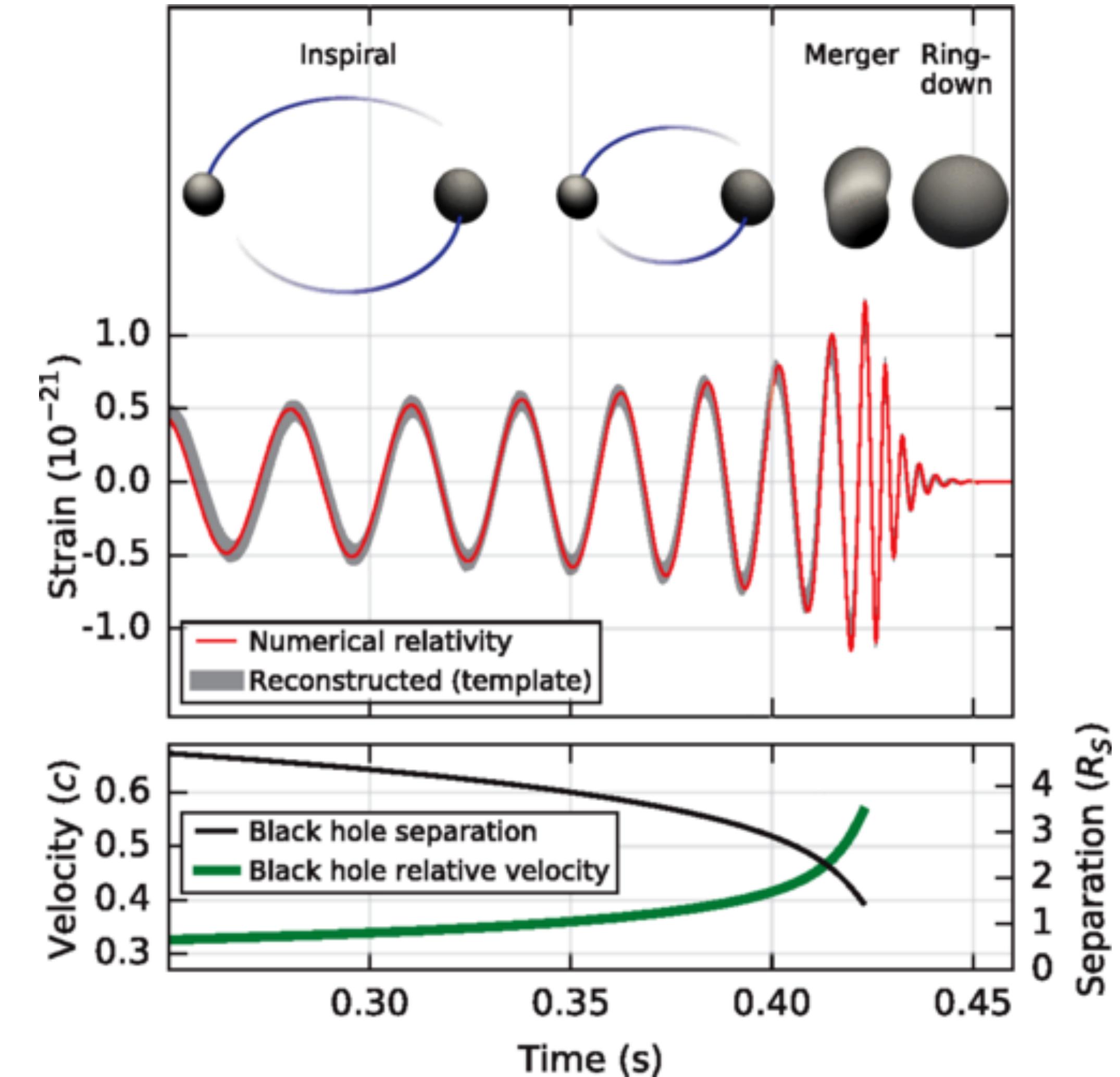


# Tests of General Relativity

Walter Del Pozzo

# Fundamental aspects of GW physics

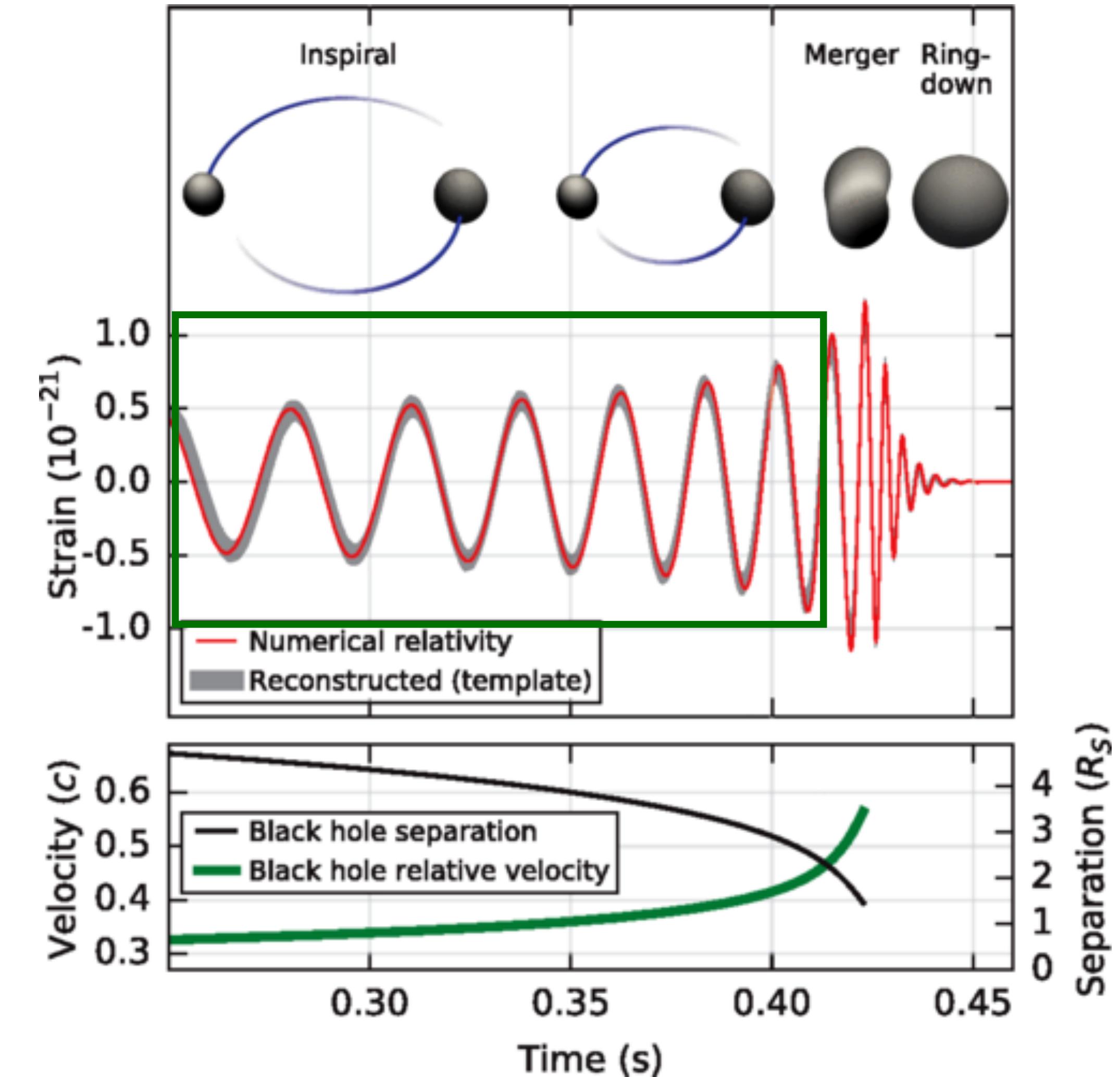
- In GR, gravitational waves (GW) are wave solutions to Einstein's equations generated from time varying mass quadrupoles and propagating at the speed of light



LVC, arXiv:1602.03837

# Fundamental aspects of GW physics

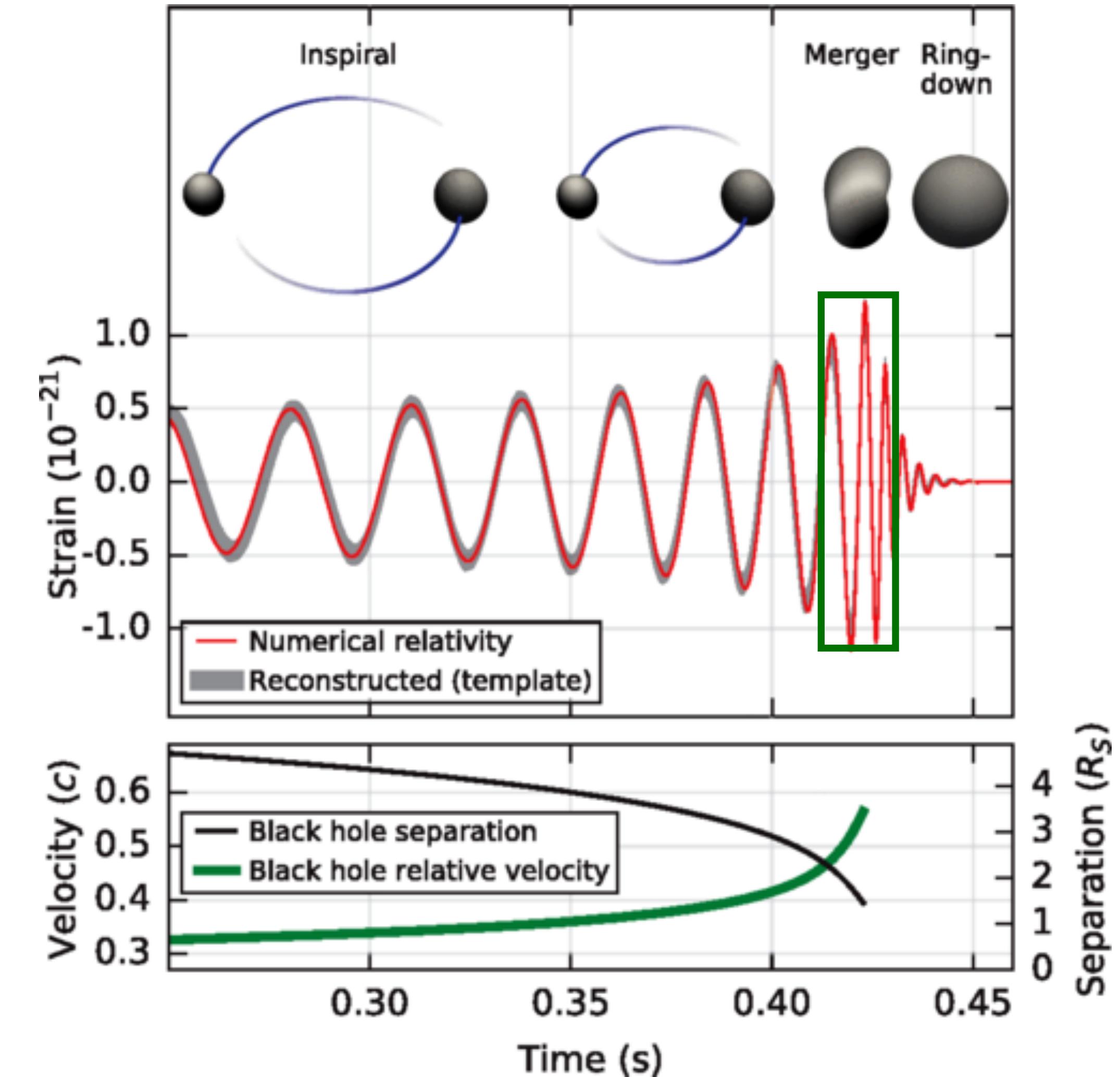
- Shape of GW signal carries information about
  - binary dynamics and component nature



LVC, arXiv:1602.03837

# Fundamental aspects of GW physics

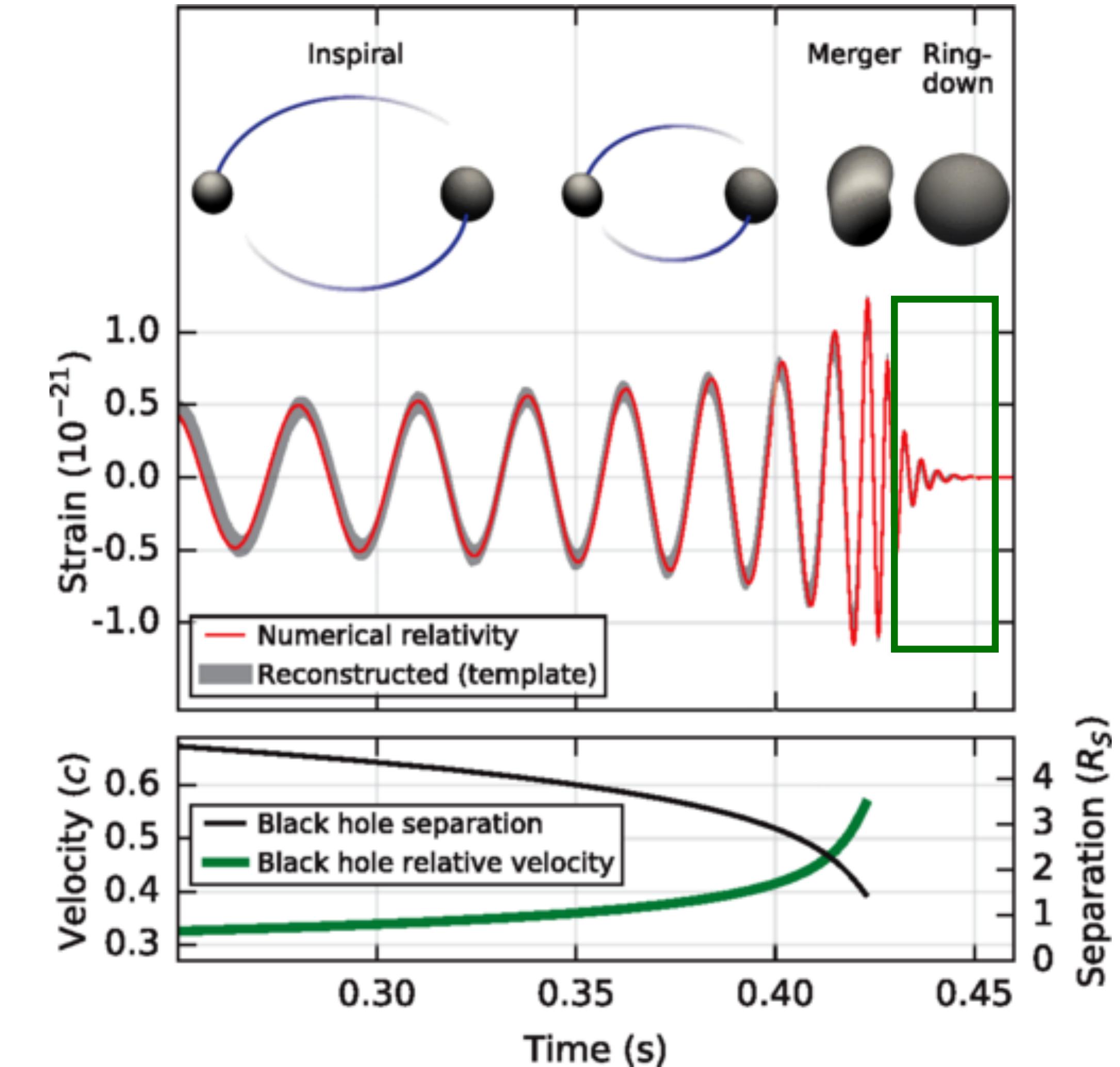
- Shape of GW signal carries information about
  - binary dynamics and component nature
  - non-linear dynamics of space-time



LVC, arXiv:1602.03837

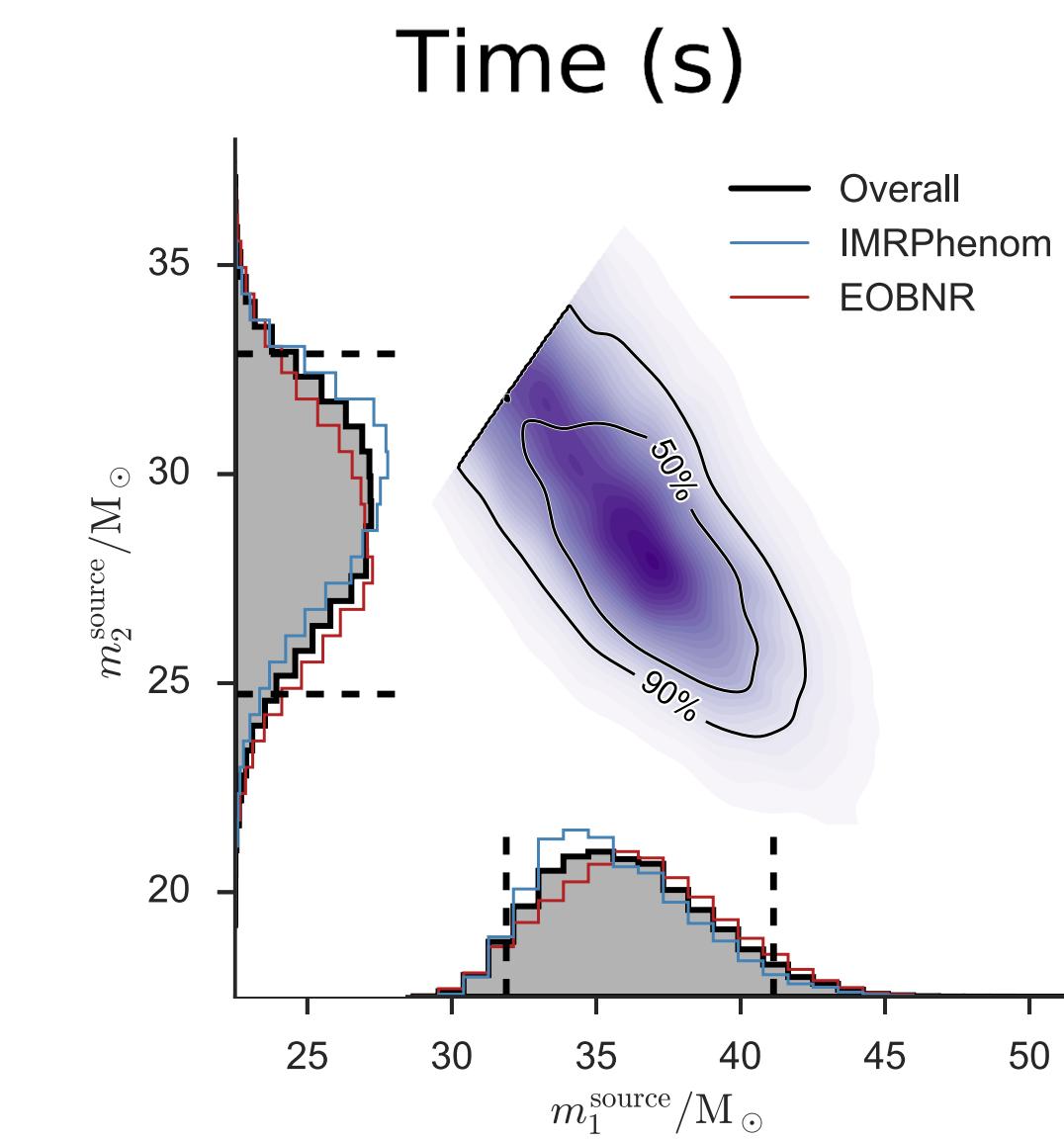
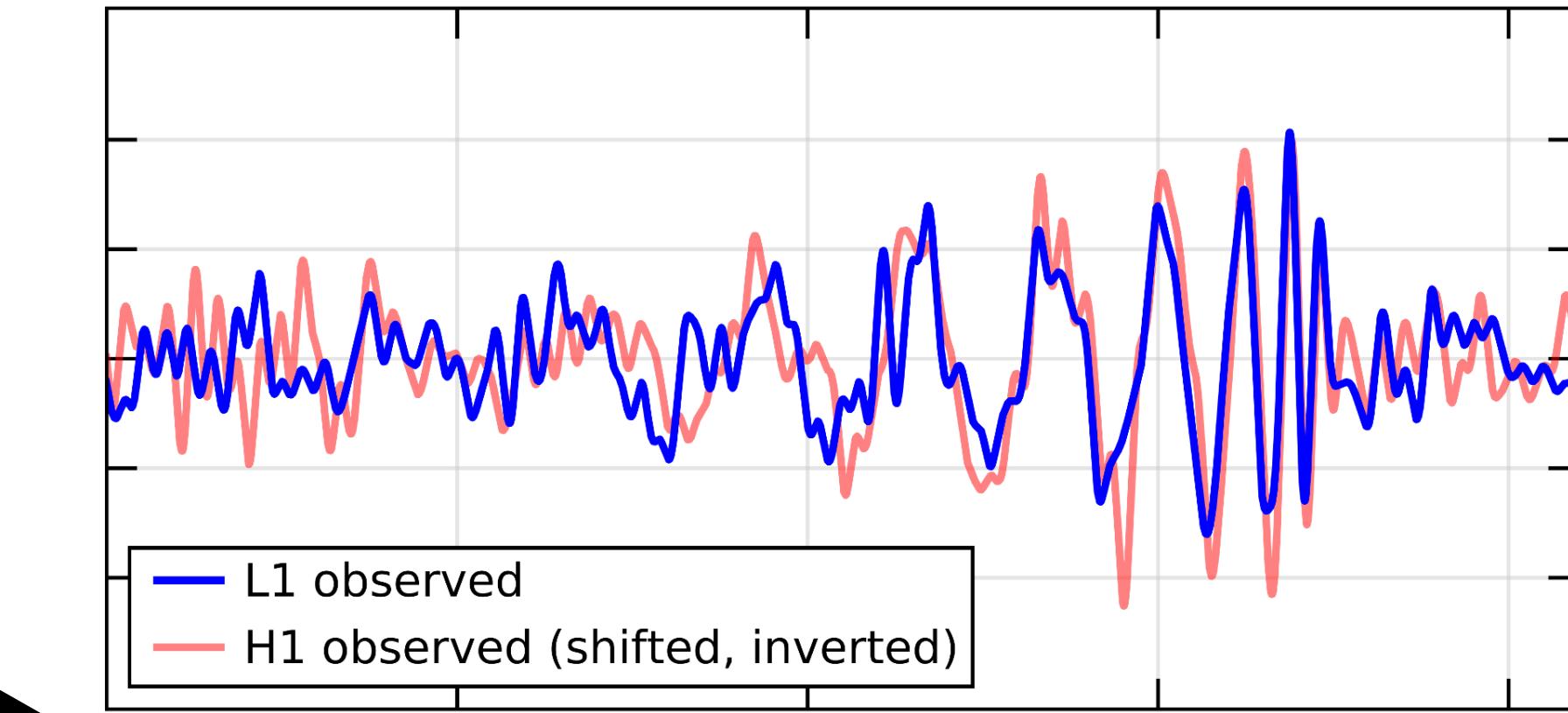
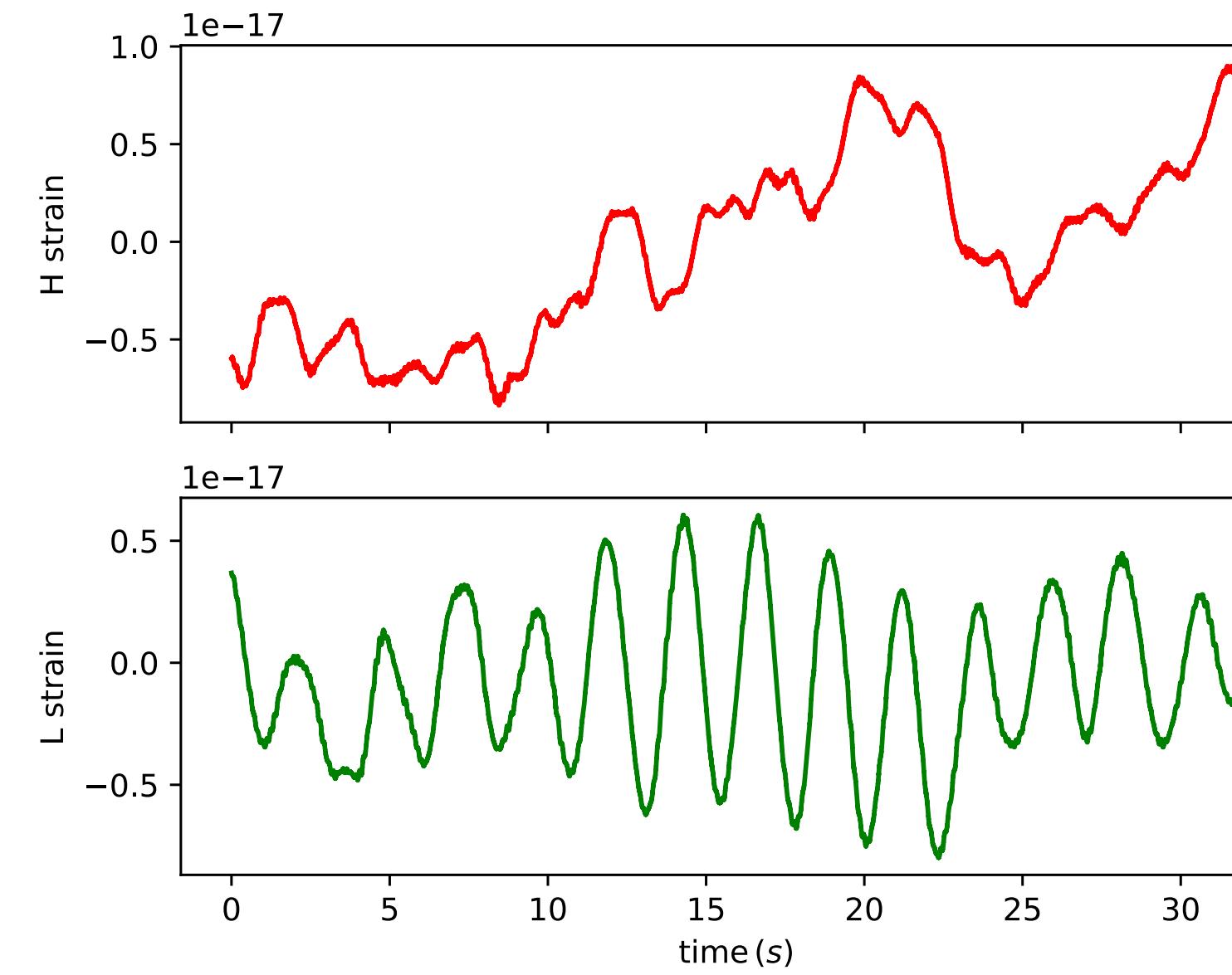
# Fundamental aspects of GW physics

- Shape of GW signal carries information about
  - binary dynamics and component nature
  - non-linear dynamics of space-time
  - final object nature

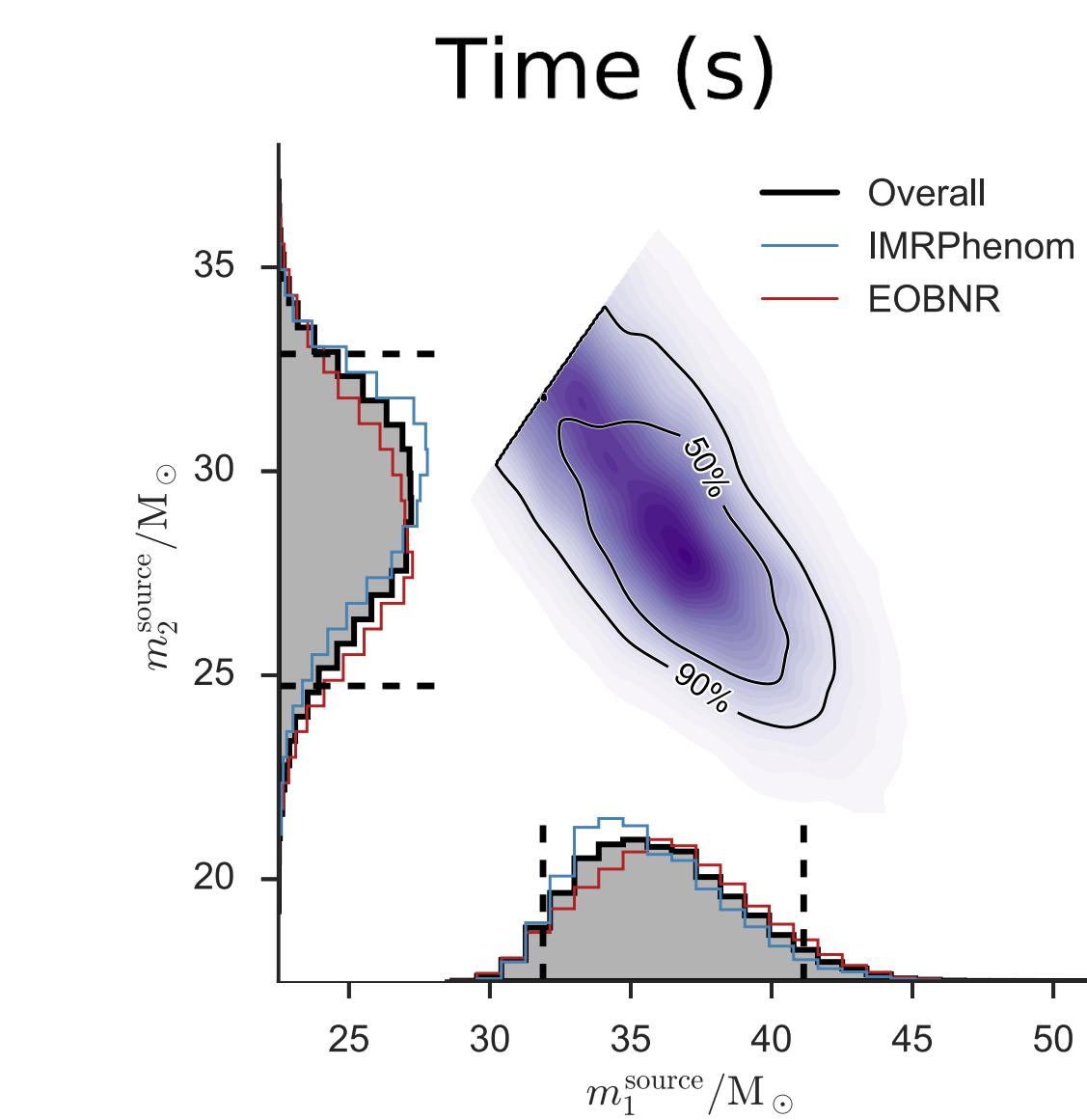
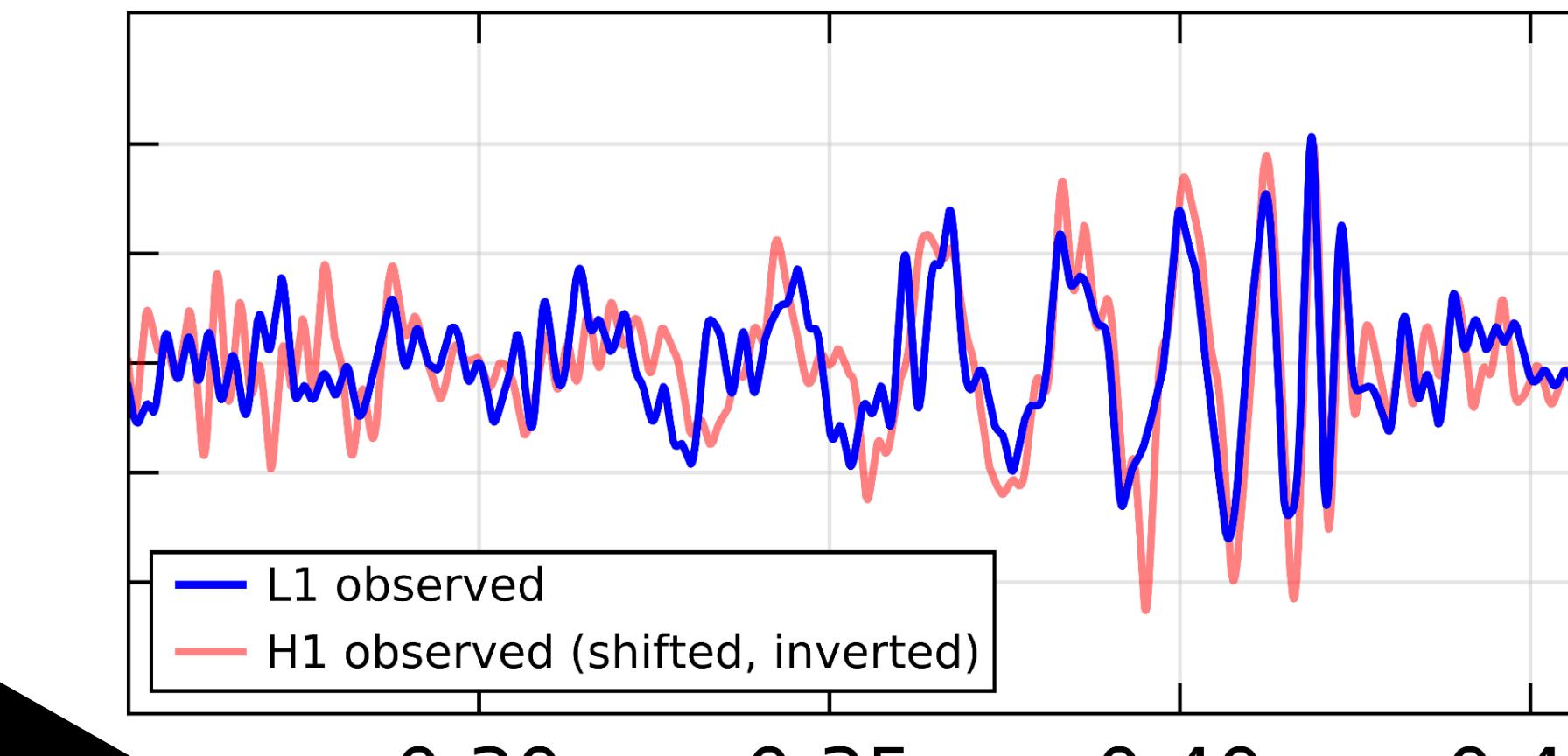
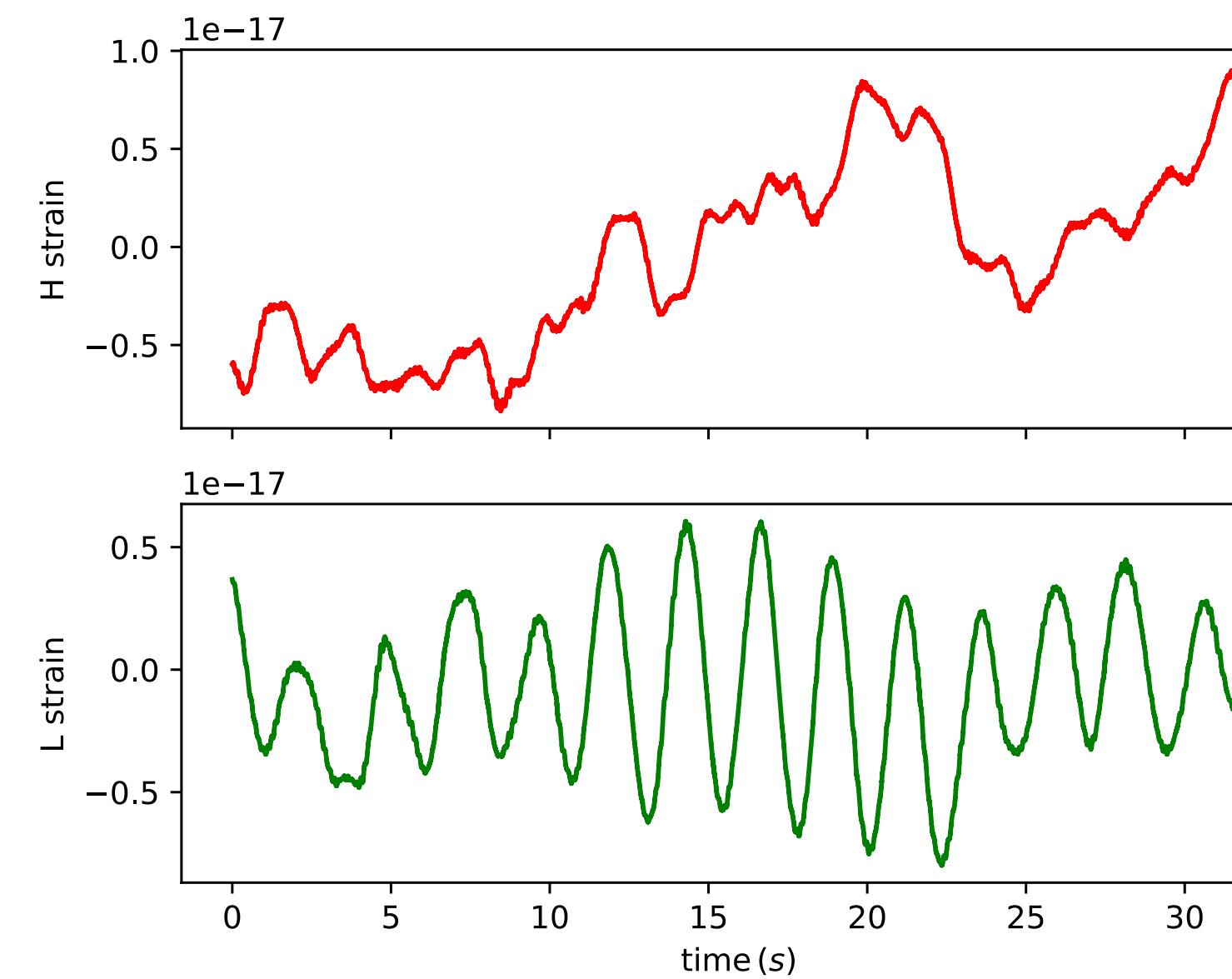


LVC, arXiv:1602.03837

## How the analysis works in a nutshell



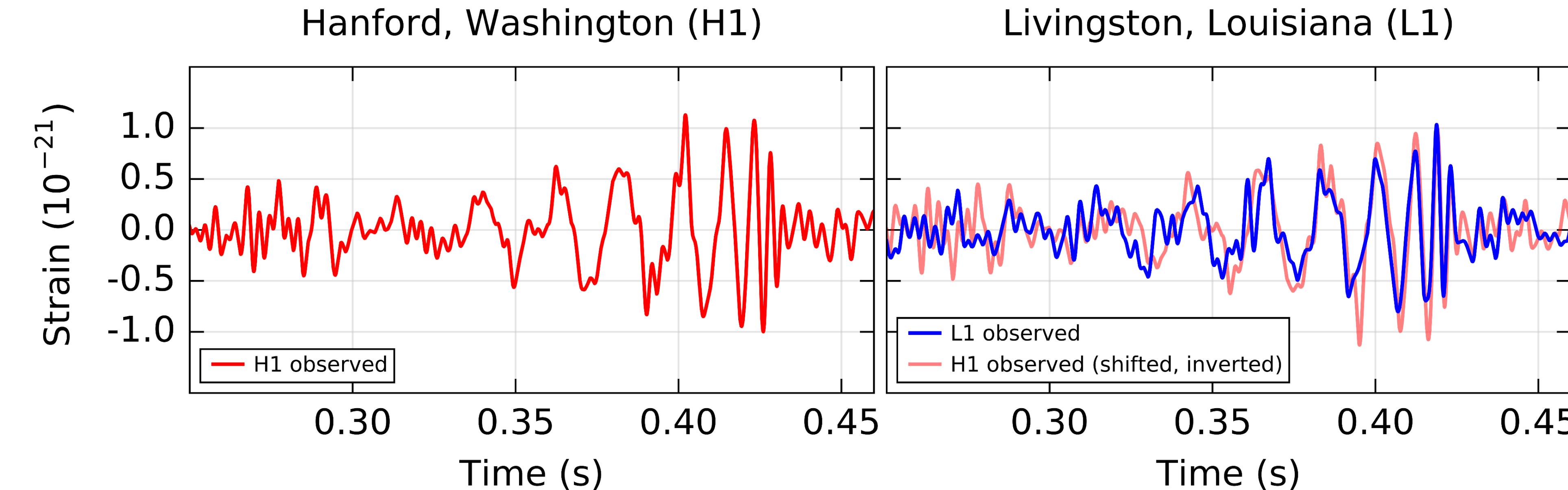
# How the analysis works in a nutshell



$$p(H|DI) = p(H|I) \frac{p(D|HI)}{p(D|I)}$$

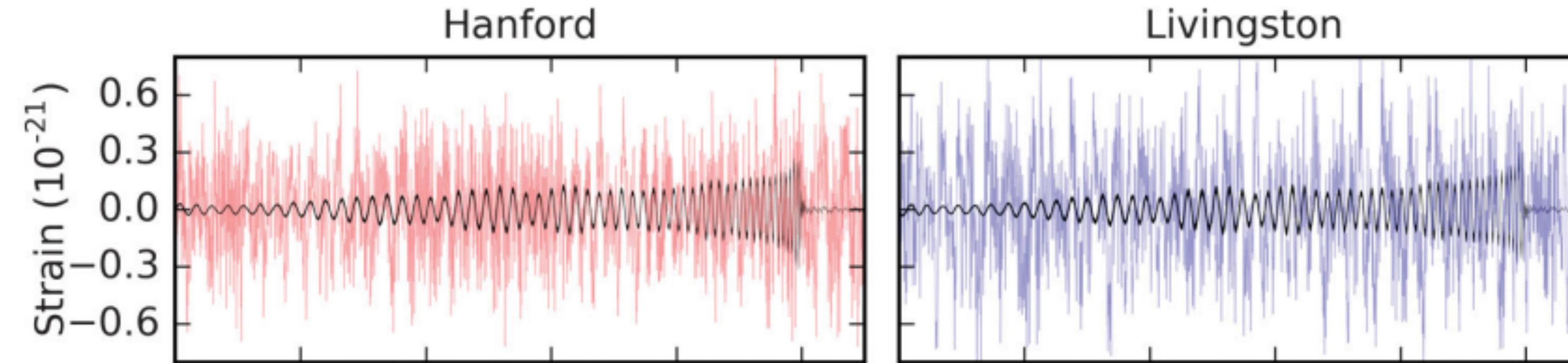
# Why Bayes' theorem?

- Gravitational wave events are rare
- Noise dominated detectors
- Need to know what we are looking for VERY well to detect it/measure its properties
  - Matched filtering



# Why Bayes' theorem?

- Matched filtering
  - Faithful models for the coalescence of compact binaries
    - effective-one-body family
    - numerical relativity
    - phenomenological models
    - surrogate models



# Why Bayes' theorem?

- Matched filtering

- Faithful

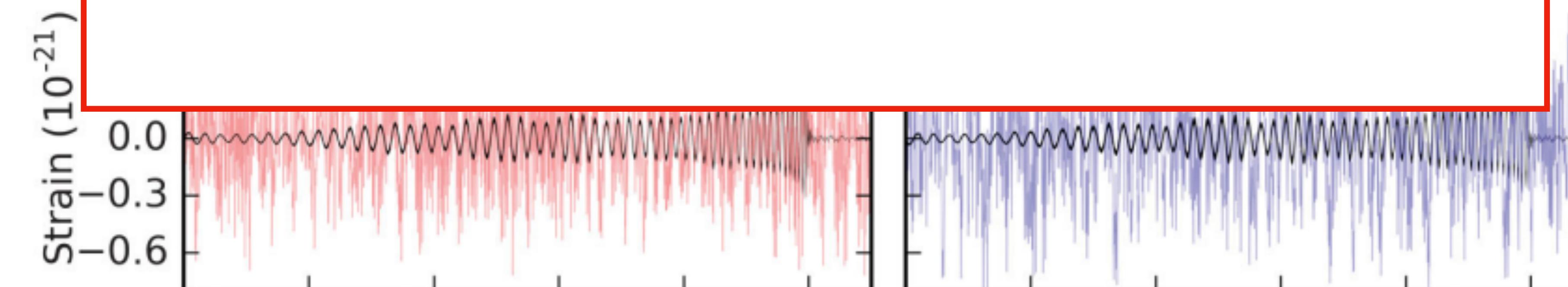
- effect

- numer

- phen

- surro

**In general, no alternative theory of GW generation/propagation has been developed with a detail and accuracy comparable to GR**



- Probability theory operates on logical propositions:
  - Admissible propositions:
    - statements to which one can assign a True (1) or False (0) value
  - $A = \text{"The sun is a star"}$
  - $B = \text{"The total mass of GW150914 was 70 Msun"}$



- Arbitrarily complex propositions constructed via basic boolean operations

- Negation (NOT):

$$\bar{A}$$

- Conjunction (AND):

$$A \cdot B \equiv AB$$

- Disjunction (OR):

$$A + B$$

- Probabilities are always conditional
  - Probability assignments depend on the “background information”



I: The die is unbiased

$$p(6|I) = \frac{1}{6}$$



I': The die is biased

$$p(6|I') > \frac{1}{6}$$

# The quantitative rules

- From Cox [1] and Jaynes [2]:
  - Product rule

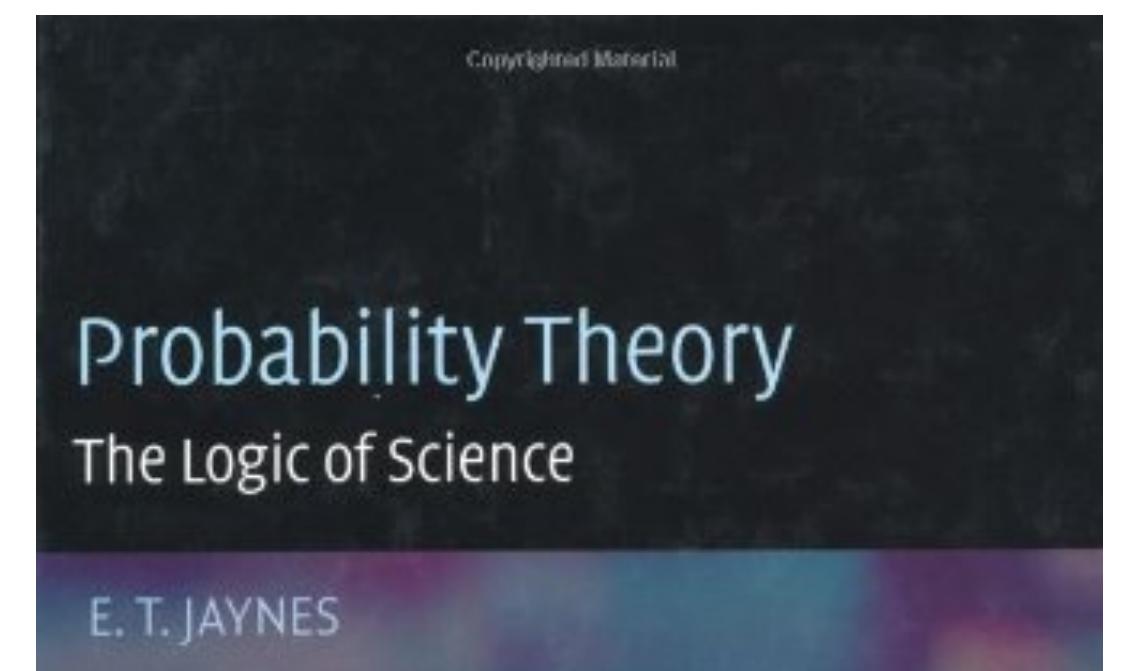
$$p(AB|C) = p(A|BC)p(B|C)$$



- Sum rule

$$\begin{aligned} p(A + B|C) &= p(A|C) + p(B|C) - p(AB|C) \\ &= p(A|C) + p(B|C) \iff p(AB|C) = 0 \end{aligned}$$

A and B are mutually exclusive (on the information C)



[1] R. T. Cox. Probability, frequency and reasonable expectation. *American Journal of Physics*, 14(1):1–13, 1946

[2] E. Jaynes. *Probability Theory: The Logic of Science*. University Press, 2003

# Bayes theorem

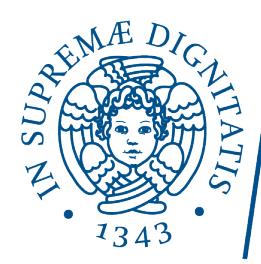
- From the product rule

$$\begin{aligned} p(AB|C) &= p(A|BC)p(B|C) \\ &= p(B|AC)p(A|C) \end{aligned}$$

- Bayes theorem:

$$p(A|BC) = \frac{p(B|AC)p(A|C)}{p(B|C)}$$





- Define the following statements:
  - A = H: hypothesis
  - B = D: observation
  - C = I: whatever relevant information

$$p(H|DI) = p(H|I) \frac{p(D|HI)}{p(D|I)}$$

posterior      prior      likelihood  
                        evidence

$$p(D|I) = \sum_i p(H_i|I)p(D|H_i I)$$

marginalisation



- Consider 2 competing hypotheses (models)  $H_1, H_2$
- Given an observation  $D$ , which model is to be preferred?

$$p(H_1|DI) = p(H_1|I) \frac{p(D|H_1 I)}{p(D|I)}$$

$$p(H_2|DI) = p(H_2|I) \frac{p(D|H_2 I)}{p(D|I)}$$

# Model selection

- The troublesome term

$$p(D|I) = \sum_i p(H_i|I)p(D|H_i I)$$

- Simplifies taking the ratio

$$O_{12} = \frac{p(H_1|I)p(D|H_1 I)}{p(H_2|I)p(D|H_2 I)} = \frac{p(H_1|I)}{p(H_2|I)} B_{12}$$

↑  
prior odds      ↑  
                    Bayes' factor

- The validity of GR in GW-based tests is quantified by the Bayes factor

# Model selection

- If the model  $H_i$  depends on a set of parameters  $\theta_i$  need to marginalise over them

$$p(D|H_i I) = \int_{\Theta} d\theta_i p(\theta_i|H_i I)p(D|\theta_i H_i I)$$

- Odds ratio

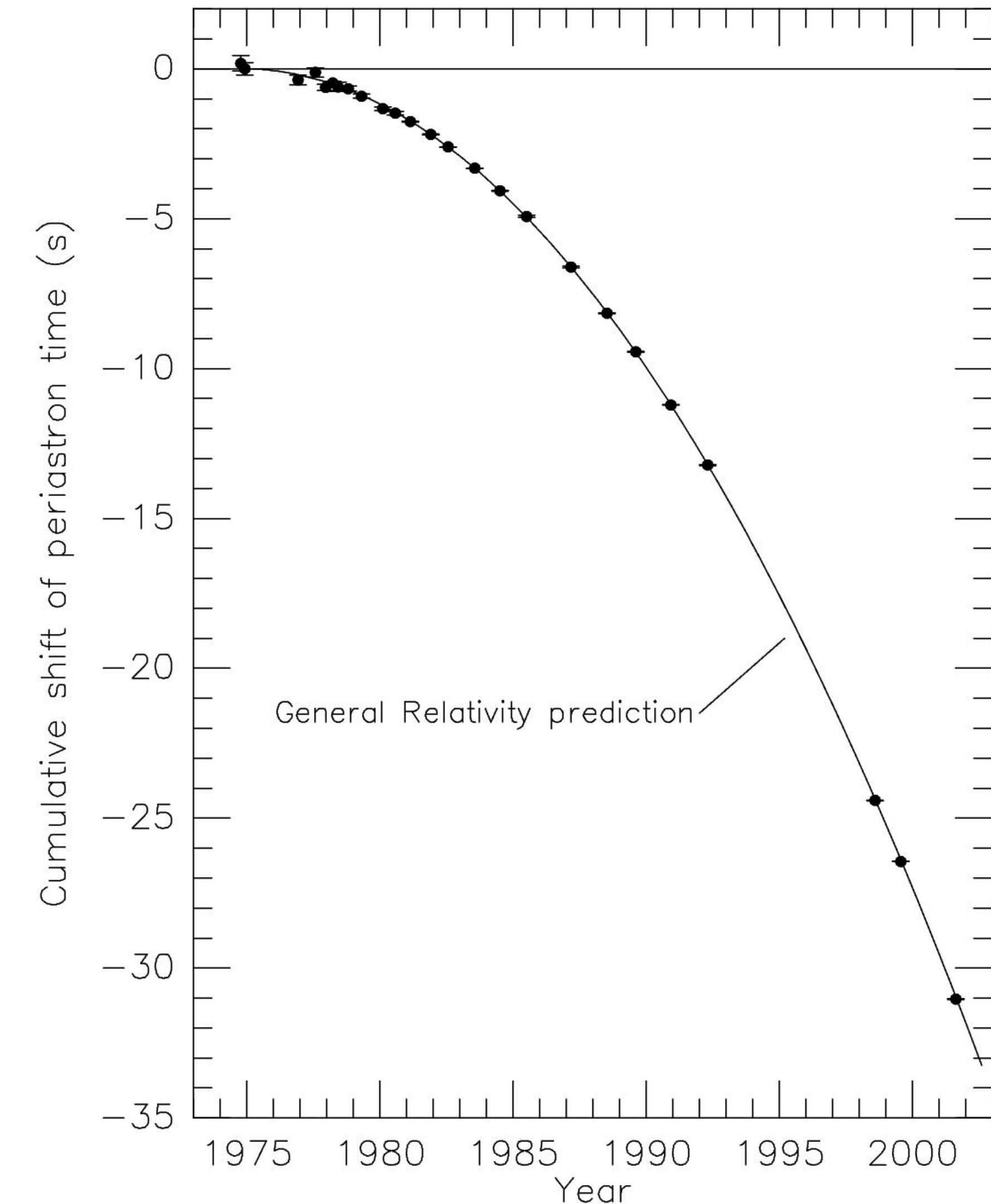
$$O_{ij} = \frac{p(H_i|I)}{p(H_j|I)} \frac{\int_{\Theta_i} d\theta_i p(\theta_i|H_i I)p(D|\theta_i H_i I)}{\int_{\Theta_j} d\theta_j p(\theta_j|H_j I)p(D|\theta_j H_j I)}$$

- Integrals are complicated to compute, dedicated stochastic samplers

# Tests of general relativity and black hole nature

# Why testing general relativity

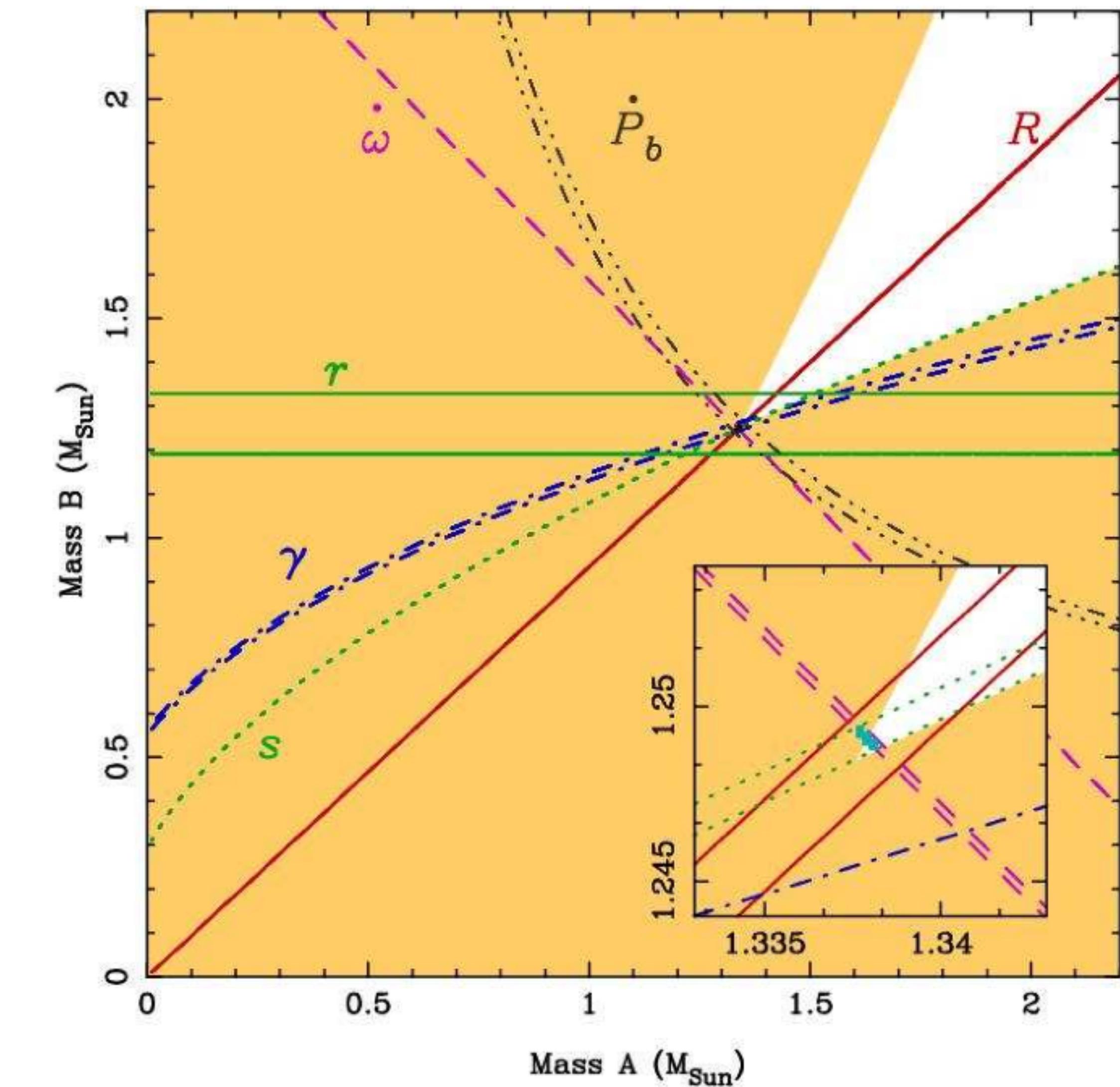
- GR is non renormalisable
  - higher order terms in the action (small scale)
- Dark matter & dark energy
  - signature of modified gravity(large scale)?
- GR is extremely well tested in between these regimes (Will, arXiv:1403.7377, Psaltis, arXiv: 0806.1531)



Weisberg &amp; Taylor, arXiv:0407149

# Double pulsar PSR J0737-3039

- Before GWs, state-of-art from PSR J0737-3039 timing
  - Compare time of arrivals (TOAs) with GR prediction
    - Damour-Deruelle (DD, 1986) model
- $$\dot{\omega} = 3T_{\odot}^{2/3} n_b^{5/3} \frac{1}{1-e^2} (m_p + m_c)^{2/3},$$
- $$\gamma_p = T_{\odot}^{2/3} n_b^{-1/3} e \frac{m_c(m_p + 2m_c)}{(m_p + m_c)^{4/3}},$$
- $$r_p = T_{\odot} m_c,$$
- $$s = \sin \iota = T_{\odot}^{-1/3} n_b^{2/3} x_p \frac{(m_p + m_c)^{2/3}}{m_c},$$
- $$\dot{P}_b = -\frac{192\pi}{5} T_{\odot}^{5/3} n_b^{5/3} f(e) \frac{m_p m_c}{(m_p + m_c)^{1/3}}.$$
- Exquisite constraints O(0.1%) on conservative dynamics
  - Weak field test



# Gravitational strong-field

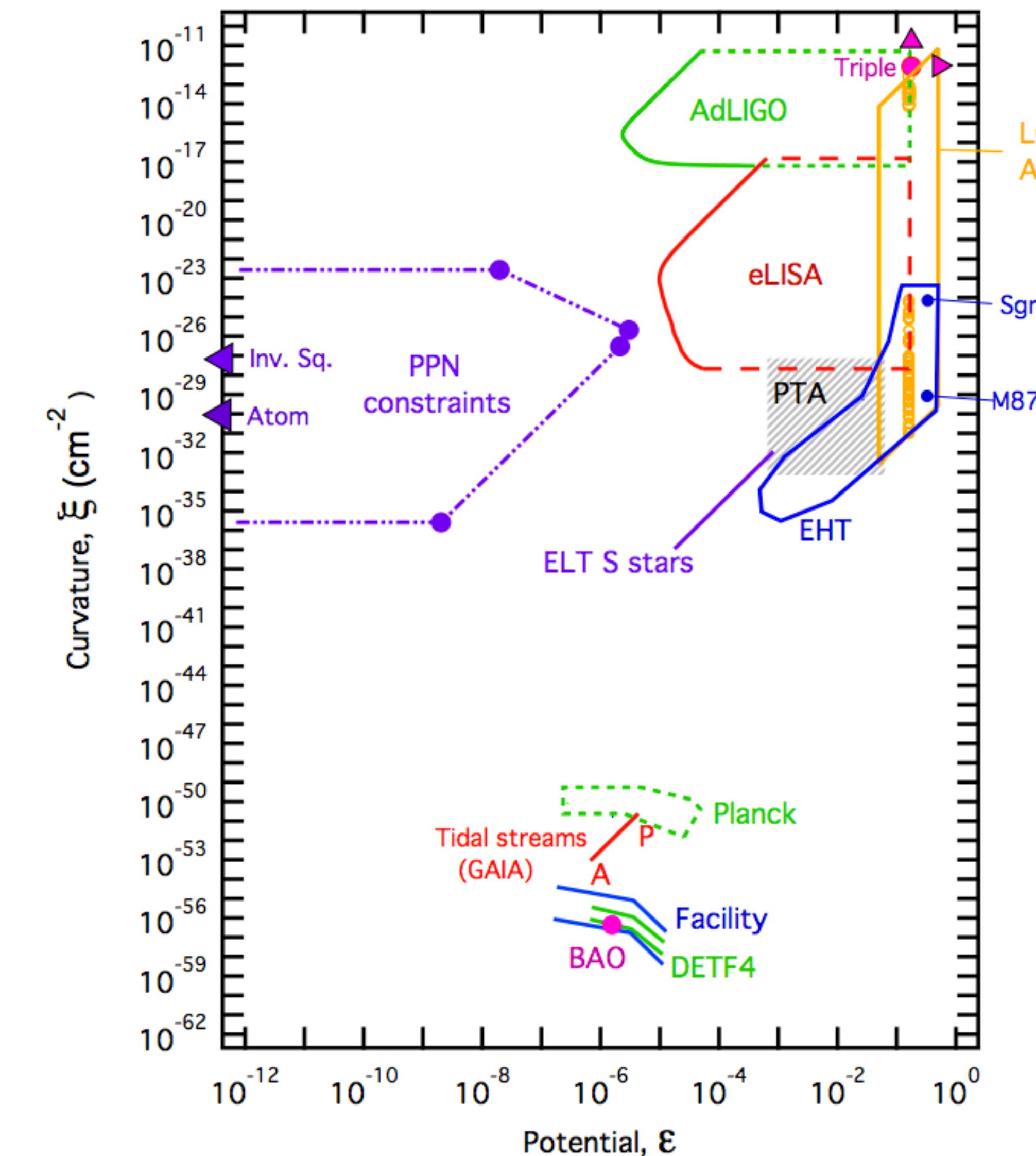
- Field strength

$$\epsilon = \frac{GM}{c^2 R}$$

- Curvature (Kretschmann scalar)

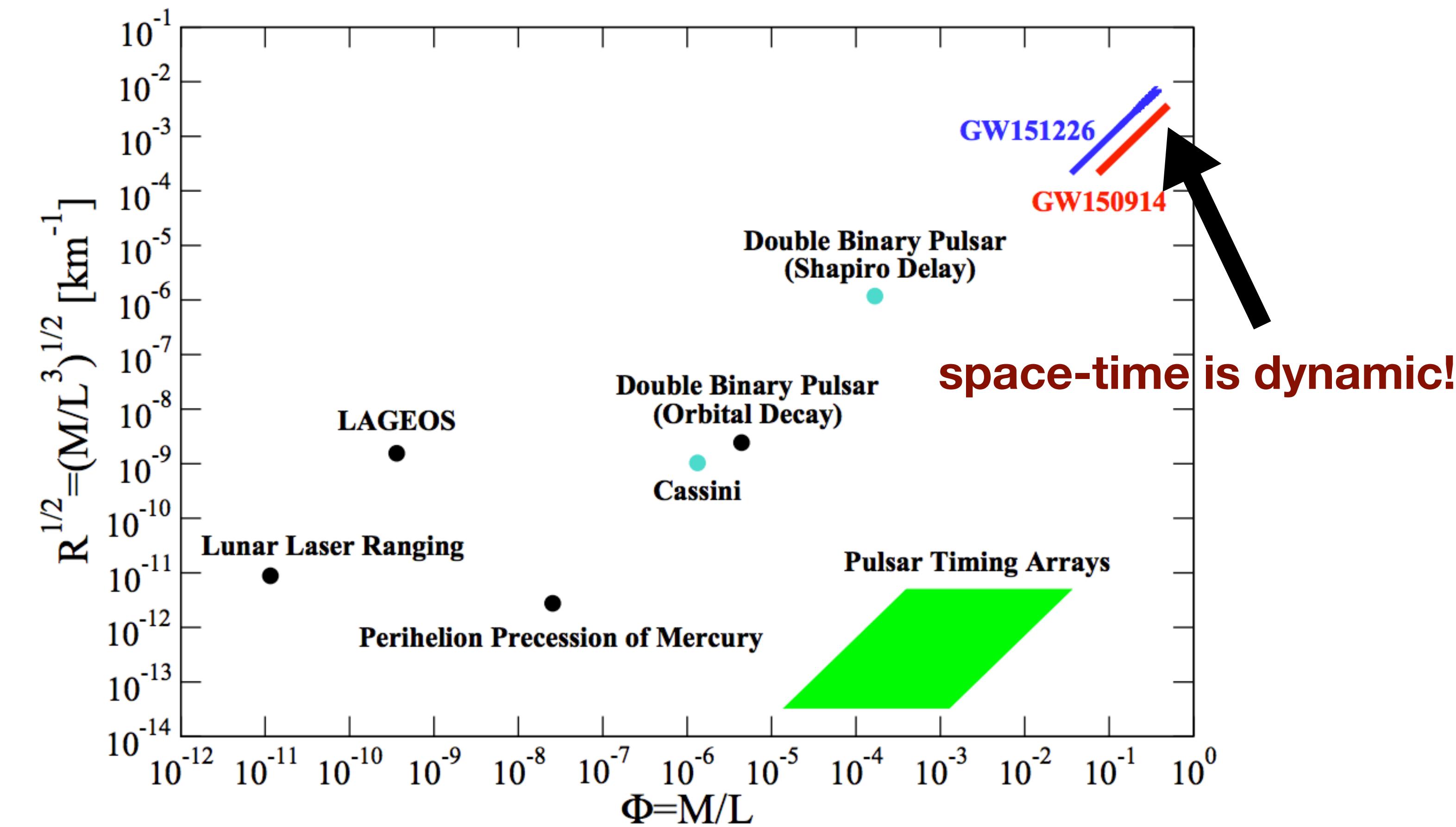
$$\xi = (R_{\alpha\beta\gamma\delta}R^{\alpha\beta\gamma\delta})^{1/2}$$

- Gravitational waves from binary black holes are the optimal probes



Baker et al, arXiv:1412.3455

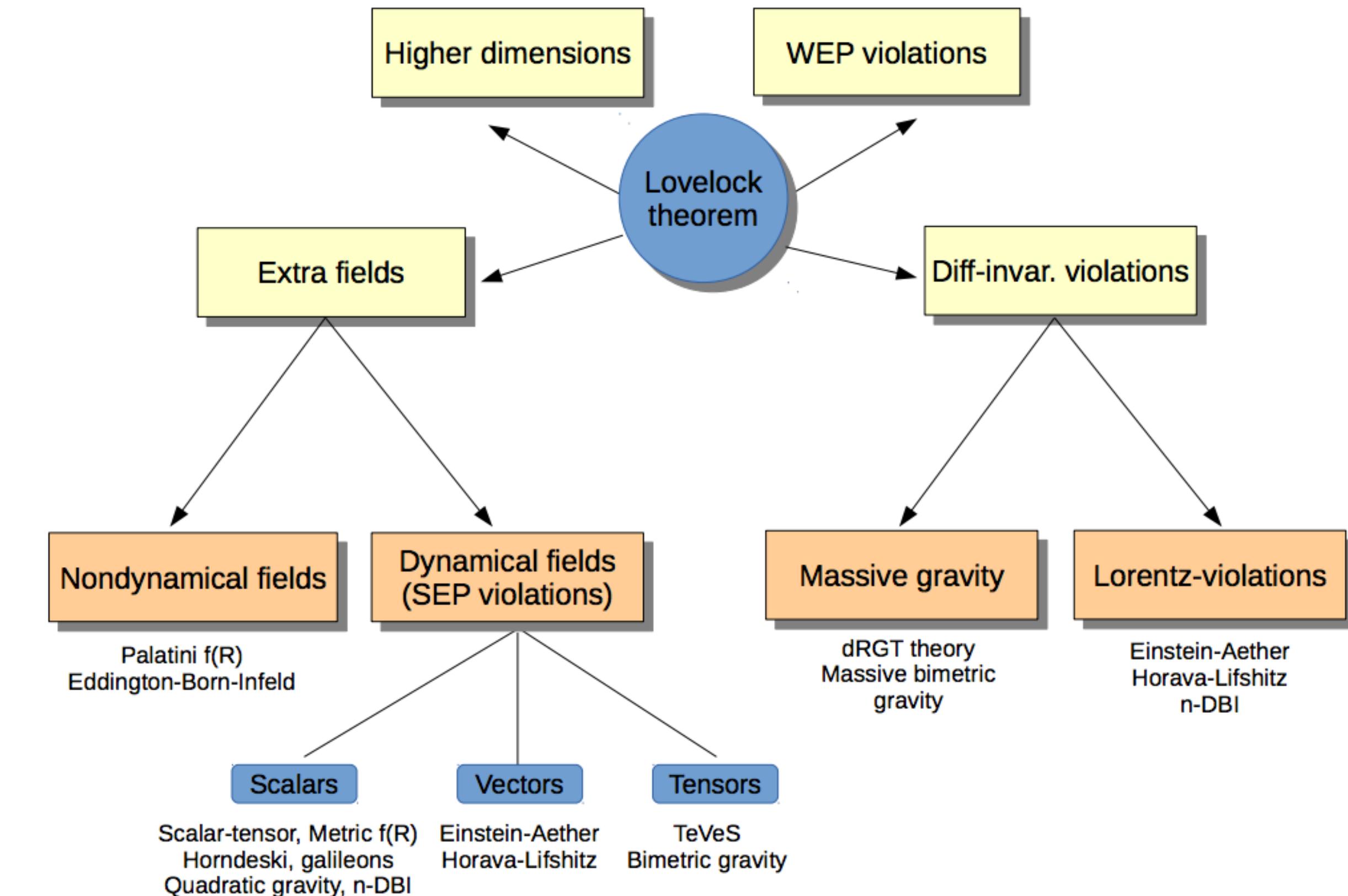
# Gravitational strong-field



# Extensions of GR

- Alternative theories
  - Introduce extra degrees of freedom:
    - additional fields
    - higher-curvature terms
  - Challenge GR assumptions:
    - Lorentz invariance
    - Equivalence principle
  - Need tests in the strong-field

**Lovelock theorem:** In 4D, the only divergence free symmetric rank-2 tensor constructed only by the metric and its derivatives up to 2nd order and preserving diffeomorphism invariance is the Einstein tensor plus a constant.



Berti et al, arXiv:1501.07274

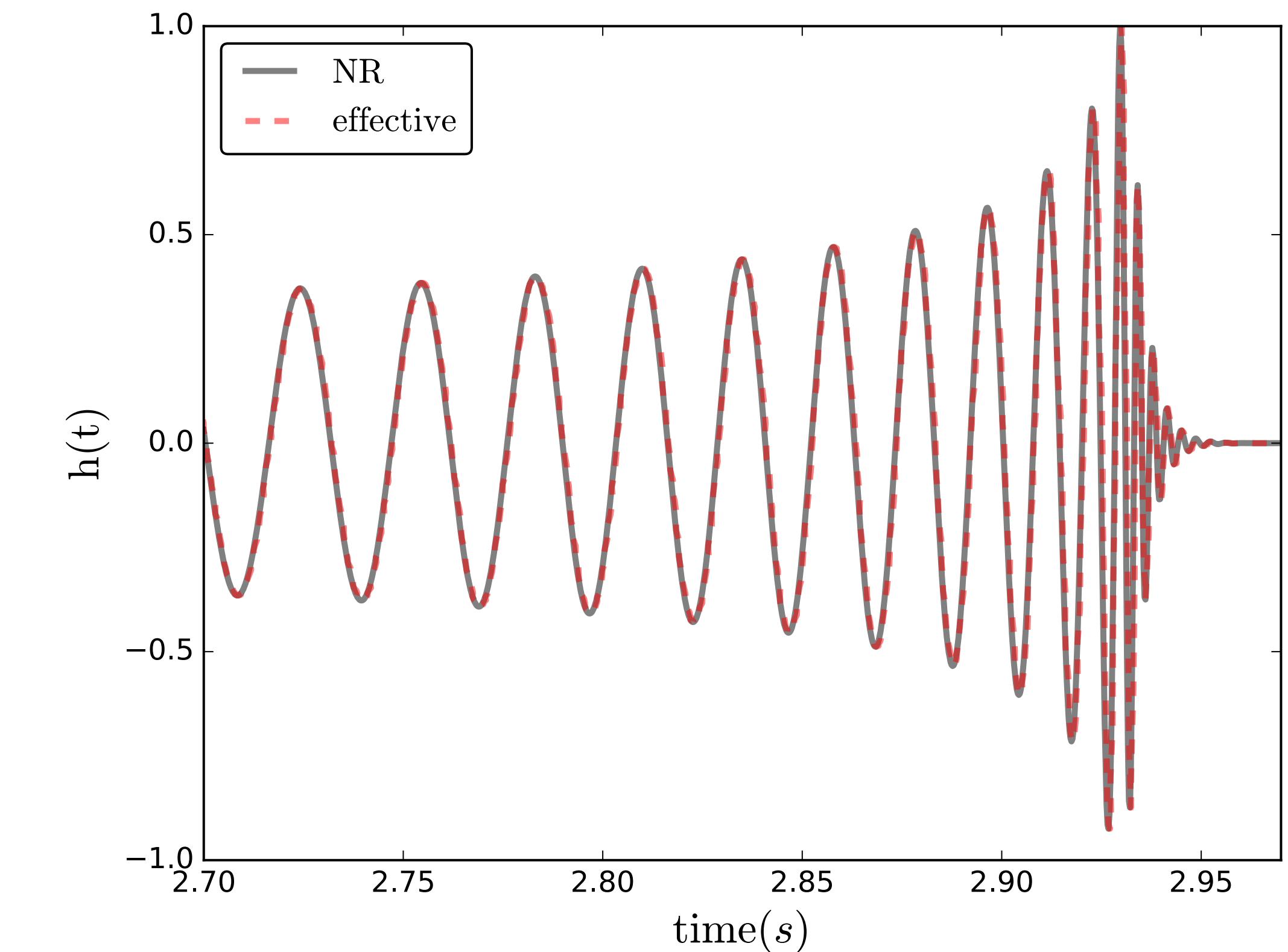
# GW templates in GR

- Analytical, parametric description of GW solution in GR

$$h(f; \theta) = A(f; \theta) e^{i\Phi(f; \theta)}$$

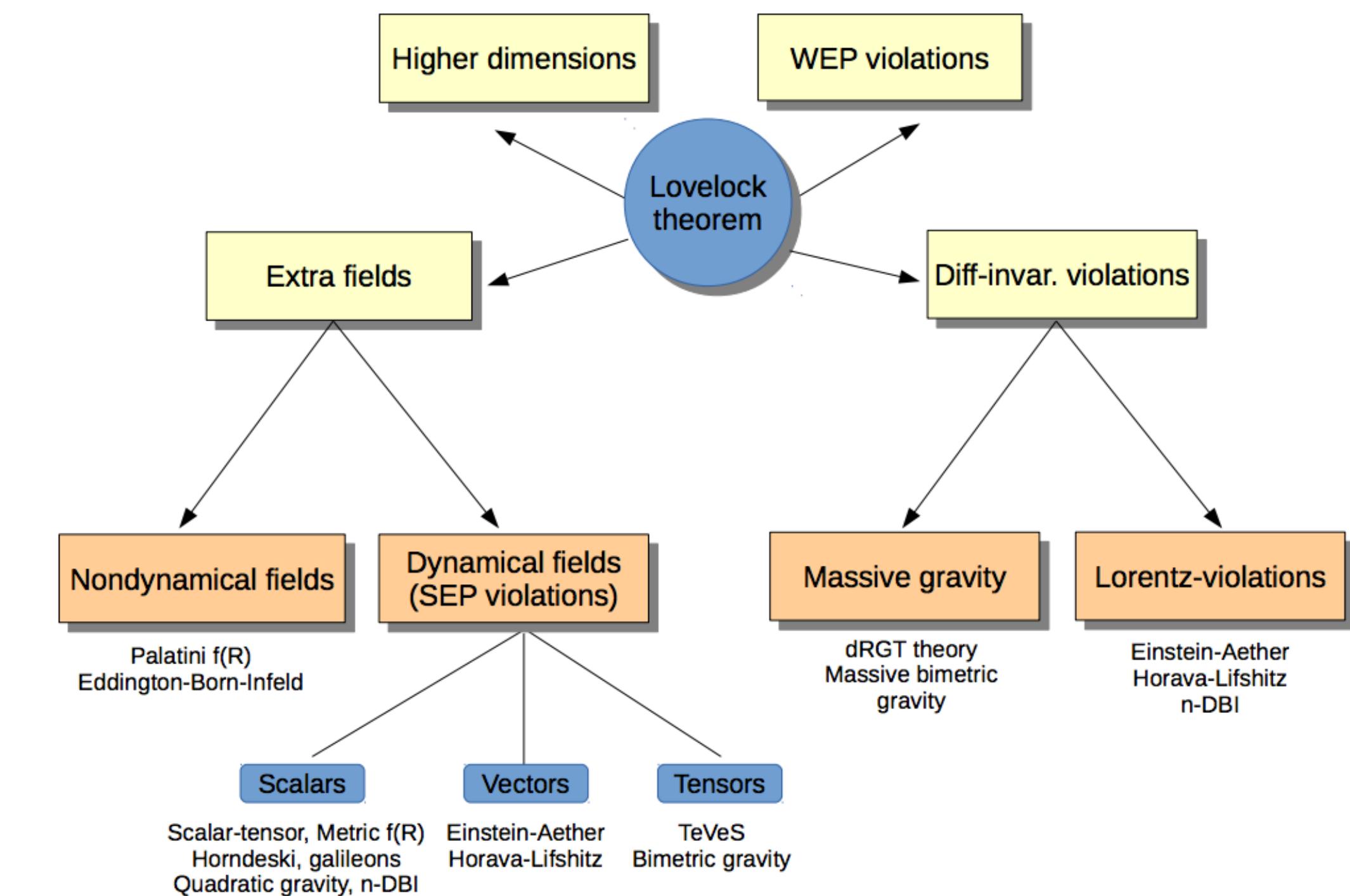
$$\Phi(f; \theta) \equiv \Phi(f; m_1, m_2, \vec{s}_1, \vec{s}_2)$$

- Suitable for detection, parameter estimation and parametric tests of general relativity



# GW in alternative gravity

- Alternative to GR introduce extra-fields, curvature terms, challenge GR pillars, ...
- Almost no full solution in non-GR known (but see Okounkova et al, arXiv:1705.07924)
- GW generation
  - non-GR action (extra fields, higher curvature, ...)
  - non-BH sources
- Propagation (Lorentz violations, graviton mass, ...):
  - GR-like BBH dynamics, but modified GW propagation
- non-BHs (extra-fields, exotic objects):
  - tidal deformability
  - ringdown spectrum
  - echoes



- Alternative theories of gravity/non-BHs modify the waveform
  - change the  $\varphi$  coefficients by introducing additional parameters
    - e.g. “massive gravity”
    - add extra orders not present in the GR waveform
      - e.g. Brans-Dicke
  - Non-BHs show different merger and ringdown spectra

$$h(f) = A(f)e^{i\Phi(f)}$$

$$\Phi(f) = \sum_{k=1}^7 (\varphi_k + \varphi_k^l \log(f)) f^{(5-k)/3} + \sum_{i \neq k} \varphi_i f^i$$

$$\varphi_j \equiv \varphi_j(m_1, m_2, \vec{s}_1, \vec{s}_2) \quad \forall j = k, i$$

- Two strategies to test GR
  1. Self-consistency tests: perturb around GR and check for evidence of inconsistencies (e.g. Li+, arXiv:1110.0530)
  2. Targeted tests: assume an alternative theory of gravity and try to constrain its parameters (e.g. Del Pozzo+, arXiv:1101.1391)

- No alternative theory of gravity extensively studied as GR
  - No full IMR models available
  - Rely on “perturbations around GR”
    - Non-committal unmodelled constraints
  - What if something is so “non-GR” that we cannot detect it?

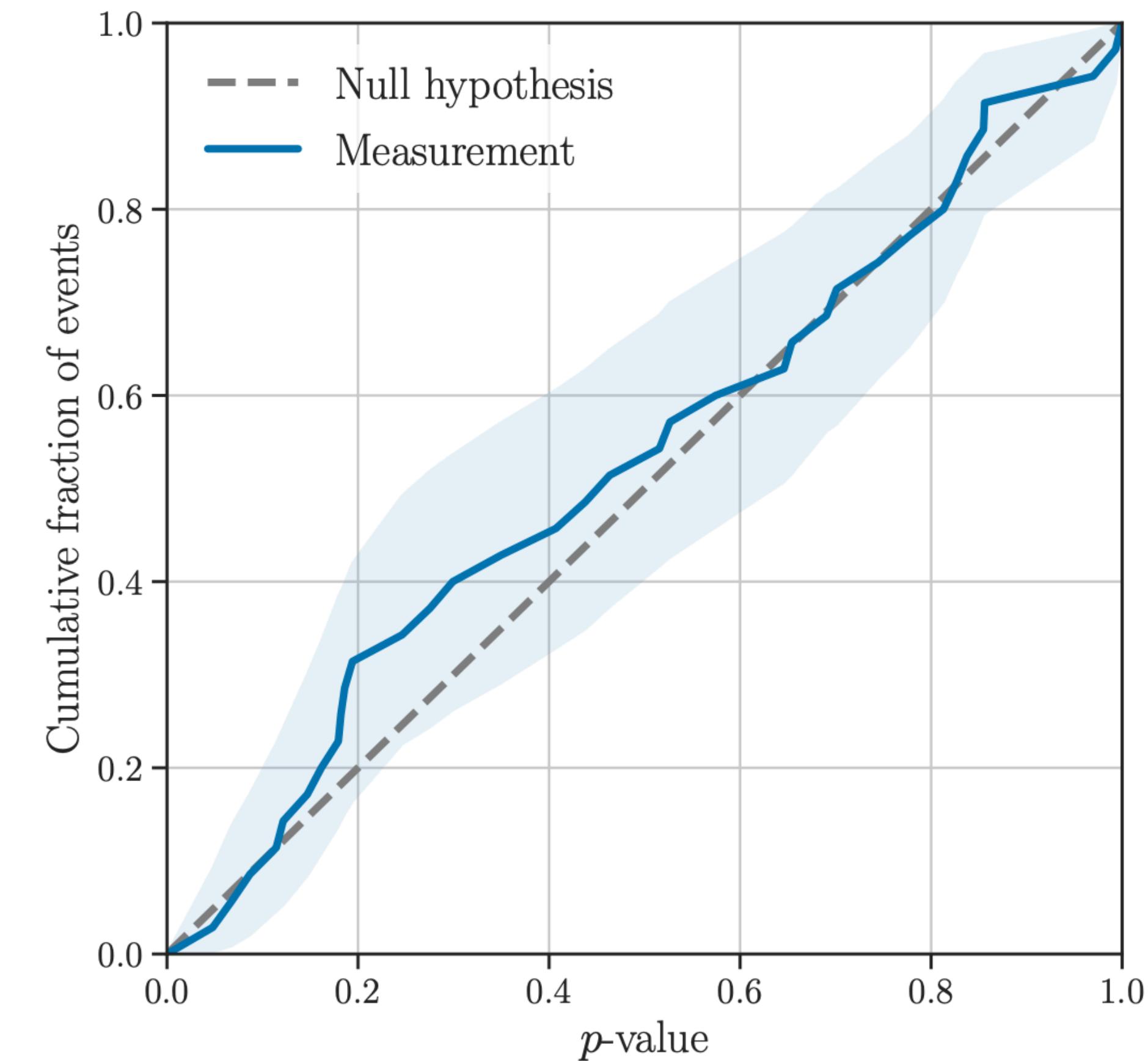
# A word of caution

---

- GR is not the only assumption entering the analysis
  - Noise properties
  - Detector calibration/characterisation
- When defining a “non-GR” hypothesis, we are questioning all of the assumptions defining the analysis
- The detection of a violation of GR does not imply that GR is violated but that at least one of our assumptions is

# Residuals test

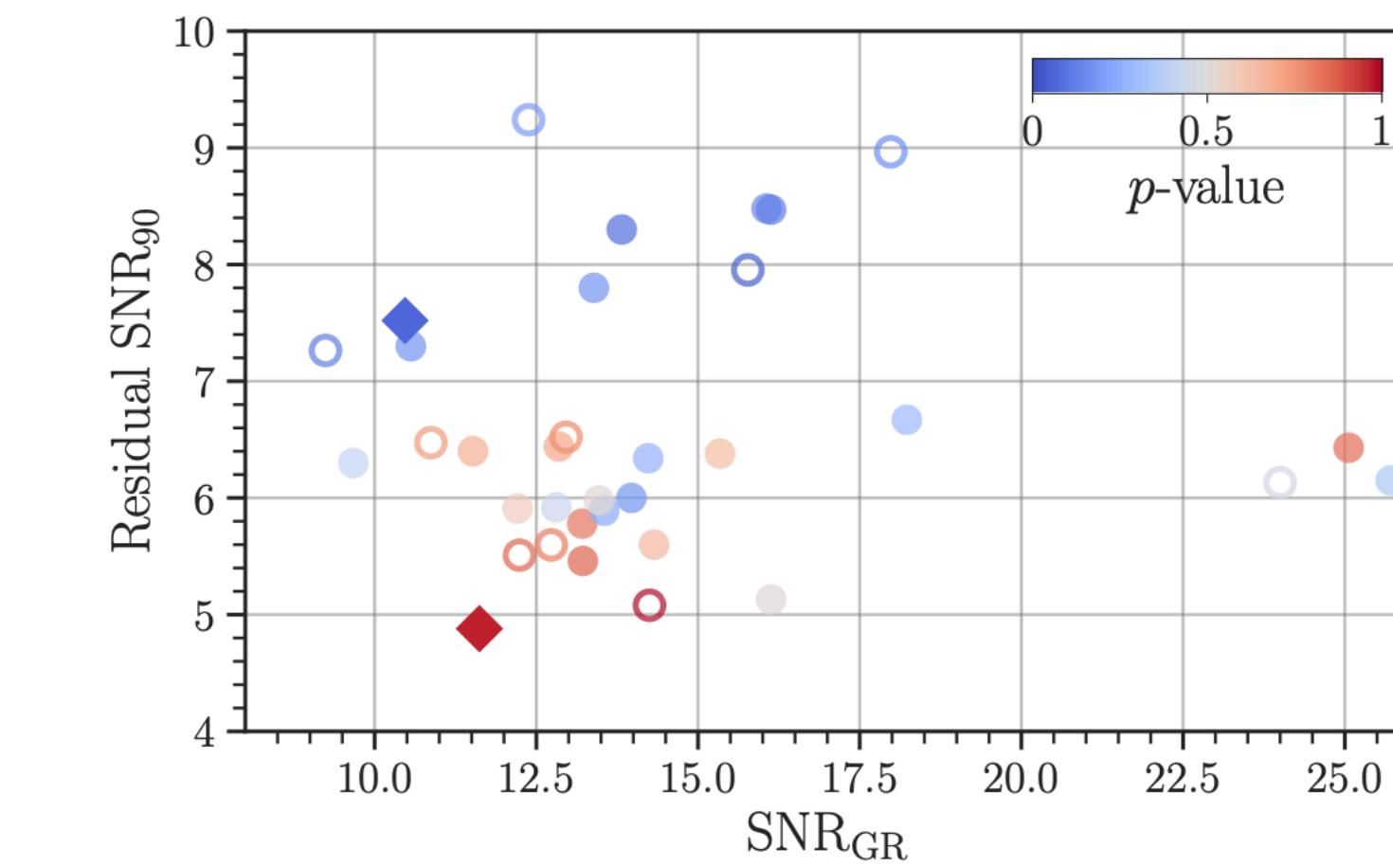
- Study the residual strain after subtracting the best-fit template for each event
- sensitive to any modeling systematics
  - deviation from GR
  - waveform
  - noise
- In the absence of systematics the residual SNR p-value should be uniformly distributed



# Residuals test

- subtract the maximum likelihood (best-fit) GRbased waveform from the data
- use BayesWave to place a 90%-credible upper-limit on the leftover coherent signal-to-noise ratio (SNR)
- p-value for noise-producing coherent power with  $SNR_{90}^n$  greater than or equal to the residual value  $SNR_{90}$ :  $p = P(SNR_{90}^n \geq SNR_{90} | noise)$ .

$$\text{fitting factor } FF_{90} = \frac{SNR_{GR}}{\sqrt{SNR_{res}^2 + SNR_{GR}^2}}$$



Events	SNR <sub>GR</sub>	Residual SNR <sub>90</sub>	FF <sub>90</sub>	p-value
GW190408_181802	16.06	8.48	0.88	0.15
GW190412	18.23	6.67	0.94	0.30
GW190421_213856	10.47	7.52	0.81	0.07
GW190503_185404	13.21	5.78	0.92	0.83
GW190512_180714	12.81	5.92	0.91	0.44
GW190513_205428	12.85	6.44	0.89	0.70
GW190517_055101	11.52	6.40	0.87	0.69
GW190519_153544	15.34	6.38	0.92	0.65
GW190521	14.23	6.34	0.91	0.28
GW190521_074359	25.71	6.15	0.97	0.35
GW190602_175927	13.22	5.46	0.92	0.86
GW190630_185205	16.13	5.13	0.95	0.52
GW190706_222641	13.39	7.80	0.86	0.18
GW190707_093326	13.55	5.89	0.92	0.25
GW190708_232457	13.97	6.00	0.92	0.19
GW190720_000836	10.56	7.30	0.82	0.18
GW190727_060333	11.62	4.88	0.92	0.97
GW190728_064510	13.47	5.98	0.91	0.53
GW190814	25.06	6.43	0.97	0.84
GW190828_063405	16.13	8.47	0.89	0.12
GW190828_065509	9.67	6.30	0.84	0.41
GW190910_112807	14.32	5.60	0.93	0.65
GW190915_235702	13.82	8.30	0.86	0.09
GW190924_021846	12.21	5.91	0.90	0.57

# Parametrised tests of GR

- GW waveforms are expressed in terms of effective series, for the Phenom family:

$$h(f; \theta) = A(f; \theta) e^{i\Phi(f; \theta)}$$

$$\Phi(f; \theta) = \sum_{k=0}^7 (\varphi_k + \varphi_k^{(l)}) f^{(k-5)/3} + \sum_{i \neq k} \varphi_i g(f)$$

post-Newtonian series      effective series

$$\varphi_j \equiv \varphi_j(m_1, m_2, \vec{s}_1, \vec{s}_2)$$

- Modified theories of gravity change the series (e.g. PPE: Yunes & Pretorius, arXiv:0909.3328, Cornish+, arXiv:1105.2088)

- Perturb the GW phase around GR (Li+, arXiv:1110.0530  
Agathos+, arXiv:1311.0420)

$$\hat{\varphi}_j \equiv \varphi_j^{GR}(1 + \delta\hat{\varphi}_j) \quad \delta\hat{\varphi}_j = 0 \iff \text{GR}$$

- Bound violations by computing posterior distributions for the  $\delta\hat{\phi}_j$ , in concert with the physical parameters of the system

waveform regime	parameter	$f$ -dependence
early-inspiral regime	$\delta\hat{\varphi}_0$	$f^{-5/3}$
	$\delta\hat{\varphi}_1$	$f^{-4/3}$
	$\delta\hat{\varphi}_2$	$f^{-1}$
	$\delta\hat{\varphi}_3$	$f^{-2/3}$
	$\delta\hat{\varphi}_4$	$f^{-1/3}$
	$\delta\hat{\varphi}_{5l}$	$\log(f)$
	$\delta\hat{\varphi}_6$	$f^{1/3}$
	$\delta\hat{\varphi}_{6l}$	$f^{1/3} \log(f)$
intermediate regime	$\delta\hat{\beta}_2$	$\log f$
	$\delta\hat{\beta}_3$	$f^{-3}$
merger–ringdown regime	$\delta\hat{\alpha}_2$	$f^{-1}$
	$\delta\hat{\alpha}_3$	$f^{3/4}$
	$\delta\hat{\alpha}_4$	$\tan^{-1}(af + b)$

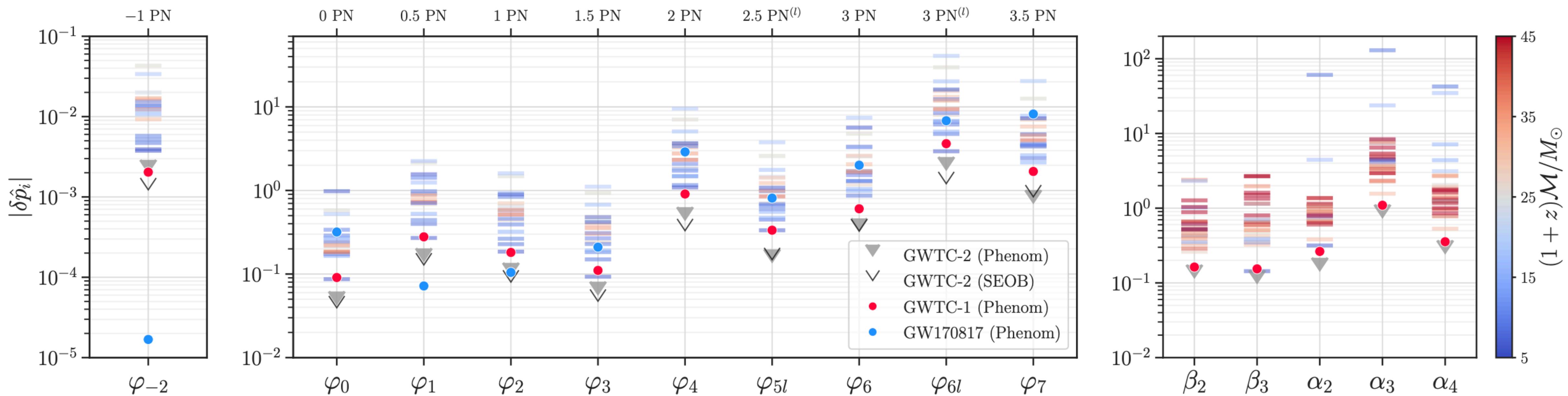
## post-Newtonian

effective

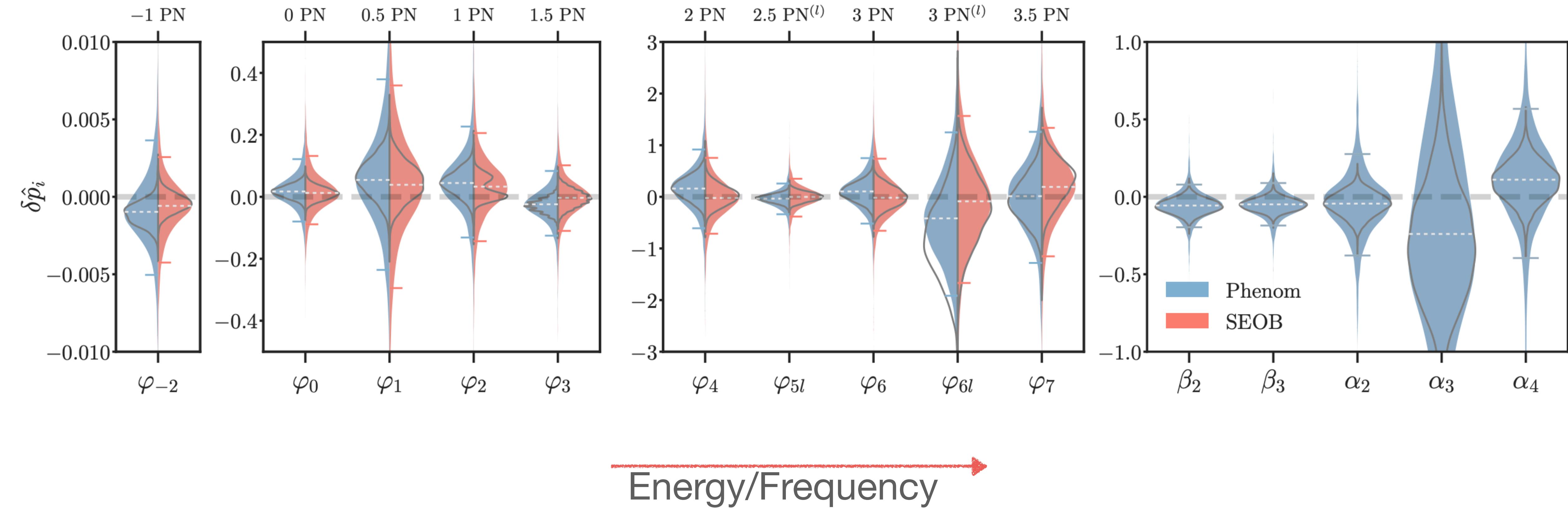
IVC arXiv:1602.03841

# post-Newtonian series

- Dynamical constraints on post-Newtonian series
- Constraints on non-linear dynamics of space-time

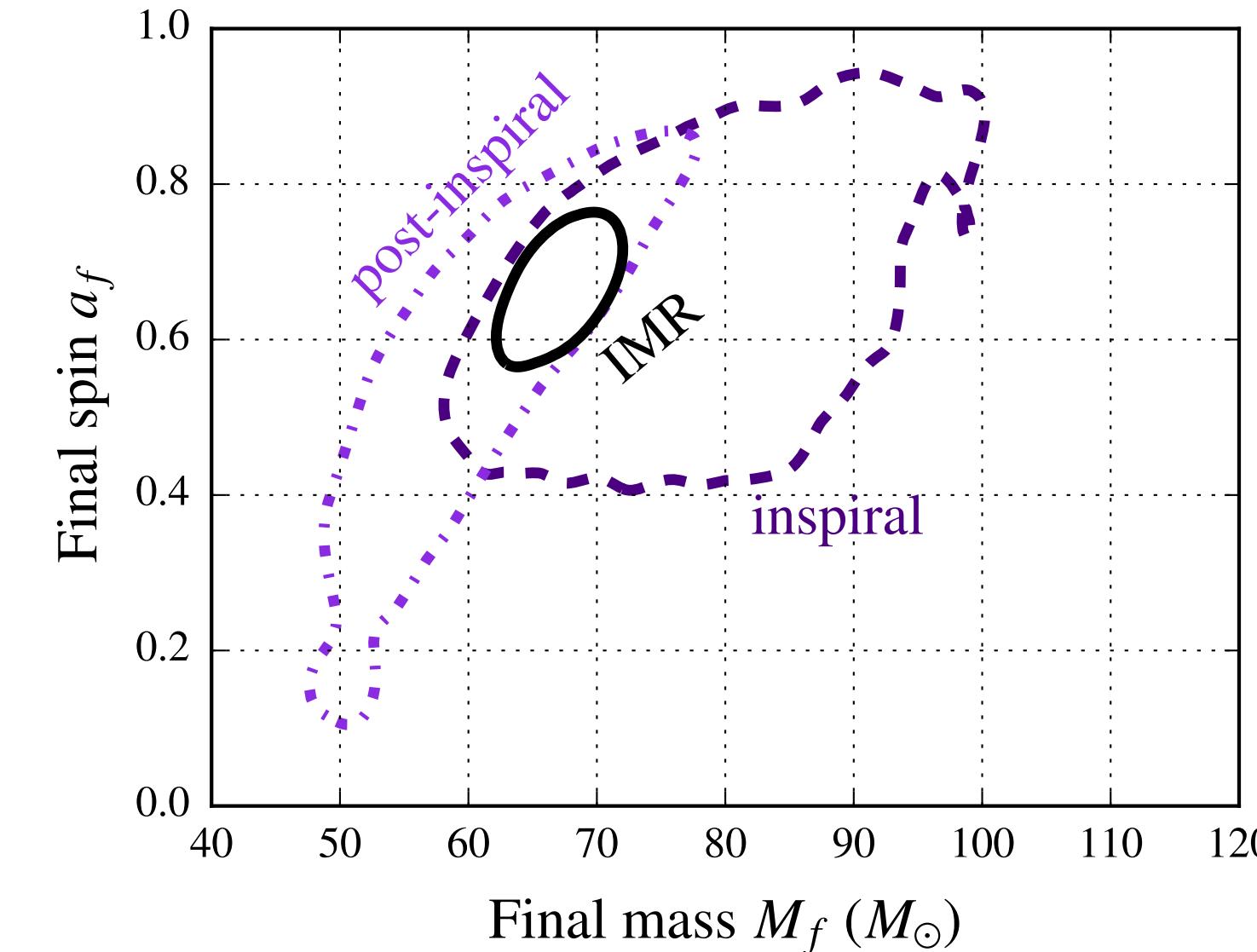
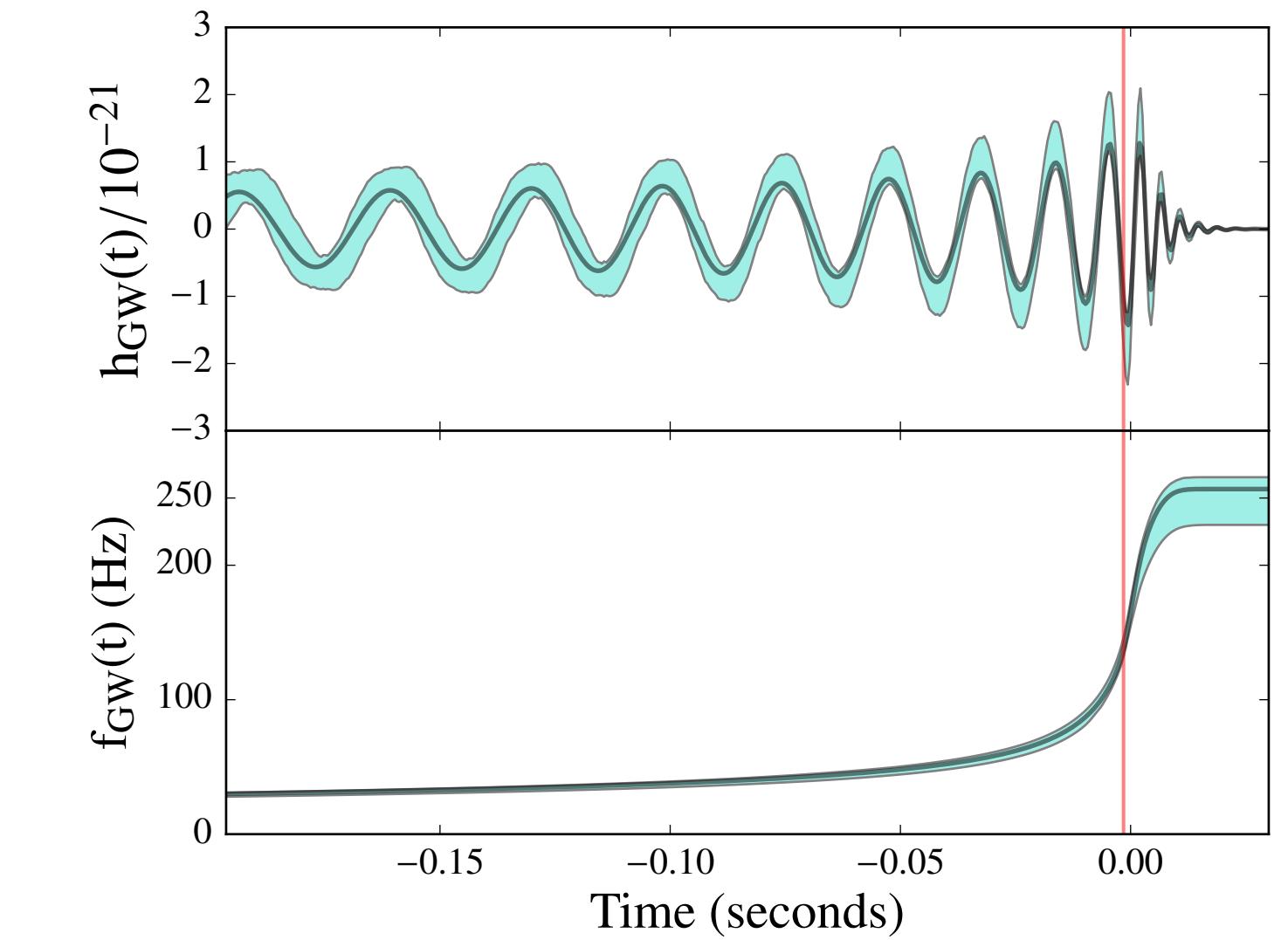


# Parametrised tests of GR



# Reconstructed waveform consistency

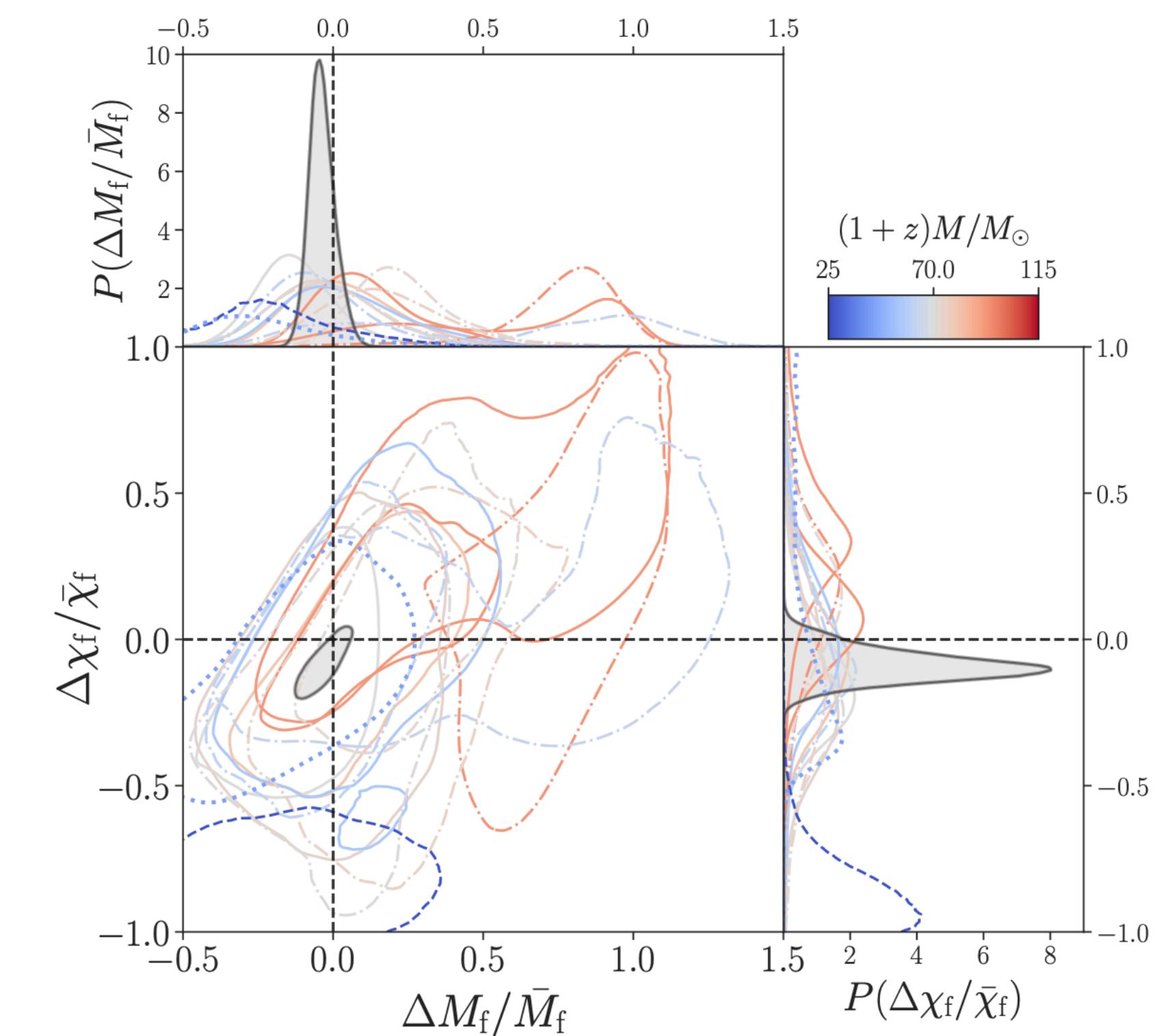
- The comparison of the final mass and spin predicted from the “inspiral” with the ones measured directly from the “merger-ringdown” is a consistency test on the waveform (Ghosh et al, 2016) and thus, on the corresponding GR solution



# IMR consistency test

- “Inspiral” analysis: infer component properties and from numerical solution provide predictions for spin and mass of remnant (e.g. Healy+, 1406.7295)
- “Post-inspiral’ analysis: infer remnant properties
- Verify self-consistency by comparing final mass and spin predicted from the “inspiral” with the ones inferred from the “post-inspiral” (Ghosh+, 1602.02453)

$$\left\{ \begin{array}{l} \Delta M_f / M_f = 0 \\ \Delta a_f / a_f = 0 \end{array} \right. \iff GR$$



# Spin-induced quadrupole moment

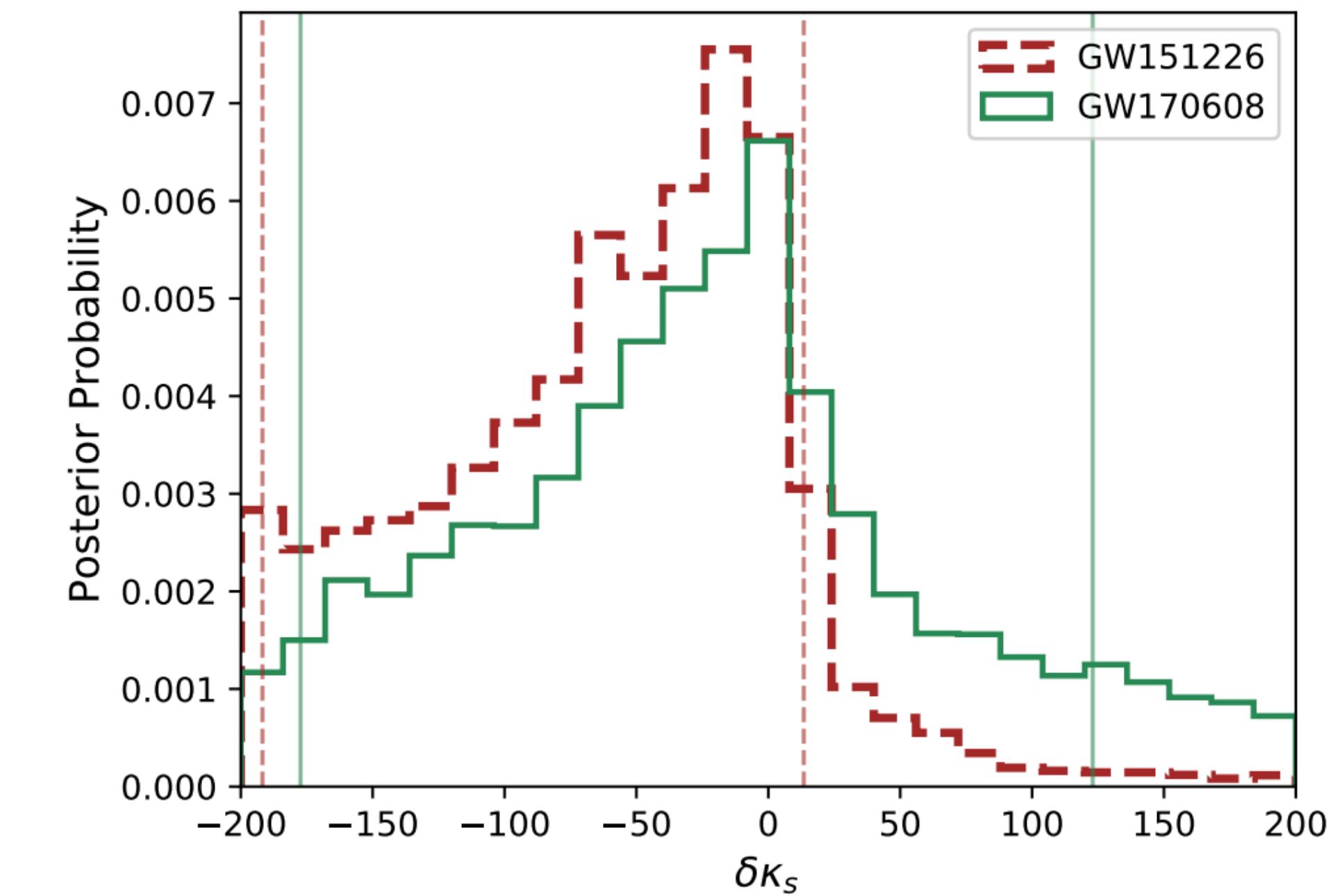
- measure of the degree of an object's oblateness due to its spin (Poisson, arXiv:97090320).

$$Q \simeq -\kappa a^2 m^3$$

- If the object is in an inspiraling binary, this effect will become imprinted in the GW waveform at various PN orders
- GR BHs have  $\kappa = 1$
- Boson stars  $\kappa = 10 - 150$  (Ryan, PRD 1997)
- Constraints on  $\kappa$  can reveal the nature of binary components (Krishnendu+, arXiv:1701.06318)

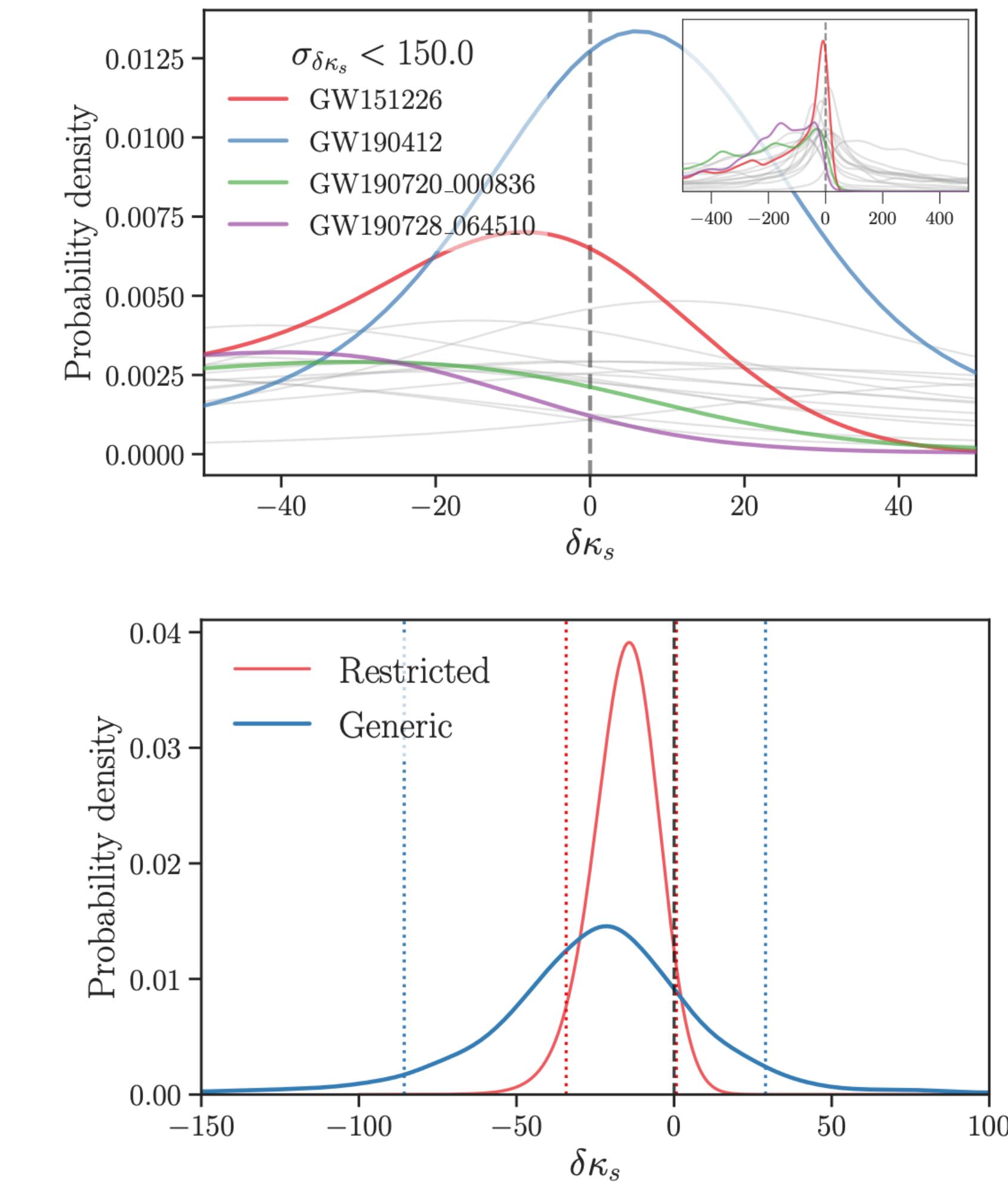
$$Q = -(1 + \delta\kappa) a^2 m^3$$

$$\delta\kappa_s = \frac{\delta\kappa_1 + \delta\kappa_2}{2}$$



Krishnendu+, arXiv:1908.02247

- Poor constraints due to low spins
- Posterior mass concentrated around  $\delta\kappa_s = 0$
- Hierarchical analysis
  - Restricted: all objects have the same  $\delta\kappa_s$
  - Generic: each object has its own  $\delta\kappa_s$
- $\delta\kappa_s = -15^{+15}_{-19}$
- $\log_{10} B_{Kerr,\overline{Kerr}} = 11.7$



# Propagation tests: massive gravity

- Families of alternative theories modify the propagation of GW
- Massive gravity (e.g. Will, arXiv:9709011)

$$E^2 = p^2 v_g^2 + m_g^2 c^4$$

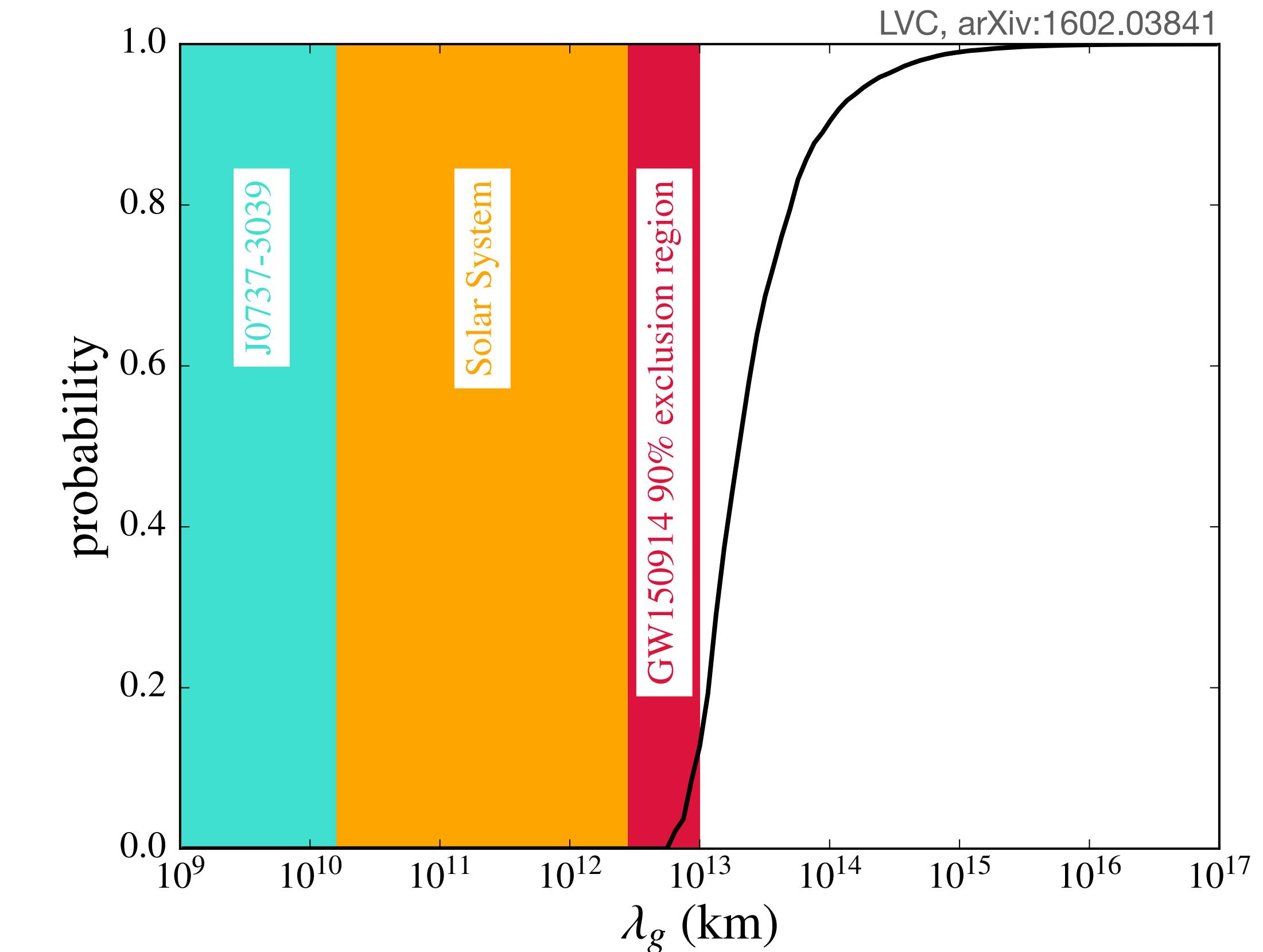
- GW phase affected

$$v_g^2/c^2 \simeq 1 - \frac{h^2 c^2}{\lambda_g^2 E^2}$$

$$\lambda_g = \frac{h}{m_g c}$$

- GW constrains gravitons Compton wavelength

$$\Delta\Phi = -\frac{\pi^2 D M}{\lambda_g^2 (1+z)}$$



$$m_g \leq 1.76 \times 10^{-23} \text{ eV}/c^2,$$

LVC, [https://dcc.ligo.org/public/0166/P2000091/010/o3a\\_tgr.pdf](https://dcc.ligo.org/public/0166/P2000091/010/o3a_tgr.pdf)

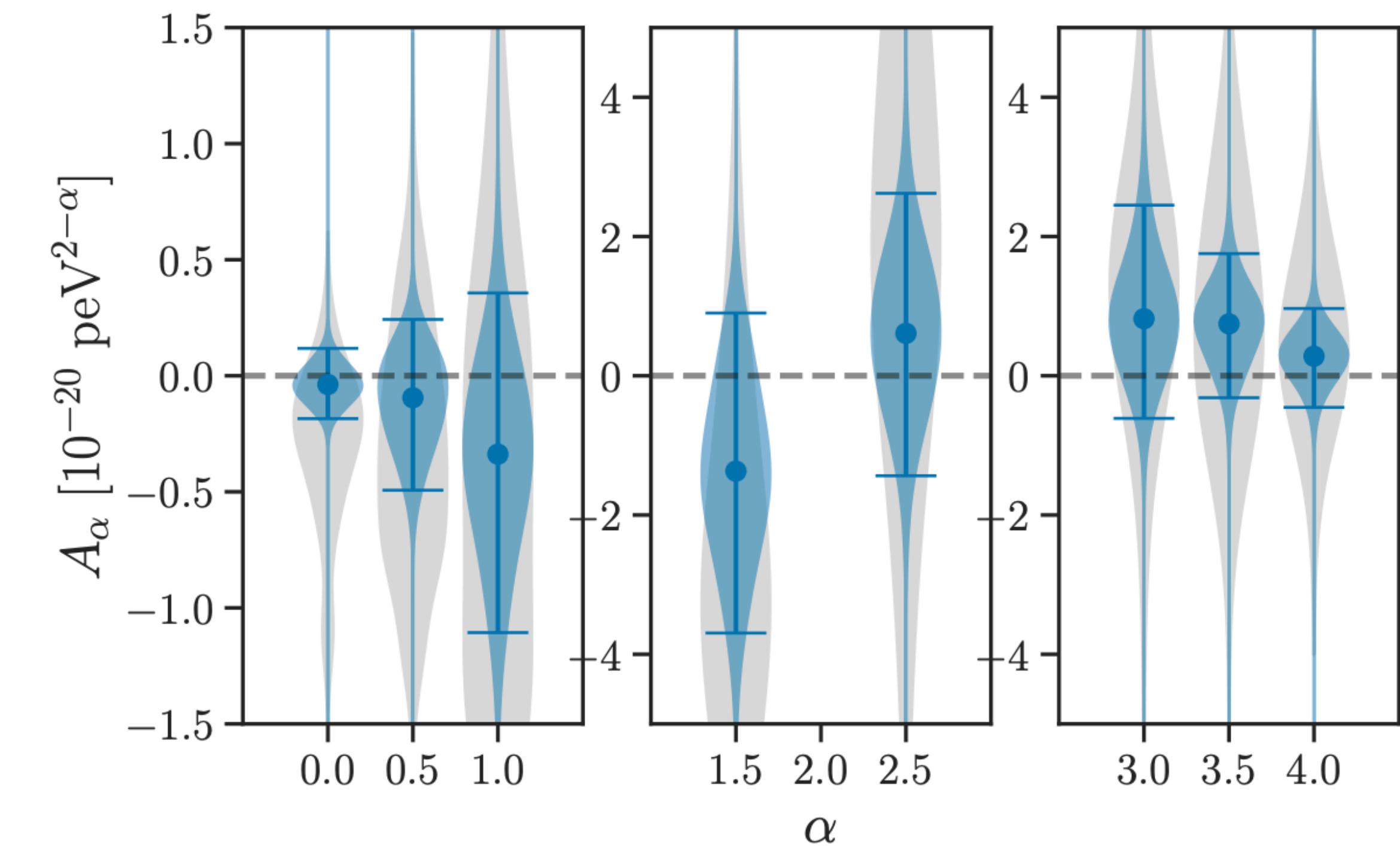
# Tests of Lorentz Invariance Violations

- Further generalised (e.g. Mirshekari et al, arXiv:1110.2720)

$$E^2 = p^2 c^2 + A p^\alpha c^\alpha \quad \alpha \geq 0$$

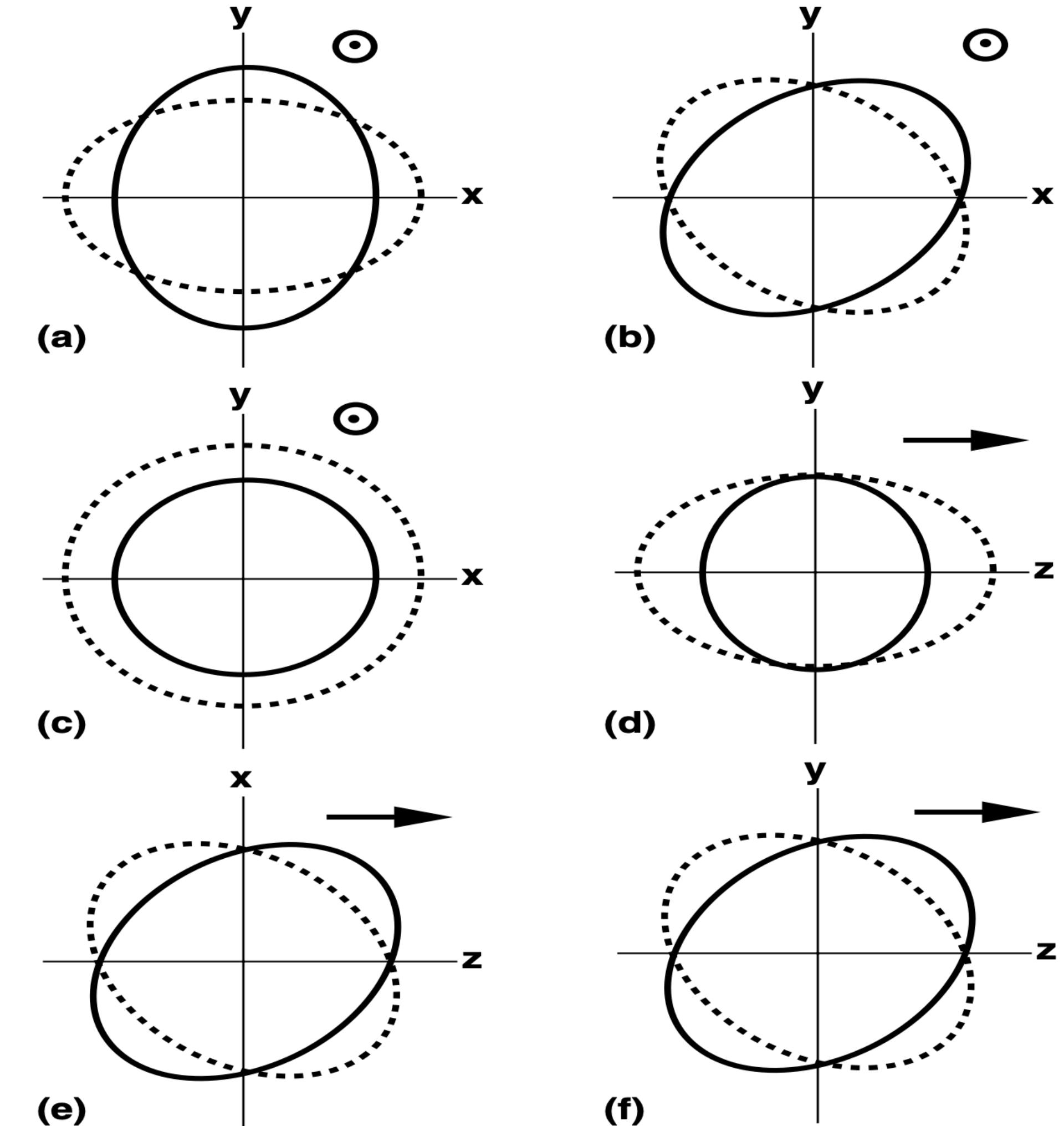
$$v_g/c = 1 + (\alpha - 1) A E^{\alpha-2} / 2$$

- No evidence for an anomalous GW dispersion



# Gravitational wave polarisation states

- Gravitational waves in general relativity are transverse, tensorial waves
- Extensions to general relativity predict up to six polarisation states
  - Two transverse tensor states
  - Two longitudinal vector states
  - Two scalar states, one longitudinal and one “breathing”



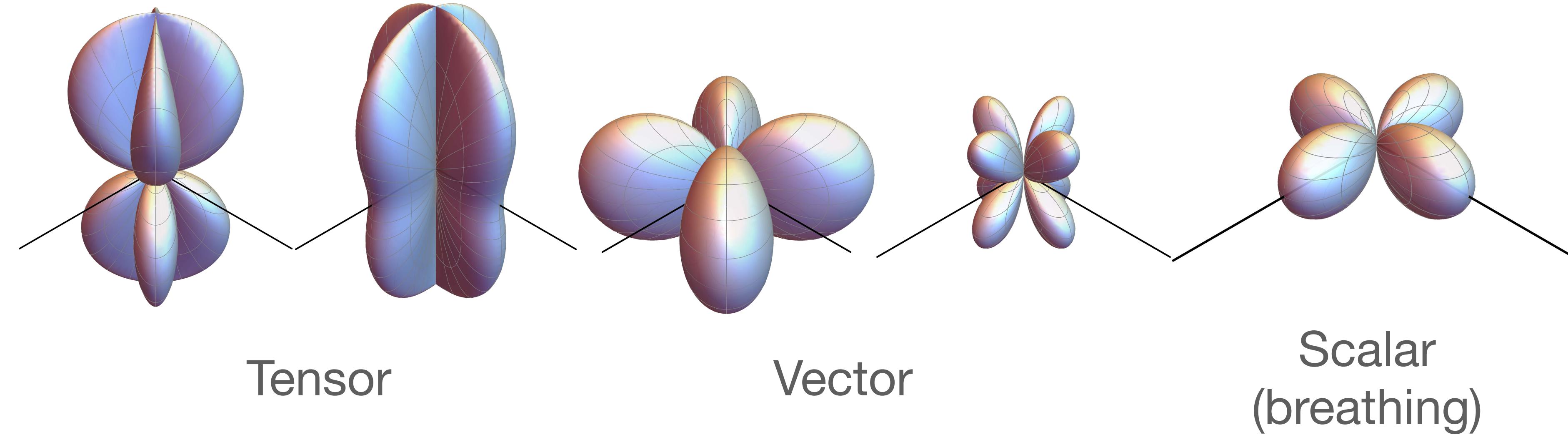
Capozziello &amp; De Laurentis, 2012

# Detector response to polarisation states

- Each polarisation state couples to the detector differently

Antenna response functions  $F_k$

$$h = \sum_{k=1}^6 F_k h_k$$

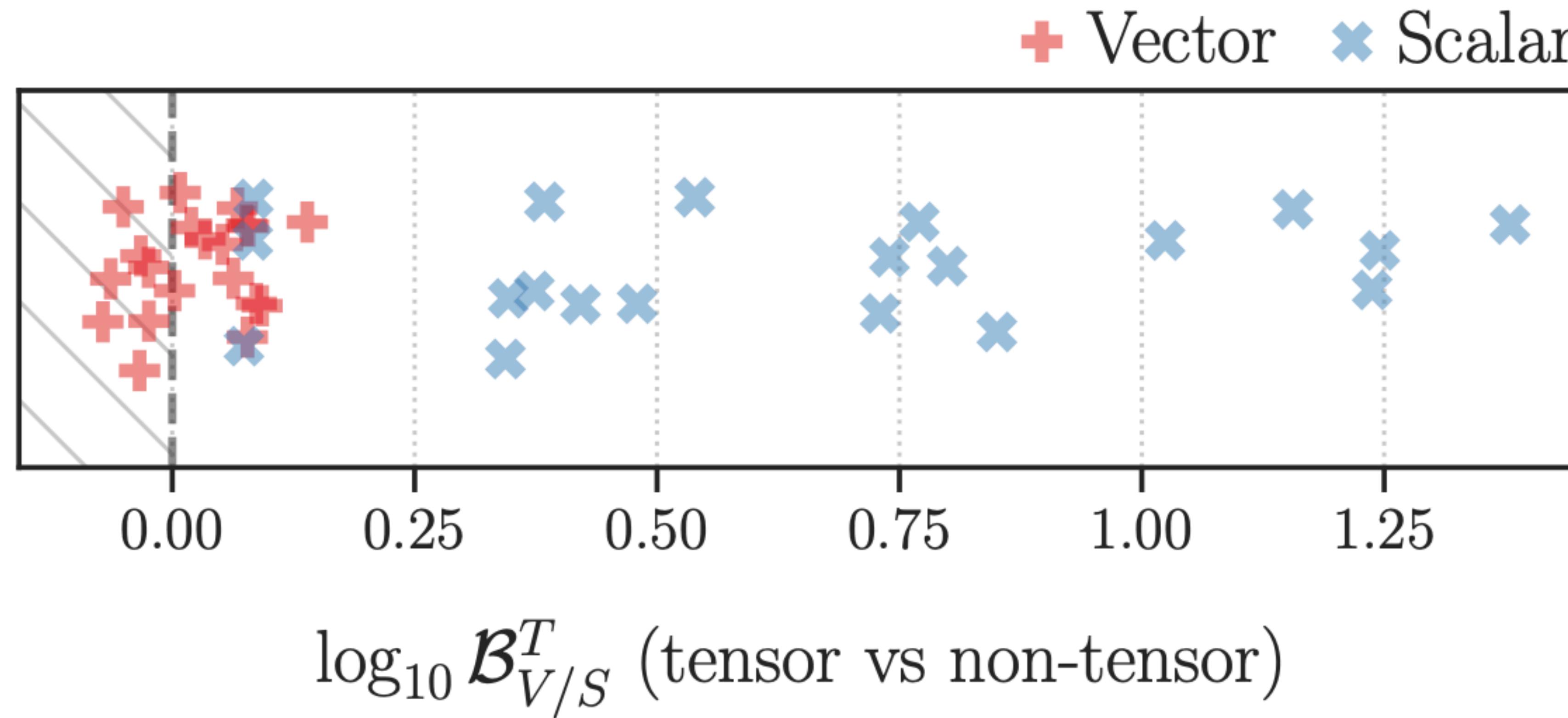


- In principle detectable with more than one detector

Courtesy of Max Isi

# Two detectors sensitivity to polarisation states

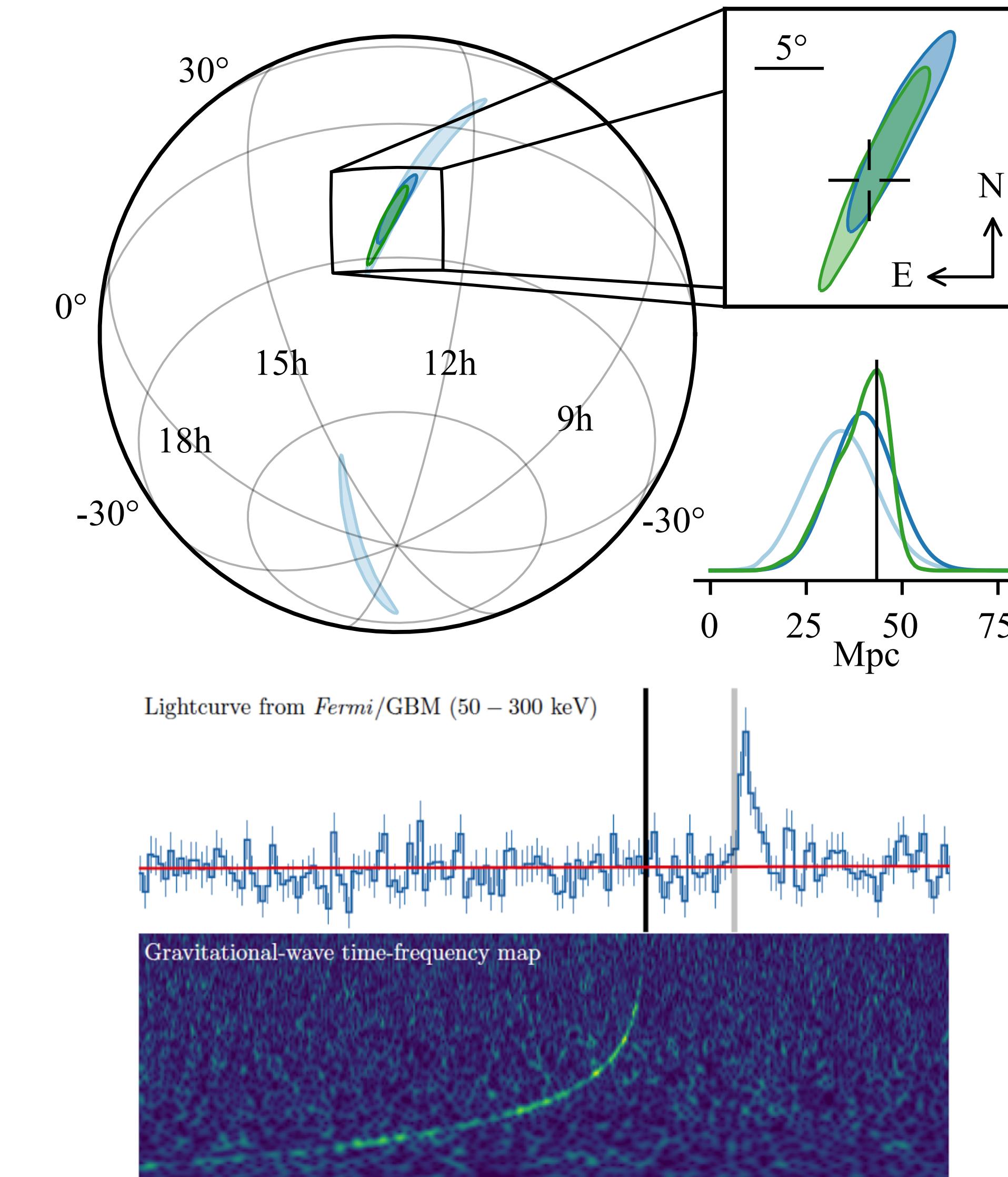
- Because of their geometry, the two LIGO detectors cannot discriminate among different polarisation states
- With Virgo detector and/or an electromagnetic counterpart we can



$\log_{10} \mathcal{B}_{V/S}^T$  (tensor vs non-tensor)

LVC, [https://dcc.ligo.org/public/0166/P2000091/010/o3a\\_tgr.pdf](https://dcc.ligo.org/public/0166/P2000091/010/o3a_tgr.pdf)

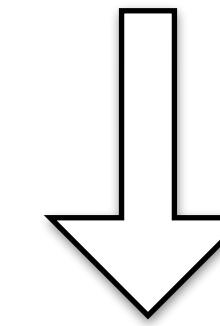
- Electromagnetic counterpart!



# GW170817 and the speed of gravity

- From  $\Delta t(GW, EM)$  we can measure the speed of GW

$$-3 \times 10^{-15} \leq \frac{\Delta v}{v_{EM}} * \leq 7 \times 10^{-16}$$

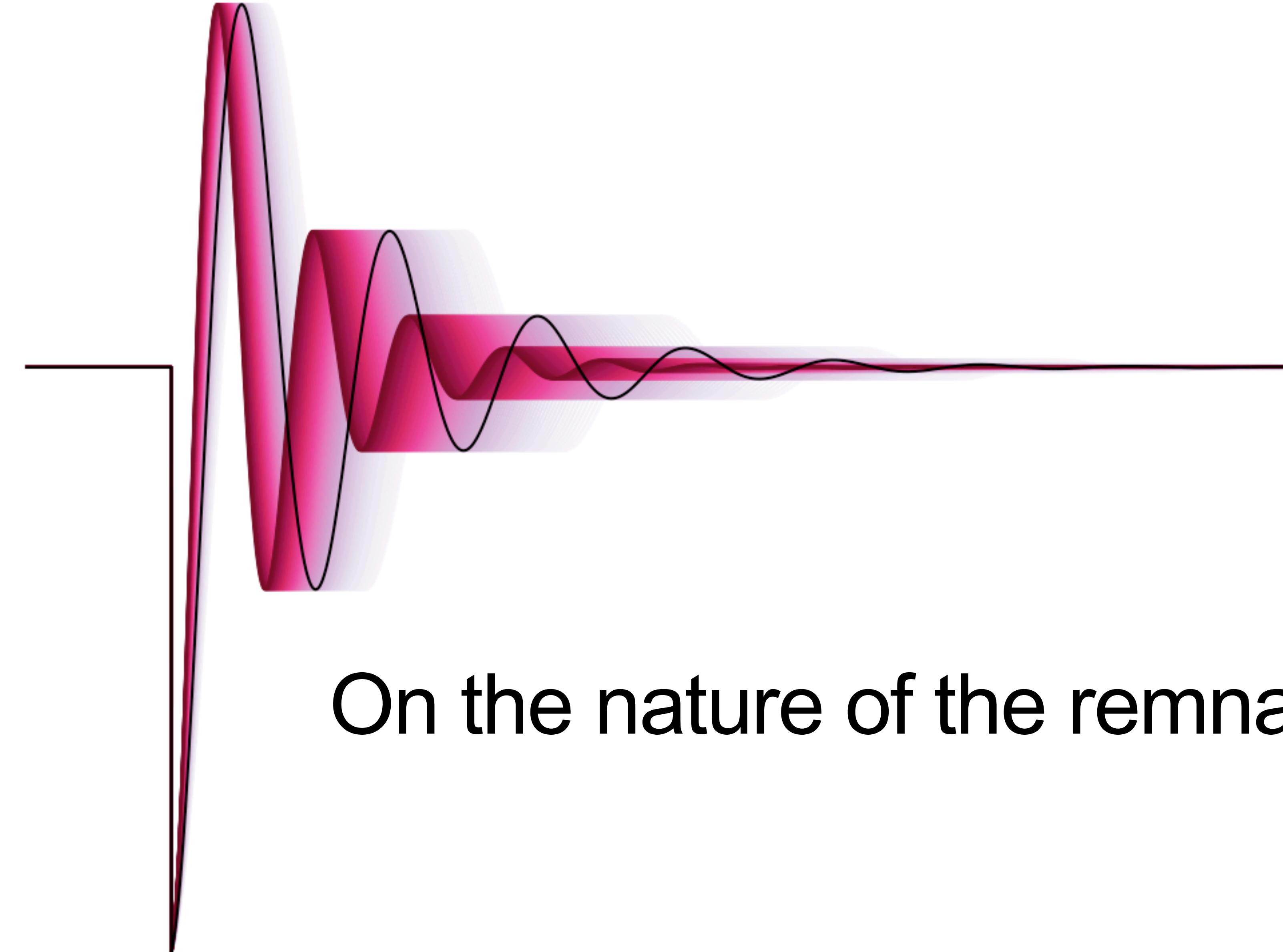


$$\begin{aligned} S = & \int d^4x \sqrt{-g} \left\{ K(\phi, X) - G_3(\phi, X) \square \phi \right. \\ & + \cancel{G_4(\phi, X) R + G_{4,X}(\phi, X) [(\square \phi)^2 - (\nabla_\mu \nabla_\nu \phi)(\nabla^\mu \nabla^\nu \phi)]} \\ & + \cancel{G_5(\phi, X) G_{\mu\nu} \nabla^\mu \nabla^\nu \phi - \frac{G_{5,X}(\phi, X)}{6} [(\square \phi)^3 - 3 \square \phi (\nabla_\mu \nabla_\nu \phi)(\nabla^\mu \nabla^\nu \phi)]} \\ & \left. + 2(\nabla_\mu \nabla_\nu \phi)(\nabla^\mu \nabla_\sigma \phi)(\nabla^\nu \nabla^\sigma \phi) \right\} \end{aligned}$$

Many models that could potentially explain the accelerated expansion yet evade solar system constraints via screening have been ruled out

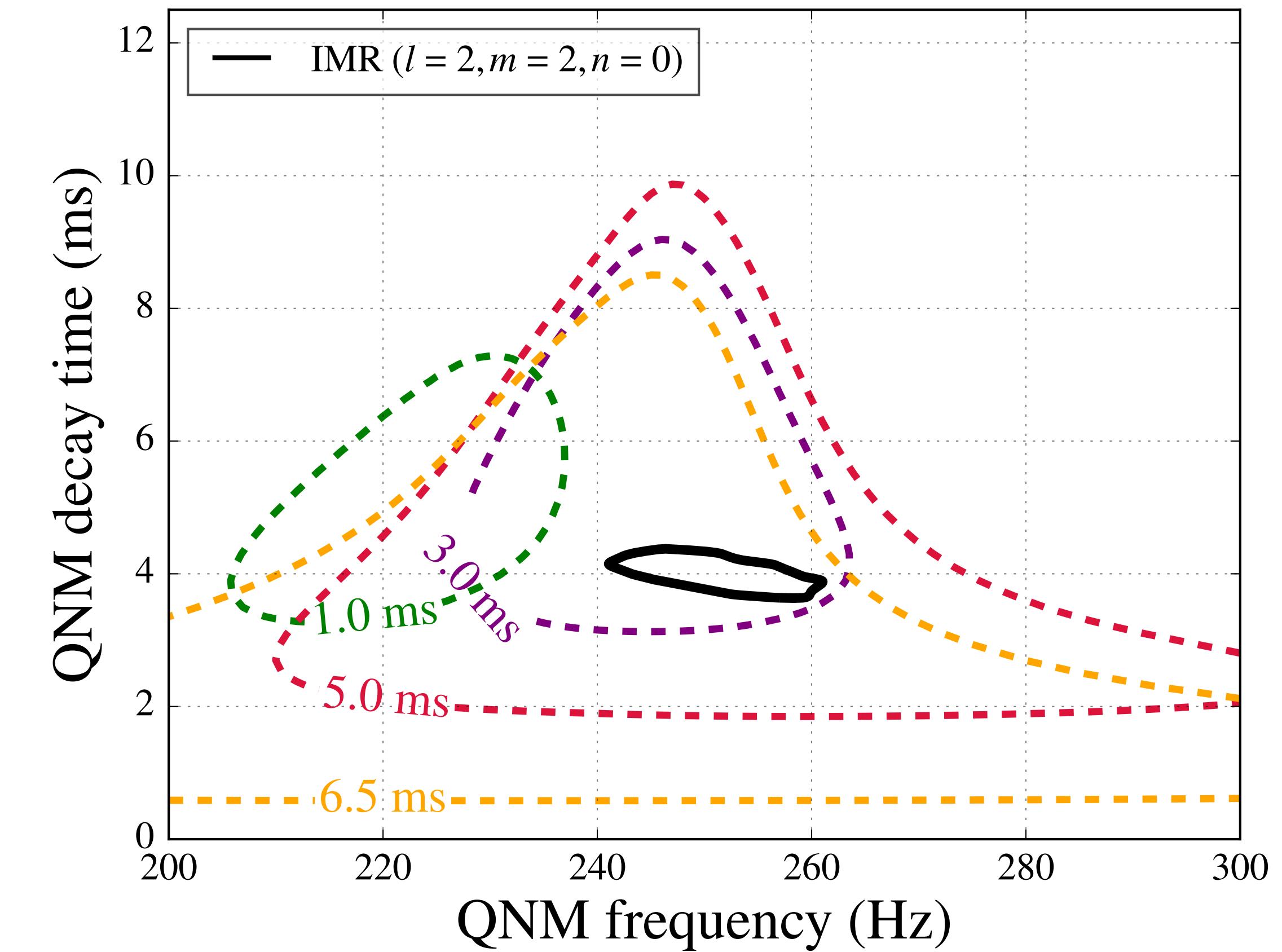
\* note that if gravity did not propagate at c, timing of binary pulsars would be impossible (Damour & Deruelle 86)

Creminelli, Vernizzi, arXiv:1710.05877  
 Sakstein, Jain, arXiv:1710.05893  
 Baker et al, arXiv:1710.06394



# On the nature of the remnants

- Search using exponentially damped sinusoids
- Evidence for a definite frequency and characteristic damping time
- Is this the remnant black hole ringing?
  - Consistency with IMR results suggests SO



- Remnant compact object nature;  
Are we really observing black holes?
- General Relativity predictions for spectral emission;  
Is General Relativity a correct description of gravity at high curvatures?
- Black Hole Uniqueness Theorems;  
Do non-extremal black holes have additional hairs?
- Possible quantum horizon effects and classical BH thermodynamics.  
Is our classical description of black holes valid?

# Black hole perturbation theory

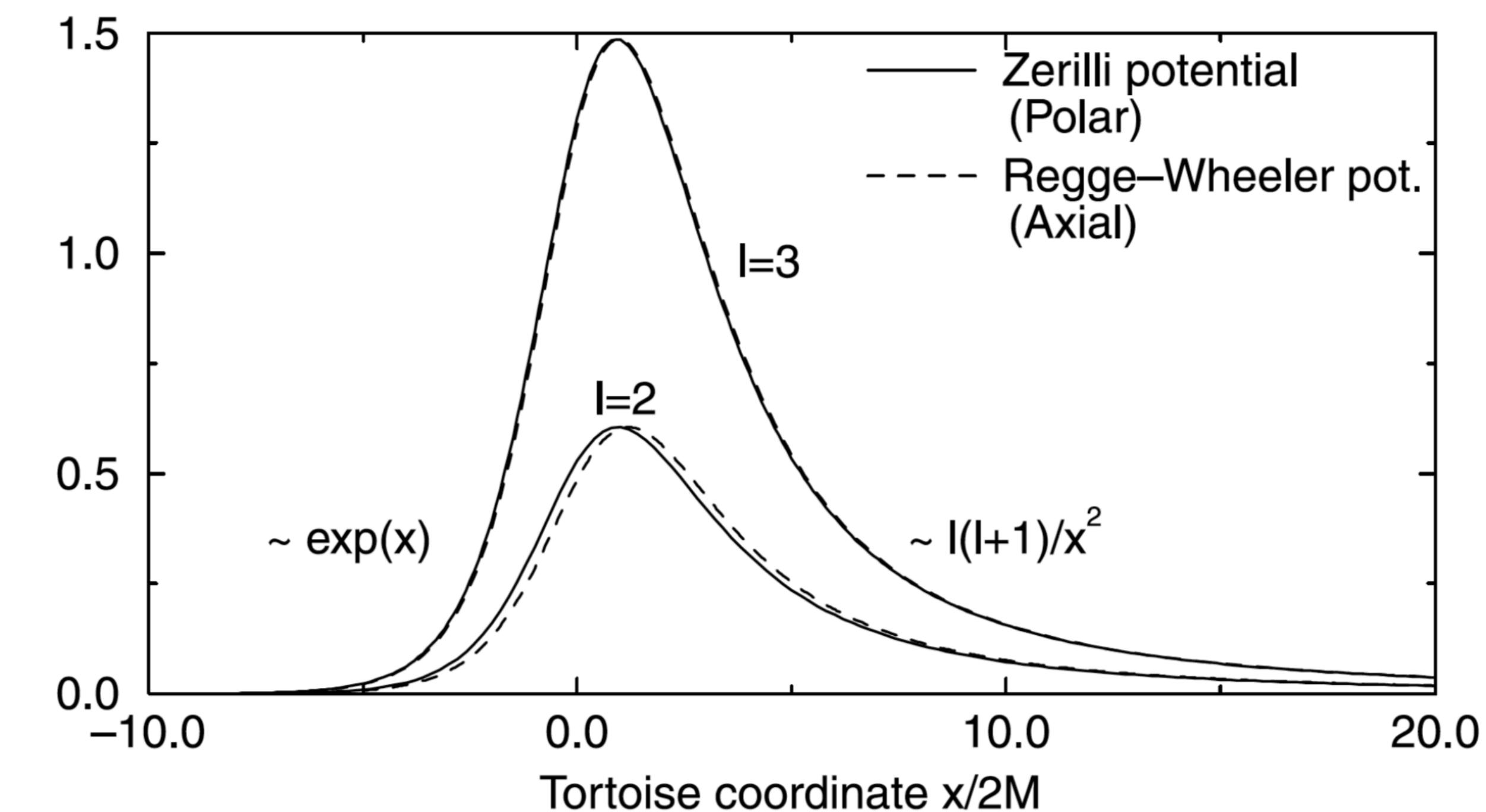
- Linear perturbations of the Schwarzschild background

$$g_{\mu\nu} = \bar{g}_{\mu\nu} + h_{\mu\nu}$$

- Einstein's equations for the perturbation
- Regge-Wheeler-Zerilli equation

$$\left( \frac{\partial^2}{\partial t^2} - \frac{\partial^2}{\partial x^2} + V_{lm}(x) \right) \psi_{lm}(x, t) = 0$$

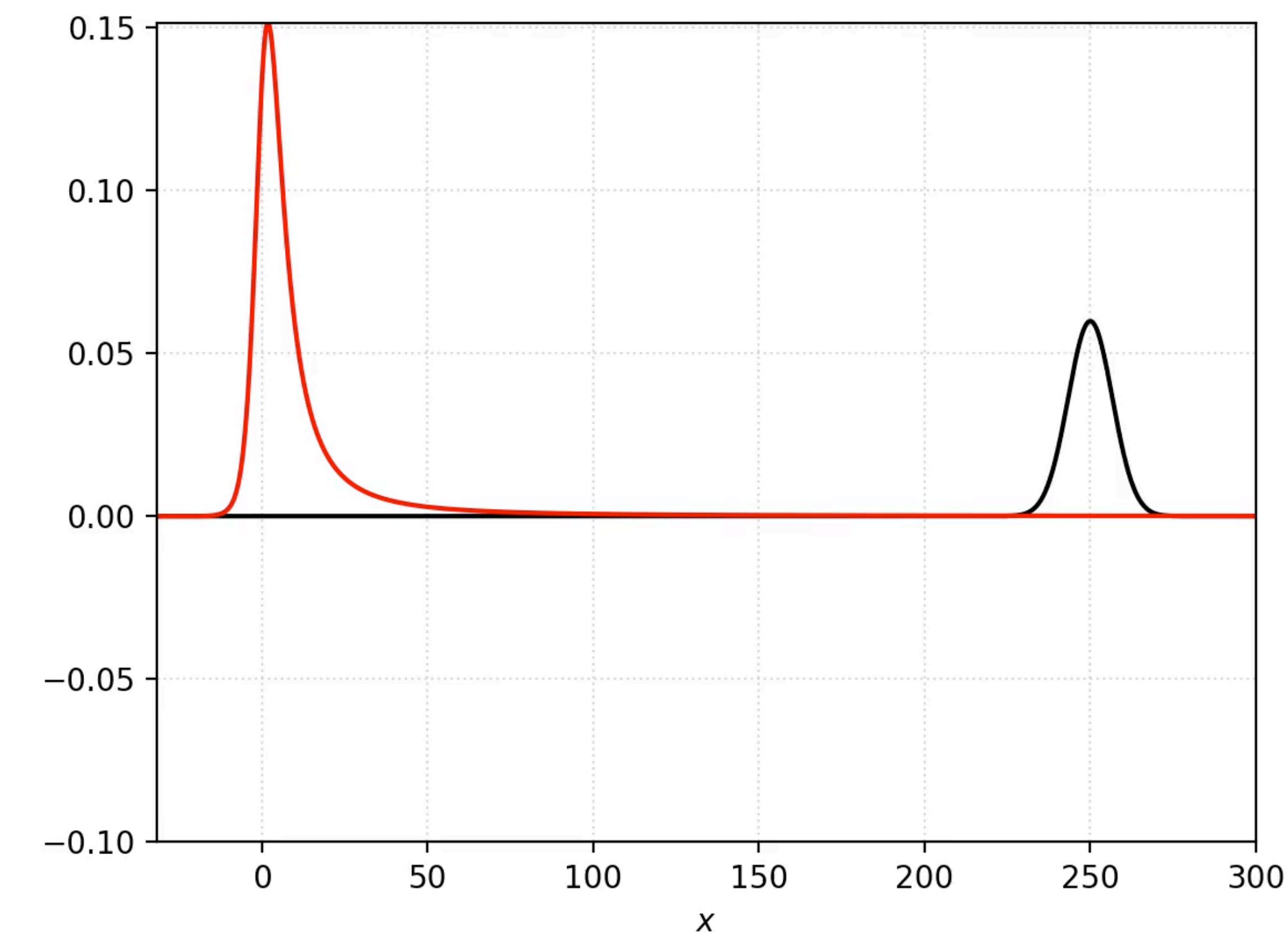
- Perturbations of Kerr black holes
  - Teukolski equation



Nollert 1999

# Black hole ringdown

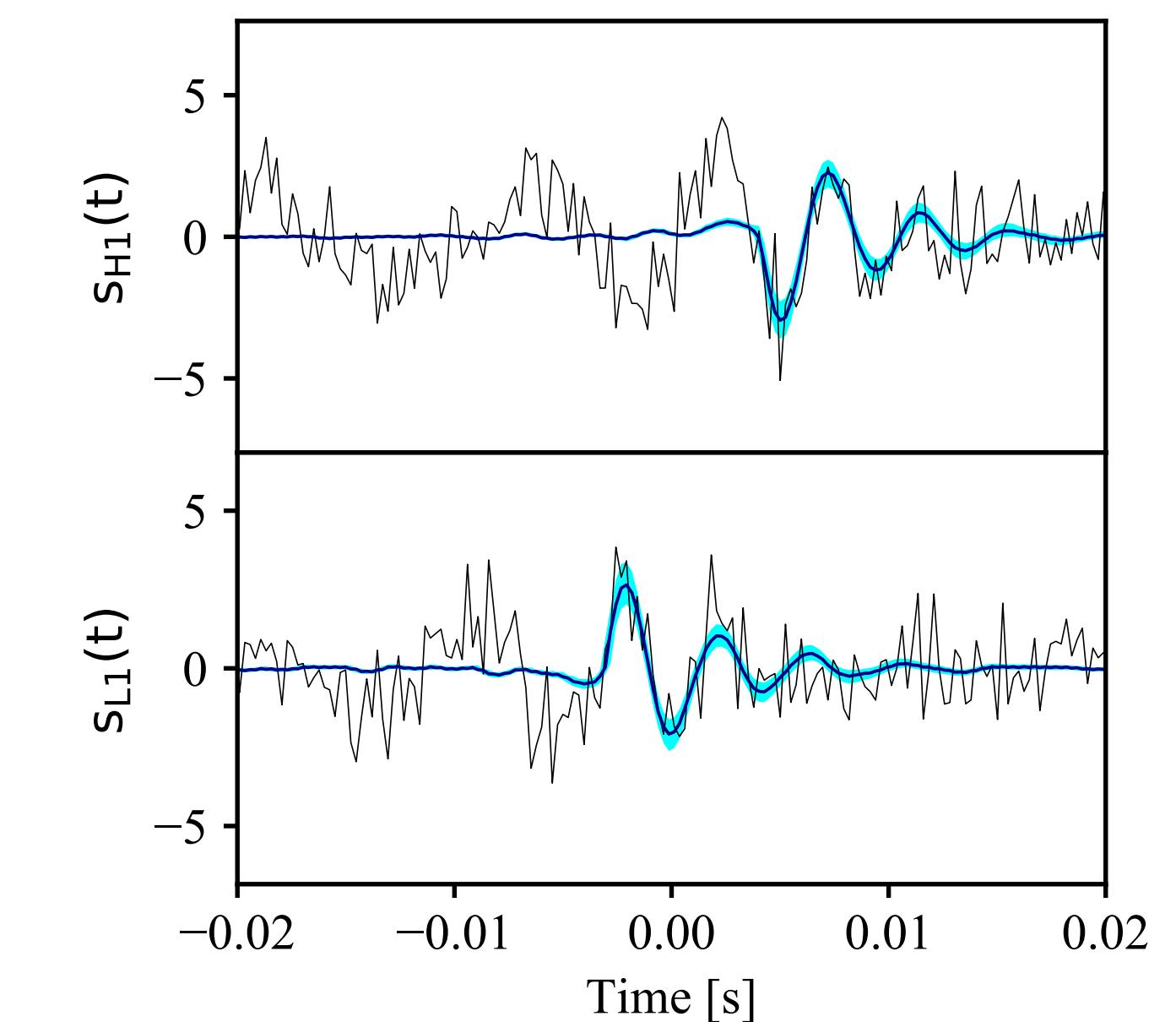
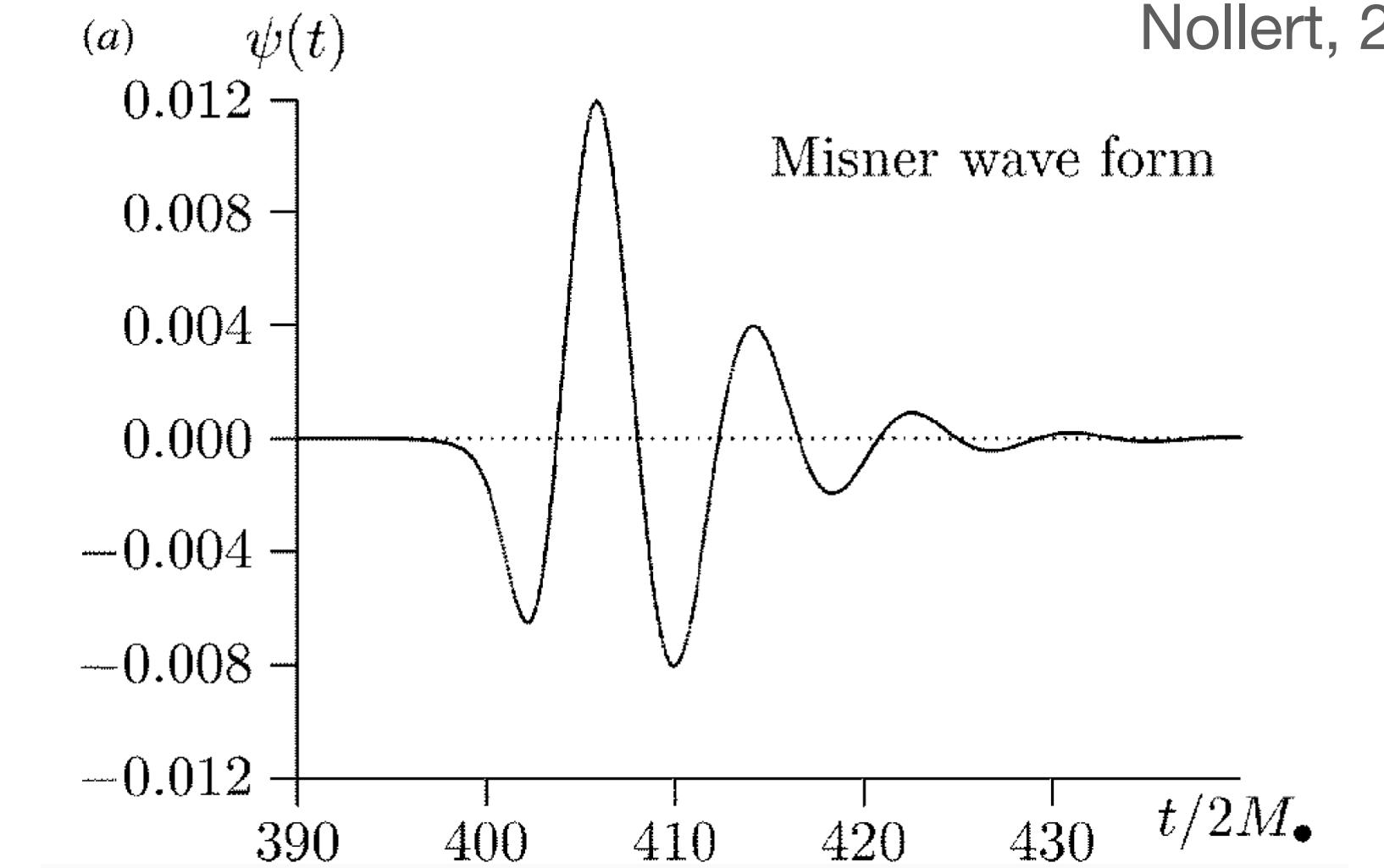
- BH responds to perturbations by “ringing” (Vishveshwara 1970, Press 1971, Ruffini+1972, Chandrasekhar 1975)
- Quasi-normal modes excited by light-ring crossing (Goebel 1972)
- Waveform is a superposition of exponentially damped sinusoids



# Ringdown waveform

$$h(t) = \sum_{nlm} A_{nlm} e^{-\frac{t-t_0}{\tau_{nlm}}} \cos(\omega_{nlm}(t - t_0) + \varphi_{nlm})$$

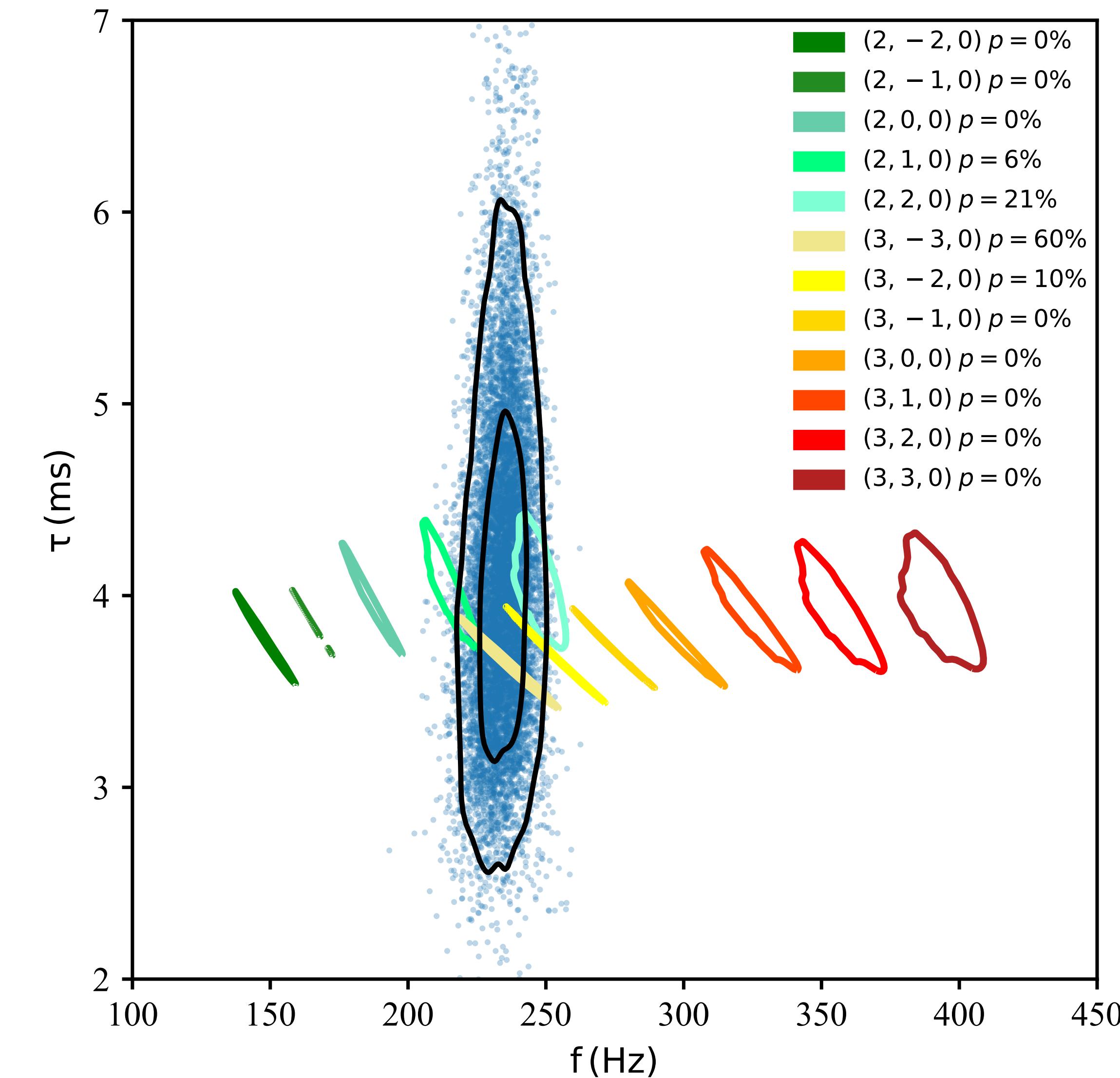
- Frequencies and damping times spectrum predicted by perturbation theory, fixed only by mass and spin (and charge) of the black hole
- Manifestation of the BH uniqueness hypothesis, Berti et al, arXiv:0512160
- Amplitudes and relative phases either predicted by numerical relativity or estimated from the data
- Independent measurement of the final black hole parameters, enabling a test of GR predictions



Carullo, Del Pozzo, Veitch 2019

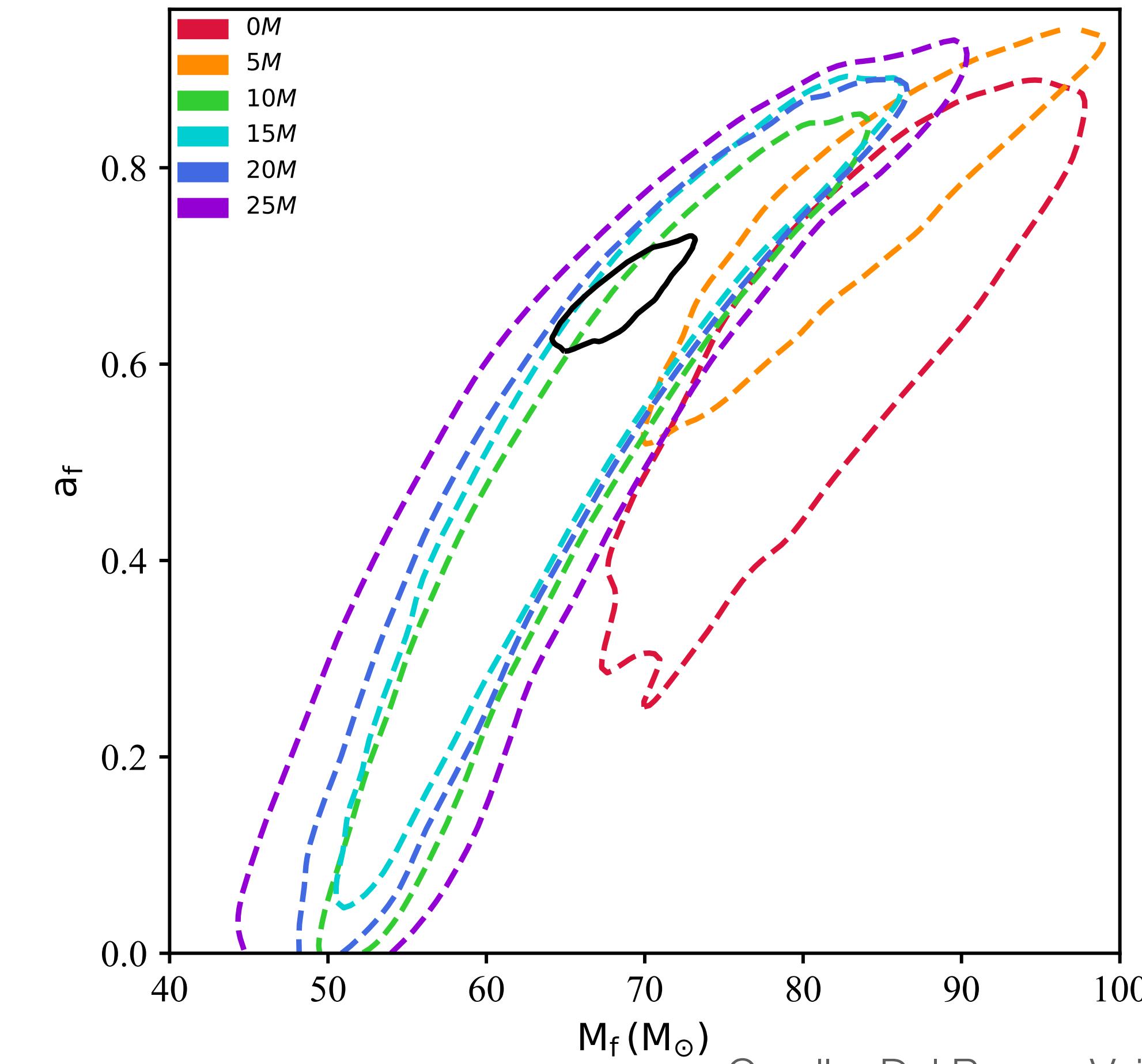
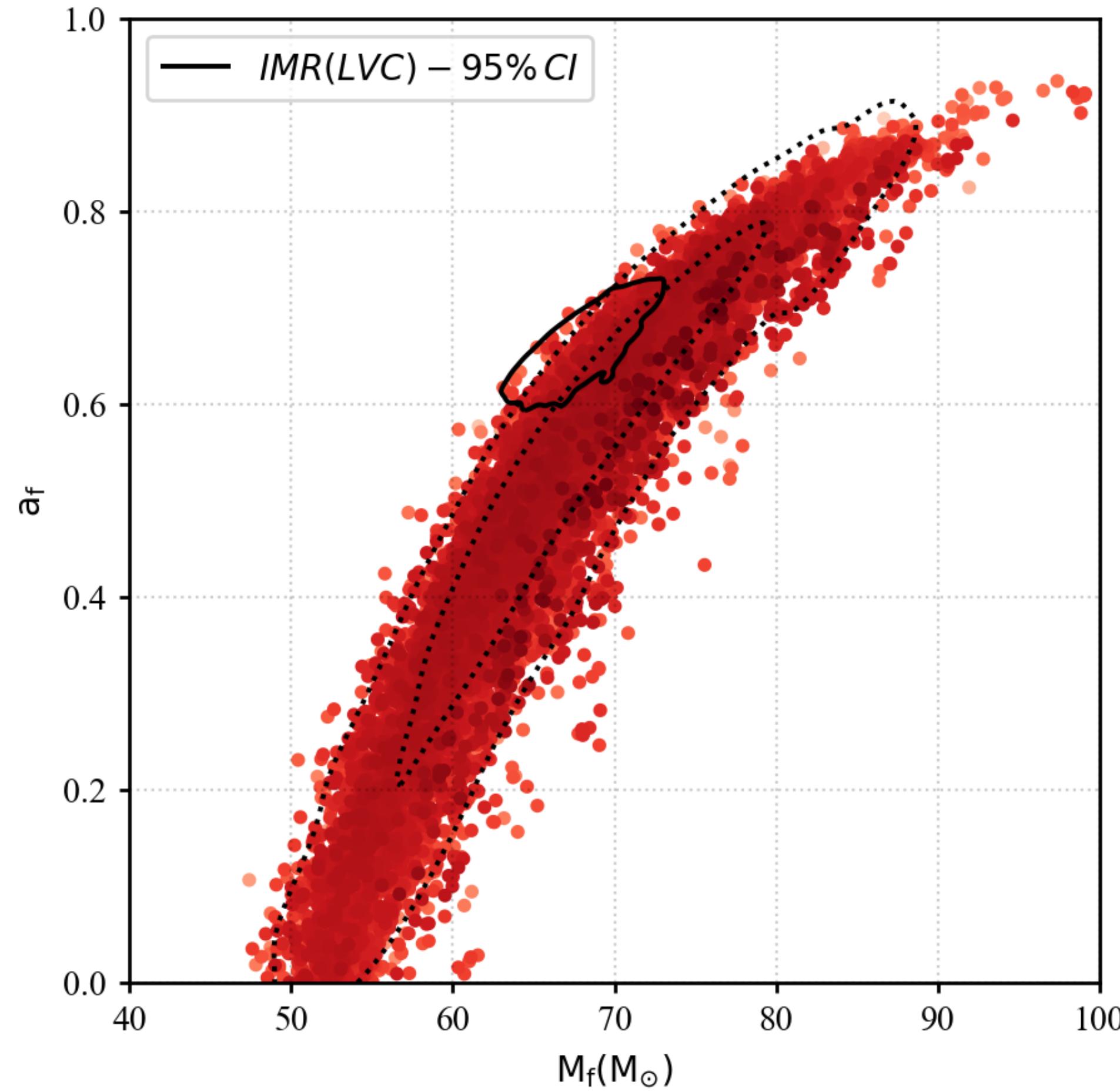
# Black hole spectroscopy

- Introduced in Dreyer+, 2004 and Berti+, 2006
- Identify central frequency and damping time directly from the data
  - Agnostic search
- Predict central frequency and damping time from NR (e.g Jimenez-Forteza+2017)
- Use Bayes theorem to compute the probability that recovered agnostic posterior corresponds to given predicted mode
- Choice of a start time: when is the system's evolution linear?
  - Time domain analysis



# Remnant parameters

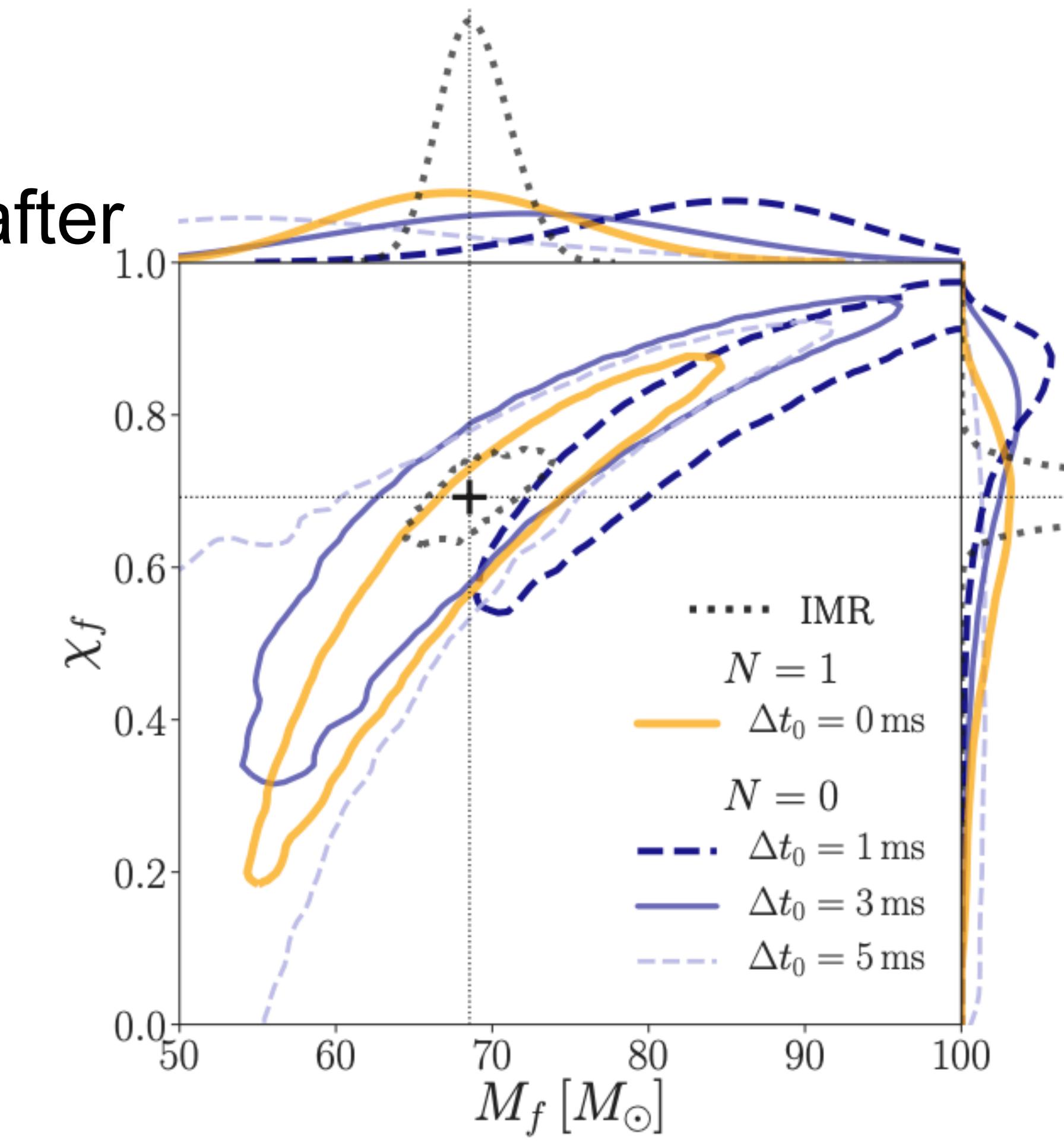
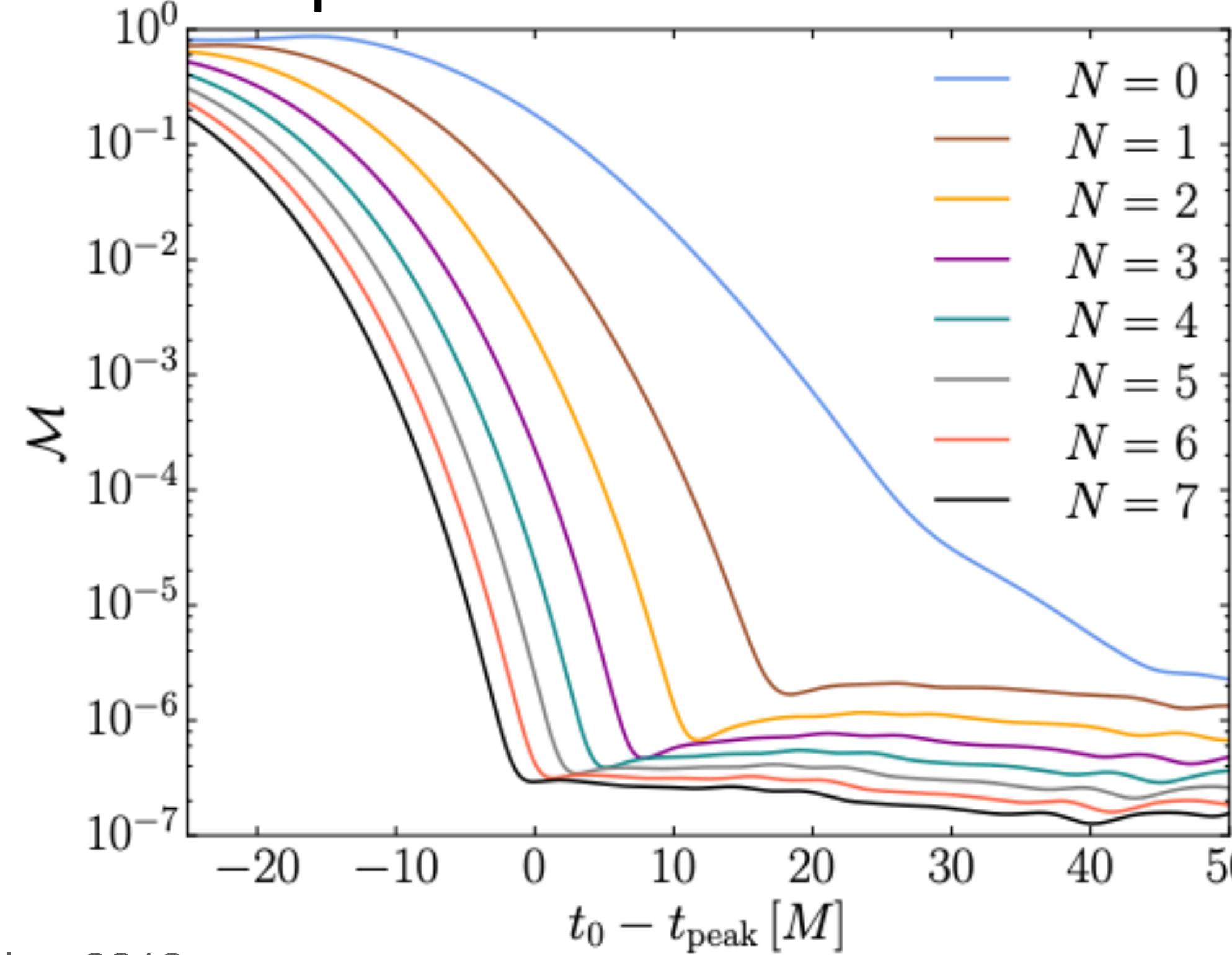
- Assume GR predictions: remnant mass and spin reconstruction



Carullo, Del Pozzo, Veitch 2019

# The role of overtones

- Overtones seem to circumvent the problem of choosing a start time
- Ringdown signals with overtones match NR after the peak of emission



- Multiple ringdown searches
  - Multi-modal agnostic search: mode identification
  - Kerr model search: remnant parameter estimation

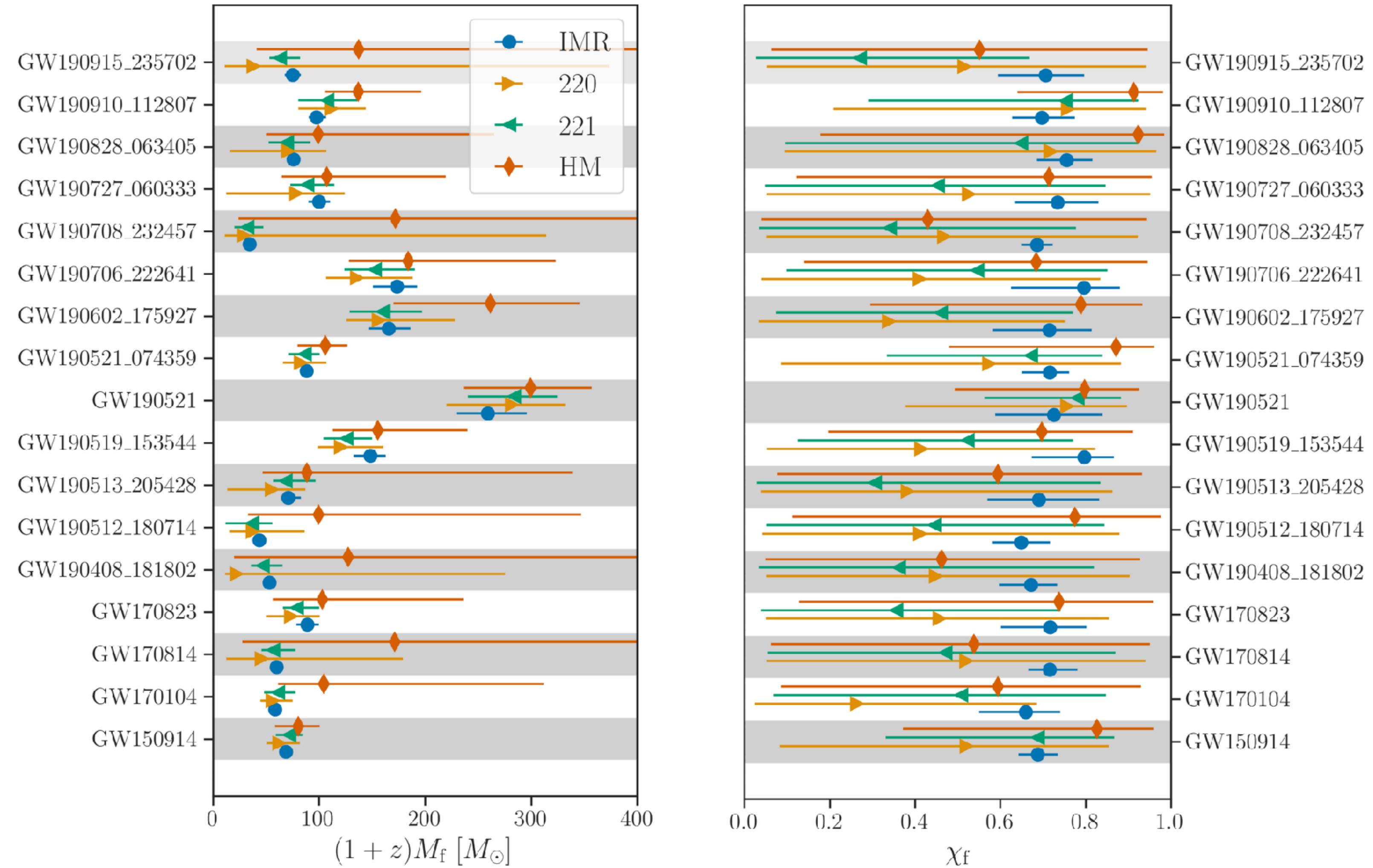
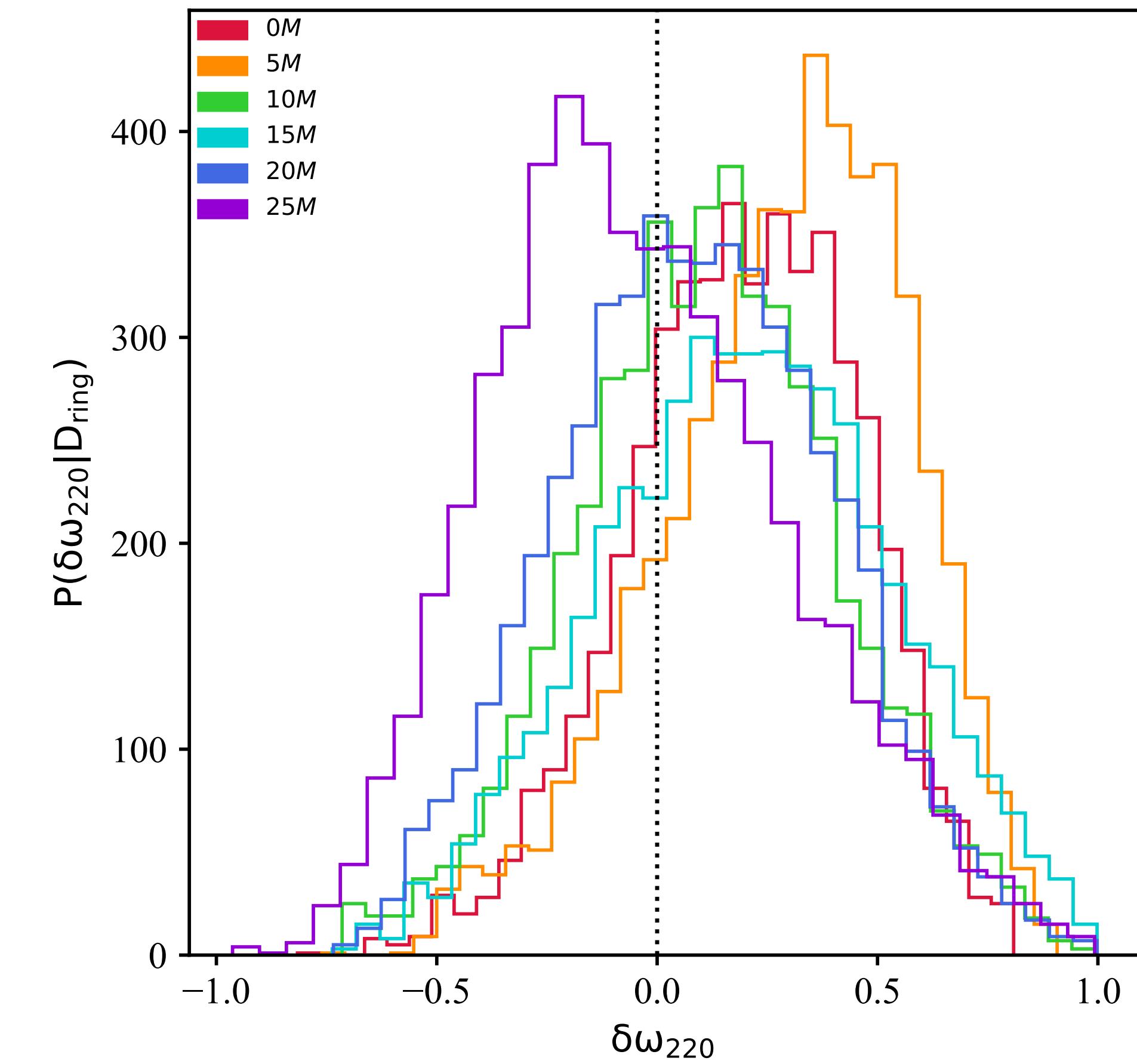


Image credit: LIGO-Virgo/Rico Lo

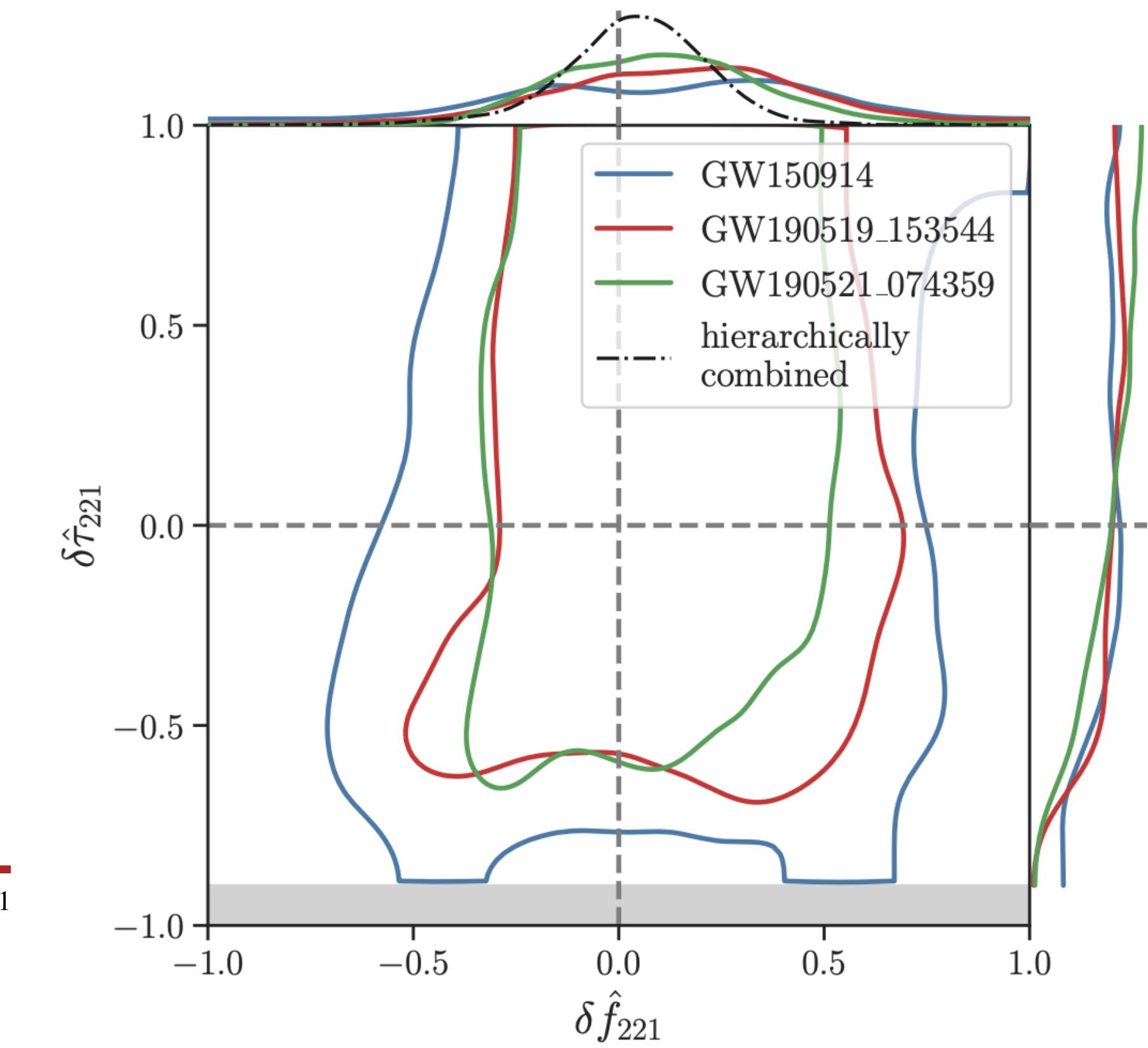
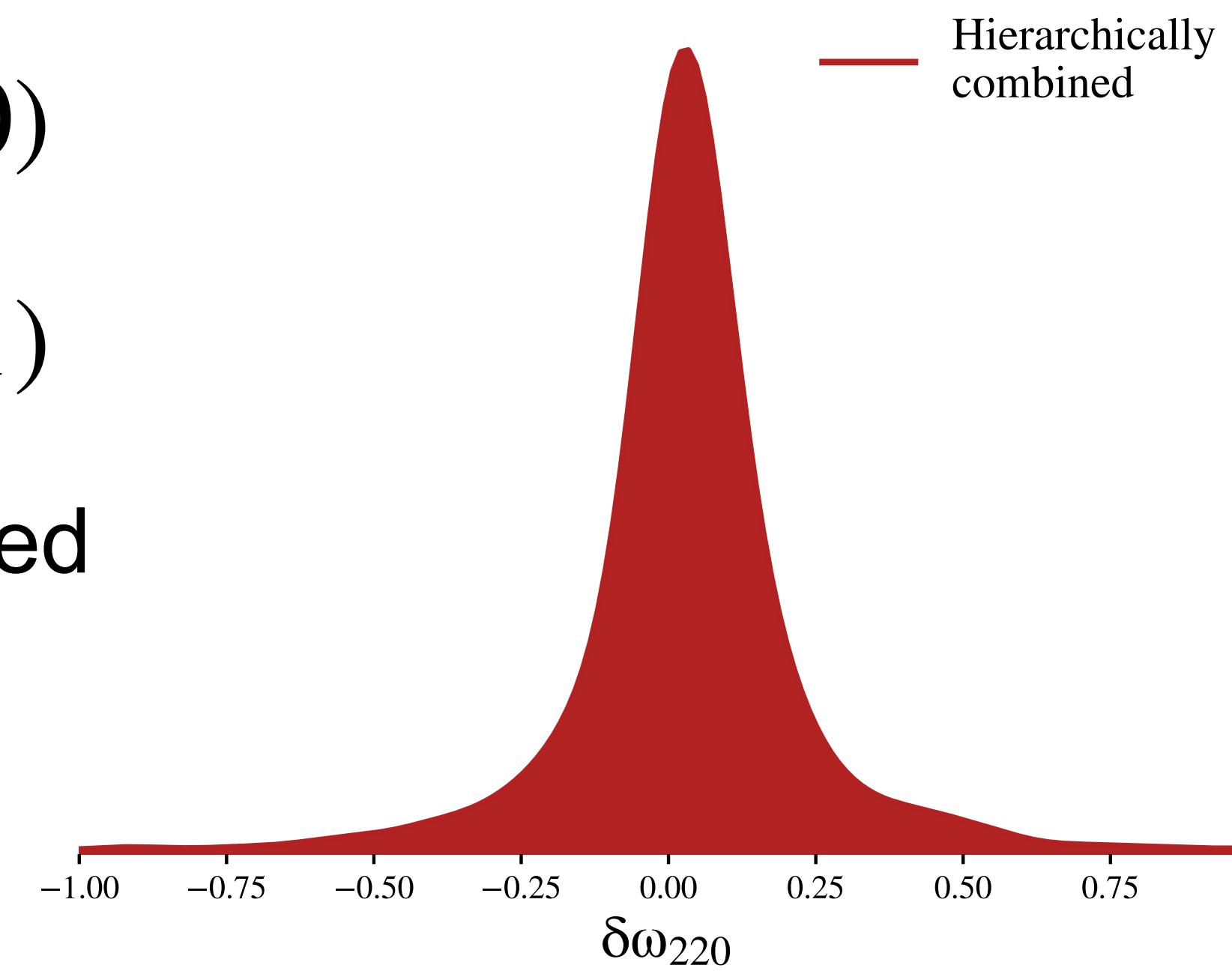
# Testing the nature of the remnant

- GR ringdown spectrum is “over-determined”
  - Mass, spin (and charge) determine whole spectrum
  - Consistency test among modes (e.g. Gossan+, 2012)
  - Allow for deviations like
 
$$\omega_{lmn}(M_f, a_f) \rightarrow (1 + \delta\hat{\omega}_{lmn}) \omega_{lmn}(M_f, a_f)$$
  - GR implies deviation parameters equal to 0

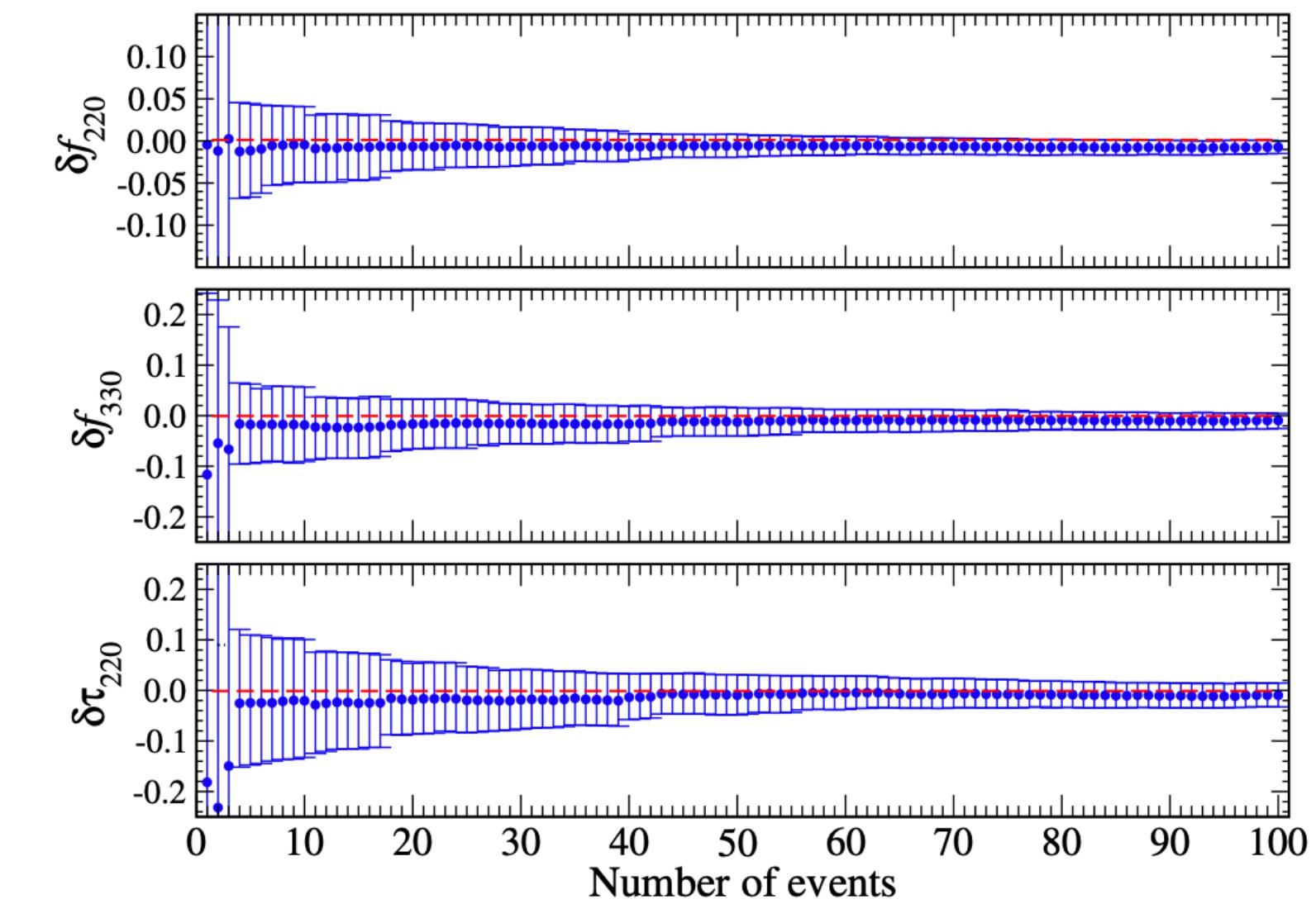
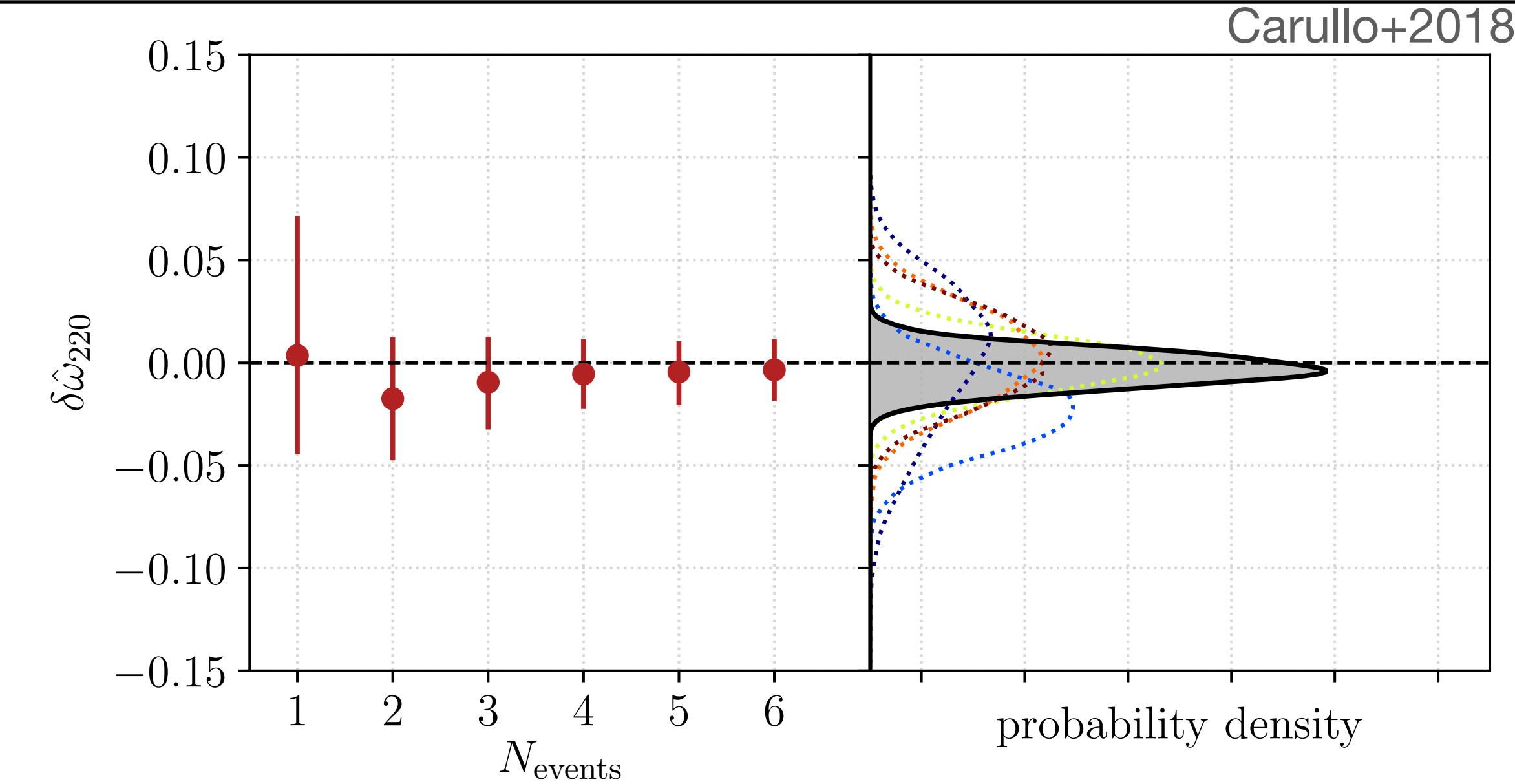


# Current bounds

- GWTC-2
  - Bounds on:
    - $(l, m, n) = (2, 2, 0)$
    - $(l, m, n) = (2, 2, 1)$
    - deviations constrained to  $O(50\%)$
    - More stringent bounds are possible with more assumptions (e.g. Carullo, 2021)



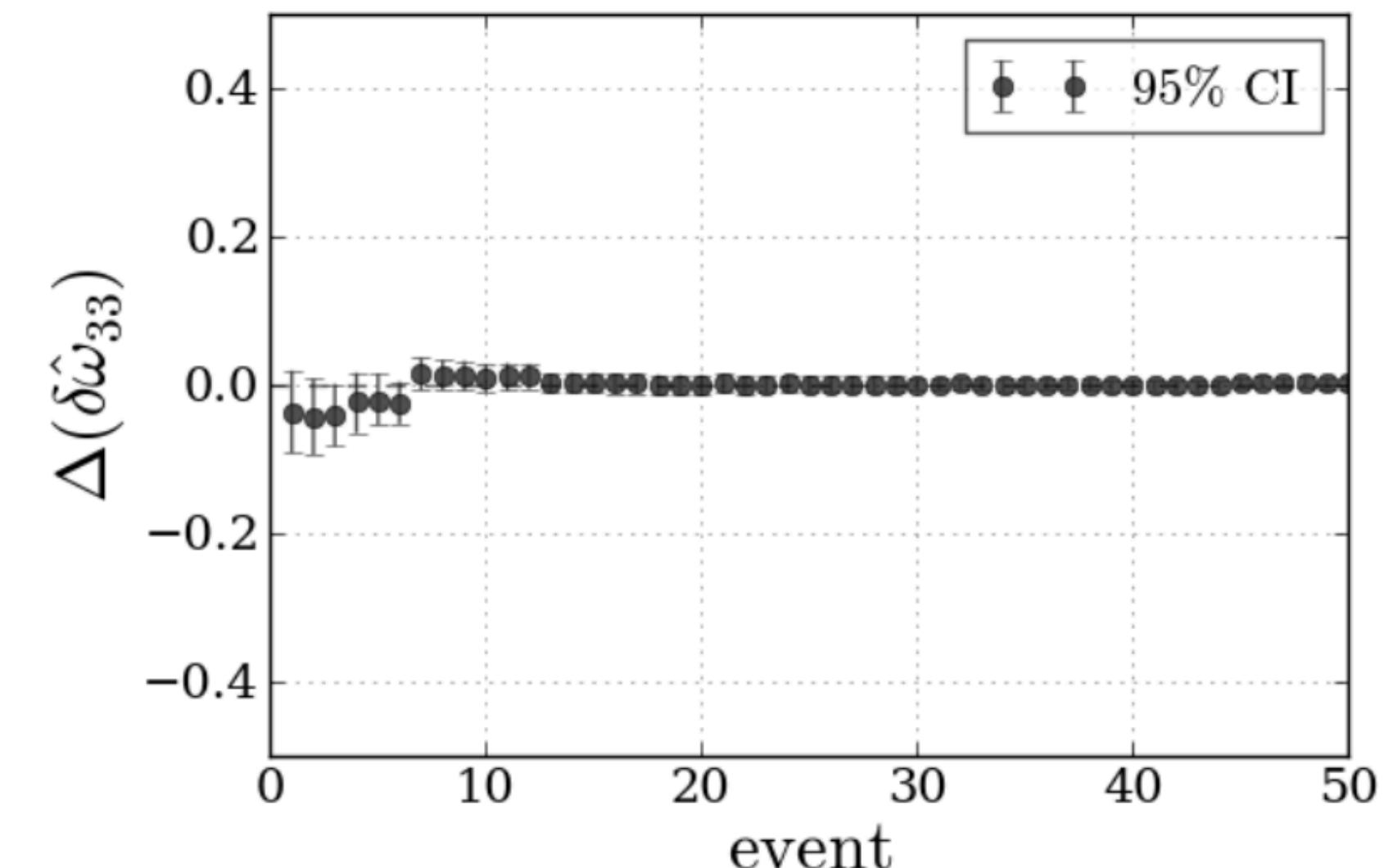
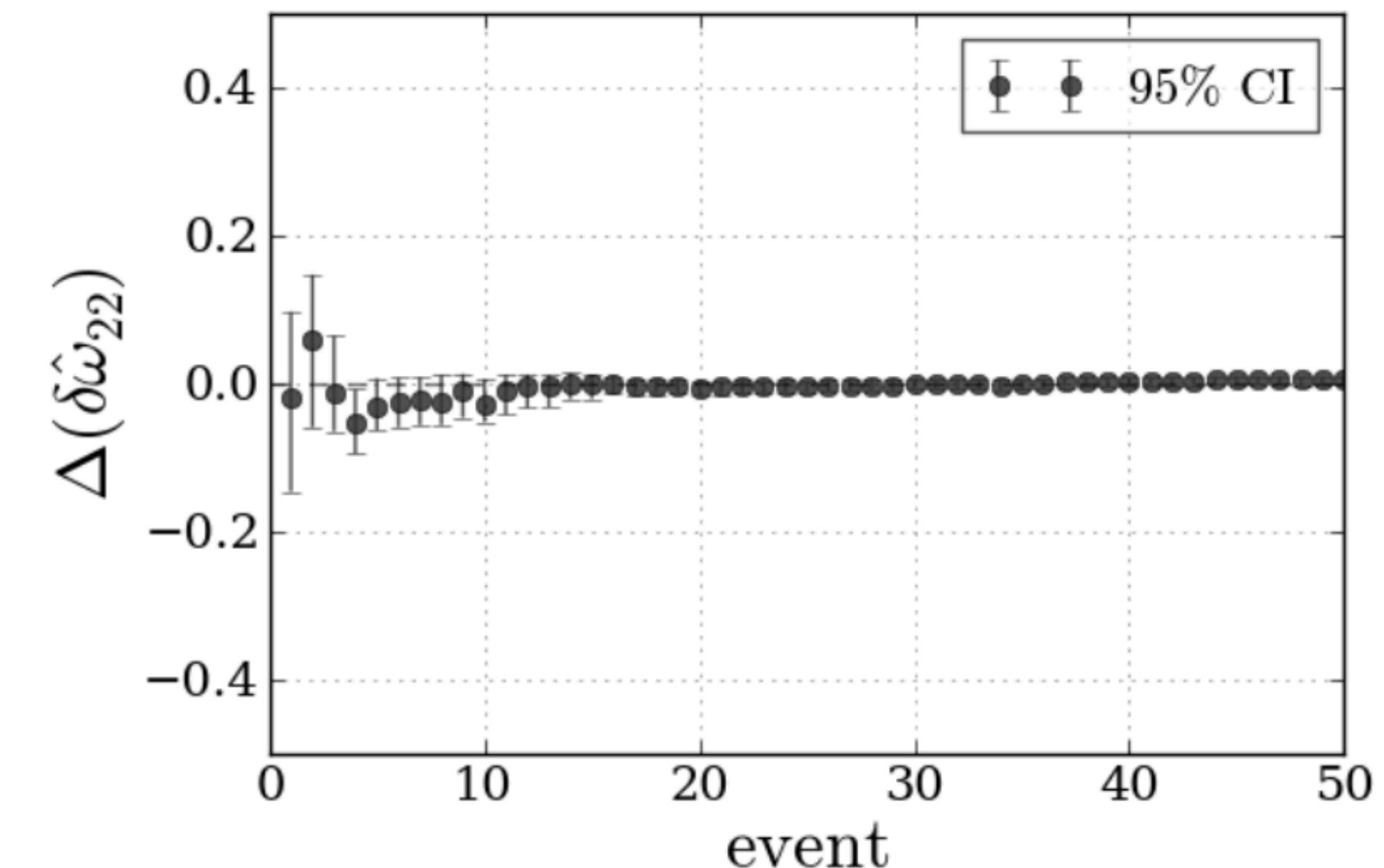
- 1.5% accuracy with 6 golden events and LV network (design)
- Similar projections from a full IMR investigation (pSEO)



Brito+2018

# The next generation of detectors

- Third generation instruments will detect thousands of BBH
- High SNR
- Sub-percent accuracy on deviations from BH uniqueness hypothesis



# Conclusions - I

- LIGO-Virgo observations put constraint to the dynamics of space-time in the dynamical high curvature regime
- Global constraints on GW waveform
- Constraints on post-Newtonian series
- Constraints on the nature of components
- Constraints of GW propagation
  - From GW170817  $v_{GW} = c$
  - Tests for the presence of additional polarisations



- LIGO-Virgo ringdown observations can already probe high-curvature regimes of GR theories and place competitive bounds on beyond-GR extensions
- Test Hawking's Area Theorem (Cabero+ 2018)
- Test of the Black Hole Uniqueness Theorems
- Test energy and angular momentum conservation during strong-field gravitational processes (Ghosh+ 2017)
- Extract implication on black hole astrophysics from final mass and spin measurements
- Test for the presence of alternative compact objects (spacetime signature), alternative theories or non-vacuum environment (Cardoso, Pani 2019)
- Constrain the graviton mass (Chung, Li 2018)
- Test quantum horizon effects and BH thermodynamics (Foit, Kleban, 2019, Hod 2019, Carullo+2021, Laghi+2021)



- LIGO-Virgo ringdown observations can already probe high-curvature regimes of GR theories and place competitive bounds on beyond-GR extensions
- Test Hawking's Area Theorem (Cobano+ 2019)
- Test of the strong equivalence principle (Ghosh+ 2019)
- Test energy-momentum tensor conservation (Ghosh+ 2019)
- Extract implied constraints on the theory (Laghi+ 2021)
- Test for the presence of non-vacuum sources (Laghi+ 2021)
- Constrain the graviton mass (Chung, Li 2010)
- Test quantum horizon effects and BH thermodynamics (Foit, Kleban, 2019, Hod 2019, Carullo+2021, Laghi+2021)

**BBHs and GW behave just like GR predicts\*!**

\*as far as we can tell

processes  
s  
e theories or