

## Euclid France Galaxy Clustering

# Contraindre la masse des neutrinos avec le spectre de puissance sur les simulations DEMNUni

**Sylvain Gouyou Beauchamps**

Thèse sous la direction de William Gillard et Stéphanie Escoffier

CPPM, RENOIR

13 Novembre 2019

# Plan of the talk

I. Massive neutrinos in cosmology

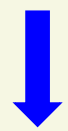
II. The power spectra of the DEMNUni simulations

III. Parameter estimation on the DEMNUni spectra

**The standard model of cosmology,  $\Lambda$ CDM.**

- Homogeneous and isotropic universe
- $\Lambda$  = Responsible for the accelerated expansion
- CDM = Cold Dark Matter (non-standard and non-relativistic)
- Flat universe

The standard model of particle physics assumes :  $m_\nu = 0$



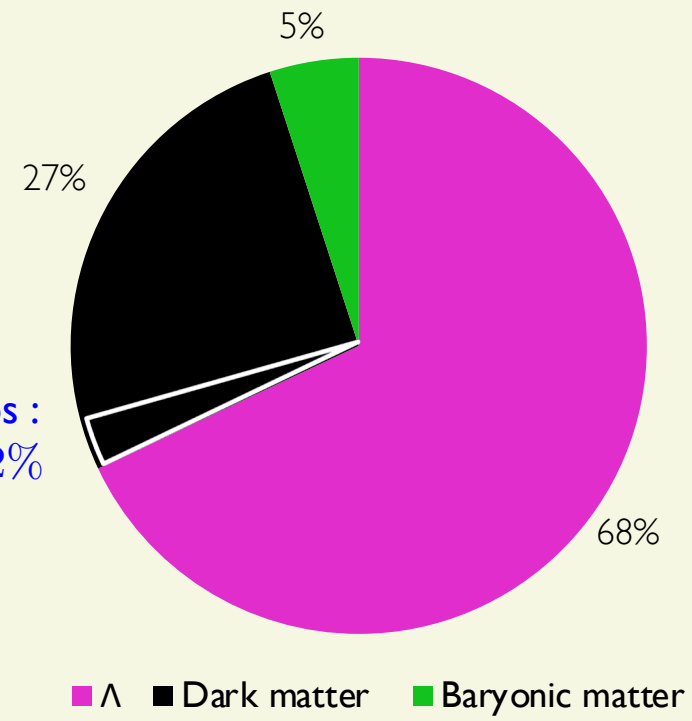
Particle Physics experiment :  
 ➔  $m_\nu \neq 0$

NH  $0.056 \text{ eV} \lesssim M_\nu \lesssim 1 \text{ eV}$   
 IH  $0.095 \text{ eV}$

Oscillation experiments (Kamiokande, SNO, T2K)      Tritium  $\beta$  decay (KATRIN)

➔ Neutrinos : 0.1% – 2%

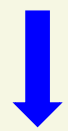
Content of our universe today :



**The standard model of cosmology,  $\Lambda$ CDM.**

- Homogeneous and isotropic universe
- $\Lambda$  = Responsible for the accelerated expansion
- CDM = Cold Dark Matter (non-standard and non-relativistic)
- Flat universe

The standard model of particle physics assumes :  $m_\nu = 0$

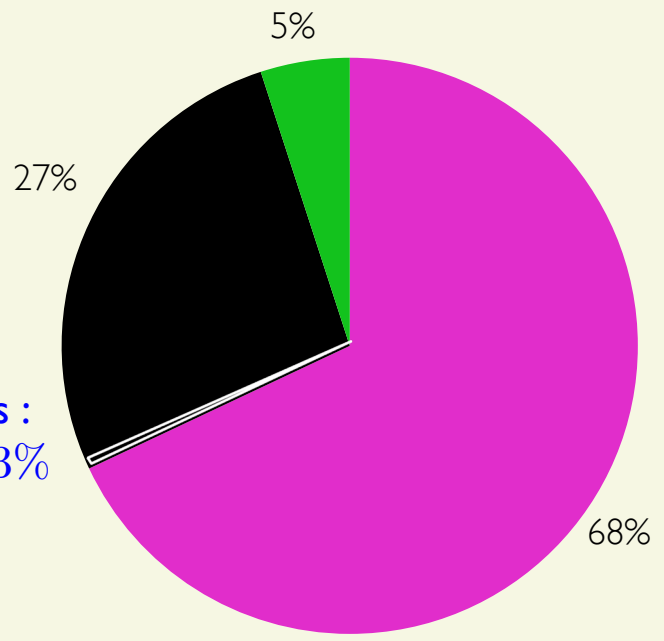


Particle Physics experiment :  
 →  $m_\nu \neq 0$

NH  $0.056 \text{ eV} \lesssim M_\nu \lesssim 1 \text{ eV}$   
 IH  $0.095 \text{ eV}$

Cosmology :  $M_\nu < 0.13 \text{ eV}$

Content of our universe today :



■  $\Lambda$  ■ Dark matter ■ Baryonic matter

[A.]. Cuesta et al. 2016]

As the universe expands its temperature decreases

Expanding universe  $\rightarrow$  Relativistic at the beginning, they become non-relativistic.

$$T_\nu \gg m_\nu$$

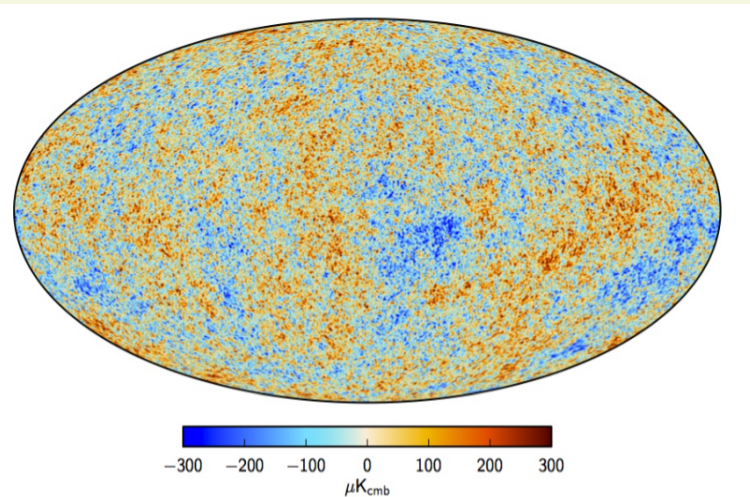
$$T_\nu \ll m_\nu$$

Radiation : No gravitational clustering.

Dark matter : Gravitational clustering.

This transition has an impact on the matter distribution.

If we can spot at which redshift  $z_{nr}$  this transition happened, we could know the value of  $m_\nu$ .



$$1 + z_{nr} = 1890 \left( \frac{m_\nu}{1 \text{ eV}} \right)$$

CMB  $\rightarrow$  No trace of non-relativistic neutrinos (in the TT power spectrum) at  $z = 1100$ .

$$\rightarrow m_\nu \lesssim 0.58 \text{ eV}$$

Because of their high velocity dispersion neutrinos are **free streaming**.

Thermal velocity :  $v_{\text{th}} = \frac{3T_\nu}{m_\nu} \approx 150(1+z) \left( \frac{1 \text{ eV}}{m_\nu} \right) \text{ km/s}$

Free streaming length  $\lambda_{\text{FS}}(t) \propto v_{\text{th}}(t)$  : causal horizon for neutrinos.

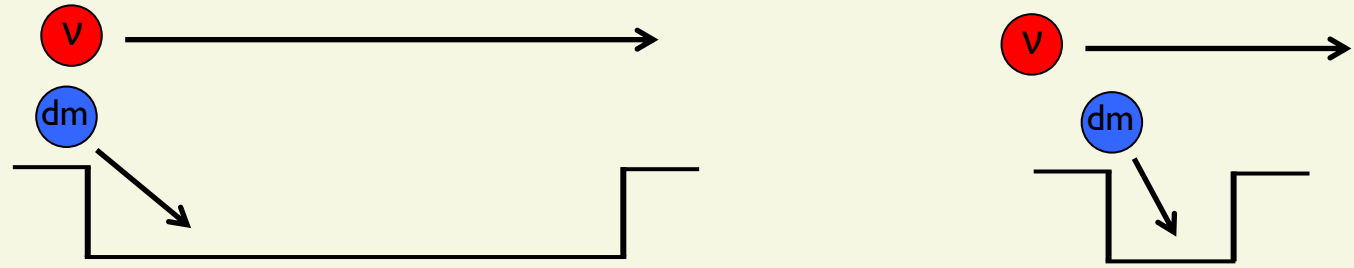
The effect of free streaming is to damp  $\delta_\nu$  on small scales.

- Before the transition :  $\lambda_{\text{FS}}$  grows like the Hubble radius (causal horizon for photons)
- After the transition :  $\lambda_{\text{FS}}$  decreases relatively to the Hubble radius

At the non-relativistic transition,  $\lambda_{\text{FS}}$  reaches a maximum value  $\lambda_{\text{nr}}$ .

$$k_{\text{nr}} = 0.018 \Omega_{\text{m}}^{1/2} \left( \frac{m_\nu}{1 \text{ eV}} \right)^{1/2} h/\text{Mpc}$$

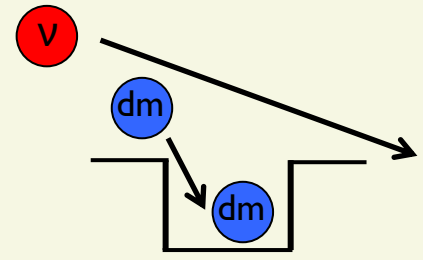
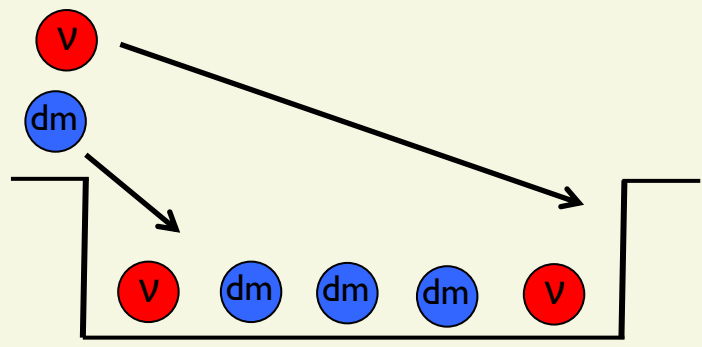
Before the transition (relativistic neutrinos) : Only CDM falls in the gravitational potential wells.



➡ Matter fluctuations are growing on all scales.

After the transition (non-relativistic neutrinos)

Free streaming  $\rightarrow$  neutrinos escape from the potential wells on small scales



For  $k < k_{nr}$ :  $\delta_{tot}$  is not affected by free streaming, because after the transition  $\delta_\nu$  behaves like  $\delta_{cdm}$ .

For  $k > k_{nr}$ :  $\delta_\nu$  do not contributes to  $\delta_{tot}$  because of the free streaming.

$$f_\nu = \frac{\Omega_\nu}{\Omega_m} \quad \Delta\Phi = 4\pi G a^2 \bar{\rho} \delta_{tot} = 4\pi G a^2 \bar{\rho} [(1 - f_\nu)\delta_{cdm} + f_\nu \delta_\nu]$$

$\rightarrow$  The matter power spectrum is damped for  $k > k_{nr}$

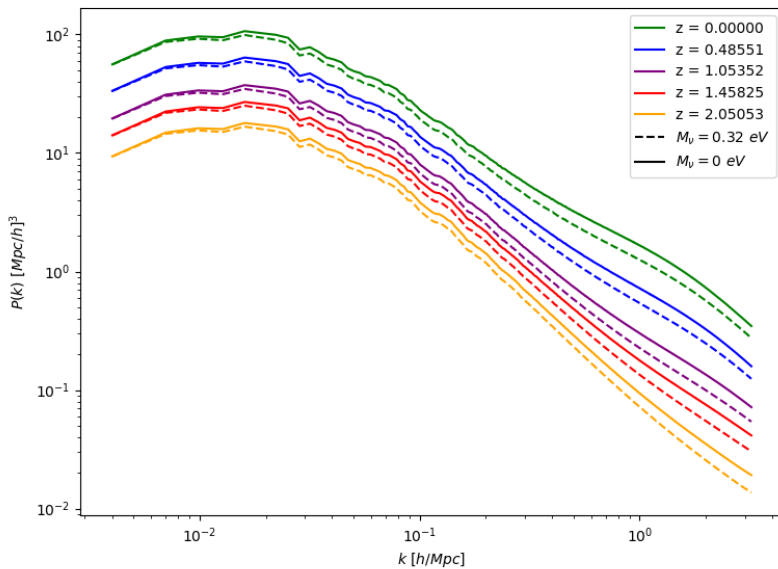


**DEMNUi** (Dark Energy and Massive Neutrino Universe) : Set of 11 simulations.

(Box with  $L = 2000 \text{ Mpc}/h$ )

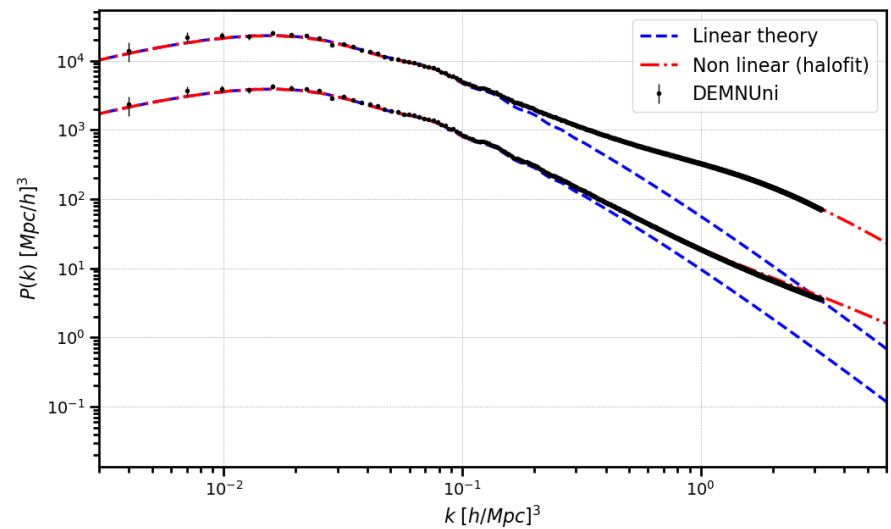
- **Massive neutrinos** :  $M_\nu = 0.00, 0.16, 0.32 \text{ eV}$
  - Different equations of state for the **dark energy** ( $w_0, w_a$ )
  - Number of particles :  $N_p^{cdm} = 2048^3 \sim 8.6 \cdot 10^9$  (+  $N_p^\nu = 2048^3 \sim 8.6 \cdot 10^9$ )
  - **Time evolution** with 5 redshifts :  $z = [0, 0.5, 1, 1.5, 2]$
- Managed by Carmelita Carbone in Milan.

DEMNUi  $P(k)$  for  $M_\nu = 0 \text{ eV}$  and  $M_\nu = 0.32 \text{ eV}$



Damping of the power spectrum on small scales.

Comparison with theory



Non linear evolution on small scales.

Estimating the power spectrum  $\longrightarrow$  estimating the amplitude of **density fluctuations** in **Fourier Space**.

[E.Sefusatti et al. 2015]

The estimator is :

$$\hat{P}(\mathbf{k}) = k_f^3 |\delta(\mathbf{k})|^2 \quad k_f = \frac{2\pi}{L}$$

There are two methods to estimate  $\delta(\mathbf{k})$

Estimating the power spectrum  $\longrightarrow$  estimating the amplitude of **density fluctuations** in **Fourier Space**.

[E.Sefusatti et al. 2015] The estimator is :  $\hat{P}(\mathbf{k}) = k_f^3 |\delta(\mathbf{k})|^2$   $k_f = \frac{2\pi}{L}$

There are two methods to estimate  $\delta(\mathbf{k})$

**Direct summation :**

$$\delta(\mathbf{k}) = \frac{1}{(2\pi)^3} \left[ \frac{1}{\bar{n}} \sum_i^{Np} e^{-i\mathbf{k}\cdot\mathbf{x}_i} - \delta_{\mathbf{k}}^K \right]$$

For each mode : take the contribution  
of **all the particles**

- **Pros :** No aliasing du to FFT
- **Cons :** (Extremely) time consuming

Estimating the power spectrum  $\rightarrow$  estimating the amplitude of **density fluctuations** in **Fourier Space**.

[E.Sefusatti et al. 2015] The estimator is :  $\hat{P}(\mathbf{k}) = k_f^3 |\delta(\mathbf{k})|^2 \quad k_f = \frac{2\pi}{L}$

There are two methods to estimate  $\delta(\mathbf{k})$

### Direct summation :

$$\delta(\mathbf{k}) = \frac{1}{(2\pi)^3} \left[ \frac{1}{\bar{n}} \sum_i^{Np} e^{-i\mathbf{k}\cdot\mathbf{x}_i} - \delta_{\mathbf{k}}^K \right]$$

For each mode : take the contribution of **all the particles**

- **Pros** : No aliasing du to FFT
- **Cons** : (Extremely) time consuming

### Sampling of the field + FFT :

Interpolate the particles on a grid  $\rightarrow \tilde{\delta}(\mathbf{x})$

Perform an FFT on it  $\rightarrow \tilde{\delta}(\mathbf{k})$

- **Pros** : Much faster
- **Cons** : The FFT induces **aliasing** for large k (near the Nyquist frequency)

Estimating the power spectrum  $\rightarrow$  estimating the amplitude of **density fluctuations** in **Fourier Space**.

[E.Sefusatti et al. 2015] The estimator is :  $\hat{P}(\mathbf{k}) = k_f^3 |\delta(\mathbf{k})|^2$   $k_f = \frac{2\pi}{L}$

There are two methods to estimate  $\delta(\mathbf{k})$

**Direct summation :**

$$\delta(\mathbf{k}) = \frac{1}{(2\pi)^3} \left[ \frac{1}{\bar{n}} \sum_i^{Np} e^{-i\mathbf{k}\cdot\mathbf{x}_i} - \delta_{\mathbf{k}}^K \right]$$

For each mode : take the contribution of **all the particles**

- **Pros :** No aliasing du to FFT
- **Cons :** (Extremely) time consuming

My code

**Sampling of the field + FFT :**

Interpolate the particles on a grid  $\rightarrow \tilde{\delta}(\mathbf{x})$

Perform an FFT on it  $\rightarrow \tilde{\delta}(\mathbf{k})$

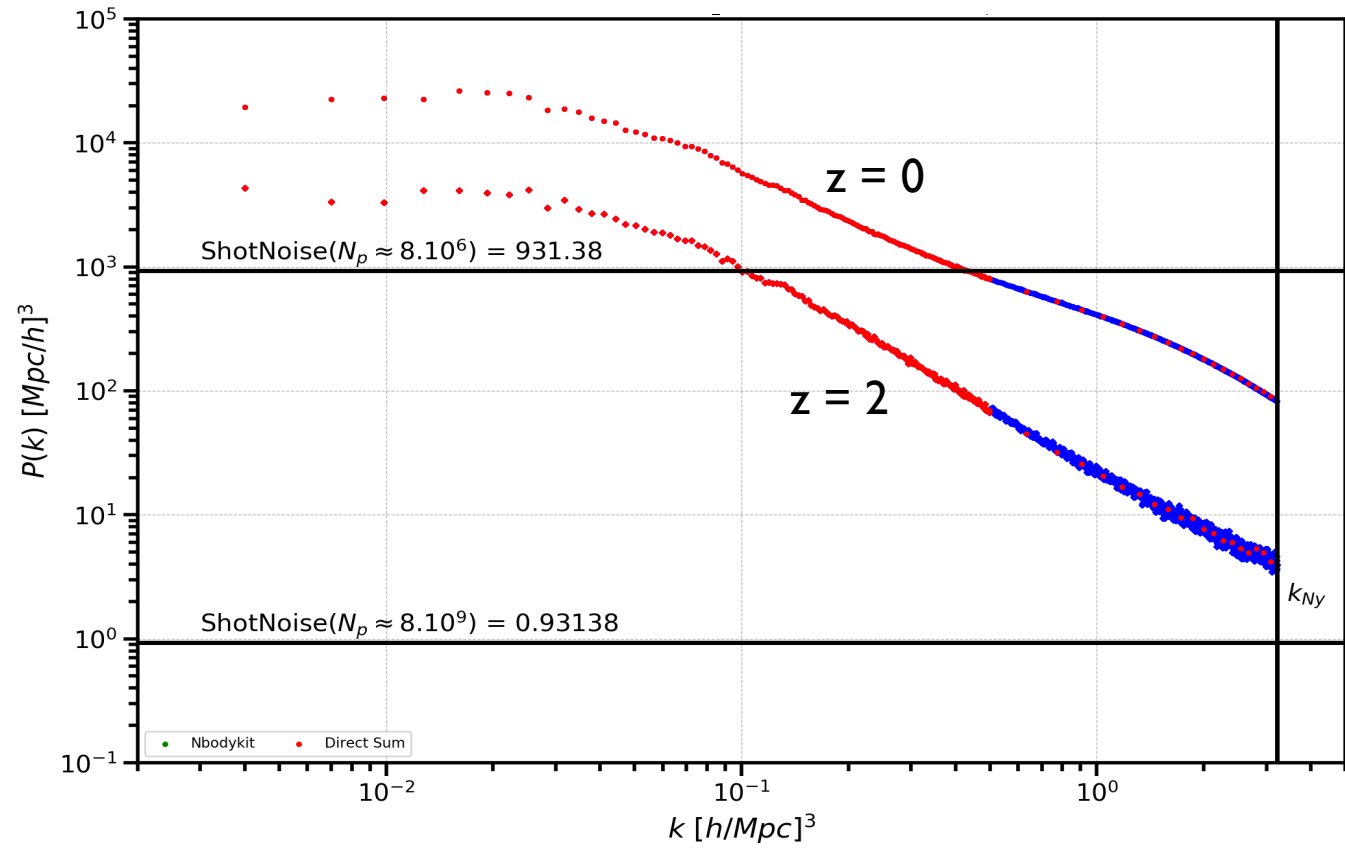
- **Pros :** Much faster
- **Cons :** The FFT induces **aliasing** for large k (near the Nyquist frequency)

Public code NbodyKit  
[N. Hand et al. 2017]

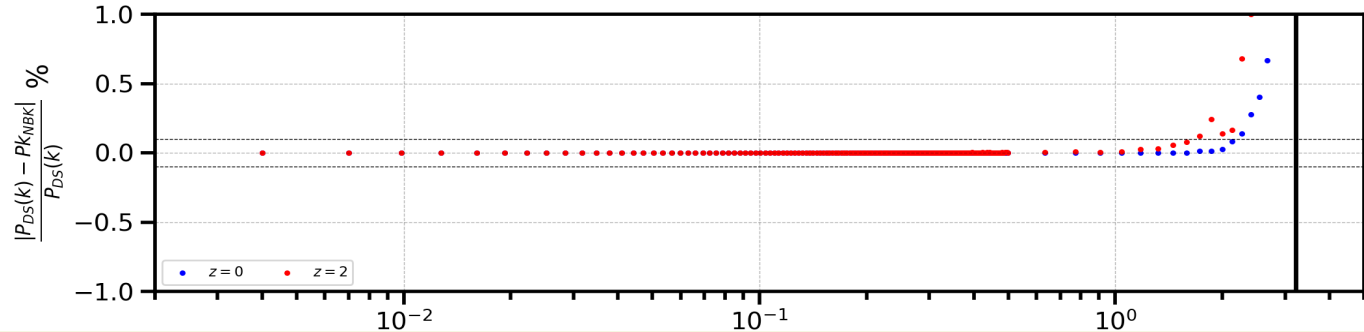
Validation of Nbodykit with my code using direct summation on the DEMNUni.

## II. The power spectra of the DEMNUni simulations

Comparison between NbodyKit and Direct Sumation for  $N_p = 8.10^6$  particles



The relative difference is below 0.1 % up to  $k \sim 1 h/\text{Mpc}$



#### Set-up for the parameter estimation using MCMC on the DEMNUni spectra :

- Choosing the simulation with  $M_\nu = 0.32 \text{ eV}$  ( $m_\nu = 0.107 \text{ eV}$ )
- Theoretical predictions ➡ class with **halofit**
- Errors on the power spectrum ➡ **Gaussian theoretical errors** (no covariance)

$$\sigma(k) = \frac{k_f P(k)}{k \sqrt{2\pi}}$$

- Using the **5 redshifts**  $z = [0, 0.5, 1, 1.5, 2]$
- Considering  $P(k)$  up to a certain  $k_{\text{max}}$ .

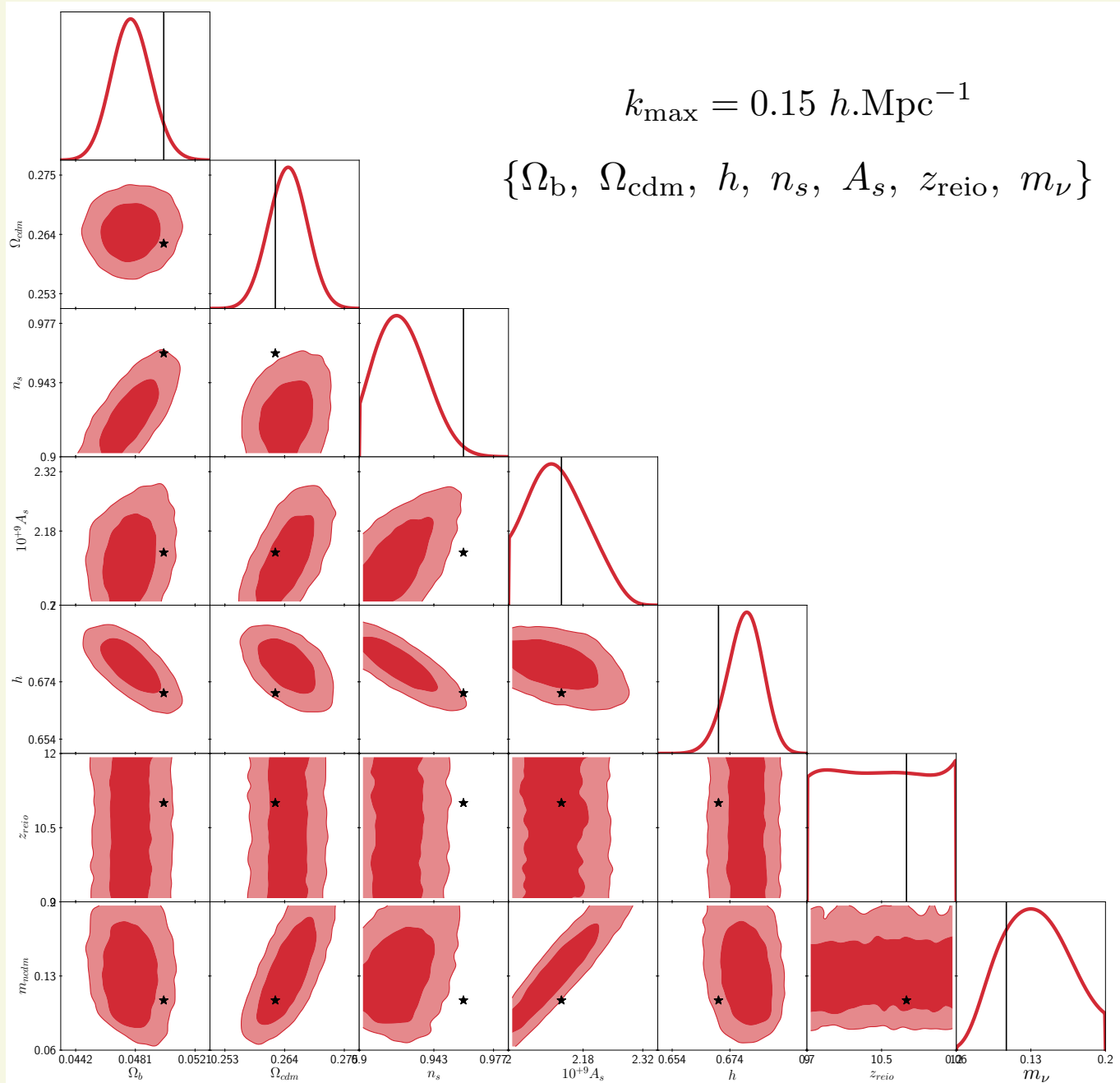
$$\{\Omega_b, \Omega_{\text{cdm}}, h, n_s, A_s, z_{\text{reio}}, m_\nu\}$$

- Set of parameters to estimate :

Or

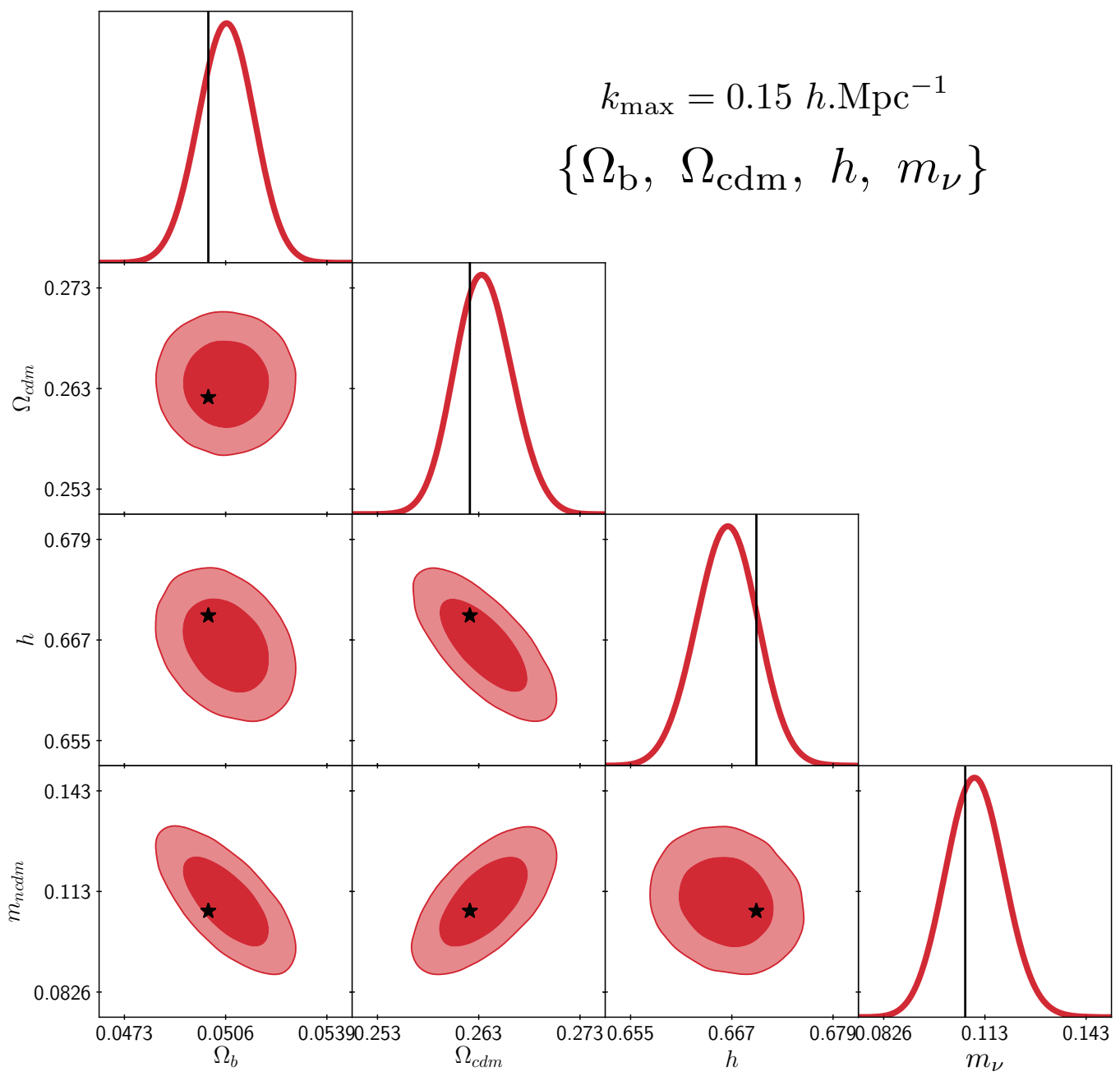
$$\{\Omega_b, \Omega_{\text{cdm}}, h, m_\nu\}$$

### III. Parameter estimation on the DEMNUni spectra

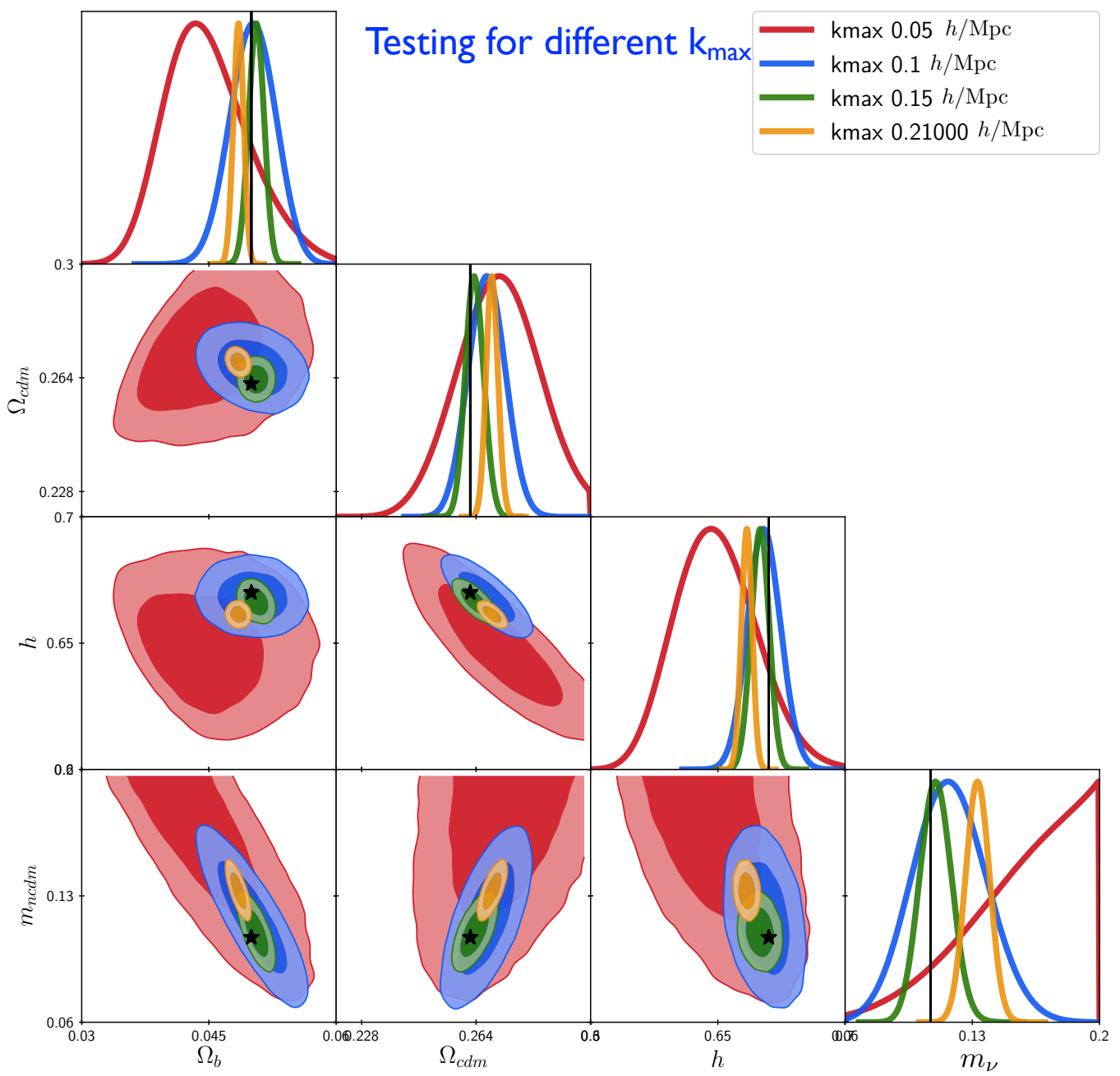




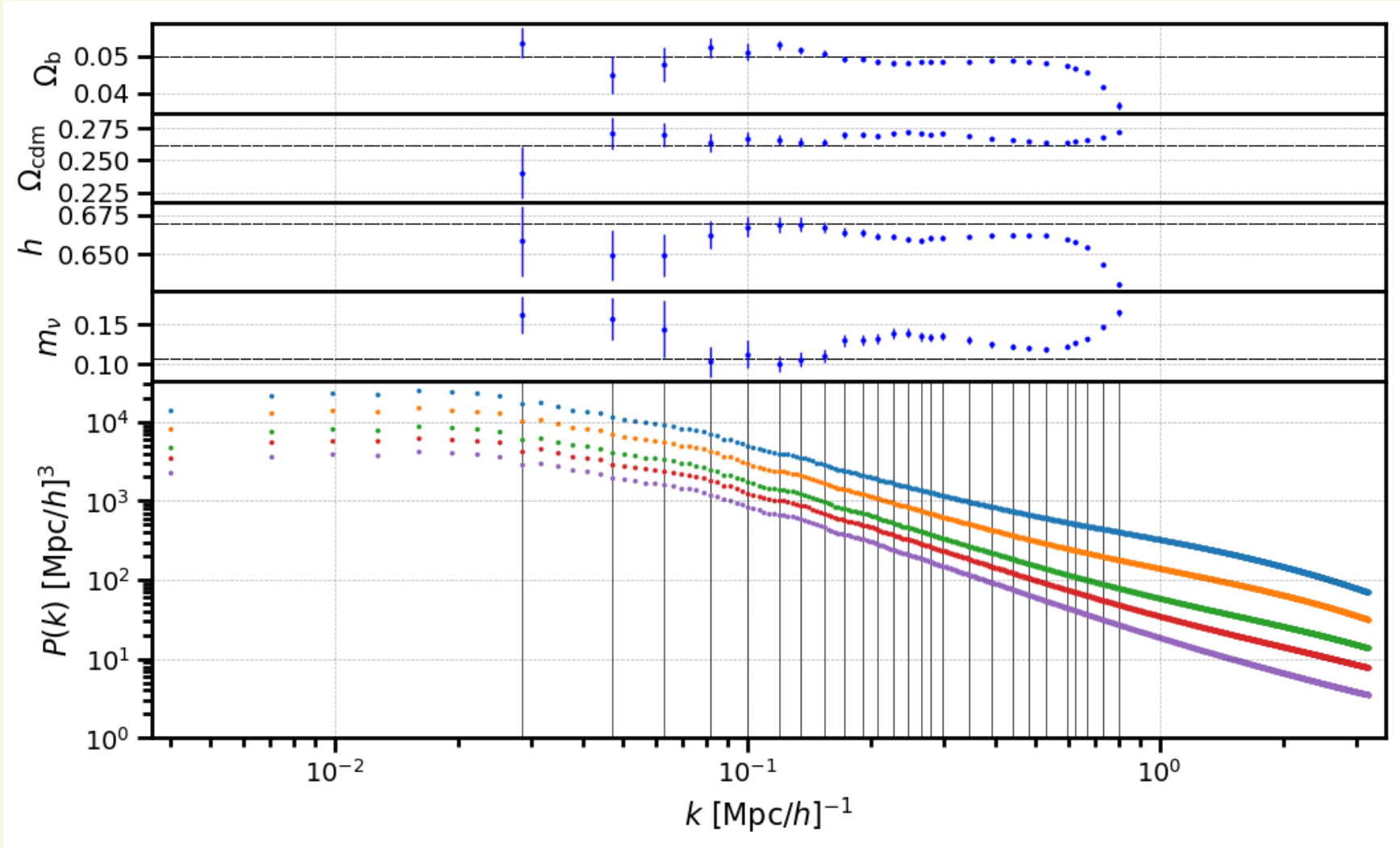
### III. Parameter estimation on the DEMNUni spectra



### III. Parameter estimation on the DEMNUni spectra



#### Testing for different $k_{\max}$



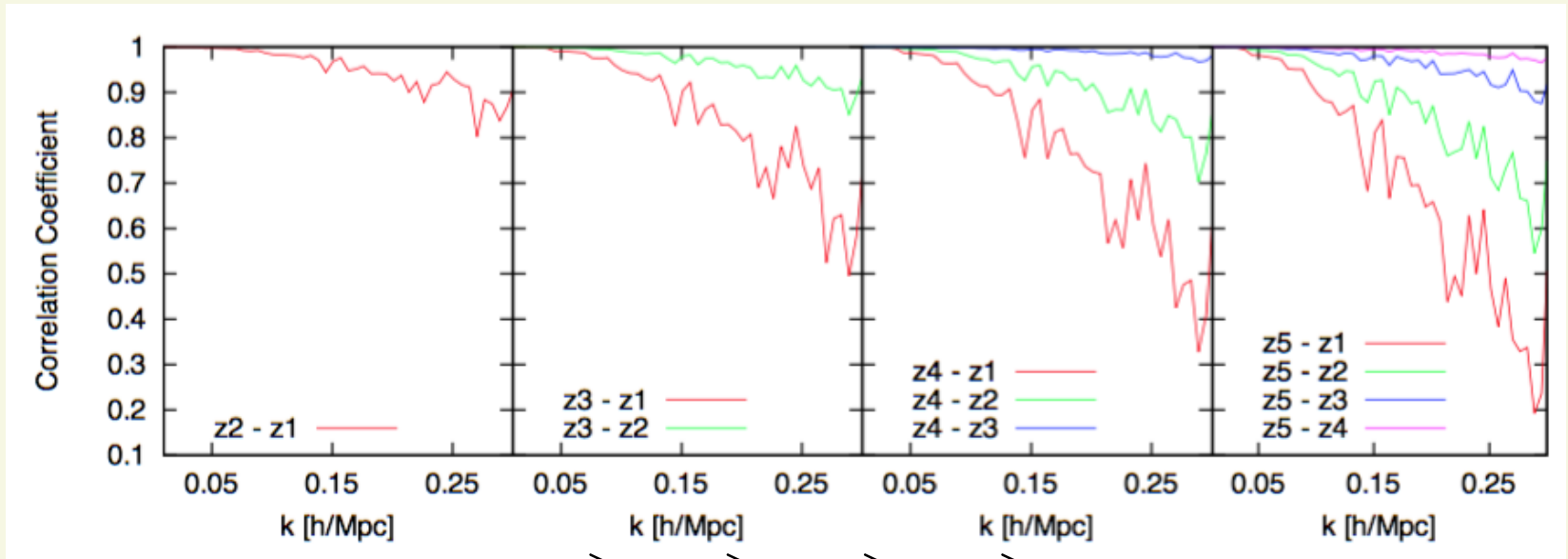
The error bars should be larger if we include the covariance.

### III. Parameter estimation on the DEMNUni spectra

Set of 50 smaller **independent realizations** to compute the **covariance matrix**.

**Snapshot problem** : One realization evolving with time  $\rightarrow$  **High correlation between the redshifts**.

Considering only the correlation for the same modes at different redshifts :  $\rho(k; z_i, z_j)$



$$z_5 > z_4 > z_3 > z_2 > z_1$$

- High correlation for linear scales.
- Consecutive redshifts  $\rightarrow$  high correlations.
- Small correlation at late times  $\rho(z_1, z_2) < \rho(z_4, z_5)$  : information is lost in non-linearities.

$\rho \sim 1 \rightarrow$  **The covariance matrix is almost singular.**

## Possible Solutions :

- Take 5 independent realizations for the 5 redshifts ➡ Remove the correlation.
- Create more simulations to divide the set of realizations in 5 subsets corresponding to the 5 redshifts ➡ Independent set for each  $z$ .
- Use Monte Carlo semi-analytique methods to predict the covariance matrix (see Philippe's talk). [Baratta et al. 2019]
- Jackknife.

**BACK UP**

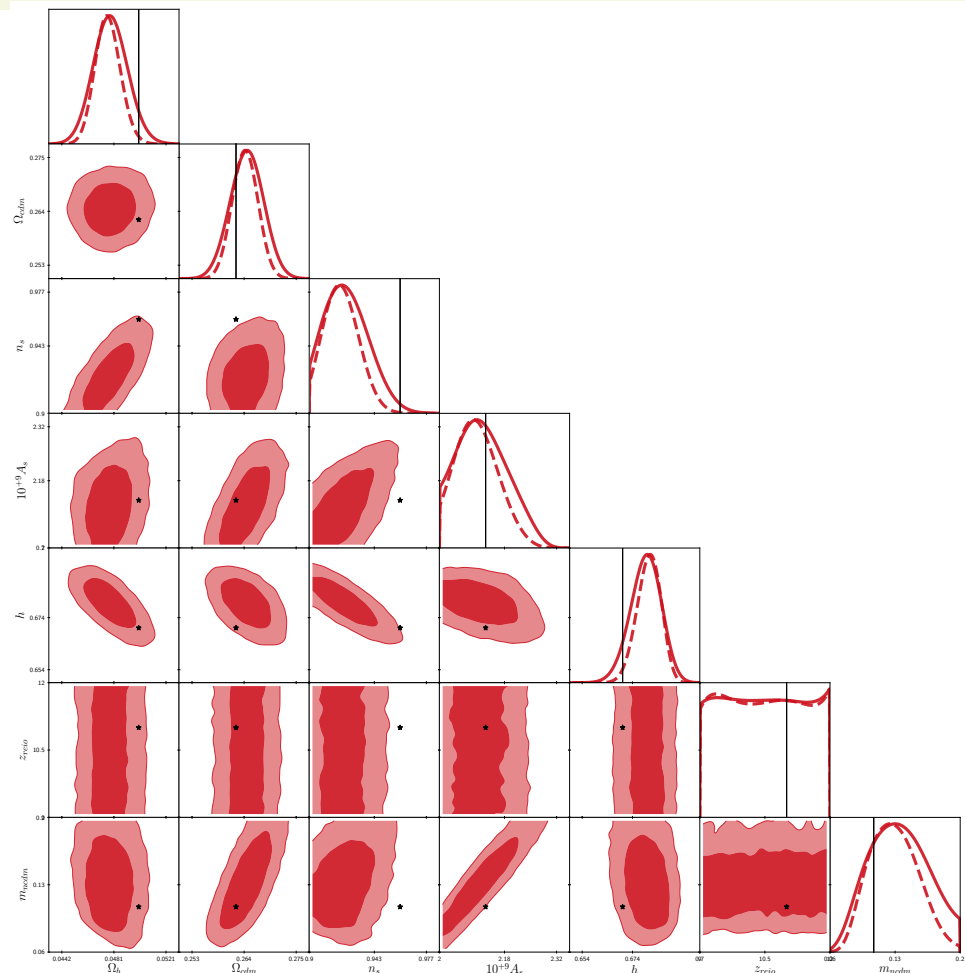
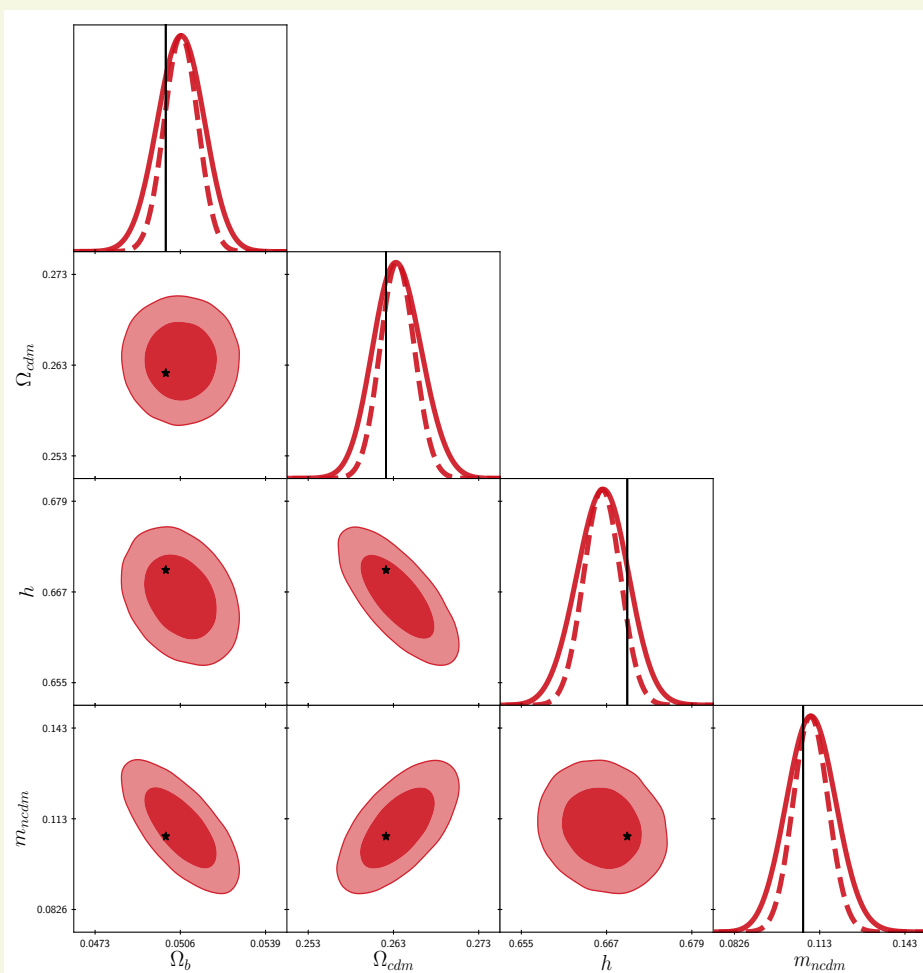
# Étude sur $\{n_s, A_s, z_{\text{reio}}\}$

With MontePython

$$k_{\text{max}} = 0.15 \text{ h.Mpc}^{-1}$$

Fixed =  $\{\Omega_b, \Omega_{\text{cdm}}, h, m_\nu\}$

All free =  $\{\Omega_b, \Omega_{\text{cdm}}, h, n_s, A_s, z_{\text{reio}}, m_\nu\}$



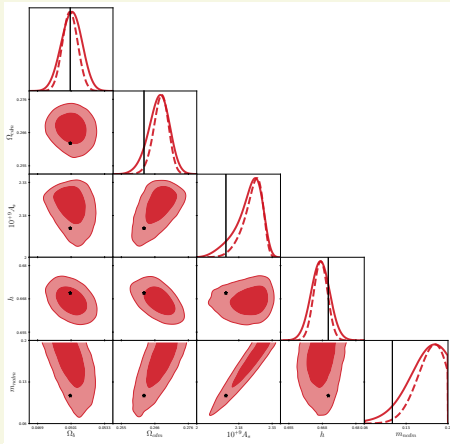
# Étude sur $\{n_s, A_s, z_{\text{reio}}\}$

With MontePython

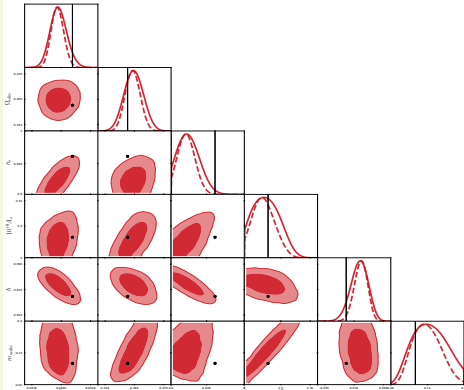
$$k_{\text{max}} = 0.15 \text{ h.Mpc}^{-1}$$

**$A_s$**

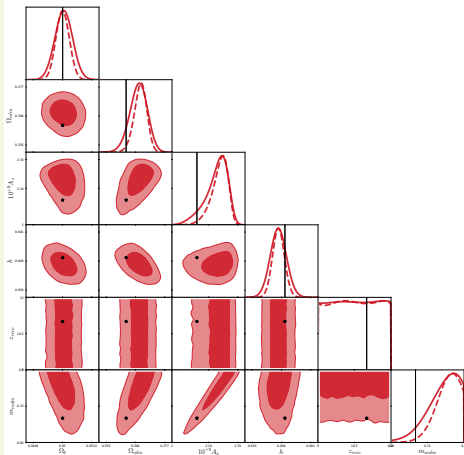
**$A_s$**



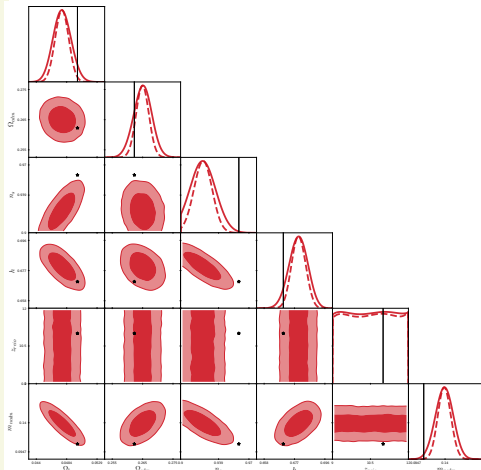
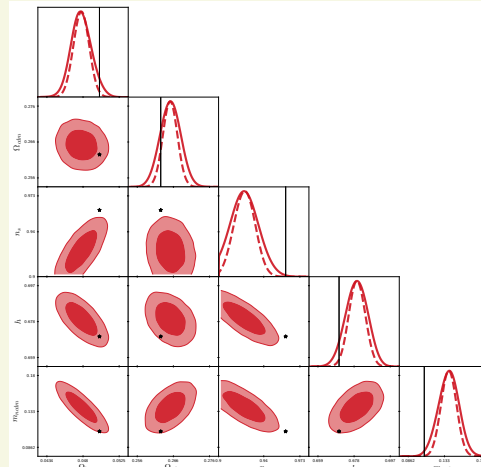
**$n_s$**



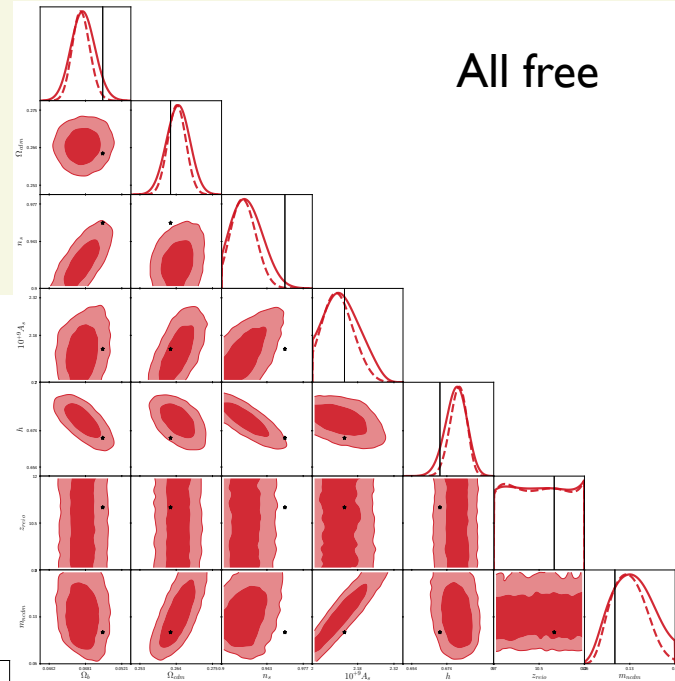
**$z$**



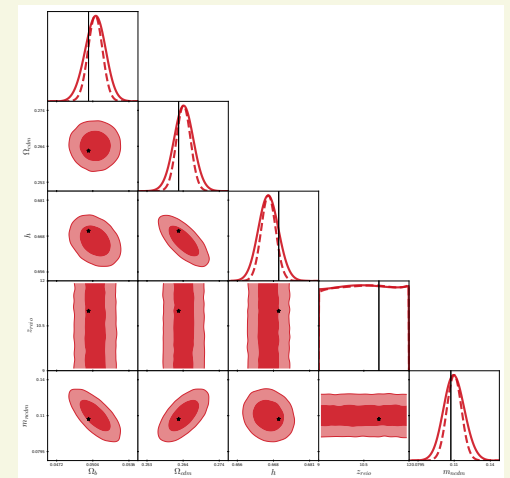
**$n_s$**



**All free**



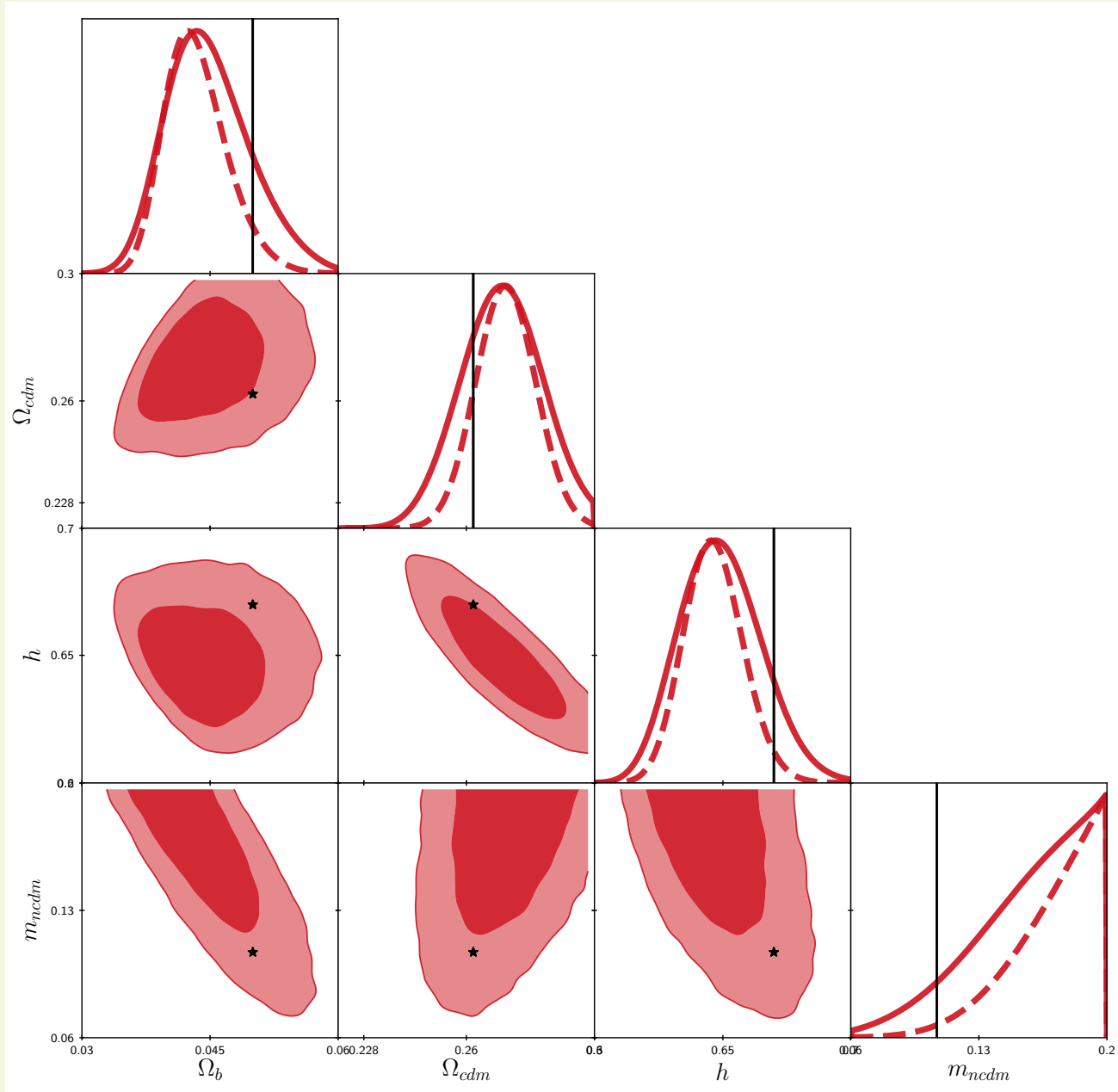
**$z$**





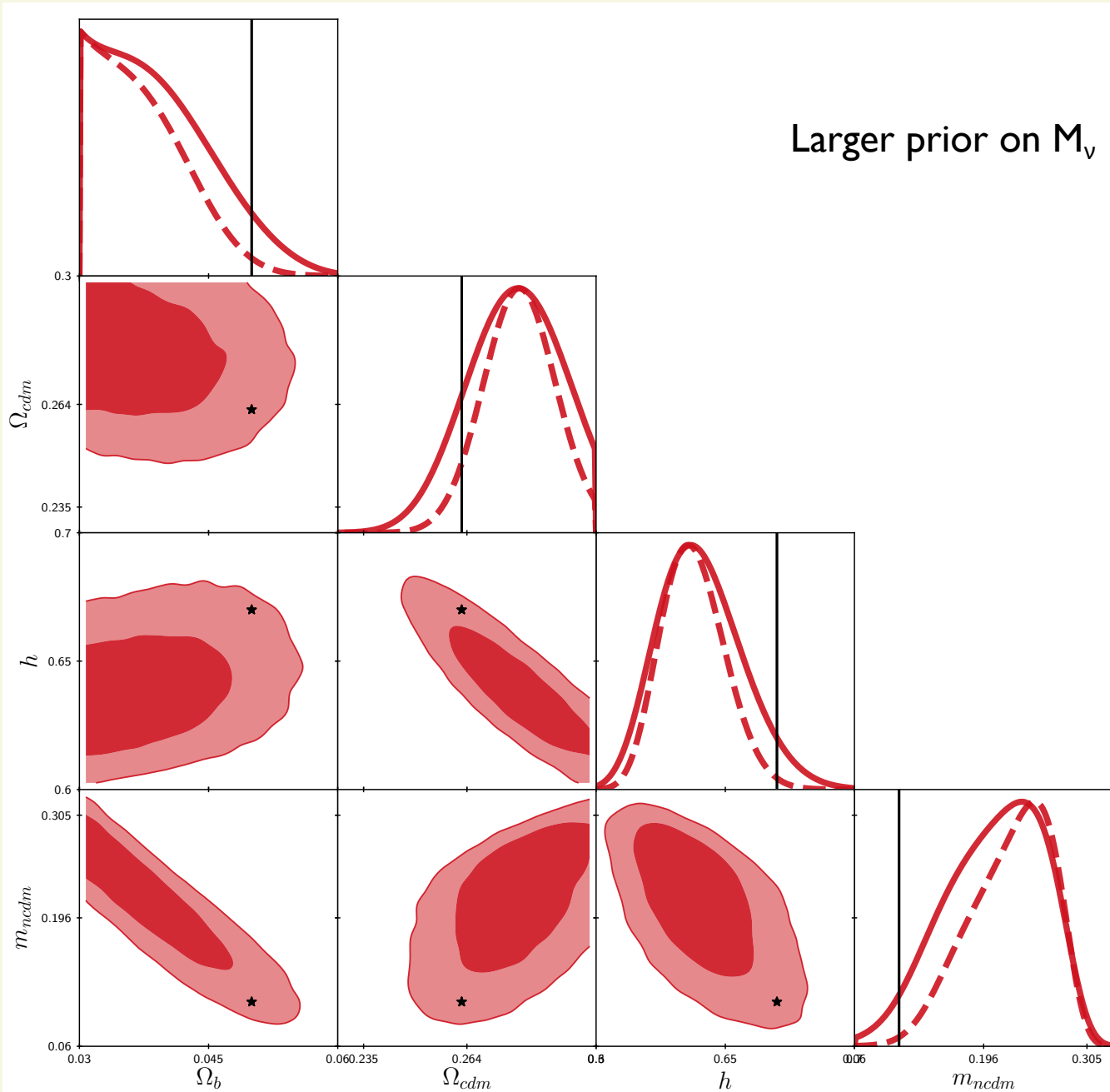
# Dégénérescence entre $\Omega_b$ et $m_\nu$

$$k_{\max} = 0.05 \text{ h.Mpc}^{-1}$$



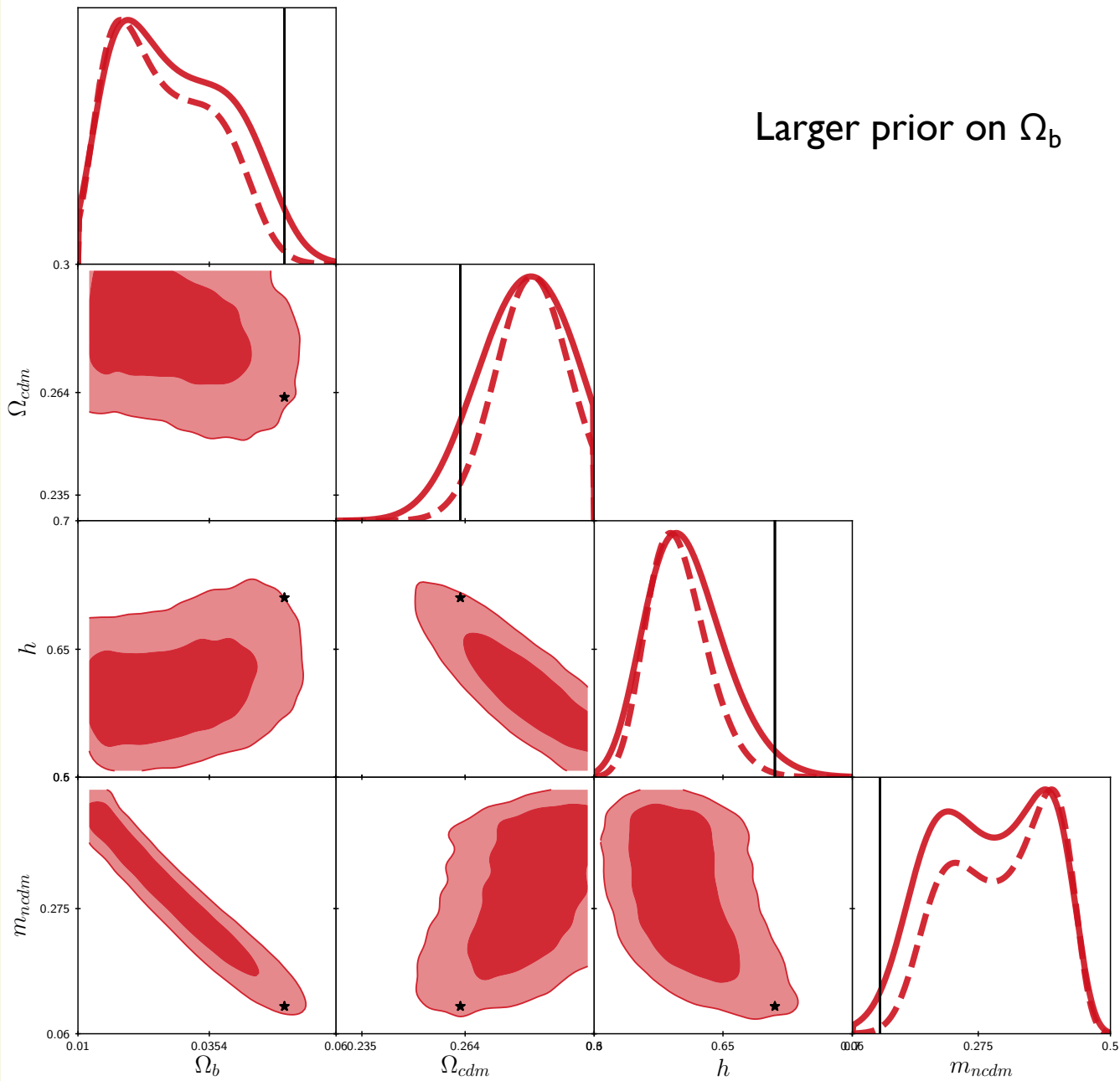
# Dégénérescence entre $\Omega_b$ et $m_\nu$

$$k_{\max} = 0.05 \text{ h.Mpc}^{-1}$$



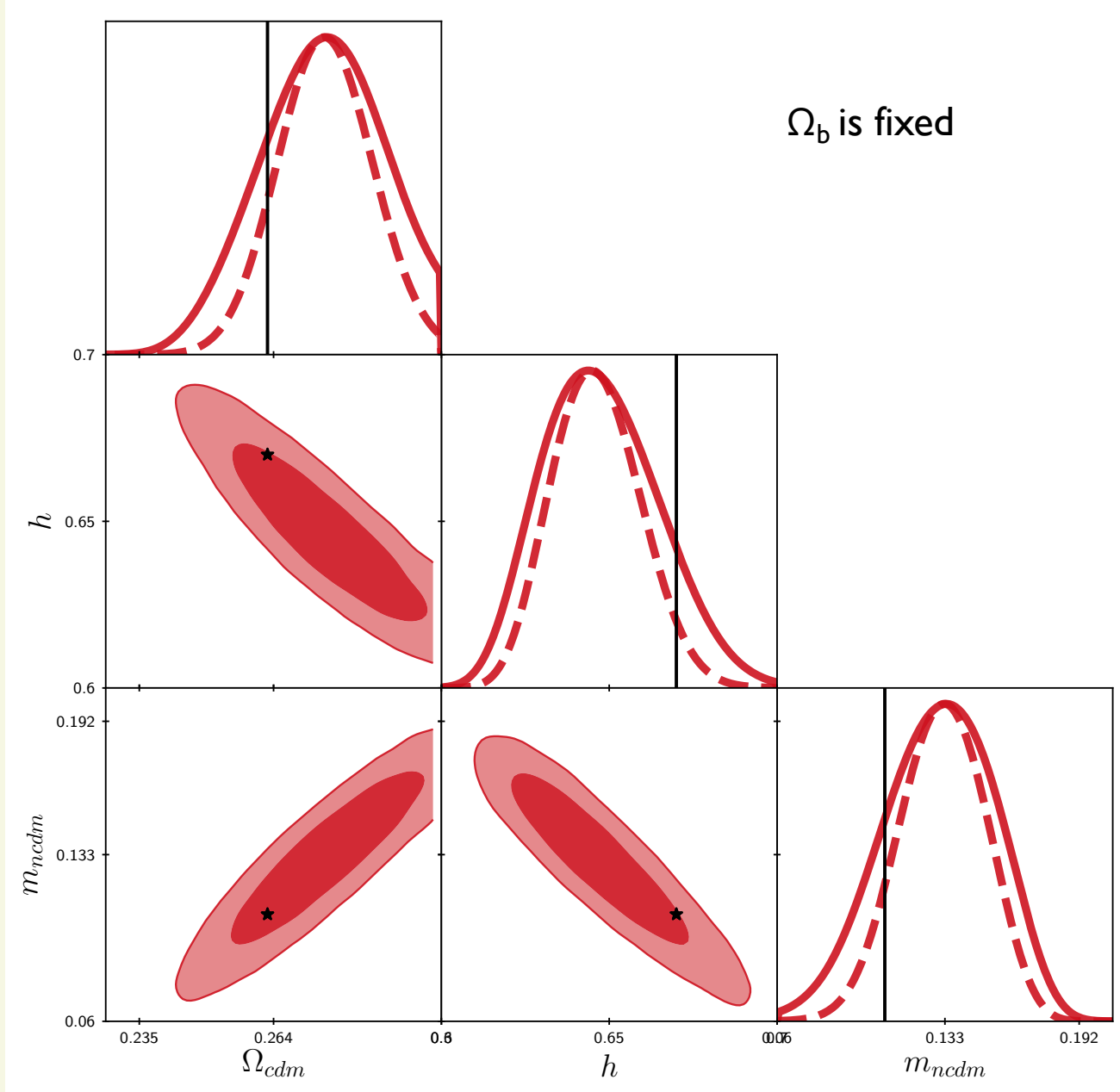
# Dégénérescence entre $\Omega_b$ et $m_\nu$

$$k_{\max} = 0.05 \text{ h.Mpc}^{-1}$$



# Dégénérescence entre $\Omega_b$ et $m_\nu$

$$k_{\max} = 0.05 \text{ h.Mpc}^{-1}$$



## Bibliographic study :

« State of the art » on the cosmological total neutrino mass constraints.

### Focus on 3 papers :

- G-B. Zhao et al. 2013
- A.J. Cuesta et al. 2016
- N. Palanque-Delabrouille et al. 2015

# CMB constraints

- If neutrinos become non-relativistic **before** the CMB emission ➡ direct effect on the CMB temperature power spectrum.

We don't see the effect ➡

$$\left. \begin{aligned} 1 + z_{\text{nr}} &= 1890 \left( \frac{m_\nu}{1 \text{ eV}} \right) \\ z_{\text{CMB}} &= 1100 \end{aligned} \right\} \begin{aligned} m_\nu &\lesssim 0.58 \text{ eV} \\ M_\nu &\lesssim 1.7 \text{ eV} \end{aligned}$$

- For any neutrino mass there are effects due to secondary anisotropies (CMB lensing and Integrated Sachs Wolff) and background effects.

Planck 2015 (TT,TE,EE + lowP + lensing) ➡  $M_\nu < 0.59 \text{ eV}$

# Power spectrum constraints

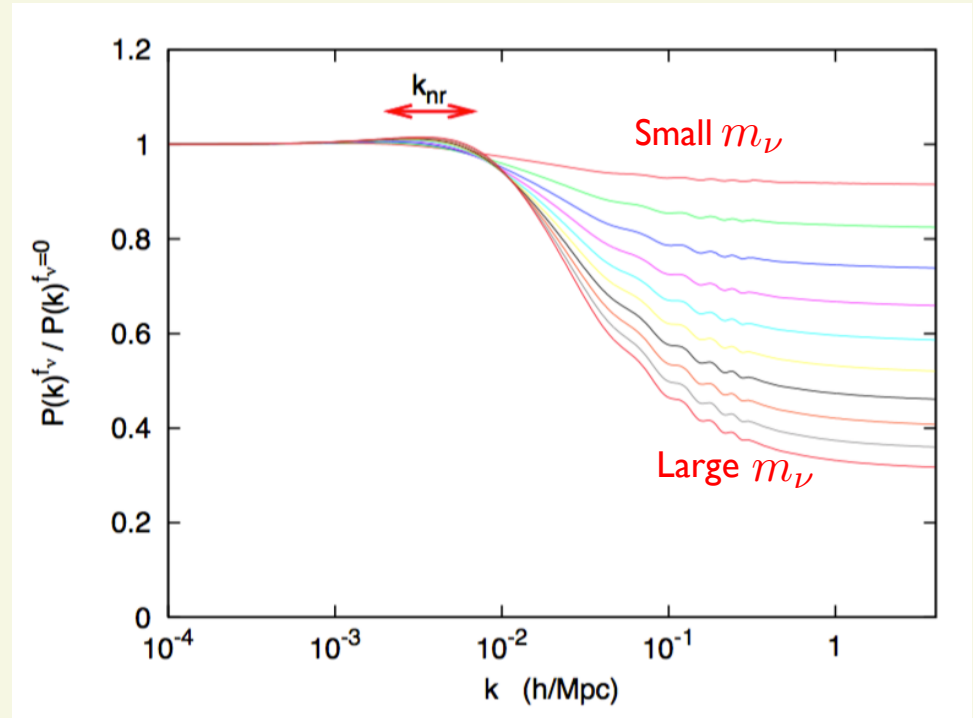
The power spectrum should be the most sensitive probe.



Add  $P(k)$  constraining power to CMB.

Focus on 3 papers :

- (1) Zhao et al. 2013 : **Galaxy** power spectrum using BOSS DR9 →  $M_\nu < 0.34$  eV
- (2) Cuesta et al. 2016 : **Halo** power spectrum using BOSS DR7 →  $M_\nu < 0.13$  eV
- (3) P-Delabrouille et al. 2015 : **Ly- $\alpha$**  power spectrum using BOSS DR9 →  $M_\nu < 0.12$  eV

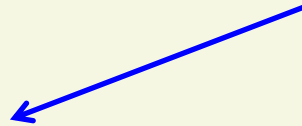


In all cases they choose to have three degenerate massive neutrinos.

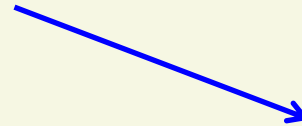
# Paper (I) : Galaxy power spectrum (BOSS DR9)

Main systematics : **Bias** determination, **RSD** and **non-linearities** modeling.

2 ways to handle the problem.



Perturbation theory (SPT)



Fitting formula

Based on N-body simulation.

**Halofit.**

$$P_m^L(k) \longrightarrow P_m^{\text{NL}}(k) \longrightarrow P_g(k) \longrightarrow P_g^S(k)$$

Can go up to different orders for each step.



# Paper (I) : Galaxy power spectrum (BOSS DR9)

Main systematics : Bias determination, RSD and non-linearities modeling.

2 ways to handle the problem.

Perturbation theory (SPT)

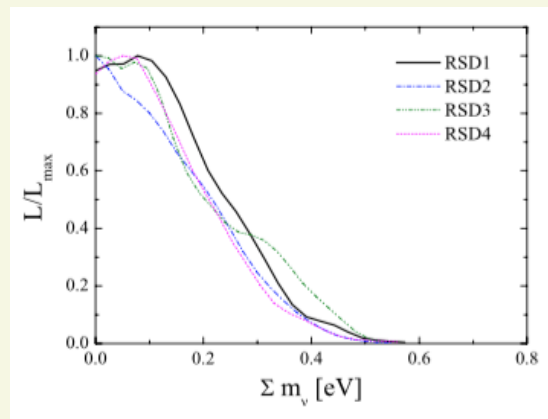
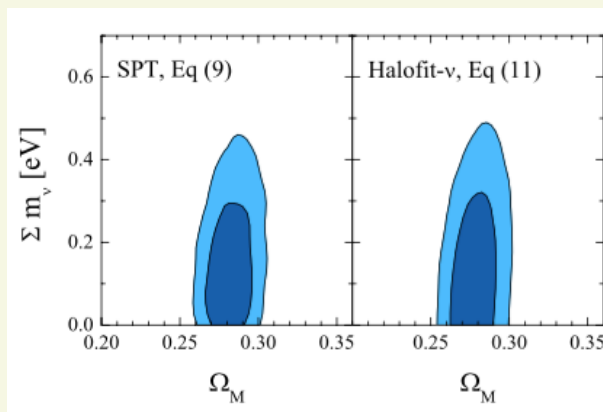
Fitting formula

Based on N-body simulation.

Halofit.

$$P_m^L(k) \rightarrow P_m^{\text{NL}}(k) \rightarrow P_g(k) \rightarrow P_g^S(k)$$

Can go up to different orders for each step

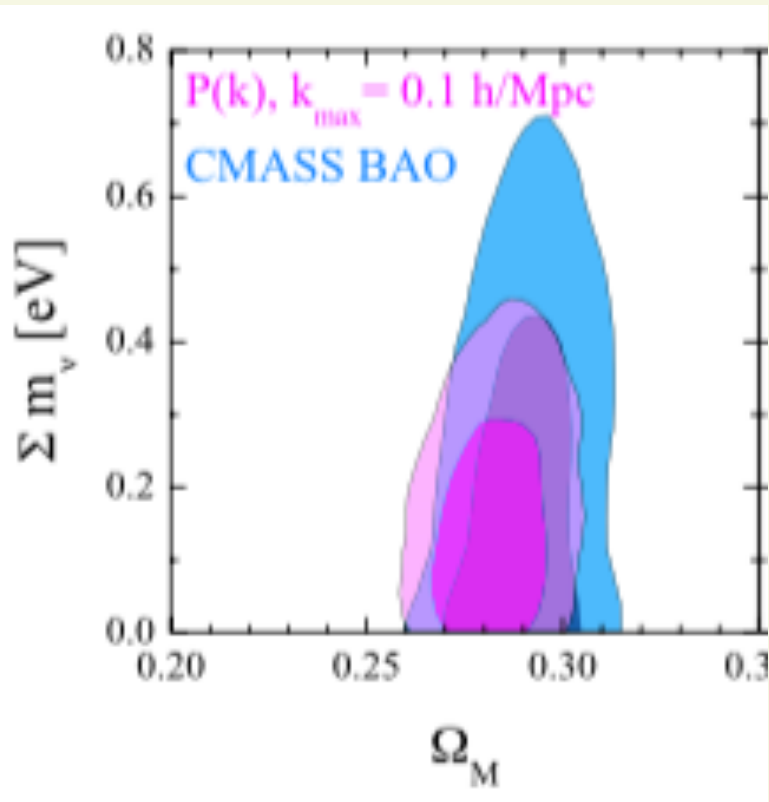


$$0.01 < k < 0.1 \text{ Mpc}^{-1} h$$

In the end they choose to use the simplest perturbation theory model.

# Paper (I) : Galaxy power spectrum (BOSS DR9)

BAO peak constraining power :



$M_\nu < 0.579 \text{ eV}$  For WMAP7 + SNLS3 + BAO

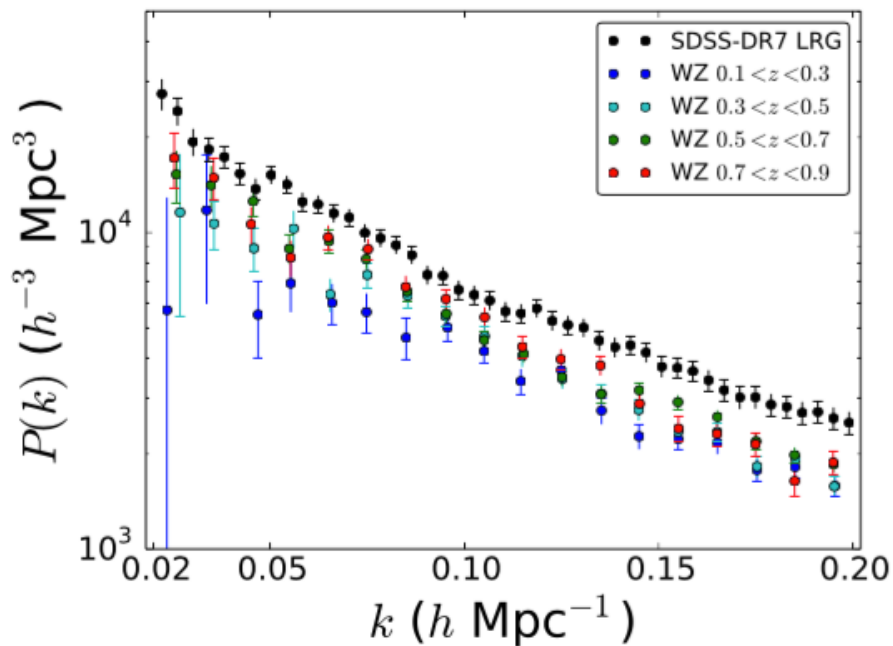
$M_\nu < 0.340 \text{ eV}$  For WMAP7 + SNLS3 + P(k)  
(+ all BAO measurement expect BOSS)

# Paper (2) : Halo power spectrum (BOSS DR7)

Combination and comparison for :  
halo  $P(k)$  from DR7 LRG and galaxy  $P(k)$  from WiggleZ ELG.



Using the halo power spectrum reduces systematics from non-linearities and RSD.  
(investigate more on this ?)

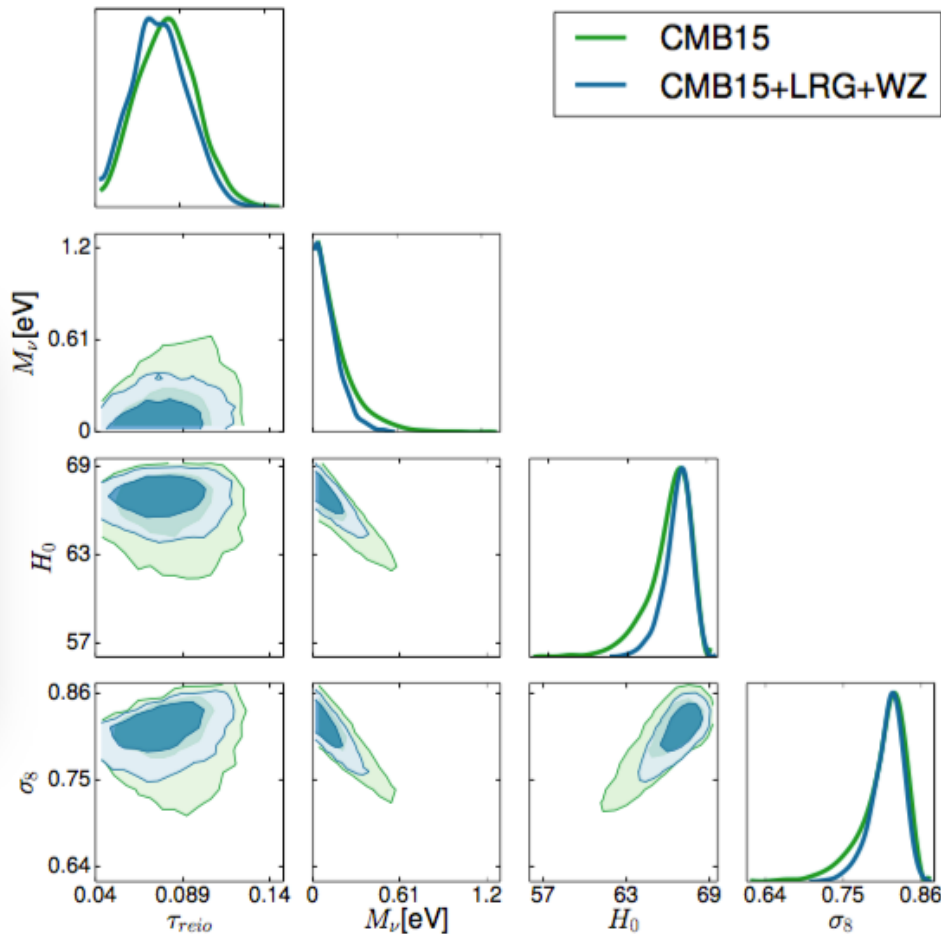


Data sets	$M_\nu$ at 95% CL
CMB15 + LRG	0.38 eV
CMB15 + WZ	0.37 eV
CMB15 + LRG + WZ	0.30 eV
CMB15 + LRG + BAO	0.13 eV
CMB15 + WZ + BAO	0.14 eV
CMB15 + LRG + WZ + BAO	0.14 eV

- Always combined with CMB (Planck).
- BAO greatly improves the constraint.

# Paper (2) : Halo power spectrum (BOSS DR7)

## CMB / Power spectrum

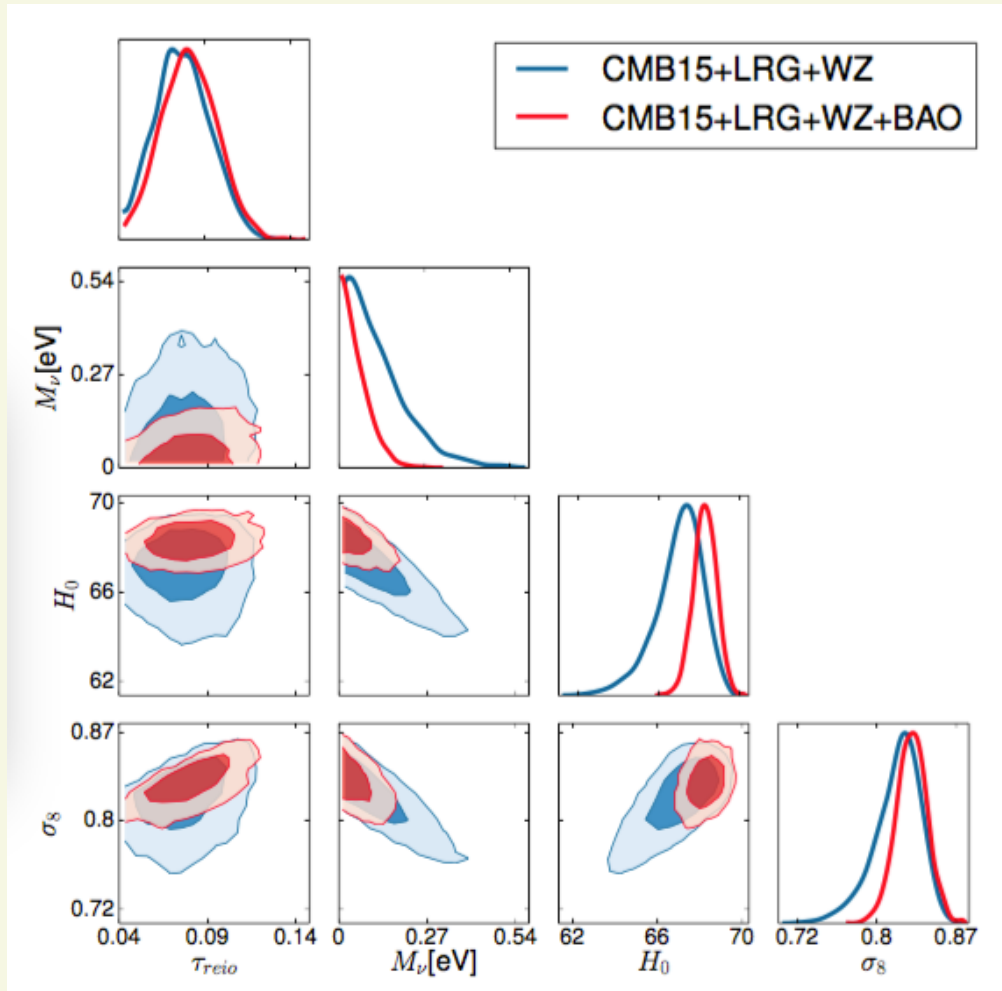


CMB alone :  $M_\nu < 0.59$  eV

Data sets	$M_\nu$ at 95% CL
CMB15 + LRG	0.38 eV
CMB15 + WZ	0.37 eV
CMB15 + LRG + WZ	0.30 eV
CMB15 + LRG + BAO	0.13 eV
CMB15 + WZ + BAO	0.14 eV
CMB15 + LRG + WZ + BAO	0.14 eV

# Paper (2) : Halo power spectrum (BOSS DR7)

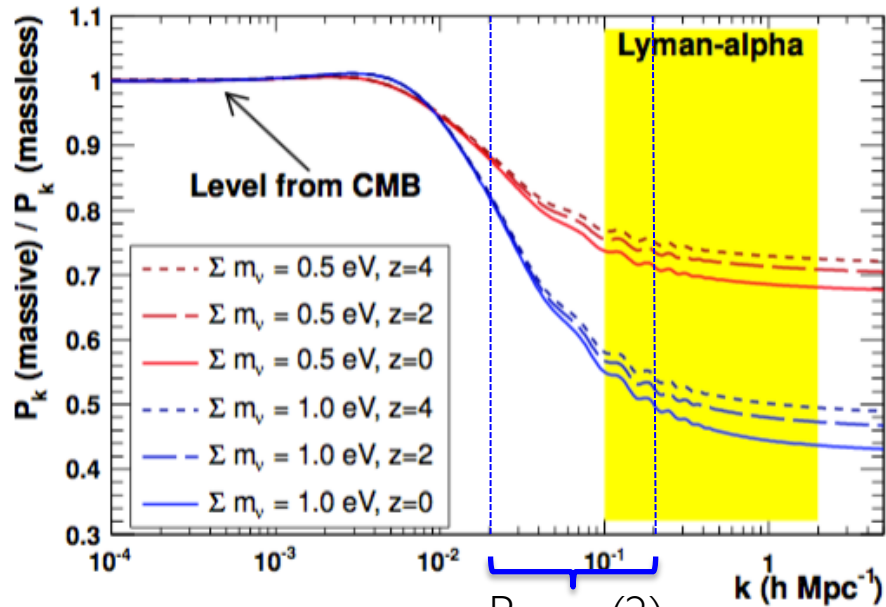
Power spectrum / BAO peak



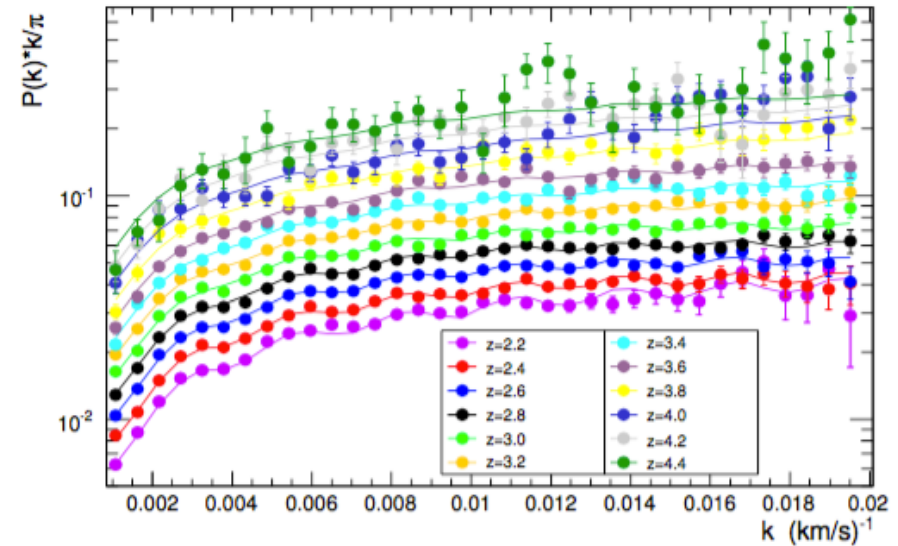
Data sets	$M_\nu$ at 95% CL
CMB15 + LRG	0.38 eV
CMB15 + WZ	0.37 eV
CMB15 + LRG + WZ	0.30 eV
CMB15 + LRG + BAO	0.13 eV
CMB15 + WZ + BAO	0.14 eV
CMB15 + LRG + WZ + BAO	0.14 eV

Break the degeneracy with  $H_0$  and  $\sigma_8$ .

# Paper (3) : Ly- $\alpha$ power spectrum (BOSS DR9)



Paper (2)



Different probe/tracer  $\rightarrow$  Different analysis and different systematics.

- Astrophysical systematics : optical depth, absorbers (Si II or Si III), heating rate of IGM.
- Noise and resolution on the spectra.
- Hydrodynamical simulation technique (instead of using Boltzmann solvers like CLASS or CAMB).

# Paper (3) : Ly- $\alpha$ power spectrum (BOSS DR9)

## Results

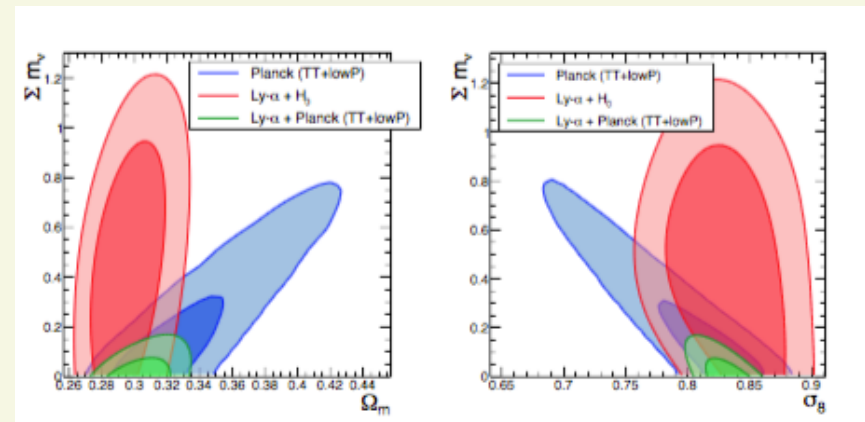
Parameter	(1) Ly $\alpha$ + $H_0^{\text{Gaussian}}$ ( $H_0 = 67.3 \pm 1.0$ )	(2) Ly $\alpha$ + Planck TT+lowP	(3) Ly $\alpha$ + Planck TT+lowP + BAO	(4) Ly $\alpha$ + Planck TT+TE+EE+lowP + BAO
$\sigma_8$	$0.831 \pm 0.031$	$0.833 \pm 0.011$	$0.845 \pm 0.010$	$0.842 \pm 0.014$
$n_s$	$0.938 \pm 0.010$	$0.960 \pm 0.005$	$0.959 \pm 0.004$	$0.960 \pm 0.004$
$\Omega_m$	$0.293 \pm 0.014$	$0.302 \pm 0.014$	$0.311 \pm 0.014$	$0.311 \pm 0.007$
$H_0$ (km s $^{-1}$ Mpc $^{-1}$ )	$67.3 \pm 1.0$	$68.1 \pm 0.9$	$67.7 \pm 1.1$	$67.7 \pm 0.6$
$\sum m_\nu$ (eV)	$< 1.1$ (95% CL)	$< 0.12$ (95% CL)	$< 0.13$ (95% CL)	$< 0.12$ (95% CL)
Reduced $\chi^2$	0.99	1.04	1.05	1.05

With Ly- $\alpha$  alone : need a prior for  $H_0$   $\rightarrow M_\nu < 1.1$  eV.

Still need the CMB.

No need for BAO to have the best actual constraint :

$$M_\nu < 0.12 \text{ eV}$$



# Conclusion

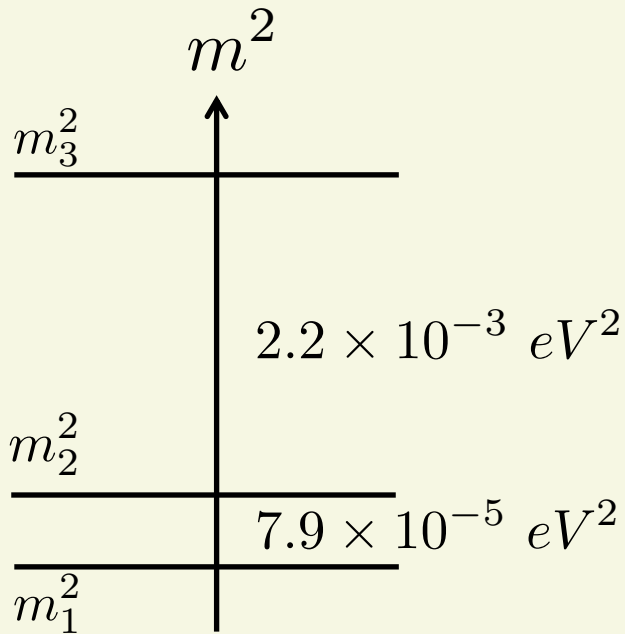
- We need the information from the CMB and the BAO peak to have tight constraints on  $M_\nu$  with the galaxy power spectrum because of the systematics and the degeneracies.
- The actual limits are getting closer to the Inverted Hierarchy limit ( $M_\nu < 0.1$  eV).
- Future : Effect of the neutrino mass ordering (only with high precision measurements) ? Sterile neutrinos with cosmology ? Neutrinos with different Dark Energy scenarios (Possible degeneracies) ?



# Hiérarchie de masse des neutrinos

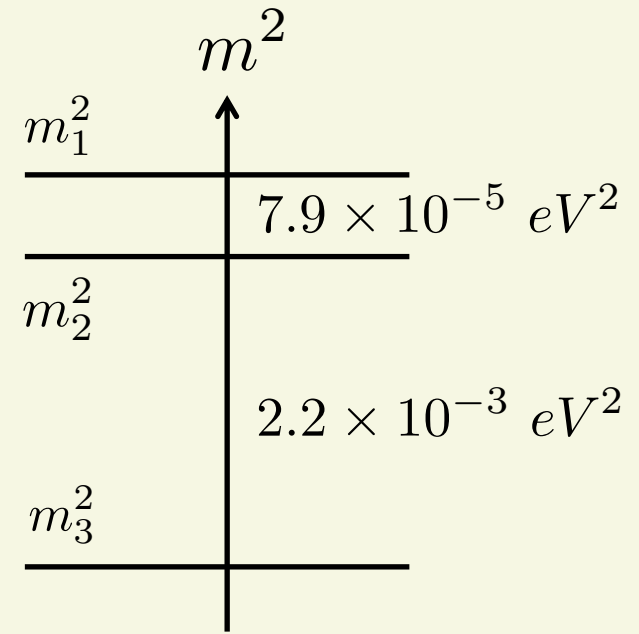
Les expériences d'oscillations mesurent  $\Delta m_{ij}^2 = m_i^2 - m_j^2$

➡ 2 hiérarchies possibles.



Normale

$$\sum m_\nu > 0.056 eV$$



Inversée

$$\sum m_\nu > 0.095 eV$$

# Sommation Direct

## 2.2 Direct summation

Theoretical predictions for the correlation functions of the matter density, or of the galaxy number density, often assume such quantities to be continuous random fields. However, in practical applications such as the analysis of N-body simulations or galaxy surveys they are given in terms of a finite number  $N_P$  of objects with positions  $\{\mathbf{x}_i\}$  for  $i = 1, \dots, N_P$ . In this case we can write the density as

$$\rho(\mathbf{x}) = \sum_{i=1}^{N_P} m \delta_D(\mathbf{x} - \mathbf{x}_i), \quad (6)$$

$m$  being the particle mass which we assume here to be the same for all particles, for simplicity. It follows that

$$\delta(\mathbf{x}) = \frac{1}{\bar{n}} \sum_{i=1}^{N_P} \delta_D(\mathbf{x} - \mathbf{x}_i) - 1, \quad (7)$$

$\bar{n} \equiv N_P/V$  being the particle density. The overdensity in Fourier space can be obtained by direct summation as the Fourier transform of the equation above, that is

$$\delta(\mathbf{k}) = \frac{1}{(2\pi)^3} \left[ \frac{1}{\bar{n}} \sum_{i=1}^{N_P} e^{-i\mathbf{k}\cdot\mathbf{x}_i} - \delta_{\mathbf{k}}^K \right]. \quad (8)$$

The Fourier-space 2-point function defining the power spectrum is now given by

$$\langle \delta(\mathbf{k}_1) \delta(\mathbf{k}_2) \rangle = \frac{\delta_{\mathbf{k}_{12}}^K}{k_j^3} \left[ P(k_1) + \frac{1}{(2\pi)^3 \bar{n}} \right], \quad (9)$$

where the second term on the r.h.s. represents the shot-noise contribution due to the self-correlation of individual particles (see, for instance, [Peebles 1980](#); [Jing 2005](#)). The direct summation estimator for the power spectrum of a particle distribution is then

$$\hat{P}(k) \equiv k_j^3 |\delta(\mathbf{k})|^2 = k_j^3 \left[ |\delta(\mathbf{k})|^2 - \frac{1}{N_P} \right], \quad (10)$$

and the true power spectrum is recovered as  $P(k) = \langle \hat{P}(k) \rangle$ .

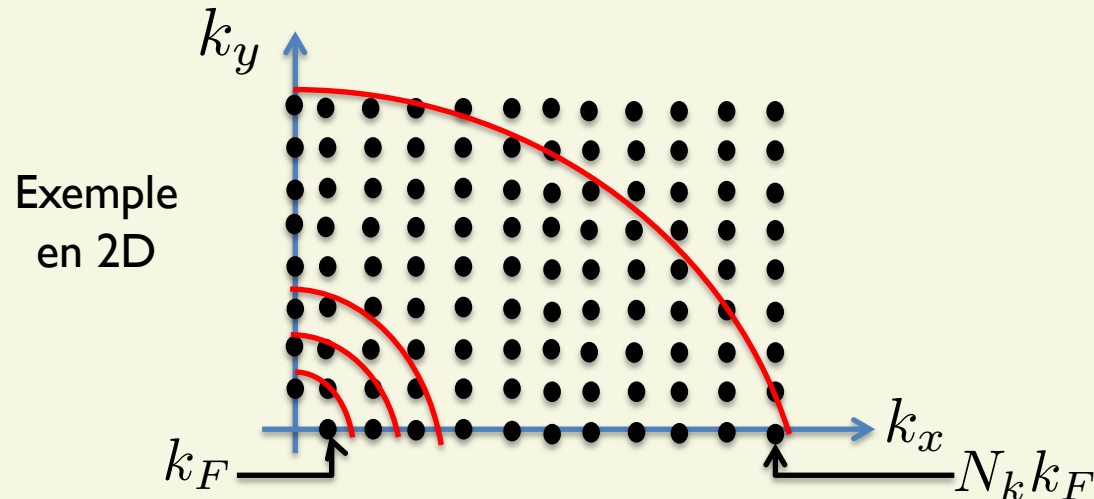
- Définir une grille de mode  $\mathbf{k}$  (arbitrairement) :

$$N_k = N_P/2$$

$$\mathbf{k}_n = k_F \begin{bmatrix} n_x \\ n_y \\ n_z \end{bmatrix} \quad n_i = 0, \dots, N_k$$

$$k_F = 2\pi/L$$

- Pour chaque mode calculer  $P(\mathbf{k})$  avec l'équation (10)
- Calculer le monopole : Par isotropie on peut définir des shells de  $|\mathbf{k}|$  constant : On obtient  $P(k)$ .



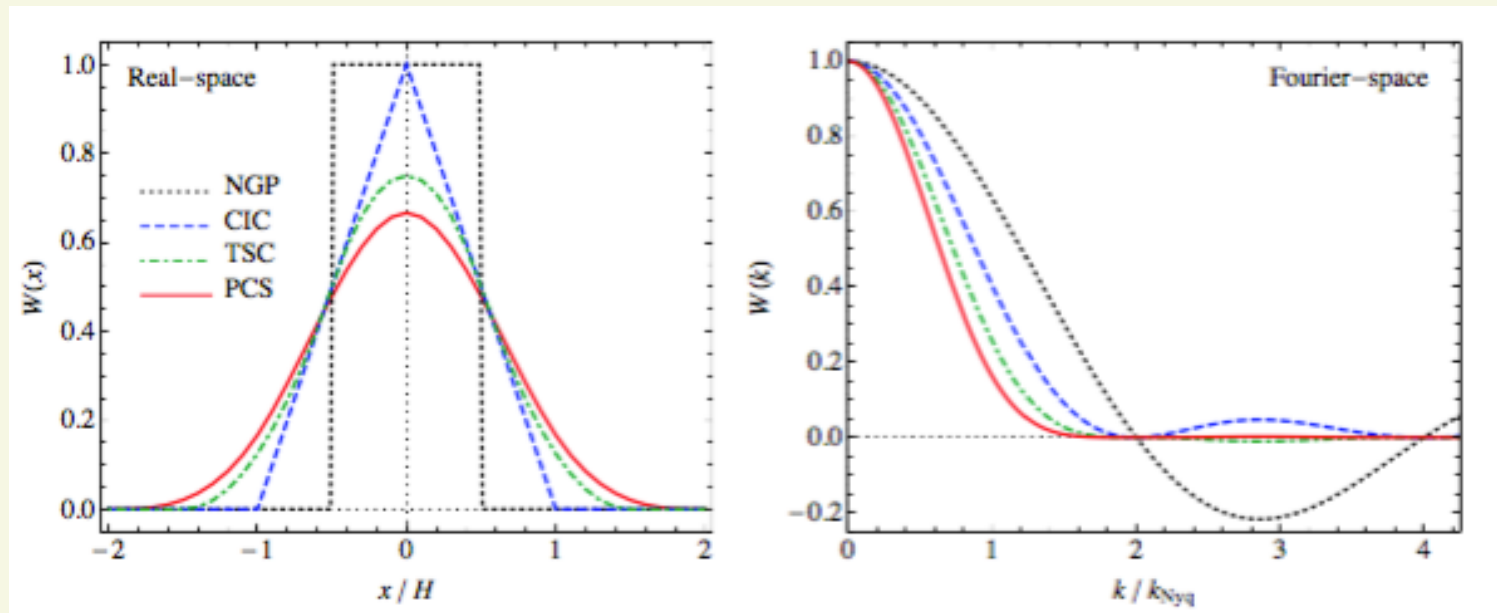
# Mass assignment

Principe : Faire une FFT du champ de densité  $\delta(x)$

Faire un sampling de  $\delta(x)$  dans l'espace réel :

Induit des effet de grille  $\rightarrow$  Aliasing dans l'espace de Fourier

- Définir une grille d'interpolation dans l'espace réel
- Choisir un schéma d'interpolation (convolution de  $W(x)$  avec  $\delta(x)$ )

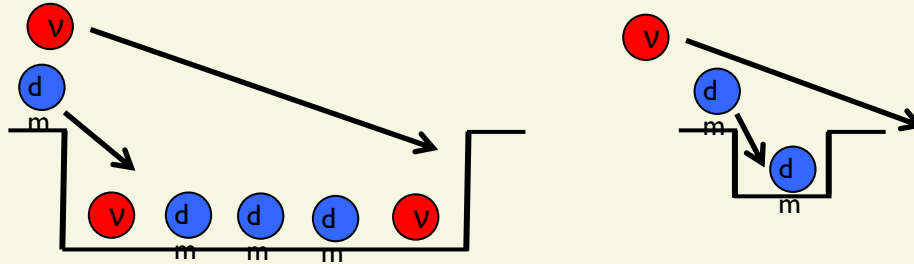


- Déconvolution de  $W(x)$  dans l'espace réel  $\rightarrow$  division dans l'espace de Fourier  $\frac{\delta(\mathbf{k})}{W(\mathbf{k})}$

# Constraining neutrino properties with the Euclid cosmological survey

When neutrinos became non-relativistic

Free streaming → neutrinos escape from the potential wells on small scales.



## Particle Physics constraints

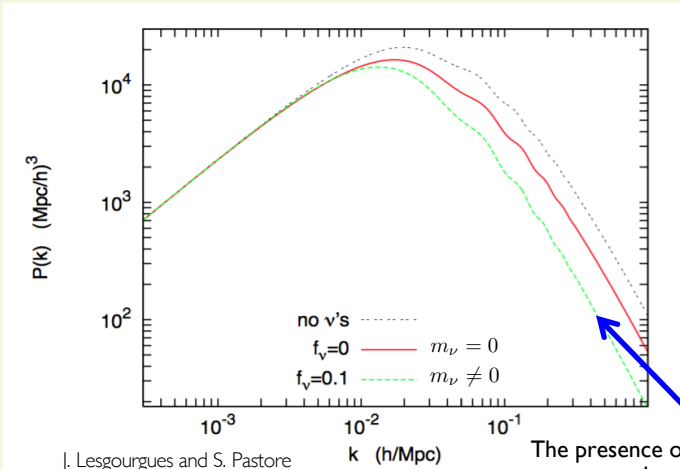
$$(NH) \quad 0.056 \text{ eV} \lesssim \sum m_\nu \lesssim 6 \text{ eV}$$

$$(IH) \quad 0.095 \text{ eV}$$

## Cosmological constraints

Galaxy clustering :  $\sum m_\nu < 0.13 \text{ eV}$  ( P(k) + BAO + Planck15 )  
 A.J. Cuesta et al. 2016

CMB :  $\sum m_\nu < 0.12 \text{ eV}$  (Planck18 + CMB-lensing + BAO)  
 Planck Collaboration 2018



J. Lesgourgues and S. Pastore

The presence of massive neutrinos causes a damping of the power spectrum on small scales.

## My work :

- Tests on the DEMNUni(i) simulations.
- Apply on eBOSS/DESI data.
- Incorporate instrumental systematics from Euclid.