

Forward modeling of galaxy kinematics in slitless spectroscopy



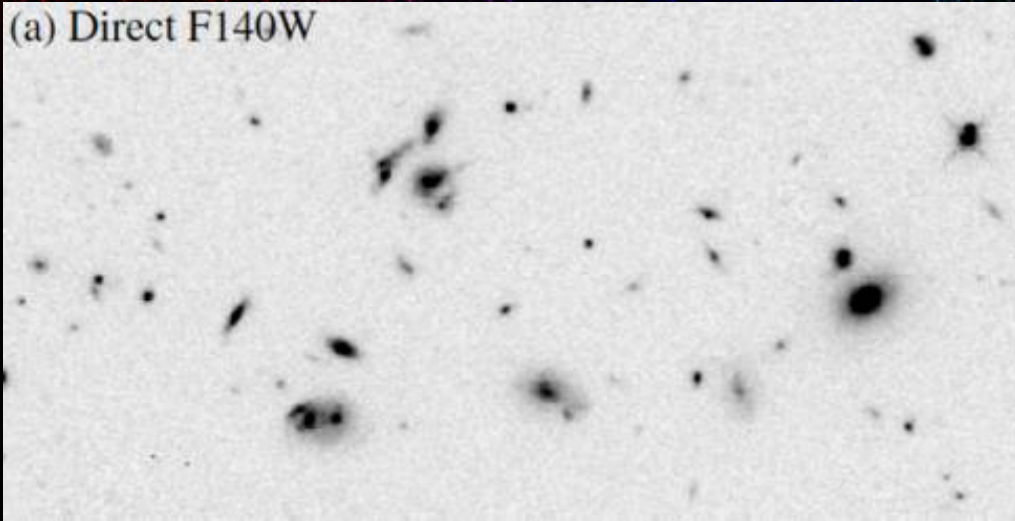
Credits:

M. Outini's PhD, 2019

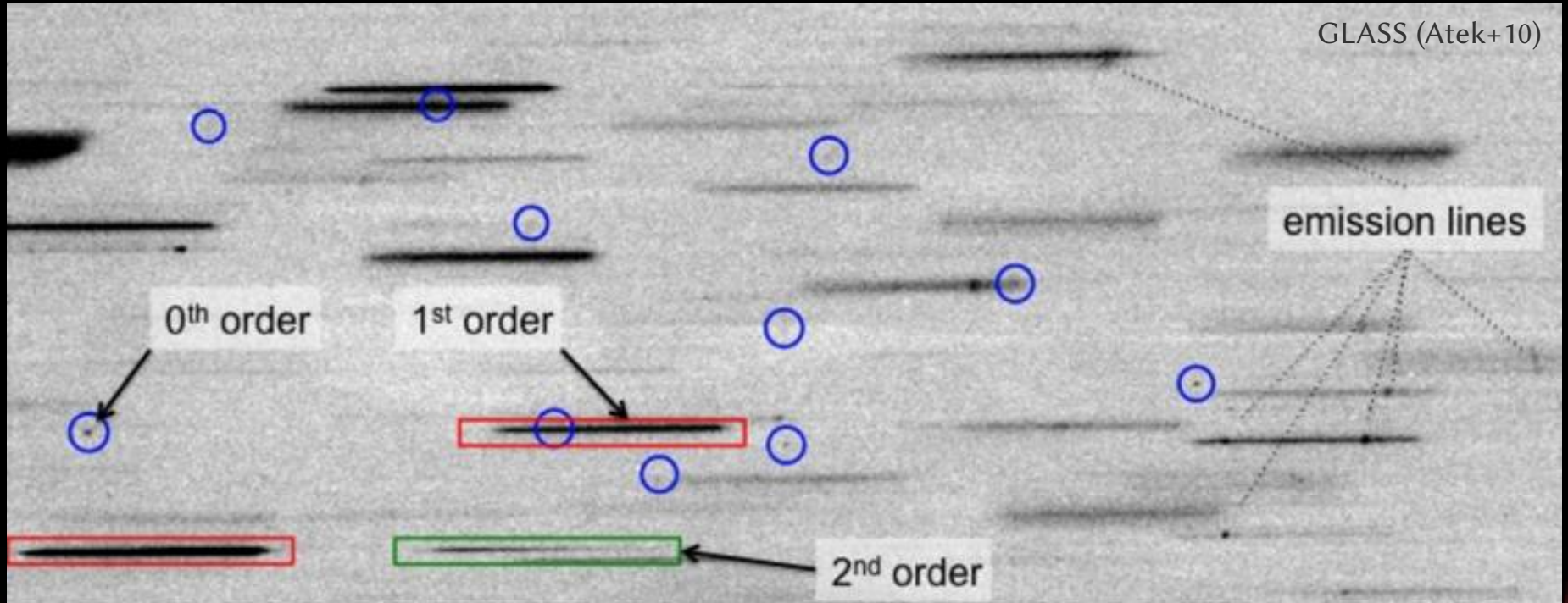
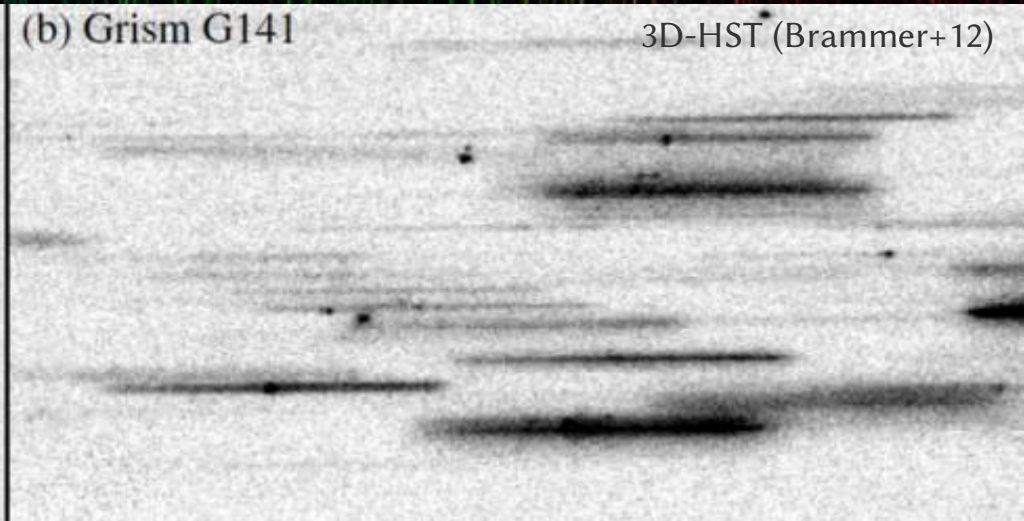
Outini & Copin, A&A (accepted), [arxiv:1910.07803](https://arxiv.org/abs/1910.07803)

Slitless spectroscopy 101

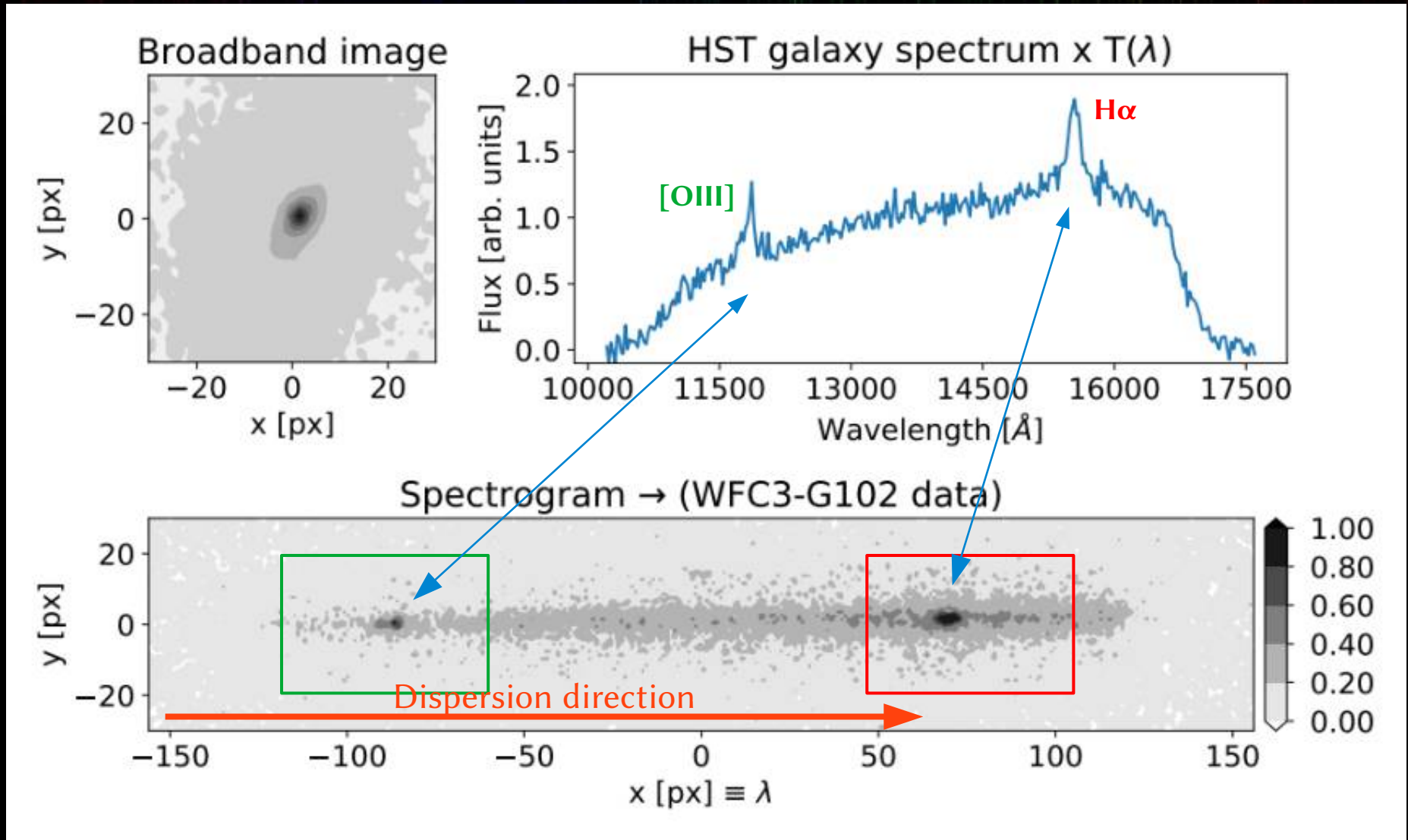
(a) Direct F140W



(b) Grism G141



Spectrogram example



Galaxy 451-MACS2129 @ $z=1.36$ (HST-GLASS)

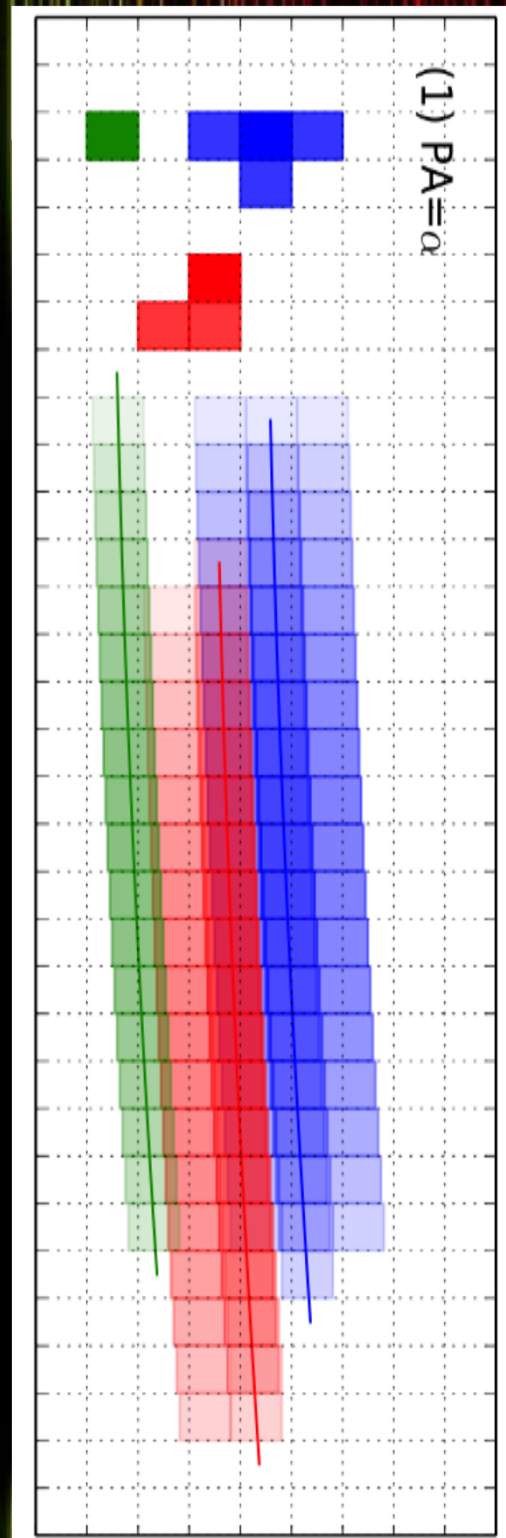
Slitless spectroscopy

- **Advantages**

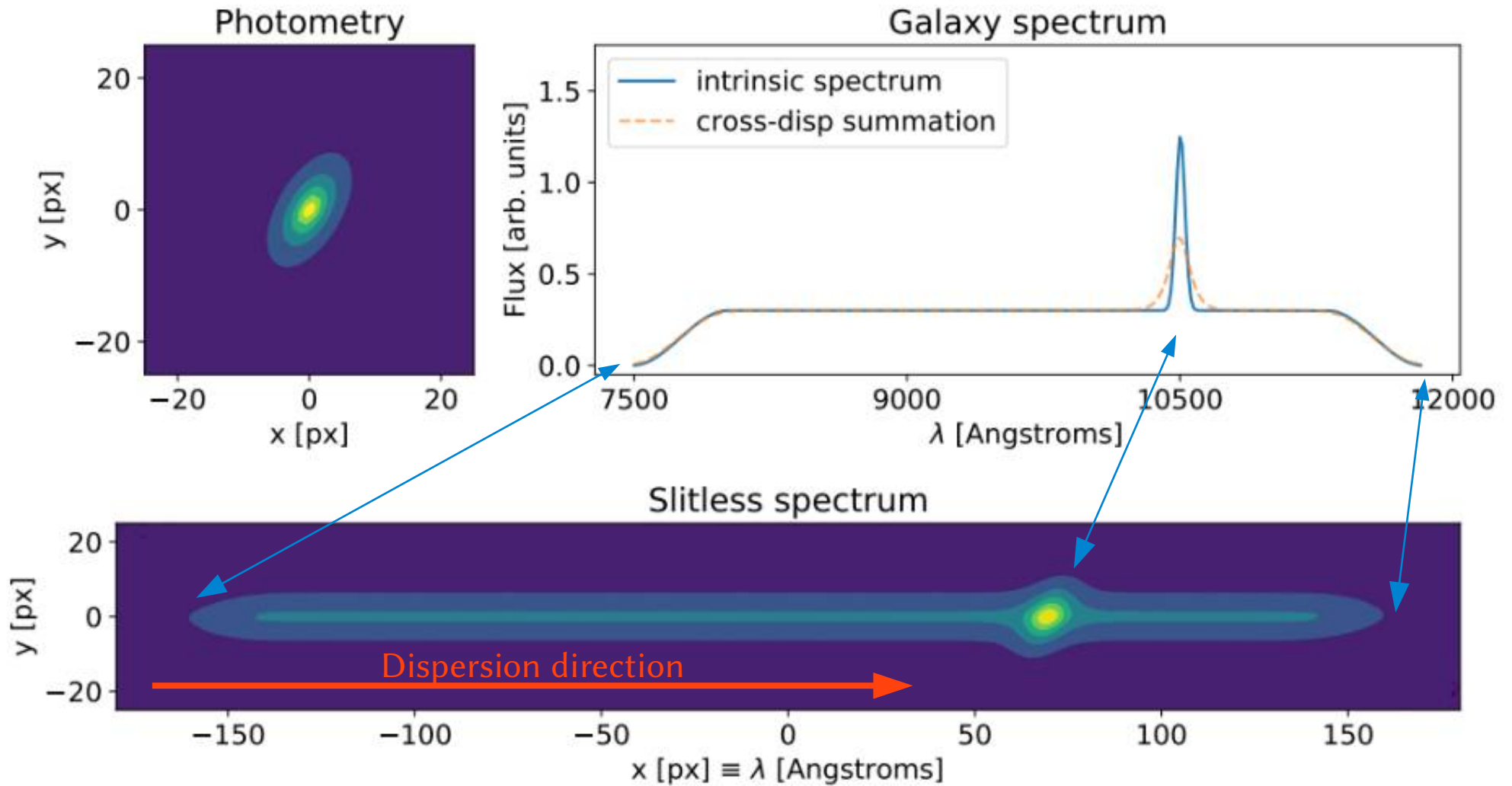
- ◆ Large FoV and high multiplexing
- ◆ Simple to build and to operate

- **Drawbacks**

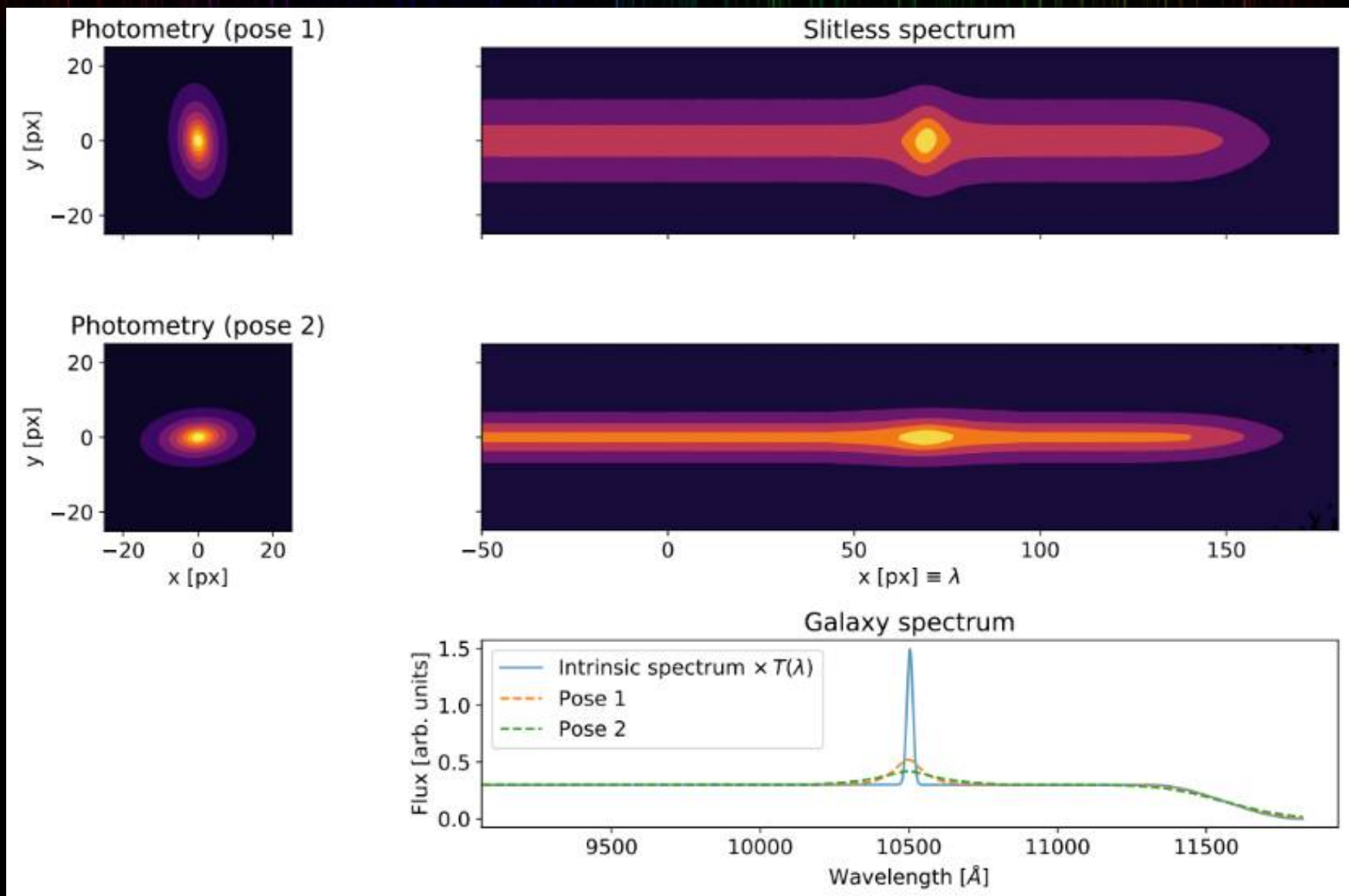
- ◆ (High background level \rightarrow space)
- ◆ **Cross-contamination:** overlap of different objects (potentially at different orders)
 - ▶ Mitigation: multi-roll observations & decont. model
- ◆ **Self-contamination:** mixing of spatial and spectral information
 - ▶ Effective spectral resolution is dependent of source size and relative orientation



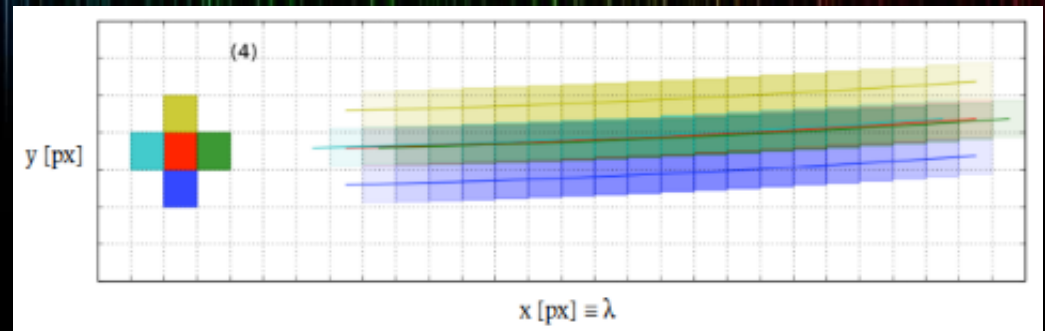
Cross-dispersion spectrum



Multi-roll x-disp. spectra



Spectrogram modeling

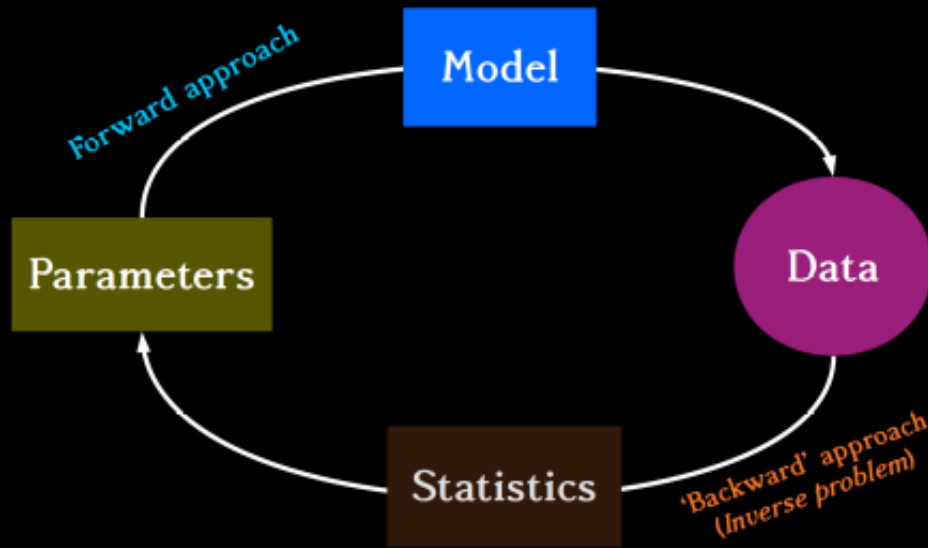


- Dispersed image

$$I(\mathbf{r}) = \int d\lambda (\mathbf{C} \otimes \mathbf{P})(\mathbf{r} - \Delta(\lambda), \lambda) \times \mathbf{T}(\lambda)$$

- ◆ **Observation $I(\mathbf{r})$** : 2D spectrogram
- ◆ **Source $C(\mathbf{r}, \lambda)$** : intrinsic spectro-spatial flux distribution (“cube”)
- ◆ **Instrumental signature**
 - ▶ $P(\lambda)$: Impulse Response Function (“PSF”)
 - ▶ $\Delta(\lambda)$: dispersion law
 - ▶ $T(\lambda)$: transmission

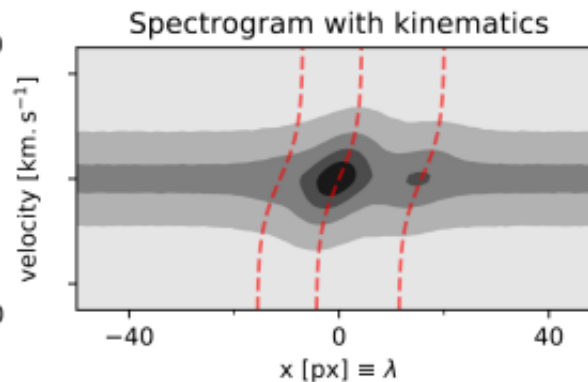
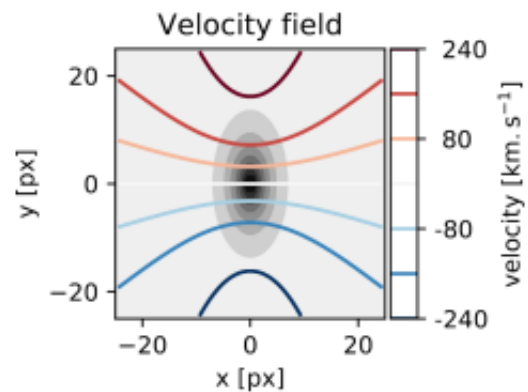
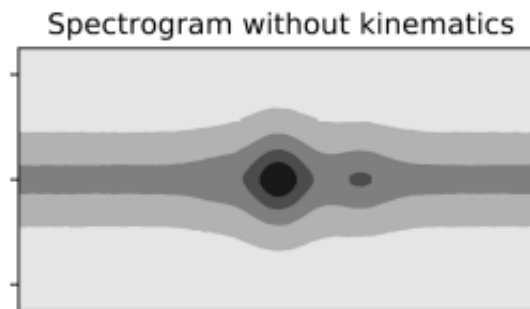
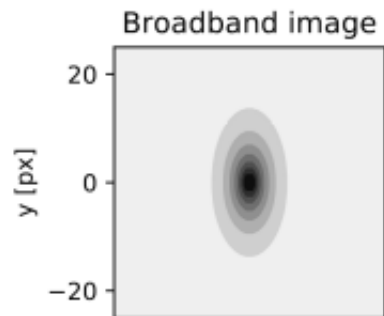
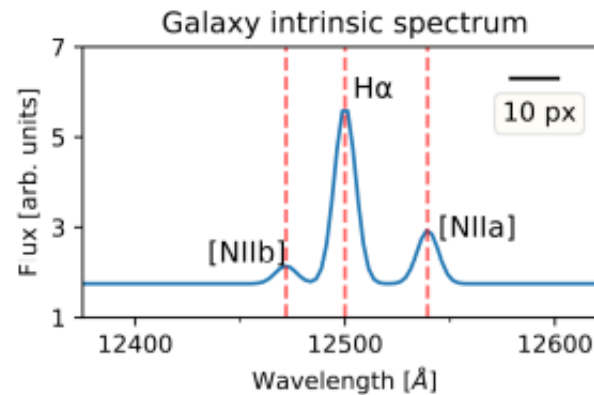
Forward modeling



- Forward modeling
 - ◆ Build a predictive model
 - ◆ Compare predicted spectrograms to observed ones
 - ◆ Derive max-likelihood parameters
- Two stages
 - ◆ Calibration: reference source (e.g. star) → **instrumental parameters**
 - ◆ Science: calibrated instrument → **intrinsic source parameters**

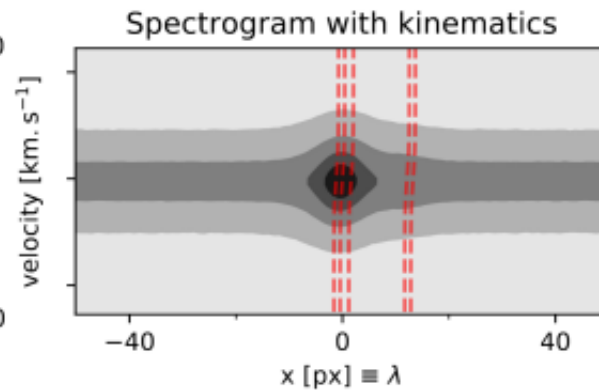
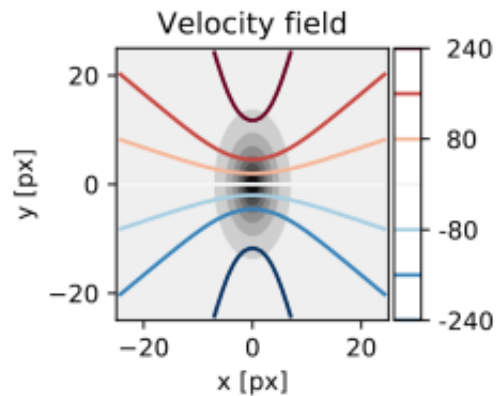
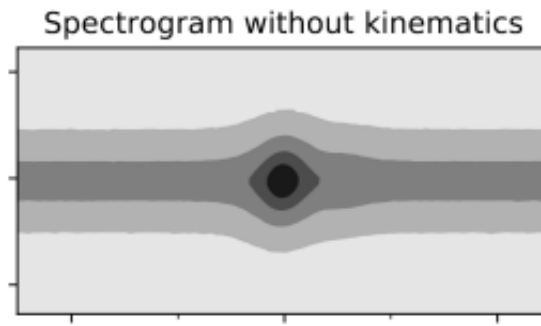
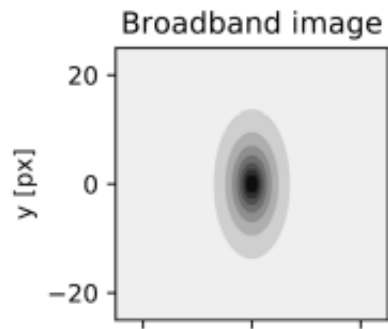
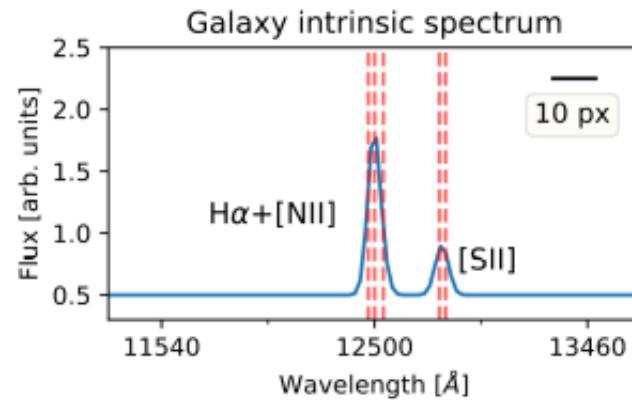
Kinematic signature in slitless

Pedagogic case !
($R \sim 2500$)



Kinematic signature in slitless

Realistic case
(HST-WFC3/G141,
 $R \sim 150$)



Forward model

- Assumptions

- ◆ $C(\mathbf{r}, \lambda) = F(\mathbf{r}) \times S(\lambda)$: separability (= uniformity)
- ◆ $\int d\lambda F \otimes P \approx B(\mathbf{r})$: broadband image

- Spectrum: continuum + emission lines

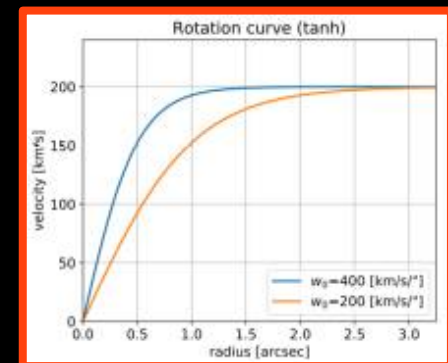
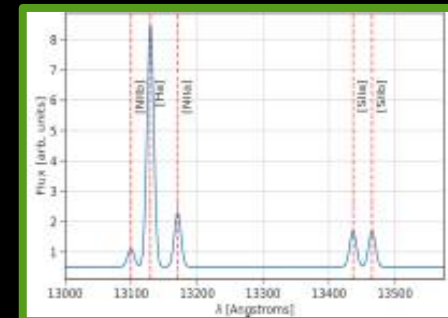
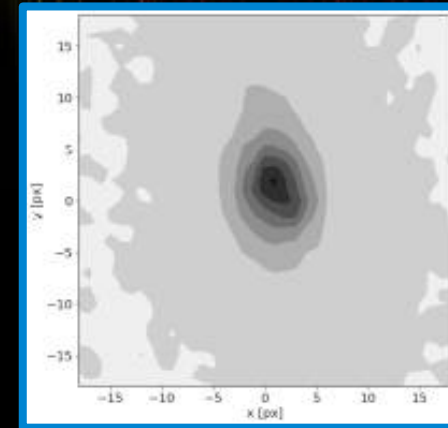
- ◆ $H\alpha + [NII], [SII], [OIII]$, etc.
- ◆ Parameters: redshift, amplitude, cont. level, etc.

- Velocity field: cold thin disk approximation

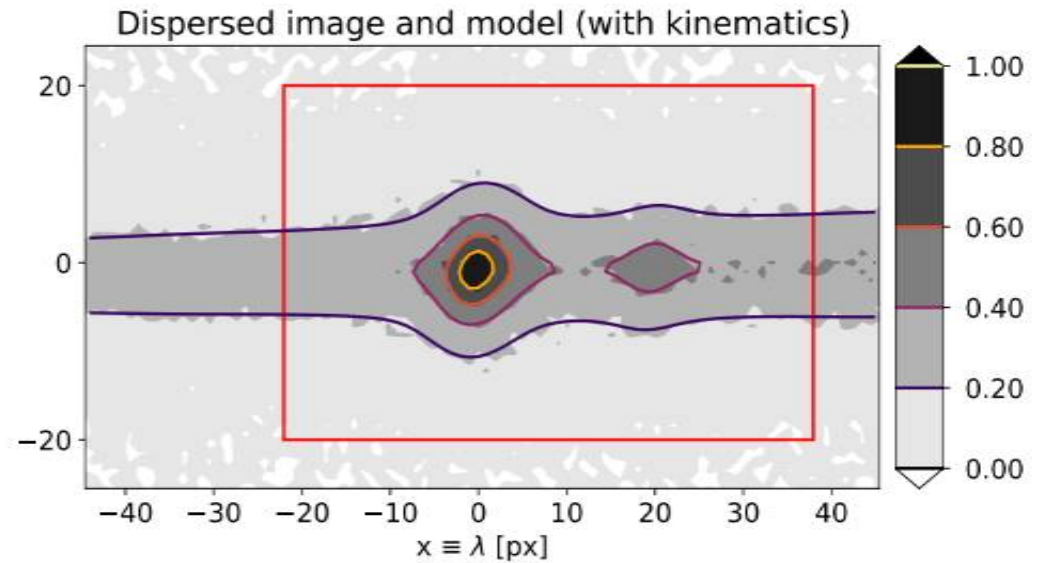
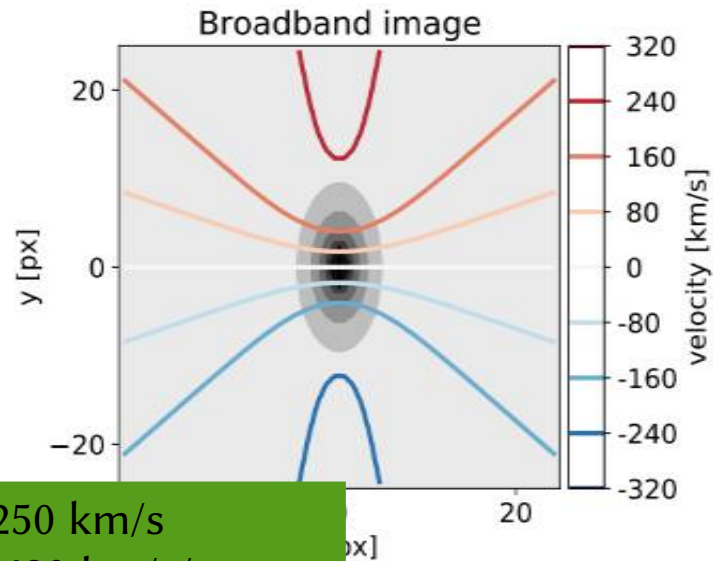
- ◆ 2-parameter RC: $v(r)/\sin i = v_0 \tanh(w_0 r / v_0)$
- ◆ Velocity field impact: $S(\lambda) \rightarrow S(\lambda / (1 + \mathbf{v}(\mathbf{r})/c))$

- Instrumental parameters: supposedly known

- ◆ Few nuisance parameters

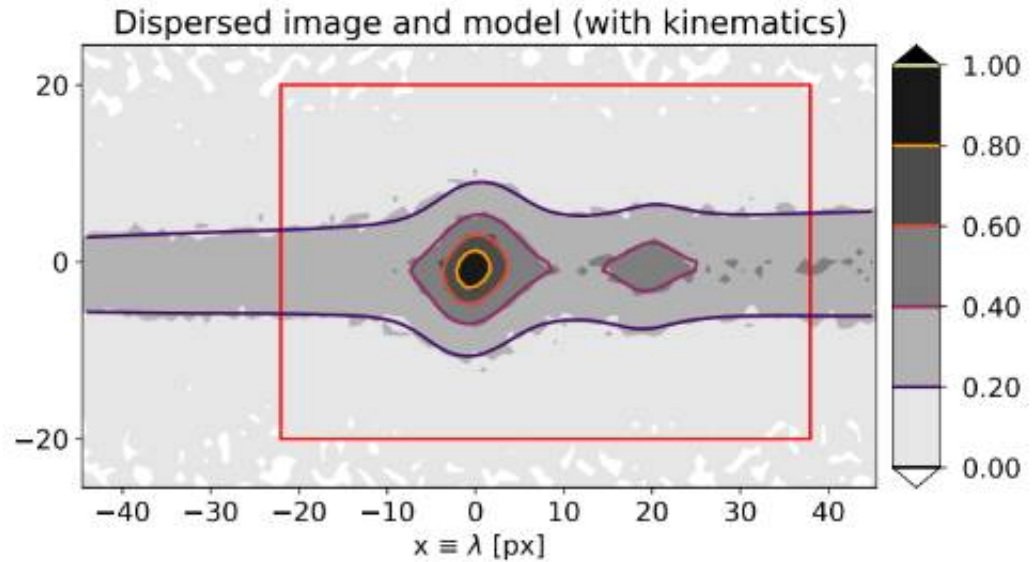
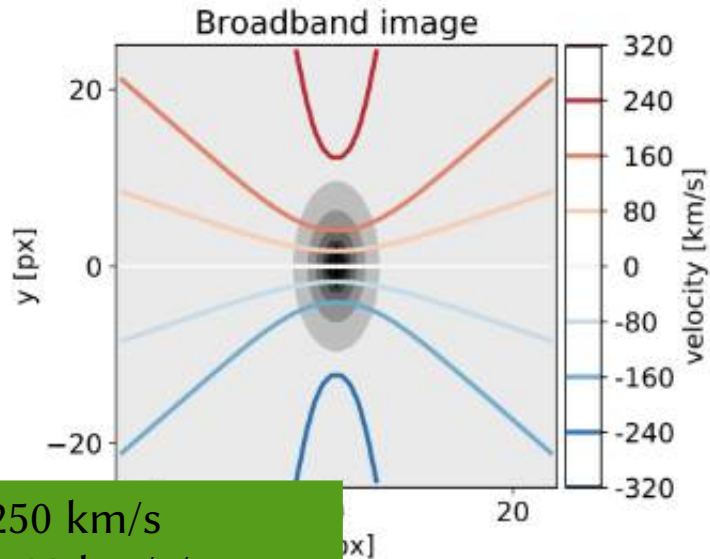


Simulations - HST-WFC3/G102



$v_0 \sin i = 250 \text{ km/s}$
 $w_0 \sin i = 420 \text{ km/s/arcsec}$
 $z = 0,55200$
PSNR = 40

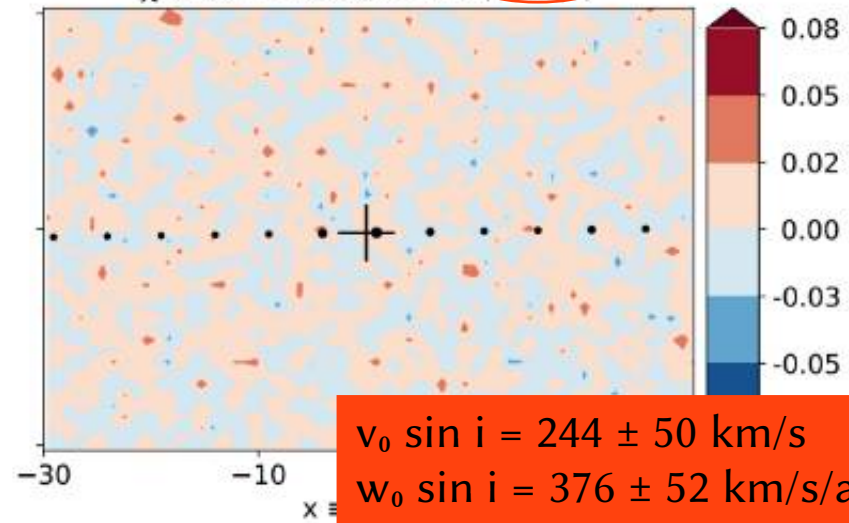
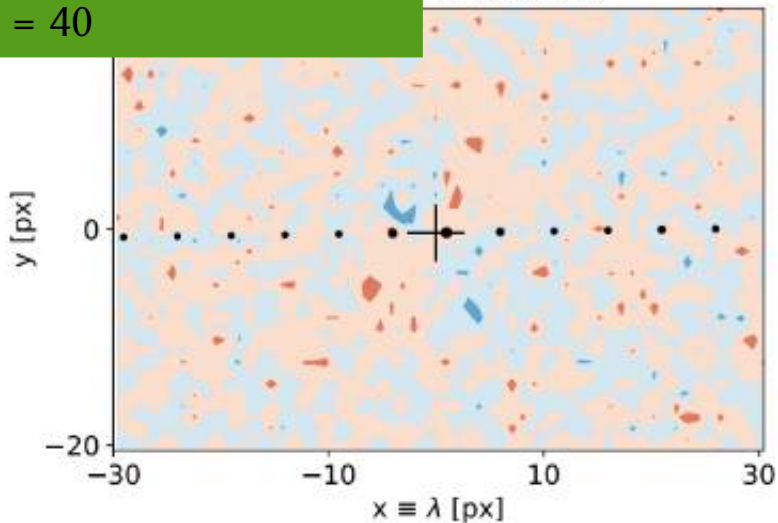
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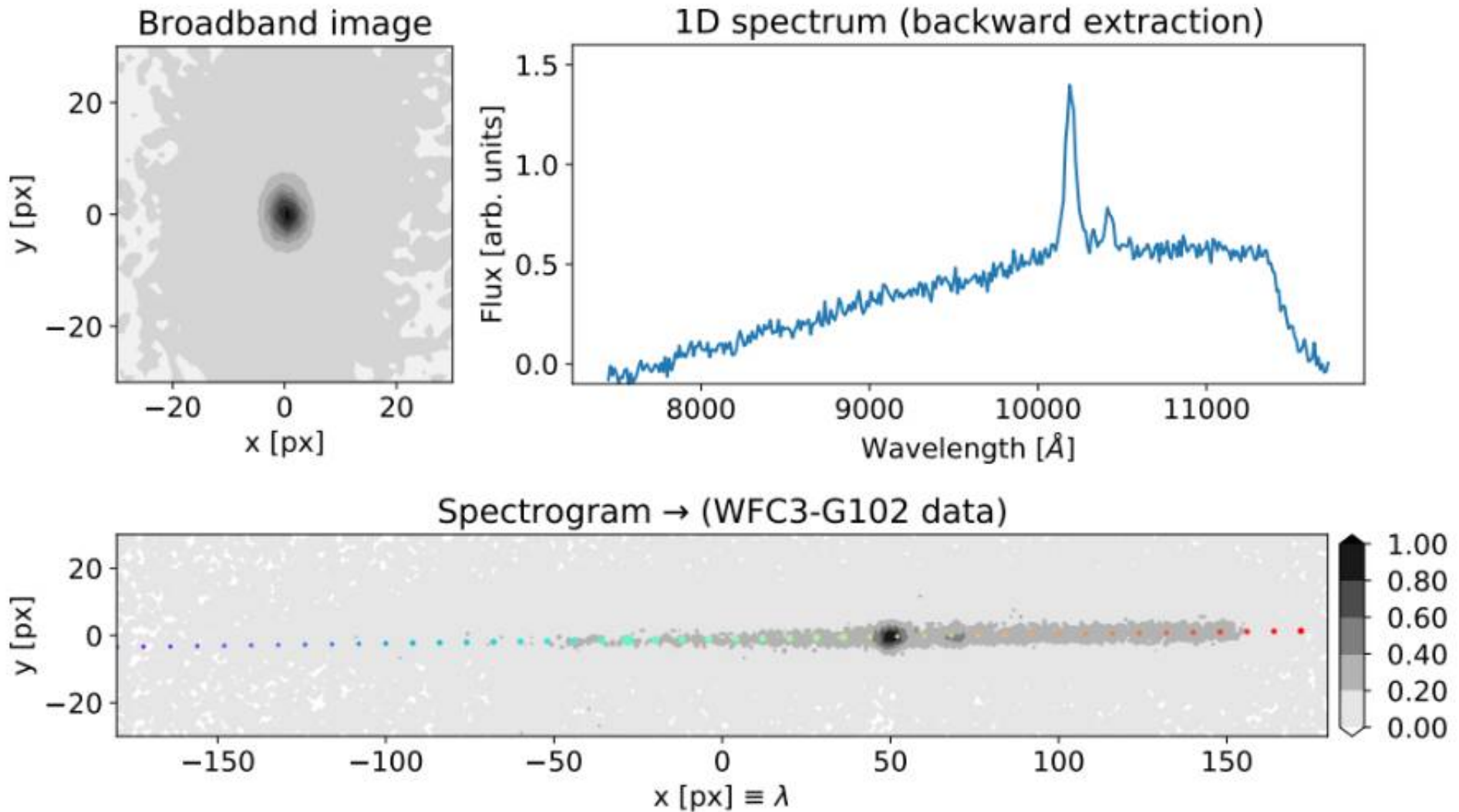
without kinematics
2600/2392

Residuals with kinematics
 $\chi^2/\text{DoF} = 2462/2390$ (11.5 σ)



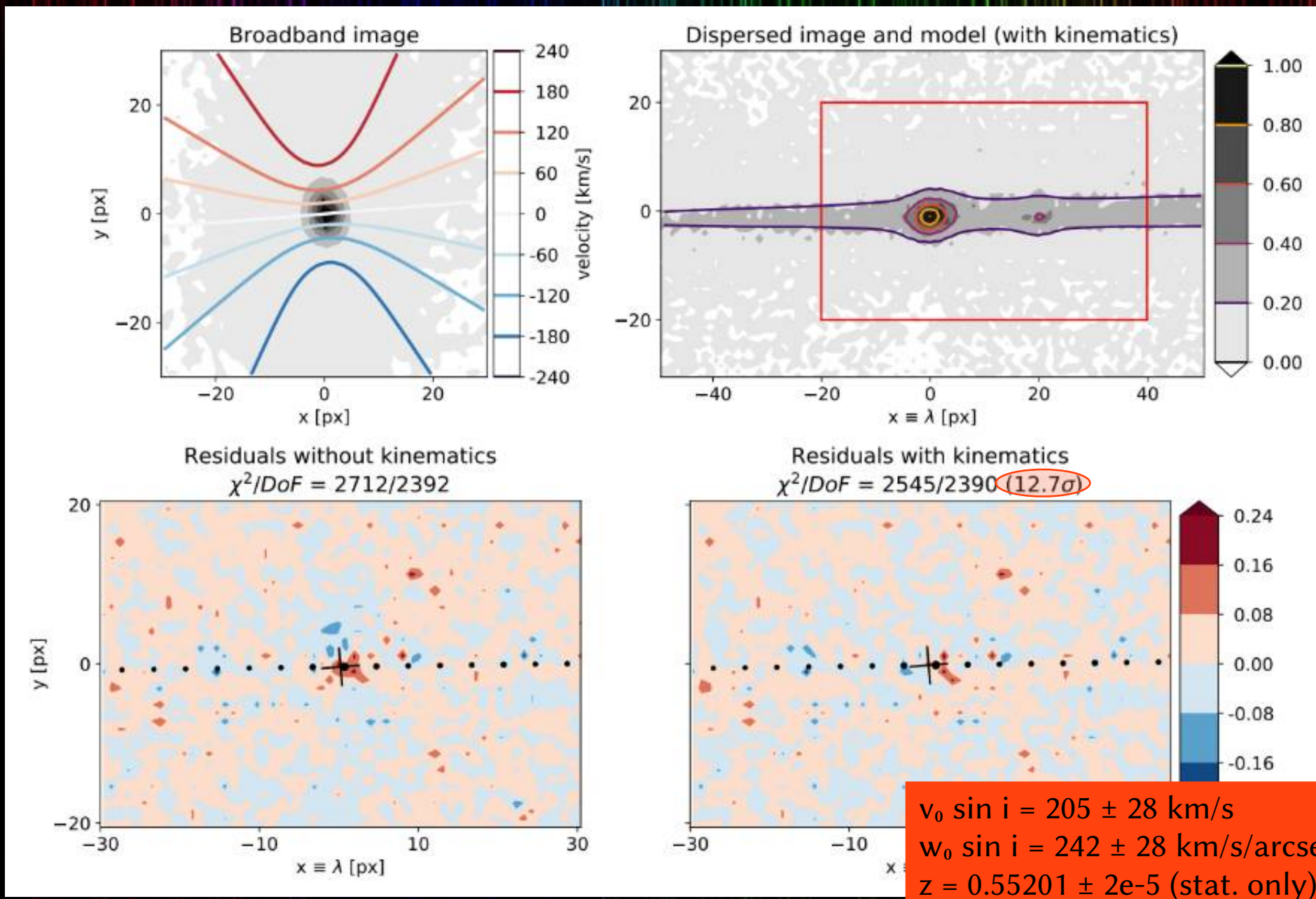
$v_0 \sin i = 244 \pm 50 \text{ km/s}$
 $w_0 \sin i = 376 \pm 52 \text{ km/s/arcsec}$
 $z = 0.55195 \pm 5e-5$ (stat. only)

Observations - HST-WFC3/G102

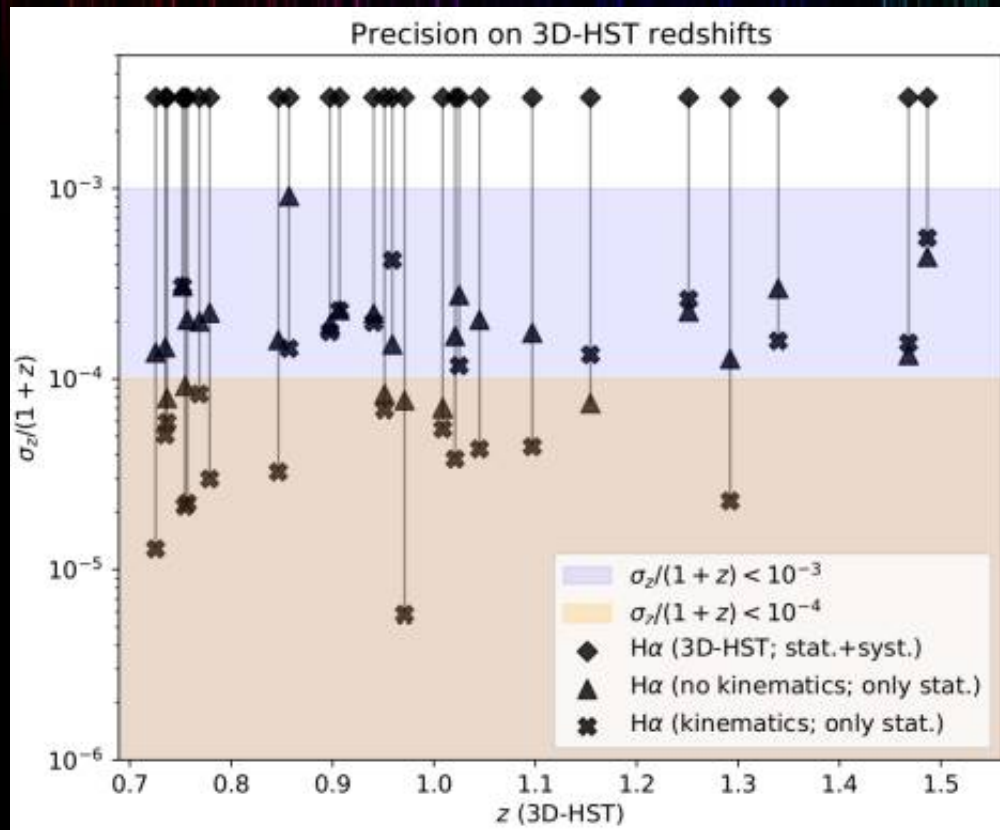


Galaxy 1134-MACS1423 @ $z=0.55$ (HST-GLASS)

1st kin. detection from slitless spectro.



Impact on redshift measurements (HST)



Backward, syst. + stat. : $3e-3$

Forward, no kinematics,
stat. only : $\sim 2-3e-4$

Forward, kinematics,
stat. only : $\sim 1e-4$ or better

● Redshift

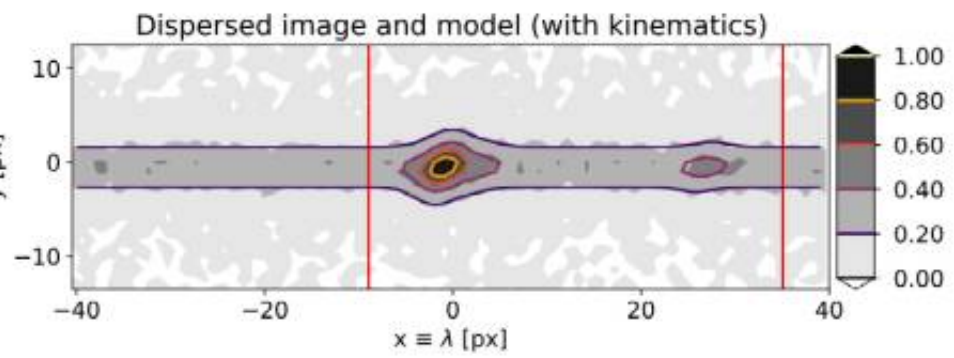
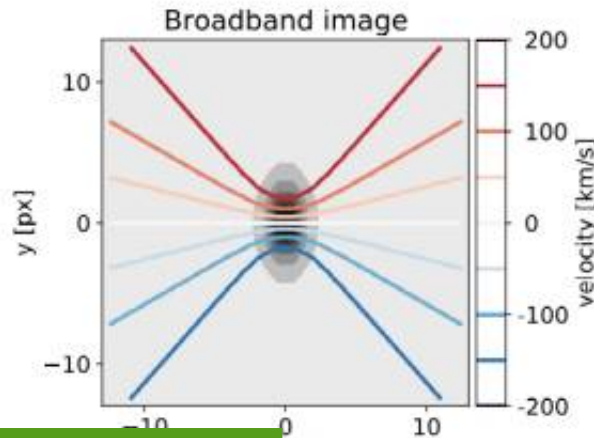
- ◆ Significant improvement for resolved galaxies, scale with multi-roll observations
- ◆ Could easily be generalized to spectral template fitting (no 2D \rightarrow 1D info loss)

● Galaxy kinematics: only for bright, large, massive disk galaxies

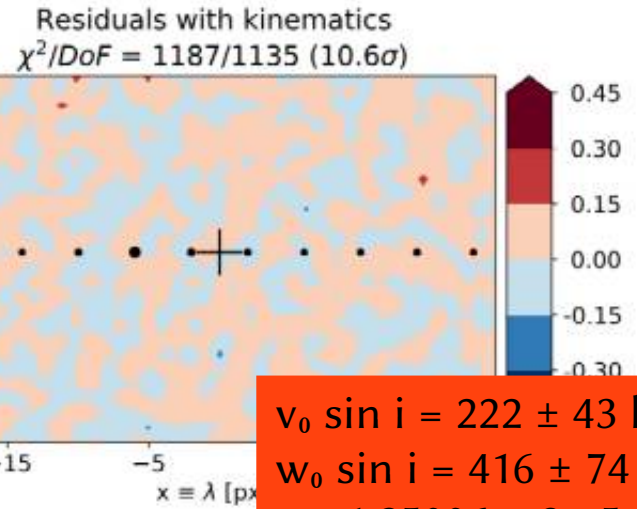
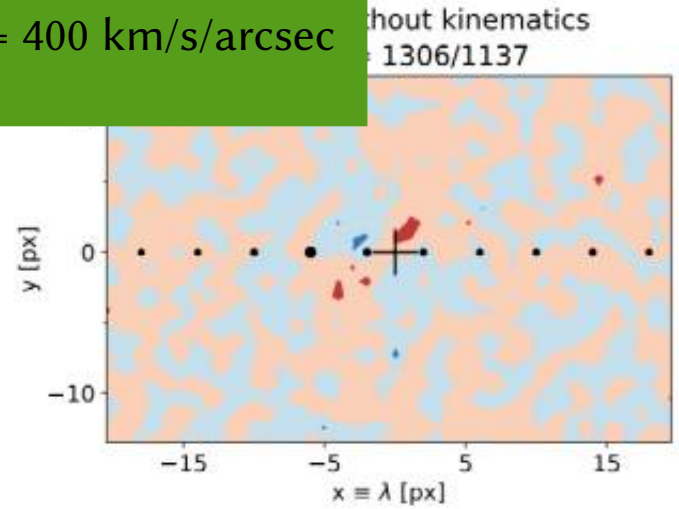
Euclid simulations – NISP-R

- Better spectral sampling ($\sim 13 \text{ \AA}/\text{px}$)
- Coarser spatial resolution ($0.3''/\text{px}$)

- Exp. disk, $r_d \sim 0.5''$
- Simulation of a single roll (dither)

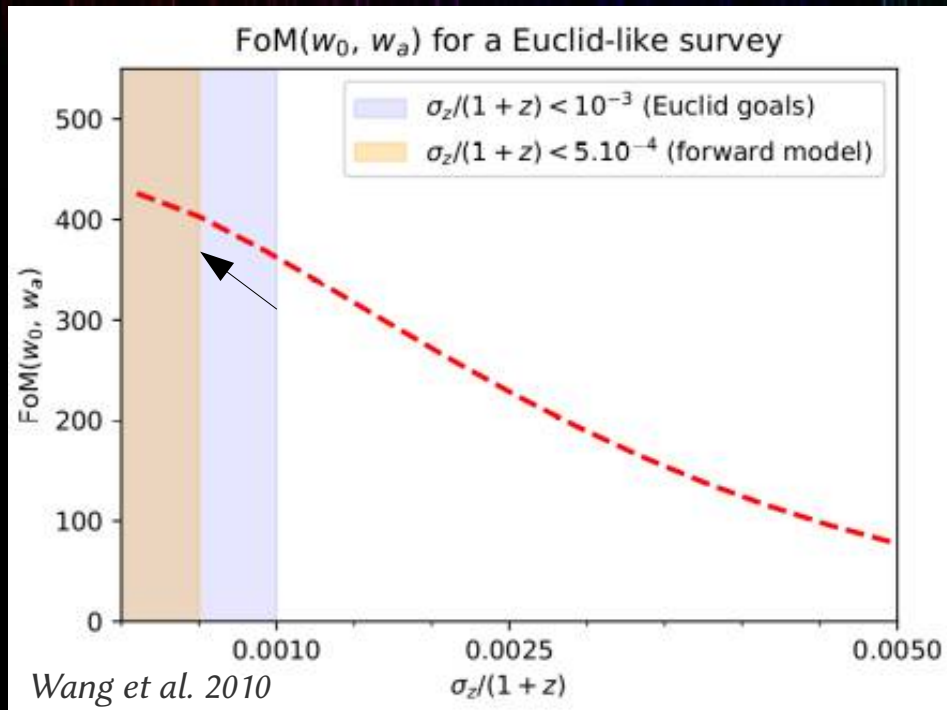


$v_0 \sin i = 200 \text{ km/s}$
 $w_0 \sin i = 400 \text{ km/s/arcsec}$
 $z = 1.35$



$v_0 \sin i = 222 \pm 43 \text{ km/s}$
 $w_0 \sin i = 416 \pm 74 \text{ km/s/arcsec}$
 $z = 1.35006 \pm 8e-5 \text{ (stat. only)}$

Impact on FoM



- **Full forward model**
 - ◆ Both for calibration and science analysis
- **Foreseeable** redshift precision: $\sigma_z/(1+z) \sim 5e-4$
 - ◆ $\times 2$ better than requirements

- **FoM prediction (Wang+10, Red Book)**

- ◆ $F_{H\alpha} > 4e-16$ erg/s/cm², $0.5 < z < 2.1$, 20 000 deg², $e = 0.5$
- ◆ Forward model: FoM + 15%

Conclusions

- Better understanding of slitless spectroscopy
 - ◆ Still, fundamental spectro-spatial degeneracy cannot be recovered
- Call for full forward modeling (calibration + analyses)
 - ◆ Optimal treatment of available observations
 - ▶ Calibration: instrument model → minimize overhead
 - ◆ Major impact on redshift precision for resolved sources
 - ◆ Natural method for decontamination
- Galaxy kinematics w/ Euclid
 - ◆ Possible for a **small fraction** (yet to be quantified) of 30M galaxies
 - ▶ Definitely easier in the Deep Survey (deeper, ~40 rolls)
 - ◆ **Open new perspectives**: morpho-kinematic classification, distance estimates (e.g. Tully-Fisher), cosmography & cosmology

To be continued...