

MAPPING THE OBSERVABLE UNIVERSE WITH 21CM



ALBERT STEBBINS
FERMILAB

COSYNE - INSTITUT D'ASTROPHYSIQUE DE PARIS
2019-12-11

Cosmic Cartography

area \propto volume

- parameter accuracy $\sim n_{\text{mode}}^{-1/2}$
- $n_{\text{mode}} \sim \text{volume}$

2D: CMB [SPT/ACT/S4]

large area galaxy imaging/spectroscopy

2D: single band imaging [APM]

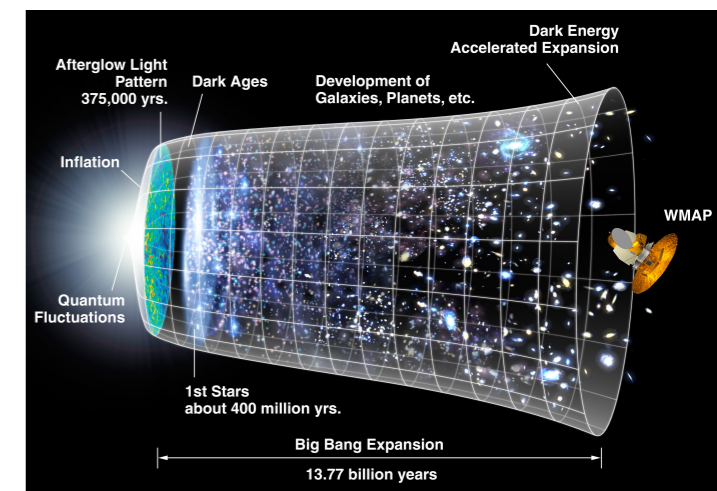
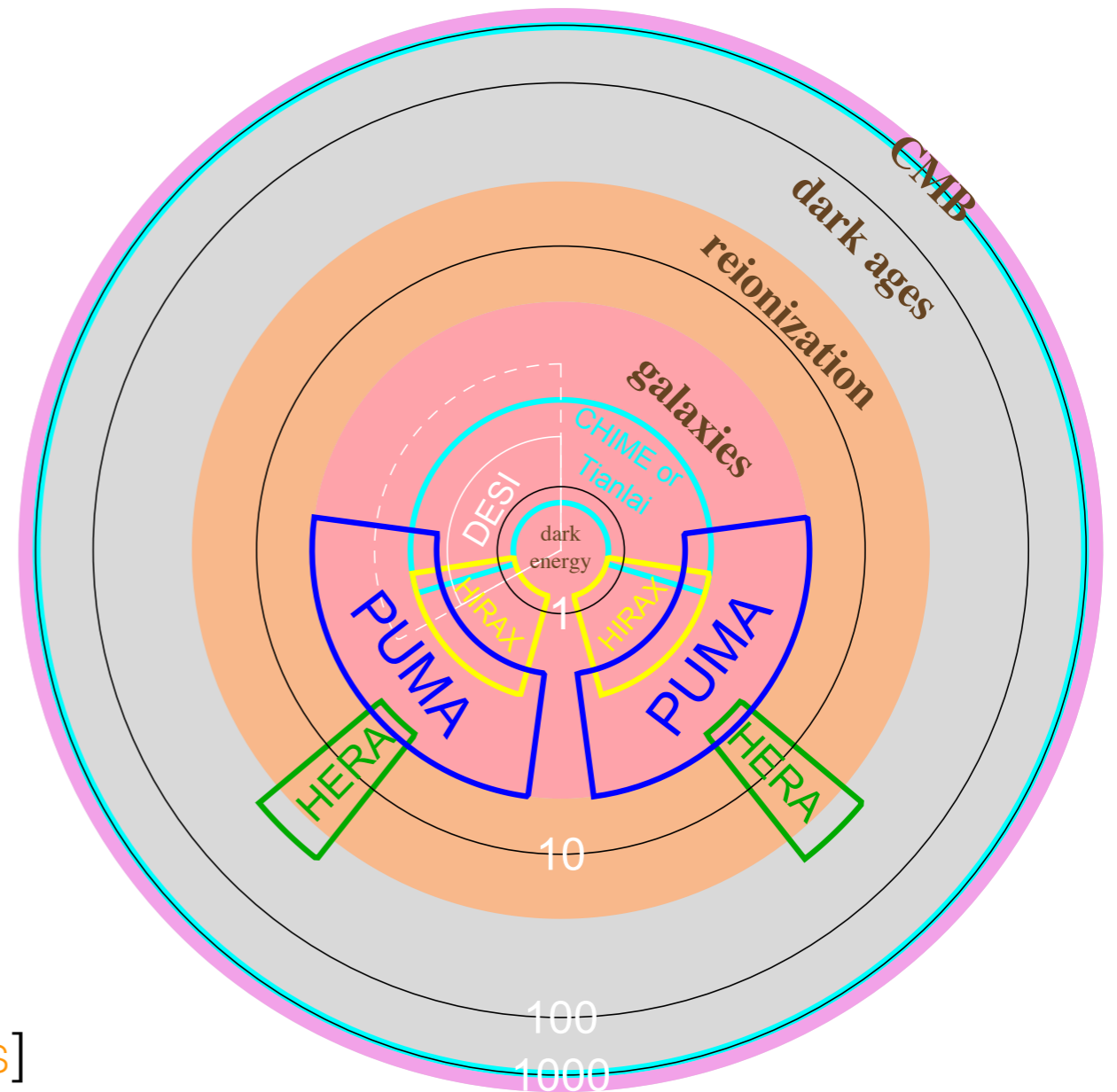
2D+: + multi-band photo-z's [DES/LSST]

3D-: + lo-res spectroscopy [PAU/JPAS/SphereX/MKIDS]

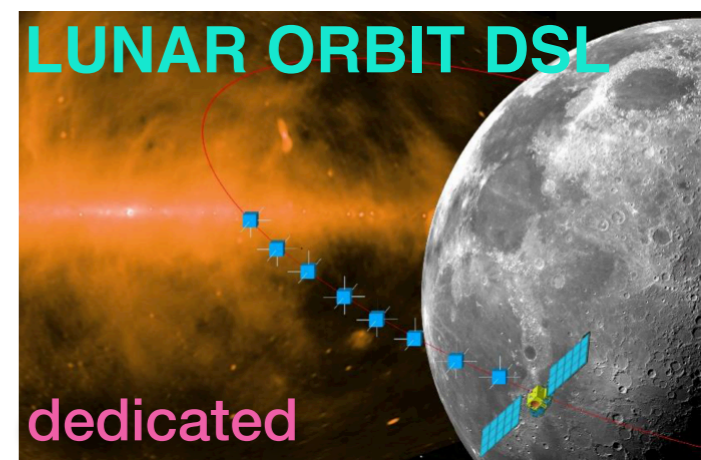
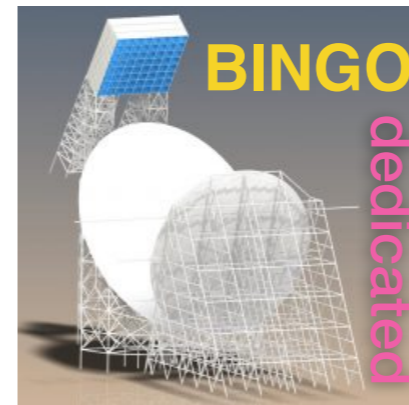
3D: + hi-res spectroscopy [APM/SDSS/DESI/4MOST/Euclid/WFIRST]

intensity imaging of galaxies/LSS

3D: + hi-res Hydrogen Intensity Mapping [CHIME/Tianlai/HIRAX/BINGO/SKA/PUMA]

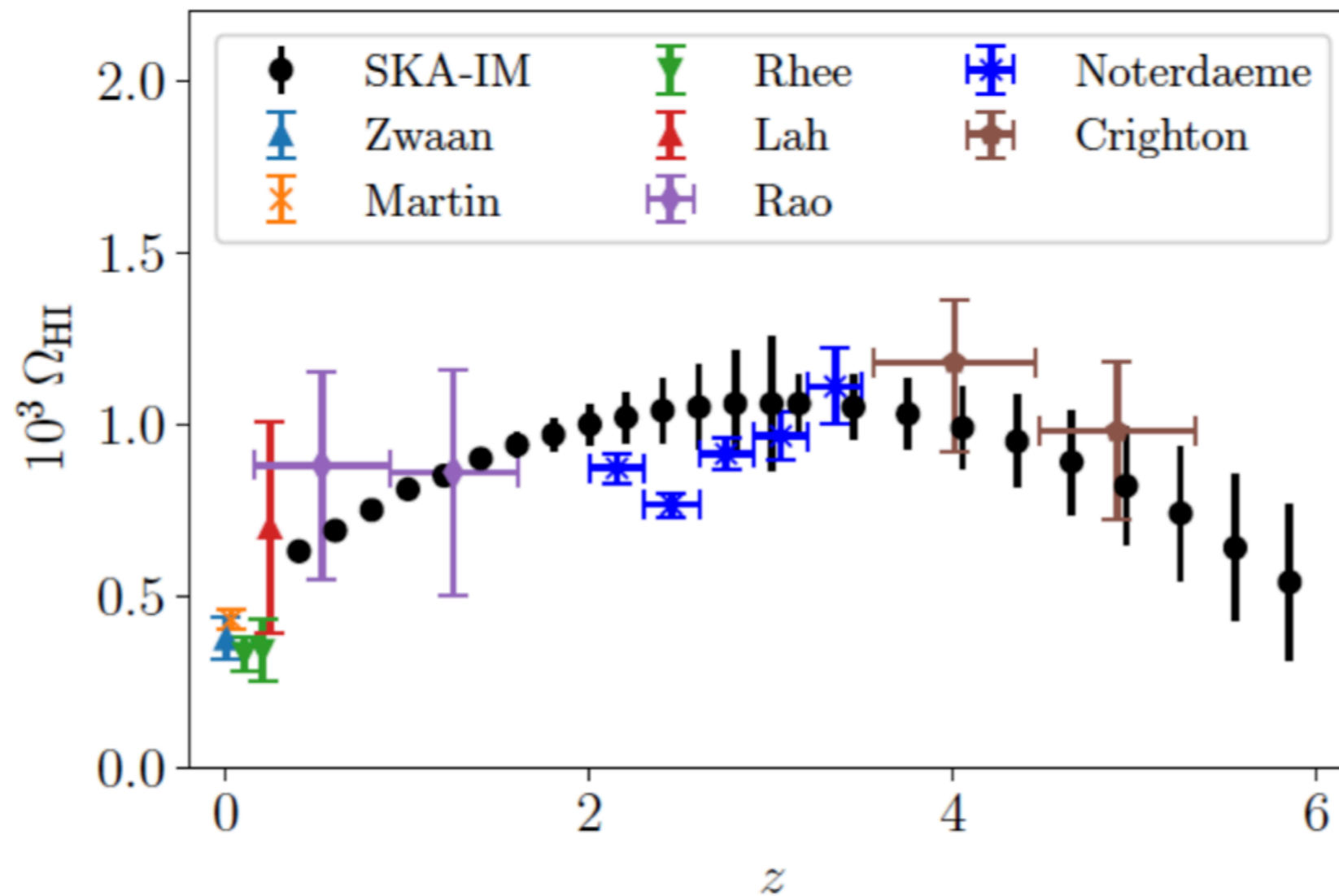


Hydrogen Intensity Mapping (HIM): experiments

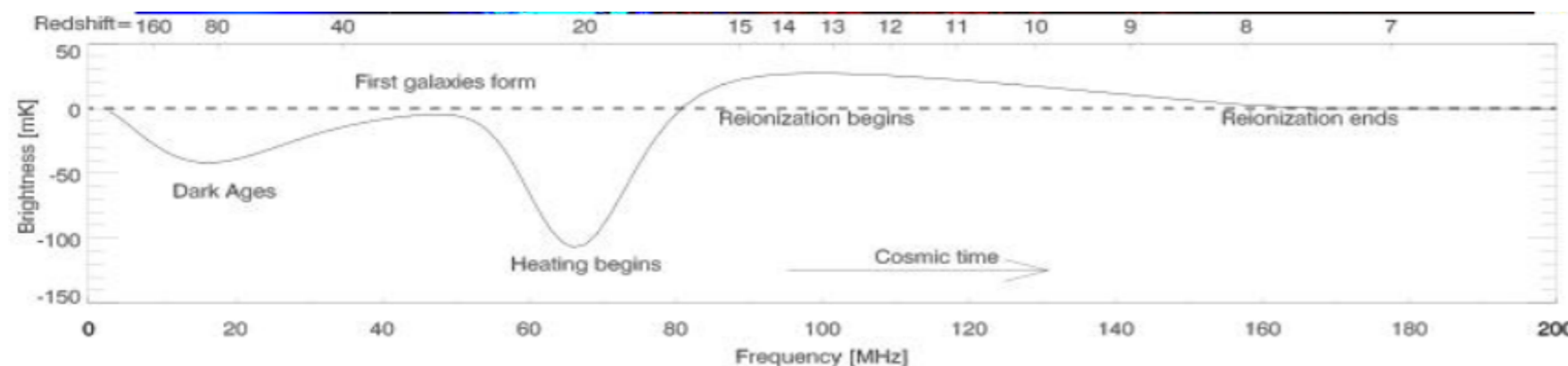


Hydrogen Intensity Mapping: neutral hydrogen (HI)

$$I_\nu = \frac{2}{\lambda^2} k T_{\text{RJ}} \quad \bar{T}_{\text{HI}} = \Omega_{\text{HI}}[z] \frac{9}{128\pi} \frac{\hbar c^3 A_{1,0} H_0}{G m_{\text{H}} \nu_{21} k} \frac{H_0 (1+z)^2}{H[z]} = 4.72 \text{ mK} \frac{\Omega_{\text{HI}}[z]}{10^{-3}} \frac{H_0 (1+z)^2}{H[z]}$$



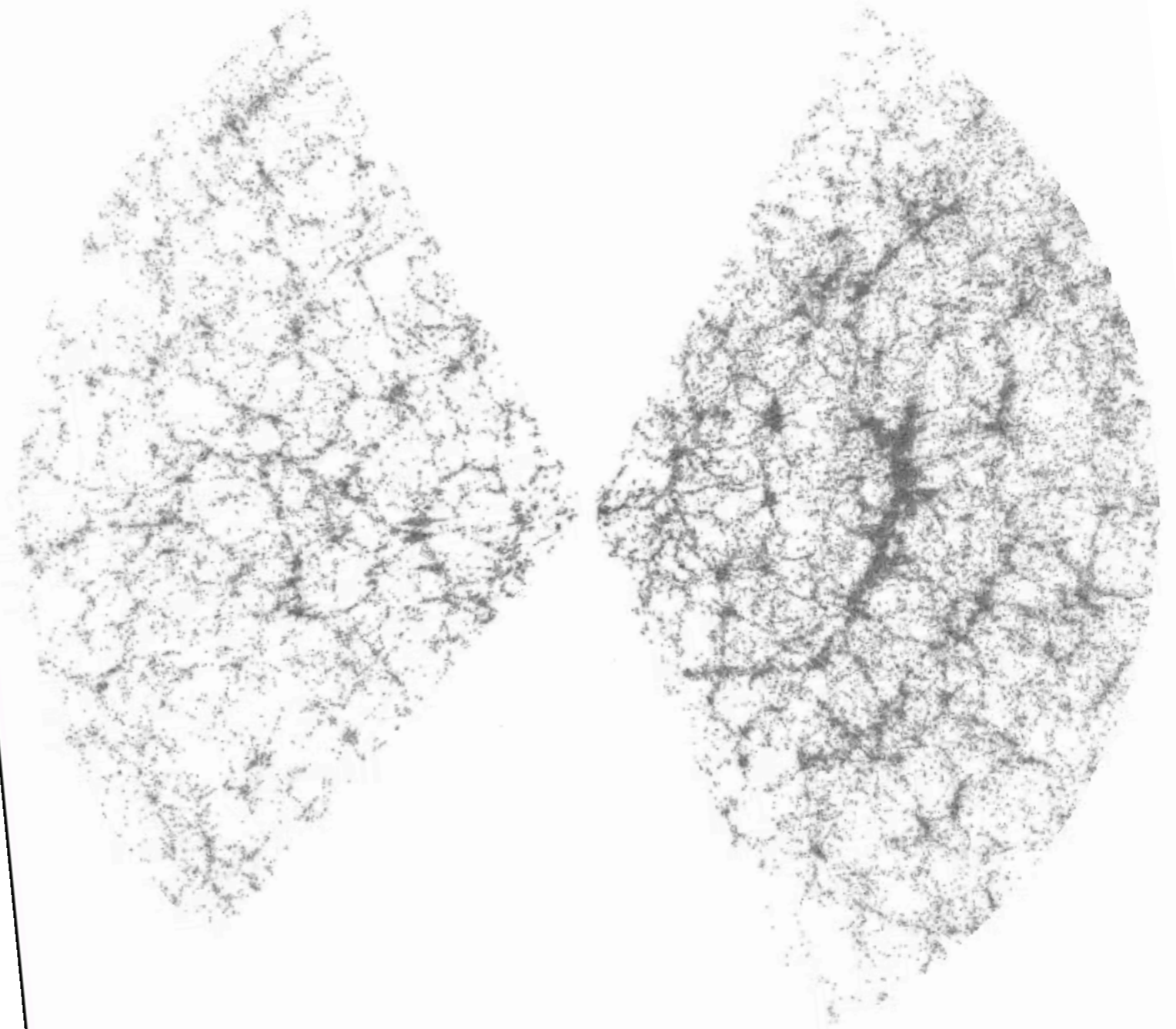
**Epoch
of
Galaxies**



**EoR /
Dark
Ages**

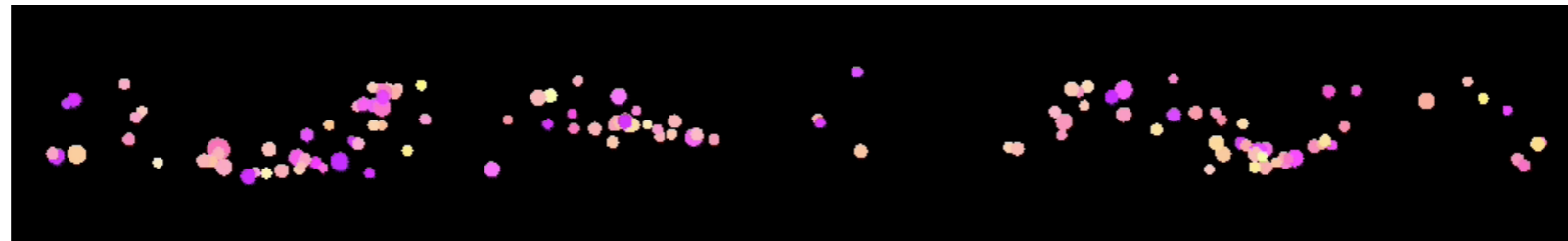
Intensity Mapping: technique

- **intensity mapping concept:** determine distribution of galaxies w/o resolving any of them by measuring the $I_{\nu}[\alpha, \delta]$.
- can only get galactic redshift this way only in parts of the EM spectrum where a single special lines “dominates” so there is no “confusion” about $z[\nu]$.
- or by correlation redshifts e.g. w/21cm
- radio broad spectrum “foregrounds” will be brighter than 21cm line emission from galaxies - however this emission is very smooth spectrum and galactic 21cm lines should dominate other “wiggles: in the spectrum.
- Intensity mapping proposed for
 - HI (21cm 1.4GHz) ($0 \leq z \leq 100$)
 - CO (14, 29 GHz) ($z \geq 6$)
 - CII (237 GHz) ($6 \leq z \leq 8$)
 - Ly- α (1.2 μ m) ($2 \leq z \leq 12$)



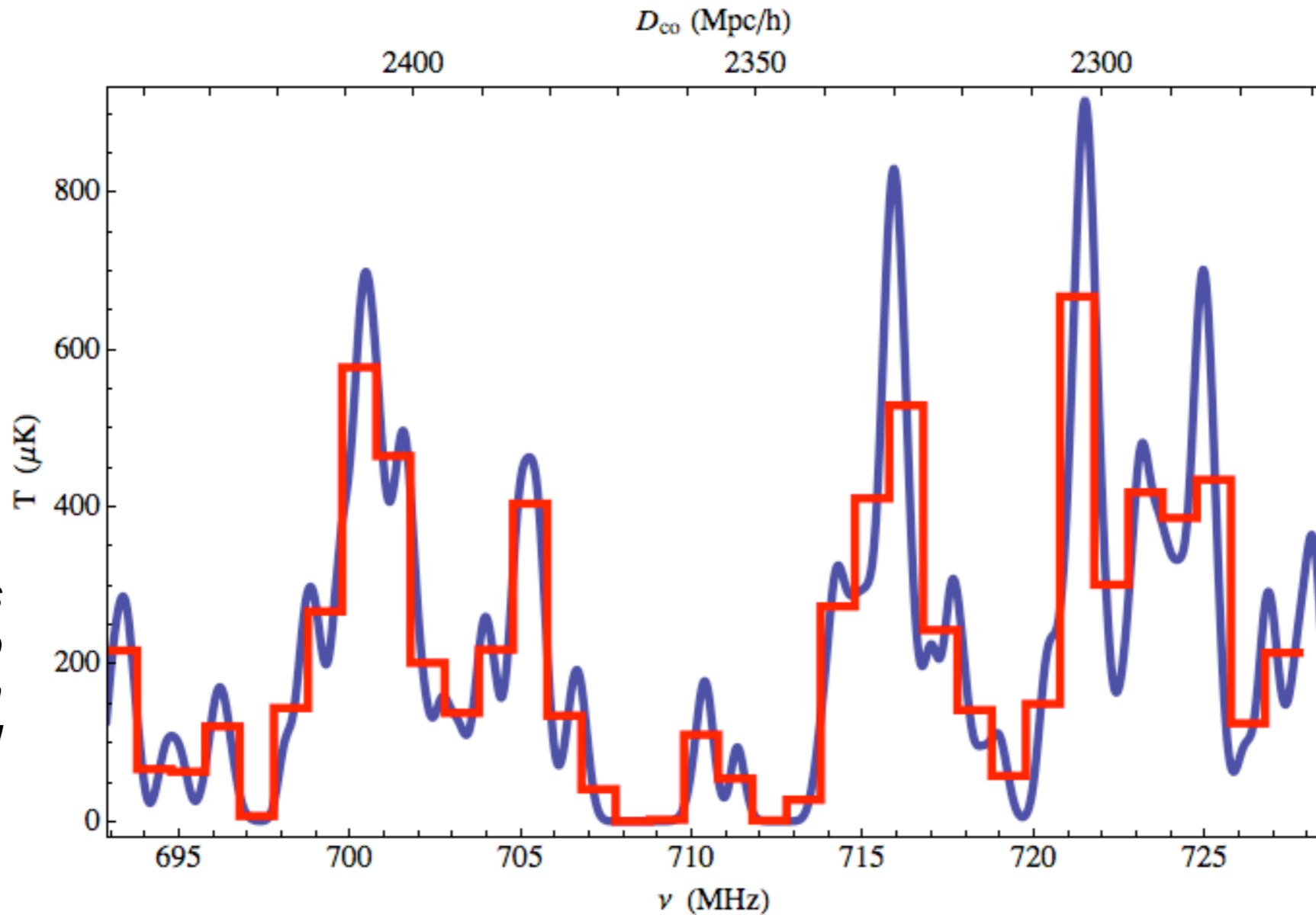
“Expensive” to resolve individual galaxies

Hydrogen Intensity Mapping: Redshift Clump Detection



DEEP2
Davis ++ 2004++

$\delta v = 1$ MHz
 $\delta \theta = 10'$
Tully-Fisher
 $M_{\text{HI}} \propto L_B$
no ellipticals
*!ellipticals
believed to
contain a
lot of HI!*



see Wang ++ 2006

21cm brightness

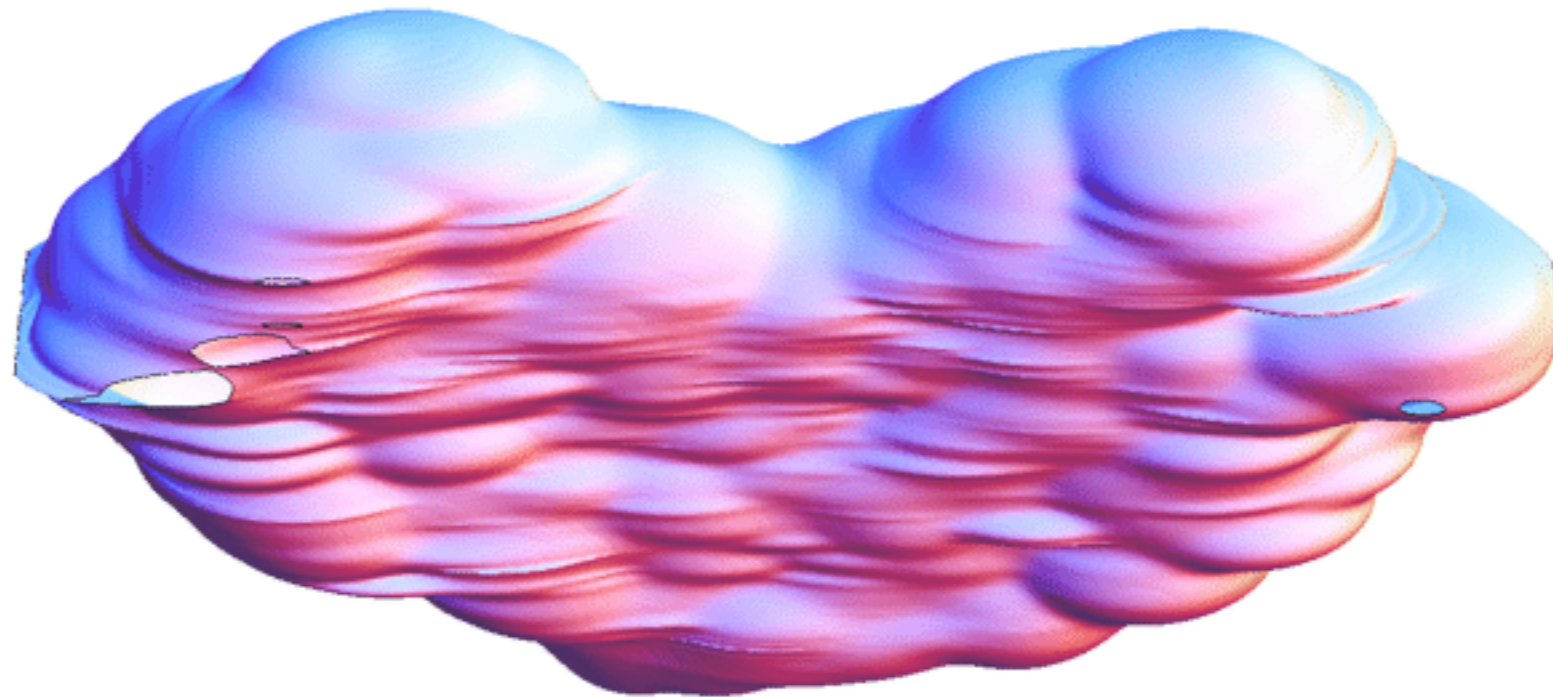
One can nearly resolve galaxy structures in redshift space.

non-Gaussian features in maps

Hydrogen Intensity Mapping: 3D Maps

21cm iso- T_{RJ} contours of slice of Alfalfa HI redshift survey
 includes galaxy line-widths / velocity dispersions
 translated to $z=1$ smoothed: $\delta\nu=100\text{kHz}$ $\delta\theta=10'$

*stack
of
pancakes*



- S/N ≥ 1 requires $\delta T_b \gtrsim 100 \mu K$

$$T_{RJ} = 1 \mu K$$

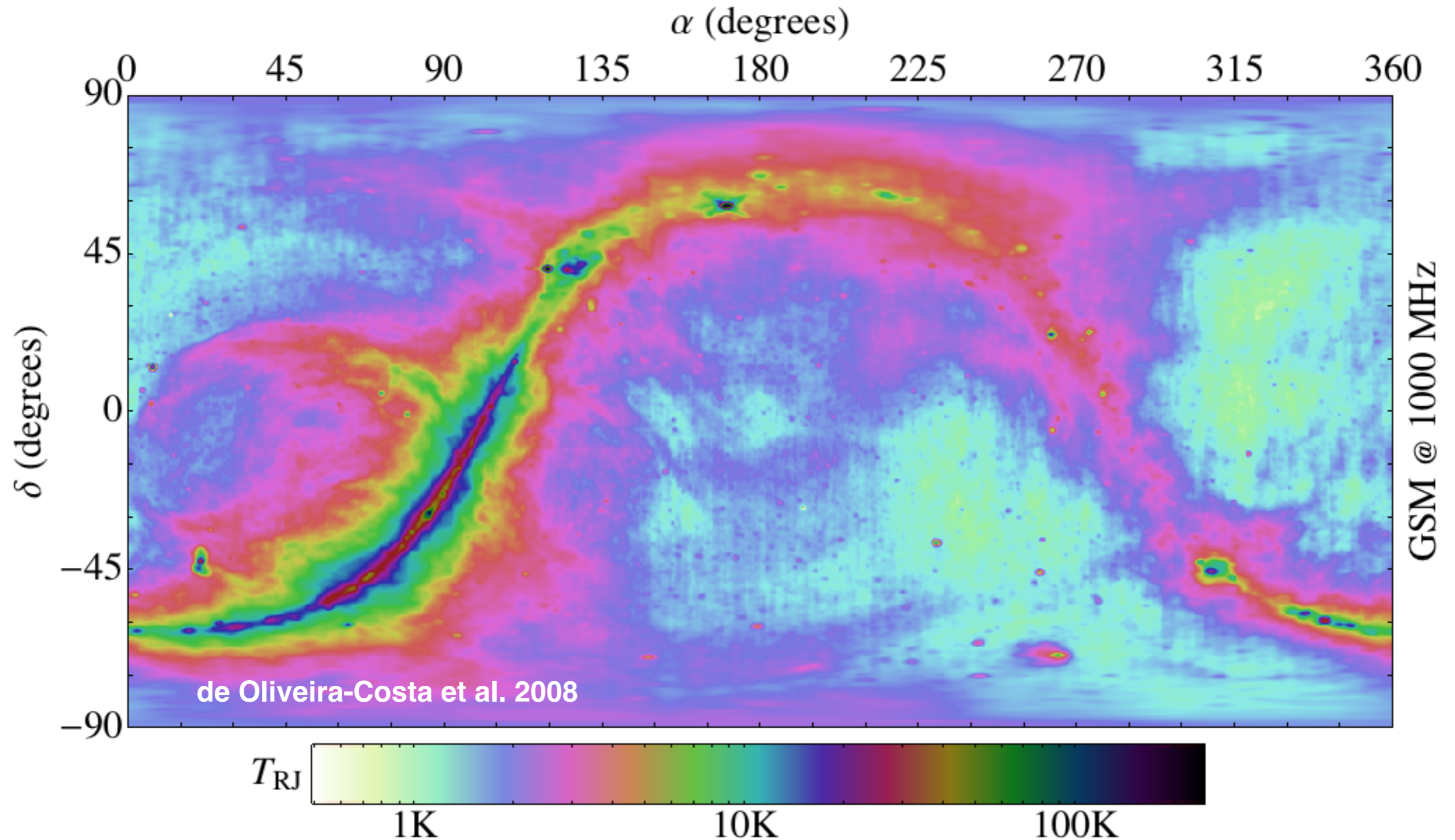
- HIM easily obtains high spectral (redshift) resolution $\delta R_{co} = (1+z)^2 \frac{c}{H[z]} \frac{\delta\nu}{\nu_{21}} = 2.9 \text{ Mpc} \left((1+z)^2 \frac{H_0}{H[z]} \right) \frac{\delta\nu}{\text{MHz}}$

$$\delta\theta \sim \frac{\lambda}{b_{\max}} = 10' \frac{72 \text{ m}}{b_{\max}} (1+z)$$

- angular resolution more difficult

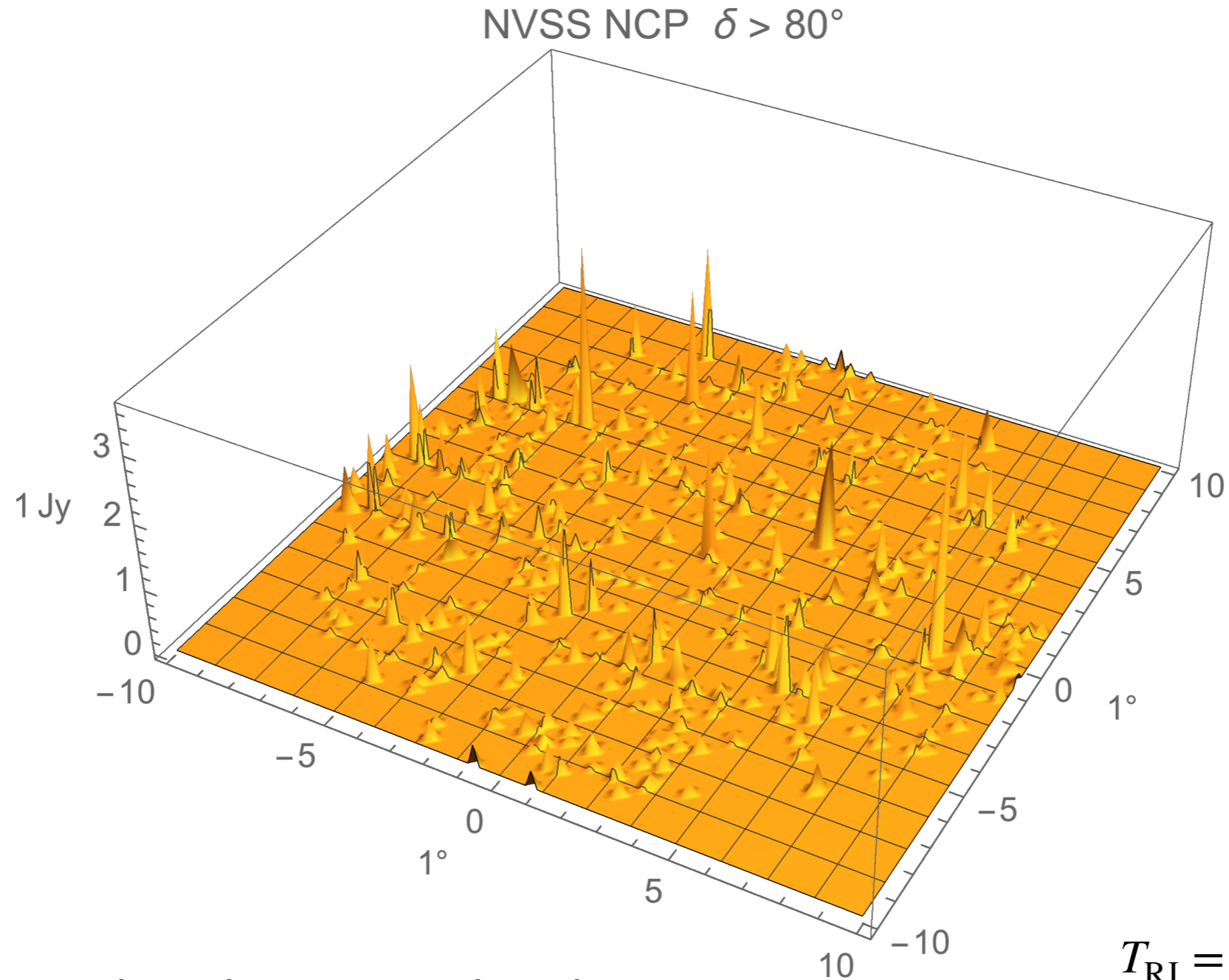
$$\delta R_{co}^{\perp} = \delta\theta \int_0^z \frac{c dz}{H[z]} = 10 \text{ Mpc} \frac{\delta\theta}{10'} \int_0^z dz \frac{H_0}{H[z]}$$

Hydrogen Intensity Mapping: Galactic Foregrounds



versus $\sim 3^+ \text{K}$! **prediction:** this will be worked out by 2020

Hydrogen Intensity Mapping: ExtraGalactic Foregrounds



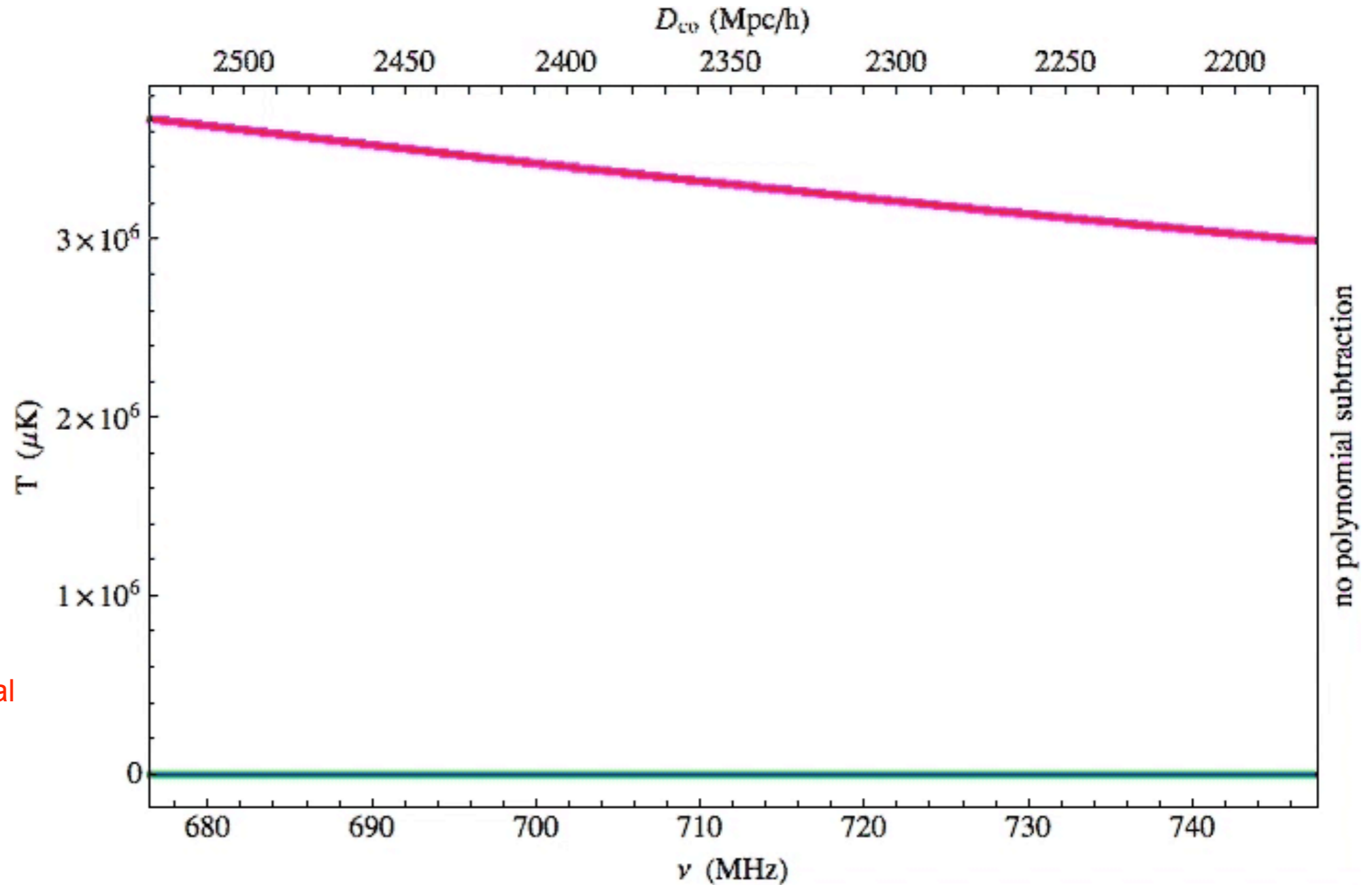
Not feasible to mask, subtract or otherwise remove every extragalactic radio sources!

Must find “generic” method of source removal in order to unmask 21cm signal.

$$T_{\text{RJ}} = \frac{\lambda^2}{2k\Omega_p} f_\nu$$
$$= 1.9 \text{ K} (1+z)^2 \frac{f_{\nu_{21}}}{\text{Jy}}$$

Hydrogen Intensity Mapping: Foreground Filtering

see also Wang ++ 2006



21 cm signal

21cm-polynomial

21 cm+synch-polynomial

residual

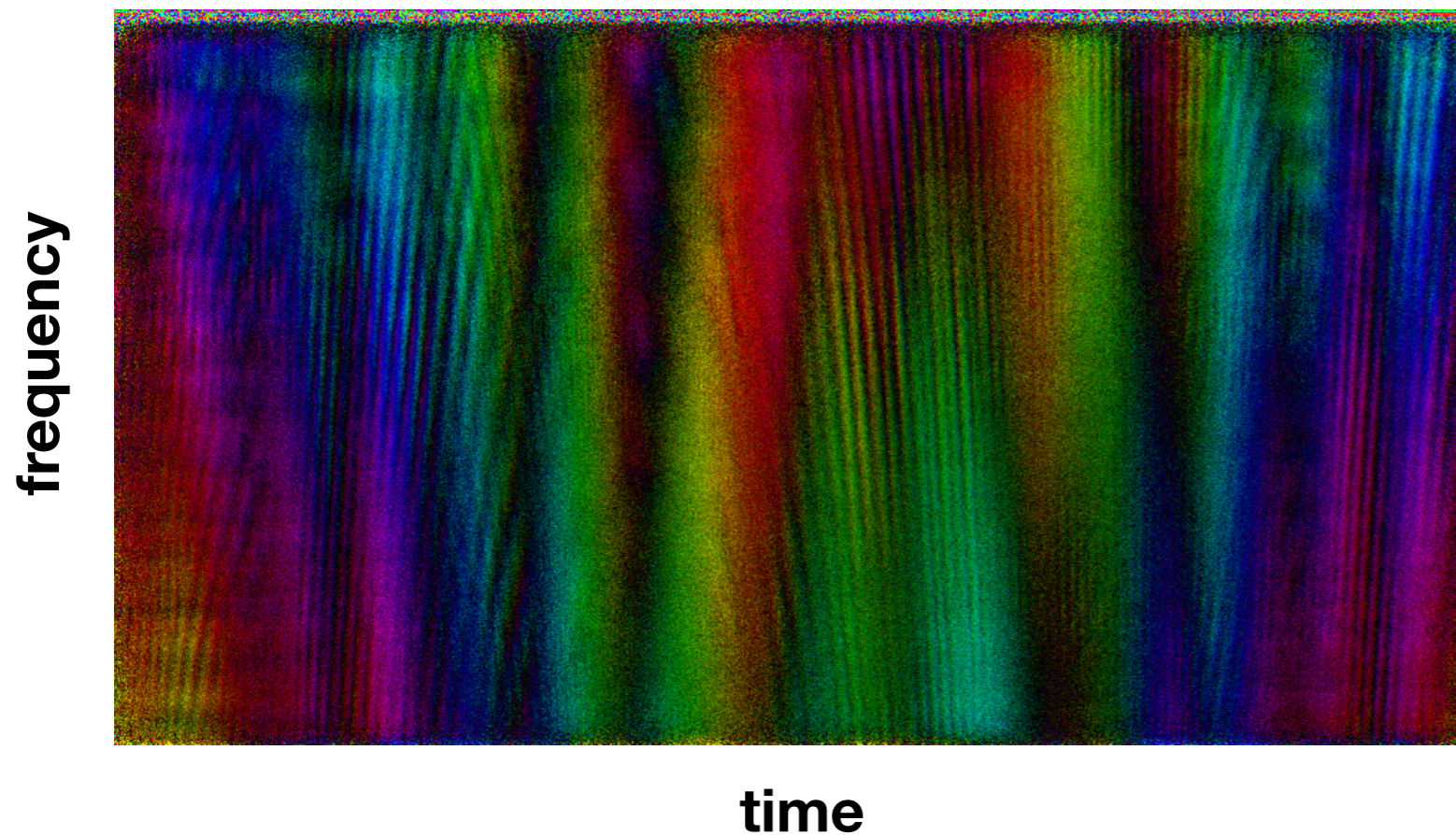
$\Delta\theta=10'$

Model: Maximally Curved Synchrotron + DEEP2 galaxies

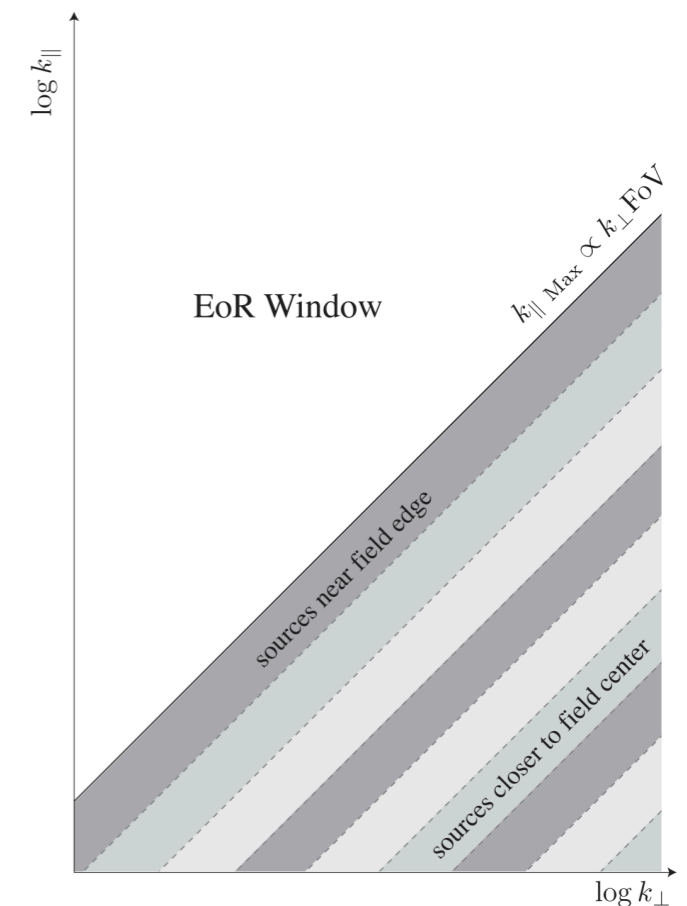
Hydrogen Intensity Mapping: The Wedge

In radio astronomy beams are always *chromatic*

- beam patterns on sky vary with frequency.
- this mixes angular variation which can be very non-smooth with frequency variation which might be smooth (*mode mixing*)
- lo-pass filtering in frequency will first reveal spatial variations



(complex) interferogram or visibility



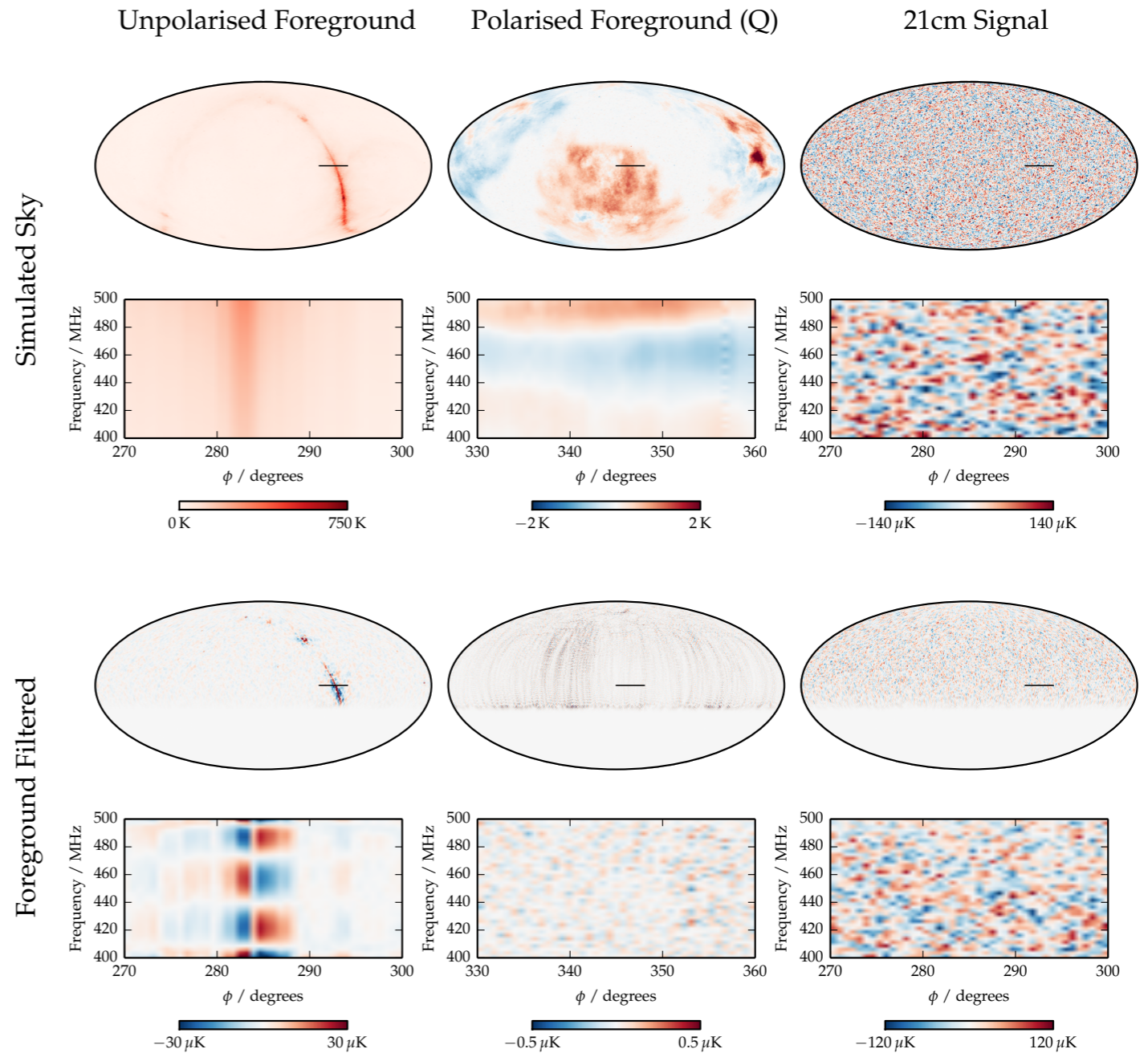
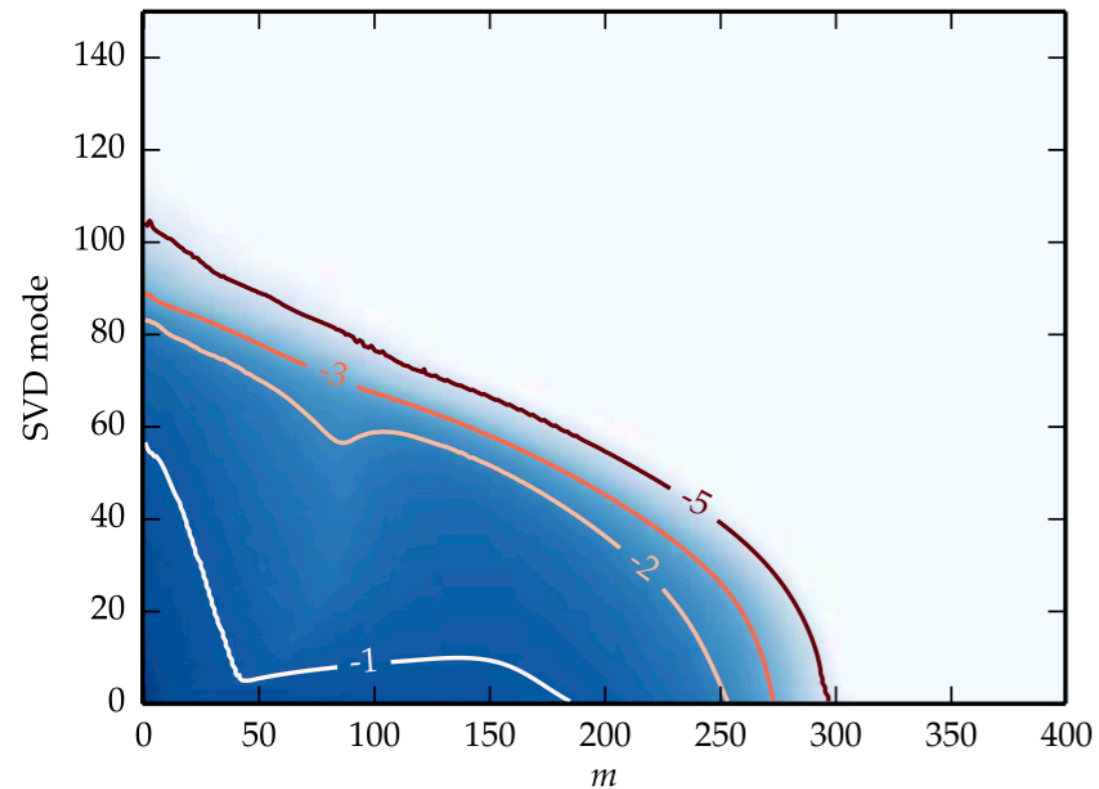
Hydrogen Intensity Mapping: Non Smooth Foregrounds

- RFI (human made Radio Frequency Interference) often line like.
 - it is not the obvious RFI that is the problem - other low level RFI will persist in data.
 - intermittent RFI will not repeat with sidereal day - astrophysical sources will
- Self absorbed synchrotron may be more non-smooth
 - GPS (Gigahertz Peaked Sources) may be example of this.
- Faraday rotated linearly-polarized source will oscillate with frequency in each linear polarization but not intensity.
 - Some leakage of polarization into intensity is inevitable for off axis sources.
 - proper map-making can reduce polarization leakage

Hydrogen Intensity Mapping: Foreground Filtering

m-mode
21cm / foreground
Karhunen-Loève decomposition

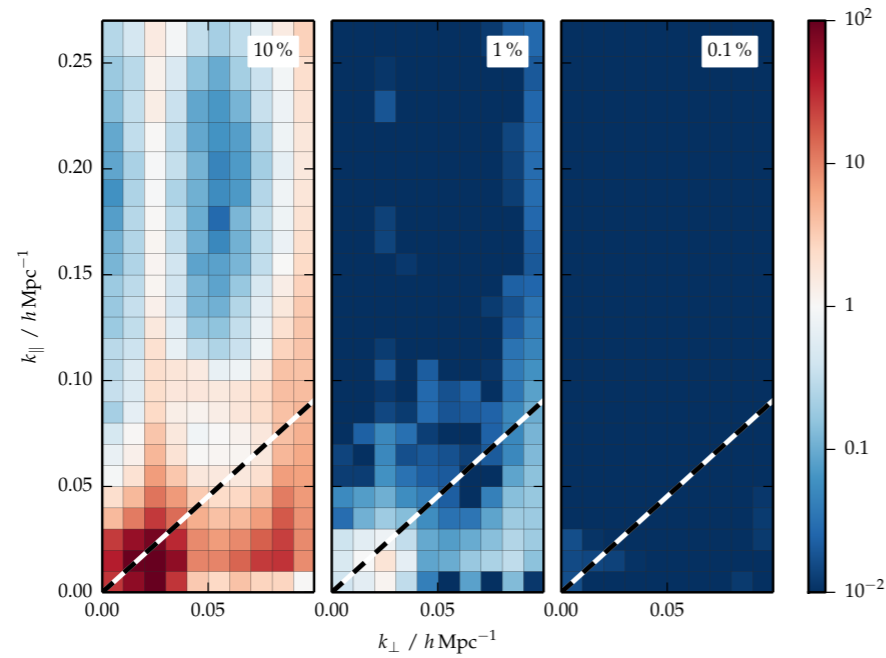
SVD spectrum ($\log_{10} \Sigma / \Sigma_{\max}$)



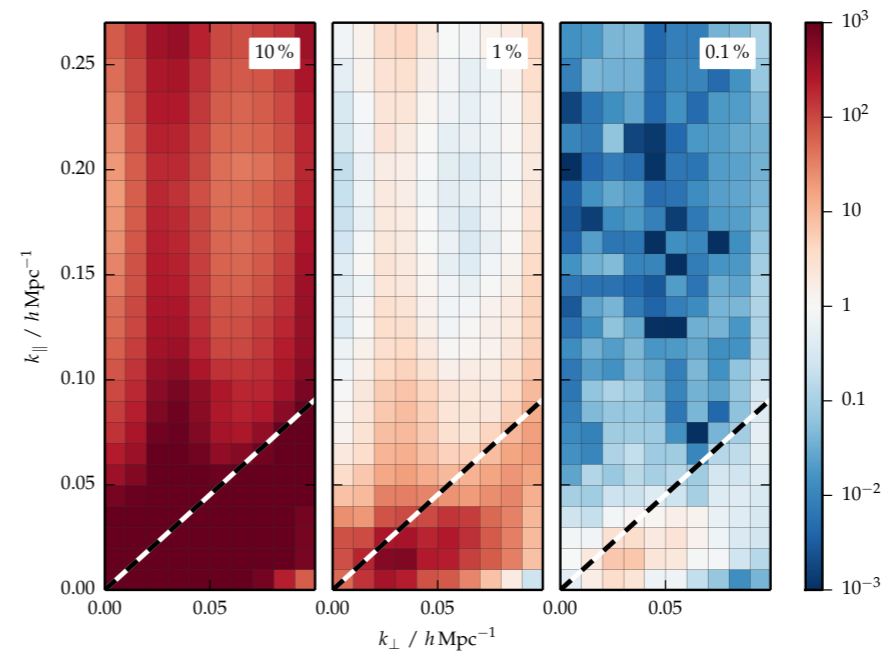
Hydrogen Intensity Mapping: Beam Calibration

foreground leakage

gain errors

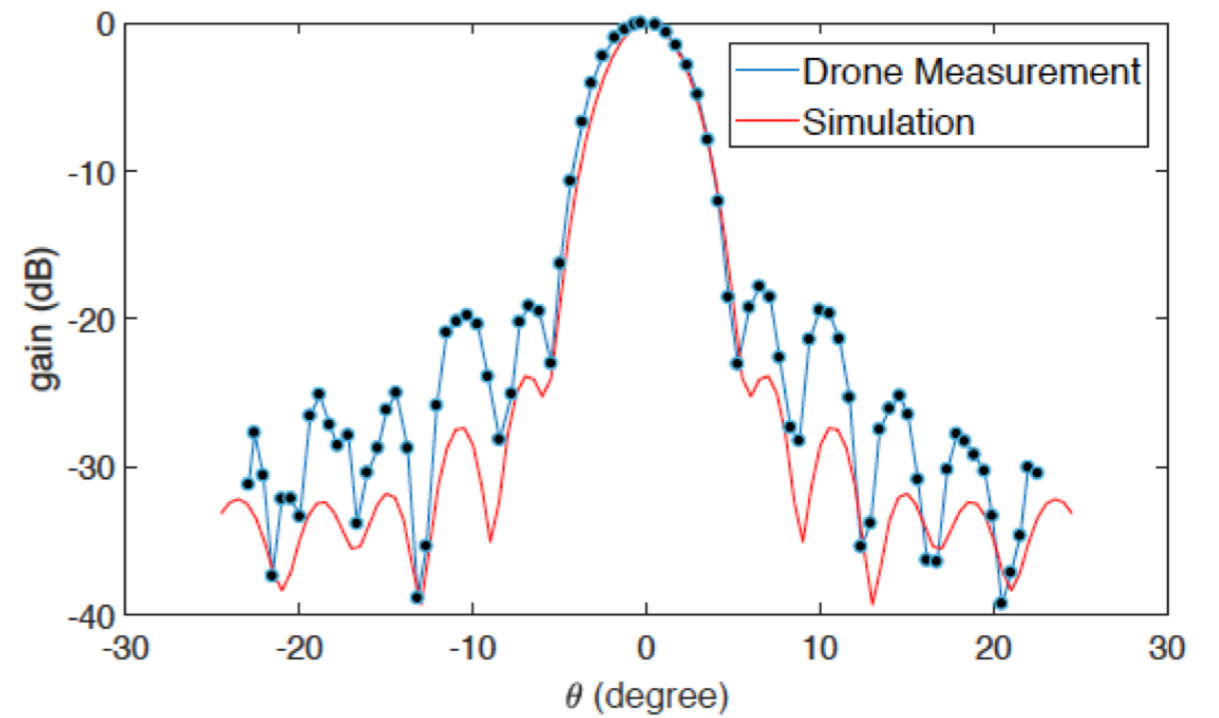


beam errors



Shaw++ 2014

Tianlai drone



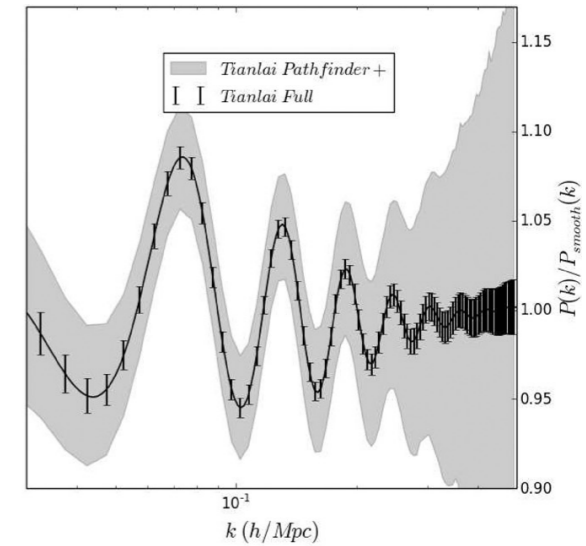
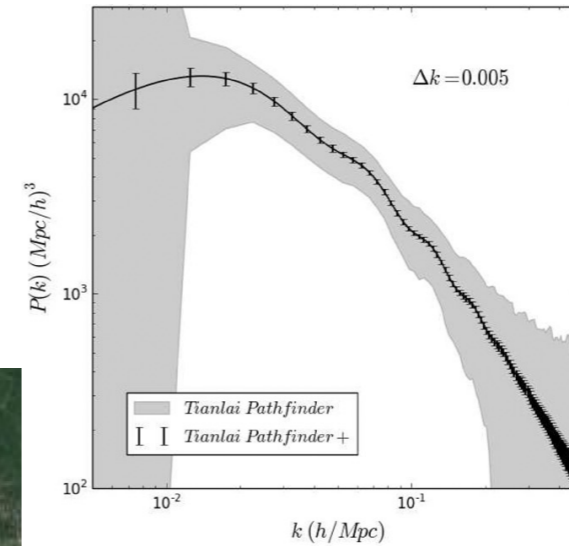
The Tianlai Project



Tianlai Pathfinder

Hydrogen Intensity Mapping: The Tianlai Project

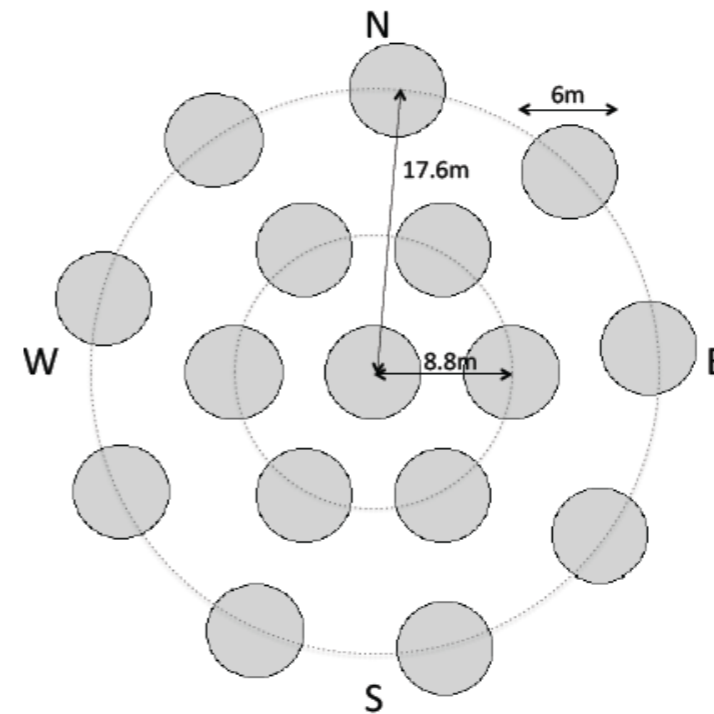
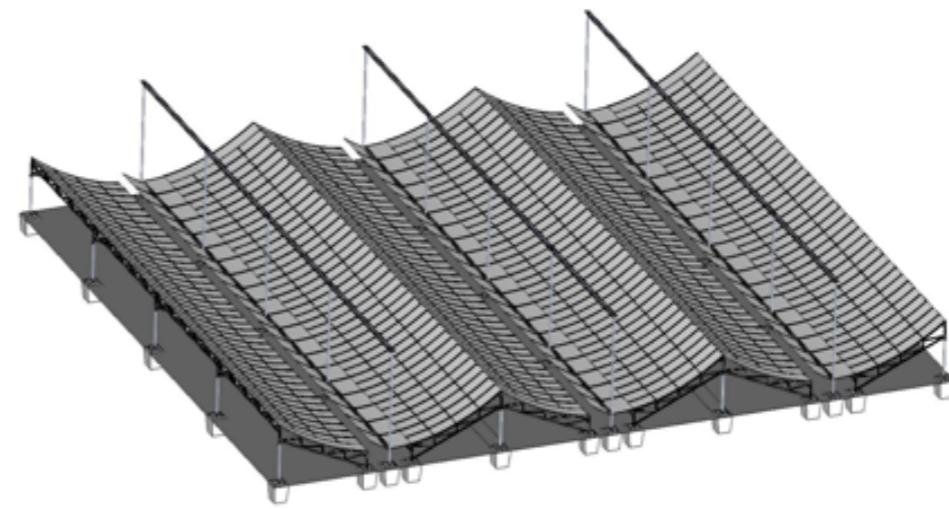
Tianlai ~ “*Heavenly Sound*”



Hydrogen Intensity Mapping: The Tianlai Pathfinder

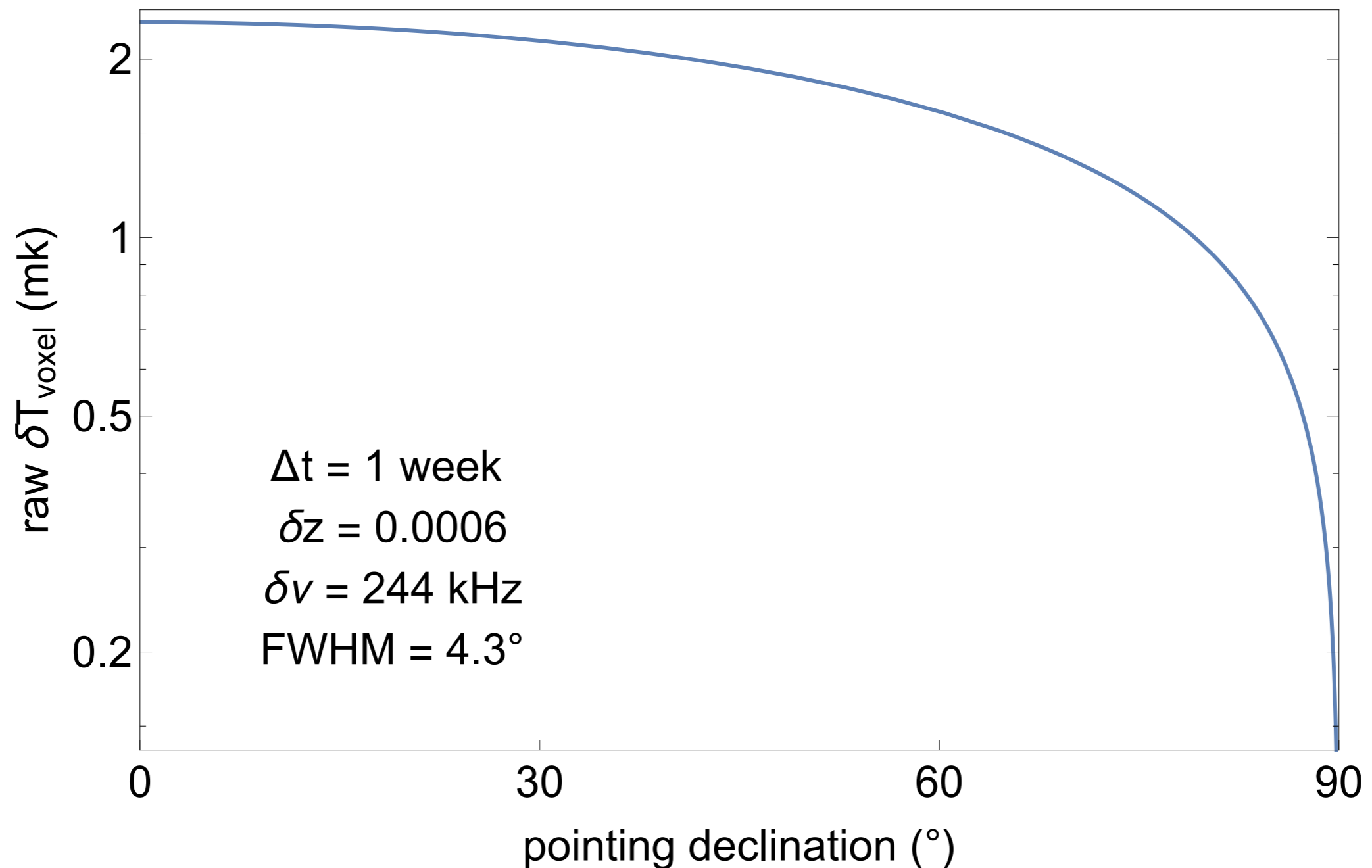
Pathfinders to demonstrate basic principle
and encounter all issues rapidly

- **Band** 685-810MHz ($0.77 < z < 1.3$)
512 frequency channels
($\Delta\nu=125\text{MHz}$ $\delta\nu=244\text{kHz}$ $\delta z=0.0002$)
tunable in 600-1420MHz ($0 < z < 1.5$)
- **Cylinder Array** 3 x 15m x 40m cylinders
96 dual polarization feeds
4 sec sampling
- **Dish Array** 16 x 6m dishes
16 dual polarization feeds
1 sec sampling
- **Pathfinder+ Cylinder Array**
216 dual polarization feeds
4 sec sampling
- **Proposed Full Cylinder Array** 8 x 15m x 120m
2048 dual polarization feeds
400-1420MHz



HIM: Tianlai Dish Polarscope

BY POINTING DISH ARRAY TOWARD POLE WILL INTEGRATE DOWN TO LOW MAP NOISE TEMPERATURE VERY RAPIDLY SINCE ONE IS ALWAYS POINTING AT SAME SPOT ON SKY.



HIM: Tianlai Visibility: 10 Days

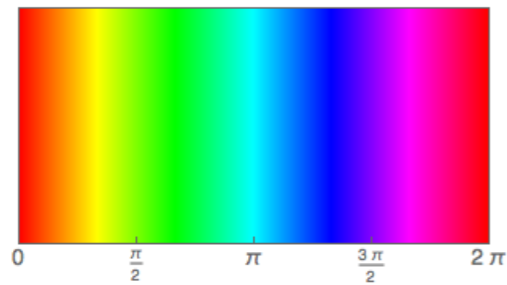
example of one “good” visibility $V_{3 \times 31}$.

this is raw correlator data

11 sidereal days top to bottom
2018-01-02 02:44:15 to 2018-01-11 20:44:12

brightness gives $|V_{3 \times 31}|$

color gives complex phase

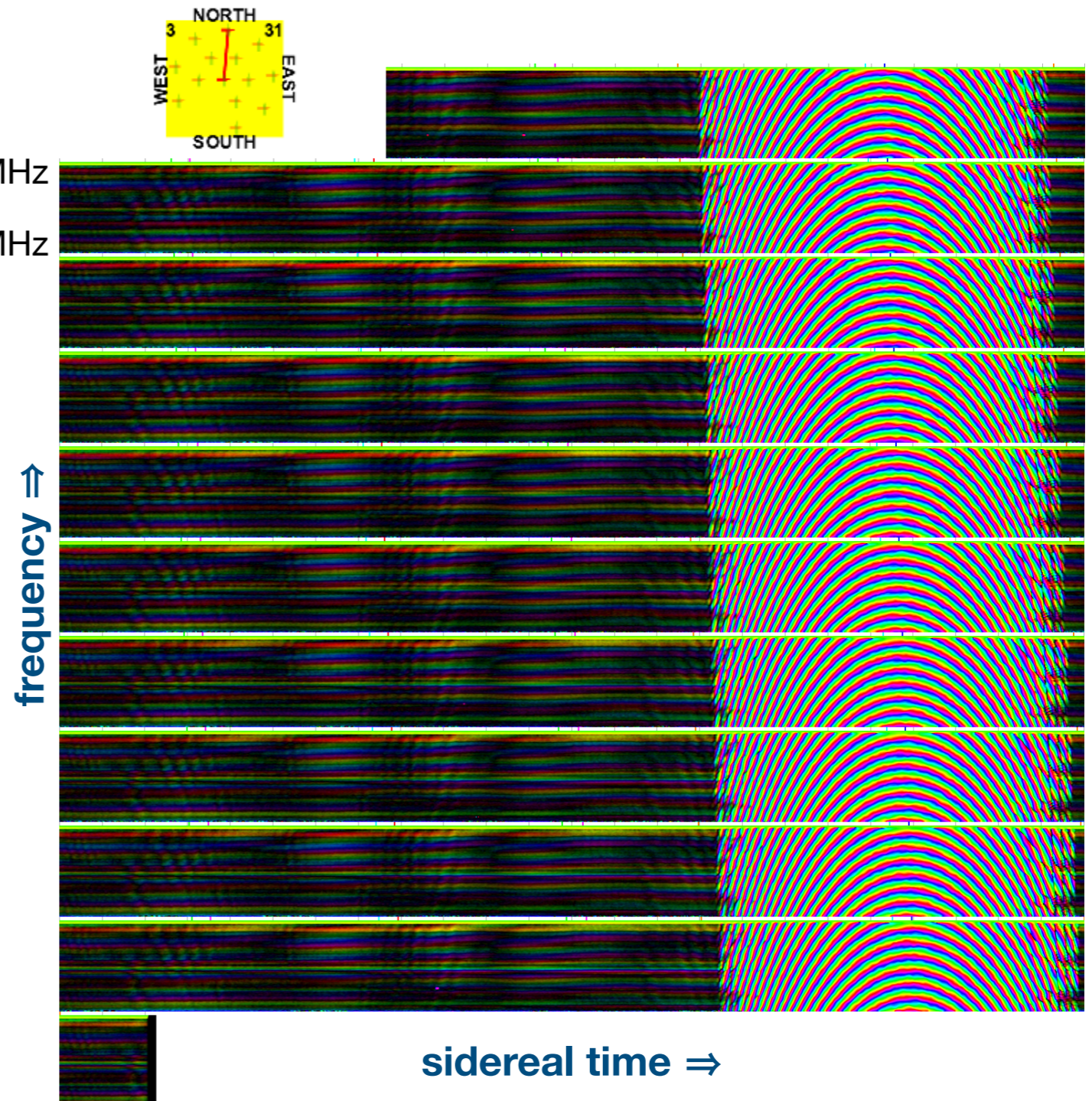


bright swath of fringes from Sun

fringes vary because Earth rotates
bow occurs when Sun passes “above” baseline
direction

Sun dominant source even 110° off axis

dimmer fringes still visible at night



(complex) interferogram or visibility

HIM: Tianlai Visibility: 10 Nights

nighttime only view of $V_{3 \times 31}$
nighttime mean subtracted for each frequency
image intensified to show nighttime fringes

visibilities repeat with sidereal day period
signal from the sky

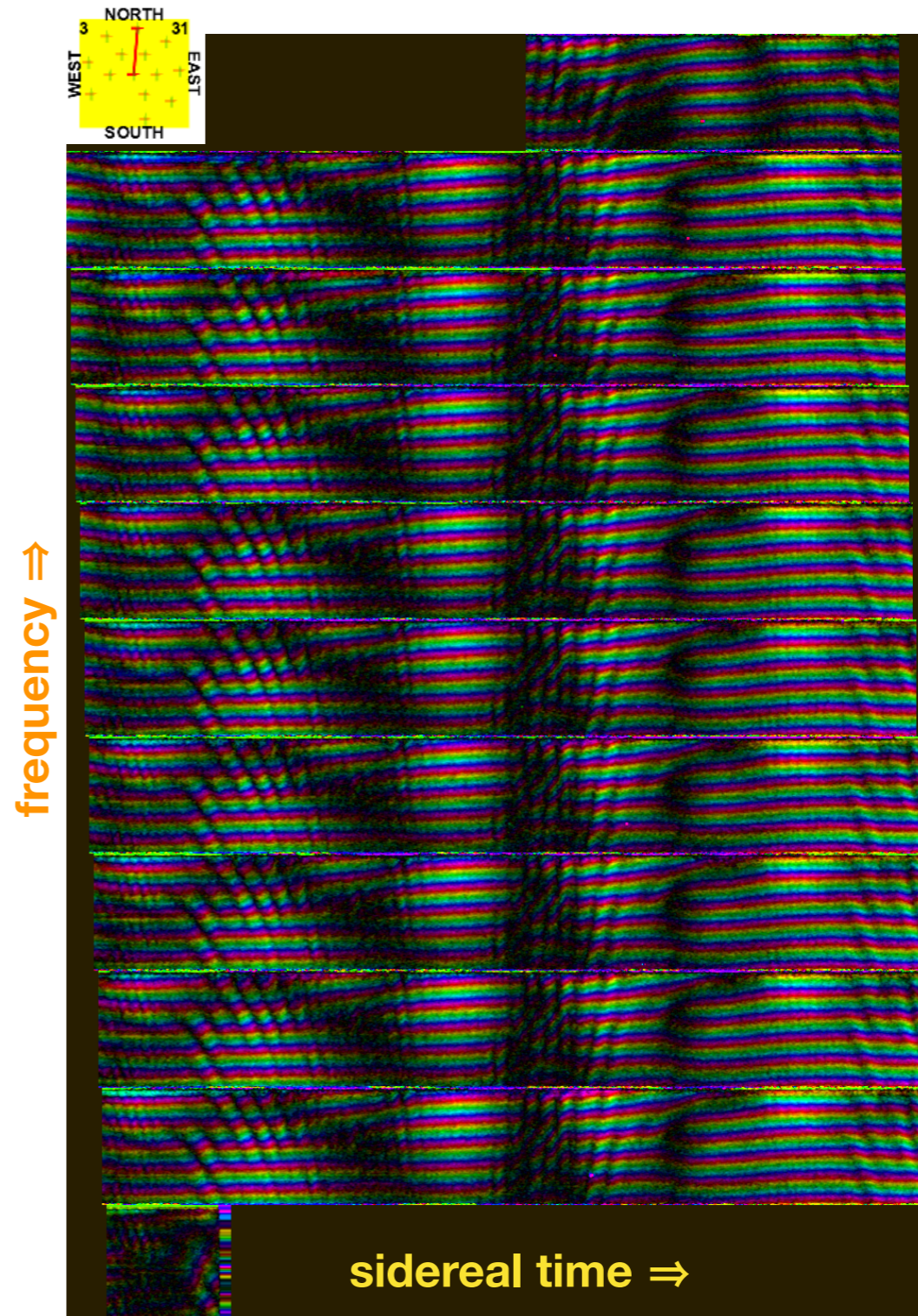
fringe pattern more complicated than bow
indicating multiple bright sources in 2° beam
centered on North Celestial Pole

bright and dark patches
constructive/destructive interference between sources

good S/N in 1 min \times 1 MHz pixels

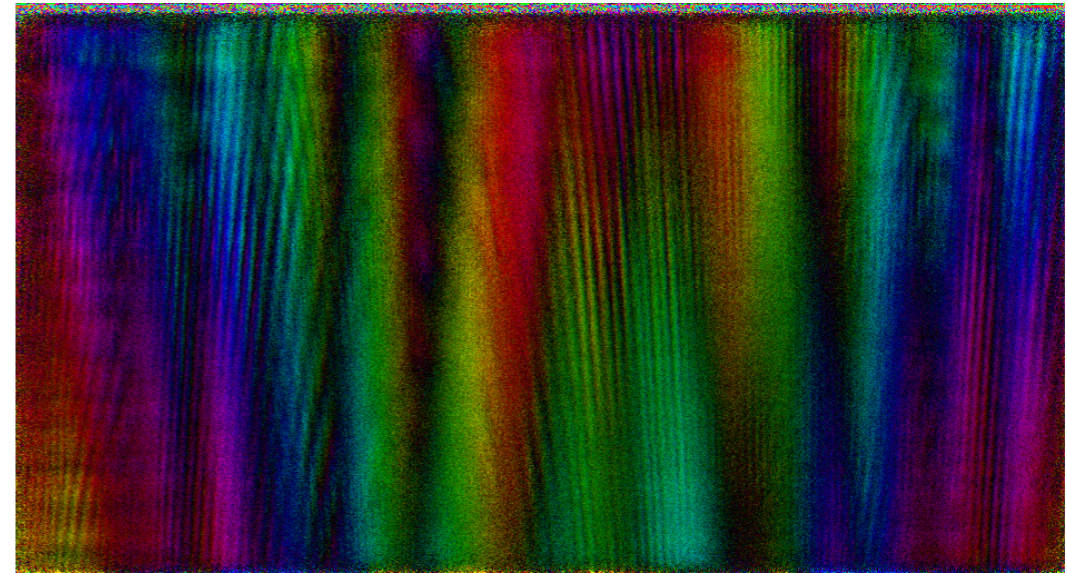
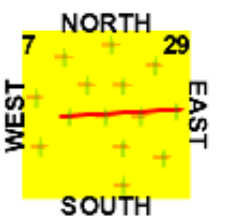
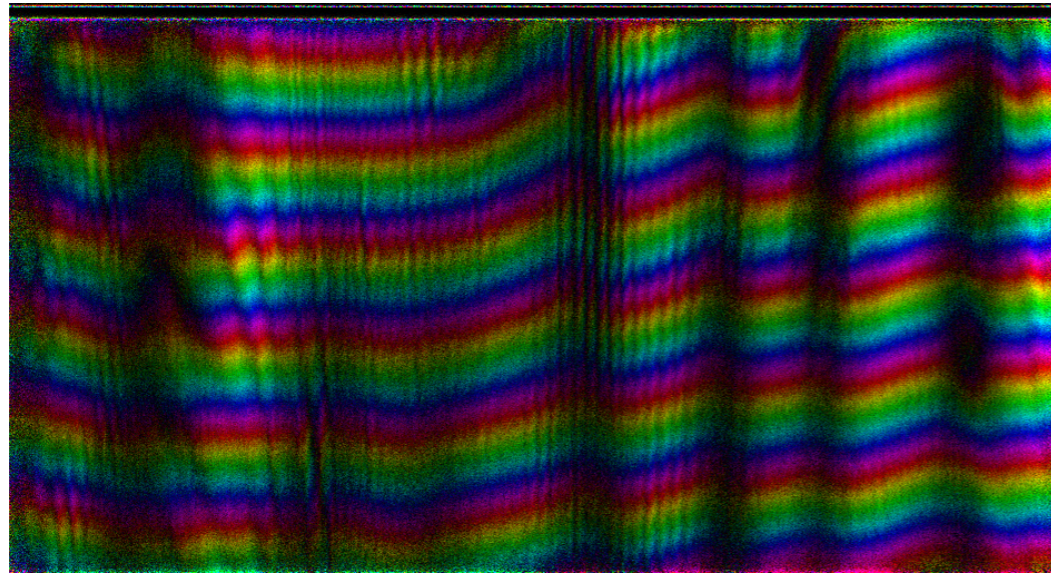
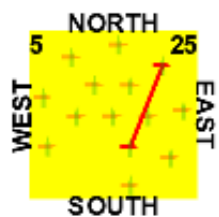
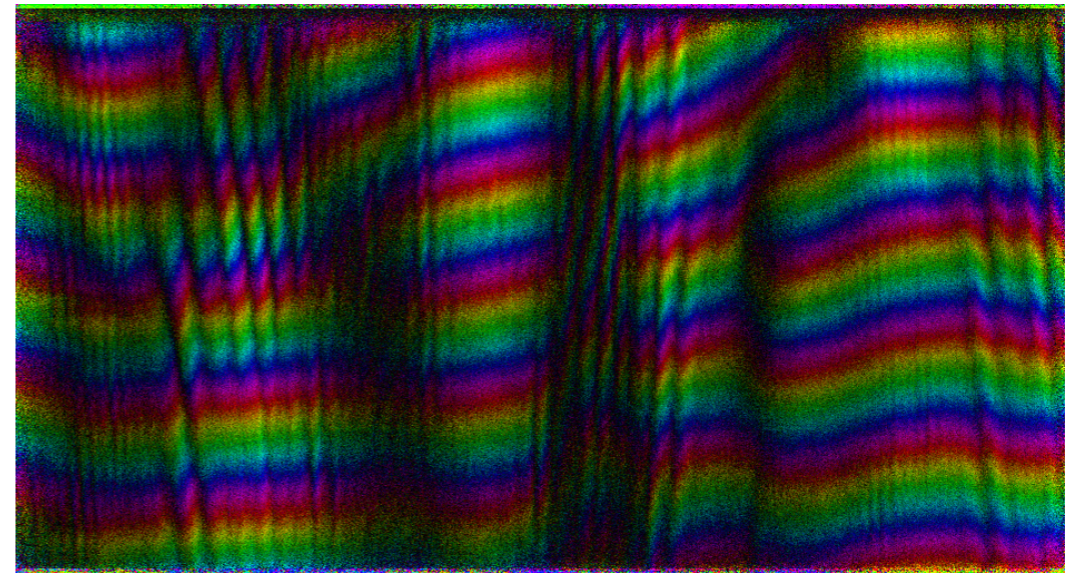
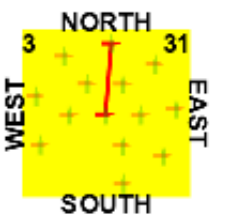
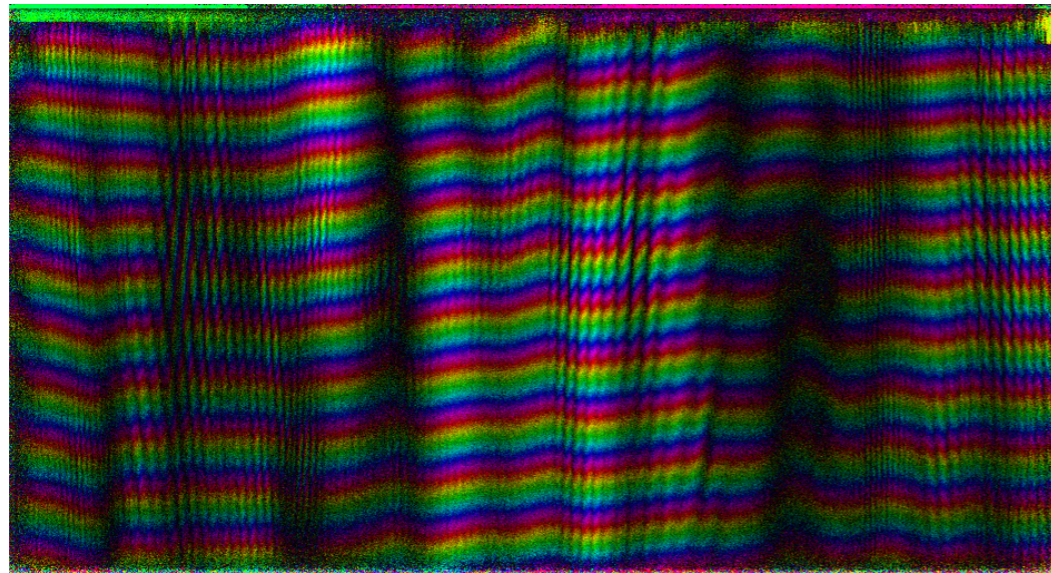
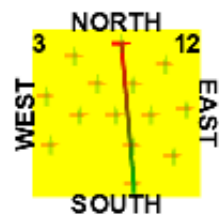
rapid frequency fringe rate
N-S baseline: large ν -dependent phase difference

variable temporal fringe rate
caused by Earth rotation - sources at different declinations



HIM: Tianlai Visibility: Night Median Averaging

*ribbon
candy*



have good measure of visibilities from foreground sources

Hydrogen Intensity Mapping: Power Law Decomposition

Numerical Tests on Sinusoids+

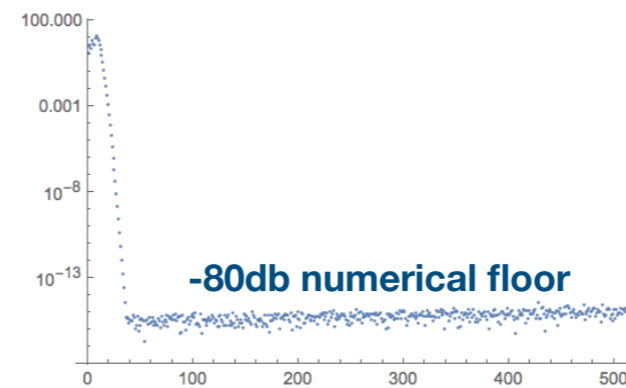
One can expand a visibility covering a given band into Legendre polynomials (or any other polynomial expansion)

$$V[\nu] = \sum_{n=0}^N a_n P_n \left[\frac{2(\nu - \nu_{\text{mid}})}{\nu_{\text{max}} - \nu_{\text{min}}} \right]$$

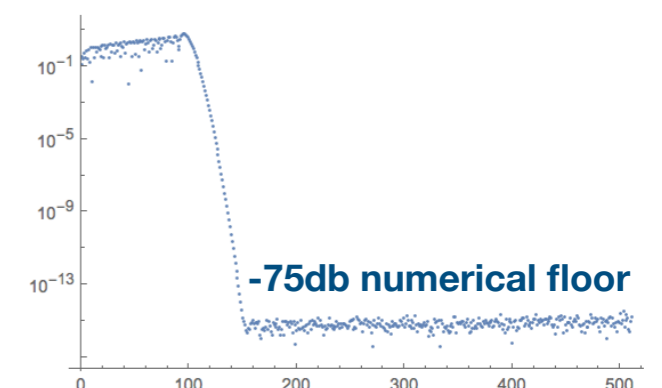
the larger n is the less smooth the frequency dependence. A *carefully designed discrete analog* of this works better than a discrete Fourier transform. The integer index n is an analog of k_{\parallel} . For small bandwidth

$$k_{\parallel} \approx \frac{2\pi}{\Delta R_{\text{co}}} (n + 1)$$

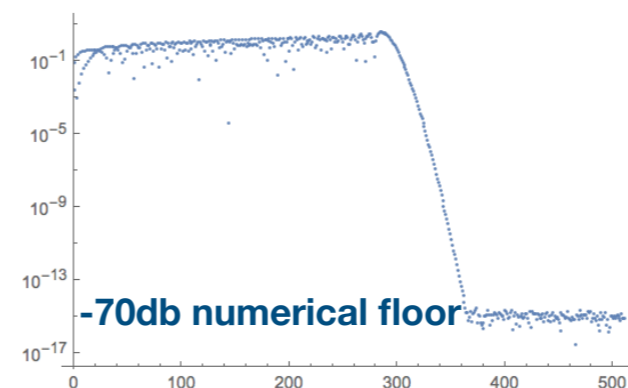
psLegendreDecomposePowerTest [Exp[10 i #] &, 512]



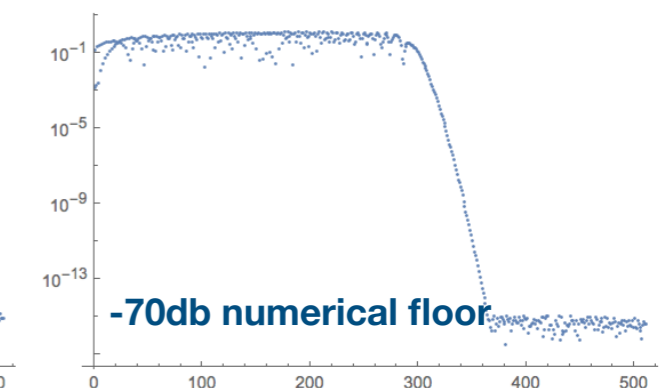
psLegendreDecomposePowerTest [Exp[100 i #] &, 512]



psLegendreDecomposePowerTest [Exp[300 i #] &, 512]



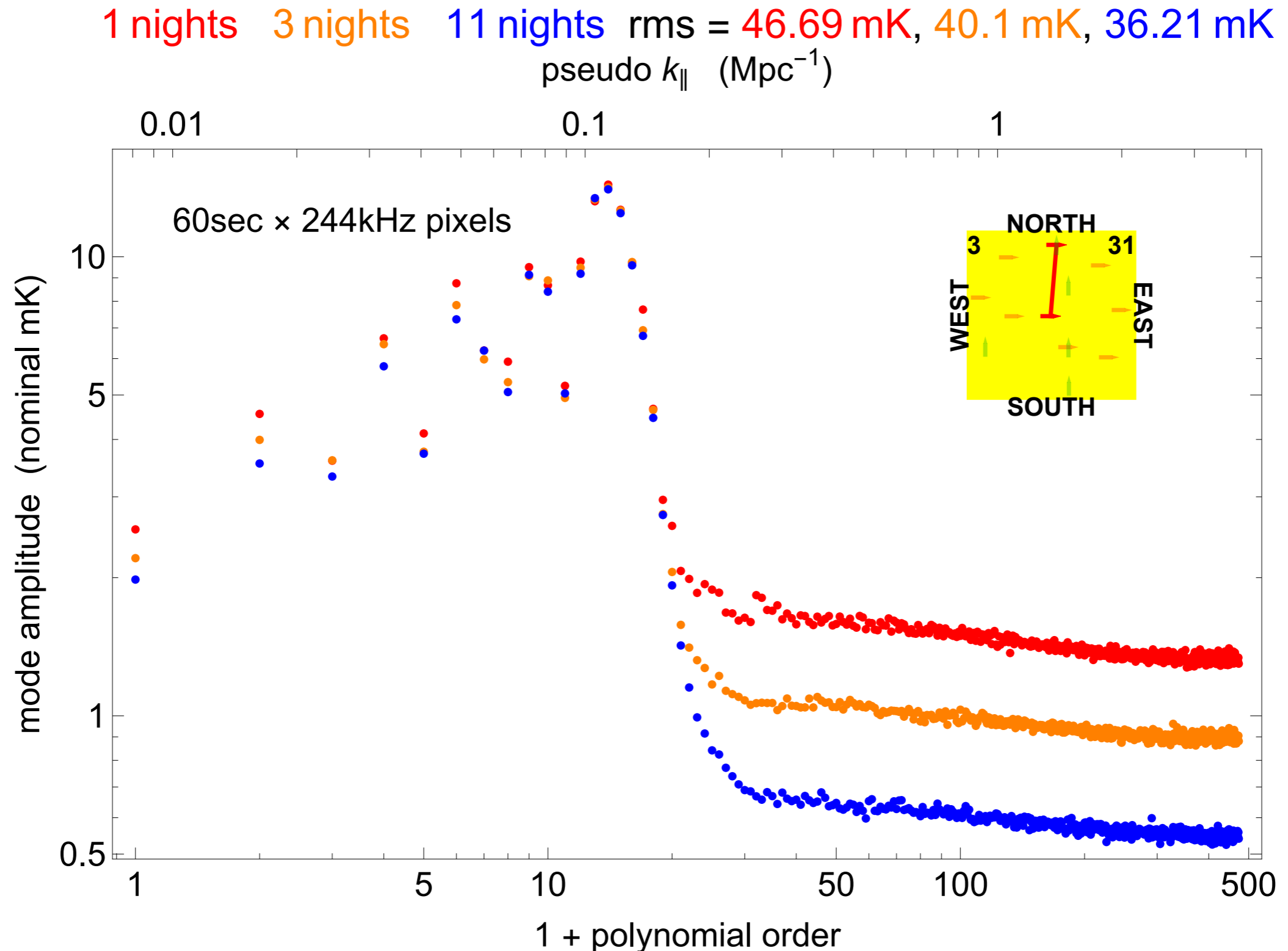
psLegendreDecomposePowerTest [# Exp[300 i #] &, 512]



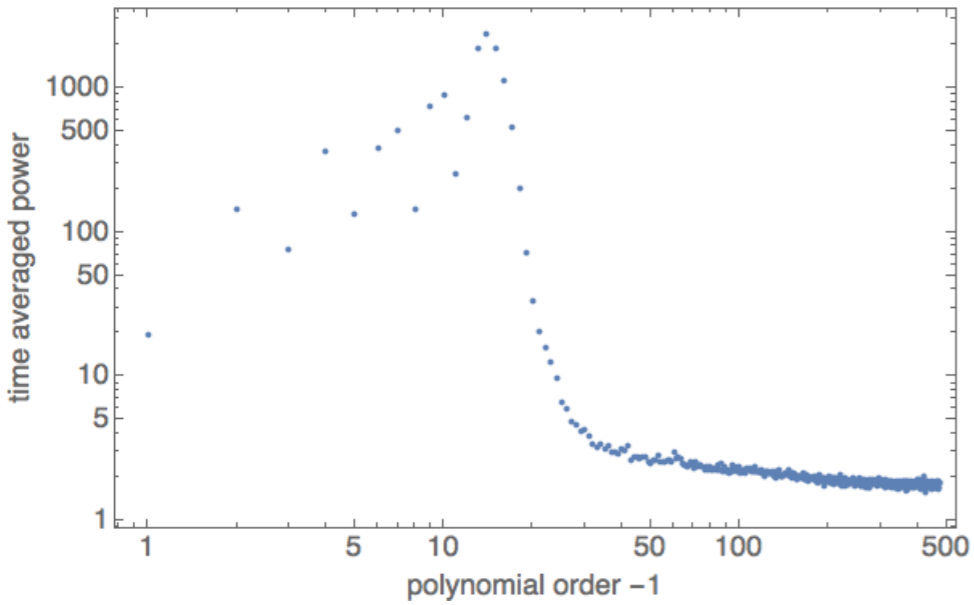
much spill-back, rapid fall-off, little spill-forward

HIM: Tianlai Visibility: Foreground Separation

Are Good Tianlai Visibilities Smooth Spectrum?

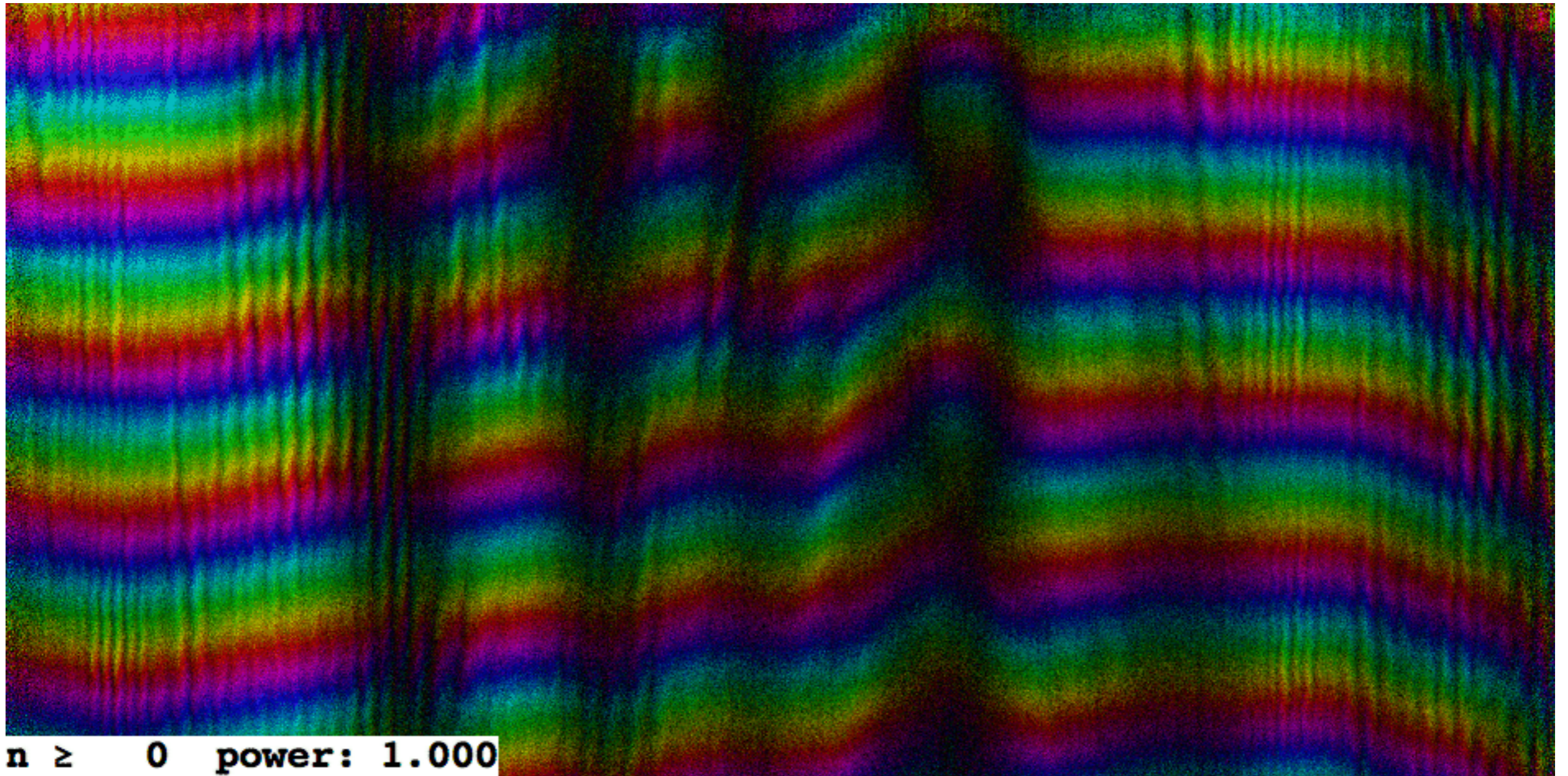
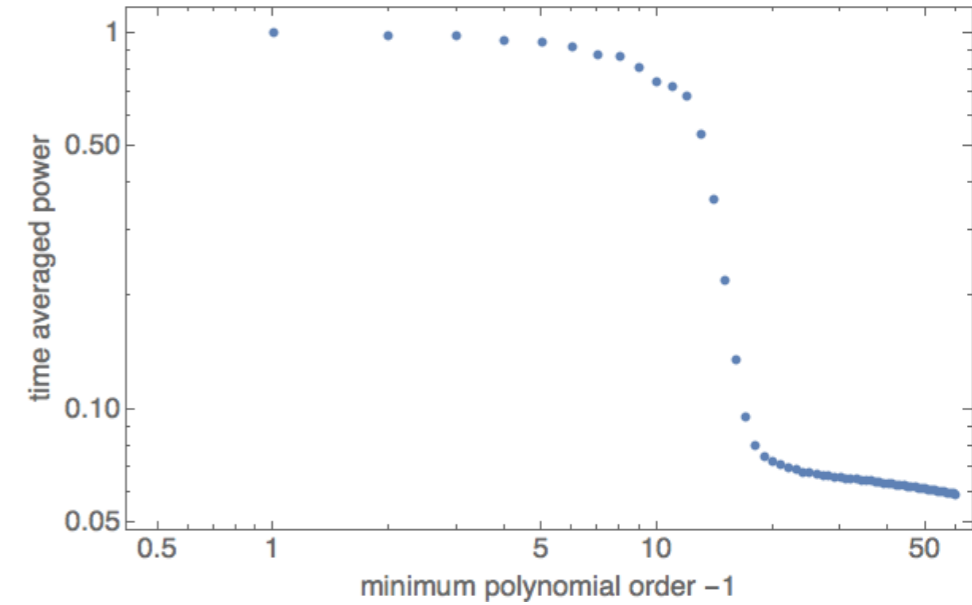


HIM: Tianlai Visibility: Foreground Subtraction



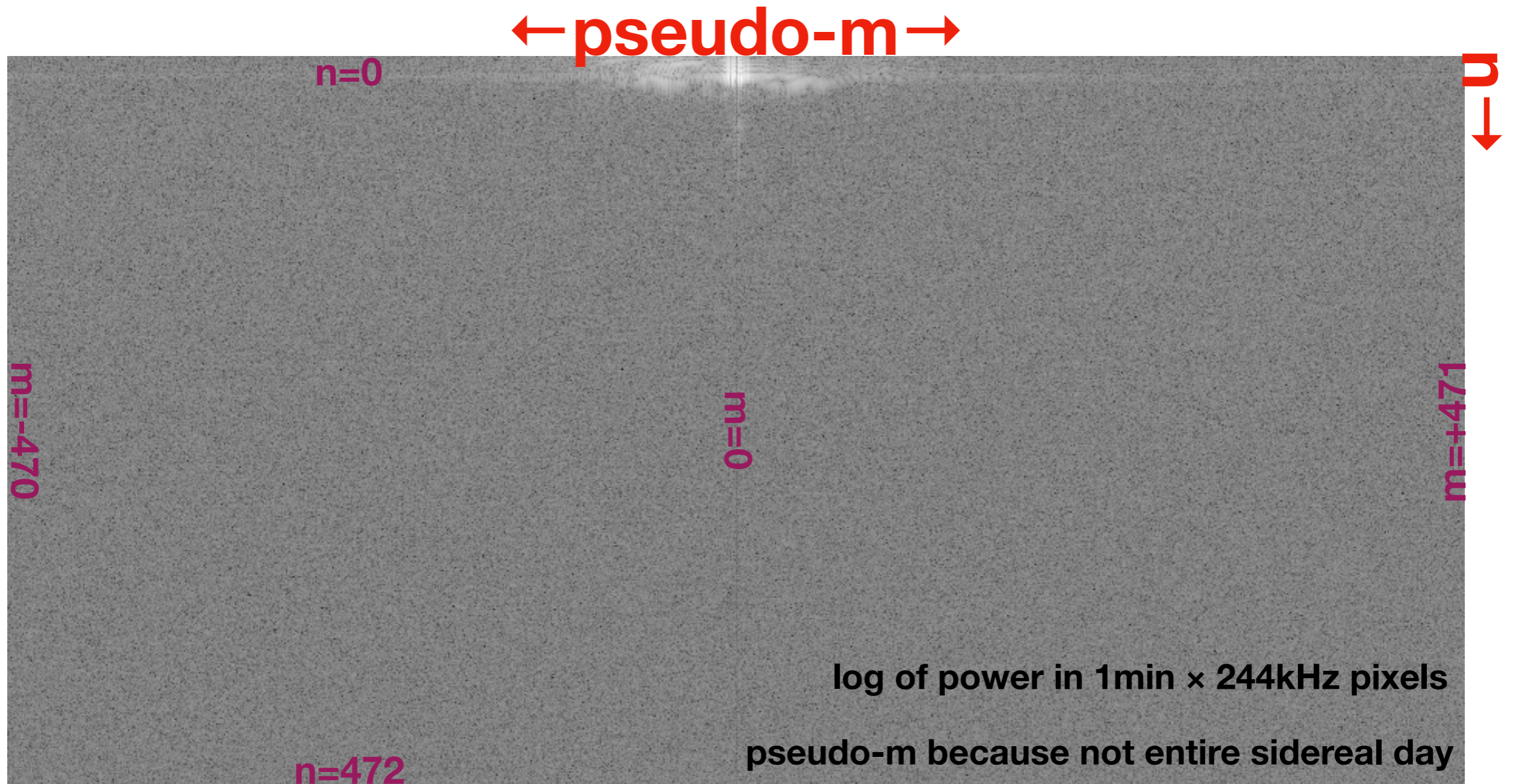
10 night median averaged visibility discrete polynomial subtraction.

residuals $n > 60!$



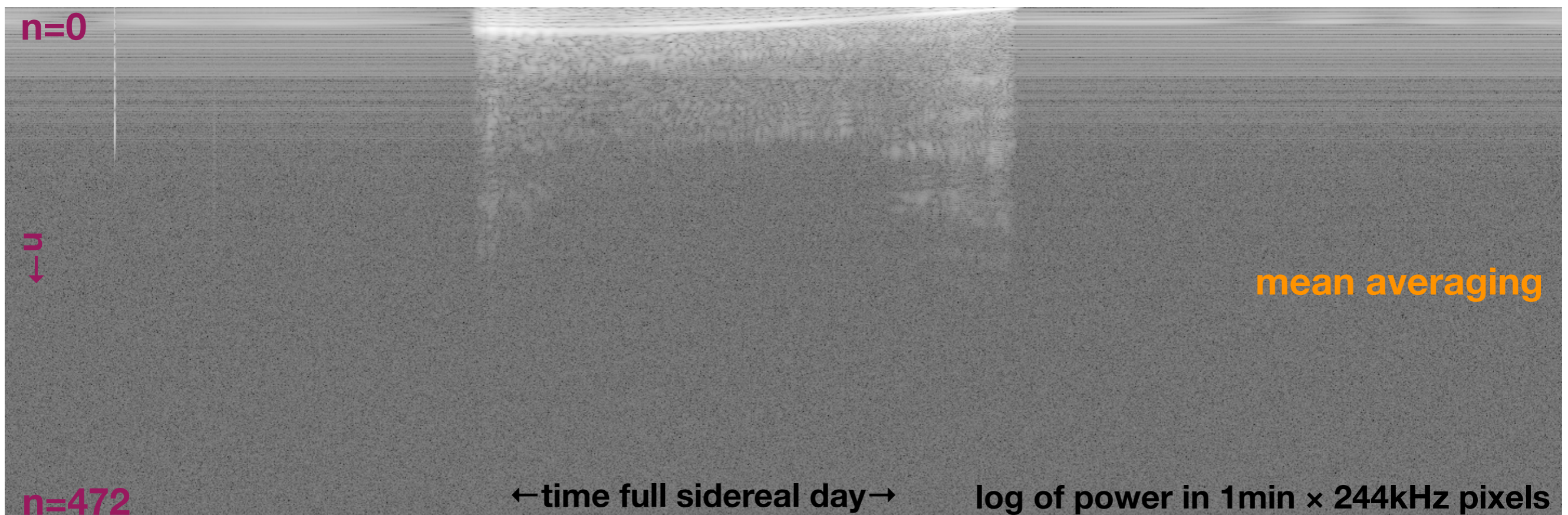
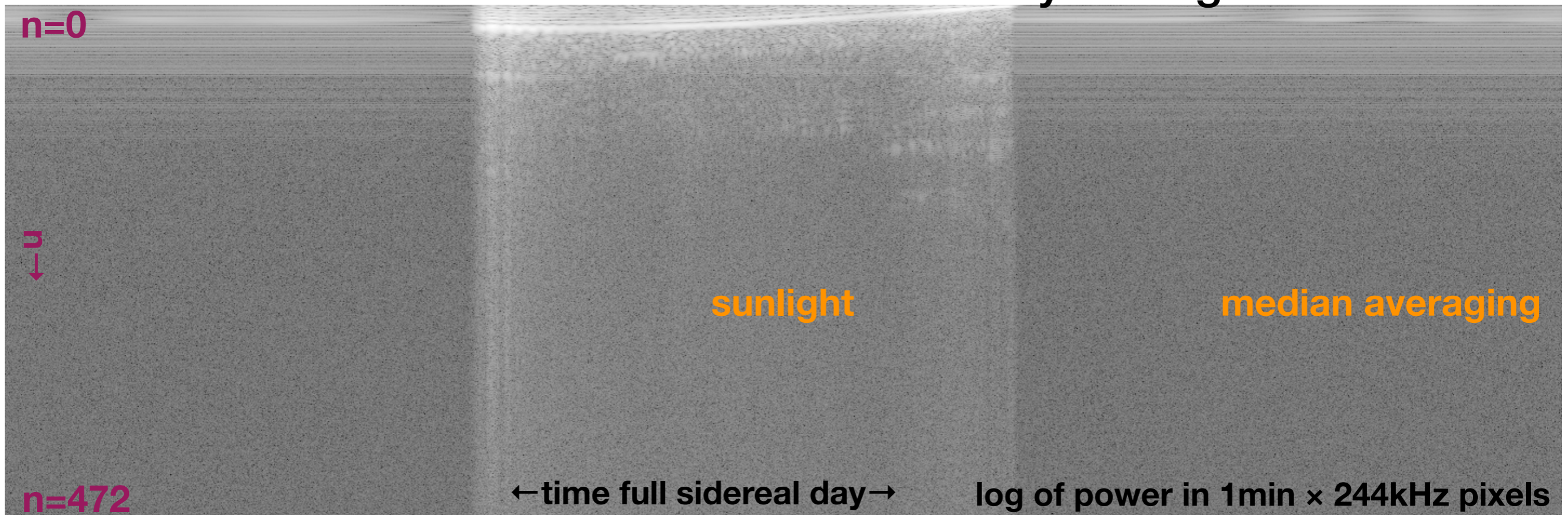
HIM: Tianlai Visibility: Foreground Separation

Power Distribution 03x31

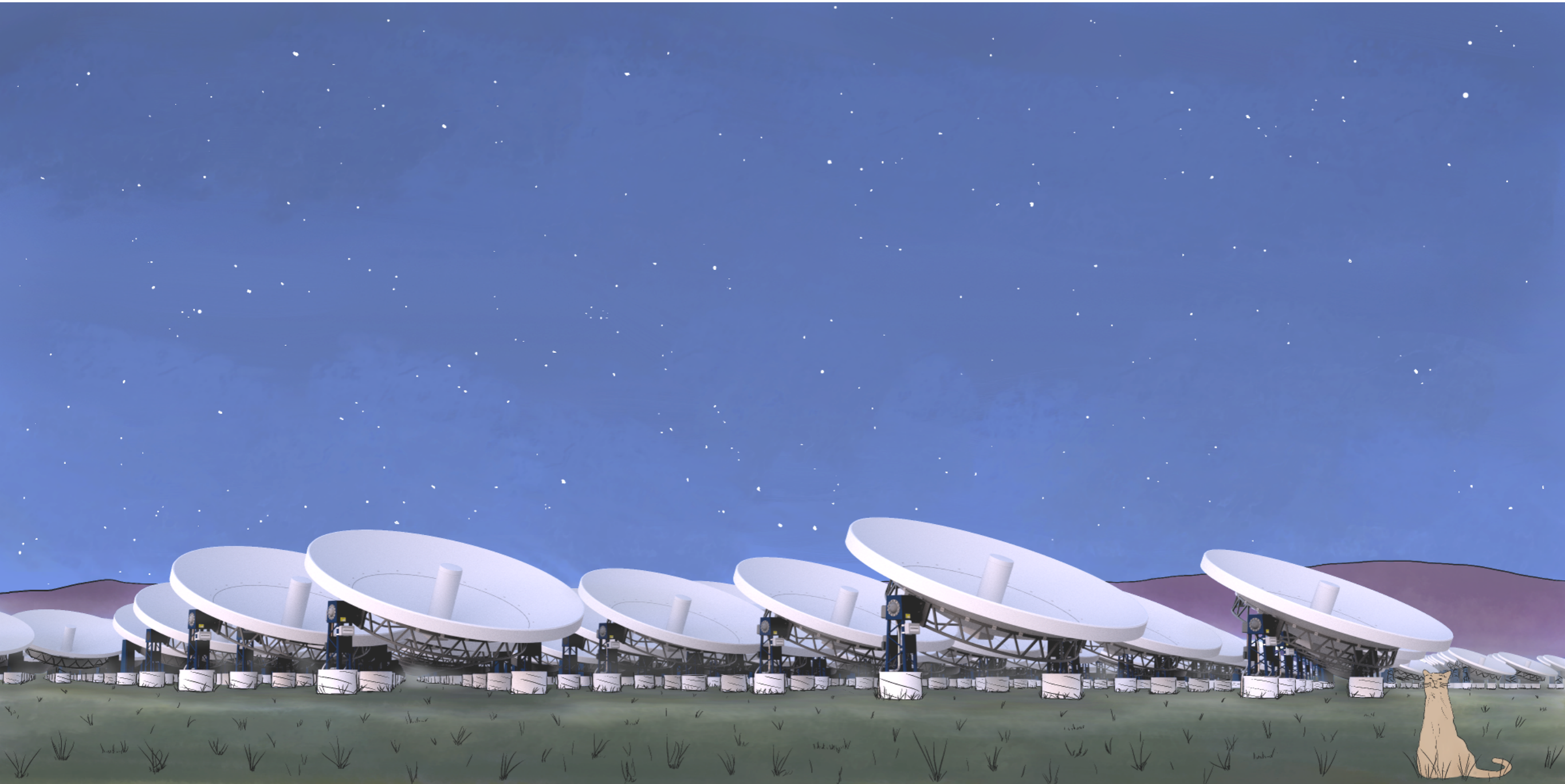


HIM: Tianlai Visibility: Sun Contamination

Power Distribution 09x22 10 day average



PUMA



**Packed Ultrawideband Mapping Array
formerly known as “Stage II”**

PUMA

$2 < z < 6$ (200-500 MHz)

bandwidth smaller than CHIME/HIRAX

256 x 256 array 6m dishes

64 x HIRAX

dual polarization feeds

close packed

$\sim 1.5 \text{ km}^2$

(very different design than SKA)

highly redundant baseline

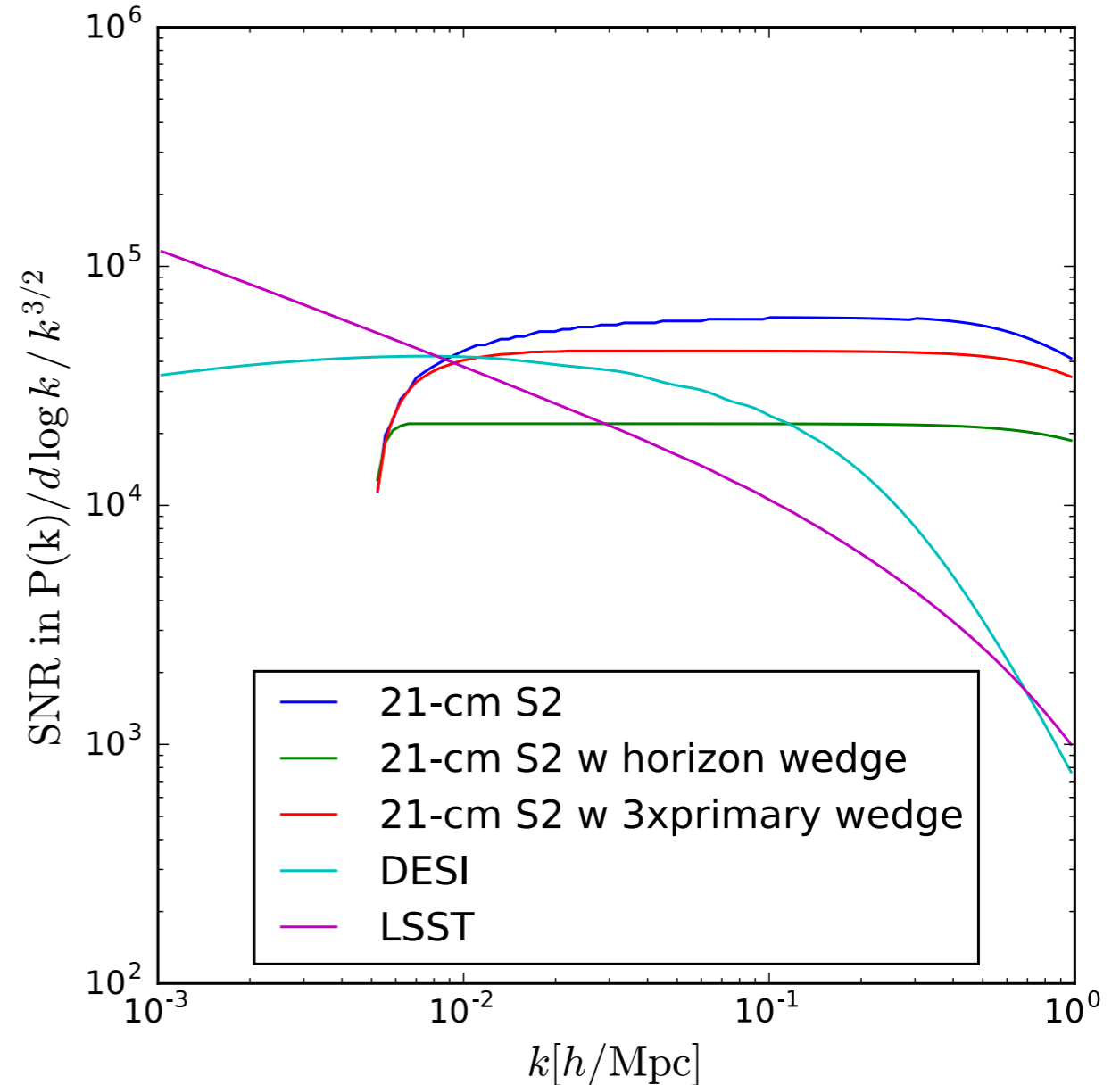
correlator

FFT ($n \log n$) or direct summation ($n^{3/2}$)

learn from HIRAX

radial resolution $\sim 3 \text{ kHz}$

\sim HIRAX



Total S/N in the power spectrum

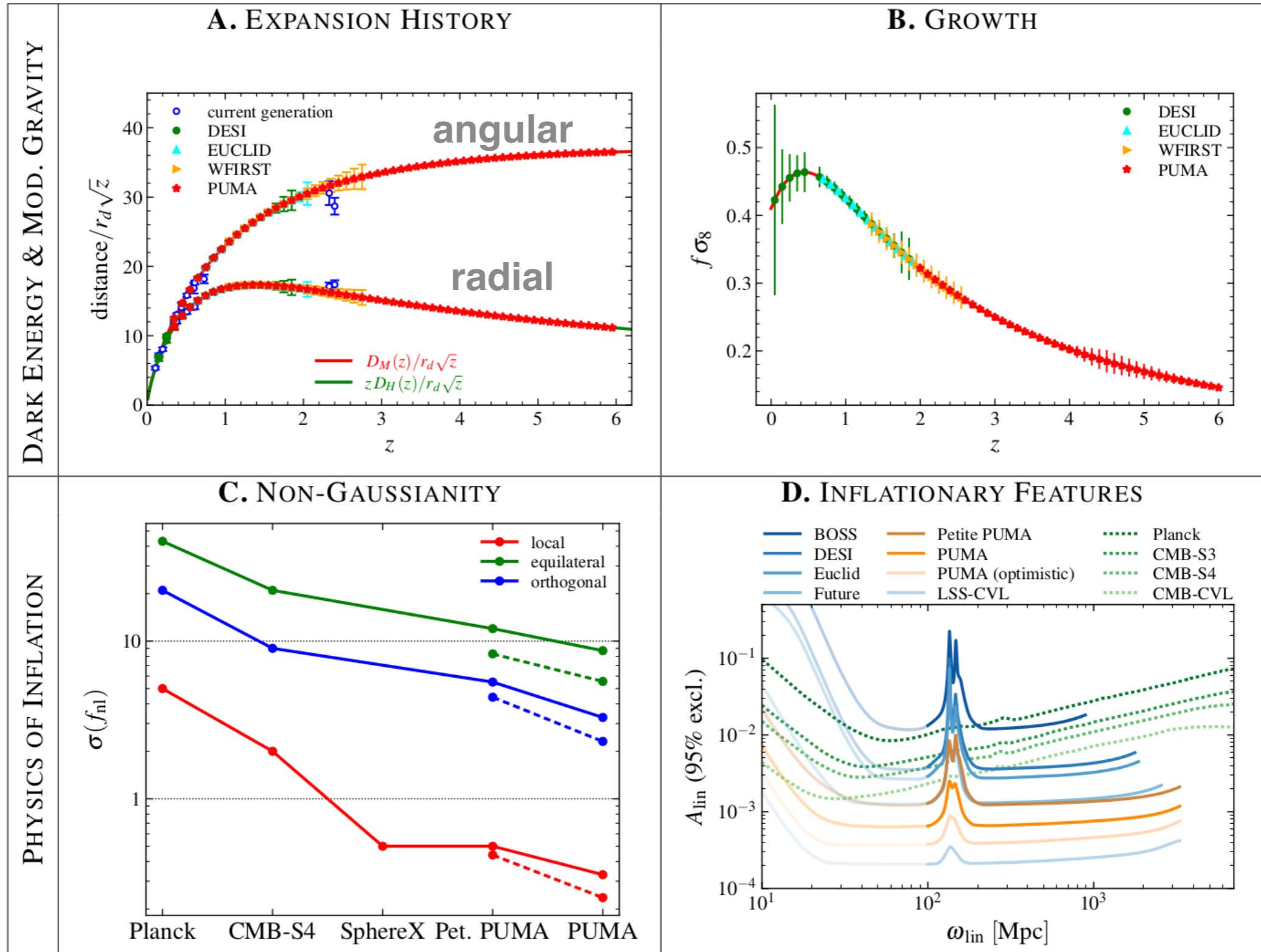
DESI limited by the number density of sources

LSST by the precision of photometric redshifts.

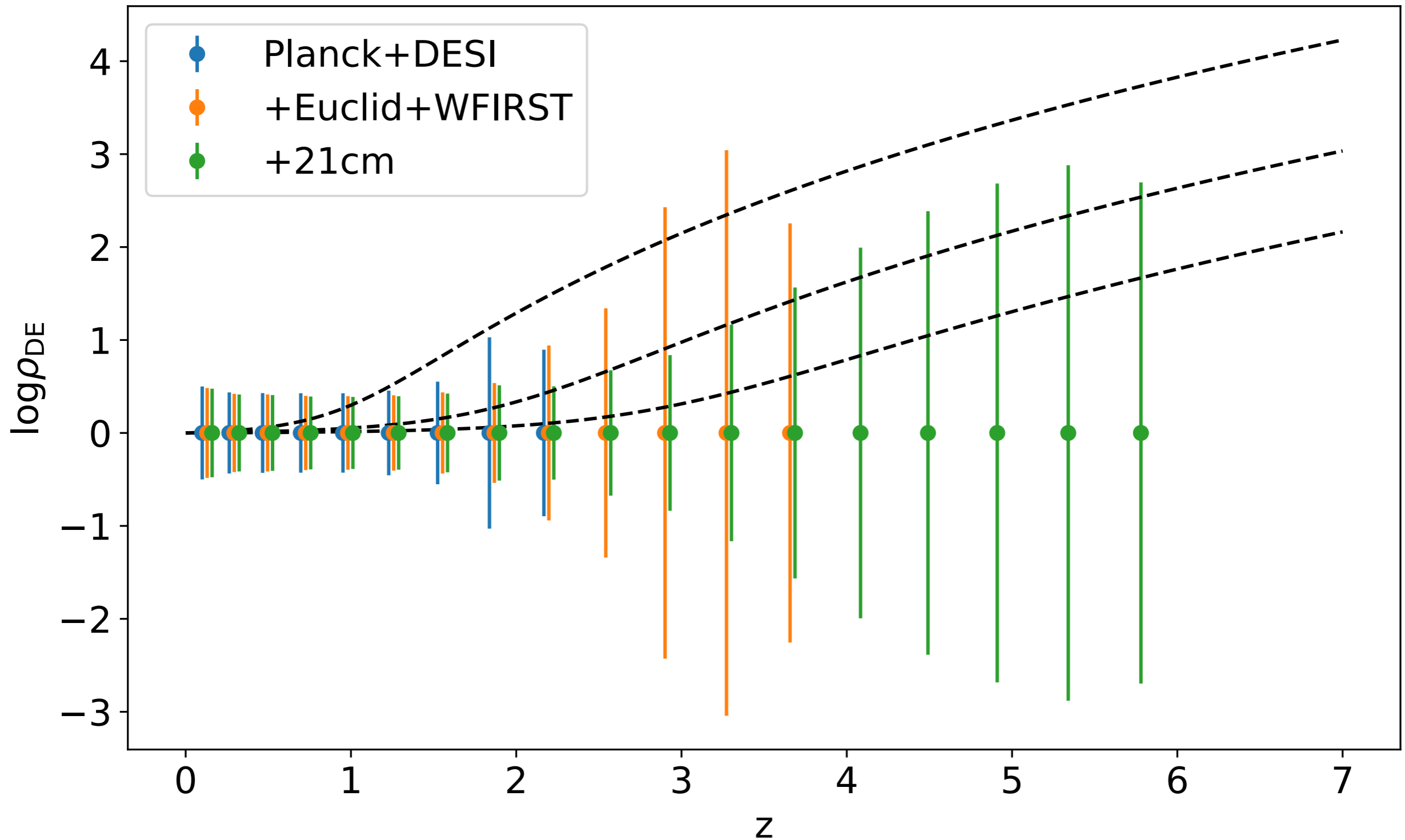
21cm-S2 loses sensitivity at low- k due to foreground contamination but **has most volume and most accurate sampling.**

DOE21 “Cosmic Visions Dark Energy: 21-cm Roadmap” Slosar & co.

Projected Cosmological Constraints



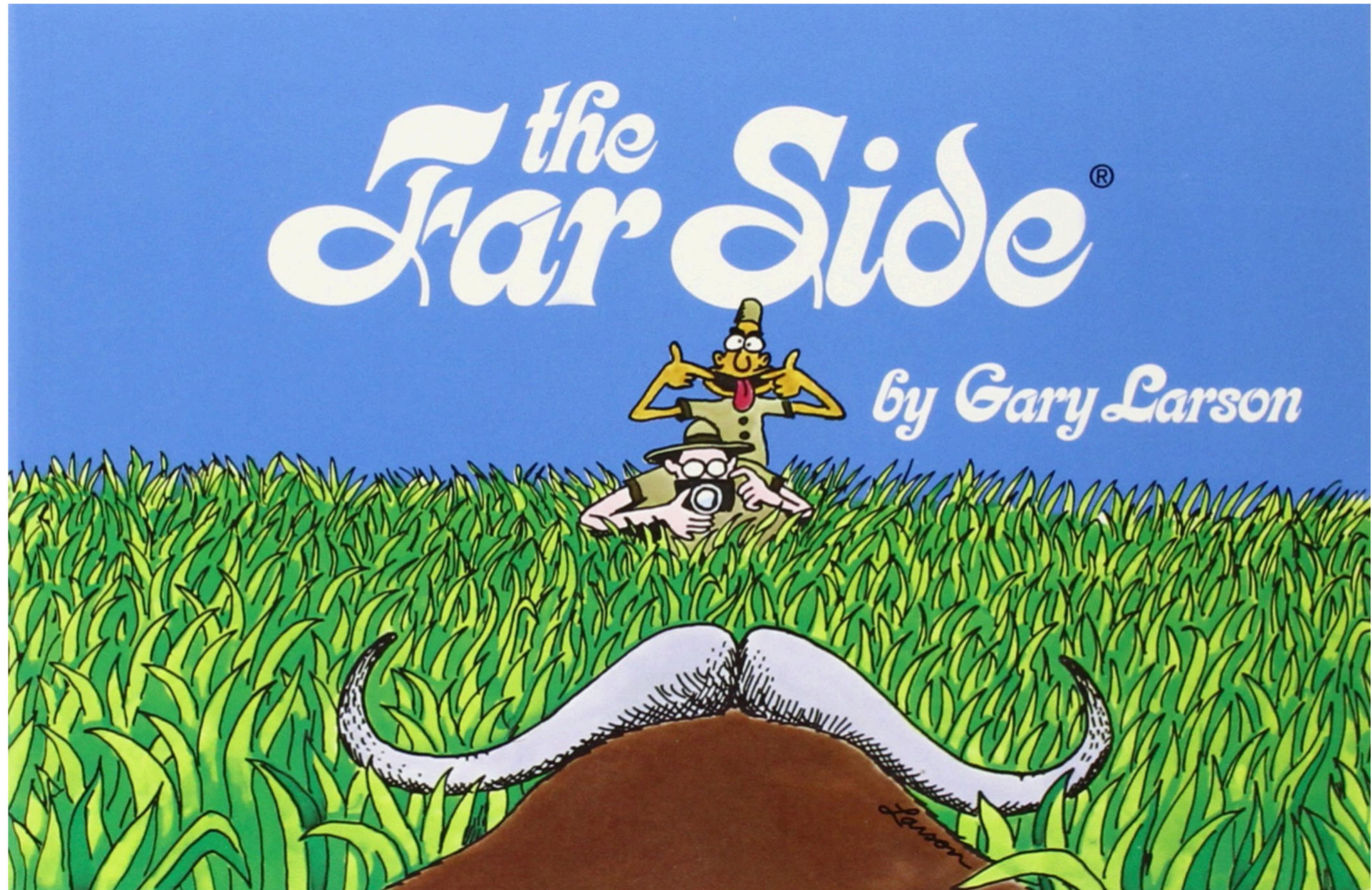
Dark Energy Density



DOE21: 21cm Roadmap

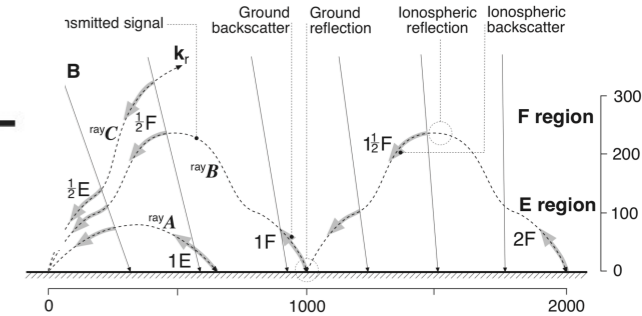
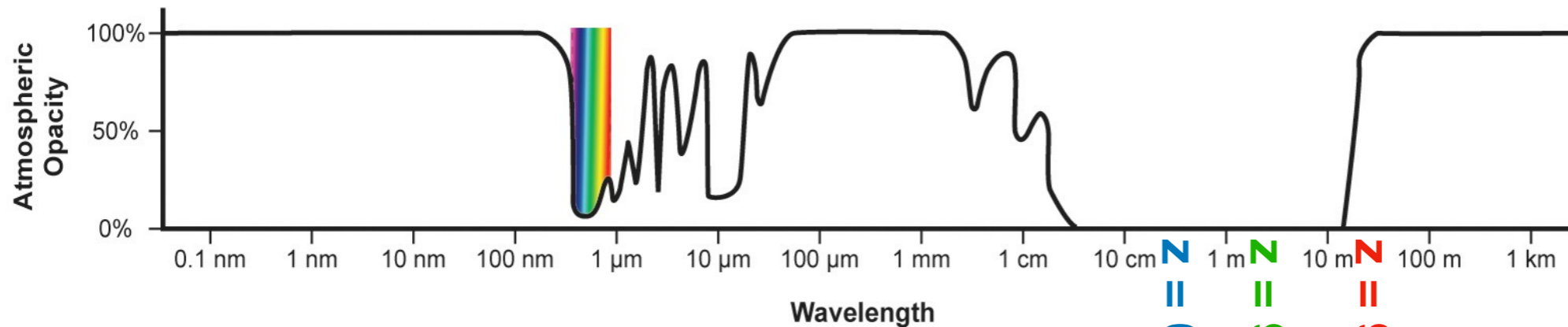
	generation 1 post reionization $0 < z < 2$	generation 2 post reionization $2 < z < 6$	generation 3 dark ages $30 < z < 150$	context
2018-2020	data taking construction 1st results	community building		LSST/DESI ongoing stage 1 first results decadal survey submission
2020-2025	stage 1 results continuation?	R&D based on stage 1 simulations firm up science case		LSST/DESI/Stage 1 P5 submission Decadal Survey results P5 results SKA online
2025-2030		optimize design collaboration forming CD0/CD1		LSST/DESI ending SKA results
2030-2035		construction start of data taking	feasibility study preliminary design	?
2035-2040		data taking analysis	construction start of data taking	?
2040-2045			data taking analysis	?

Space Based 21 cm Cosmology



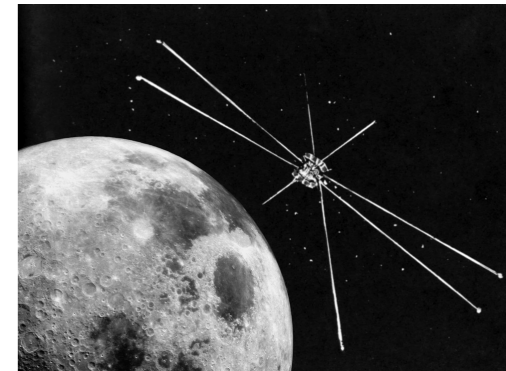
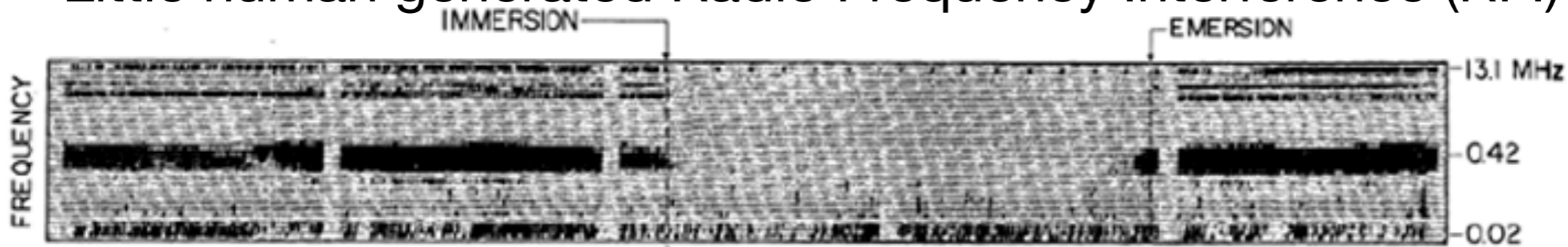
Why the Far Side? (of the Moon)

- No ionosphere (atmosphere or magnetic fields)



- $\nu \approx 30\text{MHz}$ EM waves don't propagate in straight lines

- Little human generated Radio Frequency Interference (RFI)



1973: Radio Astronomy Explorer B / Explorer 49

2018: Longjiang satellites (interferometer)

2018: Chang'e 4 lander (2018)

Discovering the Sky at the Longest Wavelength (DSL)

Dark Ages Radio Explorer (DARE)

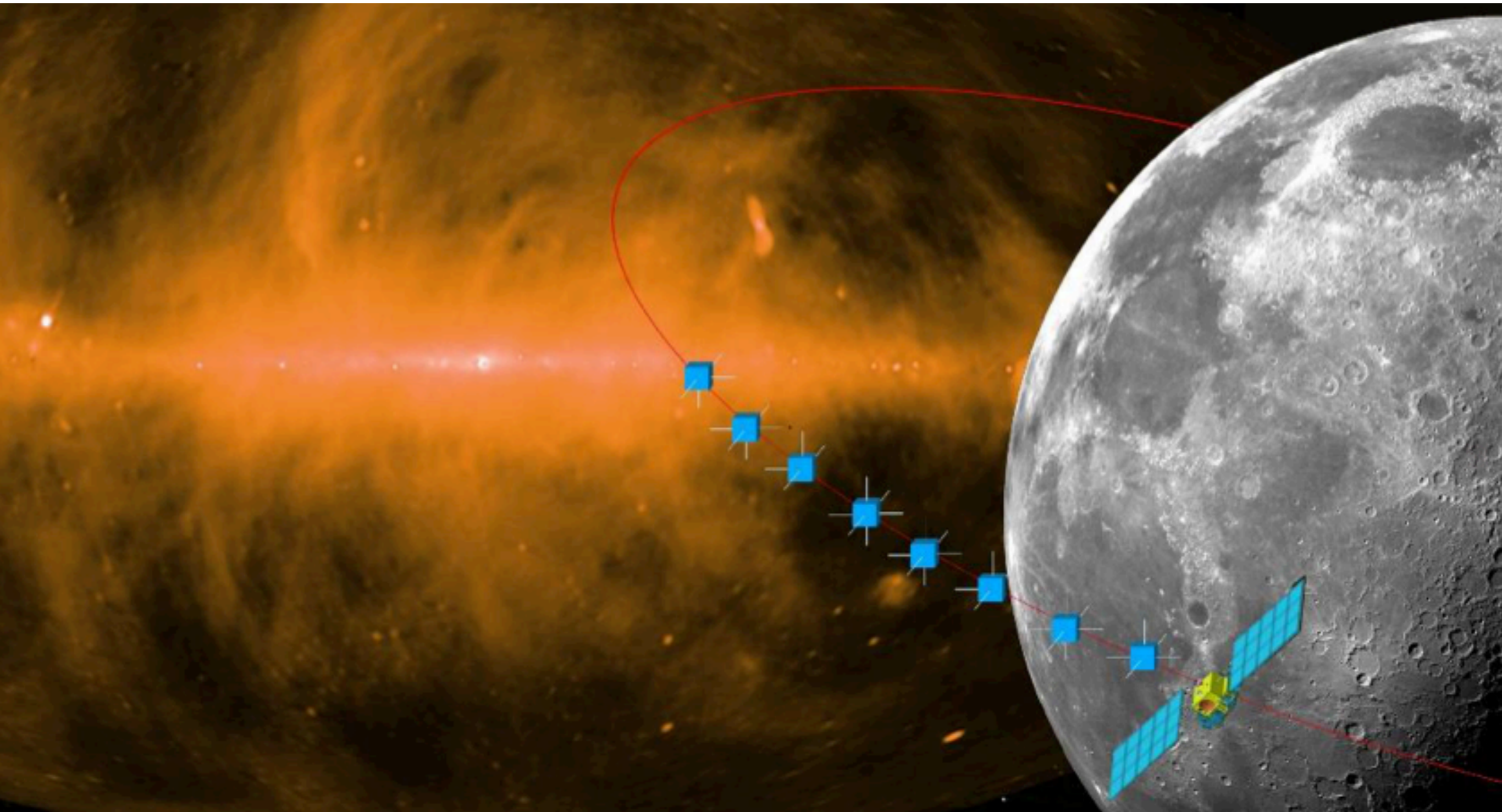
Dark Ages Polarimeter Pathfinder (DAPPER)

Probing Reionization of the Universe using Signal from Hydrogen (PRATUSH)

Jester Falcke (2009)

Chen Burns Koopmans et al. (2019)

Lunar Orbit DSL

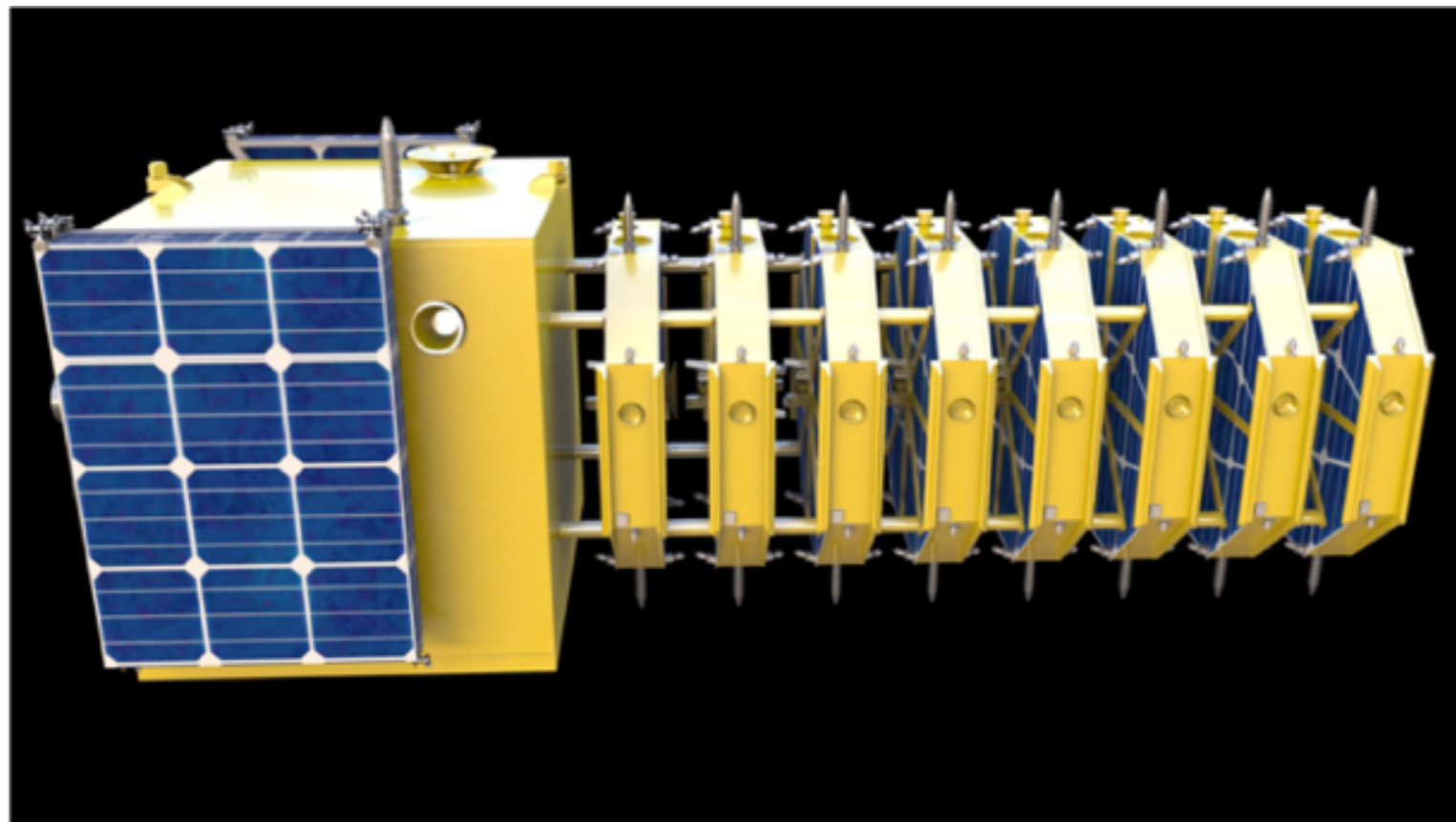


Discovering the Sky at the Longest wavelengths

PI: Xuelei Chen

DSL Technology and Challenges

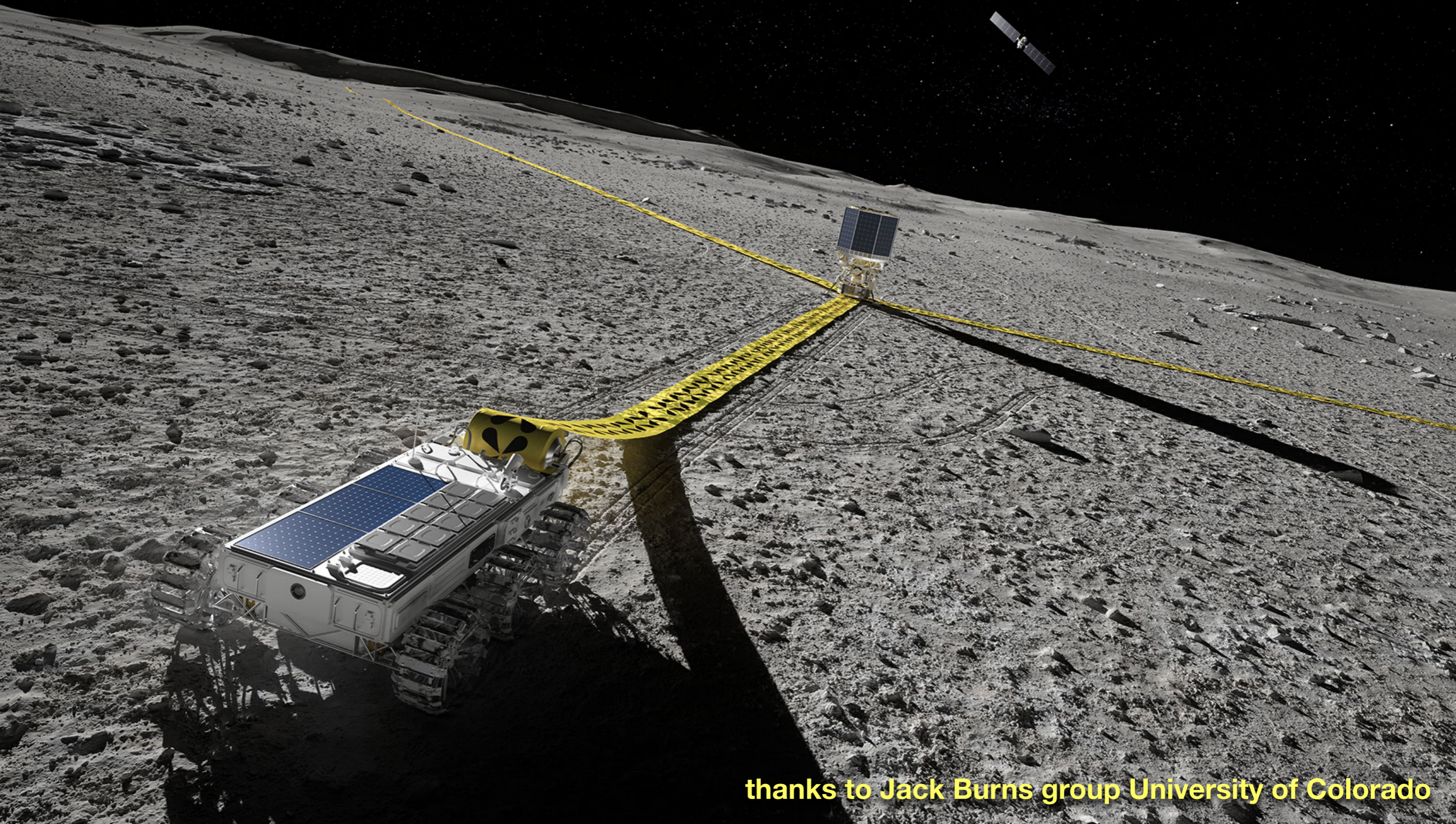
- ① **Satellite Formation Fly in lunar orbit with large variation on scales**
- ② **Precision Measurement of Relative Positions and synchronization**
- ③ **High precision calibration of phase and amplitude**
- ④ **Imaging algorithm with large field of view, 3D baseline distribution, and time-dependent blockage**
- ⑤ **Electromagnetic interference (EMI) suppression and removal**



DSL Parameters

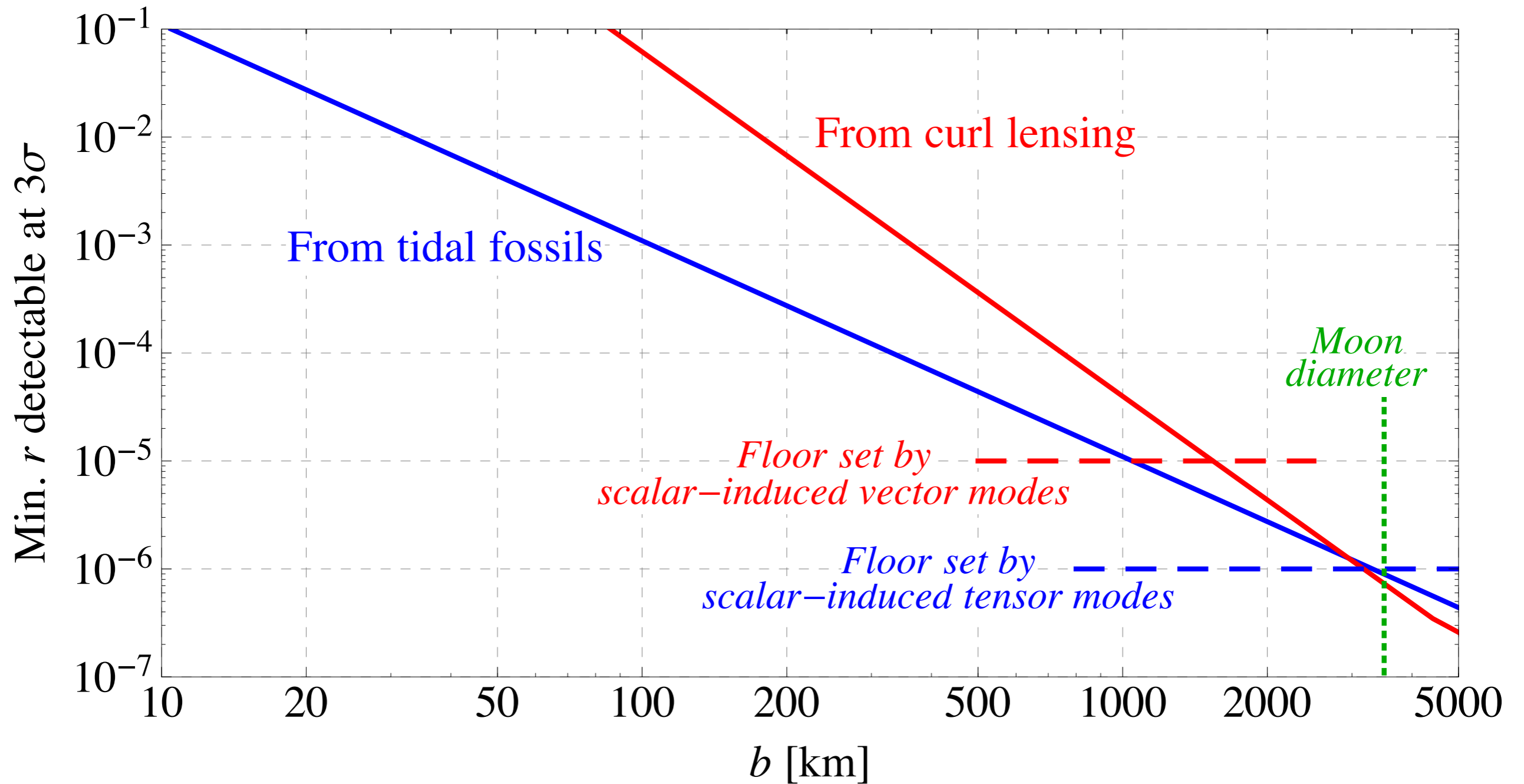
System	Parameter
Number of Satellites	1 mother + 5~8 daughters
Orbit	300km lunar circular orbit, about 30° inclination
Baselines	0.1~100km
Sensitivity	<0.1K@30MHz (1 year integration, 1MHz BW)
angular resolution	<0.2 degree@1MHz, 0.012 degree@30MHz
Individual	
Polarization	3 linear polarization
Frequency	1MHz~30MHz (interferometry incl. spectrum) 30MHz~120MHz (global spectrum)
Baseline precision in each direction (1σ)	< 1m
Synchronization	<3.3ns
Inter-satellite data communication	>20Mbps each daughter satellite

the Dark Side

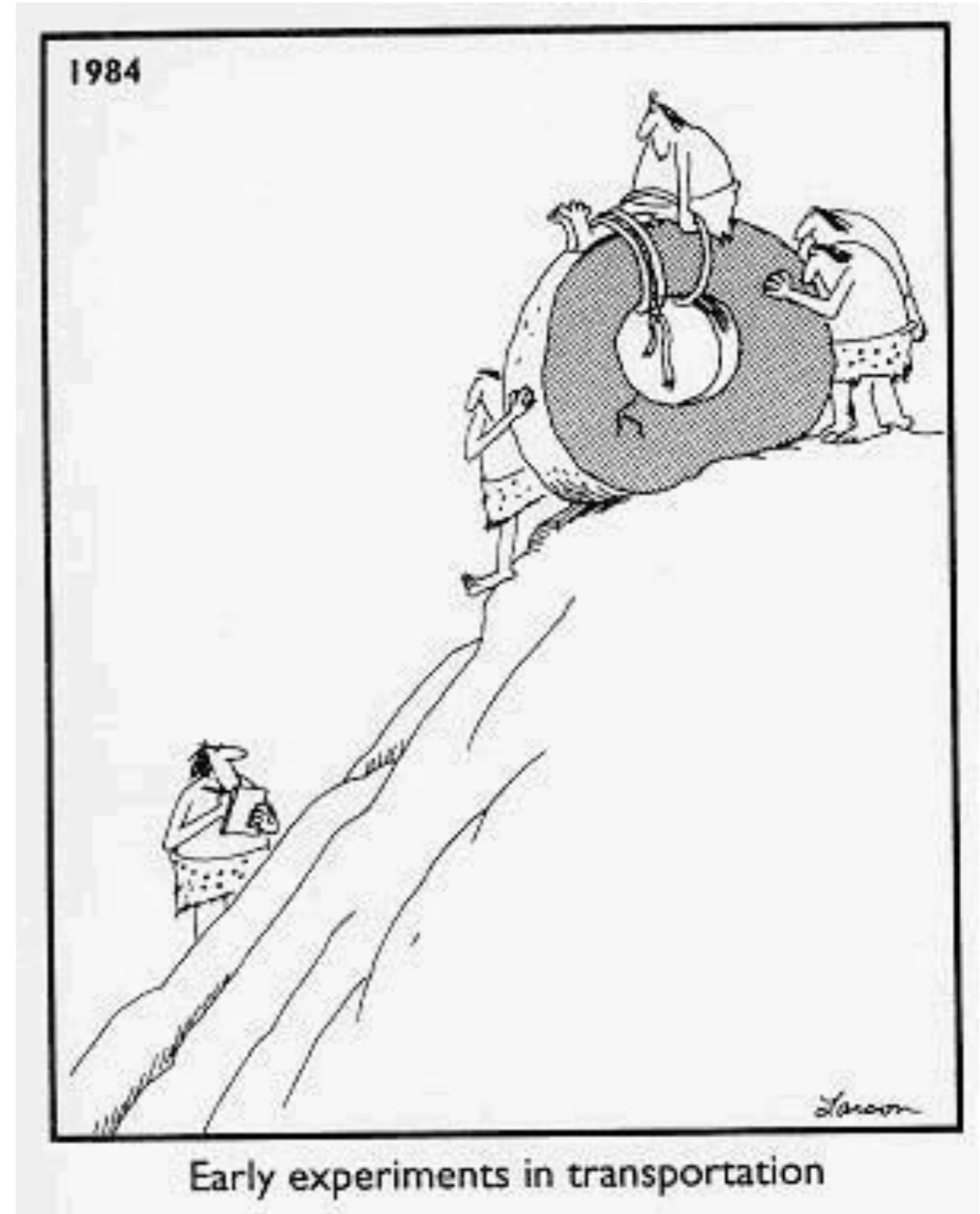
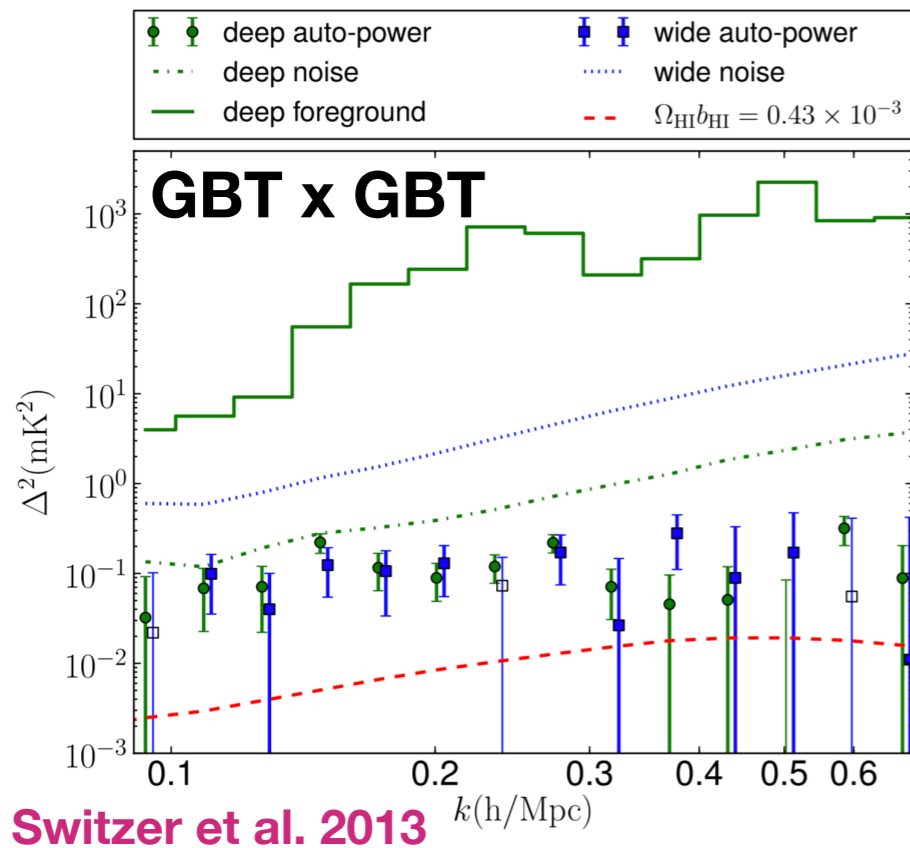
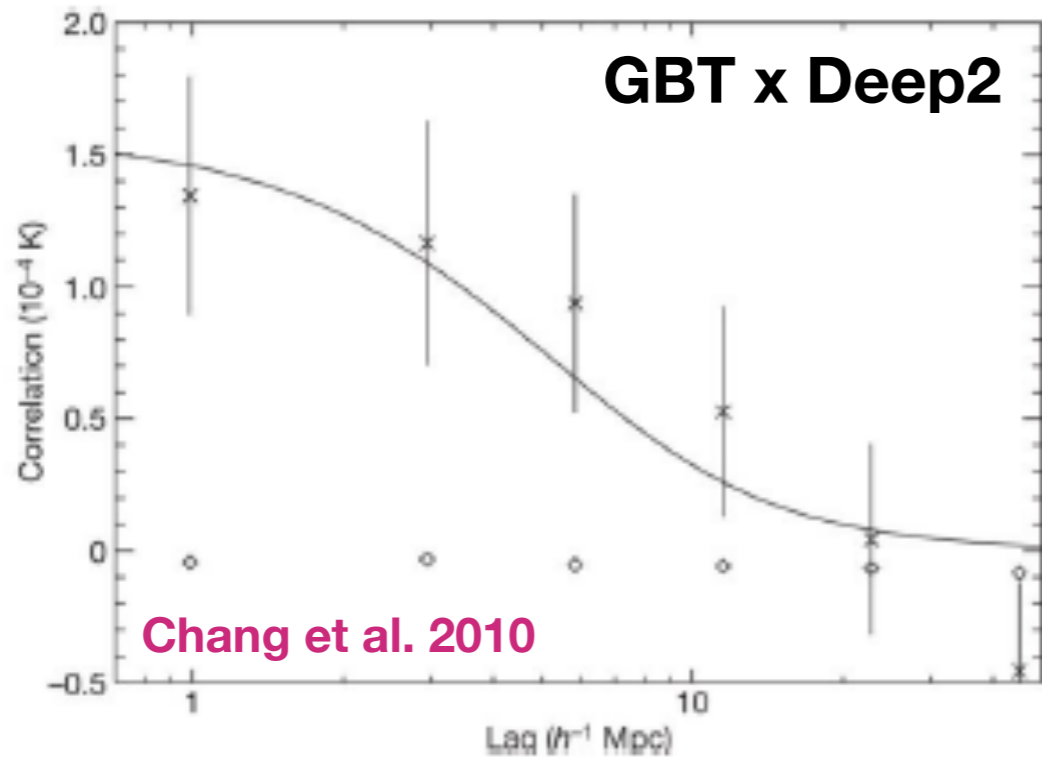


thanks to Jack Burns group University of Colorado

Primordial Gravity Waves from The Dark Side



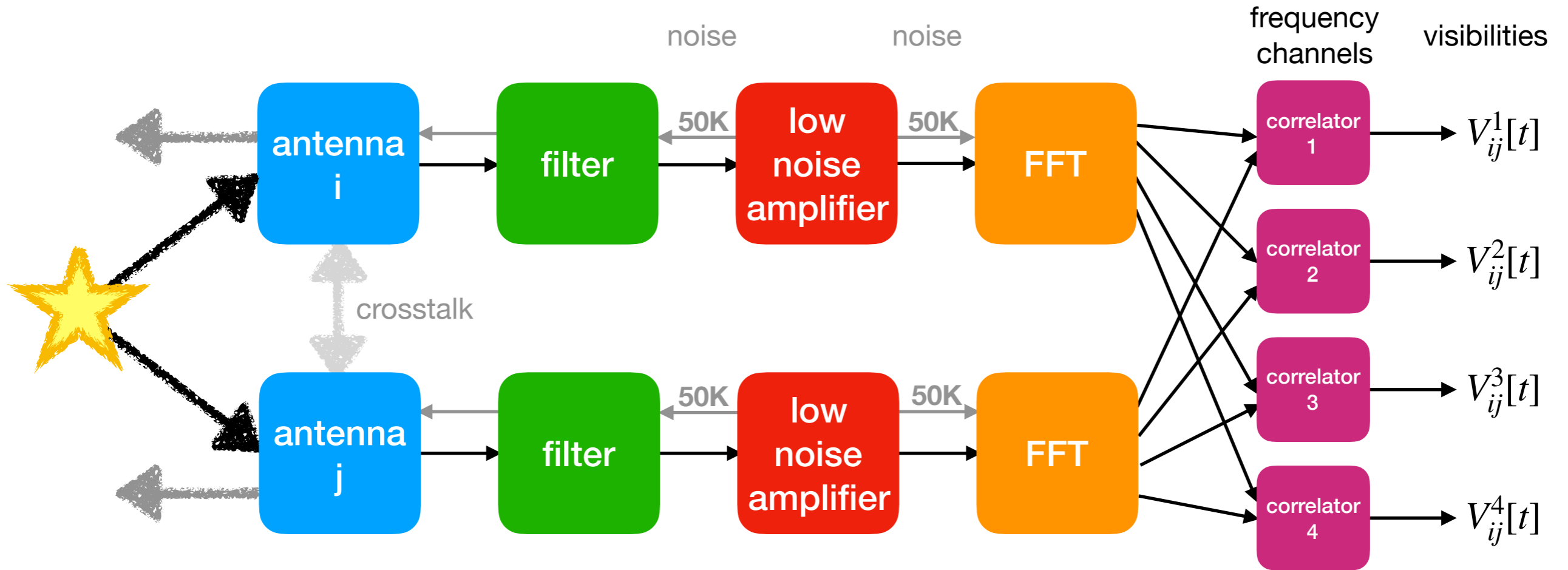
Where's the HI?



see also
 Masui et al. 2013
 Anderson et al 2017

**expect
new 21cm
detections
soon
(hopefully)**

Hydrogen Intensity Mapping: Visibilities



- $n(n+1)/2$ visibilities $n = \#$ of antennae $\sim 10^2-10^3$
- number of frequency channels $\sim 10^3$
- visibilities computed every $\delta t = 1/\delta v \sim \mu\text{sec}$
- visibilities averages over $\Delta t \sim \text{sec}$
- time ordered data produced $\sim 10^0-10^2$ PByte/year
- final 3D HI maps < 1 TByte

Hydrogen Intensity Mapping: Smooth Spectrum Foregrounds

e.g. optically thin ultra-relativistic synchrotron emission

$$I_\nu[\vec{\theta}] = \frac{3}{4\pi^2} \frac{e^3}{m_e c^2} \int d\ell \int d^2 \hat{\beta} \int_0^\infty d\gamma \frac{d^3 n_e}{d^2 \hat{\beta} d\gamma}[\ell, \hat{\beta}, \gamma] \frac{\nu}{\nu_c} F\left[\frac{\nu}{\nu_c}\right] \frac{\delta[\psi - \delta]}{\text{Cos}[\psi]} \quad \nu_c = \gamma^2 \frac{3eB}{4\pi m_e c}$$

$$F[y] = y \int_{-\infty}^{\infty} dX (1 + X^2)^2 \left(K_{2/3} \left[\frac{1}{2} y (1 + X^2)^{3/2} \right] \right)^2 + \frac{X^2}{1 + X^2} K_{1/3} \left[\frac{1}{2} y (1 + X^2)^{3/2} \right] \right)^2$$

$F[y]$ is an extremely smooth function.

Fourier transform fall off as k^{-4} .

No matter what the electron distribution is I_ν will be a smooth function of ν .

Mono-energetic electrons / fixed B produces most non-smooth spectrum

this is always the example we will use.

In contrast 21cm line emission can be arbitrarily non-smooth

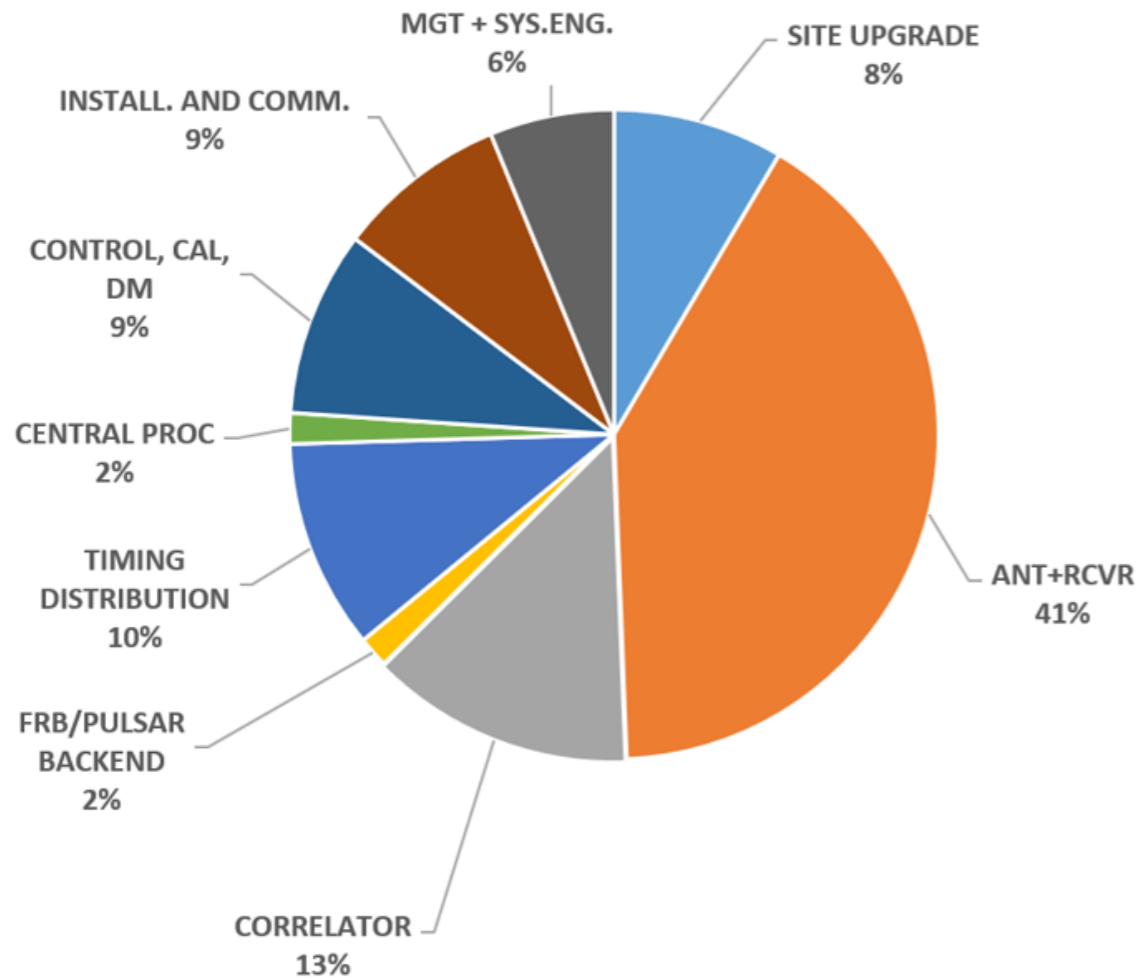
Lo-pass filtering in frequency should reveal 21cm emission

HIM: Transit Telescopes and m-Mode Analysis

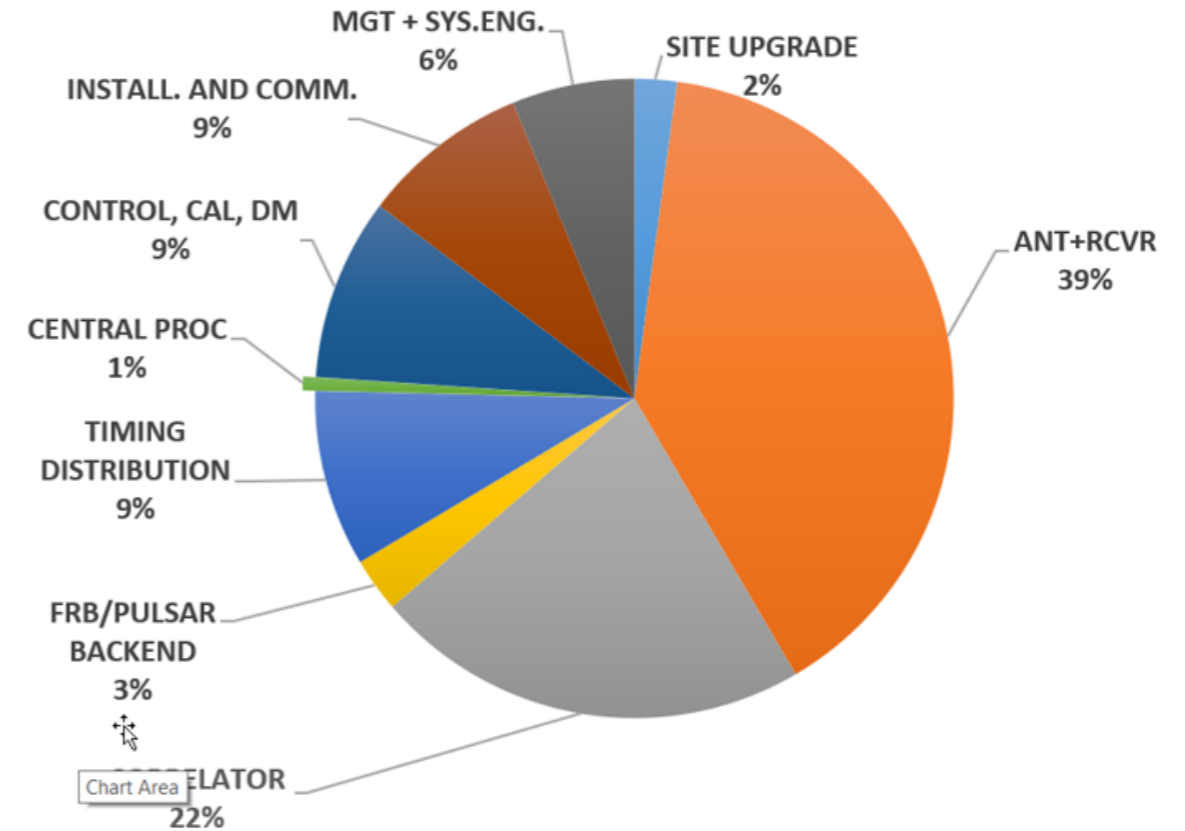
- Due to *extreme* sensitivity to telescope beam pattern it is best not to move the telescope array during observation.
 - Moving optical elements wrt each other changes beam pattern.
 - so one does not “point” the telescope.
 - Earth rotation will scan the sky
 - this is a **transit telescope**
- If a transit telescope is “stable”
 - time weighted visibility $e^{-i m \varphi} V_{ij}[t]$ where $\varphi = 2 \pi t_{\text{sidereal}} / \text{day}_{\text{sidereal}}$ will only be sensitive to $e^{i m \alpha}$ component of illumination where α is right ascension (RA) in radians.
 - **there is no uncertainty in RA dependence of “synthetic” beam pattern!**
 - however one must determine declination (dec) dependence.
 - (non varying) astronomical sources provide a constant (RA,dec) illumination
 - non-astronomical sources in Solar System, RFI (human generated Radio Frequency Interference) do not.
- Sidereal time $t_{\text{sidereal}} = \text{Mod}[t + (\text{longitude}/360^\circ), \text{day}_{\text{sidereal}}]$ angle or time: xxx° or $\text{xx}^{\text{h}}\text{yy}^{\text{m}}\text{zz}^{\text{s}}$

Cost

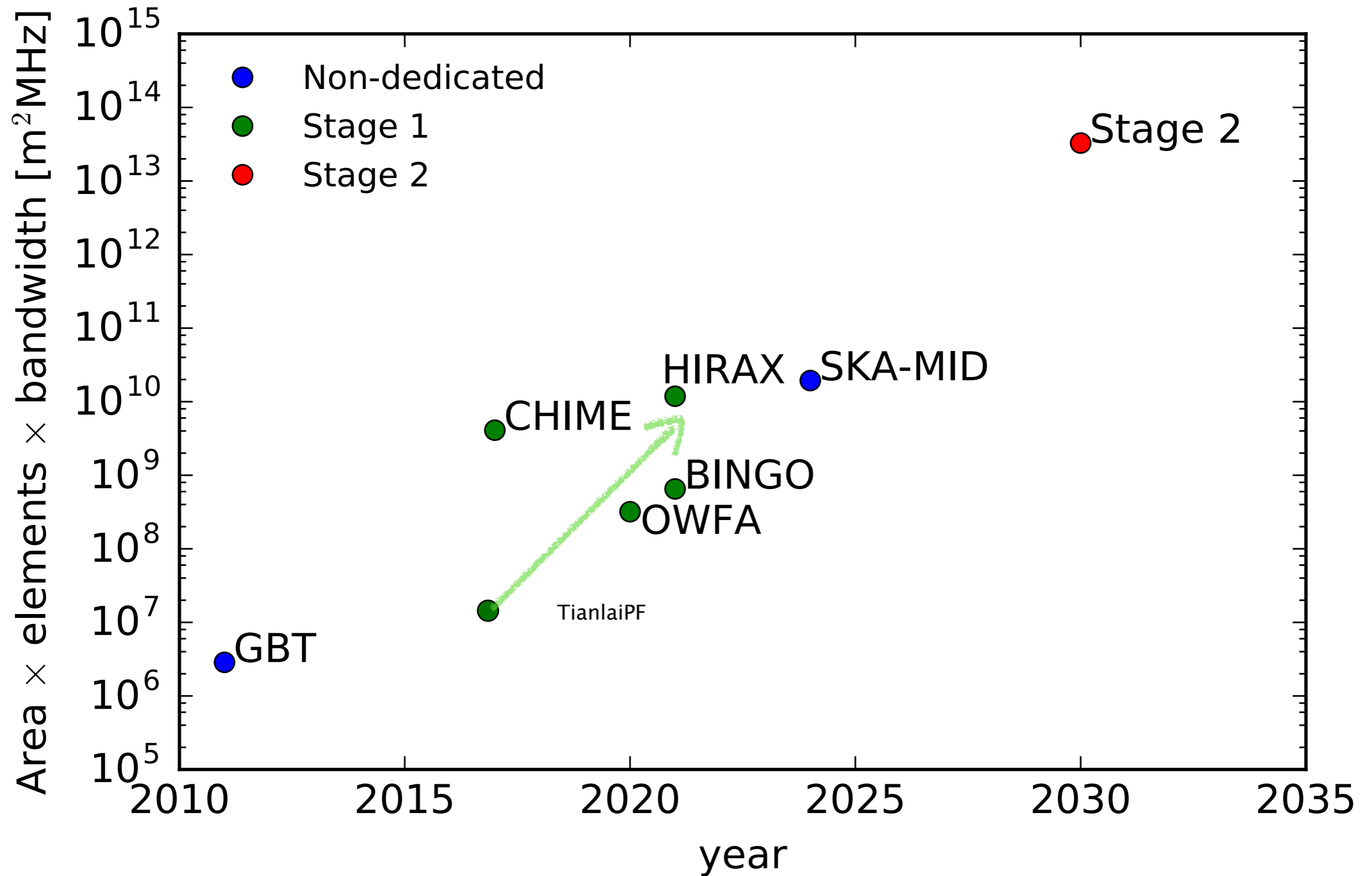
PUMA-5K
TOTAL \$58.8M



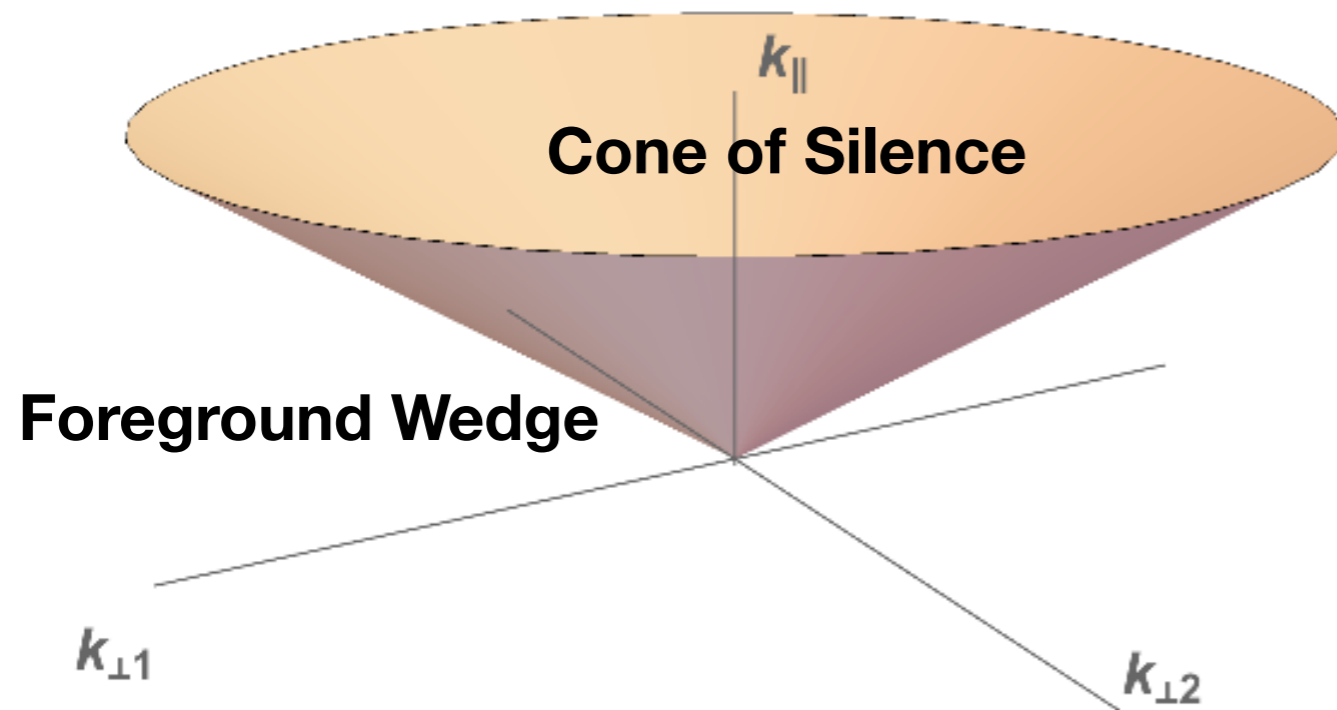
PUMA-32K
TOTAL \$373.4M



Hydrogen Intensity Mapping (HIM): experiments



Hydrogen Intensity Mapping: hi- k_{\parallel} analysis



To search for non-smooth spectrum emission one might *initially* look as far away from the foreground wedge as possible, e.g. large k_{\parallel} for individual visibilities.

This requires no knowledge of the beam, only that $|k_{\parallel}| \gg |k_{\perp}|$.

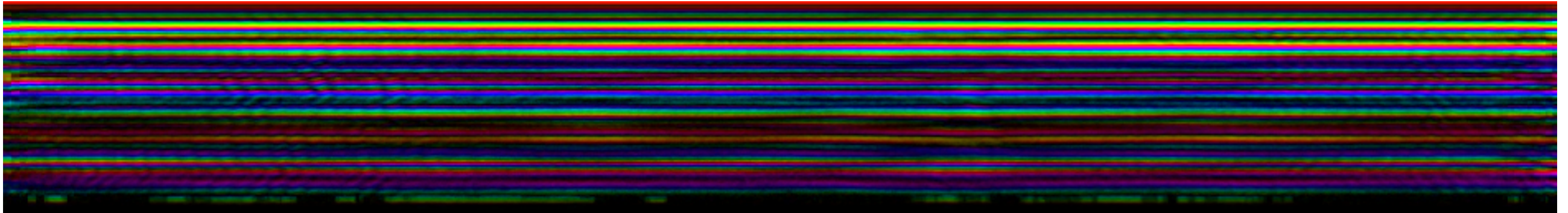
Due to chromaticity of beams non-smooth angular structure of sources will leak into frequency structure (mode mixing) filling the **foreground wedge**. Ideally the **cone of silence**, the complement of the wedge, is not contaminated by smooth spectrum sources, however there is no well defined boundary so one must determine the leakage of smooth spectrum sources into all parts of k-space.

Discover the Hilbert subspace of the “space of beams” with little contamination.

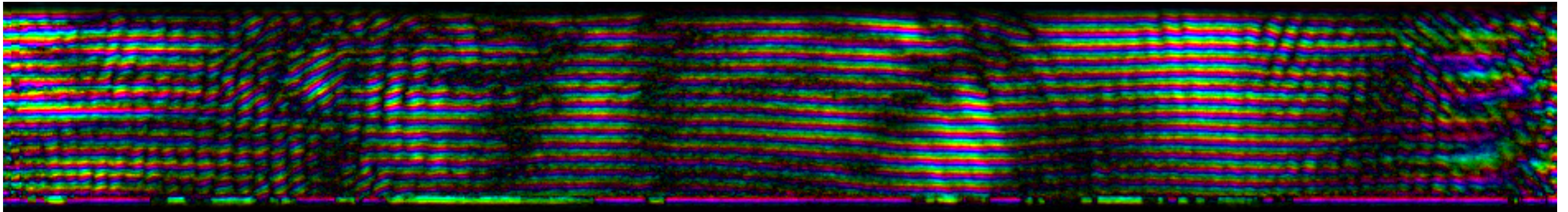
At present 21cm intensity mapping experiments suffer from non-detection of 21cm emission. *“Finding it” should be a high priority.* We can do so by looking for non-smooth spectrum emission away from the wedge.

HIM: Tianlai Visibility: Nighttime Mean Subtraction

without subtraction



with subtraction



? Correlated noise / “cross talk” ?

Hydrogen Intensity Mapping: The Tianlai Site

