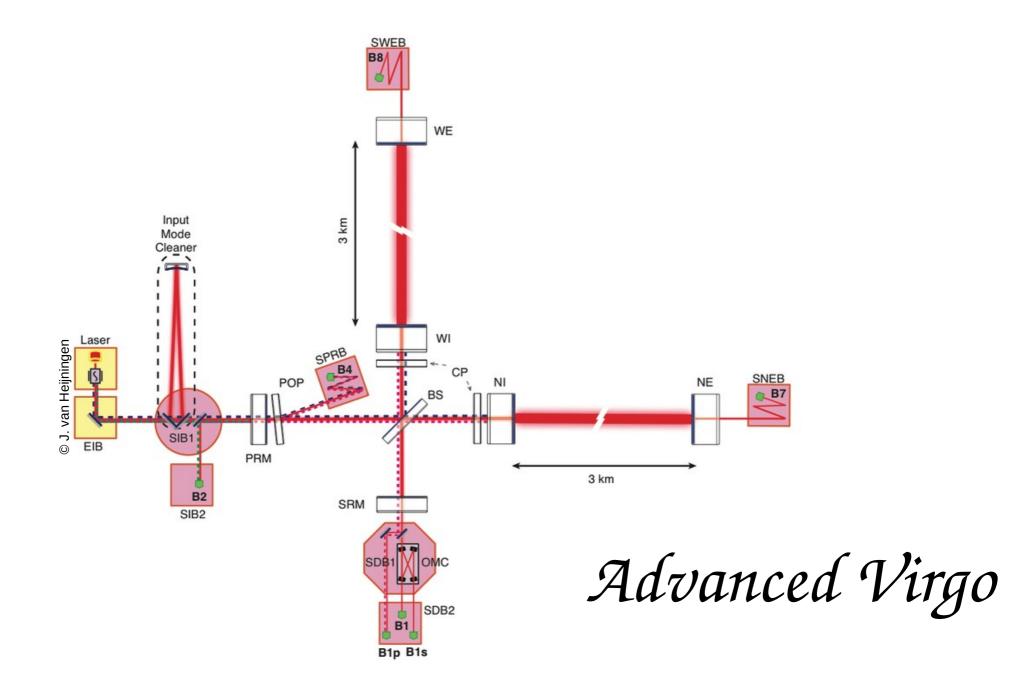
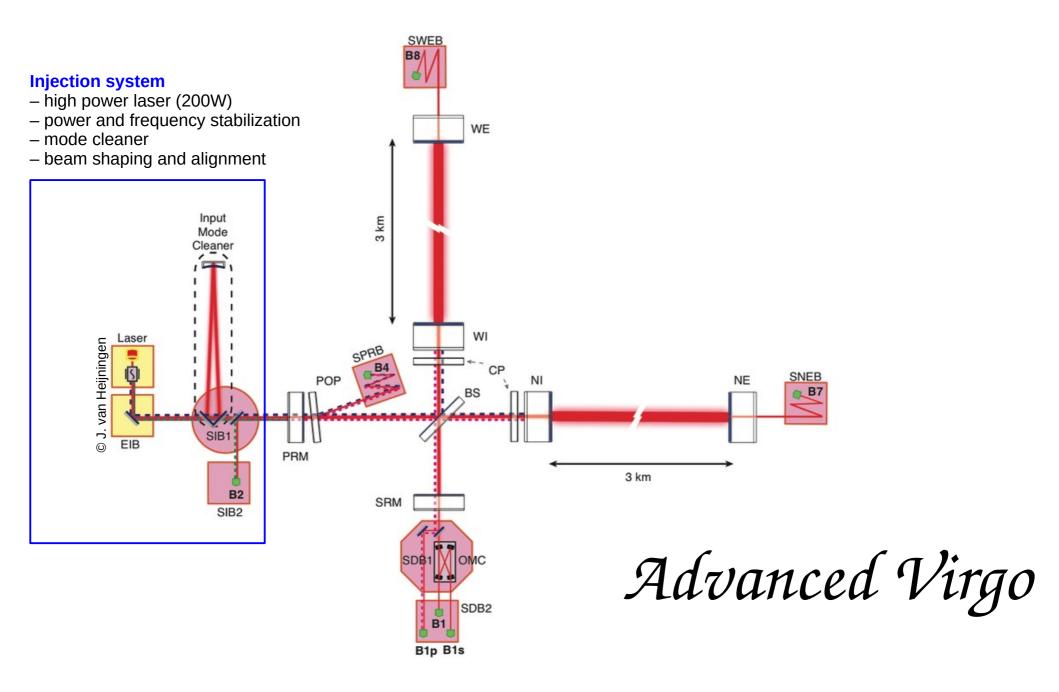
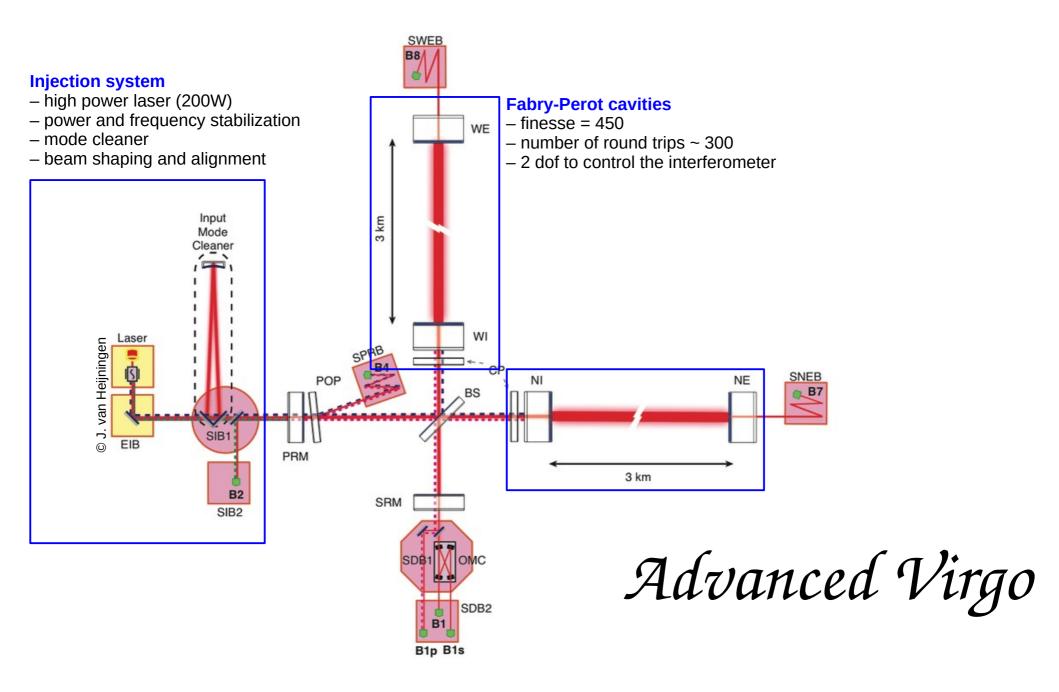


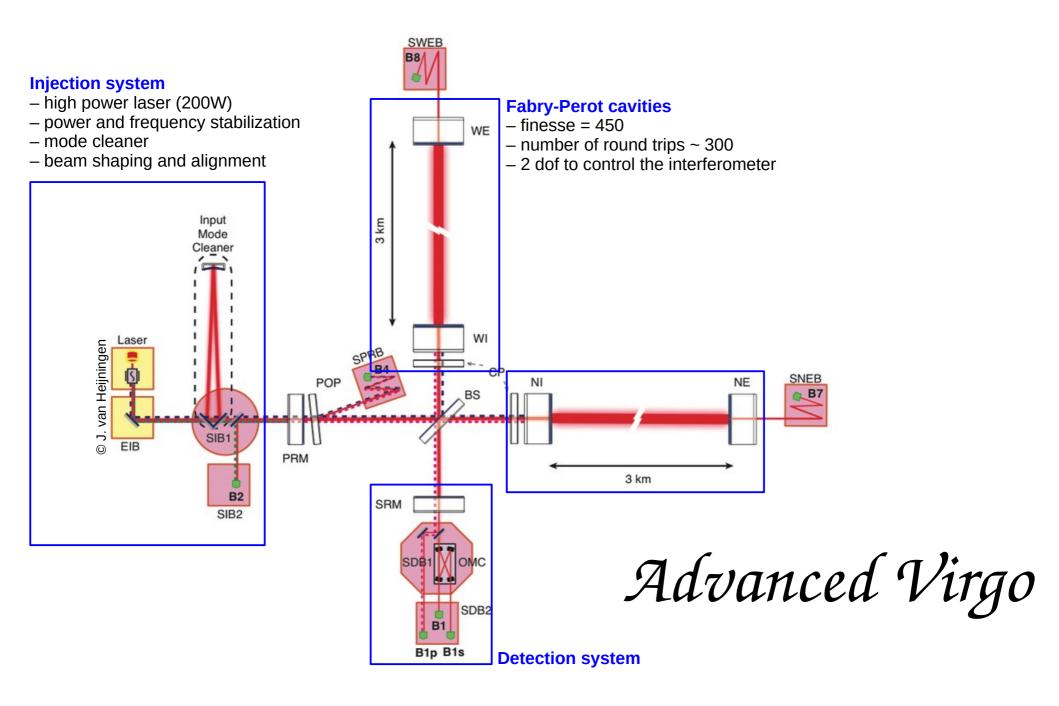
# Searches for gravitational-wave signals with ground-based interferometers

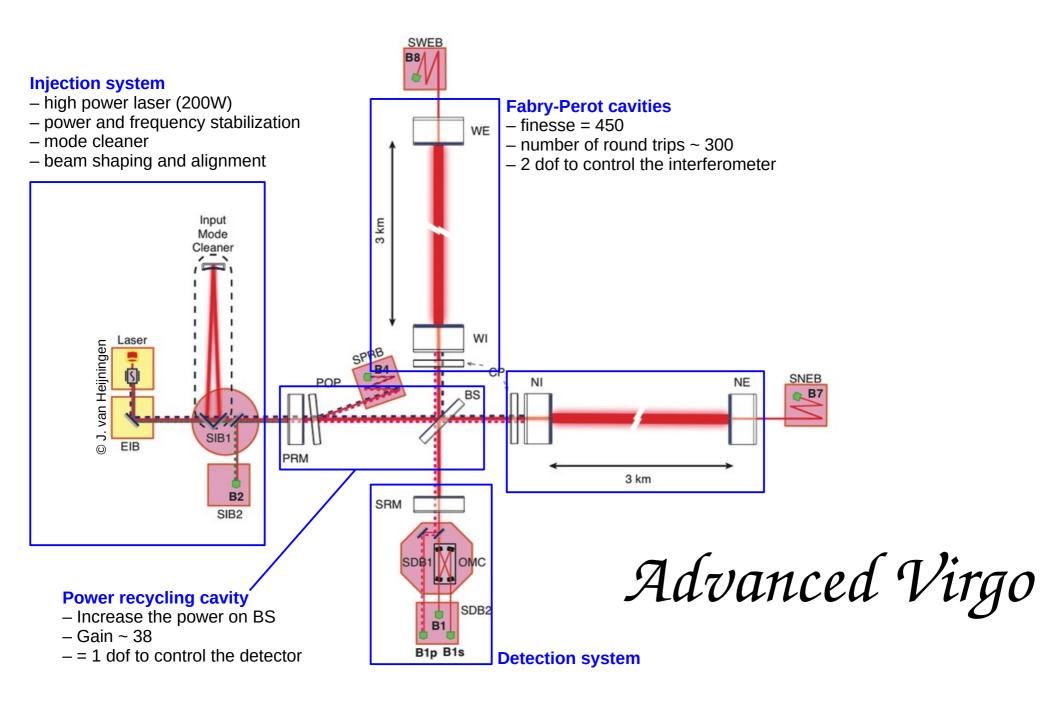
- Introduction: LIGO-Virgo gravitational-wave detectors
- Noise description
- Searching for:
  - → transient signals
  - → continuous signals
  - → stochastic backgrounds

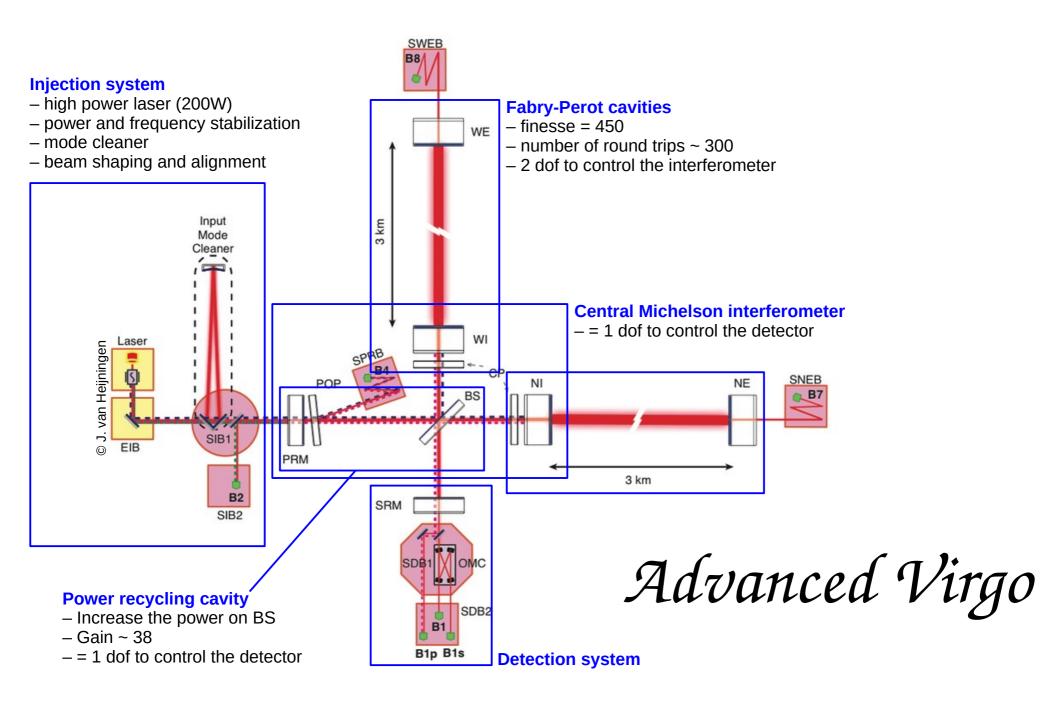


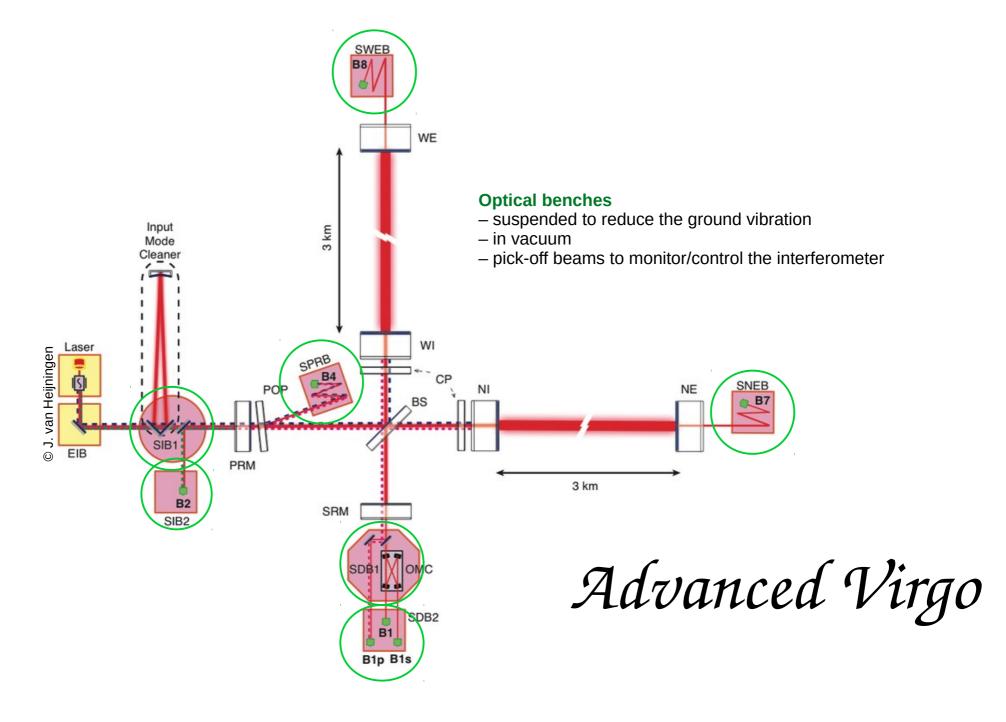


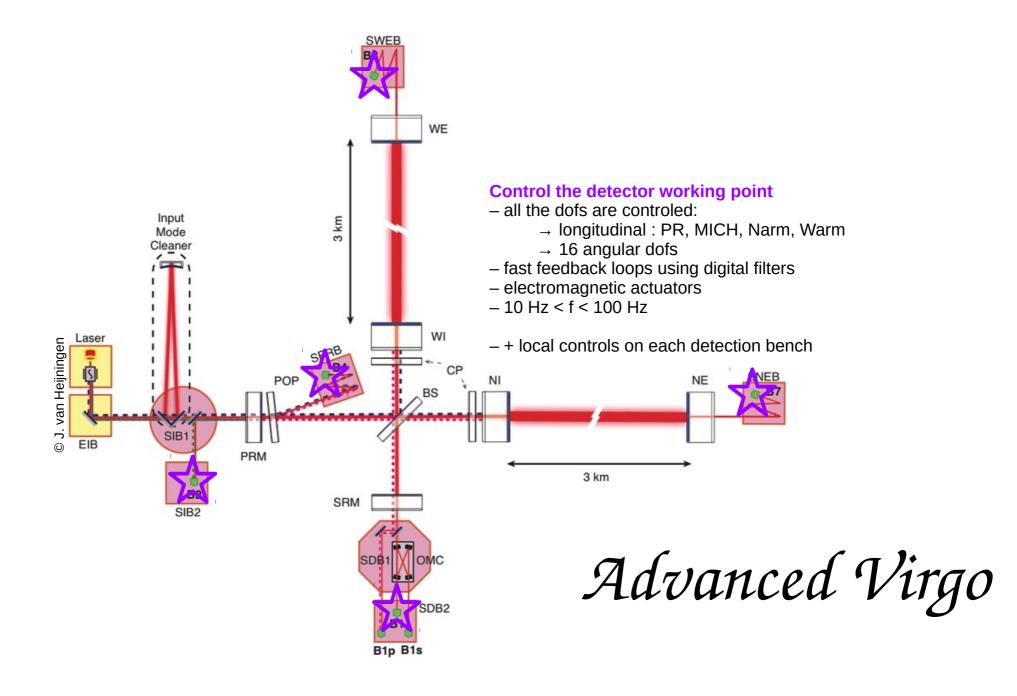


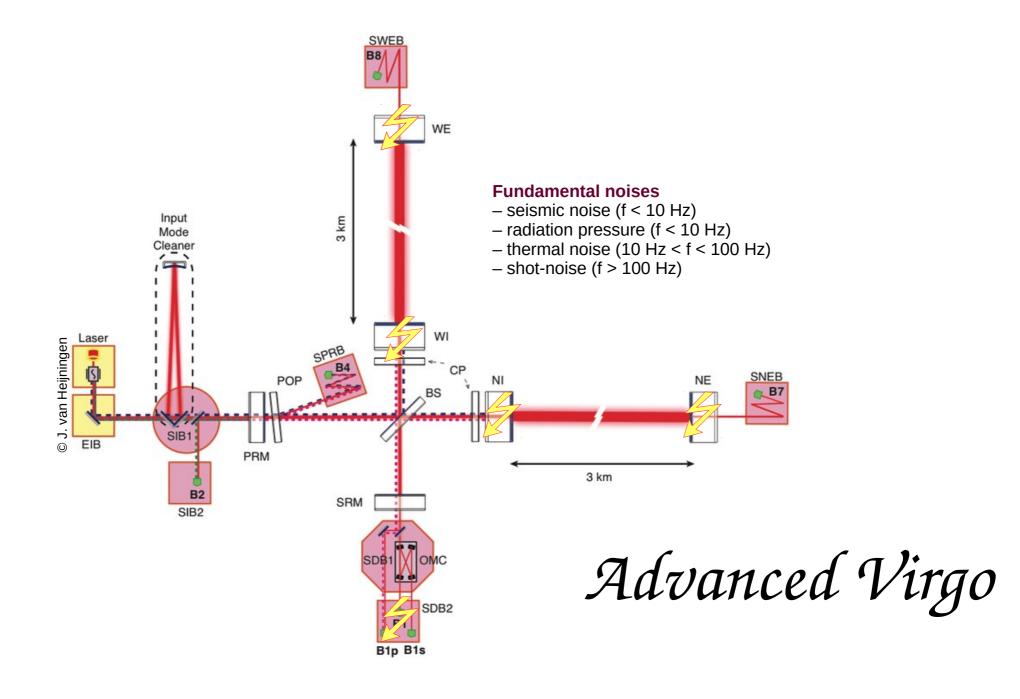


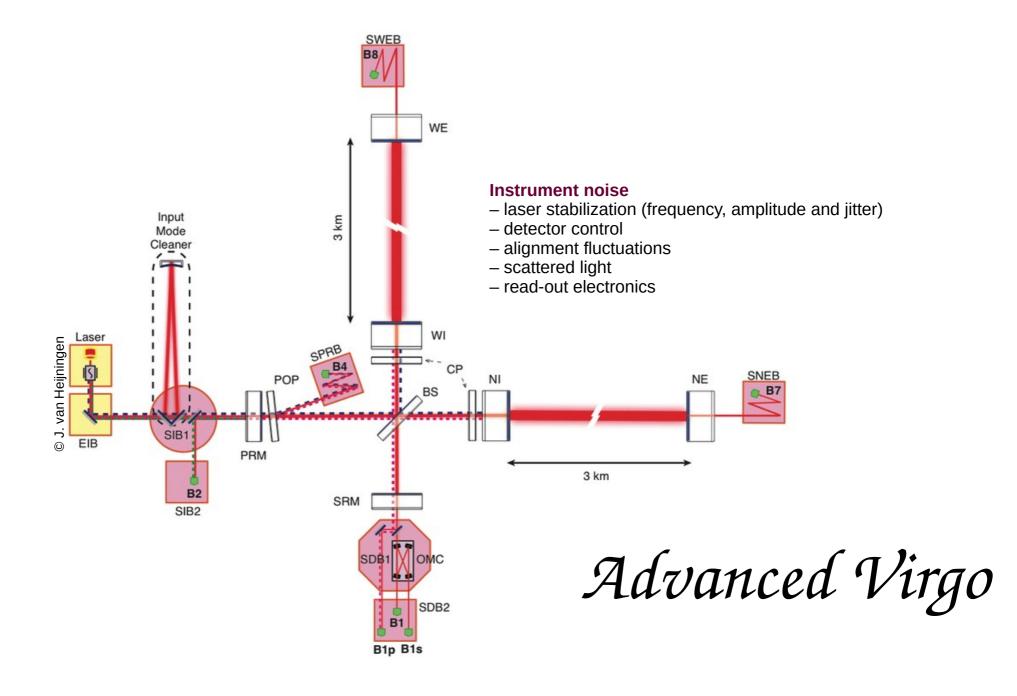


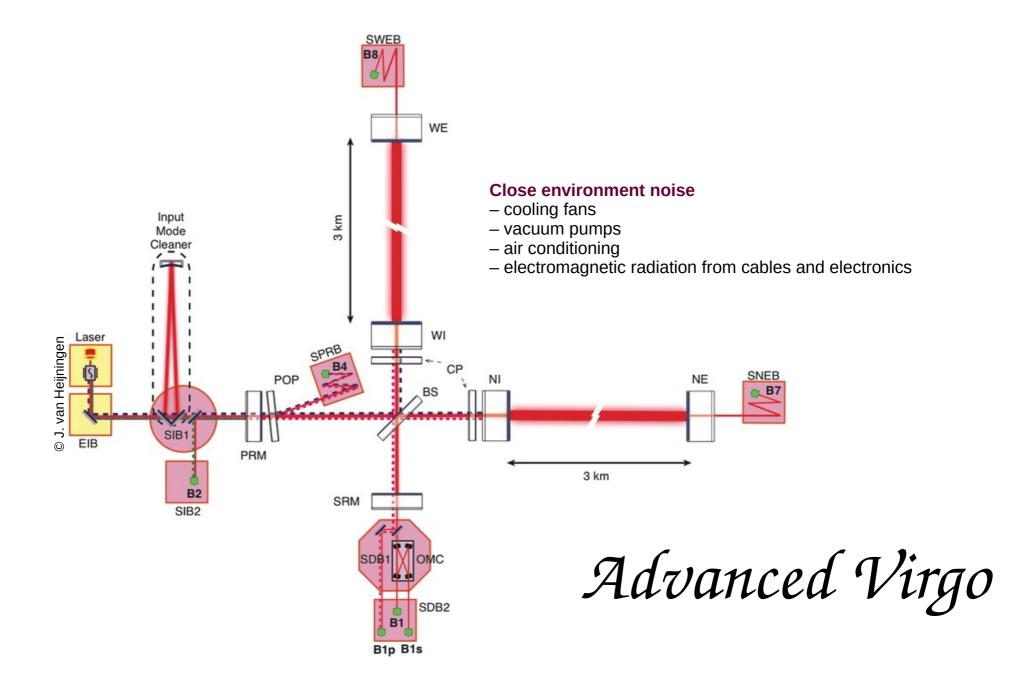


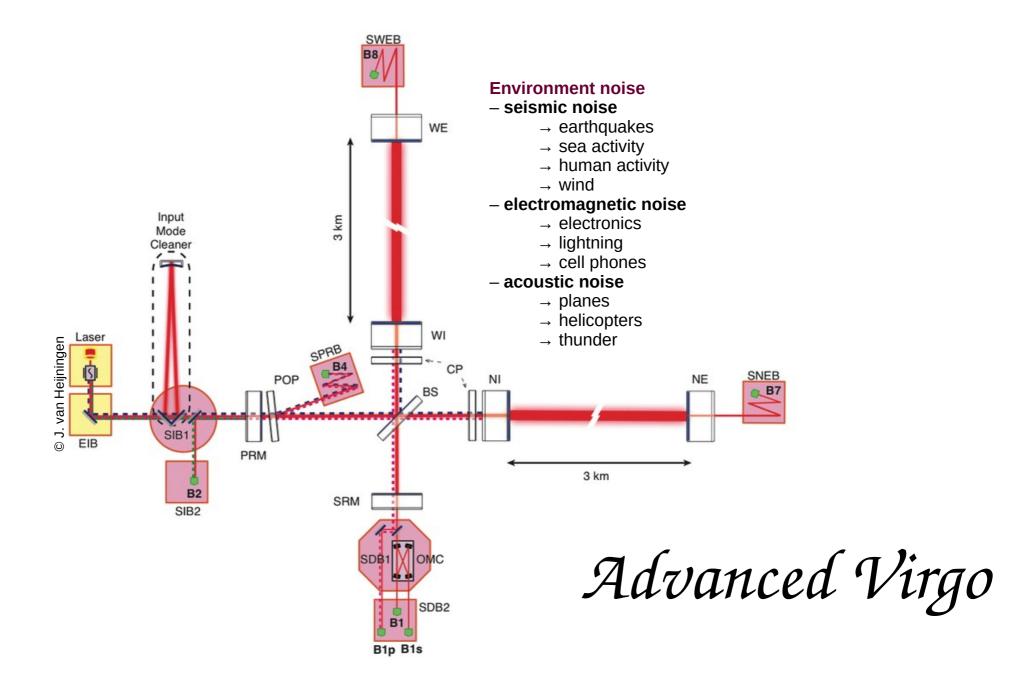








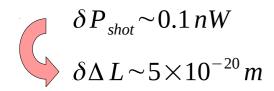




#### Detector response:

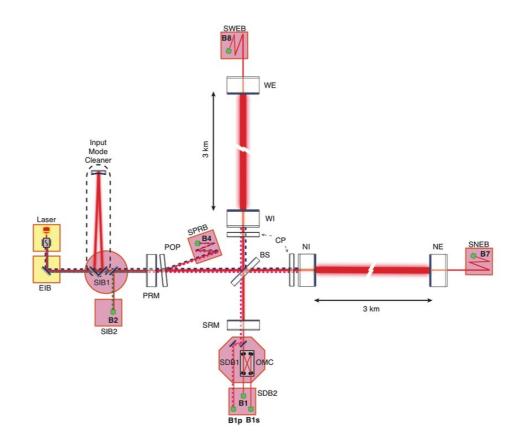
$$\delta P_o = G_{PR} P_i C \frac{2\pi}{\lambda} \sin\left(\frac{4\pi}{\lambda} \Delta L_0\right) \frac{2F}{\pi} \delta \Delta L$$

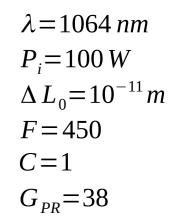
Typical shot noise at 50 mW:



Strain amplitude (reconstruction)

$$h = \frac{\delta \Delta L}{L_0} \sim 10^{-23}$$

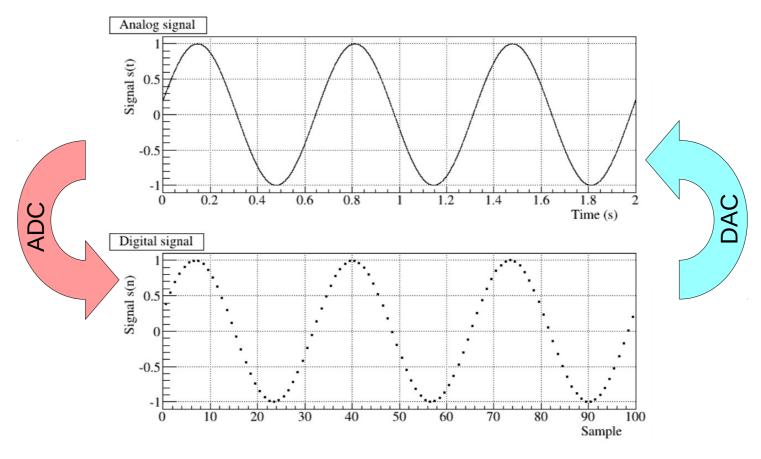






In reality the reconstruction is frequency dependent

# Signal digitization



- → The photodiode analog signal (a voltage) is digitized
- → The signal is processed numerically

$$\rightarrow h(t) \Rightarrow h[j] \quad t_{j+1} - t_j = 1/f_s$$

→ The strain amplitude time series is saved to disk

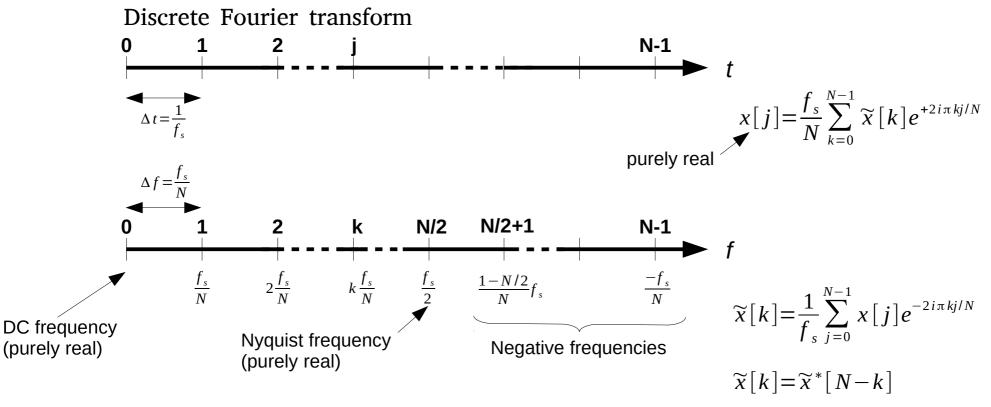
### Fourier transform

A time series s(t) can be projected over a basis of sinusoidal functions:

$$\widetilde{x}(f) = \int_{-\infty}^{\infty} x(t) e^{-2i\pi ft} dt$$
 (forward)

$$x(t) = \int_{-\infty}^{\infty} \widetilde{x}(f) e^{2i\pi f t} df \qquad \text{(backward)}$$

The signal is decomposed in characteristic frequencies



Power spectral density (PSD)

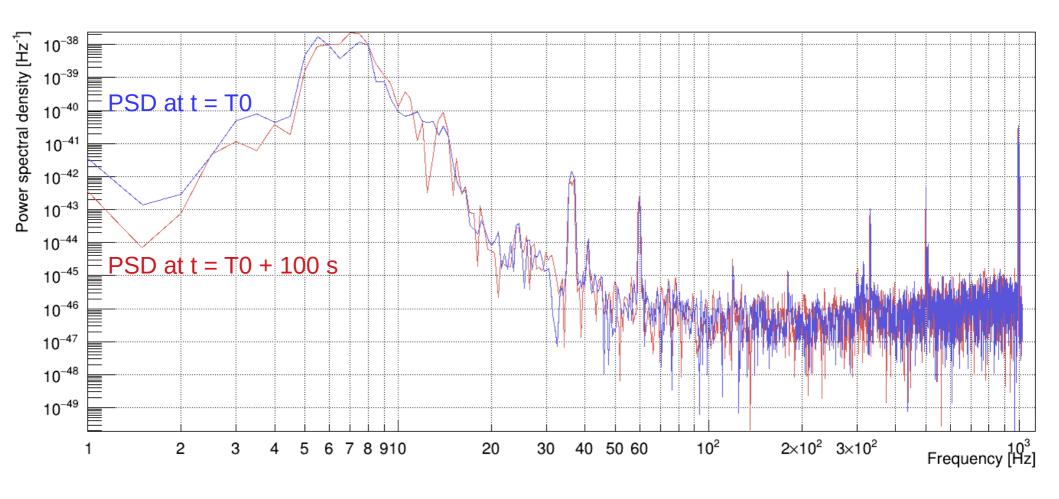
$$\lim_{T\to\infty}\frac{1}{T}|\widetilde{x_T}(f)|^2$$

Estimator for a finite data set: **periodogram**  $\frac{1}{T}|\widetilde{x_T}(f)|^2$ 

The data must be windowed to prevent spectral leakage

$$\frac{1}{Nf_{s}} \left| \sum_{j=0}^{N-1} x[j] w[j] e^{-2i\pi jk/N} \right|^{2}$$

→ The frequency resolution is set by the number of points (N must be large)



- → LIGO h(t) data sampled at 2048 Hz
- → Periodogram evaluated over 2 seconds
- $\rightarrow$  N = 2048 x 2 = 4096  $\rightarrow$  df = 0.5 Hz

Power spectral density (PSD)

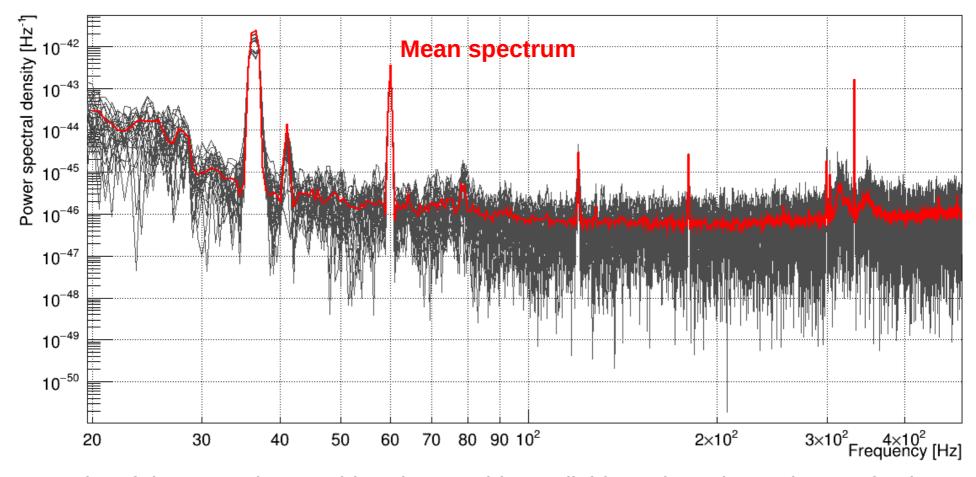
$$\lim_{T\to\infty}\frac{1}{T}|\widetilde{x_T}(f)|^2$$

Estimator for a finite data set: **periodogram**  $\frac{1}{T}|\widetilde{x_T}(f)|^2$ 

The data must be windowed to prevent spectral leakage

$$\frac{1}{Nf_{s}} \left| \sum_{j=0}^{N-1} x[j] w[j] e^{-2i\pi jk/N} \right|^{2}$$

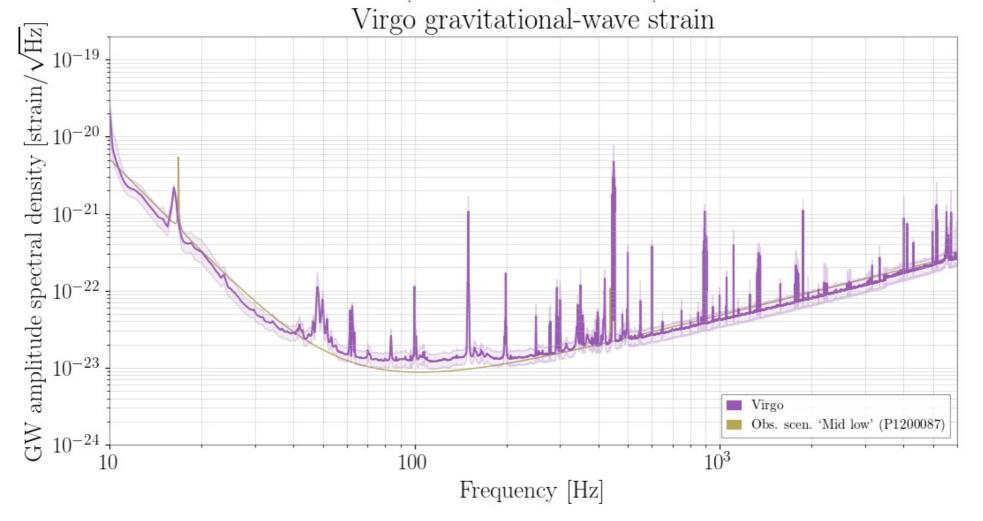
Welch method: average multiple periodograms to reduce the variance

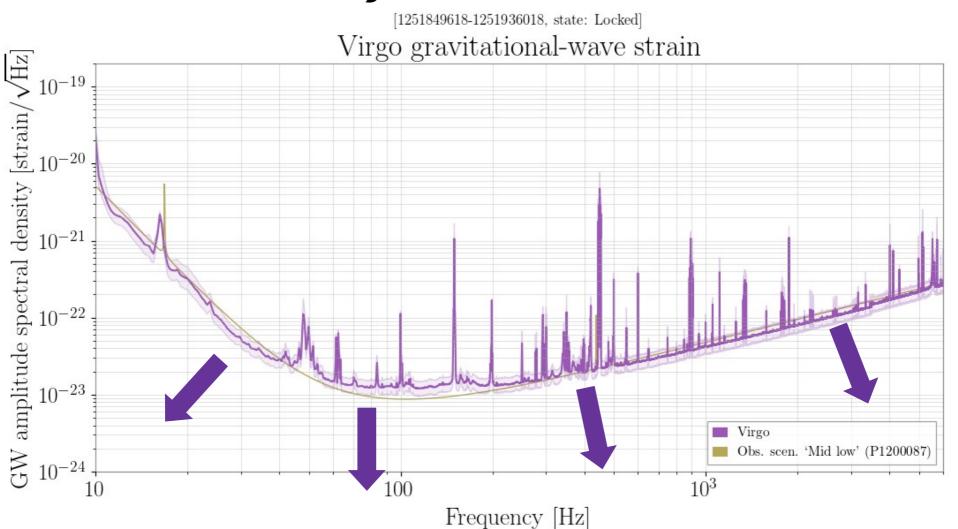


A lot of data must be considered to provide a reliable and precise estimate of noise:

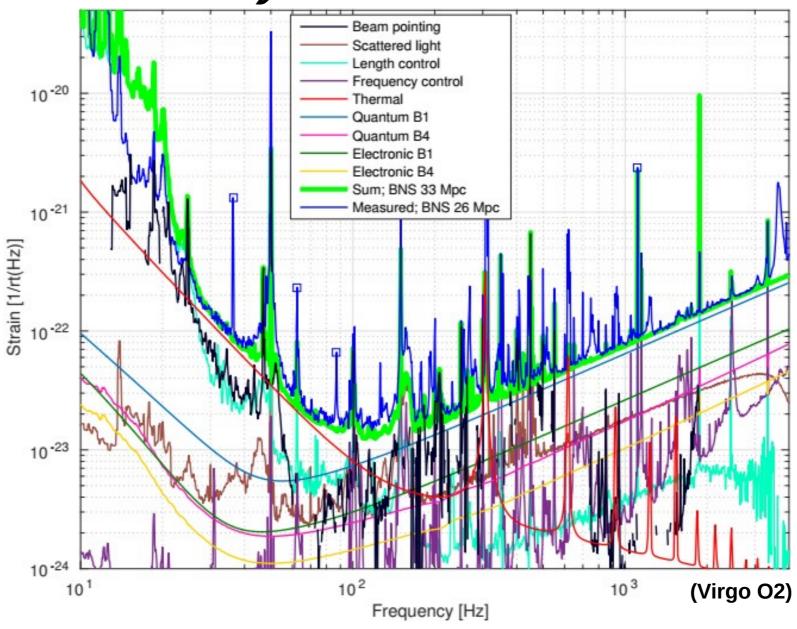
- → maximize N for each periodograms
- → average many periodograms to reduce the variance

[1251849618-1251936018, state: Locked]



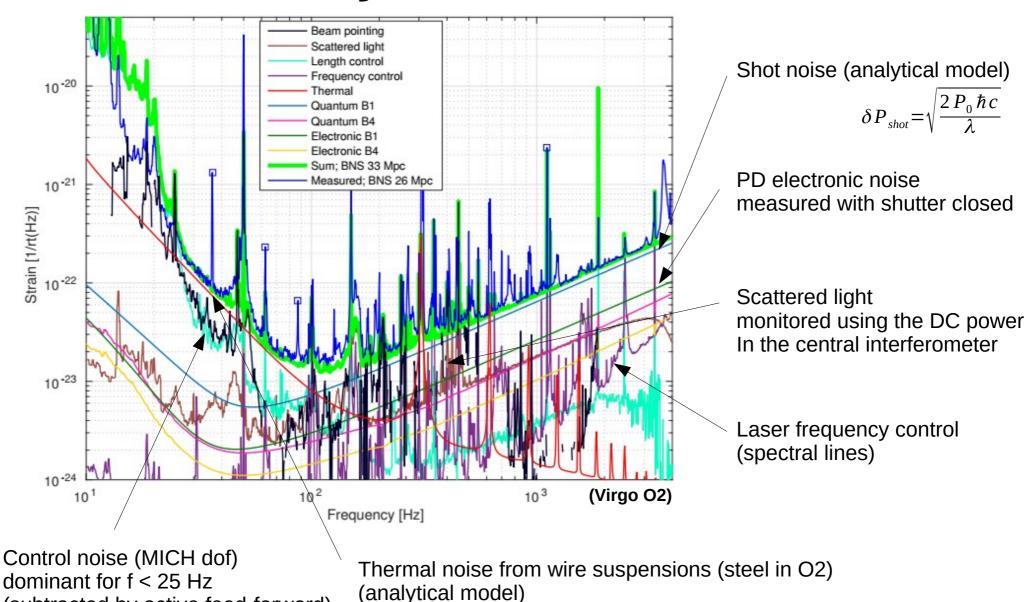


**Noise hunt**: bring the sensitivity curve down to the fundamental noise (seismic+thermic+quantum noise)



23

10/17/19 Florent Robinet - JOGLy

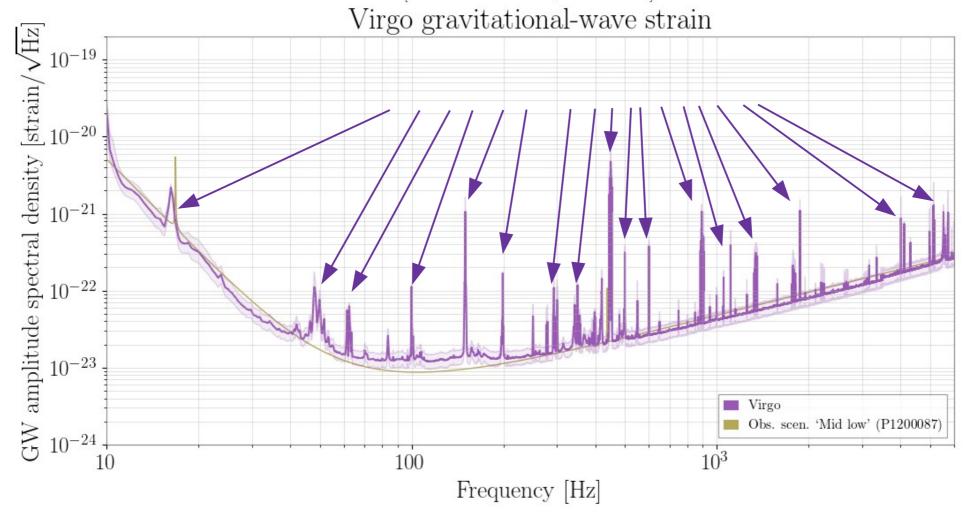


10/17/19

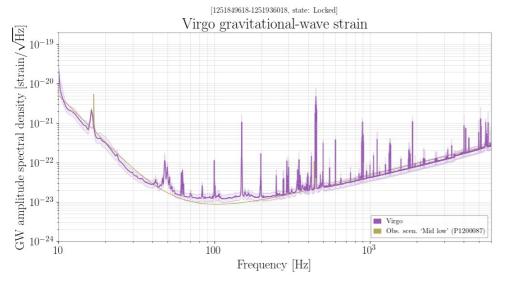
(subtracted by active feed-forward)

# Detector noise spectral structures

[1251849618-1251936018, state: Locked]



### Detector noise spectral structures



- → mechanical resonant modes (mirror and suspensions): typical lorentzian spectral shape
- → very narrow lines associated to electronic devices
- → line combs often associated to digitized clocks
- → **Line harmonics** resulting of the coupling of 2+ frequencies
- → Calibration lines are intentionally injected to monitor the detector response

The line frequency can often be associated to electronic devices: cooling fans, vaccum pumps, water pumps, wi-fi, badges identification devices...

Spectral noise investigation is often based on a deep knowledge of the detector and its environment

#### Noise variations

The detector noise varies at all time scales during a LIGO-Virgo science run

O(run) → The detector performance is often improved during a run

O(1 month) → The data set often covers several seasons; the noise gets worse in winter

O(1 day) → Day/night variation (mostly temperature driven)

 $O(1 \text{ hour}) \rightarrow Environment (temperature, human activity, weather...)$ 

O(<1 min) → Transient noise (so many sources!)

#### Noise variations

The detector noise varies at all time scales during a LIGO-Virgo science run

O(run) → The detector performance is often improved during a run

O(1 month) → The data set often covers several seasons; the noise gets worse in winter

O(1 day) → Day/night variation (mostly temperature driven)

O(1 hour) → Environment (temperature, human activity, weather...)

O(<1 min) → Transient noise (so many sources!)

Typically noise is estimated every few minutes



Welch method is biased by transient noise

→ Use a median estimator instead of mean

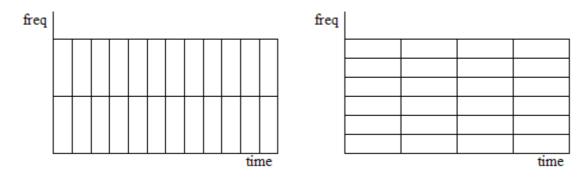
$$S_{n}(k) = Median_{0 \le m < M} \left\{ \frac{1}{Nf_{s}} \left| \sum_{j=0}^{N-1} x_{m}[j] w[j] e^{-2i\pi jk/N} \right|^{2} \right\}$$

### Spectrograms

Short Fourier transforms

$$X(\tau,\phi) = \int_{-\infty}^{+\infty} x(t) w(t-\tau,\phi) e^{-2i\pi\phi\tau} dt$$

Time-frequency analysis: the signal amplitude is computed in small regions in time and frequency



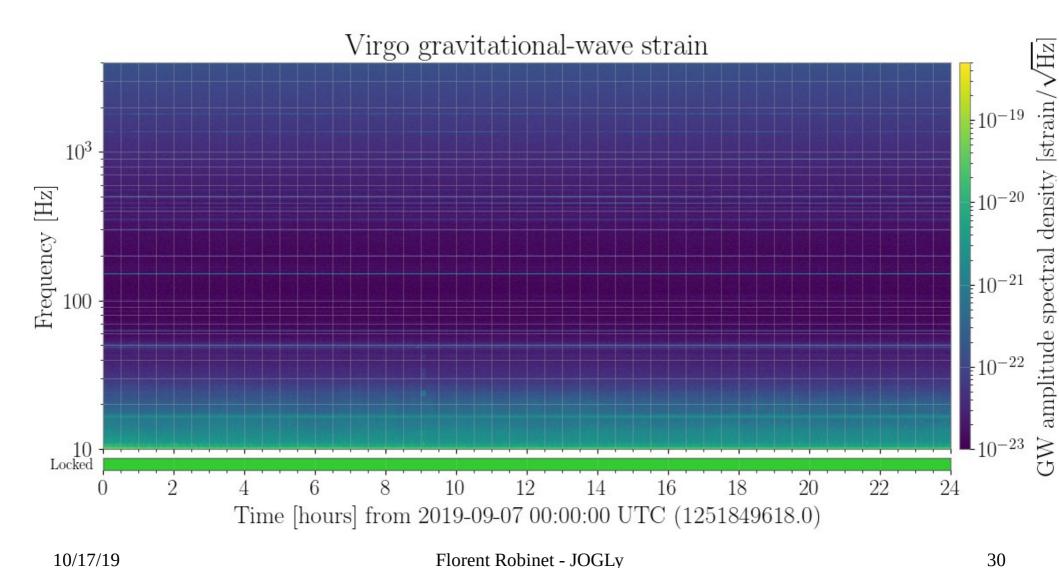
Heisenberg uncertainty principle: time and frequency resolutions are inversely proportional

Generalization of SFT: wavelet decomposition

### Spectrograms

Short Fourier transforms

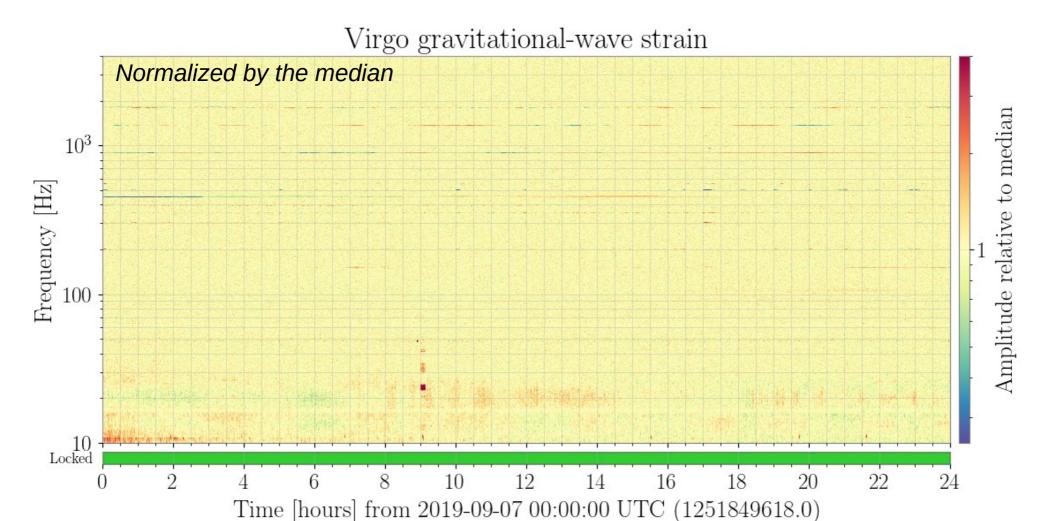
$$X(\tau,\phi) = \int_{-\infty}^{+\infty} x(t) w(t-\tau,\phi) e^{-2i\pi\phi\tau} dt$$



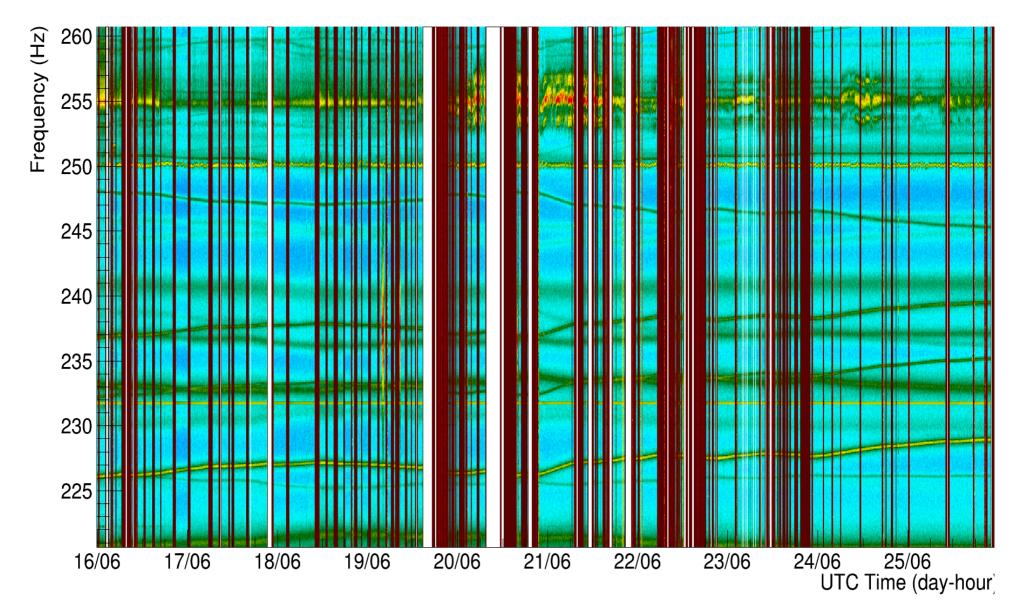
### Spectrograms

Short Fourier transforms

$$X(\tau,\phi) = \int_{-\infty}^{+\infty} x(t) w(t-\tau,\phi) e^{-2i\pi\phi\tau} dt$$



# Wandering lines



# Whitening

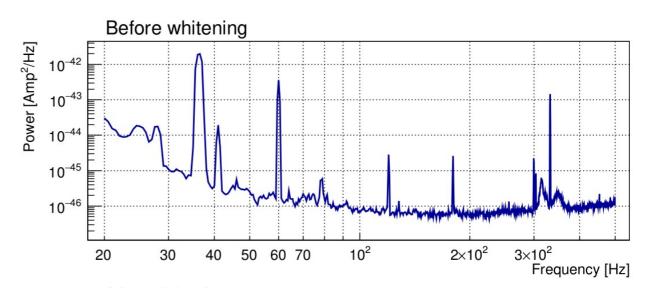
GW data must be whitened.

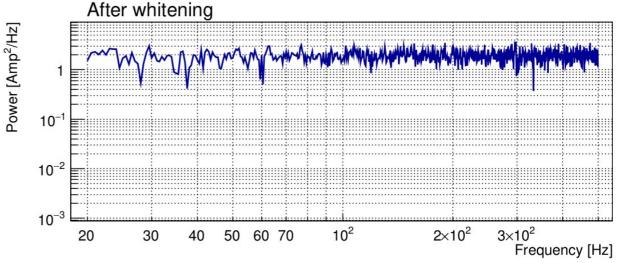
Several methods are used:

- reweighting of frequency bins

$$\widetilde{x}(f) \rightarrow \frac{\widetilde{x}(f)}{\sqrt{S_n(f)}}$$

- linear prediction
- → white noise is mandatory for a statistical interpretation of the data
- → measure of signal-to-noise ratio





#### Transient noise

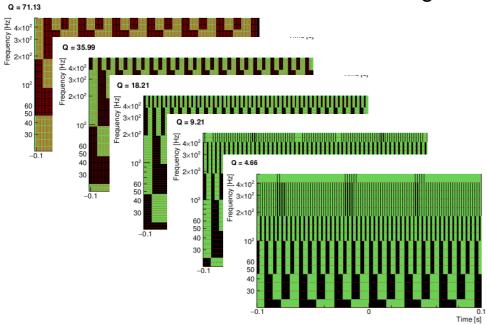
Example: Q-transform

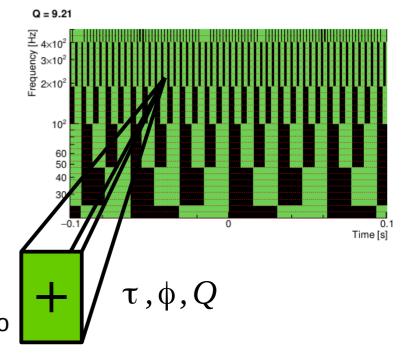
$$X(\tau,\phi,Q) = \int_{-\infty}^{+\infty} x(t)w(t-\tau,\phi,Q)e^{-2i\pi\phi\tau}dt$$

 $\rightarrow$  window width  $\sim 1/\phi$ 

~ Short Fourier transform with a Gaussian window

→ Use whitened data to measure a signal-to-noise ratio





10/17/19

Florent Robinet - JOGLy

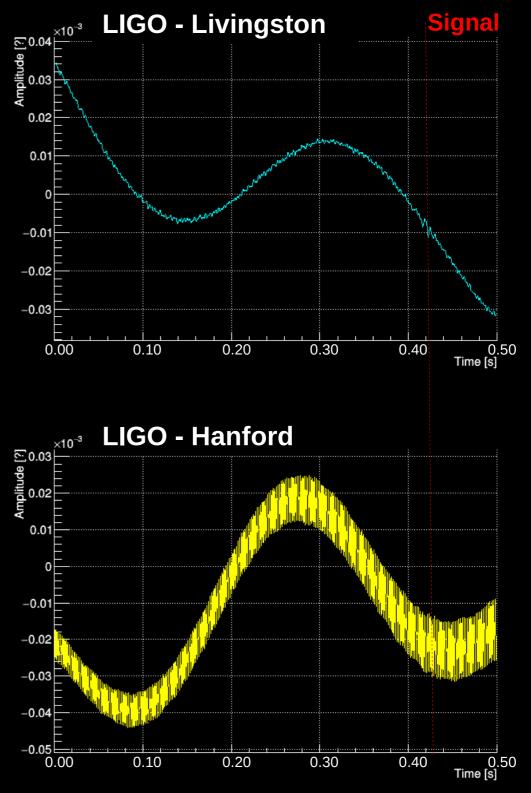
# GW150914

**Output power** 



Output power

10/17/19 Flo



# GW150914

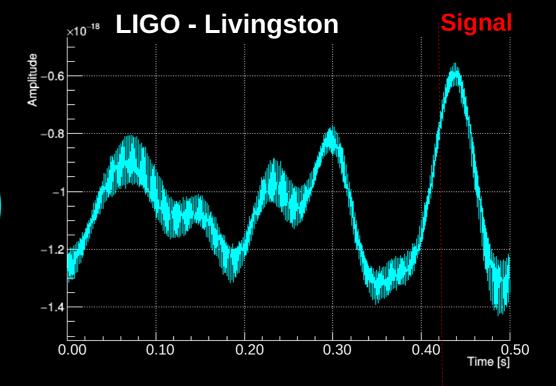
h(t)

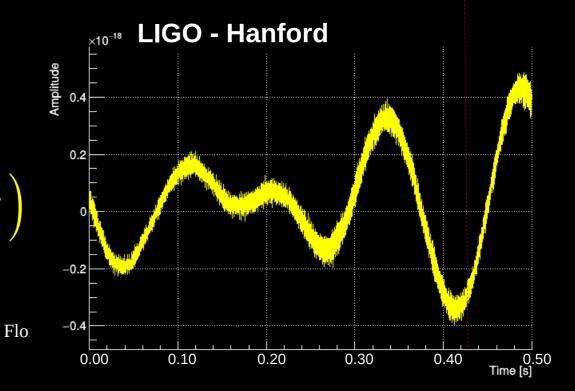
Data is calibrated

 $\rightarrow$  GW strain amplitude h(t)

(including high-pass filter f > 10 Hz)

h(t)

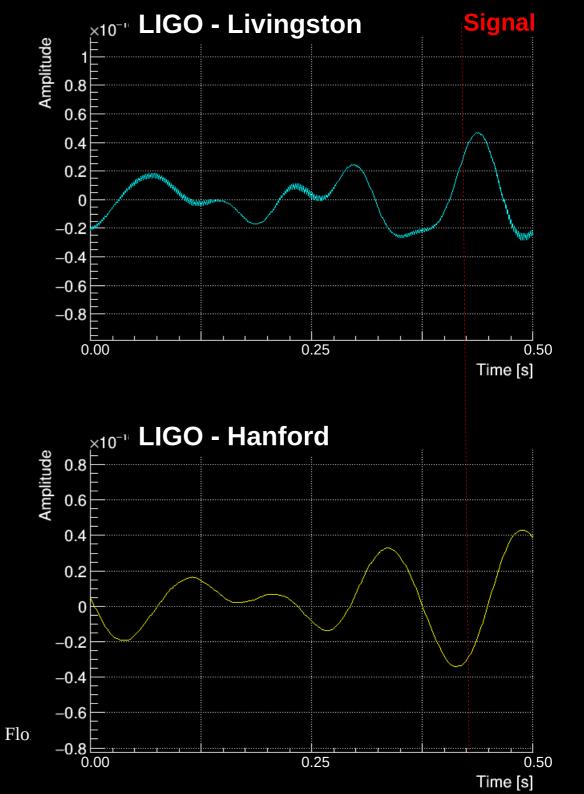




10/17/19

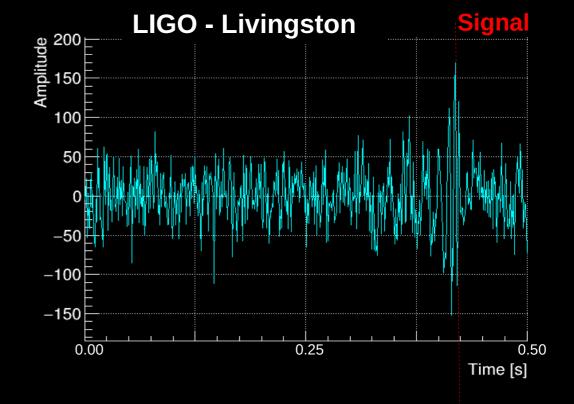
## GW150914

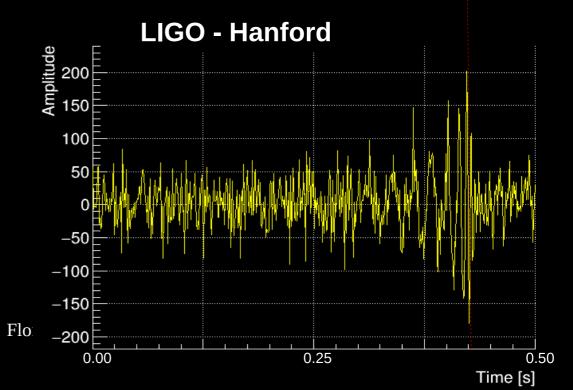
Data are low-pass filtered (here, < 500 Hz)



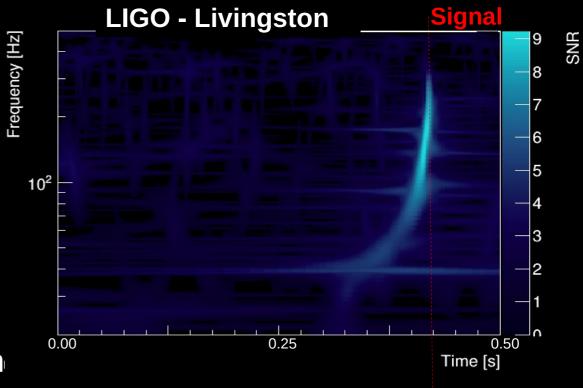
## GW150914

Data are whitened

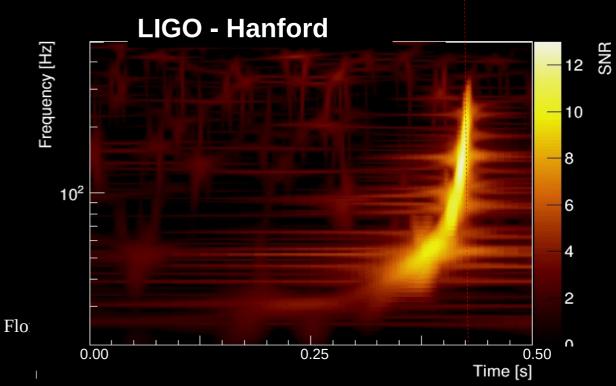




# GW150914



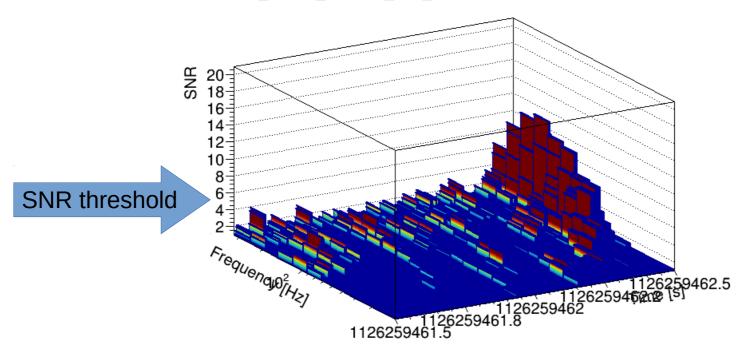
Time-frequency decomposition (Short Fourier transforms)



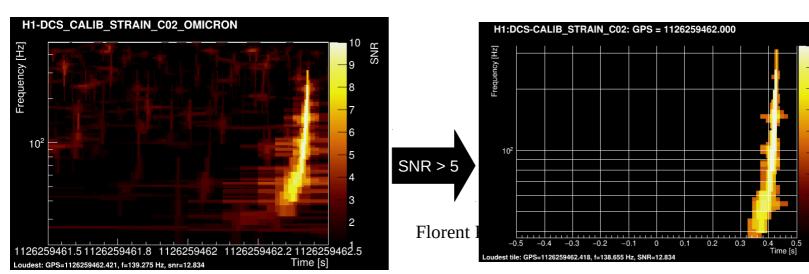
10/17/19

#### Transient triggers

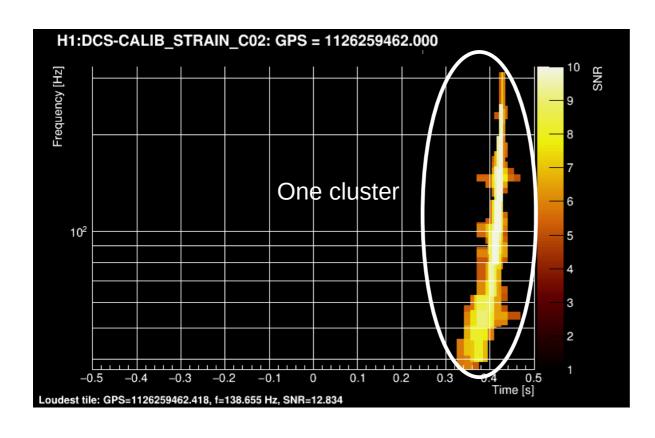
H1-DCS\_CALIB\_STRAIN\_C02\_OMICRON: Q=5.851



A trigger = a tile with a SNR value above a given threshold



### Transient triggers



Triggers are clustered in time

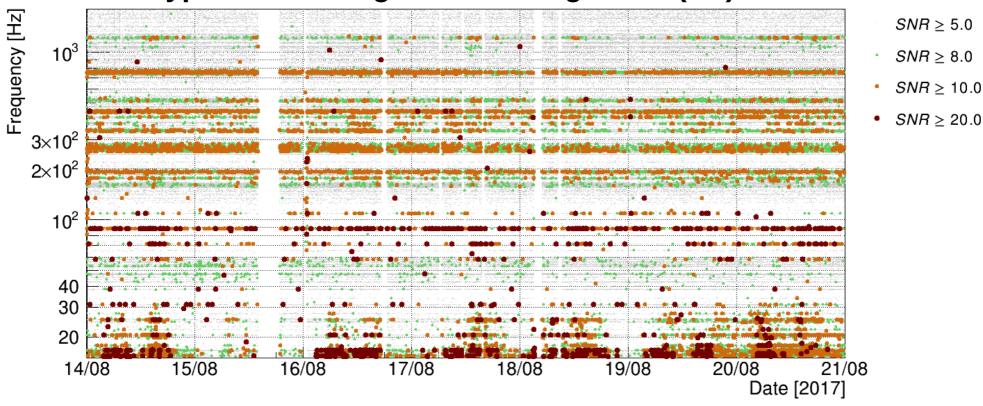
One cluster:

- time
- frequency
- SNR
- → given by the tile with the highest SNR
- + duration, bandwidth...

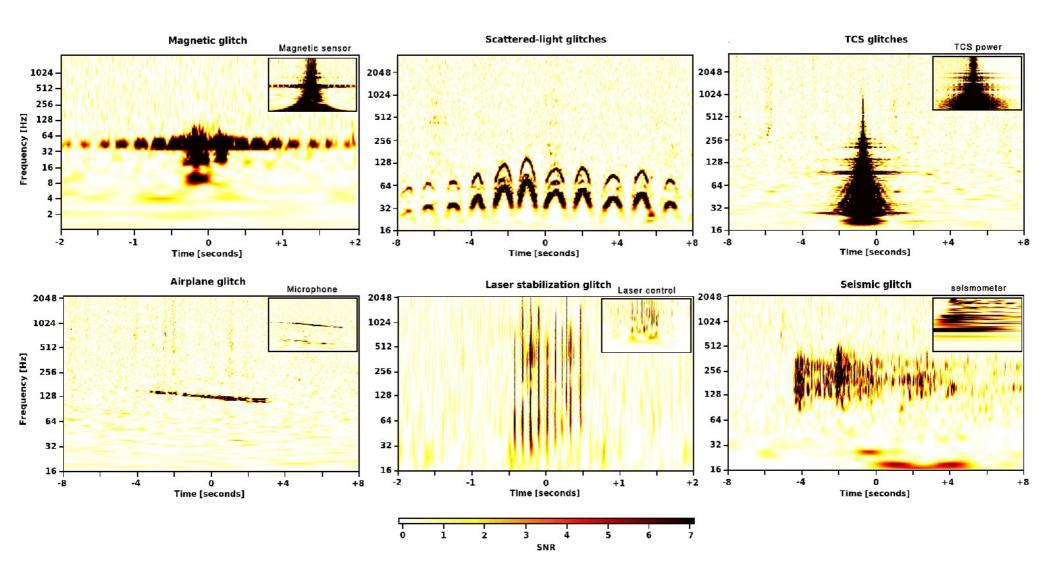
Triggers are saved to disk for further analysis

## Transient triggers = glitches

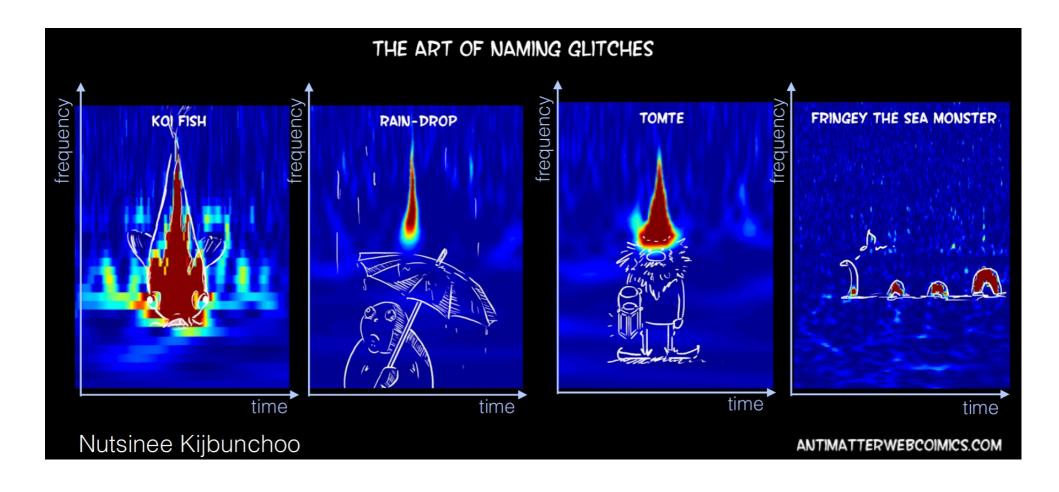
#### One typical week of glitches in Virgo data (O2)



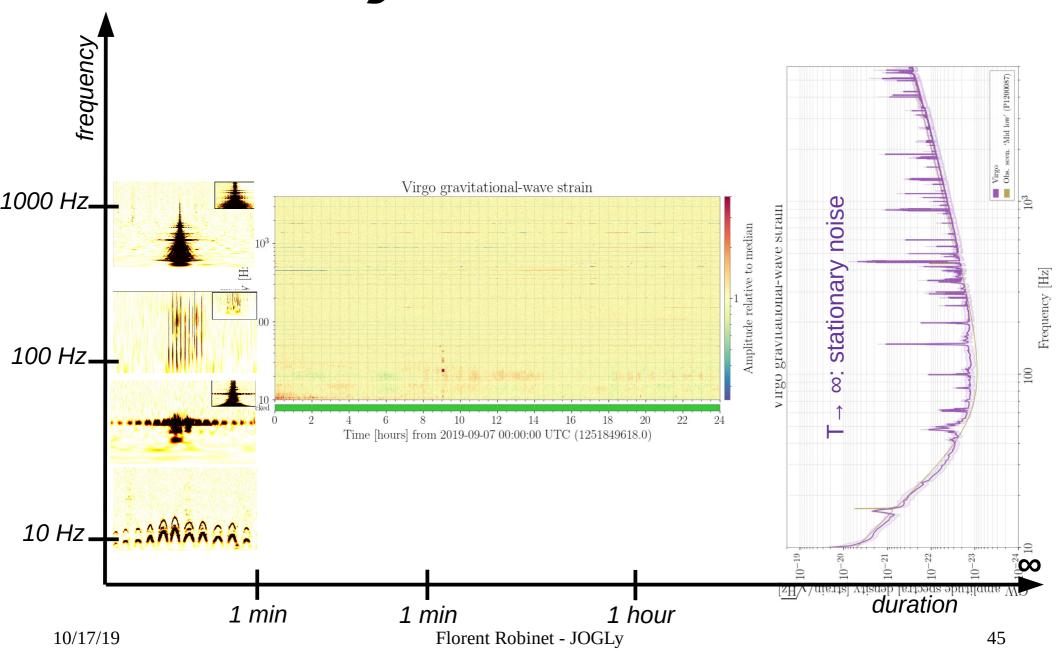
### Transient triggers = glitches

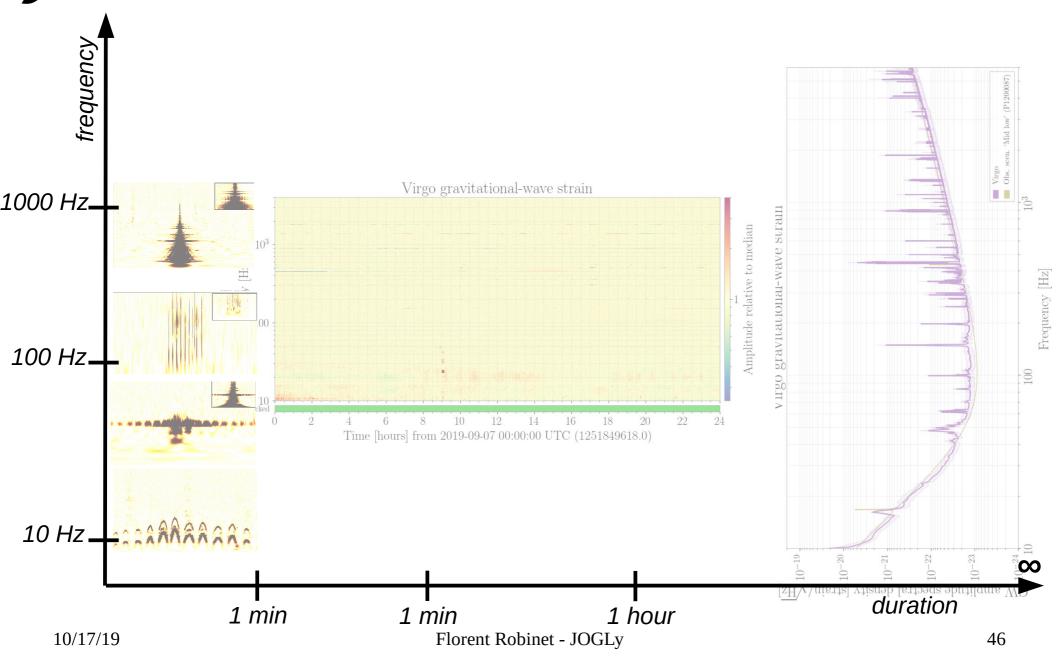


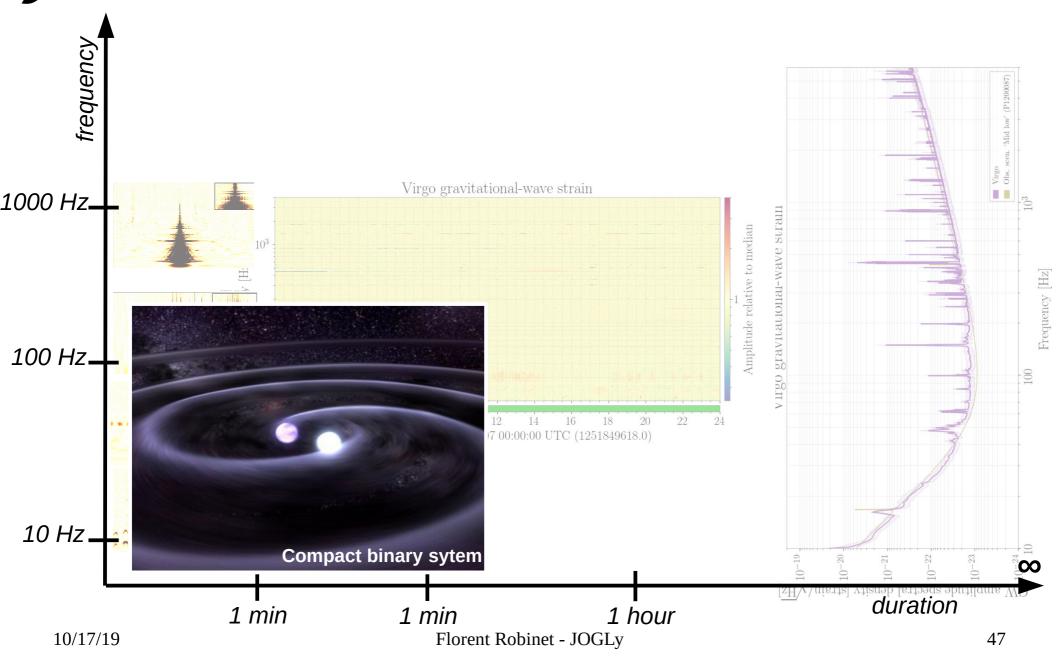
## Transient triggers = glitches



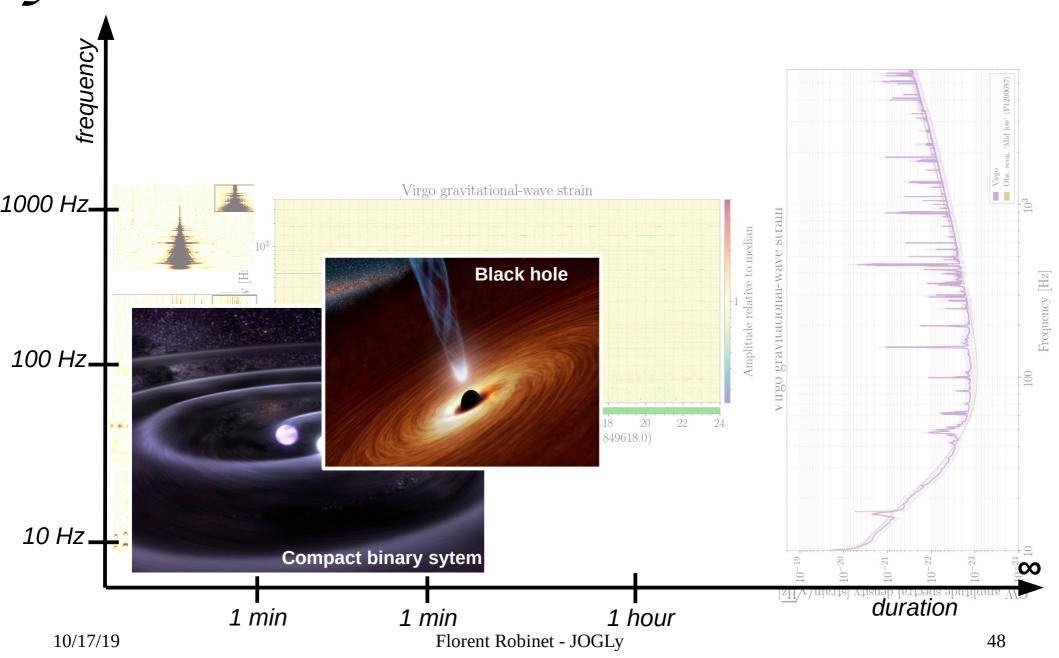
#### Noise summary



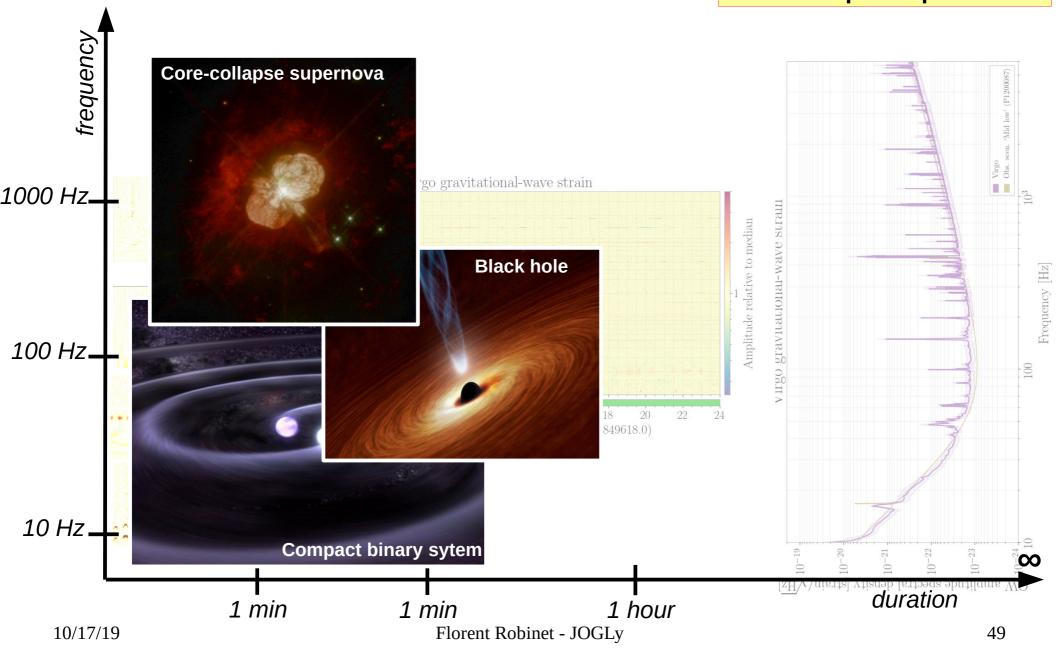




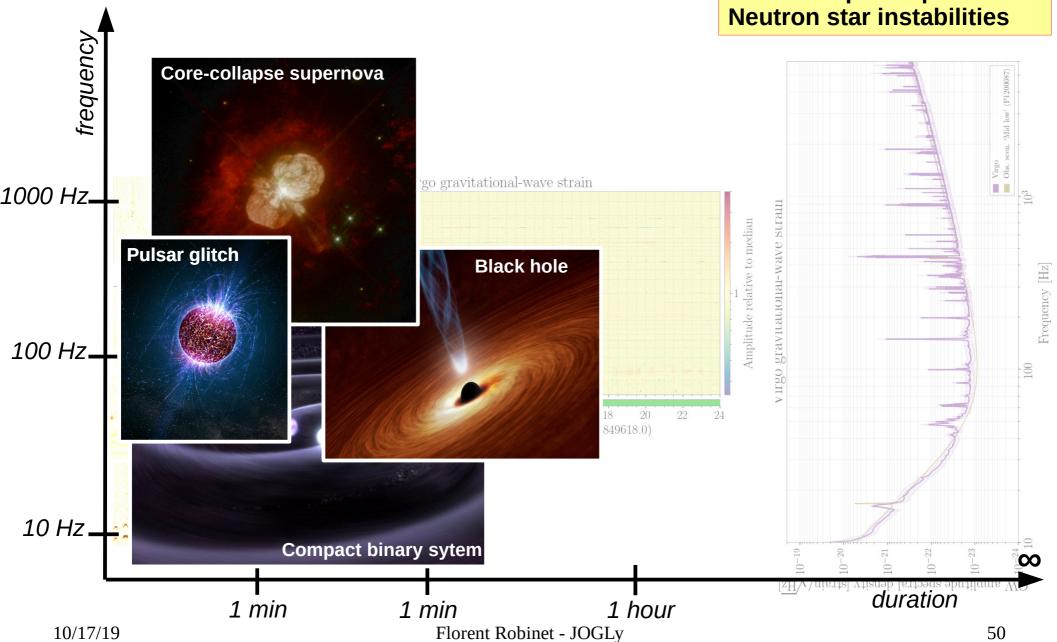
# Gravitational-wave sources Compact binary merger Newly-formed black-holes



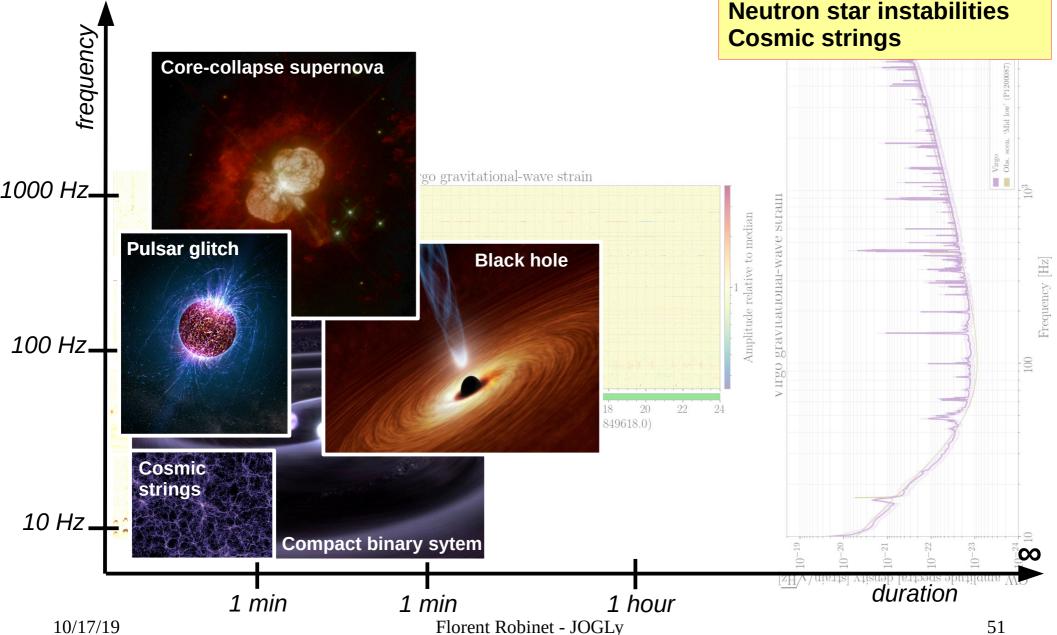
Compact binary merger Newly-formed black-holes Core-collapse supernovae

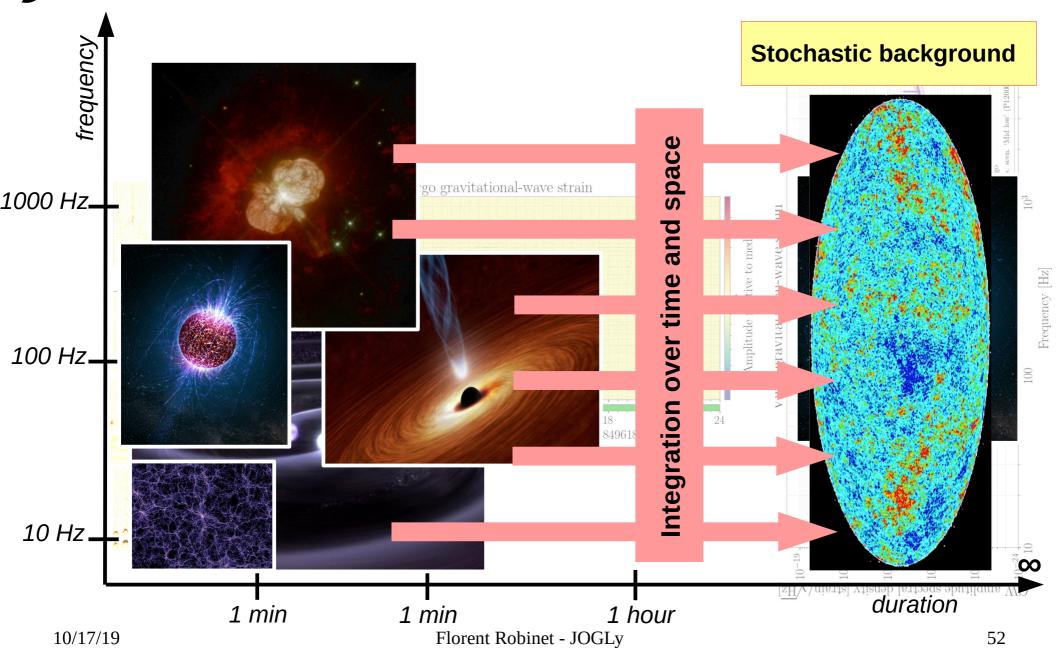


Compact binary merger
Newly-formed black-holes
Core-collapse supernovae
Neutron star instabilities

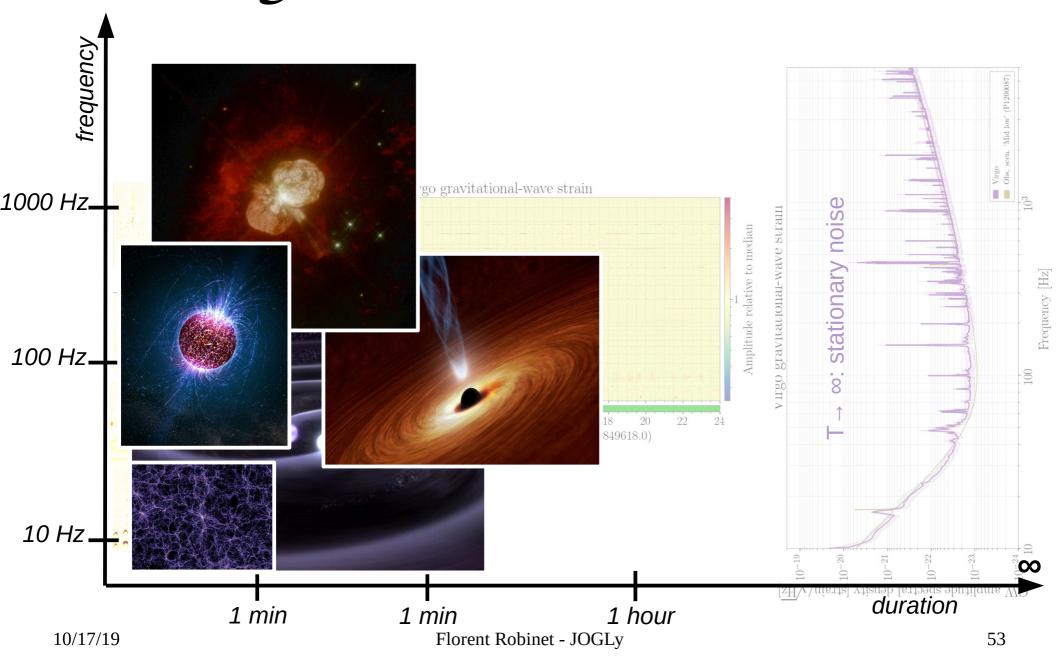


Compact binary merger Newly-formed black-holes Core-collapse supernovae Neutron star instabilities Cosmic strings





#### Transient gravitational waves



#### Transient gravitational waves

#### **Burst searches**

- → Compact binary merger
  - for low-mass systems, less sensitive than a template search
  - signal reconstruction → deviation from GR
- → Core-collapse supernovæ
  - iconic burst source
  - different GW signatures (rotating core collapse / neutrino-driven SN)
  - model/simulation are incomplete
  - use ad-hoc models (damped sine, white-noise burst)
- → Pulsar glitches
  - cause is unclear: crust fragmentation, stellar interior dynamic
- → Cosmic strings
  - simple waveform model → template search

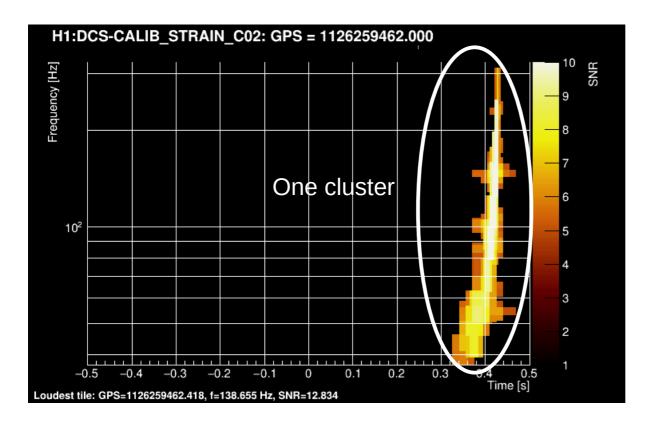
#### Goals

- 1/ make a detection
- 2/ reconstruct the waveform
- 3/ extract the source parameters

#### Transient gravitational waves

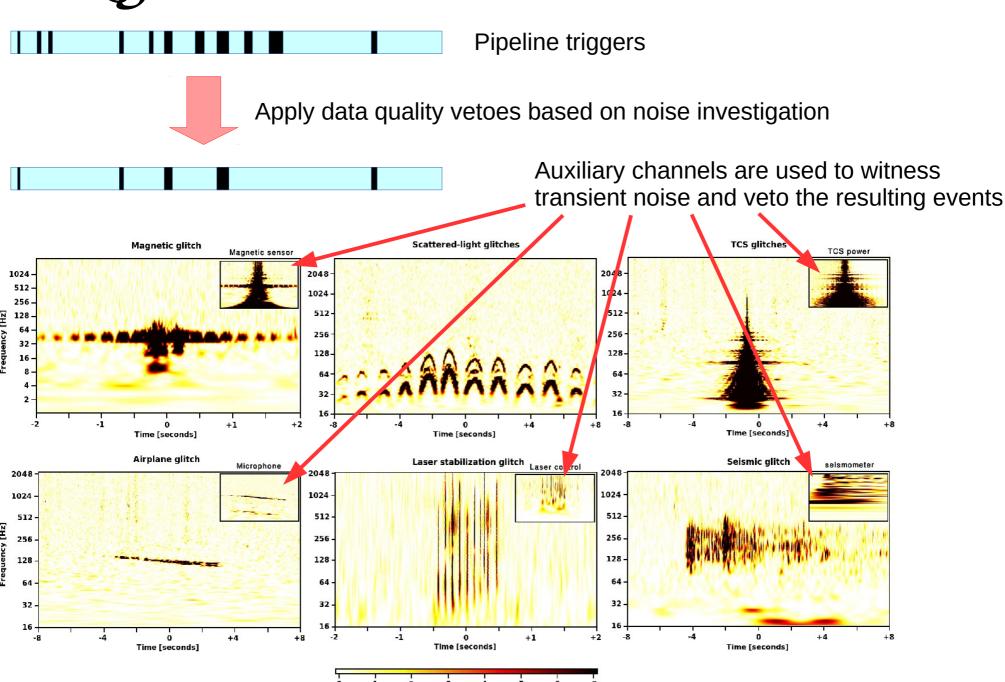
#### **Burst searches**

→ Several search pipelines were developed, all of them based on time-frequency analysis



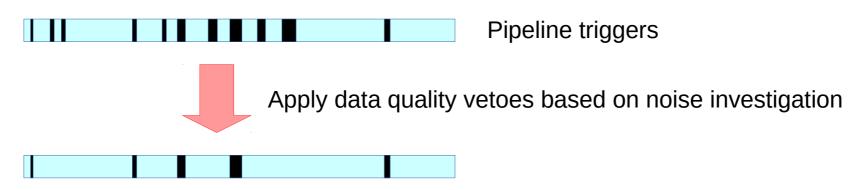
How to separate a true signal from a glitch?

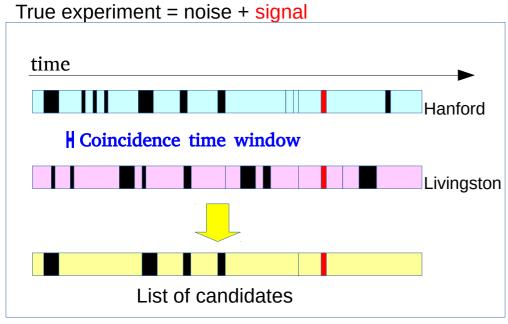
#### Back ground reduction



SNR

#### Back ground reduction





#### Coincidence rate:

$$R_{coinc} \sim R_H R_L \Delta t_{win}$$
  
  $\sim (1 Hz) \times (1 Hz) \times (10^{-2} s) = 10^{-2} Hz$ 

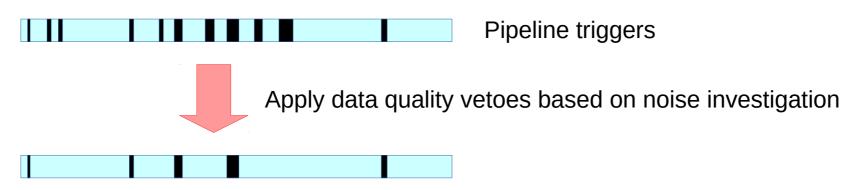
#### Coincidence between detectors

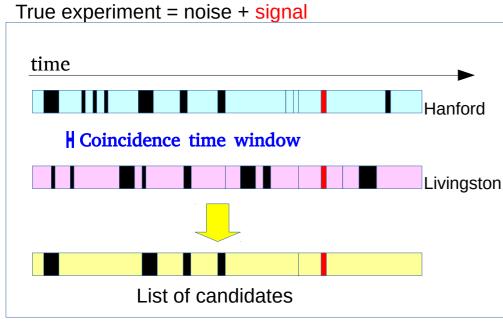


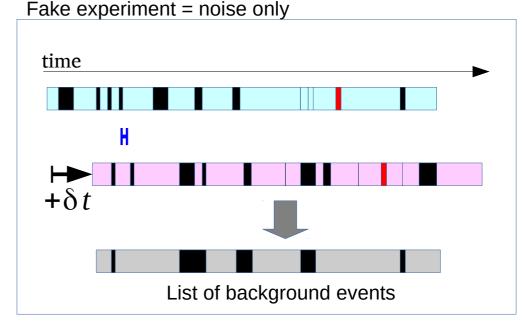




#### Back ground estimation





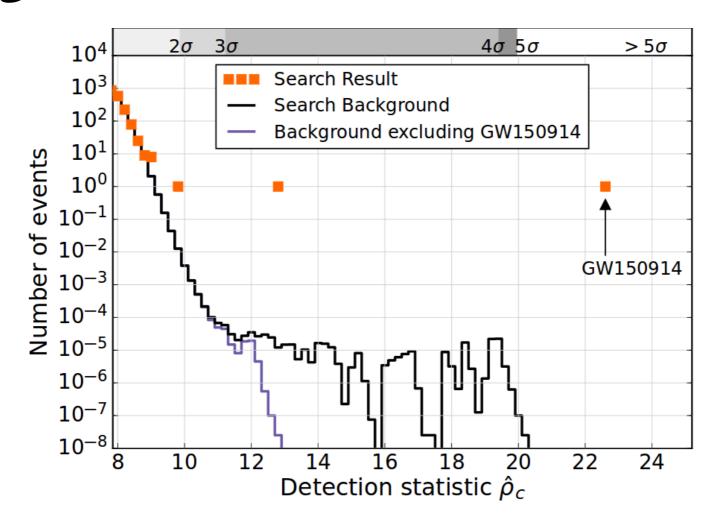


Coincidence rate:

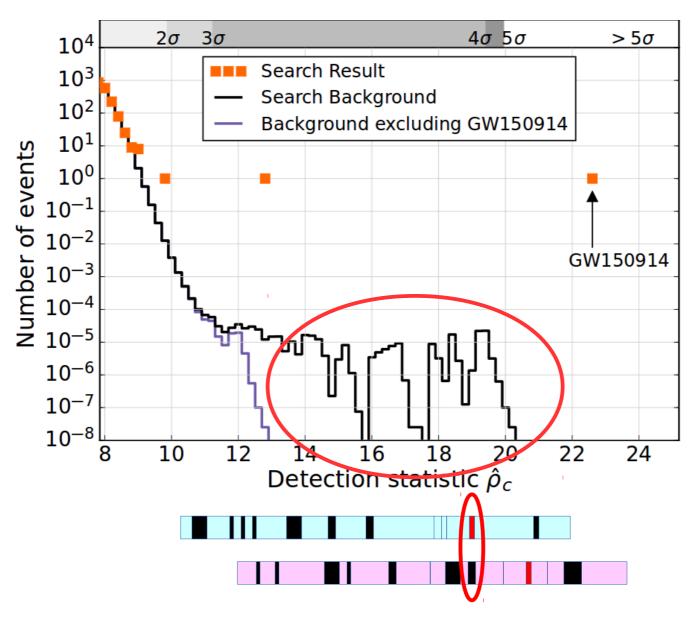
$$R_{coinc} \sim R_H R_L \Delta t_{win}$$
  
  $\sim (1 Hz) \times (1 Hz) \times (10^{-2} s) = 10^{-2} Hz$ 

A very large number of fake experiments can be simulated using multiple offsets O(1,000,000)

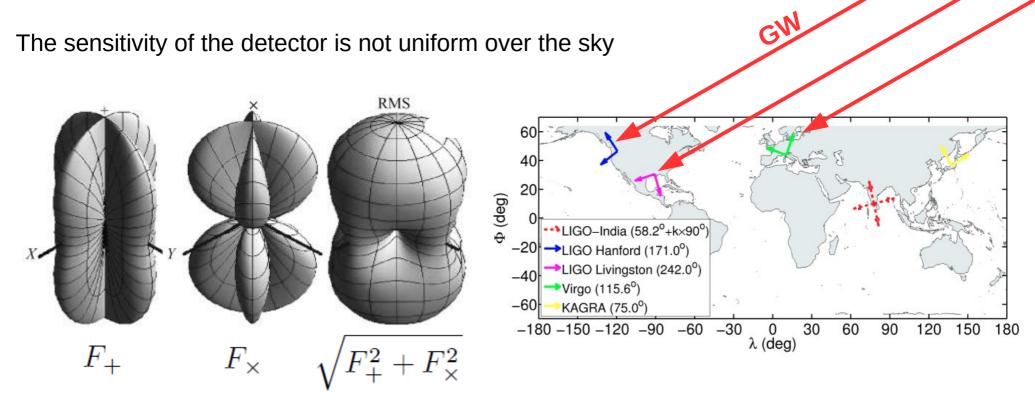
### Background & detection



### Back ground & detection



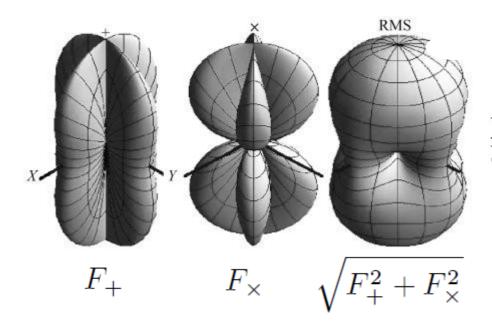
#### Coherent search

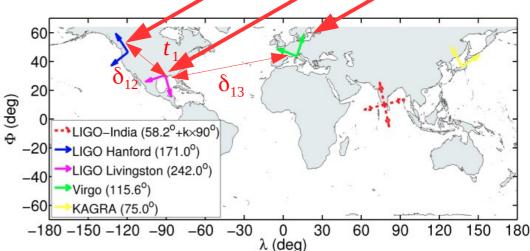


The signal is coherent between detectors, the noise is generally not

#### Coherent search

The sensitivity of the detector is not uniform over the sky





$$GW_1(t_1) = F_{+1}(t_1, ra, dec, \Psi) \times h_{+}(t_1) + F_{\times 2}(t_1, ra, dec, \Psi) \times h_{\times}(t_1)$$

$$GW_{2}(t_{2}) = F_{+2}(t_{2}, ra, dec, \Psi) \times h_{+}(t_{2}) + F_{\times 2}(t_{2}, ra, dec, \Psi) \times h_{\times}(t_{2})$$

$$GW_3(t_3) = F_{+3}(t_3, ra, dec, \Psi) \times h_{+}(t_3) + F_{\times 3}(t_3, ra, dec, \Psi) \times h_{\times}(t_3)$$

$$\longrightarrow GW_1(t_1)+GW_2(t_1+\delta_{12})+GW_3(t_1+\delta_{13})$$

#### Coherent search

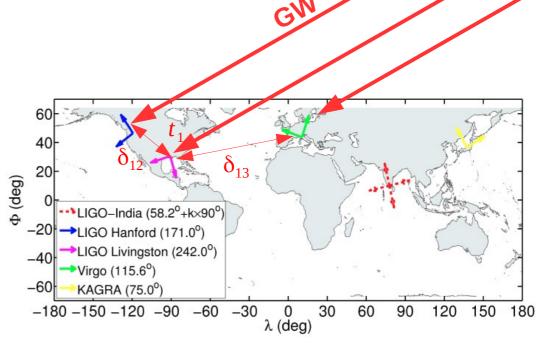
A coherent data stream is considered:

$$h_{coh} = h_1(t) + h_2(t + \delta_{12}) + h_3(t + \delta_{13})$$

The times of arrival are unknown:

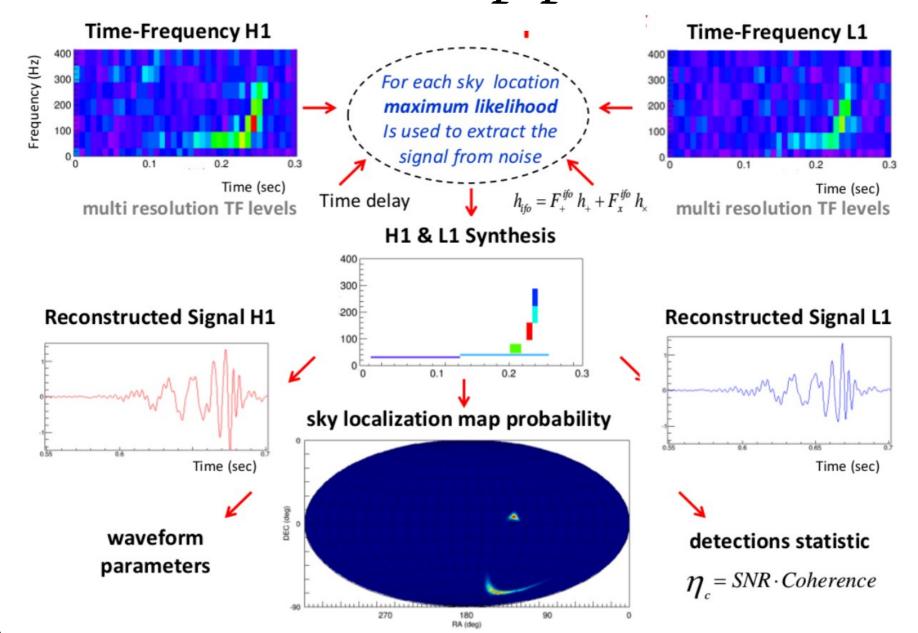
$$|\delta_{12}| < \delta_{12}^{max} (=10 \, ms) \quad |\delta_{13}| < \delta_{13}^{max} (=27 \, ms)$$

Multiple values of  $\delta$  must be tested such that the coherent SNR is maximized



- → To optimize the computing, the coherent burst pipeline time-shifts time-frequency maps
- → Maximum-likelihood-ratio method
- → Null data stream to reject spurious events
- → The network sensitivity is not limited by the least sensitive detector
- → Source location is reconstructed

#### Coherent-wave burst pipeline



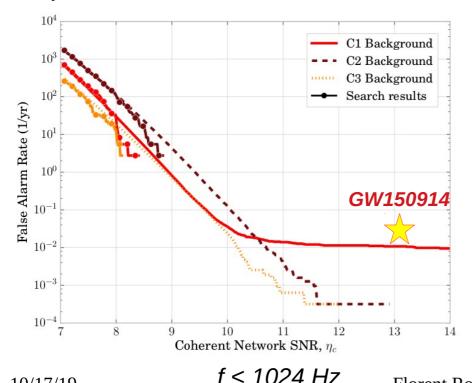
#### Coherent search results (O1)

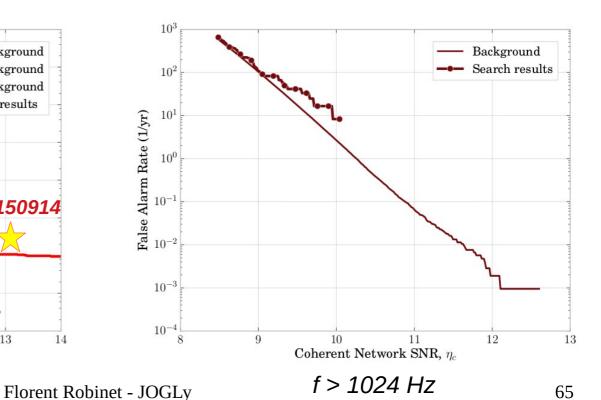
C1: low-Q events (short-duration & wide-band)

C3: events for which the frequency increases with time

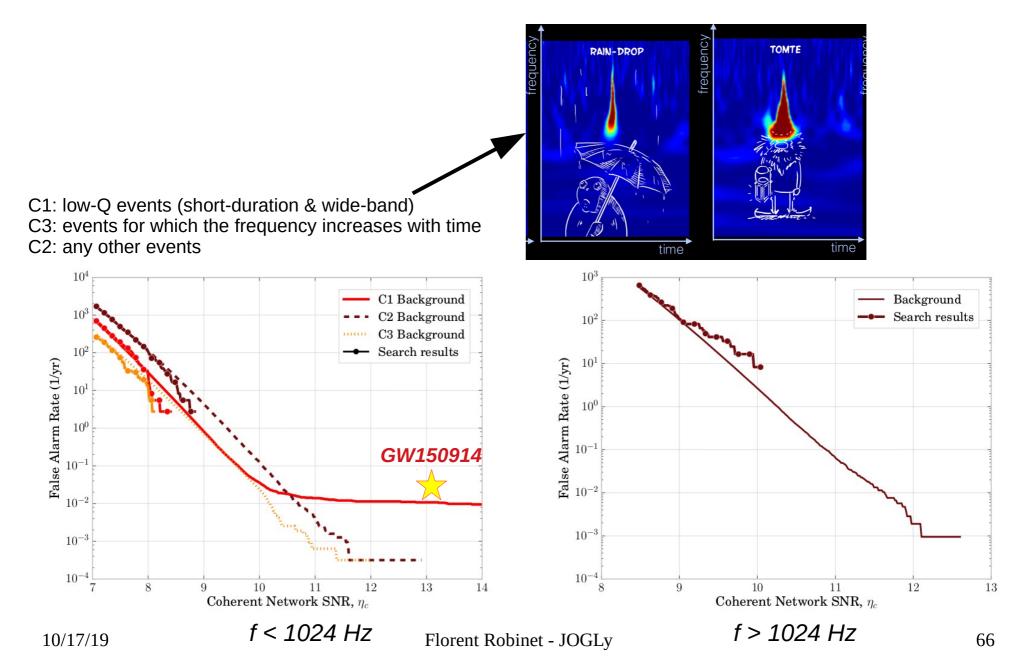
C2: any other events

10/17/19



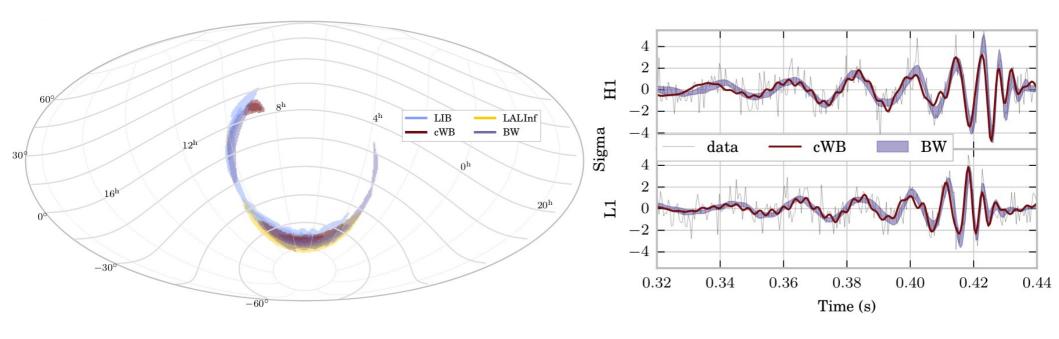


#### Coherent search results (O1)

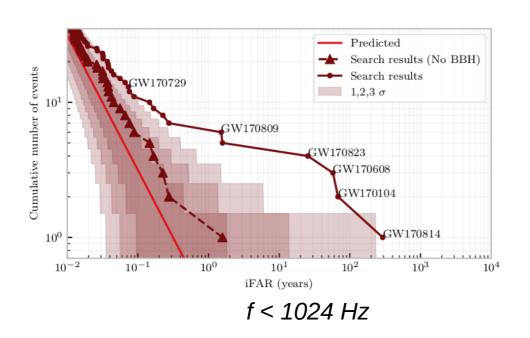


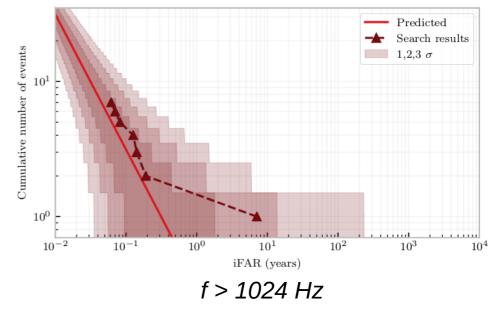
#### Coherent search results (O1)

#### Parameter estimation for GW150914

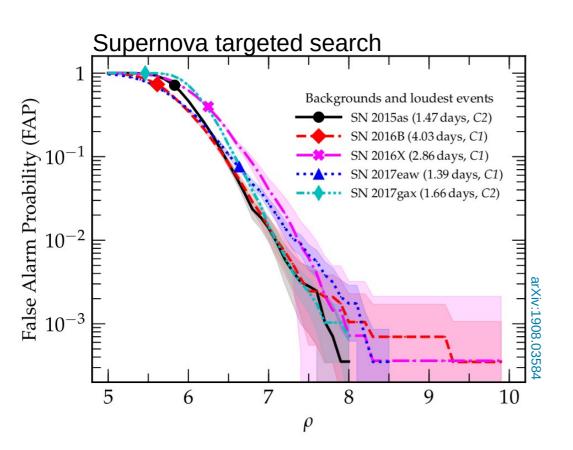


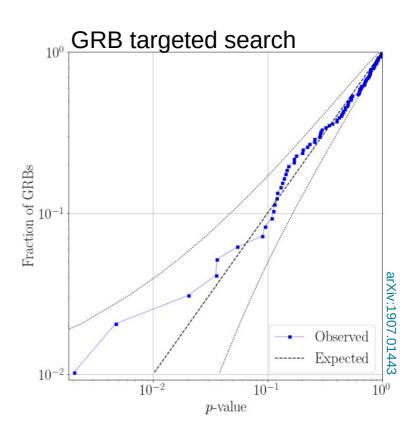
#### Coherent search results (O2)





#### Targeted burst searches



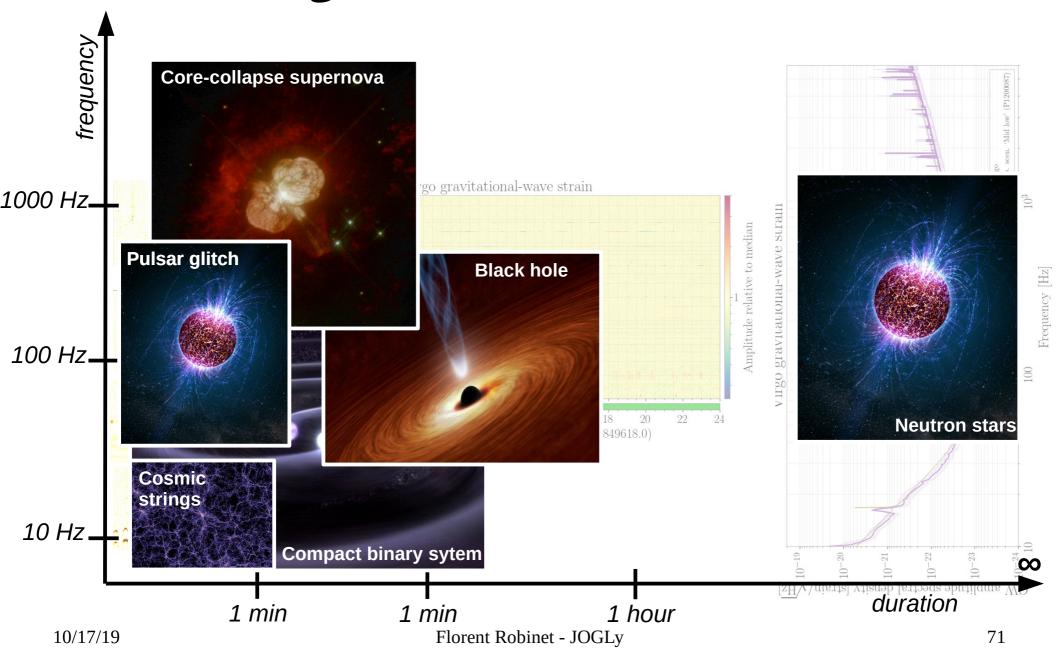


See also: GW + high-energy neutrino trigger coincidence

## Low-latency searches

GW ID	Event Time UTC	Final status	Source	Source Triggers		Latency (min)	
			Classification	Search(es) <sup>a</sup>	Online FAR $(yr^{-1})$	GraceDb submission	Initial GCN notice
G268556 GW170104	2017-01-04 10:11:58	Confident	BBH EM-Bright: 0%	PyCBC, cWB GstLAL, oLIB	1.9 b	264	395
G270580	2017-01-20 12:30:59	Retracted	Burst EM-Bright: N/A	cWB	5.0	2	67
G274296	2017-02-17 06:05:53	NFI	Burst EM-Bright: N/A	cWB	5.4	715	813
G275404	2017-02-25 18:30:21	NFI	NS-BH EM-Bright: 90%	PyCBC, GstLAL	6.0	<1	24
G275697	2017-02-27 18:57:31	NFI	BNS EM-Bright: 100%	PyCBC, GstLAL, MBTAOnline	4.5	<1	27
G277583	2017-03-13 22:40:09	NFI	Burst EM-Bright: N/A	cWB	2.7	3	30
G284239	2017-05-02 22:26:07	NFI	Burst EM-Bright: N/A	oLIB	4.0	12	963
G288732 GW170608	2017-06-08 02:01:16	Confident	BBH EM-Bright: 0%	PyCBC, cWB, GstLAL <sup>c</sup>	2.6	650	818
G296853 GW170809	2017-08-09 08:28:22	Confident	BBH EM-Bright: 0%	GstLAL, cWB MBTAOnline	0.2	<1	49
G297595 GW170814	2017-08-14 10:30:44	Confident	BBH EM-Bright: 0%	GstLAL, oLIB, PyCBC, cWB <sup>d</sup>	$1.2 \times 10^{-5}$	<1	31
G298048 GW170817	2017-08-17 12:41:04	Confident	BNS EM-Bright: 100%	GstLAL <sup>d</sup> , PyCBC	$1.1 \times 10^{-4}$	6	27 <sup>e</sup>
G298389	2017-08-19 15:50:46	NFI	Burst EM-Bright: N/A	oLIB	4.9	16	192
G298936 GW170823	2017-08-23 13:13:59	Confident	BBH EM-Bright: 0%	cWB, oLIB, <b>GstLAL</b> , PyCBC, MBTAOnline	$5.5 \times 10^{-4}$	<1	22
G299232	2017-08-25 13:13:37	NFI	NS-BH EM-Bright: 100%	MBTAOnline <sup>f</sup>	5.3	<1	25

### Continuous gravitational waves



#### Continuous gravitational waves

Gravitational-wave radiation from a time-varying quadrupolar mass-moment:

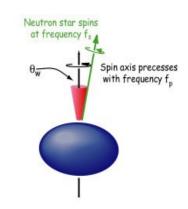
$$h_{\mu\nu} = \frac{2G}{rc^4} \frac{d^2}{dt^2} [I_{\mu\nu}]$$

Rapidly-rotating neutron star with ellipticity

$$h \approx 1.1 \times 10^{-24} \left(\frac{r}{1 \, kpc}\right)^{-1} \left(\frac{f_{GW}}{1 \, kHz}\right)^{2} \left(\frac{\epsilon}{10^{-6}}\right) \left(\frac{I_{zz}}{10^{38} \, kg \cdot m^{2}}\right)$$
$$f_{GW} = 2 f_{rot}$$

#### Mass asymmetry:

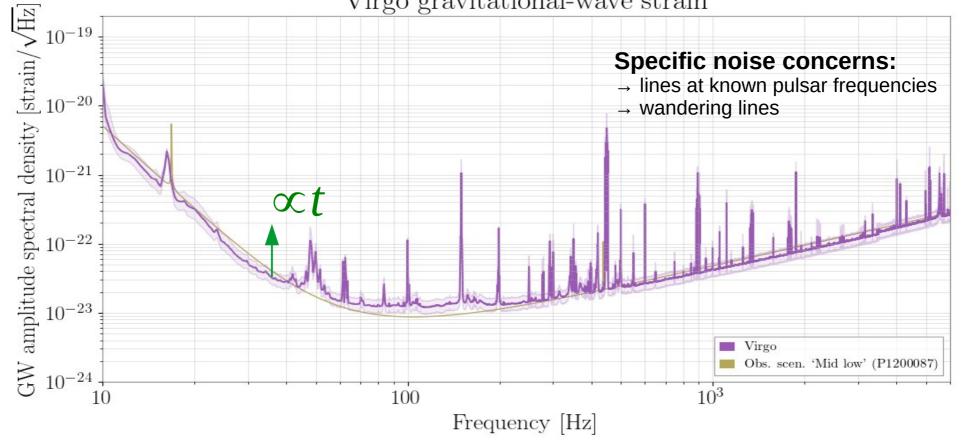
- → distortion due to elastic stresses or magnetic field
- → distortion due to matter accretion
- → free precession around rotation axis
- → excitation of long-lasting oscillations (e.g. r-modes)



The continuous gravitational waveform is well modeled by a sinusoidal wave

$$h(t) = h_0 \left( F_+(t, \alpha_0, \delta_0, \psi) \frac{1 + \cos^2(\iota)}{2} \cos(\Phi(t)) + F_\times(t, \alpha_0, \delta_0, \psi) \cos(\iota) \sin(\Phi(t)) \right),$$

Virgo gravitational-wave strain



Florent Robinet - JOGLy

10/17/19

→ The continuous gravitational waveform is well modeled by a sinusoidal wave

→ Rupture point of neutron star matter

<ul> <li>Normal nuclear matter</li> </ul>	$\epsilon$ < $10^{-5}$
<ul><li>Hybrid (hadron-quark core)</li></ul>	$\epsilon$ < $10^{-3}$
<ul><li>– Quark star</li></ul>	$\epsilon$ < $10^{-1}$

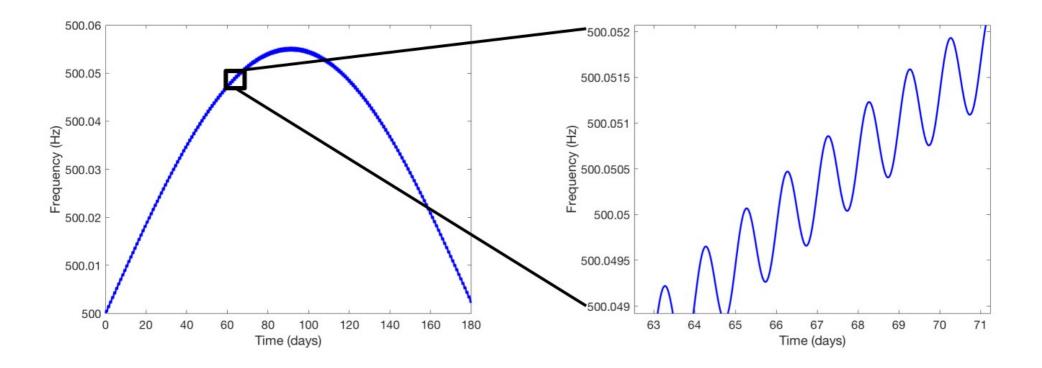
→ Gravitational-wave frequency

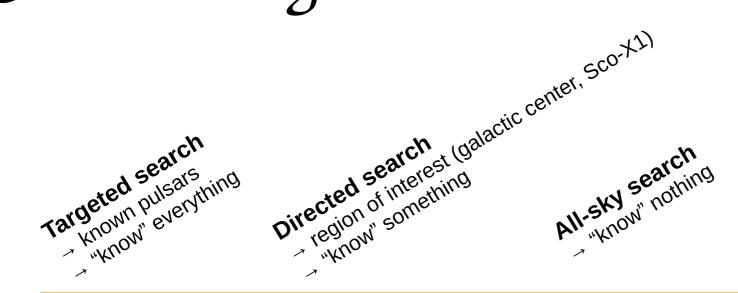
<ul><li>Tri-axial ellipsoid</li></ul>	$f_{GW} = 2f_{rot}$
<ul> <li>r-mode fluid oscillations</li> </ul>	$f_{GW} \approx 4/3 f_{rot}$
<ul><li>free-precession</li></ul>	$f_{GW} = f_{rot} \pm f_{pre}$

- → The science of continuous waves
  - Neutron star equation of state, maximum mass, spin and ellipticity
  - Exotic state of matter
  - Tests of general relativity
  - Neutron star dynamics

The gravitational waveform is Doppler-modulated by the Earth rotational & orbital motion

→ you need to correct for that for every sky location you observe

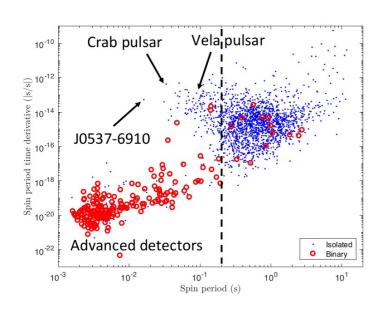




**Computational cost** 







- ~ 600 known pulsars spinning faster than 5 Hz
- ~ Almost half of them are in binary systems

Neutron stars spin down

→ result of gravitational radiation

Spin-down ( $\dot{f}_{rot}$ ) limit can be used to place constraints on GW emission  $\rightarrow$  useful benchmark

Targeted search

Targeted search

Known Pulsars

Known everything

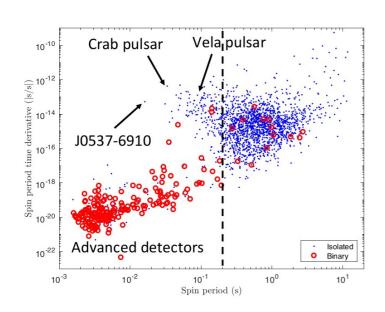
Directed search

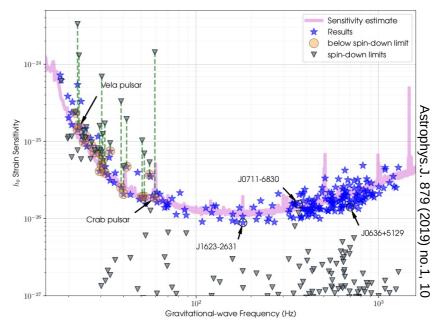
region of interesting

region of something

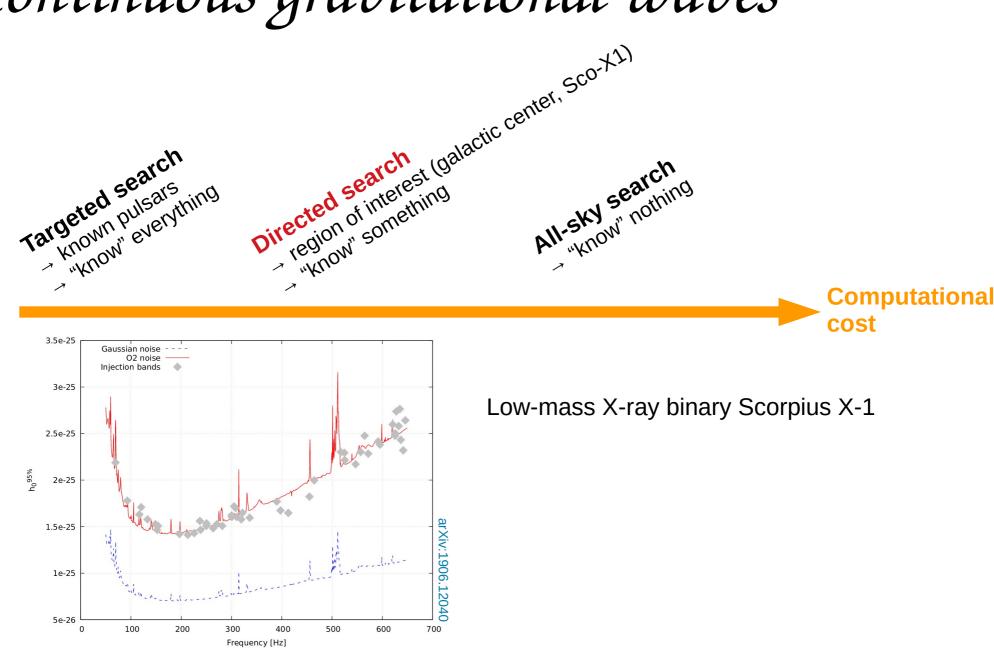
All-sky search

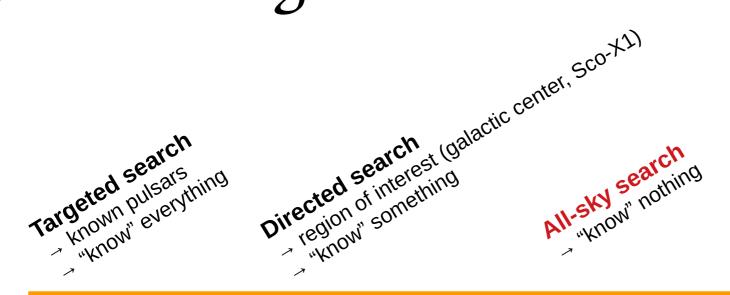






Florent Robinet - JOGLy





Computational cost

#### Brute-force (and very expensive) search over a huge parameter space:

- → gravitational-wave frequency (LIGO-Virgo sensitive band)
- → frequency derivative (~±10<sup>-8</sup> Hz/s)
- → sky location (all-sky)
- → source inclination and polarization angle (anything)
- → signal phase (anything)

(more parameters for binary systems !!!)

Targeted search

Targeted search

Known Pulsars

Known everything

Directed search

Oirected search

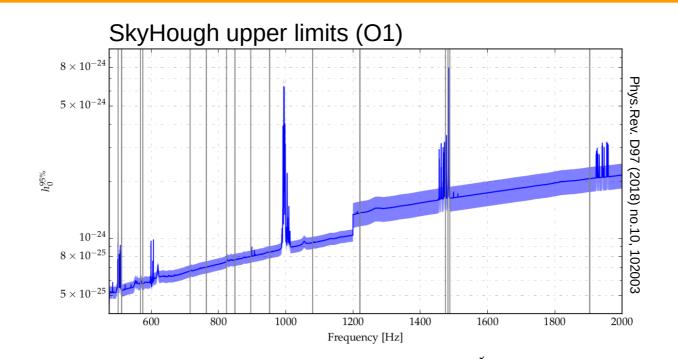
Tegion of interesting

Tegion of interesting

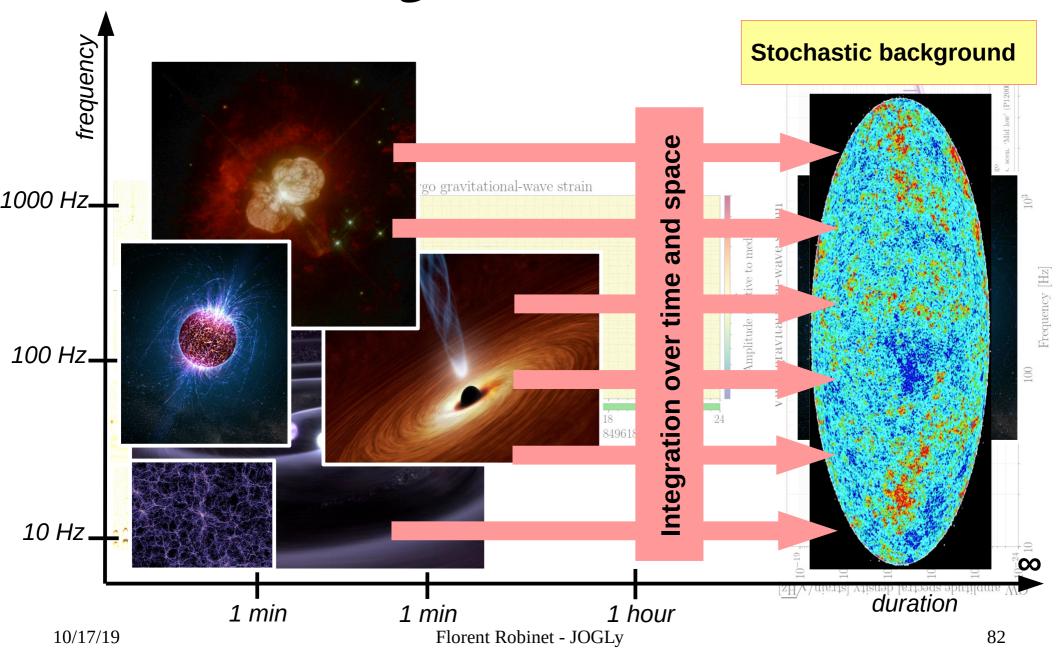
Tegion of interesting

All-sky search nothing

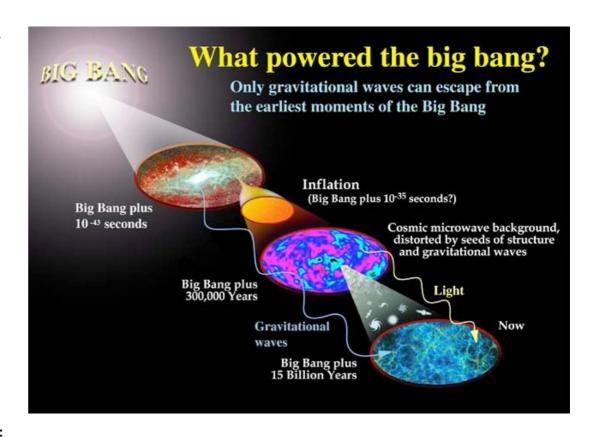
**Computational** cost



10/17/19

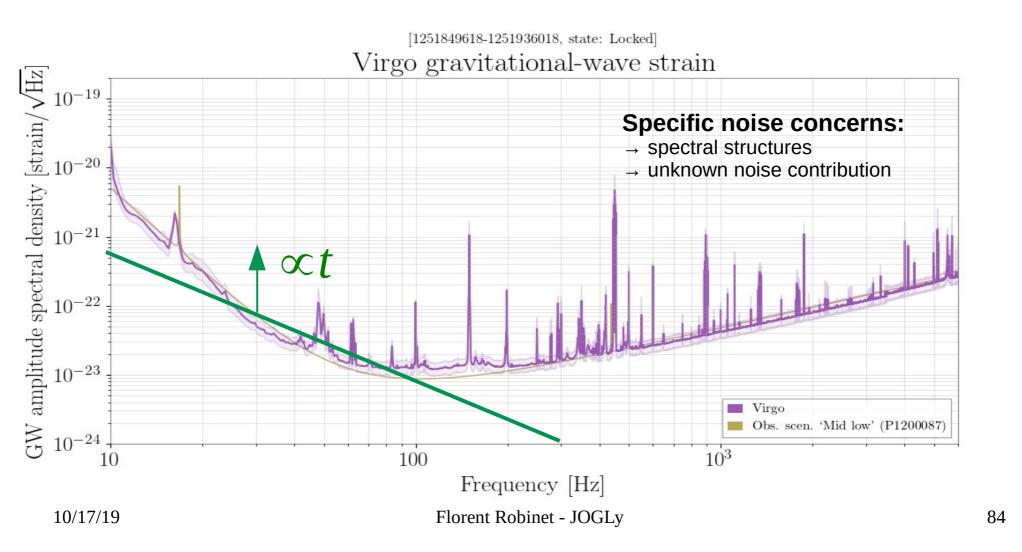


- Incoherent superposition of many unresolved sources.
- Cosmological:
  - Inflationary epoch, preheating, reheating
  - Phase transitions
  - Cosmic strings
  - Alternative cosmologies
- Astrophysical:
  - Supernovae
  - Magnetars
  - Binary black holes
- Potentially could probe physics of the very-early Universe.



$$\Omega_{GW}(f) = \frac{f}{\rho_c} \frac{d\rho_{GW}}{df}$$

 $\rightarrow$  A physical gravitational-wave spectrum is produced by the superposition of astrophysical (or cosmological) sources



Assumption: stationary, unpolarized, and Gaussian stochastic background

→ Cross correlate the output of detector pairs to eliminate the noise

$$\begin{aligned} h_i &= n_i + GW_i \\ \langle h_1, h_2 \rangle &= \langle GW_1, GW_2 \rangle + \langle n_1, GW_2 \rangle + \langle GW_1, n_2 \rangle + \langle n_1, n_2 \rangle \\ 0 & 0 & 0 \end{aligned}$$
 With  $\langle x_1, x_2 \rangle = \int_{-\infty}^{+\infty} \widetilde{x}_1^*(f) \widetilde{Q}(f) \widetilde{x}_2(f) df$ 

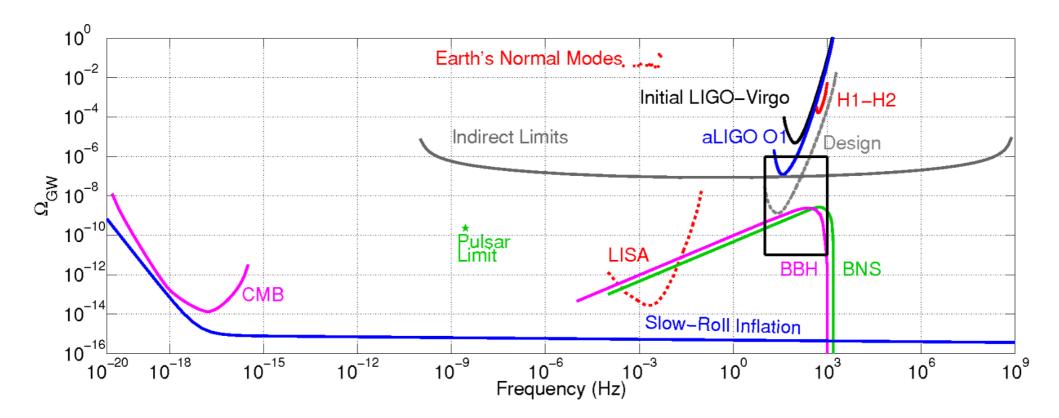
Optimal filter:

overlap of antenna pattern 
$$\widetilde{Q}(f) \propto \frac{\gamma(f)\Omega_{GW}(f)}{f^3 S_{n,1}(f) S_{n,2}(f)}$$
 GW spectrum 
$$\Omega_{GW}(f) = \Omega_{\alpha} f^{\alpha}$$
 Detector PSDs

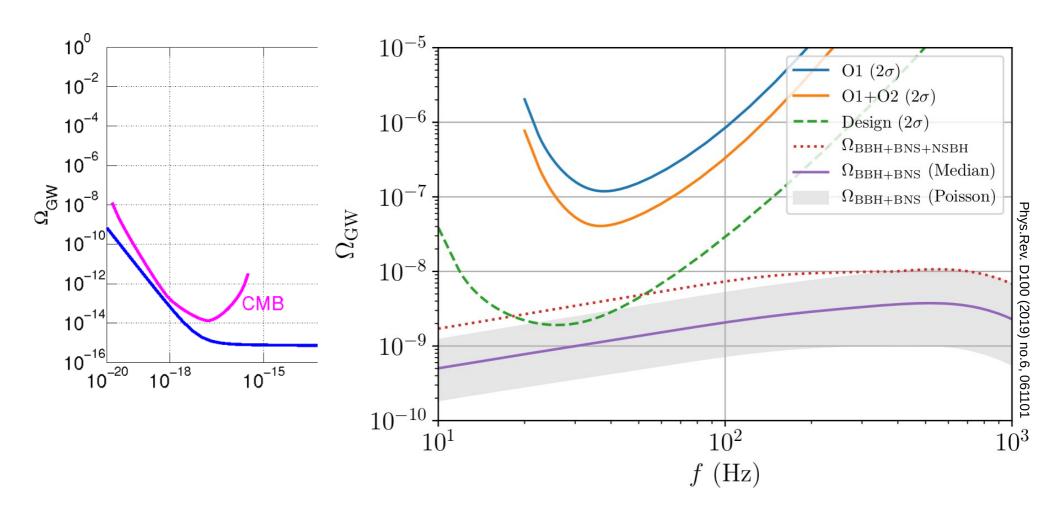
O1 isotropic search, for  $\alpha$  = 0 :  $\Omega_{GW}(25\,Hz)$  < 6.0  $\times 10^{-8}$ 

PRL.118.121101 (2017)

Use astrophysical (/cosmological) models to predict expected backgrounds and amplitude  $\rightarrow$  constraints on models



Use astrophysical (/cosmological) models to predict expected backgrounds and amplitudes → constraints on models



#### Conclusions

#### **O3**:

- → The LIGO-Virgo O3 run started on Apr. 1st 2019
- → The detectors improved their sensitivity (/O2)
- → The first half of the run is completed, offline data analyses are on-going

#### **Burst:**

- → 1 single public alert so far (excluding CBC): it has been retracted
- → Lots of work on transient noise to maximize the search sensitivity
- → Great hopes to witness THE supernova of the 21st century

#### **Continuous waves:**

→ keep digging the noise...

#### **Stochastic background:**

- → BBH/BNS background is not far...
- → Challenge: identify the source