

# Journée de rencontre des jeunes chercheurs

26/11/19

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DUBARRY (CEA)

# Introduction

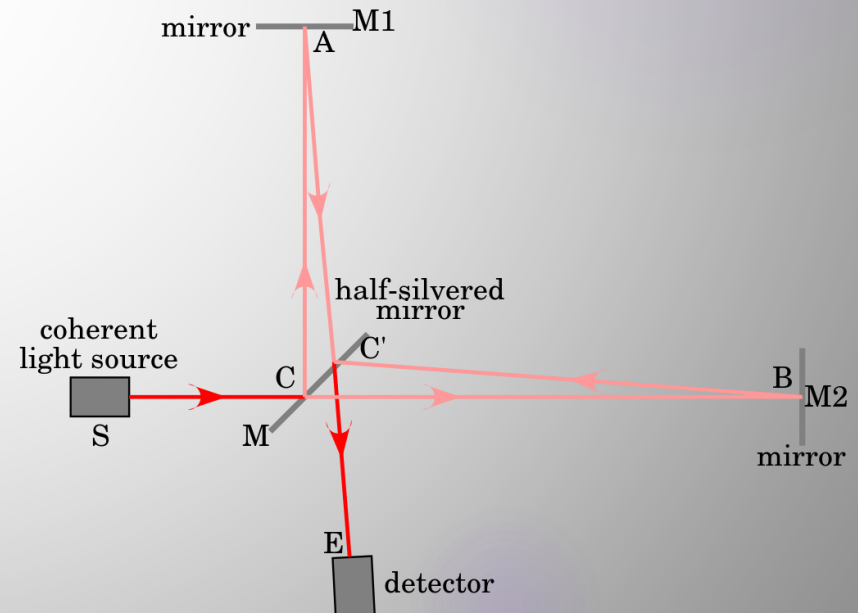
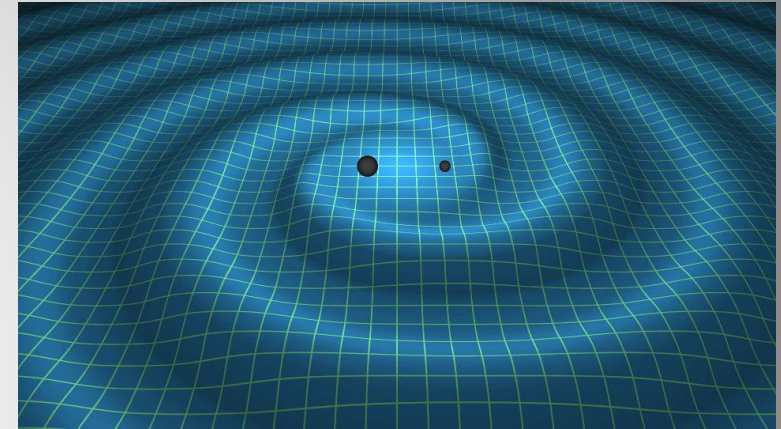
- ▶ Thesis title: AlGaAs crystalline mirrors for the space-time metrology and their application to gravitational wave detectors
- ▶ Idea : Searching for methods to reduce thermal noises on the mirrors of Virgo
- ▶ A good solution to reduce thermal noises : Crystalline coatings

# Outline

- ▶ Introduction
- ▶ The interferometer Virgo
- ▶ Thermal noises
- ▶ Thermal noise models
  - ▶ Thermal noise model for small beams
  - ▶ Thermal noise model for Higher Order Modes
- ▶ Development of crystalline coatings

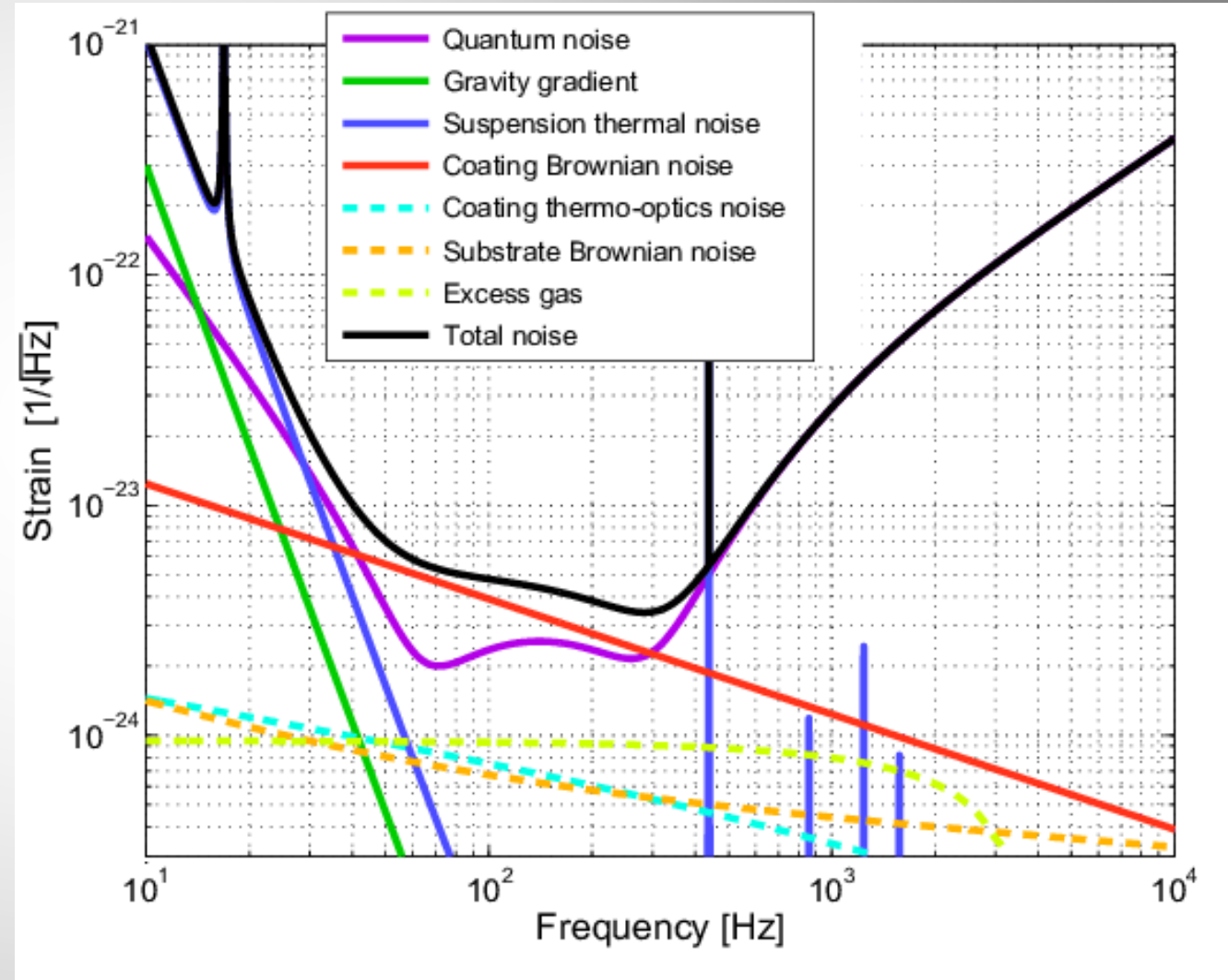
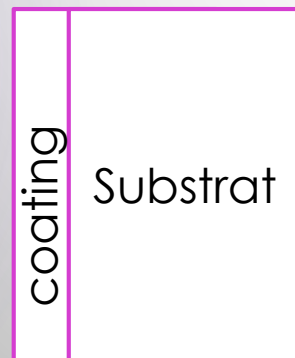
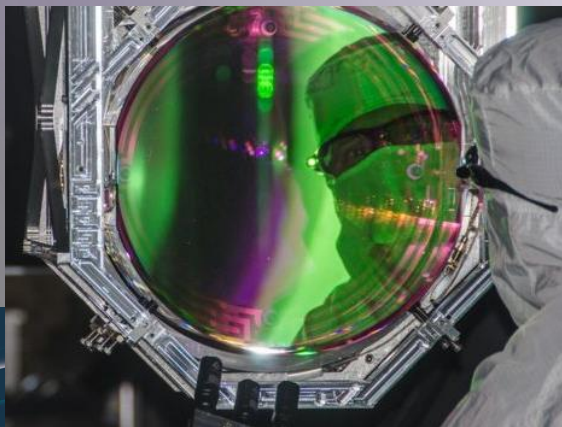
# Introduction

- ▶ VIRGO interferometer: Detection of Gravitational Waves



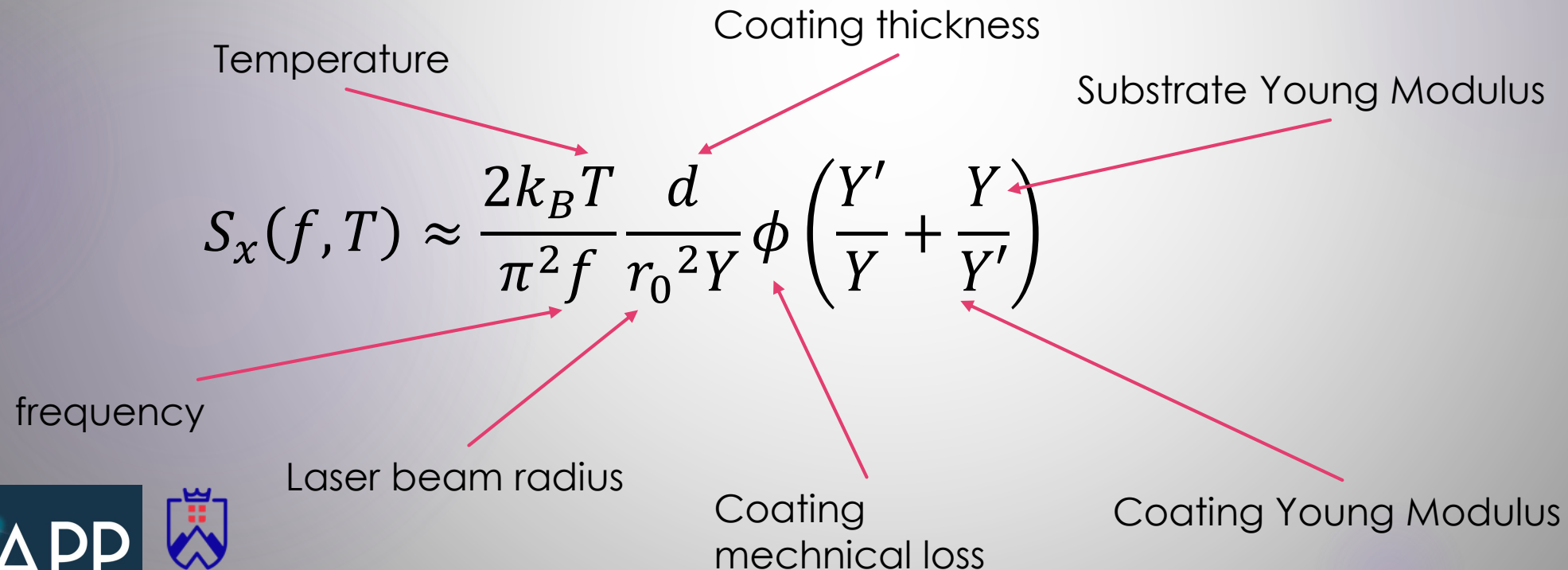
# Motivation

- ▶ One of the main limitation of the sensitivity is the thermal noises on the mirrors of the interferometer
- ▶ Two main thermal noises in the coating:
  - ▶ Brownian noise
  - ▶ Thermo-optic noise



# Brownian noise

- ▶ Caused by Brownian motion of mirror surface
- ▶ Largest contribution to the overall detector noise by the optics



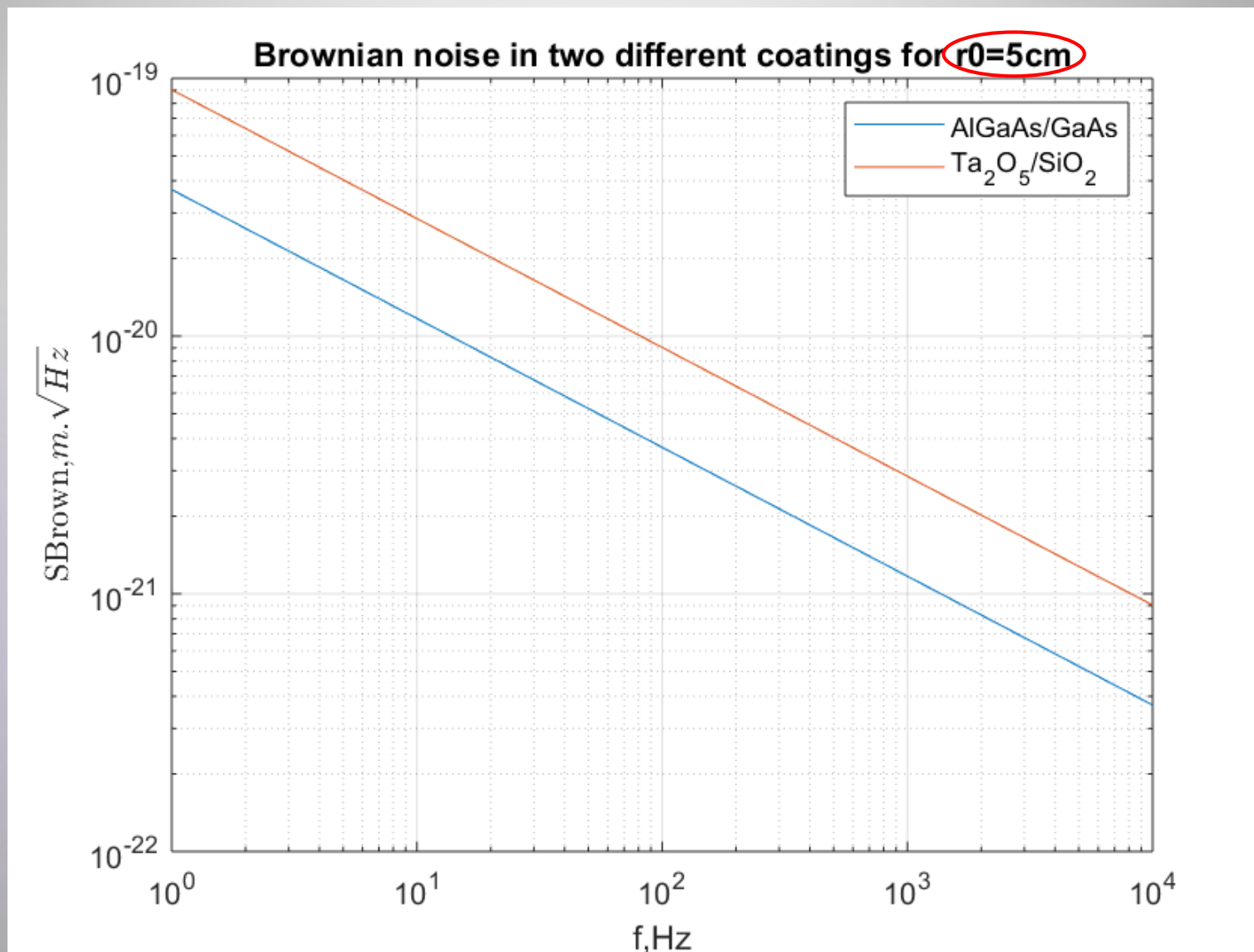
# Reduction of thermal noise

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- ▶ Coatings used for now : amorphous coatings
  - ▶  $Ta_2O_5/SiO_2$
  - ▶ Made at LMA (Laboratoire des Matériaux Avancés)
- ▶ How to reduce thermal noise?
  - ▶ Operating the interferometer at cryogenic temperature
  - ▶ Manufacturing new coatings
- ▶ Reduction of thermal noise with crystalline coatings (G. Cole et al. 2013)
  - ▶ Better mechanical properties



# Brownian noise





# Thermo-optic noise

- ▶ Two noises that compose coating thermo-optic noise :  
Thermoelastic noise and Thermorefractive noise
- ▶ Induced by the fluctuations of the temperature in the coating

# Thermoelastic noise

Thermoelastic noise is the apparent expansion of the mirror coating into the probe beam causing change in phase

$$\Delta\varphi_{TE} = \frac{4\pi}{\lambda} \alpha_c x \delta T$$

$\alpha_c$  : coating coefficient of thermal expansion

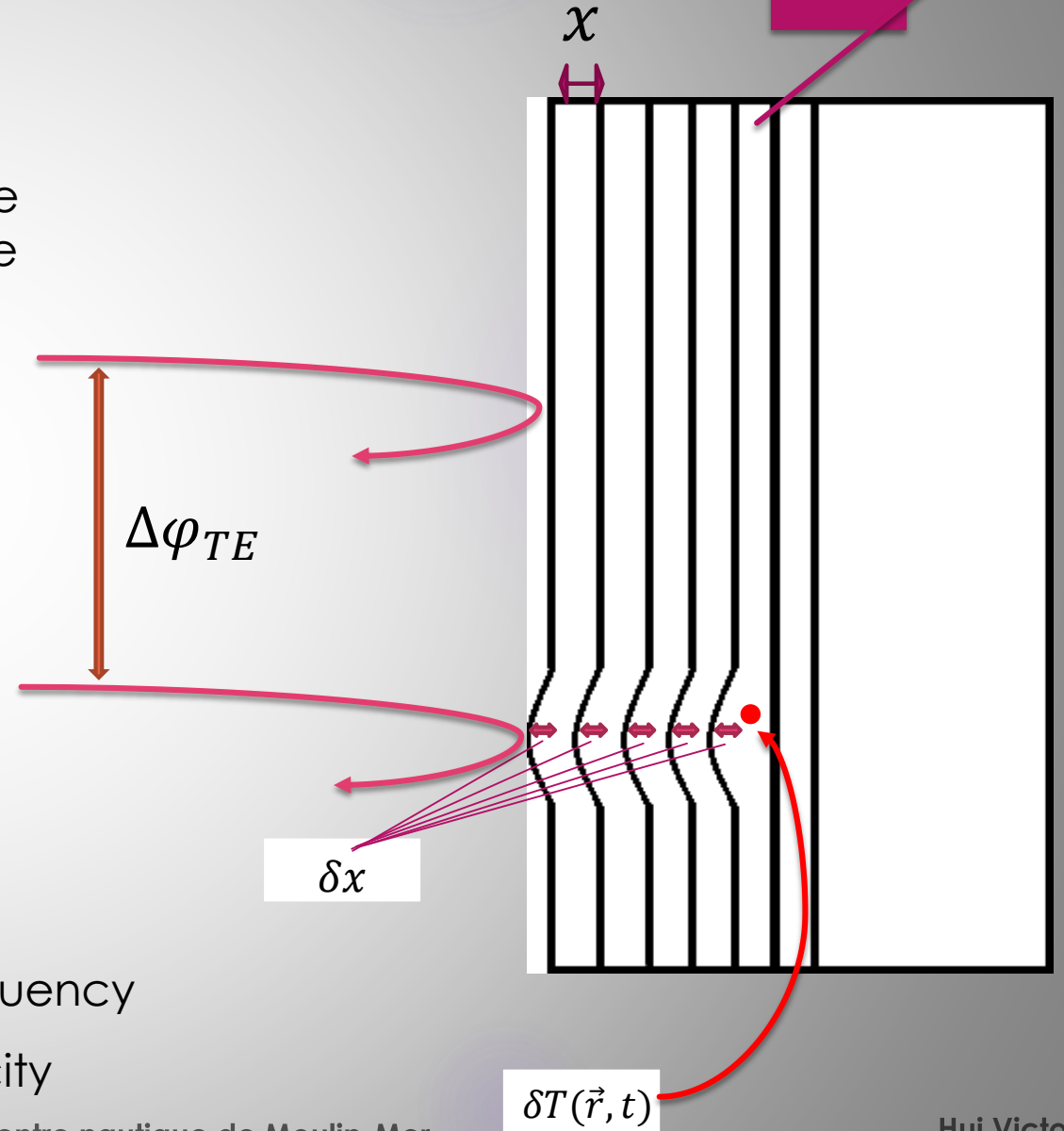
$$S_{TE}(\omega, T) \approx \frac{2\sqrt{2}k_B T^2}{\pi r_0^2 \sqrt{\kappa_S C_S \omega}} (\alpha_c d)^2$$

Coating thickness  $d$

Angular frequency  $\omega$

Substrate thermal conductivity  $\kappa_S$

Substrate heat capacity  $C_S$



# Thermorefractive noise

Thermorefractive noise comes from both the physical change in size of coating layers and the change in refractive index with temperature in the coating

$$\Delta\varphi_{TR} = \frac{4\pi}{\lambda} \beta \lambda \delta T$$

$\beta$ : coefficient of thermorefraction ( $\beta = \frac{dn}{dT}$ )

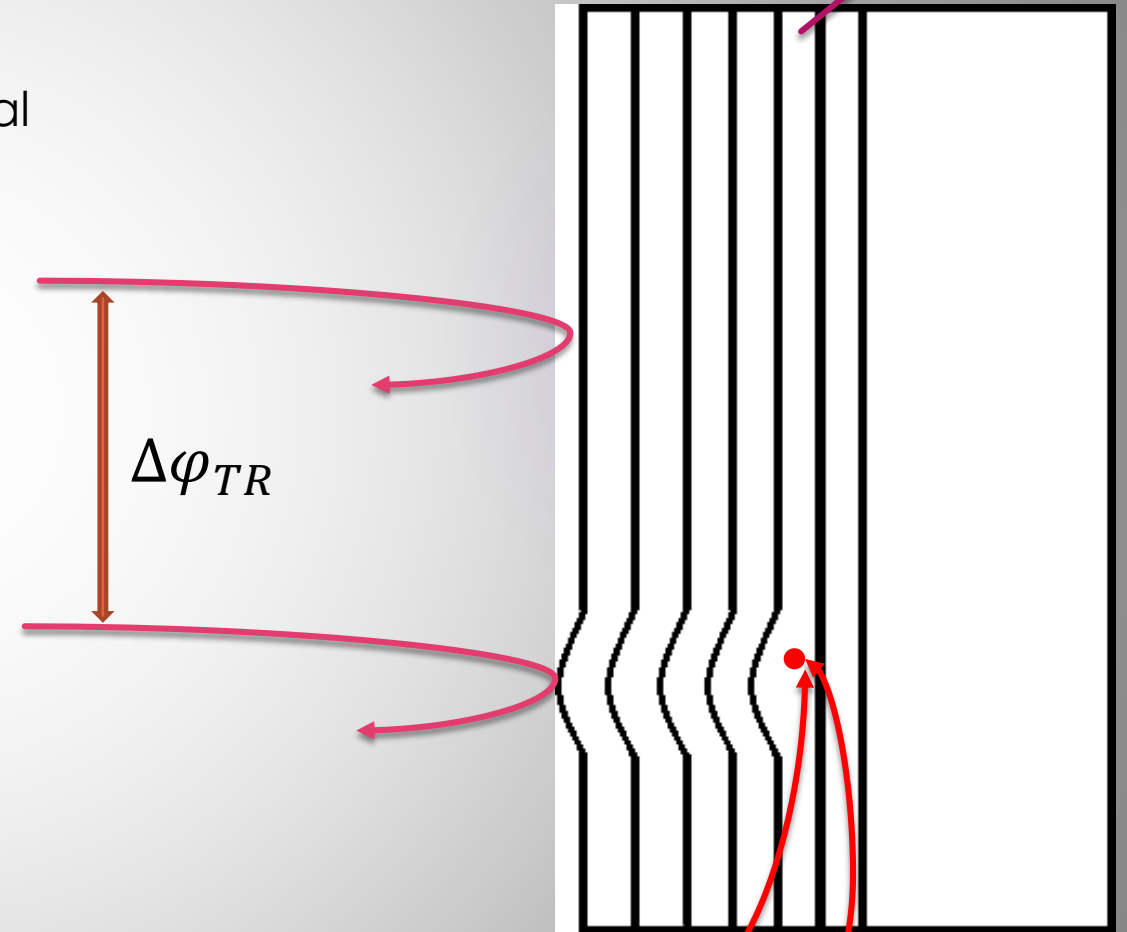
$\lambda$ : wavelength of the laser

$$S_{TR}(\omega, T) \approx \frac{2\sqrt{2}k_B T^2}{\pi r_0^2 \sqrt{\kappa_S C_S \omega}} (\beta \lambda)^2$$

Angular frequency

Substrate thermal conductivity

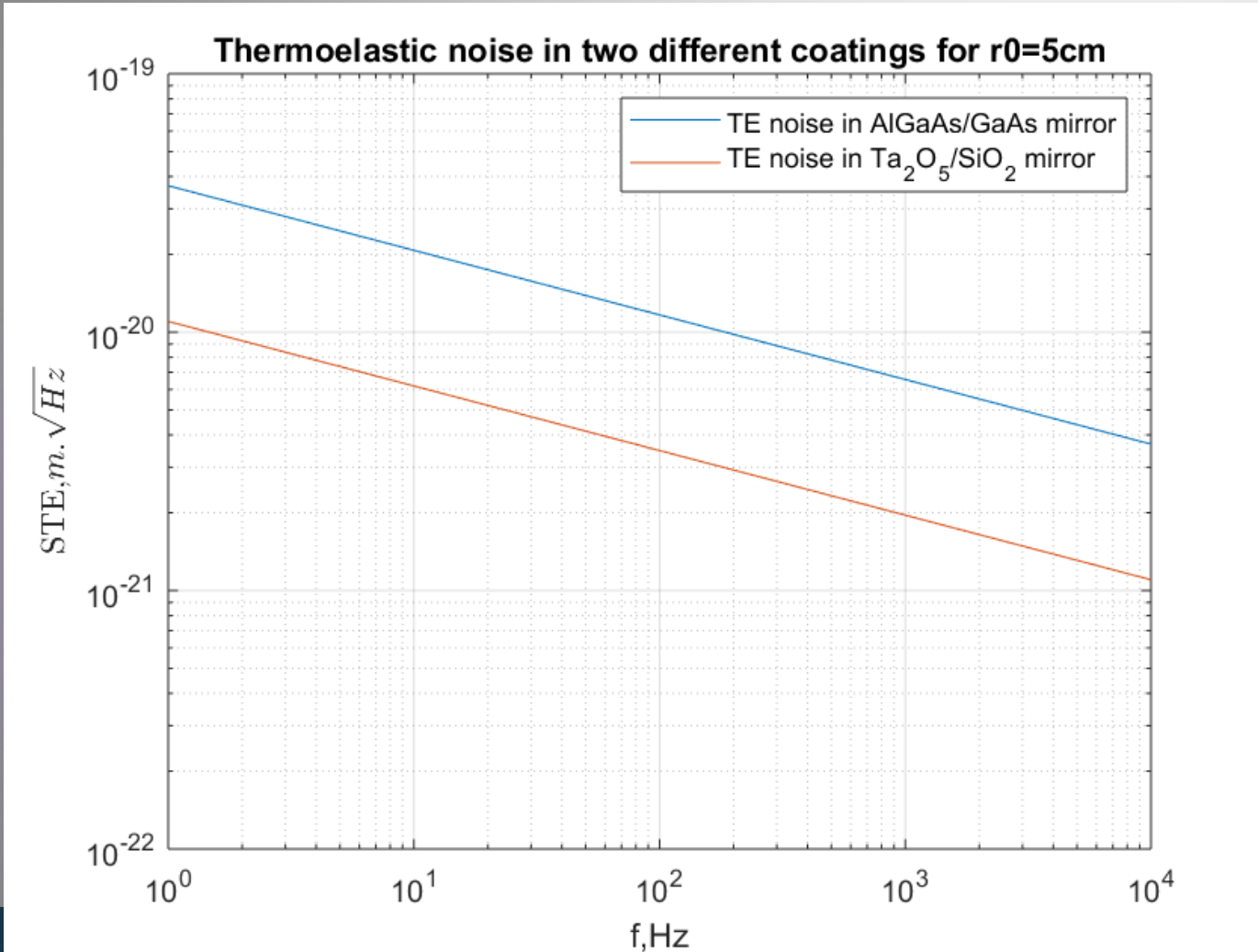
Substrate heat capacity



$\delta T(\vec{r}, t)$

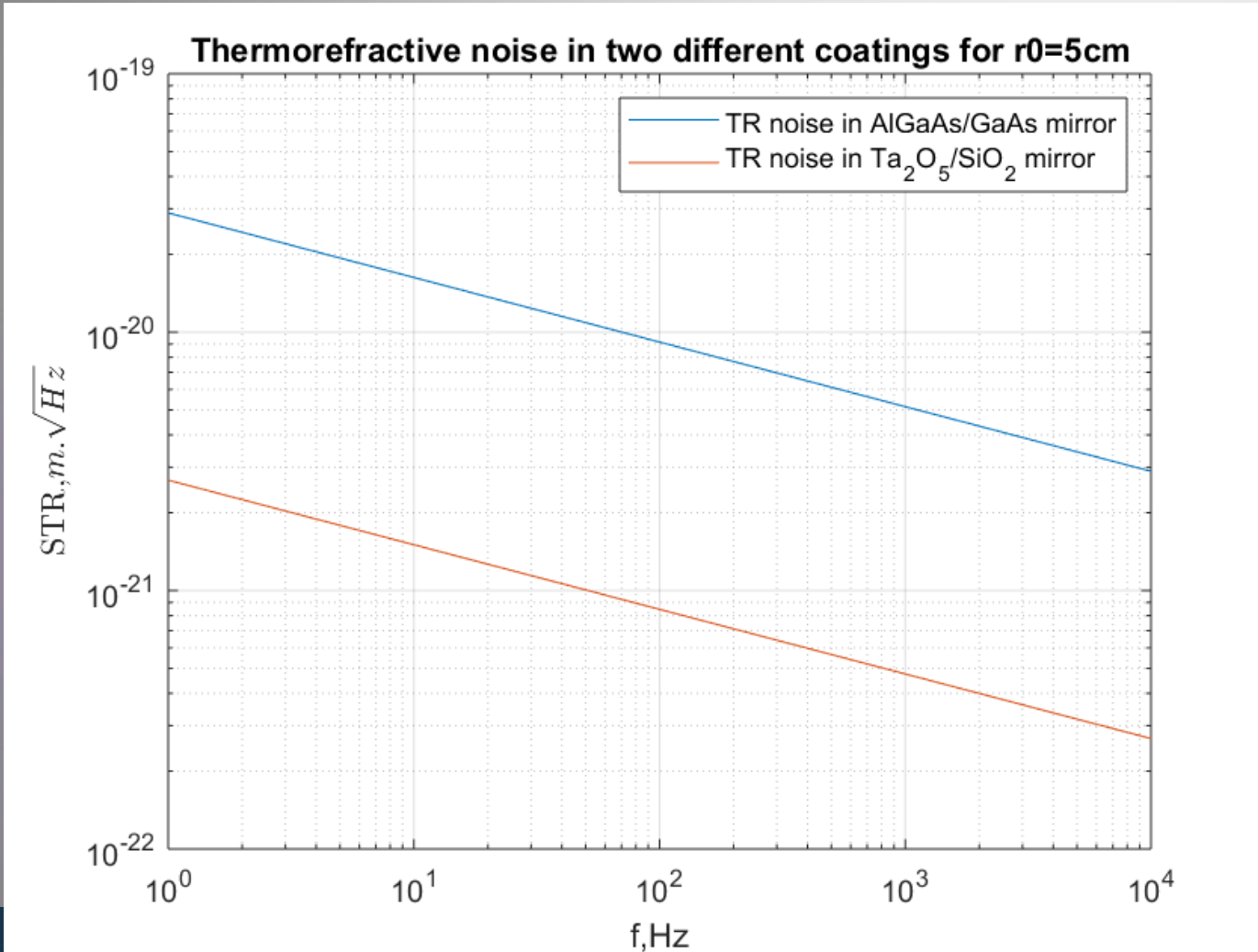
$n(\vec{T}, t)$

# Thermoelastic noise



$\alpha_c(\text{Ta}_2\text{O}_5/\text{SiO}_2)$	$6\text{e-}6 \text{ K}^{-1}$
$d(\text{Ta}_2\text{O}_5/\text{SiO}_2)$	$6 \mu\text{m}$
$\alpha_c(\text{AlGaAs}/\text{GaAs})$	$2\text{e-}5 \text{ K}^{-1}$
$d(\text{AlGaAs}/\text{GaAs})$	$4.7 \mu\text{m}$

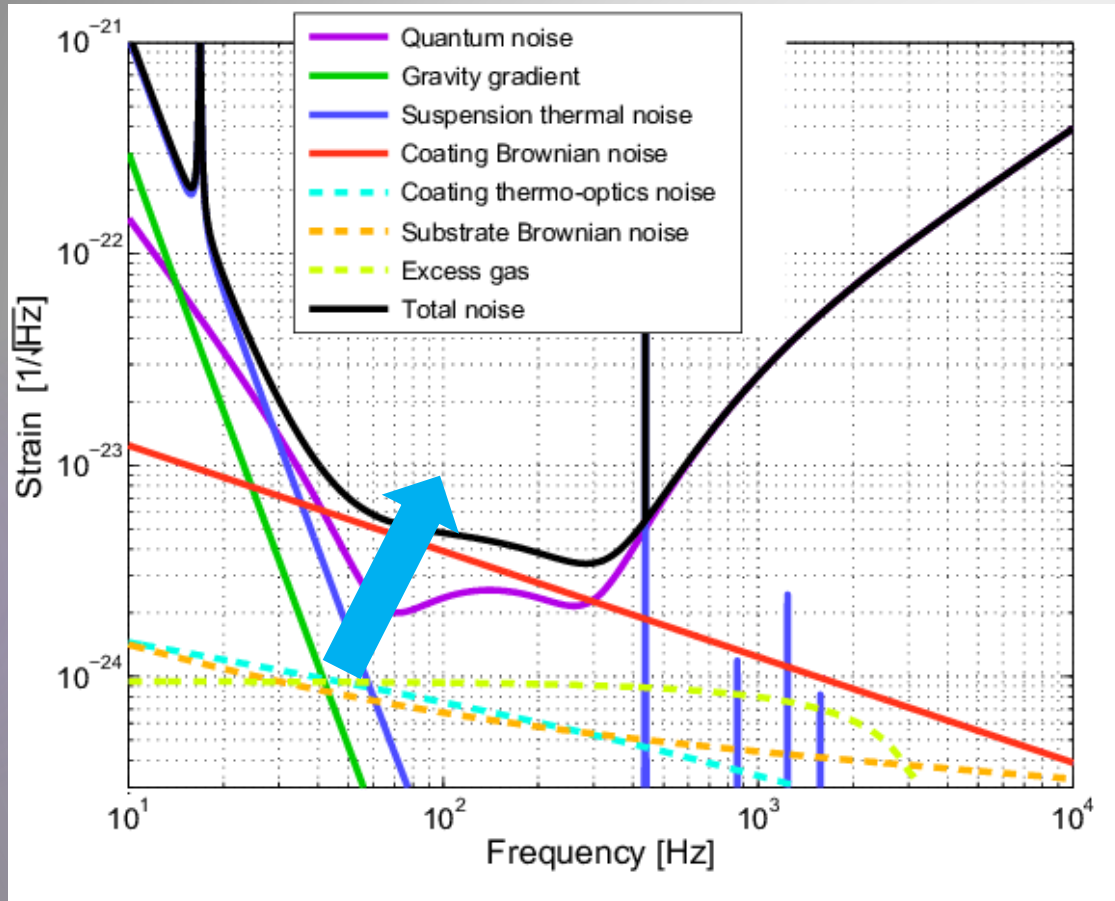
# Thermorefractive noise



$\beta$ (Ta <sub>2</sub> O <sub>5</sub> /SiO <sub>2</sub> )	7e-6 K <sup>-1</sup>
$\beta$ (AlGaAs/GaAs)	8e-5 K <sup>-1</sup>
$\lambda$	1064 $\mu$ m

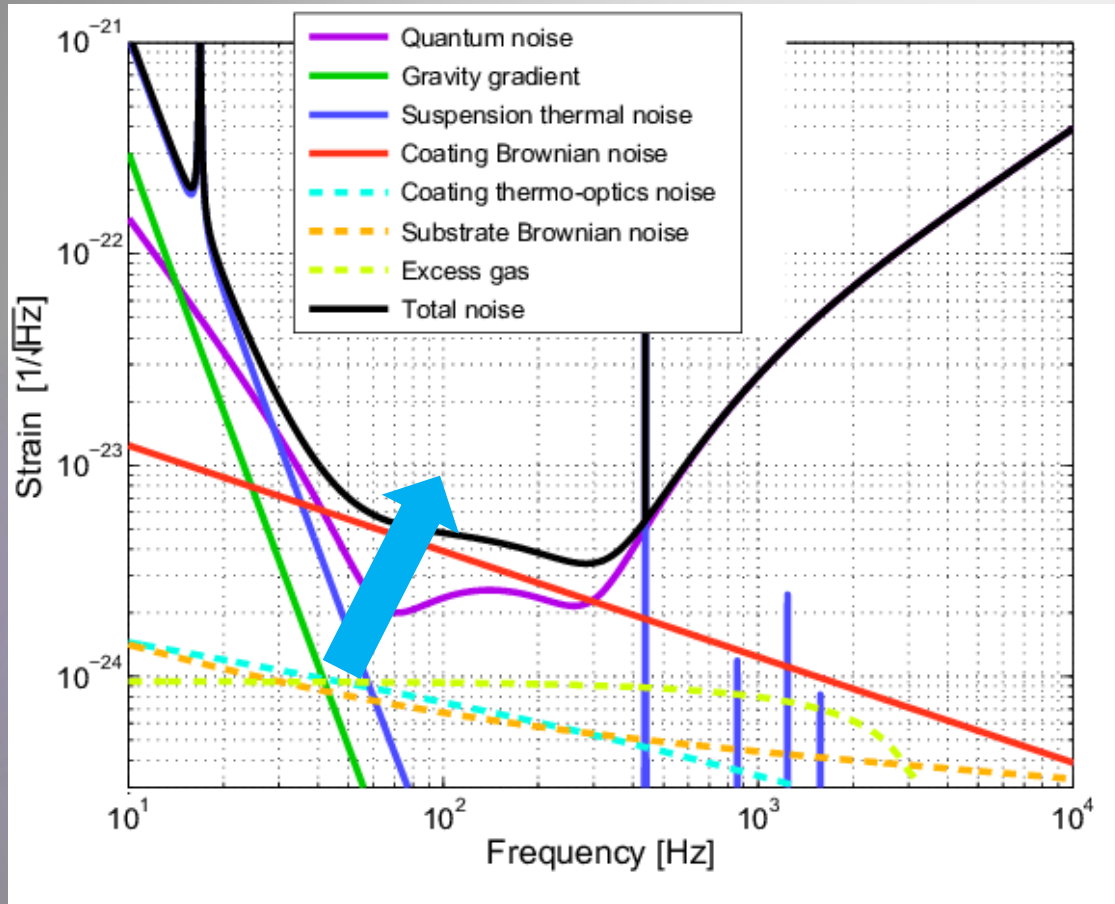
➤ TE and TR noise higher in crystalline coatings???

# Thermo-optic noise



TO higher in crystalline coatings???

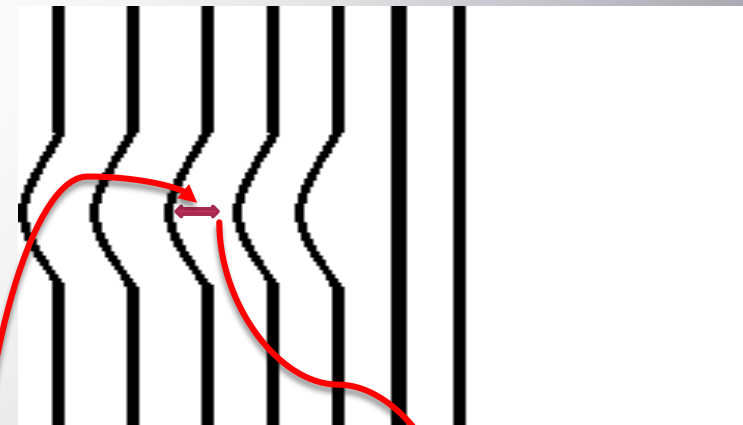
# Thermo-optic noise



TO higher in crystalline coatings???

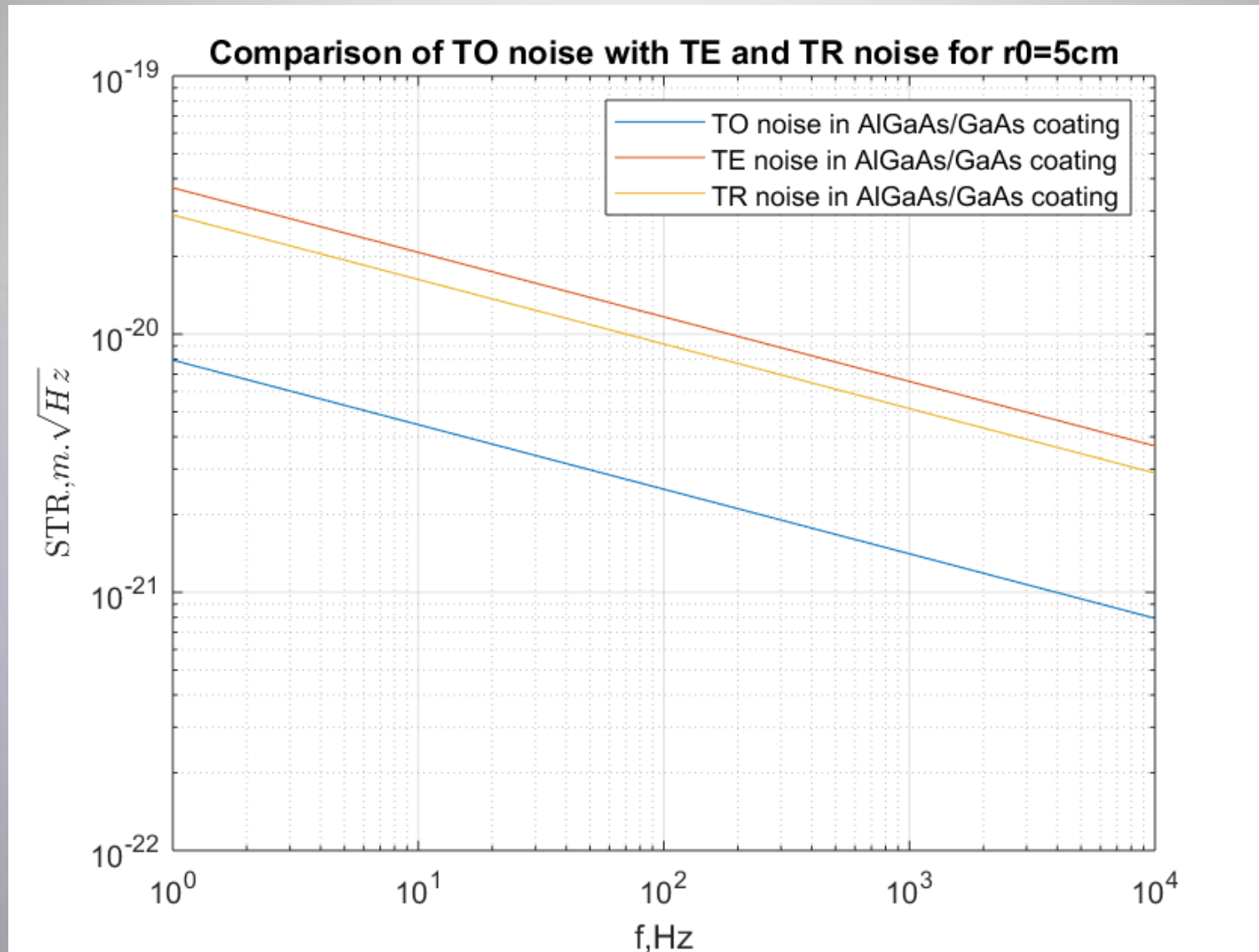
TO noise is not a sum of TE and TR noise

TR and TE noise are correlated and they tend to « compensate » each other



Expansion => Refraction Index decreasing

# Thermo-optic noise





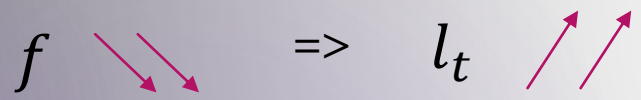
# Thermal noise model for small beams

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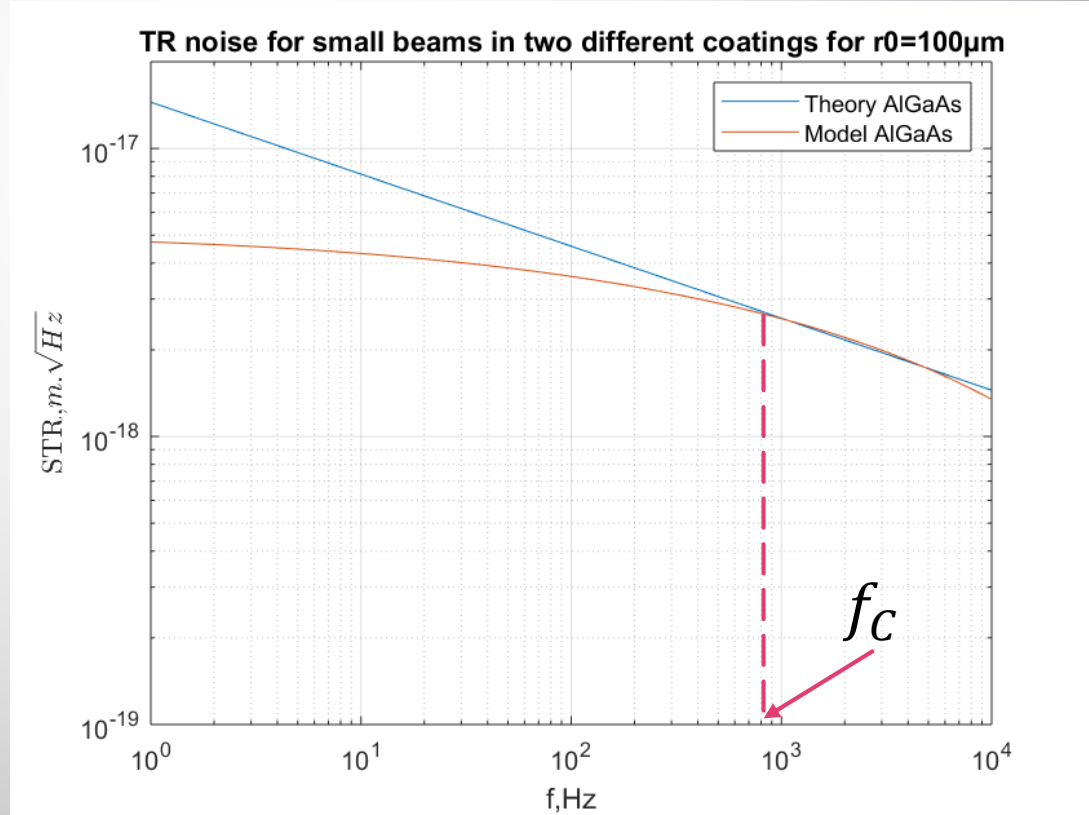
- ▶ We cannot test coatings directly in Virgo
- ▶ Need to do the measurements in Lab : short cavities => small beams
- ▶ Thermal noise increases when  $r_0$  decreases (Thermal noise  $\propto \frac{1}{r_0^2}$ ) => easier to measure
- ▶ Until now: coating thermal noises measured for  $r_0 \sim cm - mm$ 
  - ▶ Approximations can be applied => thermal diffusion negligible
- ▶ For small radius ( $\sim 100\mu m$ )
  - ▶ Approximation not valid anymore at low frequencies
  - ▶ Need to build a new model

# Thermal noise model for small beams

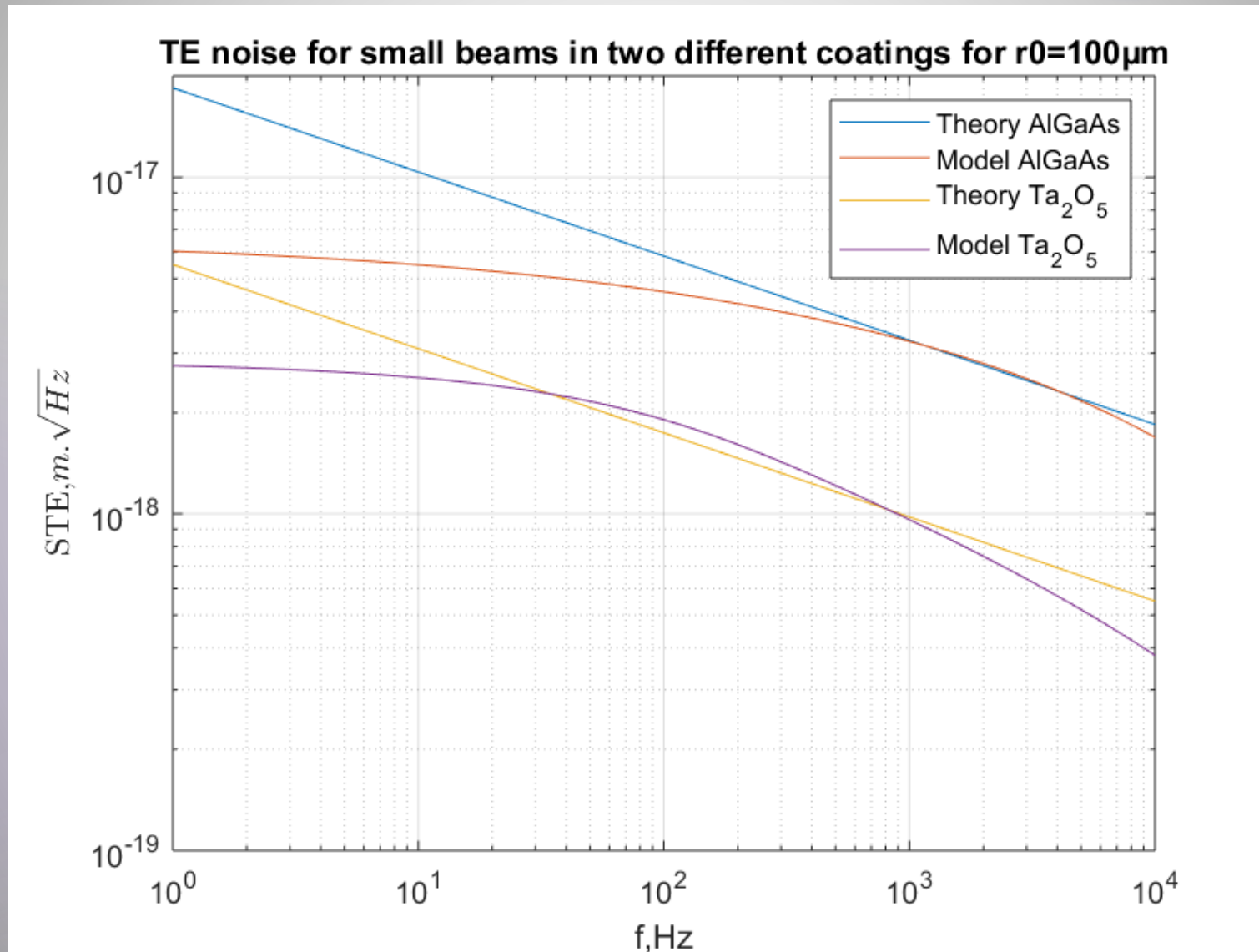
$$l_t = \sqrt{\frac{\kappa}{\rho C f}} \text{ to be compared to } r_0 \quad l_t \gg r_0 \Rightarrow \text{thermal diffusion significant}$$



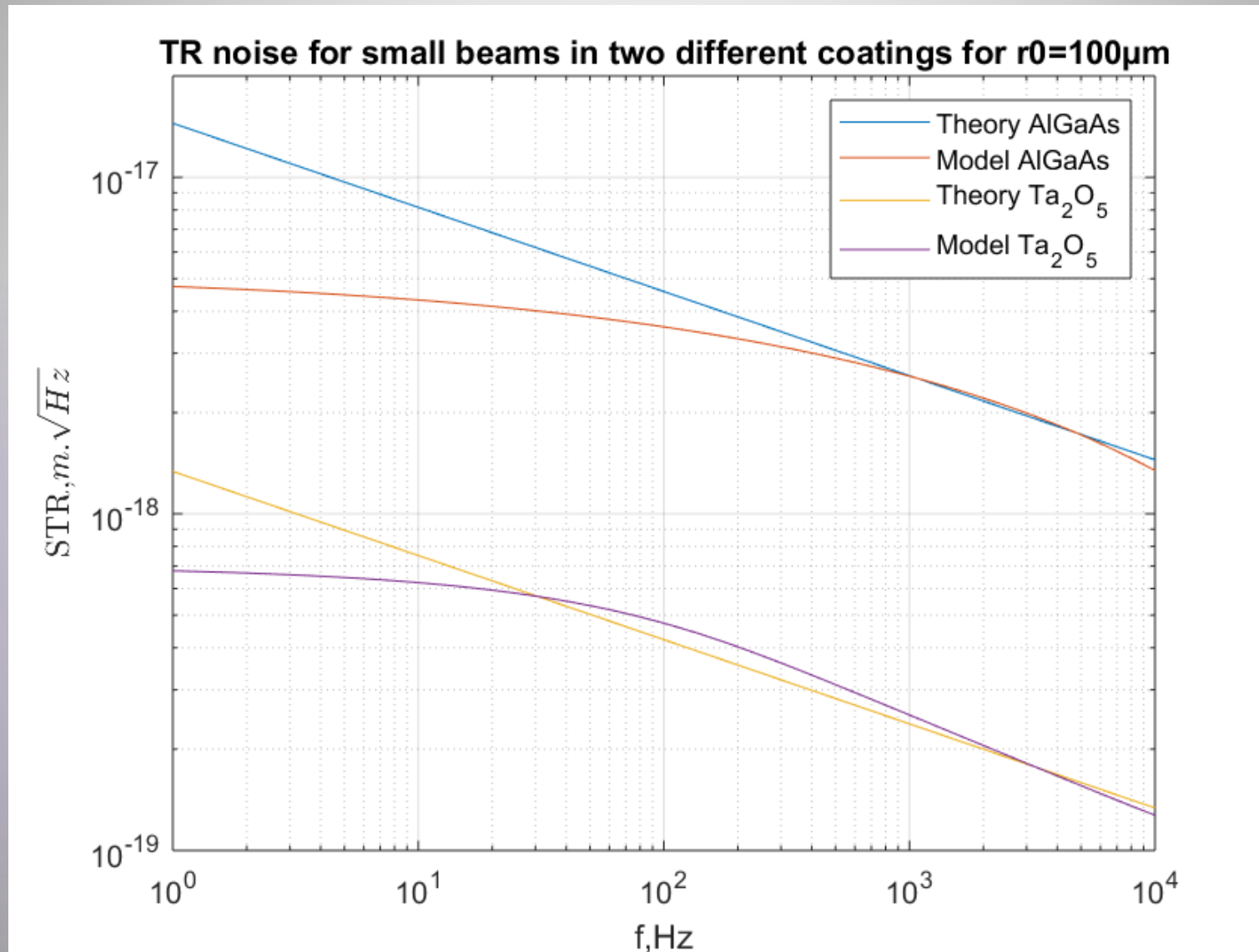
- $l_t$  : Thermal diffusion length
- $\kappa$  : Thermal conductivity
- $\rho$  : Volumic mass
- $C$  : Heat capacity
- $f$  : frequency



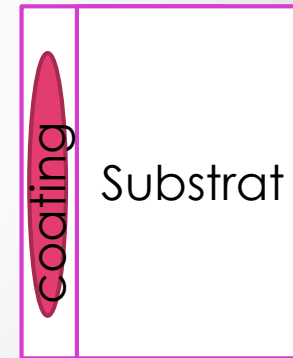
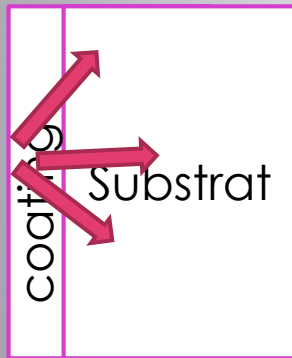
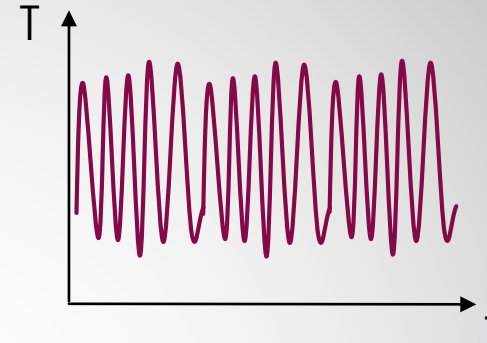
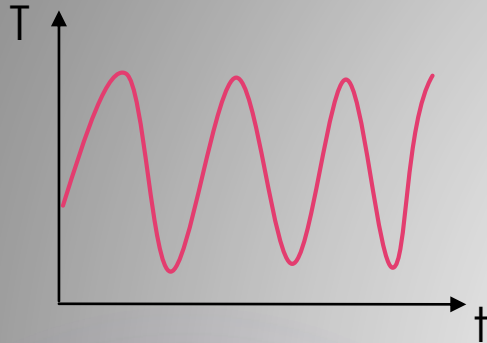
# Thermal noise model for small beams



# Thermal noise model for small beams



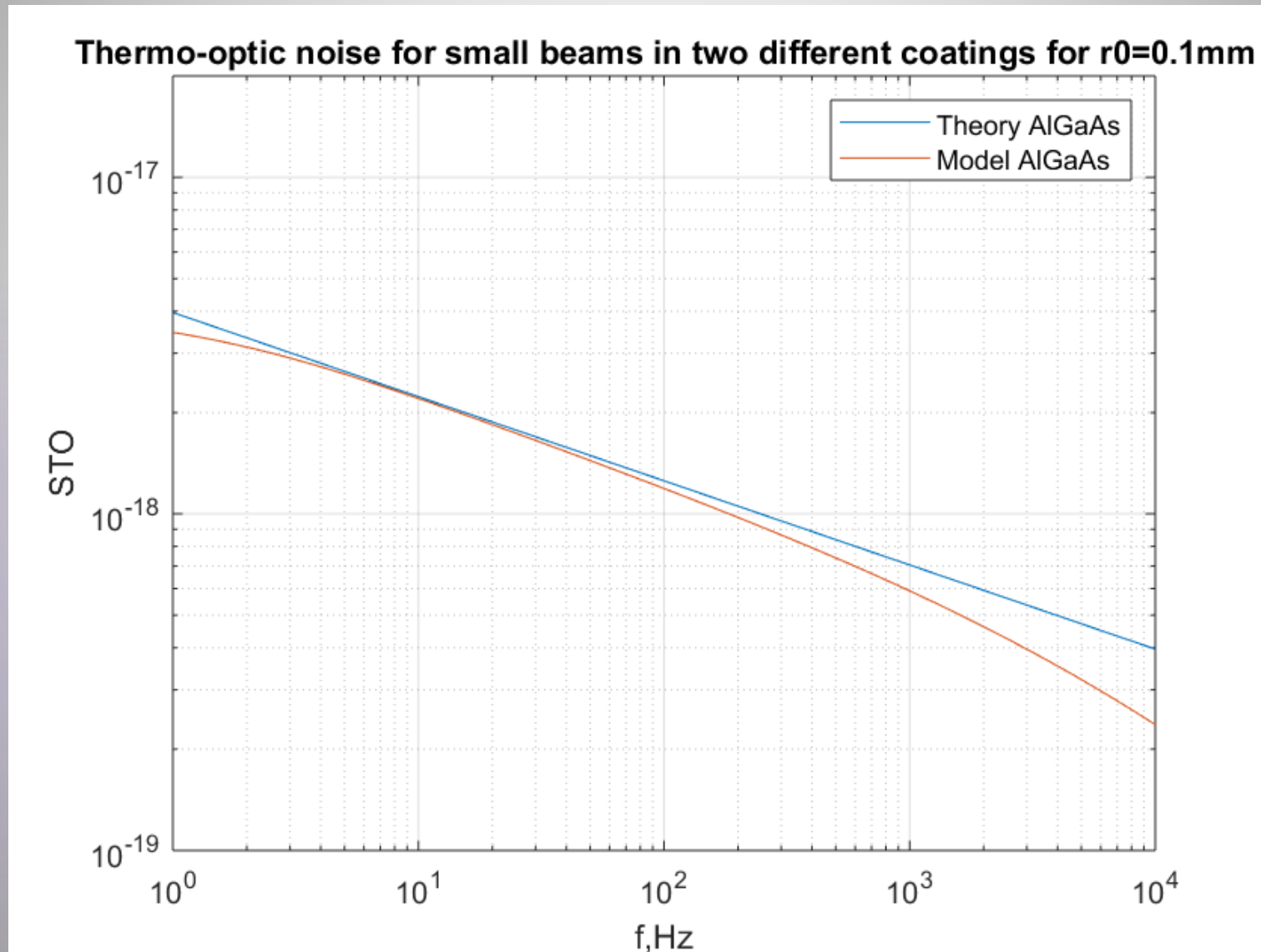
# Thermal noise model for small beams



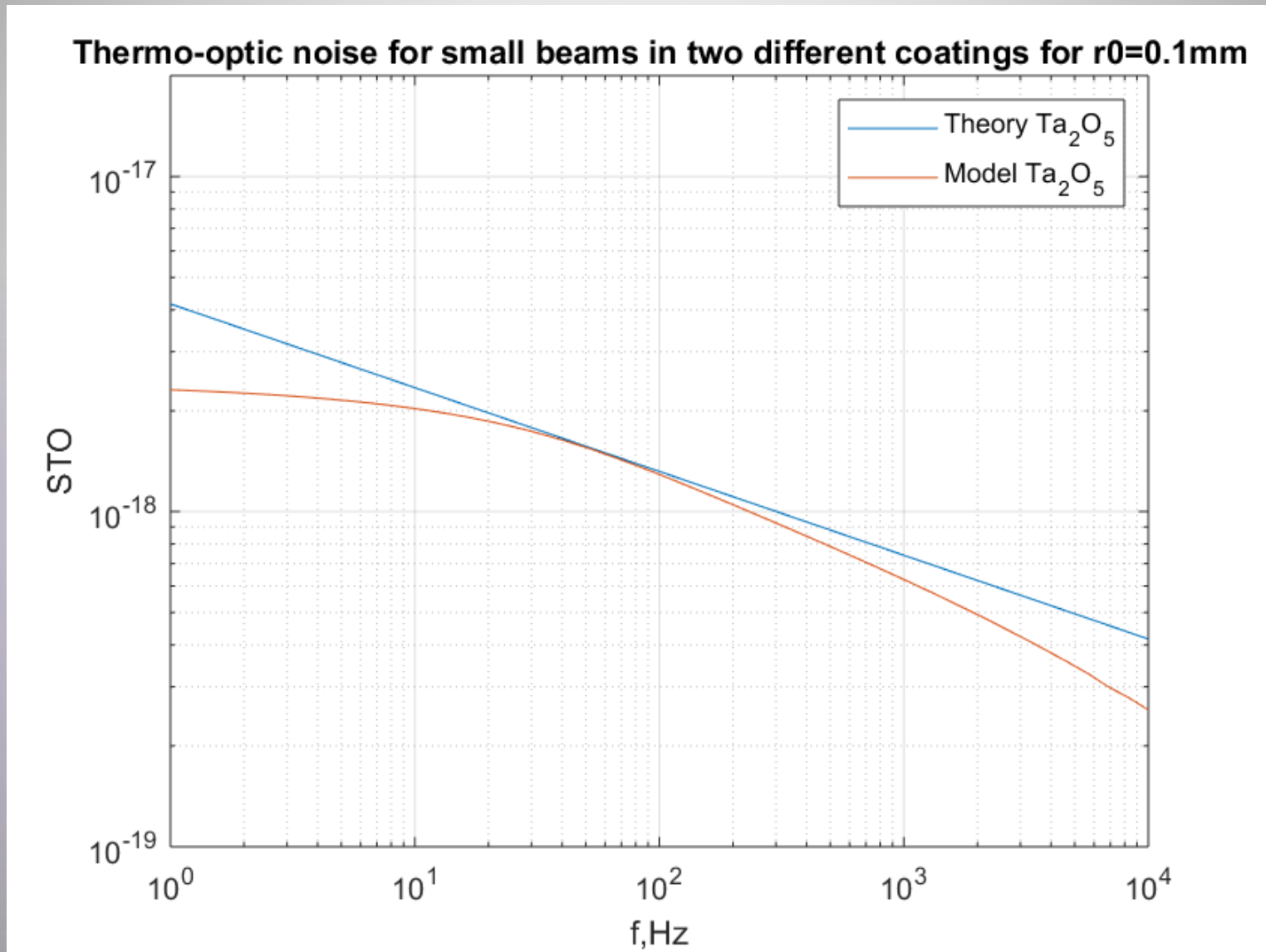
Low frequency  
-> bigger heat volume  
-> grad(T)

High frequency  
-> Thermal diffusion negligible  
-> Heat essentially in the coating

# Thermal noise model for small beams

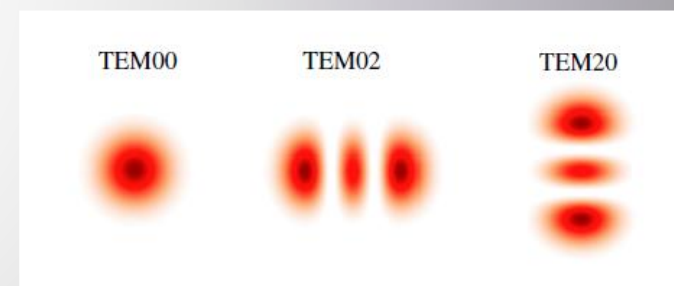
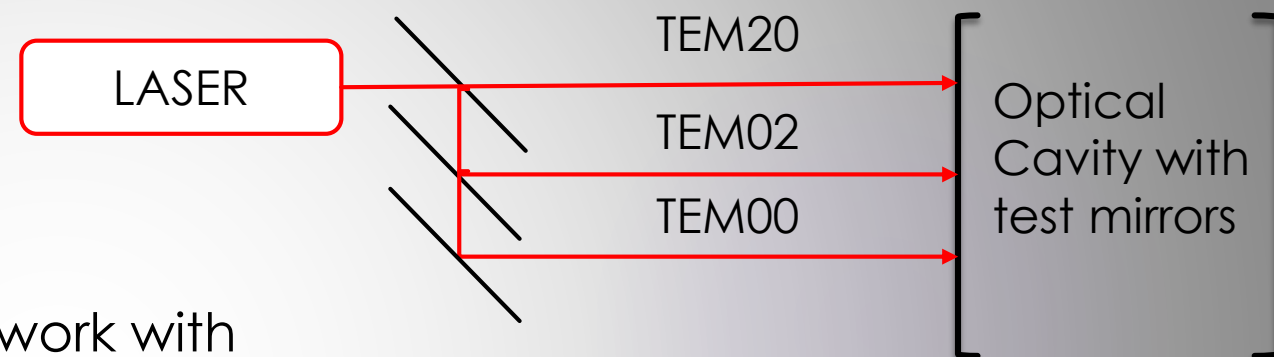


# Thermal noise model for small beams



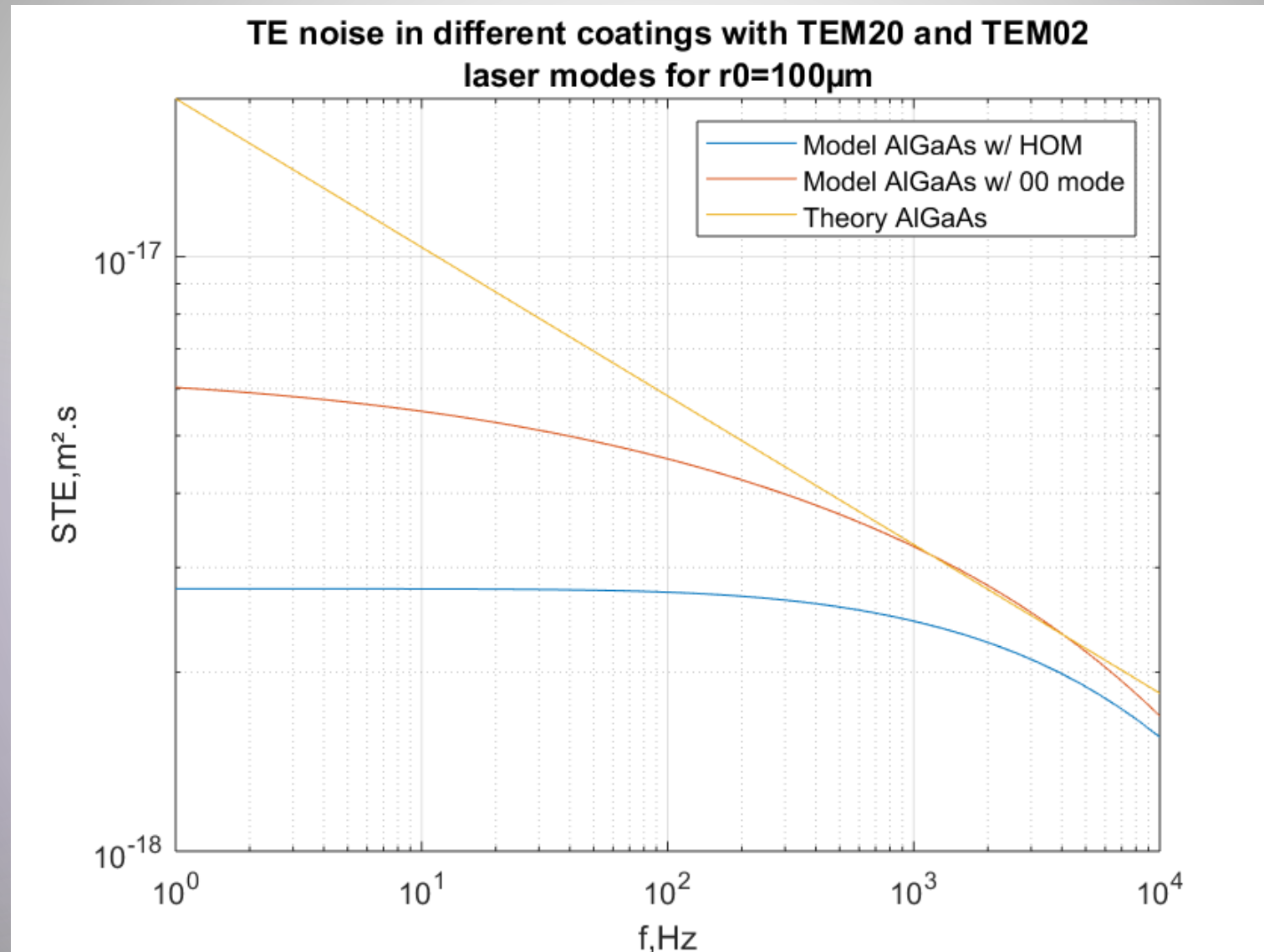
# Thermal noise models with higher order modes

- ▶ We cannot only use small  $r_0$
- ▶ To reduce laser noises we need to work with higher order modes
- ▶ MIT experiment
  - ▶ Reducing laser noise
  - ▶ Measurements of thermal noise
- ▶ The model to describe thermal noise will be different

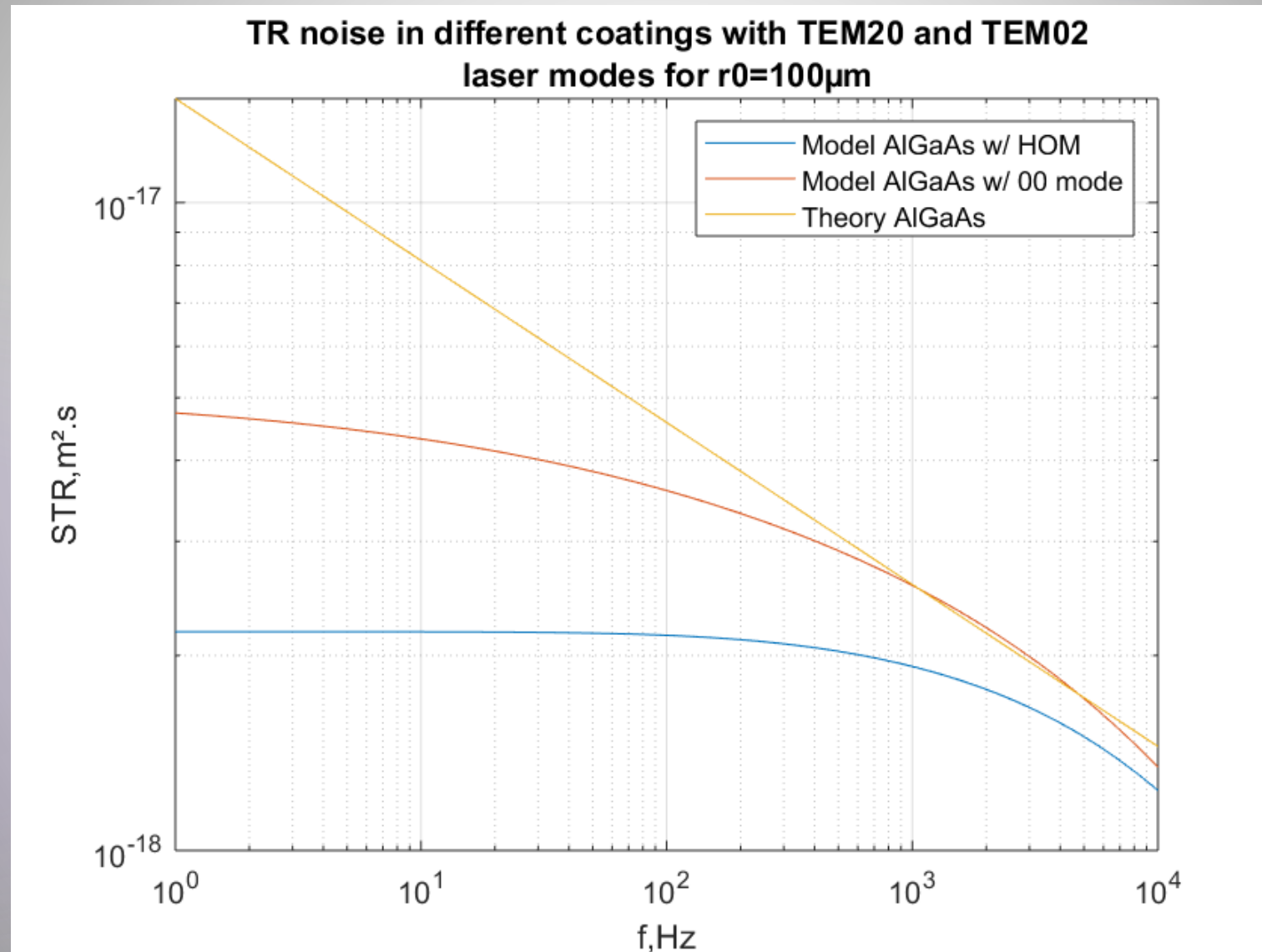




# Thermoelastic noise model with HOM laser

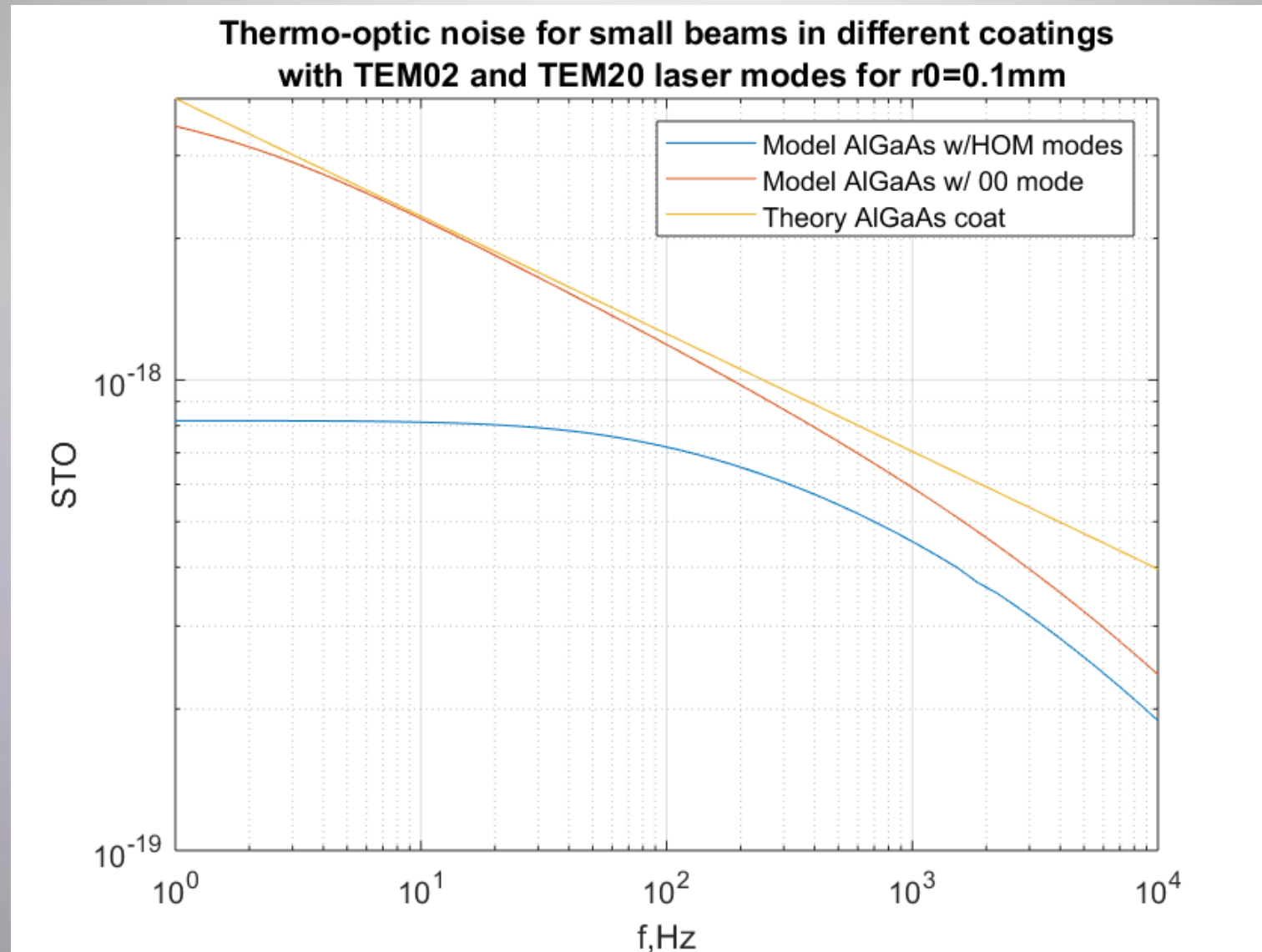


# Thermorefractive noise model with HOM laser



# Thermo-optic noise model with HOM laser

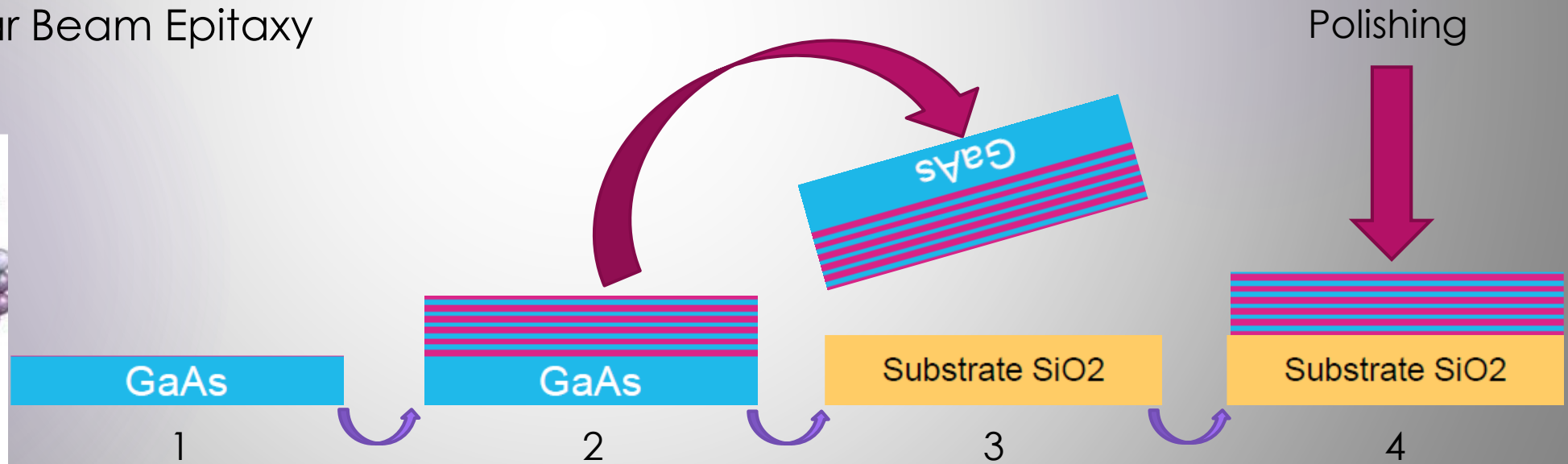
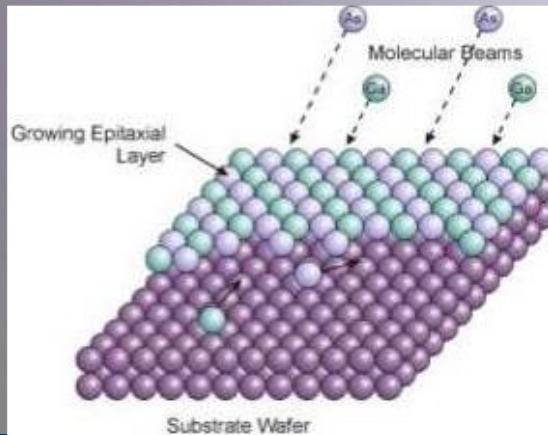
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# Development of crystalline mirrors

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- ▶ Until now, measurements of thermal noise on small coatings ( $\sim cm$ )
- ▶ For Virgo => bigger mirrors (30+cm)
- ▶ Goal : to make bigger coatings at CEA Leti
- ▶ Molecular Beam Epitaxy



# Development of crystalline mirrors

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- ▶ GaAs and Silica Substrates characterized at CEA



- ▶ GaAs substrate sent to LAAS (Laboratoire Analyse et Architecture Systèmes)

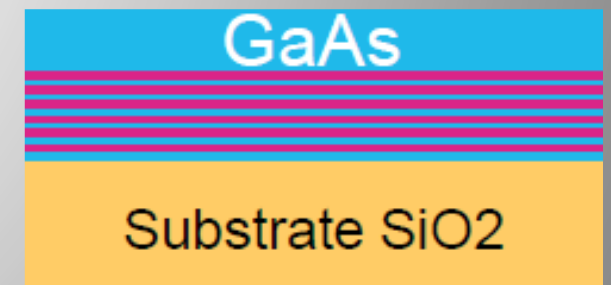
- ▶ MBE to grow crystalline coatings



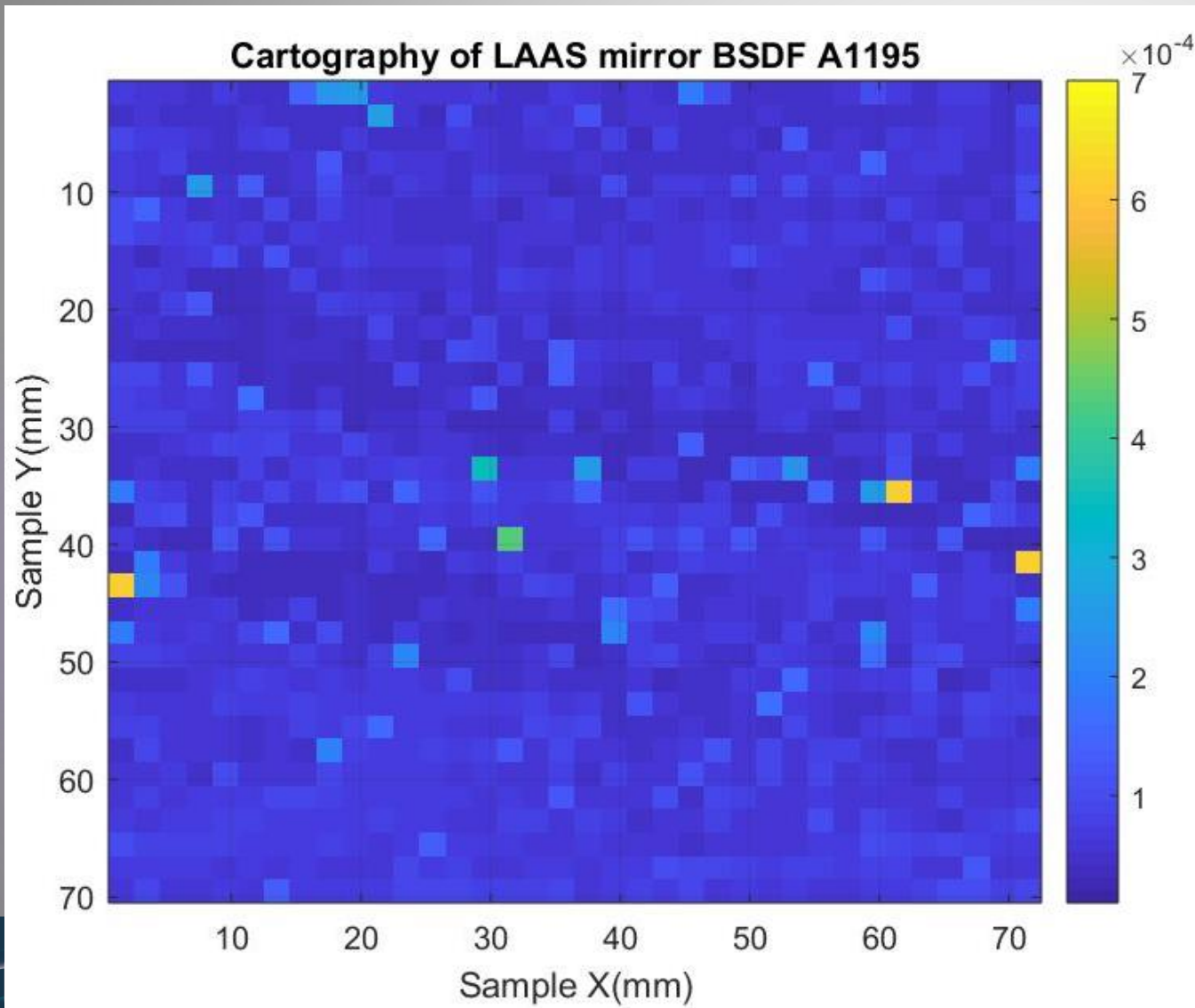
- ▶ Characterization at LMA

- ▶ Scattering map
  - ▶ Defaults map

- ▶ Transfert on silica substrate at CEA



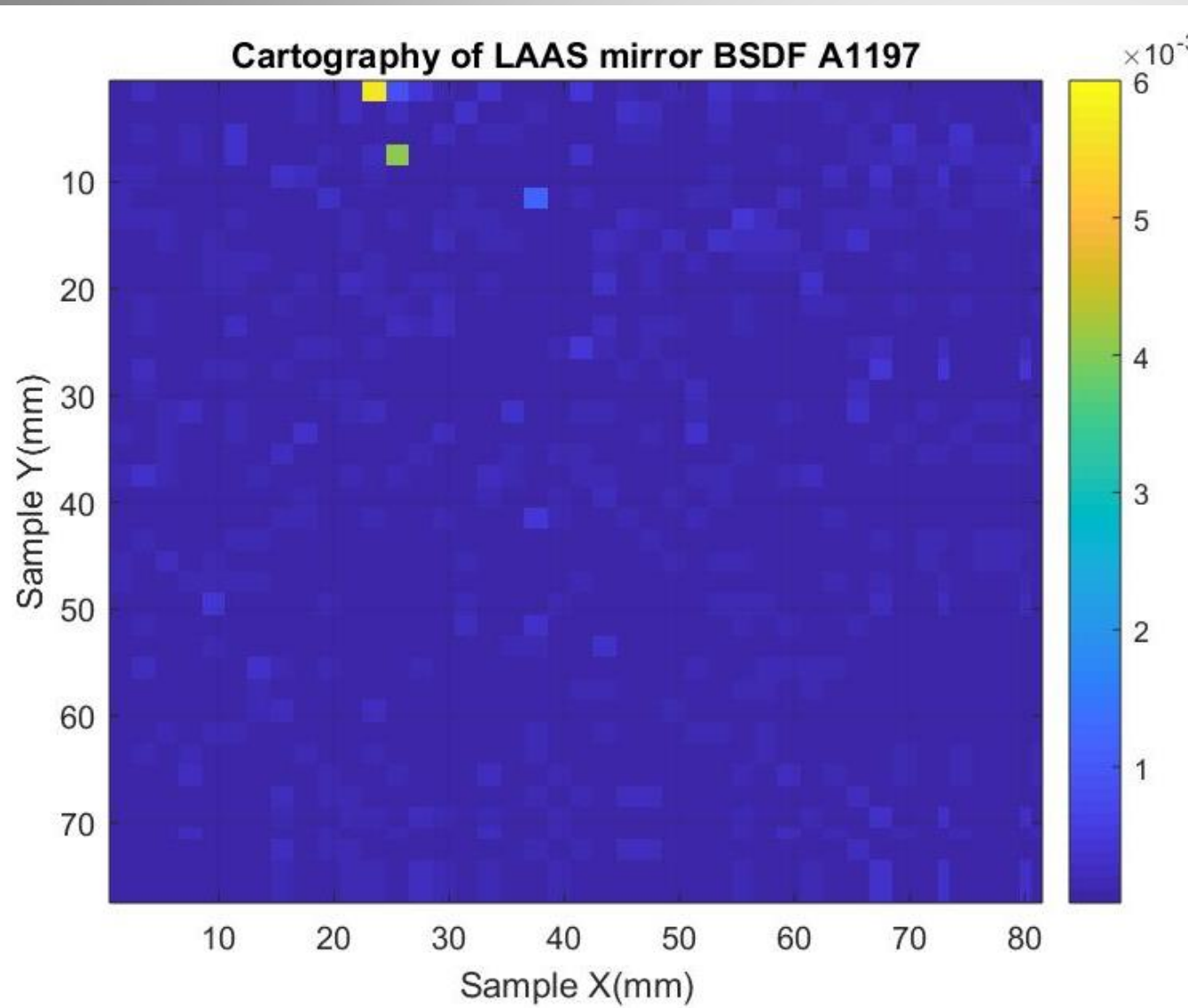
# Characterization at LMA



Mean : 45 ppm

Virgo : 5-10 ppm

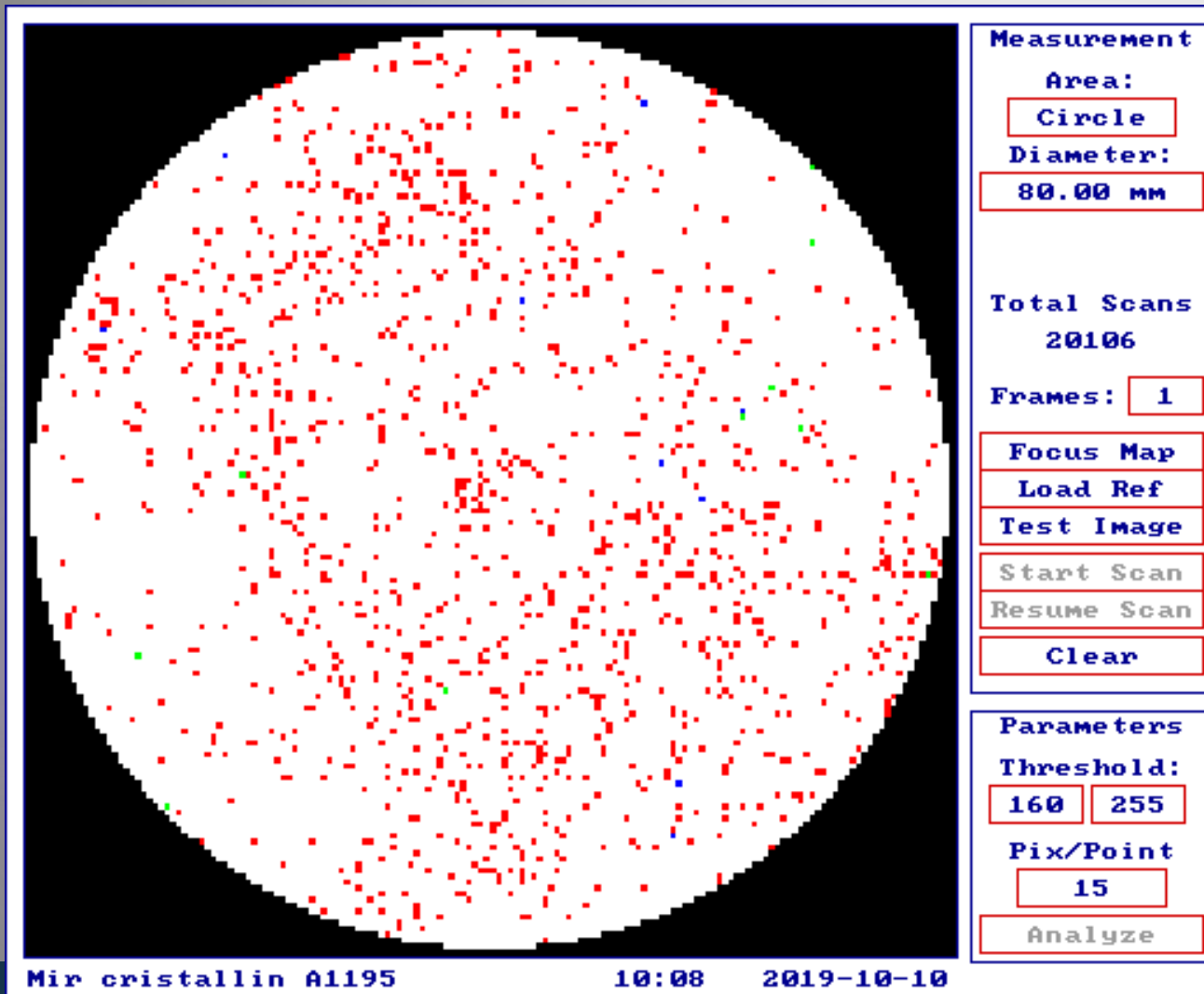
# Characterization at LMA



Mean : 60 ppm

Virgo : 5-10 ppm

# Characterization at LMA



800 defects/cm<sup>2</sup>



# Development of crystalline mirrors

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- ▶ Collaboration between three laboratories
  - ▶ CNRS/LAPP
    - ▶ Thermal noise measurements on optical bench
  - ▶ CEA/LETI
    - ▶ Epitaxy for growth of crystalline coatings, wafer transfer, wafer bondings
  - ▶ CNRS/LMA
    - ▶ Optical characterizations on crystalline mirrors

**leti**  
cea tech



Pré



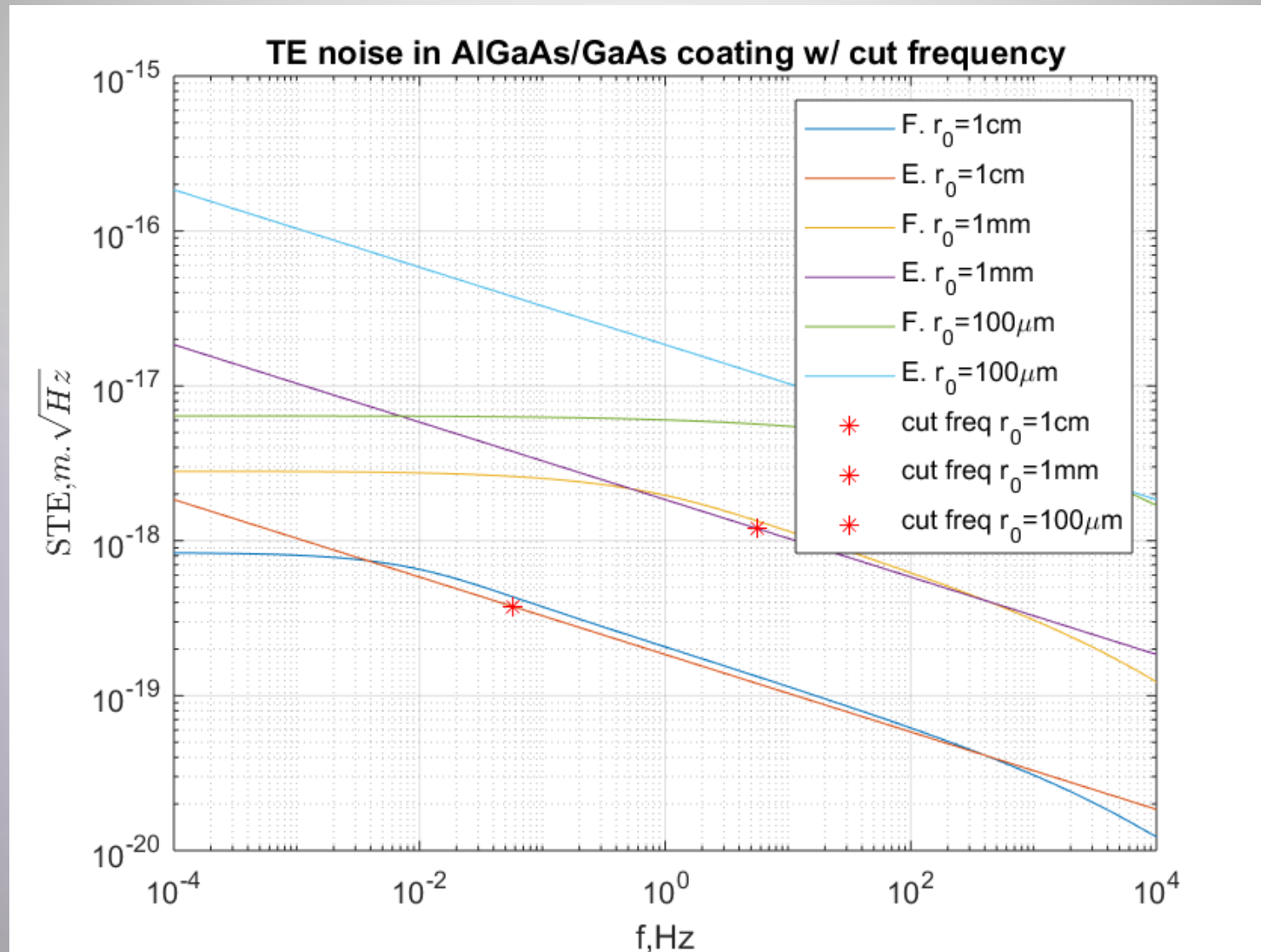
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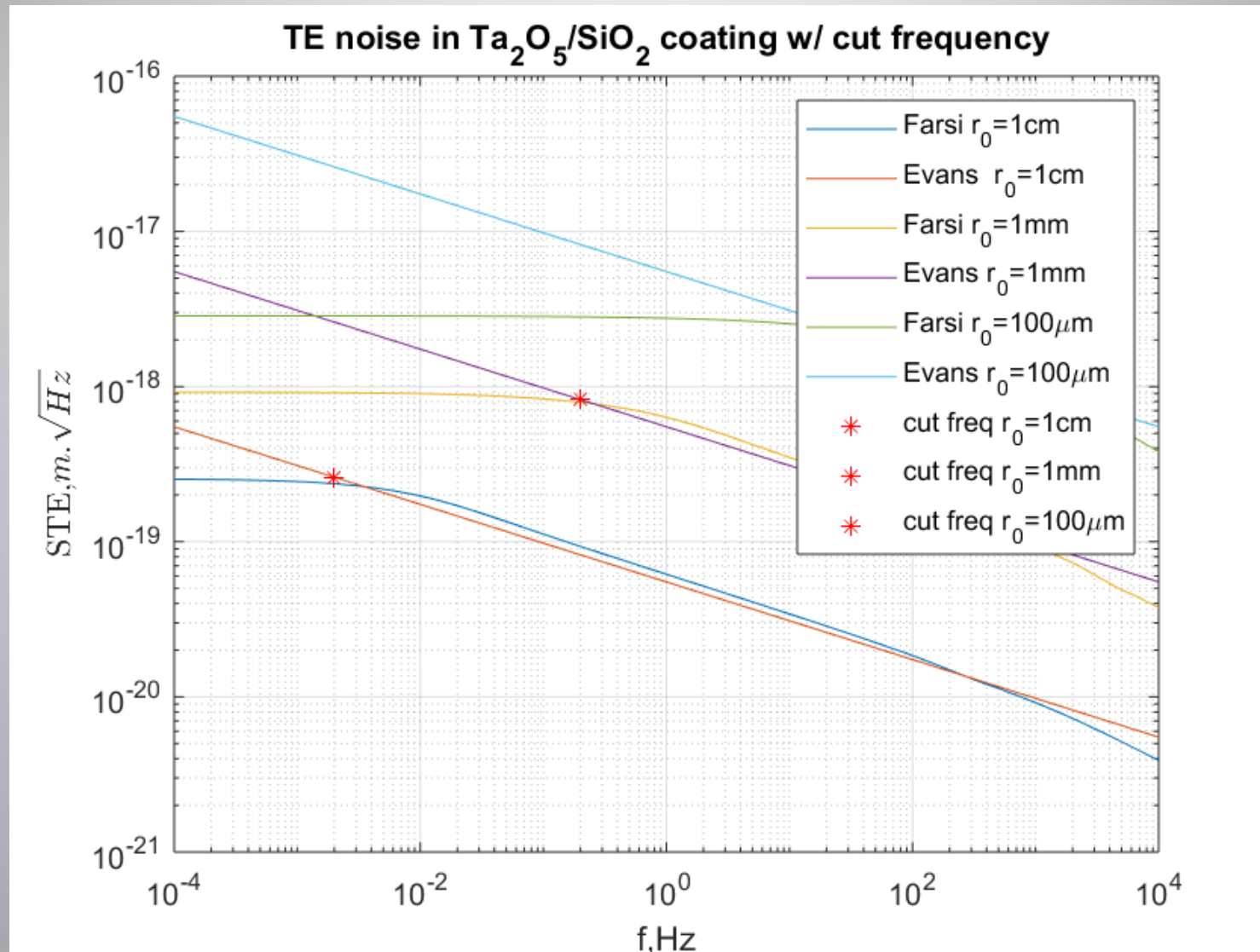
Thank you for your  
attention!

# Back-up slides

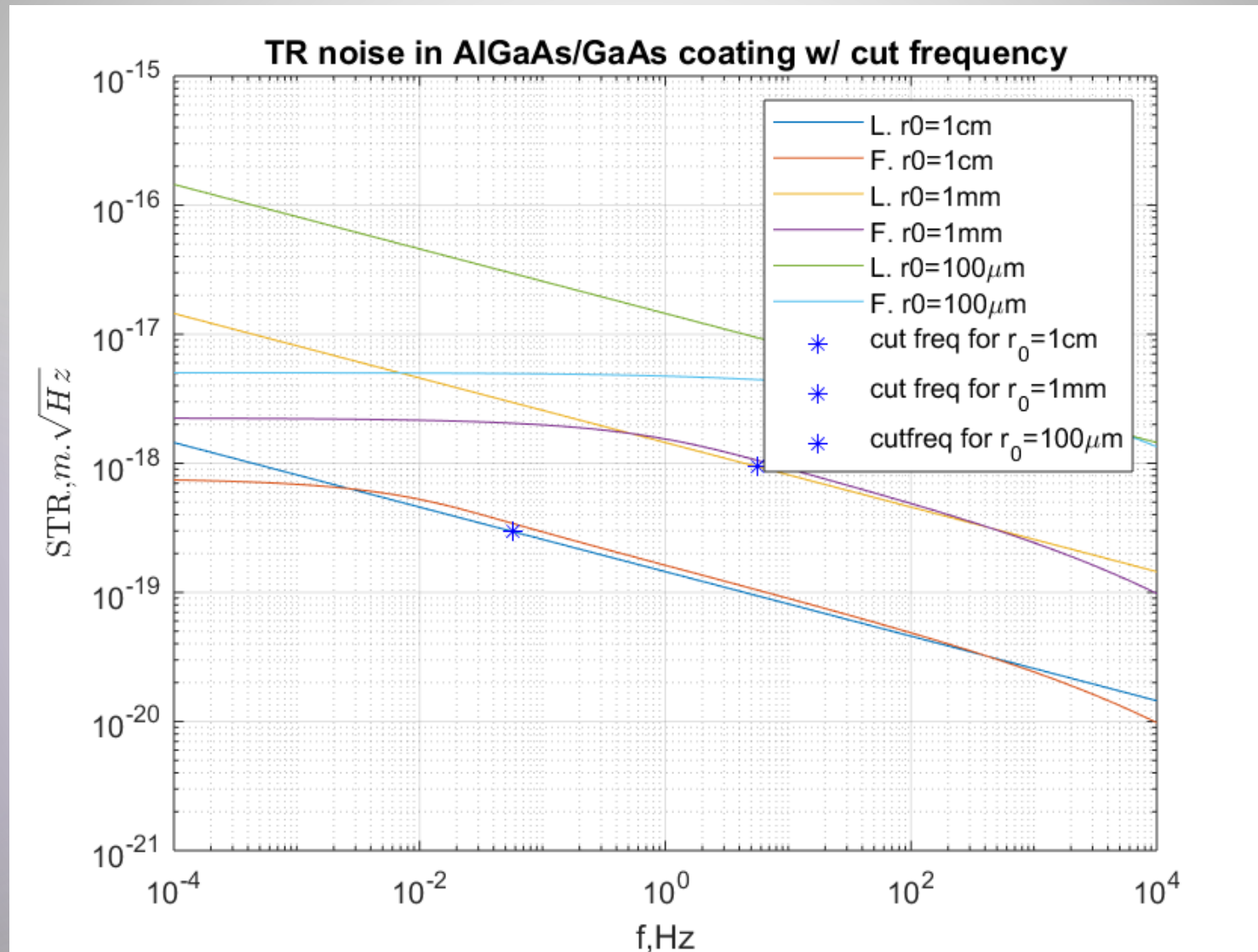
# Thermal noise model for small beams



# Thermal noise model for small beams



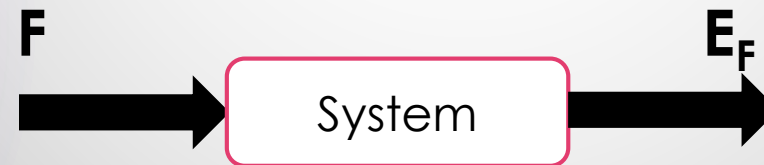
# Thermal noise model for small beams



# Modelizing thermal noise

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- ▶ Fluctuation dissipation theorem  $S_{\Delta T}(\omega) \propto \text{Re}(Z(\omega))$
- ▶ In a linear system, fluctuation of a observable is linked to the amplitude of its dissipation
- ▶ Injecting a force  $F$  and we study the energy dissipated by this force

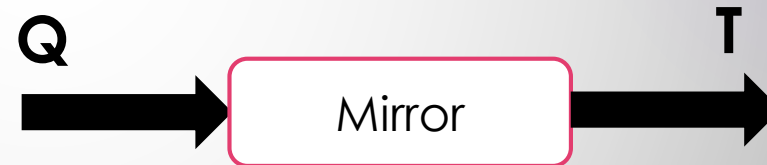


# Modelizing thermal noise

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- ▶ Application to the thermal noise
- ▶ Injection of Entropy and study of the temperature dissipation

$$S_{\Delta T}(\omega) \propto P_{diss}(T(z, t))$$

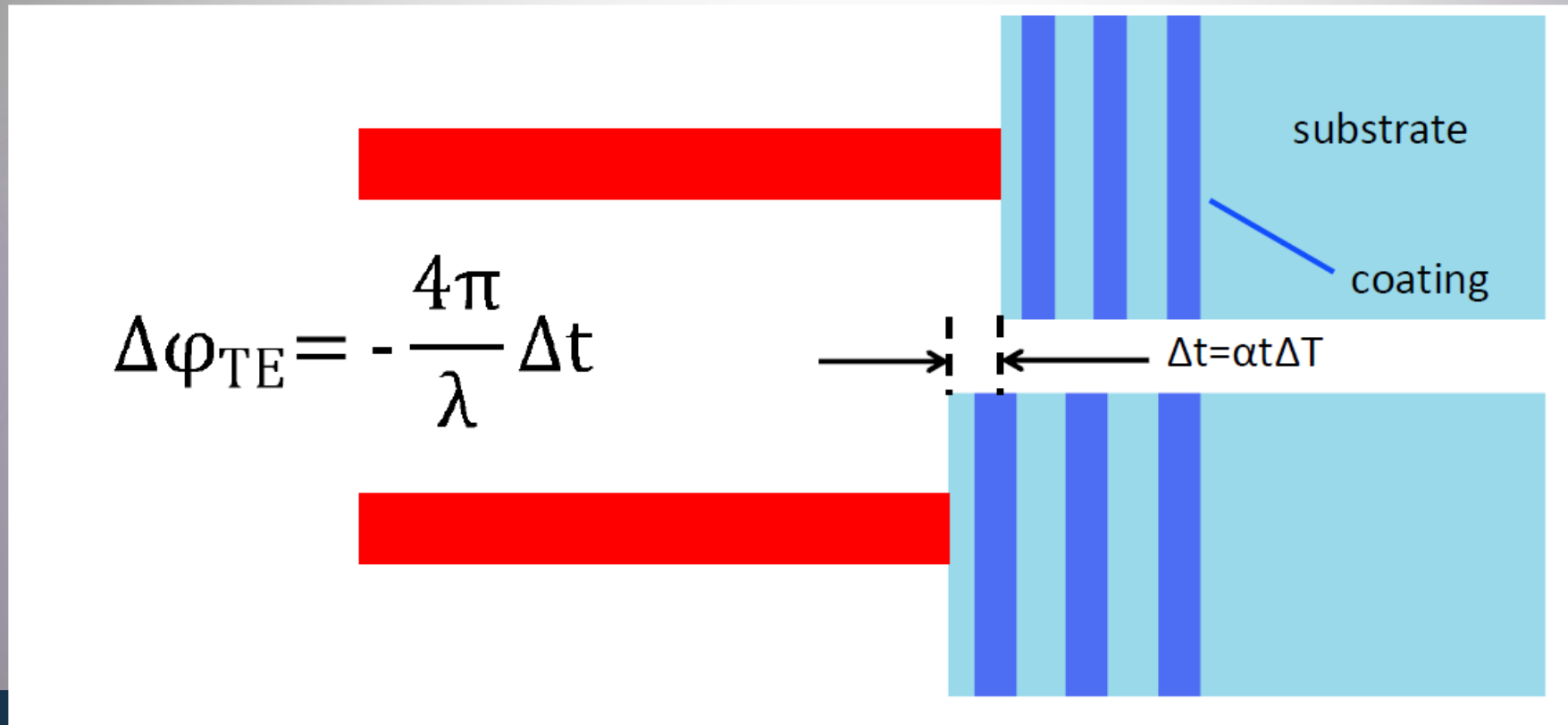


- ▶ Temperature dissipation given by the diffusion equation
- ▶ Boundary conditions given by the study of how the light is reflected

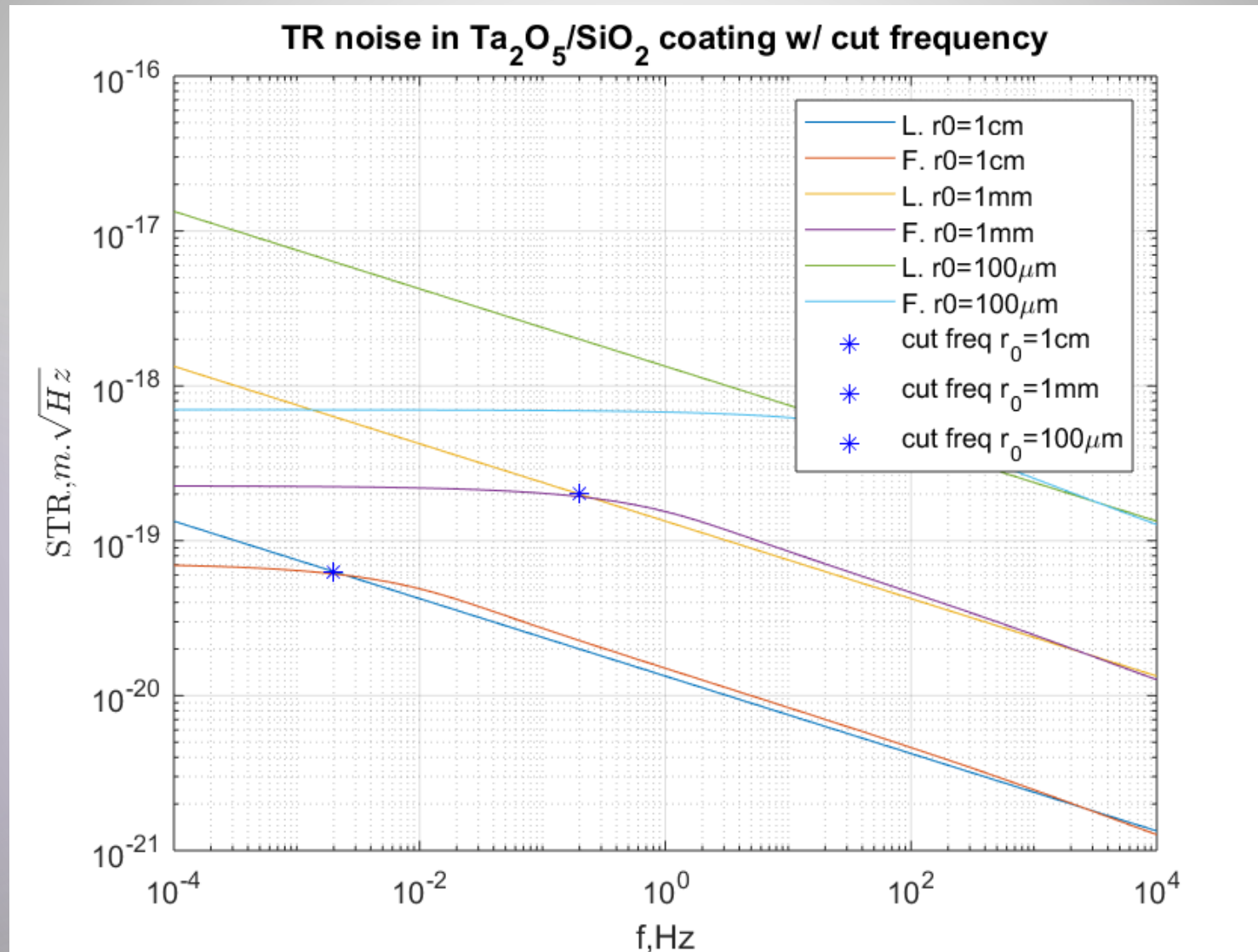


# Back up

- ▶ Thermoelastic noise is the apparent expansion of the mirror coating into the probe beam causing change in phase



# Thermal noise model for small beams



# Research areas

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- ▶ Collaboration with CEA Leti
  - ▶ Design of crystalline coatings
  - ▶ Evaluation of substrate surface state
  - ▶ Epitaxy (crystalline growth from crystalline substrate GaAs)
  - ▶ Transfer techniques to separate the coating from the substrate and then bonding with silica substrate
- ▶ Collaboration with LMA
  - ▶ Optical measurements (diffusivity, reflectivity, defects...)