

## ***WP21: JRA3 - PrecisionSM***

***QCD and precision hadron structure for low-energy tests of the SM***

*Mikhail Gorshteyn - JGU Mainz*

**STRONG-2020 Kick-off meeting**

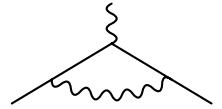
*October 23-25, 2019*

- JRA3 unifies 18 Institutions from 9 EU countries
- Fosters cooperation with 5 non-EU based partners (USA, Russia, China)
- Leading institutions: Mainz and Uppsala
- Spokespersons: Mikhail Gorshteyn (Mainz), Andrzej Kupsc (Uppsala)
- Goal: provide decisive support to the interpretation of low-energy precision tests of SM in the electroweak sector
- Dispersion relations as the main tool. Input extensively uses data, directly (HVP to muon  $g-2$ ) or indirectly (HLbL to muon  $g-2$ , EW boxes for extraction of  $V_{ud}$  and weak mixing angle)

Dirac theory: gyromagnetic ratio  $g=2$

Small deviations observed in HF structure of atoms:  
1948 explained by Schwinger - radiative correction

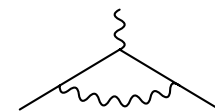
$$a_{\mu} = \frac{g - 2}{2} = \frac{\alpha}{2\pi} = 0.001161$$



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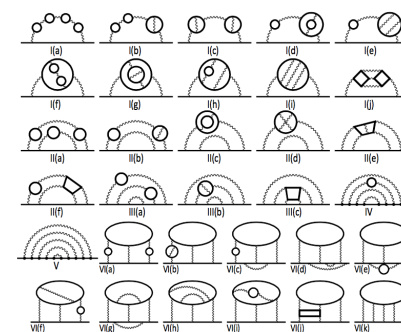
Since then QED calculations went a long way:

**Aoyama, Hayakawa, Kinoshita, Nio 2012**

Complete 5-loop QED calculation >12000 diagrams

$$a_{\mu}^{\text{QED}} = 116\,584\,718.951 (0.009) (0.019) (0.007) (0.077) \times 10^{-11}$$

errors from: lepton masses, 4-loop, 5-loop,  $\alpha$  from  $^{87}\text{Rb}$

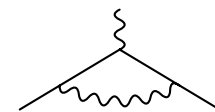




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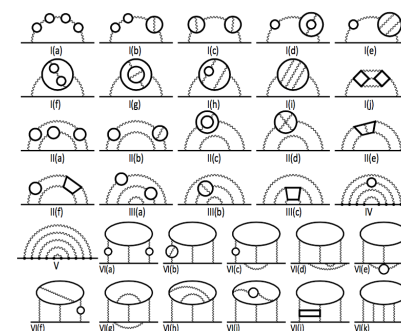
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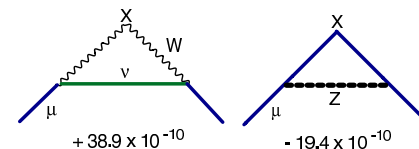


Electroweak corrections 1 and 2-loop

**Czarnecki, Krause, Marciano, Vainshtein;**

**Knecht, Peris, Perrotet, de Rafael; Gneding, Stöckinger, Kim**

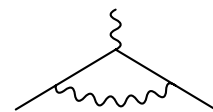
$$a_\mu^{\text{EW}(1+2 \text{ loop})} = (153.6 \pm 1.0) \times 10^{-11}$$



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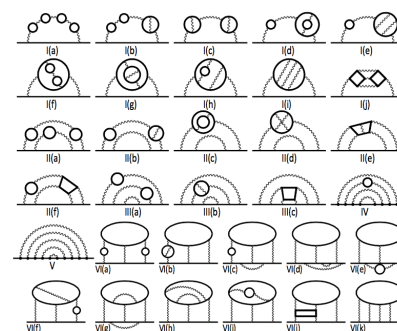
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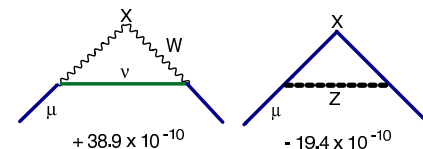


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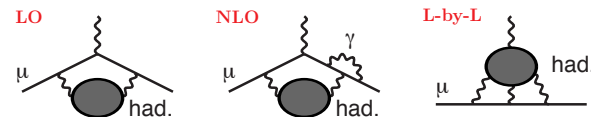
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Hadronic corrections 2 and 3-loop: main limitation

$$a_\mu^{\text{had}} = a_\mu^{\text{had,VP LO}} + a_\mu^{\text{had,VP NLO}} + a_\mu^{\text{had,Light-by-Light}}$$

Main focus of *Muon g-2 Theory Initiative*

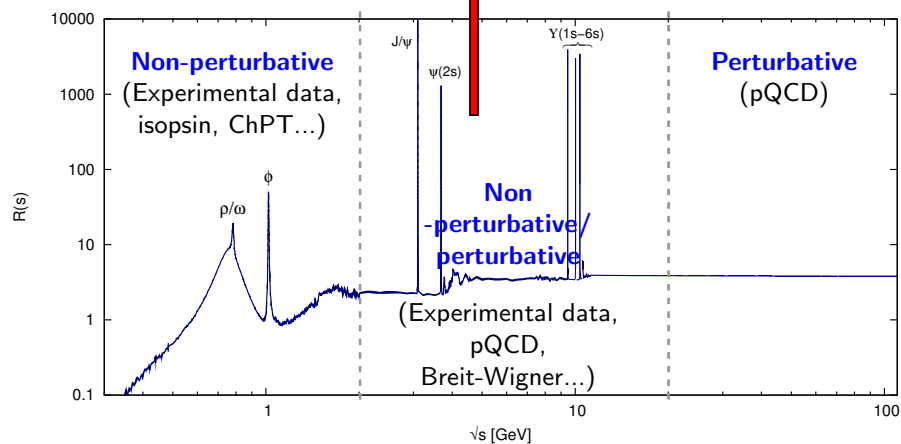


This project has received funding from the European Union's Horizon 2020 research and innovation programme under grant agreement No 824093.

# HVP Contribution to $a_\mu$ from Dispersion Relations

For HVP  $\Rightarrow 2 \operatorname{Im} \text{had.} = \sum_{\text{had.}} \int d\Phi \left| \text{had.} \right|^2 \Rightarrow \operatorname{Im} \Pi_{\text{had}}(s) = \left( \frac{s}{4\pi\alpha} \right) \sigma_{\text{had}}(s)$

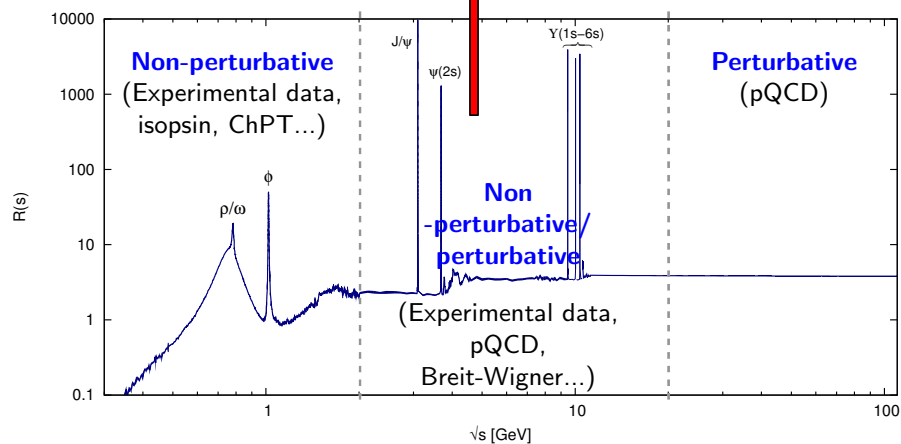
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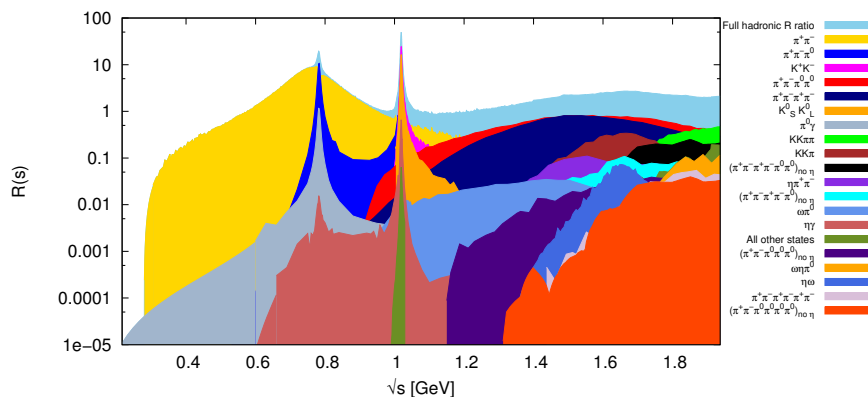
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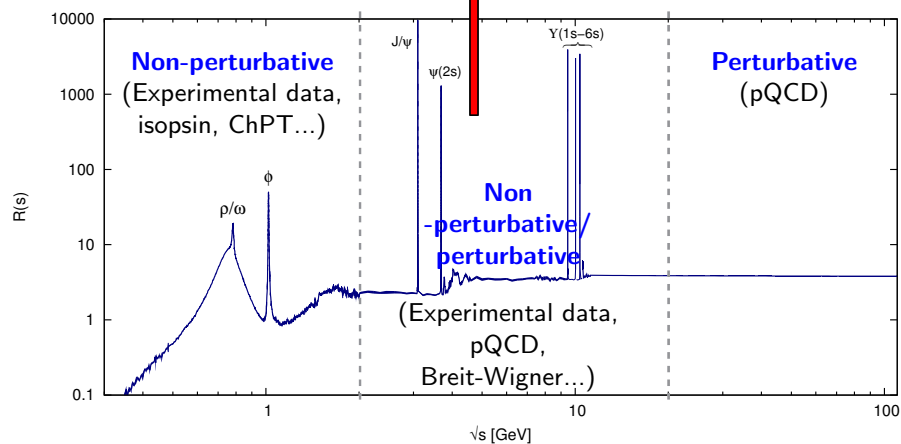
Low energies: sum  $\sim 35$  exclusive channels  
( $2\pi$ ,  $3\pi$ ,  $4\pi$ ,  $5\pi$ ,  $6\pi$ ,  $KK$ ,  $KK\pi$ ,  $KK\pi\pi$ ,  $\eta\pi$ , ...)  
Below 0.9 GeV dominated by  $2\pi$



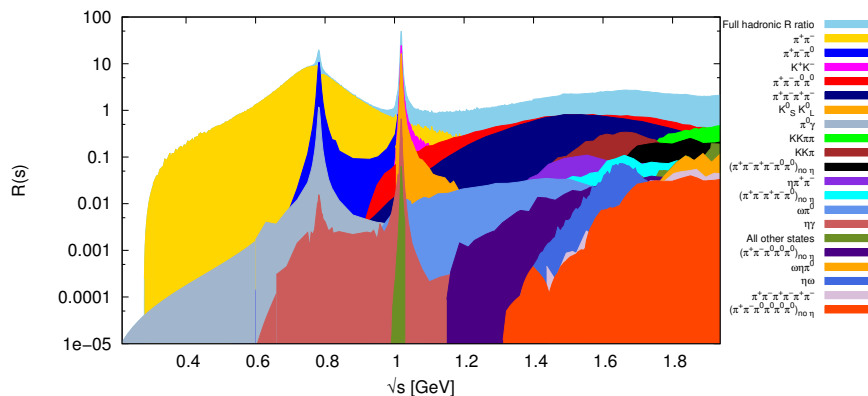
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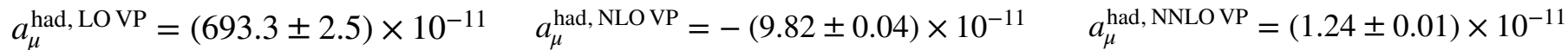
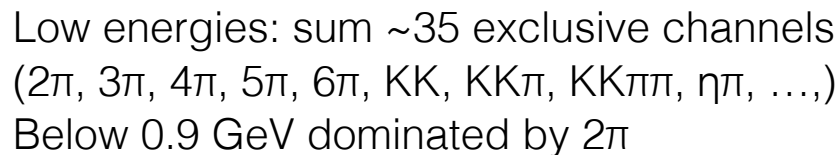
$$a_\mu^{\text{had, LO VP}} = (693.3 \pm 2.5) \times 10^{-11}$$

$$a_\mu^{\text{had, NLO VP}} = -(9.82 \pm 0.04) \times 10^{-11}$$

$$a_\mu^{\text{had, NNLO VP}} = (1.24 \pm 0.01) \times 10^{-11}$$

**Keshavarzi, Nomura, Teubner 2018**

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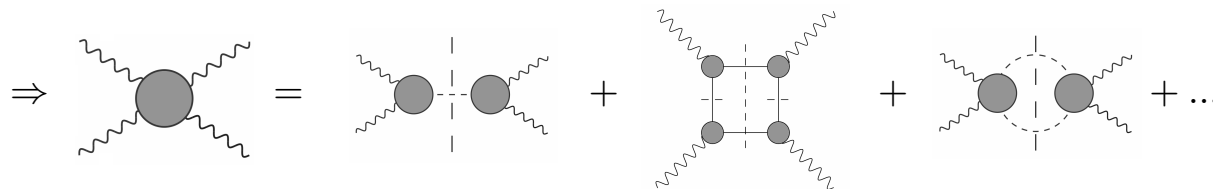
Novel idea: MUonE @ CERN: 150 GeV muons scattering on atomic electrons  
Probe the HVP in the space like regime - complementary to the R-scan

4

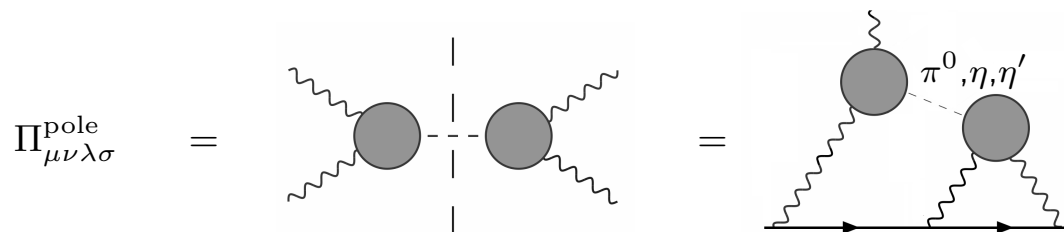
# HVP Contribution to $a_\mu$ from Dispersion Relations

Hadronic LbL contribution is constrained by the data (but not fully determined)

For HLbL  $\Rightarrow \Pi_{\mu\nu\lambda\sigma} = \Pi_{\mu\nu\lambda\sigma}^{\text{pole}} + \Pi_{\mu\nu\lambda\sigma}^{\text{box}} + \bar{\Pi}_{\mu\nu\lambda\sigma} + \dots$



$\Rightarrow$  Dominated by pole (pseudoscalar exchange) contributions



$\Rightarrow$  Sum all possible diagrams to get  $a_\mu^{\text{HLbL}}$

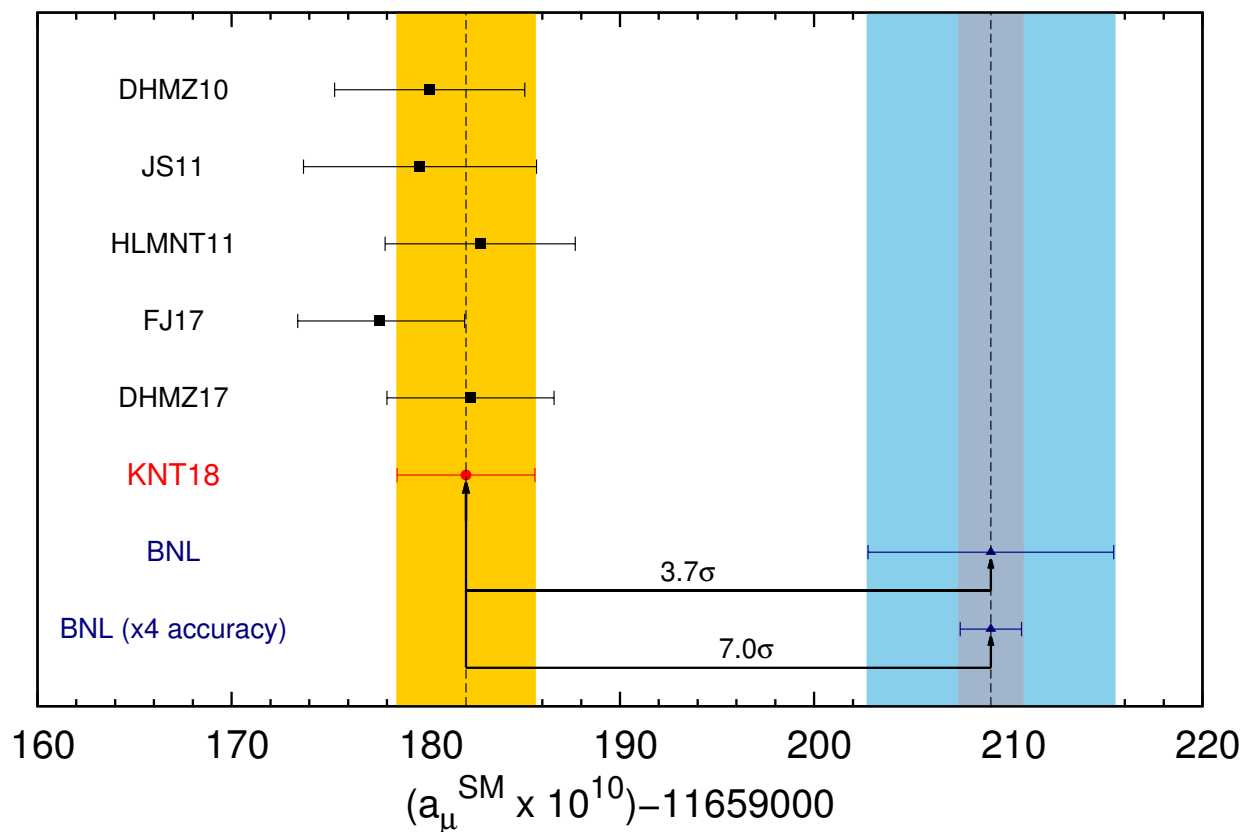
**Pauk, Vanderhaeghen 2014;  
Colangelo, Hoferichter, Procura, Stoffer 2017**

Summary of HLbL contribution of (Colangelo, INT g-2 workshop September 2019):

$$a_\mu^{\text{HLbL}} \times 10^{11} = 93.8(4.0)^{\text{PS poles}} - 15.9(2)^{\text{pion box}} - 8(1)^{\text{S-wave } \pi\pi} - 2(3)^{\text{S,T} > 1 \text{ GeV}} + 8(3)^{\text{Axial}} + 10(10)^{\text{SD}} = 85 \pm (12 - 21)$$

Danilkin, Redmer, Vanderhaeghen 2019  $a_\mu^{\text{HLbL}} \times 10^{11} = 87 \pm 13$

This project has received funding from the European Union's Horizon 2020 research and innovation programme under grant agreement No 824093.



New experiments: E989@FNAL (concluded - analysis), E34@J-PARC (start 2022 on): will reduce the exp. error by factor 4;

If central value stays —  $7\sigma$  discrepancy; Theory uncertainty needs further reduction



## Polarization and entanglement in baryon-antibaryon pair production in electron-positron annihilation

The BESIII Collaboration\*

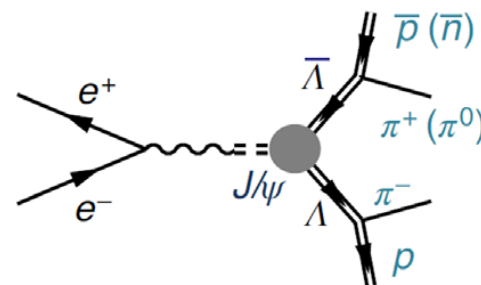
Online: May 6<sup>th</sup>

$$e^+ e^- \rightarrow J/\psi \rightarrow \Lambda \bar{\Lambda}:$$

Observation of  $\Lambda$  transverse polarization  
Determination of  $\Lambda$  decay asymmetry

**BESIII**

arXiv:1808.08917

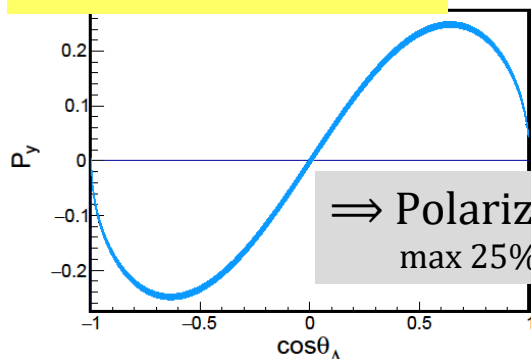


G.Fäldt, AK PLB772 (2017) 16

E.Perotti,G.Fäldt,AK,S.Leupold,JJ.Song PRD99 (2019)056008

This project has received funding from the European Union's Horizon 2020 research and innovation programme under grant agreement No 824093.

$$\Delta\Phi = 42.3^\circ \pm 0.6^\circ \pm 0.5^\circ$$



$\Rightarrow$  Polarization:  
max 25%

$$\bar{\alpha}_0/\alpha_+ = 0.913 \pm 0.028 \pm 0.012$$

$\Delta I = \frac{1}{2}$  rule violation

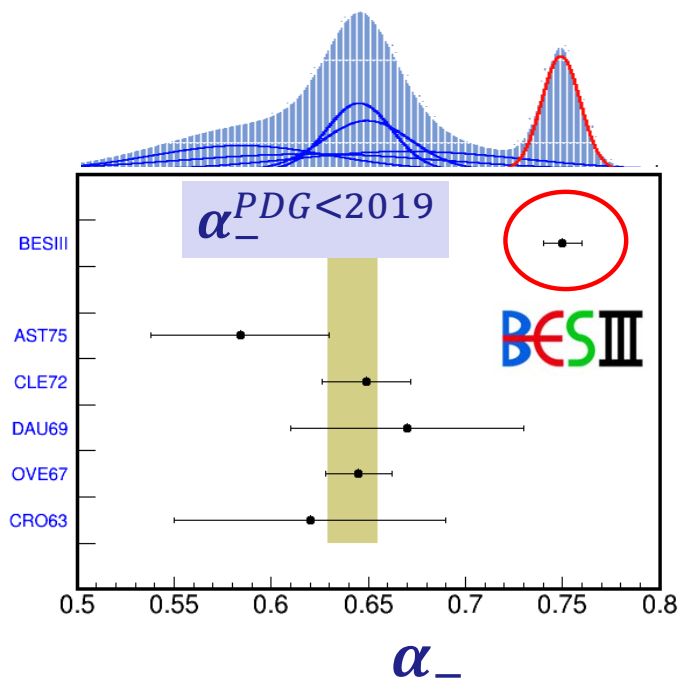
CP test:  $A_\Lambda = \frac{\alpha_- + \alpha_+}{\alpha_- - \alpha_+}$

$$A_\Lambda = -0.006 \pm 0.012 \pm 0.007$$

$$A_\Lambda = 0.013 \pm 0.021$$

PS185 PRC54(96)1877

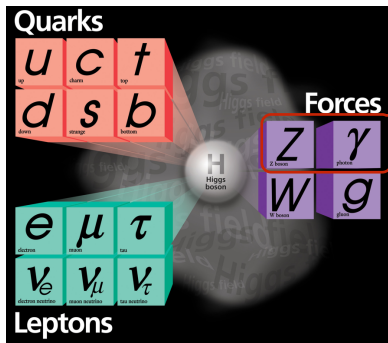
$$\Lambda \rightarrow p\pi^-: \alpha_- = 0.750 \pm 0.009 \pm 0.004$$



17(3)% larger

Included in the PDG 2019 update

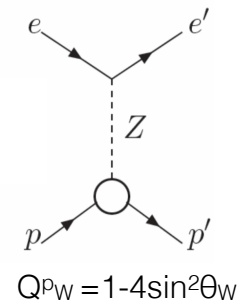
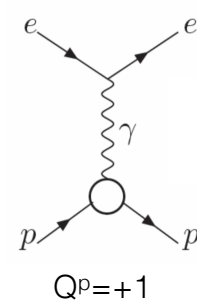
# Precision determination of the weak mixing angle



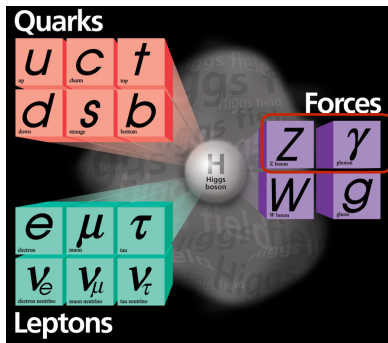
Weak mixing angle - mixing of the NC gauge fields

$$\begin{pmatrix} \gamma \\ Z^0 \end{pmatrix} = \begin{pmatrix} \cos \theta_W & \sin \theta_W \\ -\sin \theta_W & \cos \theta_W \end{pmatrix} \begin{pmatrix} B^0 \\ W^0 \end{pmatrix}$$

WMA determines the relative strength  
of the weak NC vs. e.-m. interaction



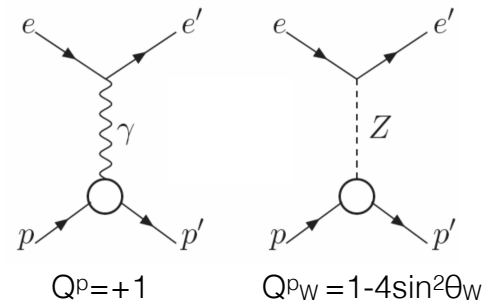
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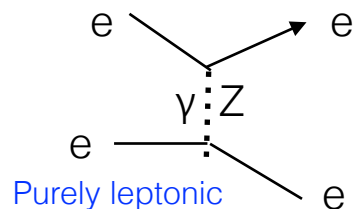
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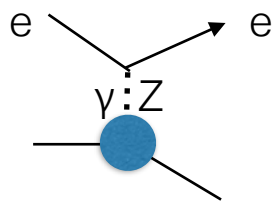


Møller scattering

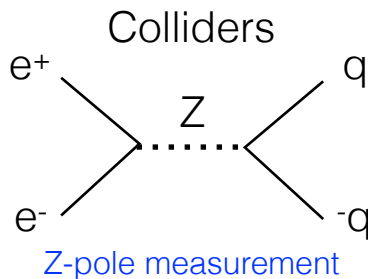


P2 MESA @ Mainz

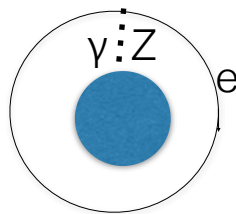
Q-Weak @ JLab



Coherent quarks in p or  $^{12}\text{C}$

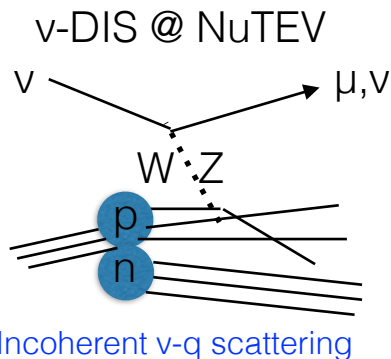
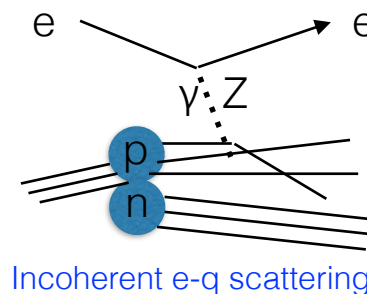


Atomic PV



Coherent quarks in a nucleus

e-DIS @ JLab, EIC

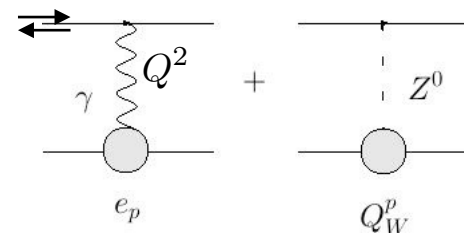


## Weak charge of the proton from PVES

Elastic scattering of polarized electrons off unpolarized protons at low momentum transfer

$$A^{PV} = \frac{\sigma_{\rightarrow} - \sigma_{\leftarrow}}{\sigma_{\rightarrow} + \sigma_{\leftarrow}} = -\frac{G_F Q^2}{4\sqrt{2}\pi\alpha} [Q_W^p + Q^2 B(Q^2)]$$

Effects of hadronic structure - kinematically suppressed  
Existing hadronic data and LQCD used to obtain B and  $\delta B$



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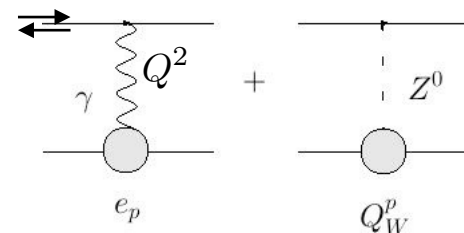
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Reward: a factor  $\sim 16$  gain in precision for  $\sin^2 \theta_W$



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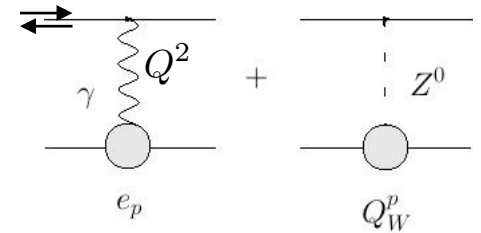
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Qweak@JLab:  $Q^2 \sim 0.03 \text{ GeV}^2$

$$A^{PV} = -(226.5 \pm 9.3) \text{ ppb}$$

$$Q_W^p = 0.0718 \pm 0.0044 \text{ (rel. 6\%)}$$

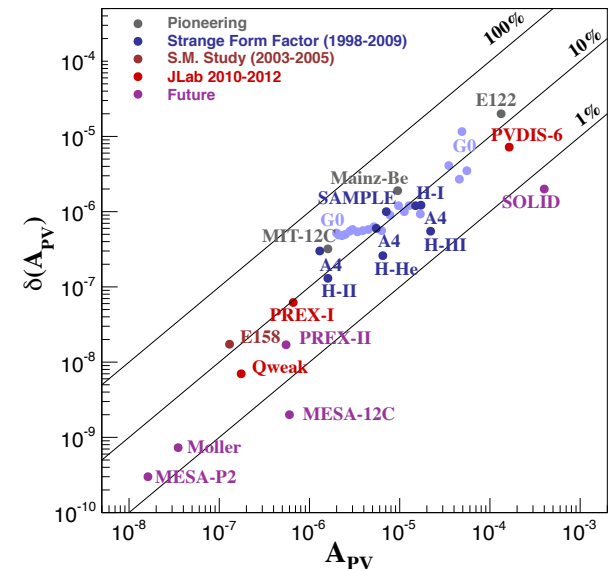
**D. Androic et al [Qweak Coll.], Nature 557 (2018), 207**

**P2 @ MESA/Mainz:**

go down to  $Q^2 \sim 0.005 \text{ GeV}^2$

Unprecedented challenge: tiny asymmetry to 1.5%

PVeS Experiment Summary



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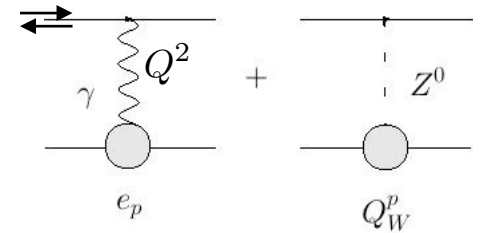
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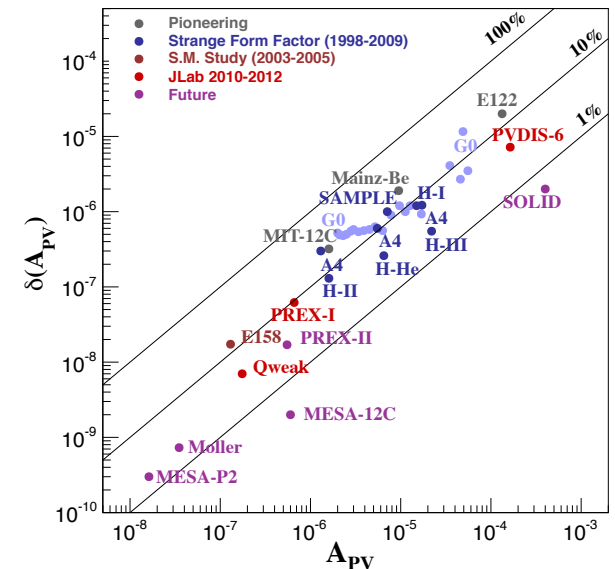
go down to  $Q^2 \sim 0.005 \text{ GeV}^2$

Unprecedented challenge: tiny asymmetry to 1.5%

Need to know radiative corrections sufficiently precise



PVeS Experiment Summary

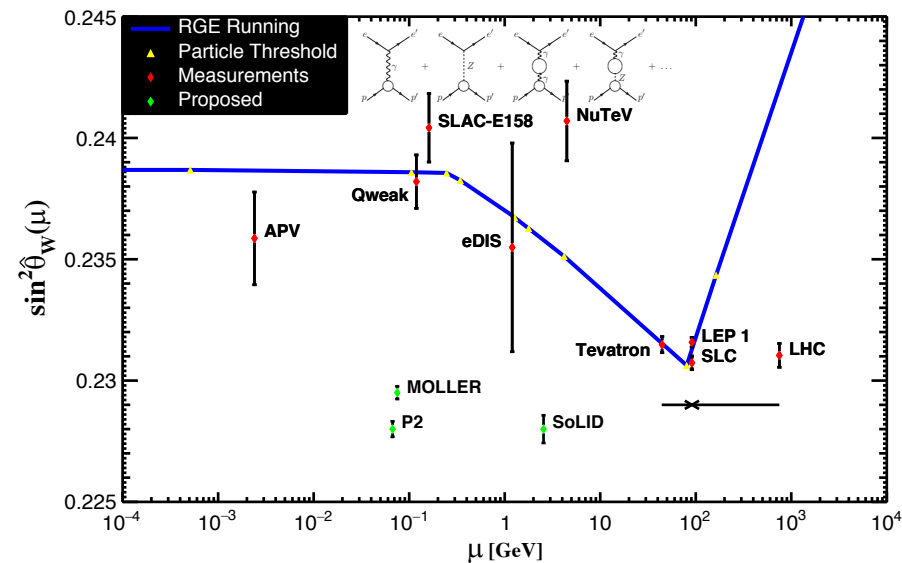




Universal quantum corrections absorbed into running, scale-dependent  $\sin^2\theta_W(\mu)$

**SM uncertainty: few  $\times 10^{-4}$**

Universal running - clean prediction of SM  
Deviation anywhere - BSM signal

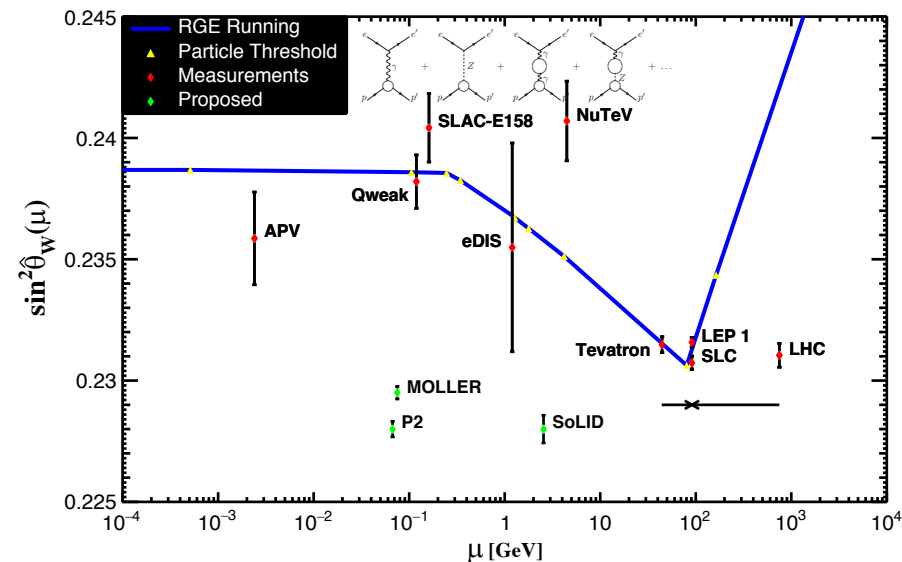


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Process-specific SM radiative corrections:



$$Q_W^{p, 1-loop} = (1 + \Delta_\rho + \Delta_e)(1 - 4 \sin^2 \hat{\theta}_W + \Delta'_e) + \square_{WW} + \square_{ZZ} + \square_{\gamma Z}$$

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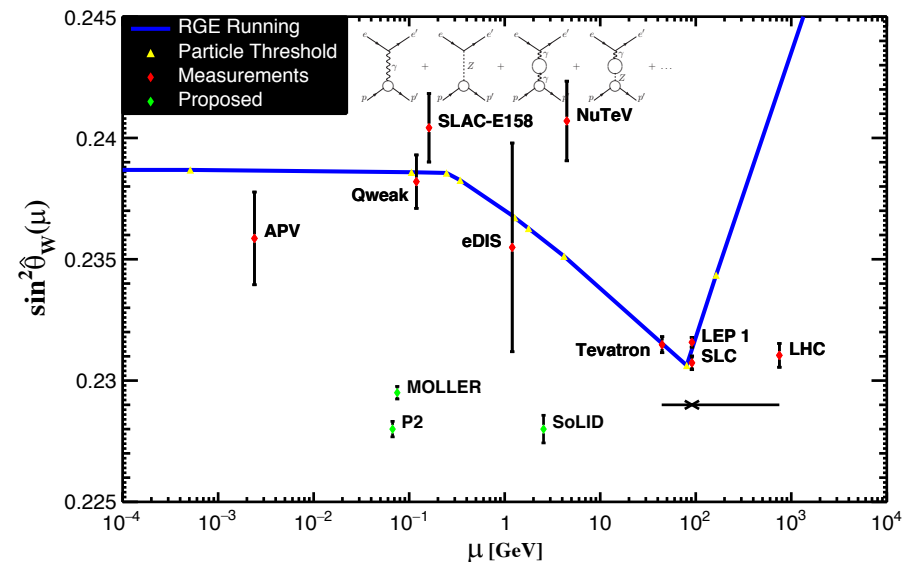
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Process-specific SM radiative corrections:

Hadronic effects under control

$$Q_W^{p, 1-loop} = (1 + \Delta_\rho + \Delta_e)(1 - 4 \sin^2 \hat{\theta}_W + \Delta'_e) + \square_{WW} + \square_{ZZ} + \square_{\gamma Z}$$

**Marciano, Sirlin '83,84; Erler, Musolf '05**



Universal quantum corrections absorbed into running, scale-dependent  $\sin^2\theta_W(\mu)$

**SM uncertainty: few  $\times 10^{-4}$**

Universal running - clean prediction of SM  
Deviation anywhere - BSM signal

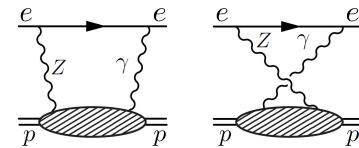
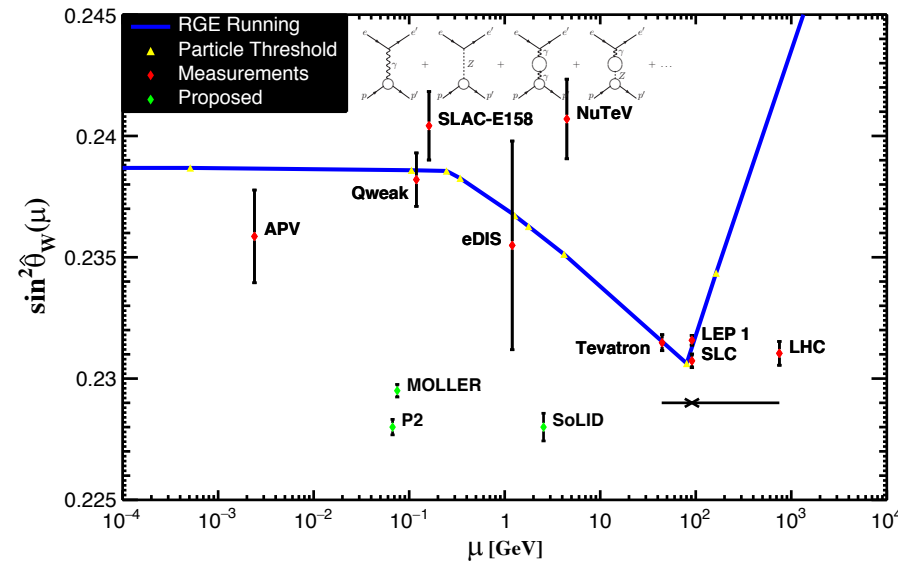
Process-specific SM radiative corrections:

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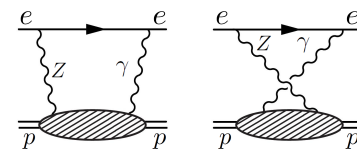
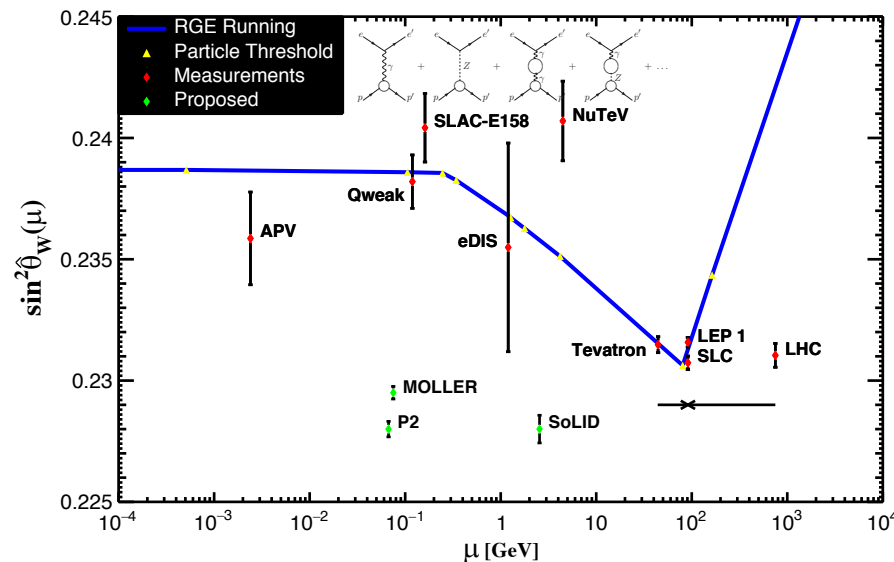
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$$\square_{\gamma Z}(E) = \frac{\alpha}{\pi} \int_0^\infty dQ^2 \int_{thr}^\infty dW^2 \left[ A(E, W, Q^2) F_1^{\gamma Z} + B(E, W, Q^2) F_2^{\gamma Z} + C(E, W, Q^2) F_3^{\gamma Z} \right]$$



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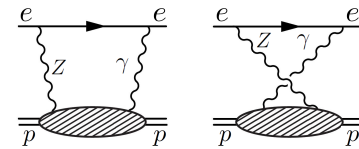
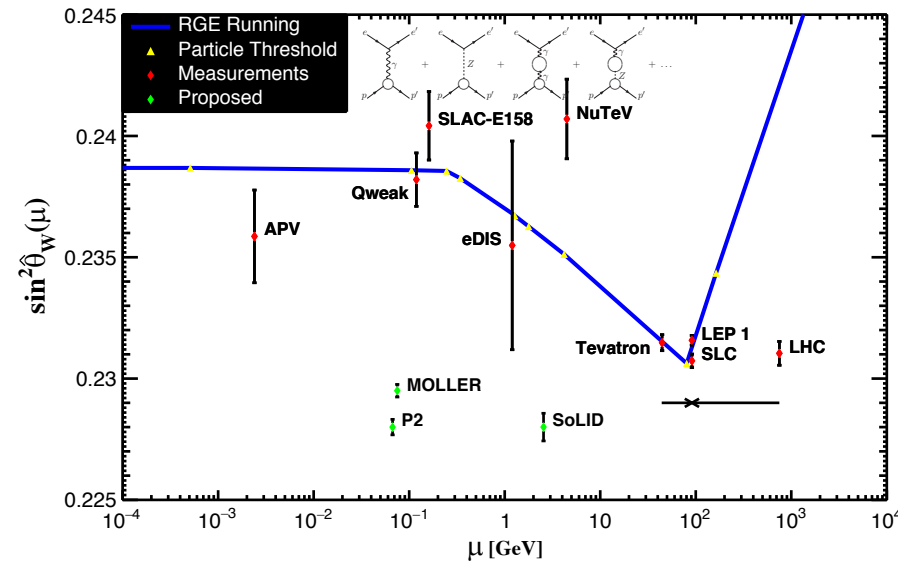
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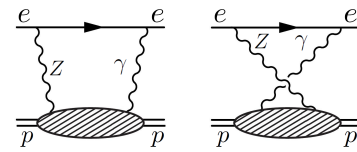
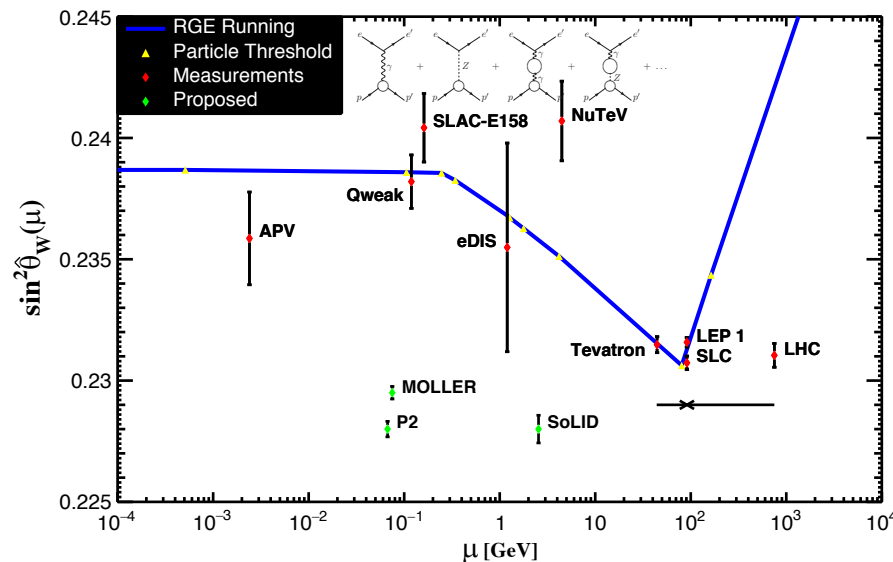
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Known kinematical functions

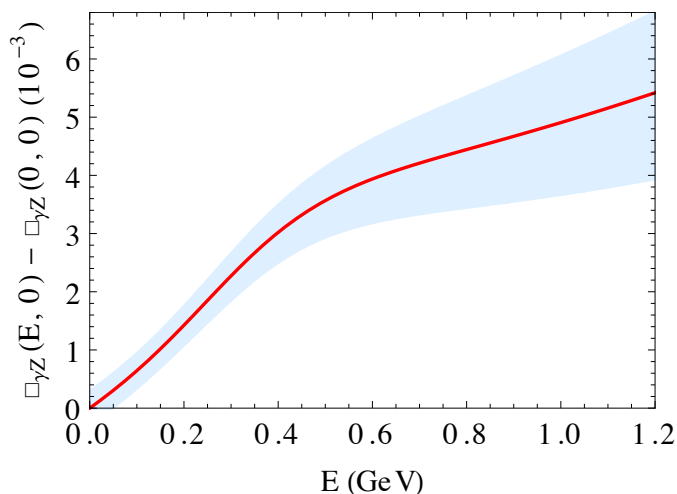
Inelastic structure functions (related to data)



Reference value: 1-loop SM  $Q_W^p(SM) = 0.0713 \pm 0.0008$

7.6% correction in Q-Weak kinematics  
- missed in the original analysis

$$\square_{\gamma Z}(E = 1.165 \text{ GeV}) = (5.4 \pm 2.0) \times 10^{-3}$$



**MG, Horowitz, PRL 102 (2009) 091806;**

Nagata, Yang, Kao, PRC 79 (2009) 062501;

Tjon, Blunden, Melnitchouk, PRC 79 (2009) 055201;

Zhou, Nagata, Yang, Kao, PRC 81 (2010) 035208;

Sibirtsev, Blunden, Melnitchouk, PRD 82 (2010) 013011;

Rislow, Carlson, PRD 83 (2011) 113007;

**MG, Horowitz, Ramsey-Musolf, PRC 84 (2011) 015502;**

Blunden, Melnitchouk, Thomas, PRL 107 (2011) 081801;

Rislow, Carlson PRD 85 (2012) 073002;

Blunden, Melnitchouk, Thomas, PRL 109 (2012) 262301;

Hall et al., PRD 88 (2013) 013011;

Rislow, Carlson, PRD 88 (2013) 013018;

Hall et al., PLB 731 (2014) 287;

**MG, Zhang, PLB 747 (2015) 305;**

Hall et al., PLB 753 (2016) 221;

**MG, Spiesberger, Zhang, PLB 752 (2016) 135;**

**Erler, MG, Koshchii, Seng, Spiesberger, PRD100 (2019), 053007**

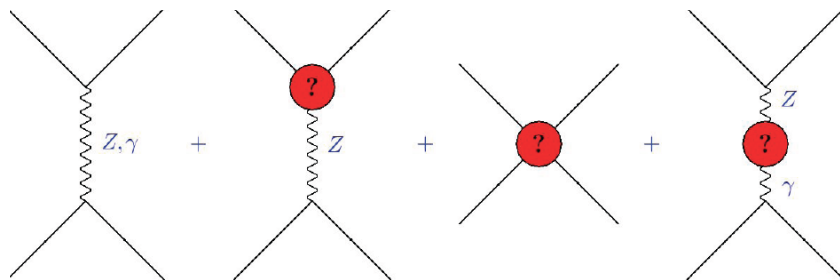
Steep energy dependence observed - added strong motivation for P2 @ MESA

$$\square_{\gamma Z}(E = 0.155 \text{ GeV}) = (1.1 \pm 0.3) \times 10^{-3}$$

The model dependence: no or very little inelastic PVES data available

This project has received funding from the European Union's Horizon 2020 research and innovation programme under grant agreement No 824093.





Extra Z

Mixing with  
Dark photon or  
Dark Z

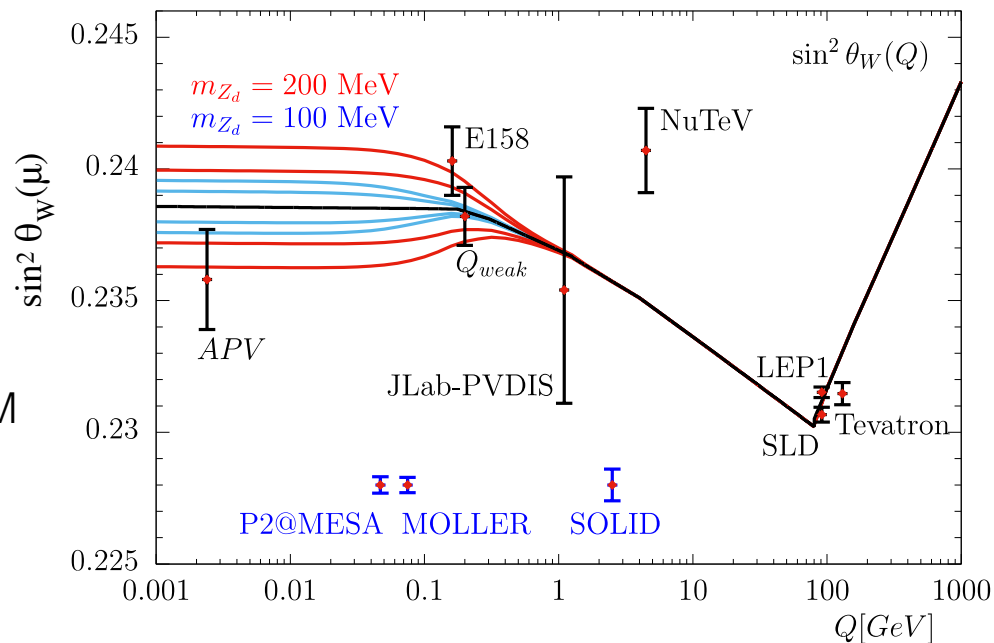
Contact interaction

New  
Fermions

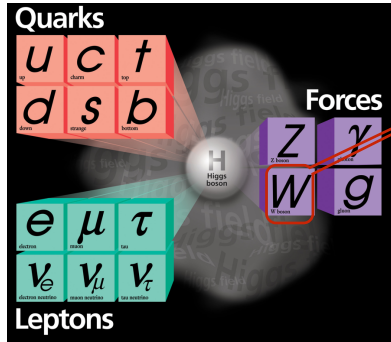
Heavy BSM reach: up to 50 TeV  
Light dark gauge sector: down to 70 MeV  
**Complementary to colliders**

P2@MESA will set stringent constraints on BSM

Precision comparable to Z-pole @ colliders

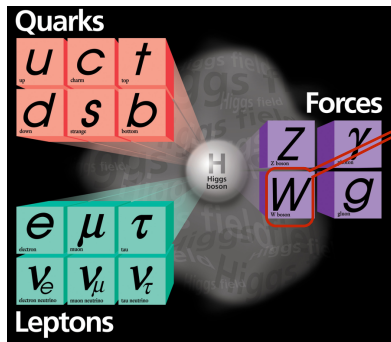


# Precision determination of $V_{ud}$

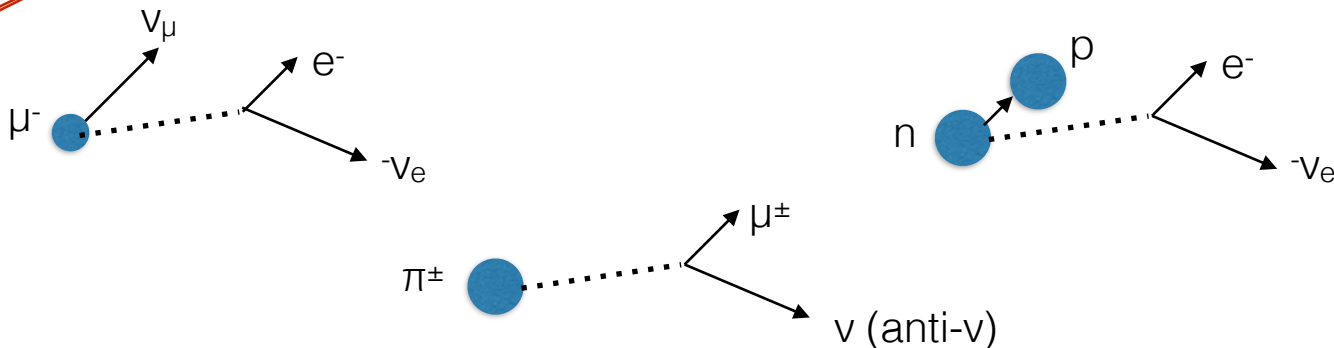


Charged current interaction -  $\beta$ -decay ( $\mu$ ,  $\pi^\pm$ ,  $n$ )

# Precision determination of $V_{ud}$



Charged current interaction -  $\beta$ -decay ( $\mu$ ,  $\pi^\pm$ ,  $n$ )



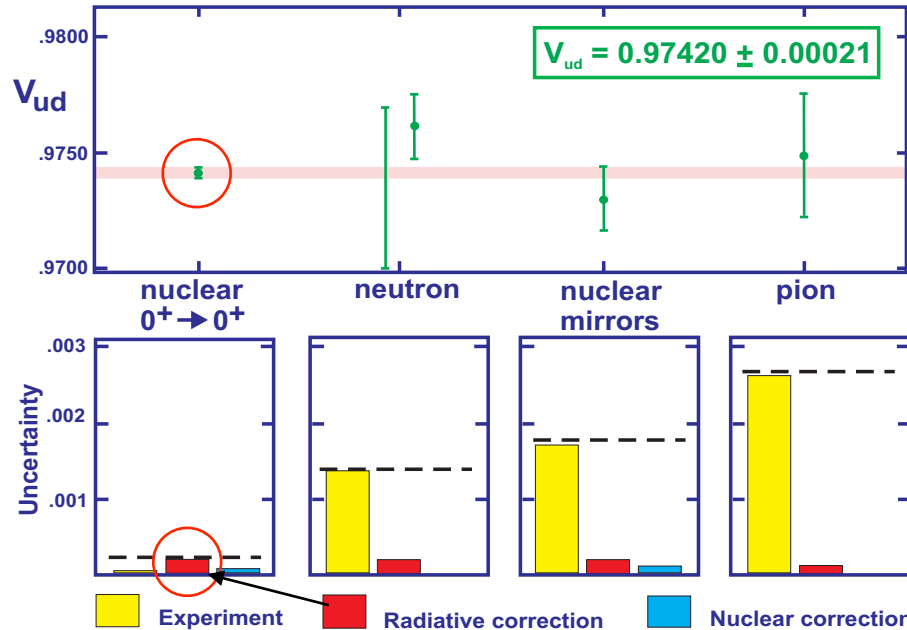
W coupling to leptons and hadrons very close but not exactly the same:  
quark mixing - Cabbibo-Kabayashi-Maskawa matrix

$$\begin{pmatrix} d' \\ s' \\ b' \end{pmatrix} = \begin{pmatrix} V_{ud} & V_{us} & V_{ub} \\ V_{cd} & V_{cs} & V_{cb} \\ V_{td} & V_{ts} & V_{tb} \end{pmatrix} \begin{pmatrix} d \\ s \\ b \end{pmatrix} = V_{CKM} \begin{pmatrix} d \\ s \\ b \end{pmatrix}$$

CKM - Determines the relative strength of the weak CC interaction of quarks vs. that of leptons

CKM unitarity - measure of completeness of the SM:  $|V_{ud}|^2 + |V_{us}|^2 + |V_{ub}|^2 = 1$

# $V_{ud}$ and CKM unitarity in early 2018

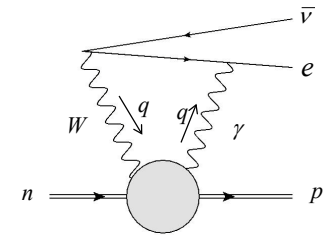


From neutron decay

$$|V_{ud}|^2 = \frac{5099.34s}{\tau_n(1 + 3g_A^2)(1 + \Delta_R)}$$

From superallowed decays

$$|V_{ud}|^2 = \frac{2984.43s}{\mathcal{F}t(1 + \Delta_R^V)}$$



Model dependence resides in  $\gamma W$ -box  $\Delta_R^V = 2\Box_{\gamma W}^{A \times V} + \dots$

Previous calculation of  $\gamma W$ -box: **Marciano & Sirlin 2006**

$$|V_{ud}|^2 + |V_{us}|^2 + |V_{ub}|^2 = 0.9994 \pm 0.0005$$

$0^+ \rightarrow 0^+$  nuclear decays

$$|V_{ud}|^2 = 0.94906 \pm 0.00041$$

Kl3 and Kl2 average

$$|V_{us}|^2 = 0.05031 \pm 0.00022$$

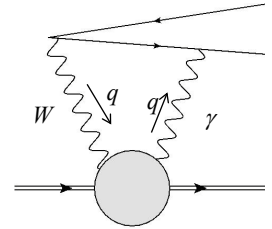
B decays

$$|V_{ub}|^2 = 0.00002$$

CKM unitarity:  $V_{ud}$  the main contributor to the sum and to the uncertainty

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$$T_{\gamma W} = \sqrt{2}e^2 G_F V_{ud} \int \frac{d^4 q}{(2\pi)^4} \frac{\bar{u}_e \gamma^\mu (\not{k} - \not{q} + m_e) \gamma^\nu (1 - \gamma_5) v_\nu}{q^2 [(k - q)^2 - m_e^2]} \frac{M_W^2}{q^2 - M_W^2} T_{\mu\nu}^{\gamma W}$$



Hadronic tensor: two-current correlator  $T_{\gamma W}^{\mu\nu} = \int dx e^{iqx} \langle f | T[J_{em}^\mu(x) J_W^{\nu,\pm}(0)] | i \rangle$

General gauge-invariant decomposition of a spin-independent tensor

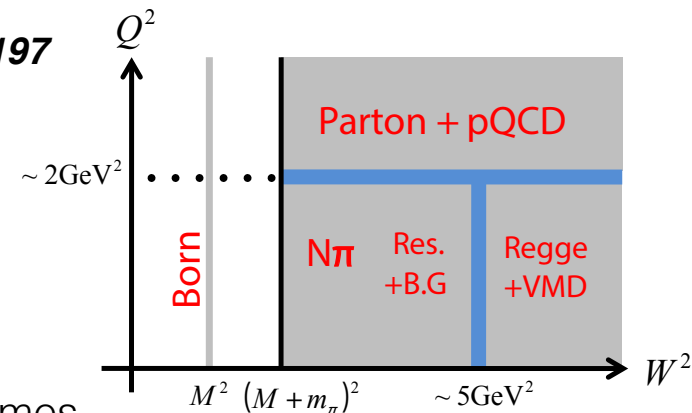
$$T_{\gamma W}^{\mu\nu} = \left( -g^{\mu\nu} + \frac{q^\mu q^\nu}{q^2} \right) T_1 + \frac{1}{(p \cdot q)} \left( p - \frac{(p \cdot q)}{q^2} q \right)^\mu \left( p - \frac{(p \cdot q)}{q^2} q \right)^\nu T_2 + \frac{i\epsilon^{\mu\nu\alpha\beta} p_\alpha q_\beta}{2(p \cdot q)} T_3$$

$\gamma W$  box from DR **Seng, MG, Patel, Ramsey-Musolf, 1807.10197**

$$\text{Re } \Box_{\gamma W}^{\text{even}} = \frac{\alpha}{\pi N} \int_0^\infty dQ^2 \int_{\nu_{thr}}^\infty d\nu \frac{F_3^{(0)}}{M\nu} \frac{\nu + 2q}{(\nu + q)^2}$$

Include dispersion in energy;  
Connection to data established

Explicit matching between nuclear, hadronic and pQCD regimes



Input into the integral was related to neutrino data on Gross-Llewellyn-Smith sum rule

Gross-Llewellyn-Smith sum rule  $\int_0^1 dx (u_v^p(x) + d_v^p(x)) = 3$

At sub-asymptotic  $Q^2$  receives pQCD corrections

$$M_3^{WW}(1, Q^2) = 3(1 - \alpha_s/\pi - \dots)$$

$$M_3^{WW}(1, Q^2)$$



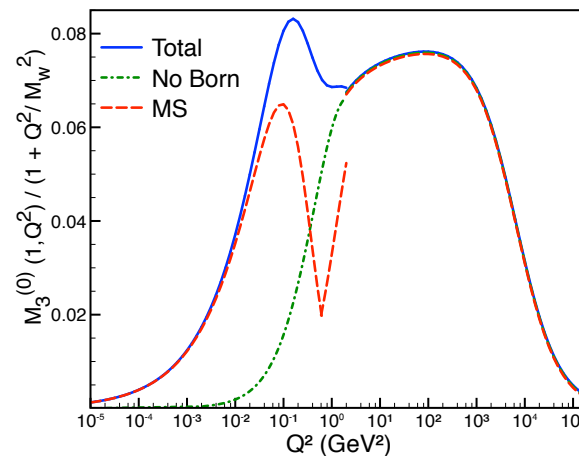
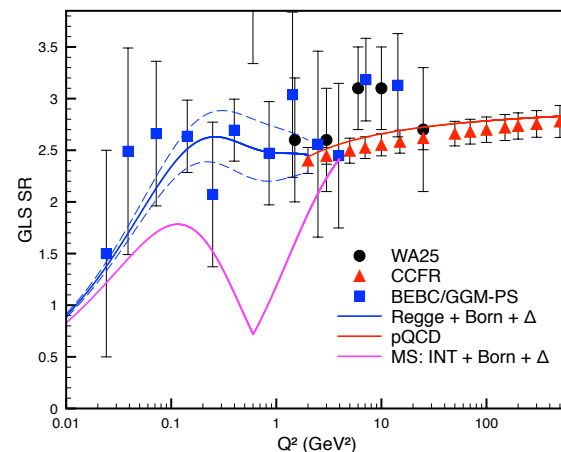
Isospin symmetry

$$M_3^{VW}(1, Q^2)$$

**MS 2006:**  $\Delta_R^V = 0.02361(38)$   $|V_{ud}| = 0.97420(10)_{Ft(18)_{RC}}$

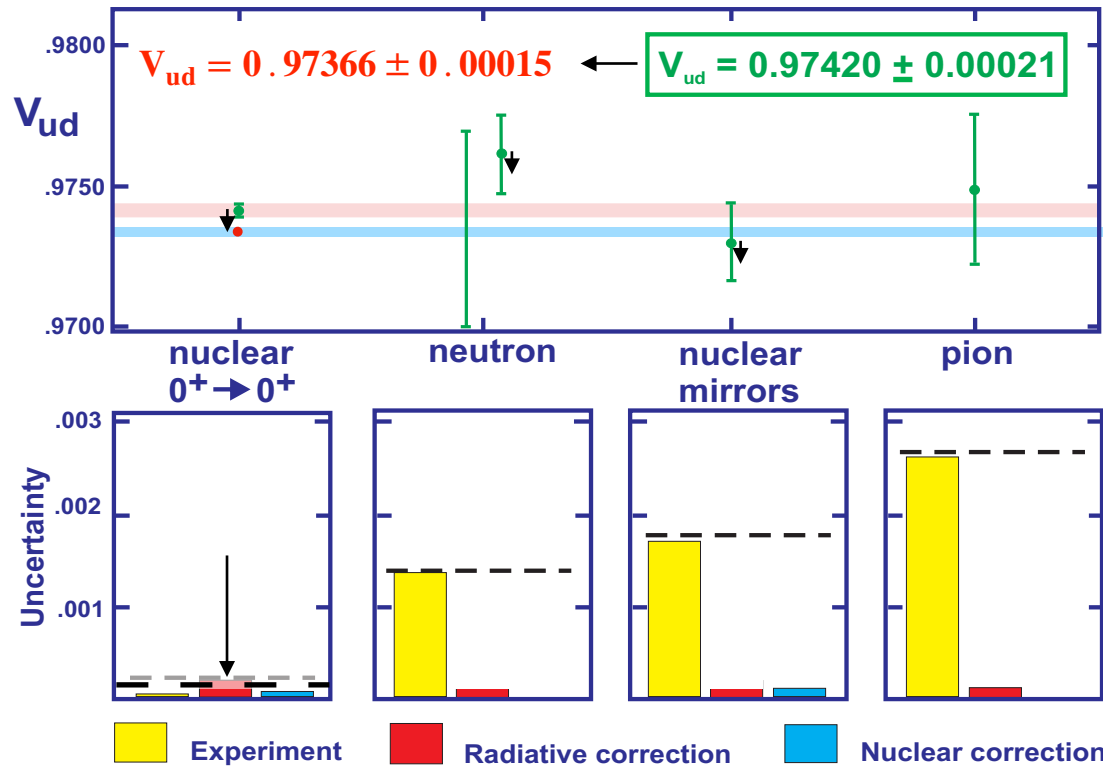
**DR:**  $\Delta_R^V = 0.02467(22)$   $|V_{ud}| = 0.97370(10)_{Ft(10)_{RC}}$

Uncertainty halved;  $3\sigma$  away from the old value



# CKM unitarity in Fall 2018 - $5\sigma$ deficit

Seng, MG, Patel, Ramsey-Musolf, 1807.10197



$$|V_{ud}|^2 + |V_{us}|^2 + |V_{ub}|^2 = 0.9979 \pm 0.0004$$

$0^+-0^+$  nuclear decays

$$|V_{ud}|^2 = 0.94801 \pm 0.00029$$

CKM unitarity:  $V_{ud}$  und  $V_{us}$  contribute equally to the uncertainty

Kl3 decays

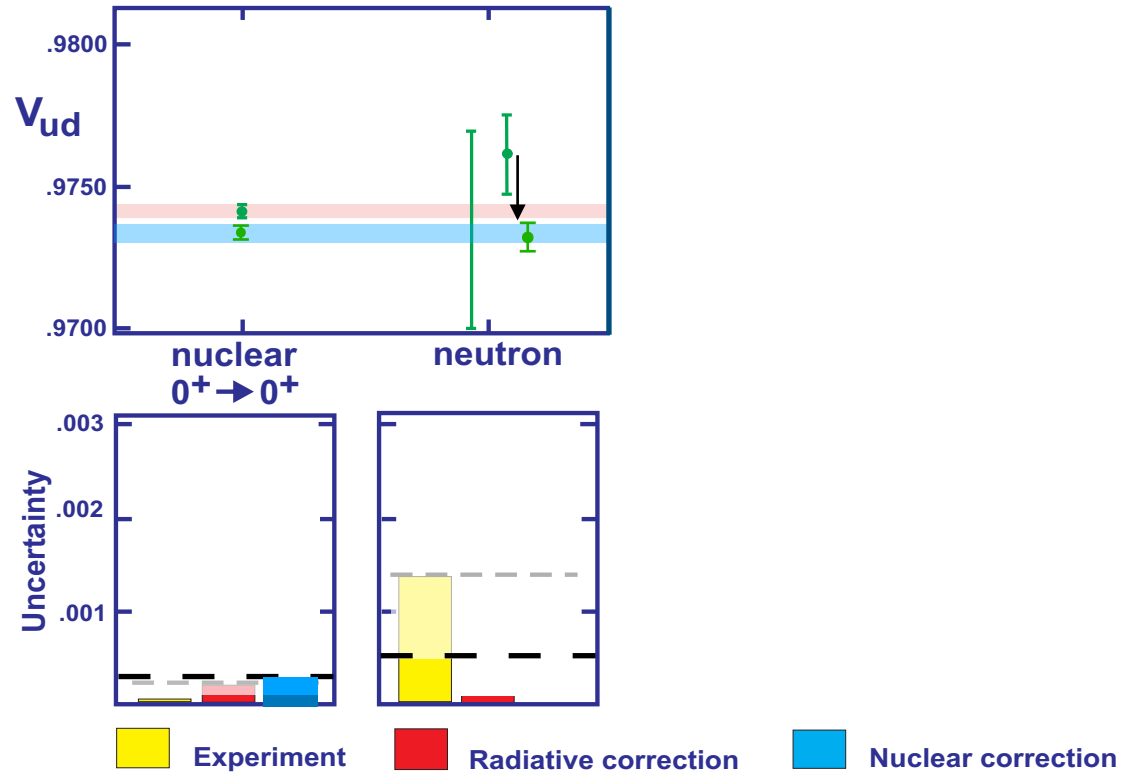
$$|V_{us}|^2 = 0.04987 \pm 0.00027$$

**Bazavov et al. (FNAL/MILC), 1809.02827**

This project has received funding from the European Union's Horizon 2020 research and innovation programme under grant agreement No 824093.

# STRONG CKM unitarity in December 2018 - $3\sigma$ deficit

## 2020



This project has received funding from the European Union's Horizon 2020 research and innovation programme under grant agreement No 824093.



Major improvement in exp. determination of  $g_A$

PDG2018

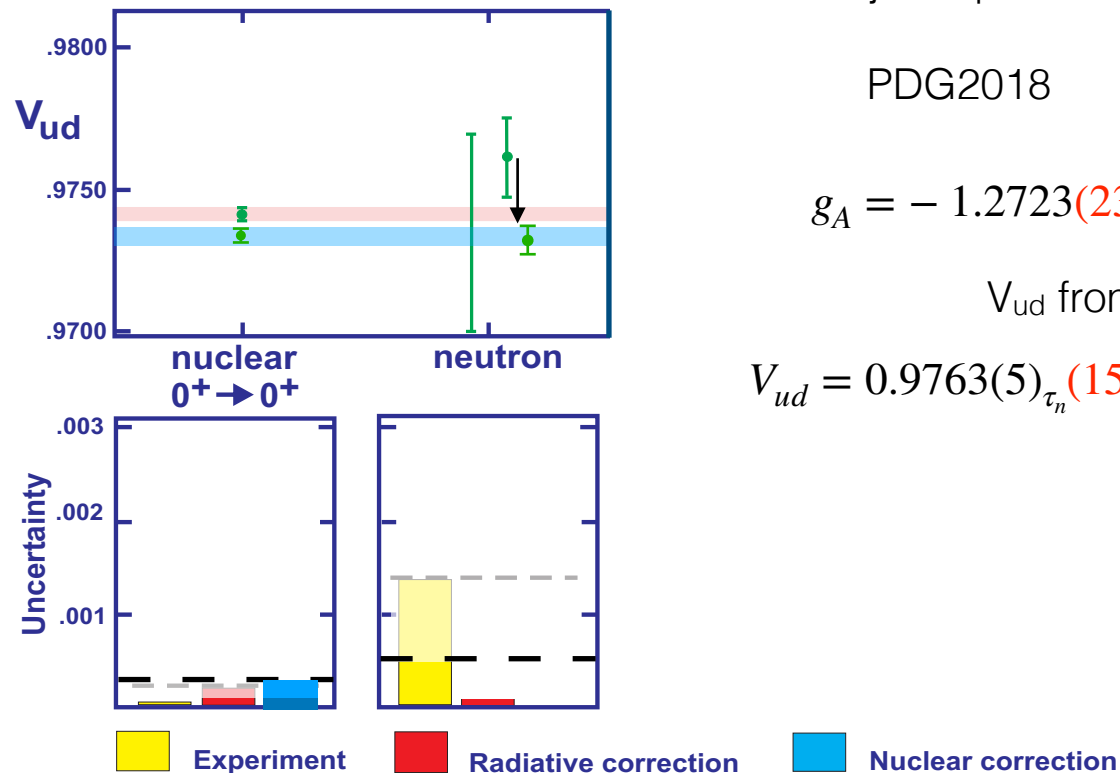
PERKEO-III

**Märkisch et al., 1812.04666**

$$g_A = -1.2723(23) \longrightarrow g_A = -1.2764(6)$$

$V_{ud}$  from free neutron decay

$$V_{ud} = 0.9763(5)_{\tau_n(15)}_{g_A(2)_{RC}} \longrightarrow V_{ud} = 0.9735(5)_{\tau_n(3)}_{g_A(1)_{RC}}$$



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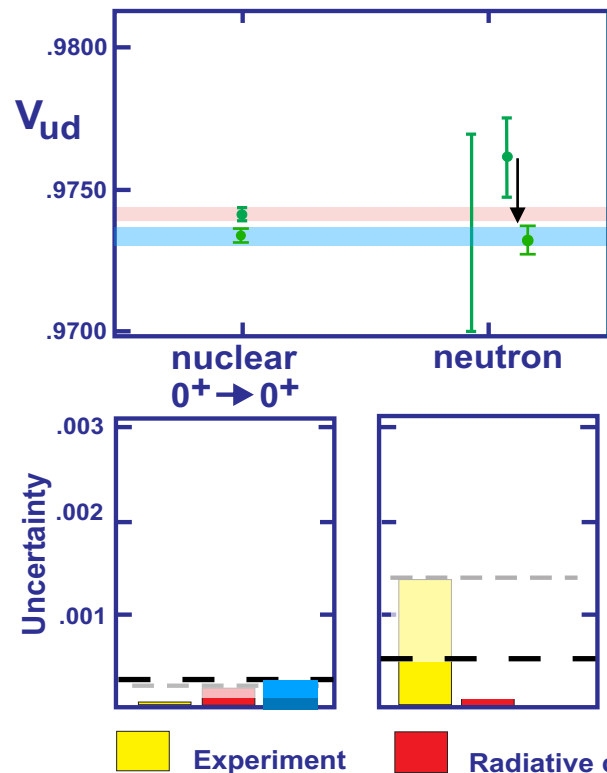
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Revision of nuclear corrections to  $0^+ \rightarrow 0^+$ -beta decay

**Seng, MG, Ramsey-Musolf, 1812.03352; MG 1812.04229**

$$V_{ud} = 0.97366(10)_{Ft(10)_{RC}} \longrightarrow V_{ud} = 0.97366(32)_{Ft(10)_{RC}}$$



Major improvement in exp. determination of  $g_A$

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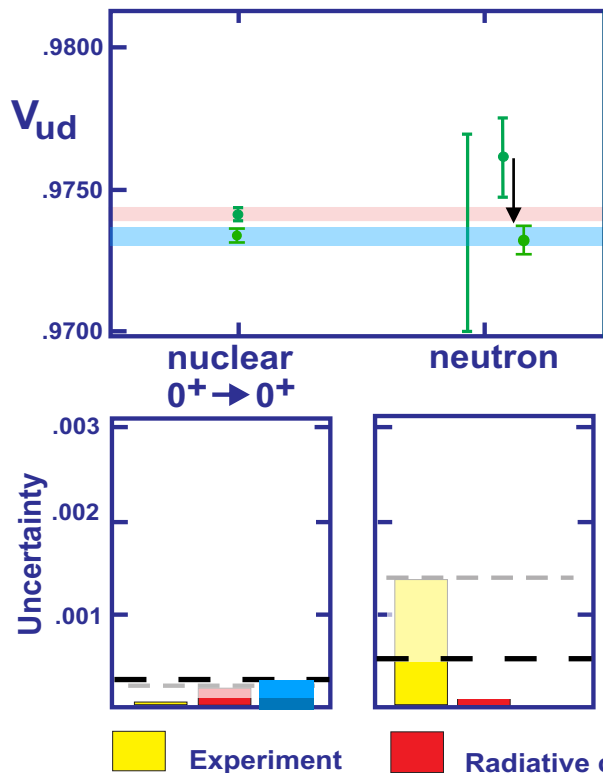
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Free neutron decay becomes competitive -  $\tau_n$ !  
 Scrutiny of nuclear corrections with new methods  
 BSM: superallowed nuclear decays  
 - main constraint on new S,T interactions!

Top-row unitarity: 2,5-3,5 $\sigma$  deficit

$$\Delta_u = -(0.0016 - 0.0021) \pm 0.0006$$

(depending on  $V_{us}$ )

This project has received funding from the European Union's Horizon 2020 research and innovation programme under grant agreement No 824093.

Input necessary for EW box calculations

- structure functions with vector and axial weak current

$$\text{Im}\langle N|T[J_Z^\mu J_\gamma^\nu]|N\rangle = \sum_X \rho_X \langle N|J_Z^\mu|X\rangle \langle X|J_\gamma^\nu|N\rangle$$

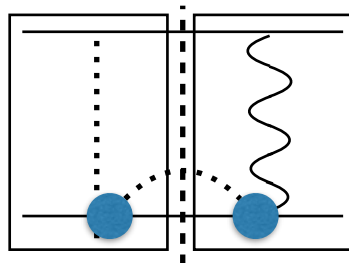
$$\text{Im}\langle N|T[J_W^\mu J_\gamma^\nu]|N\rangle = \sum_X \rho_X \langle N|J_W^\mu|X\rangle \langle X|J_\gamma^\nu|N\rangle$$

Saturate the dispersion integral with exclusive channels at low-energies, match onto pQCD, Regge  
MAID — existing Mainz web-based partial wave analysis of PS meson e.m. production

Proposed weak MAID

Needed at

$Q^2 < 2 \text{ GeV}^2$ ,  $W < 4 \text{ GeV}$



$X = \pi N, \eta N, \eta' N, K\Lambda, K\Sigma$

Existing e.-m. MAID

$Q^2 < 2 \text{ GeV}^2$ ,  $W < 2 \text{ GeV}$

To saturate the dispersion integral for EW boxes extend MAID to include multi-pion,  $KK$ -bar, ...

Has only been attempted in simple models - need to do better!

Currently: the absolute and relative strength of  $\gamma(Z,W)N \rightarrow \rho N, \omega N, \phi N$  channels for  $W > 2 \text{ GeV}$  is used to constrain the HE continuum contribution to EW boxes within VDM - Regge model  
- main uncertainty in the  $\gamma Z$ - and  $\gamma W$ -box (vector, axial NC, CC currents)

- WP tasks:
- Task 1: Hadronic effects in precision tests of the weak sector of SM
  - Task 1.1: Electroweak MAID
  - Task 1.2: New neutrino pion-production MC simulator for DUNE, T2HK
  - Task 1.3: Electroweak box correction calculations for PVES and  $\beta$ -decay
- Task 2: Hadronic effects in precision tests of the electromagnetic sector of the Standard Model
  - Task 2.1: Database for hadronic VP + contribution to  $(g - 2)_\mu$
  - Task 2.2: Database for hadronic LbL + contribution to  $(g - 2)_\mu$

To provide improved calculations:

new data if these directly determine the integrand of DR (HVP);

new methods to obtain input to DR from existing data (HLbL & EW boxes)

Plenary Meeting of PrecisionSM planned — **June 2-3, 2020 in Krakow, Poland**

- HVP and HLbL: new data (improved precision and coverage) + unified database
- Contact with HEP-DB group has been made; Alberto Lusiani is the Coordinator for submitting information to the database.
- First channel to submit data -  $e^+e^- \rightarrow \pi^+\pi^-$
- MUonE: test measurements at CERN were conducted; dedicated MC & RC developed; postdoc position funded by STRONG-2020 to be filled
- Electroweak MAID: MG officially joined the Mainz-Tuzla-Zagreb Collaboration; the MAID web platform will straightforwardly accommodate the new EW MAID; work has started with focus on the upcoming DUNE@FNAL kinematics; early 2020 visit to FNAL planned; postdoc position funded by STRONG-2020 to be filled.
- EW boxes: dispersion representation obtained; established connection to exp. data; first calculations already show very high impact on the field; plans for K13 decay

- Deliverables due for Reporting Period 1 (18 months, June 2019-November 2020): D21.1 is due M18 (November 2020)

Deliverable Number <sup>14</sup>	Deliverable Title	Lead beneficiary	Type <sup>15</sup>	Dissemination level <sup>16</sup>	Due Date (in months) <sup>17</sup>
D21.1	Electroweak MAID	9 - JGU MAINZ	Websites, patents filling, etc.	Public	18

- D21.1 Electroweak MAID - Task well on track (joined MAID collaboration, several publications towards EW MAID); postdoc position to be filled soon

- MS37 corresponding to D21.1 has to be achieved M18
- First EW MAID option will include  $\nu/\bar{\nu}$ -induced single pion production off nucleon
- Extended MAID energy range  $W < 5$  GeV (currently  $W < 2$  GeV)
- Pilot EW MAID website expected to run in fall 2020

Milestone number <sup>18</sup>	Milestone title	Lead beneficiary	Due Date (in months)	Means of verification
MS37	Weak MAID	9 - JGU MAINZ	18	Website up and running

- Summary: project work towards D21.1 and MS37 has started;
- At first stages of EW MAID local expertise in Mainz is sufficient
- Next steps will be done in a close collaboration with other nodes of JRA3 - Valencia, Krakow and Fermilab, involvement in JPAC@JLab is expected
- Dispersive formulation of RC to precision tests in context of this JRA have high impact on the field already