Gravitational Wave Detectors

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- The LIGO Lab MIT, Caltech, Hanford and Livingston Observatories
- The LIGO Scientific Collaboration; Virgo and KAGRA
- NASA; LISA Consortium and Pulsar Timing Array Collaborations
- The US National Science Foundation for extraordinary support and perseverance for LIGO



References

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- Einstein telescope <u>http://www.et-gw.eu</u>
- Cosmic explorer <u>https://cosmicexplorer.org</u>
- Hobbs G, Dai S. Gravitational wave research using pulsar timing arrays <u>https://export.arxiv.org/pdf/1707.01615</u>
- The NANOGrav 12.5-year Data Set: Search For An Isotropic Stochastic Gravitational-Wave Background https://arxiv.org/pdf/2009.04496
- LISA Mission Proposal https://dms.cosmos.esa.int/COSMOS/doc_fetch.php?id=3753414

Scope

- This talk is intended to present the basic concepts of laser interferometry for gravitational-wave observation
- Focus on ground-based detectors for stellar-mass events
 - » I'll mostly refer to LIGO due to familiarity
- Qualitative in orientation; references for deeper study
- Other talks will cover the current realization (Virgo, LIGO, KAGRA) and the future plans (Einstein Telescope, Cosmic Explorer) in detail.

GWs in GR

- While tests of deviation from GR are important, the detectors I will discuss are built to be sensitive to GR-predicted signals, so assume waves:
- Propagating at the speed of light
- Creating strain $h = \Delta L/L$ in space with (in general) a time dependence h(t)
- Wavelengths $\lambda_{GW} = c/f_{GW}$ ground based currently in short-antenna limit
- Two polarizations, 45° to each other
- Ring of free 'test masses' is deformed by a passing GW this enables observation



Detection methods, Projects



Detection methods, Projects

- B-mode Polarization of the Cosmic Microwave Background
 - » Search for a primordial GW Background: A very interesting target!
 - » Does not provide a time series h(t) of strain; not discussed further here
- Pulsar timing arrays (Stanislav Babak)
 - » Use pulsars as test masses with clocks
 - » Look using radio telescopes for timing shifts in spatially-separated pulsars
 - » Astrophysical stochastic background the initial target
 - » Science target $\sim 10^7 10^{10} M_{\odot}$ systems
- Space-based laser interferometric detectors (Stanislav Babak)
 - » LISA for example (launch in mid-2030's)
 - » Science target ~ $10^3 10^7 M_{\odot}$ systems; 2.5x10⁶ km arms
 - » and: DECIGO concept targeting primordial Background around 0.1 Hz
- Ground-based laser interferometric detectors
 - » LIGO (2xUS, LIGO-India), Virgo, KAGRA; 3 4 km arms
 - » Einstein Telescope, Cosmic Explorer future; 10 40 km arms
 - » Science target ~ $<1 10^3$ M_{\odot} systems

Detection methods, Projects



Ground-based Detector requirements \rightarrow specifications

- Elegant to take a science case and use it to place requirements on a ground-based detector design
 - » The future ET and CE detectors can take this approach
- Ground-based detectors are *presently* best-effort technically
 - Where were optical or radio telescopes, X-ray satellites, etc. 5 years after their first successful operation? That's where GW detectors are!
 - » Seek observational science enabled with what can be built now
 - » Parallel development of future science-driven observatories/detectors
- Low frequency limit enable studies of BH systems up to ~150M_☉
 - » enables long observation times for lighter systems
 - » NSNS system seen for >30sec
- High frequency limit to enable studies of NS coalescence
 - » Ideally 3-4 kHz, currently more like 0.7-1 kHz
- Data must be sufficiently stationary and free of defects; good data segments significantly longer than transient signals
- Signal rate impedance matched to human impatience ~1/week

LIGO and Virgo sensitivity

• LIGO-Virgo noise floor $h = \Delta L/L \sim 10^{-23}$ in a 1 Hz bandwidth



NS-NS inspiral mapped onto detector sensitivity



NS-NS inspiral mapped onto detector sensitivity



NS-NS inspiral mapped onto detector sensitivity



NS-NS inspiral mapped onto detector sensitivity





What is our measurement technique?

- Enhanced Michelson interferometers
- GWs modulate the distance between the end test mass optic and the beam splitter
- The interferometer acts as a transducer, turning GWs into photocurrent proportional to the strain amplitude
- For a given strain $h = \Delta L/L$,

$$\Delta P_{\rm GW} \sim h L P_{\rm laser} / \lambda_{\rm laser}$$

Increase P_{laser} Use short wavelength laser λ_{laser}

Magnitude of h at Earth: Detectable signals h ~ 10⁻²¹ (1 hair / Alpha Centauri) For L = 1 m, $\Delta L = 10^{-21}$ m For L = 4km, $\Delta L = 4 \times 10^{-18}$ m

Enhanced Michelson interferometers

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Increase arm length L

What is our measurement technique?



What are the 'fundamental' limits to sensitivity?

Useful paradigm in considering limits to detector sensitivity

- Ability to measure the position of our test mass
 - » Shot noise
 - » Scattered light
 - » Laser light defects intensity, position, mode shape, frequency noise
 - » Electronics noise
- True noise motions of the reference surface on our 'free test mass' which can mask GWs
 - » Thermal noise
 - » Radiation pressure
 - » Environmental mechanical forces seismic, anthropogenic, weather
 - » Stray electric, magnetic fields
 - » Accidental noise forces from our control systems and sensors We'll start with noise motions

Measuring $\Delta L = 4 \times 10^{-18}$ m Internal motion

- Thermal noise kT of energy per mechanical mode
- Über die von der molekularkinetischen Theorie der Wärmegeforderte Bewegung von in ruhenden Flüssigkeiten suspendierten Teilchen, A. Einstein, 1905
- Simple Harmonic Oscillator:

$$x_{rms} = \sqrt{\left\langle (\delta x)^2 \right\rangle} = \sqrt{k_B T / k_{spring}}$$

Distributed in frequency according to real part of impedance $\Re(Z(f))$

$$\widetilde{x}(f) = \frac{1}{\pi f} \sqrt{\frac{k_B T}{\Re(Z(f))}}$$

Low-loss materials, monolithic construction





Measuring $\Delta L = 4 \times 10^{-18}$ m Internal motion

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Measuring $\Delta L = 4x10^{-18}$ m Internal motion

- In in the best coatings, the dielectric optical coating has a rather large loss tangent
 - » Some 10⁻⁴, compared to 10⁻⁸ for fused silica
- The Fluctuation-Dissipation theorem says this is where the greatest motion is found
- And: the coating is the surface that is sensed by the laser

This is the dominant limit in the critical 50-200 Hz band



Frequency [Hz]

coating elastic loss $\phi \equiv \operatorname{Im} Y / \operatorname{Re} Y$

$$\left\langle \Delta x(f,T)^2 \right\rangle \approx \frac{2k_B T}{\pi^2 f} \frac{d}{w^2 Y} \phi(f)$$

coating thickness

beam radius Y Levin Phys. Rev. D 57 659 (1998)

Basic Coating Concepts

$$\left\langle \Delta x(f,T)^2 \right\rangle \approx \frac{2k_BT}{\pi^2 f} \frac{d}{w^2 Y} \phi(f)$$

Dielectric mirror

$$\lambda/4n_H - \lambda/4n_L$$

- $n_L n_H$
- alternating high/low index ~¼ wavelength-thick layers
- large index contrast \Rightarrow fewer, thinner required layers
- Key optical properties
 - absorption < 0.5 ppm, scatter ppm's, point absorbers ↓
 - industry standard: ion-beam sputtering
 R.T. deposition followed by 300 C 500 C annealing
 - scaling to >30 cm nontrivial
 with ~1 nm RMS figure: LMA, Lyon
- Current LIGO mirrors:

- Ti(20%):Ta₂O₅:
$$n = 2.07$$
, $\phi = 3 \ge 10^{-4}$
SiO₂: $n = 1.45$, $\phi = 4 \ge 10^{-5}$

$$\frac{d_{{\rm Ta}_2{\rm O}_5}}{d_{{\rm Ta}_2{\rm O}_5} + d_{{\rm SiO}_2}} \sim 40\%$$

FoM (roughly)
$$\propto \frac{(n_{\rm H} / n_L) \ln(n_{\rm H} / n_L)}{\phi_H}$$

Measuring $\Delta L = 4 \times 10^{-18}$ m Forces on test mass



- Seismic noise must prevent masking of GWs, enable practical control systems
- Not 'fundamental physics', but 'fundamental to success'
- aLIGO uses active servocontrolled platforms, multiple pendulums



Active and passive seismic isolation



Basic Building Blocks: Pendulums

- Pendulum suspensions for optics which serve as test masses
- Need test masses to be 'free' in along the relevant measurement axis
- Ground-based detectors operate in Earth's gravitational field
- Hang optics like a clock pendulum; above the resonant frequency, mirror is 'free'
- Inertia of the mass provides seismic isolation
 - » Single stage $(f_o/f)^2$; two stages $(f_o/f)^4$...
- Provides flexibility for alignment and actuation



















Multi-stage Isolation Performance







Multi-stage Isolation Performance









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Vertical Degree-of-Freedom

- Projection of 'vertical' motion along the optical axis if mirror is not normal to the laser beam
 - » \rightarrow requirement on 'levelness' of the Observatory site
 - Typ. 3-4 x 10⁻⁴ radians
 - \rightarrow coupling growing linearly with length of detector
 - (but GW sensitivity also grows linearly; not a worry!)
- Coupling due to imperfections in suspension design
 - » E.g., unbalanced suspension fiber diameters, actuators which have an internal cross coupling, etc.
 - » Difficult to measure but appears to be $\leq 10^{-3}$





LIGO Facility Beam Tube Alignment

- Requirement to maintain a 1m clear aperture through the 4 km long arms
- A straight line in space varies in ellipsoidal height by 1.25 m over a 4km baseline
- A maximum deviation from straightness in inertial space of 5 mm rms
- Average angle with respect to local gravity of 3x10⁻⁴ radians





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Suspension violin modes



Very high Q (~1 billion) silica fiber violin modes at 500 Hz and higher harmonics, excited by thermal noise Brett Shapiro



Some of the many modes of a quadruple pendulum





0.43 Hz

Brett Shapiro





Top Mass Damping



Other DOF; **Nonlinear Upconversion**





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Cavity Length Control





Measuring $\Delta L = 4 \times 10^{-18}$ m External Forces on test mass

- Advanced LIGO (and Virgo) expect to be limited by this noise source –
 - » After all technical noise sources beaten down
 - » At low optical power (no radiation pressure noise)
 - » In the 10-30 Hz range
- We would *love* to be limited only by this noise source!
- Want to go a bit lower? Go underground.
- Want to go much lower? Go to space.





Mid-path summary

- Interferometry comparing the light travel time along (more or less) orthogonal arms can measure a passing gravitational wave
- The limits to sensitivity come from
 - » Undesired motions of the interferometer mirrors
 - » Limitations in our ability to measure the positions of the mirrors
- Thermal noise is one cause of undesired motions, managed through use of low-mechanical-loss materials and concentrating motion in a narrow band
- External motion must be very strongly filtered to make those forces negligible; pendulums are a very useful approach, complemented with servo-control systems
- Time-varying Newtonian gravity fields remain, and cannot be filtered only reduced through facility design (including underground) or sensed and subtracted
- ...Tomorrow we continue with sensing limitations, some general considerations, and a tour of the facilities

Interferometry

- Quantum measurement effects present both limits to sensitivity and means to improve the sensitivity
- First, increase the light power to reduce shot noise
 - » High power laser
 - » Low loss, high-precision optical components
 - » Optical topologies to increase circulating light power
 - » Optical topologies to distribute light power optimally
 - » ... until radiation pressure starts to dominate
 - » ...and our selected topologies couple shot noise and radiation pressure
- Second, use squeezed light to improve sensitivity
 - Manage coupling between light intensity and light phase (pondermotive squeezing)
 - » Sneak around Heisenberg's uncertainty principle





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Squeezed light to reduce quantum noise

Heisenberg Uncertainty Principle of QM dictates that precise values of phase, and amplitude, of light cannot be known at the same time:

$$\Delta \hat{X}_{\text{phase}} \Delta \hat{Y}_{\text{amp}} \ge \hbar/2$$

- We can choose however to e.g., know the amplitude less well and look more closely at the phase
- This corresponds to reducing the high-frequency Shot Noise in our interferometer noise budget
 - BUT increasing the low-frequency **>> Radiation Pressure noise**
- This is frequency **in**dependent squeezing
- Squeezing is made by creating pairs of photons using an optical parametric oscillator
- The pairs are quantum-mechanically entangled and have correlated arrival times at the detector
- This reduces the randomness of the time distribution



PRM

SRM

phase

shifter

LASER

Quantum shot noise limits the high frequency sensitivity



Frequency Independent Squeezing



Frequency Dependent Squeezing

- We can be more clever!
- We can adjust the phase of the squeezed light used
 - » Pass through an optical resonant cavity acting as a filter tuned to the transition from Radiation Pressure to Shot Noise
- Heisenberg's principle still holds at any given frequency, but we look more carefully at the amplitude at low frequencies and the phase at high frequencies
- Being implemented in Virgo and LIGO, probably for next observing run O5



J. Kimble et al., PRD 65, 022002 (2001); S.L. Danilishin



Frequency Dependent Squeezing



Frequency Dependent Squeezing



Cross coupling between motion and sensing: Parametric Instabilities

- A coupling between the optical sensing system and the mechanical system being sensed
- One limitation to the usable light power in a GW detector



Thermally excited acoustic mode scatters TEM₀₀ mode \rightarrow sidebands $\omega_0 \pm \omega_m$

Resonance condition: $\omega_0 - \omega_1 = \omega_m$ & high spatial overlap



Parametric Instabilities

Overlap between mechanical and optical modes

Active and passive control scheme to suppress

Adv LIGO Target Design Sensitivity, basic noise sources



Observatory Infrastructure

Vacuum System

 The 3 or 4km path of the laser from BeamSplitter to end mirror must be in an excellent vacuum



• Polarizability α of the remaining gas molecules induces path-length fluctuations; again, Poisson Statistics, and an effect proportional to square root of density $\rho^{1/2}$ along the path 1

$$h(f) \approx 4\pi \alpha \left(\frac{2\rho}{v_0 w_0 L}\right)^2$$

Connect locomotive transformer to tubing for I²R heating to outgas
1 pump every 2km

Residual gas: path-length fluctuations, pendulum damping

- Pygwinc model for residual gas, for
 - » The path length fluctuations for gas along the n*km path
 - » Pendulum suspension thermal noise due to transfer of momentum to/from gas molecules from/to test mass



How scattered light affects the IFO

 Scattered light is especially problematic if the light can re-enter the main beam path, scattered back from moving objects like baffles or chamber walls.



- Scattered light noise is seen in the DARM spectrum in the frequency range 10-200 Hz.
- Significant noise source.

Beam Tube Scattered Light

- Laser wavelength determines the minimum beam size after 4km propagation for 1064nm Nd:YAG, this leads to 10-12cm diameter for 1/e² but in fact must be much further in the tails of Gaussian to 10⁻⁶
- In addition, the mirrors are not perfect
 - » 'dust' and point defects
 - » Large-scale 'waviness' (~10 nm over 10 cm)
- \rightarrow 1.2m diameter beam tube
- \rightarrow baffles to catch scattered light







And many other 'technical' noise sources....



Length: The ultimate solution

- In addition to understanding and adjusting the design for thermal noise, quantum limits, Newtonian background, seismic noise, there are important parameters to consider
- Length is good for sensitivity! Technically much easier than lowering noises
 - » Signals get larger, noises tend not until one is comparable to $\lambda/2$
 - » Optimum for coalescence of BNS around 20km

	Longth scaling dominatos	Noise	Scaling
	the cost for a detector	Coating Brownian	$1/L^{3/2}$
		Substrate Thermo-Refractive	$1/L^2$
		Suspension Thermal	1/L, 1
		Seismic	1/L, 1
		Newtonian	1/L
		Residual Gas Scattering	$1/L^{3/4}$
	Strain sensitivity as	Residual Gas Damping	1/L
		*Quantum Shot Noise	$1/L^{1/2}$
	function of length L	*Quantum Radiation pressure	$1/L^{3/2}$

Depth

- Burying the detector has unique advantages to improve the lowfrequency sensitivity; esp. reducing the Newtonian background
- The Science Case should drive the design decision here, modulated by cost
- Asking for both an optimal length and and a buried detector is probably unrealistic from a cost standpoint
- Next-generation detectors are a wonderful illustration
 - » Cosmic Explorer: 40km, surface detector, best reach
 - » Einstein Telescope: 10km, underground, best low-frequency
- Also practical considerations:
 - » Working underground, safely, is hard! Can expect slower progress in activities leading up to observation
 - » On the surface, Blocking migratory paths, occupying land belonging to indigenous peoples present very difficult puzzles to solve

Risk

- Different projects can adopt different risk levels
- GEO-600 is a great example of a situation where high risks can be taken
- Also different cultures, funding agencies, collaborations have different levels of tolerable risk
- More ambitious designs require more R&D to be successful to be realized, and may
 - » Take more time to get working
 - » Lead to a more sensitive detector
 - » Make more significant steps forward in measurement science
 - » And be risky!
- Safety
 - » A different kind of risk, but human safety is very important
 - » One person seriously injured or worse is not only a human tragedy
 - it can also kill a project

System Engineering

- To find solutions which meet the observational science goals, and which fit in the other constraints just discussed, is tricky
- Requires compromises both in the initial design, and dynamically as the project advances
- Constant modeling of the sensitivity is crucial, along with modeling of schedule and cost
- A mixture of engineering, instrument science, observational science, and project management is needed to succeed
- Just keep in mind that a full design process has a great deal of richness!

One more fundamental element in interferometer designs

Collaboration

- Table-top scientists precision measurement, laser, atomic started the field; tradition of small groups, small projects, and some competition
- Early general relativists, theorists, astrophysicists much the same
- Transformation when High Energy Physics types got involved
 - » Engineering, project organization, computing, analysis
- Funding agencies also saw a need for a shift
 - » There is a real skill in spending hundreds of millions of Euros!
- Goal pre-discovery was crystal-clear: Make a detection
- Afer the Collaborations formed and were stable, meta-collaborations: 'The LVK' – KAGRA, Virgo, and LIGO Scientific Collaborations all sharing data
 - » The science that is possible is qualitatively greater
 - » The sociology of a (mostly) non-competitive environment nurturing and supportive
- LISA and Pulsar Timing also in collaborations/consortia
- Now perhaps 3000 persons worldwide
 - Maybe you will join us!

LIGO 'Virtual' Tour




Hanford Corner building



Laser Clean Room; extraterrestrials for scale

200 W, single frequency, single mode, Nd:YAG laser

Challenging requirements:

- $\delta f \sim 10^{-6} \text{ Hz/Hz}^{1/2}$
- $\delta I/I \sim 10^{-8}/Hz^{1/2}$



Vacuum chambers to protect and isolate optics



Inspecting mirror during fabrication





Test Mass Suspension





End-mirror assembly (humans removed before pumpdown)



Active and passive seismic isolation



Seismic Isolation Platform

Civil Construction: Beam Tube cover, foundation



Cover useful to protect against 2-ton masses at 100 km/hour





Sensitivity improvements are very well rewarded

Simulated Event Stream for a one year duration O4 run

- LIGO 'A+' Incremental changes to the Advanced LIGO design
 - » Similar changes planned for Virgo
- Rough doubling of reach
 - $\gg 2^3 = 8$ greater volume
 - » 8x higher rate
 - 17-300 BBH/month >>
 - 1-13 BNS/month >>
 - » 2-11 BNS x SGRB coincidences/year
- **Population studies**
- Hubble Constant
- ...higher SNR for e.g., tests of GR
- Plan to be observing ~2025 (uncertain pandemic delay) G2101171



Projections toward aLIGO+ (Comoving Ranges: NSNS 1.4/1.4 M_{\odot} and BHBH 20/20 M_{\odot})



Onward

- Hope this introduction gives a good basis for the talks to follow
- Do feel free to follow up with questions in the Office Hours
- Also email to <u>dhs@mit.edu</u> (but may need to be a bit patient for responses)