# Quantum Computing (QC) for many-body systems at the nucleonic scale or below: some current international status and recent examples

## **Denis Lacroix**



## Summary

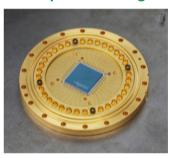
- Generalities
- Few examples of recent QC applications to nuclear/particle physics
- Example of international initiative: the US QC/QIS collaboration
- Discussion

## Some recent technical realizations



## Example

**RIGETTI superconducting 19 Qubit** 



## Limitations:

- ~ 50 qubits
- ~ 50 gates

IBM QX5 (16 qubits)

→ IBM Q Experience

(from G. Hagen)

~ 500 qubits

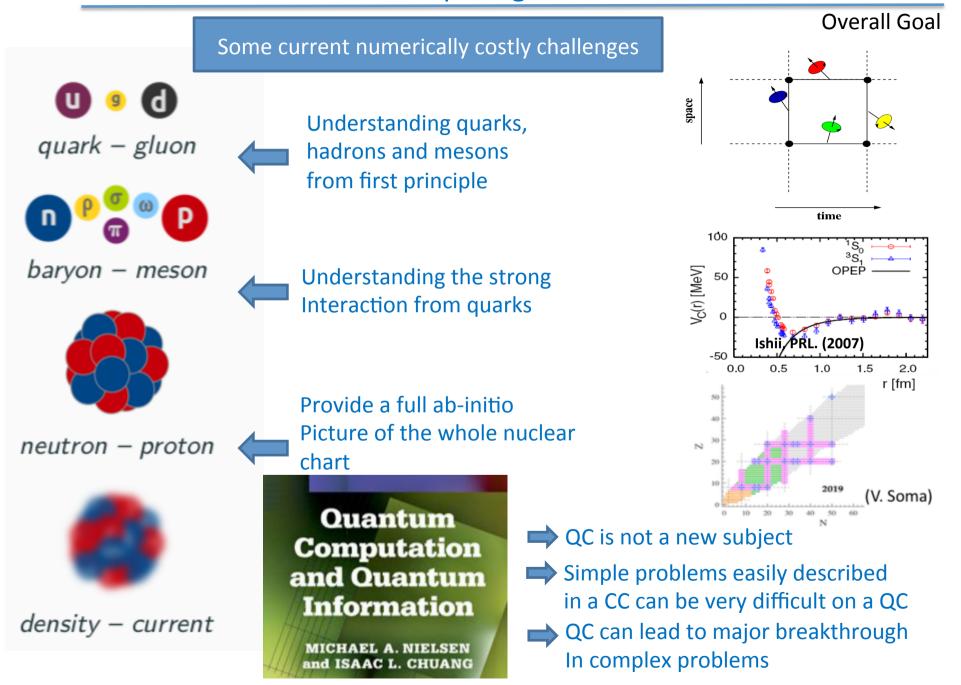
~ 500 gates

A timely period

There is a lot of excitement in this field due to substantial progress

- 1. Quantum processing units now have ten(s) of qubits
- 2. Businesses are driving this: Google, IBM, Microsoft, Rigetti, D-Wave, ...
- 3. Software is publicly available (PyQuil, XACC, OpenQASM, OpenFermion)
- 4. First real-world problems solved: H2 molecule on two gubits [O'Malley et al., Phys. Rev. X 6, 031007 (2016)]; BeH2 on six qubits [Kalandar et al., Nature 549, 242 (2017)]; ...

## Quantum Computing at the nucleon scale and below



## Strategy

Take a simple version of your favorite many-body problem



Map/formulate it as a problem with Qubit



Use standard QC algorithms or Propose new QC algorithms





Test on a QC emulator

Test on a true QC

### Constraint: -Work with a restricted number of operation

			controlled-NUT	<del></del>	$\begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 1 \\ 0 & 0 & 1 & 0 \end{bmatrix}$
			swap	×	$\begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}$
Hadamard	-H	$\frac{1}{\sqrt{2}} \begin{bmatrix} 1 & 1 \\ 1 & -1 \end{bmatrix}$	${\tt controlled-} Z$	·	$\begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & -1 \end{bmatrix}$
Pauli- $X$	-X	$\begin{bmatrix} 0 & 1 \\ 1 & 0 \end{bmatrix}$	controlled-phase	<u>-</u> [s]-	$\begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & i \end{bmatrix}$
Pauli- $Y$	- $Y$ $-$	$\left[ egin{matrix} 0 & -i \ i & 0 \end{array}  ight]$	T. W. V.		$\begin{bmatrix} 1 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 1 & 0 & 0 & 0 & 0 \end{bmatrix}$
Pauli– $Z$	- z	$\begin{bmatrix} 1 & 0 \\ 0 & -1 \end{bmatrix}$	Toffeli	<del></del>	$ \begin{bmatrix} 0 & 0 & 0 & 0 & 1 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 1 \\ 0 & 0 & 0 & 0 & 0 & 0 & 1 & 0 \end{bmatrix} $
Phase	-S	$\begin{bmatrix} 1 & 0 \\ 0 & i \end{bmatrix}$			$\begin{bmatrix} 1 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 1 & 0 & 0 & 0 & 0 \end{bmatrix}$
$\pi/8$	T	$\begin{bmatrix} 1 & 0 \\ 0 & e^{i\pi/4} \end{bmatrix}$	Fredkin (controlled-swap)	×	0 0 0 0 1 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0
			measurement		Projection onto $ 0\rangle$ and $ 1\rangle$
			qubit		wire carrying a single qubit (time goes left to right)
			classical bit		wire carrying a single classical bit
			n qubits	/-	wire carrying n qubits

- -Design new algorithms adapted to the many-body problem
- -Control the inherent quantum noise

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#### Cloud Quantum Computing of an Atomic Nucleus

E. F. Dumitrescu, <sup>1</sup> A. J. McCaskey, <sup>2</sup> G. Hagen, <sup>3,4</sup> G. R. Jansen, <sup>5,3</sup> T. D. Morris, <sup>4,3</sup> T. Papenbrock, <sup>4,3,\*</sup> R. C. Pooser, <sup>1,4</sup> D. J. Dean, <sup>3</sup> and P. Lougovski<sup>1,†</sup>

#### Schematic deuteron Hamiltonian in Harmonic basis

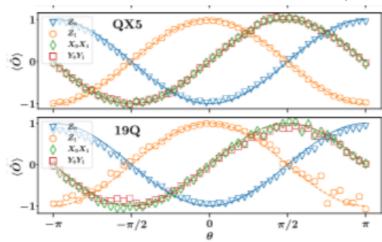
$$H_N=\sum_{n,n'=0}^{N-1}\langle n'|(T+V)|n
angle a_{n'}^{\dagger}a_n.$$
  $a_n^{\dagger}(a_n)$  create (annih.)  $n,n'=0,1,...N-1$  1 deuteron in  $|n
angle$ 

Use Pauli matrices+Jordan-Wigner transformation

$$a_n^{\dagger} \to \frac{1}{2} \left[ \prod_{j=0}^{n-1} -Z_j \right] (X_n - iY_n)$$
 0 (1) particles in  $|n\rangle \longrightarrow |\uparrow\rangle (|\downarrow\rangle)$ 

This automatically map the Hamiltonian as a function of Pauli Matrix

Use the VQE quantum-classical algorithm with 10000 measurements on QX5 (19Q)



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#### $\sigma$ Models on Quantum Computers

Andrei Alexandru, 1,2,\* Paulo F. Bedaque, 2,† Henry Lammo, 2,‡ and Scott Lawrence 2,§

(NuQS Collaboration)

Start with the discretized  $\sigma$  model

$$\mathcal{H} = \sum_{r} \left( \frac{g^2}{2} \boldsymbol{\pi}(r)^2 + \frac{1}{2g^2 \Delta x^2} [\mathbf{n}(r+1) - \mathbf{n}(r)]^2 \right)$$

Map it to a Spin algebra (fuzzy sphere)

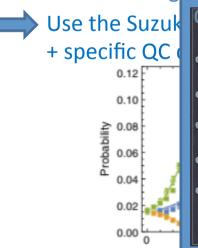
$$-\frac{g^2}{2}\nabla^2\psi\to H^0\Psi=\kappa\frac{g^2}{2}\sum_{k=1}^3\big[\mathbb{J}_k,\big[\mathbb{J}_k,\Psi\big]\big],$$

 $J_k$  are generators of the SU(2) algebra

"only" j=1/2 was considered

$$j_1 = 1 \otimes \sigma_2/\sqrt{3}$$
,  $j_2 = \sigma_2 \otimes \sigma_3/\sqrt{3}$ ,  $j_3 = \sigma_2 \otimes \sigma_1/\sqrt{3}$ ,

This gives the link with Pauli matrices



## Use the Suzuk GAUGE THEORIES FOR QUANTUM COMPUTING

Very limited studies exist, e.g.:

- 1+1 D QED (Schwinger model) on a few-qubit trapped-ion quantum computer (E. A. Martinez et al., Nature 534 (2016) 516, arXiv: 1605.045701
- Quantum-Classical calculation of Schwinger Model [N. Klco et al., Phys. Rev. A 98 (2018) 032331, arXiv:1803.03326]
- U(1) lattice gauge theory without matter in 2 & 3 spatial dimensions (D. Kaplan, J. Stryker, arXiv:1806.08797)
- Zeta-regularized vacuum expectation values [T. Hartung, K. Jansen, arXiv:1808.06784]
- 0(3) nonlinear sigma model in 1+1 dimensions

Extending the studies to 2+1 dimensions is extremely hard and has not been established yet on quantum devices

(from M. constantinou, Santa Fe)

## International context

Illustration of the QC/QIS for nuclear theory project (USA)

Nov. 2017

Early INT-Seattle workshop on Quantum Computing for Nuclear Physics

Decision for a pre-pilot project granted by DOE





































Quantum Information Science and Quantum Computing have the potential to enable breakthrough discoveries in nuclear physics and alter paradigms in theoretical research in disruptive ways. Our goal is to anticipate and prepare the community for these changes, and to identify opportunities to make rapid progress toward the Grand Challenges facing our field.

Jan. 2019

Sante Fe meeting of the QC/QIS for nuclear theory



Converge on the final project (5 years, size: 20 PostDoc, 30 PhD)

- Identify main areas-of-focus within NT, e.g.
  - Nuclear Structure and Reactions
  - Quantum Chromodynamics and Quantum Field Theories
  - Nuclear Astrophysics and the Early Universe
- close collaboration with qubit/quantum device/algorithm efforts at National Labs and Technology companies

## CERN Quantum Computing for High Energy Physics workshop

5-6 novembre 2018 CERN

Fuseau horaire Europe/Zurich

There is a live webcast for this event.

Rechercher...

Accueil

Ordre du jour

Liste des contributions

Inscription

Salles de visioconférence

Accommodation

How to get to CERN

#### **Motivations and Objectives**

The ambitious upgrade programme for CERN's Large Hadron Collider (LHC) will result in significant challenges related to information and communications technologies (ICTs) over the next decade and beyond. It is therefore vital that we — members of the high-energy physics (HEP) research community and beyond — keep looking for innovative technologies, so as to ensure that we can continue to maximise the discovery potential of the world-leading research infrastructures at our disposal. Technologies related to quantum computing hold the promise of substantially speeding up computationally expensive tasks.



#### Quantum computing

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June 12-14th

**PROGRAM** 

ProgramESNT\_QC\_NuclPhys\_June19.pdf

Quantum computing and scientific research: state of the art and potential impact in nuclear physics

## Some general concluding (personal) remarks

- Computation with QC is a very challenging/exciting challenge
- It is also intellectually satisfactory to think about our problem in a very different way
- It might ultimately lead to major breakthrough in different IN2P3 fields
- It also leads to natural synergies between public research and private companies
- There is nowadays emerging strong collaborations that start to work actively in the field
- (Rapid) actions if we want to be competitive? And major effort should be done to learn and be at the forefront of the field.
- Eventually this will not work...

Thank you ...