

$$S_{\text{part}} = -n \int |A(\phi)| \, \mathrm{d}\tau$$