

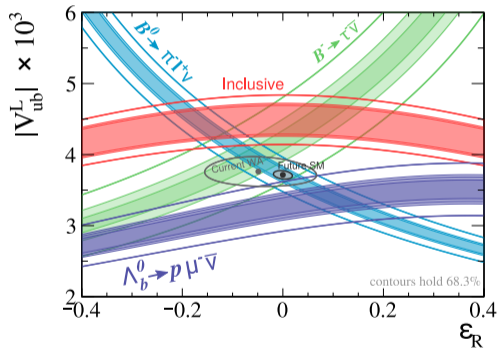
$\Lambda_b \rightarrow \Lambda^*$  and  $\Lambda_b \rightarrow \Lambda_c^*$  form factors  
from lattice QCD

Stefan Meinel

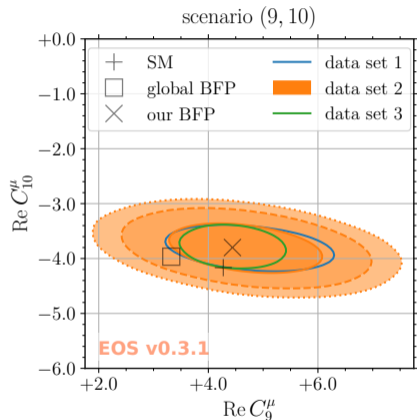


*b*-baryon Fest, November 5-6, 2020 (updated January 5: corrected sign of tensor FFs)

# $b$ baryons provide important constraints on physics beyond the SM



[J. Albrecht *et al.*, arXiv:1709.10308]



[T. Blake *et al.*, arXiv:1912.05811/PRD 2020]

## $\Lambda_b \rightarrow p, \Lambda, \Lambda_c$ : precision

- Uncertainties in  $|V_{ub}/V_{cb}|$  from  $\Lambda_b \rightarrow p\mu\bar{\nu}$  ( $q^2 > 15 \text{ GeV}^2$ ) and  $\Lambda_b \rightarrow \Lambda_c\mu\bar{\nu}$  ( $q^2 > 7 \text{ GeV}^2$ )
  - 2015: **experiment 5%**, **lattice QCD 5%**
  - $\sim 2030$ : **experiment 1-2%**, **lattice QCD ???**
- Uncertainty in  $R(\Lambda_c)$ :
  - **2015 lattice QCD 3%**, **experiment ???**
- $\Lambda_b \rightarrow \Lambda(\rightarrow p\pi)\mu^+\mu^-$ 
  - Angular observables at high  $q^2$ : **2016 lattice QCD uncertainties** are much smaller than **2018 experimental uncertainties**
  - Differential BF at high  $q^2$ : **2016 lattice QCD uncertainties** are somewhat smaller than **2015 experimental uncertainties**
  - Differential BF at low  $q^2$ : **2016 lattice QCD uncertainties** are somewhat LARGER than **2015 experimental uncertainties**

Improved lattice QCD calculations for  $\Lambda_b \rightarrow p, \Lambda, \Lambda_c$  are in progress (see extra slide).

# Additional $b$ -baryon decay modes

Other decays to QCD-stable baryons?

- $\Xi_b^- \rightarrow \Xi^- \ell^+ \ell^-$
- $\Omega_b^- \rightarrow \Omega^- \ell^+ \ell^-$
- $\Xi_b^- \rightarrow \Xi_c^0 \ell^- \bar{\nu}_\ell$
- ...

Lattice calculations of the form factors would be straightforward.

Decays to QCD-unstable baryon resonances:

- $\Lambda_b \rightarrow \Lambda^* \ell^+ \ell^-$
- $\Lambda_b \rightarrow \Lambda_c^* \ell^- \bar{\nu}_\ell$
- ...

Lattice calculations of the form factors are possible for 1) narrow resonances, using single-hadron treatment; 2) general two-body-only resonances, using Lellouch-Lüscher finite-volume formalism, but this is very challenging.

**1**  $\Lambda_b \rightarrow \Lambda^*(1520)$  form factors

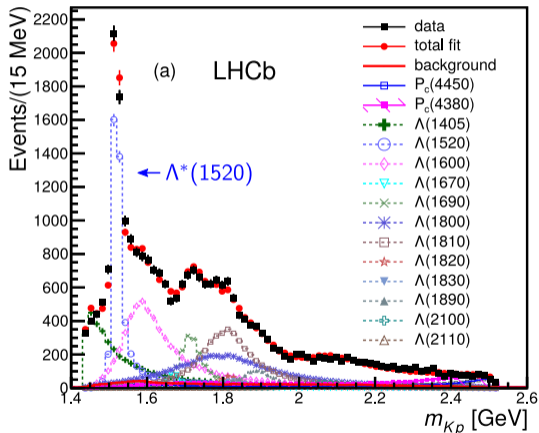
[SM and Gumaro Rendon, [arXiv:2009.09313](https://arxiv.org/abs/2009.09313)]

**2**  $\Lambda_b \rightarrow \Lambda_c^*(2595)$  and  $\Lambda_b \rightarrow \Lambda_c^*(2625)$  form factors

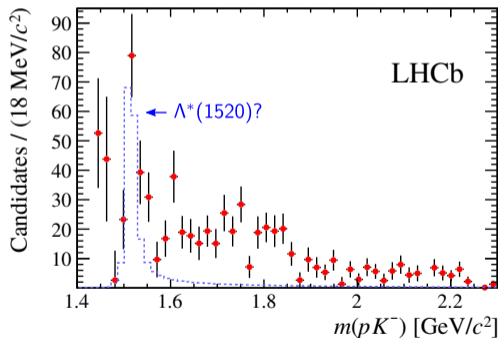
$\Lambda_b \rightarrow pK^- \mu^+ \mu^-$  observed by LHCb

$q^2 \approx m_{J/\psi}^2$

$q^2 \notin [0.98, 1.1] \cup [8.0, 11] \cup [12.5, 15] \text{ GeV}^2$



[arXiv:1507.03414/PRL 2015]



[arXiv:1703.00256/JHEP 2017]

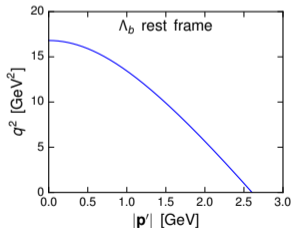
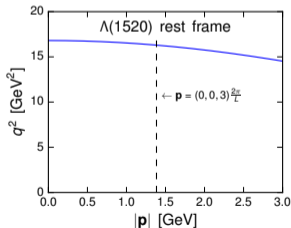
$$\Lambda_b \rightarrow \Lambda^*(1520)\mu^+\mu^-$$

- The  $\Lambda^*(1520)$  is the lightest isospin-0,  $J^P = \frac{3}{2}^-$  strange baryon resonance. It has a mass of  $1519.5 \pm 1.0$  MeV, a width of  $15.6 \pm 1.0$  MeV, and decays mainly into  $N\bar{K}$ ,  $\Sigma\pi$ , or  $\Lambda\pi\pi$ .
- The phenomenology of  $\Lambda_b \rightarrow \Lambda^*(1520)\mu^+\mu^-$  was recently studied in:
  - S. Descotes-Genon, M. Novoa-Brunet, [arXiv:1903.00448/JHEP 2019](#)
  - D. Das, J. Das, [arXiv:2003.08366/JHEP 2020](#)
  - Y. Amhis *et al.*, [arXiv:2005.09602](#)
- The form factors have previously been calculated in a quark model:
  - L. Mott, W. Roberts, [arXiv:1108.6129/IJMPA 2012](#)

# $\Lambda_b \rightarrow \Lambda^*(1520)$ on the lattice

We use the narrow-width approximation: we assume that the lowest finite-volume energy level with the correct quantum numbers corresponds to the  $\Lambda^*(1520)$ . Even in this approximation, the calculation is substantially more challenging than for  $\Lambda_b \rightarrow \Lambda$ :

- At nonzero momenta, the irreducible representations of the lattice symmetry groups mix positive and negative parities and also mix  $J = \frac{1}{2}$  and  $J = \frac{3}{2}$ . We must therefore work in the  $\Lambda^*(1520)$  rest frame and give momentum to the  $\Lambda_b$  instead. This limits us to near  $q_{\max}^2$ .





$\Lambda_b \rightarrow \Lambda^*(1520)$  on the lattice

- The simplest choices of three-quark interpolating fields with  $I = 0$  and  $J^P = \frac{3}{2}^-$  dominantly couple to higher-lying ( $S = 3/2$ ,  $L = 0$ , flavor- $SU(3)$  octet) states. We found it necessary to use an interpolating field with an ( $S = 1/2$ ,  $L = 1$ , flavor- $SU(3)$  singlet) structure obtained using covariant spatial derivatives. This requires additional quark propagators with derivative sources.
- Correlation functions for negative-parity “excited” baryons have even more statistical noise than correlation functions for the lightest baryons  $\rightarrow$  need many samples on many gauge configurations

# Data sets and hadron masses

We use gauge-field configurations generated by the RBC and UKQCD Collaborations, with  $2 + 1$  flavors of domain-wall fermions.

Label	$N_s^3 \times N_t$	$a$ [fm]	$m_\pi$ [GeV]
C01	$24^3 \times 64$	0.1106(3)	0.4312(13)
C005	$24^3 \times 64$	0.1106(3)	0.3400(11)
F004	$32^3 \times 64$	0.0828(3)	0.3030(12)

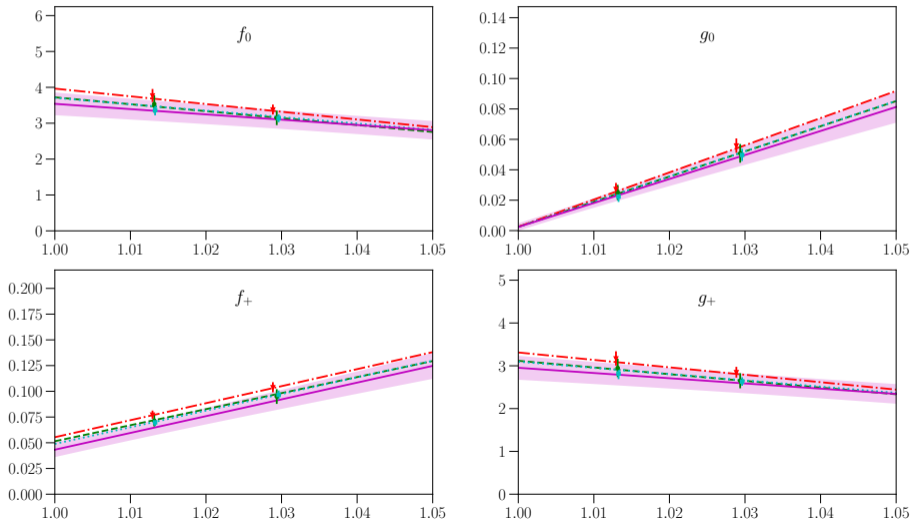
Label	$m_K$ [GeV]	$m_N$ [GeV]	$m_\Lambda$ [GeV]	$m_\Sigma$ [GeV]	$m_{\Lambda^*}$ [GeV]	$m_{\Lambda_b}$ [GeV]
C01	0.5795(19)	1.2647(51)	1.3494(61)	1.3877(61)	1.825(16)	5.793(17)
C005	0.5501(19)	1.1649(58)	1.2659(66)	1.3173(60)	1.740(17)	5.726(17)
F004	0.5361(24)	1.1197(59)	1.2382(54)	1.303(12)	1.757(15)	5.722(23)

$m_{\Lambda^*} - m_\Sigma - m_\pi$  ranges from approximately +80 to +150 MeV (physical value: +192 MeV),

$m_{\Lambda^*} - m_N - m_K$  ranges from approximately -20 to +100 MeV (physical value: +89 MeV)

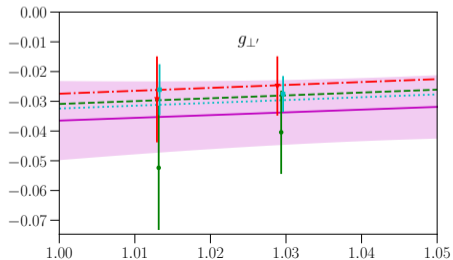
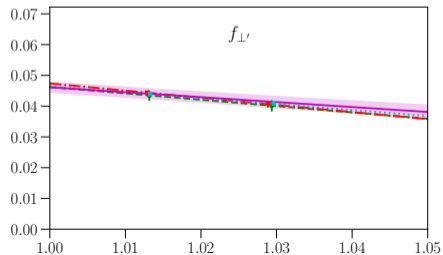
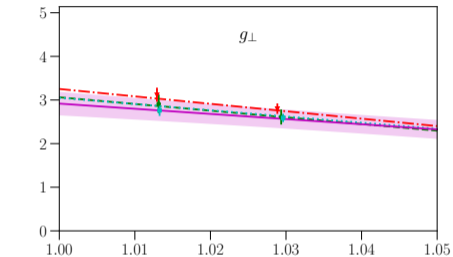
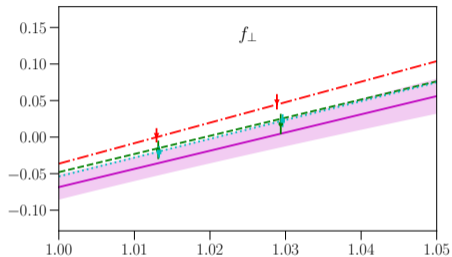
$\Lambda_b \rightarrow \Lambda^*(1520)$  form factors as a function of  $w = v \cdot v'$

◆ C01    ◆ C005    ◆ F004     $a = 0, m_\pi = 135 \text{ MeV}$

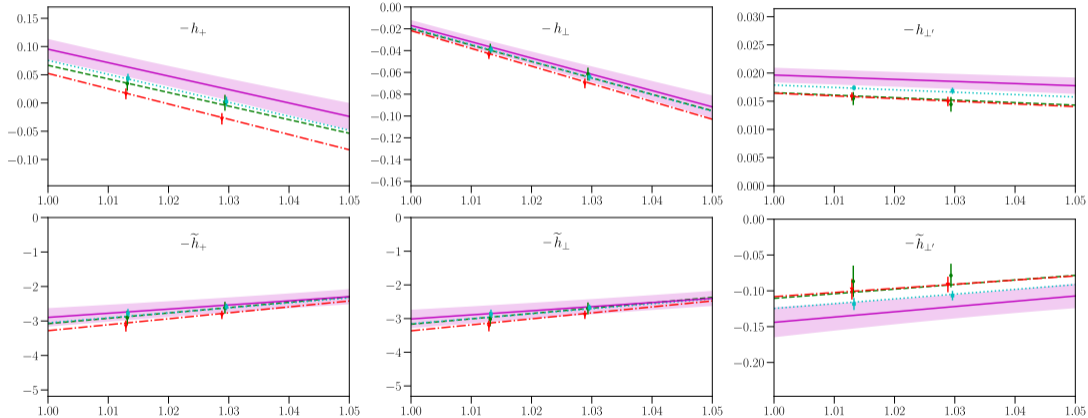


$\Lambda_b \rightarrow \Lambda^*(1520)$  form factors as a function of  $w = v \cdot v'$

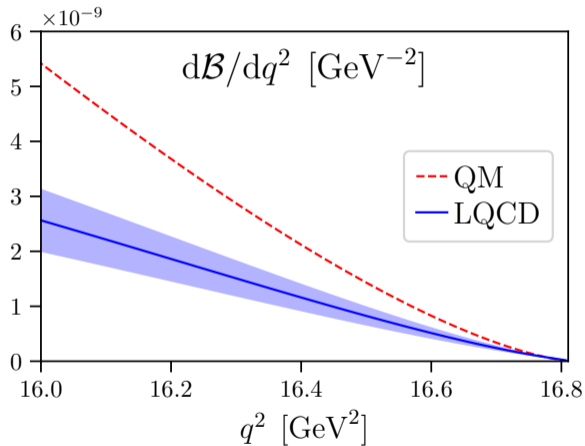
◆ C01    ◆ C005    ◆ F004     $a = 0, m_\pi = 135 \text{ MeV}$



$\Lambda_b \rightarrow \Lambda^*(1520)$  form factors as a function of  $w = v \cdot v'$

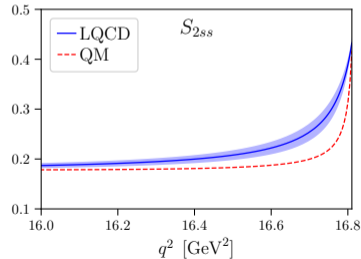
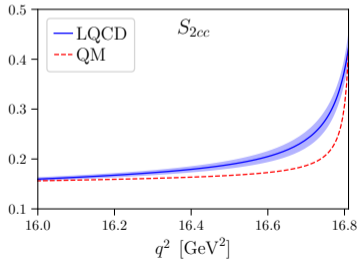
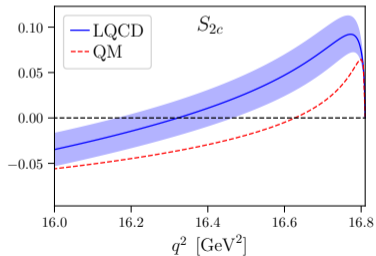
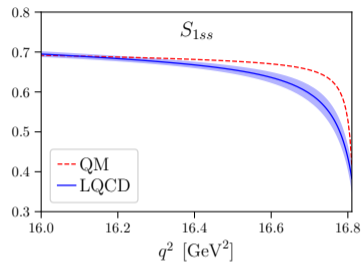
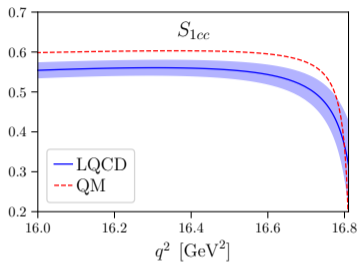
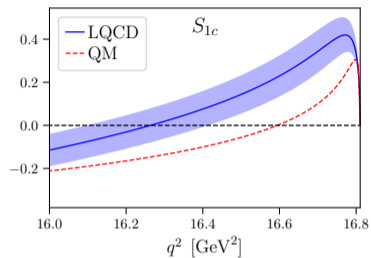


$\Lambda_b \rightarrow \Lambda^*(1520)l^+l^-$  observables



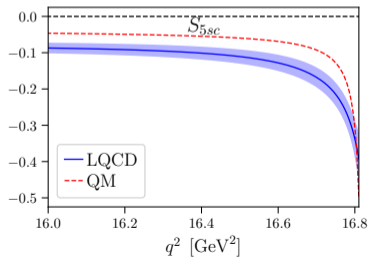
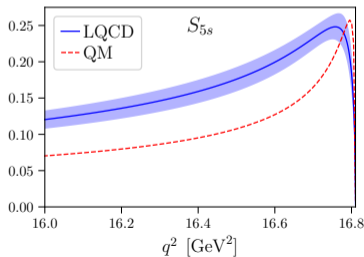
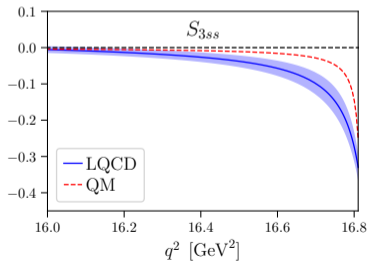
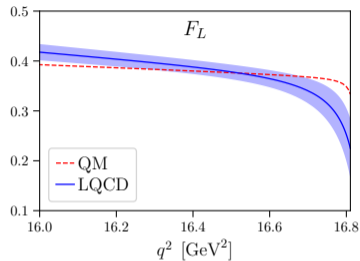
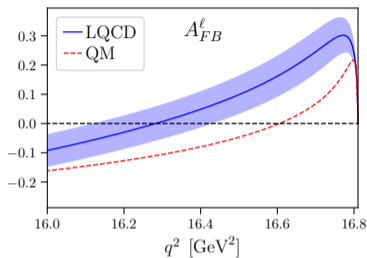
QM = using form factors from [L. Mott, W. Roberts, arXiv:1108.6129/IJMPA 2012]

# $\Lambda_b \rightarrow \Lambda^*(1520)(\rightarrow pK^-)l^+l^-$ observables



See [S. Descotes-Genon, M. Novoa-Brunet, [arXiv:1903.00448](https://arxiv.org/abs/1903.00448)/JHEP 2019] for definitions

# $\Lambda_b \rightarrow \Lambda^*(1520)(\rightarrow pK^-)l^+l^-$ observables



See [S. Descotes-Genon, M. Novoa-Brunet, [arXiv:1903.00448](https://arxiv.org/abs/1903.00448)/JHEP 2019] for definitions



1  $\Lambda_b \rightarrow \Lambda^*(1520)$  form factors

2  $\Lambda_b \rightarrow \Lambda_c^*(2595)$  and  $\Lambda_b \rightarrow \Lambda_c^*(2625)$  form factors

[SM and Gumaro Rendon, in preparation. Results are preliminary.]

$$\Lambda_b \rightarrow \Lambda_c^* \ell^- \bar{\nu}_\ell$$

Name	$J^P$	Mass [MeV]	Width [MeV]	Decays to
$\Lambda_c^*(2595)$	$\frac{1}{2}^-$	2592.25(28)	2.6(6)	$\Lambda_c \pi^+ \pi^-$
$\Lambda_c^*(2625)$	$\frac{3}{2}^-$	2628.11(19)	< 0.97	$\Lambda_c \pi^+ \pi^-$

Motivations include:

- Tests of lepton-flavor universality with  $R(\Lambda_c^*)$   
[P. Böer *et al.*, [arXiv:1801.08367/JHEP 2018](#)]
- Tests of HQET  
[A. Leibovich, I. Stewart, [arXiv:hep-ph/9711257/PRD 1998](#);  
P. Böer *et al.*, [arXiv:1801.08367/JHEP 2018](#)]
- Knowledge of  $\Lambda_b \rightarrow \Lambda_c^*$  form factors can tighten global unitarity constraints on other  $b \rightarrow c$  form factors (including mesonic form factors)  
[T. Cohen, H. Lamm, R. Lebed, [arXiv:1909.10691/PRD 2019](#)]

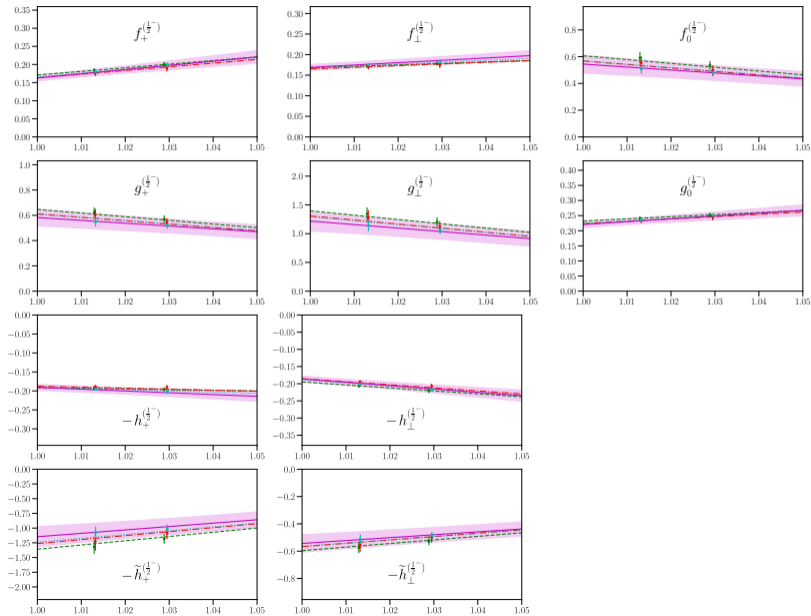
# Data sets and hadron masses

Same three ensembles as used for  $\Lambda_b \rightarrow \Lambda^*(1520)$ . Resulting hadron masses in GeV:

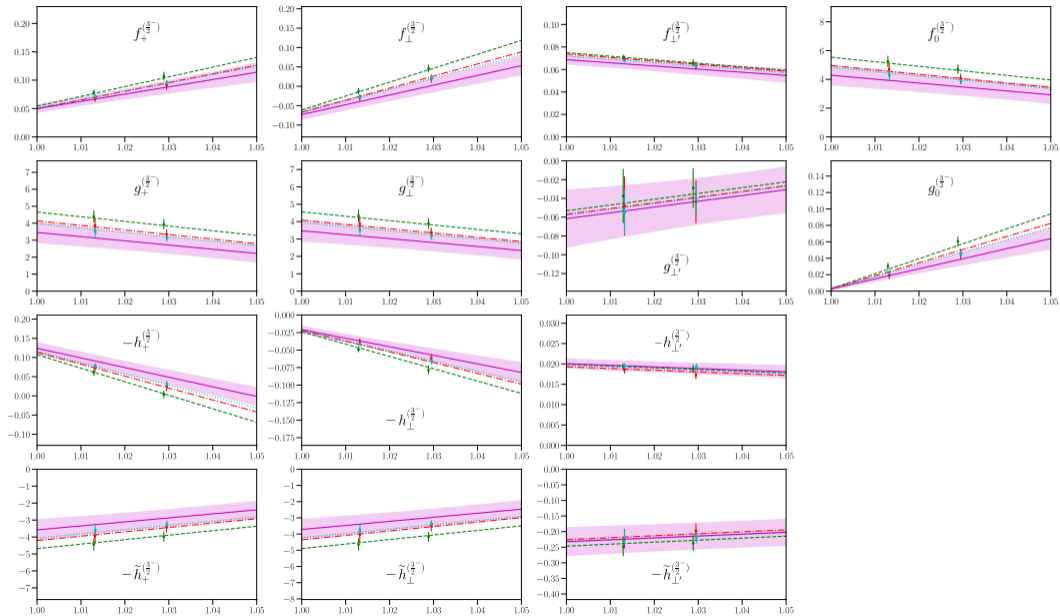
Label	$m_\pi$	$m_D$	$m_N$	$m_{\Lambda_c}$	$m_{\Sigma_c}$	$m_{\Lambda_c^*,1/2}$	$m_{\Lambda_c^*,3/2}$	$m_{\Lambda_b}$
C01	0.4312(13)	1.9119(54)	1.2647(51)	2.4652(82)	2.617(10)	2.882(12)	2.909(12)	5.793(17)
C005	0.3400(11)	1.8942(54)	1.1649(58)	2.4038(75)	2.565(12)	2.819(13)	2.839(13)	5.726(17)
F004	0.3030(12)	1.8880(70)	1.1197(59)	2.367(12)	2.550(19)	2.781(18)	2.815(18)	5.722(23)

For these data sets, the  $\Lambda_c^*(2595)$  and  $\Lambda_c^*(2625)$  are in fact stable (their masses are lower than the sum of masses of possible decay products)

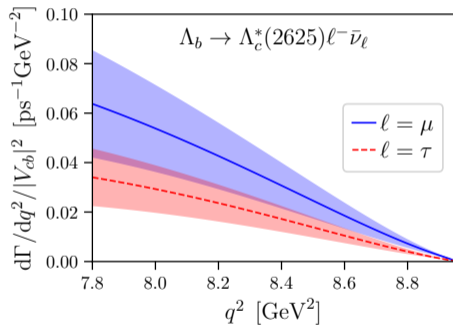
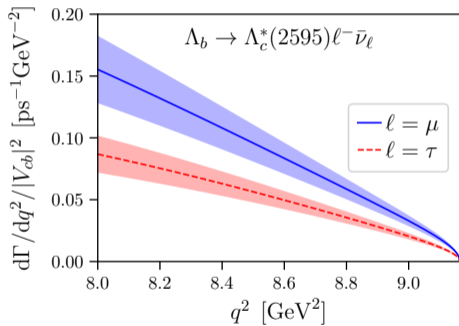
$\Lambda_b \rightarrow \Lambda_c^*(2595)$  form factors as a function of  $w = v \cdot v'$



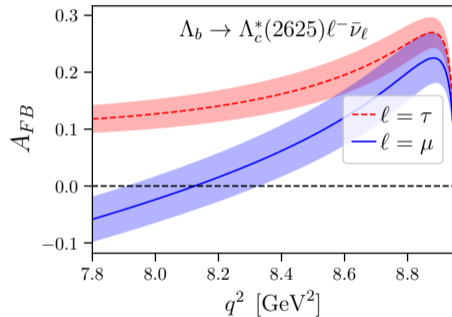
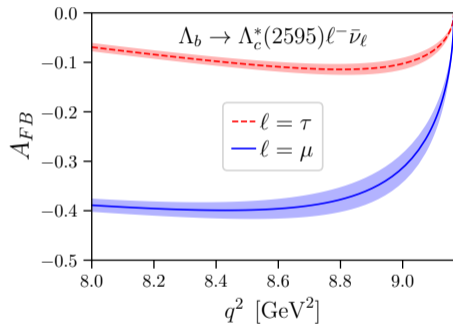
$\Lambda_b \rightarrow \Lambda_c^*(2625)$  form factors as a function of  $w = v \cdot v'$



$\Lambda_b \rightarrow \Lambda_c^* \ell^- \bar{\nu}_\ell$  observables

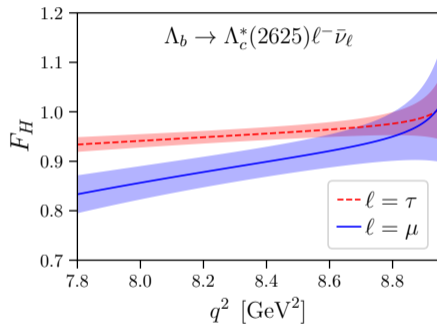
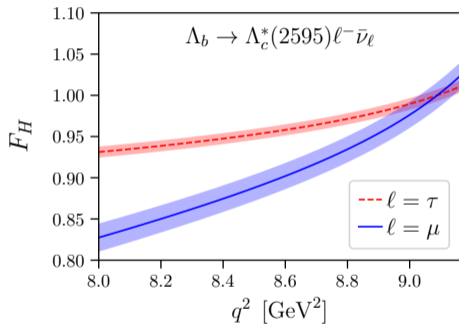


$\Lambda_b \rightarrow \Lambda_c^* \ell^- \bar{\nu}_\ell$  observables



See [P. Böer *et al.*, [arXiv:1801.08367](https://arxiv.org/abs/1801.08367)/JHEP 2018] for definitions

$\Lambda_b \rightarrow \Lambda_c^* \ell^- \bar{\nu}_\ell$  observables



See [P. Böer *et al.*, [arXiv:1801.08367](https://arxiv.org/abs/1801.08367)/JHEP 2018] for definitions



# Questions/Challenges

- What is the best way to isolate the  $\Lambda^*(1520)$  contribution from the  $\Lambda_b \rightarrow pK^- \mu^+ \mu^-$  decay distribution?
- For  $\Lambda_b \rightarrow \Lambda^*(1520)$ ,  $q_{\text{max}}^2 \approx 16.8 \text{ GeV}^2$  means that there is not much phase space above the narrow-charm-resonance region. Is this enough to treat charm effects with the OPE?
- Lattice calculations in the  $\Lambda^*$  rest frame could reach lower  $q^2$  using the moving-NRQCD action for the  $b$ -quark (which allows higher  $\Lambda_b$  momenta).
- I have attempted HQET fits (including  $1/m_Q$  effects) to our lattice results for the  $\Lambda_b \rightarrow \Lambda_c^*$  form factors. The fits have very bad  $\chi^2$ , with fit curves far away from the lattice data for some of the form factors. Are  $1/m_Q^2$  corrections large?
- Can our lattice QCD results be combined with experimental measurements of the  $\Lambda_b \rightarrow \Lambda_c^* \mu^- \bar{\nu}$  decay distribution to predict  $R(\Lambda_c^*)$ ?

Extra slides

# References: $b$ and $c$ baryon decay form factors from lattice QCD

Early work on  $\Lambda_b \rightarrow \Lambda_c$  (quenched, focused on Isgur-Wise function):

K. C. Bowler *et al.* (UKQCD Collaboration), [arXiv:hep-lat/9709028/PRD 1998](#)

S. Gottlieb and S. Tamhankar, [arXiv:hep-lat/0301022/Lattice 2002](#)

Our lattice calculations, using RBC/UKQCD 2 + 1 flavor ensembles:

Transition	$m_Q$	$a$ [fm]	$m_\pi$ [MeV]	Reference
$\Lambda_b \rightarrow \Lambda$	$\infty$	0.083, 0.111	230–360	WD, DL, SM, MW, <a href="#">arXiv:1212.4827/PRD 2013</a>
$\Lambda_b \rightarrow p$	$\infty$	0.083, 0.111	230–360	WD, DL, SM, MW, <a href="#">arXiv:1306.0446/PRD 2013</a>
$\Lambda_b \rightarrow p$	phys.	0.083, 0.111	230–360	WD, CL, SM, <a href="#">arXiv:1503.01421/PRD 2015</a>
$\Lambda_b \rightarrow \Lambda_c$	phys.	0.083, 0.111	230–360	WD, CL, SM, <a href="#">arXiv:1503.01421/PRD 2015</a>
$\Lambda_b \rightarrow \Lambda$	phys.	0.083, 0.111	230–360	WD, SM, <a href="#">arXiv:1602.01399/PRD 2016</a>
$\Lambda_b \rightarrow \Lambda^*$	phys.	0.083, 0.111	300–430	SM, GR, <a href="#">arXiv:2009.09313</a>
$\Lambda_b \rightarrow \Lambda_c^*$	phys.	0.083, 0.111	300–430	SM, GR, in preparation
$\Lambda_c \rightarrow \Lambda$	phys.	0.083, 0.111, 0.114	140–360	SM, <a href="#">arXiv:1611.09696/PRL 2017</a>
$\Lambda_c \rightarrow p$	phys.	0.083, 0.111	230–360	SM, <a href="#">arXiv:1712.05783/PRD 2018</a>

# Forthcoming improved calculation of $\Lambda_b \rightarrow p, \Lambda, \Lambda_c$ form factors

- Remove data sets with  $m_{u,d}^{(\text{val})} < m_{u,d}^{(\text{sea})}$ , add **three new ensembles** to better control finite-volume effects, chiral and continuum extrapolations
- For  $\Lambda_b \rightarrow \Lambda$ : physical  $m_s^{(\text{val})}$
- More accurate tuning of charm and bottom actions
- All-mode-averaging for higher statistics
- Better source smearing
- Fully nonperturbative renormalization (?)

$N_s^3 \times N_t$	$\beta$	$am_{u,d}^{(\text{sea})}$	$am_{u,d}^{(\text{val})}$	$am_s^{(\text{sea})}$	$a$ (fm)	$m_\pi^{(\text{sea})}$ (MeV)	$m_\pi^{(\text{val})}$ (MeV)	Status
$32^3 \times 64$	2.13	0.005	0.005	0.04	$\approx 0.111$	$\approx 340$	$\approx 340$	done
$24^3 \times 64$	2.13	0.005	0.005	0.04	$\approx 0.111$	$\approx 340$	$\approx 340$	done
<del><math>24^3 \times 64</math></del>	<del>2.13</del>	<del>0.005</del>	<del>0.002</del>	<del>0.04</del>	<del><math>\approx 0.111</math></del>	<del><math>\approx 340</math></del>	<del><math>\approx 270</math></del>	
<del><math>24^3 \times 64</math></del>	<del>2.13</del>	<del>0.005</del>	<del>0.001</del>	<del>0.04</del>	<del><math>\approx 0.111</math></del>	<del><math>\approx 340</math></del>	<del><math>\approx 250</math></del>	
$48^3 \times 96$	2.13	0.00078	0.00078	0.0362	$\approx 0.114$	$\approx 140$	$\approx 140$	done
$32^3 \times 64$	2.25	0.006	0.006	0.03	$\approx 0.083$	$\approx 360$	$\approx 360$	done
$32^3 \times 64$	2.25	0.004	0.004	0.03	$\approx 0.083$	$\approx 300$	$\approx 300$	done
<del><math>32^3 \times 64</math></del>	<del>2.25</del>	<del>0.004</del>	<del>0.002</del>	<del>0.03</del>	<del><math>\approx 0.083</math></del>	<del><math>\approx 300</math></del>	<del><math>\approx 230</math></del>	
$48^3 \times 96$	2.31	0.002144	0.002144	0.02144	$\approx 0.073$	$\approx 230$	$\approx 230$	ongoing

$\Lambda_b \rightarrow \Lambda_c^*(\frac{1}{2}^-, \frac{3}{2}^-)$  form factor definitions

In the following we use the notation

$$\langle \Lambda_{c,1/2}^*(\mathbf{p}', s') | \bar{c} \Gamma b | \Lambda_b(\mathbf{p}, s) \rangle = \bar{u}(m_{\Lambda_{c,1/2}^*}, \mathbf{p}', s') \gamma_5 \mathcal{G}^{(\frac{1}{2}^-)}[\Gamma] u(m_{\Lambda_b}, \mathbf{p}, s),$$

$$\langle \Lambda_{c,3/2}^*(\mathbf{p}', s') | \bar{c} \Gamma b | \Lambda_b(\mathbf{p}, s) \rangle = \bar{u}_\lambda(m_{\Lambda_{c,3/2}^*}, \mathbf{p}', s') \mathcal{G}^{\lambda(\frac{3}{2}^-)}[\Gamma] u(m_{\Lambda_b}, \mathbf{p}, s)$$

and

$$s_\pm = (m_{\Lambda_b} \pm m_{\Lambda_c^*})^2 - q^2.$$

$\Lambda_b \rightarrow \Lambda_c^*(\frac{1}{2}^-, \frac{3}{2}^-)$  form factor definitions

$$\begin{aligned} \mathcal{G}^{(\frac{1}{2}^-)}[\gamma^\mu] &= f_0^{(\frac{1}{2}^-)} (m_{\Lambda_b} + m_{\Lambda_{c,1/2}^*}) \frac{q^\mu}{q^2} \\ &+ f_+^{(\frac{1}{2}^-)} \frac{m_{\Lambda_b} - m_{\Lambda_{c,1/2}^*}}{s_-} \left( p^\mu + p'^\mu - (m_{\Lambda_b}^2 - m_{\Lambda_{c,1/2}^*}^2) \frac{q^\mu}{q^2} \right) \\ &+ f_\perp^{(\frac{1}{2}^-)} \left( \gamma^\mu + \frac{2m_{\Lambda_{c,1/2}^*}}{s_-} p^\mu - \frac{2m_{\Lambda_b}}{s_-} p'^\mu \right), \end{aligned}$$

$$\begin{aligned} \mathcal{G}^{(\frac{1}{2}^-)}[\gamma^\mu \gamma_5] &= -g_0^{(\frac{1}{2}^-)} \gamma_5 (m_{\Lambda_b} - m_{\Lambda_{c,1/2}^*}) \frac{q^\mu}{q^2} \\ &- g_+^{(\frac{1}{2}^-)} \gamma_5 \frac{m_{\Lambda_b} + m_{\Lambda_{c,1/2}^*}}{s_+} \left( p^\mu + p'^\mu - (m_{\Lambda_b}^2 - m_{\Lambda_{c,1/2}^*}^2) \frac{q^\mu}{q^2} \right) \\ &- g_\perp^{(\frac{1}{2}^-)} \gamma_5 \left( \gamma^\mu - \frac{2m_{\Lambda_{c,1/2}^*}}{s_+} p^\mu - \frac{2m_{\Lambda_b}}{s_+} p'^\mu \right), \end{aligned}$$

$\Lambda_b \rightarrow \Lambda_c^*(\frac{1}{2}^-, \frac{3}{2}^-)$  form factor definitions

$$\begin{aligned} \mathcal{G}^{(\frac{1}{2}^-)}[i\sigma^{\mu\nu}q_\nu] &= -h_+^{(\frac{1}{2}^-)} \frac{q^2}{s_-} \left( p^\mu + p'^\mu - (m_{\Lambda_b}^2 - m_{\Lambda_{c,1/2}^*}^2) \frac{q^\mu}{q^2} \right) \\ &\quad - h_\perp^{(\frac{1}{2}^-)} (m_{\Lambda_b} - m_{\Lambda_{c,1/2}^*}) \left( \gamma^\mu + \frac{2m_{\Lambda_{c,1/2}^*}}{s_-} p^\mu - \frac{2m_{\Lambda_b}}{s_-} p'^\mu \right), \end{aligned}$$

$$\begin{aligned} \mathcal{G}^{(\frac{1}{2}^-)}[i\sigma^{\mu\nu}\gamma_5q_\nu] &= -\tilde{h}_+^{(\frac{1}{2}^-)} \gamma_5 \frac{q^2}{s_+} \left( p^\mu + p'^\mu - (m_{\Lambda_b}^2 - m_{\Lambda_{c,1/2}^*}^2) \frac{q^\mu}{q^2} \right) \\ &\quad - \tilde{h}_\perp^{(\frac{1}{2}^-)} \gamma_5 (m_{\Lambda_b} + m_{\Lambda_{c,1/2}^*}) \left( \gamma^\mu - \frac{2m_{\Lambda_{c,1/2}^*}}{s_+} p^\mu - \frac{2m_{\Lambda_b}}{s_+} p'^\mu \right). \end{aligned}$$

$\Lambda_b \rightarrow \Lambda_c^*(\frac{1}{2}^-, \frac{3}{2}^-)$  form factor definitions

$$\begin{aligned}
 \mathcal{G}^{\lambda(\frac{3}{2}^-)}[\gamma^\mu] &= f_0^{(\frac{3}{2}^-)} \frac{m_{\Lambda_c^*}}{s_+} \frac{(m_{\Lambda_b} - m_{\Lambda_c^*}) p^\lambda q^\mu}{q^2} \\
 &+ f_+^{(\frac{3}{2}^-)} \frac{m_{\Lambda_c^*}}{s_-} \frac{(m_{\Lambda_b} + m_{\Lambda_c^*}) p^\lambda (q^2(p^\mu + p'^\mu) - (m_{\Lambda_b}^2 - m_{\Lambda_c^*}^2) q^\mu)}{q^2 s_+} \\
 &+ f_\perp^{(\frac{3}{2}^-)} \frac{m_{\Lambda_c^*}}{s_-} \left( p^\lambda \gamma^\mu - \frac{2 p^\lambda (m_{\Lambda_b} p'^\mu + m_{\Lambda_c^*} p^\mu)}{s_+} \right) \\
 &+ f_{\perp'}^{(\frac{3}{2}^-)} \frac{m_{\Lambda_c^*}}{s_-} \left( p^\lambda \gamma^\mu - \frac{2 p^\lambda p'^\mu}{m_{\Lambda_c^*}} + \frac{2 p^\lambda (m_{\Lambda_b} p'^\mu + m_{\Lambda_c^*} p^\mu)}{s_+} + \frac{s_- g^{\lambda\mu}}{m_{\Lambda_c^*}} \right),
 \end{aligned}$$

$$\begin{aligned}
 \mathcal{G}^{\lambda(\frac{3}{2}^-)}[\gamma^\mu \gamma_5] &= -g_0^{(\frac{3}{2}^-)} \gamma_5 \frac{m_{\Lambda_c^*}}{s_-} \frac{(m_{\Lambda_b} + m_{\Lambda_c^*}) p^\lambda q^\mu}{q^2} \\
 &- g_+^{(\frac{3}{2}^-)} \gamma_5 \frac{m_{\Lambda_c^*}}{s_+} \frac{(m_{\Lambda_b} - m_{\Lambda_c^*}) p^\lambda (q^2(p^\mu + p'^\mu) - (m_{\Lambda_b}^2 - m_{\Lambda_c^*}^2) q^\mu)}{q^2 s_-} \\
 &- g_\perp^{(\frac{3}{2}^-)} \gamma_5 \frac{m_{\Lambda_c^*}}{s_+} \left( p^\lambda \gamma^\mu - \frac{2 p^\lambda (m_{\Lambda_b} p'^\mu - m_{\Lambda_c^*} p^\mu)}{s_-} \right) \\
 &- g_{\perp'}^{(\frac{3}{2}^-)} \gamma_5 \frac{m_{\Lambda_c^*}}{s_+} \left( p^\lambda \gamma^\mu + \frac{2 p^\lambda p'^\mu}{m_{\Lambda_c^*}} + \frac{2 p^\lambda (m_{\Lambda_b} p'^\mu - m_{\Lambda_c^*} p^\mu)}{s_-} - \frac{s_+ g^{\lambda\mu}}{m_{\Lambda_c^*}} \right),
 \end{aligned}$$



$\Lambda_b \rightarrow \Lambda_c^*(\frac{1}{2}^-, \frac{3}{2}^-)$  form factor definitions

$$\begin{aligned} \mathcal{G}^{\lambda(\frac{3}{2}^-)}[i\sigma^{\mu\nu}q_\nu] &= -h_+^{(\frac{3}{2}^-)} \frac{m_{\Lambda_c^*,3/2}^*}{s_-} \frac{p^\lambda(q^2(p^\mu + p'^\mu) - (m_{\Lambda_b}^2 - m_{\Lambda_c^*,3/2}^2)q^\mu)}{s_+} \\ &\quad - h_\perp^{(\frac{3}{2}^-)} \frac{m_{\Lambda_c^*,3/2}^*}{s_-} (m_{\Lambda_b} + m_{\Lambda_c^*,3/2}^*) \left( p^\lambda \gamma^\mu - \frac{2p^\lambda(m_{\Lambda_b} p'^\mu + m_{\Lambda_c^*,3/2}^* p^\mu)}{s_+} \right) \\ &\quad - h_{\perp'}^{(\frac{3}{2}^-)} \frac{m_{\Lambda_c^*,3/2}^*}{s_-} (m_{\Lambda_b} + m_{\Lambda_c^*,3/2}^*) \left( p^\lambda \gamma^\mu - \frac{2p^\lambda p'^\mu}{m_{\Lambda_c^*,3/2}^*} + \frac{2p^\lambda(m_{\Lambda_b} p'^\mu + m_{\Lambda_c^*,3/2}^* p^\mu)}{s_+} + \frac{s_- g^{\lambda\mu}}{m_{\Lambda_c^*,3/2}^*} \right), \end{aligned}$$

$$\begin{aligned} \mathcal{G}^{\lambda(\frac{3}{2}^-)}[i\sigma^{\mu\nu}q_\nu\gamma_5] &= -\tilde{h}_+^{(\frac{3}{2}^-)} \gamma_5 \frac{m_{\Lambda_c^*,3/2}^*}{s_+} \frac{p^\lambda(q^2(p^\mu + p'^\mu) - (m_{\Lambda_b}^2 - m_{\Lambda_c^*,3/2}^2)q^\mu)}{s_-} \\ &\quad - \tilde{h}_\perp^{(\frac{3}{2}^-)} \gamma_5 \frac{m_{\Lambda_c^*,3/2}^*}{s_+} (m_{\Lambda_b} - m_{\Lambda_c^*,3/2}^*) \left( p^\lambda \gamma^\mu - \frac{2p^\lambda(m_{\Lambda_b} p'^\mu - m_{\Lambda_c^*,3/2}^* p^\mu)}{s_-} \right) \\ &\quad - \tilde{h}_{\perp'}^{(\frac{3}{2}^-)} \gamma_5 \frac{m_{\Lambda_c^*,3/2}^*}{s_+} (m_{\Lambda_b} - m_{\Lambda_c^*,3/2}^*) \left( p^\lambda \gamma^\mu + \frac{2p^\lambda p'^\mu}{m_{\Lambda_c^*,3/2}^*} + \frac{2p^\lambda(m_{\Lambda_b} p'^\mu - m_{\Lambda_c^*,3/2}^* p^\mu)}{s_-} - \frac{s_+ g^{\lambda\mu}}{m_{\Lambda_c^*,3/2}^*} \right). \end{aligned}$$