .....

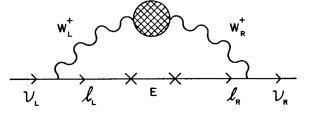


Figure from Babu, He (1988);

For clarifications of radiative Dirac neutrino mass generation: see e.g. Farzan, Pascoli, Schmidt (2012)

#### Clockwork Seesaw Mechanism

S.C. Park, C.S. Shin (2017); Hong, Kurup, Perelstein (2019); Babu, Saad (2020) ...

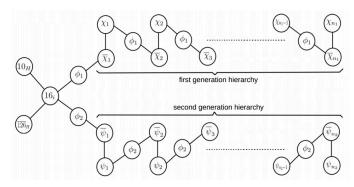
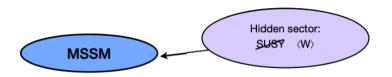


Figure from Babu, Saad (2020)

#### SUSY Breaking

Arkani-Hamed, Hall, Murayama, Tucker-Smith, Weiner (2001)



$$Y_{\nu} \sim \frac{m_{3/2}}{M_{\rm P}} \sim \frac{\mu}{M_{\rm P}}$$

## Flavor structure anarchy symmetry VS

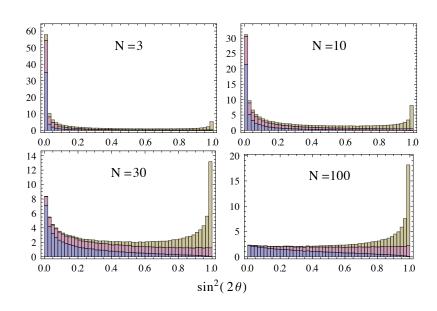


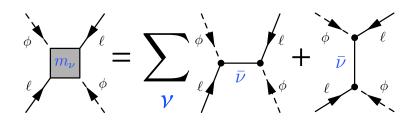


- there are no parametrically small
   numbers
   Hall, Murayama, Weiner (2000); de Gouvea, Murayama (2003);
- large mixing angle, near mass degeneracy statistically preferred
- UV theory prediction can resemble anarchy
  - · warped extra dimensions
  - heterotic string models: O(100) RH
     neutrinos
     Buchmüller, Hamaguchi, Lebedev, Ramos-Sánchez, Ratz (2007)

 statistical expectations with large N (= # of RH neutrinos)

Feldstein, Klemm (2012)





 $m_{\nu}$  ~

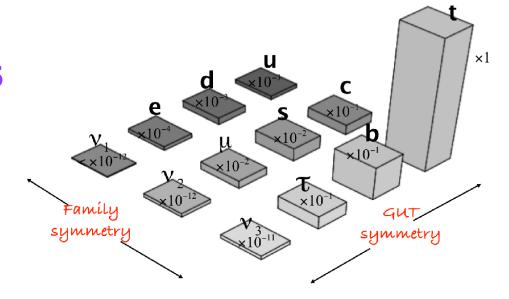




## Flavor Structure from Symmetries

#### Grand Unified Theories: GUT symmetry

Quarks → Leptons



Family Symmetry:

[Figure Credit: arXiv:1301.1340]

e-family → muon-family → tau-family

## Symmetry Relations

Symmetry ⇒ relations among parameters

⇒ reduction in number of fundamental parameters

## Symmetry Relations

Symmetry ⇒ relations among parameters

⇒ reduction in number of fundamental parameters

Symmetry ⇒ experimentally testable correlations among physical observables

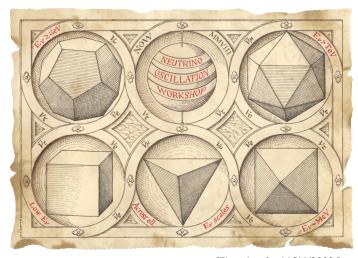
#### Testing Symmetry Relations ⇒ Precision

Symmetry ⇒ experimentally testable correlations among physical observables

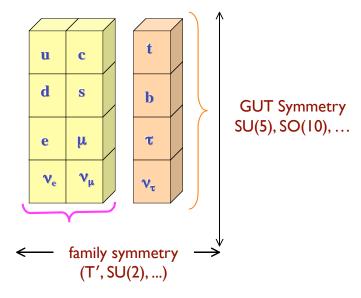
Testing correlations ⇒ Precision

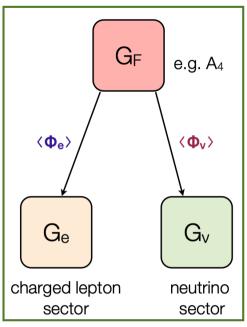
### Non-Abelian Discrete Flavor Symmetries

- Large neutrino mixing motivates discrete flavor symmetries
  - A<sub>4</sub> (tetrahedron)
  - T´ (double tetrahedron)
  - S<sub>3</sub> (equilateral triangle)
  - S<sub>4</sub> (octahedron, cube)
  - A<sub>5</sub> (icosahedron, dodecahedron)
  - ∆27
  - Q<sub>6</sub>
  - •



[Eligio Lisi for NOW2008]





## Tri-bimaximal Neutrino Mixing

#### Latest Global Fit (3σ)

$$\sin^2 \theta_{23} = 0.437 \ (0.374 - 0.626)$$

$$\sin^2 \theta_{12} = 0.308 \ (0.259 - 0.359)$$

$$\sin^2 \theta_{13} = 0.0234 \ (0.0176 - 0.0295)$$

Esteban, Gonzalez-Garcia, Maltoni, Schwetz, Zhou (2020)

$$[\Theta^{lep}_{23} \sim 49.2^{\circ}]$$

$$[\Theta^{lep}_{12} \sim 33.4^{\circ}]$$

$$[\Theta^{lep}_{13} \sim 8.57^{\circ}]$$

#### Tri-bimaximal Mixing Pattern

Harrison, Perkins, Scott (1999)

$$U_{TBM} = \begin{pmatrix} \sqrt{2/3} & \sqrt{1/3} & 0 \\ -\sqrt{1/6} & \sqrt{1/3} & -\sqrt{1/2} \\ -\sqrt{1/6} & \sqrt{1/3} & \sqrt{1/2} \end{pmatrix} \qquad \sin^2 \theta_{\text{atm, TBM}} = 1/2 \qquad \sin^2 \theta_{\odot, \text{TBM}} = 1/3 \\ \sin \theta_{13, \text{TBM}} = 0.$$

$$\sin^2 \theta_{\text{atm, TBM}} = 1/2$$
  $\sin^2 \theta_{\odot, \text{TBM}} = 1/3$   $\sin \theta_{13, \text{TBM}} = 0$ .

#### Neutrino Mass Matrix from A4

Imposing A4 flavor symmetry on the Lagrangian

Ma, Rajasekaran (2001); Babu, Ma, Valle (2003); Altarelli, Feruglio (2005)

A4 spontaneously broken by flavon fields

$$M_{
u} = rac{\lambda v^2}{M_x} \left(egin{array}{cccc} 2\xi_0 + u & -\xi_0 & -\xi_0 \ -\xi_0 & 2\xi_0 & u - \xi_0 \ -\xi_0 & u - \xi_0 & 2\xi_0 \end{array}
ight) \hspace{1cm} ext{relative strengths} \ 
ightarrow ext{CG's}$$

2 free parameters

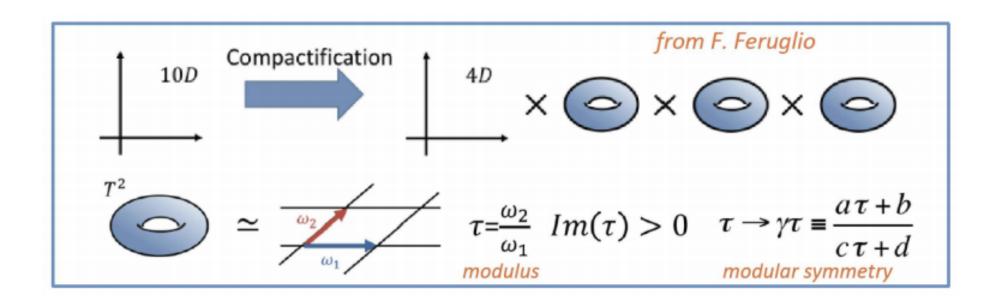
 always diagonalized by TBM matrix, independent of the two free parameters

$$U_{
m TBM} = \left( egin{array}{cccc} \sqrt{2/3} & 1/\sqrt{3} & 0 \\ -\sqrt{1/6} & 1/\sqrt{3} & -1/\sqrt{2} \\ -\sqrt{1/6} & 1/\sqrt{3} & 1/\sqrt{2} \end{array} 
ight)$$
 Angl

**Neutrino Mixing** Angles from Group Theory

## Modular Flavor Symmetries

- Extra dimensional origin of non-Abelian discrete symmetries
- Modular symmetries Altarelli, Feruglio (2005); Feruglio (2017), .....
  - Inspired by string theories
  - ullet Imposing modular invariance Y=Y( au)
  - Highly predictive models



## A Toy Modular A<sub>4</sub> Model

Feruglio (2017)

• Weinberg Operator 
$$\mathscr{W}_{v} = \frac{1}{\Lambda} [(H_{u} \cdot L) \ Y \ (H_{u} \cdot L)]_{1}$$

- Traditional A4 Flavor Symmetry
  - Yukawa Coupling Y → Flavon VEVs (A<sub>4</sub> triplet, 6 real parameters)

$$Y \to \langle \phi \rangle = \begin{pmatrix} a \\ b \\ c \end{pmatrix} \implies m_v = \frac{v_u^2}{\Lambda} \begin{pmatrix} 2a & -c & -b \\ -c & 2b & -a \\ -b & -a & 2c \end{pmatrix}$$

- Modular A4 Flavor Symmetry
  - Yukawa Coupling Y → Modular Forms (A4 triplet, 2 real parameters)

$$Y \to \begin{pmatrix} Y_1(\tau) \\ Y_2(\tau) \\ Y_3(\tau) \end{pmatrix} \implies m_v = \frac{v_u^2}{\Lambda} \begin{pmatrix} 2Y_1(\tau) & -Y_3(\tau) & -Y_2(\tau) \\ -Y_3(\tau) & 2Y_2(\tau) & -Y_1(\tau) \\ -Y_2(\tau) & -Y_1(\tau) & 2Y_3(\tau) \end{pmatrix}$$

## A Toy Modular A<sub>4</sub> Model

Feruglio (2017)

#### • Input Parameters:

$$\tau = 0.0111 + 0.9946i$$

$$v_u^2/\Lambda$$

#### Predictions:

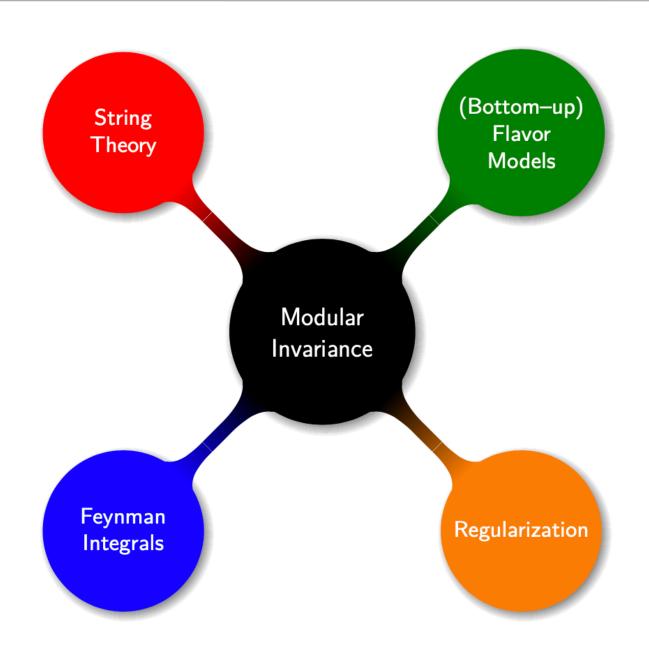
$$\begin{split} \frac{\Delta m_{sol}^2}{|\Delta m_{atm}^2|} &= 0.0292 \\ \sin^2\theta_{12} &= 0.295 & \sin^2\theta_{13} = 0.0447 & \sin^2\theta_{23} = 0.651 \\ \frac{\delta_{CP}}{\pi} &= 1.55 & \frac{\alpha_{21}}{\pi} = 0.22 & \frac{\alpha_{31}}{\pi} = 1.80 \quad . \end{split}$$

$$m_1 = 4.998 \times 10^{-2} \ eV$$
  $m_2 = 5.071 \times 10^{-2} \ eV$   $m_3 = 7.338 \times 10^{-4} \ eV$ 

$$m_2 = 5.071 \times 10^{-2} \ eV$$

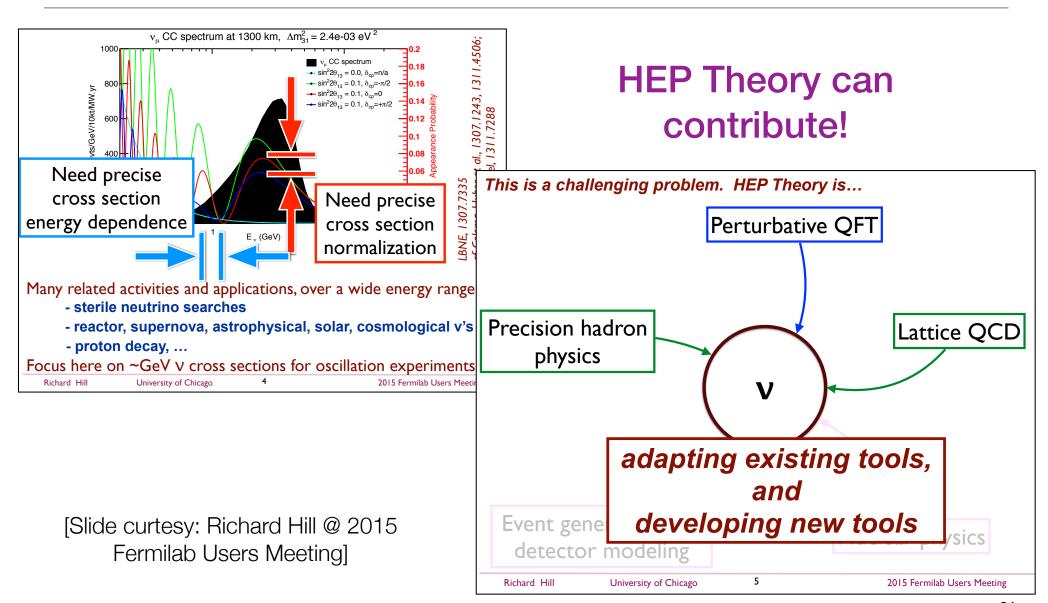
$$m_3 = 7.338 \times 10^{-4} \ eV$$

#### Modular Invariance Beyond Neutrino Flavor

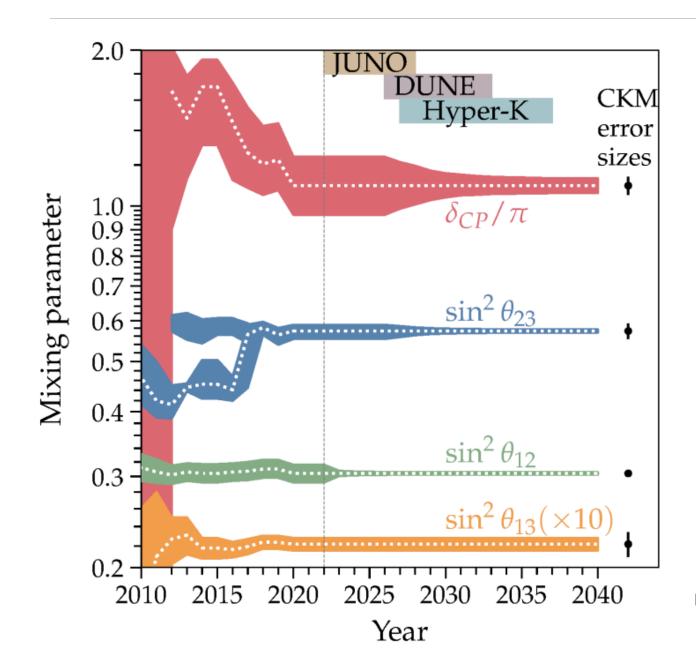


#### **Precision**

## Experimental Precision



## Precision of Theory Predictions



Are precision in model predictions compatible with experimental precision?

Talk by Michael Ratz

Figure from Song, Li, Argüelles, Bustamante, Vincent (2020)

#### **CP Violation**

#### Origin of CP Violation

CP violation 
 ⇔ complex mass matrices

$$\overline{U}_{R,i}(M_u)_{ij}Q_{L,j} + \overline{Q}_{L,j}(M_u^{\dagger})_{ji}U_{R,i} \xrightarrow{\mathfrak{CP}} \overline{Q}_{L,j}(M_u)_{ij}U_{R,i} + \overline{U}_{R,i}(M_u)_{ij}^*Q_{L,j}$$

- Conventionally, CPV arises in two ways:
  - Explicit CP violation: complex Yukawa coupling constants Y

- Spontaneous CP violation: complex scalar VEVs <h>
- Complex CG coefficients in certain discrete groups ⇒ explicit CP violation
  - CPV in quark and lepton sectors purely from complex CG coefficients

CG coefficients in non-Abelian discrete symmetries

⇒ relative strengths and phases in entries of Yukawa matrices

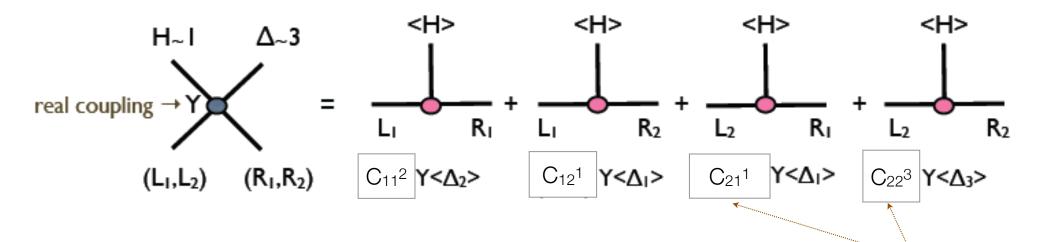
⇒ mixing angles and phases (and mass hierarchy)

#### Group Theoretical Origin of CP Violation

Basic idea

Discrete symmetry **G** 

M.-C.C., K.T. Mahanthappa Phys. Lett. B681, 444 (2009)



- if  $Z_3$  symmetric  $\Rightarrow \langle \Delta_1 \rangle = \langle \Delta_2 \rangle = \langle \Delta_3 \rangle \equiv \langle \Delta \rangle$  real
- Complex effective mass matrix: phases determined by group theory

C<sub>ij</sub><sup>k</sup>: complex CG coefficients of **G** 

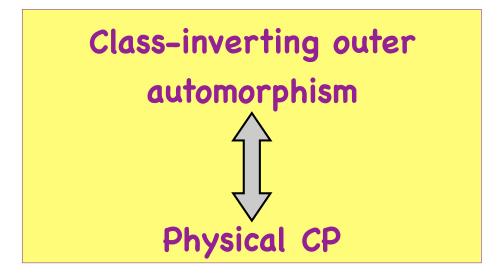
$$M = \begin{pmatrix} C_{11^2} & C_{21^1} \\ C_{12^1} & C_{22^3} \end{pmatrix} Y \langle \Delta \rangle$$

## Group Theoretical Origin of CP Violation

L(x)canonical CP automorphism L' (Px) transformation U

M-CC, Mahanthappa (2009); M.-C.C, M. Fallbacher, K.T. Mahanthappa, M. Ratz, A. Trautner, NPB (2014)

complex CGs  $\Rightarrow$  G and physical CP transformations do not always commute



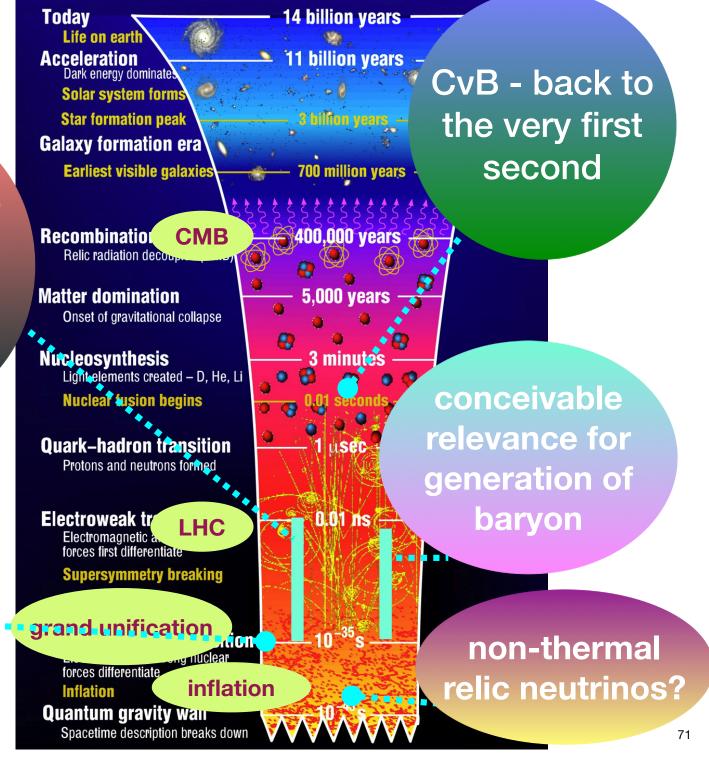


## Outlook

## History of the Universe

physics for v mass generation unknown

unique
window into
GUT scale
physics



#### Outlook

- Fundamental origin of fermion mass & mixing patterns still unknown
  - It took decades to understand the gauge sector of SM
- Uniqueness of Neutrino masses offers exciting opportunities to explore BSM Physics
  - Many NP frameworks; addressing other puzzles
  - Early Universe (baryogengesis thru leptogenesis, non-thermal relic neutrinos)
- New Tools/insights:
  - Non-Abelian Discrete Flavor Symmetries ⇒ origin of CP
    - Deep connection between outer automorphisms and CP
  - Modular Flavor Symmetries
    - Enhanced predictivity of flavor models
    - Possible connection to more fundamental physics

