

# A PROPOSAL FOR THE CFT DUAL OF ADS3 AT THE STRING SCALE

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AND

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IN COLLABORATION WITH G. GIRIBET, C. HULL,  
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- REVIEW OF THE PERTURBATIVE ADS3 STRING SPECTRUM
- ADS3 AT THE STRING SCALE  $\alpha' = L^2$
- THE FATE OF THE VACUUM
- A PHASE TRANSITION AT  $\alpha' = L^2$ ?
- THE FULL NON-PERTURBATIVE LONG STRING SPECTRUM AT  $\alpha' = L^2$ ?
- AN EXACT CFT DUAL FOR THE LONG STRING SPECTRUM?
- WHAT ABOUT SHORT STRINGS, SPECTRAL DENSITY, INTERACTIONS ETC.?
- A TENTATIVE ANSWER INSTEAD OF A CONCLUSION

# PERTURBATIVE SPECTRUM OF ADS3 STRINGS (WZW, N=1)

## WORLD-SHEET SIGMA MODEL

$$SL(2, R)_{k+2} \times SL(2, R)_{-2} \times \mathcal{N}$$

BOSONIC AFFINE  
ALGEBRA  $c=3+6/k$

3 FREE  
FERMIONS  
 $c=3/2$

$$c=15-9/2-6/k$$

THE SIGMA MODEL IS EXACT TO ALL ORDERS IN  $\alpha'$

IT IS VALID EVEN WHEN  $k = L^2/\alpha'$  IS SMALL

SINCE  $L_P/L \sim g_S^2$ , THIS IS WHEN THE ADS3 RADIUS IS OF  
ORDER OF THE STRING SCALE, BUT STILL MUCH LARGER  
THAN THE PLANCK SCALE, FOR WEAKLY-COUPLED STRINGS

# PERTURBATIVE SPECTRUM OF ADS3

## STRINGS (WZW, N=1)

UNFLOWED REPRESENTATIONS ARE AFFINE ALGEBRA  
DESCENDANTS OF AFFINE PRIMARIES

NEW REPRESENTATIONS OBTAINED BY DEFINING:

$$J_n^3 = \tilde{J}_n^3 + \frac{k}{2} w \delta_{n,0}, \quad J_n^\pm = \tilde{J}_{n \mp w}^\pm, \quad L_n = \tilde{L}_n - w \tilde{J}_n^3 - \frac{k}{4} w^2 \delta_{n,0}$$

THE (STANDARD) **TILDED** REPRESENTATION DEFINES A  
**FLOWED** REPRESENTATION OF THE (NON-TILDED) ALGEBRA

THE AFFINE PRIMARIES CAN BELONG TO EITHER LOWEST-  
WEIGHT OR PRINCIPAL CONTINUOUS REPRESENTATIONS  
OF SL(2,R)

# THE PERTURBATIVE STRING SPECTRUM IS MADE OF THE FOLLOWING REPRESENTATIONS

1) LOWEST-WEIGHT REPRESENTATIONS OF THE BOSONIC AFFINE ALGEBRA:

DISCRETE REPRESENTATION

$\mathcal{D}_j$

$\mathcal{C}_{j=1/2+is}^\alpha$

CONTINUOUS REPRESENTATION

2) REPRESENTATIONS OF THE FERMIONIC AFFINE ALGEBRA:

FOCK SPACE OF THE THREE FREE FERMIONS, WITH EITHER NS OR R BOUNDARY CONDITIONS

REPEAT FOR LEFT MOVERS

3) ALL THE REPRESENTATIONS OBTAINED BY LEFT-RIGHT SYMMETRIC SPECTRAL FLOW ( $w$ =INTEGER) OF THE ABOVE

THE PHYSICAL STATE CONDITION IN THE NS SECTOR IS

$$L_0 - 1/2 = 0 \rightarrow \tilde{L}_0 - wJ_0 + kw^2/4 - 1/2 = 0$$

IN THE R SECTOR IT IS

$$L_0 = 0 \rightarrow \tilde{L}_0 - wJ_0 + kw^2/4 = 0$$

THE TILDED VARIABLES ARE VIRASORO GENERATORS OBTAINED BY THE STANDARD SUGAWARA CONSTRUCTION OUT OF TILDED CURRENTS.

THE REPRESENTATIONS OF THE TILDED CURRENTS ARE STANDARD LOWEST-WEIGHT REPRESENTATIONS OF THE AFFINE ALGEBRA. SO:

$$\tilde{L}_0 = -\frac{j(j-1)}{k} + N + h$$

THE SPACE-TIME ENERGY AND SPIN OF STRING STATES ARE

$$E = J_0^3 + \bar{J}_0^3, \quad s = J_0^3 - \bar{J}_0^3$$

$$\tilde{L}_0 = -\frac{j(j-1)}{k} + N + h$$

CONFORMAL WEIGHT IN  $\mathcal{N}$

LEVEL IN CURRENT ALGEBRA

$$N = \frac{1}{k} \left[ \sum_{m=1}^{\infty} j_{-m}^+ j_m^- + j_{-m}^- j_m^+ - 2j_{-m}^3 j_m^3 + \sum_{r>0} r (\psi_{-r}^+ \psi_r^- + \psi_{-r}^- \psi_r^+ - 2\psi_r^3 \psi_r^3) \right]$$

THE GSO PROJECTION DOES NOT ELIMINATE ANY  
CONFORMAL WEIGHT IN THE R SECTOR.  
IN THE NS SECTOR IT DOES BECAUSE IT SAYS

$$N + N_{\mathcal{N}} + (w + 1)/2 \in \mathbb{Z}$$

THE  $SL(2, \mathbb{C})$  INVARIANT VACUUM OF THE TARGET SPACE  
BELONGS TO THE  $j=1$  REPRESENTATION

MALDACENA AND OOGURI SHOWED THAT A MODULAR-INVARIANT, UNITARY STRING THEORY IS OBTAINED BY PERFORMING A SPECTRAL FLOW, WITH ARBITRARY INTEGER  $w$ ,

OF ALL THE PRINCIPAL CONTINUOUS REPRESENTATIONS BUT ONLY THE DISCRETE REPRESENTATIONS OBEYING

$$1/2 < j < (k+1)/2$$

WHEN  $k < 1$  THE SPACE-TIME VACUUM DOES NOT BELONG TO THE PHYSICAL SPECTRUM. BECAUSE OF MODULAR INVARIANCE OF DUAL CFT (CARDY'S FORMULA) BTZ CANNOT BE PART OF THE SPECTRUM EITHER.

THESE FEATURES AND THE BEHAVIOR OF THE COUPLING TO THE DILATON IN THE EFFECTIVE THEORY OF LONG STRINGS LED GIVEON, KUTASOV, RABINOVICI AND SEVER TO CONJECTURE IN [hep-th/0503121](https://arxiv.org/abs/hep-th/0503121) THAT STRING ON ADS3 UNDERGO A PHASE TRANSITION AT  $k=1$

$k=1$  CORRESPONDS PHYSICALLY TO AN ADS3 RADIUS

$$\alpha' = L^2$$

GKRS PROPOSE THAT AT  $k < 1$  THE SPECTRUM OF STRING THEORY IS DOMINATED AT HIGH ENERGY BY WEAKLY INTERACTING LONG STRINGS INSTEAD OF BTZ BLACK HOLES. IN SUCH A REGIME, THE DENSITY OF STATES OBEYS CARDY'S FORMULA BUT WITH AN EFFECTIVE CENTRAL CHARGE

$$c_{eff} = c \left[ 1 - \frac{(k-1)^2}{k^2} \right] \leq c$$

UNITARITY OF WORLD-SHEET CFT CONSTRAINS  $k \geq \frac{4}{7}$

$k=1$  APPEARS TO BE A PHASE TRANSITION POINT  
SEVERAL INTERESTING FACTS POINT TOWARD IT:

- THE CONTINUOUS SPECTRUM OF LONG STRINGS BECOMES GAPLESS AND ITS EFFECTIVE WORLD-SHEET CFT REDUCES TO THAT OF A FREE BOSON.
- THE EFFECTIVE COUPLING CONSTANT OF THE LONG-STRING WORLD-SHEET CFT SWITCHES FROM DIVERGING AT THE BOUNDARY OF ADS3 TO VANISHING. AT  $k=1$  IT IS CONSTANT THROUGHOUT ADS3
- THE SPACE-TIME VACUUM IS NO LONGER NORMALIZABLE BUT ONLY PLANE-WAVE NORMALIZABLE. IT BECOMES PART OF THE CONTINUUM.

- BTZ STATES MUST ALSO BECOME ONLY PLANE-WAVE NORMALIZABLE AND PART OF A CONTINUUM.
- THE CENTRAL CHARGE OF THE (PUTATIVE) DUAL CFT BECOMES EQUAL TO THE EFFECTIVE CENTRAL CHARGE COMPUTED BY ASSUMING THAT THE SPECTRUM IS DOMINATED AT HIGH ENERGY BY A GAS OF FREE LONG STRINGS INSTEAD OF BTZ BLACK-HOLE MICROSTATES.

ALL THESE FACTS MAKE IT PLAUSIBLE THAT THE **NONPERTURBATIVE** SPECTRUM OF STRING THEORY AT  $k=1$  (THAT IS AT THE STRING RADIUS) IS MADE ONLY OF THE (PERTURBATIVE) STATES OF MALDACENA AND OOGURI.

THE EXACT KNOWLEDGE OF THE STRING SPECTRUM MAKES IT MAY BE POSSIBLE TO CONJECTURE A CFT DUAL OF SUPERSTRINGS AT  $k=1$  THAT DESCRIBES (MOST OF) THE COMPLETE THEORY RATHER THAN JUST THE BPS SECTOR

# THE SPECTRUM OF LONG STRINGS IN ADS3

$$(E + S)/2 = \frac{1}{w} \left( s^2 + N + N_{\mathcal{N}} + h_0 + \frac{a}{2} \right) + \frac{1}{4} \left( w - \frac{1}{w} \right)$$

$$(E - S)/2 = \frac{1}{w} \left( s^2 + \bar{N} + \bar{N}_{\mathcal{N}} + \bar{h}_0 + \frac{b}{2} \right) + \frac{1}{4} \left( w - \frac{1}{w} \right)$$

SUBJECT TO THE CONSTRAINT

$$N + N_{\mathcal{N}} + h_0 + \frac{a}{2} - \bar{N} - \bar{N}_{\mathcal{N}} - \bar{h}_0 - \frac{b}{2} \in w \left( \mathbb{Z} + \frac{a}{2} - \frac{b}{2} \right)$$

**a,b=0** IN NS SECTOR, **1** IN R SECTOR

THIS IS THE SPECTRUM OF ONE-PARTICLE STATES. FOR SMALL STRING COUPLING CONSTANT  $g$ , THE SPECTRUM OF THE THEORY IS OBTAINED BY TENSORING ONE-PARTICLE STATES AND EITHER SYMMETRIZING OR ANTISYMMETRIZING ACCORDING TO THE SPACE-TIME STATISTICS OF THE PARTICLES

THE MULTIPLICITY OF ONE-PARTICLE STATES OBEYING THE PHYSICAL-STATE AND AUXILIARY CONDITIONS CAN BE FOUND BY THE METHOD USED BY MALDACENA AND OOGURI IN THE BOSONIC CASE

MALDACENA AND OOGURI SHOW THAT PHYSICAL STATES ARE IN ONE-TO-ONE CORRESPONDENCE WITH THE FOCK STATES OF ONE FREE BOSON

THE SUPERSYMMETRIC EXTENSION OF THEIR RESULT IS THAT PHYSICAL SUPERSTRING STATES IN ADS3 MAP ONE-TO-ONE TO STATES IN THE FOCK SPACE OF ONE FREE BOSON PLUS ONE FREE FERMION

# A PROPOSAL FOR A DUAL CFT

RELATED TO WORK BY ARGURIO, GIVEON, SHOMER,  
GABERDIEL, GOPAKUMAR, EBERHARDT

ASSUME THAT WE KNOW INDEED THE COMPLETE,  
NONPERTURBATIVE SPECTRUM AT  $k=1$ .

WE CAN THEN CONJECTURE A DUAL THAT REPRODUCES THE  
FULL LONG STRING SPECTRUM

WE PROPOSE THAT THE FULL LONG-STRING SPECTRUM OF  
STRING THEORY AT  $k=1$  ON

$$AdS_3 \times \mathcal{N}$$

IS GIVEN BY THE PERMUTATION ORBIFOLD

$$(\mathbb{R} \times \mathcal{N})^N / S_N$$

THE STRING COUPLING CONSTANT AND THE NUMBER OF  
COPIES OF THE SEED THEORY ARE RELATED BY

$$g_S^2 = 1/N$$

TO BE PRECISE, WE WILL SHOW THAT THE PERMUTATION ORBIFOLD CFT EXACTLY MATCHES THE LONG-STRING SPECTRUM WHEN THE INTERNAL CFT IS

$$\mathcal{N} = S^1 \times SU(2)_2 \times SU(2)_2 = S^1 \times S^3 \times S^3$$

| FREE BOSON + (1+3+3) FREE FERMIONS:  $c=9/2$

THE TWISTED SECTORS OF THE ORBIFOLD ARE LABELED BY THE CONJUGACY CLASSES OF THE PERMUTATION GROUP OF  $N$  ELEMENTS. THESE ARE ASSOCIATED TO PARTITIONS OF  $N$  INTO POSITIVE INTEGERS

$$[g] = (1)^{M_1} (2)^{M_2} \dots (N)^{M_N}, \quad \sum_{i=1}^N n M_n = N$$

THE HILBERT SPACE OF THE TWISTED SECTOR  $[g]$  IS THE INVARIANT SUBSPACE OF THE COMMUTANT OF  $[g]$

$$H_g^C = \bigotimes_{n=1}^N S^{M_n} H_{(n)}^{Z_n}$$

## FIRST CHECK OF THE CORRESPONDENCE

WE MAP A STATE CONTAINING

$$(M_1, M_2, \dots, M_N)$$

LONG STRINGS WITH WINDING NUMBERS  $w=1,2,\dots,N$

INTO THE HILBERT SPACE OF THE TWISTED SECTOR  $[g]$

THE (ANTI)SYMMETRIZATION IN THE ORBIFOLD AGREES  
PRECISELY WITH THE (ANTI)SYMMETRIZATION OF MULTI-  
STRING STATES DICTATED BY SPIN-STATISTICS

## A MORE DETAILED CHECK

THE SPECTRUM OF SINGLE-PARTICLE STATES IN THE LONG-  
STRING SECTOR AT WINDING NUMBER  $w=n$  MATCHES  
WITH

$$H_{(n)}^{Z_n}$$

# TWISTED SECTOR ( $n$ ): MAPS FROM WORLDSHEET

$$\mathbb{R} \times S^1, \quad (\sigma, t) \sim (\sigma + \pi, t)$$

TO TARGET SPACE  $(\mathbb{R} \times \mathcal{N})^N / S_N$

$$X_j(\sigma + \pi) = X_{j+1}(\sigma), \quad \psi_j(\sigma + \pi) = -\psi_{j+1}(\sigma), \quad j + n \equiv j$$

FOR  $n$  ODD FERMIONS ARE NS, FOR  $n$  EVEN THEY ARE R

THE MAP IS FROM A CIRCLE  $n$  TIMES LONGER THAN THE WORLDSHEET CIRCLE SO THE CONFORMAL WEIGHTS ARE

$$h_n = \frac{h}{n} + \frac{c}{24} \left( n - \frac{1}{n} \right) \leftarrow \text{CASIMIR ENERGY}$$

NOTICE THAT FOR  $n$  EVEN THE MINIMUM WEIGHT IS  $h=d/16$ , THE ENERGY OF THE R VACUUM OF  $d$  FERMIONS.

IN OUR CASE  $d=8$  SO  $h=1/2$

THE CONFORMAL WEIGHTS IN OUR ORBIFOLD ARE

$$h_n = \frac{1}{n} \left( \frac{1}{2} p^2 + N + N_{\mathcal{N}} + h_0 \right) + \frac{1}{4} \left( n - \frac{1}{n} \right)$$
$$\bar{h}_n = \frac{1}{n} \left( \frac{1}{2} p^2 + \bar{N} + \bar{N}_{\mathcal{N}} + \bar{h}_0 \right) + \frac{1}{4} \left( n - \frac{1}{n} \right)$$

THEY ARE EVIDENTLY VERY SIMILAR TO THE SPACE-TIME CONFORMAL WEIGHT IN **ADS3** IN FACT THEY ARE IDENTICAL ONCE THE PROJECTION OVER INVARIANT STATE OF THE ORBIFOLD IS TAKEN INTO PROPER ACCOUNT

IT IS STRAIGHTFORWARD TO SHOW THAT THE PROJECTION OVER  $\mathbb{Z}_n$  INVARIANT STATES IS

$$N + N_{\mathcal{N}} + h_0 - \bar{N} - \bar{N}_{\mathcal{N}} - \bar{h}_0 \in n(\mathbb{Z} + F/2 + \bar{F}/2)$$

## WITH THE IDENTIFICATIONS

$$p = \sqrt{2}s, \quad n = w$$

THE SPECTRUM AND MULTIPLICITIES OF STATES OF THE ORBIFOLD MATCHES EXACTLY THAT OF THE LONG STRINGS IF THE ORBIFOLD CONSTRAINT

$$N + N_{\mathcal{N}} + h_0 - \bar{N} - \bar{N}_{\mathcal{N}} - \bar{h}_0 \in n(\mathbb{Z} + F/2 + \bar{F}/2)$$

IS EQUIVALENT TO THE ADS3 STRING CONSTRAINTS

$$N + N_{\mathcal{N}} + (w + 1)/2 \in \mathbb{Z}$$

$$N + N_{\mathcal{N}} + h_0 + \frac{a}{2} - \bar{N} - \bar{N}_{\mathcal{N}} - \bar{h}_0 - \frac{b}{2} \in w \left( \mathbb{Z} + \frac{a}{2} - \frac{b}{2} \right)$$

TO PROVE THIS WE MUST DISTINGUISH TWO CASES:

**n** ODD AND **n** EVEN

**n** ODD

THE FERMIONS OF THE SYMMETRIC ORBIFOLD ARE IN THE NS SECTOR SO THEIR GROUND STATE IS UNIQUE AND HAS ZERO ENERGY

EVEN NUMBER OF ORBIFOLD FERMIONS MAPS ONE-TO-ONE TO FULL NS SECTOR OF THE SUPERSTRING

$$d_{-1/2-m}^I d_{-1/2-n}^J |0\rangle_O \Leftrightarrow \psi_{-1/2-m}^I \psi_{-1/2-n}^J |0\rangle_S$$

THANKS TO THE GSO PROJECTION OF THE SUPERSTRING

$$(-1)^F = (-1)^{n+1} = 1 = (-1)^{\bar{F}}$$

ODD NUMBER OF ORBIFOLD FERMIONS MAPS ONE-TO-ONE TO R SECTOR OF THE SUPERSTRING

**n** ODD

$$d_{-1/2-m}^I d_{+1/2-n}^J d_{-1/2}^K |0\rangle_O \Leftrightarrow \psi_{-m}^I \psi_{-n}^J |K\rangle_S, \quad |K\rangle_S = \delta_s, \quad m > n \text{ or } m = n, \quad I > J$$

BY SO(8) TRIALITY

WITH THESE IDENTIFICATIONS, THE ORBIFOLD PROJECTION  
OVER  $Z_n$  INVARIANT STATES AND THE LEFT-RIGHT LEVEL  
MATCHING CONDITION OF THE SUPERSTRING COINCIDE

**n EVEN**

ORBIFOLD FERMIONS ARE IN THE R SECTOR  
WHEN THE SUPERSTRING FERMIONS ARE IN THE R SECTOR  
IDENTIFY

$$|\alpha\rangle_S = |\alpha\rangle_O, \quad d_{-n}^I = \psi_{-n}^I$$

THE ORBIFOLD IS NOT GSO PROJECTED SO AT EACH LEVEL IT  
HAS TWICE THE NUMBER OF STATES OF THE NS SECTOR OF  
THE SUPERSTRING

THE EXTRA STATES MATCH THE NS-SECTOR SUPERSYMMETRIC  
PARTNERS OF THE R-SECTOR SUPERSTRING STATES

AGAIN, WITH THESE IDENTIFICATIONS, THE ORBIFOLD  
PROJECTION OVER  $Z_n$  INVARIANT STATES AND THE  
LEFT-RIGHT LEVEL MATCHING CONDITION OF THE  
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WHILE THE SHORT STRING DIMENSION DEPENDS ON THE WINDING **w** AS (MALDACENA OOGURI)

$$h_w = q + w + \frac{1}{2} + \sqrt{\frac{1}{4} + k \left( h - 1 + N_w - \frac{1}{2}w(w + 1) \right)}$$

# SHORT STRINGS AND INTERACTIONS

- CAN WE NEGLECT SHORT STRING?
- ALWAYS? OR ONLY FOR SOME DYNAMICAL PROCESS?
- DO WE EVEN GET THE RANGE OF  $p$  RIGHT?
- DO WE GET THE RIGHT SPECTRAL MEASURE FOR THE CONTINUOUS SPECTRUM?
- CAN WE MATCH THREE- AND HIGHER POINT CORRELATION FUNCTIONS BETWEEN ORBIFOLD AND ADS3 SUPERSTRING?

# CAN WE NEGLECT SHORT STRINGS?

IN SOME OBSERVABLES, YES, BECAUSE THEY HAVE A DISCRETE SPECTRUM AND THE CONTINUUM BEGINS AT ZERO ENERGY

EXAMPLE: CANONICAL PARTITION FUNCTION

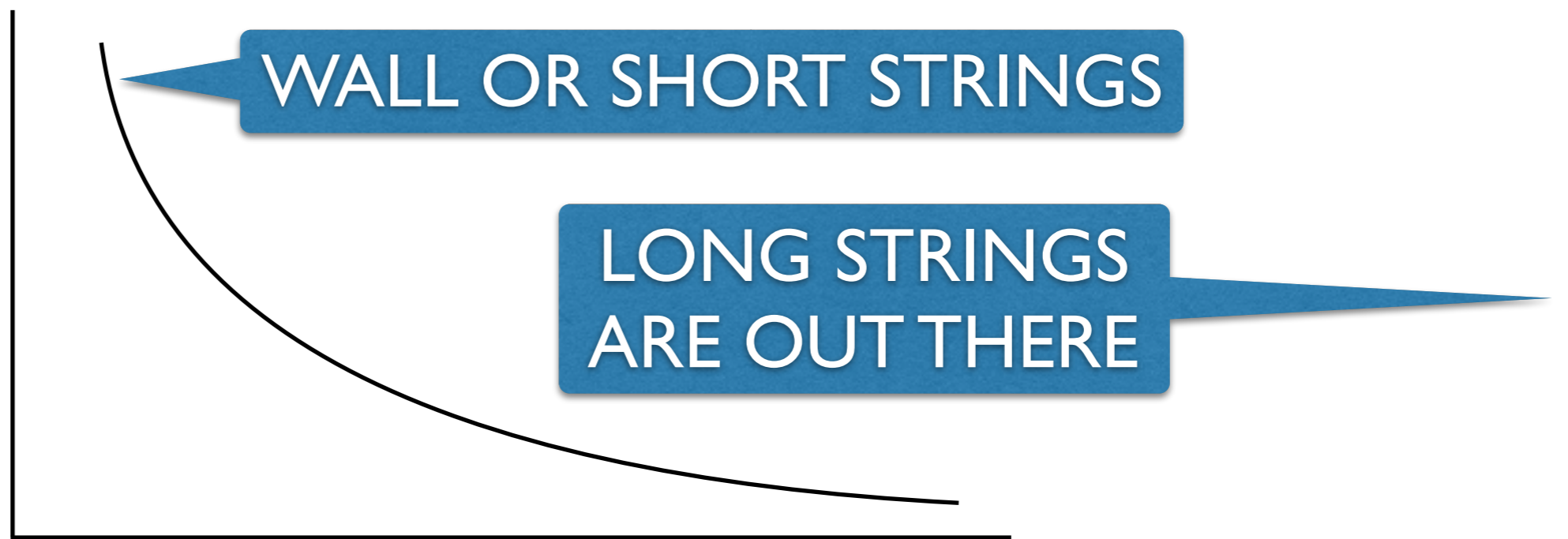
$$\exp(-\beta F) = \lim_{L \rightarrow \infty} L \int dE \rho(E) \exp(-\beta E) + \sum_j D_j \exp(-\beta E_j)$$

THIS TERM IS NEGLIGIBLE AT ALL TEMPERATURES BECAUSE  $L$  DIVERGES AND THE SPECTRUM IS GAPLESS

BETTER EXAMPLE: LONG STRINGS NEAR THE BOUNDARY

THEY TAKE INFINITE CFT TIME TO REACH THE BOUNDARY SO THEY BEHAVE AS PARTICLES IN A WALL POTENTIAL

$$\lim_{\rho \rightarrow +\infty} V(\rho) = 0, \quad \lim_{\rho \rightarrow -\infty} V(\rho) = +\infty$$



FINITE-TIME LONG-STRING DYNAMICS IS INSENSITIVE TO THE EXISTENCE OF A WALL OR A SHORT STRING (CONFINED INSIDE ADS3). BOTH ARE AT DISTANCE

$$L \rightarrow +\infty$$

IT TAKES A TIME  $O(2L/v)$   $v$ =RADIAL SPEED OF LONG STRING, TO DETECT THEM.

DYNAMICS FAR FROM THE WALL DEPENDS ONLY ON THE (UNIVERSAL) DIVERGENT PART OF THE SPECTRAL DENSITY

$$d\mu(p) = [L + \delta(p)]dp/2\pi$$

# FAR AWAY FROM THE WALLS LONG-STRING DYNAMICS IS TRANSLATIONALLY INVARIANT

IF WE CAN FIND A LIMIT THAT DECOUPLES THE NEAR-BOUNDARY DYNAMICS OF LONG STRINGS FROM THE DYNAMICS OF SHORT STRINGS IN THE BULK, CORRELATORS OF LONG STRING VERTICES SHOULD VANISH UNLESS THE SUM OF MOMENTA IS ZERO

3-POINT CORRELATORS OF THE CORRESPONDING VERTICES IN STRING THEORY CAN BE COMPUTED

$$\langle V_{p_1} V_{p_2} V_{p_3} \rangle \propto (k - 1)^i \sum_j p_j$$

THE SELECTION RULE IS RECOVERED IN THE DISTRIBUTIONAL SENSE, BUT ONLY IF THE VERTICES ARE **NOT** RENORMALIZED  
AS

$$V_p^R = (k - 1)^{-ip} V_p$$

# PROPOSAL AND CONCLUSIONS

- THE ORBIFOLD CFT DESCRIBES EXACTLY THE DYNAMICS OF LONG STRINGS NEAR THE BOUNDARY OF ADS3
- IT IS SUFFICIENT TO DETERMINE THE THERMODYNAMICS AND FINITE-TIME DYNAMICS OF LONG STRINGS, WHICH ARE BOTH INSENSITIVE TO SHORT STRINGS, TO THE RANGE IN  $p$  AND TO THE FINITE PART OF THE SPECTRAL DENSITY.
- TO GO BEYOND THIS APPROXIMATION WE NEED TO UNDERSTAND INTERACTIONS. THE ORBIFOLD SEEMS TO MATCH THE SUPERSTRINGS IN A SINGULAR LIMIT AT  $k=1$ .
- COMPUTING INTERACTIONS IS NECESSARY TO DISTINGUISH BETWEEN VARIOUS POSSIBILITIES FOR THE CONTINUOUS-SPECTRUM PART OF THE ORBIFOLD CFT:

$\mathbb{R}$ ,  $\mathbb{R}/\mathbb{Z}_2$ , Runkel-Watts  $c = 1$  CFT, **LIOUVILLE**  $c = 1\dots$