

Probing light dark matter with pulsar observations

Diego Blas

based on DB, D. Lopez-Nacir, S. Sibiryakov | 6 | 2.06789 + | 9 | 10.08544

A. Caputo, L. Sberna, M. Frias, DB, P. Pani, L. Shao, W. Yan | 9 | 02.02695

A. Caputo, DB, J. Zavala | 7 | 09.0399 |

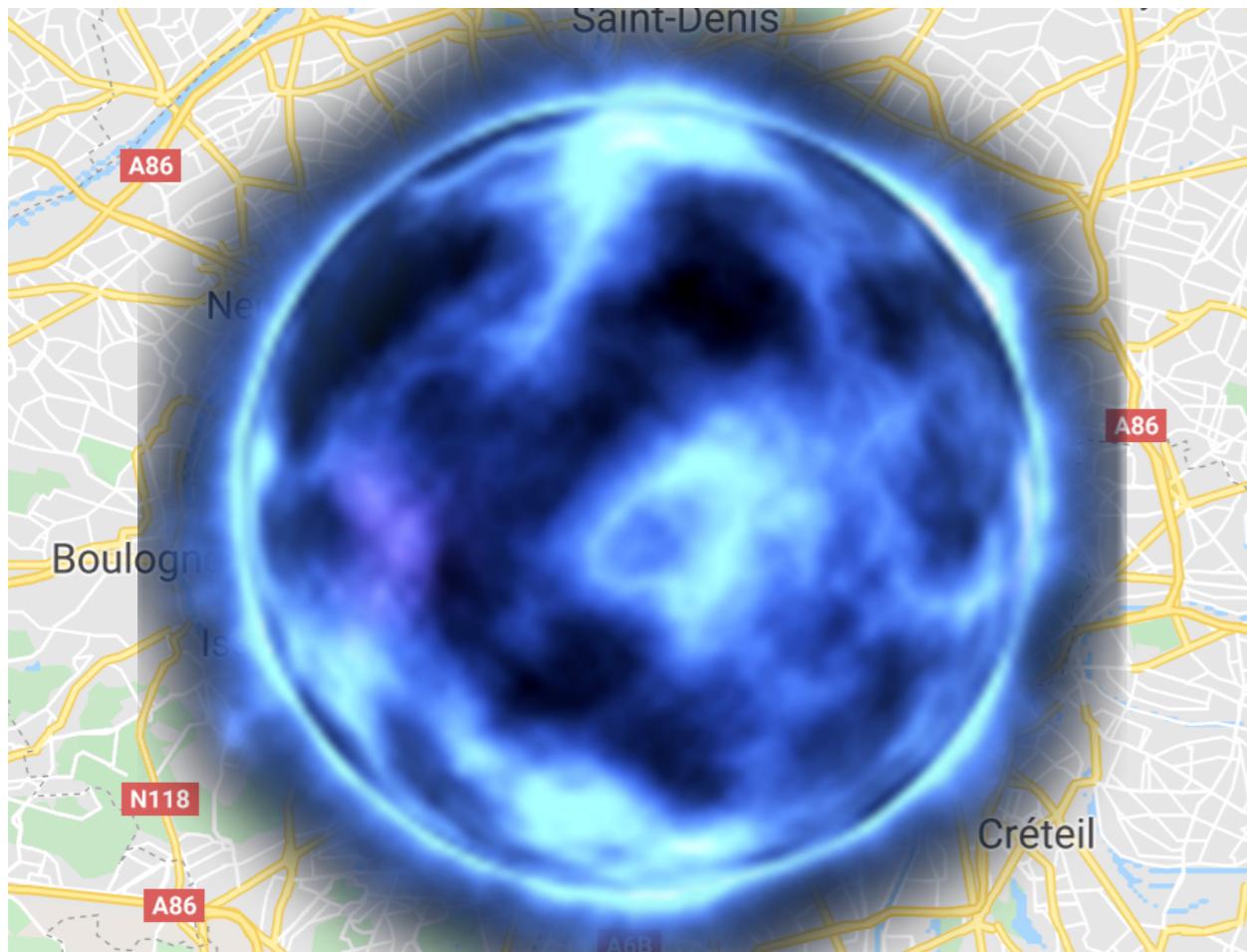
The extreme numbers of pulsars

Pulsars are neutron stars with strong magnetic fields and a significant magnetosphere



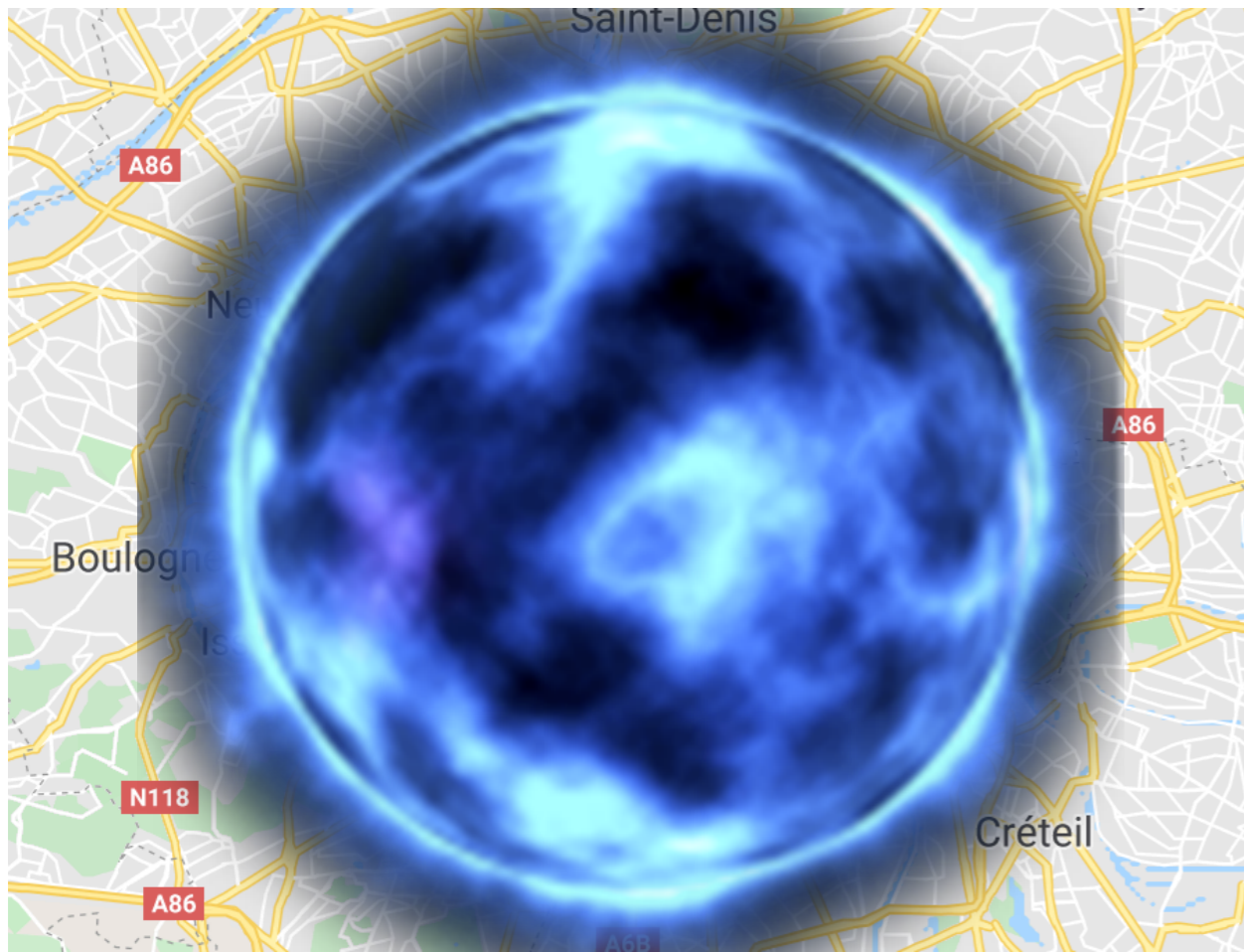
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Some properties

$$r \sim 10 \text{ km}$$

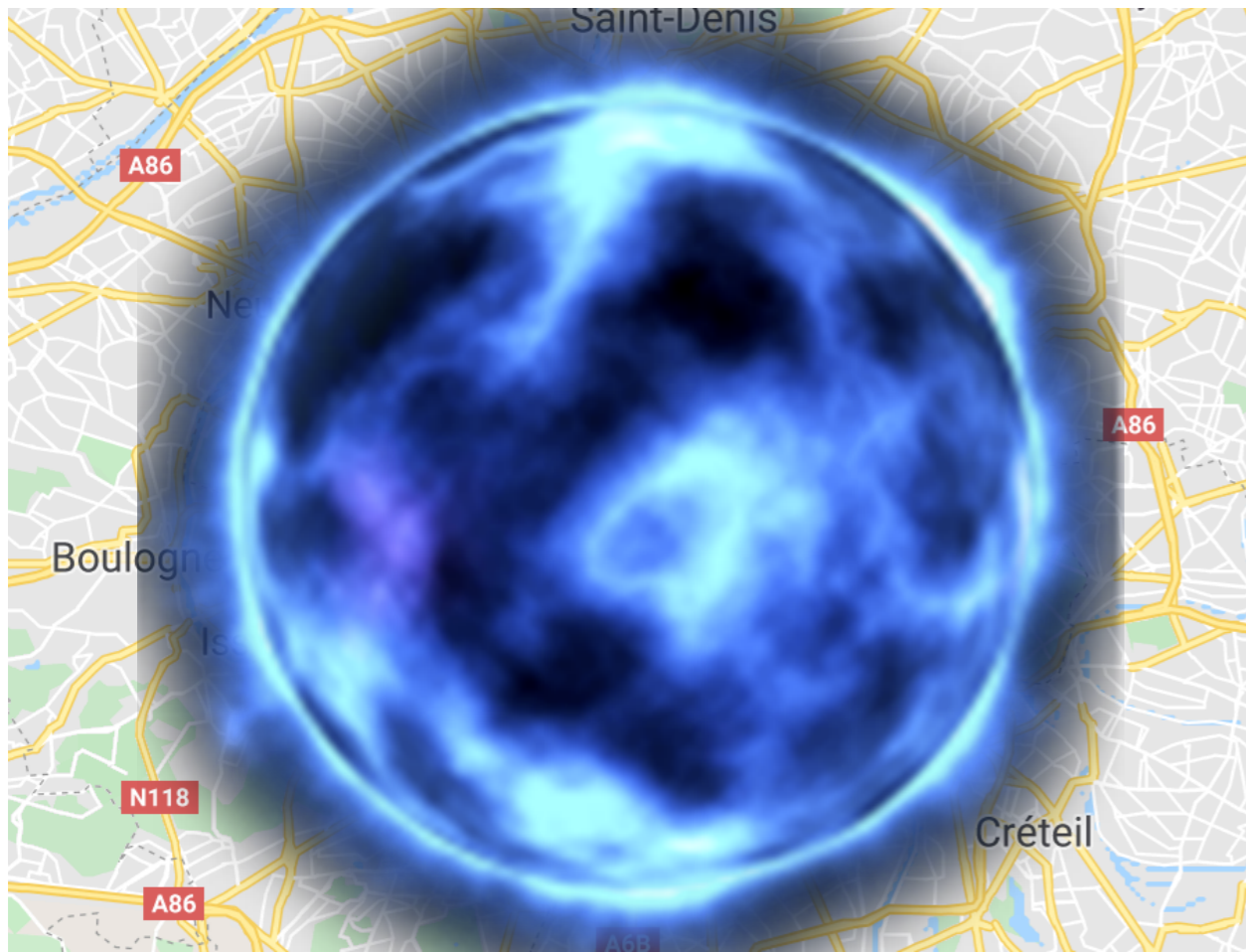
$$\mathcal{M} \sim \# \mathcal{M}_{\odot}$$

$$\rho_c > \text{nuclear} \sim 10^{17} \text{ kg/cm}^3$$

$$B \sim 10^{14} \text{ G}$$

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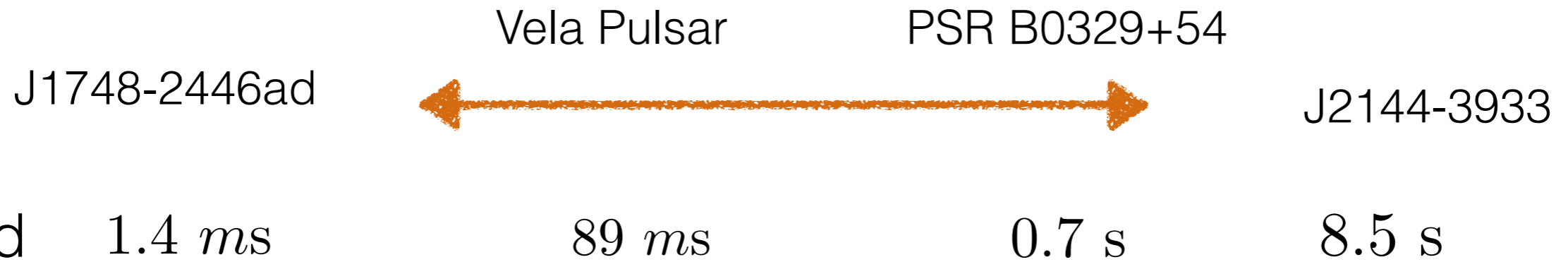
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But there is more...

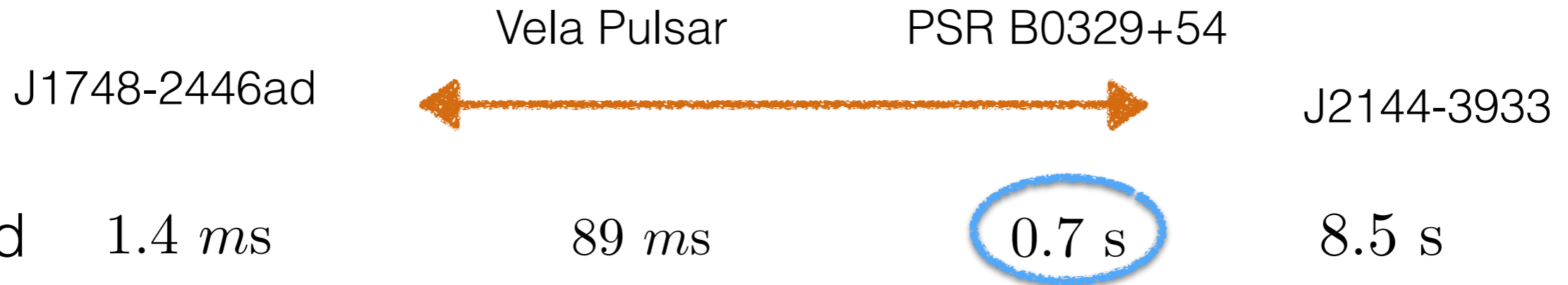
The extreme numbers of pulsars

pulsars can spin very fast!



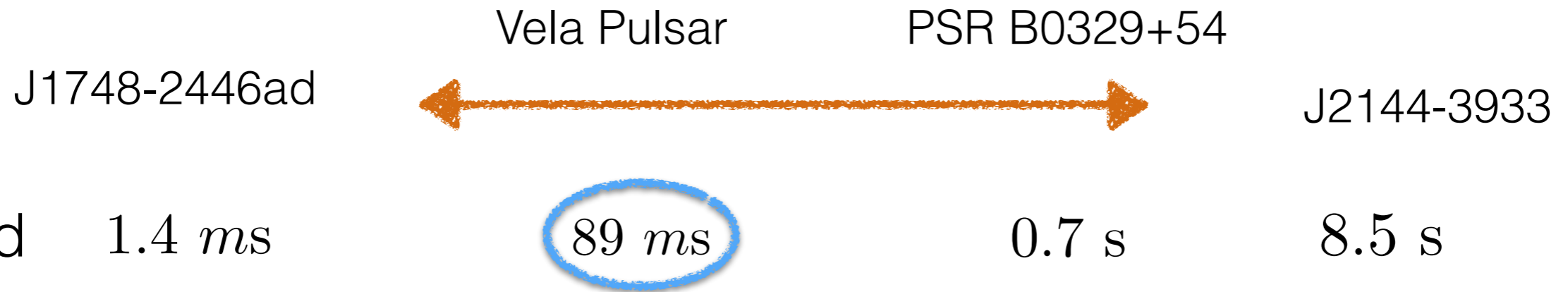
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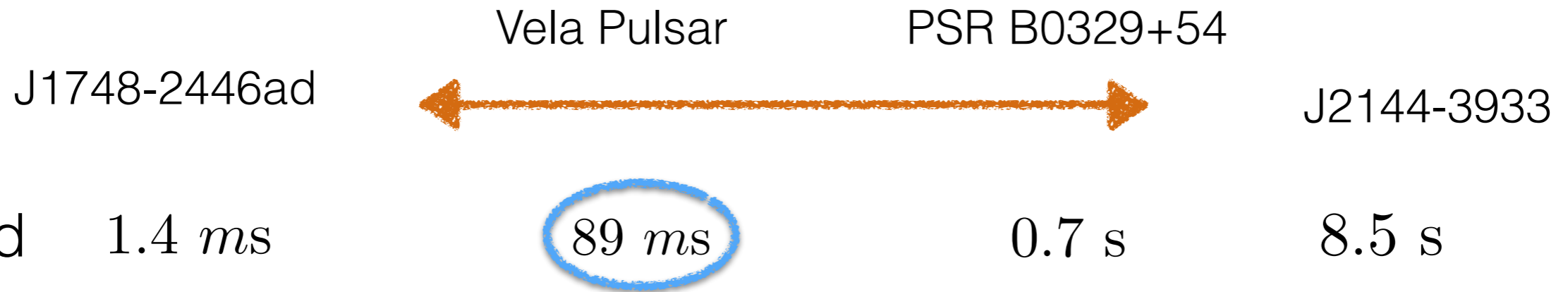
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J1748-2446ad

Vela Pulsar

PSR B0329+54

J2144-3933

Period

1.4 *ms*

89 *ms*

0.7 s

8.5 s



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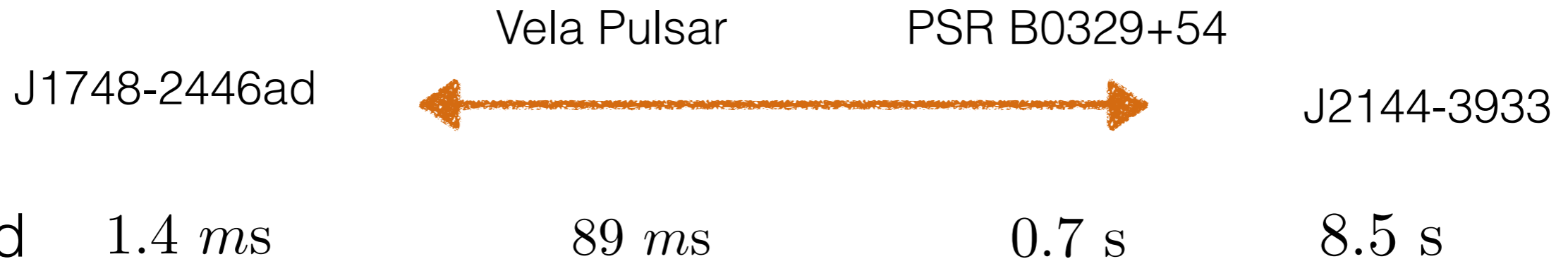
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The extreme numbers of pulsars

pulsars can spin very fast!



speed at equator: $10^{-3} c$

gravity at the equator: $10^{11} g$

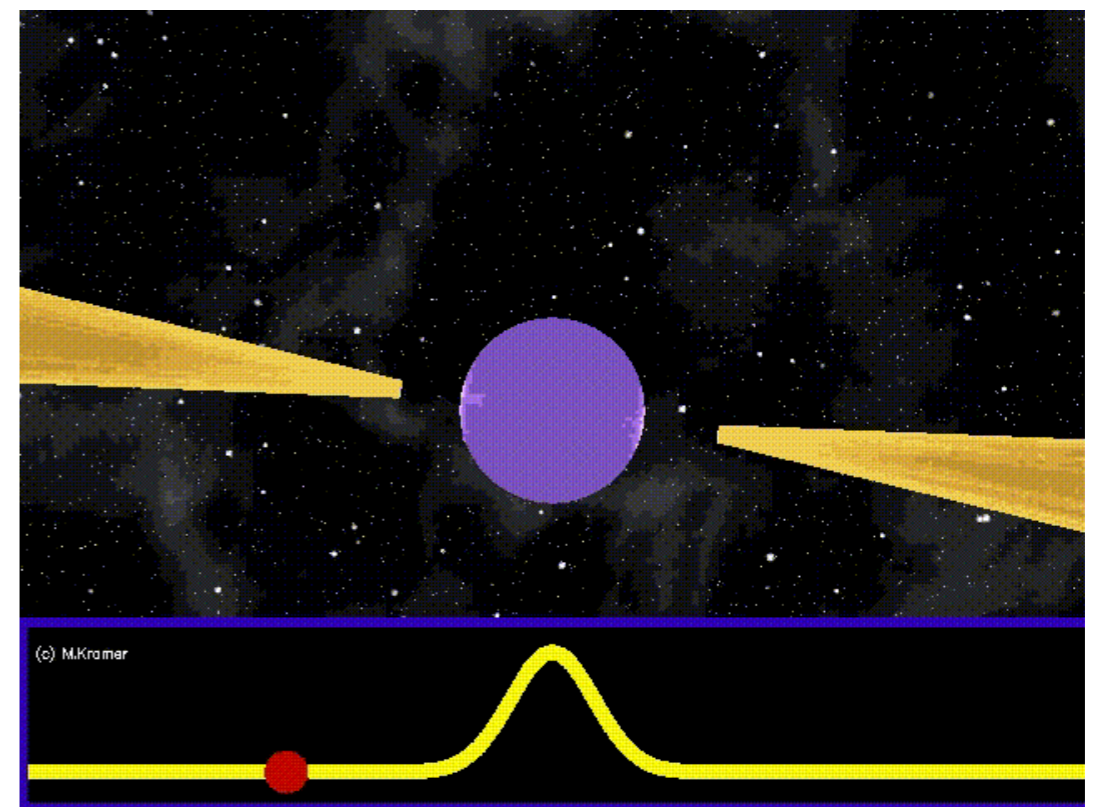
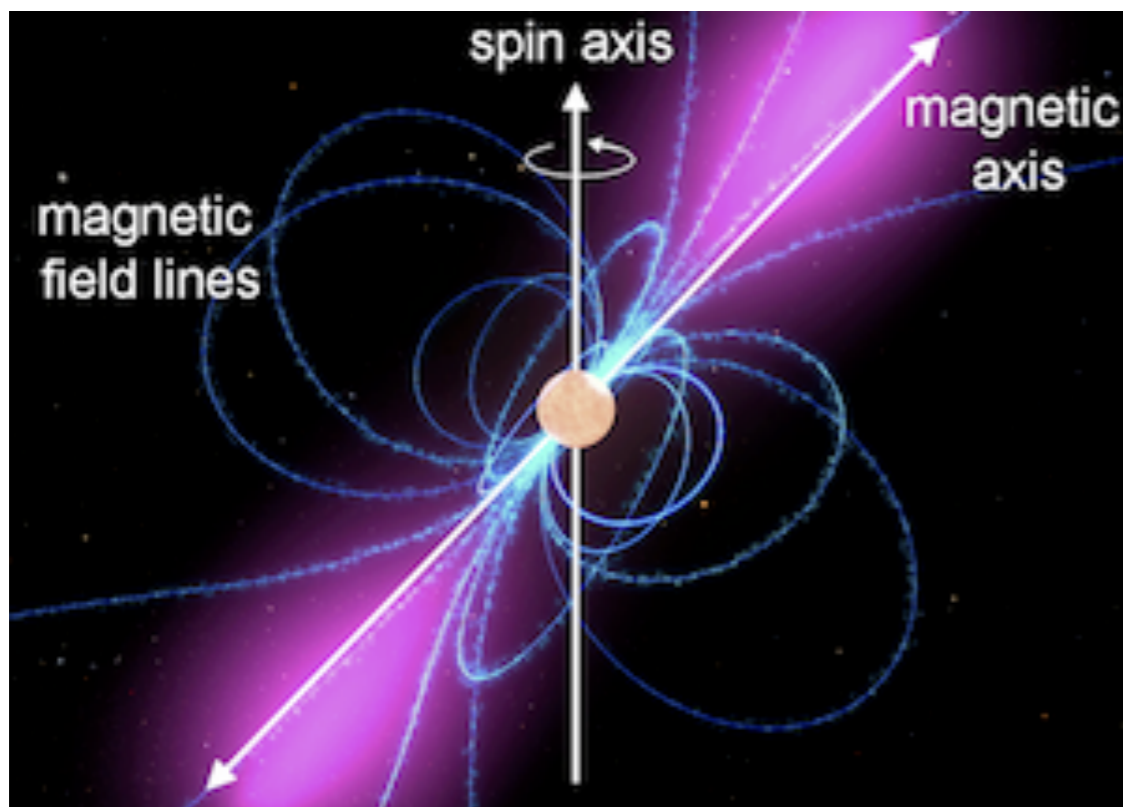
Pulsars are gigantic fly wheels!



Very precise clocks!

Beacons in the sky

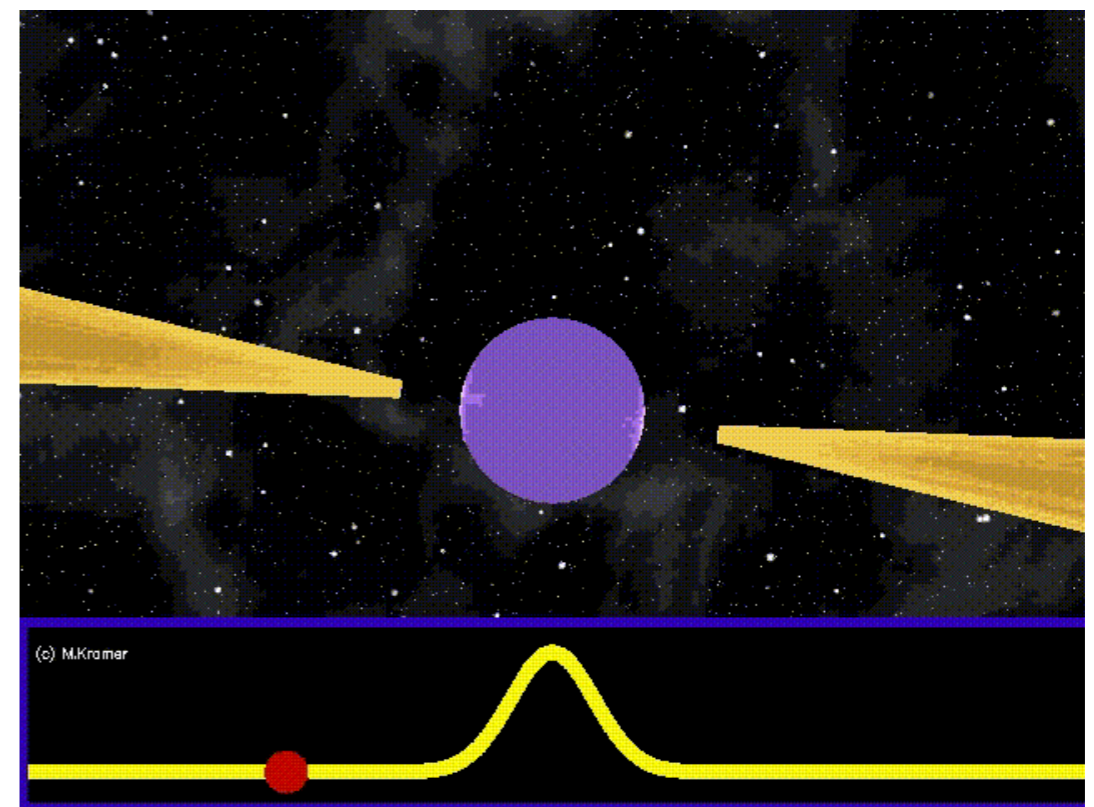
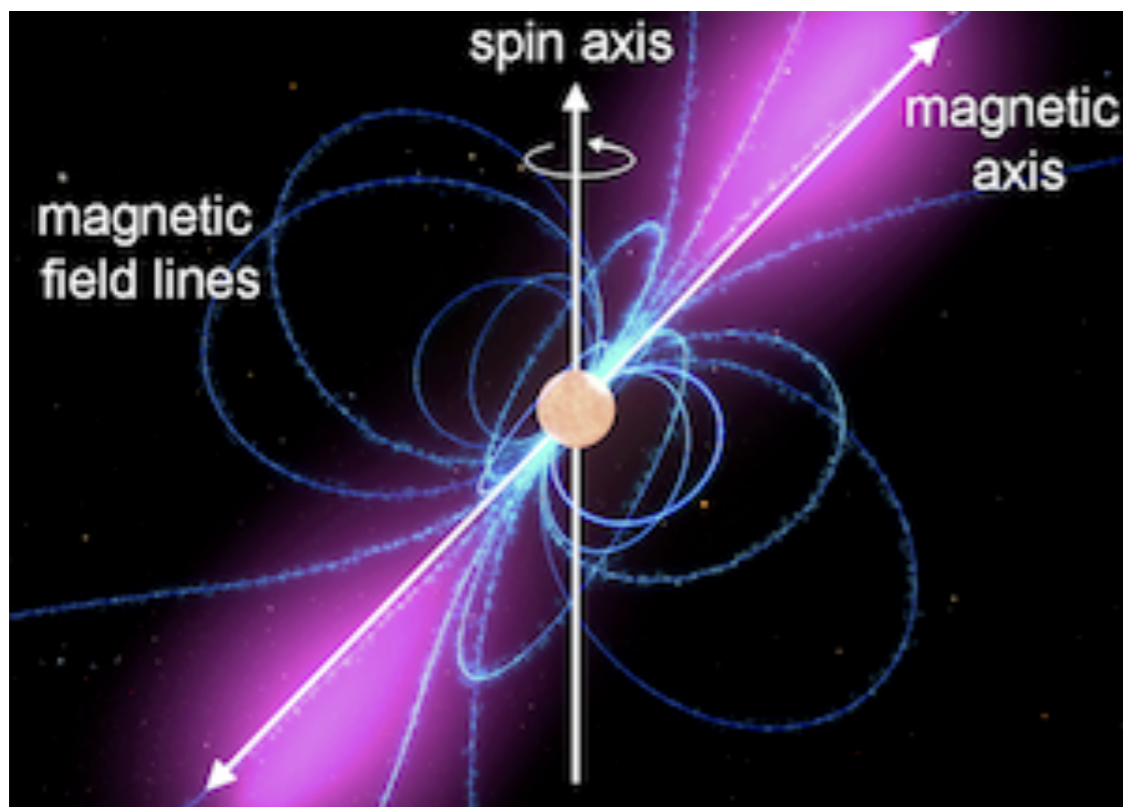
pulsars have radio beams along the magnetic axes
(related to the physics of the magnetosphere)



a main observable is the ToA (time of arrival) at different ν

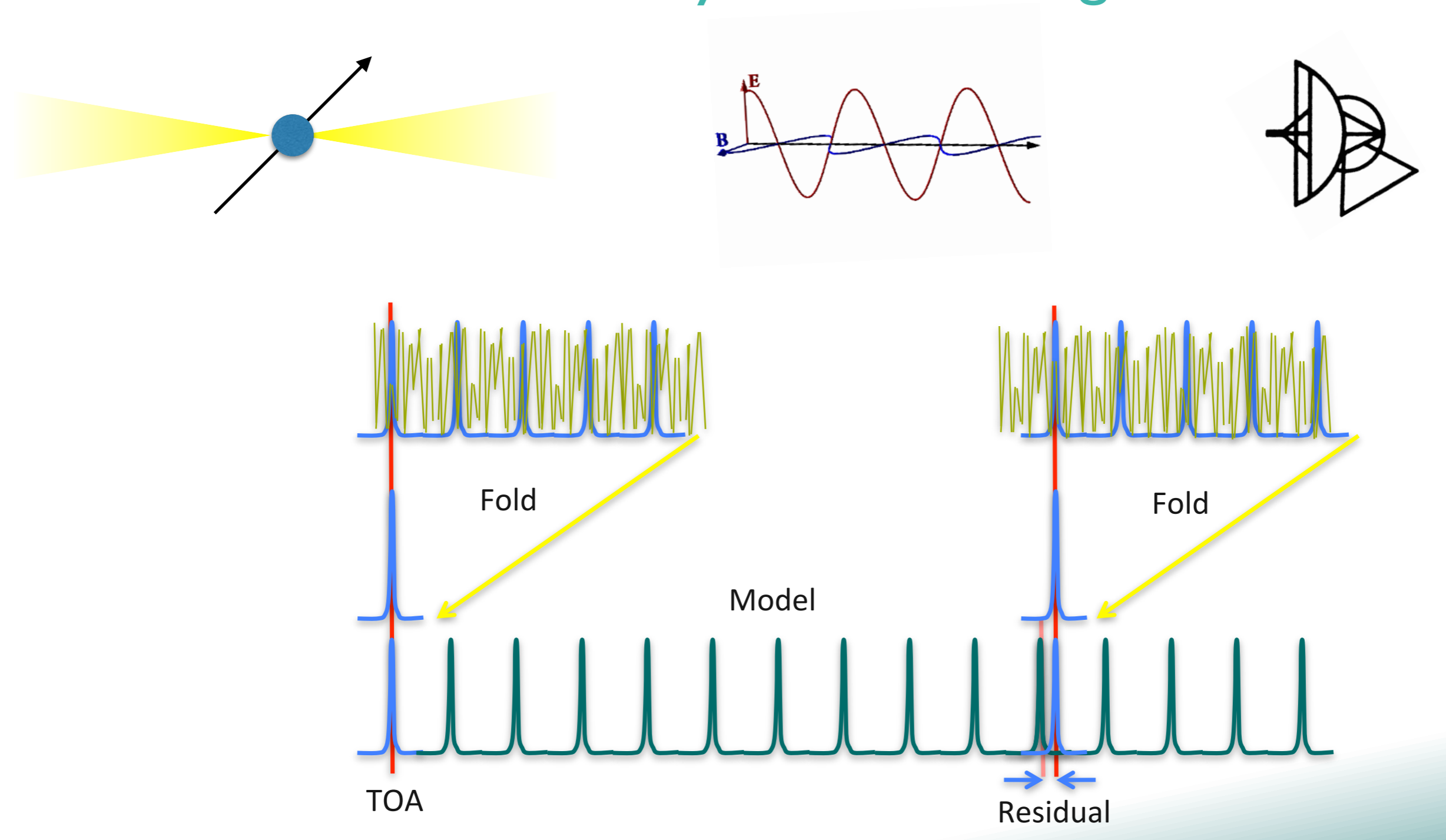
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The beauty of the ToA signal

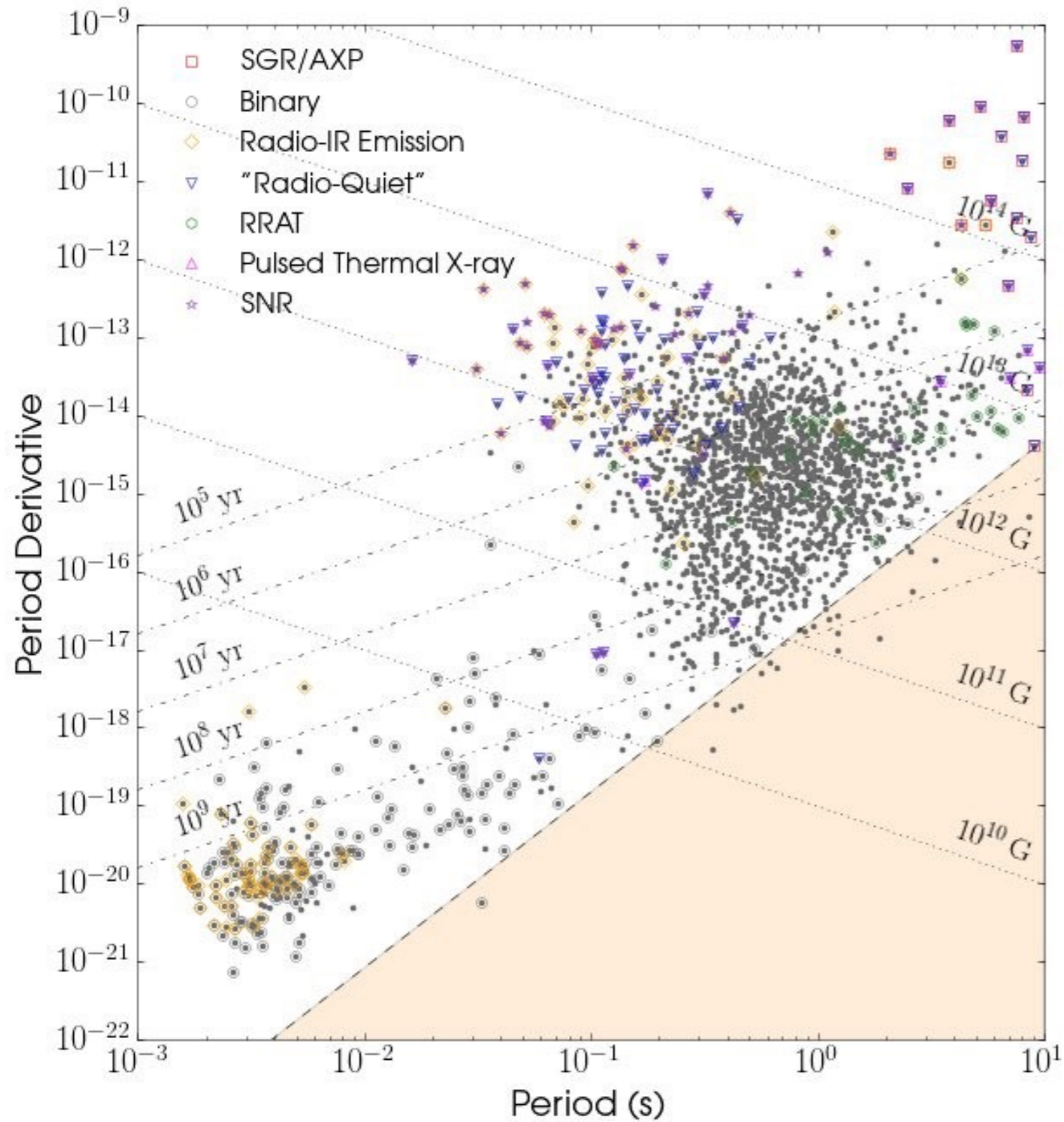


PSR J0437-4715

$P_s = 5.757451924362137(2) \text{ ms}$ (2 atto seconds uncertainty)

(for different frequencies and including polarization)

Pulsars in binaries

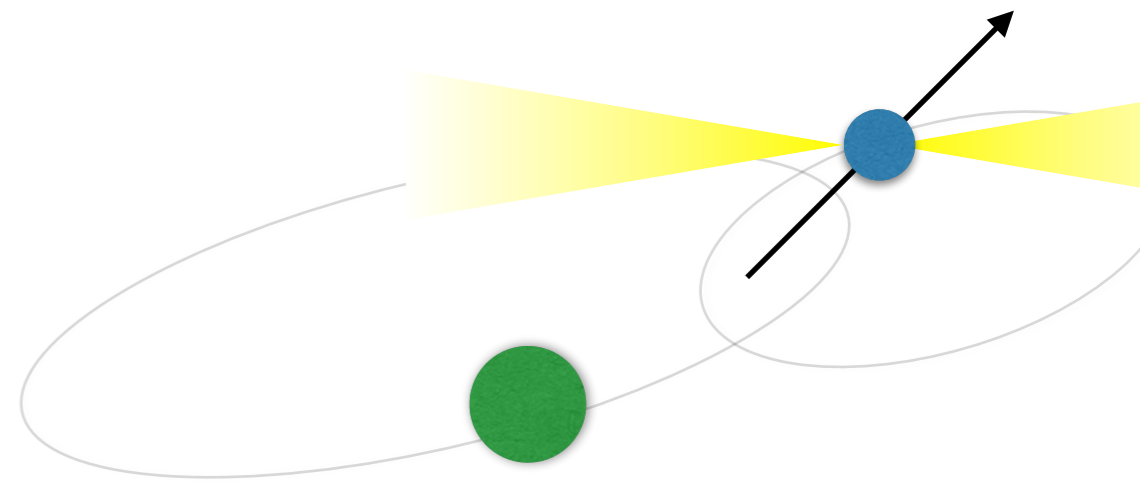


~ 2800 radio pulsars

10 % are in binaries
(MSS, WD, NS, planets)!

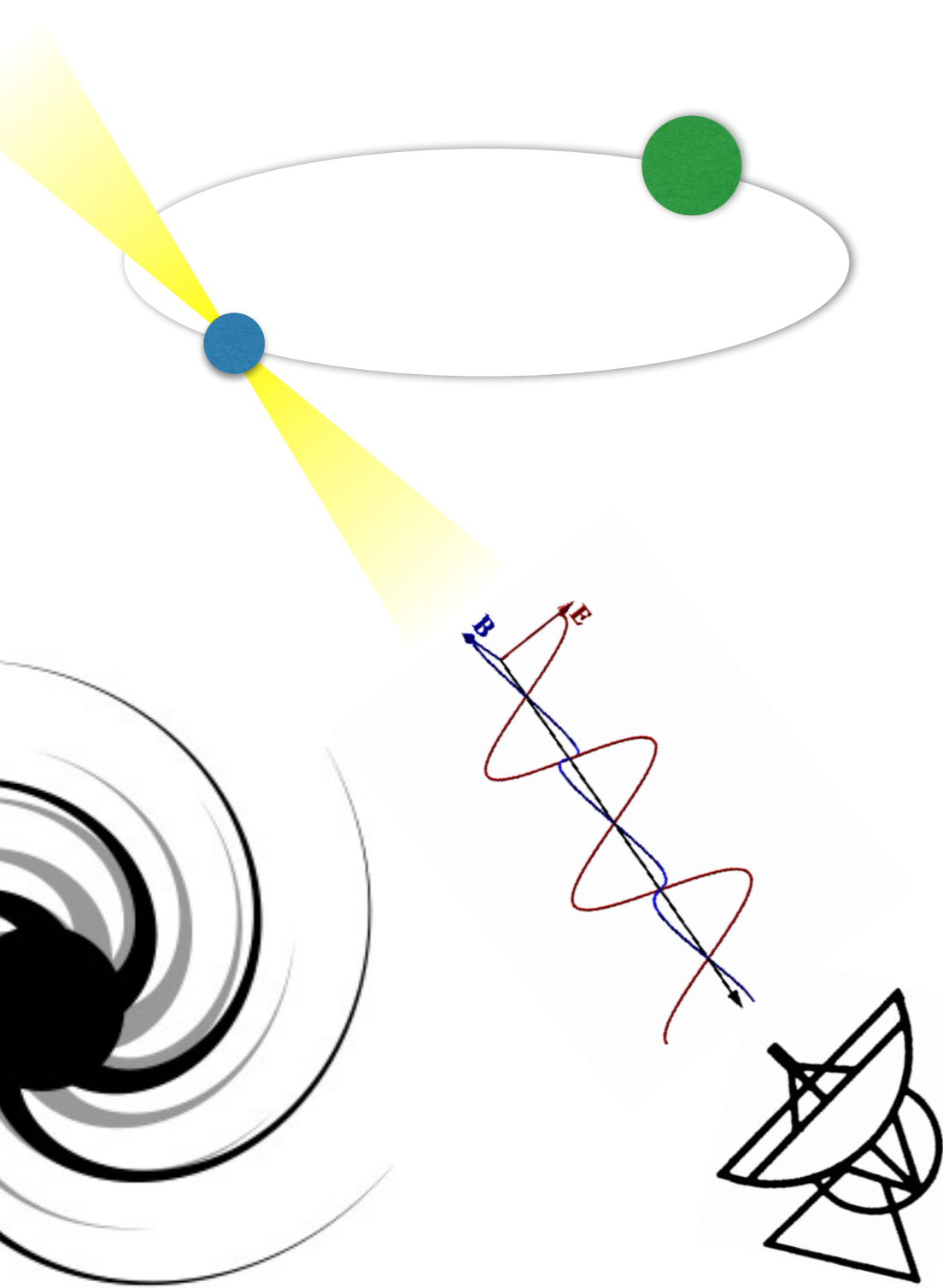
1 known double pulsar

$$P_b = 94 \text{ min} - 5 \text{ yr}$$



the **ToA** of the signal is sensitive to the orbit:
a precise clock falling in the potential

Pulsar timing for fundamental physics



At emission

- Properties of NSs (dense matter, B , \mathbf{X})
- Dynamics of the system: binary (GR, \mathbf{X}) and external (\mathbf{X} , matter) interactions

Propagation

- Propagation in the magnetosphere

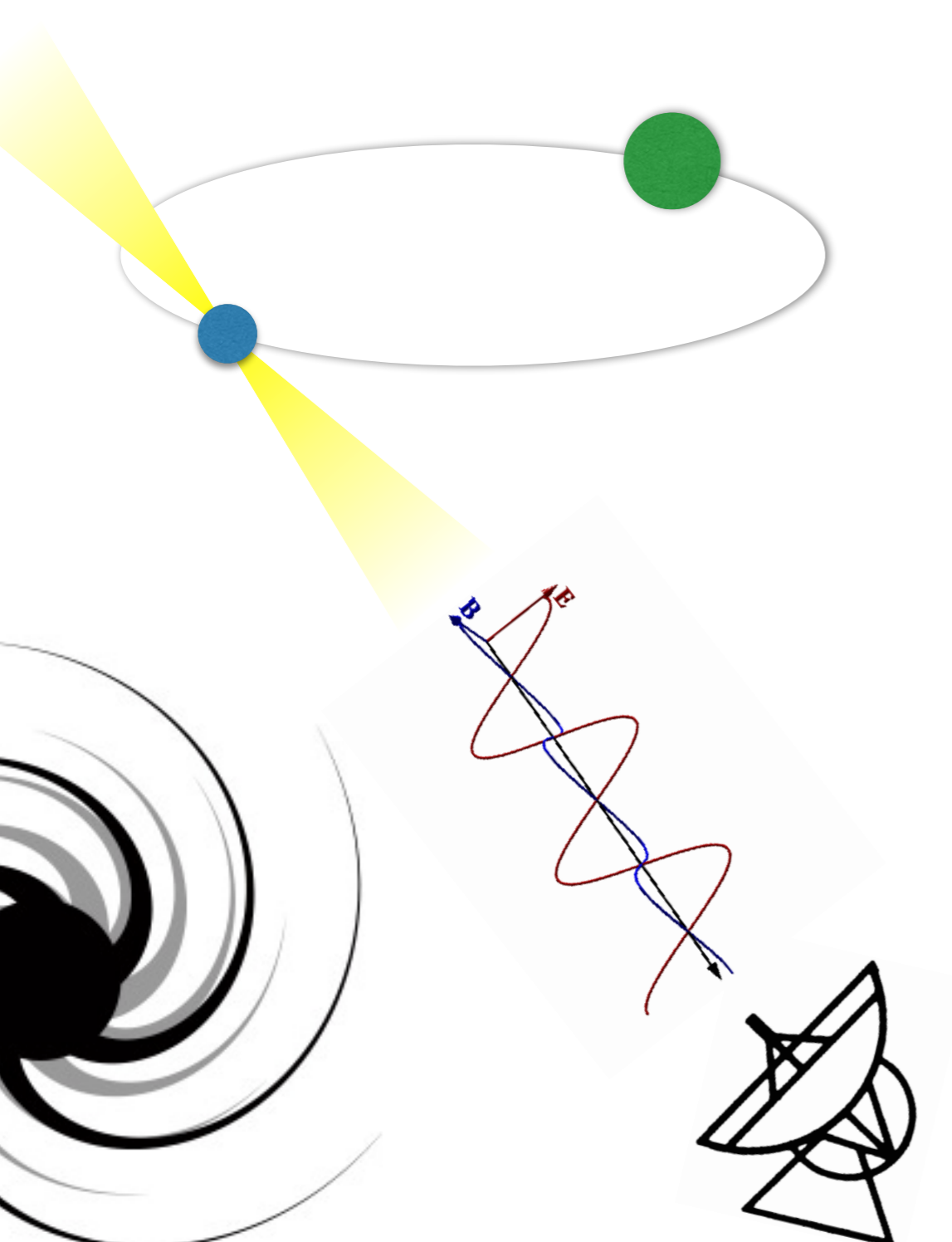
$$X = \mathcal{L}(\phi, F^{\mu\nu}) = \phi \vec{E} \cdot \vec{B}$$

- Propagation of signal in the interstellar medium: ions, e, GWs, \mathbf{X}

At detection

- Fundamental 'constants' (\mathbf{X})

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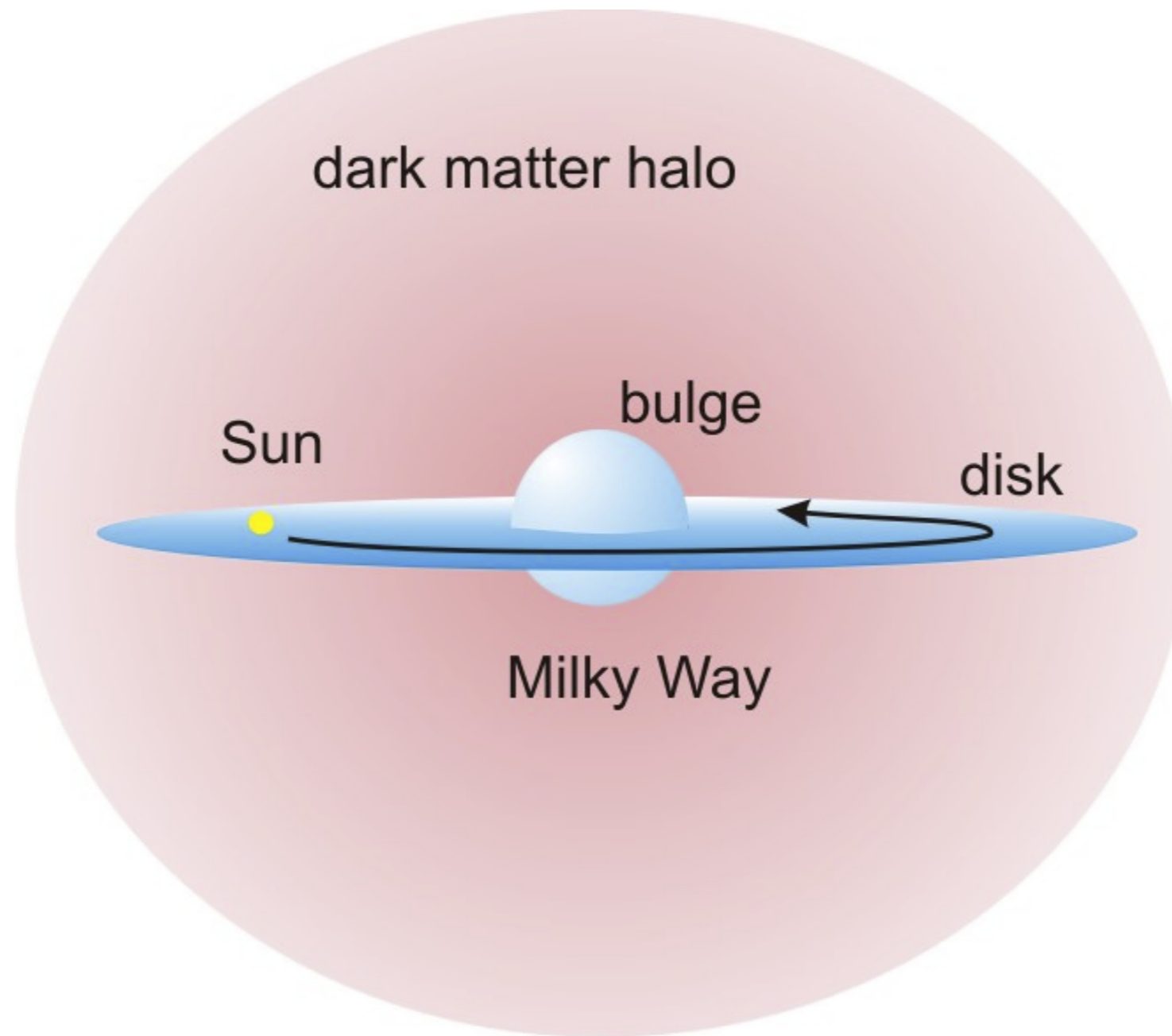
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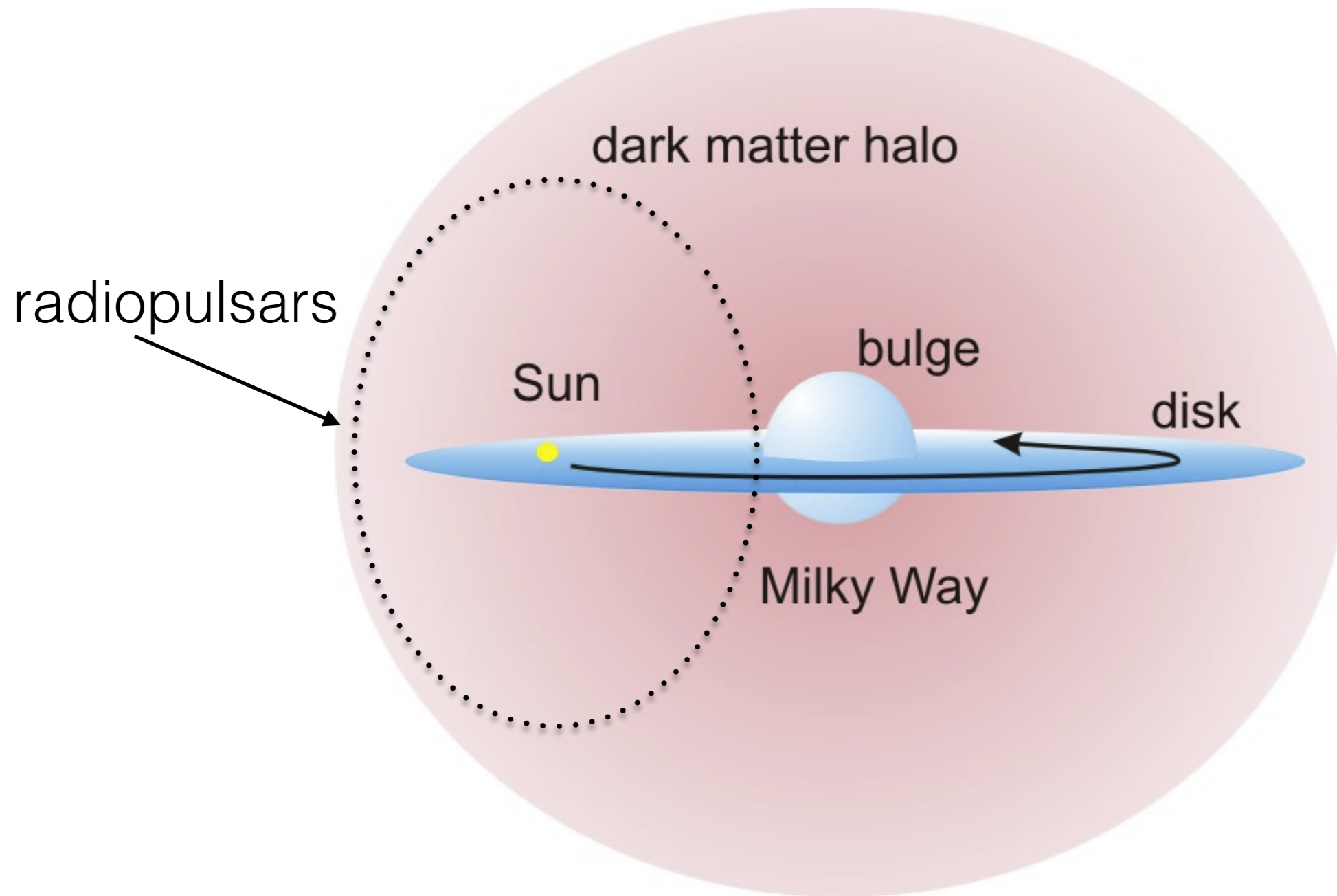
- Fundamental 'constants' (\mathbf{X})

\mathbf{X} = (Ultra) light DM

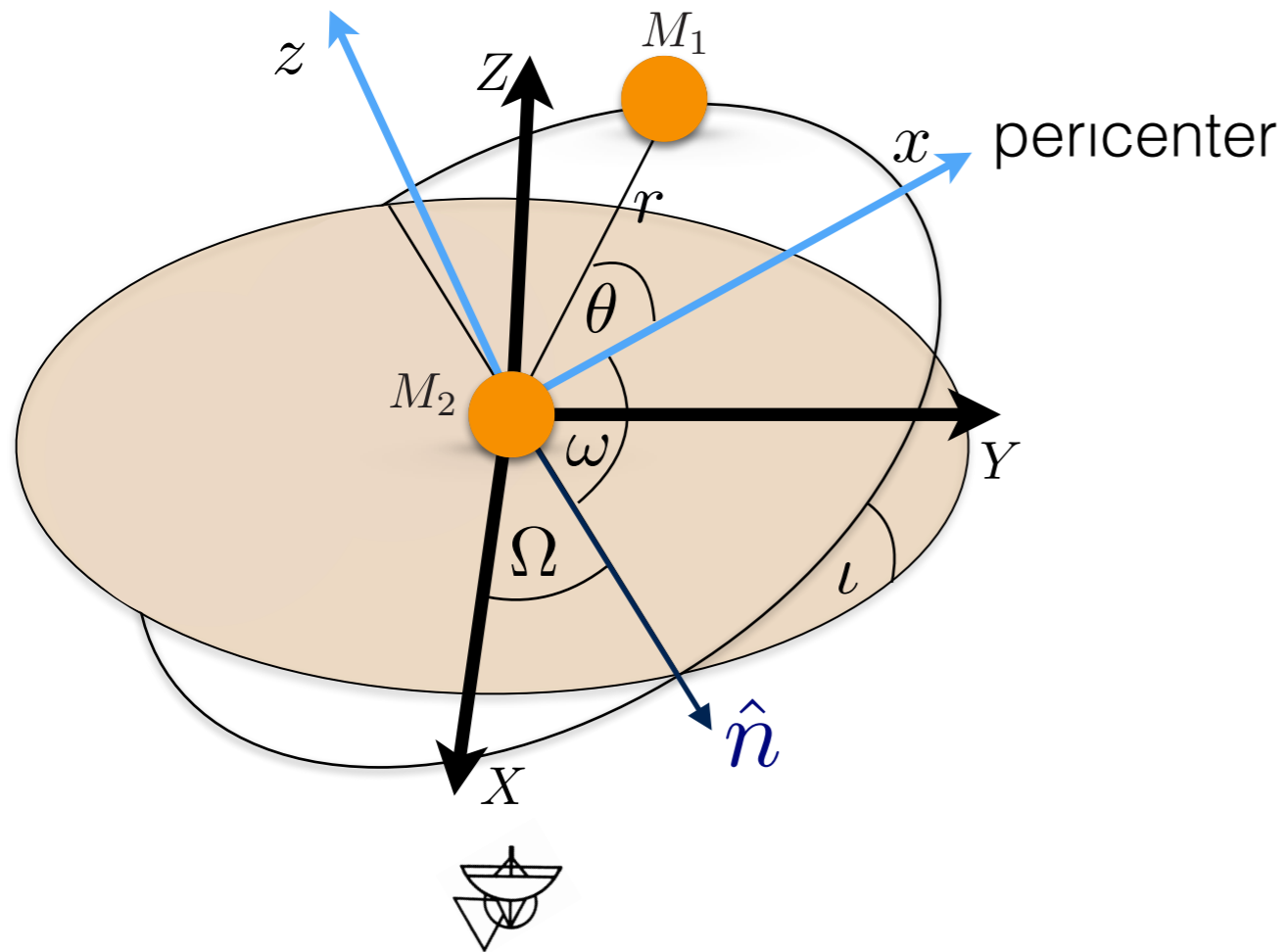
DM in galaxies (e.g. MW)



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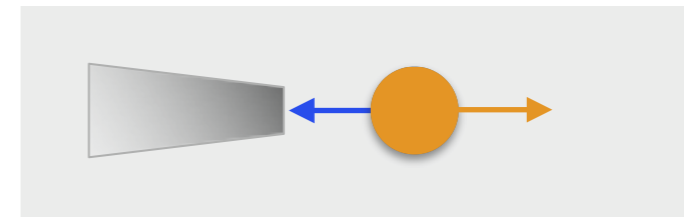


Orbital motion in the presence of WIMPS



fixed orbital parameters
 $a, e, \omega, \Omega, \epsilon_1, l$

In a WIMP medium
 dynamical friction in each object



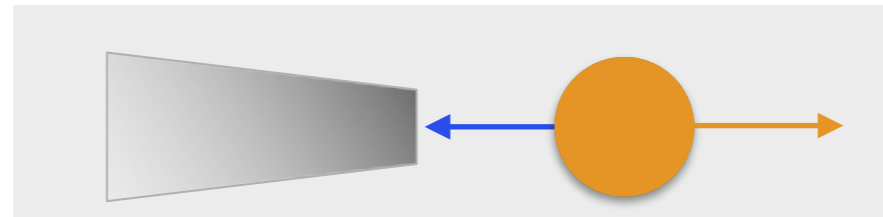
$$m_i \ddot{\mathbf{r}}_i = \pm \frac{Gm_1 m_2}{r^3} \mathbf{r} + \mathbf{F}_i^{\text{ext}}$$

(drift of orbital parameters! method of *osculating orbits*)

e.g.
$$\dot{a} = 2 \sqrt{\frac{r_0^3}{GM}} \mathbf{F}_i^{\text{ext}} \cdot \mathbf{e}_\theta$$

Orbital motion in the presence of WIMPS

Chandrasekhar, 1940s, Binney & Tremaine, "Galactic Dynamics", 1987



σ : DM dispersion

$$x \equiv v / (\sqrt{2}\sigma) \ll 1$$

Dynamical friction:

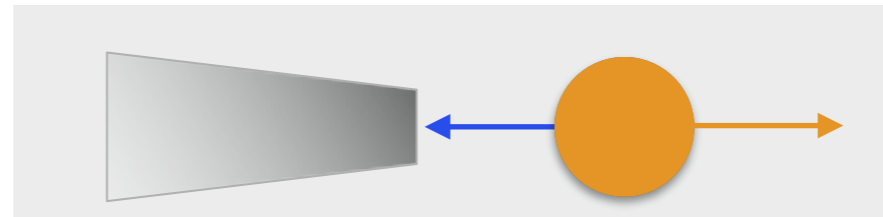
$$\mathbf{F}_i^{\text{DF}} = -4\pi\rho_{\text{DM}}\lambda\frac{G^2m_i^2}{v_i^3}\left(\frac{4x^3}{3\sqrt{\pi}} - \frac{4x^5}{5\sqrt{\pi}} + O(x^7)\right)\mathbf{v}_i$$

Pani 2015

$$\langle \dot{P}_b^{\text{DF}} \rangle \approx -3 \times 10^{-14} \left(\frac{\lambda}{20}\right) \left(\frac{\mu}{M_\odot}\right) \left(\frac{\rho_{\text{DM}}}{2 \times 10^3 \text{ GeV/cm}^3}\right) \left(\frac{P_b}{100 \text{ day}}\right) \left(\frac{150 \text{ km/s}}{\sigma}\right)^3$$

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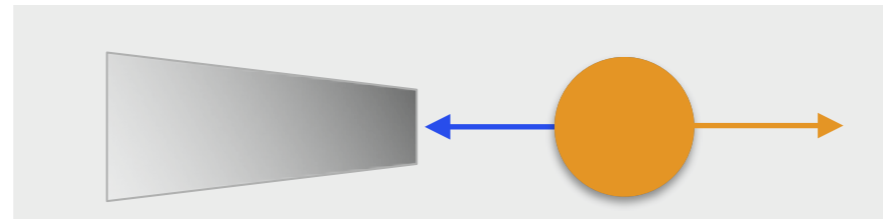
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$$\rho_\odot \sim 0.3 \text{ GeV/cm}^3$$

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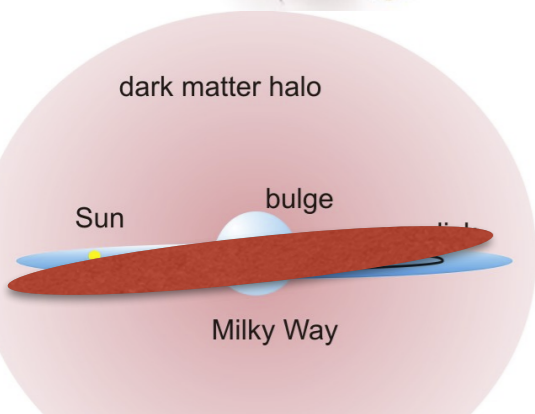
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better prospects for other WIMP models Caputo, DB, Zavala 2017

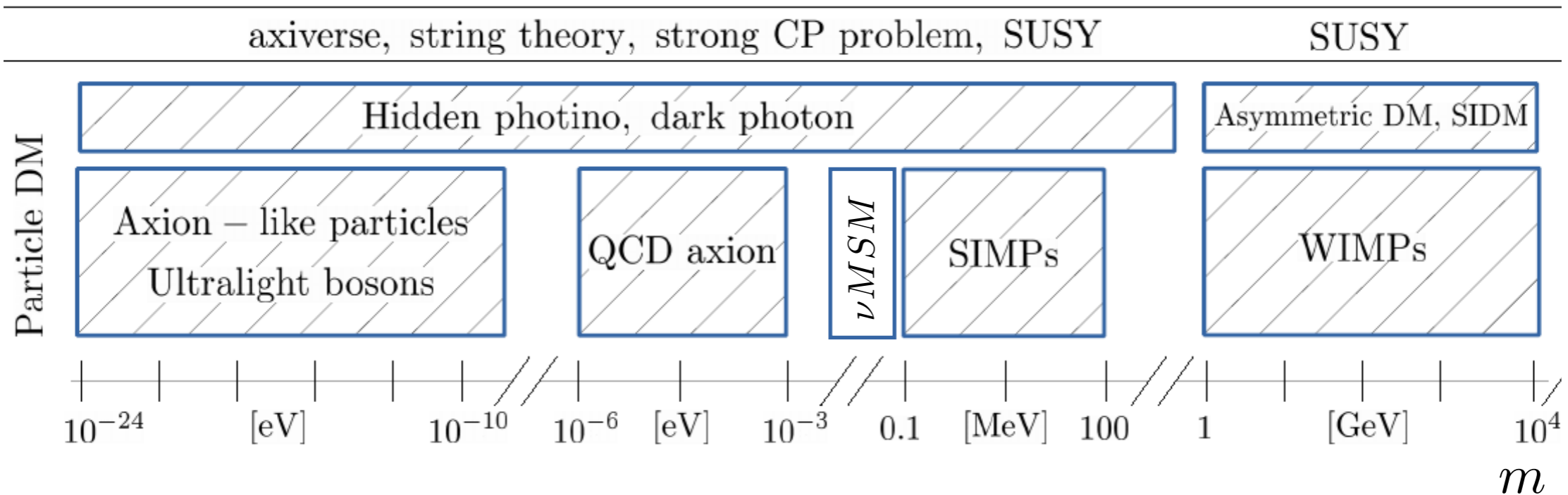
(Randall et al 2014)

- * Double disk models have higher ρ and lower σ
- * Maybe SM-DM interacting through a light mediator?



Ultra light DM models

- ☑ DM candidate should be a cold gravitating medium
- ☑ Production mechanism and viable cosmology
- ☑ Motivation from fundamental physics
- ☑ Possibility of (direct or indirect) detection



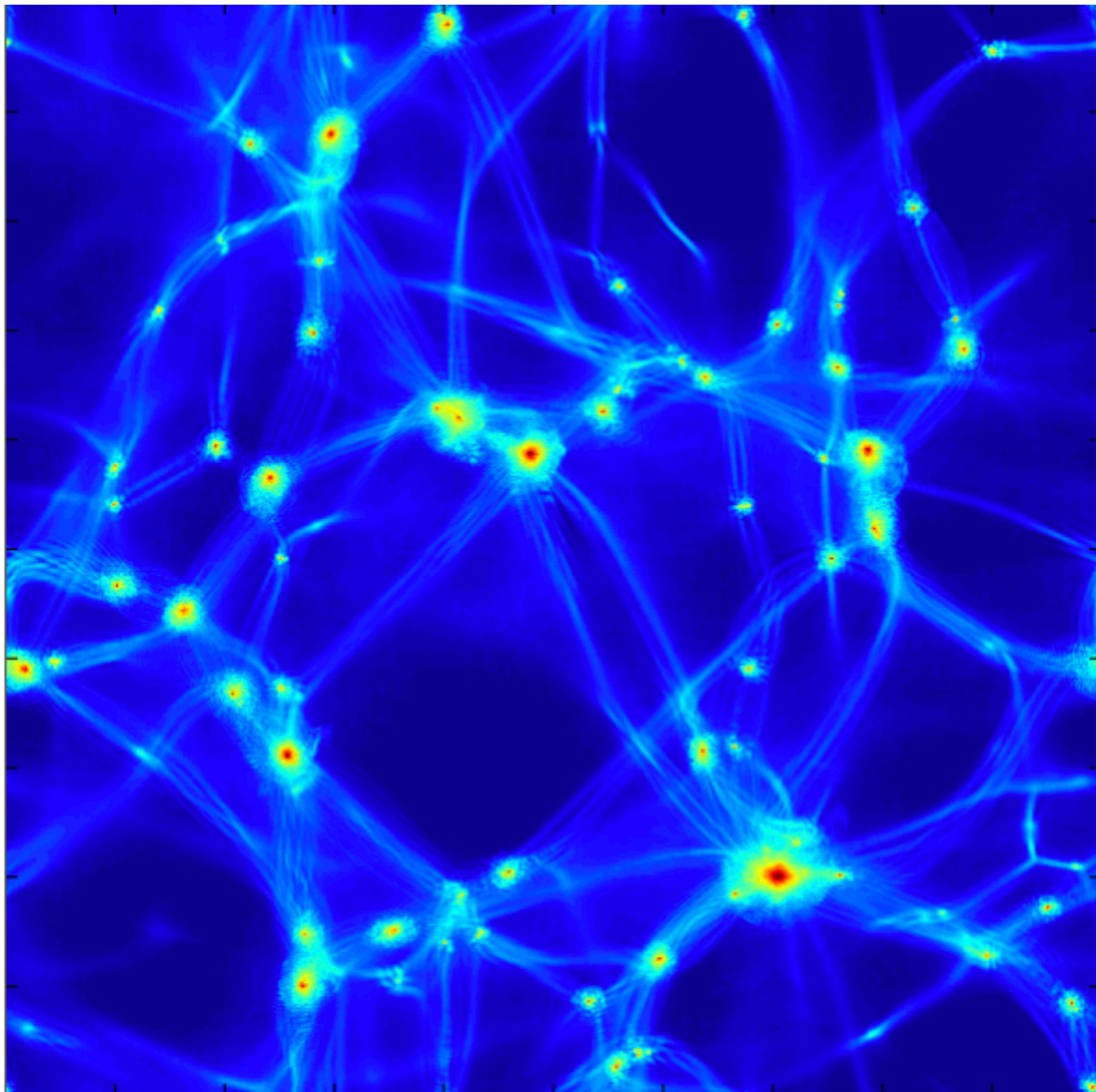
MACHOS, BHS,...

ULDM behaves like CDM at large-scales

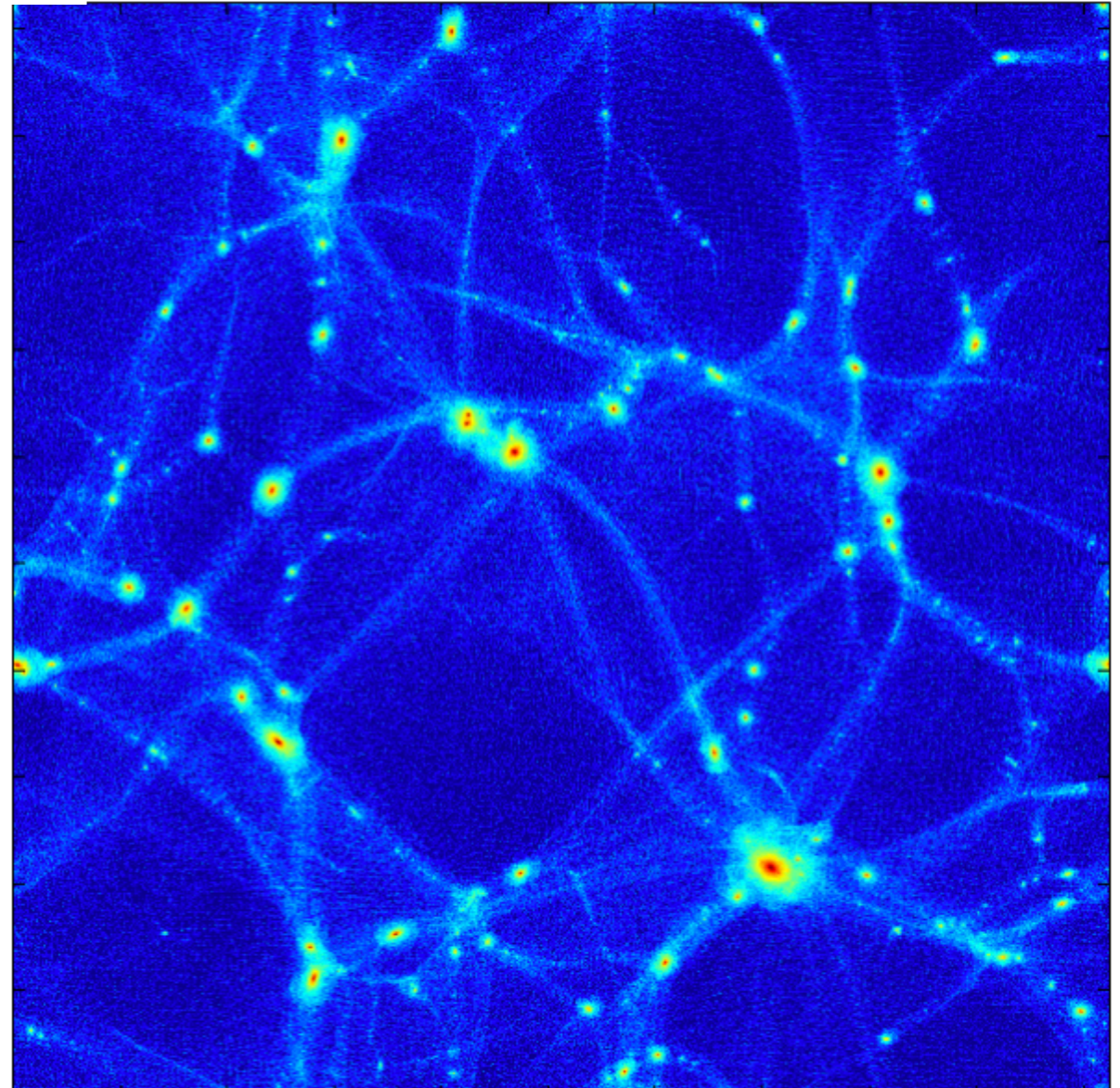
$$\mathcal{L} = \frac{1}{2} \left[(\partial_\mu \phi)^2 - m^2 \phi^2 \right] + \text{gravity}$$

Scale of ~ 30 Mpc, Schive et al. 1406.6586

ULDM

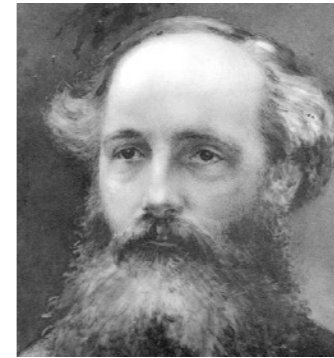


CDM



Ultra light DM in our Galaxy

$\hbar\omega$



$F_{\mu\nu}$

- i) escape velocity $\sim 2 \times 10^{-3}c$ ii) size 100 kpc

$$\Delta x \Delta p \gtrsim \hbar \rightarrow N_s \sim 10^{75} \left(\frac{m}{\text{eV}} \right)^3$$

$$N_p = \frac{M_{MW}}{N_s m} \sim 10^3 \left(\frac{\text{eV}}{m} \right)^4$$



For ULDM, field has huge occupation numbers with random phases:

it can be treated as a classical field

$$\mathcal{L} = \frac{1}{2} \left[(\partial_\mu \phi)^2 - m^2 \phi^2 \right] \rightarrow \phi_k \sim e^{i(\omega t - kx)}$$

in a virialized halo

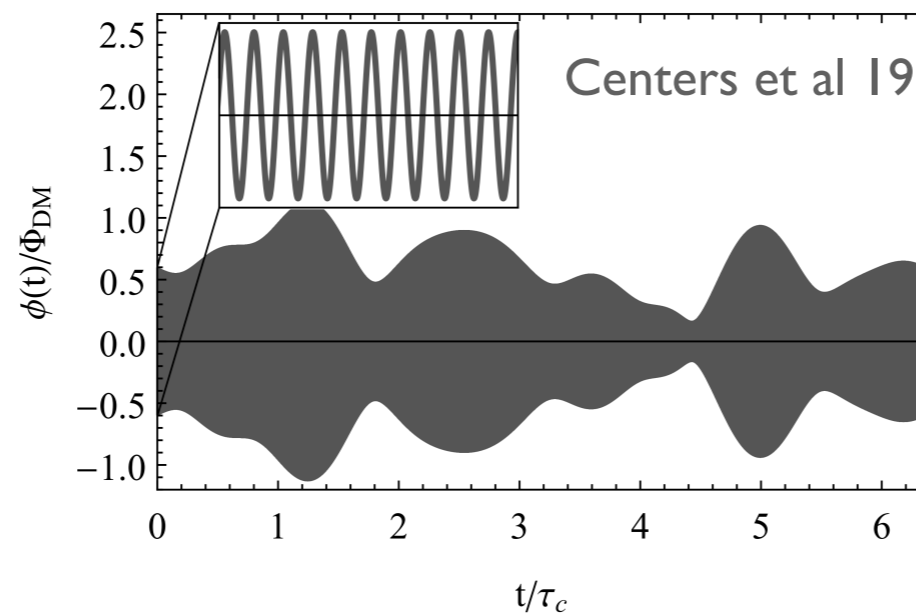
'Coherent' effects of ULDM in the MW

Virialized configuration: collection of waves with distribution determined by properties from the galaxy

$$\phi \propto \int_0^{v_{max}} d^3v e^{-v^2/\sigma_0^2} e^{i\omega_v t} e^{-im\vec{v}\cdot\vec{x}} e^{if\vec{v}} + c.c.$$

↓
distribution: $\sigma_0 \sim 10^{-3}c$ in the MW

since $v \sim \sigma_0 \ll 1 \Rightarrow \omega_v \approx m(1 + v^2) \Rightarrow \phi \propto \phi_0 \cos(mt + f)$



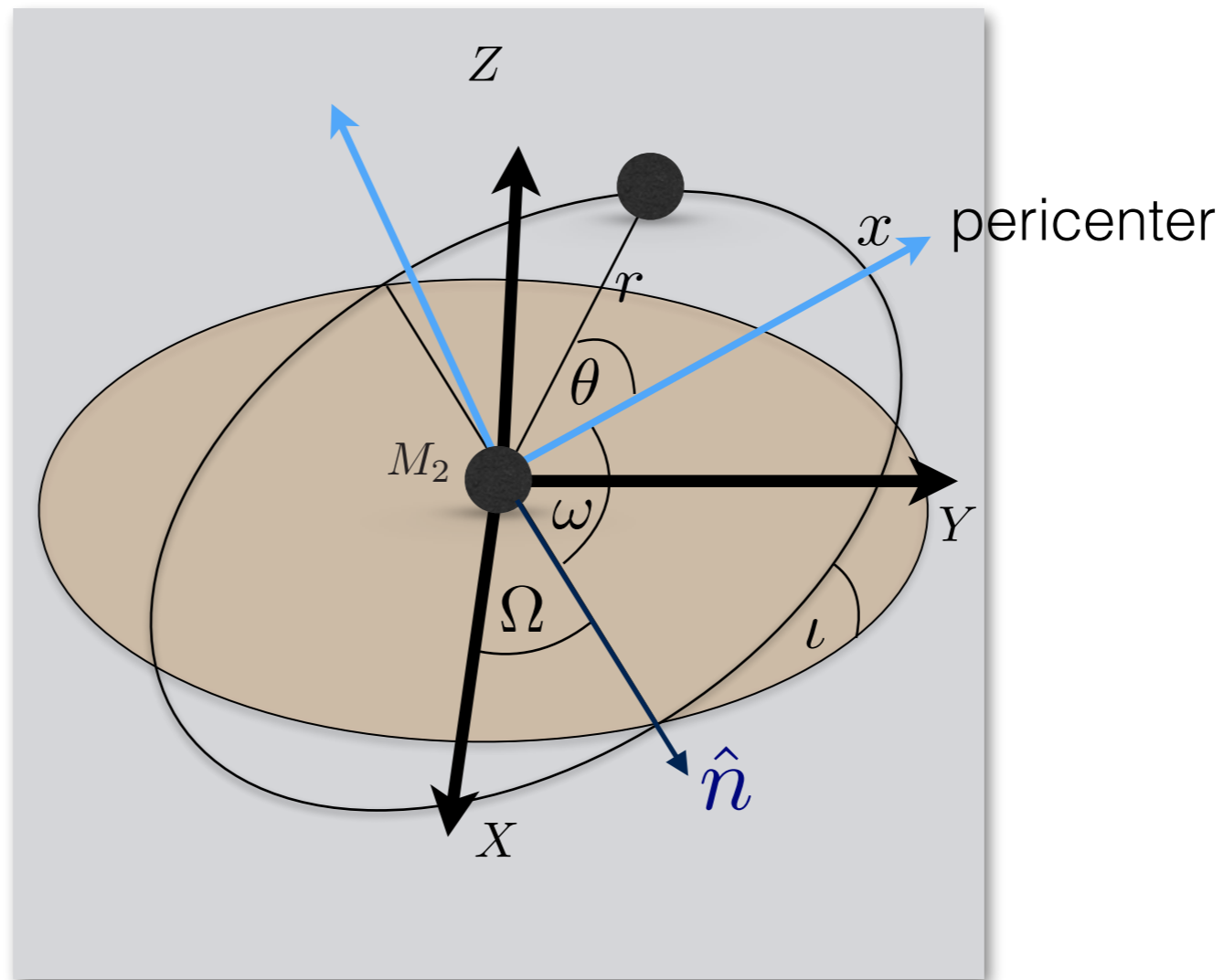
$$\tau_c \sim 65 \text{ years} \left(\frac{10^{-3}}{V_0} \right)^2 \left(\frac{10^{-18} \text{ eV}}{m_\Phi} \right)$$

It is also very homogenous

the field is homogeneous at scales

$$\lambda_{\text{dB}} \sim 1.3 \times 10^{12} \text{km} \left(\frac{10^{-3}}{V_0} \right) \left(\frac{10^{-18} \text{eV}}{m_\Phi} \right)$$

$$\phi_0 \cos(mt + f)$$



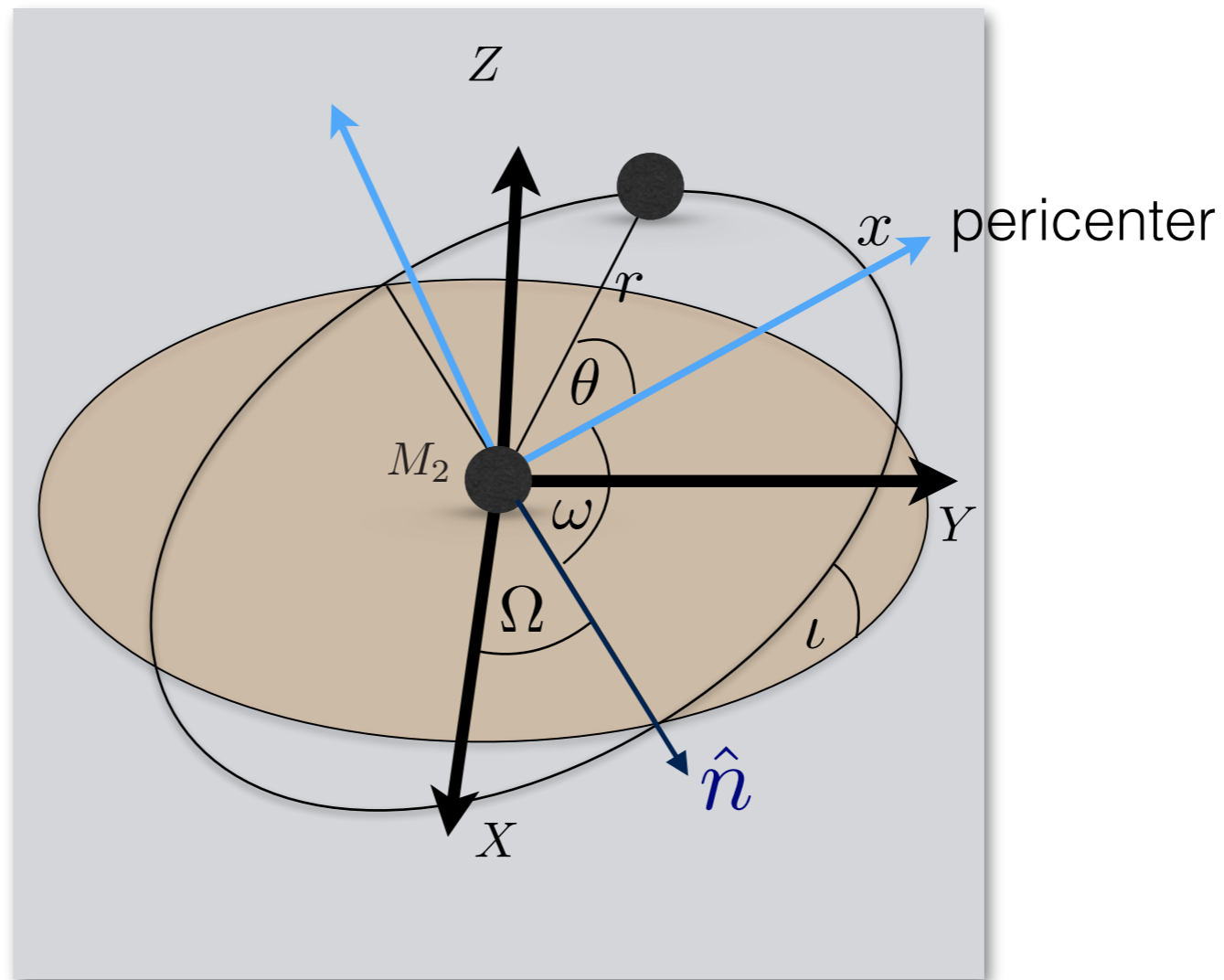
$$\rho_{DM} = \frac{m^2 \phi_0^2(t)}{2} \quad p = -\rho_{DM} \cos(2mt + 2\alpha) \quad \rightarrow \quad (\varphi_N^{\text{gal}}(t), \psi_N^{\text{gal}}(t))$$

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Effects on binary system: pure gravity

DB, LopezNacir, Sibiryaikov 16, 19

$$\ddot{\vec{R}}_{CM} = 0$$

$$\mu \ddot{\vec{r}} = \vec{F}_{GR} + \vec{F}_{DM,halo} \propto \vec{r}$$

$$\delta E_b = \mu \int_0^{P_b} dt \dot{\vec{r}} \cdot \vec{F} \quad \rightarrow \quad \dot{P}_b$$

$P_b \propto |E_b|^{-3/2}$

Can also be found from the osculating method

$$\frac{\dot{a}}{a} = -\frac{2e}{\omega_b \sqrt{1-e^2}} \ddot{\psi} \frac{r}{a} \sin \theta$$

$$\dot{e} = -\frac{\sqrt{1-e^2}}{\omega_b} \ddot{\psi} \frac{r}{a} \sin \theta$$

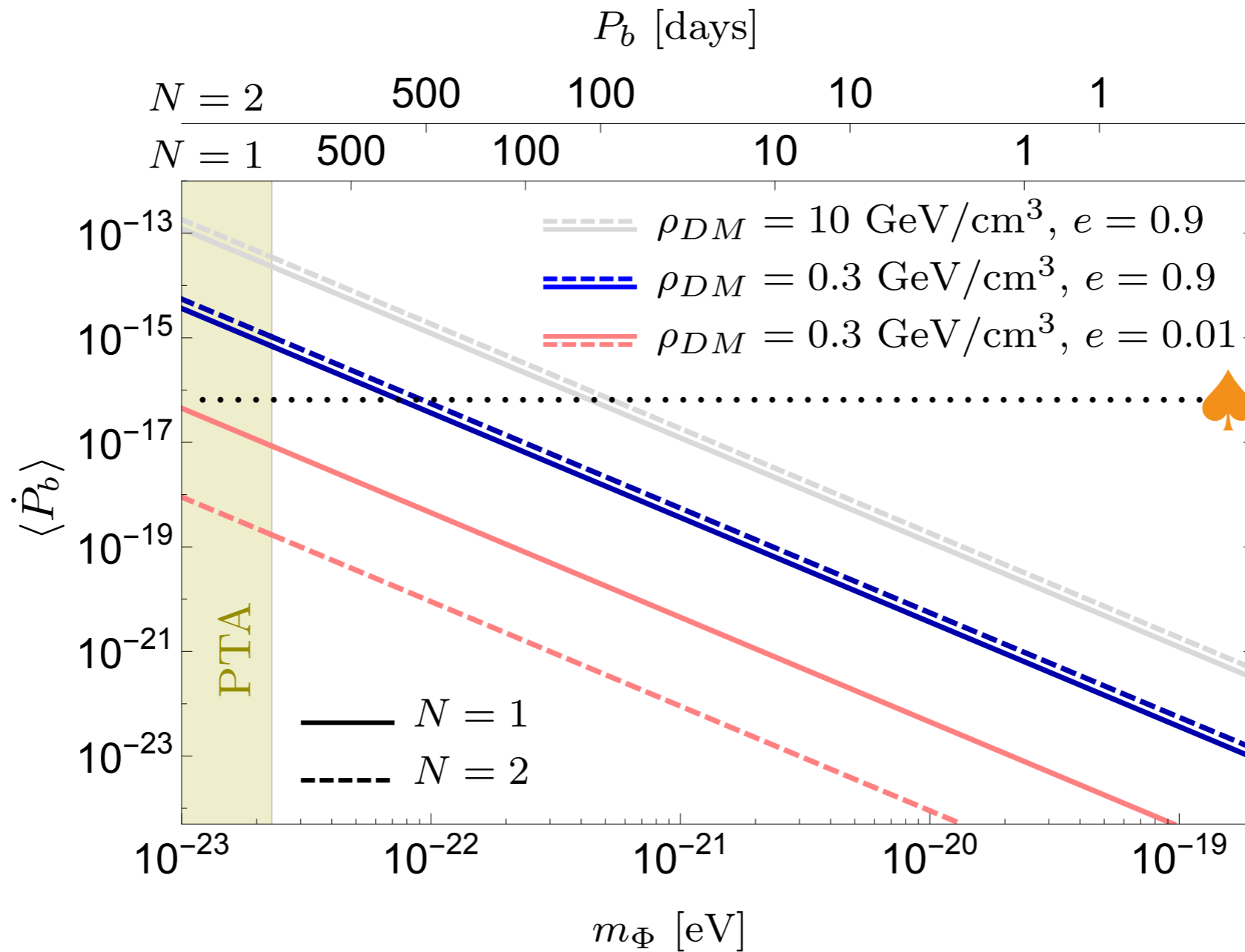
$$\text{if } m \approx N \frac{2\pi}{P_b}$$

the effect accumulates
in every orbit
(resonant effect)

Prospects of observation

DB, LopezNacir, Sibiryakov 16

This pure gravitational test of ULDM
is beyond reach....

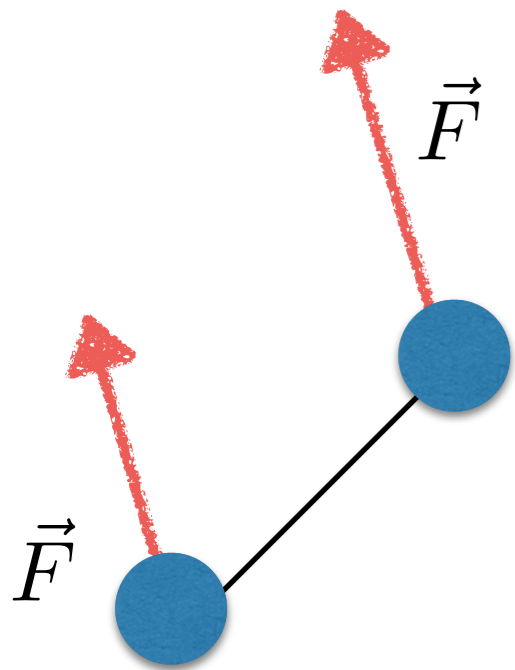


Effects on binary system: DM-matter interaction

DB, LopezNacir, Sibiryakov 16, 19

DM can couple directly to matter

$$m_i \alpha \int \phi(x_{pp}) ds_i + m_i \beta \int [\phi(x_{pp})]^2 ds_i \dots$$



again $m_i \ddot{\mathbf{r}}_i = \pm \frac{Gm_1 m_2}{r^3} \mathbf{r} + \mathbf{F}_i^{\text{ext}}$

$$\ddot{\mathbf{R}}_{CM} \neq 0 \quad (\text{swamped by systematics})$$

$$\mu \ddot{\vec{r}} = \vec{F}_{\text{GR}} + \vec{F}_{\text{DM,halo}}(\phi(t))$$

$$\delta L_b = \mu \int_0^{P_b} dt \vec{r} \times \vec{F} \quad \Rightarrow \quad L_b^2 \propto P_b^{2/3} (1 - e^2) \quad \Rightarrow \quad \dot{e}$$

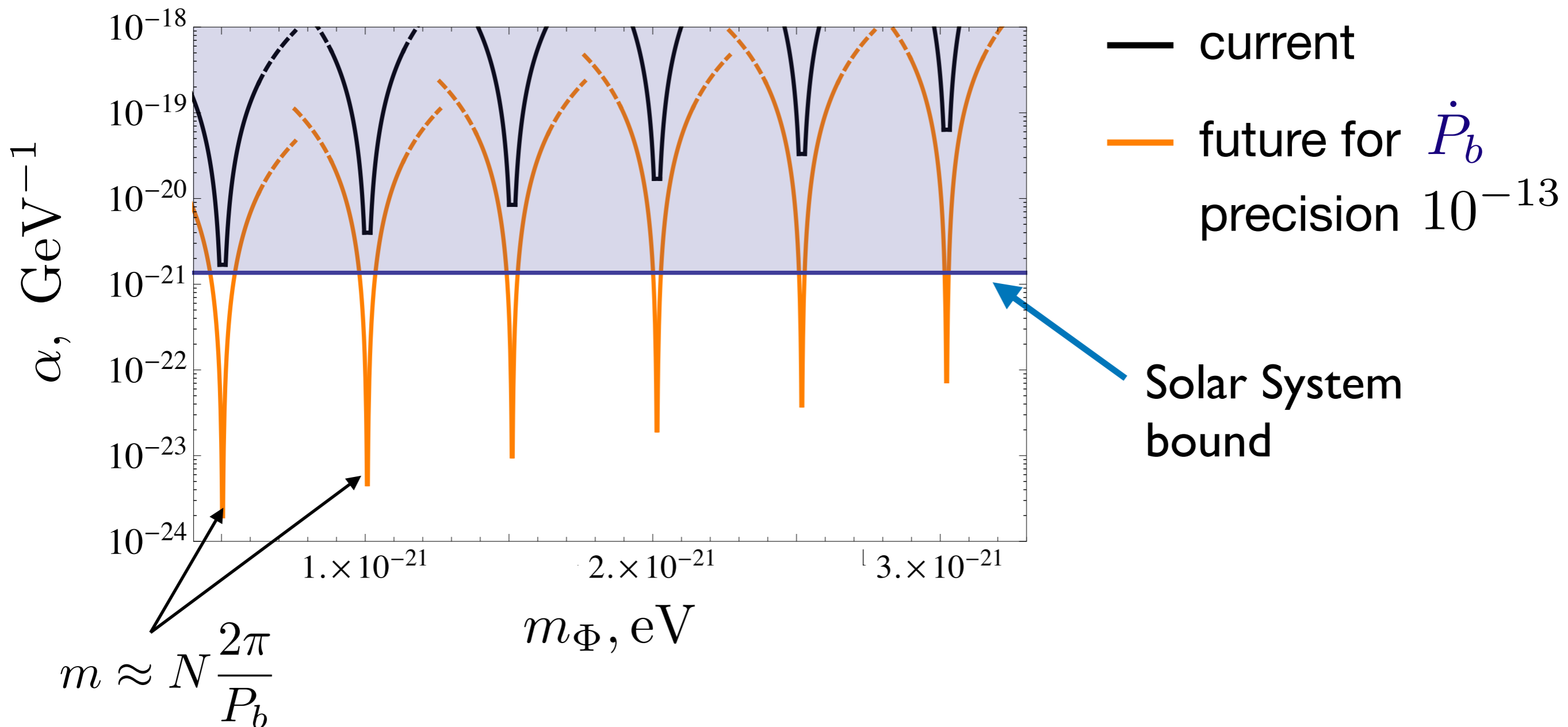
Secular effects at J1903+0327

Freire et al 2011

$$P_b = 95 \text{ days}, e = 0.44$$

$$\dot{P}_b = (-52 \pm 33) \times 10^{-12}$$

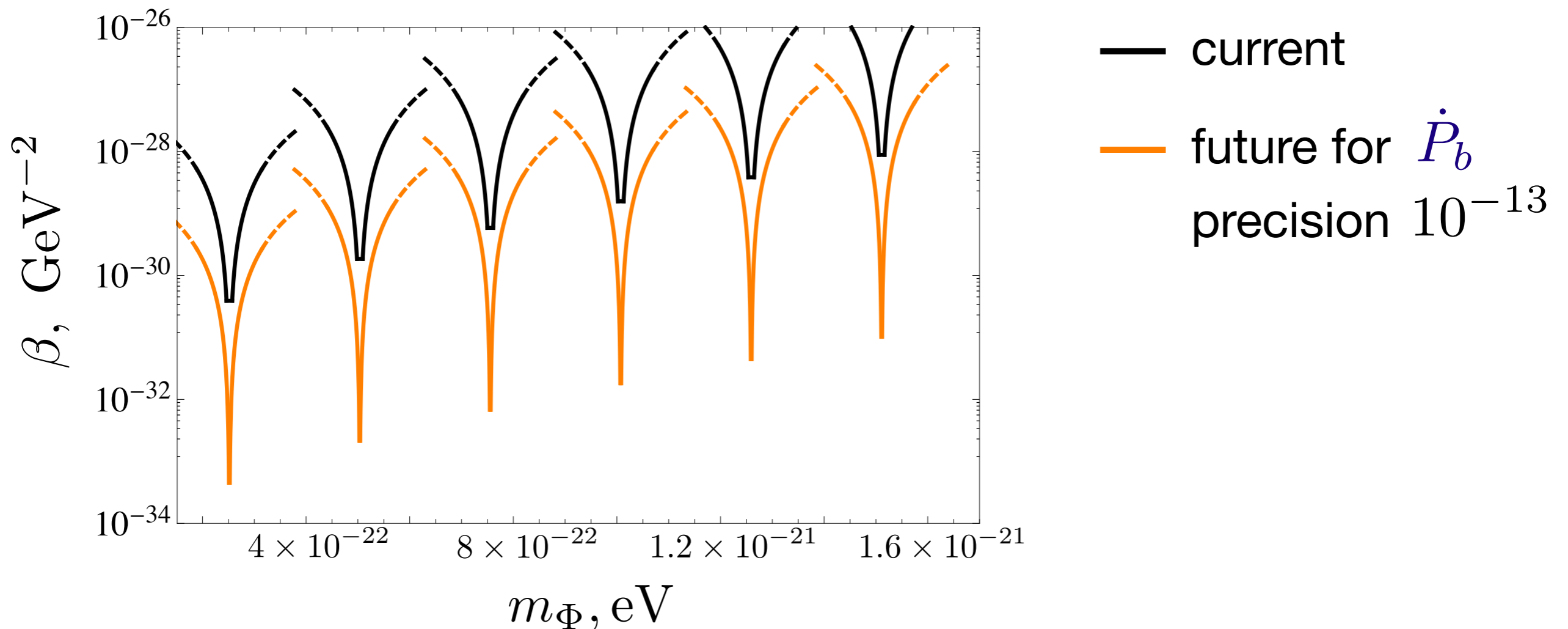
DB, LopezNacir, Sibiryakov 16, 19



Secular effects at J1903+0327

$$m_i \alpha \int \phi(x_{pp}) ds_i + m_i \beta \int [\phi(x_{pp})]^2 ds_i$$

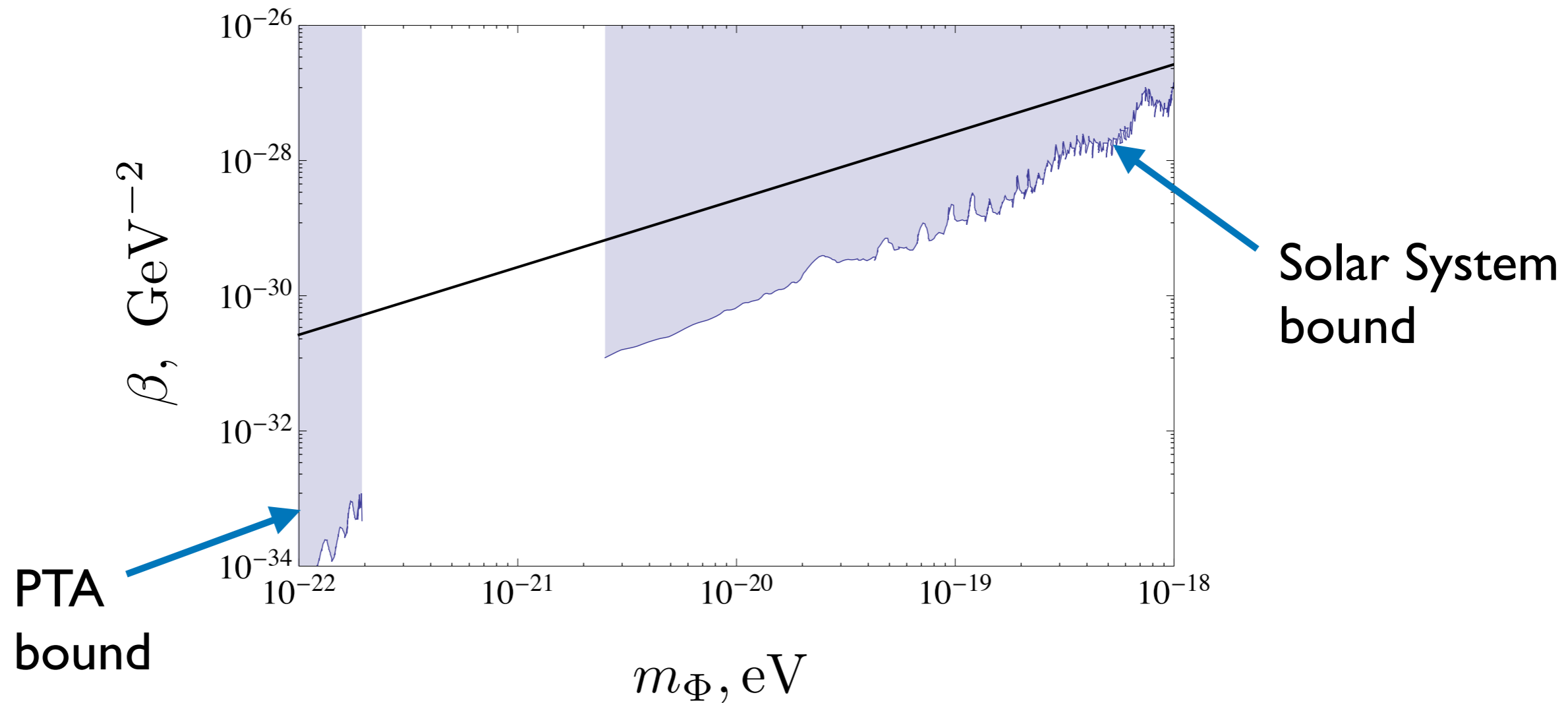
Limits on quadratic coupling



Broadband limits

from J1713+0747 ($P_b = 67.8$ days , $e = 7 \times 10^{-5}$)

$$\dot{e} \lesssim 10^{-17} \text{ s}^{-1}$$



Propagation of EM waves in a DM medium

Caputo, Sberna, Frias, DB, Pani, Shao, Yan 19

The DM may be also coupled to photons

charged DM

$$q_{\text{DM}} \int A_{\mu}(x_{pp}) dx_{\text{DM}}^{\mu}$$

⋮

axions

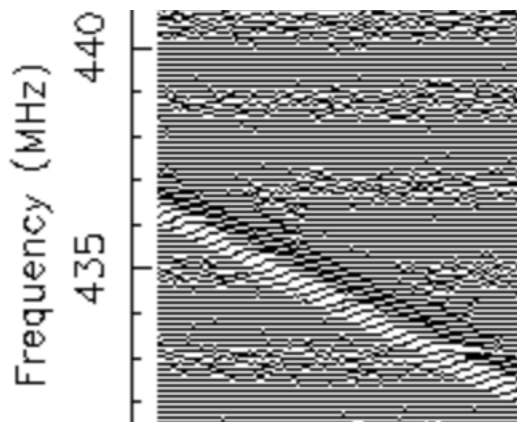
$$g \phi F_{\mu\nu} \tilde{F}^{\mu\nu} = g \phi \vec{E} \cdot \vec{B}$$

modify the dispersion relation of light

$$\omega^2 = k^2 + \sum_{\chi} \frac{4\pi n_{\chi} q_{\chi}^2}{m_{\chi}}$$



$$\Delta T(\omega) \propto \frac{q_{\chi}^2}{m_{\chi}^2 \omega^2}$$

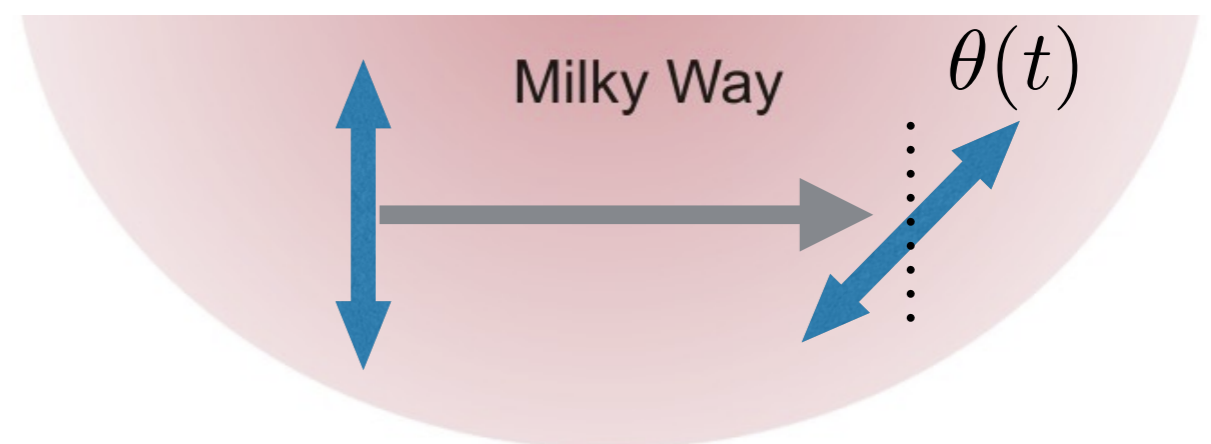


⋮

$$\phi = \phi_0 \cos(mt + \alpha(x))$$

$$\omega^2 = k^2 \pm 2\dot{\phi}(t) k$$

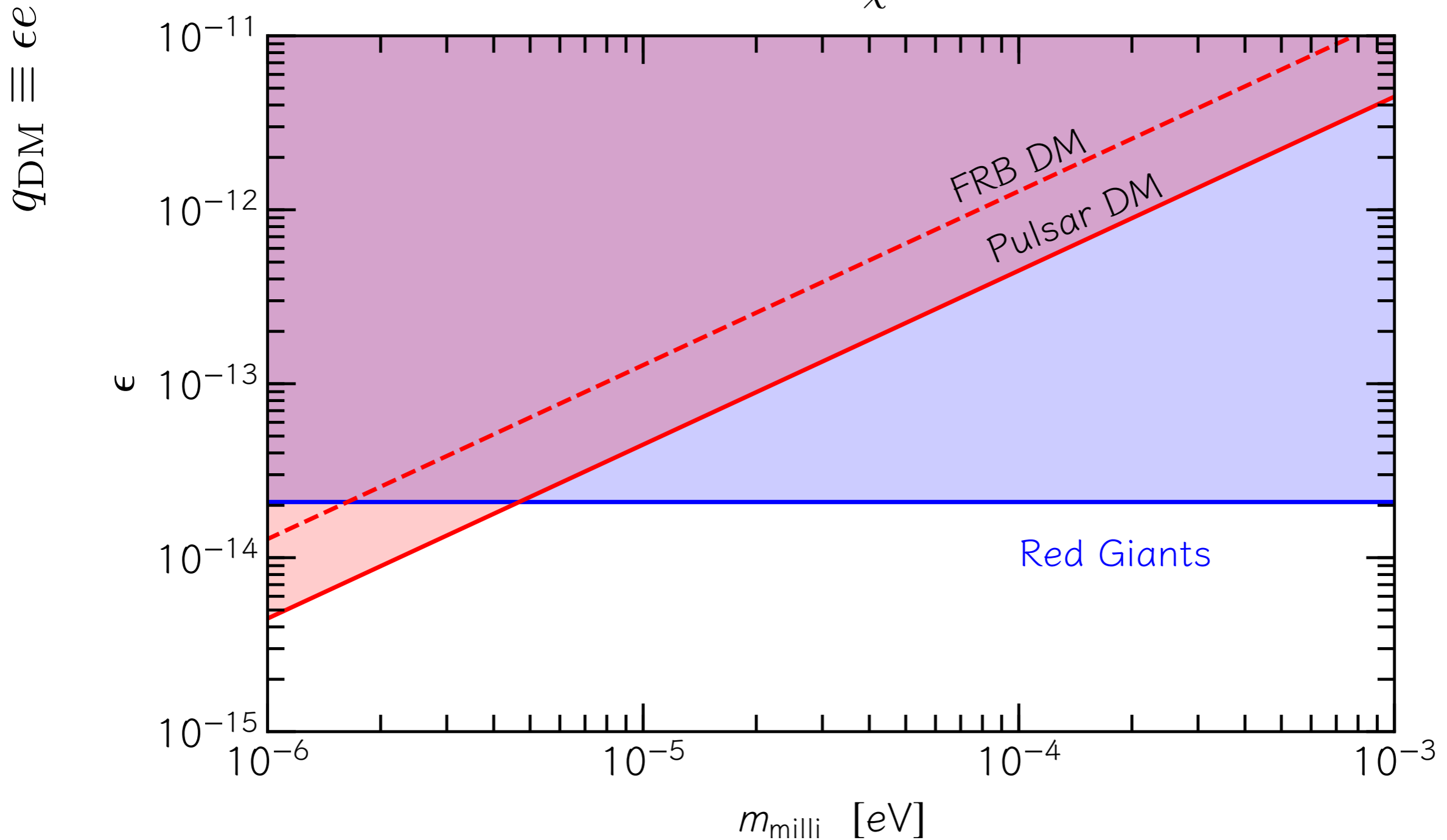
oscillating polarisation angle!



Constraints on DM charge

Caputo, Sberna, Frias, DB, Pani, Shao, Yan 1902.02695

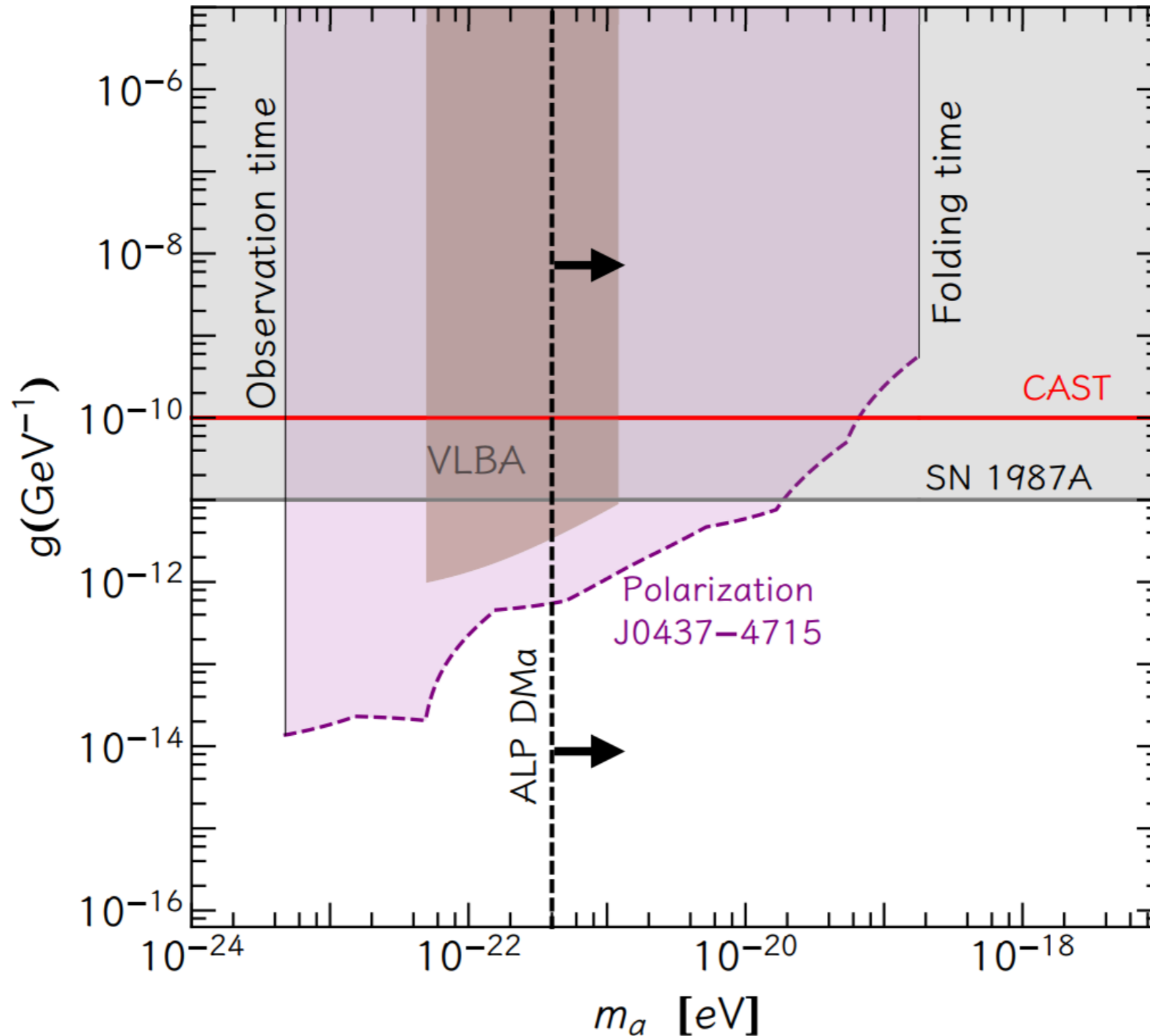
$$\Delta T(\omega) \propto \frac{q_\chi^2}{m_\chi^2 \omega^2}$$



Constraints on axion-EM coupling

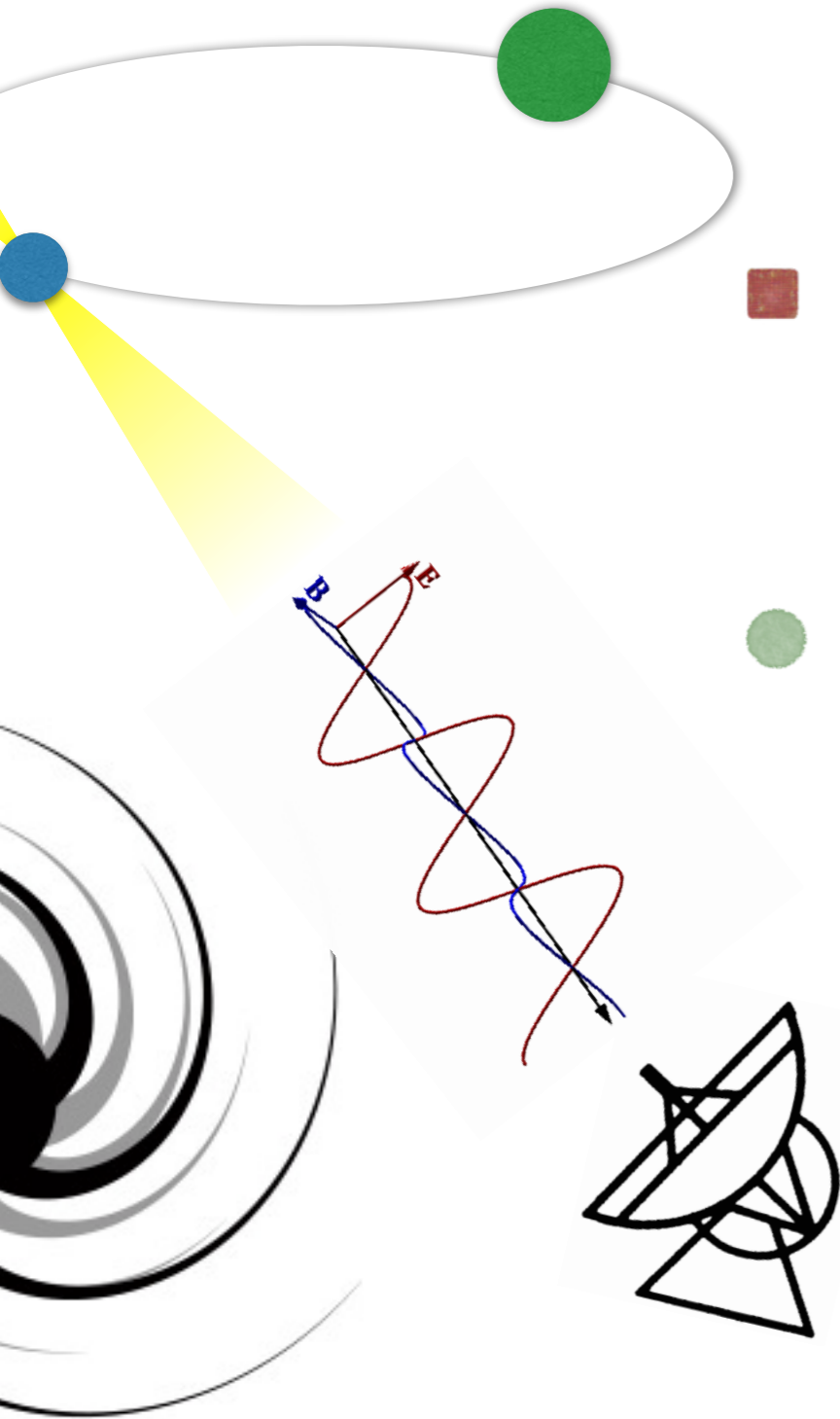
Caputo, Sberna, Frias, DB, Pani, Shao, Yan 1902.02695

using signals from pulsars



Conclusions

- The signals from pulsars can test new physics at production, propagation, detection
- WIMPS at the binary location modifies the orbits but hard to measure
- ULDM has better chances: rich phenomenology **coherent oscillations, large density gradients**
 - Pure gravity case out of reach
 - Case of DM-Matter interaction generates best constraints for certain DM models



Future work

- Detailed analysis of specific systems
- Study the effects in populations (not instantaneously)
- DM substructure with large over-densities
- Other interactions (torques?)
- Other effects related to propagation or at production

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- Other effects related to propagation or at production
- P. Freire: “Nature has always been good pulsar timing”

SKA, MeerKAT, FAST,...: new observations may bring new surprises!