

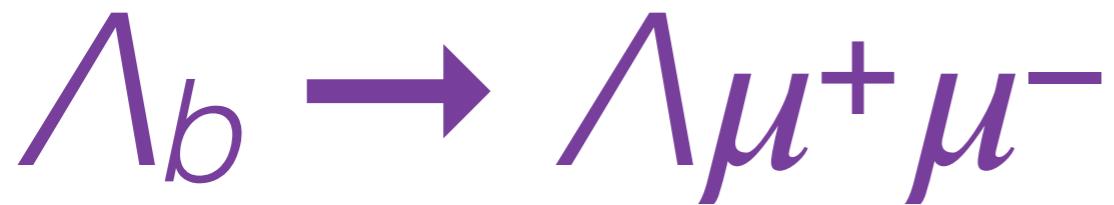
# Review of results on $\Lambda_b \rightarrow \Lambda\mu^+\mu^-$ and $\Lambda_b \rightarrow J/\psi\Lambda$

T. Blake

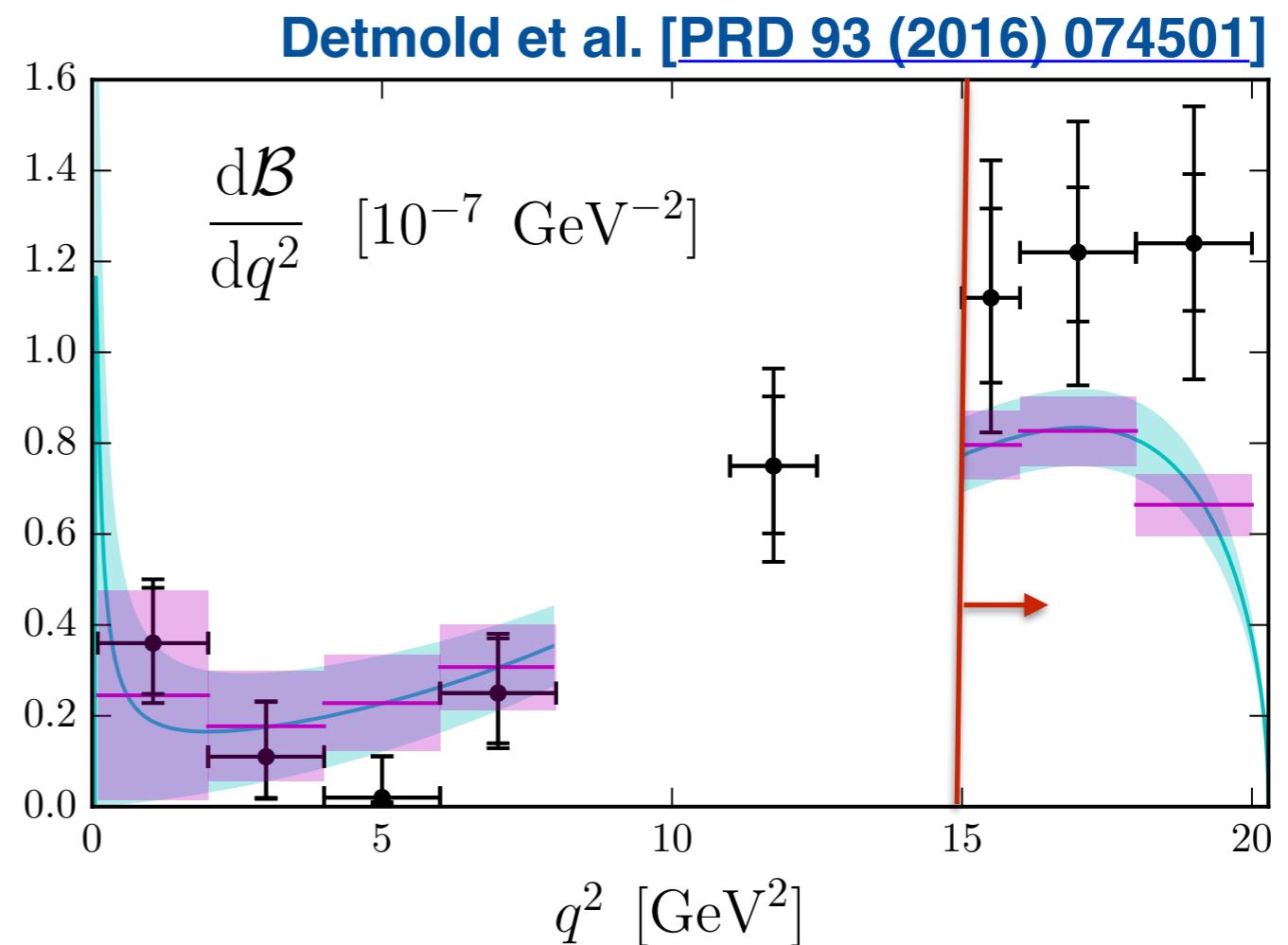


**b-baryon Fest**  
5-6th of November 2020





- Qualitatively different situation to the  $B$  meson decay measurements:
  - Baryonic decay.
  - $\Lambda_b$  can be polarised.
  - $\Lambda$  decays weakly.
  - Signal is predominantly seen at large  $q^2$ .



**Data from LHCb**  
[\[JHEP 06 \(2015\) 115\]](#)  
[\[Erratum: JHEP 09 \(2018\) 145\]](#)

# $\Lambda_b \rightarrow \Lambda \mu^+ \mu^-$ amplitudes

- In the massless limit, the decay is described by 8 complex amplitudes:

Left-right-handed chirality  
of dilepton system

$$A_{\perp 0}^{L(R)} = +\sqrt{2}N\sqrt{s_-}\frac{m_{\Lambda_b} + m_\Lambda}{\sqrt{q^2}} \left[ C_{9,10,+}^{L(R)} f_0^V + \frac{2m_b(C_7 + C_{7'})}{m_{\Lambda_b} + m_\Lambda} f_0^T + \left(\frac{4}{3}C_1 + C_2\right) r_{\perp 0} \right]$$

$$A_{\parallel 0}^{L(R)} = -\sqrt{2}N\sqrt{s_+}\frac{m_{\Lambda_b} - m_\Lambda}{\sqrt{q^2}} \left[ C_{9,10,-}^{L(R)} f_0^A + \frac{2m_b(C_7 - C_{7'})}{m_{\Lambda_b} - m_\Lambda} f_0^{T5} + \left(\frac{4}{3}C_1 + C_2\right) r_{\parallel 0} \right]$$

$$A_{\perp 1}^{L(R)} = -2N\sqrt{s_-} \left[ C_{9,10,+}^{L(R)} f_\perp^V + \frac{2m_b(m_{\Lambda_b} + m_\Lambda)(C_7 + C_{7'})}{q^2} f_\perp^T + \left(\frac{4}{3}C_1 + C_2\right) r_{\perp 1} \right]$$

$$A_{\parallel 1}^{L(R)} = +2N\sqrt{s_+} \left[ C_{9,10,+}^{L(R)} f_\perp^A + \frac{2m_b(m_{\Lambda_b} - m_\Lambda)(C_7 - C_{7'})}{q^2} f_\perp^{T5} + \left(\frac{4}{3}C_1 + C_2\right) r_{\parallel 1} \right]$$

Spin of dilepton system

Transversity basis ( $\parallel$  corresponds to  $\langle \Lambda | \bar{s} \gamma^\mu b | \Lambda_b \rangle$  and  $\perp$  to  $\langle \Lambda | \bar{s} \gamma^\mu \gamma^5 b | \Lambda_b \rangle$ )

see e.g. Böer et al. [\[JHEP 01 \(2015\) 155\]](#)

# $\Lambda_b \rightarrow \Lambda \mu^+ \mu^-$ amplitudes

- In the massless limit, the decay is described by 8 complex amplitudes:

$$\begin{aligned}
 A_{\perp 0}^{L(R)} &= +\sqrt{2}N\sqrt{s_-} \frac{m_{\Lambda_b} + m_\Lambda}{\sqrt{q^2}} \left[ C_{9,10,+}^{L(R)} f_0^V + \frac{2m_b(C_7 + C_{7'})}{m_{\Lambda_b} + m_\Lambda} f_0^T + \left( \frac{4}{3}C_1 + C_2 \right) r_{\perp 0} \right] \\
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 \end{aligned}$$

Short distance contributions

$$C_{9,10,\pm}^{\text{L,R}} = (C_9 \mp C_{10}) \pm (C'_9 \mp C'_{10})$$

see e.g. Böer et al. [\[JHEP 01 \(2015\) 155\]](#)

# $\Lambda_b \rightarrow \Lambda \mu^+ \mu^-$ amplitudes

- In the massless limit, the decay is described by 8 complex amplitudes:

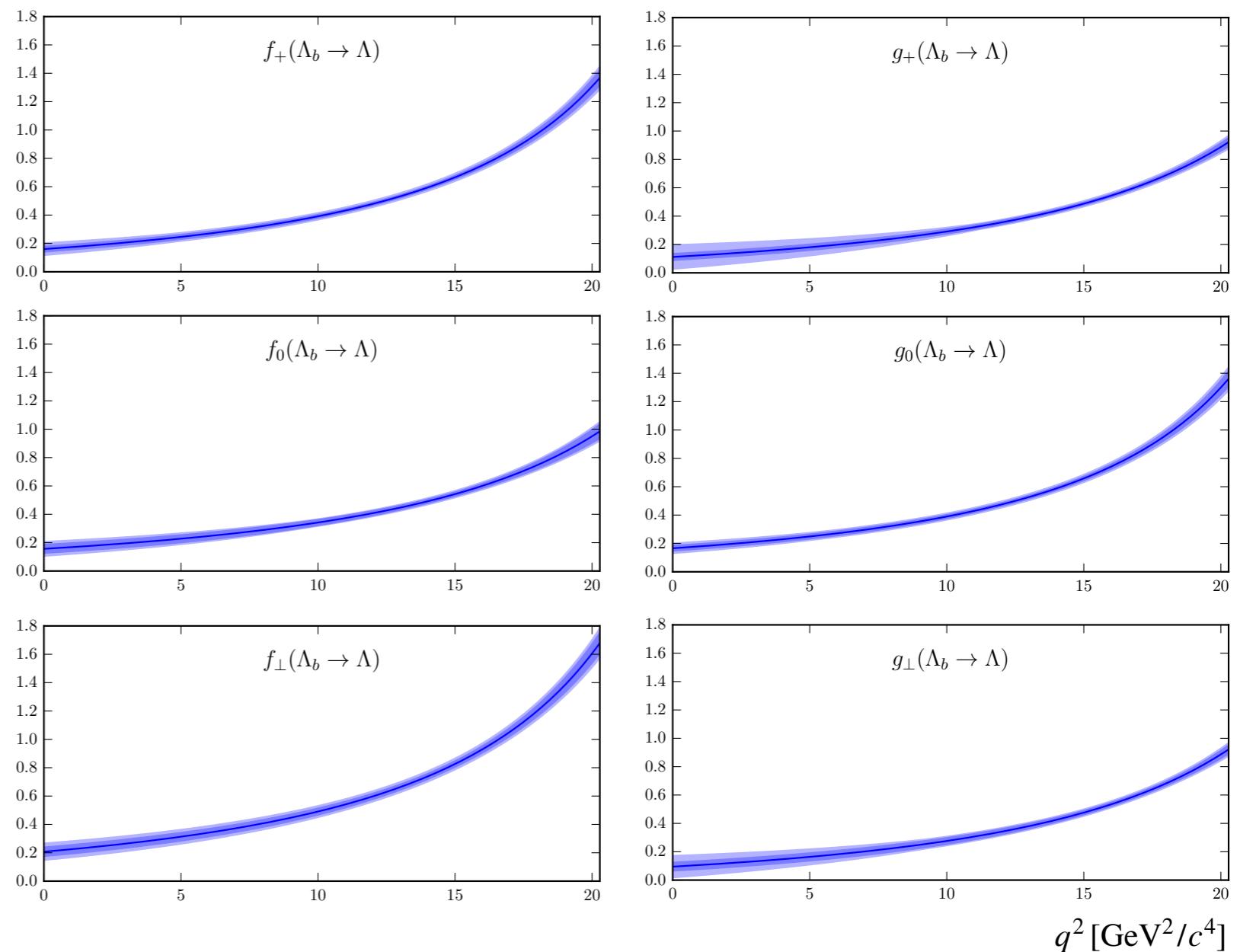
Form-factors from lattice  
 Detmold et al. [\[PRD 93 \(2016\) 074501\]](#)

$$\begin{aligned}
 A_{\perp 0}^{L(R)} &= +\sqrt{2}N\sqrt{s_-}\frac{m_{\Lambda_b} + m_\Lambda}{\sqrt{q^2}} \left[ C_{9,10,+}^{L(R)} f_0^V + \frac{2m_b(C_7 + C_{7'})}{m_{\Lambda_b} + m_\Lambda} f_0^T + \left(\frac{4}{3}C_1 + C_2\right) r_{\perp 0} \right] \\
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 \end{aligned}$$

see e.g. Böer et al. [\[JHEP 01 \(2015\) 155\]](#)

# $\Lambda_b \rightarrow \Lambda$ form factors

- Form-factors are determined with impressive precision from the lattice.  
Detmold et al.  
[\*\*\[PRD 93 \(2016\) 074501\]\*\*](#)
- Extrapolated to full  $q^2$  range using a  $z$ -expansion.



# $\Lambda_b \rightarrow \Lambda \mu^+ \mu^-$ amplitudes

- In the massless limit, the decay is described by 8 complex amplitudes:

Power corrections

$$A_{\perp 0}^{L(R)} = +\sqrt{2}N\sqrt{s_-} \frac{m_{\Lambda_b} + m_\Lambda}{\sqrt{q^2}} \left[ C_{9,10,+}^{L(R)} f_0^V + \frac{2m_b(C_7 + C_{7'})}{m_{\Lambda_b} + m_\Lambda} f_0^T + \left( \frac{4}{3}C_1 + C_2 \right) r_{\perp 0} \right]$$

$$A_{\parallel 0}^{L(R)} = -\sqrt{2}N\sqrt{s_+} \frac{m_{\Lambda_b} - m_\Lambda}{\sqrt{q^2}} \left[ C_{9,10,-}^{L(R)} f_0^A + \frac{2m_b(C_7 - C_{7'})}{m_{\Lambda_b} - m_\Lambda} f_0^{T5} + \left( \frac{4}{3}C_1 + C_2 \right) r_{\parallel 0} \right]$$

$$A_{\perp 1}^{L(R)} = -2N\sqrt{s_-} \left[ C_{9,10,+}^{L(R)} f_\perp^V + \frac{2m_b(m_{\Lambda_b} + m_\Lambda)(C_7 + C_{7'})}{q^2} f_\perp^T + \left( \frac{4}{3}C_1 + C_2 \right) r_{\perp 1} \right]$$

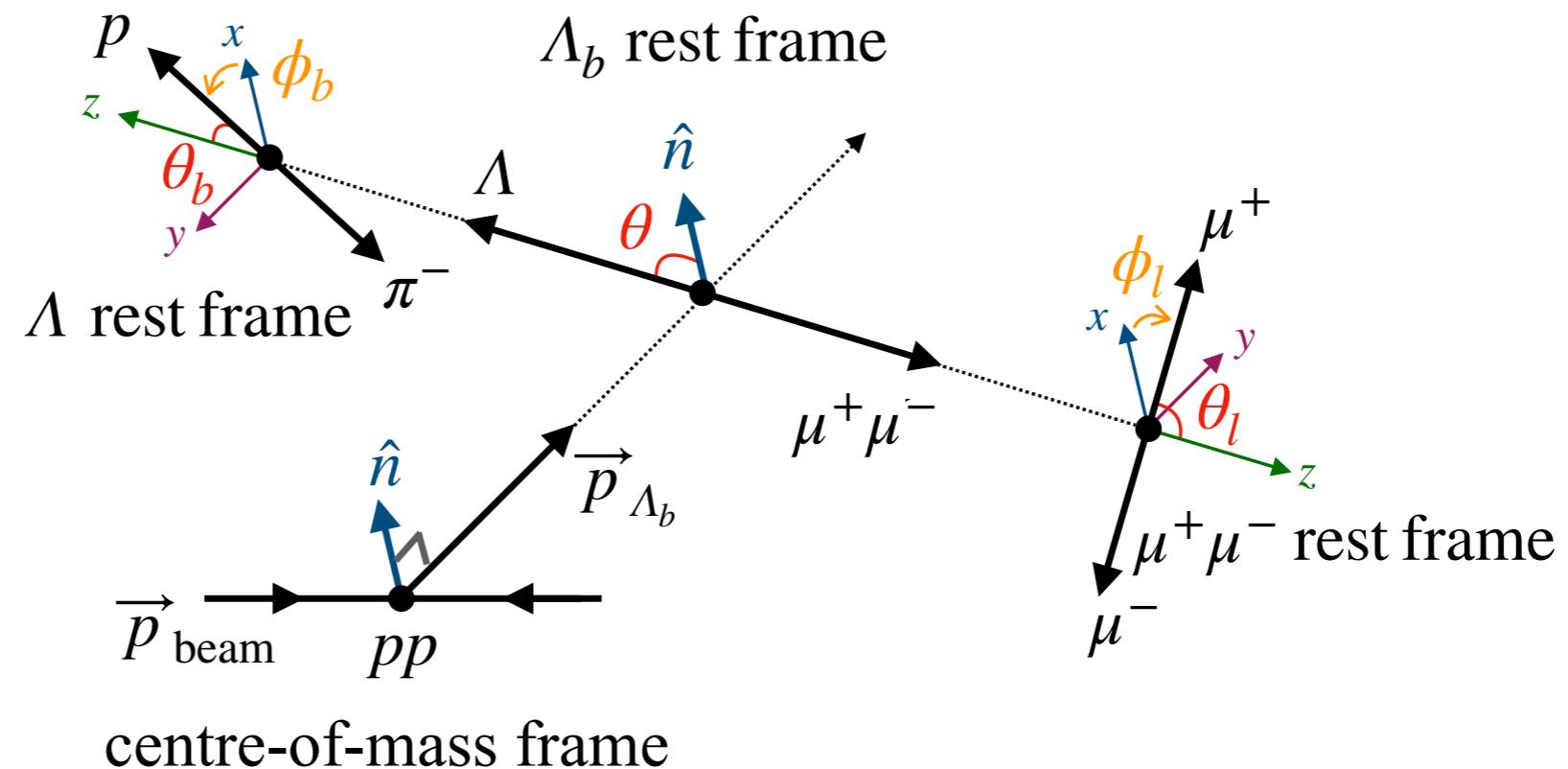
$$A_{\parallel 1}^{L(R)} = +2N\sqrt{s_+} \left[ C_{9,10,+}^{L(R)} f_\perp^A + \frac{2m_b(m_{\Lambda_b} - m_\Lambda)(C_7 - C_{7'})}{q^2} f_\perp^{T5} + \left( \frac{4}{3}C_1 + C_2 \right) r_{\parallel 1} \right]$$

Assume prior of  $0.00 \pm 0.03$

see e.g. Böer et al. [\[JHEP 01 \(2015\) 155\]](#)

# $\Lambda_b \rightarrow \Lambda \mu^+ \mu^-$ angular distribution

- In general can be parameterised by 5 angles:



# $\Lambda_b \rightarrow \Lambda \mu^+ \mu^-$ angular distribution

- Unpolarised case:

$$\frac{d^4}{dq^2 d\vec{\Omega}} = \frac{3}{8\pi} \sum_i K_i f_i(\cos \theta_b, \cos \theta_l, \phi) \quad \text{Depend on products of transversely amplitudes}$$

Böer et al. [\[JHEP 01 \(2015\) 155\]](#)

- Depends on 3 decay angles ( $\phi = \phi_l + \phi_b$ ).
- Ten observables.
- Observables also depend on the  $\Lambda$  asymmetry parameter  $\Lambda$ .

# $\Lambda_b \rightarrow \Lambda \mu^+ \mu^-$ angular distribution

- Generalisation to the polarised case:

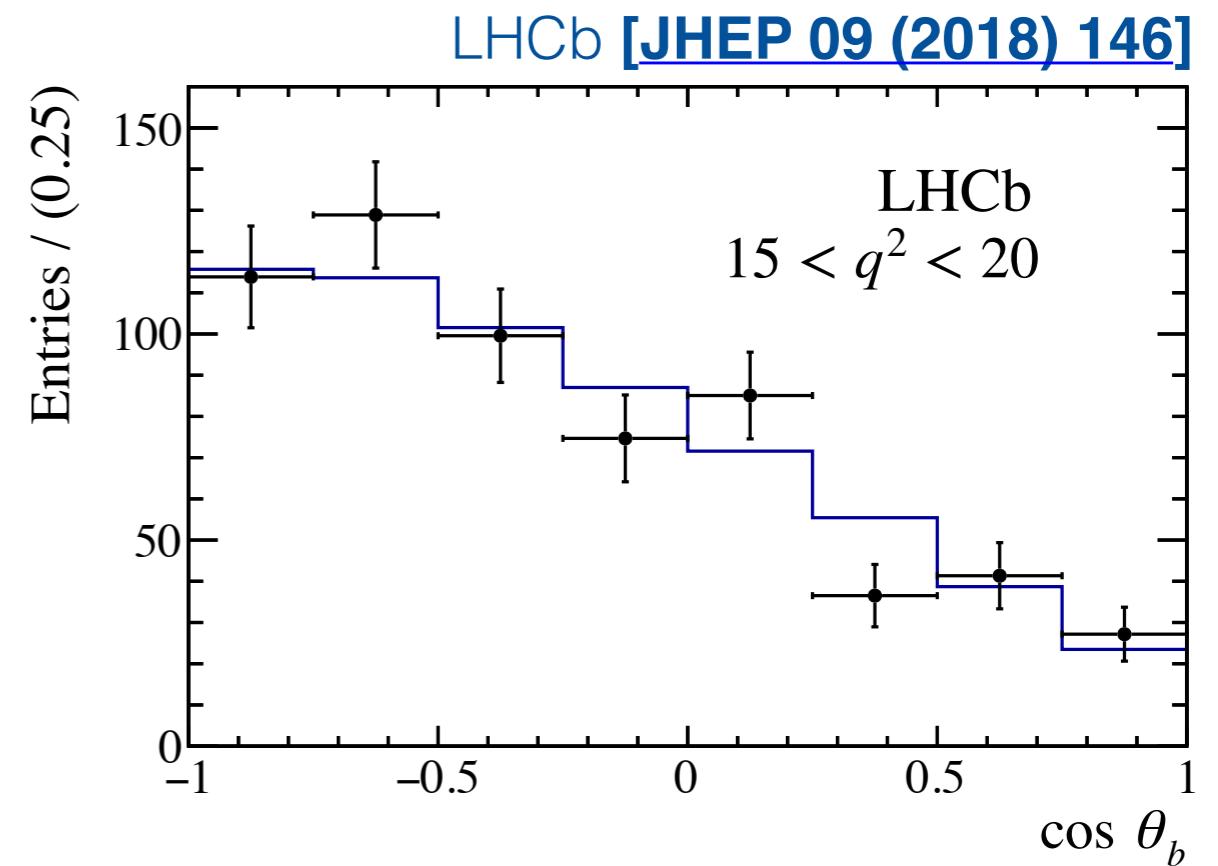
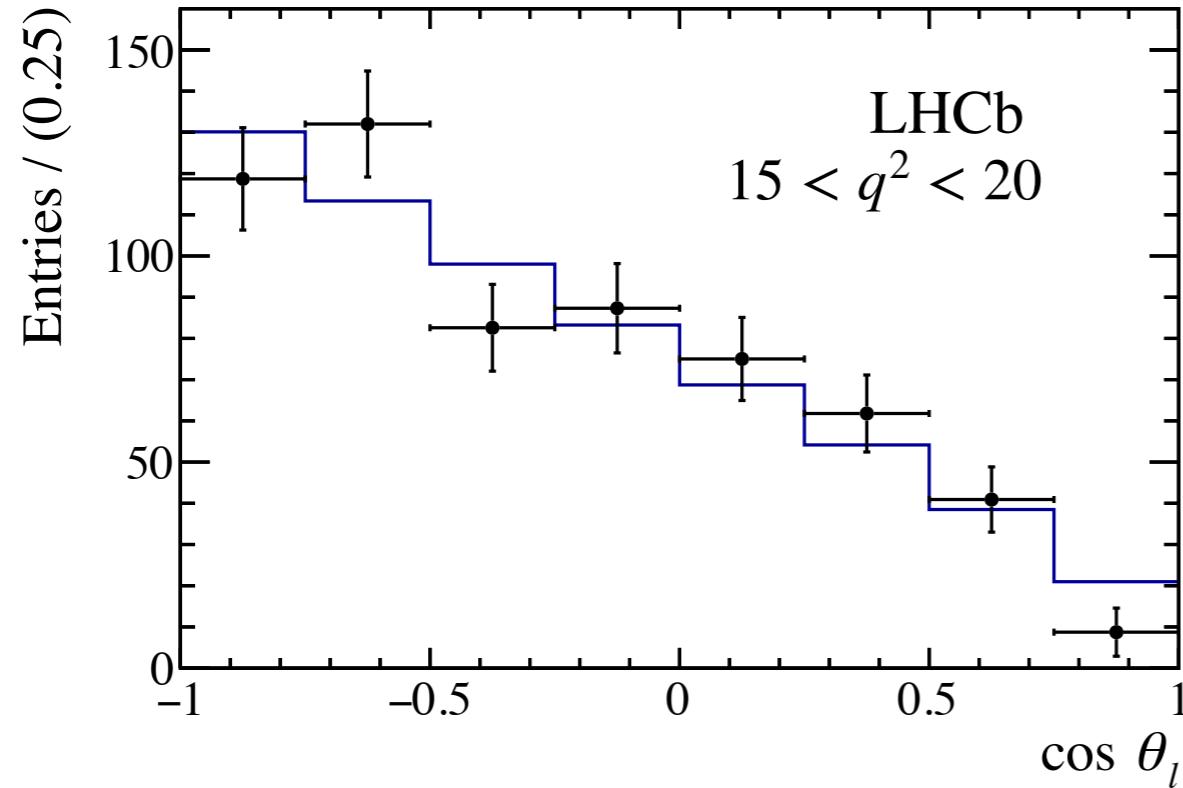
$$\frac{d^6}{dq^2 d\vec{\Omega}} = \frac{3}{32\pi^2} \sum_i K_i f_i(\cos \theta_b, \phi_b, \cos \theta_l, \phi_l, \cos \theta)$$

Depend on products of transversely amplitudes

Blake et al. [\[JHEP 11 \(2017\) 138\]](#)

- Depends on 5 decay angles.
- 34 observables  
(the 24 new observables are proportional to the polarisation).

# Angular distribution



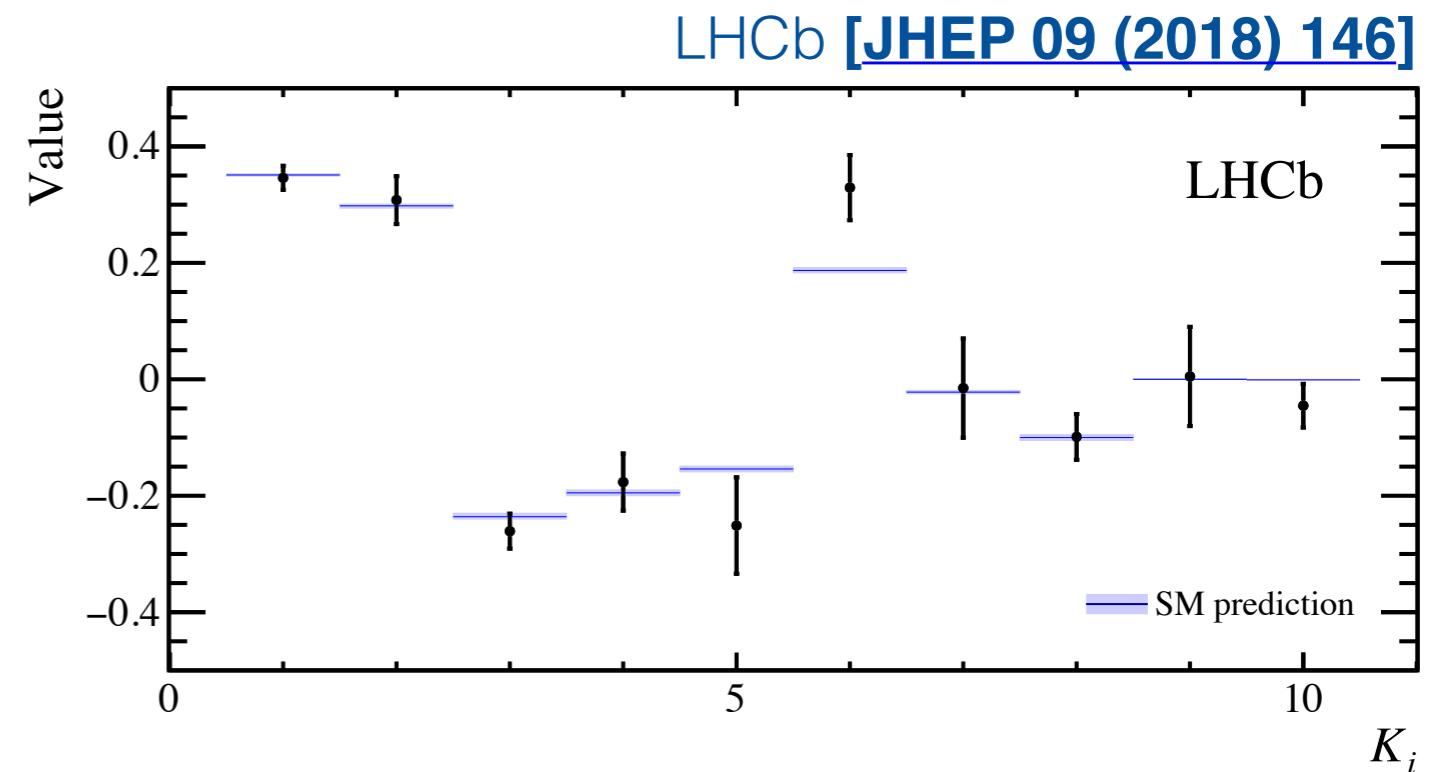
- Get large forward-backward asymmetries in  $\cos \theta_l$  and in  $\cos \theta_b$  (due to the weak decay of the  $\Lambda$  baryon):

$$A_{\text{FB}}^l = -0.39 \pm 0.04 \pm 0.01$$

$$A_{\text{FB}}^b = -0.30 \pm 0.05 \pm 0.02$$

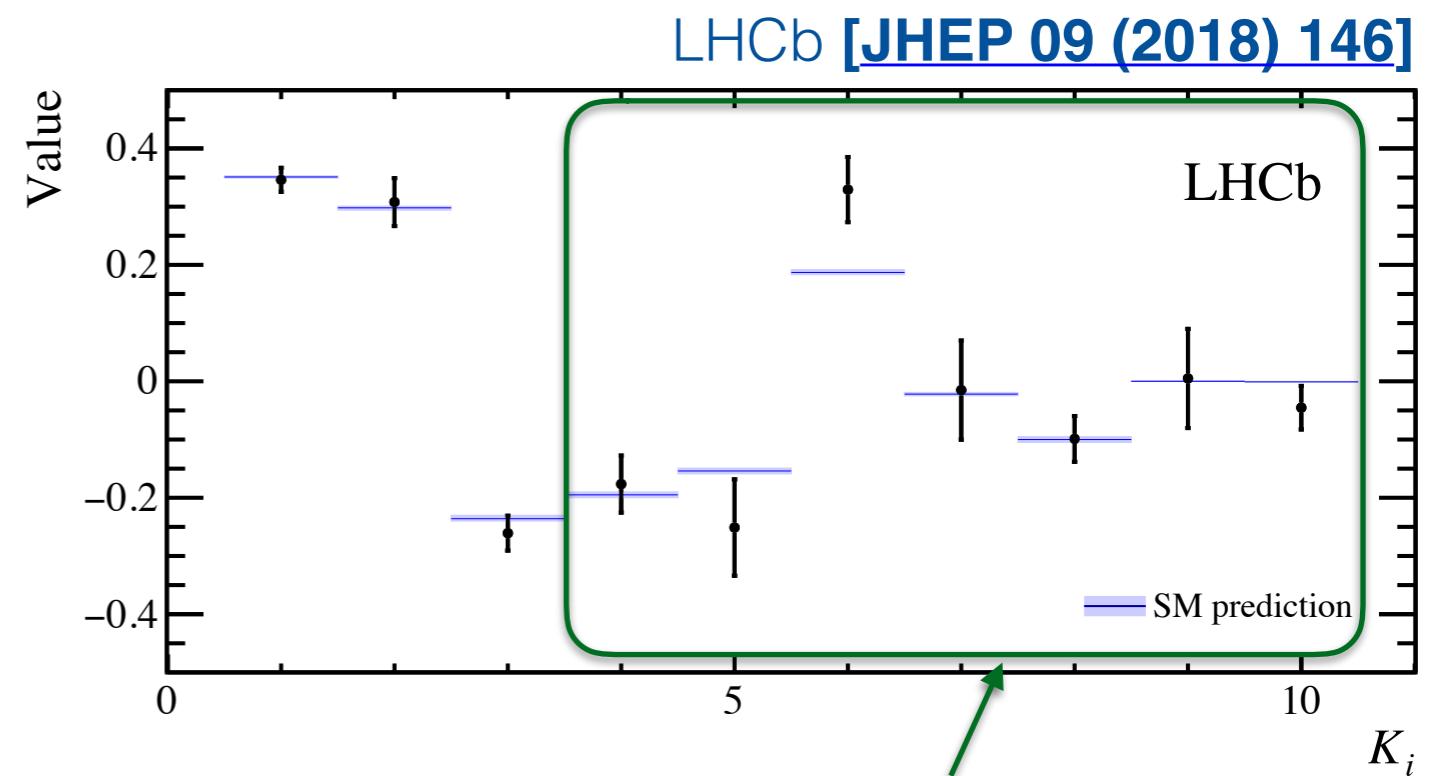
# Angular observables

- Determine observables using a moment analysis in  $15 < q^2 < 20 \text{ GeV}^2/c^4$
- Data are consistent with SM predictions and consistent with zero production polarisation.



# Angular observables

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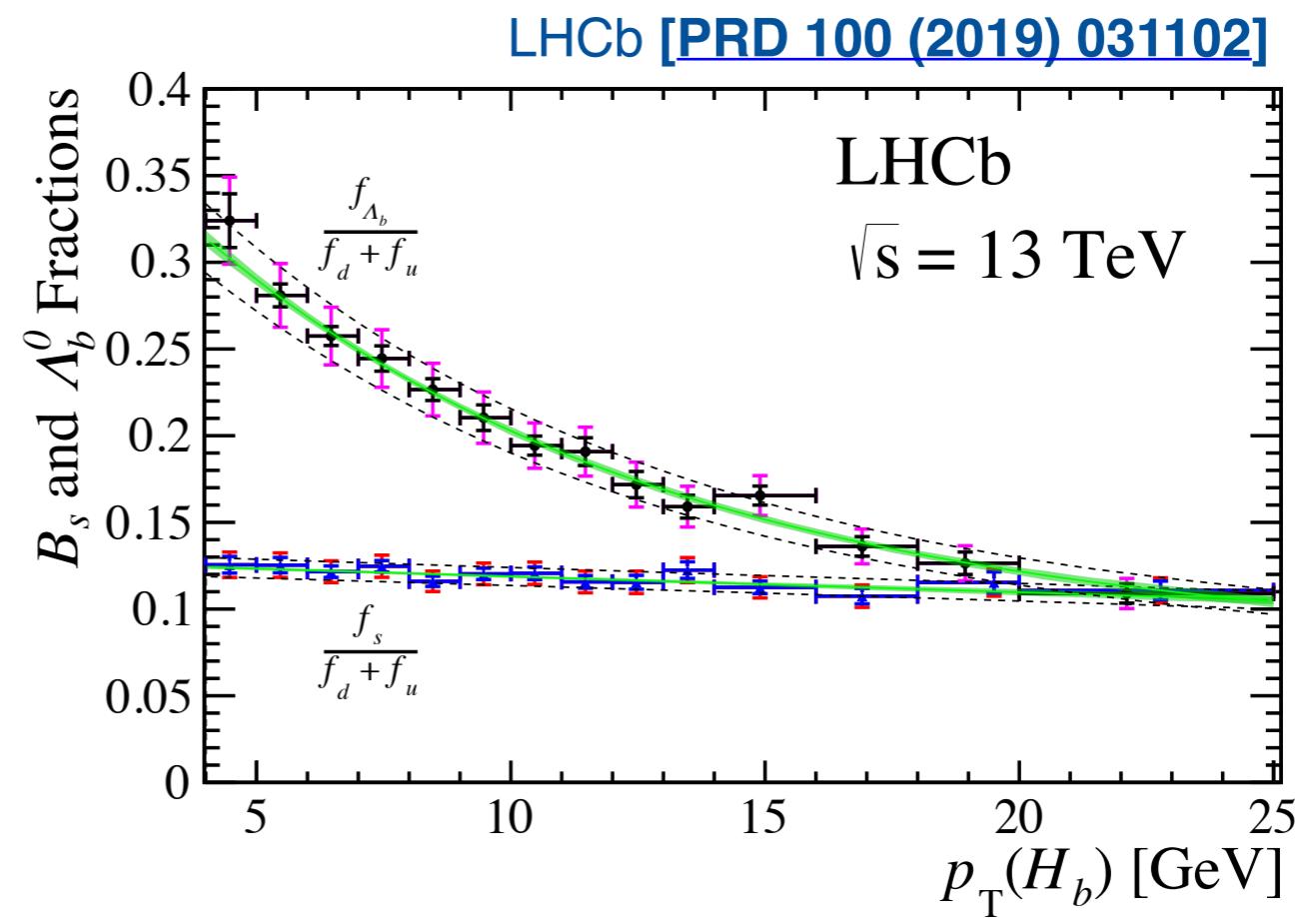


Note, SM predictions need to be updated to account for a change in the  $\Lambda$  asymmetry parameter from  $\alpha_\Lambda = 0.642 \pm 0.013$  to  $\alpha_\Lambda = 0.750 \pm 0.010$

c.f. BES III [Nature Phys. 15 (2019) 631–634]

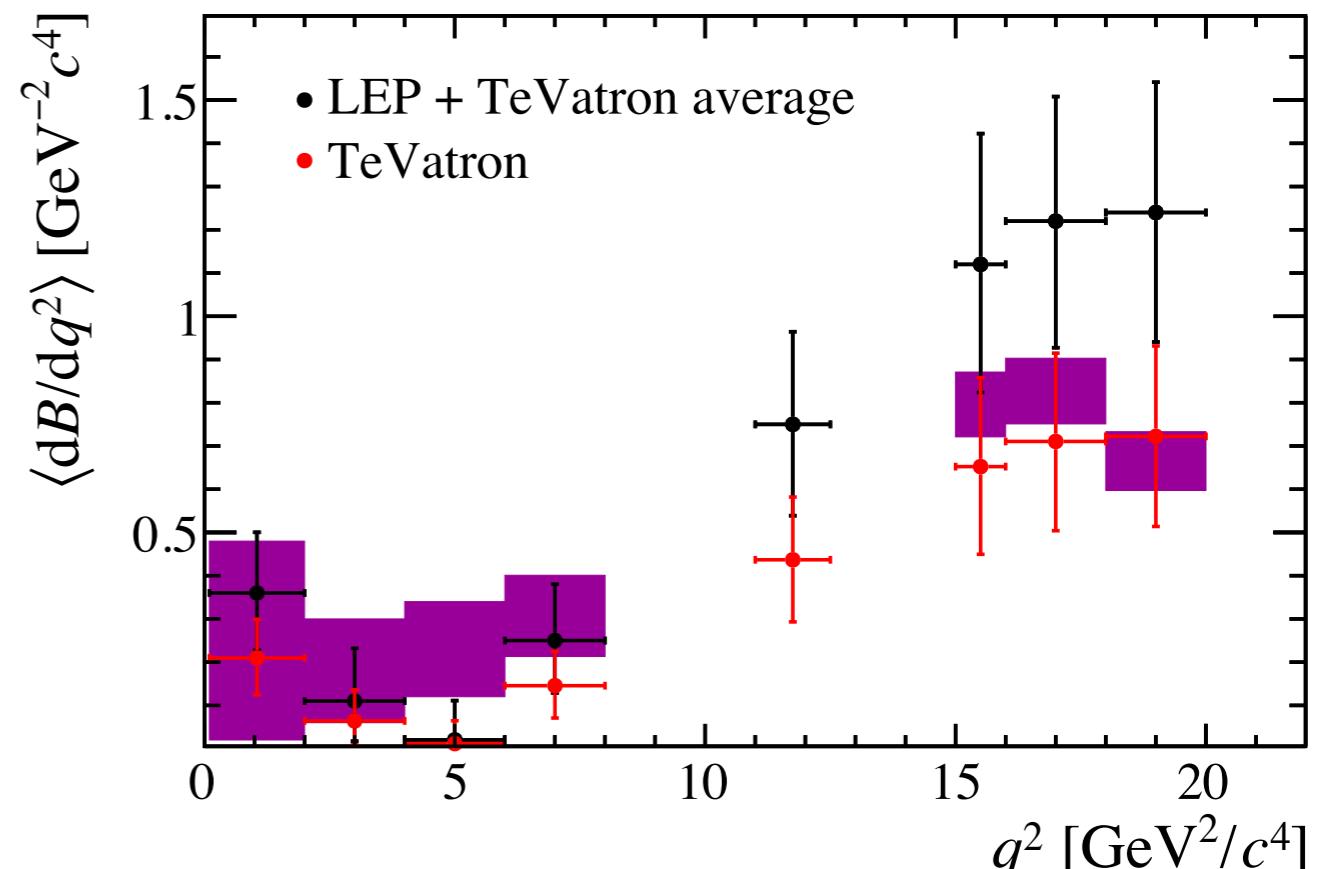
# $\Lambda_b \rightarrow \Lambda \mu^+ \mu^-$ branching fraction

- Existing branching fraction measurement uses CDF/D0 average of  $f_{\Lambda_b} \times \mathcal{B}(\Lambda_b \rightarrow J/\psi \Lambda) = (5.8 \pm 0.8) \times 10^{-5}$ , with  $f_{\Lambda_b}$  taken as a LEP + TeVatron average.
- Now know that the baryon production fractions exhibit a strong  $p_T$  dependences in  $pp$  collisions.
- $\Lambda_b$  baryons are produced with lower average  $p_T$  at the TeVatron than LEP.



# $\Lambda_b \rightarrow \Lambda \mu^+ \mu^-$ branching fraction

- Re-evaluating the branching fraction using only TeVatron inputs on  $f(b \rightarrow \text{baryon})$  significantly changes the picture.
- Ultimately want to re-measure the branching fraction using  $\mathcal{B}(B^0 \rightarrow J/\psi K_S)$  and the  $f_{\Lambda_b}/f_d$  production fraction at the LHC (this is ongoing).



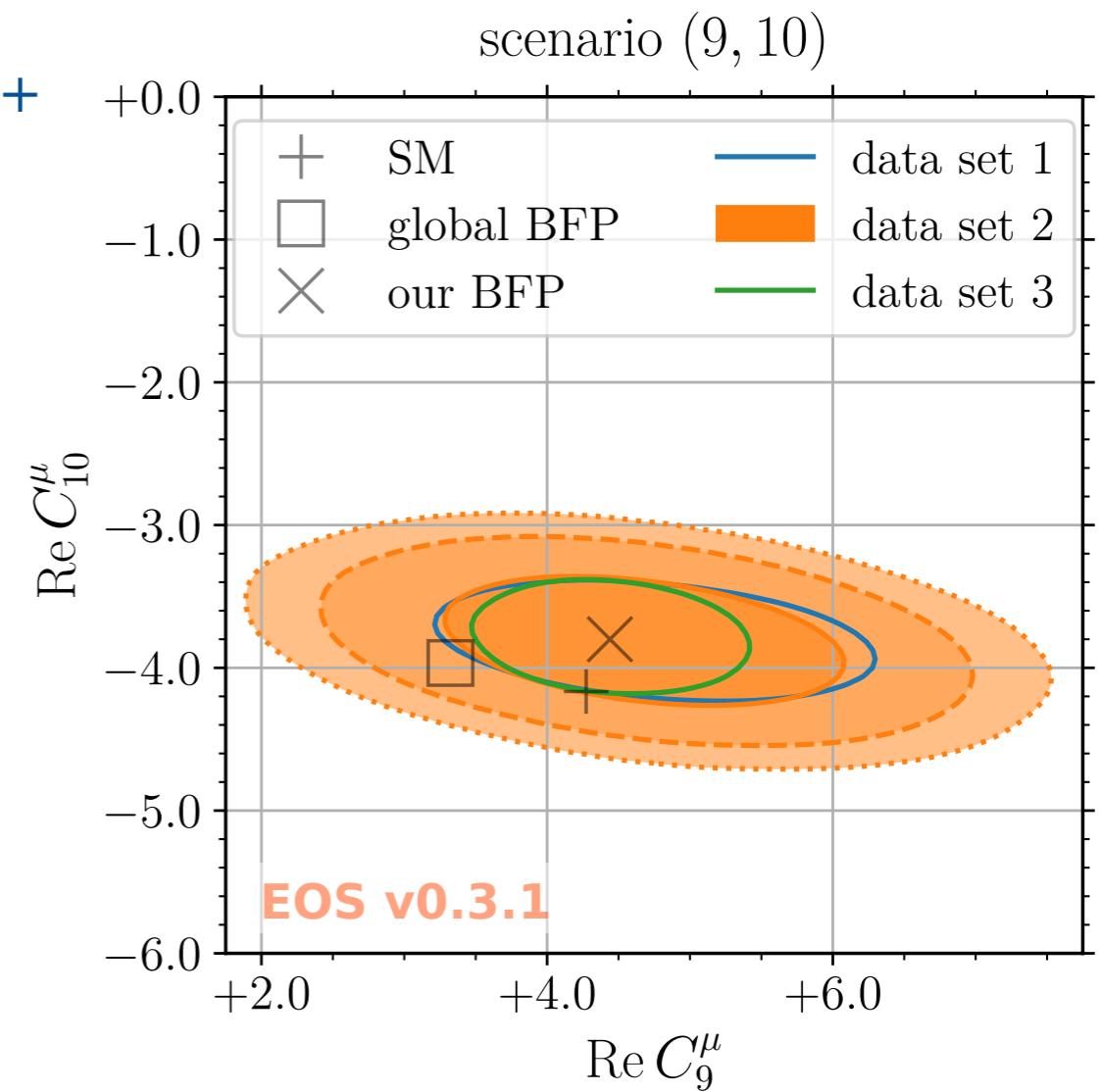
Data LHCb [\[JHEP 06 \(2015\) 115\]](#)

SM Detmold et al. [\[PRD 93 \(2016\) 074501\]](#)

# Bayesian analysis of $\Lambda_b \rightarrow \Lambda\mu^+\mu^-$

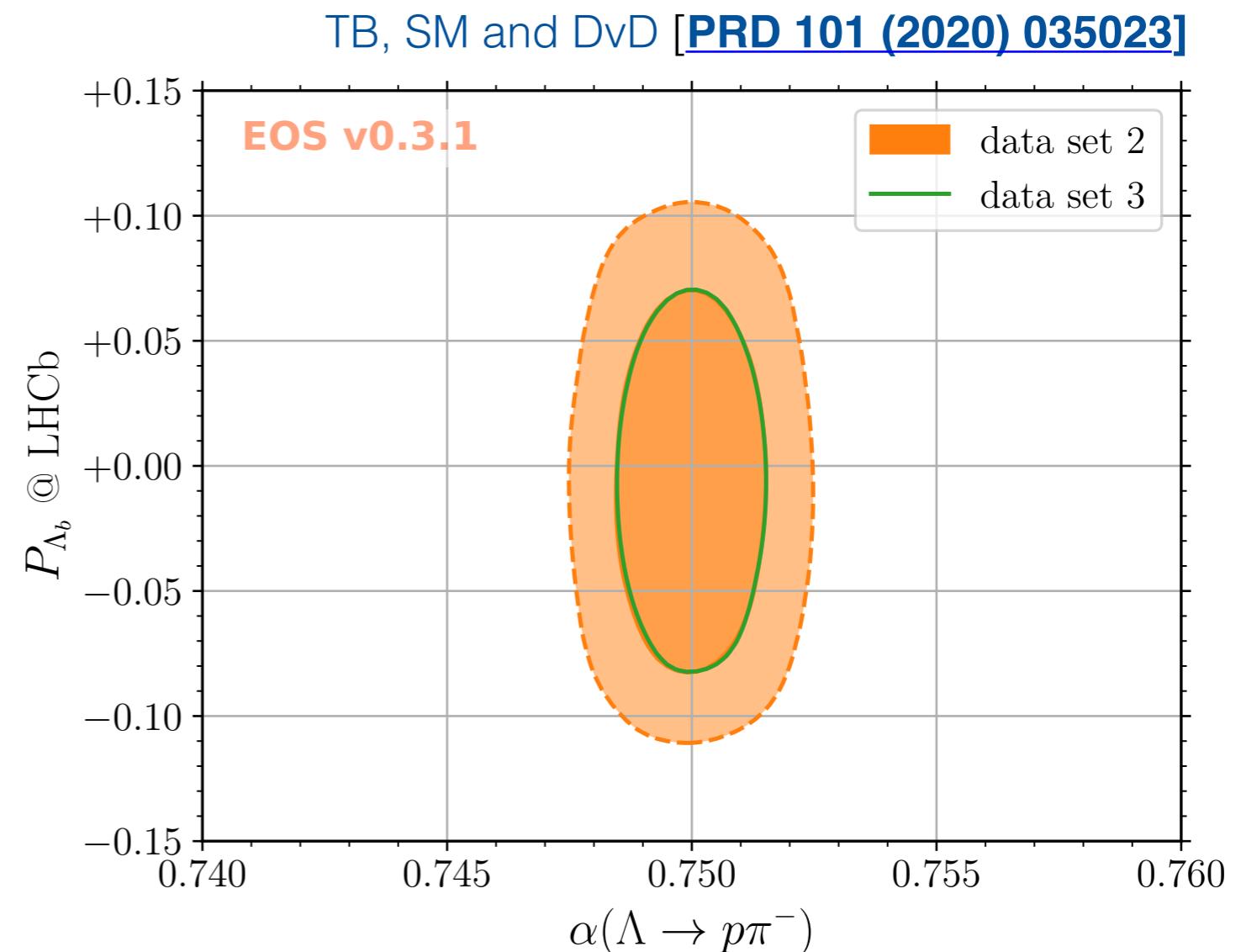
- Determine the Wilson coefficients using a Bayesian analysis.
- Try three scenarios:
  - ATLAS, CMS & LHCb  $\mathcal{B}(B_s \rightarrow \mu^+\mu^-) +$  unpolarised  $\Lambda\mu^+\mu^-$  angular observables.
  - + Polarised angular observables.
  - + Updated branching fraction.
- SM point has good p-value.
- Data are consistent with both the best-fit point and the point favoured by  $B$  meson decays.

TB, SM and DvD [[PRD 101 \(2020\) 035023](#)]



# Bayesian analysis of $\Lambda_b \rightarrow \Lambda\mu^+\mu^-$

- Can also determine polarisation from the moments assuming no  $\sqrt{s}$  dependence.
- Result is compatible with zero production polarisation.



# $\Lambda_b \rightarrow J/\psi \Lambda$ angular distribution

- Described by four helicity amplitudes,  $H_{\lambda_\Lambda, \lambda_\psi}$ , the  $\Lambda_b$  production polarisation,  $P_b$ , and the  $\Lambda$  asymmetry parameter,  $\alpha_\Lambda$ .
- Use the convention:

$$a_- = H_{-1/2, 0}$$

$$a_+ = H_{+1/2, 0}$$

$$b_- = H_{+1/2, +1}$$

$$b_+ = H_{-1/2, -1}$$

see e.g.: Hrivnac et al.  
[\[J.Phys. G21 \(1995\) 629-638\]](#)

Moments	Amplitude dependence
$M_1$	$\frac{1}{4}(2 a_+ ^2 + 2 a_- ^2 +  b_+ ^2 +  b_- ^2)$
$M_2$	$\frac{1}{2}( b_+ ^2 +  b_- ^2)$
$M_4$	$\frac{\alpha}{4}( b_- ^2 -  b_+ ^2 + 2 a_+ ^2 - 2 a_- ^2)$
$M_5$	$\frac{\alpha}{2}( b_- ^2 -  b_+ ^2)$
$M_7$	$\frac{\alpha}{\sqrt{2}}\text{Re}(-b_+^* a_+ + b_- a_-^*)$
$M_9$	$\frac{\alpha}{\sqrt{2}}\text{Im}(b_+^* a_+ - b_- a_-^*)$
$M_{11}$	$P_b \frac{1}{4}( b_+ ^2 -  b_- ^2 + 2 a_+ ^2 - 2 a_- ^2)$
$M_{12}$	$P_b \frac{1}{2}( b_+ ^2 -  b_- ^2)$
$M_{14}$	$P_b \frac{\alpha}{4}(- b_- ^2 -  b_+ ^2 + 2 a_+ ^2 + 2 a_- ^2)$
$M_{15}$	$-P_b \frac{\alpha}{2}( b_+ ^2 +  b_- ^2)$
$M_{17}$	$-P_b \frac{\alpha}{\sqrt{2}}\text{Re}(b_+^* a_+ + b_- a_-^*)$
$M_{19}$	$P_b \frac{\alpha}{\sqrt{2}}\text{Im}(b_+^* a_+ + b_- a_-^*)$
$M_{21}$	$-P_b \frac{1}{\sqrt{2}}\text{Im}(b_+^* a_- - b_- a_+^*)$
$M_{23}$	$P_b \frac{1}{\sqrt{2}}\text{Re}(b_+^* a_- - b_- a_+^*)$
$M_{25}$	$P_b \frac{\alpha}{\sqrt{2}}\text{Im}(b_+^* a_- + b_- a_+^*)$
$M_{27}$	$-P_b \frac{\alpha}{\sqrt{2}}\text{Re}(b_+^* a_- + b_- a_+^*)$
$M_{30}$	$P_b \alpha \text{Im}(a_+ a_-^*)$
$M_{32}$	$-P_b \alpha \text{Re}(a_+ a_-^*)$
$M_{33}$	$-P_b \frac{\alpha}{2}\text{Re}(b_+^* b_-)$
$M_{34}$	$P_b \frac{\alpha}{2}\text{Im}(b_+^* b_-)$

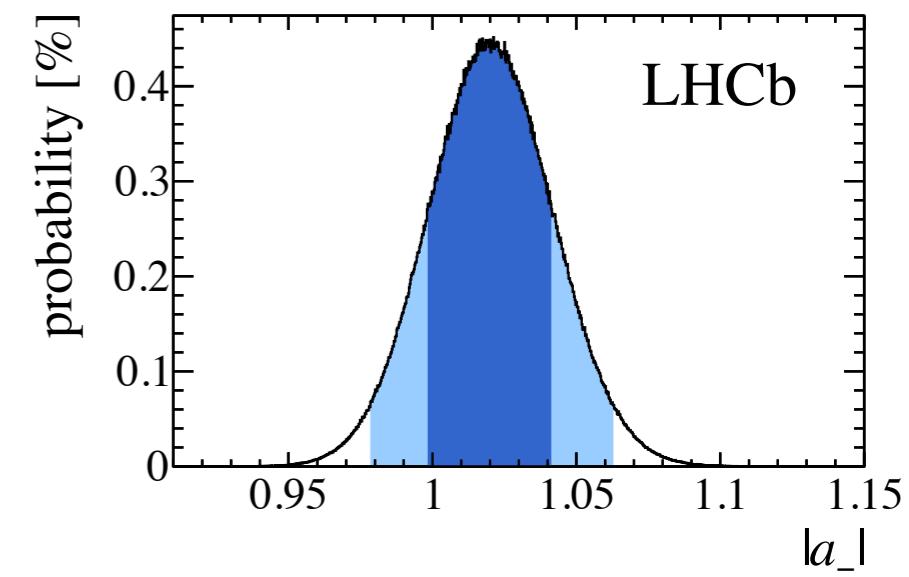
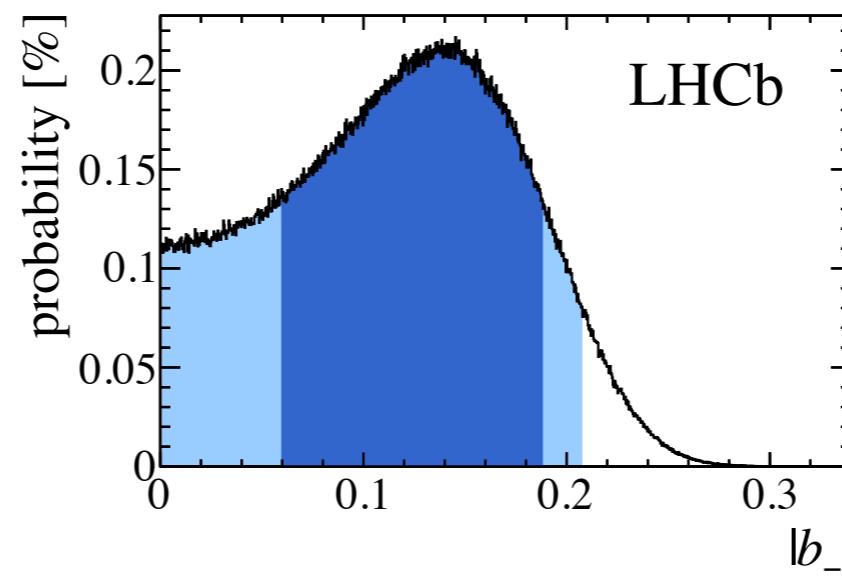
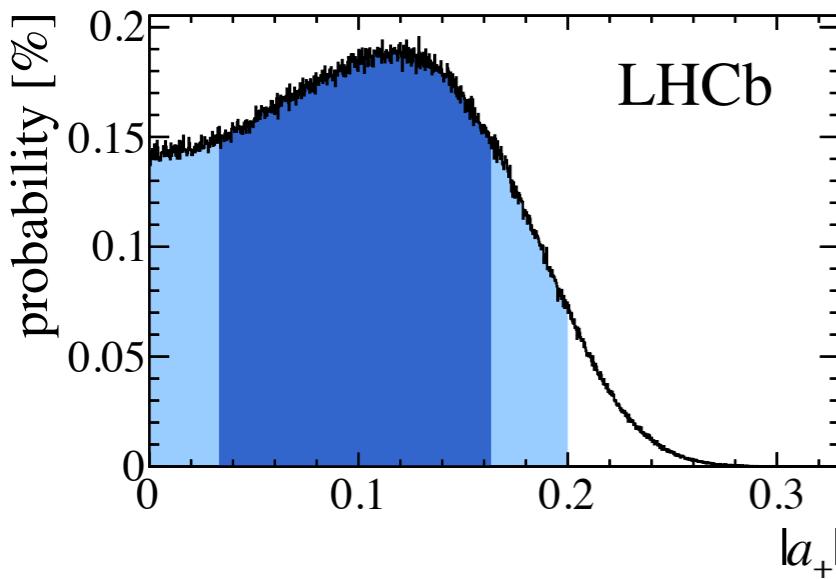
# $\Lambda_b \rightarrow J/\psi \Lambda$ angular distribution

- Large number of observables vanish if the  $\Lambda_b$  is unpolarised:
  - ✗ No longer have enough constraints to determine phases of the amplitudes.
- Even if the polarisation is large expect two amplitudes to be small:  $a_+ \approx b_- \approx 0$ .

Moments	Amplitude dependence
$M_1$	$\frac{1}{4}(2 a_+ ^2 + 2 a_- ^2 +  b_+ ^2 +  b_- ^2)$
$M_2$	$\frac{1}{2}( b_+ ^2 +  b_- ^2)$
$M_4$	$\frac{\alpha}{4}( b_- ^2 -  b_+ ^2 + 2 a_+ ^2 - 2 a_- ^2)$
$M_5$	$\frac{\alpha}{2}( b_- ^2 -  b_+ ^2)$
$M_7$	$\frac{\alpha}{\sqrt{2}}\text{Re}(-b_+^* a_+ + b_- a_-^*)$
$M_9$	$\frac{\alpha}{\sqrt{2}}\text{Im}(b_+^* a_+ - b_- a_-^*)$
$M_{11}$	$P_b \frac{1}{4}( b_+ ^2 -  b_- ^2 + 2 a_+ ^2 - 2 a_- ^2)$
$M_{12}$	$P_b \frac{1}{2}( b_+ ^2 -  b_- ^2)$
$M_{14}$	$P_b \frac{\alpha}{4}(- b_- ^2 -  b_+ ^2 + 2 a_+ ^2 + 2 a_- ^2)$
$M_{15}$	$-P_b \frac{\alpha}{2}( b_+ ^2 +  b_- ^2)$
$M_{17}$	$-P_b \frac{\alpha}{\sqrt{2}}\text{Re}(b_+^* a_+ + b_- a_-^*)$
$M_{19}$	$P_b \frac{\alpha}{\sqrt{2}}\text{Im}(b_+^* a_+ + b_- a_-^*)$
$M_{21}$	$-P_b \frac{1}{\sqrt{2}}\text{Im}(b_+^* a_- - b_- a_+^*)$
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# $\Lambda_b \rightarrow J/\psi \Lambda$ amplitudes

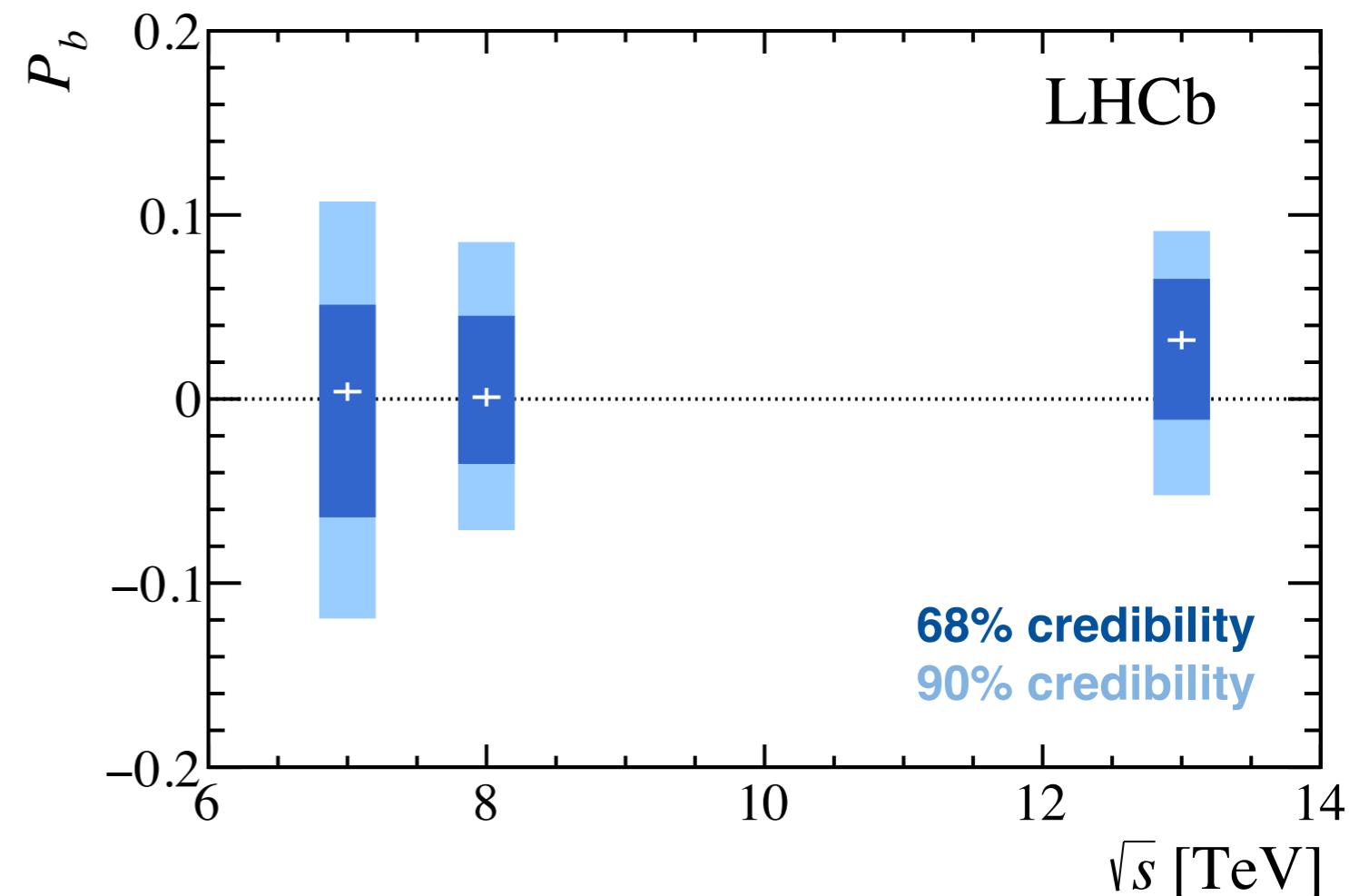
- Determine  $M_1 - M_{34}$  using a moment analysis.
- Determine amplitudes and polarisation using Bayesian inference from  $M_1 - M_{34}$ .
- Fix the magnitude and phase such that:
  - $\text{Re}(b_+) = 1$  and  $\text{Im}(b_+) = 0$
- Posterior distributions with uniform priors:



# $\Lambda_b$ production polarisation

- Data are consistent with zero production polarisation in  $pp$  collisions.

LHCb [[JHEP 06 \(2020\) 110](#)]

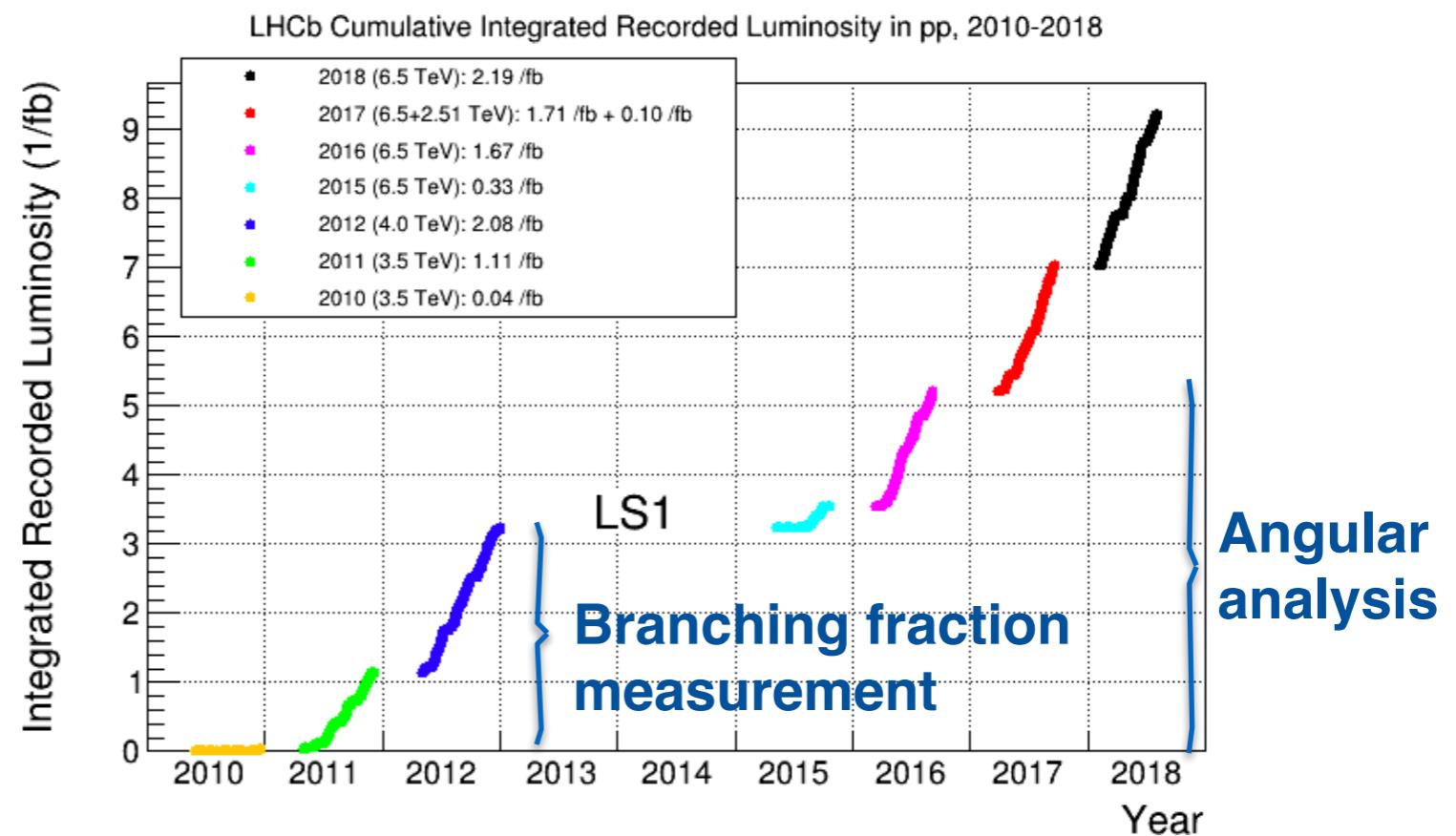


# Summary

- The branching fraction and angular distribution of  $\Lambda_b \rightarrow \Lambda\mu^+\mu^-$  decays are consistent with SM expectations.
- The results of a Bayesian analysis of observables in  $\Lambda_b \rightarrow \Lambda\mu^+\mu^-$  decays are consistent with both the SM and with the point favoured by the analysis of  $B$  meson decays.
- A Bayesian model comparison favours the SM (nuisance only) and modified  $C_9$  scenarios over scenarios with  $(C_9, C_{10})$  varied.
- The production polarisation of  $\Lambda_b$  baryons is consistent with zero in  $pp$  collisions at the LHC (which is unfortunate!)

# Summary

- Expect more to come with the full Run 2 dataset:

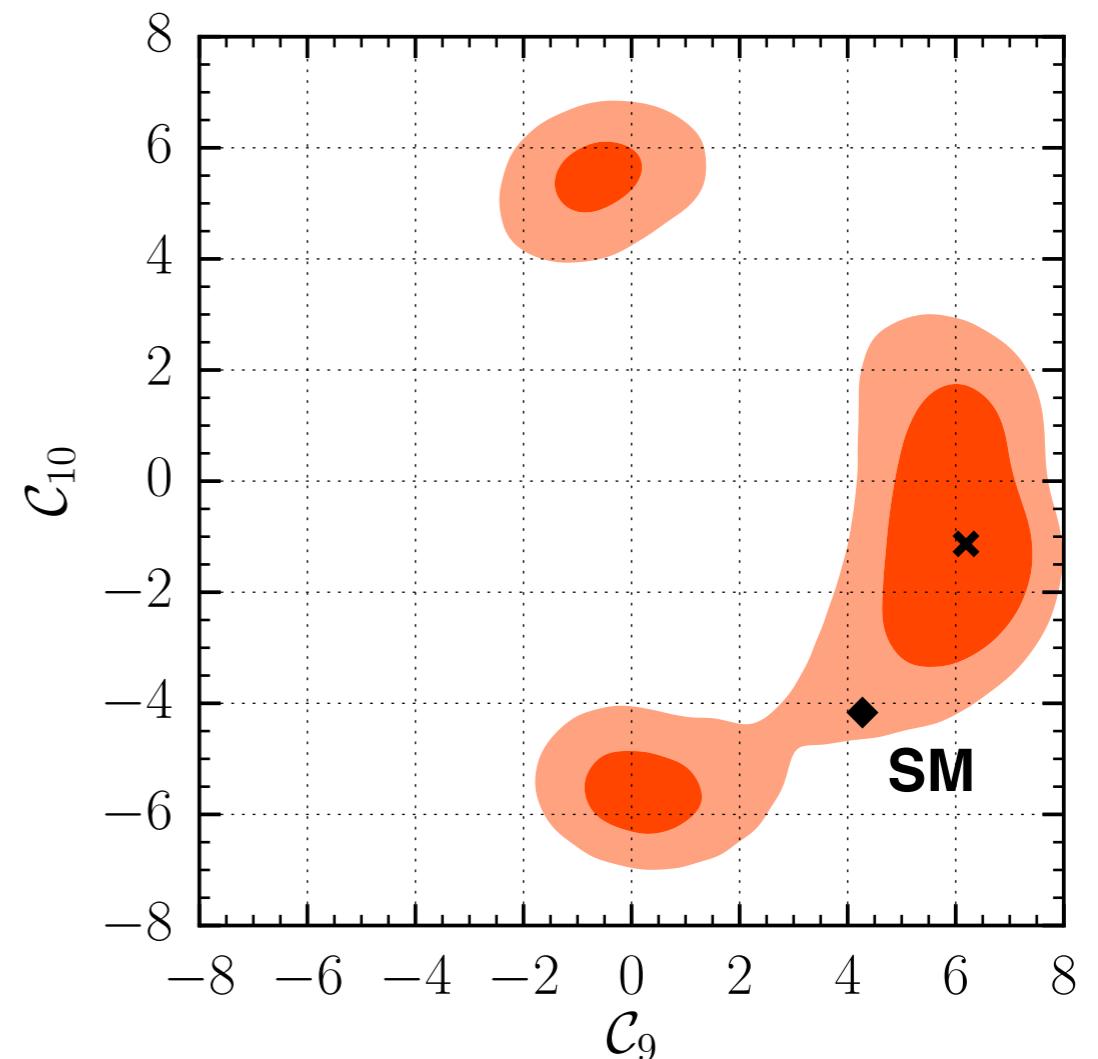




# Using $\Lambda_b \rightarrow \Lambda\mu^+\mu^-$ data within a Bayesian analysis of $|\Delta B|=|\Delta S|=1$ decays

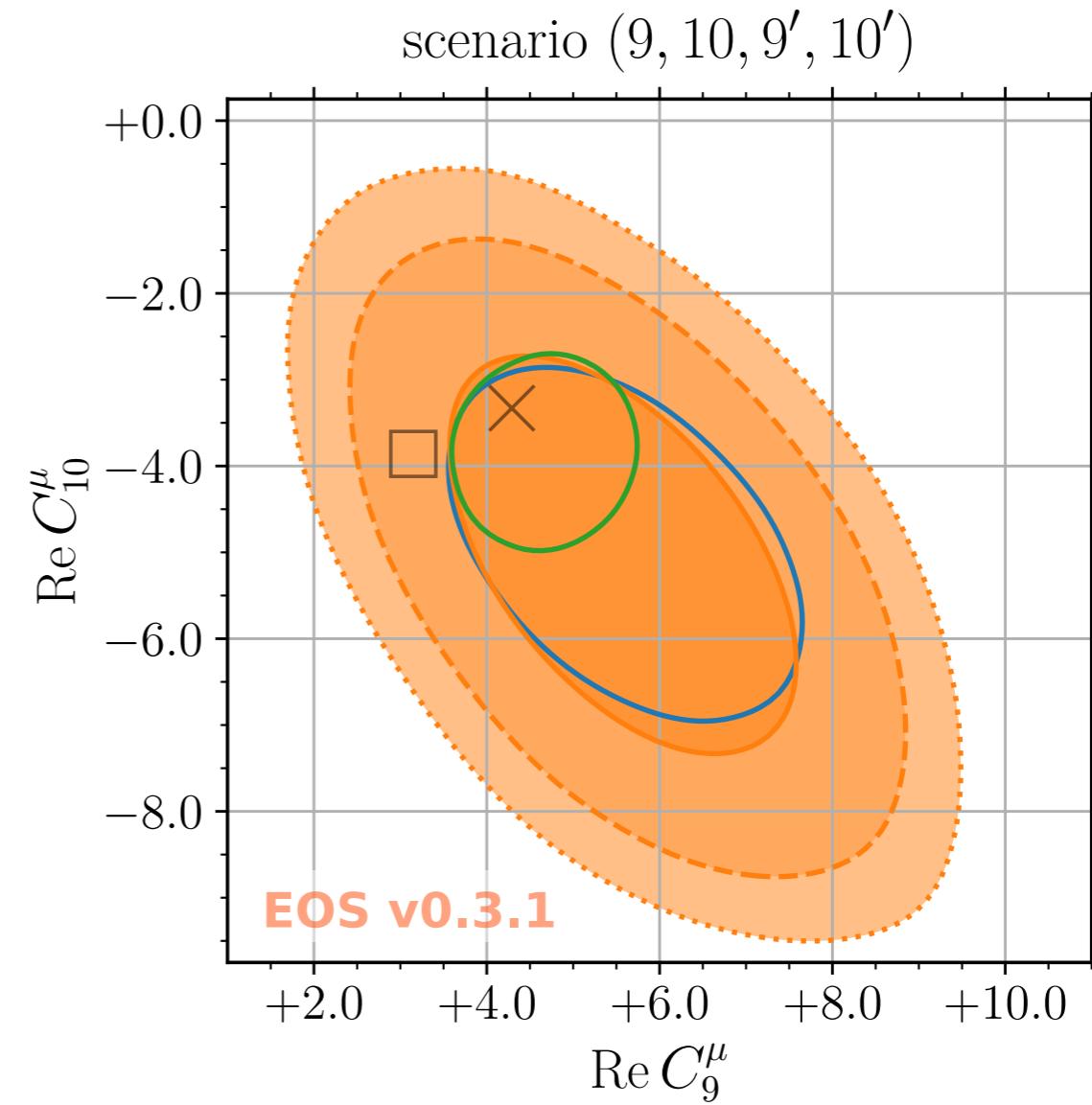
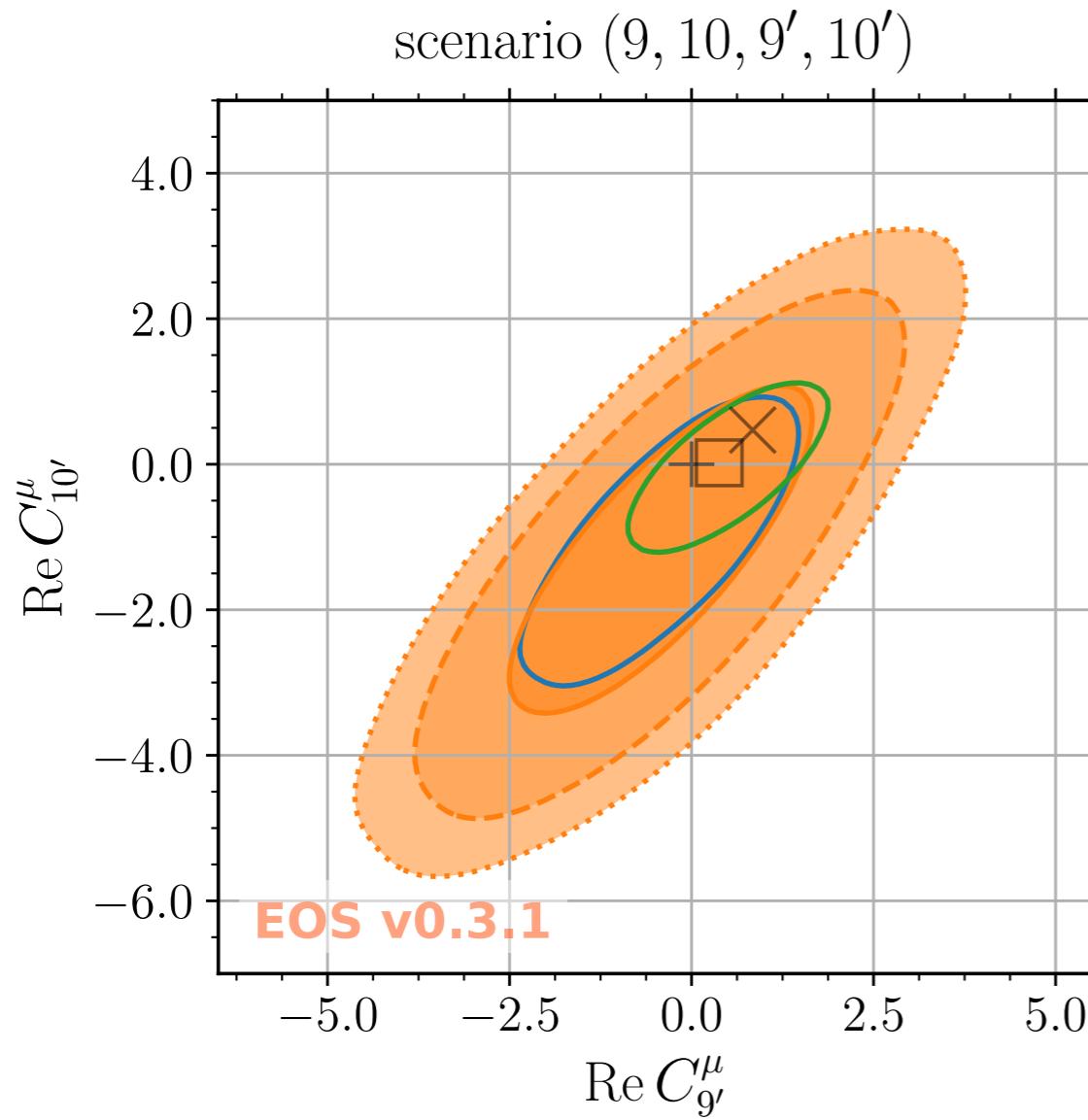
- A previous Bayesian analysis favoured a shift in  $C_9$  with an opposite sign to the  $B$  meson data.
- There are several changes between the two analyses:
  - Updated value of  $\alpha_\Lambda$  from BESIII.
  - Updated  $B_s^0 \rightarrow \mu^+\mu^-$  branching fraction measurements from ATLAS, CMS and LHCb.
  - Inclusion of the complete set of angular observables from LHCb.
  - LHCb erratum affecting  $A_{FB}^l$ . ← Has the largest impact on the best-fit point

Meinel et al. [\[PRD 94 \(2016\) 013007\]](#)



# Bayesian posteriors in the (9,10,9',10') scenario

- Including primed Wilson coefficients:



Blake et al. [[PRD 101 \(2020\) 035023](#)]

# $\Lambda$ asymmetry parameter

- Recent measurement by BESIII [[Nature Phys. 15 \(2019\) 631–634](#)] is 17% larger than the old world average value from secondary scattering.

$$\alpha_\Lambda = 0.642 \pm 0.013 \quad \text{PDG}$$

$$\alpha_\Lambda = 0.750 \pm 0.010 \quad \text{BESIII}$$

- The larger BESIII value likely solves the problems with the older LHCb, the ATLAS and CMS analyses of  $\Lambda_b \rightarrow J/\psi \Lambda$ , which favour an unphysical solution [[LHCb, PLB 724 \(2013\) 27](#)][[ATLAS, PRD 89 \(2014\) 092009](#)]  
[\[CMS, PRD 97 \(2018\) 072010\]](#).

# $\Lambda_b \rightarrow \Lambda \mu^+ \mu^-$ angular distribution

- Can expand the angular distribution in terms of helicity states:

$$\frac{d^6\Gamma}{dq^2 d\vec{\Omega}} \propto \sum_{\substack{\lambda_1, \lambda_2, \lambda_p, \lambda_{\ell\ell}, \lambda'_{\ell\ell}, \\ J, J', m, m', \lambda_\Lambda, \lambda'_\Lambda,}} \left( (-1)^{J+J'} \times \right. \\ \rho_{\lambda_\Lambda - \lambda_{\ell\ell}, \lambda'_\Lambda - \lambda'_{\ell\ell}}(\theta) \times \\ H_{\lambda_\Lambda, \lambda_{\ell\ell}}^{m, J}(q^2) H_{\lambda'_\Lambda, \lambda'_{\ell\ell}}^{\dagger, m', J'}(q^2) \times \\ h_{\lambda_1, \lambda_2}^{m, J}(q^2) h_{\lambda_1, \lambda_2}^{\dagger, m', J'}(q^2) \times \\ D_{\lambda_{\ell\ell}, \lambda_1 - \lambda_2}^{J*}(\phi_l, \theta_l, -\phi_l) D_{\lambda'_{\ell\ell}, \lambda_1 - \lambda_2}^{J'}(\phi_l, \theta_l, -\phi_l) \times \\ h_{\lambda_p, 0}^{\Lambda} h_{\lambda_p 0}^{\dagger, \Lambda} \times \\ \left. D_{\lambda_\Lambda, \lambda_p}^{1/2*}(\phi_b, \theta_b, -\phi_b) D_{\lambda'_\Lambda, \lambda_p}^{1/2}(\phi_b, \theta_b, -\phi_b) \right)$$

# $\Lambda_b \rightarrow \Lambda \mu^+ \mu^-$ angular distribution

- Unpolarised case:

$$\frac{d^4}{dq^2 d\vec{\Omega}} = \frac{3}{8\pi} \left( (K_{1ss} \sin^2 \theta_l + K_{1cc} \cos^2 \theta_l + K_{1c} \cos \theta_l) + \right.$$
$$(K_{2ss} \sin^2 \theta_l + K_{2cc} \cos^2 \theta_l + K_{2c} \cos \theta_l) \cos \theta_b +$$
$$(K_{3sc} \sin \theta_l \cos \theta_l + K_{3s} \sin \theta_l) \sin \theta_b \sin \phi$$
$$\left. (K_{4sc} \sin \theta_l \cos \theta_l + K_{4s} \sin \theta_l) \sin \theta_b \cos \phi \right)$$

Böer et al. [\[JHEP 01 \(2015\) 155\]](#)

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