

BROKEN $U(1)$ SYMMETRY
and new LIGHT neutral BOSONS
in ψ and Υ decays

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cf. Phys. Lett. B 675, 267 (2009) (= hep-ph/0812.3980)

One usually expects new physics at **very high energies** :

B-E-Higgs bosons / origin of mass ...

supersymmetry, grand unification,

new spacetime dimensions ...



Explore the high-energy frontier

at

(LEP) FermiLab, LHC, ILC ...

But another frontier exists at lower energies !

Search for relatively light

weakly (or very weakly) coupled new particles

ψ and Υ decays offer great possibilities

to search for **new light particles**,

which would have stayed **unobserved**

due to their **(very) weak couplings.**

Under which circumstances should we expect new light particles ?

**Would they have anything to do with
other constructions discussed for higher energies (Susy, etc.) ?**

Discuss :

**new neutral spin-1 or spin-0 particles
coupled to quarks and leptons.**

in a general way, but also within the context of a larger framework

But why should /how could such particles be light ??

A spin-1 gauge boson (*massless from gauge invariance*)

may be light if spont. broken gauge symmetry,

with **small gauge coupling** (*or symmetry breaking scale*)

A spin-0 boson

(*massless from Goldstone theorem, if spontaneously broken global symmetry*)

may acquire a small mass if **small explicit breaking of global symmetry**

\Rightarrow

Consider (*spontaneously or explicitly*)

broken local or global **$U(1)$ symmetries**

(*for the moment, independently of supersymmetry*)

What could be such broken $U(1)$ symmetries ?

$B ? \quad L ? \quad B - L ? \quad Y ?$ (or a combination) ?

Other $U(1)$ symmetries ? *(none in SM ...)*



Extend the Standard Model, to allow for new particles, and

new (broken) $U(1)$ SYMMETRIES ...

(local or global ...)

Starting point: *Nucl. Phys. B* 90, 104, 1975

electroweak symmetry breaking in SUSY, with

two Brout-Englert-Higgs doublets

$$\varphi_{SM} \rightarrow \{ \varphi'', \varphi' \}$$

→ **h_1** and **h_2** of SUSY extensions of the standard model

$$\mathbf{h}_1 = \begin{pmatrix} h_1^\circ \\ h_1^- \end{pmatrix}, \quad h_2^c = \begin{pmatrix} -h_2^{\circ*} \\ h_2^- \end{pmatrix} \rightarrow \mathbf{h}_2 = \begin{pmatrix} h_2^+ \\ h_2^\circ \end{pmatrix}$$

allows for the possibility of rotating independently the two doublets, i.e.:

→ a possible new $U(1)$ symmetry acting on the two doublets as

$$h_1 \rightarrow e^{i\alpha} h_1, \quad h_2^c \rightarrow e^{-i\alpha} h_2^c \rightarrow h_2 \rightarrow e^{i\alpha} h_2$$

introduced in 2-higgs-doublet model in Nucl. Phys. B 78, 14 (1974)

(often known as ‘PQ-symmetry’)

constraining interaction potential and Yukawa couplings

Not all terms compatible with Lorentz and gauge symmetries are allowed

further restrictions due to additional symmetry ...

also reminiscent of

***R*-symmetry**

of supersymmetric theories,

and actually was at the origin of R symmetry ...

$U(1)$ symmetry, called Q , decomposed as

$$Q = R U$$

the continuous R -symmetry does not act on h_1 and h_2

so that it can survive electroweak breaking, while Q and U get broken

(R will later act on *superpartners*)

under U :

$$h_1 \rightarrow e^{i\alpha} h_1, \quad h_2 \rightarrow e^{i\alpha} h_2$$

U symmetry will act axially on quarks and leptons

(axial $U(1)$, also known as $U(1)_{PQ}$)

It commutes with the Susy generator

while R and Q do not commute with Susy

Allowed quartic interactions in $V(h_1, h_2)$:

$$(h_1^\dagger h_1)^2, (h_2^\dagger h_2)^2, (h_1^\dagger h_1)(h_2^\dagger h_2), |h_1 h_2|^2$$

if only one Higgs v.e.v., we get an “inert doublet model”

*but we are interested in **2-Higgs v.e.v.’s**:*

$$\langle h_1^\circ \rangle = \frac{v_1}{\sqrt{2}}, \quad \langle h_2^\circ \rangle = \frac{v_2}{\sqrt{2}}, \quad \text{with} \quad \tan \beta = \frac{v_2}{v_1}$$

(mixing angle β initially called δ in 74)

With SUSY these (already restricted) quartic Higgs interactions
 appear as **electroweak gauge interactions**, with

$$V_{\text{quartic}} = \frac{g^2 + g'^2}{8} (h_1^\dagger h_1 - h_2^\dagger h_2)^2 + \frac{g^2}{2} |h_1^\dagger h_2|^2$$

= **quartic Higgs potential of the MSSM**

Quartic Higgs couplings fixed by electroweak gauge couplings !

at the origin of mass inequality

$$m \text{ (lightest Higgs)} \leq m_Z + \text{rad. corr. in MSSM}$$

(potentially problematic, as it requires radiative correction effects to be rather large)

The “ μ problem”, in 1974

There is also a μ term: $\mu H_1 H_2$ mass term in superpotential

$$\Rightarrow \mu^2 (|h_1|^2 + |h_2|^2), \quad \text{or} \quad \sum_{1,2} \left| \mu^2 \pm \xi \frac{g'}{2} \right| |h_i^2|$$

μ term a problem to get correct electroweak breaking with 2-Higgs doublet v.e.v.'s!

(at classical level)

Get rid of the μ term by making it dynamical

generates extra term $\propto m_3^2 \Re(h_1 h_2)$ in the potential at the origin \Rightarrow

$$\langle h_1^\circ \rangle = \frac{v_1}{\sqrt{2}} \neq 0, \quad \langle h_2^\circ \rangle = \frac{v_2}{\sqrt{2}} \neq 0,$$

(both μ and m_3^2 terms break explicitly the U symmetry \Rightarrow no massless axionlike particle (A) here:

it gets its mass from m_3^2 i.e. from trilinear λ coupling)

Make μ parameter of MSSM dynamical, taken to be superfield $\mu(x, \theta)$:

superpotential:

$$\mu H_1 H_2 \rightarrow \lambda H_1 H_2 S$$

trilinear coupling with extra singlet superfield S

(Nucl. Phys. B 90, 104, 1975)

(+ possible $f(S)$ superpotential terms,

depending on the other $U(1)$ symmetries imposed)

→ **N/nMSSM**, or **USSM** if an extra $U(1)$ symmetry is gauged

(Phys.Lett. B 69, 489, 1977)

$$\begin{aligned} \mathcal{W} = & \lambda_e H_1 \cdot \bar{E} L + \lambda_d H_1 \cdot \bar{D} Q - \lambda_u H_2 \cdot \bar{U} Q \\ & + \lambda H_1 H_2 S + \underbrace{\frac{\kappa}{3} S^3 + \frac{\mu_S}{2} S^2 + \sigma S}_{f(S)} \end{aligned}$$

This **extra- $U(1)$** symmetry acts as

$$H_1 \xrightarrow{U} e^{i\alpha} H_1, \quad H_2 \xrightarrow{U} e^{i\alpha} H_2, \quad S \xrightarrow{U} e^{-2i\alpha} S$$

$$(Q, \bar{U}, \bar{D}; L, \bar{E}) \xrightarrow{U} e^{-i\frac{\alpha}{2}} (Q, \bar{U}, \bar{D}; L, \bar{E})$$

for the superpotential to be invariant.

(acts axially on quarks and leptons, as a PQ symmetry)

What is the fate of this extra- $U(1)$ symmetry, **global** or **local**,

broken **explicitly**

(by small superpotential terms and/or small soft susy-breaking terms)

or **spontaneously**

through the 2 Higgs doublets and possibly a large Higgs singlet v.e.v. ?

It may be gauged, or not ...

New neutral gauge boson U

*possibly **light** if the extra- $U(1)$ gauge coupling is **small***

*or new **light spin-0 ‘axionlike’ pseudoscalar quasiGoldstone boson a***

associated with small explicit breaking of extra- $U(1)$ symmetry

Goldstone eaten by Z: $\text{Im}(\cos \beta h_1^\circ - \sin \beta h_2^\circ)$

\perp combination:

$$A = \sqrt{2} \text{Im}(\sin \beta h_1^\circ + \cos \beta h_2^\circ)$$

(cf. standard axion, or (light) A of MSSM)

*In the presence of a (possibly large) singlet v.e.v.:
pseudoscalar Goldstone or quasi-Goldstone boson a :*

$$a = \cos \zeta \left(\sqrt{2} \text{Im}(\sin \beta h_1^\circ + \cos \beta h_2^\circ) \right) + \sin \zeta \left(\sqrt{2} \text{Im} s \right)$$

$r = \cos \zeta =$ invisibility parameter

would-be “axion” $a =$ mixing of doublet and singlet components

PLB 95, 285, 1980; NPB 187, 184, 1981

(allows to reduce strength or effective strength of U or a interactions, cf. “invisible axion”)

**It may either acquire a small mass if extra- $U(1)$ symmetry gets explicitly broken
or gets eaten into the third degree of freedom of a new neutral gauge boson U ,
if extra- $U(1)$ symmetry is local and spontaneously broken.**

SEARCHING FOR A NEW LIGHT GAUGE BOSON

NPB 187, 184, [1981](#), ..., PRD 74, 054034 (2006); 75, 115017 (2007); [PLB 675, 267 \(2009\)](#)

*The amplitude for producing a new gauge boson (U) is proportional
to the new gauge coupling constant, g''*

$$\mathcal{A}(A \rightarrow B + U_{\text{long}}) \propto g'' \dots$$

g'' may be very small !!

*Is such a gauge boson unobservable,
if its gauge coupling is extremely small ?*

NO !

For the longitudinal polarisation state of a light gauge boson

$$\epsilon_L^\mu \simeq \frac{k^\mu}{m_U}$$

gets singular when $g'' \rightarrow 0$, as $m_U \propto g'' \dots \rightarrow 0$ as well !

$$\mathcal{A}(A \rightarrow B + U_{\text{long}}) \propto g'' \frac{k_U^\mu}{m_U} \langle B | J_{\mu U} | A \rangle = \frac{1}{F_U} k_U^\mu \langle B | J_{\mu U} | A \rangle$$

$$k^\mu \bar{\psi} \gamma_\mu \gamma_5 \psi \rightarrow 2 m_q \psi \gamma_5 \psi$$

*A very light U boson does not decouple in the limit of very small gauge coupling !
behaves as “eaten-away” pseudoscalar Goldstone boson associated with the sp. breaking
of the global U(1).*

effective pseudoscalar coupling:

$$f_{q,l P} = f_{q,l A} \frac{2 m_{q,l}}{m_U}$$

in the low mass and low coupling regime:

**A light spin-1 gauge boson behaves very much
as a quasi-massless spin-0 particle,**

*i.e. as corresponding spin-0 Goldstone boson ...
with pseudoscalar couplings to quarks and leptons*

“Equivalence theorem”

similar to “Equivalence theorem of supersymmetry”

very light spin- $\frac{3}{2}$ gravitino behaves as spin- $\frac{1}{2}$ goldstino of sp. broken global susy

(cf. “GMSB” models ...)

Consequence:

$$B(\Upsilon \rightarrow \gamma U) \simeq B(\Upsilon \rightarrow \gamma a)$$

*The same experiment may be used to search for
light spin-1 neutral gauge bosons,
as well as light spin-0 pseudoscalars.*

(but remember: standard axion excluded ...)

Decay modes:

$$\left\{ \begin{array}{l} U \rightarrow \nu \bar{\nu} \text{ (or light dark matter particles)} \\ U \rightarrow e^+ e^-, \mu^+ \mu^-, \dots \text{ (depending on } m_U) \end{array} \right.$$

\Rightarrow search for

$$\left\{ \begin{array}{l} \Upsilon \rightarrow \gamma + \textit{invisible} \\ \Upsilon \rightarrow \gamma + e^+e^- \\ \Upsilon \rightarrow \gamma + \mu^+\mu^- \\ \dots \end{array} \right.$$

as possible signal for either

spin-1 U boson,

or spin-0 pseudoscalar particle a

(or also scalar)

Determining the couplings:

$$\text{couplings of } h_1^\circ \text{ and } h_2^\circ \text{ to } q, l: \frac{m \sqrt{2}}{v \cos \beta}, \frac{m \sqrt{2}}{v \sin \beta}$$

$$\text{with } v = 2^{-1/4} G_F^{-1/2} \simeq 246 \text{ GeV}$$

Pseudoscalar couplings of $A = \sqrt{2} \text{Im} (\sin \beta h_1^\circ + \cos \beta h_2^\circ)$

$$\begin{cases} (m/v) \times (\tan \beta = 1/x) & \text{(charged leptons and } d \text{ quarks)} \\ (m/v) \times (\cot \beta = x) & \text{(u quarks)} \end{cases}$$

i.e. pseudoscalar couplings of standard axion (or A of MSSM)

$$2^{\frac{1}{4}} G_F^{\frac{1}{2}} m_{q,l} \times (\tan \beta \text{ or } \cot \beta).$$

*When A mixes with $\text{Im } s$ into doublet/singlet pseudoscalar combination a associated with extra- $U(1)$ breaking,
we get the pseudoscalar (or effective pseudoscalar) couplings,
now also proportional the invisibility parameter $r = \cos \zeta$.*

Pseudoscalar coupling

$$f_{q,l P} \simeq \underbrace{\frac{2^{\frac{1}{4}} G_F^{\frac{1}{2}} m_{q,l}}{4 \cdot 10^{-6} m_{q,l}(\text{MeV})}} \times \begin{cases} r x = \cos \zeta \cot \beta & (u, c, t) \\ r/x = \cos \zeta \tan \beta & (d, s, b; e, \mu, \tau) \end{cases}$$

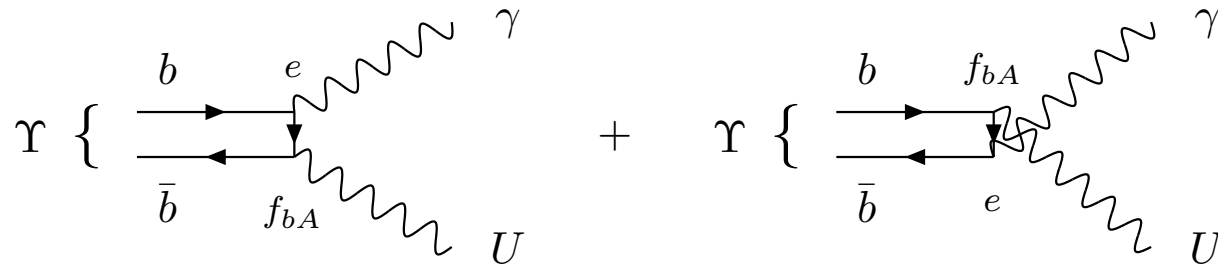
Equivalent axial coupling

$$f_{q,l A} \simeq \underbrace{\frac{2^{-\frac{3}{4}} G_F^{\frac{1}{2}} m_U}{2 \cdot 10^{-6} m_U(\text{MeV})}} \times \begin{cases} r x = \cos \zeta \cot \beta & (u, c, t) \\ r/x = \cos \zeta \tan \beta & (d, s, b; e, \mu, \tau) \end{cases}$$

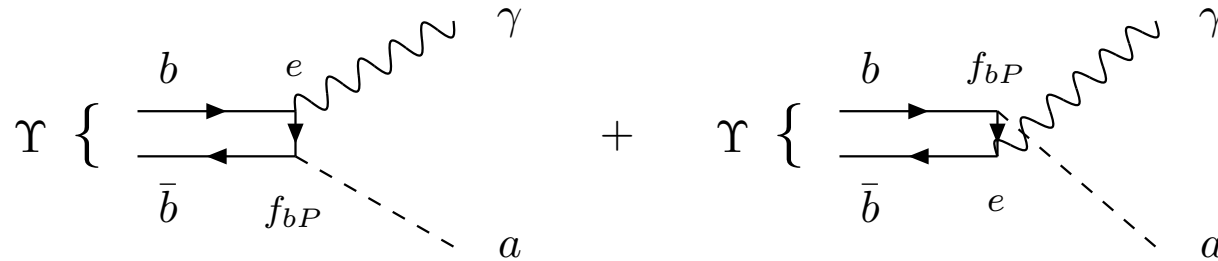
$$\text{ratio: } 2 \frac{m_{q,l}}{m_U}$$

$$r = \cos \zeta = \text{invisibility parameter} \quad \tan \beta = \frac{v_2}{v_1}$$

ψ and Υ DECAYS



$\Upsilon \rightarrow \gamma U$ induced by the axial coupling f_{bA} . For a light U the amplitude is essentially the same as for a spin-0 a with pseudoscalar coupling $f_{bP} = f_{bA} \frac{2m_b}{m_U}$.



Production of a spin-0 pseudoscalar in $\Upsilon \rightarrow \gamma a$.

$$\frac{B(\text{onium} \rightarrow \gamma U/a)}{B(\text{onium} \rightarrow \mu^+ \mu^-)} = \frac{2 f_{qP}^2}{e^2} = \frac{G_F m_q^2}{\sqrt{2} \pi \alpha} \left(r^2 x^2 \text{ or } \frac{r^2}{x^2} \right)$$

$$\implies$$

$$\frac{B(\psi \rightarrow \gamma U/a)}{B(\psi \rightarrow \mu^+ \mu^-)} = \frac{G_F m_c^2}{\sqrt{2} \pi \alpha} r^2 x^2 C_\psi F_\psi \simeq 8 \cdot 10^{-4} r^2 x^2 C_\psi F_\psi$$

$$\frac{B(\Upsilon \rightarrow \gamma U/a)}{B(\Upsilon \rightarrow \mu^+ \mu^-)} = \frac{G_F m_b^2}{\sqrt{2} \pi \alpha} \frac{r^2}{x^2} C_\Upsilon F_\Upsilon \simeq 8 \cdot 10^{-3} \frac{r^2}{x^2} C_\Upsilon F_\Upsilon$$

(F phase space factor; $C \gtrsim \frac{1}{2}$ for QCD radiative and rel. corrections)

\implies

$$B(\psi \rightarrow \gamma U/a) \simeq 5 \cdot 10^{-5} \cos^2 \zeta \cot^2 \beta C_\psi F_\psi$$

$$B(\Upsilon \rightarrow \gamma U/a) \simeq 2 \cdot 10^{-4} \cos^2 \zeta \tan^2 \beta C_\Upsilon F_\Upsilon$$

ψ DECAYS

$$B(\psi \rightarrow \gamma + \text{invisible}) < 1.4 \cdot 10^{-5} \quad (1982) \quad \Rightarrow$$

$$rx = \cos \zeta \cot \beta < .75 / \sqrt{B_{\text{inv}}} \quad \Longleftrightarrow$$

$$\left\{ \begin{array}{l} |f_{cA}| < 1.5 \cdot 10^{-6} m_U(\text{MeV}) / \sqrt{B_{\text{inv}}} \\ |f_{cP}| < 5 \cdot 10^{-3} / \sqrt{B_{\text{inv}}} , \quad |f_{cS}| < 10^{-2} / \sqrt{B_{\text{inv}}} \end{array} \right.$$

Υ DECAYS

PLB 675, 267 (2009)

CLEO, BABAR

BABAR: hep-ex/0808.0017

Limit on $\Upsilon \rightarrow \gamma + \text{invisible}$ improved with $\Upsilon(3S)$ by more than 4

prel. limit from 3.2 to $3.5 \cdot 10^{-6}$ for neutral mass 0 to 1 GeV, down to $.7 \cdot 10^{-6}$ for 3 GeV,
and $< 4 \cdot 10^{-6}$ up to 6 GeV.

$$r/x = \cos \zeta \tan \beta < .2 / \sqrt{B_{\text{inv}}} \iff$$

$$|f_{bA}| < 4 \cdot 10^{-7} m_U(\text{MeV}) / \sqrt{B_{\text{inv}}}, \text{ or } |f_{bP}| < 4 \cdot 10^{-3} / \sqrt{B_{\text{inv}}}$$

takes into account invisible B.R. of the new boson

valid up to $\simeq 5$ GeV (as long as invisible decay modes are present)

For an invisibly decaying boson:

limit on pseudoscalar (or effective pseudoscalar) coupling

$$f_{bP} < 4 \cdot 10^{-3}$$

5 times smaller than standard Higgs coupling to b , $m_b/v \simeq 2 \cdot 10^{-2}$

For a scalar coupling,

$$|f_{bS}| < 6 \cdot 10^{-3} / \sqrt{B_{\text{inv}}}$$

Υ limit \implies

$$\text{doublet fraction: } r^2 = \cos^2 \zeta < 4\% / (\tan^2 \beta B_{\text{inv}}) ,$$

(stronger than ψ limit for $\tan \beta > .5$), requires

a ($< 4\%$ doublet, $> 96\%$ singlet) for $\tan \beta > 1$; and $< .5\%$ doublet for $\tan \beta > 3$, for invisible decays of the new boson.

Dependence on B_{inv} disappears for the production, in radiative decays of the ψ , of a new boson decaying invisibly.

Non-observation of a signal in $\Upsilon \rightarrow \gamma + \text{invisible neutral} \implies$

$$B(\psi \rightarrow \gamma + \text{neutral}) B_{\text{inv}} \lesssim 10^{-6} / \tan^4 \beta ,$$

i.e. $\lesssim 10^{-8}$ for $\tan \beta \gtrsim 3$, independently of the invisible branching ratio B_{inv}
(also applicable, to a scalar particle).

Consequences for couplings to LEPTONS

implications for the couplings of the new spin-1 or spin-0 boson to e , μ or τ . !!

Universality of the axial coupling of the U

*family-independent and identical for all charged leptons and d quarks.
(from gauge invariance of Yukawa couplings responsible for m_l , m_q in a 2-HD model)*

$$f_{eA} = f_{\mu A} = f_{\tau A} = f_{dA} = f_{sA} = f_{bA}$$

It also reflects that the couplings of the corresponding pseudoscalar a to d quarks and l^- are proportional to masses :

$$f_{eP} = f_{bP} \frac{m_e}{m_b}$$

\Rightarrow limit on f_{bA} also applies to f_{eA} :

$$|f_{eA}| < 4 \cdot 10^{-7} m_U(\text{MeV}) / \sqrt{B_{\text{inv}}}, \quad |f_{eP}| < 4 \cdot 10^{-7} / \sqrt{B_{\text{inv}}}$$

for invisible decays of the new boson:

Limit on pseudoscalar coupling f_{eP} 5 times smaller than the standard Higgs coupling to the electron, $m_e/v \simeq 2 \cdot 10^{-6}$,

As scalar couplings are also proportional to masses, with $f_{eS} = f_{bS} m_e/m_b$, the limit on $|f_{eP}|$, slightly relaxed, may be applied to a scalar coupling.

$$|f_{eS}| < 6 \cdot 10^{-7} / \sqrt{B_{\text{inv}}}$$

For a spin-1 U the strong limit on f_{eA} agrees with atomic physics parity-violation experiments (strong limit on $|f_{eA} f_{qV}|$).

$$\sqrt{|f_{eA} f_{qV}|} < 10^{-7} m_U(\text{MeV})$$

$\Rightarrow e^+e^- \rightarrow \gamma U$ annihilation cross section, roughly $\propto (f_{eV}^2 + f_{eA}^2)$,

very small for a light U , unless $f_{eV} \gg f_{eA}$.

$$\Upsilon \text{ DECAYS} \rightarrow \gamma + (\mu^+ \mu^-)$$

BABAR: arXiv:hep-ex/0902.2176

$B(\Upsilon \rightarrow \gamma + \text{neutral}) B_{\mu\mu} \lesssim 2 \cdot 10^{-6}$ in most of the mass range considered
(compared to $B(\Upsilon \rightarrow \gamma + \text{neutral}) B_{\text{inv}} \lesssim 3.5 \cdot 10^{-6}$)

$$r/x = \cos \zeta \tan \beta \lesssim .15 / \sqrt{B_{\mu\mu}} \implies$$

$$|f_{bA}| \lesssim 3 \cdot 10^{-7} m_U(\text{MeV}) / \sqrt{B_{\mu\mu}}$$

$$|f_{bP}| \lesssim 3 \cdot 10^{-3} / \sqrt{B_{\mu\mu}}, \text{ or } |f_{bS}| \lesssim 5 \cdot 10^{-3} / \sqrt{B_{\mu\mu}}$$

(for $B_{\mu\mu} \simeq 1$, lim. on f_{bP} is $\simeq 15\%$ of SM Higgs coupling to b).

May be or not more constraining than invisible decays, depending on whether $B_{\mu\mu}$ is larger than $\approx B_{\text{inv}}$.

(e.g. $B_{\text{inv}} \approx 16\%$ and $B_{\mu\mu} \approx 10\%$, for a 1 GeV U , ignoring light dark matter particles).

$$\text{doublet fraction: } r^2 = \cos^2 \zeta \lesssim 2\% / (\tan^2 \beta B_{\mu\mu}) .$$

$B_{\mu\mu}$ disappears for the production, in radiative decays of the ψ ,
of a new boson decaying into $\mu^+\mu^-$.

Non-observation of $\Upsilon \rightarrow \gamma + (\text{neutral} \rightarrow \mu^+\mu^-)$ decays implies

$$B(\psi \rightarrow \gamma + \text{neutral}) B_{\mu\mu} \lesssim 5 \cdot 10^{-7} / \tan^4 \beta ,$$

i.e. $\lesssim 5 \cdot 10^{-9}$ for $\tan \beta \gtrsim 3$, independently of $B_{\mu\mu}$.

Limits on b couplings may be translated into limits on
pseudovector, pseudoscalar or scalar couplings to electrons:

$$|f_{eA}| \lesssim 3 \cdot 10^{-7} m_U(\text{MeV}) / \sqrt{B_{\mu\mu}}$$

$$|f_{eP}| \lesssim 3 \cdot 10^{-7} / \sqrt{B_{\mu\mu}} \quad \text{or} \quad |f_{eS}| \lesssim 5 \cdot 10^{-7} / \sqrt{B_{\mu\mu}}$$

SEARCHING for LIGHT DARK MATTER in Υ DECAYS

PF + Kaplan, PLB 269, 213 (1991); PF, PRD 74, 054034, 2006, ...

Search for the decays

$$\left\{ \begin{array}{l} \Upsilon \rightarrow \chi\chi \\ \Upsilon \rightarrow \gamma \chi\chi \end{array} \right.$$

mediated by a light U boson (or a spin-0 particle in the case of $\gamma \chi\chi$)

(no decay $\Upsilon \rightarrow$ *invisible* mediated by the direct exchange of a spin-0 particle)

*give limits on the product of couplings of the U boson
to the b quark and the light dark matter particle χ*

($\Upsilon \rightarrow \chi \chi$ and $\gamma \chi \chi$ test the vector and axial couplings to the b , respectively)

From $\Upsilon \rightarrow \underbrace{\chi \chi}_{\text{inv}}$

$$|c_\chi f_{bV}| \lesssim \begin{cases} 9 \cdot 10^{-2} & \text{(spin-0) ,} \\ 6 \cdot 10^{-2} & \text{(Majorana) ,} \\ 4.5 \cdot 10^{-2} & \text{(Dirac) .} \end{cases}$$

(Υ limits weaker than ψ ones by more than 2)

$c_\chi f_{bA}$ may be constrained from $\Upsilon \rightarrow \gamma \underbrace{\chi \chi}_{\text{inv}}$

Many other processes may also be discussed ...

Dark Matter

Parity violations in atomic physics

$$e^+ e^- \rightarrow \gamma U$$

$$g - 2$$

ν scatterings

Supernovae explosions

...

CONCLUSIONS