

# Simulation, optimization and applications of near-term quantum computers

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# Bridging the gap

## Many theoretical ideas

### ▶ Quantum algorithmics

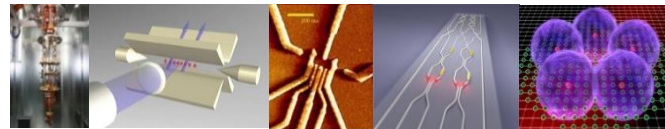
Very few known algorithms (+need many good quality gates & many qubits)



### ▶ NISQ: Hybrid quantum classical programs

- Variational Quantum Eigensolver and Simulator (VQE, VQS)
- Error mitigation...

## Many hardware implementations



?



No killer app yet!

- ▶ Different connectivities
- ▶ Different gatesets
- ▶ Different gate qualities/durations
- ▶ Different readout errors
- ▶ Different coherence times
- ▶ Different scalability
- ▶ Analog vs digital
- ▶ Adiabatic vs diabatic

# Outline

## ▶ Simulation

efficiently simulating the (imperfect) behavior of each platform

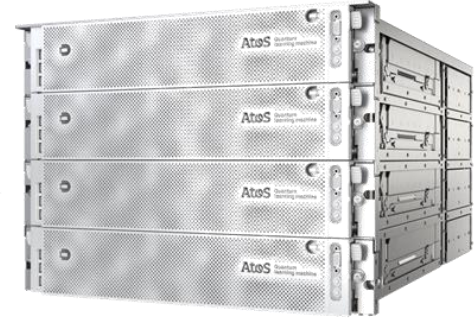
## ▶ Optimization

developing quantum programs in a hardware-agnostic way... but suitably optimized for target platform

## ▶ Applications

Focus: Schwinger model energy with variational algorithms

## Atos Quantum Learning Machine



a dedicated quantum programming platform

**myQLM: "QLM lite", free!**

quantum programming

perfect simulation

quantum libraries

noisy simulation

circuit optimization

interface to IBM, Rigetti...

**application libraries**  
(fermion-spin transforms, VQE, QAOA...)

hardware/noise models

# Atos quantum: worldwide...

On-going PoC with

**BAYER** & **RWTHAACHEN UNIVERSITY**

**Argonne NATIONAL LABORATORY**

**OAK RIDGE National Laboratory**

**Hartree Centre**  
Science & Technology Facilities Council

**CSC**

**SURF SARA**

**JÜLICH**  
Forschungszentrum

**FH OBERÖSTERREICH**

**TOTAL**

**cea**

**CCRT**

**UNIVERSITÉ DE REIMS CHAMPAGNE-ARDENNE**

# ... and at home: our collaborations

## Quantum programming, classical simulation

**BPI project Quantex** (with Paris Saclay, CNRS-LORIA, CEA-LETI). *Quantum programming, hardware-acceleration for classical simulation of quantum circuits*

**ANR SoftQPro** (with Paris Saclay, CNRS-LORIA, CEA-LIST). *Numerical simulation of high-level quantum programming languages.*

**CIFRE PhD thesis with Supélec/Saclay**: *numerical techniques for quantum circuit generation*

## Quantum algorithmics

**QUANTERA QuantAlgo** (with CNRS-IRIF, CWI-QuSoft, Cambridge, Univ. of Latvia, Univ. Libre de Bruxelles). *Machine Learning, exploration of use cases.*

**ANR QuData** (with CNRS-IRIF, Paris-Sorbonne, CNRS-LABRI). *Assessment of industrial use cases.*

**CIFRE PhD thesis with IRIF**: *algorithms for Quantum Machine Learning.*

## Quantum hardware

**EU-Flagship project AQTION** (with Univ. Innsbruck (Blatt group), Oxford, ETHZ, Mainz, Fraunhofer, Swansea, Toptica). *Programming frontend, compilation, industrial use cases*

**Chaire industrielle NASNIQ** (with CEA-DRF Qnantronics lab). *Computational architecture, noise models*

**Merlion project Siliquon qubits** (with CNRS-Néel, Singapore Institute of Quantum Computing). *Noise simulation of Si Qubits*

## Analog quantum simulation

**EU-Flagship PASQUANS** Flagship project (with Institut d'Optique, Univ. Innsbruck (Zoller group), ETHZ, Univ Munich, LKB, Univ Strathclyde, Univ Ulm, Univ Padova, Univ Heidelberg).

*WP leader of applications*



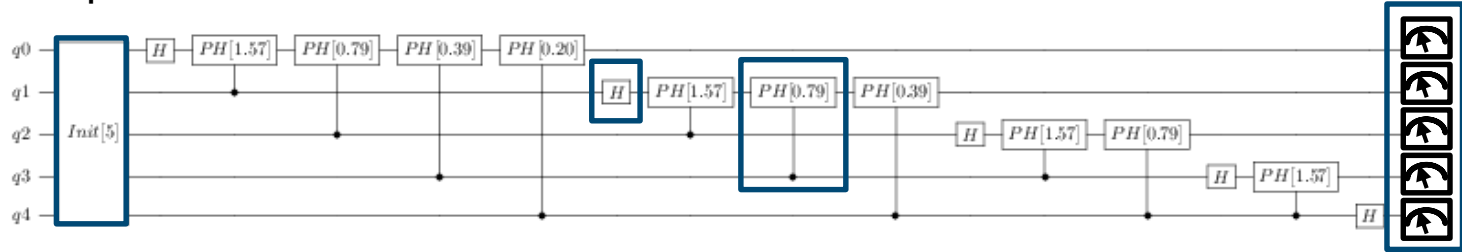
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## Simulation

efficiently simulating the (imperfect) behavior  
of each platform

# The quantum Fourier transform: theory...

- ▶ Textbook quantum circuit:



state preparation ➡ computation: apply quantum gates ➡ final step: measurement

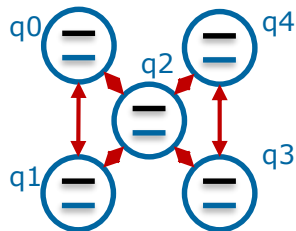
- ▶ In theory: **exponential speedup** (over fast Fourier transform)
- ▶ Key ingredient of **Shor's factoring algorithm**

Promise of huge speedups... if "ideal" quantum computer

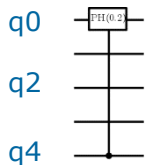
# ... and practice

## Hardware constraints

### Limited connectivity



how to run such a gate:



### Limited expressivity

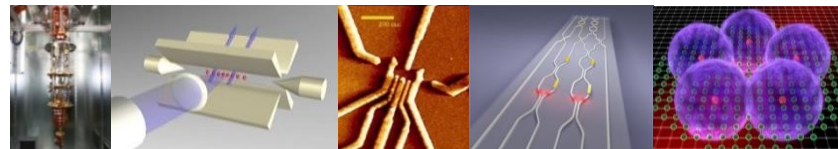
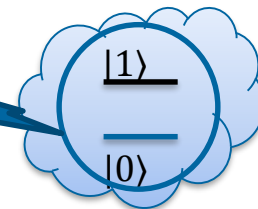
“only CNOT gates”

insert swaps,  
rewrite as  
combination of  
native gates...

Larger gate counts

## Quantum decoherence

Outside world  
(electro-magnetic fields,  
other energy levels,  
unwanted couplings, ...)



Shorter time window

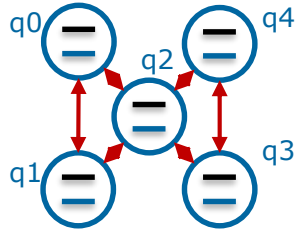
This information is essential to assess quality of final result



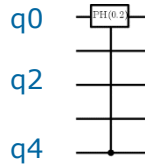
# ... and practice

## Hardware constraints

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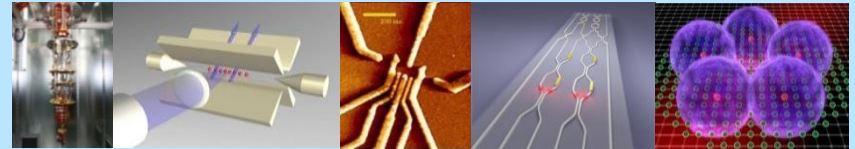
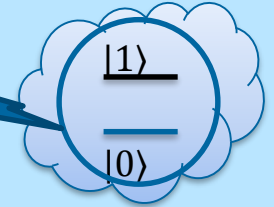
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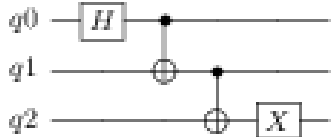


Shorter time window

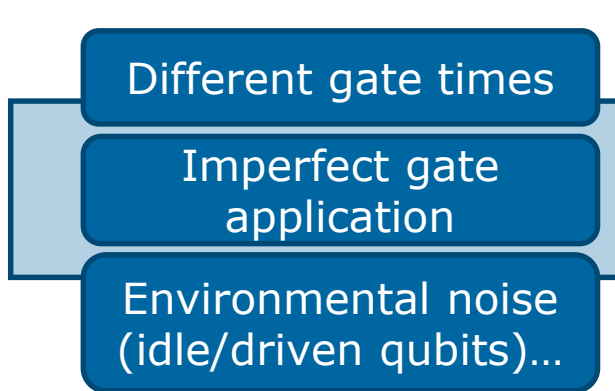
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# Discrete modeling of noise

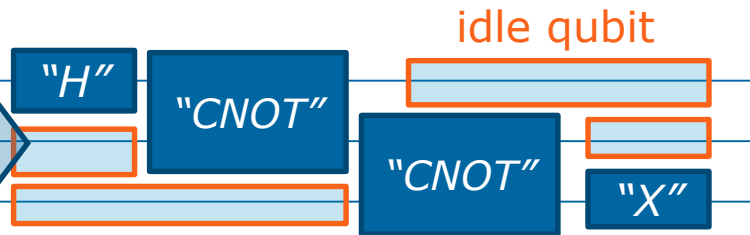
Ideal circuit



Hardware model



Noisy circuit



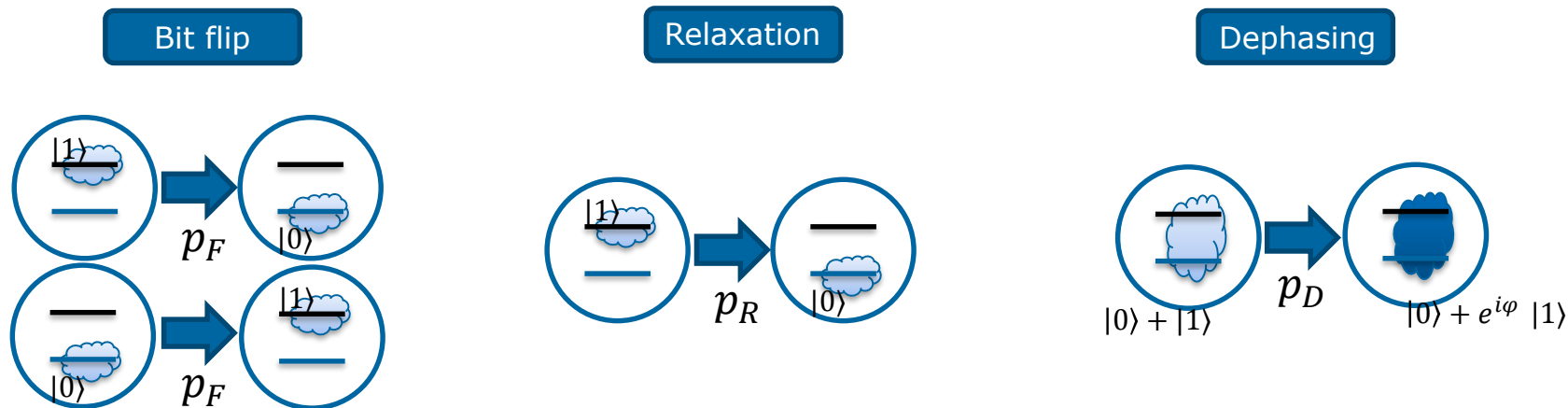
- ▶ Modular, hence **scalable** approach
- ▶ Can capture **large variety of noises** (incl. spatially correlated, crosstalk, leakage...)

- ▶ **Caveat:** does not capture all memory effects

What do the boxes look like?

# Textbook noise models...

see e.g. Nielsen & Chuang



Challenge: what is  $p_F, p_R, p_D$  ... for a given hardware?  
Are there other important types of noise?

# ... and more 'ab initio' approaches: tomography

- ▶ Characterize noise processes:  
    **"process tomography"**
- ▶ Two complementary strategies:

prepare  
(enough)  
input  
states



measure  
(enough)  
observables

## Experiment (phenomenology)

- **Quantum process tomography:** assume known state preparation & measure (aka SPAM) (!)
- **Gateset tomography:** consistent handling of SPAM error

Merkel et al / Blume-Kohout et al 2013

**Advantage:** phenomenological ("black box") approach

## Numerics (microscopic model)

- Write **Hamiltonian model** for given operation
- Solve **Schrödinger/master equation** for all inputs

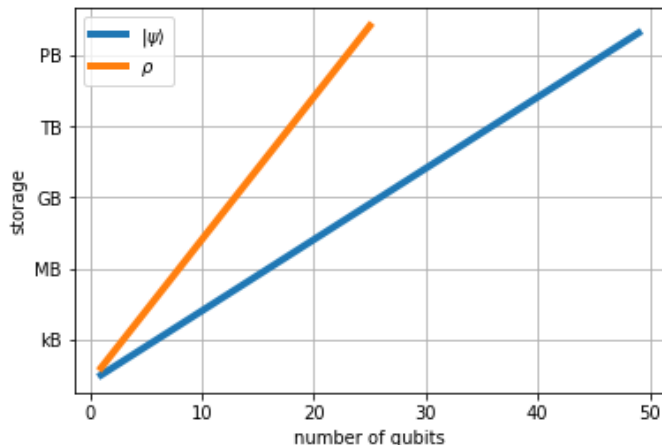
**Advantage:** inputs are usually experimentally accessible (microscopic) parameters.

# Ideal vs Noisy quantum computation

## Ideal circuit simulation

- ▶ Quantum state:
  - pure state  $|\psi\rangle$
  - generically:  $2^n$  **complex numbers**
- ▶ Gates:
  - **unitary operators  $U$**  acting on subsets of qubits
- ▶ Simulation:
$$|\psi_f\rangle = U_M \dots U_1 |\psi_i\rangle$$

## Memory footprint



## Noisy simulation

- ▶ Quantum state:
  - mixed state  $\rho = \sum_i p_i |\psi_i\rangle\langle\psi_i|$
  - generically:  $2^n \times 2^n$  **complex numbers**
- ▶ Gates:
  - **linear, "CPTP" maps  $\mathcal{E}(\rho)$**  (completely positive, trace preserving)
- ▶ Simulation:
$$\rho_f = \mathcal{E}_M \circ \dots \circ \mathcal{E}_1(\rho_i)$$

# Ideal circuit simulation

Unitary evolution  $|\psi_f\rangle = U_M \dots U_1 |\psi_i\rangle$

## “Brute-force” simulation

- ▶ Store  $2^n$  amplitude vector:

$$|\psi\rangle = \sum_{b_1..b_N} a_{b_1..b_N} |b_1..b_N\rangle$$

$$a_{b_1 b_2 b_3 b_4} = \text{[Diagram: A blue horizontal bar with four vertical lines extending upwards, representing a 4-qubit amplitude vector.]}$$

- ▶ Up to 40-41 qubits

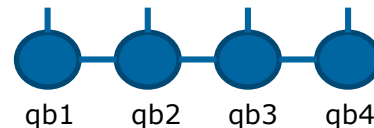
## Stabilizer simulation

- ▶ Only “Clifford” gates: can represent state with  $O(n^2)$  cost
- ▶ Can simulate >1000 qubits
- ▶ Extensions for “Clifford+T”...

Gottesman & Knill

## Matrix product states (and tensor networks)

- ▶ MPS representation (4 qubits):

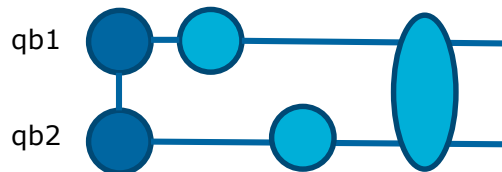


see e.g.  
Schollwöck '10,  
Orus '14

- ▶ “Bond dimension” and entanglement relation
- ▶ Can simulate >40 qubits

## Tensor-network contraction

- ▶ Space-time network (here: 2 qubits + 3 gates)



- ▶ Challenge: find fast contraction order

# Noisy simulation

## Density-matrix evolution:

- ▶ Use e.g 'Kraus' representation

$$\rho_f = \sum_{k_M} \left( E_{k_M}^{(M)} \dots \left( \sum_{k_1} E_{k_1}^{(1)} \rho E_{k_1}^{(1)\dagger} \right) \dots E_{k_M}^{(M)\dagger} \right)$$

- ▶ ~OK for <20 qubits

## Stochastic sampling:

- ▶  $\rho_f \approx \frac{1}{N} \sum_{i=1..N} |\psi_i\rangle\langle\psi_i|$
- ▶ Can use ideal circuit simulator to compute each "trajectory"  $|\psi_i\rangle$
- ▶ Can simulate many more qubits

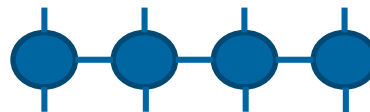
## Near-Clifford simulation

- ▶ Decompose  $\mathcal{E}^{(j)} = \sum_i q_i^{(j)} S_i$   
with  $S_i$  stabilizer channel
- ▶ Sample resulting sum over stabilizer channels

Bennink et al

## Matrix product operators (and tensor networks)

- ▶ MPO representation (4 qubits):



# 2

## Optimization

developing quantum programs in a hardware-agnostic way...

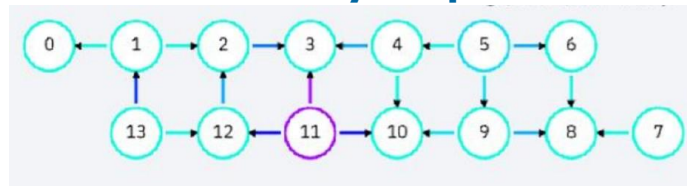
but suitably optimized for a target platform



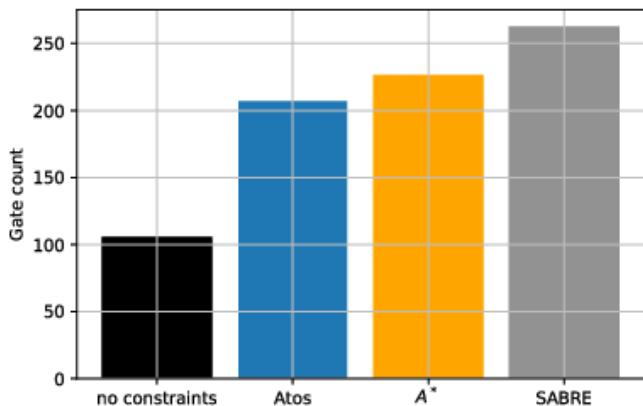
# Example 1: Compilation of a Quantum Fourier Transform

- ▶ Fourier transform on IBM's 14-qbit Melbourne chip  
Need to insert SWAPs + use only CNOTs
- ▶ Two different optimization metrics:

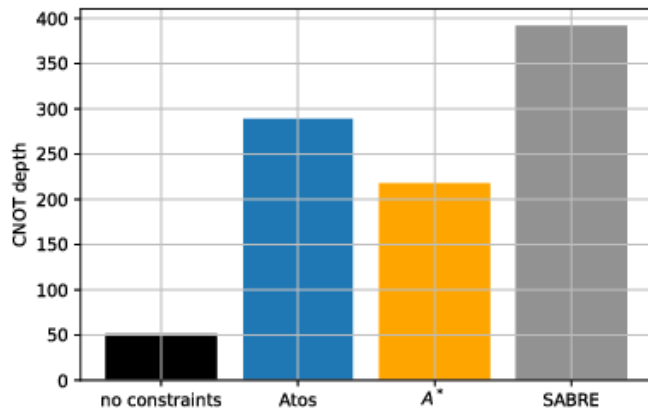
Connectivity map:



Gate count



CNOT depth

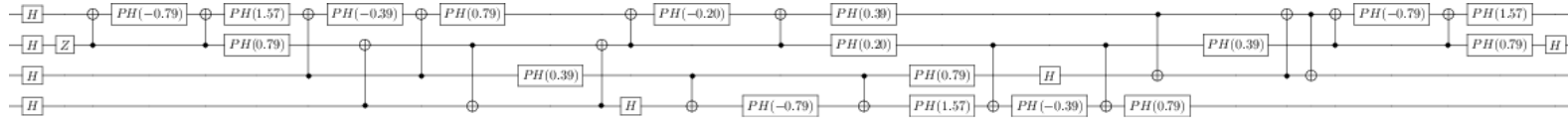


A\*: 1712.04722, SABRE: 1809.02573

1 SWAP=3 CNOTs, 1 C-PH=2 CNOTs

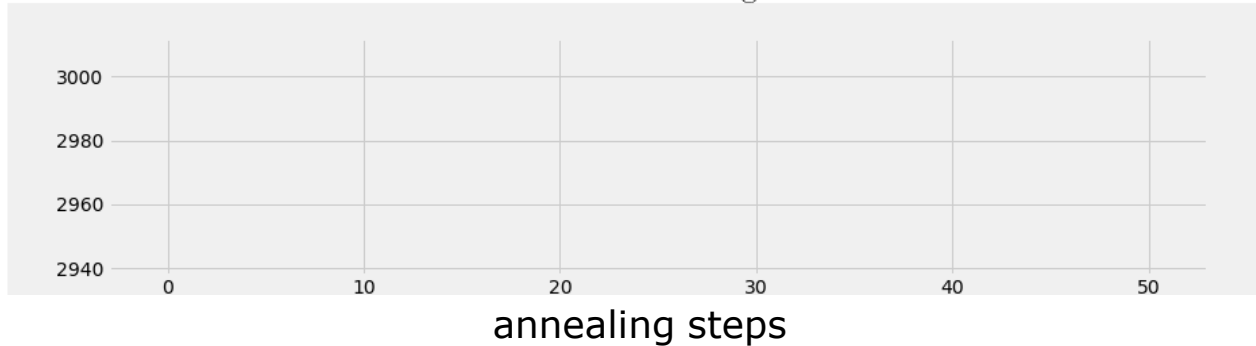
# Example 2: Minimization of the total idling time

- ▶ Start compiled Quantum Fourier (here 4 qubits)
- ▶ Use **commutation patterns** to reduce **total idling time**
- ▶ Minimization via (classical) **simulated annealing**



Minimize overall idling time

total  
idling  
time



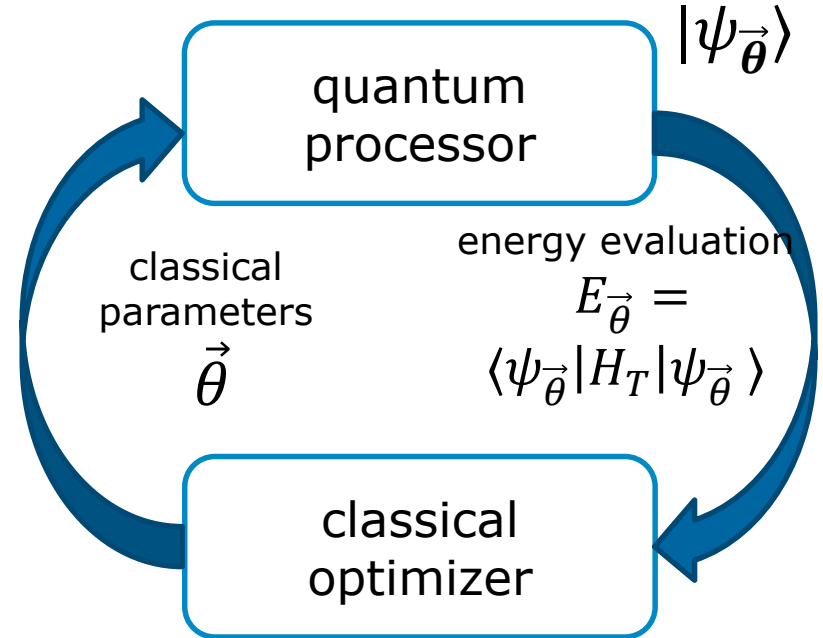
# 3

Applications  
with near-term processors

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# Variational quantum algorithms

- ▶ Overcome
  - short coherence times
- ▶ Split work between
  - quantum processor
  - classical optimizer
- ▶ **Goal:**
  - find lowest eigenenergy of Hamiltonian  $H_T$



# Applications of variational quantum algorithms

- ▶ Quantum chemistry (“VQE”)
  - Many small molecules (H<sub>2</sub>, LiH, ...)
  - Well-known variational states: unitary coupled cluster (UCC), etc.
- ▶ Combinatorial optimization (“QAOA”)
  - Special ansatz inspired from quantum annealing
- ▶ **Focus:** Variational quantum algorithms for **quantum field theory?**
  - Lattice QCD: a gauge theory plagued by Monte-Carlo sign problem in interesting regimes (hot quark-gluon plasma, neutron stars...)
  - Here, take Schwinger model (1+1-dim QED) as proxy for lattice QCD physics

## Challenge I:

# translate problem to quantum computer language

---

- ▶ (Kogut-Susskind) **fermions**... in **spin**/qbit-based quantum computer?
  - Jordan-Wigner transformation
- ▶ infinite gauge degrees of freedom... in finite-dim quantum computer?
  - Use Gauss law to eliminate gauge d.o.f -> traded for exotic **long-range spin-spin interactions**

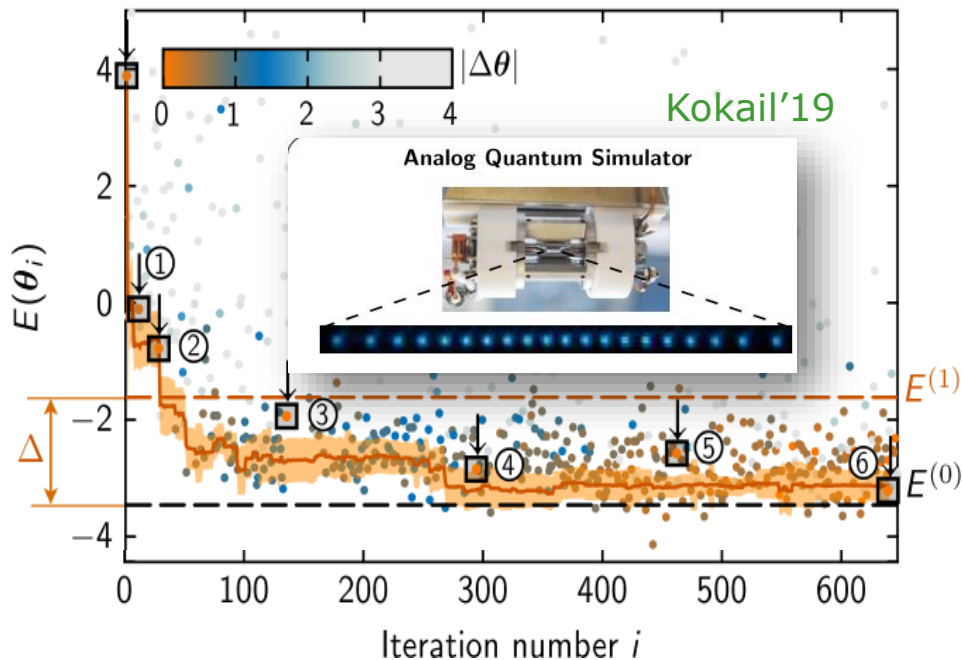
### ▶ Final Hamiltonian:

$$H_T = \sum_j \sigma_j^+ \sigma_{j+1}^- + h.c. + \frac{m}{2} \sum_j (-)^j \sigma_j^z + \frac{g}{4} \sum_j \left( \sum_{l \leq j} \sigma_l^z + (-)^l \right)^2$$

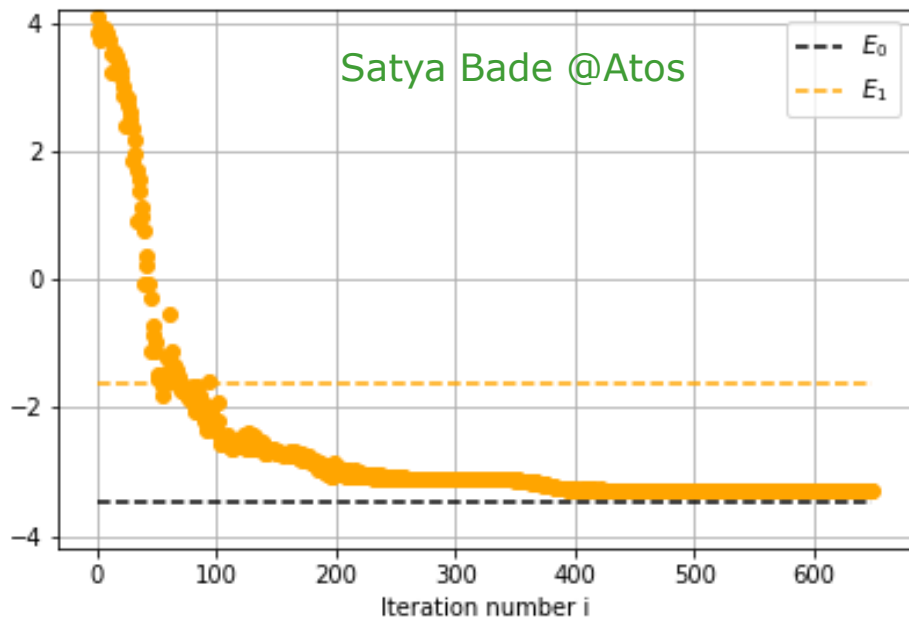
with mass  $m$ , coupling  $g$

# Challenge II: Experimental realization and simulation

► Experimental result (Nions=8):



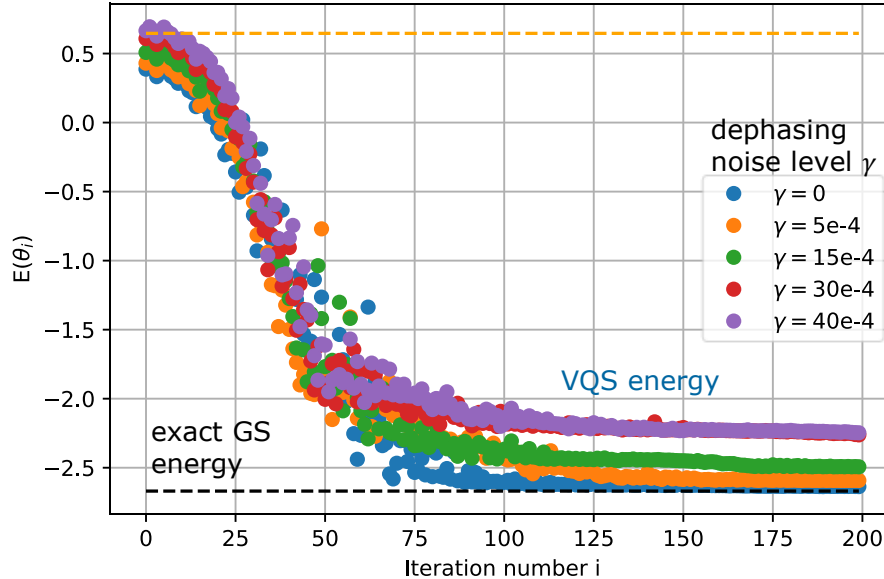
► Our simulation (Nions=8)



See also: digital computation with 4 ions (Martinez et al, Nature '16), 5 SC qubits (Klco et al PRA '18), ...

# Going beyond: impact of noise

- ▶ Noisy simulations with varying noise levels
  - Dephasing noise (Lindblad equation)





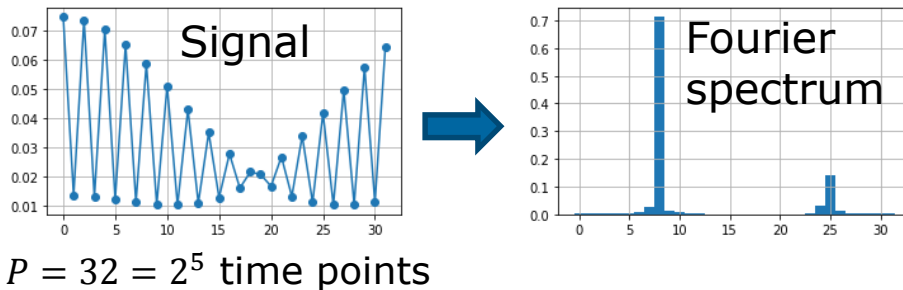
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Demonstration

# A Noisy Quantum Fourier Transform on the Atos Quantum Learning Machine

- ▶ Key ingredient of quantum factoring algorithms (“Shor algorithm”)

- ▶ From time to frequency:



- ▶ Best known classical algorithm: Fast Fourier Transform

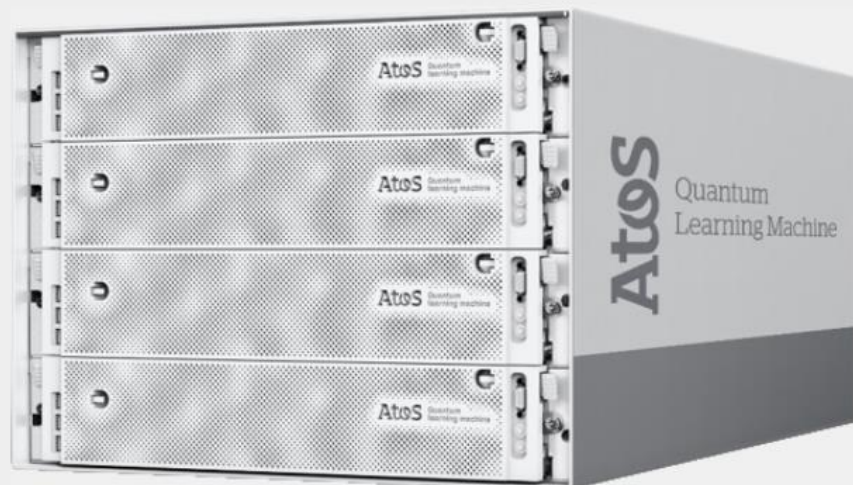
Number of operations:  $\sim P \log P$  for a signal of size  $P$

- ▶ Quantum Fourier Transform (QFT):

$\log P \log P$  operations: **exponential speedup!**

# A Noisy Quantum Fourier Transform on the Atos Quantum Learning Machine

Demonstration: simulate a (noisy) processor on the QLM



Part I: Writing an universal quantum program

Part II: IBM QX4 - superconducting qubits

Part III: AQTion-related results - trapped ions

## Part I: Writing an universal quantum program

Example: Quantum Fourier transform,  $\text{QFT}(|x\rangle) = \frac{1}{\sqrt{2^n}} \sum_{k=0}^{2^n-1} \left( e^{\frac{2i\pi}{2^n}} \right)^{xk} |k\rangle$

Key ingredient to e.g Shor's factoring algorithm.



# I.1 Writing the quantum program

The QLM provides usual quantum gates + libraries of quantum routines

```
Entrée [1]: from qat.lang.AQASM import Program
from qat.lang.AQASM.qftarith import QFT
from qat.linalg.oracles import StatePreparation
from demo_init import prepare_ft_signal, format_qft_output

nqbits = 5
prog = Program()
reg = prog.qalloc(nqbits)
state_prep = StatePreparation(prepare_ft_signal(nqbits))
prog.apply(state_prep, reg)
prog.apply(QFT(nqbits), reg)
qft_circ_boxed = prog.to_circ(inline=False)

%qatdisplay qft_circ_boxed
```

Out[1]:





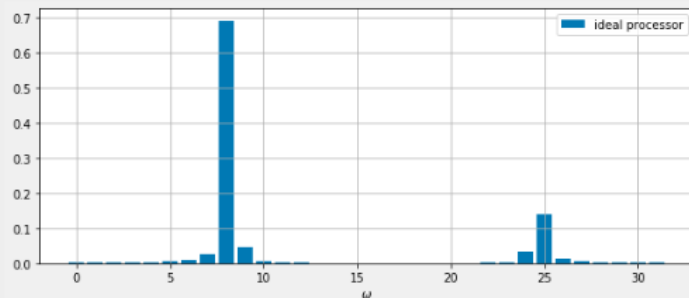
## I.2 Ideal simulation

```
Entrée [2]: import numpy as np
import matplotlib.pyplot as plt
%pylab inline
from qat.qpus import LinAlg

results = LinAlg().submit(qft_circ_boxed.to_job())

resprobs = np.zeros(shape=(2**nqubits))
for result in results.raw_data: resprobs[result.state.int]=result.probability
plt.figure(figsize=(10,4))
plt.bar(np.array(range(2**nqubits)), np.abs(format_qft_output(resprobs)), width=4/5, label="ideal processor")
plt.legend(); plt.grid(); plt.xlabel(r"$\omega$");
```

Populating the interactive namespace from numpy and matplotlib



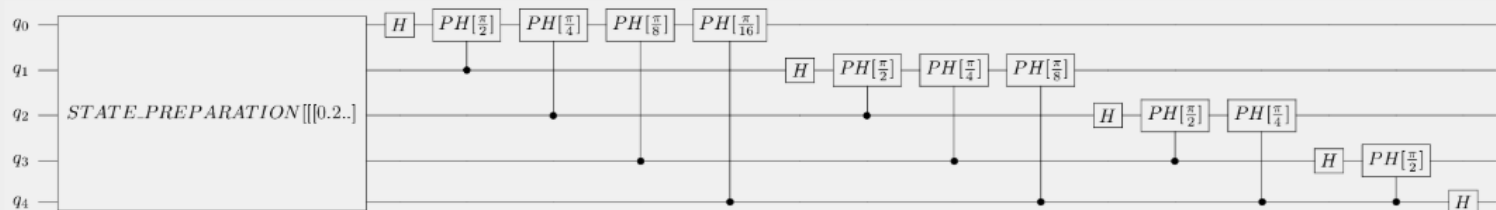


## I.3 Universal circuit

```
Entrée [3]: qft_circ = prog.to_circ(inline=True)
print("Number of gates:", len(qft_circ))
%qatdisplay qft_circ
```

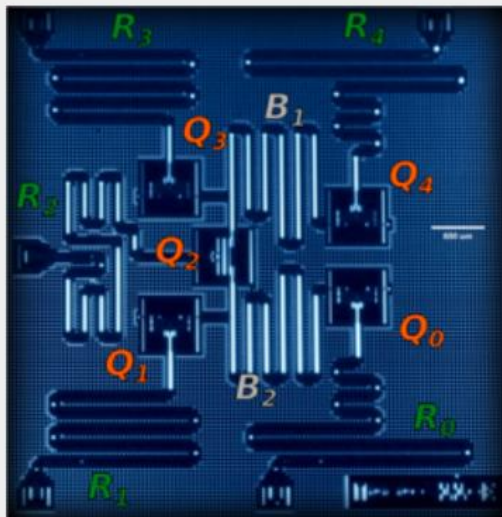
Number of gates: 16

Out[3]:





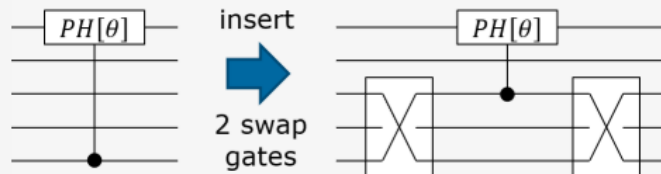
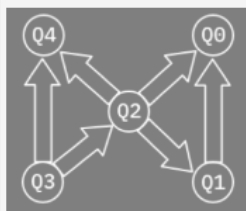
## Part II: IBM QX4 - superconducting qubits





## II.1 Connectivity

IBM QX4 has a limited qubit connectivity:



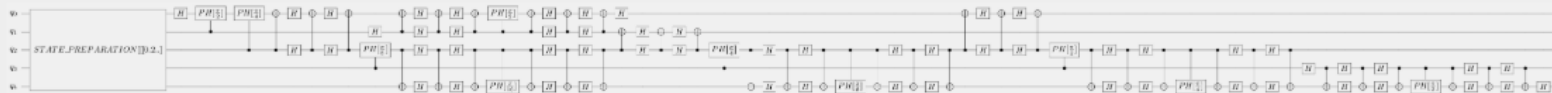
```
Entrée [4]: %cat graph_ibmqx4.json
```

```
{"edges": {"1": [0], "2": [0, 1, 4], "3": [2, 4]}}
```

```
Entrée [5]: import json
from qat.core.simutil import optimize_circuit
from qat.core import Topology, HardwareSpecs, TopologyType
graph_dict = json.load(open("graph_ibmqx4.json", 'r'))["edges"]
topology = Topology(type=TopologyType.CUSTOM, is_directed=True,
                    graph={int(vertex): edges for vertex, edges in graph_dict.items()})
hw_specs = HardwareSpecs(nqbqbits=nqbqbits, topology=topology)
from qat.plugins import Nnizer
nnizer = Nnizer(ignore_large_gates=True)
qft_conn_circ = optimize_circuit(qft_circ, nnizer, specs=hw_specs)
print("Number of gates:", len(qft_conn_circ))
%qatdisplay qft_conn_circ
```

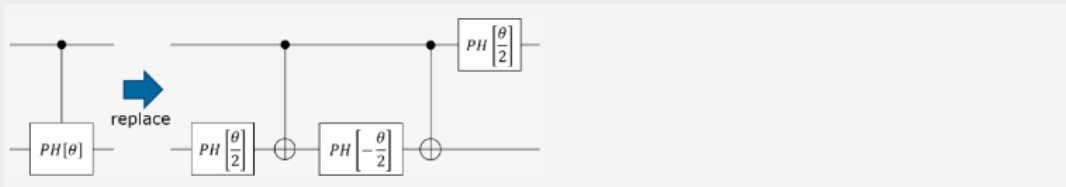
Number of gates: 107

Out[5]:



## II.2 Compilation (continued)

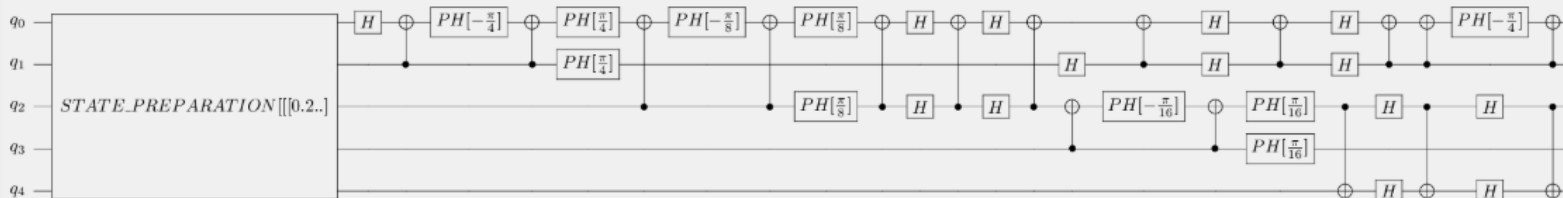
IBM QX4 only accepts CNOT gates for two-qubit operations:



```
Entrée [6]: from qat.pbo import VAR
from qat.plugins import GateRewriter
compiler = GateRewriter()
theta = VAR()
compiler.add_gate("C-PH",
                 variables=[theta],
                 pattern=[("CNOT", [0, 1]), ("PH", [1, -theta / 2]), ("CNOT", [0, 1]),
                          ("PH", [1, theta / 2]), ("PH", [0], theta / 2)])
compiler.add_abstract_gate("STATE_PREPARATION", lambda x: StatePreparation(x, False))
qft_conn_gates_circ = optimize_circuit(qft_conn_circ, compiler)
print("Number of gates:", len(qft_conn_gates_circ))
%qatdisplay qft_conn_gates_circ
```

Number of gates: 147

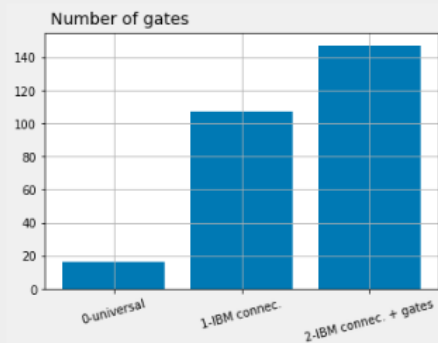
Out[6]:





## II.3 Gate counts before and after compilation

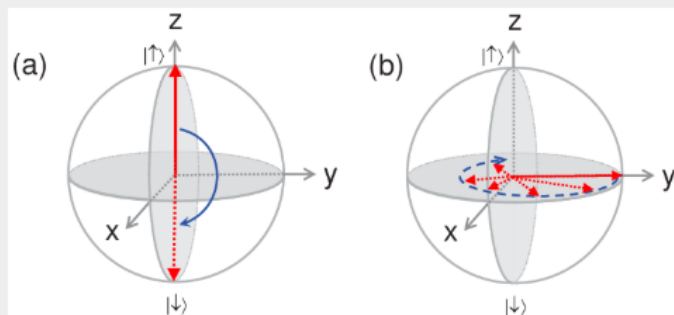
```
Entrée [7]: import matplotlib.pyplot as plt
%matplotlib inline
plt.bar(["0-universal", "1-IBM connec.", "2-IBM connec. + gates"],
        [len(c.ops) for c in [qft_circ, qft_conn_circ, qft_conn_gates_circ]])
plt.xticks(rotation=15); plt.text(-0.5,160,"Number of gates", size=14); plt.grid();
```



## II.4 Noisy simulation

Live simulation of noisy simulation on Atos QLM, with **simplified hardware model**:

- "Idle" qubits suffer from decoherence: **amplitude damping** (A.D) and **pure dephasing** (P.D).
- Relaxation and dephasing times from constructor:  $T_1$  and  $T_2$



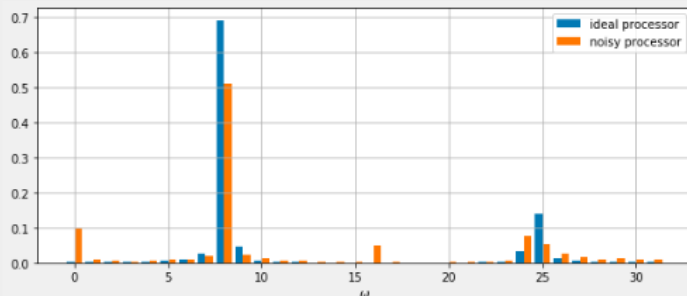
```
Entrée [8]: from qat.hardware import DefaultGatesSpecification, HardwareModel
from qat.core.circuit_builder.matrix_util import get_predef_generator
from qat.quops.quantum_channels import ParametricPureDephasing, ParametricAmplitudeDamping
gate_durations = {"H":60, "X":120, "Y":120, "S":1, "T":1, "D-T":1, "Z":1,
                  "RZ": lambda angle: 1, "PH": lambda angle: 1, "C-PH": lambda angle: 1,
                  "CNOT":386, "SWAP":100, "STATE_PREPARATION": 10}
pred_generator = get_predef_generator()
pred_generator["STATE_PREPARATION"] = prepare_ft_signal(nqubits)
ibm_gates_spec = DefaultGatesSpecification(gate_durations, predef_generator=pred_generator)
T1, T2 = 44000, 38900 #nanosecs
amp_damping = ParametricAmplitudeDamping(T_1=T1)
pure_dephasing = ParametricPureDephasing(T_phi=1/(1/T2 - 1/(2*T1)))
ibm_hardware = HardwareModel(ibm_gates_spec, idle_noise=[amp_damping, pure_dephasing])
```





## II.6 Result: Noisy Fourier spectrum

```
Entrée [10]: import numpy as np
from qat.qpus import LinAlg, NoisyQProc
from qat.plugins import QuameleonPlugin
plt.figure(figsize=(10,4))
ideal_qpu = LinAlg()
noisy_qpu = nnizer | compiler | QuameleonPlugin(specs=hw_specs) | NoisyQProc(hardware_model=ibm硬件)
for nqpu, (qpu, label) in enumerate([(ideal_qpu, "ideal processor"), (noisy_qpu, "noisy processor")]):
    results = qpu.submit(qft_circ.to_job())
    allprobs = np.zeros(shape=(2**nqubits))
    for result in results.raw_data: allprobs[result.state.int]=result.probability
    plt.bar(np.array(range(2**nqubits))+nqpu*2/5-1/5, np.abs(format_qft_output(allprobs)), width=2/5, label=label)
plt.legend(); plt.grid(); plt.xlabel(r"$\omega$");
```



## II.7 Fidelity optimization

```
Entrée [11]: from qat.plugins import PatternManager
from qat.noisy.noisy_circuit import total_idling_time

metric = lambda circ: -total_idling_time(circ, ibm_hardware)
manager = PatternManager(global_metric=metric)
x, y = VAR(), VAR()
group1 = manager.new_group()
group1.add_pattern([('PH', [1], x), ('CNOT', [0, 1]), ('PH', [1], y), ('CNOT', [0, 1])])
group1.add_pattern([('CNOT', [0, 1]), ('PH', [1], y), ('CNOT', [0, 1]), ('PH', [1], x)])
group2 = manager.new_group()
group2.add_pattern([('PH', [1], x), ('CNOT', [0, 1]), ('H', [0]), ('H', [1]), ('CNOT', [0, 1]), ('H', [0]), ('H', [1]), ('CNOT', [0, 1])])
group2.add_pattern([('CNOT', [0, 1]), ('H', [0]), ('H', [1]), ('CNOT', [0, 1]), ('H', [0]), ('H', [1]), ('CNOT', [0, 1]), ('PH', [0], x)])
group3 = manager.new_group()
group3.add_pattern([('PH', [0], x), ('CNOT', [0, 1]), ('H', [0]), ('H', [1]), ('CNOT', [0, 1]), ('H', [0]), ('H', [1]), ('CNOT', [0, 1])])
group3.add_pattern([('CNOT', [0, 1]), ('H', [0]), ('H', [1]), ('CNOT', [0, 1]), ('H', [0]), ('H', [1]), ('CNOT', [0, 1]), ('PH', [1], x)])
group4 = manager.new_group()
group4.add_pattern([('PH', [1], x), ("H", [1]), ("CNOT", [0, 1]), ("H", [1])])
group4.add_pattern([('H", [1]), ("CNOT", [0, 1]), ("H", [1]), ('PH', [1], x)])
group5 = manager.new_group()
group5.pattern_to_remove([('PH', [0], x), ('PH', [0], y)])
group5.add_pattern([('PH', [0], x + y)])
group6 = manager.new_group()
group6.pattern_to_remove([('CNOT', [0, 1]), ('CNOT', [0, 1])])
group6.pattern_to_remove([('H', [0]), ('H', [0])])
group6.add_pattern([])
manager.add_abstract_gate("STATE_PREPARATION", lambda x: StatePreparation(x, False))
qft_fid_optim_circ = manager.replace_pattern(
    qft_conn_gates_circ, method="annealing", max_iterations=250)
print("Number of gates:", len(qft_fid_optim_circ))
%qatdisplay qft_fid_optim_circ
```

Number of gates: 79

Out[11]:





## II.8 Results

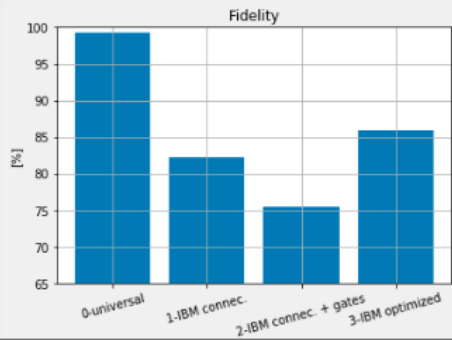
```
Entrée [12]: from qat.noisy import compute_fidelity
print("Initial idle time:", total_idling_time(qft_conn_gates_circ, ibm_hardware))
print("Final idle time:", total_idling_time(qft_fid_optim_circ, ibm_hardware))

fid_1 = compute_fidelity(qft_circ, ibm_hardware, use_linalg=True)
fid_2 = compute_fidelity(qft_conn_circ, ibm_hardware, use_linalg=False)
fid_3 = compute_fidelity(qft_conn_gates_circ, ibm_hardware, use_linalg=False)
fid_4 = compute_fidelity(qft_fid_optim_circ, ibm_hardware, use_linalg=False)

plt.bar(["0-universal", "1-IBM connec.", "2-IBM connec. + gates", "3-IBM optimized"],
        [fid_1[0]*100, fid_2[0]*100, fid_3[0]*100, fid_4[0]*100])
plt.title("Fidelity"); plt.xticks(rotation=15); plt.ylim(65,100); plt.grid();
plt.ylabel("%");
```

Initial idle time: 56722

Final idle time: 28106



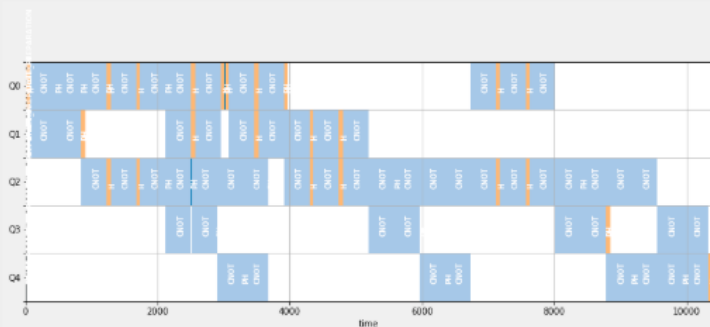
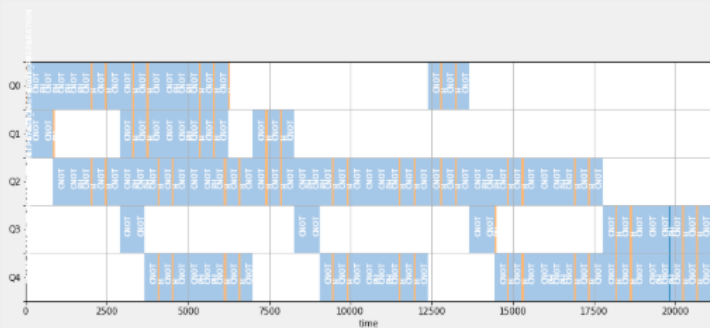




```
Entrée [13]: print("Number of gates:", len(qft_conn_gates_circ))
%qatdisplay qft_conn_gates_circ ibm_hardware
print("Number of gates:", len(qft_fid_optim_circ))
%qatdisplay qft_fid_optim_circ ibm_hardware
```

Number of gates: 147

Number of gates: 79





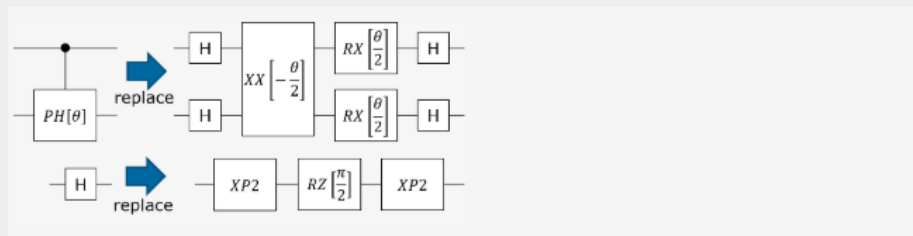
## Part III: AQTion-related results - trapped ions





## III.1 Compiling for ions

We use the same plugin as for IBM, but with different patterns:



Use abstract gates to create custom parametrized gates, like

$$XX[\phi] = \frac{1}{\sqrt{2}} \begin{bmatrix} 1 & 0 & 0 & -ie^{i\phi} \\ 0 & 1 & -i & 0 \\ 0 & -i & 1 & 0 \\ -ie^{-i\phi} & 0 & 0 & 1 \end{bmatrix}$$



```

Entrée [14]: from qat.pbo import VAR
from qat.plugins import GateRewriter
gr_compiler = GateRewriter()
theta = VAR()

## C-PH => XX & H & RZ
gr_compiler.add_gate("C-PH",
                    variables=[theta],
                    pattern=[("H", [0]), ("H", [1]), ("XX", [0, 1], -theta/2),
                             ("RX", [0], theta/2), ("RX", [1], theta/2), ("H", [0]), ("H", [1])])

## H => XZX
gr_compiler.add_gate("H",
                    variables=[],
                    pattern=[("XP2", [0]), ("RZ", [0], np.pi/2), ("XP2", [0])])

## RX(theta) ==> XP2 & RZ(theta)
gr_compiler.add_gate("RX",
                    variables=[theta],
                    pattern=[("RZ", [0], np.pi/2), ("XP2", [0]), ("RZ", [0], theta - np.pi),
                             ("XP2", [0]), ("RZ", [0], np.pi/2)])
gr_compiler.add_abstract_gate("STATE_PREPARATION", lambda x: StatePreparation(x, False))

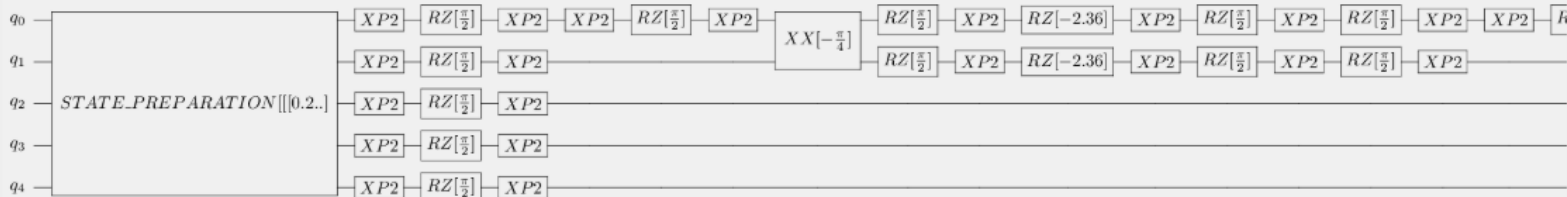
from ion_gate_set import ion_gate_set
for _, gatedef in ion_gate_set.gate_signatures.items():
    gr_compiler.add_abstract_gate(gatedef)
qft_gates_circ = optimize_circuit(qft_circ, gr_compiler | gr_compiler)

print("Number of gates:", len(qft_gates_circ))
%qatdisplay qft_gates_circ

```

Number of gates: 246

Out[14]:





## III.2 Noisy simulation with tomography data

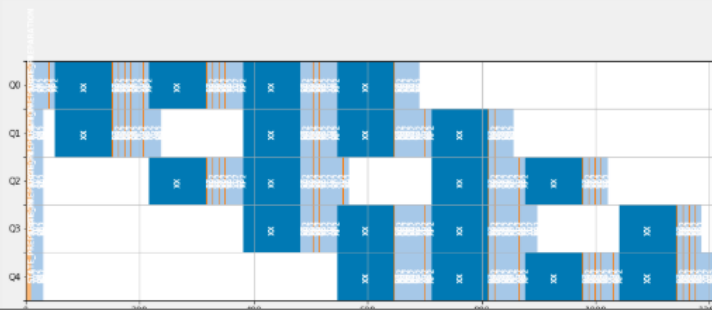
Here we load a noise model computed by performing tomography of some gates of the trapped-ion processor of the University of Innsbruck (UIBK):

```
Entrée [15]: from qat.errmitigation.UIBK import get_hdw_gate_spec
             from qat.quops import QuantumChannelKraus

             #Loading noise model computed from linear gateset tomography
             ion_gspec = get_hdw_gate_spec(channel_representation="Kraus")

             # adding perfect XX (no tomography data) and RZ gate (always perfect because done 'in software')
             ion_gspec.quantum_channels["XX"] = lambda angle: QuantumChannelKraus([gen_XX(angle, 2)])
             ion_gspec.quantum_channels["RZ"] = lambda angle: QuantumChannelKraus([gen_Z(angle)])
             ion_gspec.quantum_channels["STATE_PREPARATION"] \
                 = QuantumChannelKraus([prepare_ft_signal(nqbits)], name="state_preparation")
             ion_gspec.gate_times = {"RZ": lambda angle: 1,
                                    "XX": lambda angle: 100,
                                    "STATE_PREPARATION": 10, "XP2": 10}
             ion_hardware2 = HardwareModel(gates_specification=ion_gspec)
             print("Number of gates:", len(qft_gates_circ))
             %qatdisplay qft_gates_circ ion_hardware2
```

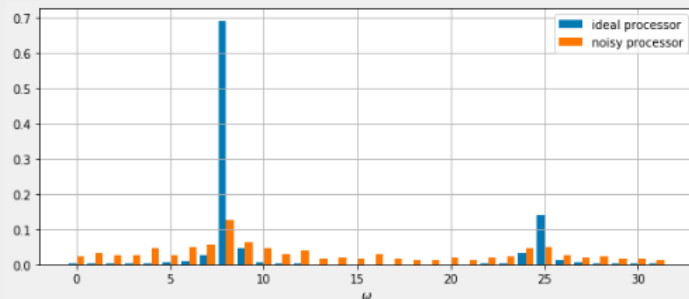
Number of gates: 246





```
Entrée [16]: from ion_gate_set import gen_X, gen_Z, gen_XX
             compiler = gr_compiler | gr_compiler #need 2 passes to replace all patterns
             ideal_qpu = LinAlg()
             noisy_qpu = compiler | NoisyQProc(hardware_model=ion_hardware2)

             plt.figure(figsize=(10,4))
             for nqpu, (qpu, label) in enumerate([(ideal_qpu, "ideal processor"), (noisy_qpu, "noisy processor")]):
                 results = qpu.submit(qft_circ.to_job())
                 allprobs = np.zeros(shape=(2**nqubits))
                 for result in results.raw_data: allprobs[result.state.int]=result.probability
                 plt.bar(np.array(range(2**nqubits))+nqpu*2/5-1/5, np.abs(format_qft_output(allprobs)), width=2/5, label=label)
             plt.legend(); plt.grid(); plt.xlabel(r"$\omega$");
```



In summary,

We have

⇒ defined a simple universal circuit

*with an Oracle and a QRoutine from the QLib*

⇒ simulated it on a perfect QPU

*with the ideal Linear Algebra simulator*

⇒ optimized it for specific hardware (superconducting qubits and trapped ions)

*with NNizer (for topology),*

*with Pattern-Based Optimizer (for gate replacement and idle time optimization)*

*with Abstract Gates*

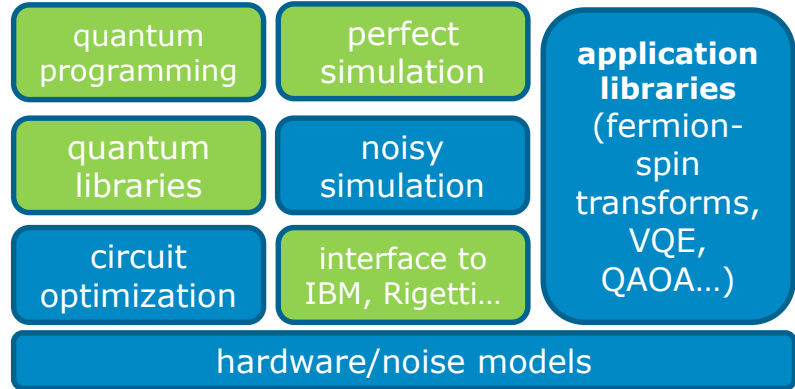
*with Noise Simulation*

# Conclusion

---

- ▶ Hands-on tutorial this afternoon (3:30pm) with Jean-Christophe Jaskula
  - make sure you have downloaded the myQLM docker
- ▶ Menu:
  - write and run quantum programs
  - variational minimization using quantum circuits

## myQLM: “QLM lite”, free!





# Thank you

[thomas.ayral@atos.net](mailto:thomas.ayral@atos.net)

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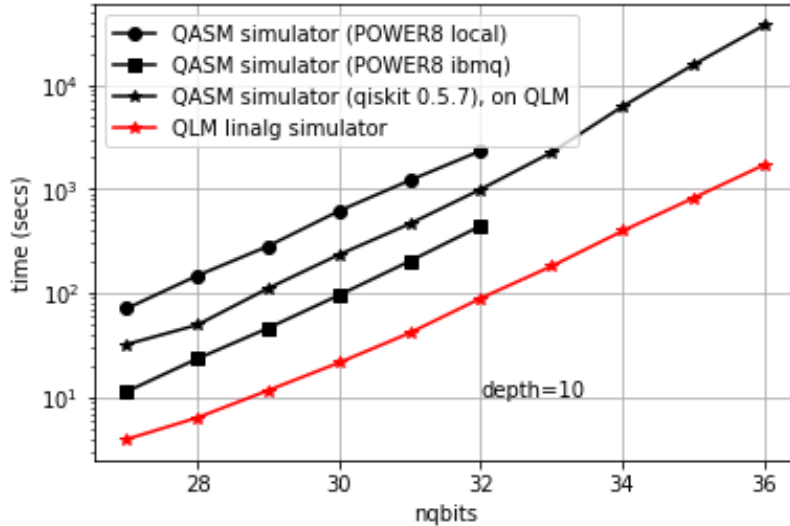
The Atos logo is displayed in white, bold, sans-serif capital letters. The letter 'o' is stylized with a white circle inside it. The logo is positioned in the bottom right corner of the slide.

# Speed comparison

QLM vs IBM Qiskit simulator

Perfect simulation

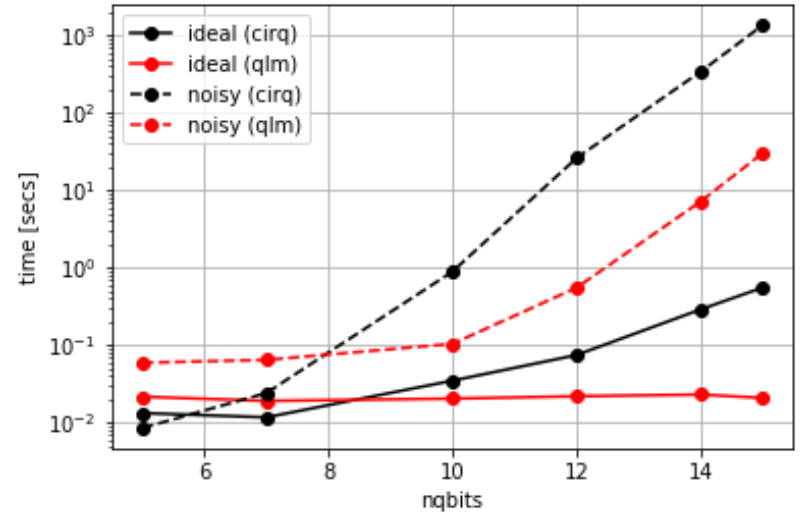
'Quantum volume' benchmark circuit



QLM vs Google cirq simulator

Perfect + noisy simulation

H+CNOT circuit



QLM: **qat.linalg** simulator

IBM POWER8 benchmark data from

[www.ibm.com/blogs/research/2018/05/quantum-circuits](http://www.ibm.com/blogs/research/2018/05/quantum-circuits)

QLM: **qat.linalg** and **qat.noisy**

**(deterministic-vectorized)** simulator