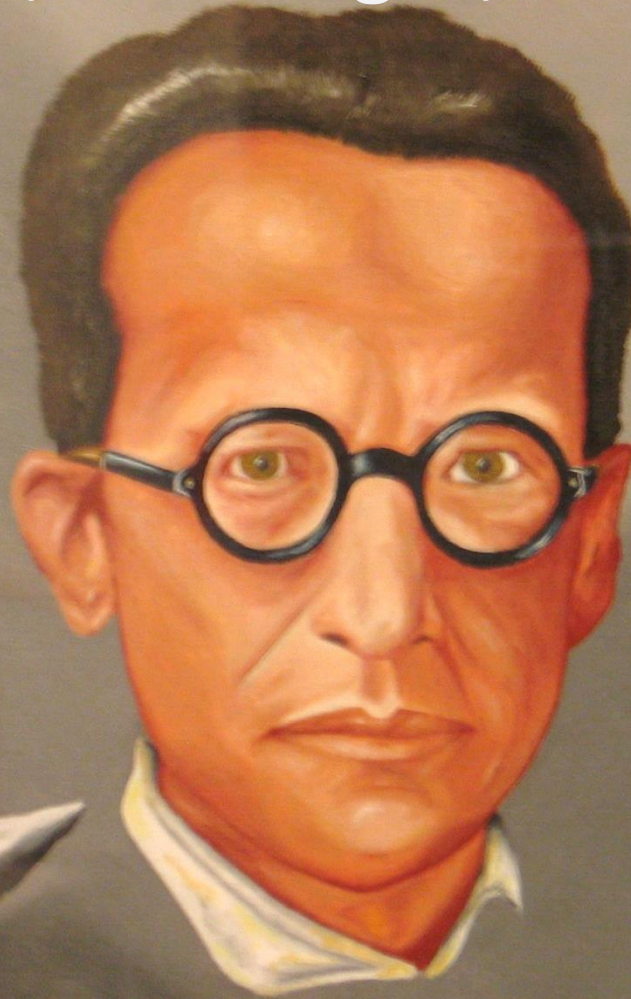


# Electrical circuits for quantum computing: first results, challenges, strategies,

Journées thématiques IN2P3  
Quantum computing:  
state of the art and applications



Daniel ESTEVE

QUANTUM  
ELECTRONICS GROUP



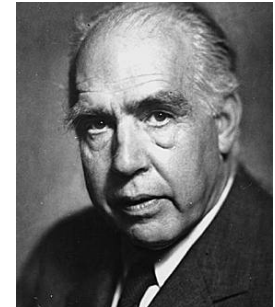
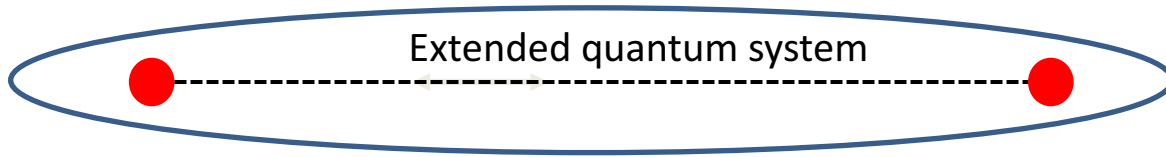
ED. C. 04

# From quantum weirdness to quantum resources

1935... The EPR paradox and the Bohr-Einstein controversy



*This cannot be described by a quantum state  
Formalism is incomplete!*



*This is it !*

1964: This debate can be addressed

done in 1982



John Bell

$$|left+, right-\rangle + |left-, right+\rangle$$



(non factorisable) entangled state  $|left\rangle \otimes |right\rangle$

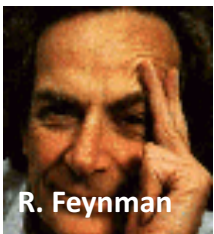


Alain Aspect

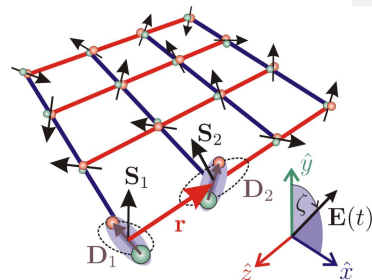
Non-local correlations  
in agreement with  
quantum predictions

1982: Quantum systems too hard to crack,  
quantum simulation needed!

1984 quantum cryptography protocol  
1985 an unexpected breakthrough



R. Feynman



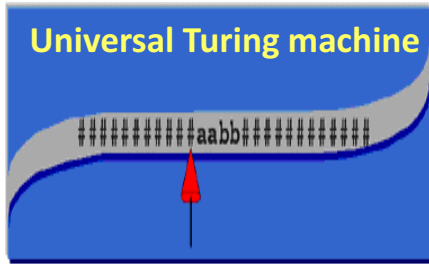
D. Deutsch

*Quantum mechanics  
provides  
computational resources*

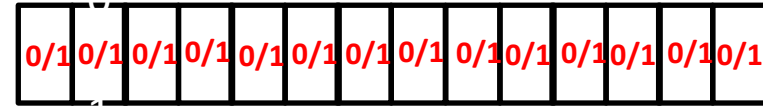


# Quantum computing in a nut

## Classical computing:



$N$  (0,1) bits evolving  
among  $2^N$  states



$$R = (i_1, i_2, i_3 \dots i_{2^N}) \quad i_k = 0, 1$$

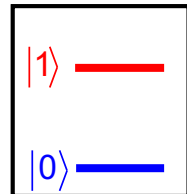
Turing machine not universal !  
complexity classes scrambled  
for quantum hardware

## Quantum computing:

evolution of a  $N$  qubit quantum register using quantum gates  
among **superpositions of  $2^N$  basis states**

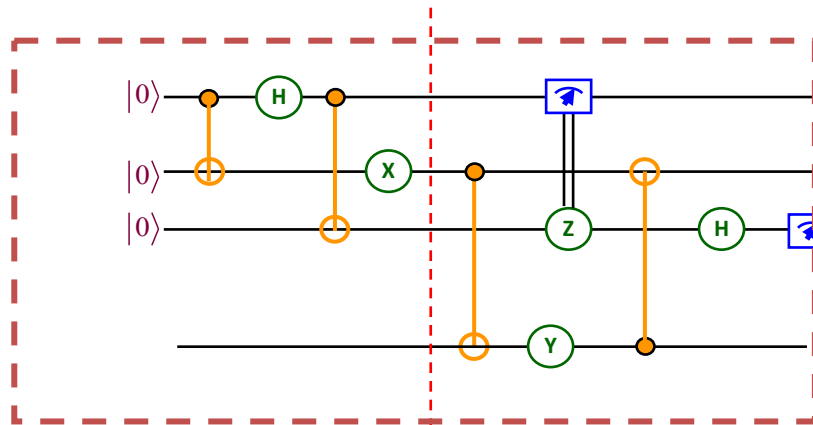
qubit

2 level system



$N = 2^n$  computational  
basis states

$$\overbrace{|010001\dots 1\rangle}^n = |p\rangle$$



Readout

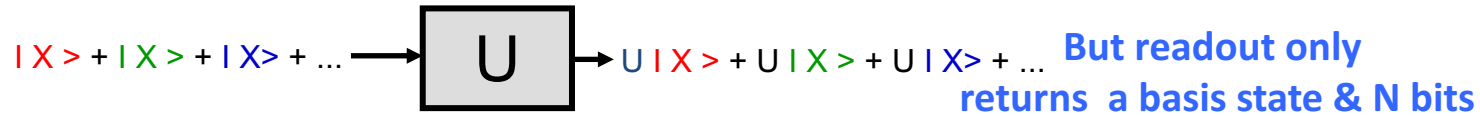
returns 0 or 1  
for each qubit :  
**a basis state**

**non factorizable entangled state:**  $\sum_{i_k=0,1} a_{i_1 i_2 i_3 \dots i_{2^N}} |i_1, i_2, i_3 \dots i_{2^N}\rangle$

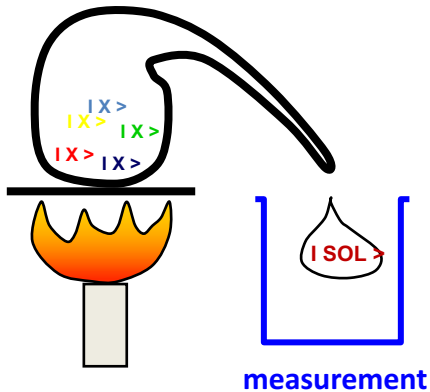
**entanglement delivers  
computing power**

# The art of QC

QM linearity provides massive parallelism



The method:



Difficult

not so many different quantum algorithms

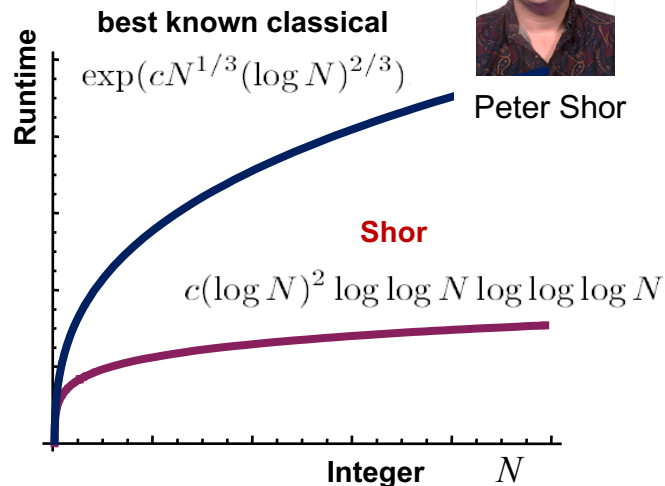
How many qubits for overcoming a classical computer ?

A 50-100 ideal qubit qu. computer could overcome classical computers (for some tasks)

Factorization algorithm (1994)



Peter Shor

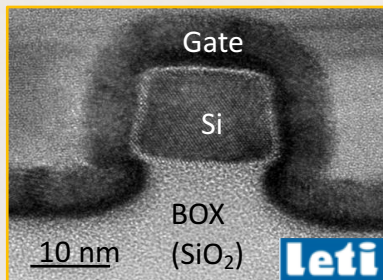




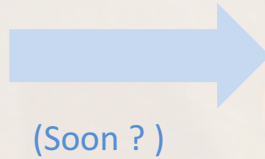
# The hpc context:

## massive integration reaches physical limits

Semiconducting circuits reach physics limits  
+ increasing needs

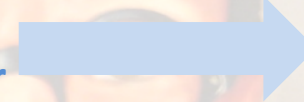


Ultimate CMOS



(Soon ? )

3D stacking  
ultra low power



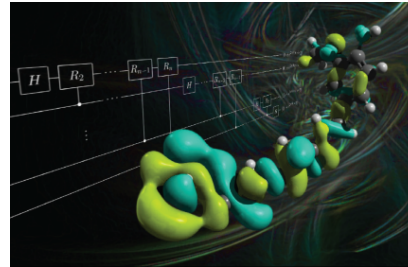
Alternative  
technologies  
for HPC ?

Quantum Computing  
now envisioned

# QC: A potential breakthrough in HPC (?)

## Use-cases

Many-body physics:  
quantum chemistry, materials  
nuclear physics ...



Fermionized Hamiltonians  
map well on qubits

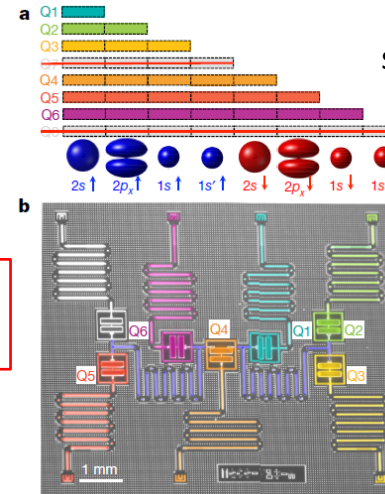
needs: >100 qubits

Linear algebra:  
quantum inversion of  
sparse matrices

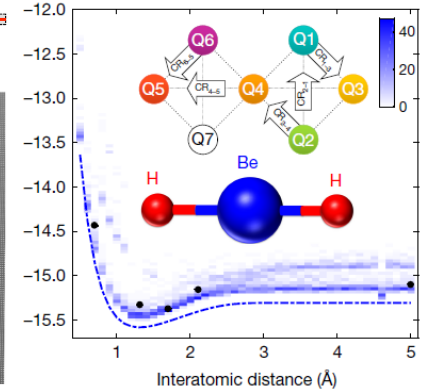
HHL algorithm

Harrow, Hassidim, Lloyd, PRL 103, 150502 (2009)

Classification,  
Optimization  
Machine learning



small scale demos:



variational quantum eigensolver :  
IBM Kandala et al., Nature 549, 242 (2017)

quantum RAM needed !

Big players attracted, strong partnerships developed



"Strong " Eu flagship initiative

Eu:

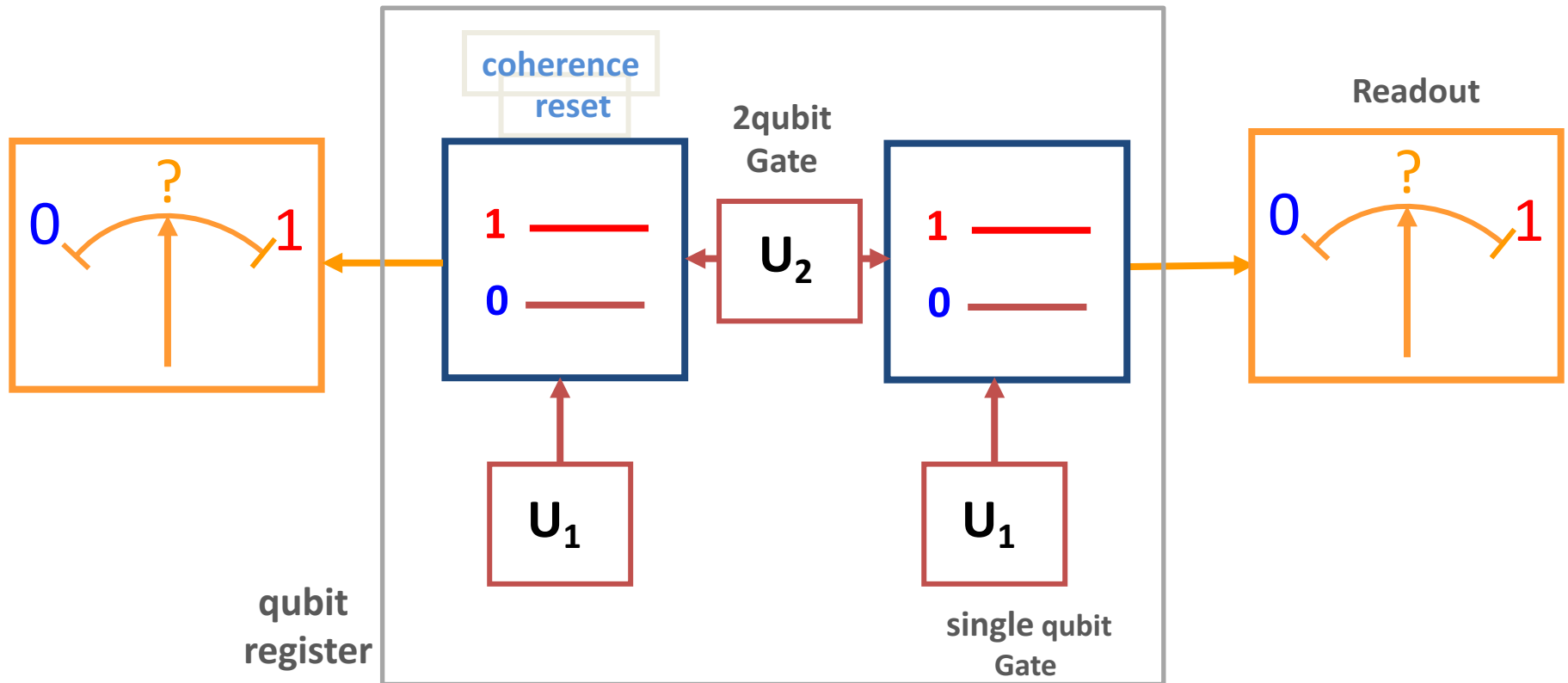
Atos

# blueprint of a quantum processor (based on quantum gates)

qubits  
(2 level systems)

Universal set of  
unitary gates

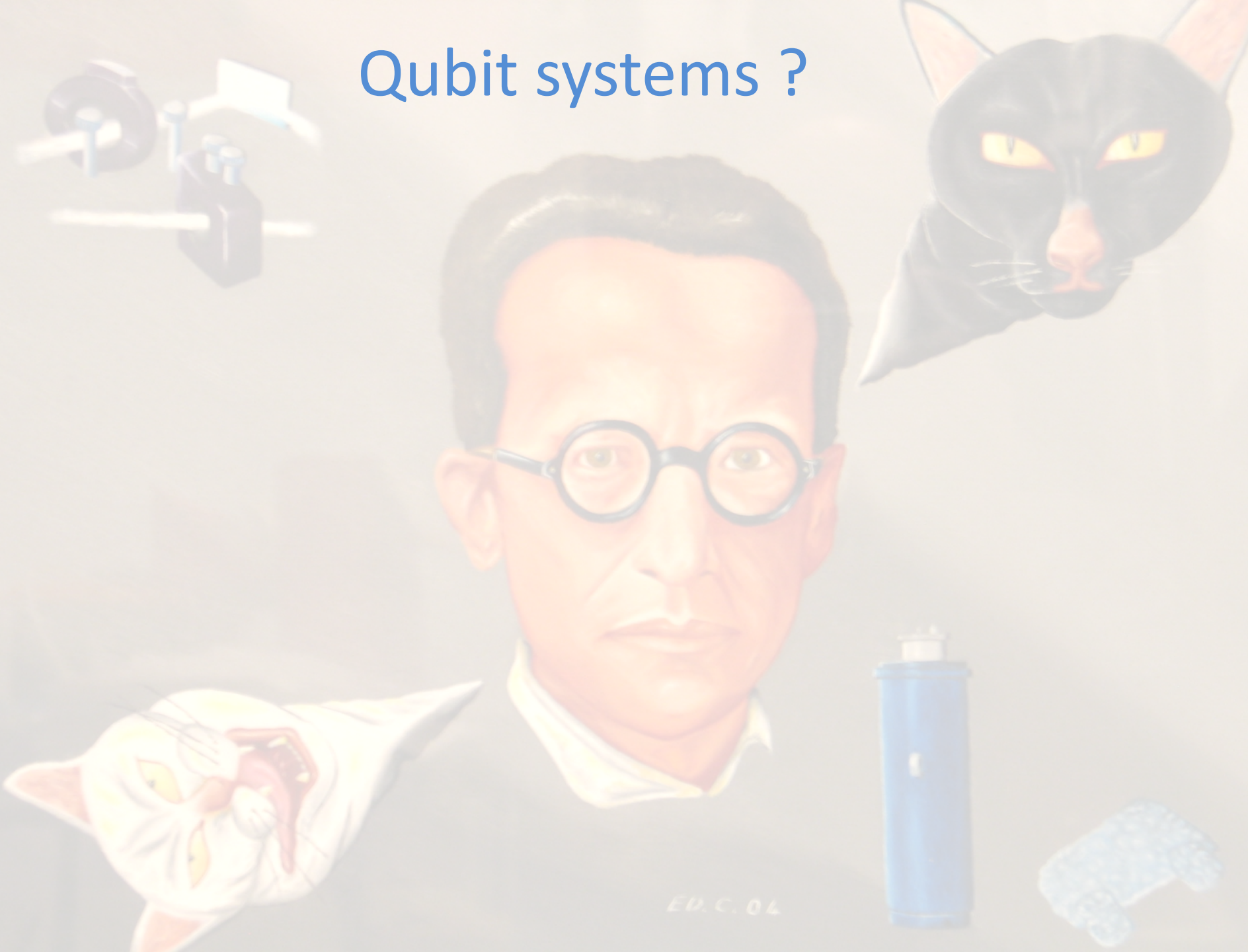
high fidelity  
projective readout



"DiVincenzo criteria"



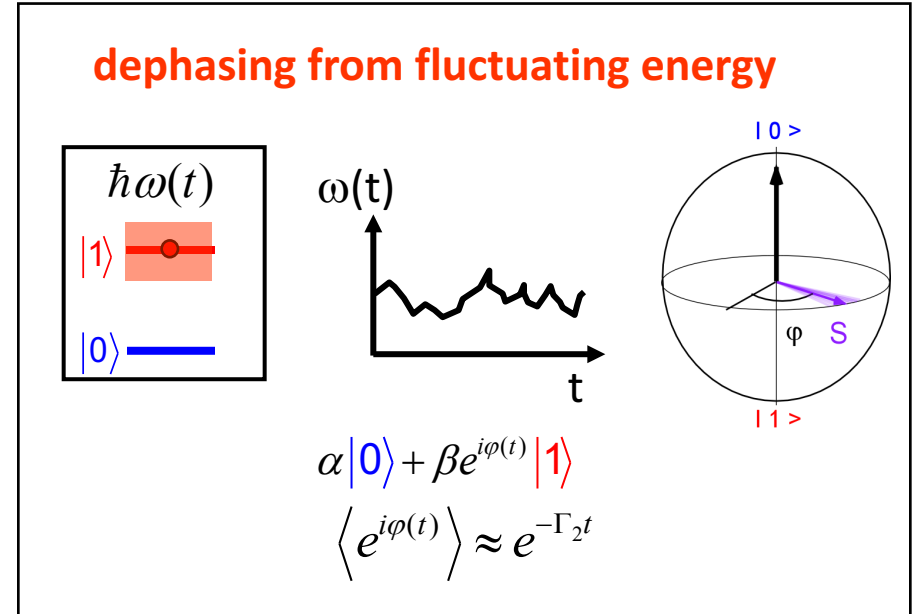
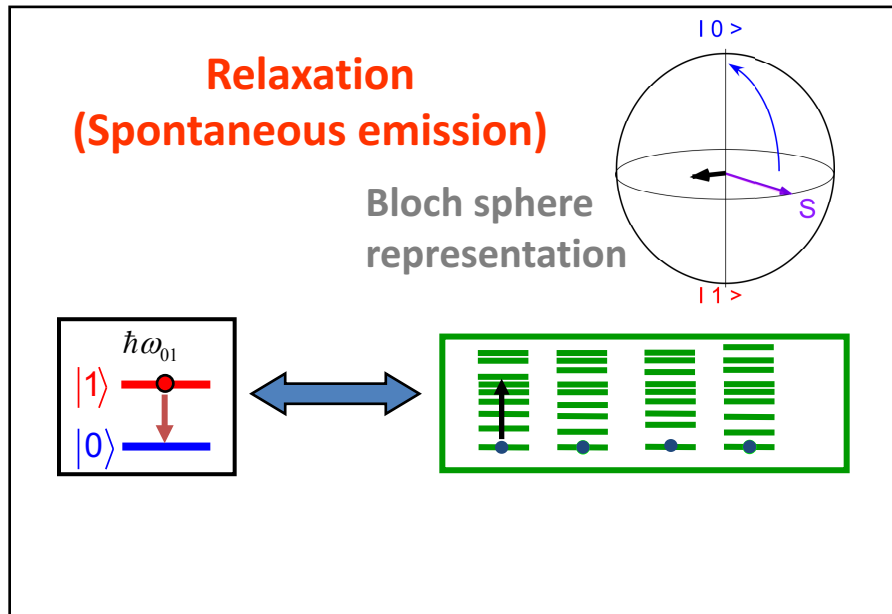
# Qubit systems ?



# Why is any quantum system not a quantum bit ?

coupling to environment yields **decoherence**

cf Ithier et al., PRB 72, 134519, 2005



**Microscopic systems**  
weakly coupled to their environment  
quantum regime easy  
not easily addressable

**Macroscopic systems**  
strongly coupled to their environment  
quantum regime difficult  
easily addressable

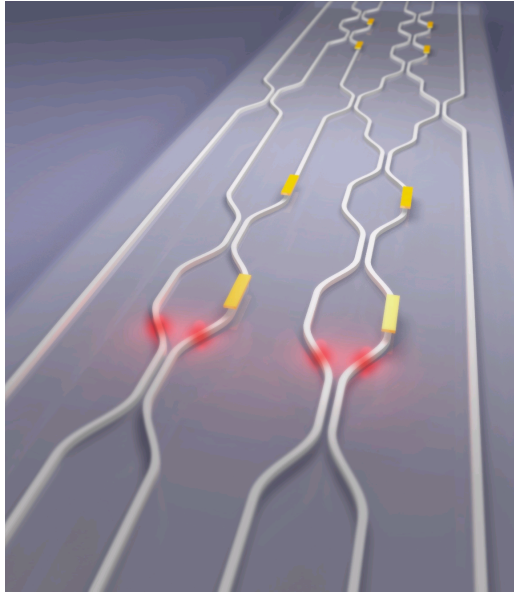
**solutions ?**

# Physical implementations ?

## NMR

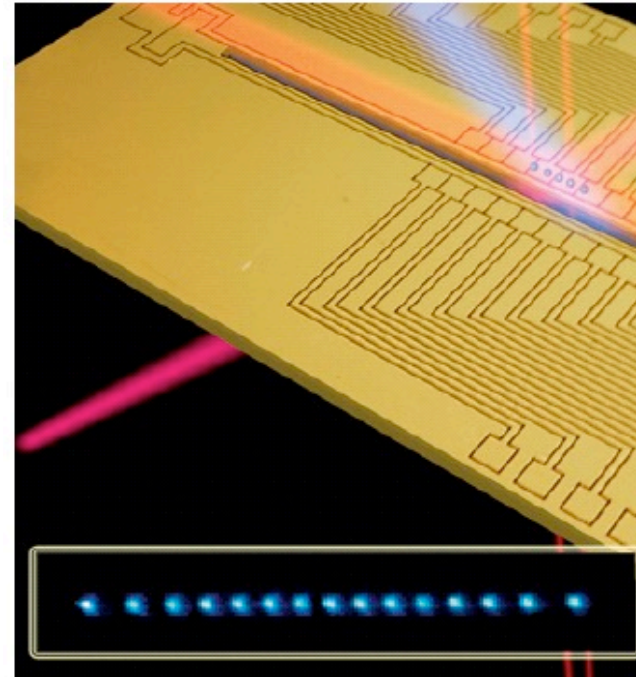


## Photons



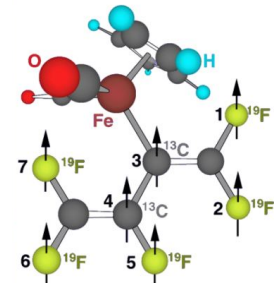
Measurement based QC:  
not efficient

## Trapped ions (or atoms)

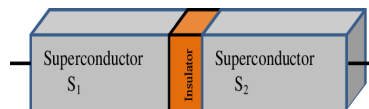


The most advanced platform

## Electrical circuits ? usually not quantum !



not scalable:  
code=molecules



Quantum Mechanics of a Macroscopic Variable:  
The Phase Difference of a **Josephson Junction**

Clarke, Cleland, Devoret, Esteve and Martinis, Science 239, 992, 1988

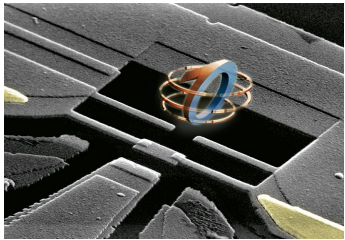
**A quantum component**  
**The Josephson junction**



# Electrical qubit circuits (in a nut)

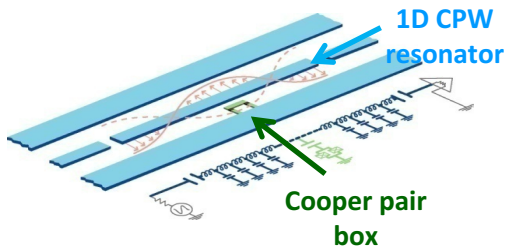
quantum states  
of superconducting circuits

Superconducting qubits based on the  
Single Cooper Pair Box circuit



functional SC qubit  
(CEA 2002)

Now: Transmon type Cooper Pair Box circuit

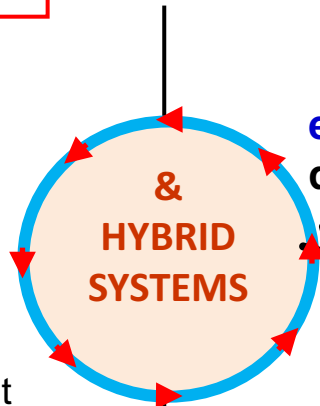
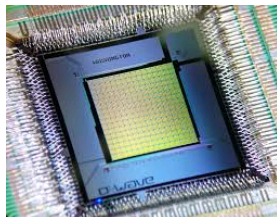


Yale  
(2004-2006-2010)

Different computing strategy  
quantum annealing

difficult problems solved  
quantum speed-up not  
demonstrated

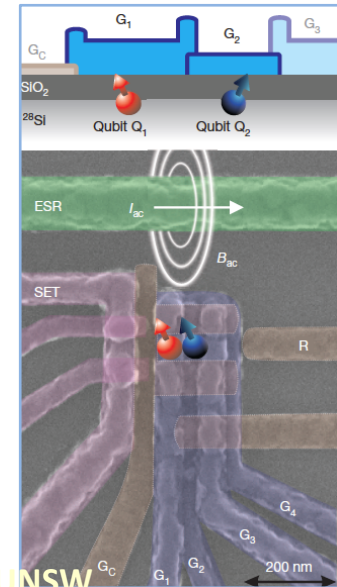
DWAVE



e spins in  
quantum dots

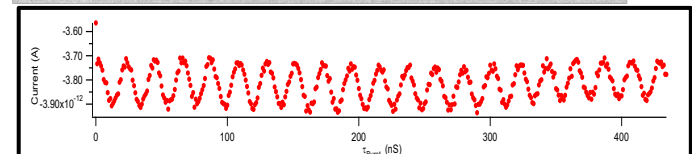
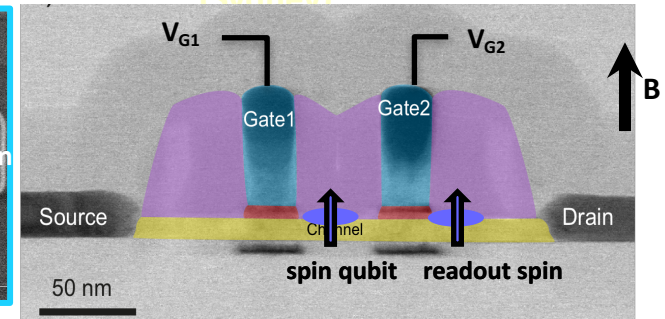
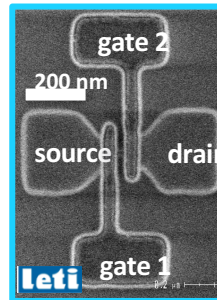
UNSW, TUDelft,  
Harvard,  
CEA (INAC-LETI)

Electron spin states  
in semiconductor structures



UNSW  
(Sydney)

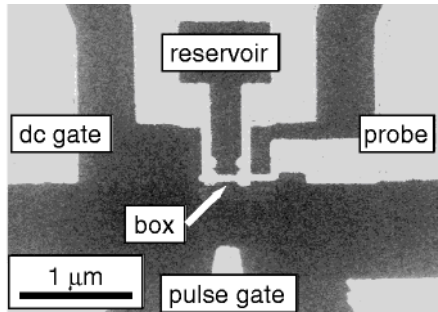
First qubit from  
on an industrial  
fab line at CEA



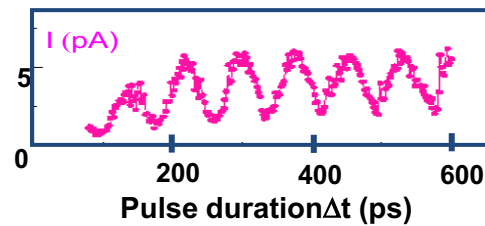
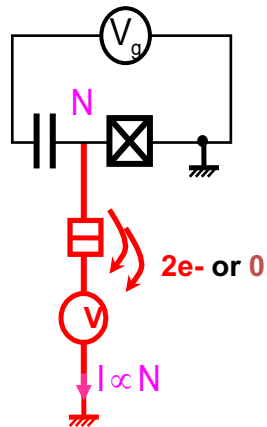
# The Cooper Pair Box quantum bit: a brief survey

## first Cooper Pair Box qubit

Nakamura, Pashkin & Tsai (NEC, 1999)

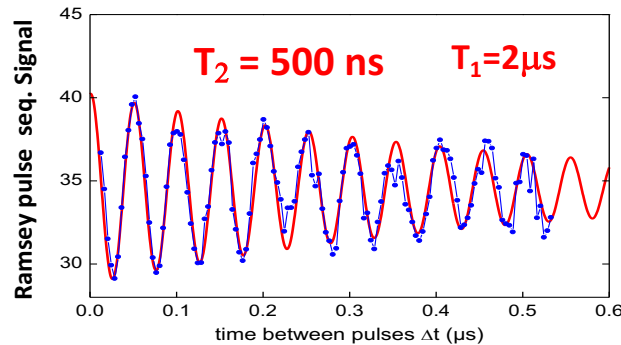
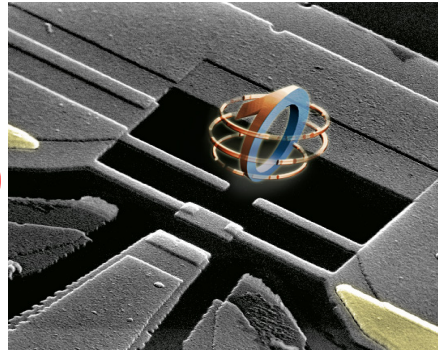


x100



## First operational qubit

Vion et al., (Quantronics, 2002)

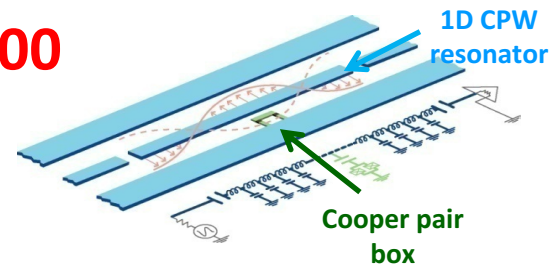


## Circuit QED: transmon Cooper pair box in a microwave cavity (2D, 3D)

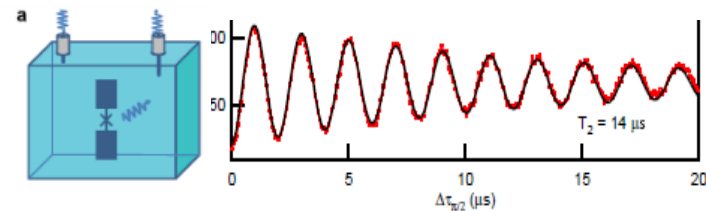
Schoelkopf lab., Yale ; Wallraff et al., Nature 2004

-Koch et al., PRB 2007; Paik et al., PRL 2011

x100

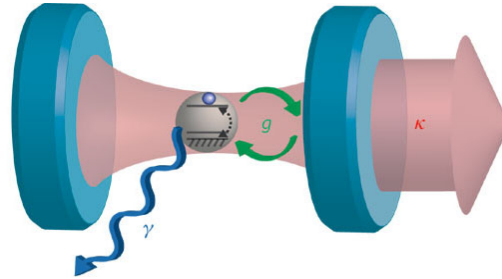


CPBox in a 3D resonator



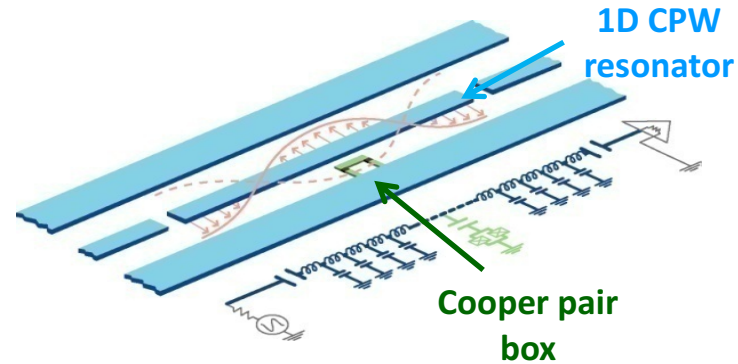
# The modern Cooper pair box: Circuit QED

Inspired from cavity QED



S. Haroche, JM Raimond, M. Brune  
LKB- ENS Paris

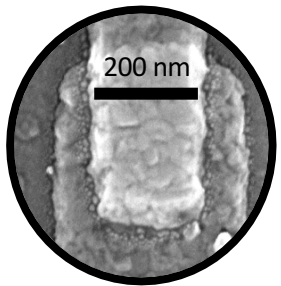
**Cooper Pair Box 'atom' in resonator**  
(Schoelkopf group, Yale, 2004)



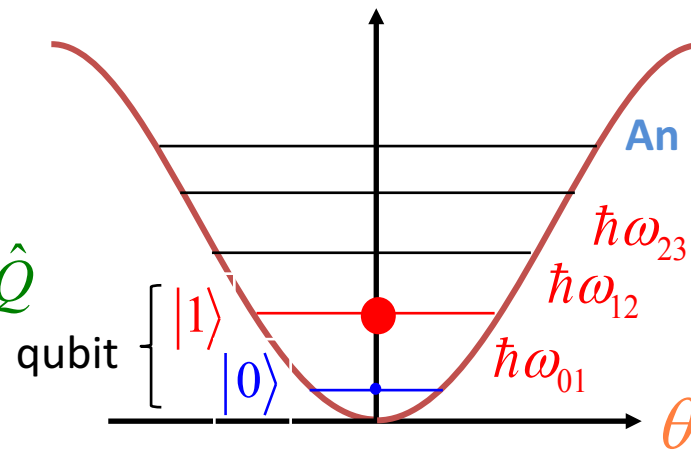
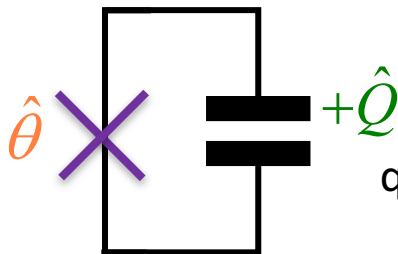
**Transmon Cooper pair box**  
**insensitive to charge noise**

Koch et al., Yale, 2007

The transmon



Al/Al<sub>2</sub>O<sub>3</sub>/Al



An artificial atom based on an  
anharmonic oscillator

$$E_J \gg E_C$$

embedded in a  
microwave resonator

$$\hat{H} = -E_J \cos(\theta) + E_C (\hat{Q}/2e)^2$$

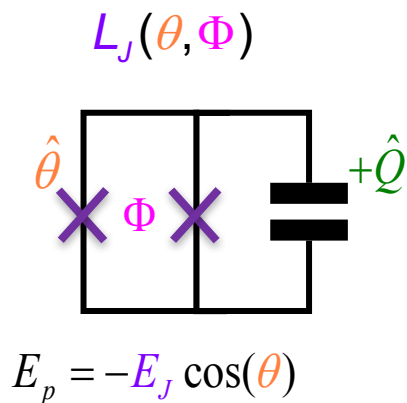
$$E_C = (2e)^2 / 2C$$

Bonus: insensitive to charge noise

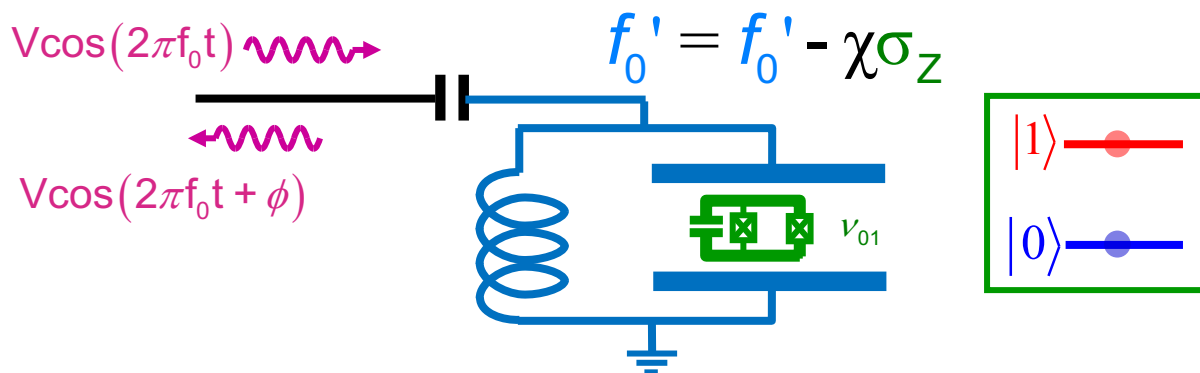


# Circuit-QED architecture to readout a Josephson qubit

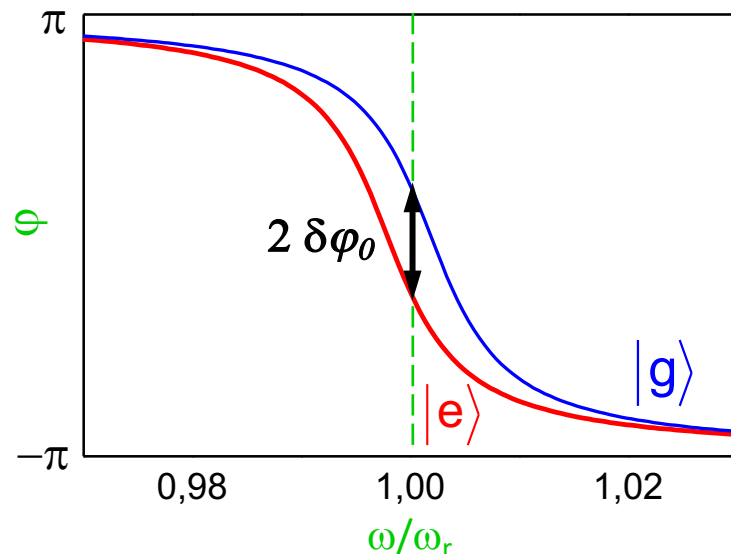
flux tunable qubit



Dispersive readout with a resonator :



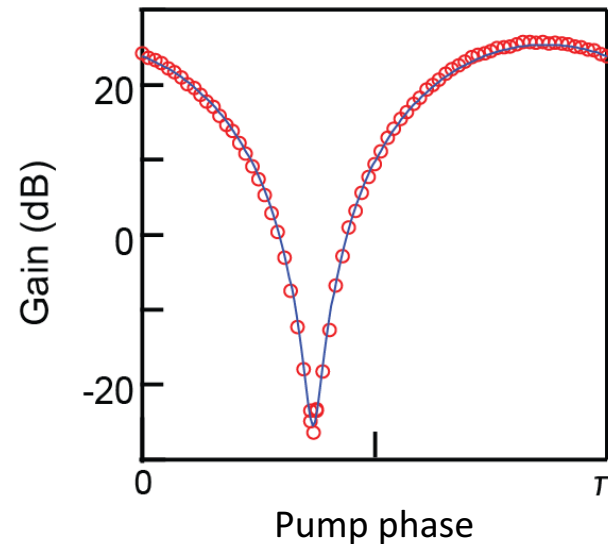
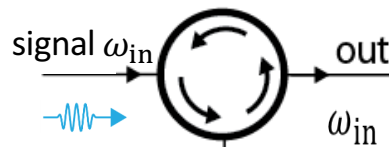
qubit controlled  
**Cavity pull**  
used for qubit readout



# A key element for low power measurements: the Josephson Parametric Amplifier

M. Castellanos-Beltran et al., APL (2007)...TWPA (wide band): Macklin et al. Science 2015

## JPA in degenerate mode

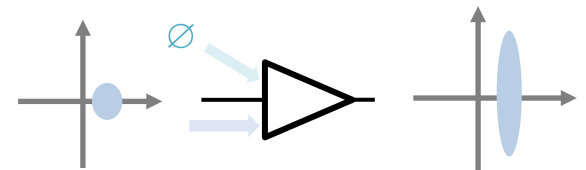


Flux parametric pumping design:  
X. Zhou et al., PRB (2014)

DC bias  
AC pump tone  
 $\omega_p = 2\omega_{in}$

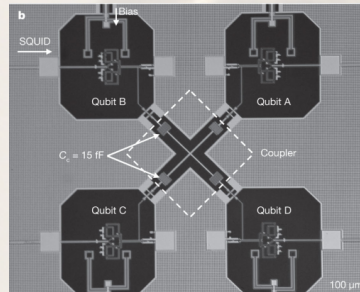
Noiseless amplifier

Unitary transformation of input signal

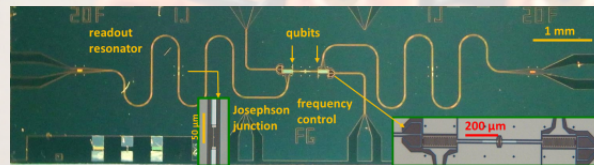


# Running quantum algorithms on elementary processors

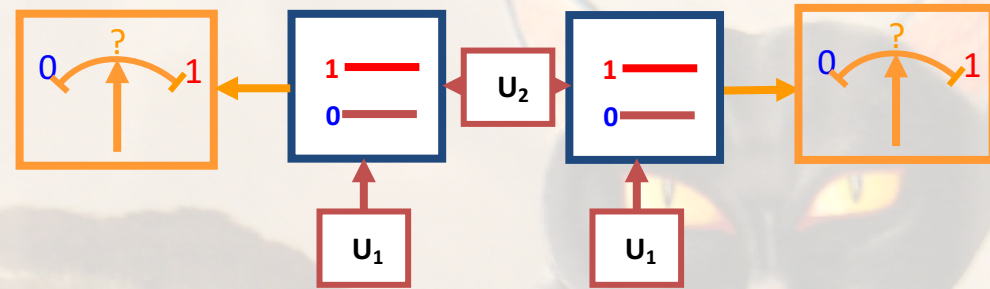
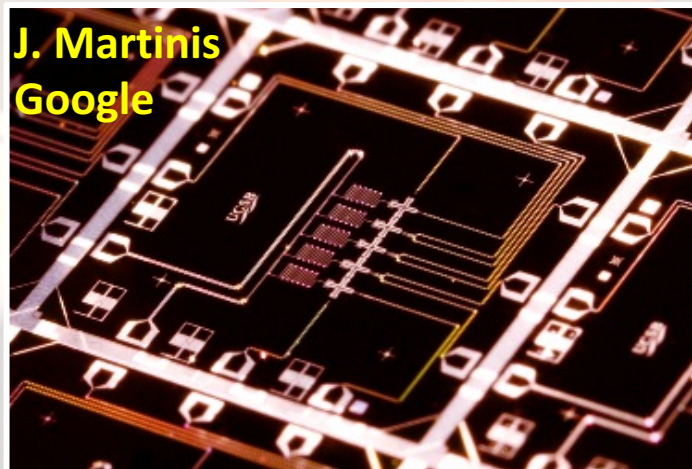
Martinis Lab, UC Santa Barbara  
Yamamoto et.al. ,  
PRB 82 2010 , Nat Phys 2012



Quntronics, CEA  
Dewes et. al., PRL & PRB 2012



Martinis lab, Google 2015...  
IBM, TUD



*Shor factorization  
algorithm*

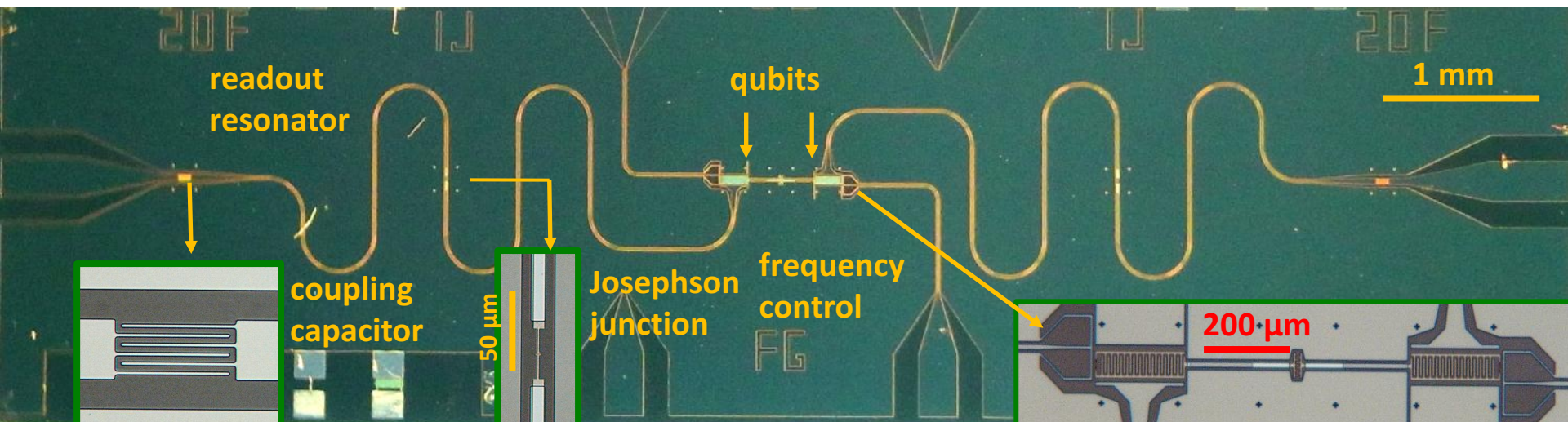
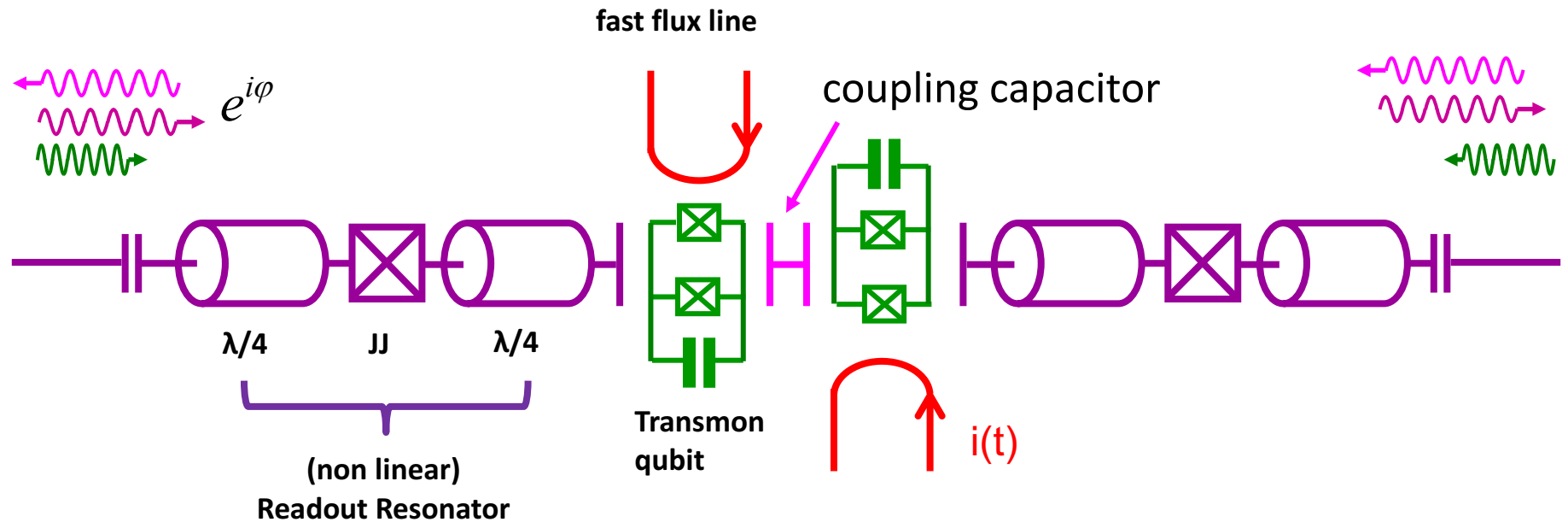
*Grover search  
algorithm*

*correcting  
some errors*



# The simplest case: a two-transmon processor

Dewes et al., Phys. Rev. Lett. 108, 057002 (2012)



# Capacitive coupling yields iSWAP Gate

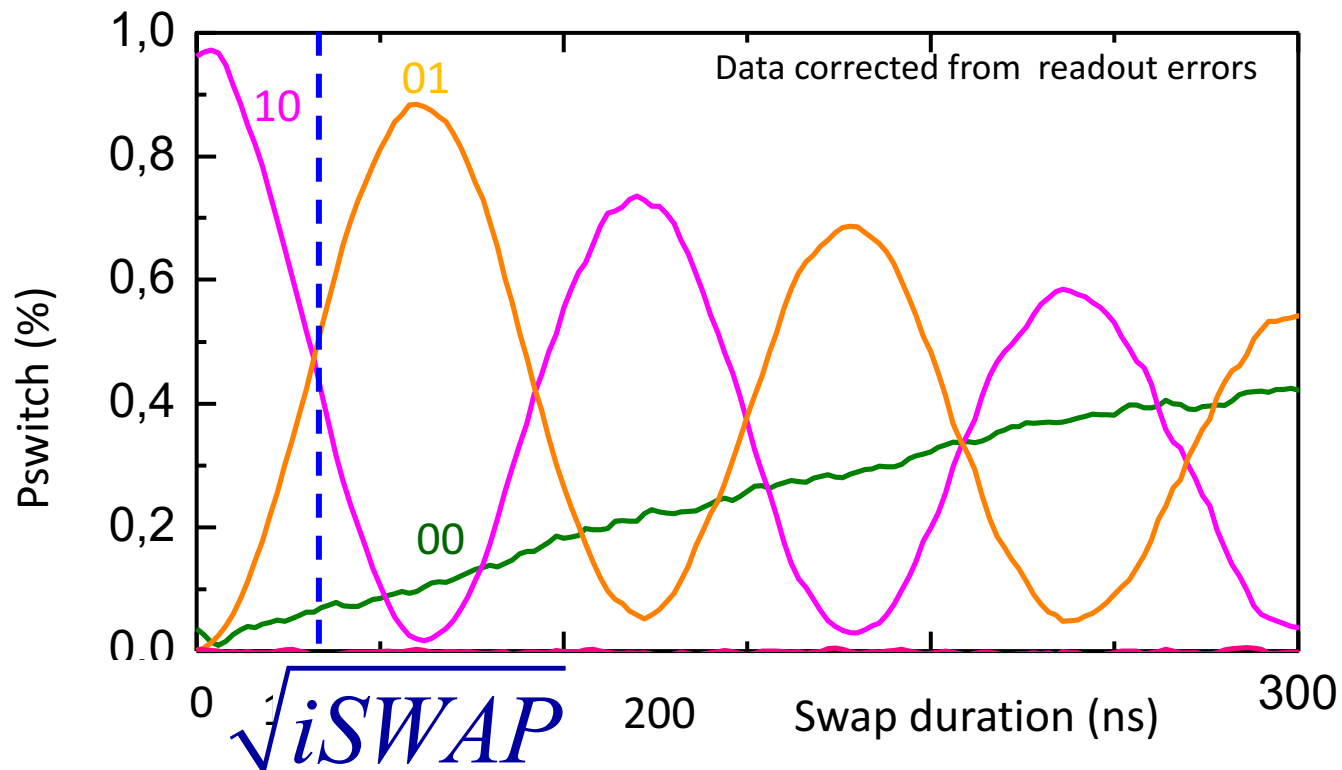
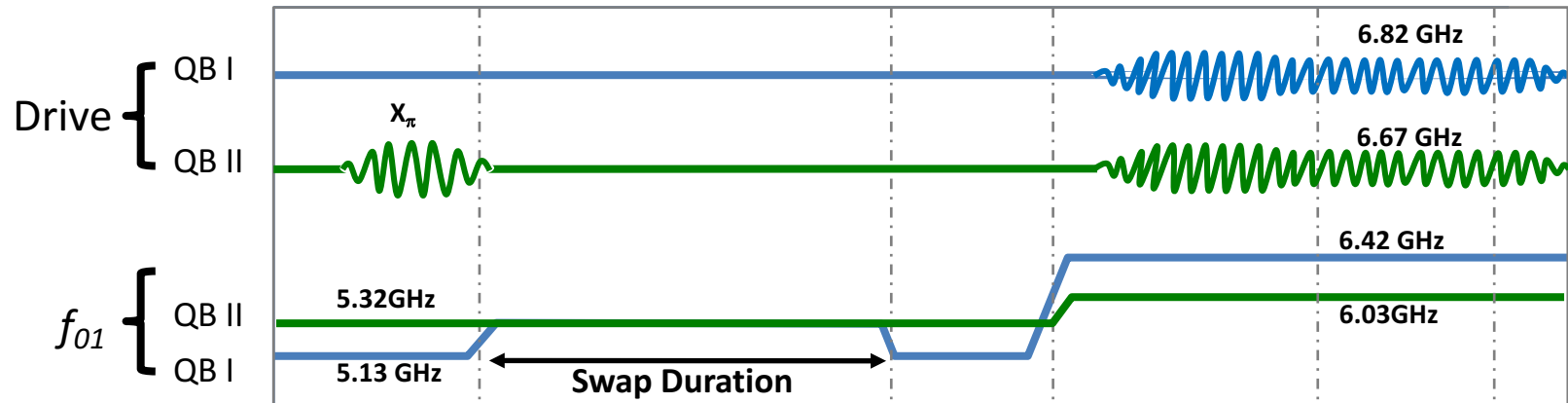
$$H / \hbar = -\frac{\omega_{01}^I}{2} \sigma_z^I - \frac{\omega_{01}^{II}}{2} \sigma_z^{II} + \overbrace{g \left( \sigma_+^I \sigma_-^{II} + \sigma_-^I \sigma_+^{II} \right)}^{H_{\text{int}}}$$

➡ « Natural » universal gate :  $\sqrt{i\text{SWAP}}$

On resonance,  $(\omega_{01}^I = \omega_{01}^{II})$

$$U_{\text{int}}(t) = \begin{array}{cc} \text{00} & \text{10} & \text{01} & \text{11} \\ \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & \cos(gt) & -i \sin(gt) & 0 \\ 0 & -i \sin(gt) & \cos(gt) & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix} \end{array} U_{\text{int}}\left(\frac{\pi}{2g}\right) = \begin{array}{c} \boxed{\begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 1/\sqrt{2} & -i/\sqrt{2} & 0 \\ 0 & -i/\sqrt{2} & 1/\sqrt{2} & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}} = \sqrt{i\text{SWAP}} \end{array}$$

# SWAP between two transmon qubits



# The Grover search algorithm on 4 objects

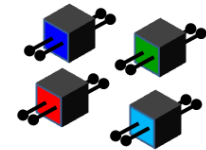
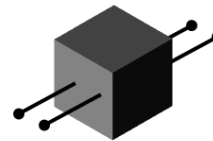
*the search problem*



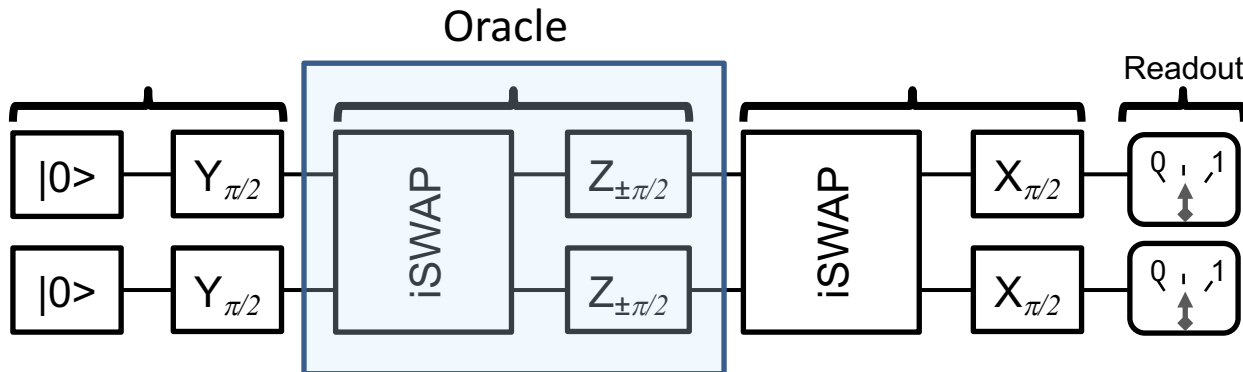
Classical search:  $O(N)$  steps    Quantum search :  $O(\sqrt{N})$  steps

4 object benchmark case: **1 try enough !**

Oracle  
marking  
a state

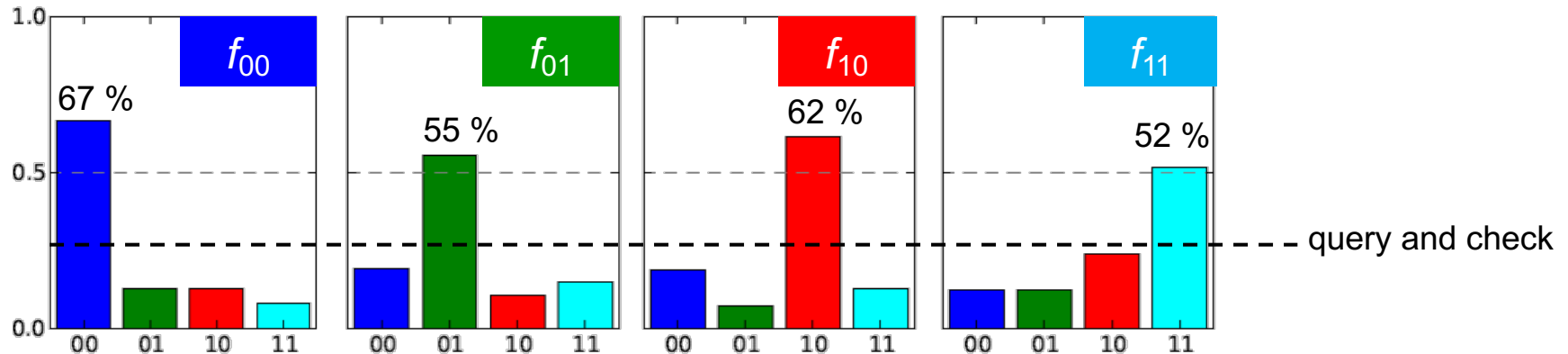
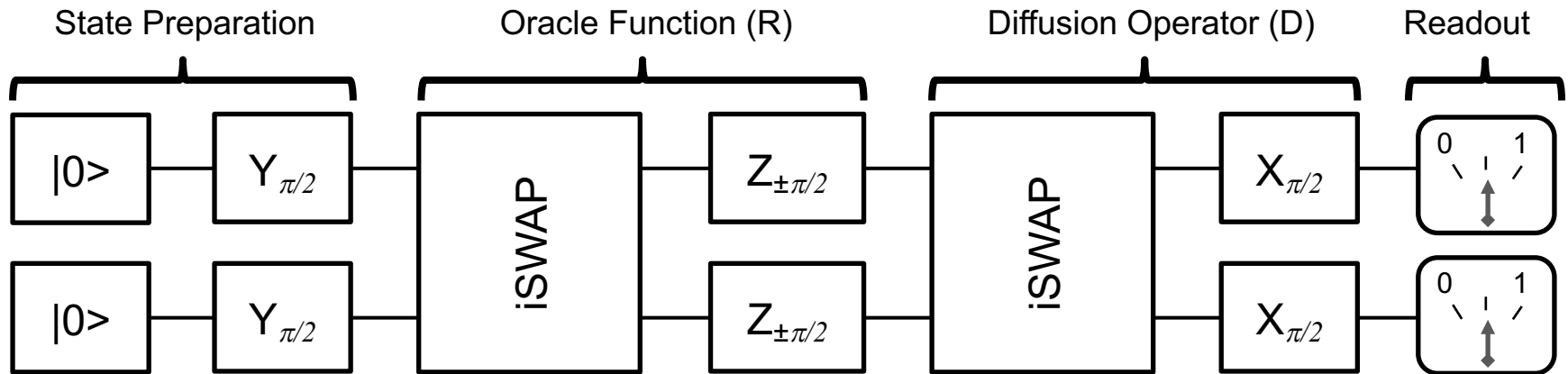


$$i \in \{00 \quad 01 \quad 10 \quad 11\}$$





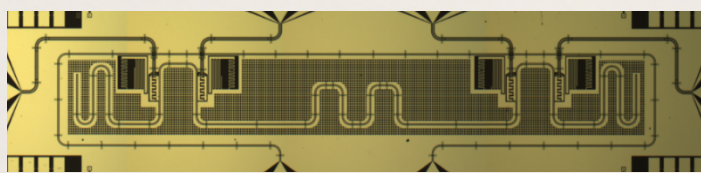
# The Grover search algorithm: success probability



$F_i > 25 \% \rightarrow$  Quantum speed-up

# Scaling up ?

4 qubit processor (2014) :



multiplexed readout  
2 qubit gates through common bus

**& did not work well**

**Scalability challenge ahead**

**Challenge:**  
interesting tasks need 100 perfect qubits (at least) !

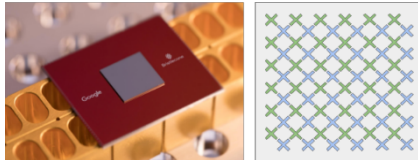
# A quantum computing perspective: the scalability challenge *from toys to devices (?)*

## ELECTRICAL GATE BASED PROCESSORS

### Larger superconducting processors

### The Noisy Intermediate-Scale Quantum (NISQ) technology era

Google, IBM, Rigetti



Google 's sicamore

No quantum advantage yet ,  
But quantum « supremacy »

Processors ?  
~50 qubits,  
benchmarking

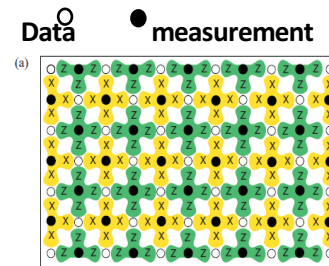
### Addressing Quantum Error Correction

### fault-tolerant architectures

reminder:  
copying forbidden!

### surface code fabric

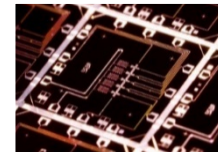
(see Fowler et al, PRA 86 (2012))



Pb: huge resource overhead

1 logical qubit >> 1000 physical qubits

Google, IBM, TUD, ... test circuits  
for quantum error correction



Preliminary results since 2015

# Quantum Supremacy

## QUANTUM COMPUTING AND THE ENTANGLEMENT FRONTIER

JOHN PRESKILL

We therefore hope to hasten the onset of the era of *quantum supremacy*, when we will be able to perform tasks with controlled quantum systems going beyond what can be achieved with ordinary digital computers. To realize that dream, we must overcome the formidable enemy of *decoherence*, which makes typical large quantum systems behave classically. So another question looms over the subject:

*Is controlling large-scale quantum systems merely **really, really hard**, or is it **ridiculously hard**?*





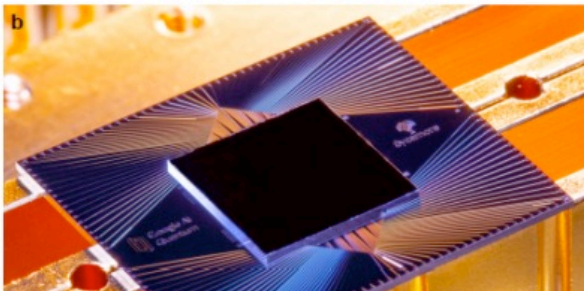
# Google's achievement towards NISQ machines

53 Qubit Sycamore processor  
operated at sub 1% error /gate

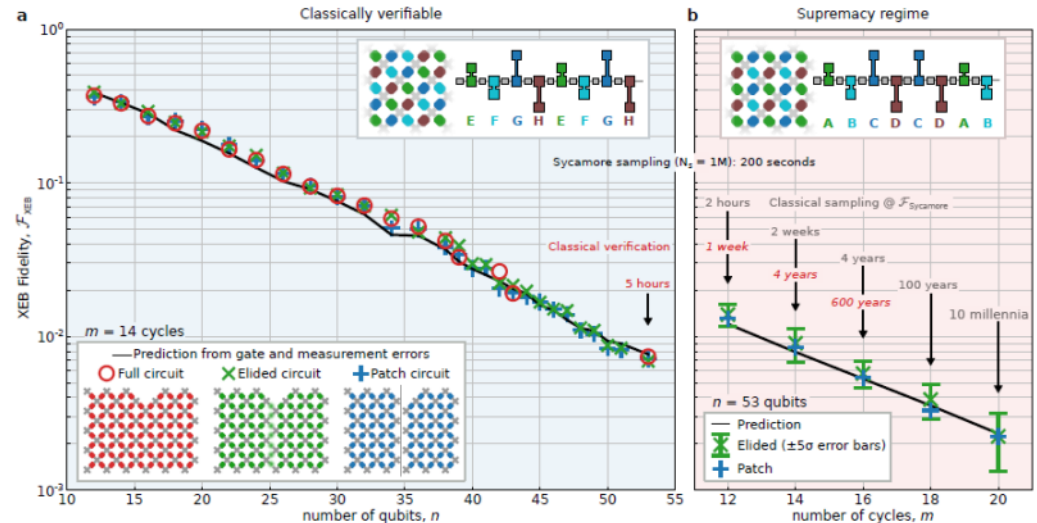
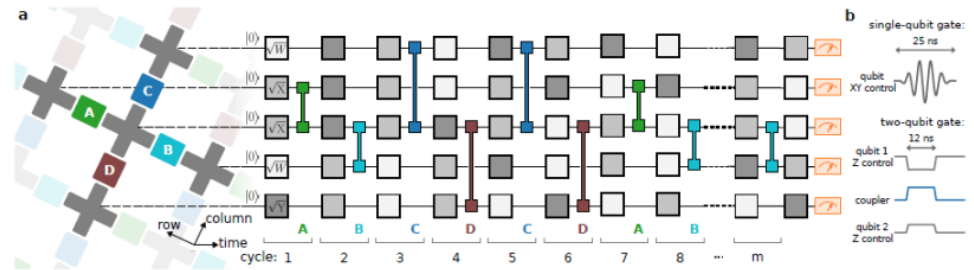
Al. and J. Martinis,  
Nature 574, 461, 2019

Pauli and measurement errors

	Average error	Isolated	Simultaneous
Single-qubit ( $e_1$ )		0.15%	0.16%
Two-qubit ( $e_2$ )		0.36%	0.62%
Two-qubit, cycle ( $e_{2c}$ )		0.65%	0.93%
Readout ( $e_r$ )		3.1%	3.8%



Application of ~random complex gate sequences  
for fidelity tests  
(hard task for classical computers)

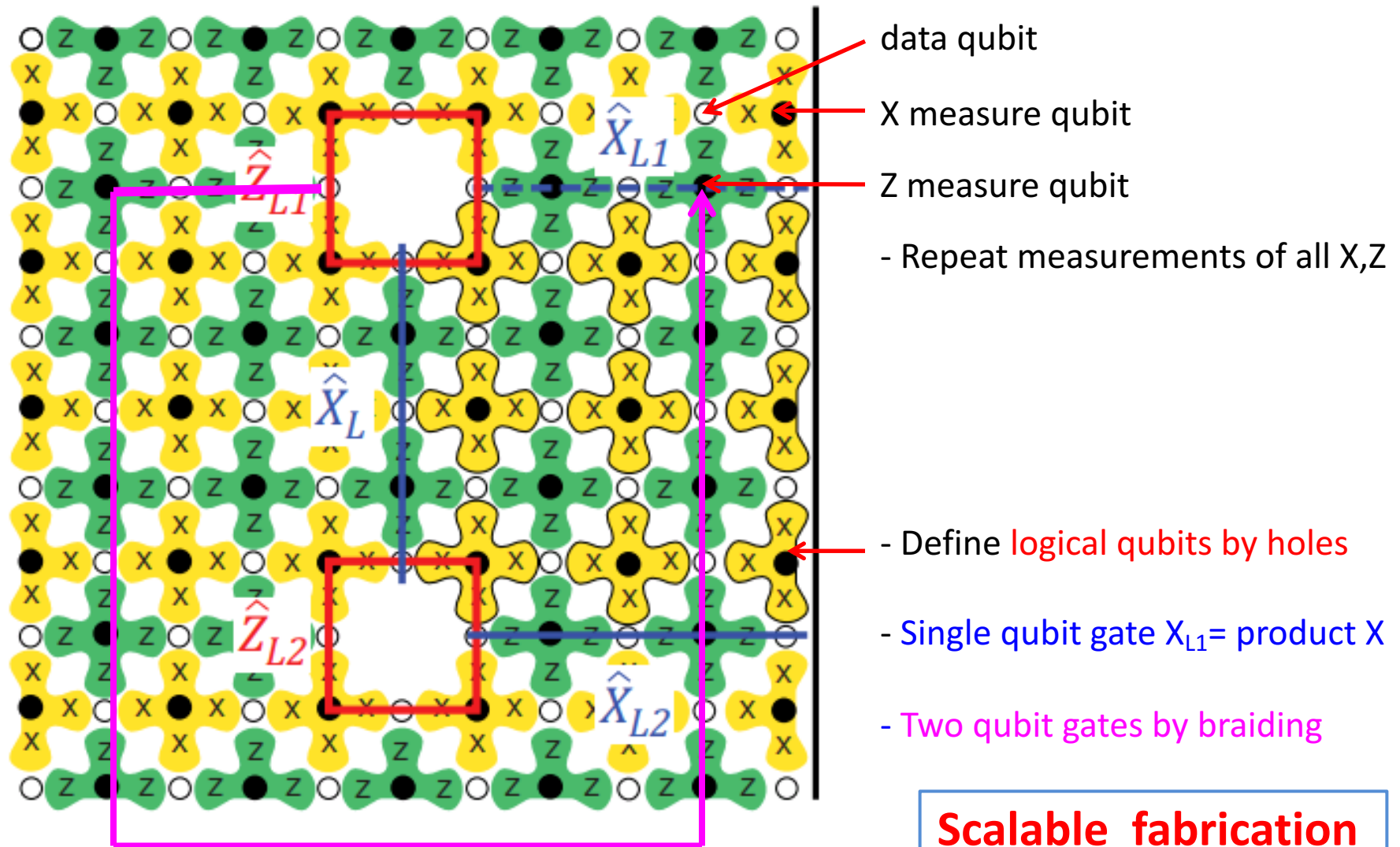


$F \sim (0.995..)^{N(\#gates/step, \#depth)} \rightarrow 0$  too quickly for being useful

Quantum advantage still far away ?

More nines and more scalable fab. needed!

# The surface (stabilizer) code architecture (just a flavor)



But ... huge overhead: >3600 qubit/logical qubit  
@ 0.1% error/gate !

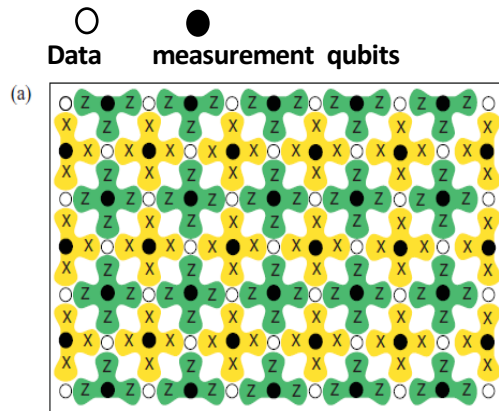
**Scalable fabrication  
mandatory!**

# Strategies for addressing the scalability challenge

fault-tolerant architectures

## surface code fabric

(see Fowler et al, PRA 86 (2012))



**huge overhead:**  
>3600 qubit/logical qubit  
@ 0.1% error/gate !

Better qubits requesting easier quantum error correction

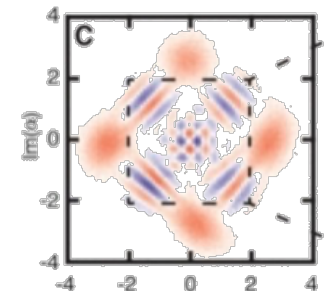
## Dissipation engineering

Yale Quantlab,  
INRIA- ENS Paris, ENS Lyon

Schrödinger cat states in  
high Q resonators

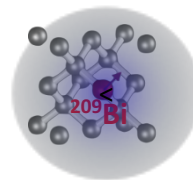
### Autonomous qubits

Mirrahimi et al.  
NJP 16, 32014 (2014)

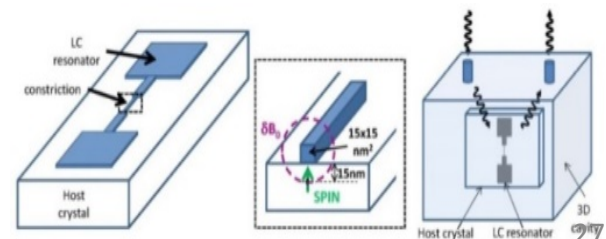


## Hybrid structures

spins and quantum circuits, and others



quantum coherence, control issue

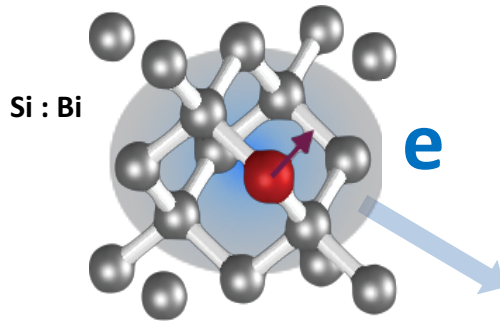


# A new hybrid route : spins coupled to superconducting circuits

Nuclear spins

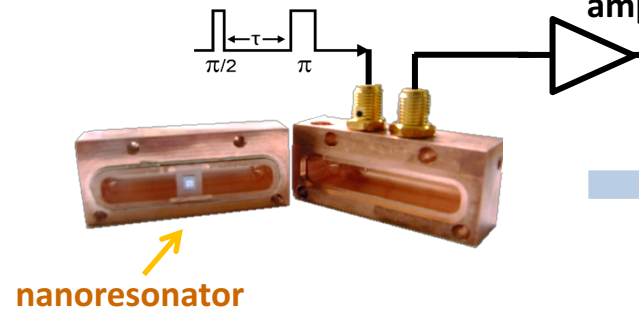
Electronic spins

hyperfine coupling



low mode volume high Q  
resonators

Quantum  
limited  
amplifier



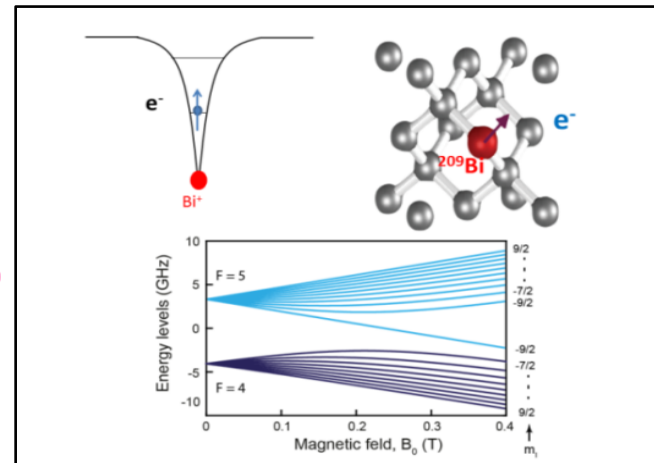
hybrid  
architecture ?

Highly coherent  
quantum system

- Electronic spin = 1/2
- Nuclear spin  $I=9/2$
- Large hyperfine coupling  $\frac{A}{2\pi} = 1.4754\text{GHz}$

$$\frac{H}{\hbar} = \mathbf{AI} \cdot \mathbf{S} + \mathbf{B}_0 \cdot (-\gamma_e \mathbf{S} - \gamma_n \mathbf{I})$$

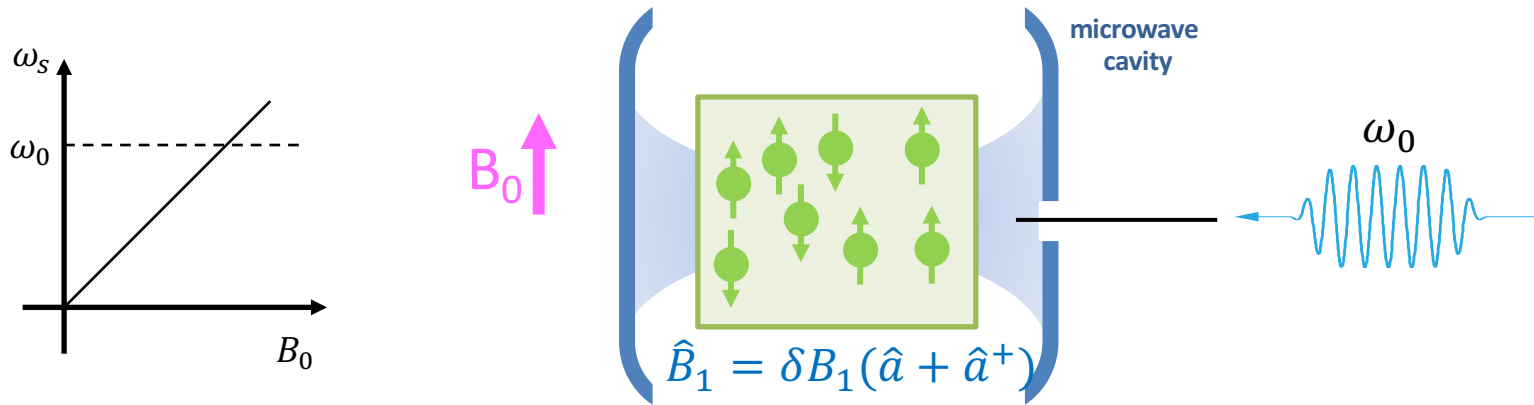
20 electro-nuclear states  
for making qubits



Preliminary  
ESR work



# Magnetic resonance in a quantum microwave field

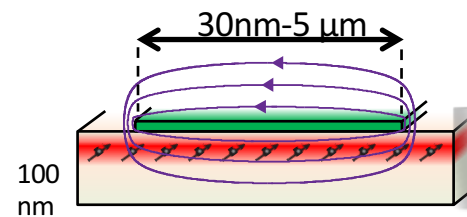
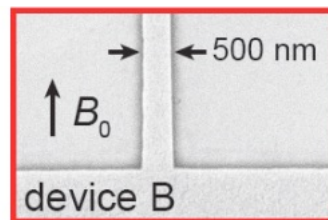
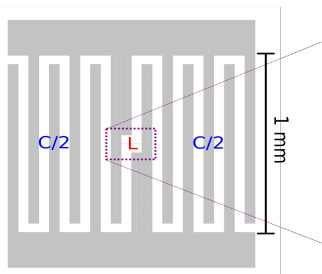


$$\hat{H} = -\sum \hat{M}_j \cdot \hat{B}_1 = \sum g_j (\hat{\sigma}_j^+ \hat{a} + \hat{\sigma}_j^- \hat{a}^+)$$

$$g_j = -\gamma \delta B_1(r_j) \langle \downarrow | S_{x,j} | \uparrow \rangle$$

coupling :  
**1 photon magnetic field  
 at spin position**

Small mode volume high Q resonators



spins close to  
 nanowire inductor

$$L = 0.1 \text{ mm}$$

$$w = 0.5 \mu\text{m}$$

$$V \approx 200 fL$$

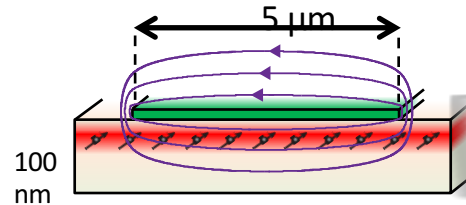
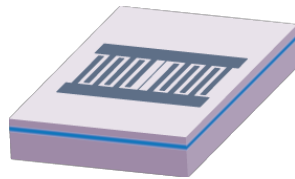
$$\frac{g}{2\pi} \approx 450 \text{ Hz}$$

# Superconducting micro-resonator geometries

$$L=1\text{mm}$$

$$w=5\mu\text{m}$$

$$V \approx 20pL$$

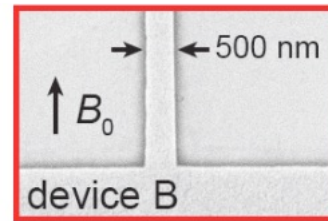
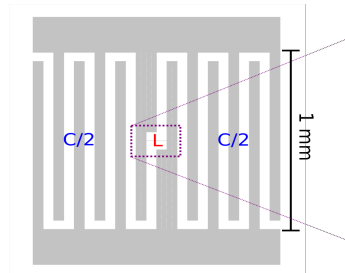


$$\frac{g}{2\pi} \approx 60\text{Hz}$$

$$L=0.1\text{mm}$$

$$w=0.5\mu\text{m}$$

$$V \approx 200fL$$

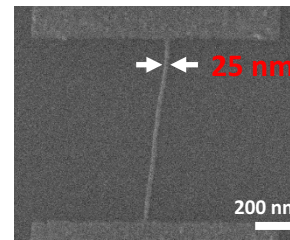
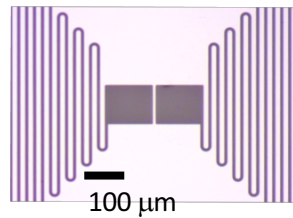


$$\frac{g}{2\pi} \approx 450\text{Hz}$$

$$L=2\mu\text{m}$$

$$w \approx 25\text{ nm}$$

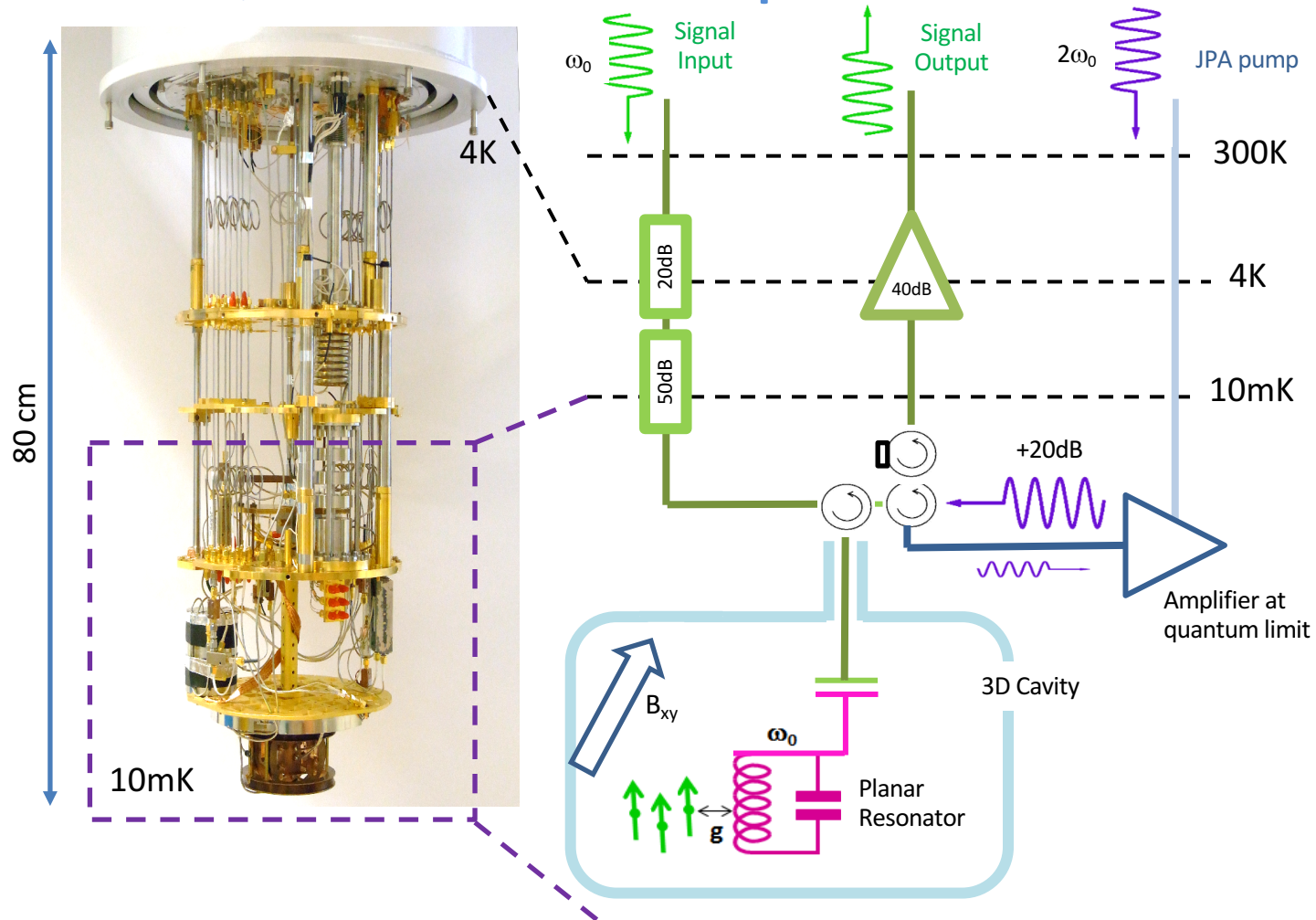
$$V \approx 0.1 fL$$



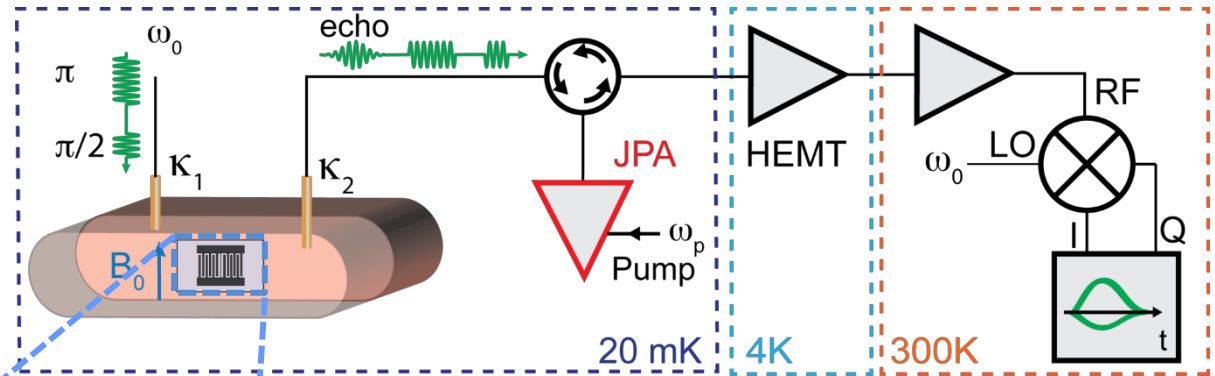
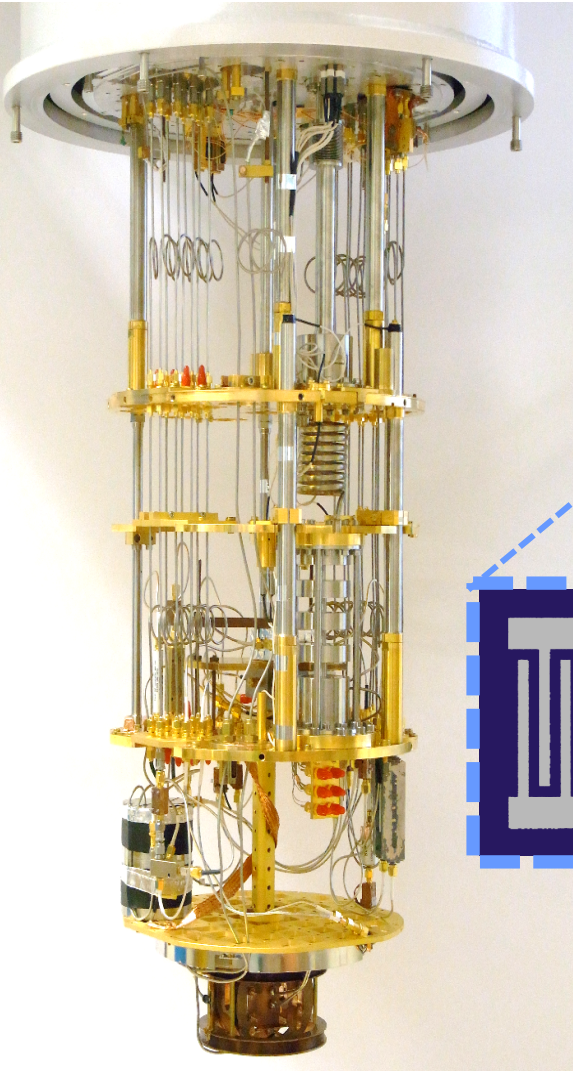
$$\frac{g}{2\pi} \approx 2 - 8\text{ kHz}$$

**not yet probed**

# Quantum limited ESR spectrometer



# Quantum limited ESR with Parametric Amplifier



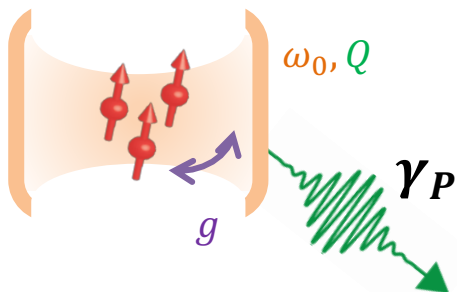
**JPA: Josephson Parametric Amplifier**  
reaching the quantum limit



# High Q low mode volume bonus: the Purcell effect



1946  
E. Purcell



$$\gamma_P = \frac{4Qg^2}{\omega_0} \frac{1}{1 + 4Q^2 \left[ \frac{\omega_s - \omega_0}{\omega_0} \right]^2}$$

Bi spins & resonator

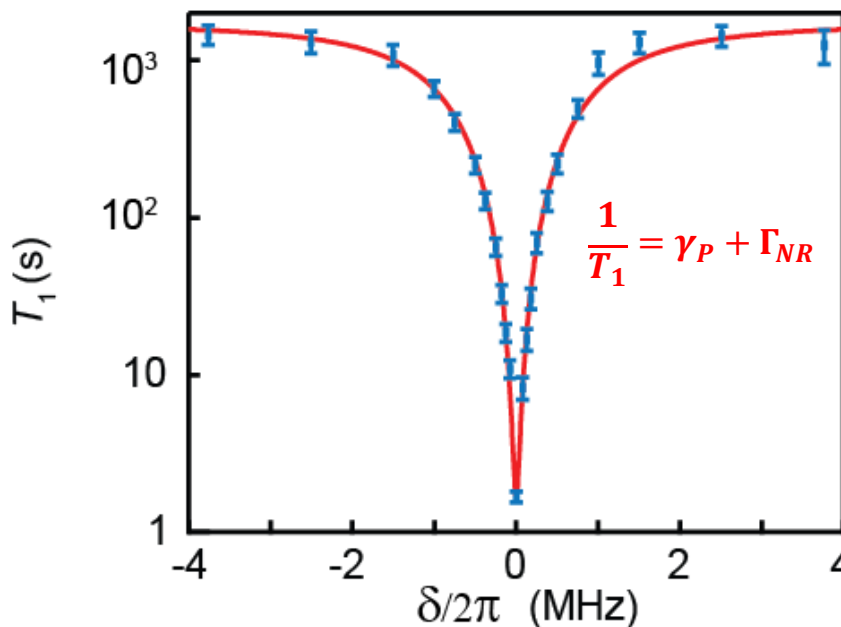
L=1mm

w=5μm

V ≈ 20pL

fit yields:

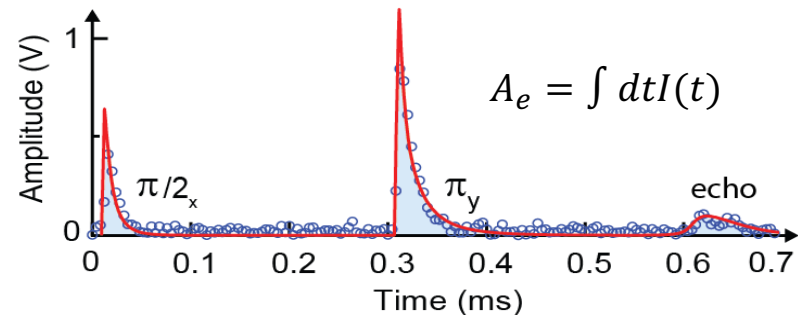
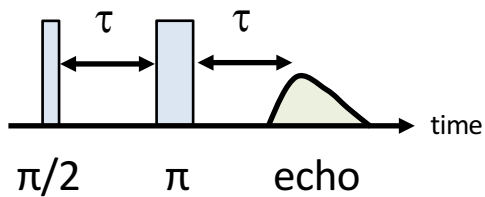
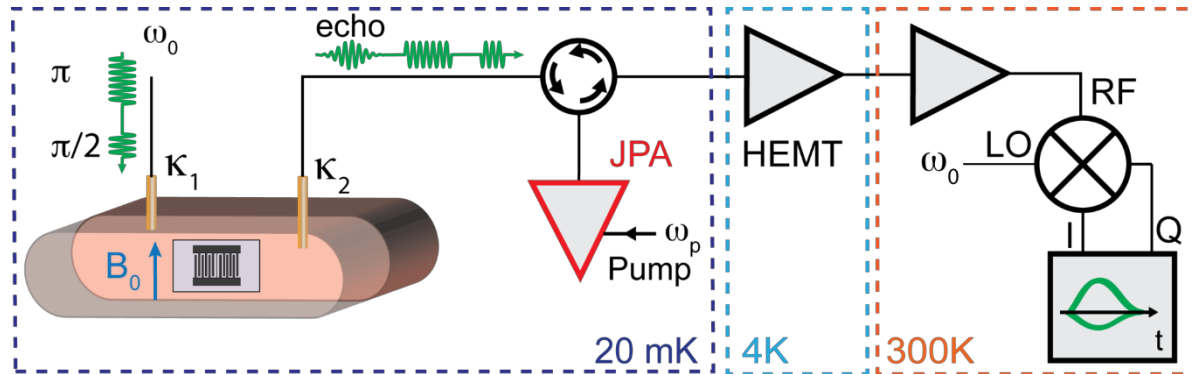
$$\frac{g}{2\pi} = 60 \pm 10 \text{ Hz}$$



A. Bienfait et al.,  
Nature 531, 74 (2016)

Purcell relaxation allows to increase the repetition rate

# Quantum limited ESR with Parametric Amplifier

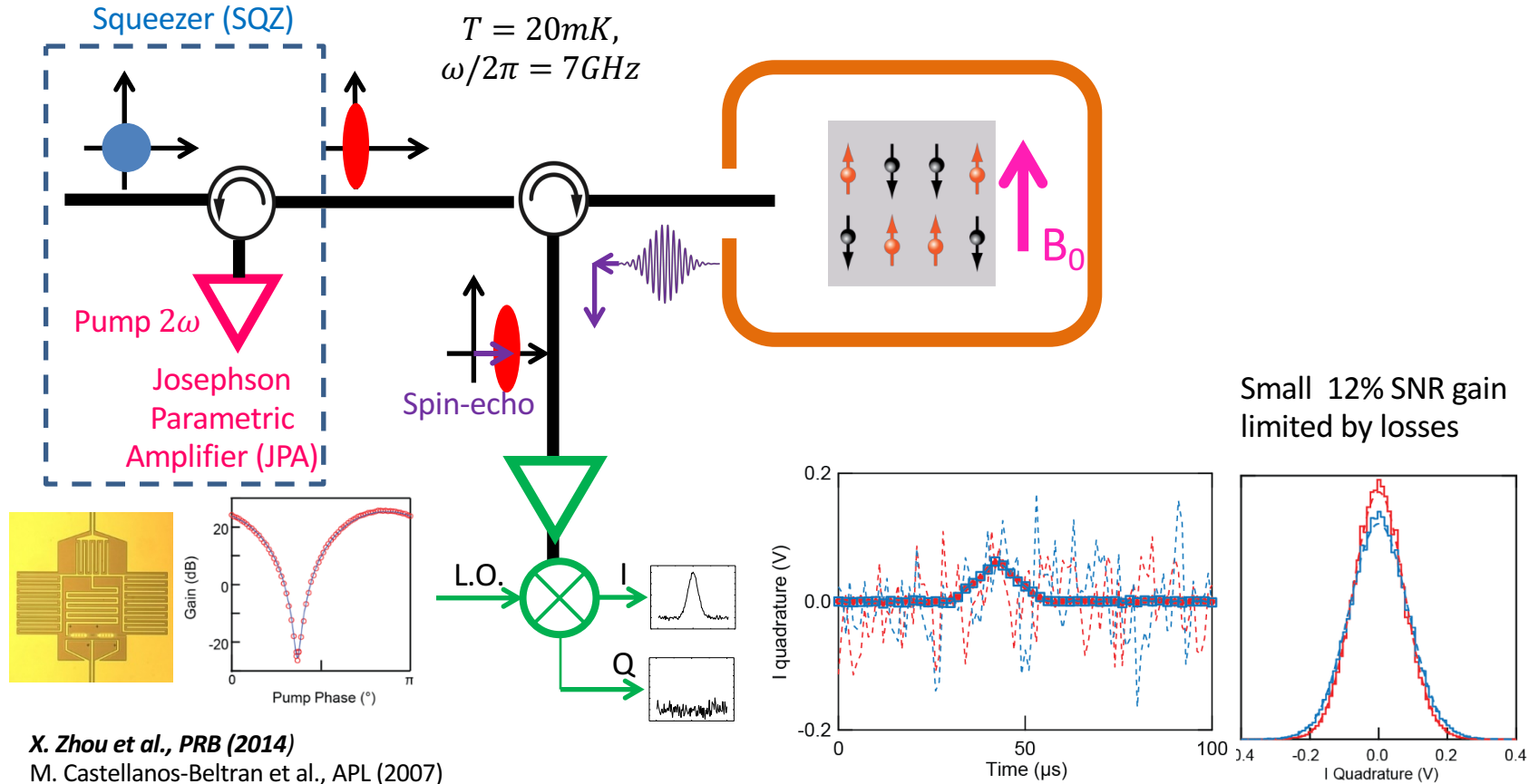


S. Probst et al., Appl. Phys. Lett. (2017)

$L=0.1\text{mm}$   
 $w=0.5\mu\text{m}$   
 $V \simeq 200fL$

**best achieved ESR detection sensitivity:**  
**single echo : ~100 spins**  
**@  $T_1 = 21\text{ ms}$  :  $10\text{ spins}/\sqrt{\text{Hz}}$**

# Squeezing-enhanced magnetic resonance : principle



**X. Zhou et al., PRB (2014)**

M. Castellanos-Beltran et al., APL (2007)

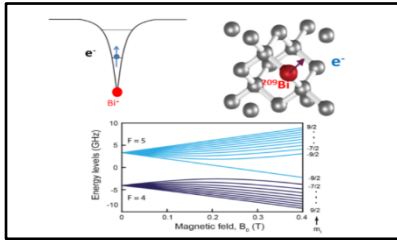
C. Eichler et al., PRL (2010)

N. Bergeal et al., Nature (2010)

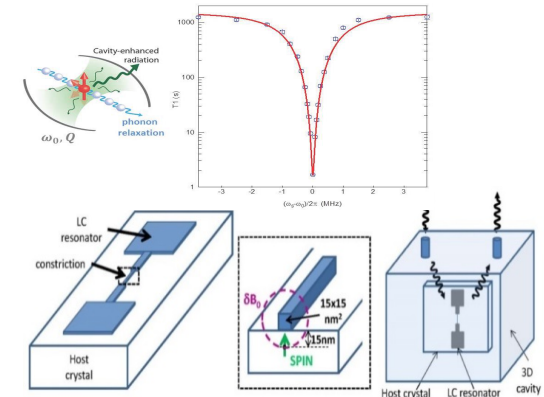
# An hybrid route toward quantum information ?

## Electro-nuclear spin system

with good quantum coherence

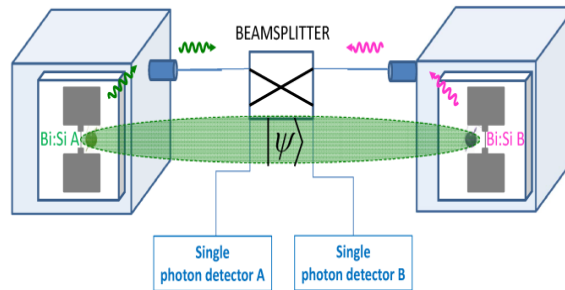


controlled coupling to environment

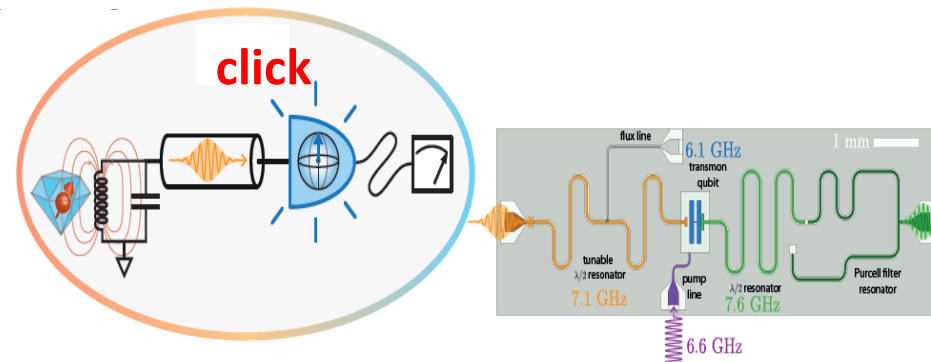
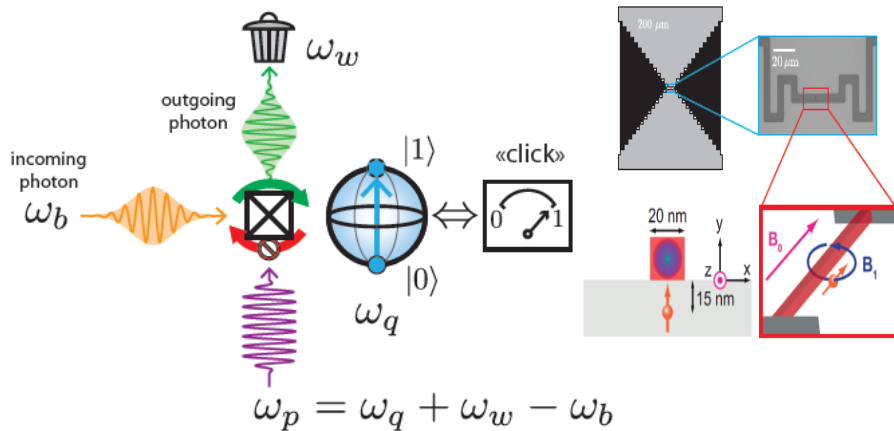


## Quantum information perspective :

generating entanglement ?



key element: new quantum optics photon detector design (E. Flurin, 2017)



Work in progress...

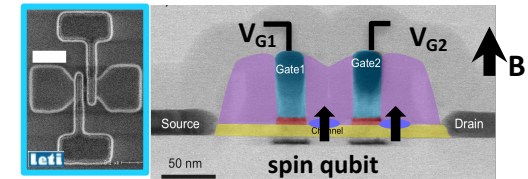
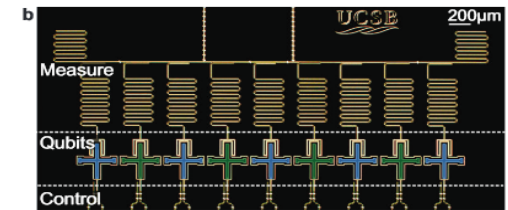
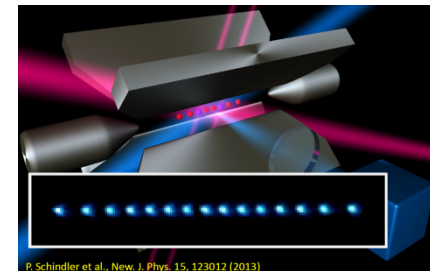
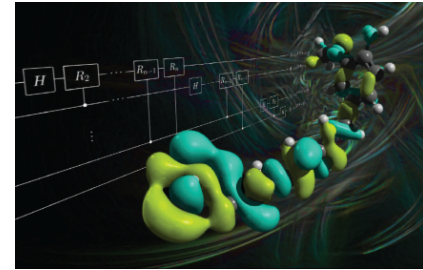


# Conclusions

- Interesting use-cases identified  
**many-body problem**, classification, ....  
but >100 logical (error corrected) qubits needed ...

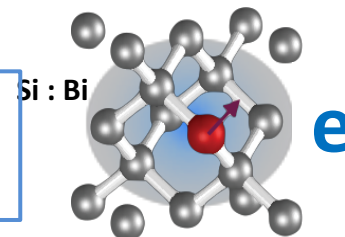


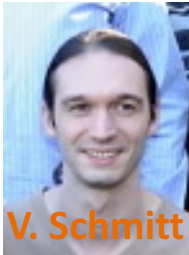
- Low depth processors at Google, IBM, Rigetti  
**targeting quantum advantage**
- Sizeable progress on different platforms
- gate-based processors with quantum error correction  
**very difficult.**  
**Scalable fab. mandatory.**
- Other route **more coherent qubits**  
autonomous correction, Schröd. cat states, spins, ...



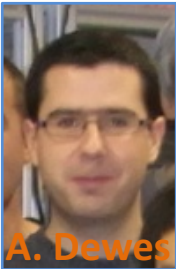
Appealing potential,  
but  
perspectives still unclear

Rich quantum physics  
on the road





& V. Ranjan, M. Rancic, M. Lee, F. Barbosa,  
B. Albanese, E. Albertinale, M. le Dantec  
& former members: A. Dewes, X. Zhou, V. Schmitt, A. Bienfait, S. Probst



European  
Research  
Council