



# Theory

(flavour and lattice)

**the latest news**

Aoife Bharucha, CPT Marseille

Séminaire thématique GT01 "Physique des particules"

Prospectives nationales 2020-2030.

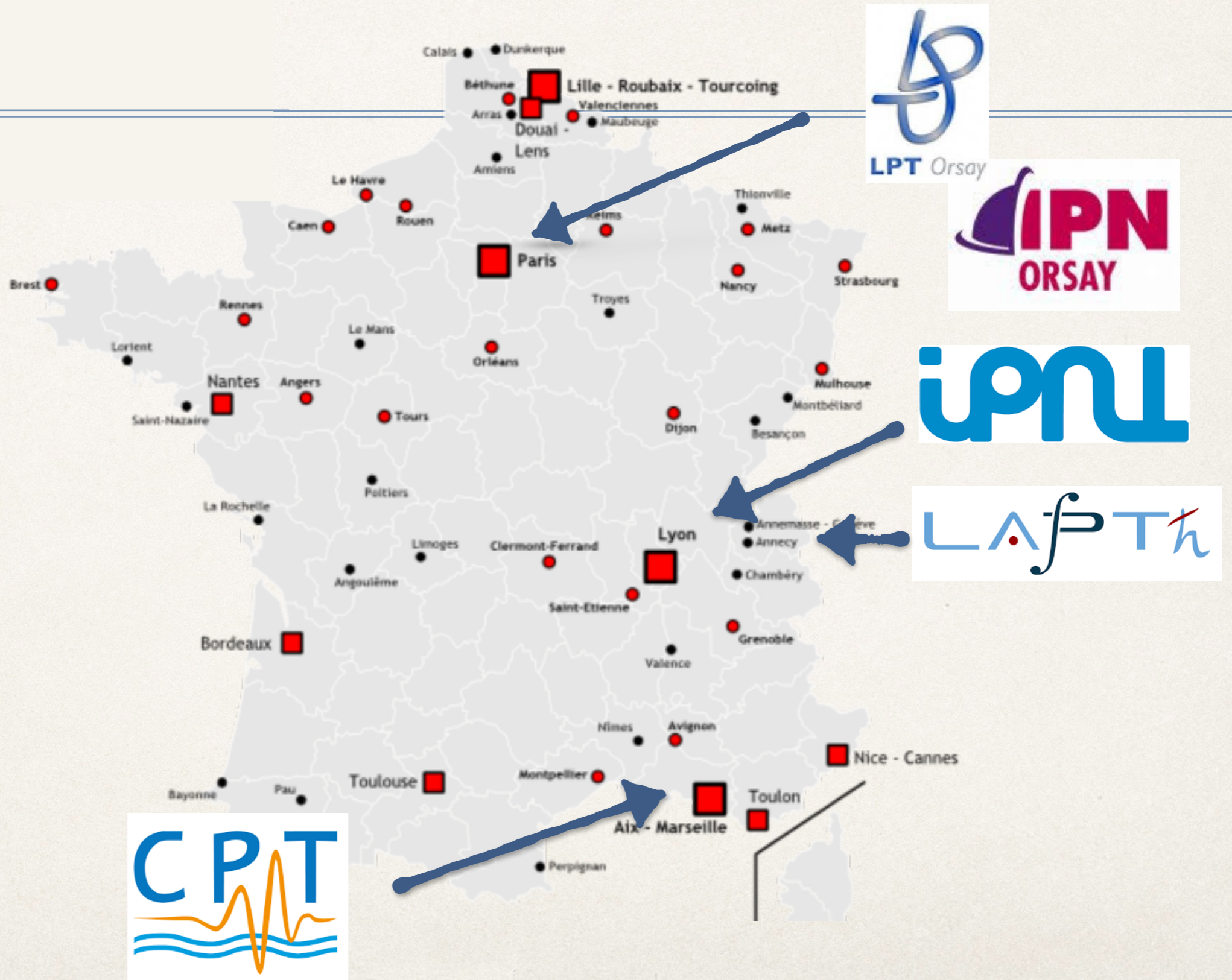
13/3/2020

# Overview

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- ❖ Neutral currents searches for BSM
- ❖ Charged currents / high precision CKM
- ❖  $(g-2)_\ell$
- ❖ Further Lattice QCD activities

# Neutral current BSM searches



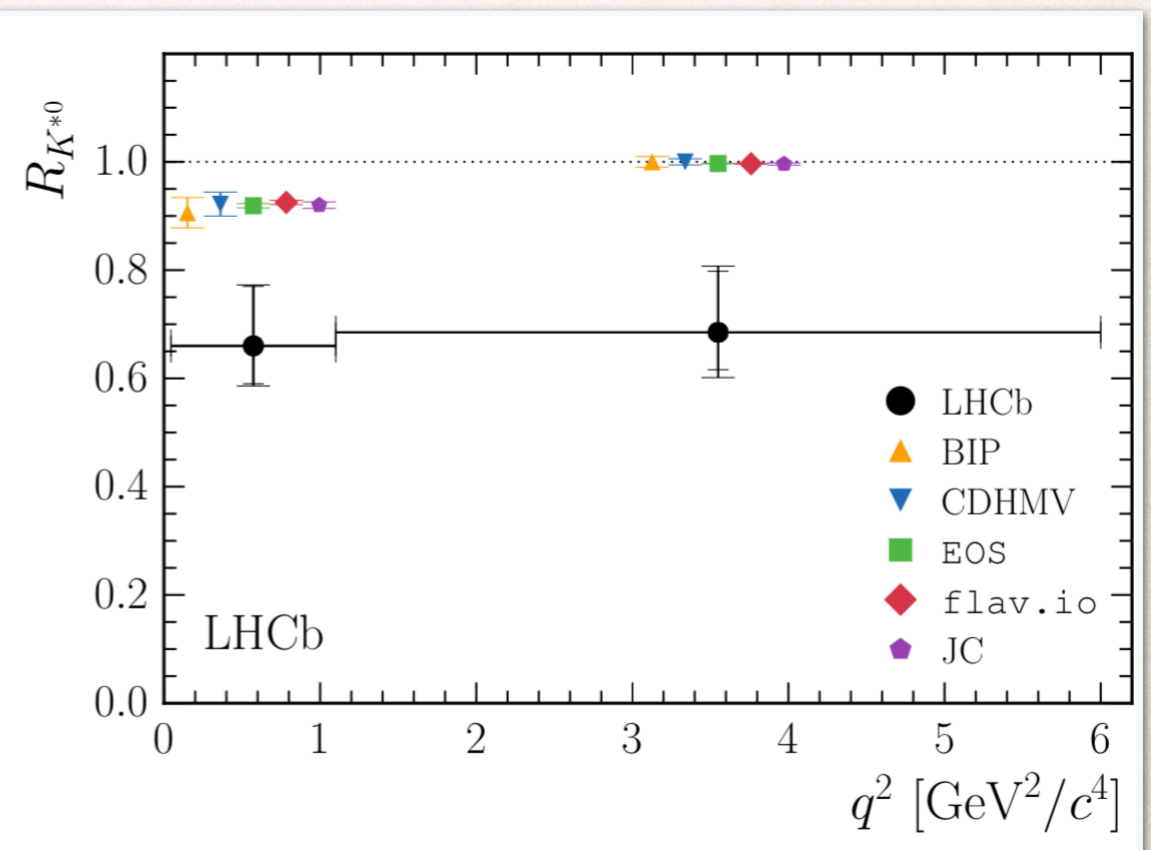
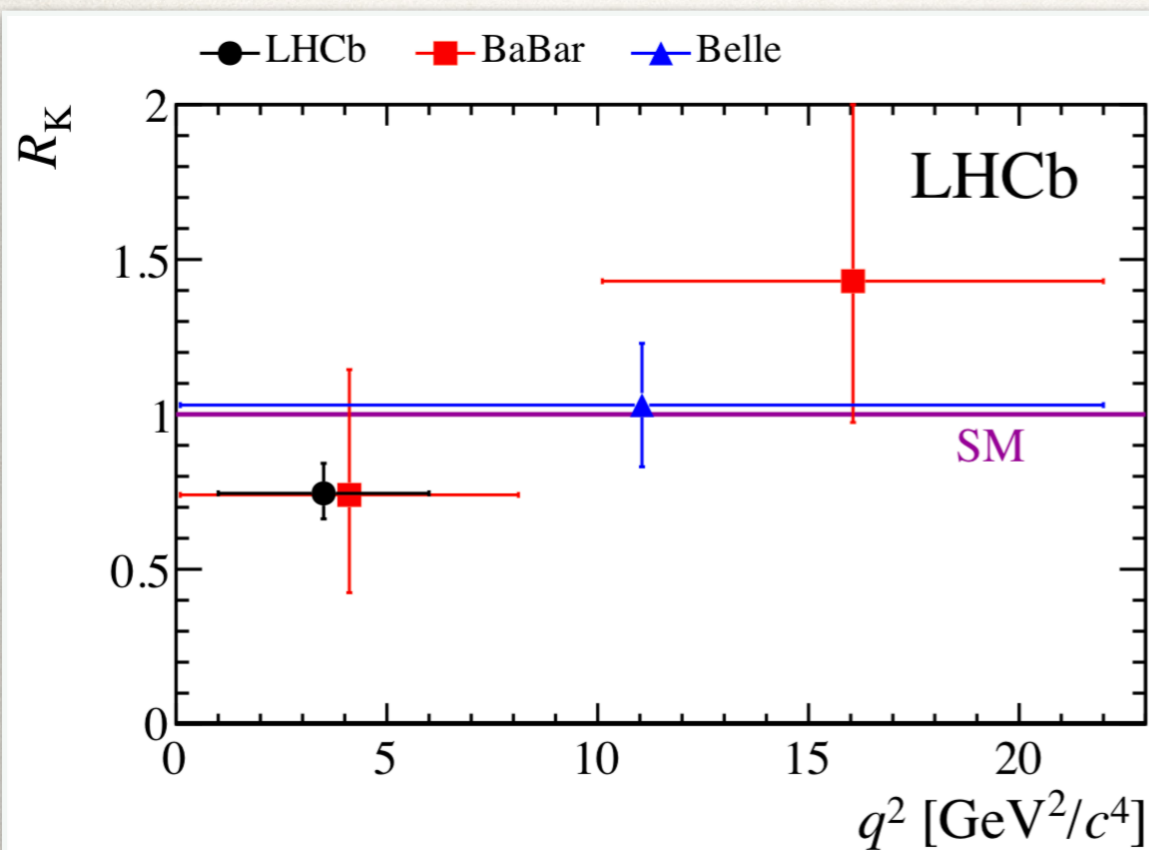
# History of the anomalies part I:

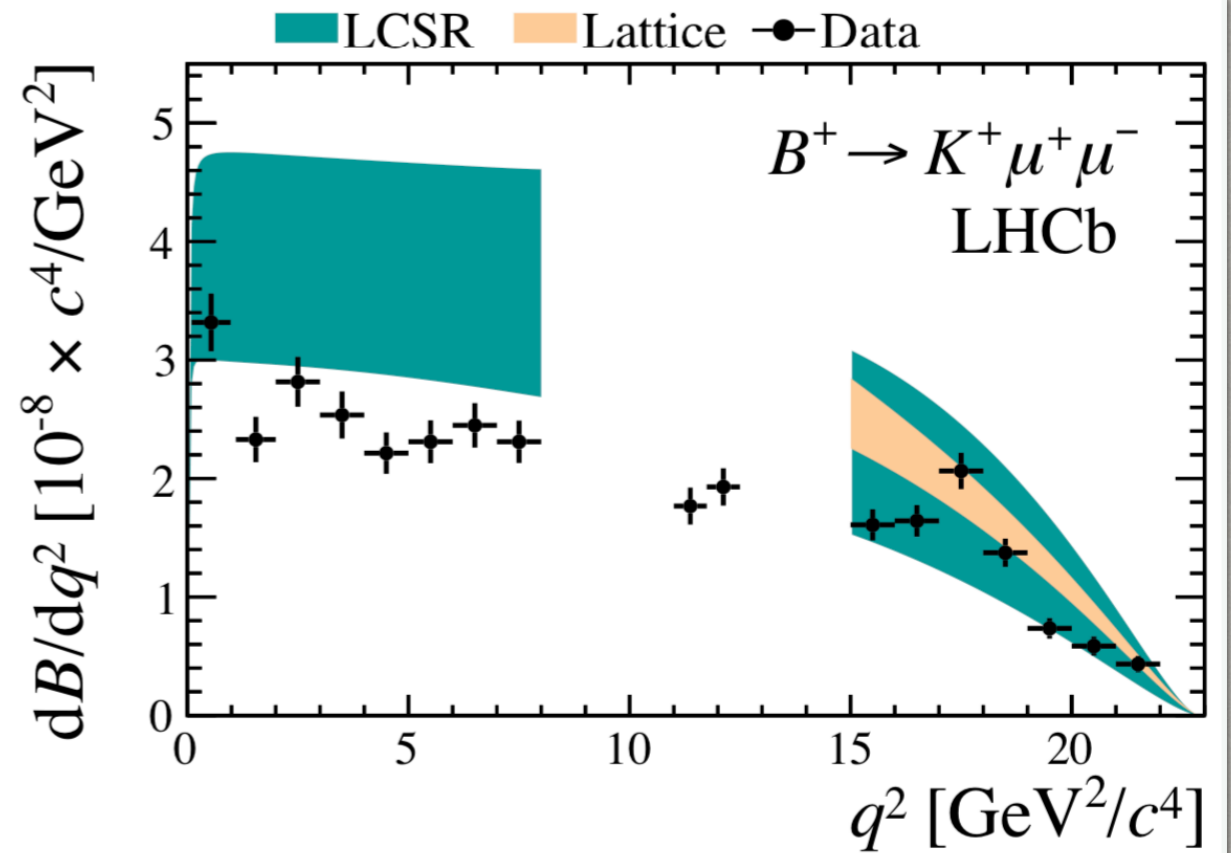
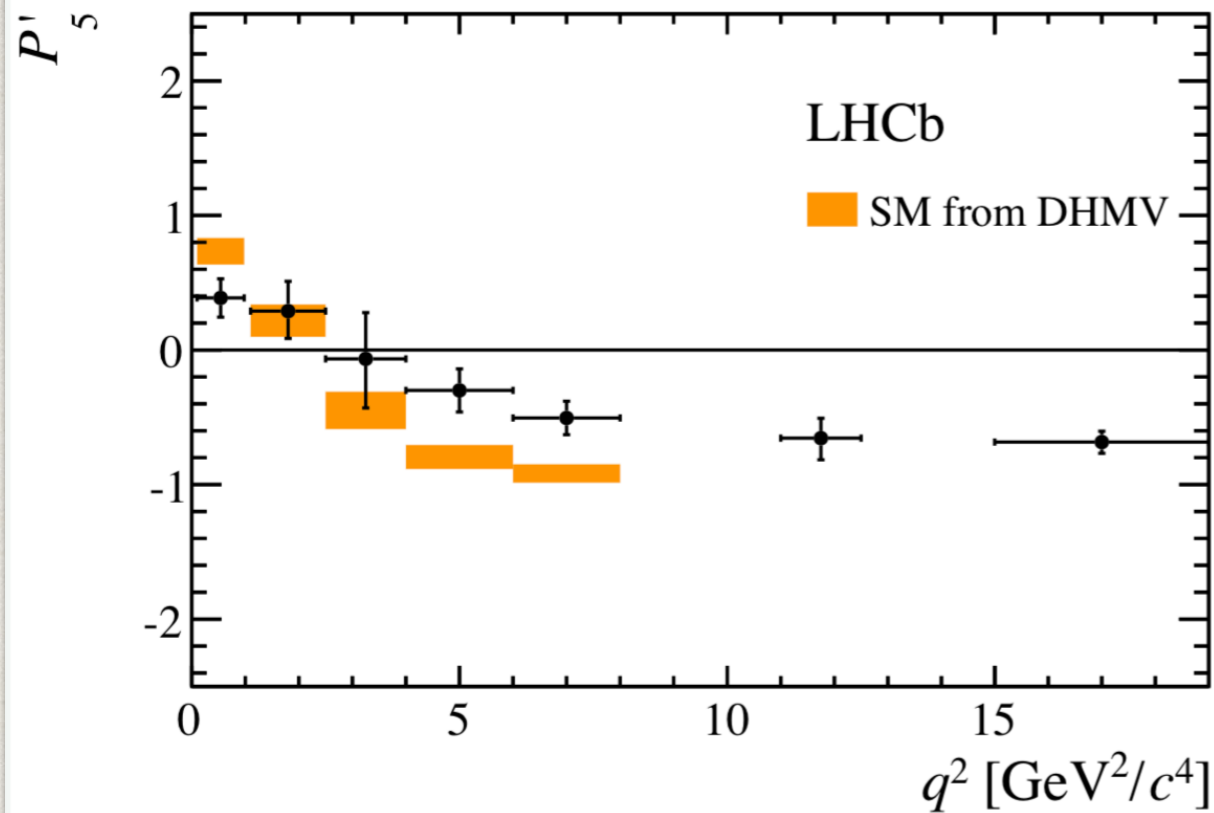
Several LHCb measurements deviate from Standard model (SM) predictions by 2-3 $\sigma$

Measurements of lepton flavour universality (LFU) ratios  $R_K$  and  $R_{K^*}$  showed deviations from SM by about 2.5 $\sigma$  each.

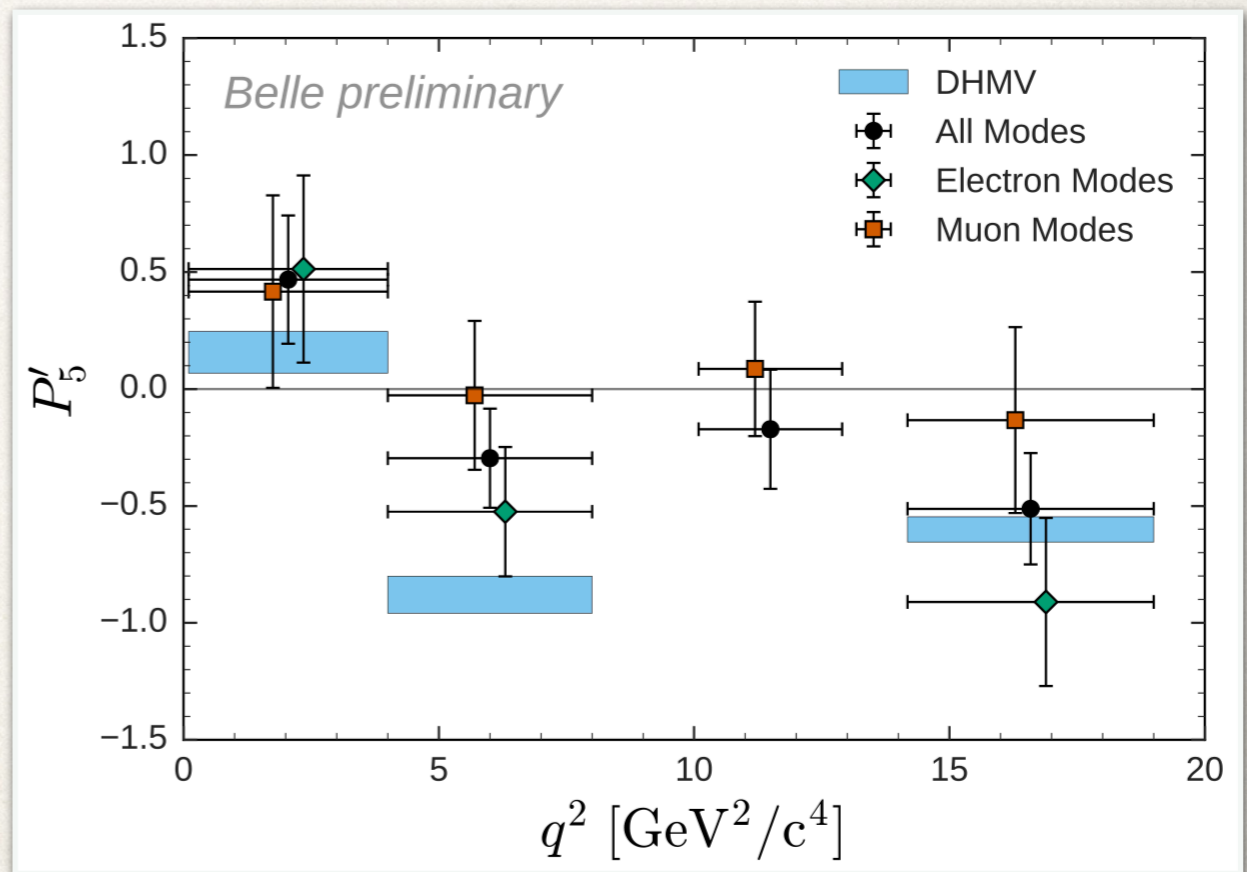
[LHCb [arXiv:1406.6482](#), [arXiv:1705.05802](#)]

$$R_{K^{(*)}} = \frac{\mathcal{B}(B \rightarrow K^{(*)} \mu^+ \mu^-)}{\mathcal{B}(B \rightarrow K^{(*)} e^+ e^-)}$$



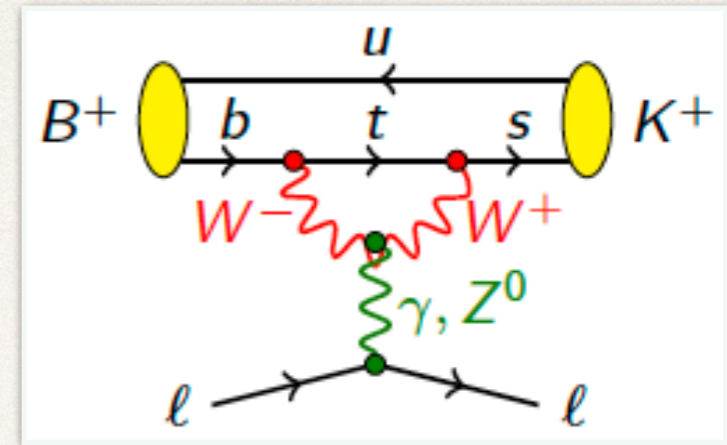


- ❖ Angular observable  $P'_5$  in  $B \rightarrow K^* \mu^+ \mu^-$ :
  - 2013:  $1\text{fb}^{-1}$  LHCb found  $3.7\sigma$ .
  - 2015:  $3\text{fb}^{-1}$  LHCb found  $3\sigma$  in 2 bins [[arXiv:1512.04442](#)]
  - 2016: Belle found a similar result in the bin
- ❖ LHCb found several tensions in the Branching ratios of  $B \rightarrow K^{(*)} \mu^+ \mu^-$  and  $B_s \rightarrow \phi \mu^+ \mu^-$  [[arXiv:1403.8044](#), [arXiv:1506.08777](#), [arXiv:1606.04731](#)]



# Introduction to FCNC processes

$$B \rightarrow K l^+ l^-$$

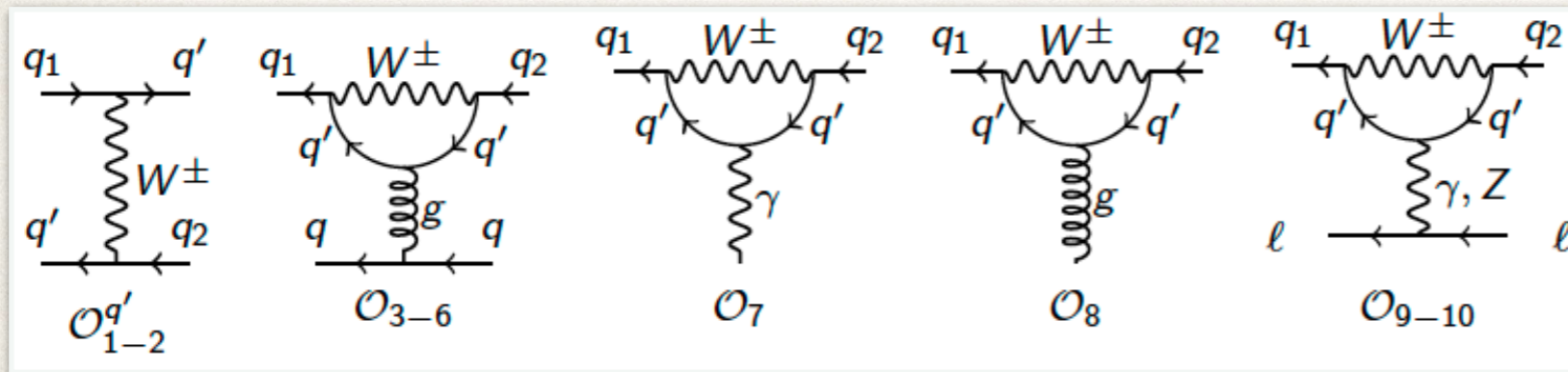


$$d\Gamma \propto \underbrace{|\langle K^* l l | \mathcal{H} | B \rangle|^2}_{\text{decay amplitude}} \underbrace{d\Phi}_{\text{phase space factor}}$$

$$\langle K^* l l | \mathcal{H} | B \rangle \sim \langle K^* l l | \mathcal{H}_{\text{eff}} | B \rangle = \frac{G_F}{\sqrt{2}} \sum_i C_i \underbrace{\langle K^* l l | \mathcal{O}_i | B \rangle}_{\text{matrix element}}$$

$$\mathcal{H}_{\text{eff}} = \frac{G_F}{\sqrt{2}} \sum_i C_i \mathcal{O}_i$$

Operator basis:



Focus on:

$$\mathcal{O}_{9l} = \frac{e^2}{16\pi^2} (\bar{s} \gamma_\mu P_L b) (\bar{l} \gamma^\mu l)$$

$$\mathcal{O}_{10l} = \frac{e^2}{16\pi^2} (\bar{s} \gamma_\mu P_L b) (\bar{l} \gamma^\mu \gamma_5 l)$$

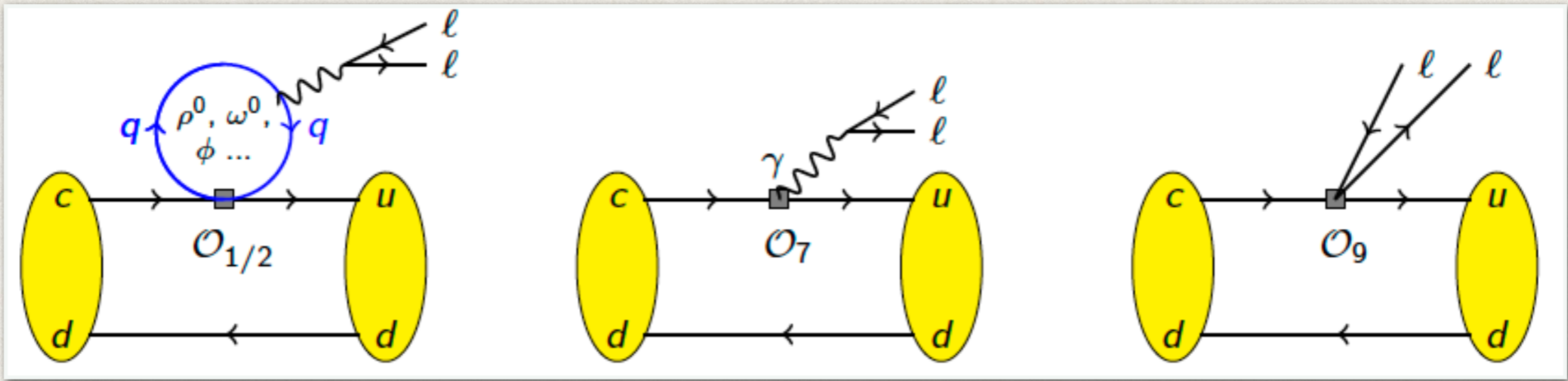
Factorization:

$$\langle l l K^* | \mathcal{O}_i | B \rangle \sim \langle l l | j_\ell | 0 \rangle \cdot \underbrace{\langle K^* | j_q | B \rangle}_{FF(q^2)} + \text{Resonances} + \text{QCDF corrections}$$

$$\mathcal{O}_i = j_q \cdot j_\ell$$

Form Factors calculated in LCSR [AB, Straub, Zwicky

arXiv:1503.05534] or LQCD [Horgan et al arXiv:1310.3887]

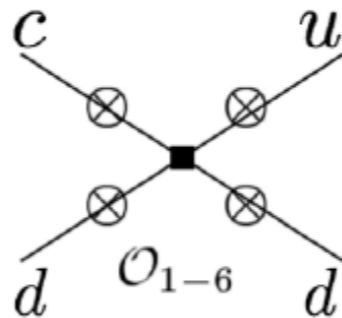


Naive factorization (leading order):  $\langle ll\pi | \mathcal{O}_i | D \rangle \sim \langle ll | j_\ell | 0 \rangle \cdot \underbrace{\langle \pi | j_q | D \rangle}_{FF(q^2)}$

QCDf (NLO):  $\langle \pi ll | \mathcal{H}_{\text{eff}} | D \rangle \sim P(s) f f(s) + \underbrace{\phi_D}_{\text{LCDA}} \otimes \underbrace{T(s)}_{\text{pert. QCD}} \otimes \phi_\pi + \mathcal{O}\left(\frac{\Lambda_{\text{QCD}}}{m_c}\right)$

At LO in  $\alpha_s$ :

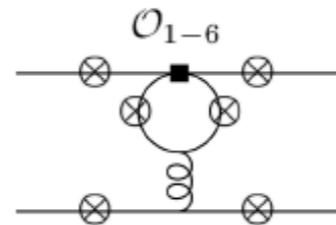
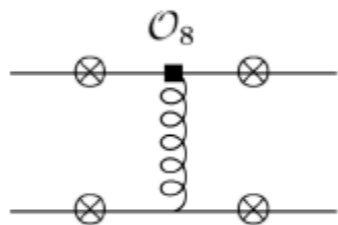
- Annihilation



$\otimes$ : possible insertion of a virtual photon line.

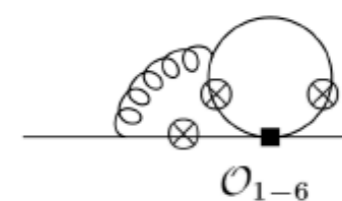
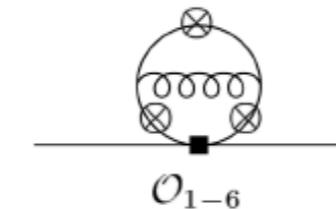
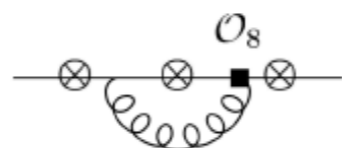
At NLO in  $\alpha_s$ :

- Spectator Scattering



Diagrams taken from [Beneke, Feldmann, Seidel/arXiv 0106067]

- Form Factors



# Observables: What is $P'_5$ ??

$$\frac{d^4\Gamma}{dq^2 d\cos\theta_l d\cos\theta_{K^*} d\phi} = \frac{9}{32\pi} I(q^2, \theta_l, \theta_{K^*}, \phi) \quad \leftarrow \text{Differential Decay rate}$$

$$I_1^s \sin^2 \theta_K + I_1^c \cos^2 \theta_K + (I_2^s \sin^2 \theta_K + I_2^c \cos^2 \theta_K) \cos 2\theta_l + I_3 \sin^2 \theta_K \sin^2 \theta_l \cos 2\phi \\ + I_4 \sin 2\theta_K \sin 2\theta_l \cos \phi + I_5 \sin 2\theta_K \sin \theta_l \cos \phi + (I_6^s \sin^2 \theta_K + I_6^c \cos^2 \theta_K) \cos \theta_l \\ + I_7 \sin 2\theta_K \sin \theta_l \sin \phi + I_8 \sin 2\theta_K \sin 2\theta_l \sin \phi + I_9 \sin^2 \theta_K \sin^2 \theta_l \sin 2\phi$$

$$S_i^{(a)} = \left( I_i^{(a)} + \bar{I}_i^{(a)} \right) / \frac{d(\Gamma + \bar{\Gamma})}{dq^2} \quad \leftarrow \text{Set of CP averaged angular observables}$$

[Ball, AB et al  
arXiv:0811.1214]

$$S_5 = -\frac{4}{3} \left[ \int_{\pi/2}^{3\pi/2} - \int_0^{\pi/2} - \int_{3\pi/2}^{2\pi} \right] d\phi \left[ \int_0^1 - \int_{-1}^0 \right] d\cos\theta_K \frac{d^3(\Gamma - \bar{\Gamma})}{dq^2 d\cos\theta_K d\phi} / \frac{d(\Gamma + \bar{\Gamma})}{dq^2}$$

$$P'_5 = \frac{S_5}{\sqrt{-S_2^c(1 + S_2^c)}}$$

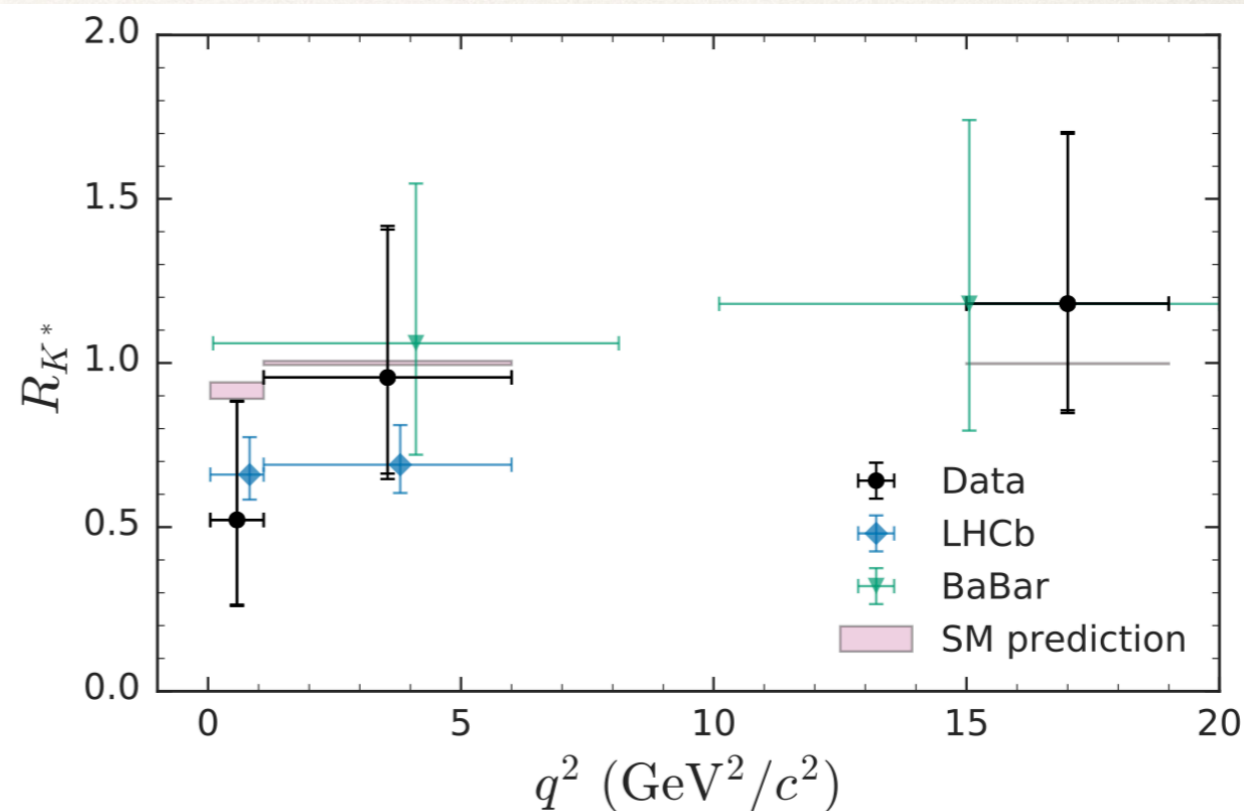
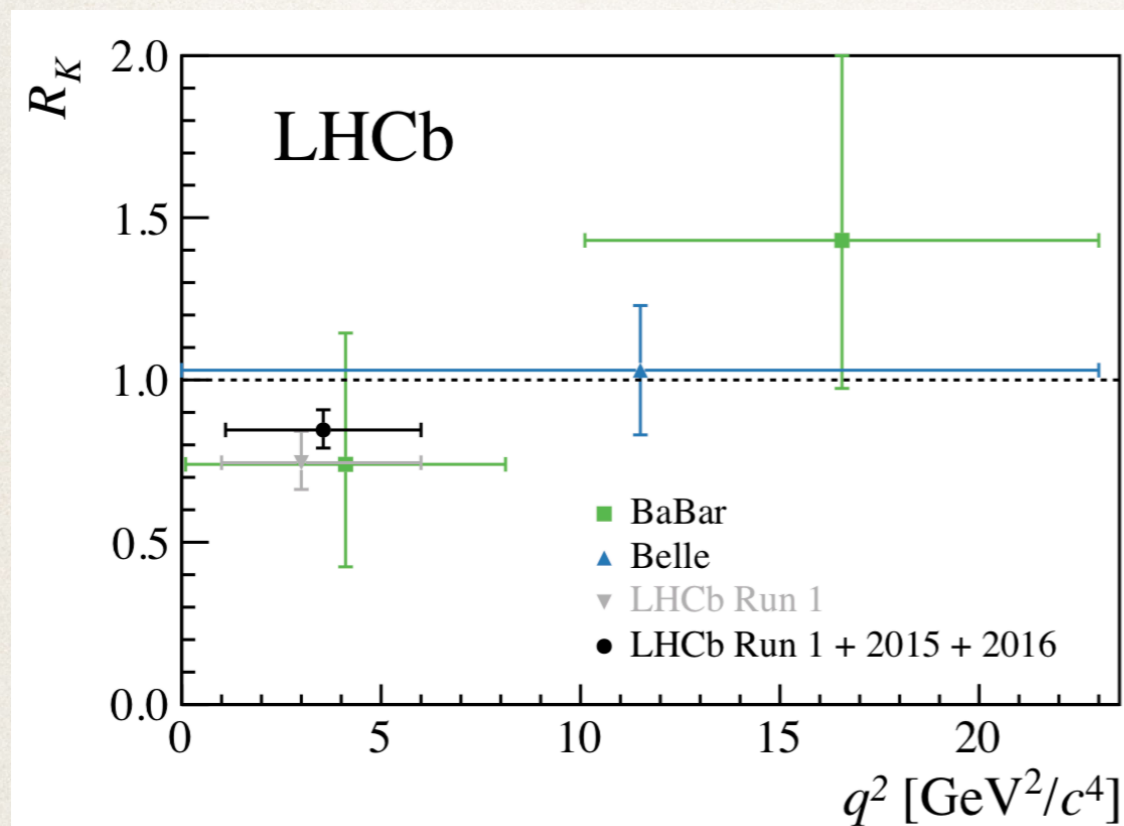
“Optimised” observables to  
minimise the hadronic  
dependence and maximise  
experimental sensitivity

[Descotes-Genon  
et al arXiv:  
1207.2753]



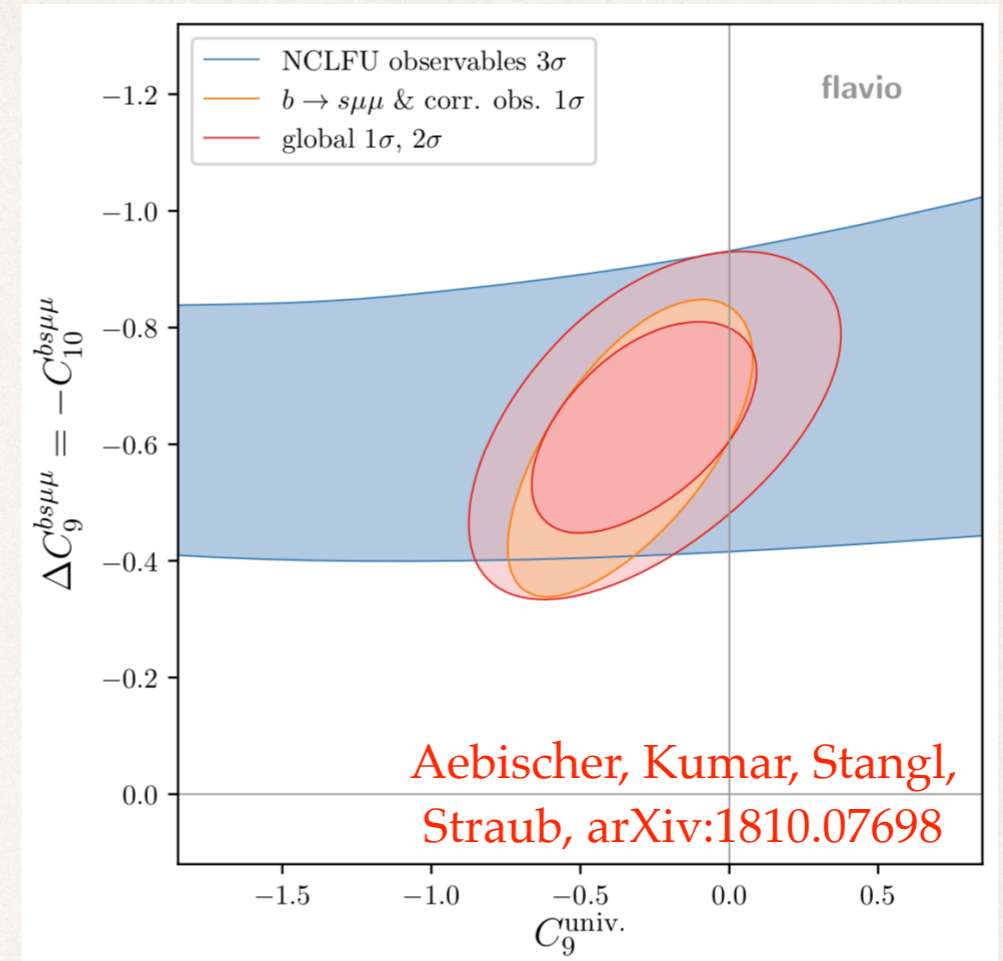
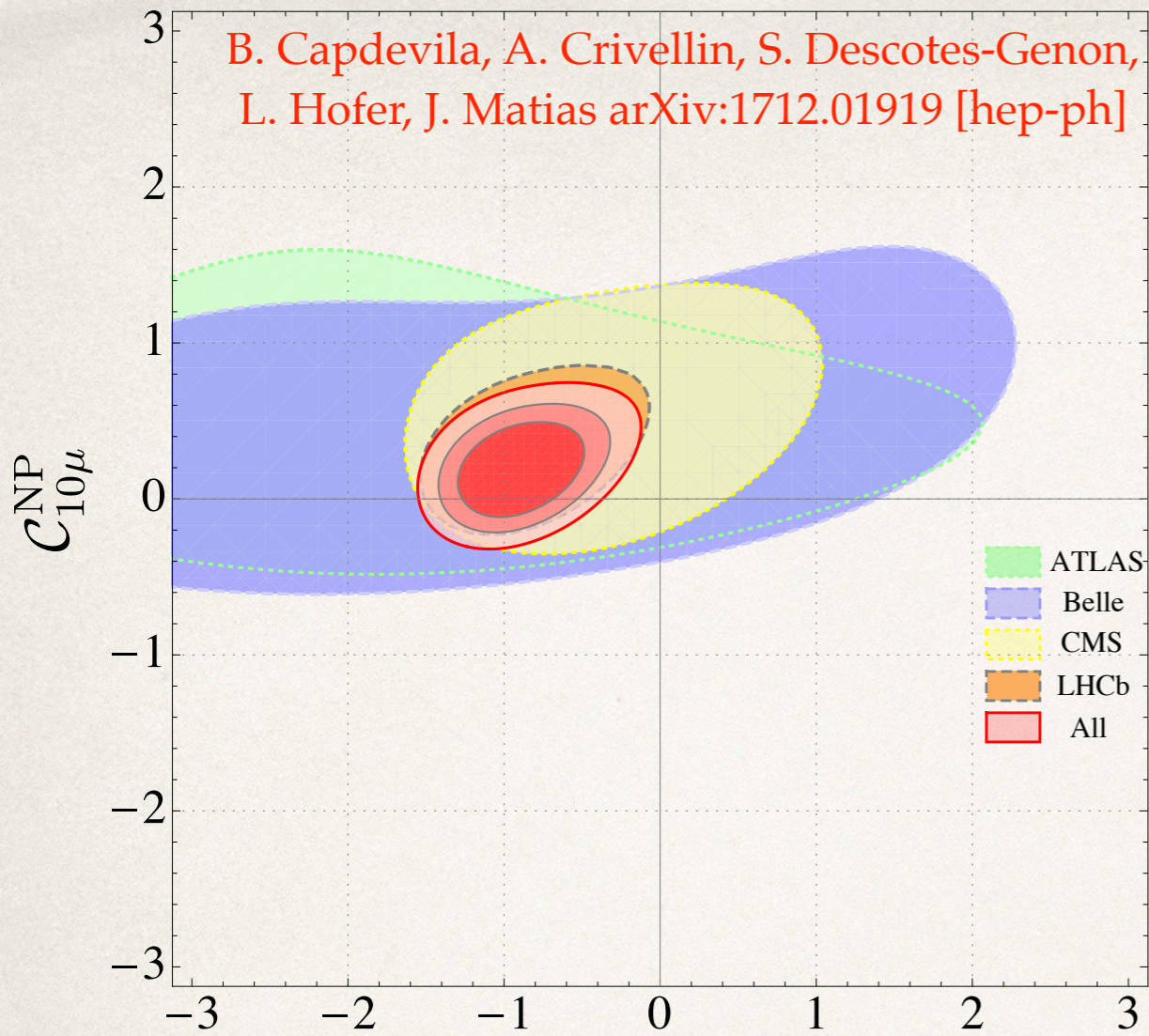
# Update from Moriond 2019

- ❖ Updated measurement of  $R_K$  by LHCb [[LHCb, arXiv:1903.09252](#)]
- ❖ New measurement of  $R_{K^*}$  by Belle [[Belle, arXiv:1904.02440](#)]

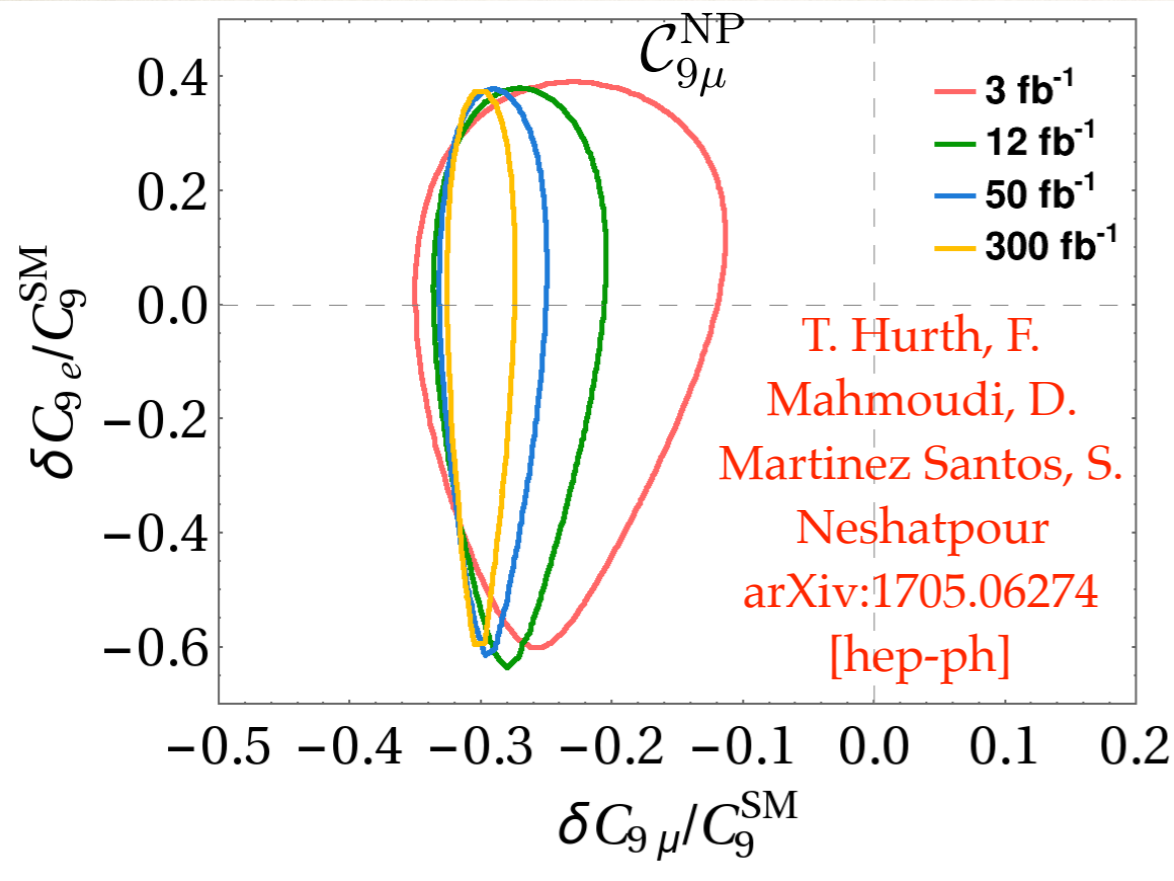


# Global fits for BSM

B. Capdevila, A. Crivellin, S. Descotes-Genon,  
L. Hofer, J. Matias arXiv:1712.01919 [hep-ph]



Aebischer, Kumar, Stangl,  
Straub, arXiv:1810.07698



T. Hurth, F. Mahmoudi, D. Martinez Santos, S. Neshatpour  
arXiv:1705.06274 [hep-ph]

Introduce univ. NP contribution in  $C_9$

$$C_9^{bsee} = C_9^{\text{univ}}$$

$$C_{10}^{bsee} = 0$$

$$C_9^{bs\mu\mu} = C_9^{\text{univ}} + \Delta C_9^{bs\mu\mu}$$

$$C_{10}^{bs\mu\mu} = -\Delta C_9^{bs\mu\mu}$$

$$C_9^{bs\tau\tau} = C_9^{\text{univ}}$$

$$C_{10}^{bs\tau\tau} = 0$$

Software development and statistical analysis (N Mahmoudi):

Need to include RGE running from UV scale to mb (SMEFT): non-trivial issues e.g. operator mixing / large logs. Need automated methods to reliably explore parameter space and tools to recast the constraints from LHC high- $p_T$  searches

Link to direct searches for LUV (A Iyer / B Fuks):

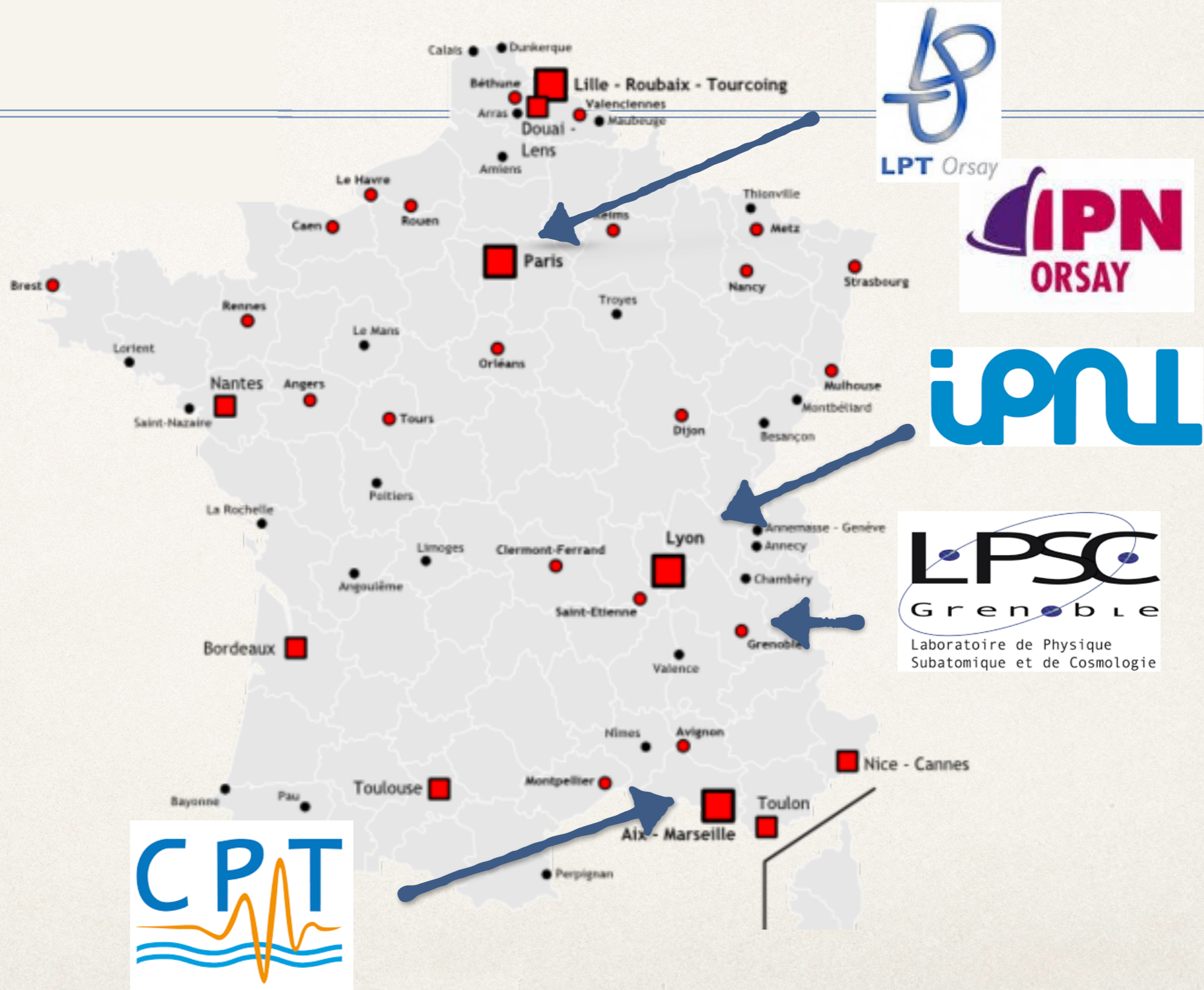
e.g. for incl.  $\ell^+\ell^-$  measurements, acceptance and reconstruction efficiencies important, to separate 'physical' non-universality, induced by different couplings, from the detector-induced LFUV

# Future prospects

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- ❖ Main challenge comes from hadronic effects in QCD: calculation of form factors via LCSR (AB,SDG) or LQCD (see later); additional non-perturbative effects when factorization breaks down due to hadronic (charmonium) contributions to the quark loop mediating the decay.
- ❖ Form factors for the non-resonant channels (e.g.  $B \rightarrow K\pi$ ) which contribute to the background [Sébastien Descotes-Genon et al arXiv:1908.02267 [hep-ph]].
- ❖ Study as many related channels as possible, e.g. baryon decays [S. Descotes-Genon, M. Novoa Brunet, arXiv:1903.00448 [hep-ph]] subject of GDR workshop (b-baryon fest, 14-15 May 2020, IJCLab Orsay) or  $D \rightarrow \pi \ell \ell$  [AB, Diogo Boito, Cedric Méaux, to appear] Improve global analyses (Sebastien Descotes-Genon)
- ❖ B decays with  $\tau(s)$  in the final state (Exp/theory network in France being established including AB, Damir Becirevic, Jérôme Charles, Sebastien Descotes-Genon)/studying  $\tau$  decays (Sebastien Descote-Genon, Emi Kou)
- ❖  $b \rightarrow s \gamma$  photon polarisation measurement with  $B \rightarrow K \pi \pi \gamma$  angular distribution (Emi Kou in collaboration with Belle II-LAL, writing MC generator with many kaonic resonances)
- ❖ Theory predictions for  $B_s \rightarrow \gamma \ell \ell$  [Diego Guadanoli]
- ❖ Non-factorisable contribution to the radiative  $B \rightarrow K_{\text{res}} \gamma$  ( $K_{\text{res}}$  being the kaonic resonance) to compute charm penguin effects to the photon polarisation measurement (Emi Kou in collaboration with D. Melikhov (Moscow) and H. Sazdjian (IJCLab)),

# Charged currents-high precision CKM



# History of the anomalies part II:

## Charged Current anomalies

### ❖ B-factory measurements with leptonic $\tau$ decays:

- BaBar: 2D fit [PRD 88, 072012 (2013)]  $R_D = 0.440 \pm 0.058 \pm 0.042$   $R_{D^*} = 0.332 \pm 0.024 \pm 0.018$

- Belle: simultaneous 1D fits [PRD 92, 072014 (2015)]  $R_D = 0.375 \pm 0.064 \pm 0.029$   $R_{D^*} = 0.293 \pm 0.038 \pm 0.015$

### ❖ LHCb measurements with muonic $\tau$ decays:

-  $R_{D^*} = 0.336 \pm 0.027 \pm 0.030$  [PRL 115, 112001 (2015)]

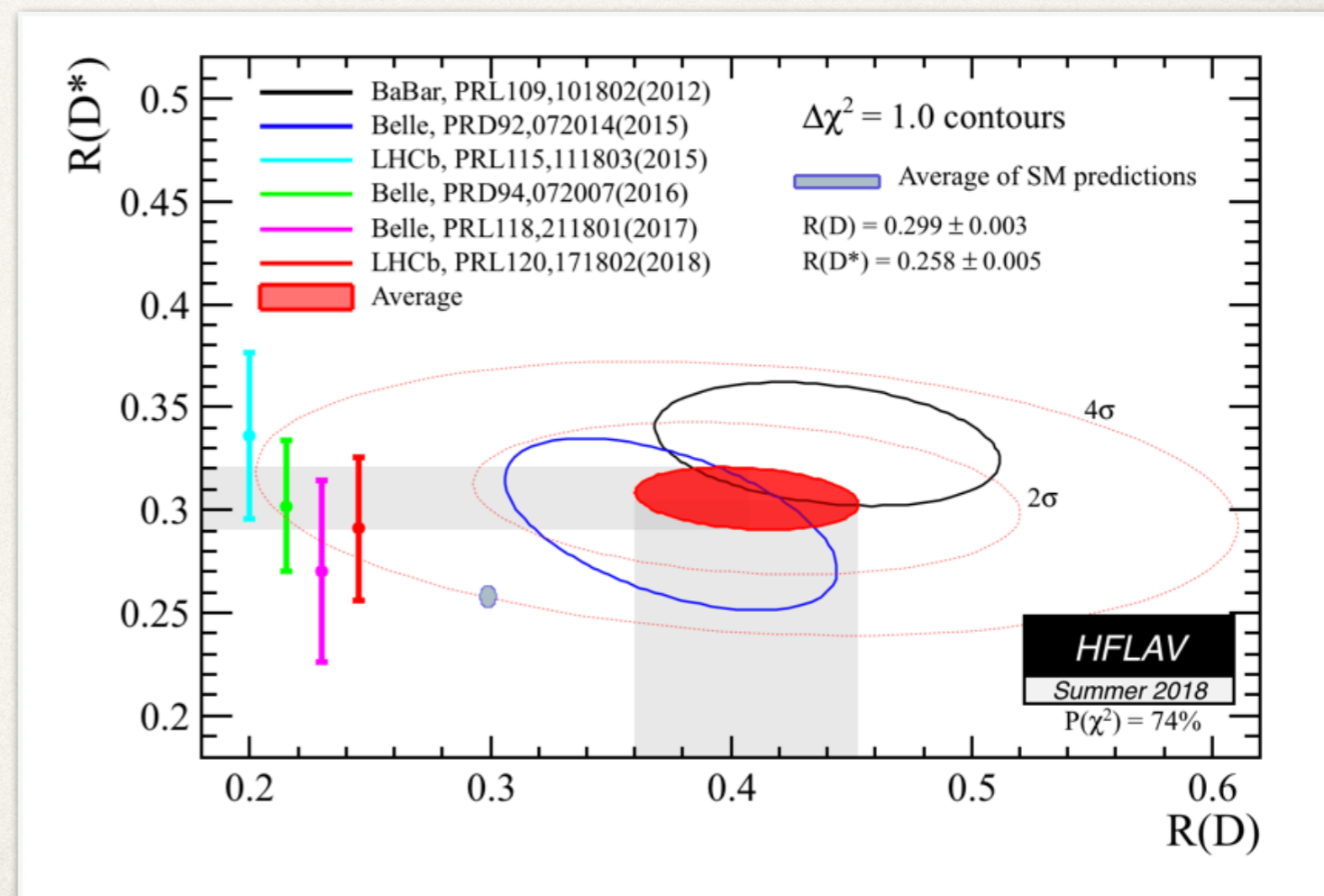
-  $R_{J/\psi} = 0.71 \pm 0.17 \pm 0.18$  [PRL 120, 121801 (2018)]

### ❖ Measurements with hadronic $\tau$ decays

- Belle  $R_{D^*}$  1-prong [PRL 118, 211801 (2017)] [PRD 97, 012004 (2018)]  $R_{D^*} = 0.270 \pm 0.035 + 0.028$

- LHCb  $R_{D^*}$  3-prong [PRL 120, 171802 (2018)] [PRL 120, 171802 (2018)]  $R_D = 0.291 \pm 0.019 \pm 0.026 \pm 0.013$

$$R_{D^{(*)}} = \frac{\mathcal{B}(B \rightarrow D^{(*)} \tau \nu)}{\mathcal{B}(B \rightarrow D^{(*)} \ell \nu)}$$

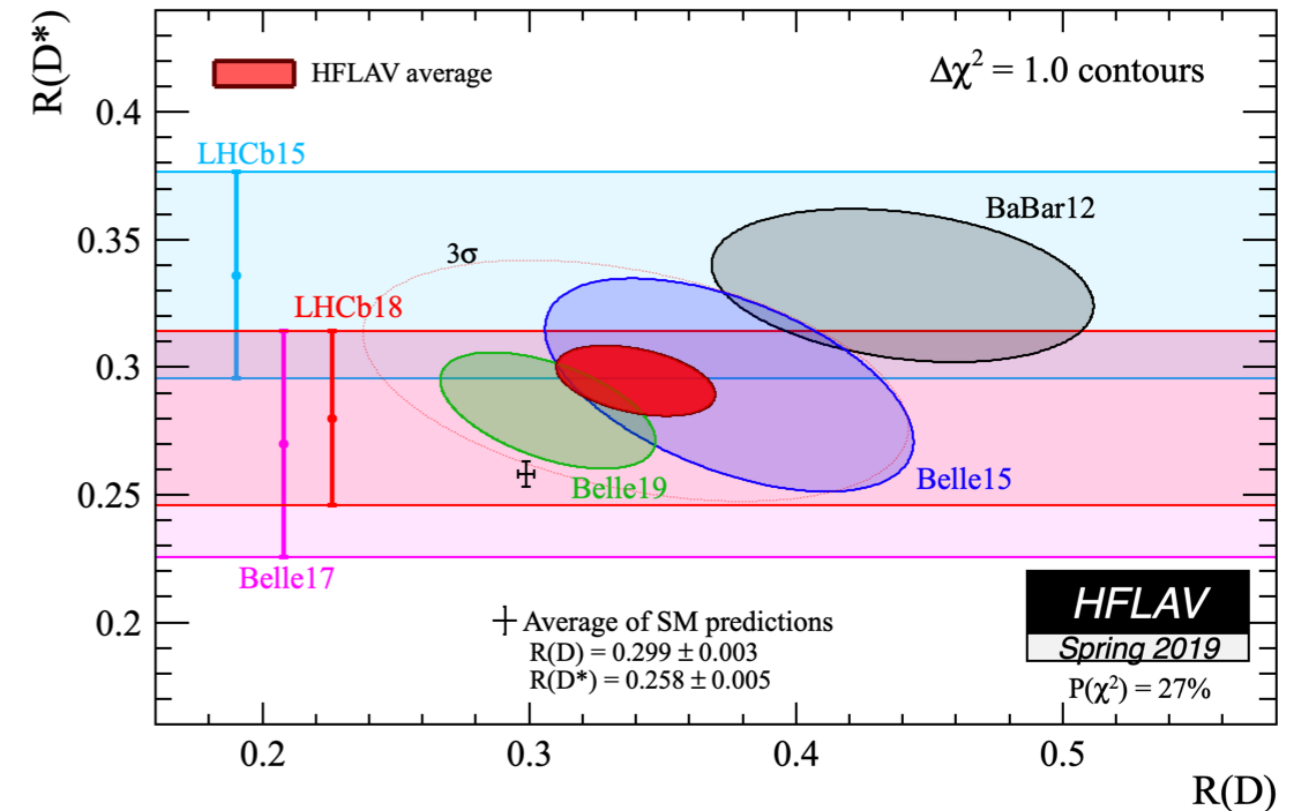


# Charged semi-leptonic processes

- ❖ The process  $B \rightarrow D^* l \nu$ , where  $l=e, \mu$  is used to measure the CKM matrix element  $V_{cb}$ , as the branching ratio is

$$\text{BR} \sim |V_{cb}|^2 |F|^2 |G_F|^2$$

- ❖ In the ratio  $R(D^*)$ , the form factor uncertainty is greatly reduced
- ❖ Huge 15% discrepancy with the SM prediction, tree-level process
- ❖ Need to be sure about SM prediction, i.e. the form factors.



Update from Belle, arXiv:1904.08794, Plot by HFLAV

$$R_{D^{(*)}} = \frac{\mathcal{B}(B \rightarrow D^{(*)} \tau \nu)}{\mathcal{B}(B \rightarrow D^{(*)} \ell \nu)}$$

- ❖ Exclusive-Inclusive discrepancy for  $V_{cb}$
- ❖ Lattice at the high  $q^2$  endpoint
- ❖ Extrapolation used to fit data
- ❖ BGI vs CLN, need more Lattice results

# Global fits including $R_D^{(*)}$

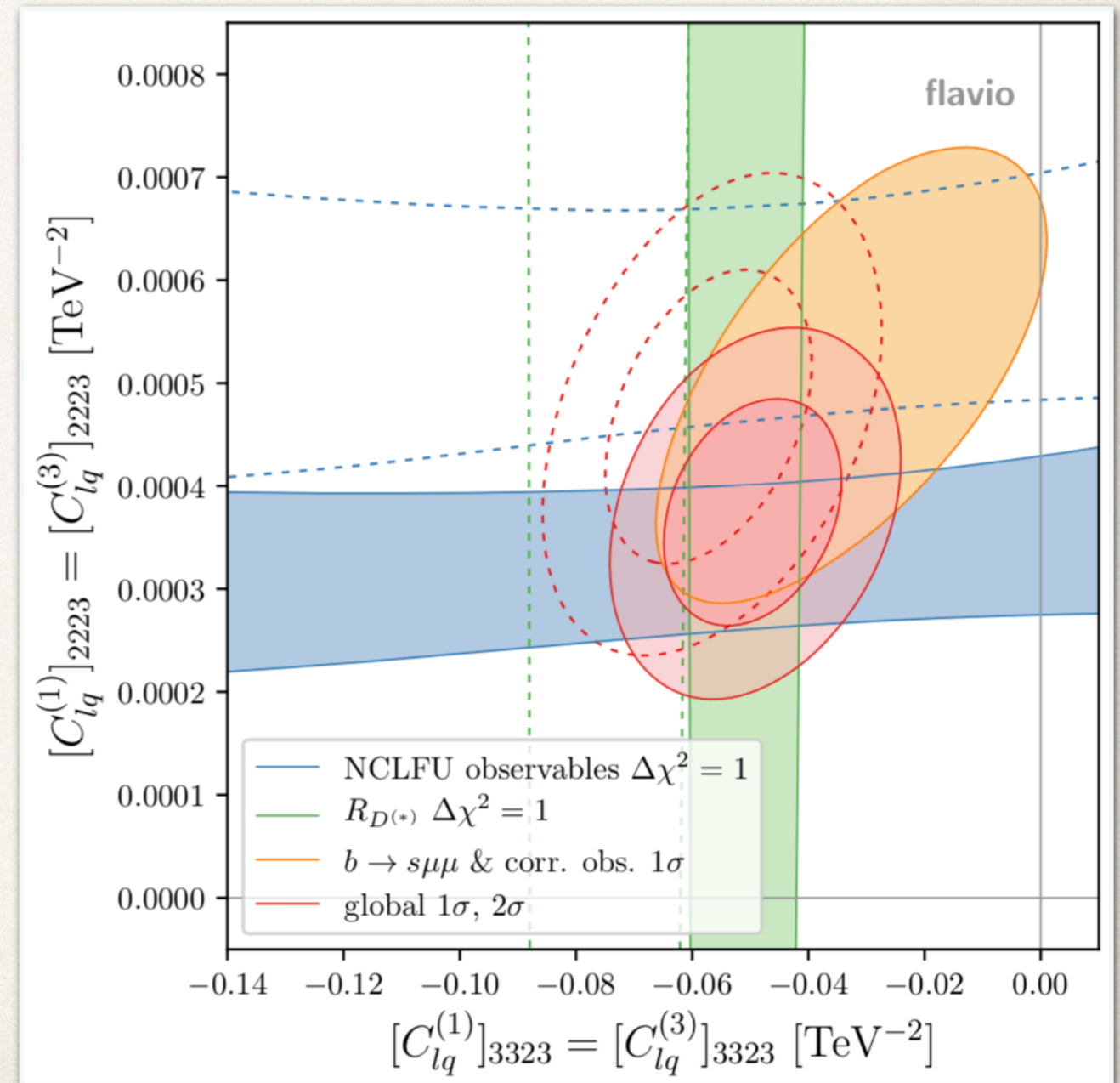
Aebischer et al, arXiv:1903.10434

The following operators with  $ii=22$  match onto  $C_9$  and  $C_{10}$  at the EW scale:

$$[O_{lq}^{(1)}]_{ii23} = (\bar{l}_i \gamma_\mu l_i) (\bar{q}_2 \gamma^\mu q_3),$$

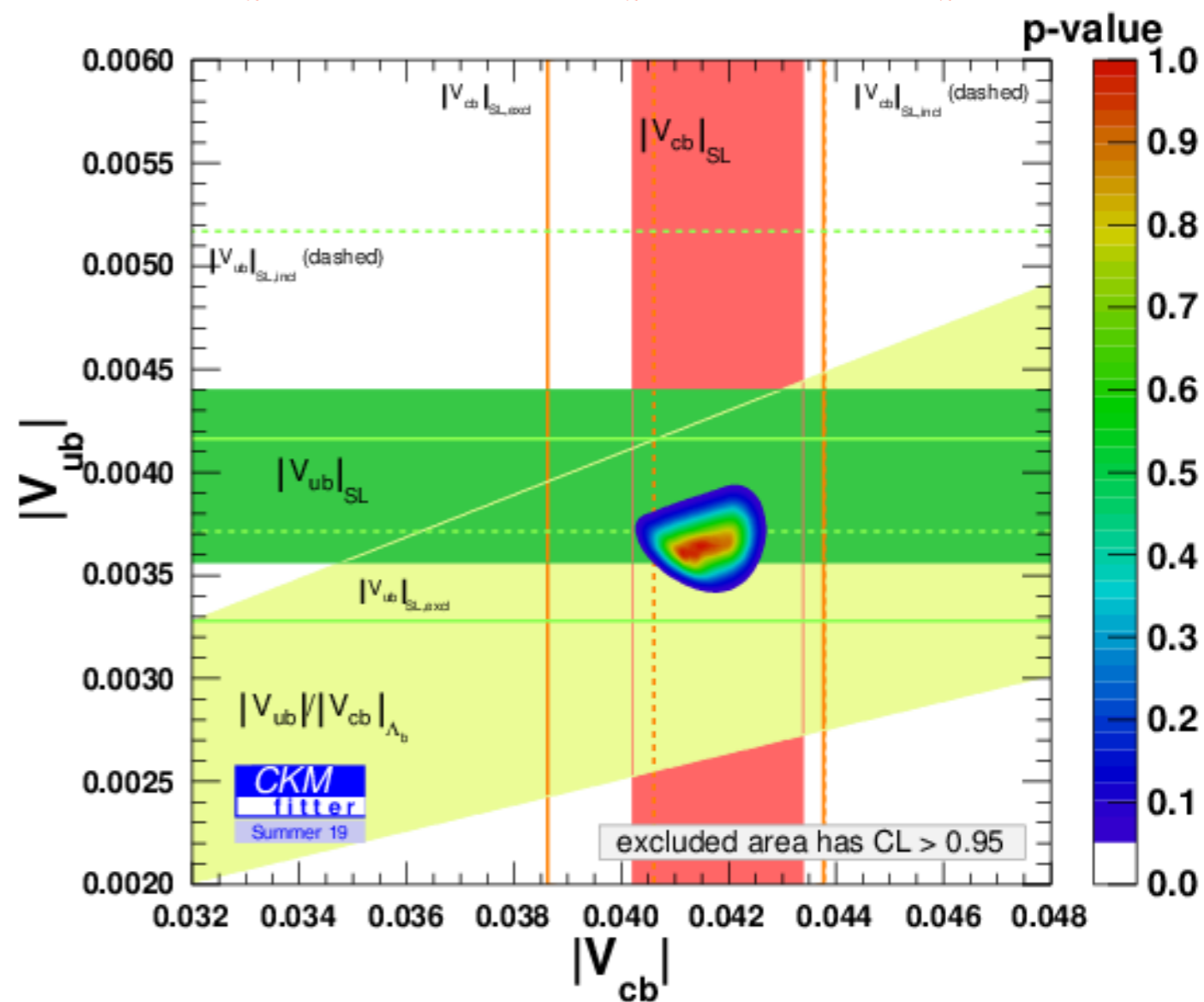
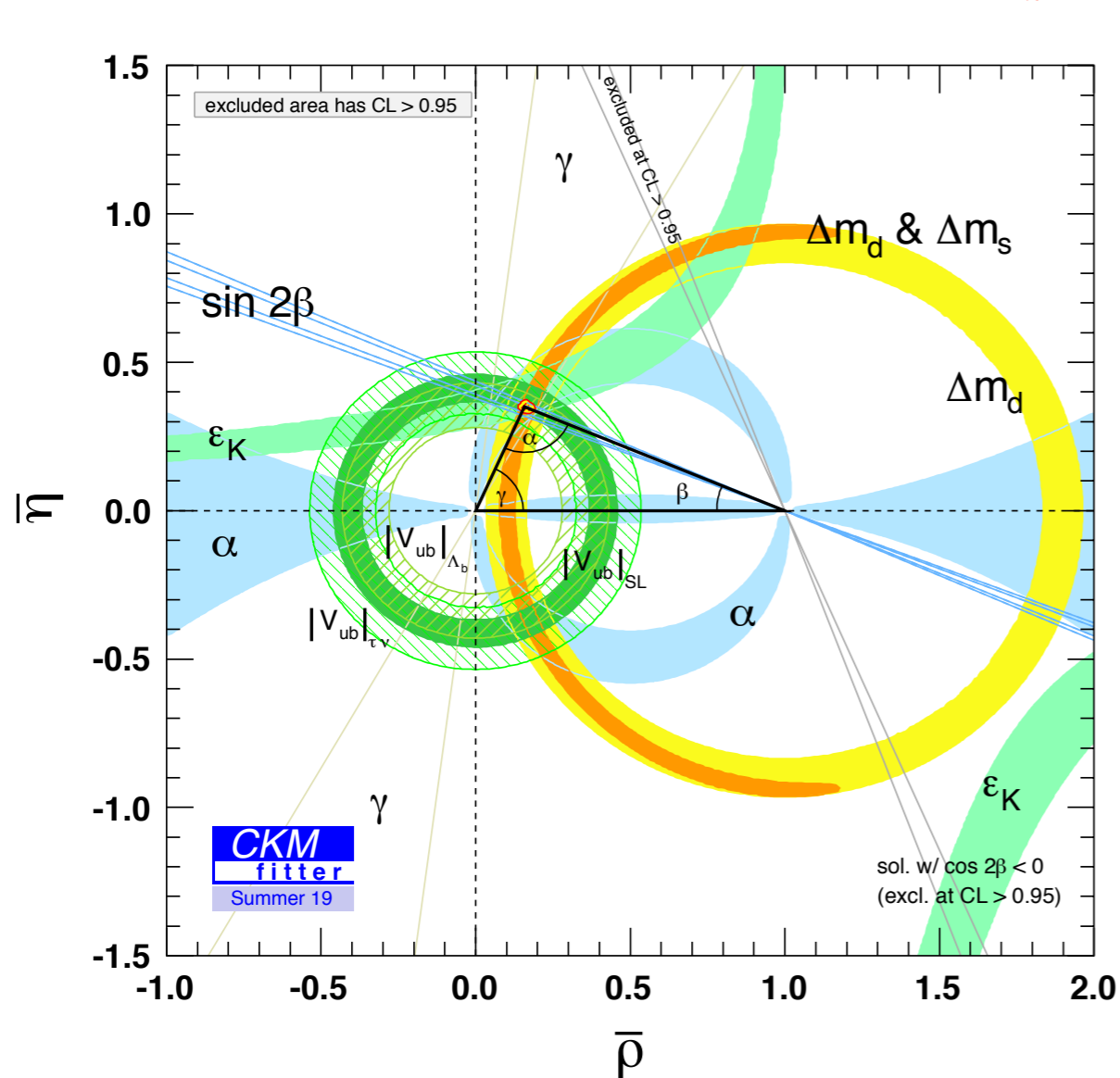
$$[O_{lq}^{(3)}]_{ii23} = (\bar{l}_i \gamma_\mu \tau^I l_i) (\bar{q}_2 \gamma^\mu \tau^I q_3)$$

- ❖ From semitauonic operators, a LFU RG contribution can be obtained by running above and below the EW scale
- ❖ The singlet/triplet Wilson coefficients should be approx. equal to avoid  $B \rightarrow K \nu \nu$  constraints
- ❖ Before Moriond best-fit point of the NCLFU and  $b \rightarrow s \mu \mu$  data was for vanishing semi-tauonic WCs
- ❖ Including the  $RK^{(*)}$  updates, this point moves to non-zero semi-tauonic WCs, as required to explain the  $R_D^{(*)}$  anomalies, with the agreement improving with the Belle 2019 update, and a pull of  $\sim 8\sigma$
- ❖ Only particle which can produce such operators: U1 LQs, transforming as  $(3,1)_{2/3}$  under the SM (Loop suppression of B mixing, Loop suppression of  $B \rightarrow K \nu \nu$ , singlet and triplet WCs are naturally equal)



# CKM Fitter results 2019

CKMfitter Group (J. Charles et al.), Eur. Phys. J. C41, 1-131 (2005) [hep-ph/0406184],  
 updated results and plots available at: <http://ckmfitter.in2p3.fr>





# Looking closer at $V_{ub}$ and $V_{cb}$

$$V_{ub} \quad |V_{cb}^{\text{excl}}| = (3.67 \pm 0.09(\text{exp}) \pm 0.12(\text{theo})) \cdot 10^{-3} \quad (\text{data} + \text{LQCD} + \text{LCSR}) \quad (\text{HFLAV 2018})$$

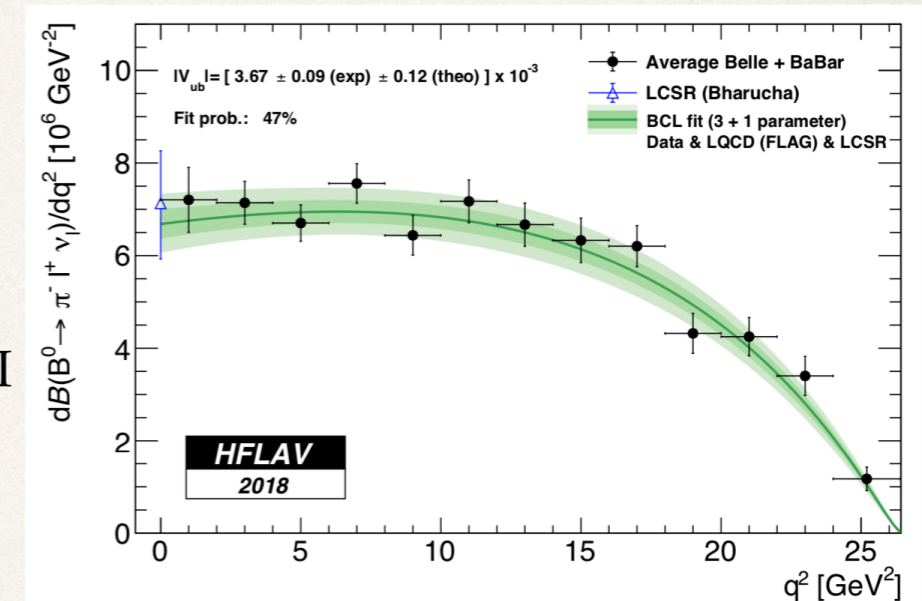
$$V_{ub} \quad |V_{cb}^{\text{excl}}| = (3.70 \pm 0.10(\text{exp}) \pm 0.12(\text{theo})) \cdot 10^{-3} \quad (\text{data} + \text{LQCD})$$

✿ Exclusive result from  $B \rightarrow \pi \ell \nu$ : LQCD and Lattice agrees well.

✿ Inclusive result:  $3 \sigma$  from excl, very model dependent, imprvs at Belle II

$$V_{cb} \quad |V_{cb}^{\text{excl}}| = 40.3(0.8) \cdot 10^{-3} \quad (\text{Bordone/Jung/vDyk'19})$$

$$V_{cb} \quad |V_{cb}^{\text{incl}}| = 42.00(64) \cdot 10^{-3} \quad (\text{Gambino, Beauty 2019})$$



✿ Including (NNLO) uncertainties properly and with more Belle/BelleII data now fits give compatible results.

Lattice FNAL-MILC and JLQCD preliminary results for FF ratio/slope, important constraint on fit. Important also for  $R(D^*)$  and  $R(D)$ .

✿ Inclusive result: Theory uncertainties dominant: further calculations in progress with aim to obtain 1% uncertainty, new observables for B factories, Lattice QCD information on local matrix elements is the next frontier

# Future Prospects

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- ❖ Aim to study the ratios linked to  $b \rightarrow c$  anomalies:  $R_{D^*_s}$ ,  $R_{J/\psi}$  and  $R_{A_b}$  (B. Blossier)
- ❖ CKM  $V_{cb}$  element determination and new physics effects in  $b \rightarrow c$  transition (Emi Kou with postdoc, KEK-lattice (JLQCD) + Belle II (Melbourne)) Form factors for particular  $b \rightarrow c$  decays,  $B \rightarrow \pi$  and  $B_s \rightarrow K$  decays in order to extract  $V_{cb}$  and  $V_{ub}$  (Antoine Gerardin/Benoit Blossier)
- ❖ Improved parameterisations for  $V_{cb}$  and  $V_{ub}$  to take into account higher order HQET contributions and combine more channels (AB, Laurent, Lellouch)
- ❖ Improved LCSR results for  $B$  to  $\pi$  and  $B_s$  to  $K$  form factors (AB)
- ❖ Probing meson DAs with  $B/D/K$  to  $3l \nu$  (AB, Marc Knecht with Emilie Passemar, Alexey Petrov)
- ❖ CKM gamma angle determination and  $D \rightarrow K\pi\pi$  decay in dispersive method (Emi Kou with B. Moussallam (IJCLab))

# LQCD input for flavour physics

Vincent Morenas, Mariane Brinet, Benoit Blossier, Antoine Gerardin, Savvas Zafeiropoulos

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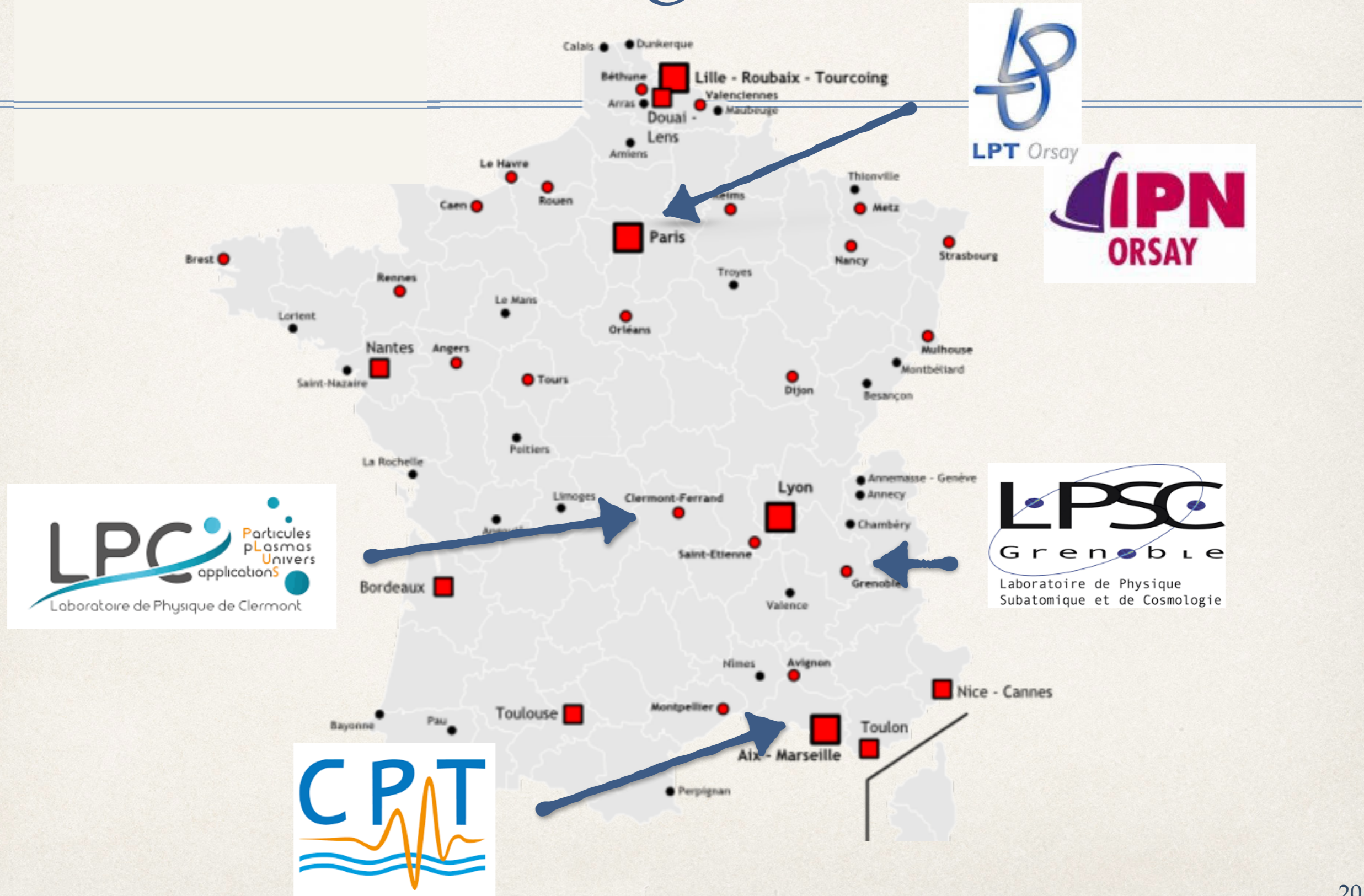
## Progress over last ten years:

- ❖ Take into account  $u=d$  quarks as well as  $s$  and  $c$  quarks in the sea (dynamical quarks).
- ❖ We can include, in our simulations, strong and electromagnetic effects of the isospin symmetry breaking.
- ❖ A wide range of observables have been computed (hadron masses, decay constants, form factors, mixing parameters which characterise weak-decay amplitudes, PDFs, quark masses, etc.)
- ❖ As an example, LQCD provides the heavy flavour decay constants for the  $D$ ,  $D_s$ ,  $B$  and  $B_s$  mesons with sub percent precision, and the most precise determination of  $\alpha_s$ .

## Future prospects:

- ❖ Study of bottomium states to probe dynamics of the strong interaction and provide constraints for some BSM scenarios.
- ❖ Meson distribution amplitudes (DAs), important universal quantities, appearing in many factorization theorems, which allow for the description of exclusive processes at large momentum transfers., e.g.  $B \rightarrow \pi l \nu$ ,  $\eta l \nu$  giving  $|V_{ub}|$ ,  $B \rightarrow D\pi$  used for tagging, and  $B \rightarrow \pi\pi$ ,  $K\pi$ ,  $KKbar$ ,  $\pi\eta$ ,...which are important channels for measuring CP violation.

# Anomalous magnetic moments



# $(g-2)_\mu$ today

- ❖  $(g-2)_\ell$ , i.e. deviation of gyromagnetic ratio of  $\ell$  with respect to classical value, promising NP search

- ❖ Calculated with impressive accuracy in SM

- ❖ Since E821 experiment of the Brookhaven National Laboratory in the early 2000s, 3:5 sigma disagreement theory and exp

- ❖ While exp / th uncertainties close, new Fermilab exp (E989) currently taking data and another planned (E34) at J-PARC in Japan, both will reduce the error by a factor four, i.e. down to 0.15 ppm.

- ❖ Reduction of the theory uncertainties (factor 10) is therefore essential to fully exploit the new experimental results.

	$a_\mu \times 10^{10}$	
QED 5-loops	$11658471.8853 \pm 0.0036$	Aoyama, et al, 2012
Weak 2-loops	$15.36 \pm 0.10$	Gnendiger et al, 2013
<b>HVP (LO)</b>	<b><math>692.5 \pm 2.7</math></b>	RBC-UKQCD and FJ17 combined
	$693.26 \pm 2.46$	KNT18
	$693.9 \pm 4.0$	DHMZ19
HVP (NLO)	$-9.93 \pm 0.07$	Fred Jegerlehner, 2017
HVP (NNLO)	$1.22 \pm 0.01$	Fred Jegerlehner, 2017
<b>HLbL</b>	$10.3 \pm 2.9$	Fred Jegerlehner, 2017
	$10.5 \pm 2.6$	Glasgow Consensus, 2007
SM Theory	$11659181.3 \pm 4.0$	
BNL E821 Exp	$11659208.9 \pm 6.3$	
Exp – SM	$27.6 \pm 7.5$	

# Theoretical challenges

Theory uncertainty limited by two hadronic contributions: hadronic vacuum polarization (HVP) and hadronic light-by-light scattering (HLbL). 4 French teams significantly contributed to the calculation of both and more work ongoing.

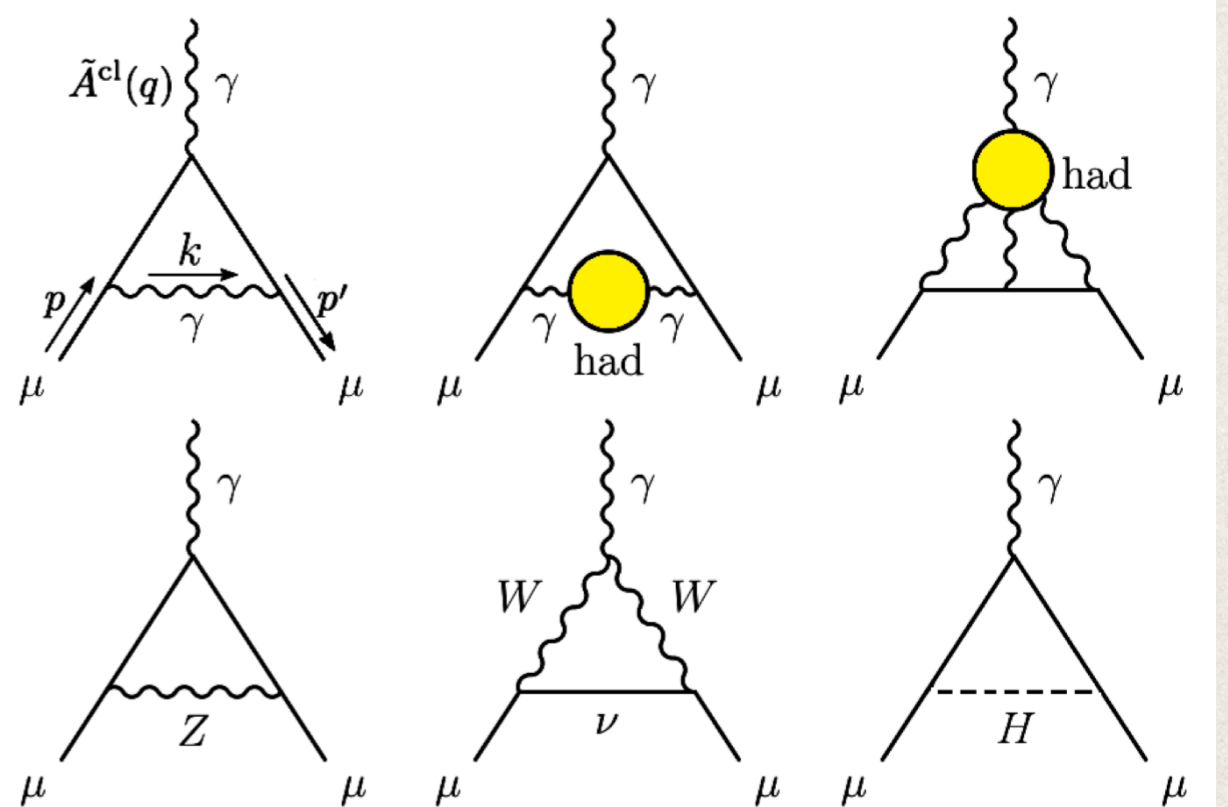
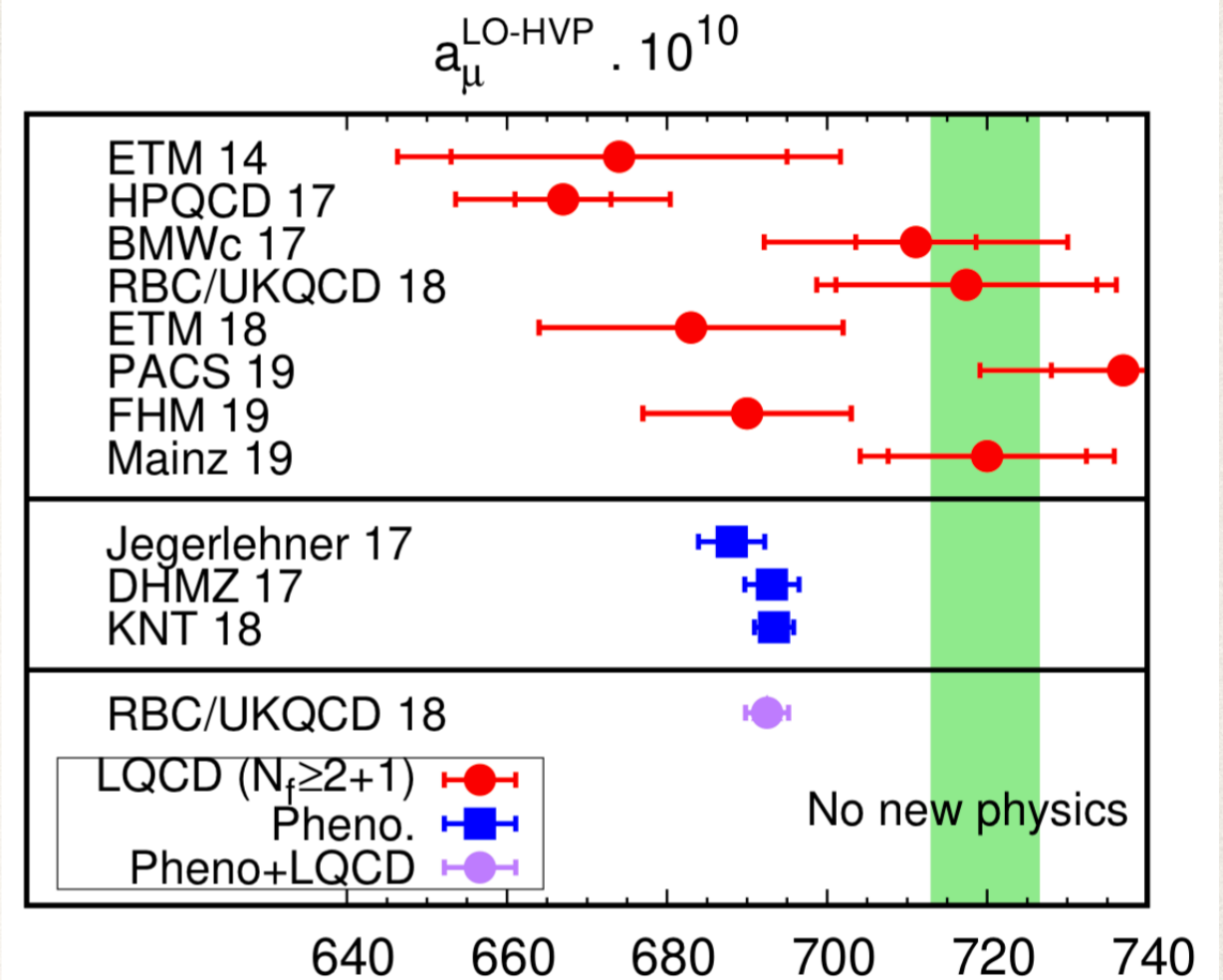
## HVP contribution:

- ❖ Pheno: dispersion relations applied to data for the cross section of  $e^+e^-$  to hadrons. (most precise and to improve with data e.g. from Belle II. )
- ❖ LQCD: 1st complete result BMWc 17), uncertainties  $\sim 6$  times  $>$  pheno.

MUonE project: proposes to determine the HVP contribution by directly measuring the eff. EM coupling in spacelike region via  $e$  scattering data.

## HLbL contribution:

- ❖ Model based calculation computing contributions of individual hadronic states. (Knecht, Nyffler 2002)
- ❖ More recently, using LQCD (aim at  $O(10\%)$  uncertainty) (N. Asmussen, E. H. Chao, A. Gerardin, J. R. Green, R. J. Hud, spith, H. B. Meyer and A. Nyffeler, arXiv:1911.05573 [hep-lat].)

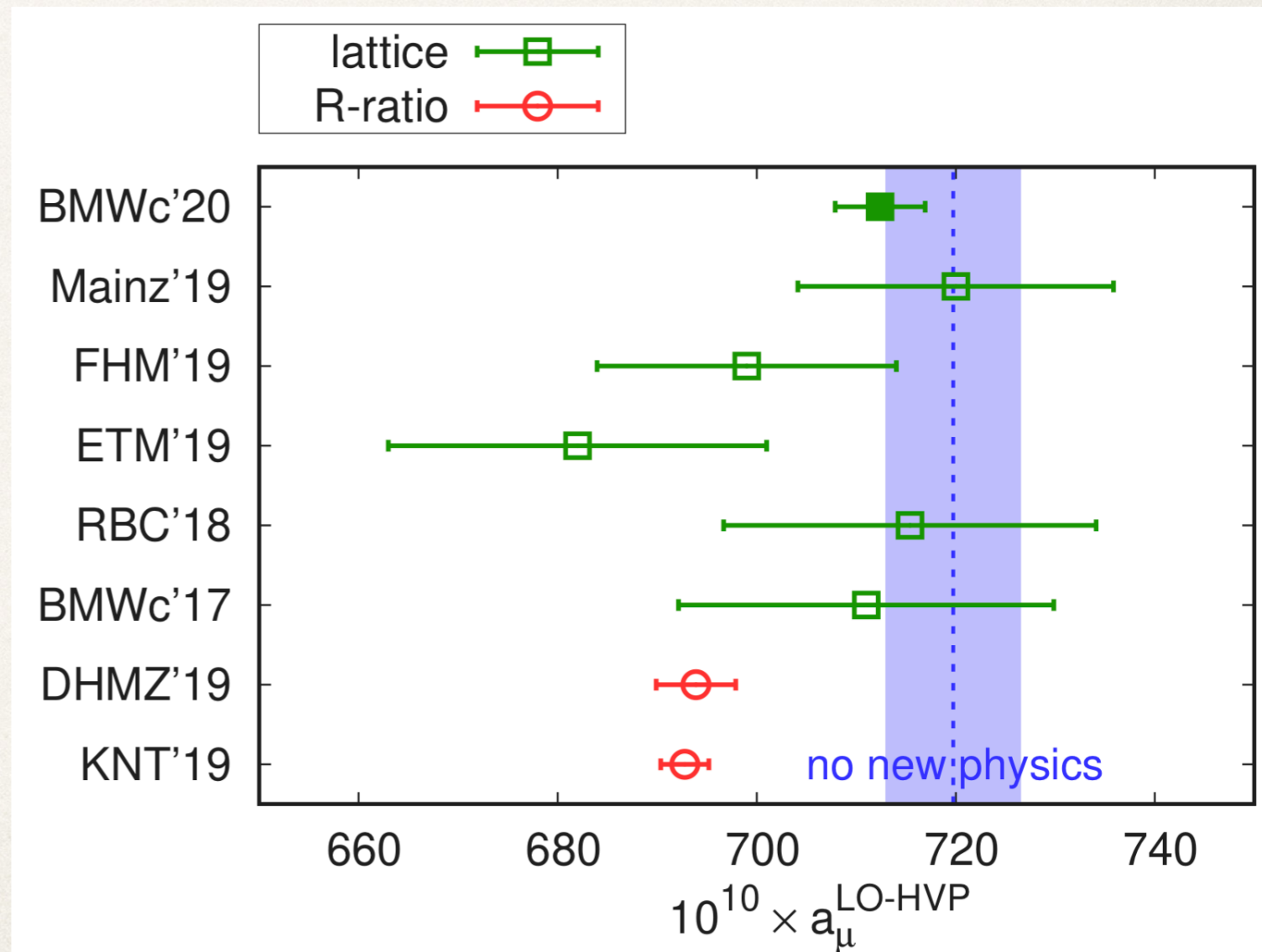


# Latest news from BMWc

Improving the uncertainty on  
HVP needs:

- ❖ advanced noise reduction techniques
- ❖ the inclusion of electromagnetic and strong-isospin breaking effects
- ❖ much larger statistics, simulations in larger volumes

- ❖ BMWc'17 consistent with both pheno and “no new physics” scenario
- ❖ BMWc'20 clearly agrees with SM and disagrees with pheno result
- ❖ Question remains why pheno inconsistent with exp, supposing that E989 confirms previous measurements.



# Additional themes in LQCD

Vincent Morenas, Mariane Brinet, Benoit Blossier, Savvas Zafeiropolous

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- ❖ **Hadron structure:** PDFs and generalised GPDFs and meson DAs will be under deep investigation in future experiments at J-Lab (JLEIC). Lattice results in regions complementary to that accessible via exp.
- ❖ **Neutron EDM:** Upper bound  $|d_n| < 3 \cdot 10^{-26}$  e·cm (90% C.L.) stringent constraint on NP. In SM, mediated by the strong CP-violating term/topological charge. Estimates from the lattice challenging but good hope to remain competitive with respect to the new experiment led at nEDM@PSI.
- ❖ **Higgs Physics and PDFs:** for hadronic initial states (e.g. pp), a complete high-precision determination of the PDFs, is crucial for measurements e.g. of the Higgs sector, multi-TeV SM/BSM cross sections.
- ❖ **Algorithmic aspects:** large vol. simulations need extremely large computer time, ( $\sim O(10^8)$  core hrs) on Tier-0 and Tier-1 high-performance systems. Developing new paradigms is potentially mandatory to optimize the cost of acceptance/rejection test in hybrid Monte-Carlo algorithms.



# Summary

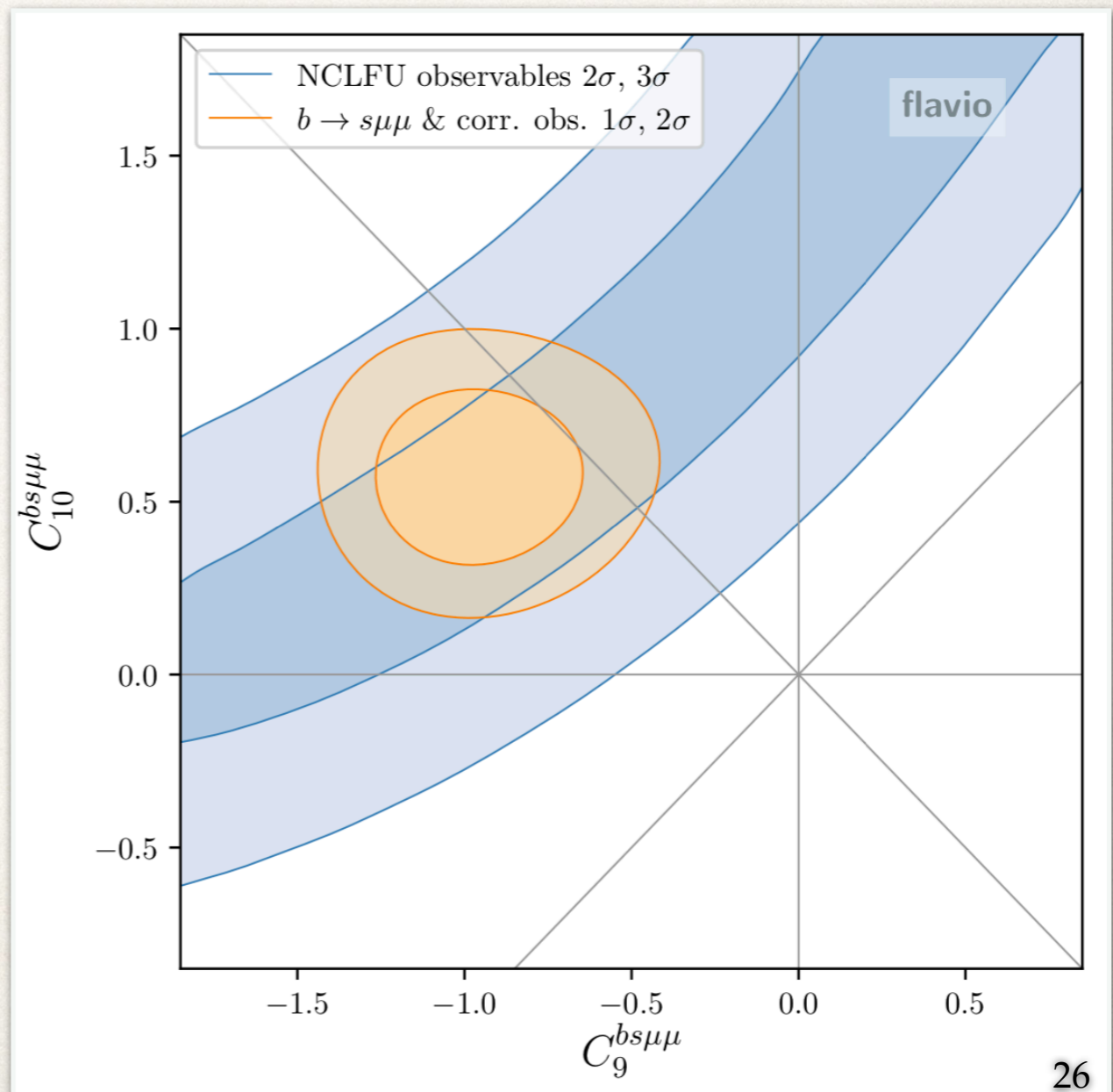
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- ❖ **Neutral currents searches for BSM:** Anomalies, global fits, deeper understanding of related uncertainties, related channels, tau physics
- ❖ **Charged currents / high precision CKM:** Anomalies and related ratios on the Lattice, improved determinations of  $V_{cb}$  and  $V_{ub}$  (Lattice form factors / new parameterisations)
- ❖  $(g-2)_\ell$ : HPV (lattice-new result from BMWc-and pheno), HLbL...
- ❖ **Further Lattice QCD activities:** PDFs, nEDM, algorithmic aspects

# Observables and Sensitivity to Wilson Coefficients and Fits

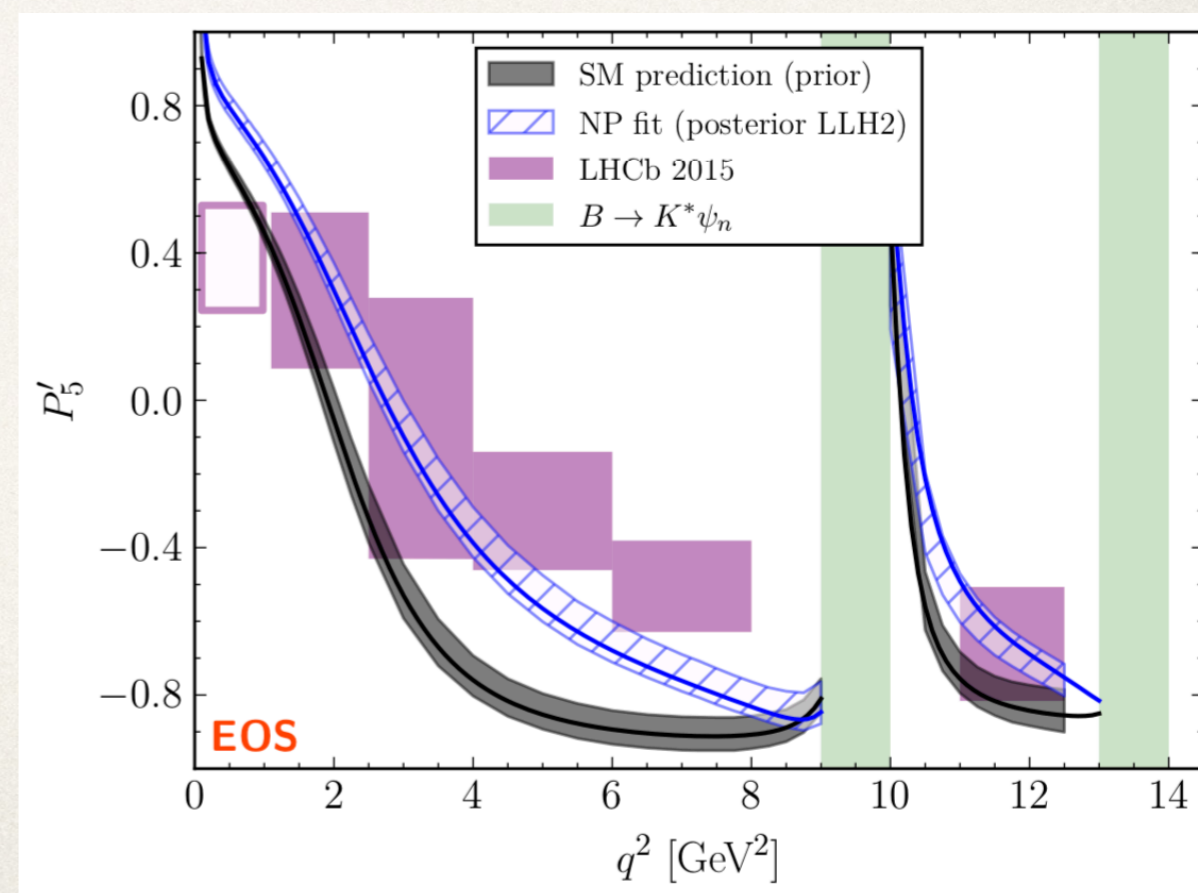
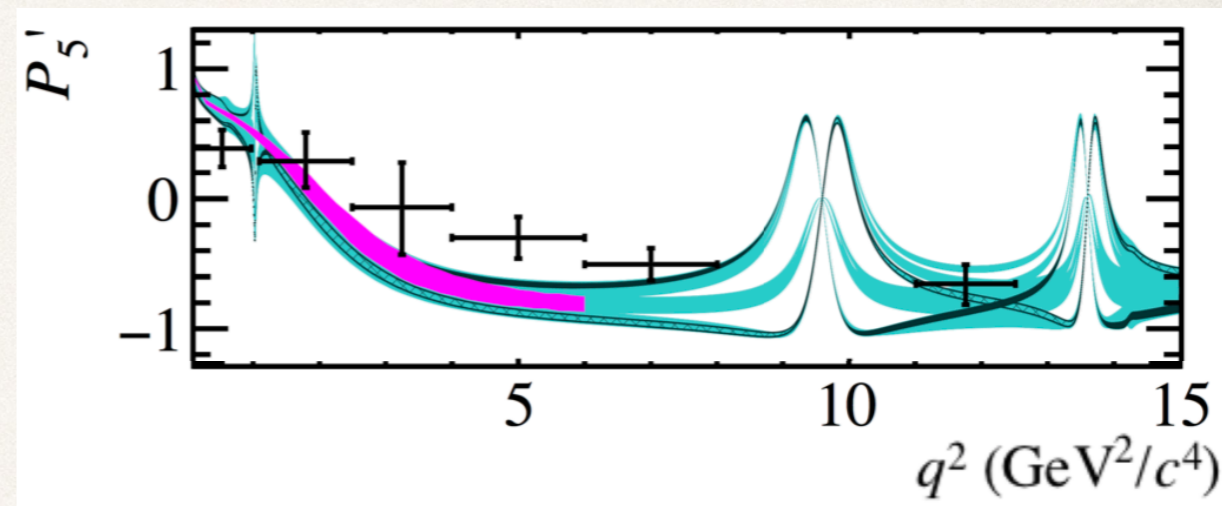
- ❖ Angular observables in  $B \rightarrow K^* \mu^+ \mu^-$  (CDF, LHCb, ATLAS, CMS)
- ❖  $\text{BR}(B \rightarrow K^* \mu^+ \mu^-)$  (CDF, LHCb, CMS)
- ❖  $\text{BR}(B \rightarrow K \mu^+ \mu^-)$  (CDF, LHCb)
- ❖  $\text{BR}(B_s \rightarrow \phi \mu^+ \mu^-)$  (CDF, LHCb)
- ❖  $B_s \rightarrow \phi \mu^+ \mu^-$  angular observables (LHCb)
- ❖  $\text{BR}(B \rightarrow X_s \mu^+ \mu^-)$  (BaBar)

Decay	$C_7^{(l)}$	$C_9^{(l)}$	$C_{10}^{(l)}$	$C_{S,P}^{(l)}$
$B \rightarrow X_s \gamma$	X			
$B \rightarrow K^* \gamma$	X			
$B \rightarrow X_s l^+ l^-$	X	X	X	
$B \rightarrow K^{(*)} l^+ l^-$	X	X	X	
$B_s \rightarrow \mu^+ \mu^-$			X	X



# Further checks: NP or QCD?

- ❖ Fit resonance contribution to  $e^+e^-$  data [Lyons and Zwicky arXiv:1406.0566]
- ❖ Breit-Wigner description of resonances fit to hadronic decays [Blake et al arXiv:1709.03921]
- ❖ Long-distance effects in  $B \rightarrow K^*ll$  from Analyticity [Bobeth, Chruszcz,, van Dyk and Virto arXiv:1707.07305, Chruszcz et al, arXiv:1805.06378]



# BGL vs CLN

Boyd, Grinstein, Lebed [arXiv:hep-ph/9705252]

$$z = \frac{\sqrt{w+1} - \sqrt{2}}{\sqrt{w+1} + \sqrt{2}} \quad w = \frac{m_B^2 + m_{D^*}^2 - q^2}{2m_B m_{D^*}},$$

$$g = h_V / \sqrt{m_B m_{D^*}}$$

$$f = \sqrt{m_B m_{D^*}} (1+w) h_{A_1} \quad f(z) = \frac{1}{P_{1+}(z) \phi_f(z)} \sum_{n=0}^{\infty} a_n^f z^n$$

$$\mathcal{F}_1 = (1+w)(m_B - m_{D^*}) \sqrt{m_B m_{D^*}} A_5$$

$$R_1(w) = (w+1) m_B m_{D^*} \frac{g(w)}{f(w)}, \quad R_2(w) = \frac{w-r}{w-1} - \frac{\mathcal{F}_1(w)}{m_B (w-1) f(w)}.$$

Caprini, Lellouch, Neubert [arXiv:hep-ph/9712417]

$$h_{A_1}(w) = h_{A_1}(1) [1 - 8\rho^2 z + (53\rho^2 - 15)z^2 - (231\rho^2 - 91)z^3],$$

$$R_1(w) = R_1(1) - 0.12(w-1) + 0.05(w-1)^2,$$

$$R_2(w) = R_2(1) + 0.11(w-1) - 0.06(w-1)^2$$

*Uncertainties from NNLO can be up to 10-20%. In exp fits never included. At current precision cannot be ignored.*

Three form factors. Series expansion, impose dispersive bounds on coefficients using unitarity. Construct useful ratios in terms of form factors. Fit to data to obtain V(cb).

Use HQET+combine bounds from B to D, B to D\*, B\* to D\* and B\* to D to obtain shape of form factors and ratios. Theory uncertainties on slope and curvature ignored.

# Role of HQET relations in $V_{cb}$ extraction

(preliminary Belle data only)

<b>STRONG HQET INPUT</b>	<b>SMALL <math>V_{cb}</math></b>	<b>Refs.</b>
“practical” CLN:	$ V_{cb}  = 38.2(1.5) \cdot 10^{-3}$	[1,5,6,7,8]
CLN+QCD sumrule errors + $B \rightarrow D$	$ V_{cb}  = 38.5(1.1) \cdot 10^{-3}$	[2]
same + lattice at non-zero recoil	$ V_{cb}  = 39.3(1.0) \cdot 10^{-3}$	[2]
BGL,HQET,LCSR, $B \rightarrow D$ ,nuisance	$ V_{cb}  = 40.9(0.9) \cdot 10^{-3}$	[3]
BGL + strong unitarity	$ V_{cb}  = 40.8(1.5) \cdot 10^{-3}$	[4]
BGL + weak unitarity	$ V_{cb}  = 41.7(2.0) \cdot 10^{-3}$	[5,6,7,8]
<b>NO HQET INPUT</b>	<b>LARGE <math>V_{cb}</math></b>	

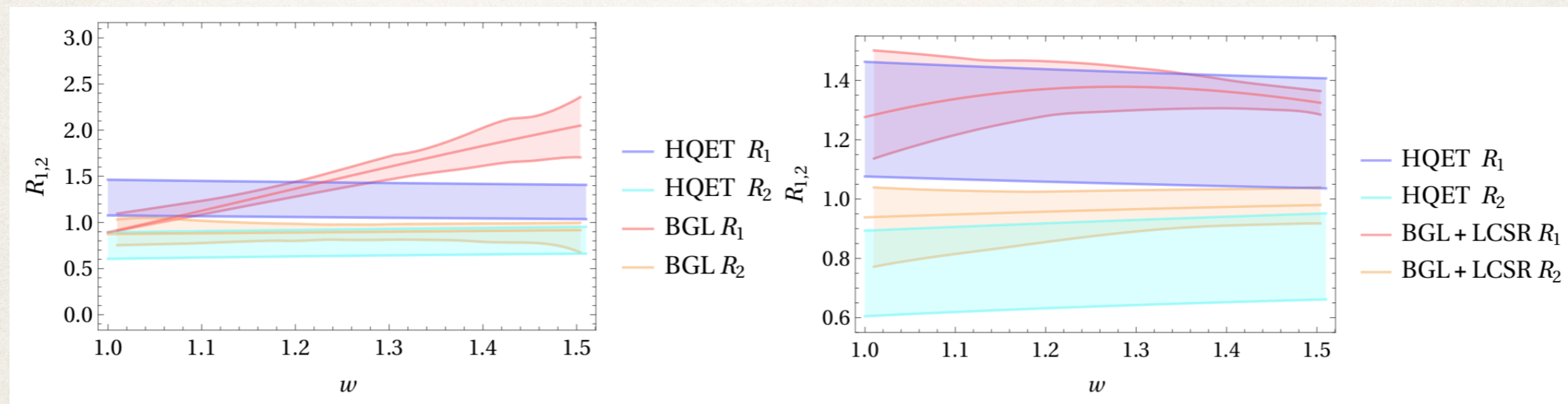
[1] [Belle 1702.01521] [2] [Bernlochner Ligeti Papucci Robinson 1703.05330]

[3] [Jaiswal Nandi Patra 1707.09977] [4] [Bigi Gambino Schacht 1707.09509]

[5] [Bigi Gambino Schacht 1703.06124] [6] [HPQCD 1711.11013]

[7] [Bernlochner Ligeti Papucci Robinson 1708.07134] [8] [Grinstein Kobach 1703.08170]

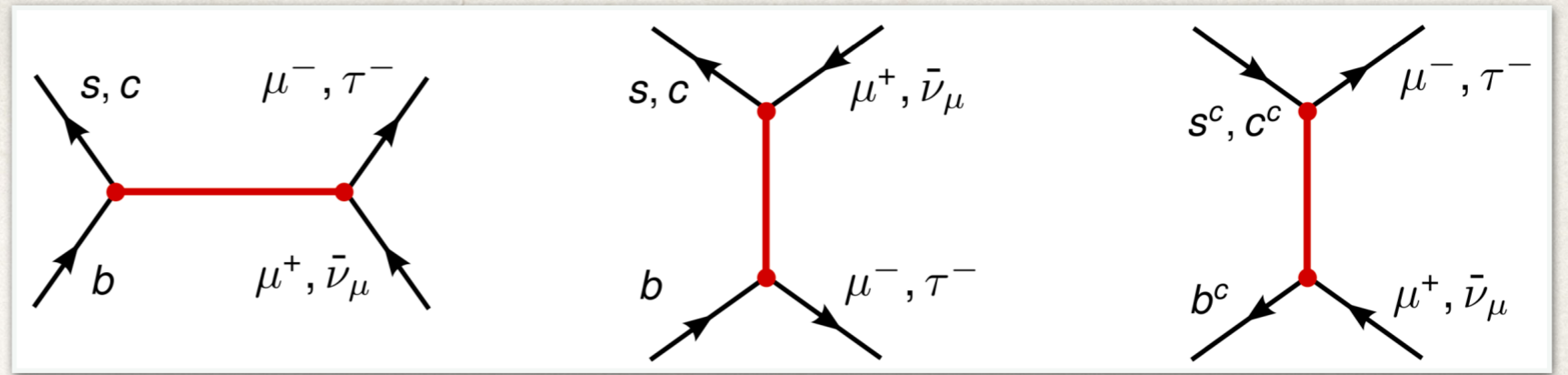
# Effect of HQET on R1 and R2



- ❖ Fits for R2 in good agreement with HQET+QCDSR.
- ❖ Same goes for R1 with LCSR. R1 without LCSR well compatible with HQET only at small/moderate recoil. At large  $w$  clear tension with both HQET and LCSR.
- ❖ Fit without LCSR appears somewhat disfavored.

Lattice will compute  $A_1$  and  $R_{1,2}$  and settle the story

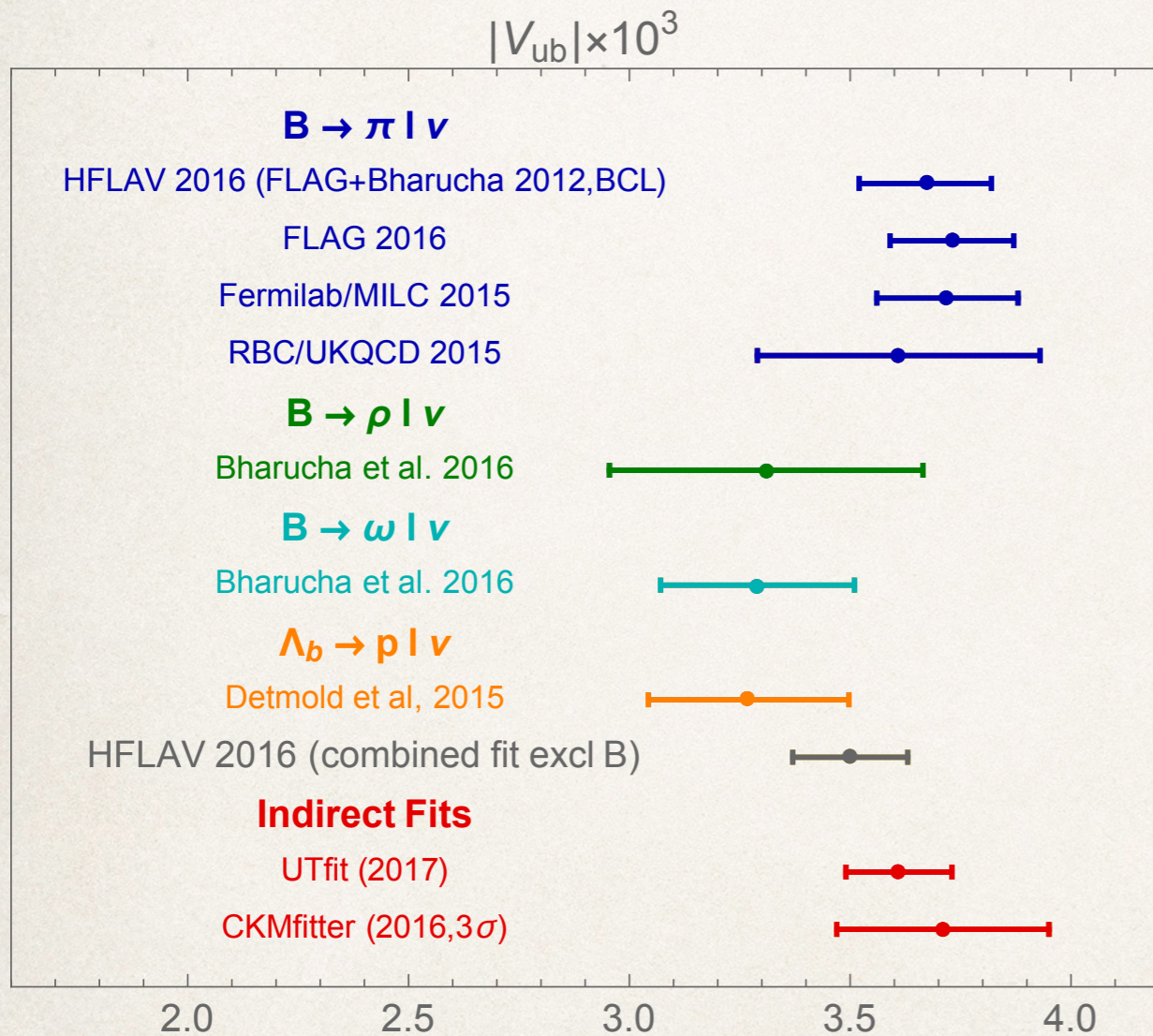
# Tree-level solutions



With help from David Straub

- ❖ Only particle which can produce such operators:  $U_1$  LQs, transforming as  $(3,1)_{2/3}$  under the SM
  - Loop suppression of B mixing
  - Loop suppression of  $B \rightarrow K\nu\nu$ , singlet and triplet WCs are naturally equal
- ❖ Vector leptoquarks require a UV completion. Several model building attempts are underway, most based on Pati-Salam (PS) gauge group,  $SU(4) \times SU(2) \times SU(2)$ 
  - Composite PS leptoquark [Barbieri et al. 1611.04930](#), [Barbieri and Tesi 1712.06844](#)
  - $SU(4) \times SU(3) \times SU(2) \times U(1)$  [Di Luzio et al. 1708.08450](#), cf. v2 of [Assad et al. 1708.06350](#)
  - PS with additional vector-like fermions [Calibbi et al. 1709.00692](#)
  - Three-site PS [Bordone et al. 1712.01368](#)
  - PS in warped extra dimensions [Blanke and Crivellin 1801.07256](#)

# Summary of $V_{ub}$ and Future Prospects



## Summary:

2012 NNLO calculation  $B \rightarrow \pi$  (AB)

2014 Bayesian uncertainty analysis for the  $B \rightarrow \pi$  form factor (Imson, Khodjamirian, Mannel van Dyk)

2015 Update for B to V form factors (AB, Straub, Zwicky)

2017 Calculation of  $f_+$  and  $f_T$  for  $B_{(s)}$  to K form factors (Khodjamirian and Rusov)

## Future Prospects:

- Find higher twist (i.e. 5,6) terms in the factorizable approximation are small, but still would be good to check the full NNLO twist 2 and twist 3 contributions
- Bayesian uncertainty analysis of all  $B \rightarrow P, D \rightarrow P$  LCSR (for  $B \rightarrow \pi$  in [Imson, AK, Mannel, van Dyk (2013)])
- $B_s \rightarrow K l \nu$  measurement at LHCb/Belle II
- Future Belle-2 data on the  $q^2$ -shape of  $B \rightarrow \pi l \nu$  will provide additional constraints on the DA parameters

inclusive (BLNP):  $(4.44 \pm 0.15 +0.21/-0.22) 10^{-3}$