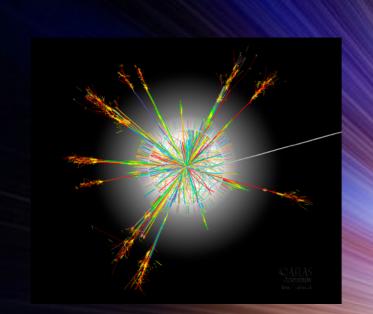
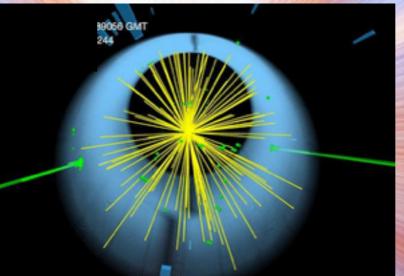
Les expériences du futur : potentiel de physique Avant-propos introductif





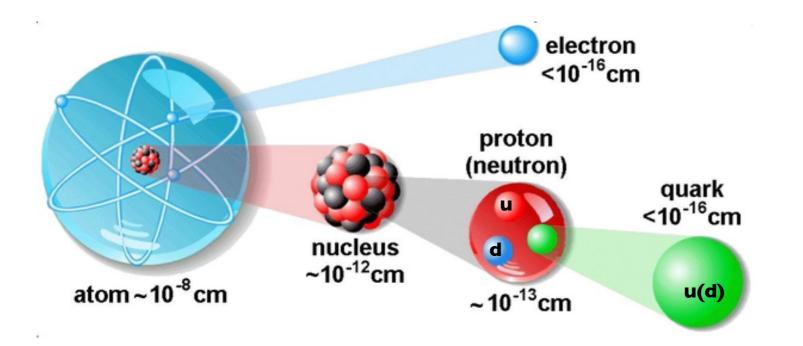




École de Gif 2019 *Questions ouvertes en physique des particules* 2-6 septembre 2019 École polytechnique, Palaiseau

Gautier Hamel de Monchenault

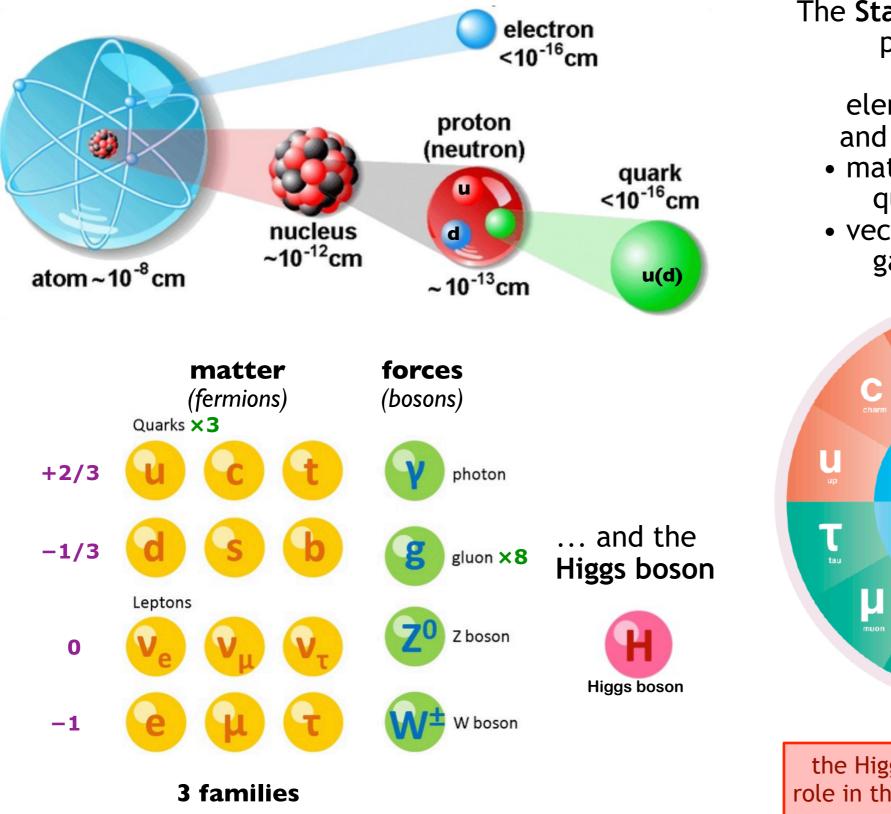
The Standard Model



The **Standard Model** (MS) of particle physics describes les elementary particles and their interactions

- matter particles: quarks and leptons
- vectors of force: gauge bosons

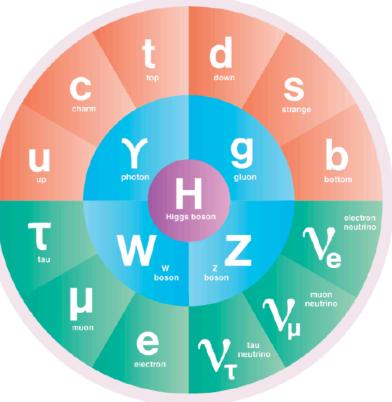
The Standard Model Theory



I2 particles (+ antiparticles)

The **Standard Model** (MS) of particle physics describes les elementary particles and their interactions

- matter particles: quarks and leptons
- vectors of force: gauge bosons



the Higgs boson plays a central role in the SM as it is linked to the origin of mass

The Origin of Mass

The Higgs field ϕ

- its non-zero vacuum expectation value breaks spontaneously the SU(2)_L⊗U(1)_Y symmetry into the U(1)_{EM} symmetry of electromagnetism: massless photon
- it gives massive W and Z bosons
- by connecting left- and right-handed fields, it allows massive fermions

Higgs field = 4 degrees of freedom (ddl) After SSB:

- 3 ddl \rightarrow long. polar. of W⁺, W⁻ and Z bosons
- 1 ddl → Higgs boson

INI⇒ LIFE!

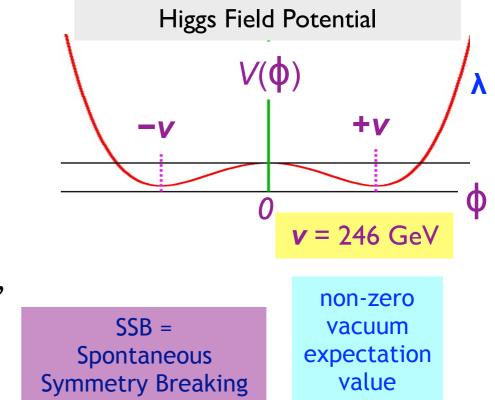
JUANTUM

ACUUM

• Yukawa couplings \rightarrow fermion masses

To be honest, "our" mass comes from QCD but Higgs Yukawa couplings play essential roles:

- mass of the electron \rightarrow atom size \rightarrow chemistry
- $m(d) > m(u) \rightarrow m(neutron > m(proton))$
- m(t) and m(H) \rightarrow stability of the EW vacuum

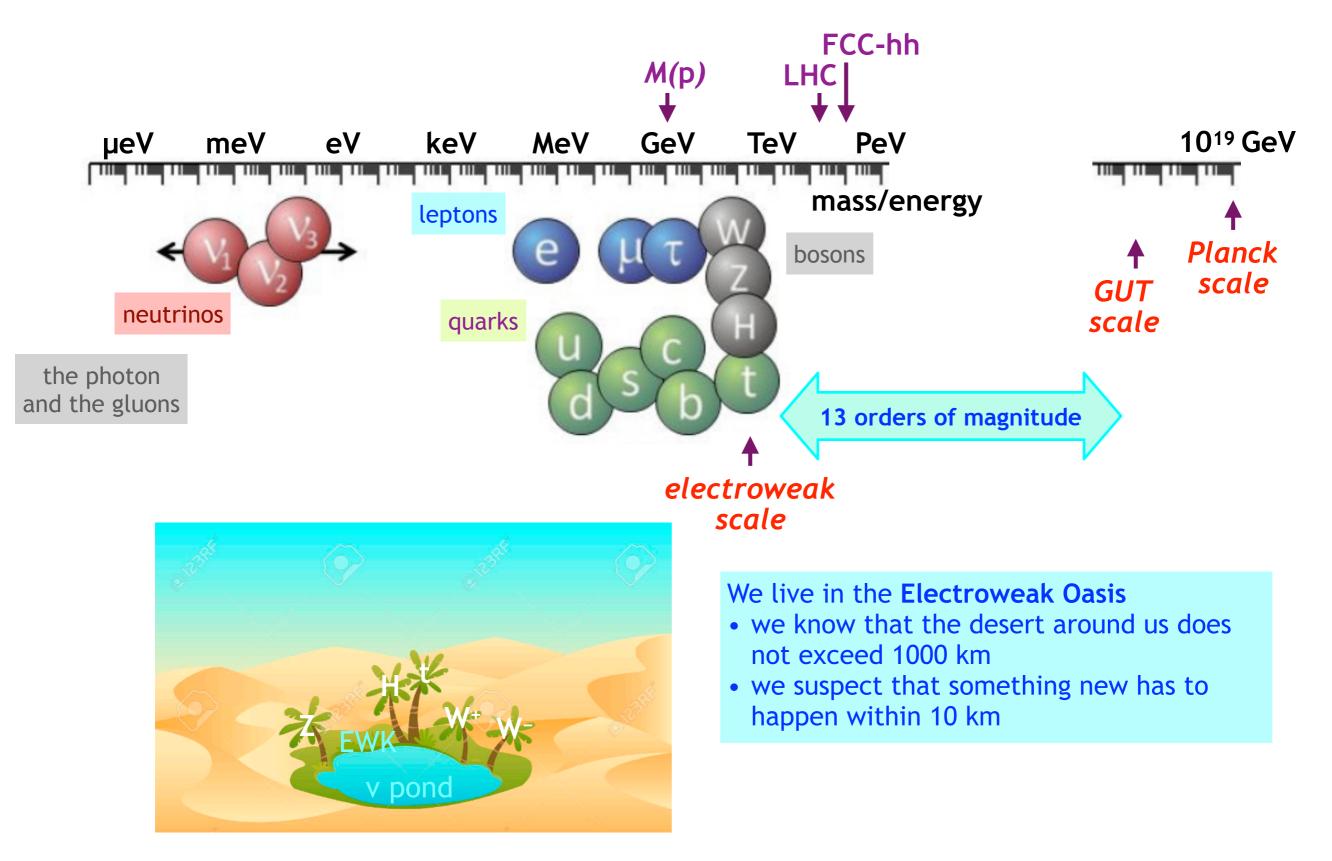




Contribution of quarks to the proton mass <10%

Most of the mass of the proton comes from the binding energy that ensures its cohesion (gluons)

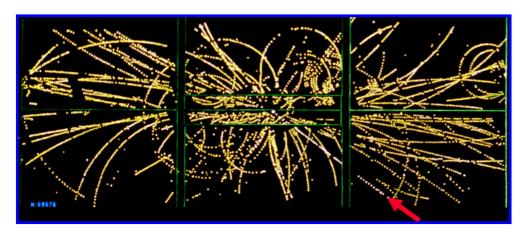
Mass Hierarchy



Three Decades of Discoveries

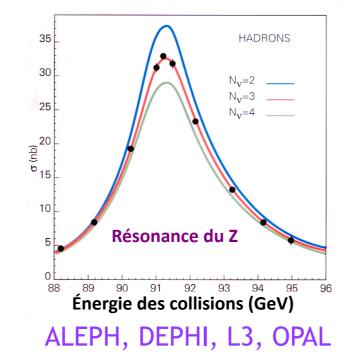
1972 – CERN 1976 – SLAC 1974 – BNL, SLAC 1979 – Fermilab neutral currents charm tau lepton beauty - Muon Trock J/Ψ Yield 177 3.00 3.25 8.2 9.8 10.2 10.6 11.0 11.4 8.6 9.0 94 total energy (GeV) Mass (GeV)



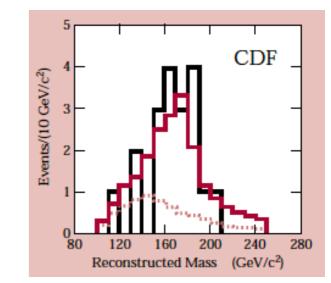


UA1, UA2

1990 — CERN/LEP 3 families of neutrinos



1994 — Fermilab/TeVatron top quark

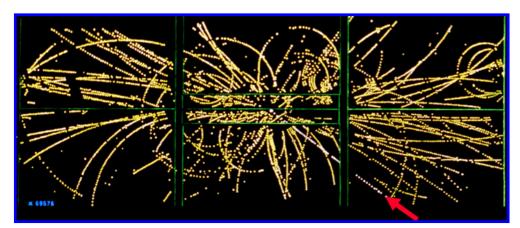


CDF, D0

Three Decades of Discoveries

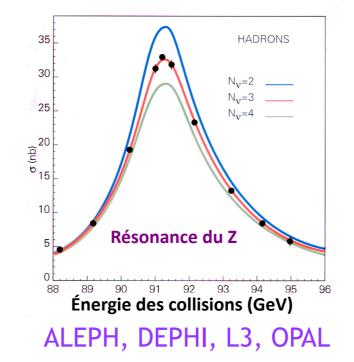
1972 – CERN 1976 – SLAC 1974 – BNL, SLAC 1979 – Fermilab neutral currents charm tau lepton beauty - Muon Trock J/Ψ Yield 177 3.00 3.25 8.2 9.8 10.2 10.6 11.0 11.4 8.6 9.0 94 total energy (GeV) Mass (GeV)

1983 – CERN/SppS W and Z boson

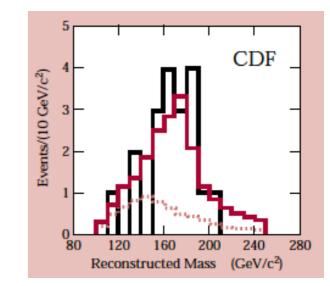


UA1, UA2

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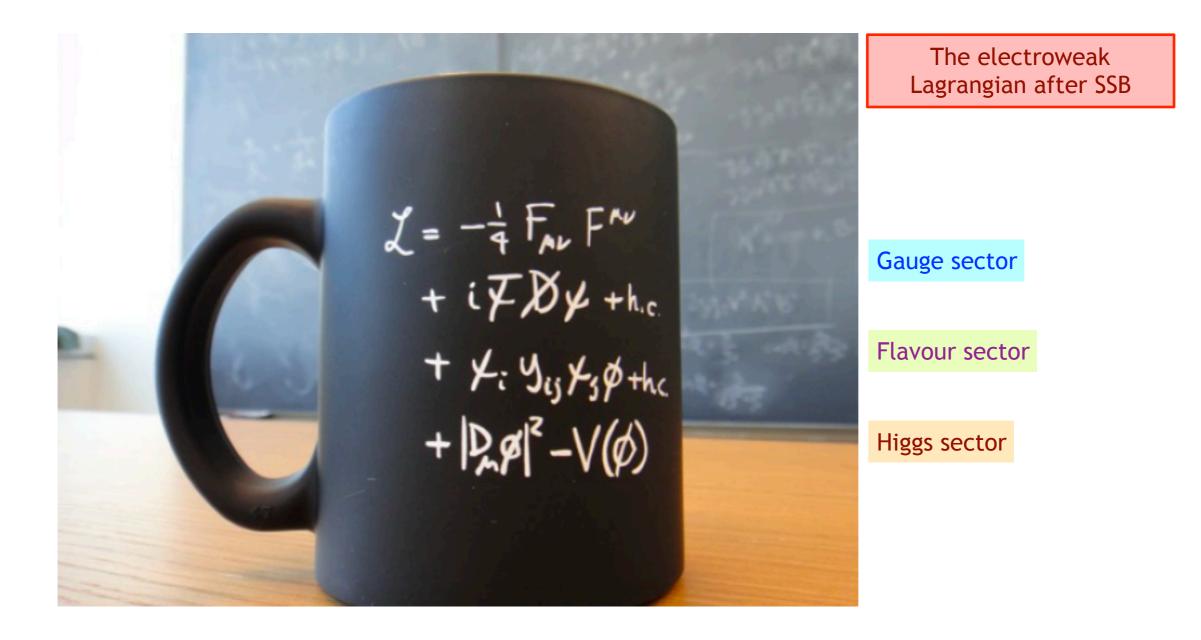


1994 — Fermilab/TeVatron top quark



CDF, D0

The Electroweak Lagrangian



The SM Lagrangian

from Symmetry Magazine, 2019

credit: T. Gutierrez, notations: M. Veltman

| $-\frac{1}{2}\partial_{\nu}g^{a}_{\mu}\partial_{\nu}g^{a}_{\mu} - g_{s}f^{abc}\partial_{\mu}g^{a}_{\nu}g^{b}_{\mu}g^{c}_{\nu} - \frac{1}{4}g^{2}_{s}f^{abc}f^{ade}g^{b}_{\mu}g^{c}_{\nu}g^{d}_{\mu}g^{e}_{\nu} +$ |
|--|
| $rac{1}{2}ig_s^2(ar{q}_i^\sigma\gamma^\mu q_j^\sigma)g_\mu^a+ar{G}^a\partial^2 G^a+g_sf^{abc}\partial_\muar{G}^aG^bg_\mu^c-\partial_ u W_\mu^+\partial_ u W_\mu^$ |
| $2 M^2 W^+_{\mu} W^{\mu} - \frac{1}{2} \partial_{\nu} Z^0_{\mu} \partial_{\nu} Z^0_{\mu} - \frac{1}{2c_w^2} M^2 Z^0_{\mu} Z^0_{\mu} - \frac{1}{2} \partial_{\mu} A_{\nu} \partial_{\mu} A_{\nu} - \frac{1}{2} \partial_{\mu} H \partial_{\mu} H - \frac{1}{2} \partial_{\mu} H$ |
| $ = \frac{1}{2}m_h^2 H^2 - \partial_\mu \phi^+ \partial_\mu \phi^ M^2 \phi^+ \phi^ \frac{1}{2}\partial_\mu \phi^0 \partial_\mu \phi^0 - \frac{1}{2c_w^2} M \phi^0 \phi^0 - \beta_h [\frac{2M^2}{q^2} + \frac{1}{2}\partial_\mu \phi^0 \partial_\mu \phi^0 - \frac{1}{2}\partial_\mu \phi^0 - \frac{1}{2}\partial_\mu \phi^0 \partial_\mu \phi^0 - 1$ |
| $\frac{2M}{q}H + \frac{1}{2}(H^2 + \phi^0\phi^0 + 2\phi^+\phi^-)] + \frac{2M^4}{q^2}\alpha_h - igc_w [\partial_\nu Z^0_\mu (W^+_\mu W^\nu - \psi^\mu W^\mu W^-$ |
| $W^{+}_{\nu}W^{-}_{\mu}) - Z^{0}_{\nu}(W^{+}_{\mu}\partial_{\nu}W^{-}_{\mu} - W^{-}_{\mu}\partial_{\nu}W^{+}_{\mu}) + Z^{0}_{\mu}(W^{+}_{\nu}\partial_{\nu}W^{-}_{\mu} - W^{-}_{\mu}) + Z^{0}_{\mu}(W^{+}_{\nu}\partial_{\nu}W^{-}_{\mu}) + Z^{0}_{\mu}(W^{+}_{\mu}\partial_{\nu}W^{-}_{\mu}) + Z^{0}_{\mu}(W^{+}_{\mu}\partial_{\nu}W^{-}_{\mu}) + Z^{0}_{\mu}(W^{+}_{\mu}\partial_{\mu}W^{-}_{\mu}) + Z^{0}_{\mu}(W^{+}_{\mu}\partial_{\mu$ |
| $W_{\nu}^{-}\partial_{\nu}W_{\mu}^{+})] - igs_{w}[\partial_{\nu}A_{\mu}(W_{\mu}^{+}W_{\nu}^{-} - W_{\nu}^{+}W_{\mu}^{-}) - A_{\nu}(W_{\mu}^{+}\partial_{\nu}W_{\mu}^{-} - W_{\mu}^{+}W_{\mu}^{-})] - igs_{w}[\partial_{\nu}A_{\mu}(W_{\mu}^{+}W_{\nu}^{-} - W_{\nu}^{+}W_{\mu}^{-})] - igs_{w}[\partial_{\nu}A_{\mu}(W_{\mu}^{+}W_{\nu}^{-} - W_{\nu}^{+}W_{\mu}^{-}]] - igs_{w}[\partial_{\nu}A_{\mu}(W_{\mu}^{+}W_{\nu}^{-} - W_{\nu}^{+}W_{\mu}^{-}]] - igs_{w}[\partial_{\nu}A_{\mu}(W_{\mu}^{+}W_{\nu}^{-} - W_{\nu}^{+}W_{\mu}^{-}]] - igs_{w}[\partial_{\nu}A_{\mu}(W_{\mu}^{+}W_{\nu}^{-} - W_{\nu}^{+}W_{\mu}^{-}]] - igs_{w}[\partial_{\nu}A_{\mu}(W_{\mu}^{+}W_{\nu}^{-} - W_{\mu}^{+}W_{\mu}^{-}]] - igs_{w}[\partial_{\mu}A_{\mu}(W_{\mu}^{+}W_{\mu}^{-}]] - igs_{w}[\partial_{\mu}A_{\mu}(W_{\mu}^{+}W_{\mu}^{-})] - igs_{w}[\partial_{\mu}A_{\mu}(W_{\mu}^{+}W_{\mu}^{-}]] - igs_{w}[\partial$ |
| $W_{\mu}^{-}\partial_{\nu}W_{\mu}^{+}) + A_{\mu}(W_{\nu}^{+}\partial_{\nu}W_{\mu}^{-} - W_{\nu}^{-}\partial_{\nu}W_{\mu}^{+})] - \frac{1}{2}g^{2}W_{\mu}^{+}W_{\mu}^{-}W_{\nu}^{+}W_{\nu}^{-} + \frac{1}{2}g^{2}W_{\mu}^{+}W_{\mu}^{-}W_{\nu}^{+} + \frac{1}{2}g^{2}W_{\mu}^{+}W_{\mu}^{-}W_{\nu}^{+} + \frac{1}{2}g^{2}W_{\mu}^{+}W_{\mu}^{-}W_{\nu}^{+} + \frac{1}{2}g^{2}W_{\mu}^{+}W_{\mu}^{-}W_{\nu}^{+} + \frac{1}{2}g^{2}W_{\mu}^{+}W_{\mu}^{-}W_{\nu}^{+} + \frac{1}{2}g^{2}W_{\mu}^{+}W_{\mu}^{-} + \frac{1}{2}g^{2}W_{\mu}^{+}W_{\mu}^{-} + \frac{1}{2}g^{2}W_{\mu}^{+}W_{\mu}^{-} + \frac{1}{2}g^{2}W_{\mu}^{+}W_{\mu}^{-} + \frac{1}{2}g^{2}W_{\mu}^{+}W_{\mu}^{-} + \frac{1}{2}g^{2}W_{\mu}^{+}W_{\mu}^{-} + \frac{1}{2}g^{2}W_{\mu}^{+} + \frac{1}{2}g^{2}W_{\mu}^{+}W_{\mu}^{-} + \frac{1}{2}g^{2}W_{\mu}^{+} + \frac{1}{2}g^{$ |
| $\frac{1}{2}g^{2}W_{\mu}^{+}W_{\nu}^{-}W_{\mu}^{+}W_{\nu}^{-} + g^{2}c_{w}^{2}(Z_{\mu}^{0}W_{\mu}^{+}Z_{\nu}^{0}W_{\nu}^{-} - Z_{\mu}^{0}Z_{\mu}^{0}W_{\nu}^{+}W_{\nu}^{-}) + c^{2}c^{2}(A_{\mu}W_{\nu}^{+}A_{\nu}W_{\nu}^{-} + A_{\mu}W_{\nu}^{+}W_{\nu}^{-}) + c^{2}c^{2}(A_{\mu}W_{\nu}^{+}A_{\nu}W_{\nu}^{-} + A_{\mu}W_{\nu}^{+}W_{\nu}^{-}) + c^{2}c^{2}(A_{\mu}W_{\nu}^{+}A_{\nu}W_{\nu}^{-} + A_{\mu}W_{\nu}^{+}W_{\nu}^{-}) + c^{2}c^{2}(A_{\mu}W_{\nu}^{+}A_{\nu}W_{\nu}^{-} + A_{\mu}W_{\nu}^{-}) + c^{2}c^{2}(A_{\mu}W_{\nu}^{+}A_{\nu}W_{\nu}^{-}) + c^{2}c^{2}(A_{\mu}W_{\mu}^{+}A_{\nu}W_{\nu}^{-}) + c^{2}c^{2}(A_{\mu}W_{\mu}^{+}A_{\nu}W_{\nu}^{-}) + c^{2}c^{2}(A_{\mu}W_{\mu}^{+}A_{\nu}W_{\nu}^{-}) + c^{2}c^{2}(A_{\mu}W_{\mu}^{+}A_{\nu}W_{\mu}^{-}) + c^{2}c^{2}(A_{\mu}W_{\mu}^{+}A_{\mu}W_{\mu}^{-}) + c^{2}c^{2}(A_{\mu}W_{\mu}^{+}A_{\mu}W_{\mu}^{-}) + c^{2}c^{2}(A_{\mu}W_{\mu}^{+}A_{\mu}W_{\mu}^{-}) + c^{2}c^{2}(A_{\mu}W_{\mu}^{+}A_{\mu}W_{\mu}^{-}) + c^{2}c^{2}(A_{\mu}W_{\mu}^{+}A_{\mu}W_{\mu}^{-}) + c^{2}c^{2}(A_{\mu}W_{\mu}^{+}A_{\mu}W_{\mu}^{-}) + c^{2}c^{2}(A_{\mu}$ |
| $g^{2}s_{w}^{2}(A_{\mu}W_{\mu}^{+}A_{\nu}W_{\nu}^{-} - A_{\mu}A_{\mu}W_{\nu}^{+}W_{\nu}^{-}) + g^{2}s_{w}c_{w}[A_{\mu}Z_{\nu}^{0}(W_{\mu}^{+}W_{\nu}^{-} - W_{\nu}^{+}W_{\mu}^{-}) - 2A_{\mu}Z_{\mu}^{0}W_{\nu}^{+}W_{\nu}^{-}] - g\alpha[H^{3} + H\phi^{0}\phi^{0} + 2H\phi^{+}\phi^{-}] - g\alpha[H^{3} + H\phi^{0}\phi^{0} + 2H\phi^{-}\phi^{-}] - g\alpha[H^{3} + H\phi^{0}\phi^{-}] - g\alpha[H^{3$ |
| $\frac{1}{8}g^{2}\alpha_{h}[H^{4} + (\phi^{0})^{4} + 4(\phi^{+}\phi^{-})^{2} + 4(\phi^{0})^{2}\phi^{+}\phi^{-} + 4H^{2}\phi^{+}\phi^{-} + 2(\phi^{0})^{2}H^{2}] - \frac{1}{8}g^{2}\alpha_{h}[H^{4} + (\phi^{0})^{4} + 4(\phi^{+}\phi^{-})^{2} + 4(\phi^{0})^{2}\phi^{+}\phi^{-} + 4H^{2}\phi^{+}\phi^{-} + 2(\phi^{0})^{2}H^{2}] - \frac{1}{8}g^{2}\alpha_{h}[H^{4} + (\phi^{0})^{4} + 4(\phi^{+}\phi^{-})^{2} + 4(\phi^{0})^{2}\phi^{+}\phi^{-} + 4H^{2}\phi^{+}\phi^{-} + 2(\phi^{0})^{2}H^{2}] - \frac{1}{8}g^{2}\alpha_{h}[H^{4} + (\phi^{0})^{4} + 4(\phi^{+}\phi^{-})^{2} + 4(\phi^{0})^{2}\phi^{+}\phi^{-} + 4H^{2}\phi^{+}\phi^{-} + 2H^{2}\phi^{-}\phi^{-} + 2H^{2}\phi$ |
| $gMW^{+}_{\mu}W^{-}_{\mu}H - \frac{1}{2}g\frac{M}{c_{w}^{2}}Z^{0}_{\mu}Z^{0}_{\mu}H - \frac{1}{2}ig[W^{+}_{\mu}(\phi^{0}\partial_{\mu}\phi^{-} - \phi^{-}\partial_{\mu}\phi^{0}) -$ |
| $ W^{-}_{\mu}(\phi^{0}\partial_{\mu}\phi^{+} - \phi^{+}\partial_{\mu}\phi^{0})] + \frac{1}{2}g[W^{+}_{\mu}(H\partial_{\mu}\phi^{-} - \phi^{-}\partial_{\mu}H) - W^{-}_{\mu}(H\partial_{\mu}\phi^{+} - \phi^{-}\partial_{\mu}H)] + \frac{1}{2}g[W^{+}_{\mu}(H\partial_{\mu}\phi^{-} - \phi^{-}\partial_{\mu}H)] + \frac{1}{2}g[W^{+}_{\mu}(H\partial_{\mu}\phi^{$ |
| $\phi^{+}\partial_{\mu}H)] + \frac{1}{2}g\frac{1}{c_{w}}(Z^{0}_{\mu}(H\partial_{\mu}\phi^{0} - \phi^{0}\partial_{\mu}H) - ig\frac{s^{2}_{w}}{c_{w}}MZ^{0}_{\mu}(W^{+}_{\mu}\phi^{-} - W^{-}_{\mu}\phi^{+}) +$ |
| $igs_w MA_\mu (W^+_\mu \phi^ W^\mu \phi^+) - ig \frac{1-2c_w^2}{2c_w} Z^0_\mu (\phi^+ \partial_\mu \phi^ \phi^- \partial_\mu \phi^+) +$ |
| $igs_w A_{\mu}(\phi^+\partial_{\mu}\phi^ \phi^-\partial_{\mu}\phi^+) - \frac{1}{4}g^2 W^+_{\mu} W^{\mu} [H^2 + (\phi^0)^2 + 2\phi^+\phi^-] - \frac{1}{4}g^2 W^+_{\mu} W^{\mu} [H^2 + (\phi^0)^2 + 2\phi^+\phi^-] - \frac{1}{4}g^2 W^+_{\mu} W^{\mu} [H^2 + (\phi^0)^2 + 2\phi^+\phi^-] - \frac{1}{4}g^2 W^+_{\mu} W^{\mu} [H^2 + (\phi^0)^2 + 2\phi^+\phi^-] - \frac{1}{4}g^2 W^+_{\mu} W^{\mu} [H^2 + (\phi^0)^2 + 2\phi^+\phi^-] - \frac{1}{4}g^2 W^+_{\mu} W^{\mu} [H^2 + (\phi^0)^2 + 2\phi^+\phi^-] - \frac{1}{4}g^2 W^+_{\mu} W^{\mu} [H^2 + (\phi^0)^2 + 2\phi^+\phi^-] - \frac{1}{4}g^2 W^+_{\mu} W^{\mu} [H^2 + (\phi^0)^2 + 2\phi^+\phi^-] - \frac{1}{4}g^2 W^+_{\mu} W^{\mu} [H^2 + (\phi^0)^2 + 2\phi^+\phi^-] - \frac{1}{4}g^2 W^+_{\mu} W^{\mu} [H^2 + (\phi^0)^2 + 2\phi^+\phi^-] - \frac{1}{4}g^2 W^+_{\mu} W^{\mu} [H^2 + (\phi^0)^2 + 2\phi^+\phi^-] - \frac{1}{4}g^2 W^+_{\mu} W^{\mu} [H^2 + (\phi^0)^2 + 2\phi^+\phi^-] - \frac{1}{4}g^2 W^+_{\mu} W^{\mu} [H^2 + (\phi^0)^2 + 2\phi^+\phi^-] - \frac{1}{4}g^2 W^+_{\mu} W^{\mu} [H^2 + (\phi^0)^2 + 2\phi^+\phi^-] - \frac{1}{4}g^2 W^+_{\mu} W^{\mu} [H^2 + (\phi^0)^2 + 2\phi^+\phi^-] - \frac{1}{4}g^2 W^+_{\mu} W^{\mu} [H^2 + (\phi^0)^2 + 2\phi^+\phi^-] - \frac{1}{4}g^2 W^+_{\mu} W^{\mu} [H^2 + (\phi^0)^2 + 2\phi^+\phi^-] - \frac{1}{4}g^2 W^+_{\mu} W^{\mu} [H^2 + (\phi^0)^2 + 2\phi^+\phi^-] - \frac{1}{4}g^2 W^+_{\mu} W^{\mu} [H^2 + (\phi^0)^2 + 2\phi^+\phi^-] - \frac{1}{4}g^2 W^+_{\mu} W^{\mu} [H^2 + (\phi^0)^2 + 2\phi^+\phi^-] - \frac{1}{4}g^2 W^+_{\mu} W^{\mu} [H^2 + (\phi^0)^2 + 2\phi^+\phi^-] - \frac{1}{4}g^2 W^+_{\mu} W^{\mu} [H^2 + (\phi^0)^2 + 2\phi^+\phi^-] - \frac{1}{4}g^2 W^+_{\mu} W^{\mu} [H^2 + (\phi^0)^2 + 2\phi^+\phi^-] - \frac{1}{4}g^2 W^+_{\mu} [H^2 + (\phi^0)^2 + 2\phi^+] - \frac{1}{4}g^2 W^+_{\mu} [H^2 + (\phi^0)^2 + $ |
| $\frac{1}{4}g^{2}\frac{1}{c_{w}^{2}}Z_{\mu}^{0}Z_{\mu}^{0}[H^{2} + (\phi^{0})^{2} + 2(2s_{w}^{2} - 1)^{2}\phi^{+}\phi^{-}] - \frac{1}{2}g^{2}\frac{s_{w}^{2}}{c_{w}}Z_{\mu}^{0}\phi^{0}(W_{\mu}^{+}\phi^{-} + \phi^{-}) + \frac{1}{2}g^{2}\frac{s_{w}^{2}}{c_{w}}Z_{\mu}^{0}\phi^{0}(W_{\mu}^{+}\phi^{-}) + \frac{1}{2}g^{2}\frac{s_{w}^{2}}{c_{w}}Z_{\mu}^{0}(W_{\mu}^{+}\phi^{-}) + \frac{1}{2}g^{2}\frac{s_{w}^{2}}{c_{w}}Z_{\mu}^{0}(W_{\mu}^{+}\phi^{-}) + \frac{1}{2}g^{2}\frac{s_{w}^{2}}{c_{w}}Z_{\mu}^{0}(W_{\mu}^{+}\phi^{-}) + \frac{1}{2}g^{2}\frac{s_{w}^{2}}{c_{w}}Z_{\mu}^{0}(W_{\mu}^{+}\phi^{-}) + \frac{1}{2}g^{2}\frac{s_{w}^{2}}{c_{w}}Z_{\mu}^{0}(W_{\mu}^{+}\phi^{-}) + \frac{1}{2}g^{2}\frac{s_{w}^{2}}{c_{w}}Z_{\mu}^{0}(W_{\mu}^{+}\phi^{-}) + \frac{1}{2}g^{2}\frac{s_{w}$ |
| $W^{-}_{\mu}\phi^{+}) - \frac{1}{2}ig^{2}\frac{s^{2}_{w}}{c_{w}}Z^{0}_{\mu}H(W^{+}_{\mu}\phi^{-} - W^{-}_{\mu}\phi^{+}) + \frac{1}{2}g^{2}s_{w}A_{\mu}\phi^{0}(W^{+}_{\mu}\phi^{-} + W^{-}_{\mu}\phi^{+}))$ |
| $ \begin{array}{c} W_{\mu}^{-}\phi^{+}) + \frac{1}{2}ig^{2}s_{w}A_{\mu}H(W_{\mu}^{+}\phi^{-} - W_{\mu}^{-}\phi^{+}) - g^{2}\frac{s_{w}}{c_{w}}(2c_{w}^{2} - 1)Z_{\mu}^{0}A_{\mu}\phi^{+}\phi^{-} - g^{1}s_{w}^{2}A_{\mu}A_{\mu}\phi^{+}\phi^{-} - \bar{e}^{\lambda}(\gamma\partial + m_{e}^{\lambda})e^{\lambda} - \bar{\nu}^{\lambda}\gamma\partial\nu^{\lambda} - \bar{u}_{j}^{\lambda}(\gamma\partial + m_{u}^{\lambda})u_{j}^{\lambda} - g^{2}\frac{s_{w}}{c_{w}}(2c_{w}^{2} - 1)Z_{\mu}^{0}A_{\mu}\phi^{+}\phi^{-} - g^{2}\frac{s_{w}}{c_{w}}(2c_{w}^{2} - 1)Z_{\mu}\phi^{+}\phi^{-} - g^{2}\frac{s_{w}}{c$ |
| $g^{1}s_{w}^{2}A_{\mu}A_{\mu}\phi^{+}\phi^{-} - \bar{e}^{\lambda}(\gamma\partial + m_{e}^{\lambda})e^{\lambda} - \bar{\nu}^{\lambda}\gamma\partial\nu^{\lambda} - \bar{u}_{j}^{\lambda}(\gamma\partial + m_{u}^{\lambda})u_{j}^{\lambda} - \bar{v}_{j}^{\lambda}(\gamma\partial + m_{u}^{\lambda})u_{j}^{\lambda}$ |
| |
| $\frac{ig}{4c_w}Z^0_\mu[(\bar{\nu}^\lambda\gamma^\mu(1+\gamma^5)\nu^\lambda) + (\bar{e}^\lambda\gamma^\mu(4s_w^2 - 1 - \gamma^5)e^\lambda) + (\bar{u}_j^\lambda\gamma^\mu(\frac{4}{3}s_w^2 - 1 - \gamma^5)e^\lambda)]$ |
| $1 - \gamma^5)u_j^{\lambda}) + (\bar{d}_j^{\lambda}\gamma^{\mu}(1 - \frac{8}{3}s_w^2 - \gamma^5)d_j^{\lambda})] + \frac{ig}{2\sqrt{2}}W_{\mu}^+[(\bar{\nu}^{\lambda}\gamma^{\mu}(1 + \gamma^5)e^{\lambda}) + \frac{ig}{2\sqrt{2}}W_{\mu}^+](\bar{\nu}^{\lambda}\gamma^{\mu}(1 + \gamma^5)e^{\lambda}) + \gamma^5)e^{\lambda})$ |
| $(\bar{u}_j^{\lambda}\gamma^{\mu}(1+\gamma^5)C_{\lambda\kappa}d_j^{\kappa})] + \frac{ig}{2\sqrt{2}}W_{\mu}^{-}[(\bar{e}^{\lambda}\gamma^{\mu}(1+\gamma^5)\nu^{\lambda}) + (\bar{d}_j^{\kappa}C_{\lambda\kappa}^{\dagger}\gamma^{\mu}(1+\gamma^5)\nu^{\lambda})] + (\bar{d}_j^{\kappa}C_{\lambda\kappa}^{\dagger}\gamma^{\mu}(1+\gamma^5)\nu^{\lambda}) + (\bar{d}_j^{\kappa}C_{\lambda\kappa}^$ |
| $\gamma^{5}(u_{j}^{\lambda})] + \frac{ig}{2\sqrt{2}} \frac{m_{e}^{\lambda}}{M} \left[-\phi^{+}(\bar{\nu}^{\lambda}(1-\gamma^{5})e^{\lambda}) + \phi^{-}(\bar{e}^{\lambda}(1+\gamma^{5})\nu^{\lambda})\right] -$ |
| $\frac{4}{2} \frac{g}{2} \frac{m_e^{\lambda}}{M} [H(\bar{e}^{\lambda} e^{\lambda}) + i\phi^0(\bar{e}^{\lambda} \gamma^5 e^{\lambda})] + \frac{ig}{2M\sqrt{2}} \phi^+ [-m_d^{\kappa}(\bar{u}_j^{\lambda} C_{\lambda\kappa}(1-\gamma^5)d_j^{\kappa}) + \frac{ig}{2M\sqrt{2}} \phi^+ [-m_d^{\kappa}(\bar{u}_j^{\lambda} C_{\lambda\kappa}(1-\gamma^5)d_j^{\kappa})] + \frac{ig}{2M\sqrt{2}} \phi^+ [-m_d^{\kappa}(\bar{u}_j^{\lambda} C_{\lambda\kappa}(1-\gamma^5)d_j^{\kappa}) + \frac{ig}{2M\sqrt{2}} \phi^+ [-m_d^{\kappa}(\bar{u}_j^{\lambda} C_{\lambda\kappa}(1-\gamma^5)d_j^{\kappa})] + \frac{ig}{2M\sqrt{2}} \phi^+ [-m_d^{\kappa}(\bar{u}_j^{\lambda} C_{\lambda\kappa}(1-\gamma^5)d_j^{\kappa}) + \frac{ig}{2M\sqrt{2}} \phi^+ [-m_d^{\kappa}(\bar{u}_j^{\lambda} C_{\lambda\kappa}(1-\gamma^5)d_j^{\kappa})] + \frac{ig}{2M\sqrt{2}} \phi^+ [-m_d^{\kappa}(\bar{u}_j^{\lambda} C_{\lambda\kappa}(1-\gamma^5)d_j^{\kappa}) + \frac{ig}{2M\sqrt{2}} \phi^+ [-m_d^{\kappa}(\bar{u}_j^{\lambda} C_{\lambda\kappa}(1-\gamma^5)d_j^{\kappa})] + \frac{ig}{2M\sqrt{2}} \phi^+ [-m_d^{\kappa}(\bar{u}_j^{\lambda} C_{\lambda\kappa}(1-\gamma^5)d_j^{\kappa}) + \frac{ig}{2M\sqrt{2}} \phi^+ [-m_d^{\kappa}(\bar{u}_j^{\lambda} C_{\lambda\kappa}(1-\gamma^5)d_j^{\kappa})] + \frac{ig}{2M\sqrt{2}} \phi^+ [-m_d^{\kappa}(\bar{u}_j^{\lambda} C_{\lambda\kappa}(1-\gamma^5)d_j^{\kappa}) + \frac{ig}{2M\sqrt{2}} \phi^+ [-m_d^{\kappa}(\bar{u}_j^{\lambda} C_{\lambda\kappa}(1-\gamma^5)d_j^{\kappa})] + \frac{ig}{2M\sqrt{2}} \phi^+ [-m_d^{\kappa}(\bar{u}_j^{\lambda} C_{\lambda\kappa}(1-\gamma^5)d_j^{\kappa}) + \frac{ig}{2M\sqrt{2}} \phi^+ [-m_d^{\kappa}(\bar{u}_j^{\lambda} C_{\lambda\kappa}(1-\gamma^5)d_j^{\kappa})] + \frac{ig}{2M\sqrt{2}} \phi^+ [-m_d^{\kappa}(\bar{u}_j^{\lambda} C_{\lambda\kappa}(1-\gamma^5)d_j^{\kappa}) + \frac{ig}{2M\sqrt{2}} \phi^+ [-m_d^{\kappa}(\bar{u}_j^{\lambda} C_{\lambda\kappa}(1-\gamma^5)d_j^{\kappa})] + \frac{ig}{2M\sqrt{2}} \phi^+ [-m_d^{\kappa}(\bar{u}_j^{\lambda} C_{\lambda\kappa}(1-\gamma^5)d_j^{\kappa}) + \frac{ig}{2M\sqrt{2}} \phi^+ [-m_d^{\kappa}(\bar{u}_j^{\lambda} C_{\lambda\kappa}(1-\gamma^5)d_j^{\kappa})] + \frac{ig}{2M\sqrt{2}} \phi^+ [-m_d^{\kappa}(\bar{u}_j^{\lambda} C_{\lambda\kappa}(1-\gamma^5)d_j^{\kappa}) + \frac{ig}{2M\sqrt{2}} \phi^+ [-m_d^{\kappa}(\bar{u}_j^{\lambda} C_{\lambda\kappa}(1-\gamma^5)d_j^{\kappa})] + \frac{ig}{2M\sqrt{2}} \phi^+ [-m_d^{\kappa}(\bar{u}_j^{\lambda} C_{\lambda\kappa}(1-\gamma^5)d_j^{\kappa}) + \frac{ig}{2M\sqrt{2}} \phi^+ [-m_d^{\kappa}(\bar{u}_j^{\lambda} C_{\lambda\kappa}(1-\gamma^5)d_j^{\kappa})] + \frac{ig}{2M\sqrt{2}} \phi^+ [-m_d^{\kappa}(\bar{u}_j^{\lambda} C_{\lambda\kappa}(1-\gamma^5)d_j^{\kappa})] + \frac{ig}{2M\sqrt{2}} \phi^+ [-m_d^{\kappa}(\bar{u}_j^{\lambda} C_{\kappa}(1-\gamma^5)d_j^{\kappa})] + $ |
| $m_u^{\lambda}(\bar{u}_j^{\lambda}C_{\lambda\kappa}(1+\gamma^5)d_j^{\kappa}] + \frac{ig}{2M\sqrt{2}}\phi^{-}[m_d^{\lambda}(\bar{d}_j^{\lambda}C_{\lambda\kappa}^{\dagger}(1+\gamma^5)u_j^{\kappa}) - m_u^{\kappa}(\bar{d}_j^{\lambda}C_{\lambda\kappa}^{\dagger}(1-\gamma^5)u_j^{\kappa})] + \frac{ig}{2M\sqrt{2}}\phi^{-}[m_d^{\lambda}(\bar{d}_j^{\lambda}C_{\lambda\kappa}^{\dagger}(1+\gamma^5)u_j^{\kappa}) - m_u^{\kappa}(\bar{d}_j^{\lambda}C_{\lambda\kappa}^{\dagger}(1+\gamma^5)u_j^{\kappa})] + \frac{ig}{2M\sqrt{2}}\phi^{-}[m_d^{\lambda}(\bar{d}_j^{\lambda}C_{\lambda\kappa}^{\dagger}(1+\gamma^5)u_j^{\kappa})] + \frac{ig}{2M\sqrt{2}}\phi^{-}[m_d^{\lambda}(\bar{d}_j^{\lambda}C_{\lambda\kappa}^{\dagger}(1+\gamma^5)u_j^{\kappa})] + \frac{ig}{2M\sqrt{2}}\phi^{-}[m_d^{\lambda}(\bar{d}_j^{\lambda}C_{\lambda\kappa}^{\dagger}(1+\gamma^5)u_j^{\kappa})] + \frac{ig}{2M\sqrt{2}}\phi^{-}[m_d^{\lambda}(\bar{d}_j^{\lambda}C_{\lambda\kappa}^{\dagger}(1+\gamma^5)u_j^{\kappa})] + \frac{ig}{2M\sqrt{2}}\phi^{-}[m_d^{\lambda}(1+\gamma^5)u_j^{\kappa})] + \frac{ig}{2M\sqrt{2}}\phi^{-}[m_d^{\lambda}(1+\gamma^5)u_j^{\kappa})] + \frac{ig}{2M\sqrt{2}}\phi^{-}[m_d^{\lambda}(1+\gamma^5)u_j^{\kappa})] + \frac{ig}{2M\sqrt{2}}\phi^{-}[m_d^{\lambda}(1+\gamma^5)u_$ |
| $\left[\gamma^{5}\right]u_{j}^{\kappa} - \frac{g}{2}\frac{m_{u}^{\lambda}}{M}H(\bar{u}_{j}^{\lambda}u_{j}^{\lambda}) - \frac{g}{2}\frac{m_{d}^{\lambda}}{M}H(\bar{d}_{j}^{\lambda}d_{j}^{\lambda}) + \frac{ig}{2}\frac{m_{u}^{\lambda}}{M}\phi^{0}(\bar{u}_{j}^{\lambda}\gamma^{5}u_{j}^{\lambda}) - \frac{g}{2}\frac{m_{u}^{\lambda}}{M}\phi^{0}(\bar{u}_{j}^{\lambda}\gamma^{5}u_{j}^{\lambda}) - \frac{g}{2}\frac{m_{u}^{\lambda}}{M}H(\bar{d}_{j}^{\lambda}d_{j}^{\lambda}) + \frac{ig}{2}\frac{m_{u}^{\lambda}}{M}\phi^{0}(\bar{u}_{j}^{\lambda}\gamma^{5}u_{j}^{\lambda}) + $ |
| $\frac{ig}{2}\frac{m_d^{\lambda}}{M}\phi^0(\bar{d}_j^{\lambda}\gamma^5 d_j^{\lambda}) + \bar{X}^+(\partial^2 - M^2)X^+ + \bar{X}^-(\partial^2 - M^2)X^- + \bar{X}^0(\partial^2 - M^2$ |
| 5 $\frac{\bar{M}^2}{c_w^2} X^0 + \bar{Y} \partial^2 Y + igc_w W^+_{\mu} (\partial_{\mu} \bar{X}^0 X^ \partial_{\mu} \bar{X}^+ X^0) + igs_w W^+_{\mu} (\partial_{\mu} \bar{Y} X^ \partial_{\mu} \bar{X}^+ X^0) + igs_w W^+_{\mu} (\partial_{\mu} \bar{Y} X^ \partial_{\mu} \bar{X}^+ X^0) + igs_w W^+_{\mu} (\partial_{\mu} \bar{Y} X^ \partial_{\mu} \bar{X}^+ X^0) + igs_w W^+_{\mu} (\partial_{\mu} \bar{Y} X^ \partial_{\mu} \bar{X}^+ X^0) + igs_w W^+_{\mu} (\partial_{\mu} \bar{Y} X^ \partial_{\mu} \bar{X}^+ X^0) + igs_w W^+_{\mu} (\partial_{\mu} \bar{Y} X^ \partial_{\mu} \bar{X}^+ X^0) + igs_w W^+_{\mu} (\partial_{\mu} \bar{Y} X^ \partial_{\mu} \bar{X}^+ X^0) + igs_w W^+_{\mu} (\partial_{\mu} \bar{Y} X^ \partial_{\mu} \bar{X}^+ X^0) + igs_w W^+_{\mu} (\partial_{\mu} \bar{Y} X^ \partial_{\mu} \bar{X}^+ X^0) + igs_w W^+_{\mu} (\partial_{\mu} \bar{Y} X^ \partial_{\mu} \bar{X}^+ X^0) + igs_w W^+_{\mu} (\partial_{\mu} \bar{Y} X^ \partial_{\mu} \bar{X}^+ X^0) + igs_w W^+_{\mu} (\partial_{\mu} \bar{Y} X^ \partial_{\mu} \bar{X}^+ X^0) + igs_w W^+_{\mu} (\partial_{\mu} \bar{Y} X^ \partial_{\mu} \bar{X}^+ X^0) + igs_w W^+_{\mu} (\partial_{\mu} \bar{Y} X^ \partial_{\mu} \bar{X}^+ X^0) + igs_w W^+_{\mu} (\partial_{\mu} \bar{Y} X^ \partial_{\mu} \bar{X}^+ X^0) + igs_w W^+_{\mu} (\partial_{\mu} \bar{Y} X^ \partial_{\mu} \bar{X}^+ X^0) + igs_w W^+_{\mu} (\partial_{\mu} \bar{Y} X^ \partial_{\mu} \bar{X}^+ X^0) + igs_w W^+_{\mu} (\partial_{\mu} \bar{Y} X^ \partial_{\mu} \bar{X}^+ X^0) + igs_w W^+_{\mu} (\partial_{\mu} \bar{Y} X^ \partial_{\mu} \bar{X}^+ X^0) + igs_w W^+_{\mu} (\partial_{\mu} \bar{Y} X^ \partial_{\mu} \bar{X}^+ X^0) + igs_w W^+_{\mu} (\partial_{\mu} \bar{Y} X^ \partial_{\mu} \bar{X}^+ X^0) + igs_w W^+_{\mu} (\partial_{\mu} \bar{Y} X^ \partial_{\mu} \bar{X}^+ X^0) + igs_w W^+_{\mu} (\partial_{\mu} \bar{Y} X^ \partial_{\mu} \bar{X}^+ X^0) + igs_w W^+_{\mu} (\partial_{\mu} \bar{Y} X^ \partial_{\mu} \bar{X}^+ X^0) + igs_w W^+_{\mu} (\partial_{\mu} \bar{Y} X^ \partial_{\mu} \bar{Y} X^ \partial_{\mu} \bar{Y} X^0) + igs_w W^+_{\mu} (\partial_{\mu} \bar{Y} X^ \partial_{\mu} \bar{Y} X^0) + igs_w W^+_{\mu} (\partial_{\mu} \bar{Y} X^ \partial_{\mu} \bar{Y} X^0) + igs_w W^+_{\mu} (\partial_{\mu} \bar{Y} X^ \partial_{\mu} \bar{Y} X^0) + igs_w W^+_{\mu} (\partial_{\mu} \bar{Y} X^ \partial_{\mu} \bar{Y} X^0) + igs_w W^+_{\mu} (\partial_{\mu} \bar{Y} X^ \partial_{\mu} \bar{Y} X^0) + igs_w W^+_{\mu} (\partial_{\mu} \bar{Y} X^ \partial_{\mu} \bar{Y} X^0) + igs_w W^+_{\mu} (\partial_{\mu} \bar{Y} X^0) + igs_w$ |
| $\partial_{\mu}\bar{X}^{+}Y) + igc_{w}W^{-}_{\mu}(\partial_{\mu}\bar{X}^{-}X^{0} - \partial_{\mu}\bar{X}^{0}X^{+}) + igs_{w}W^{-}_{\mu}(\partial_{\mu}\bar{X}^{-}Y - \partial_{\mu}\bar{X}^{0}X^{+}))$ |
| $\partial_{\mu}\bar{Y}X^{+}) + igc_{w}Z^{0}_{\mu}(\partial_{\mu}\bar{X}^{+}X^{+} - \partial_{\mu}\bar{X}^{-}X^{-}) + igs_{w}A_{\mu}(\partial_{\mu}\bar{X}^{+}X^{+} - \partial_{\mu}\bar{X}^{-}X^{-}) + igs_{w}A_{\mu}(\partial_{\mu}\bar{X}^{+}X^{+}) + igs_{w}A_{\mu}(\partial_{\mu}$ |
| $\partial_{\mu}\bar{X}^{-}X^{-}) - \frac{1}{2}gM[\bar{X}^{+}X^{+}H + \bar{X}^{-}X^{-}H + \frac{1}{c_{w}^{2}}\bar{X}^{0}X^{0}H] +$ |
| $\frac{1-2c_w^2}{2c_w}igM[\bar{X}^+X^0\phi^+ - \bar{X}^-X^0\phi^-] + \frac{1}{2c_w}igM[\bar{X}^0X^-\phi^+ - \bar{X}^0X^+\phi^-] + \frac{1}{2c_w}igM[\bar{X}^0X^-\phi^-] + \frac{1}{2c_w}igM[\bar{X}^0X^-\phi^-]$ |
| $igMs_w[\bar{X}^0X^-\phi^+ - \bar{X}^0X^+\phi^-] + \frac{1}{2}igM[\bar{X}^+X^+\phi^0 - \bar{X}^-X^-\phi^0]$ |

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The SM Lagrangian

- 1. kinematics and colour interactions of gluons (QCD)
- 2. kinematics and interactions of elementary bosons: W, Z, γ , and H
- 3. kinematics and interactions of elementary fermions: quarks and leptons (and massless neutrinos)
- 4. ghosts
- 5. more ghosts



from Symmetry Magazine, 2019

credit: T. Gutierrez, notations: M. Veltman

 $-\tfrac{1}{2}\partial_\nu g^a_\mu\partial_\nu g^a_\mu - g_s f^{abc}\partial_\mu g^a_\nu g^b_\mu g^c_\nu - \tfrac{1}{4}g^2_s f^{abc} f^{ade} g^b_\mu g^c_\nu g^d_\mu g^e_\nu +$ $\frac{1}{2}ig_s^2(\bar{q}_i^{\sigma}\gamma^{\mu}q_j^{\sigma})g_{\mu}^a + \bar{G}^a\partial^2 G^a + g_sf^{abc}\partial_{\mu}\bar{G}^aG^bg_{\mu}^c - \partial_{\nu}W_{\mu}^+\partial_{\nu}W_{\mu}^- -$ 2 $M^2 W^+_{\mu} W^-_{\mu} - \frac{1}{2} \partial_{\nu} Z^0_{\mu} \partial_{\nu} Z^0_{\mu} - \frac{1}{2c_w^2} M^2 Z^0_{\mu} Z^0_{\mu} - \frac{1}{2} \partial_{\mu} A_{\nu} \partial_{\mu} A_{\nu} - \frac{1}{2} \partial_{\mu} H \partial_{\mu} H - \frac{1}{2} \partial_{\mu} H$ $\frac{1}{2}m_{h}^{2}H^{2} - \partial_{\mu}\phi^{+}\partial_{\mu}\phi^{-} - M^{2}\phi^{+}\phi^{-} - \frac{1}{2}\partial_{\mu}\phi^{0}\partial_{\mu}\phi^{0} - \frac{1}{2c_{*}^{2}}M\phi^{0}\phi^{0} - \beta_{h}[\frac{2M^{2}}{a^{2}} + \frac{1}{2}\partial_{\mu}\phi^{0}\partial_{\mu}\phi^{0} - \frac{1}{2c_{*}^{2}}M\phi^{0}\phi^{0} - \beta_{h}[\frac{2M^{2}}{a^{2}} + \frac{1}{2}\partial_{\mu}\phi^{0}\partial_{\mu}\phi^{0} - \frac{1}{2}\partial_{\mu}\phi^{0}\partial_{\mu}\phi^{0} - \frac{1}{2}\partial_{\mu}\phi^{0}\partial_{\mu}\phi^{0} - \beta_{h}[\frac{2M^{2}}{a^{2}} + \frac{1}{2}\partial_{\mu}\phi^{0}\partial_{\mu}\phi^{0} - \frac{1}{2}\partial_{\mu}\partial_{\mu}\phi^{0} - \frac{1}{2}\partial_{\mu}\partial_{\mu}\phi^{0} - \frac{1}{2}\partial_{\mu}\partial_{\mu}\phi^{0} - \frac{1}{2}\partial_{\mu}\partial_{\mu}\partial_{\mu}\phi^{0} - \frac{1}{2}\partial_{\mu}\partial_{\mu}\partial_{\mu}\phi^{0} - \frac{1}{2}\partial_{\mu}\partial_{\mu}\partial_{\mu}\phi^{0} \frac{2M}{g}H + \frac{1}{2}(H^2 + \phi^0\phi^0 + 2\phi^+\phi^-)] + \frac{2M^4}{q^2}\alpha_h - (igc_w)\partial_\nu Z^0_\mu(W^+_\mu W^-_\nu - \psi^-)$ $\begin{array}{c} W_{\nu}^{+}W_{\mu}^{-}) - Z_{\nu}^{0}(W_{\mu}^{+}\partial_{\nu}W_{\mu}^{-} - W_{\mu}^{-}\partial_{\nu}W_{\mu}^{+}) + Z_{\mu}^{0}(W_{\nu}^{+}\partial_{\nu}W_{\mu}^{-} - W_{\nu}^{-}\partial_{\nu}W_{\mu}^{+}) \\ W_{\nu}^{-}\partial_{\nu}W_{\mu}^{+})] - igs_{w}[\partial_{\nu}A_{\mu}(W_{\mu}^{+}W_{\nu}^{-} - W_{\nu}^{+}W_{\mu}^{-}) - A_{\nu}(W_{\mu}^{+}\partial_{\nu}W_{\mu}^{-} - W_{\nu}^{-}W_{\nu}^{-})] \\ \end{array}$ $W_{\mu}^{-}\partial_{\nu}W_{\mu}^{+}) + A_{\mu}(W_{\nu}^{+}\partial_{\nu}W_{\mu}^{-} - W_{\nu}^{-}\partial_{\nu}W_{\mu}^{+})] - \frac{1}{2}g^{2}W_{\mu}^{+}W_{\mu}^{-}W_{\nu}^{+}W_{\nu}^{-} + \frac{1}{2}g^{2}W_{\mu}^{+}W_{\mu}^{-}W_{\nu}^{-}W_{\nu}^{-} + \frac{1}{2}g^{2}W_{\mu}^{+}W_{\mu}^{-}W_{\nu}^{-}W_{\nu}^{-} + \frac{1}{2}g^{2}W_{\mu}^{+}W_{\mu}^{-}W_{\nu}^{-}W_{\nu}^{-} + \frac{1}{2}g^{2}W_{\mu}^{+}W_{\mu}^{-}W_{\nu}^{-}W_{\nu}^{-} + \frac{1}{2}g^{2}W_{\mu}^{+}W_{\mu}^{-}W_{\nu}^{-}W_{\nu}^{-} + \frac{1}{2}g^{2}W_{\mu}^{+}W_{\mu}^{-}W_{\nu}^{-}W_{\nu}^{-} + \frac{1}{2}g^{2}W_{\mu}^{+}W_{\mu}^{-}W_{\nu}^{-} + \frac{1}{2}g^{2}W_{\mu}^{+}W_{\mu}^{-}W_{\nu}^{-}W_{\nu}^{-} + \frac{1}{2}g^{2}W_{\mu}^{+}W_{\mu}^{-}W_{\nu}^{-}W_{\nu}^{-} + \frac{1}{2}g^{2}W_{\mu}^{+}W_{\mu}^{-}W_{\nu}^{-} + \frac{1}{2}g^{2}W_{\mu}^{+}W_{\mu}^{-}W_{\nu}^{-} + \frac{1}{2}g^{2}W_{\mu}^{+}W_{\mu}^{-}W_{\nu}^{-} + \frac{1}{2}g^{2}W_{\mu}^{+}W_{\mu}^{-}W_{\nu}^{-} + \frac{1}{2}g^{2}W_{\mu}^{+}W_{\mu}^{-}W_{\nu}^{-} + \frac{1}{2}g^{2}W_{\mu}^{+}W_{\mu}^{-} + \frac{1}{2}g^{2}W_{\mu}^{+}W_{\mu}^{-}W_{\nu}^{-} + \frac{1}{2}g^{2}W_{\mu}^{+}W_{\mu}^{-}W_{\nu}^{-} + \frac{1}{2}g^{2}W_{\mu}^{+}W_{\mu}^{-}W_{\mu}^{-} + \frac{1}{2}g^{2}W_{\mu}^{+}W_{\mu}^{-} + \frac{1}{2}g^{2}W_{\mu}^{-} + \frac{1}$ $\frac{1}{2}g^2W^+_{\mu}W^-_{\nu}W^+_{\mu}W^-_{\nu} + g^2c^2_wZ^0_{\mu}W^+_{\mu}Z^0_{\nu}W^-_{\nu} - Z^0_{\mu}Z^0_{\mu}W^+_{\nu}W^-_{\nu}) +$ $(g^{2}s_{w}^{2})A_{\mu}W_{\mu}^{+}A_{\nu}W_{\nu}^{-} - A_{\mu}A_{\mu}W_{\nu}^{+}W_{\nu}^{-}) + (g^{2}s_{w}c_{w})A_{\mu}Z_{\nu}^{0}(W_{\mu}^{+}W_{\nu}^{-} - W_{\nu}^{-}) + (g^{2}s_{w}c_{w})A_{\mu}Z_{\nu}^{0}(W_{\mu}^{+}W_{\nu}^{-}) + (g^{2}s_{w}c_{w})A_{\mu}Z_{\mu}^{0}(W_{\mu}^{+}W_{\mu}^{-}) + (g^{2}s_{w}c_{w})A_{\mu}Z_{\mu}^{0}(W_{\mu}^{+}W_{\mu}^{-}) + (g^{2}s_{w}c_{w})A_{\mu}Z_{\mu}^{0}(W_{\mu}^{+}W_{\mu}^{-}) + (g^{2}s_{w}c_{w})A_{\mu}Z_{\mu}^{0}(W_{\mu}^{+}W_{\mu}^{-}) + (g^{2}s_{w}c_{w})A_{\mu}Z_{\mu}^{0}(W_{\mu}^{+}W_{\mu}^{-}) + (g^{2}s_{w}c_{w})A_{\mu}Z_{\mu}^{0}(W_{\mu}^{+}W_{\mu}^{-}) + (g^{2}s_{w}c_{w$ $W^{+}_{\nu}W^{-}_{\mu}) - 2A_{\mu}Z^{0}_{\mu}W^{+}_{\nu}W^{-}_{\nu}] - (g\alpha)H^{3} + H\phi^{0}\phi^{0} + 2H\phi^{+}\phi^{-}] - g\alpha^{0}H^{3} + H\phi^{0}\phi^{0} + 2H\phi^{-}\phi^{-}] - g\alpha^{0}H^{0} + 2H\phi^{0} + 2H\phi^{-}\phi^{-}] - g\alpha^{0}H^{0} + 2H\phi^{0} + 2H\phi^{-}$ - g\alpha^{0}H^{0} + 2H\phi^{0} + 2H\phi^{-} - g\alpha^{0}H^{0} + 2H\phi^{-} - g\alpha^{0}H^{0} + 2H\phi^{0} + 2H\phi^{-} - g\alpha^{0}H^{0} + 2H\phi^{0} + 2H\phi^{-} - g\alpha^{0}H^{0} + 2H\phi^{0} + 2H\phi^{0} + 2H\phi^{-} - g\alpha^{0}H^{0} + 2H\phi^{0} + 2H\phi^{0} + 2H\phi^{-} - g\alpha^{0}H^{0} + 2H\phi^{0 $\frac{1}{8}g^{2}\alpha_{h}H^{4} + (\phi^{0})^{4} + 4(\phi^{+}\phi^{-})^{2} + 4(\phi^{0})^{2}\phi^{+}\phi^{-} + 4H^{2}\phi^{+}\phi^{-} + 2(\phi^{0})^{2}H^{2}] - \frac{1}{8}g^{2}\alpha_{h}H^{4} + (\phi^{0})^{4} + 4(\phi^{+}\phi^{-})^{2} + 4(\phi^{0})^{2}\phi^{+}\phi^{-} + 4H^{2}\phi^{+}\phi^{-} + 2(\phi^{0})^{2}H^{2}] - \frac{1}{8}g^{2}\alpha_{h}H^{4} + (\phi^{0})^{4} + 4(\phi^{+}\phi^{-})^{2} + 4(\phi^{0})^{2}\phi^{+}\phi^{-} + 4H^{2}\phi^{+}\phi^{-} + 2(\phi^{0})^{2}H^{2}] - \frac{1}{8}g^{2}\alpha_{h}H^{4} + (\phi^{0})^{4} + 4(\phi^{+}\phi^{-})^{2} + 4(\phi^{0})^{2}\phi^{+}\phi^{-} + 4H^{2}\phi^{+}\phi^{-} + 4H^{2}\phi^{-} + 4H^$ $gMV^+_{\mu}W^-_{\mu}H - \frac{1}{2}g\frac{M}{c_w^2}Z^0_{\mu}Z^0_{\mu}H - \frac{1}{2}ig[W^+_{\mu}(\phi^0\partial_{\mu}\phi^- - \phi^-\partial_{\mu}\phi^0) - \psi^0]$ $W^-_{\mu}\overline{(\phi^0}\partial_{\mu}\phi^+ - \phi^+\partial_{\mu}\overline{\phi^0})] + \frac{1}{2}g[W^+_{\mu}(H\partial_{\mu}\phi^- - \phi^-\partial_{\mu}H) - W^-_{\mu}(H\partial_{\mu}\phi^+ - \phi^-\partial_{\mu}H)] + \frac{1}{2}g[W^+_{\mu}(H\partial_{\mu}\phi^- - \phi^-\partial_{\mu}H) - W^-_{\mu}(H\partial_{\mu}\phi^- - \phi^-\partial_{\mu}H)] + \frac{1}{2}g[W^+_{\mu}(H\partial_{\mu}\phi^- - \phi^-\partial_{\mu}H)] + \frac{1}{2}g[W^+_{\mu}(H\partial_{\mu}H)] + \frac{1}{2}g[W^+_{\mu}($ $\phi^{+}\partial_{\mu}H)] + \frac{1}{2}g\frac{1}{c_{w}}(Z^{0}_{\mu}(H\partial_{\mu}\phi^{0} - \phi^{0}\partial_{\mu}H) - ig\frac{s^{2}_{w}}{c_{w}}MZ^{0}_{\mu}(W^{+}_{\mu}\phi^{-} - W^{-}_{\mu}\phi^{+}) +$ $igs_w MA_{\mu}(W^{+}_{\mu}\phi^{-} - W^{-}_{\mu}\phi^{+}) - ig\frac{1-2c_w^2}{2c_w}Z^{0}_{\mu}(\phi^{+}\partial_{\mu}\phi^{-} - \phi^{-}\partial_{\mu}\phi^{+}) +$ $igs_w A_\mu (\phi^+ \partial_\mu \phi^- - \phi^- \partial_\mu \phi^+) - \frac{1}{4}g^2 W^+_\mu W^-_\mu [H^2 + (\phi^0)^2 + 2\phi^+ \phi^-] - \frac{1}{4}g^2 W^+_\mu W^-_\mu [H^2 + (\phi^0)^2 + 2\phi^+ \phi^-] - \frac{1}{4}g^2 W^+_\mu W^-_\mu [H^2 + (\phi^0)^2 + 2\phi^+ \phi^-] - \frac{1}{4}g^2 W^+_\mu W^-_\mu [H^2 + (\phi^0)^2 + 2\phi^+ \phi^-] - \frac{1}{4}g^2 W^+_\mu W^-_\mu [H^2 + (\phi^0)^2 + 2\phi^+ \phi^-] - \frac{1}{4}g^2 W^+_\mu W^-_\mu [H^2 + (\phi^0)^2 + 2\phi^+ \phi^-] - \frac{1}{4}g^2 W^+_\mu W^-_\mu [H^2 + (\phi^0)^2 + 2\phi^+ \phi^-] - \frac{1}{4}g^2 W^+_\mu W^-_\mu [H^2 + (\phi^0)^2 + 2\phi^+ \phi^-] - \frac{1}{4}g^2 W^+_\mu W^-_\mu [H^2 + (\phi^0)^2 + 2\phi^+ \phi^-] - \frac{1}{4}g^2 W^+_\mu W^-_\mu [H^2 + (\phi^0)^2 + 2\phi^+ \phi^-] - \frac{1}{4}g^2 W^+_\mu W^-_\mu [H^2 + (\phi^0)^2 + 2\phi^+ \phi^-] - \frac{1}{4}g^2 W^+_\mu W^-_\mu [H^2 + (\phi^0)^2 + 2\phi^+ \phi^-] - \frac{1}{4}g^2 W^+_\mu W^-_\mu [H^2 + (\phi^0)^2 + 2\phi^+ \phi^-] - \frac{1}{4}g^2 W^+_\mu W^-_\mu [H^2 + (\phi^0)^2 + 2\phi^+ \phi^-] - \frac{1}{4}g^2 W^+_\mu W^-_\mu [H^2 + (\phi^0)^2 + 2\phi^+ \phi^-] - \frac{1}{4}g^2 W^+_\mu W^-_\mu [H^2 + (\phi^0)^2 + 2\phi^+ \phi^-] - \frac{1}{4}g^2 W^+_\mu W^-_\mu [H^2 + (\phi^0)^2 + 2\phi^+ \phi^-] - \frac{1}{4}g^2 W^+_\mu W^-_\mu [H^2 + (\phi^0)^2 + 2\phi^+ \phi^-] - \frac{1}{4}g^2 W^+_\mu W^-_\mu [H^2 + (\phi^0)^2 + 2\phi^+ \phi^-] - \frac{1}{4}g^2 W^+_\mu W^-_\mu [H^2 + (\phi^0)^2 + 2\phi^+ \phi^-] - \frac{1}{4}g^2 W^+_\mu W^-_\mu [H^2 + (\phi^0)^2 + 2\phi^+ \phi^-] - \frac{1}{4}g^2 W^+_\mu W^-_\mu [H^2 + (\phi^0)^2 + 2\phi^+ \phi^-] - \frac{1}{4}g^2 W^+_\mu W^-_\mu [H^2 + (\phi^0)^2 + 2\phi^+ \phi^-] - \frac{1}{4}g^2 W^+_\mu W^-_\mu [H^2 + (\phi^0)^2 + 2\phi^+ \phi^-] - \frac{1}{4}g^2 W^+_\mu W^-_\mu [H^2 + (\phi^0)^2 + 2\phi^+ \phi^-] - \frac{1}{4}g^2 W^+_\mu W^-_\mu [H^2 + (\phi^0)^2 + 2\phi^+ \phi^-] - \frac{1}{4}g^2 W^+_\mu W^-_\mu [H^2 + (\phi^0)^2 + 2\phi^+ \phi^-] - \frac{1}{4}g^2 W^+_\mu W^-_\mu [H^2 + (\phi^0)^2 + 2\phi^+ \phi^-] - \frac{1}{4}g^2 W^+_\mu W^-_\mu [H^2 + (\phi^0)^2 + 2\phi^+ \phi^-] - \frac{1}{4}g^2 W^+_\mu W^-_\mu [H^2 + (\phi^0)^2 + 2\phi^+ \phi^-] - \frac{1}{4}g^2 W^+_\mu W^-_\mu [H^2 + 2\phi^+ \phi^-] - \frac{1}{4}g^2 W^+_\mu W^-_\mu [H^2 + 2\phi^+ \phi^-] - \frac{1}{4}g^2 W^+_\mu W^-_\mu [H^2 + 2\phi^- \phi^-] - \frac{1}{4}g^2 W^+_\mu W^-_\mu [$ $\underbrace{\frac{1}{4}g^2 \frac{1}{c_w^2}}_{\mu} Z^0_{\mu} Z^0_{\mu} [H^2 + (\phi^0)^2 + 2(2s_w^2 - 1)^2 \phi^+ \phi^-] - \frac{1}{2}g^2 \frac{s_w^2}{c_w} Z^0_{\mu} \phi^0 (W^+_{\mu} \phi^- + 1)^2 \phi^+ \phi^-] - \frac{1}{2}g^2 \frac{s_w^2}{c_w} Z^0_{\mu} \phi^0 (W^+_{\mu} \phi^- + 1)^2 \phi^+ \phi^-] - \frac{1}{2}g^2 \frac{s_w^2}{c_w} Z^0_{\mu} \phi^0 (W^+_{\mu} \phi^- + 1)^2 \phi^+ \phi^-] - \frac{1}{2}g^2 \frac{s_w^2}{c_w} Z^0_{\mu} \phi^0 (W^+_{\mu} \phi^- + 1)^2 \phi^+ \phi^-] - \frac{1}{2}g^2 \frac{s_w^2}{c_w} Z^0_{\mu} \phi^0 (W^+_{\mu} \phi^- + 1)^2 \phi^+ \phi^-] - \frac{1}{2}g^2 \frac{s_w^2}{c_w} Z^0_{\mu} \phi^0 (W^+_{\mu} \phi^- + 1)^2 \phi^+ \phi^-] - \frac{1}{2}g^2 \frac{s_w^2}{c_w} Z^0_{\mu} \phi^0 (W^+_{\mu} \phi^- + 1)^2 \phi^+ \phi^-] - \frac{1}{2}g^2 \frac{s_w^2}{c_w} Z^0_{\mu} \phi^0 (W^+_{\mu} \phi^- + 1)^2 \phi^+ \phi^-] - \frac{1}{2}g^2 \frac{s_w^2}{c_w} Z^0_{\mu} \phi^0 (W^+_{\mu} \phi^- + 1)^2 \phi^+ \phi^-] - \frac{1}{2}g^2 \frac{s_w^2}{c_w} Z^0_{\mu} \phi^0 (W^+_{\mu} \phi^- + 1)^2 \phi^+ \phi^-]$ $\overline{W_{\mu}^{-}\phi^{+}} - \frac{1}{2}ig^{2}\frac{s_{w}^{2}}{c}Z_{\mu}^{0}H(W_{\mu}^{+}\phi^{-} - W_{\mu}^{-}\phi^{+}) + \frac{1}{2}g^{2}s_{w}A_{\mu}\phi^{0}(W_{\mu}^{+}\phi^{-} + W_{\mu}^{-}\phi^{-}) + \frac{1}{2}g^{2}s_{w}A_{\mu}\phi^{0}(W_{\mu}^{+}\phi^{-}) + \frac{1}{2}g^{$
$$\begin{split} W^{-}_{\mu}\phi^{+}) + \frac{1}{2}ig^{2}s_{w}A_{\mu}H(W^{+}_{\mu}\phi^{-} - W^{-}_{\mu}\phi^{+}) - g^{2}\frac{s_{w}}{c_{w}}(2c_{w}^{2} - 1)Z^{0}_{\mu}A_{\mu}\phi^{+}\phi^{-} - g^{1}s_{w}^{2}A_{\mu}A_{\mu}\phi^{+}\phi^{-} - \bar{e}^{\lambda}(\gamma\partial + m_{e}^{\lambda})e^{\lambda} - \bar{\nu}^{\lambda}\gamma\partial\nu^{\lambda} - \bar{u}_{j}^{\lambda}(\gamma\partial + m_{u}^{\lambda})u_{j}^{\lambda} - \bar{v}^{\lambda}(\gamma\partial + m_{u}^{\lambda})u_{j}^{\lambda} - \bar{v}^{\lambda}($$
 $\overline{d}_{i}^{\lambda}(\gamma\partial + m_{d}^{\lambda})d_{i}^{\lambda} + igs_{w}A_{\mu}[-(\overline{e}^{\lambda}\gamma^{\mu}e^{\lambda}) + \frac{2}{3}(\overline{u}_{i}^{\lambda}\gamma^{\mu}u_{i}^{\lambda}) - \frac{1}{3}(\overline{d}_{i}^{\lambda}\gamma^{\mu}d_{i}^{\lambda})] +$ $\frac{ig}{4c_w}Z^0_\mu[(\bar{\nu}^\lambda\gamma^\mu(1+\gamma^5)\nu^\lambda) + (\bar{e}^\lambda\gamma^\mu(4s_w^2 - 1 - \gamma^5)e^\lambda) + (\bar{u}_i^\lambda\gamma^\mu(\frac{4}{3}s_w^2 - 1 - \gamma^5)e^\lambda) + (\bar{u}_i^\lambda\gamma^\mu(\frac{4}{3}s_w^2 - 1 - \gamma^5)e^\lambda) + (\bar{u}_i^\lambda\gamma^\mu(1+\gamma^5)\nu^\lambda) + (\bar{e}^\lambda\gamma^\mu(1+\gamma^5)e^\lambda) + (\bar{e}^\lambda\gamma$ $(1 - \gamma^{5})u_{j}^{\lambda}) + (\bar{d}_{j}^{\lambda}\gamma^{\mu}(1 - \frac{8}{3}s_{w}^{2} - \gamma^{5})d_{j}^{\lambda})] + \frac{ig}{2\sqrt{2}}W_{\mu}^{+}[(\bar{\nu}^{\lambda}\gamma^{\mu}(1 + \gamma^{5})e^{\lambda}) + (\bar{d}_{j}^{\lambda}\gamma^{\mu}(1 - \frac{8}{3}s_{w}^{2} - \gamma^{5})d_{j}^{\lambda})] + (\bar{d}_{j}^{\lambda}\gamma^{\mu}(1 - \frac{8}{3}s_{w}^{2} - \gamma^{5})d_{j}^{\lambda})]$ $(\bar{u}_j^{\lambda}\gamma^{\mu}(1+\gamma^5)C_{\lambda\kappa}d_j^{\kappa})] + \frac{ig}{2\sqrt{2}}W_{\mu}^{-}[(\bar{e}^{\lambda}\gamma^{\mu}(1+\gamma^5)\nu^{\lambda}) + (\bar{d}_j^{\kappa}C_{\lambda\kappa}^{\dagger}\gamma^{\mu}(1+\gamma^5)\nu^{\lambda})] + (\bar{d}_j^{\kappa}C_{\lambda\kappa}^{\dagger}\gamma^{\mu}(1+\gamma^5)\nu^{\lambda}) + (\bar{d}_j^{\kappa}C_{\lambda\kappa}^{\prime}\gamma^{\mu}(1+\gamma^5)\nu^{\lambda}) + (\bar{d}_j^{\kappa}C_{\lambda\kappa}^{\prime}\gamma^{\mu}(1+\gamma^5)\nu^{\lambda}) + (\bar{d}_j^{\kappa}C_{\lambda\kappa}^{\prime}\gamma^{\mu}(1+\gamma^5)\nu^{\lambda}) + (\bar{d}_j^{\kappa}C_{\lambda\kappa}^$ $\gamma^{5}(u_{j}^{\lambda})] + \frac{ig}{2\sqrt{2}} \frac{m_{e}^{\lambda}}{M} \left[-\phi^{+}(\bar{\nu}^{\lambda}(1-\gamma^{5})e^{\lambda}) + \phi^{-}(\bar{e}^{\lambda}(1+\gamma^{5})\nu^{\lambda})\right] \frac{g}{2}\frac{m_e^{\lambda}}{M}[H(\bar{e}^{\lambda}e^{\lambda}) + i\phi^0(\bar{e}^{\lambda}\gamma^5 e^{\lambda})] + \frac{ig}{2M\sqrt{2}}\phi^+[-m_d^{\kappa}(\bar{u}_j^{\lambda}C_{\lambda\kappa}(1-\gamma^5)d_j^{\kappa}) +$ $m_u^{\lambda}(\bar{u}_j^{\lambda}C_{\lambda\kappa}(1+\gamma^5)d_j^{\kappa}] + \frac{ig}{2M\sqrt{2}}\phi^-[m_d^{\lambda}(\bar{d}_j^{\lambda}C_{\lambda\kappa}^{\dagger}(1+\gamma^5)u_j^{\kappa}) - m_u^{\kappa}(\bar{d}_j^{\lambda}C_{\lambda\kappa}^{\dagger}(1-\gamma^5)u_j^{\kappa})] + \frac{ig}{2M\sqrt{2}}\phi^-[m_d^{\lambda}(\bar{d}_j^{\lambda}C_{\lambda\kappa}^{\dagger}(1+\gamma^5)u_j^{\kappa}) - m_u^{\kappa}(\bar{d}_j^{\lambda}C_{\lambda\kappa}^{\dagger}(1+\gamma^5)u_j^{\kappa})] + \frac{ig}{2M\sqrt{2}}\phi^-[m_d^{\lambda}(\bar{d}_j^{\lambda}C_{\lambda\kappa}^{\dagger}(1+\gamma^5)u_j^{\kappa}) - m_u^{\kappa}(\bar{d}_j^{\lambda}C_{\lambda\kappa}^{\prime}(1+\gamma^5)u_j^{\kappa})] + \frac{ig}{2M\sqrt{2}}\phi^-[m_d^{\lambda}(\bar{d}_j^{\lambda}C_{\lambda\kappa}^{\prime}(1+\gamma^5)u_j^{\kappa}) - m_u^{\kappa}(\bar{d}_j^{\lambda}C_{\lambda\kappa}^{\prime}(1+\gamma^5)u_j^{\kappa})] + \frac{ig}{2M\sqrt{2}}\phi^-[m_d^{\lambda}(\bar{d}_j^{\lambda}C_{\lambda\kappa}^{\prime}(1+\gamma^5)u_j^{\kappa})] + \frac{ig}{2M\sqrt{2}}\phi^-[m_d^{\lambda}(\bar{d}_j^{\lambda}C_{\lambda\kappa}^{\prime}(1+\gamma^5)u_j^{\kappa})] + \frac{ig}{2M\sqrt{2}}\phi^-[m_d^{\lambda}(\bar{d}_j^{\lambda}C_{\lambda\kappa}^{\prime}(1+\gamma^5)u_j^{\kappa})] + \frac{ig}{2M\sqrt{2}}\phi^-[m_d^{\lambda}(\bar{d}_j^{\lambda}C_{\lambda\kappa}^{\prime}(1+\gamma^5)u_j^{\kappa})] + \frac{ig}{2M\sqrt{2}}\phi^-[m_d^{\lambda}(\bar{d}_j^{\lambda}C_{\lambda\kappa}^{\prime}(1+\gamma^5)u_j^{\kappa})] + \frac{ig}{2M\sqrt{2}}\phi^-[m_d^{\lambda}(\bar{d}_j^$ $\gamma^{5} u_{j}^{\kappa} - \frac{g m_{u}^{\lambda}}{M} H(\bar{u}_{j}^{\lambda} u_{j}^{\lambda}) - \frac{g m_{d}^{\lambda}}{2} H(\bar{d}_{j}^{\lambda} d_{j}^{\lambda}) + \frac{ig m_{u}^{\lambda}}{2} M^{0}(\bar{u}_{j}^{\lambda} \gamma^{5} u_{j}^{\lambda}) - \frac{g m_{u}^{\lambda}}{2} H(\bar{d}_{j}^{\lambda} d_{j}^{\lambda}) + \frac{ig m_{u}^{\lambda}}{2} H(\bar{u}_{j}^{\lambda} \gamma^{5} u_{j}^{\lambda}) - \frac{g m_{u}^{\lambda}}{2} H(\bar{u}_{j}^{\lambda} u_{j}^{\lambda}) + \frac{g m_{u}^{\lambda}}{2} H(\bar{u}_{j}^{$ $\underbrace{\frac{ig}{2}\frac{m_d^{\lambda}}{M}\phi^0(\bar{d}_j^{\lambda}\gamma^5d_j^{\lambda})}_{ij} + \underbrace{\bar{X}^+(\partial^2 - M^2)X^+ + \bar{X}^-(\partial^2 - M^2)X^- + \bar{X}^0(\partial^2 - M^2)X^- + \bar{X}^0($ 5 $\frac{M^2}{c^2}X^0 + \bar{Y}\partial^2 Y + igc_w W^+_{\mu}(\partial_{\mu}\bar{X}^0X^- - \partial_{\mu}\bar{X}^+X^0) + igs_w W^+_{\mu}(\partial_{\mu}\bar{Y}X^- - \partial_{\mu}\bar{X}^+X^0)$ $\partial_{\mu}\bar{X}^{+}Y) + igc_{w}W_{\mu}^{-}(\partial_{\mu}\bar{X}^{-}X^{0} - \partial_{\mu}\bar{X}^{0}X^{+}) + igs_{w}W_{\mu}^{-}(\partial_{\mu}\bar{X}^{-}Y - \partial_{\mu}\bar{X}^{-}) +$ $\partial_{\mu}\bar{Y}X^{+}) + igc_{w}Z^{0}_{\mu}(\partial_{\mu}\bar{X}^{+}X^{+} - \partial_{\mu}\bar{X}^{-}X^{-}) + igs_{w}A_{\mu}(\partial_{\mu}\bar{X}^{+}X^{+} - \partial_{\mu}\bar{X}^{-}X^{-}) + igs_{w}A_{\mu}(\partial_{\mu}\bar{X}^{+}X^{+}) + igc_{w}Z^{0}_{\mu}(\partial_{\mu}\bar{X}^{+}X^{+}) + igc$ $\partial_{\mu}\bar{X}^{-}X^{-}) - \frac{1}{2}gM[\bar{X}^{+}X^{+}H + \bar{X}^{-}X^{-}H + \frac{1}{c_{\cdots}^{2}}\bar{X}^{0}X^{0}H] +$ $\frac{1-2c_w^2}{2c_w}igM[\bar{X}^+X^0\phi^+ - \bar{X}^-X^0\phi^-] + \frac{1}{2c_w}igM[\bar{X}^0X^-\phi^+ - \bar{X}^0X^+\phi^-] + 10$ $igMs_w[\bar{X}^0X^-\phi^+ - \bar{X}^0X^+\phi^-] + \frac{1}{2}igM[\bar{X}^+X^+\phi^0 - \bar{X}^-X^-\phi^0]$

The Gauge Sector

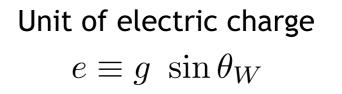
Gauge fields before SSB (massless)

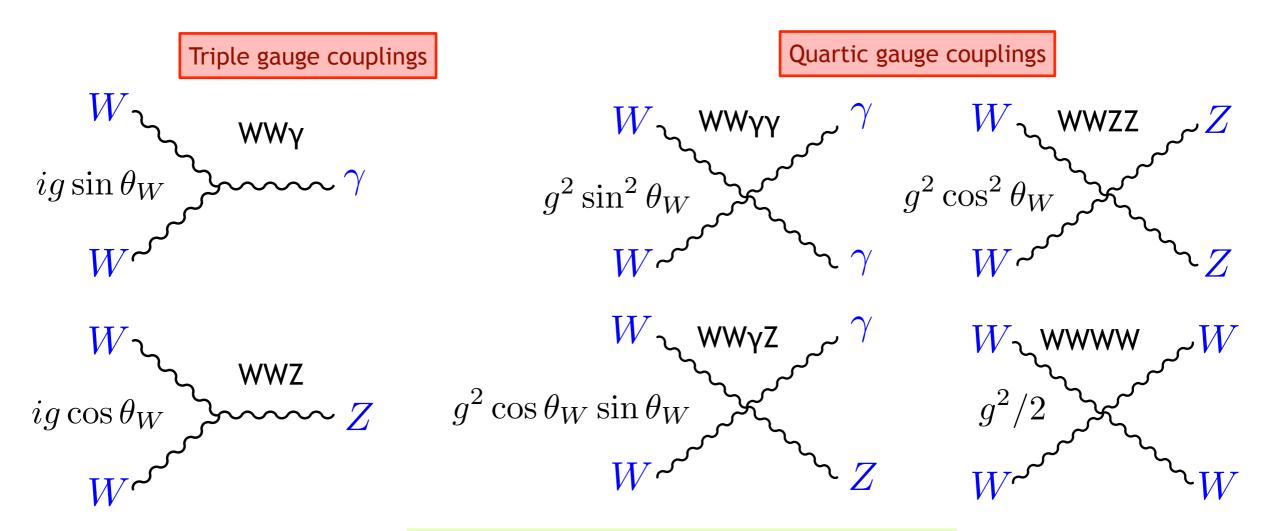
- $SU(2)_L$ (coupling = g) W^1 , W^2 and W^3
- U(1)_Y (coupling = g') B

Physical boson fields after SSB

- weak bosons (massive) W^+ , W^- and Z
- photon (massless)
 γ

Weak mixing angle $\tan \theta_W \equiv g'/g$

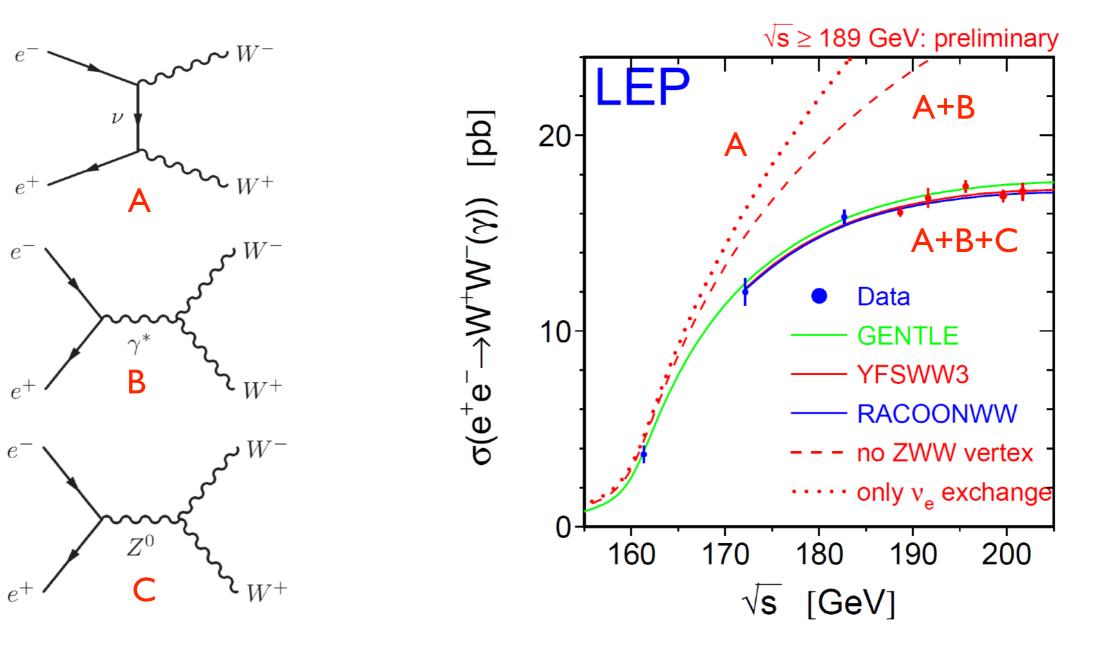




Triple and quartic gauge couplings are central predictions of the Electroweak theory

LEP-2 : W Pair Production

W-pair production in e^+e^- collisions:



Clear observation of triple gauge couplings (circa 2000 @ CERN)

amplitudes B & C are essential to avoid an high-energy catastrophe (violation of unitarity)

The Higgs Sector

v

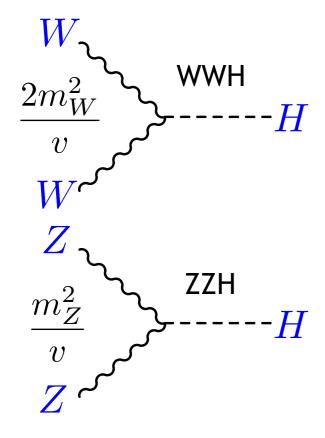
Higgs field v.e.v.

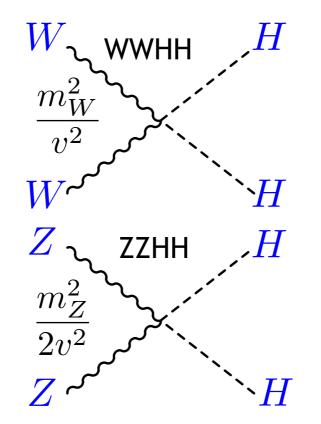
$$= \sqrt{-\mu^2/2\lambda}$$

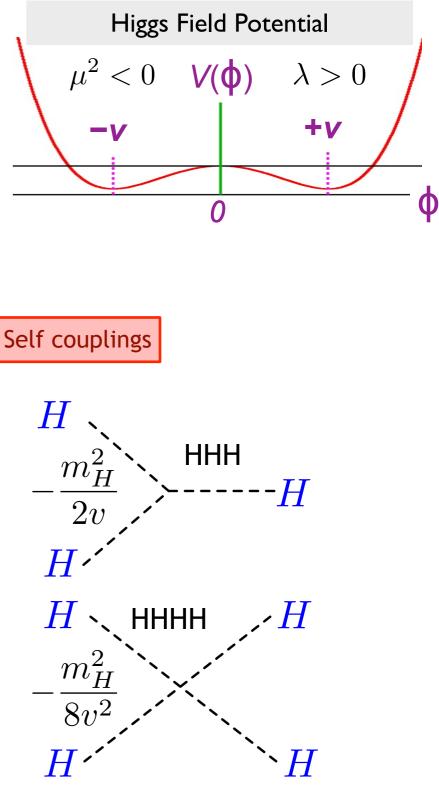
Higgs boson mass $m_H = \sqrt{2\lambda}v$

$$m_W \equiv \frac{gv}{2}$$
 and $m_Z \equiv \frac{gv}{2\cos\theta_W}$









EWK Radiative Corrections

Observables can be calculated in the SM in term of a finite number of parameters to be determined experimentally (coupling constants, masses of fermions, CKM and $M_{\rm H}$)

$$\rho \equiv \frac{m_W^2}{m_Z^2 \cos^2 \theta_W} \quad (= 1) \qquad s_W^2 \equiv 1 - \frac{m_W^2}{m_Z^2} \quad (= \sin^2 \theta_W)$$

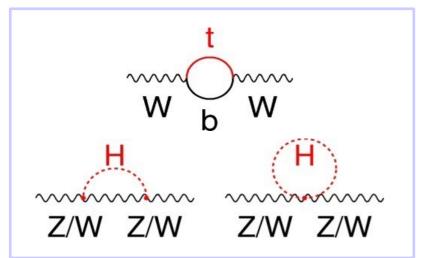
Link with Fermi theory
$$m_W^2 = \frac{\pi}{\sqrt{2}G_{\rm F}} \frac{\alpha}{\sin^2 \theta_W}$$

➡ Physical quantities

$$\rho = 1 + \Delta \rho$$
$$M_W^2 = m_W^2 \left(1 + \Delta r\right) \quad \text{and} \quad \sin^2 \theta_W^{\text{eff}} = s_W^2 (1 + \Delta \kappa)$$

with

$$\Delta r, \Delta \rho, \Delta \kappa = f(m_t^2, \ln(m_H), \dots)$$

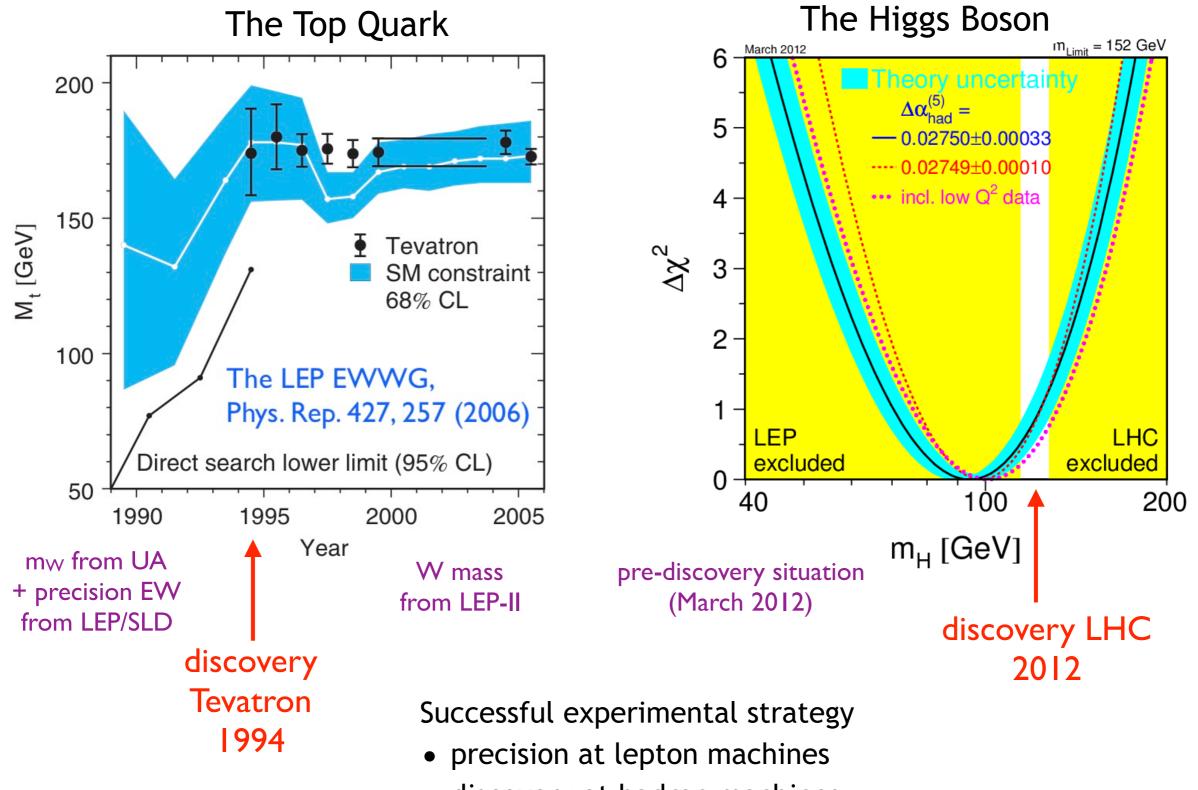


$$\Delta \rho_t \simeq 0.01 \times \left[\frac{m_t}{(175 \text{ GeV})} \right]^2$$

 $\Delta \rho_H \simeq -0.0015 \times \log(m_H/M_W)$

the electroweak radiative correction parameters are of the order of the percent and involve contributions from top quark and Higgs boson loops

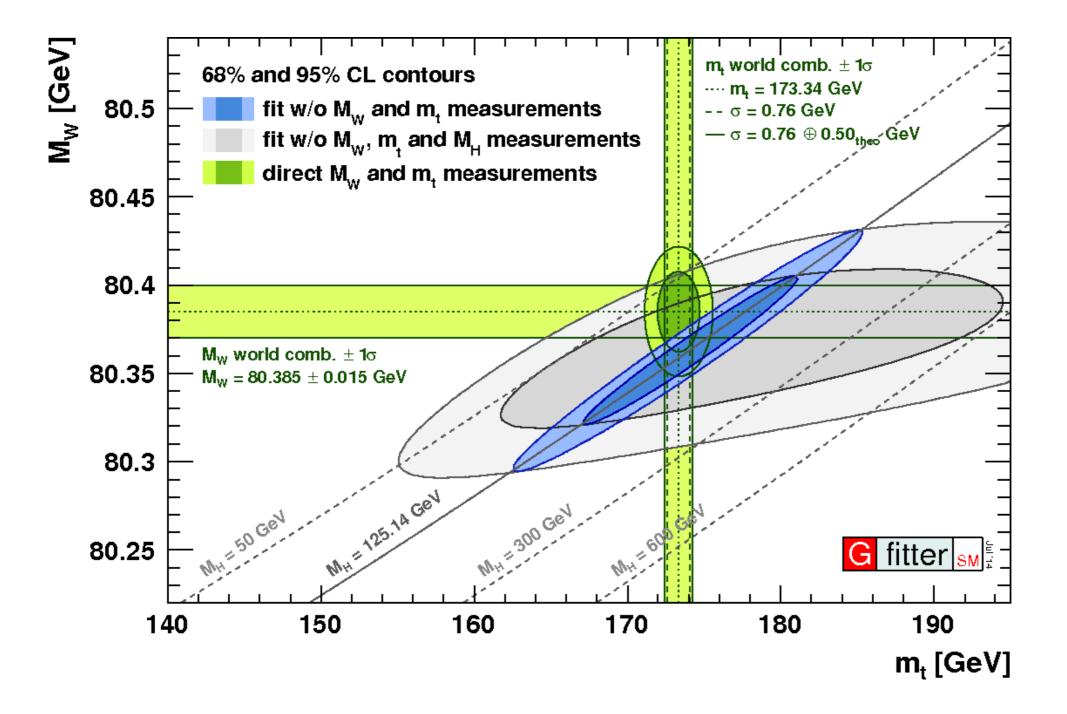
Predictive Power of the SM



discovery at hadron machines

The Electroweak Fit

Through quantum corrections, the theory establishes relations between measurable parameters

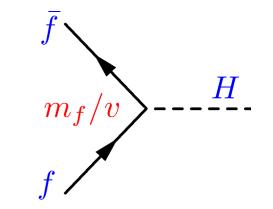


Fermion and Boson Masses

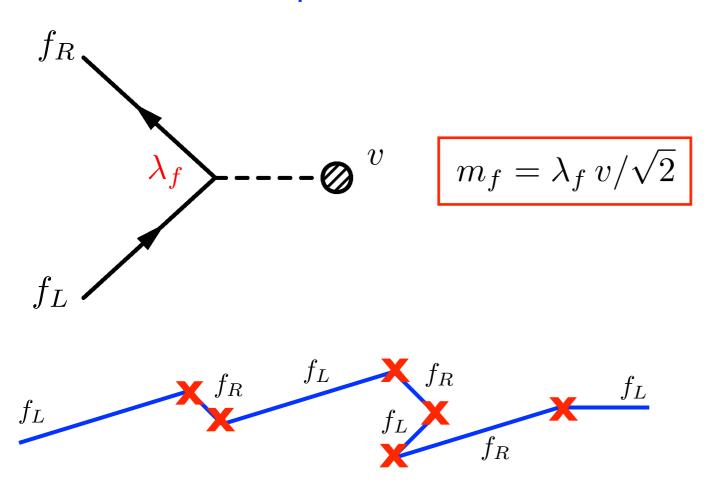
Yukawa interaction terms between fermions and the Higgs field

- Lorentz scalar
- gauge invariant

$$\lambda_f(\overline{F_L}\phi)f_R + \text{h.c.} \longrightarrow m_f \overline{f}f + m_f/v \overline{f}fh$$

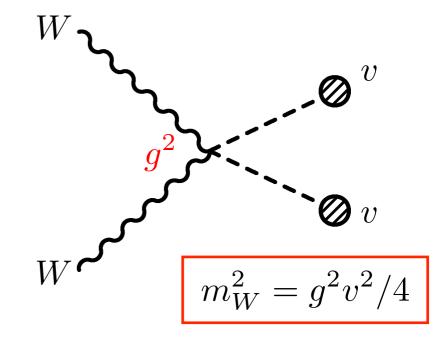


Fermions acquire mass



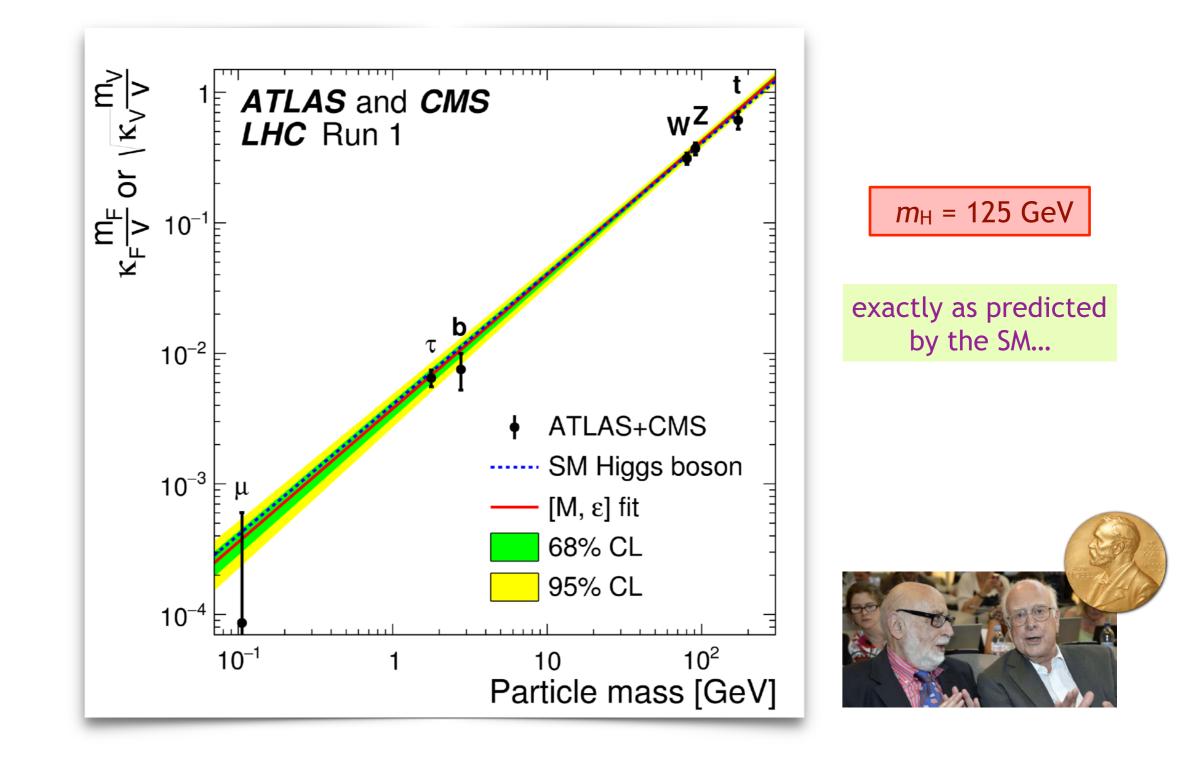
Higgs condensate connects left- and right- components

Bosons acquire mass

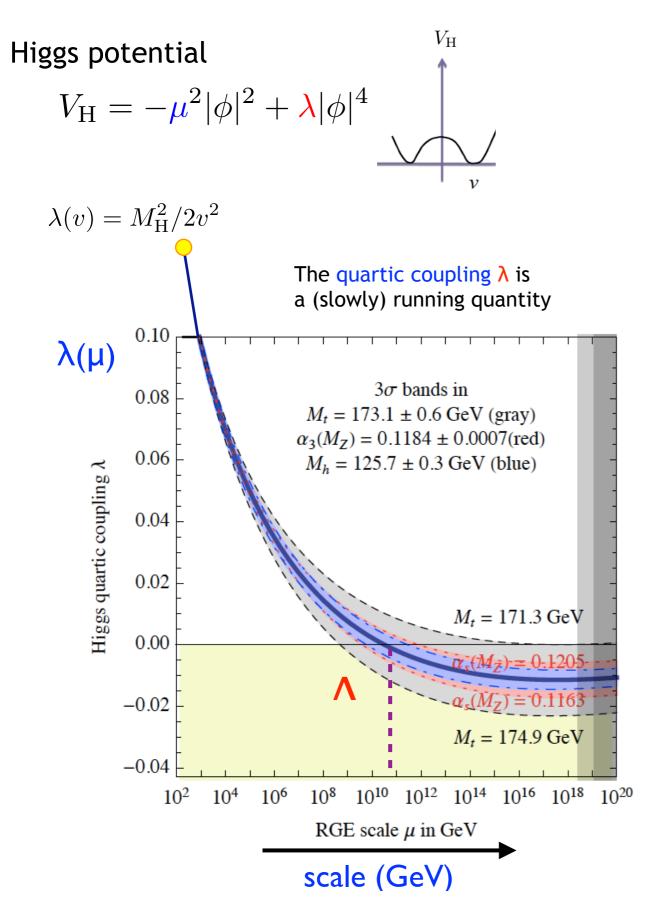


W and Z Bosons acquire a longitudinal polarisation through interaction with the Higgs condensate

The Higgs Boson's Signature

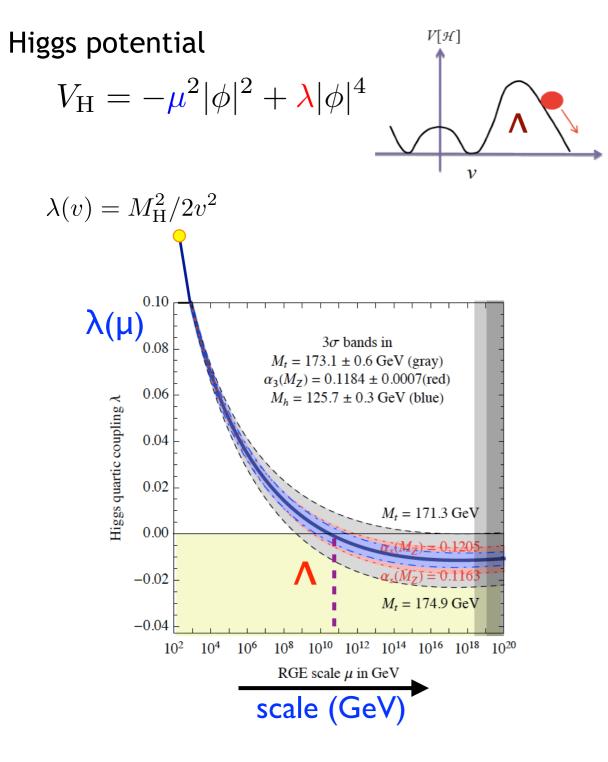


EW Vacuum Stability

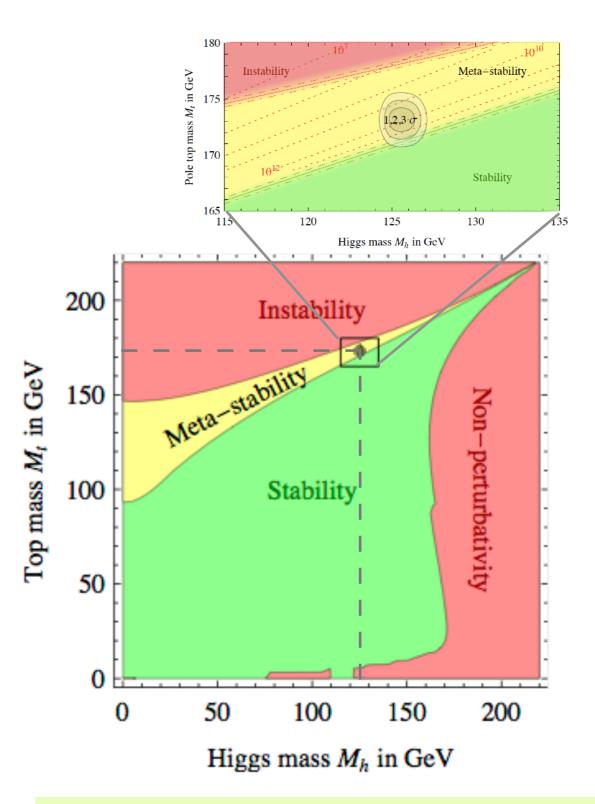


The instability scale of the SM, which depends on m_t , M_H , and α_s is of order $\Lambda \approx 10^{11}$ GeV !

EW Vacuum Stability



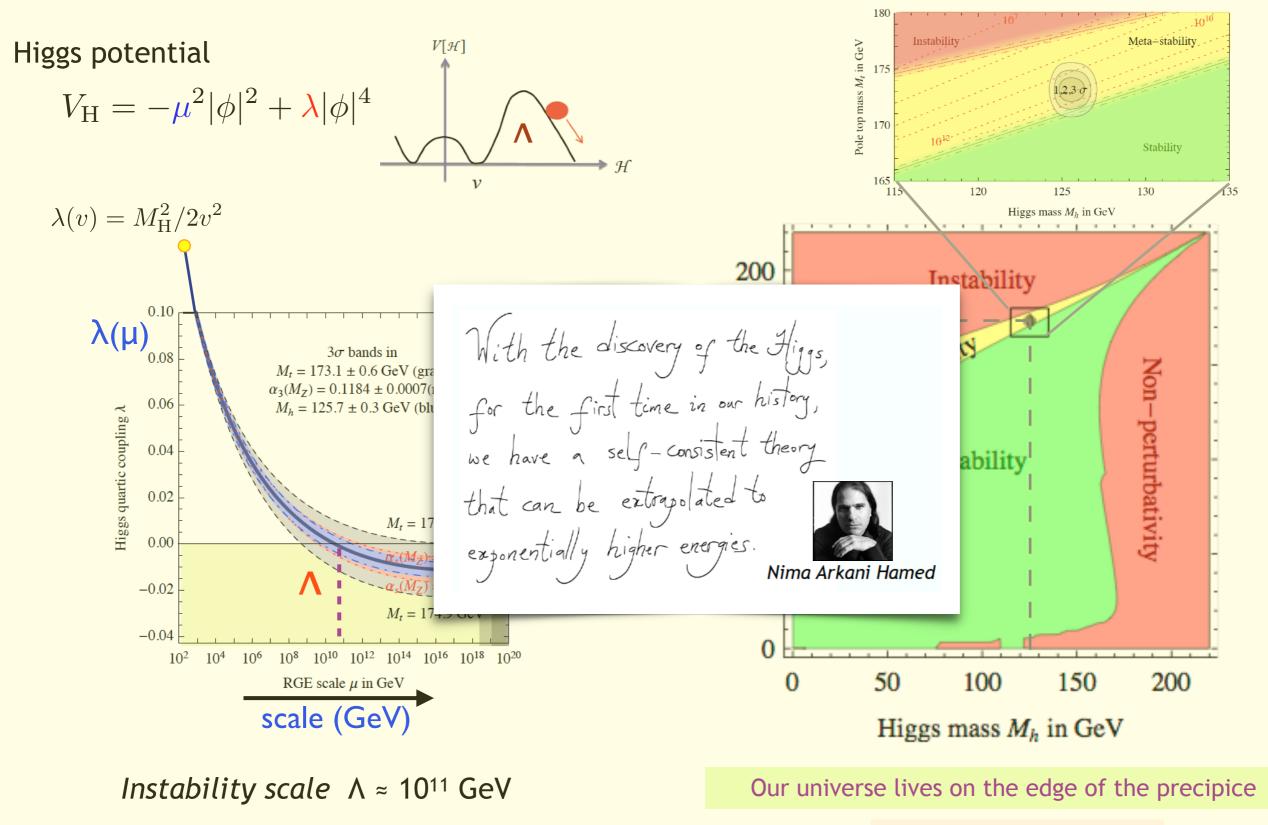




Our universe lives on the edge of the precipice

Numerical coincidence or fundamental feature ?

EW Vacuum Stability



Numerical coincidence or fundamental feature ?

Is this the End of History?



2010

Asymptotic safety of gravity and the Higgs boson mass

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12 January 2010

Abstract

PLB 683 (2010) 196

There are indications that gravity is asymptotically safe. The Standard Model (SM) plus gravity could be valid up to arbitrarily high energies. Supposing that this is indeed the case and assuming that there are no intermediate energy scales between the Fermi and Planck scales we address the question of whether the mass of the Higgs boson m_H can be predicted. For a positive gravity induced anomalous dimension $A_{\lambda} > 0$ the running of the quartic scalar self interaction λ at scales beyond the Planck mass is determined by a fixed point at zero. This results in $m_H = m_{\min} = 126$ GeV, with only a few GeV uncertainty. This prediction is independent of the details of the short distance running and holds for a wide class of extensions of the SM as well. For $A_{\lambda} < 0$ one finds m_H in the interval $m_{\min} < m_H < m_{\max} \simeq 174$ GeV, now sensitive to A_{λ} and other properties of the short distance running. The case $A_{\lambda} > 0$ is favored by explicit computations existing in the literature.

In conclusion, we discussed the possibility that the SM, supplemented by the asymptotically safe gravity plays the role of a fundamental, rather than effective field theory. We found that this may be the case if the gravity contributions to the running of the Yukawa and Higgs coupling have appropriate signs. The mass of the Higgs scalar is predicted $m_H = m_{\min} \simeq 126$ GeV with a few GeV uncertainty if all the couplings of the Standard Model, with the exception of the Higgs self-interaction λ , are asymptotically free, while λ is strongly attracted to an approximate fixed point $\lambda = 0$ (in the limit of vanishing Yukawa and gauge couplings) by the flow in the high energy regime. This can be achieved by a positive gravity induced anomalous dimension for the running of λ . A similar prediction remains valid for exten-

sions of the SM as grand unified theories, provided the split between the unification and Planck-scales remains moderate and all relevant couplings are perturbatively small in the transition region. Detecting the Higgs scalar with mass around 126 GeV at the LHC could give a strong hint for the absence of new physics influencing the running of the SM couplings between the Fermi and Planck/unification scales.

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Abstract

PLB 683 (2010) 196

There are indications that gravity is asymptotically safe. The Standard Model (SM) plus gravity could be valid up to arbitrarily high energies. Supposing that this is indeed the case and assuming that there are no intermediate energy scales between the Fermi and Planck scales we address the question of whether the mass of the Higgs boson m_H can be predicted. For a positive gravity induced anomalous dimension $A_{\lambda} > 0$ the running of the quartic scalar self interaction λ at scales beyond the Planck mass is determined by a fixed point at zero. This results in $m_H = m_{\min} = 126$ GeV, with only a few GeV uncertainty. This prediction is independent of the details of the short distance running and holds for a wide class of extensions of the SM as well. For $A_{\lambda} < 0$ one finds m_H in the interval $m_{\min} < m_H < m_{\max} \simeq 174$ GeV, now sensitive to A_{λ} and other properties of the short distance running. The case $A_{\lambda} > 0$ is favored by explicit computations existing in the literature.

In conclusion, we discussed the possibility that the SM, supplemented by the asymptotically safe gravity plays the role of a fundamental, rather than effective field theory. We found that this may be the case if the gravity contributions to the running of the Yukawa and Higgs coupling have appropriate signs. The mass of the Higgs scalar is predicted $m_H = m_{\min} \simeq 126$ GeV with a few GeV uncertainty if all the couplings of the Standard Model, with the exception of the Higgs self-interaction λ , are asymptotically free, while λ is strongly attracted to an approximate fixed point $\lambda = 0$ (in the limit of vanishing Yukawa and gauge couplings) by the flow in the high energy regime. This can be achieved by a positive gravity induced anomalous dimension for the running of λ . A similar prediction remains valid for exten-

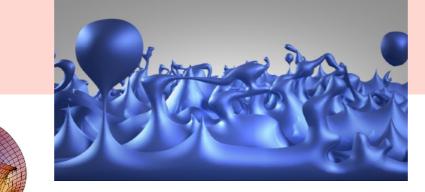
sions of the SM as grand unified theories, provided the split between the unification and Planck-scales remains moderate and all relevant couplings are perturbatively small in the transition region. Detecting the Higgs scalar with mass around 126 GeV at the LHC could give a strong hint for the absence of new physics influencing the running of the SM couplings between the Fermi and Planck/unification scales.

... the answer is: NO!

(I guess)

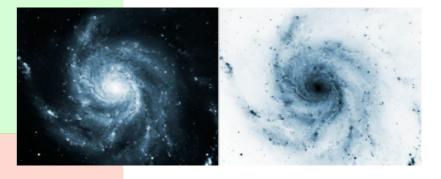
What the SM cannot explain

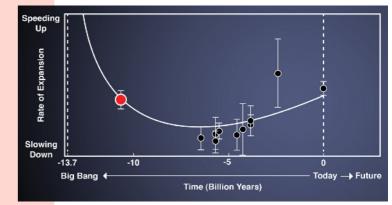
- ➡ the origin of Neutrino Masses
- ➡ the nature of Dark Matter
- the Baryonic Asymmetry of the Universe
- the Accelerated Expansion of the Universe
- + the dynamics of the **Primordial Inflation**
- Gravitation







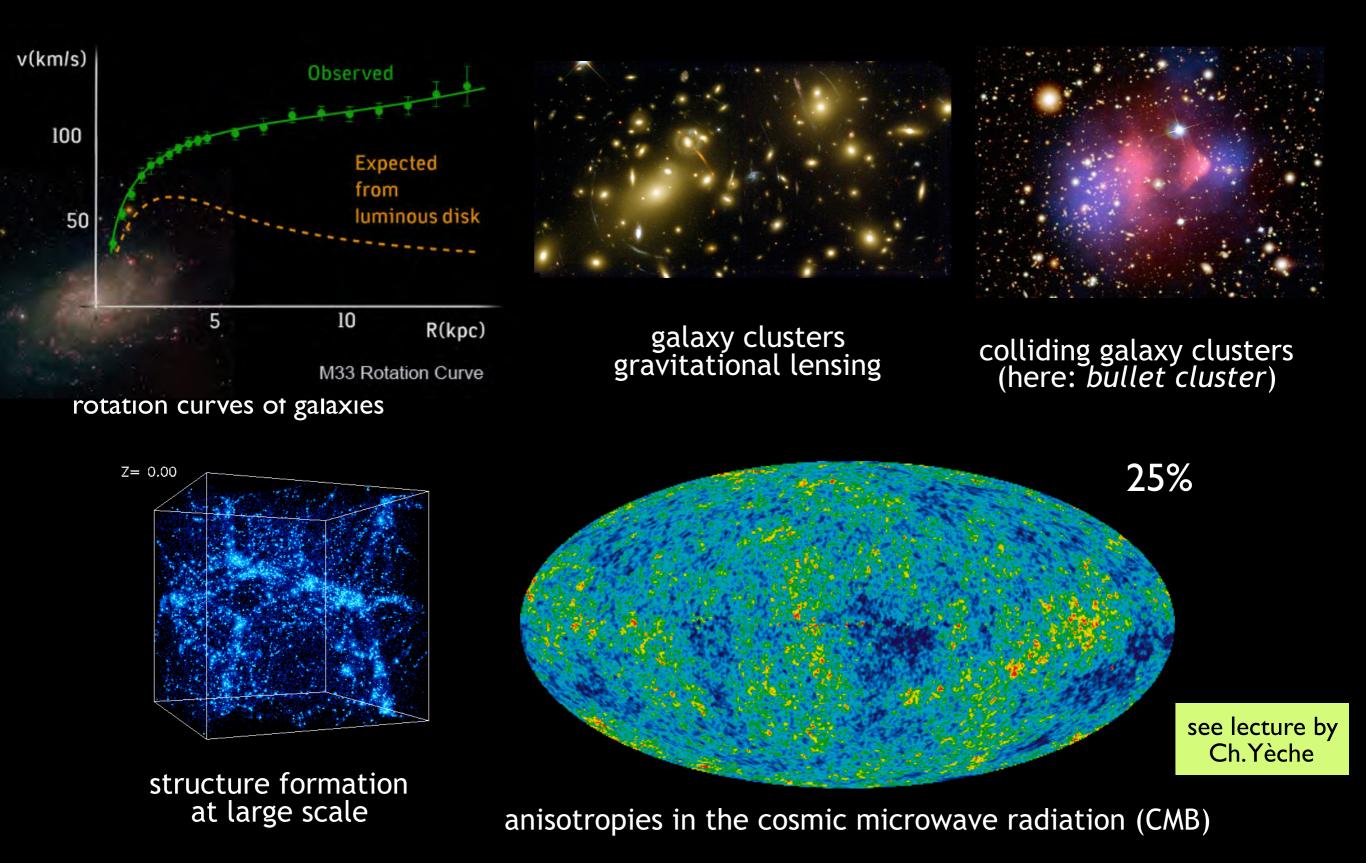




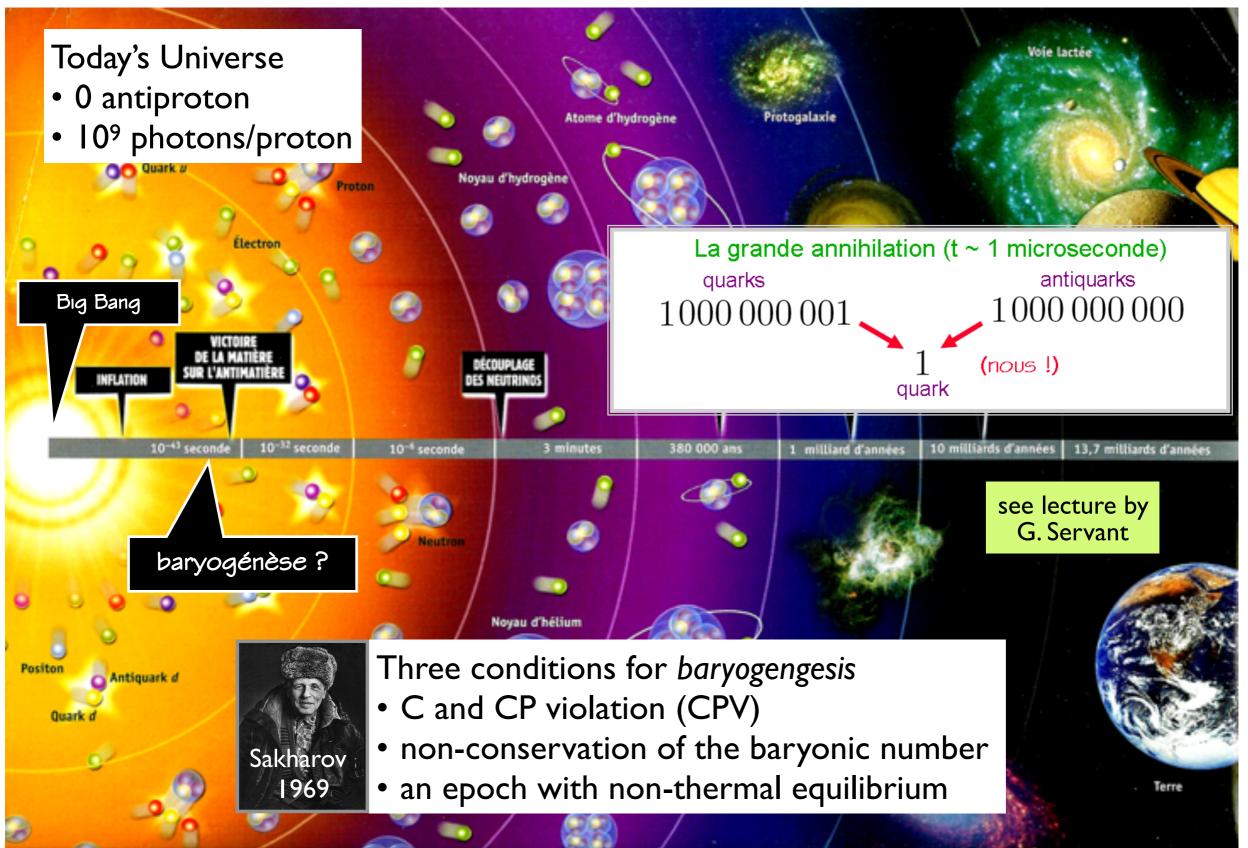


Dark Matter (DM)

Astrophysical Indications all scales



Baryonic Asymmetry of the Universe



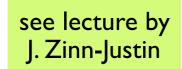
The Unbearable Lightness of the Higgs

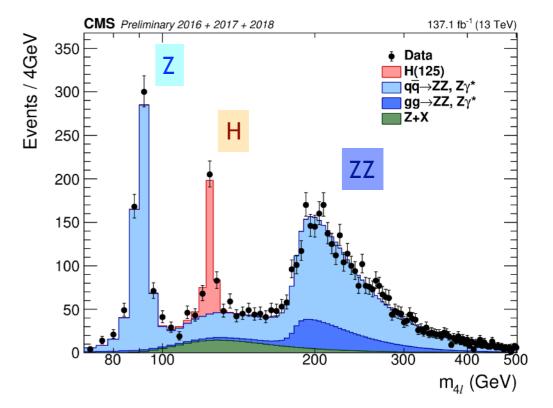
The SM of particle physics is theoretically consistent and incredibly successful at

- describing (almost) all experimental facts
- making non-trivial falsifiable predictions

Still, the SM is not the Theory of Everything (clearly) and it has problems

- aesthetical problems
 - large number of arbitrary parameters (19)
 - failure at unifying gauge couplings at high energy
- ➡ the hierarchy/naturalness problem
 - radiative corrections to $M_{\rm H^2}$
 - in the SM with cut-off $\Lambda \gg M_{\rm H}$ of order Λ^2
 - mind-blowing fine tuning for $\Lambda = M_{Plank}$





Is there a fundamental symmetry protecting the Higgs mass and linking the Z and H bosons?

How much fine tuning can we bear? → HL-LHC (no NP) ≈1% → FCC-hh (no NP) ≈ 0.01%

Physics Beyond the Standard Model

There are convincing reasons to believe that the SM is "only" a low-energy manifestation of a more fundamental theory

Mains goals of most models of physics beyond the SM (BSM):

- 1. solve the Naturalness problem
- 2. provide a Dark Matter candidate
- 3. realise Unification of coupling constants at high energy

Three BSM avenues for naturalness

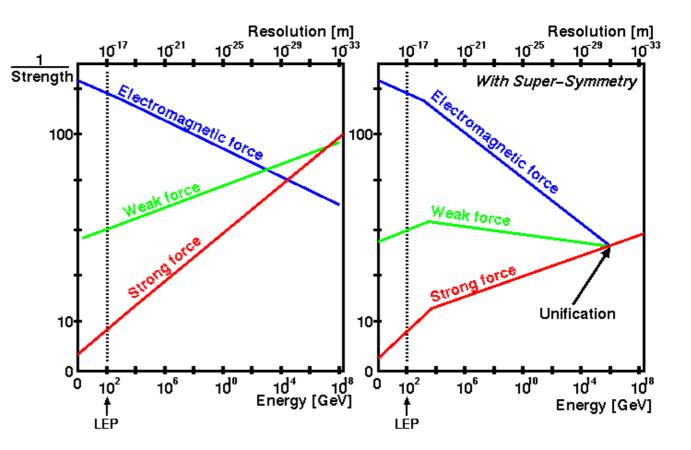
Compositness

Higgs as a bound state of fermions (pseudo Goldstone boson)

• Extra space-time dimensions

where at least spin-2 gravitons propagate (bring gravity scale down to the EW scale)

• Supersymmetry (SUSY)

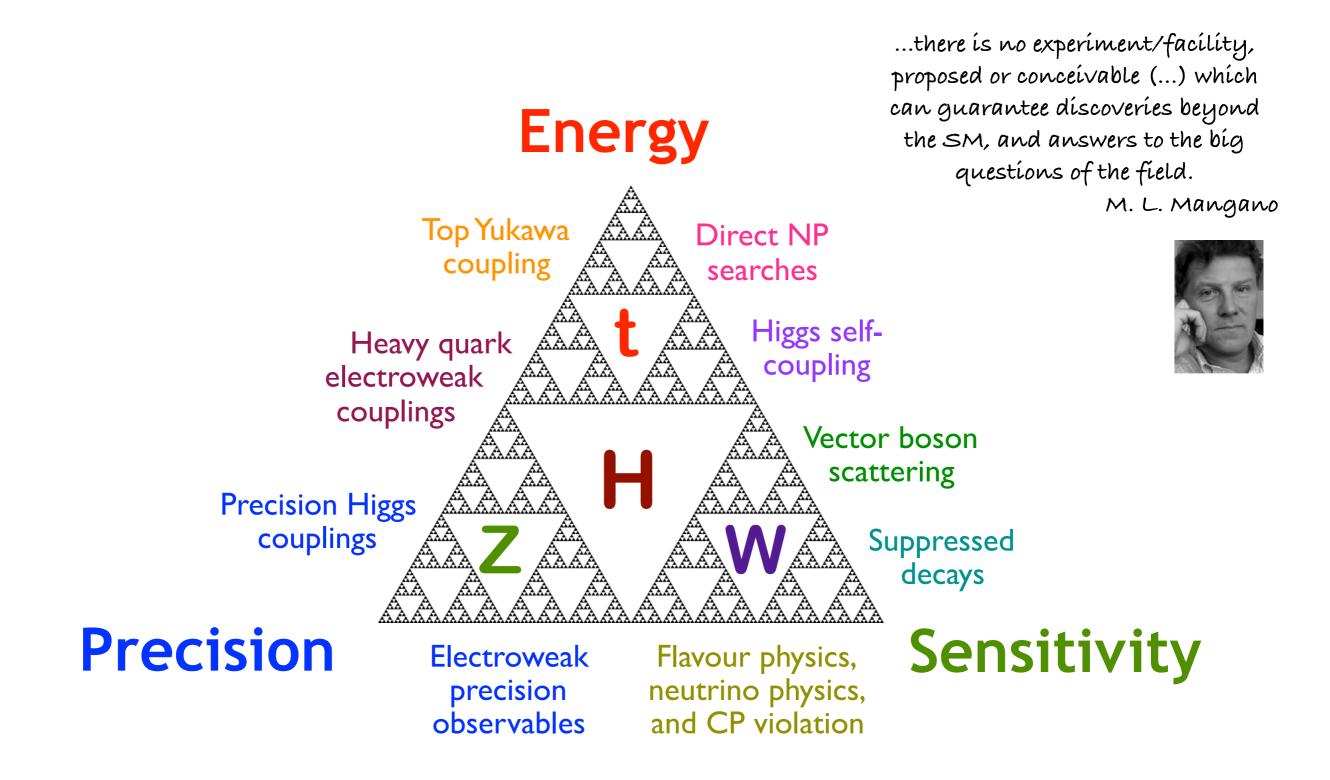




Pre-LHC SUSY models use to address 1, 2, and 3

Post-LHC surviving SUSY models are mostly guided by Naturalness

Experiments to the Rescue?



Which Colliders for Particle Physics?

High-Luminosity LHC

- luminosity×5 starting 2026
- 3000 fb⁻¹ per experiment in 10 years

Project

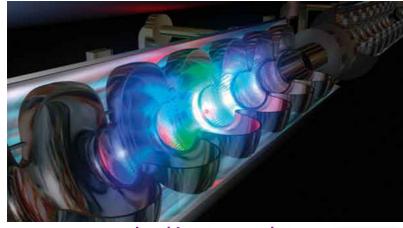








- e⁺e⁻ linear collider
- 250 GeV → 550 GeV



en attente de décision politique

Update of the European Strategy in **Particle Physics** (EPPSU) in progress (2019-2020)

CEPC in China

tunnel 100 km

• 90-250 GeV

• e⁺e⁻ circular collider

see lecture by F. Zimmermann

Project

CLIC

- e⁺e⁻ linear collider
- 380 GeV \rightarrow 3 TeV





| FCC | CM energy | collisions | tunel |
|--------|------------|------------|----------|
| HE-LHC | 27 TeV | РР | LHC |
| FCC-ee | 90-365 GeV | e+e- | 100-km |
| FCC-hh | 100 TeV | PP | TUU-KIII |



Future Collider: Official Parameters

For performance studies, the EPPSU considers conventional sets of machine

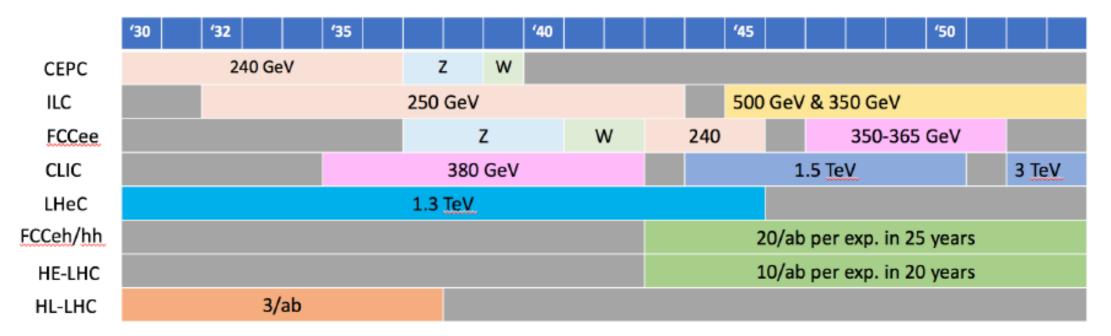
parameters

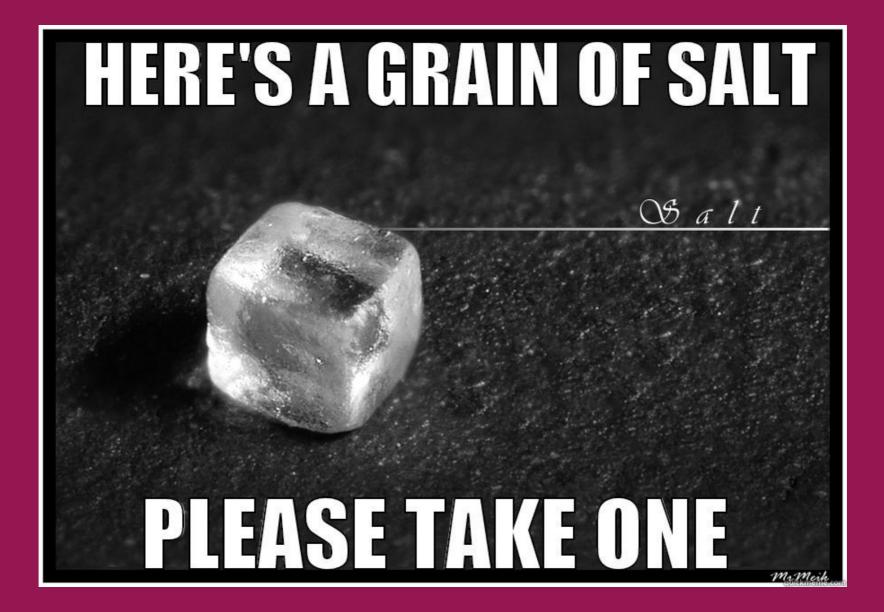
| Collider | Туре | \sqrt{s} | P [%] | N(Det.) | $\mathscr{L}_{\mathrm{inst}}$ | L | Time |
|----------|-------|-------------------------------|-----------------|---------------|---|---|-----------------|
| connuer | Type | V ^B | $[e^{-}/e^{+}]$ | M(Det.) | $[10^{34}] \text{ cm}^{-2} \text{s}^{-1}$ | $\begin{bmatrix} ab^{-1} \end{bmatrix}$ | [years] |
| HL-LHC | pp | 14 TeV | - | 2 | 5 | 6.0 | 12 |
| HE-LHC | pp | 27 TeV | _ | 2 | 16 | 15.0 | $\frac{12}{20}$ |
| FCC-hh | pp | 100 TeV | _ | 2 | 30 | 30.0 | 25 |
| FCC-ee | ee PP | $\frac{100 \text{ fe }}{M_Z}$ | 0/0 | 2 | 100/200 | 150 | 4 |
| | | $2M_W$ | 0/0 | $\frac{2}{2}$ | 25 | 10 | 1-2 |
| | | 240 GeV | 0/0 | $\frac{2}{2}$ | 7 | 5 | 3 |
| | | $2m_{top}$ | 0/0 | $\frac{1}{2}$ | 0.8/1.4 | 1.5 | 5 |
| | | <i>top</i> | 0,0 | - | 010/111 | | (+1) |
| ILC | ee | 250 GeV | $\pm 80/\pm 30$ | 1 | 1.35/2.7 | 2.0 | 11.5 |
| | | 350 GeV | $\pm 80/\pm 30$ | 1 | 1.6 | 0.2 | 1 |
| | | 500 GeV | $\pm 80/\pm 30$ | 1 | 1.8/3.6 | 4.0 | 8.5 |
| | | | | | | | (+1) |
| CEPC | ee | M_Z | 0/0 | 2 | 17/32 | 16 | 2 |
| | | $2M_W$ | 0/0 | 2 | 10 | 2.6 | 1 |
| | | 240 GeV | 0/0 | 2 | 3 | 5.6 | 7 |
| CLIC | ee | 380 GeV | $\pm 80/0$ | 1 | 1.5 | 1.0 | 8 |
| | | 1.5 TeV | $\pm 80/0$ | 1 | 3.7 | 2.5 | 7 |
| | | 3.0 TeV | $\pm 80/0$ | 1 | 6.0 | 5.0 | 8 |
| | | | | | | | (+4) |
| LHeC | ep | 1.3 TeV | - | 1 | 0.8 | 1.0 | 15 |
| HE-LHeC | ep | 2.6 TeV | - | 1 | 1.5 | 2.0 | 20 |
| FCC-eh | ep | 3.5 TeV | - | 1 | 1.5 | 2.0 | 25 |
| | | | | | | | _ |

see lecture by F. Zimmermann

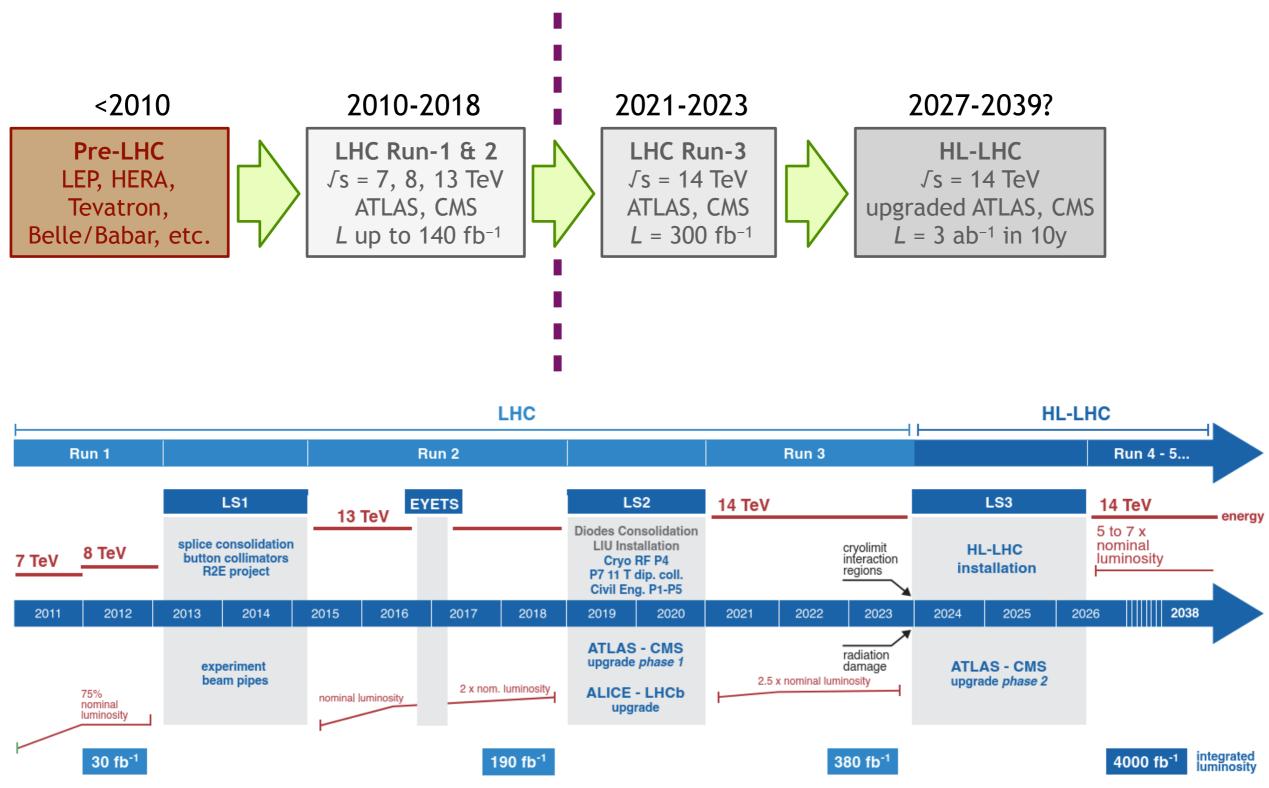
Future Colliders: Official Timelines

| | To | +5 | | | +10 | | | +15 | | | +20 | | | +26 |
|----------------------|------------------------------|------------------------------|--|----------------|-----|---------------------------------|--------------------------|------------|-----------------------------|--|---------------------------------------|--|---|-------------|
| ILC | 0.5/ab 250 GeV | | | 1.5/a 250 G | | | 1.0, 500 | /ab GeV | 0.2/ab 2m _{top} | | 3/ab 500 GeV | | | |
| CEPC | 5.6/ 240 (| | 16/ab 2.6 /ab M _Z 2M _W | | | | | | | | | | | SppC => |
| CLIC | 1.0/ab 380 GeV | | | | | | 2.5/ab 1.5 <u>TeV</u> | | | | 5.0/ab => until +28 3.0 <u>TeV</u> | | | |
| FCC | 150/ab ee, M _z | 10/ab ee, 2M _w | | ′ab Ю GeV | | 1.7/ab ee, 2m _{top} | | | | | | | ļ | hh.eh => |
| LHeC | 0.06/ab | | | 0.2/a | b | | 0.72/ab | | | | | | | |
| HE- LHC | | | | | | | | | | | | | | |
| FCC eh/ <u>hh</u> | | | | | | | | | | | | | | |





Hadron Colliders



from F. Bordry, RRB CERN 29/10/2018

High-Lumi LHC: the only future collider one can say with certain confidence it will actually exist

11:3

->

E lu

HL-LHC Physics in a Nutshell



Higgs, Top and Electroweak

- recision H coupling measurements
- 🖛 m_H, m_W et m_t
- 🖛 H properties: width, CP
- aTGC and aQGC constraints
- 🖛 differential measurements
- rare processes (VBS, VVV, 4-tops)

New Particles and Supersymmetry

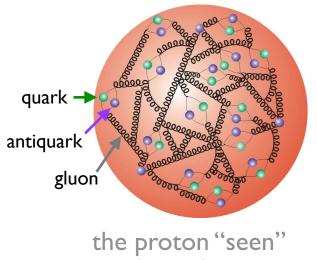
- direct searches of heavy resonances
- searches for new Higgs bosons
- stringent tests of BSM scenarios
- novel techniques allowed by high statistics and better detectors
- rew trigger strategies
- better sensitivity to long-lived particles
- new topologies for Dark Matter searches

Top Quark Factory 2 × 3 billion tt pairs

> Higgs Boson Factory 2 × 150 million H 2 × 120 thousand HH

Flavour Physics rare suppressed decays QCD spectroscopy CKM metrology flavour anomalies

A Quark Gluon Collider



proton

the proton "seen" at short distance (= high energy)

Study of hard interactions

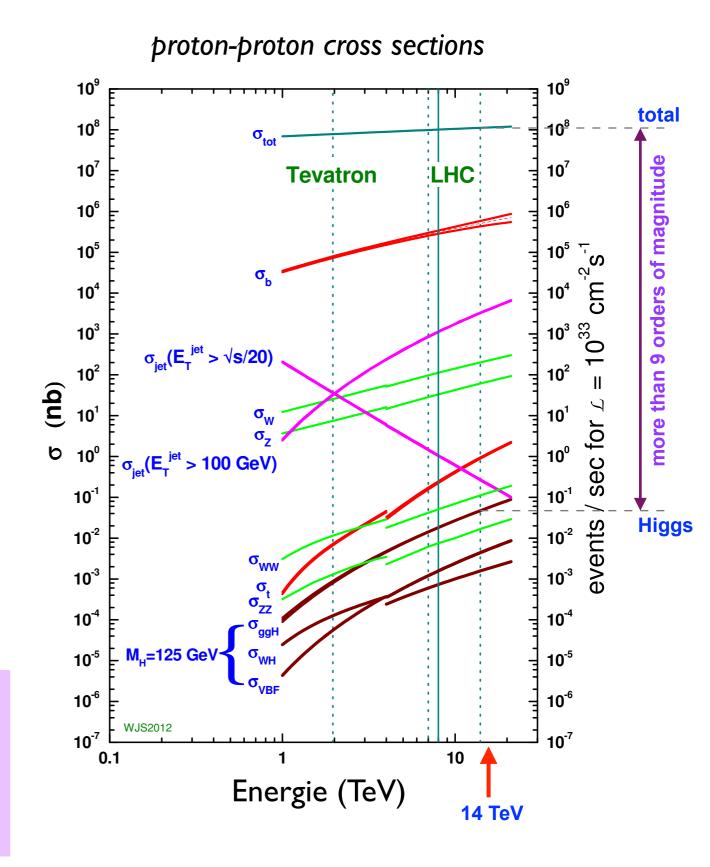
- gluon & gluon (dominant)
- quark & antiquark
- (anti)quark & gluon
- etc.

Cross sections in nanobarn (nb) $rac{1}{r}$ 1 nb = 10⁻³³ cm²

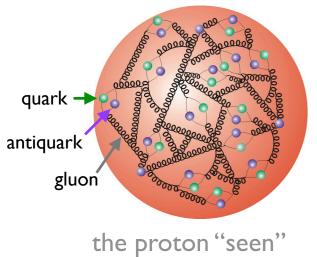
at 14 TeV : σ_{tot} = 10⁸ nb, σ_H = 0.05 nb

Instantaneous luminosity LHC : $\mathcal{L} = 1 \times 10^{34} \text{ cm}^{-2} \text{s}^{-1}$

- ➡ 1 billion inelastic collisions per second
- 1 Higgs boson every 2 seconds



A Quark Gluon Collider



proton

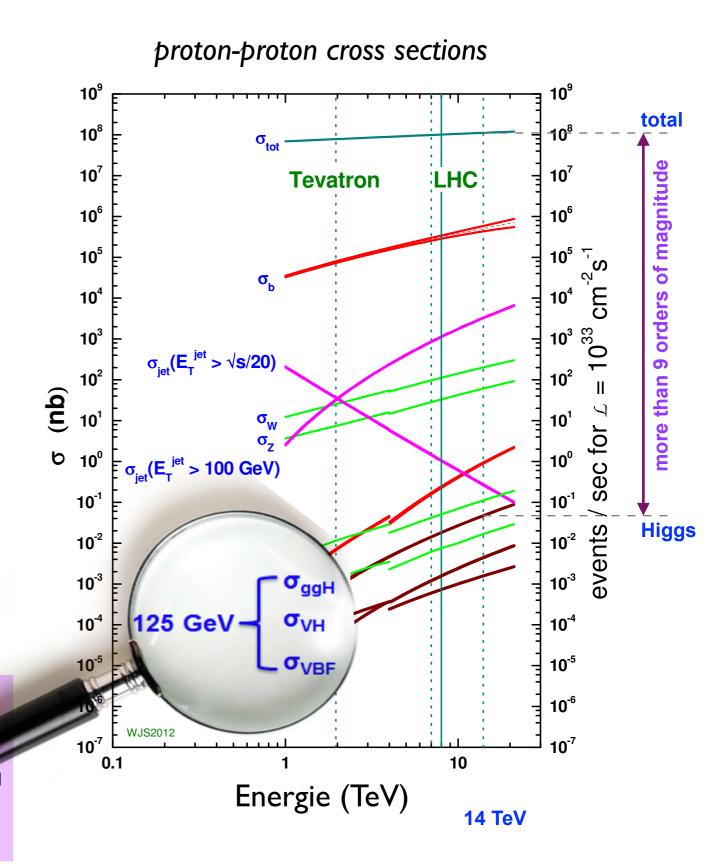
the proton "seen" at short distance (= high energy)

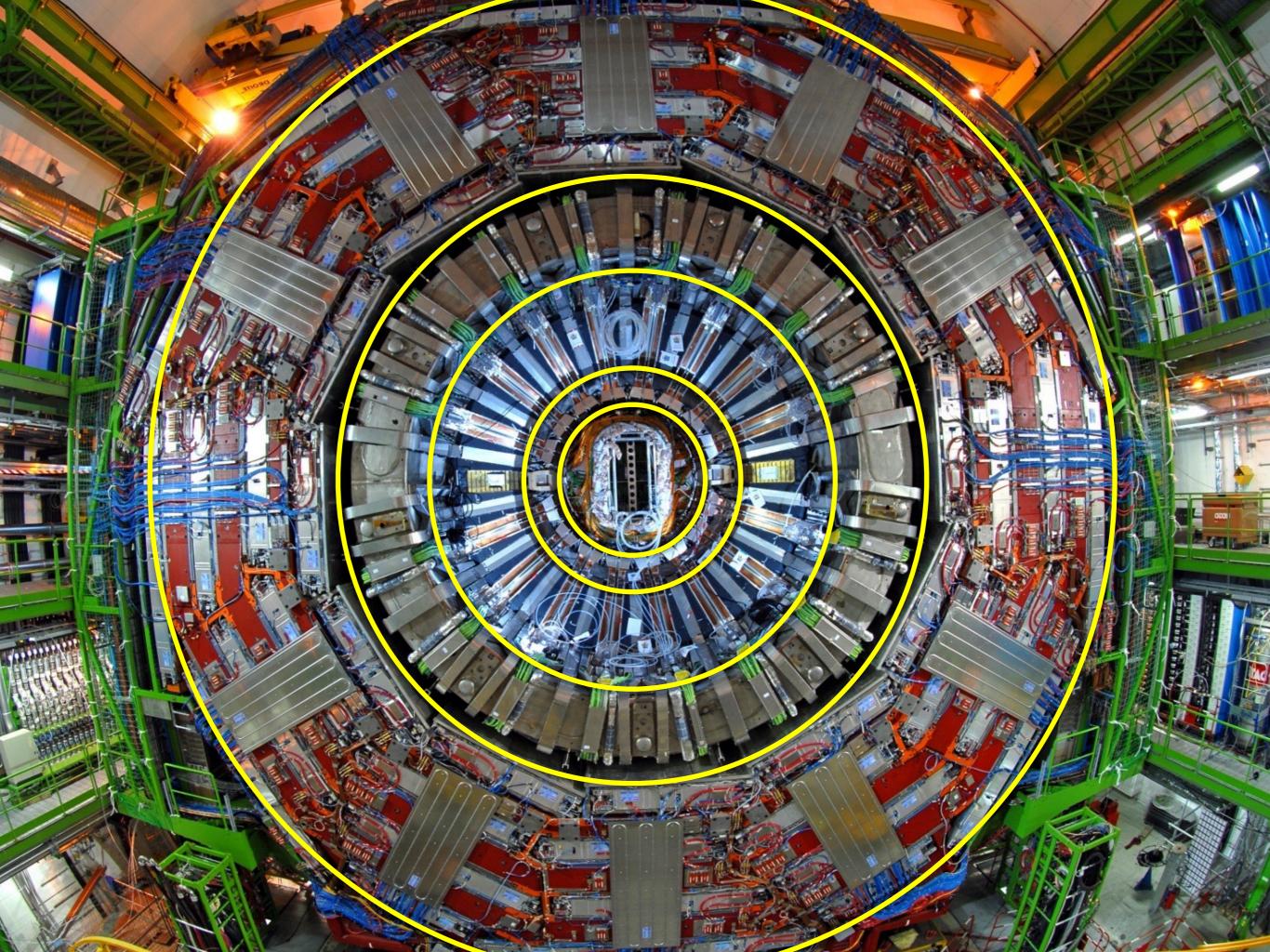
Study of hard interactions

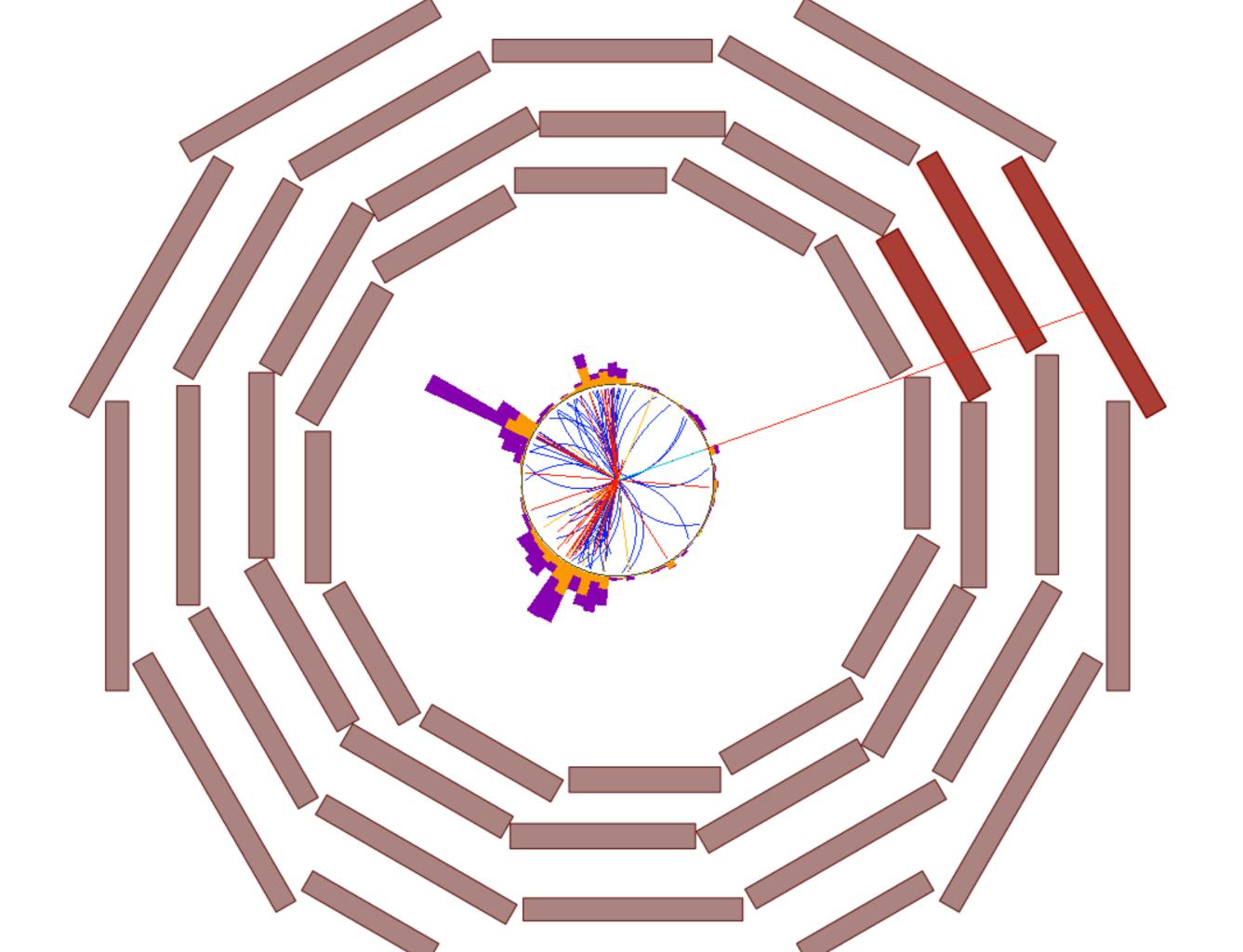
- gluon & gluon (dominant)
- quark & antiquark
- (anti)quark & gluon
- etc.

Cross sections in nanobarn (nb) $rac{1}{r}$ 1 nb = 10⁻³³ cm²

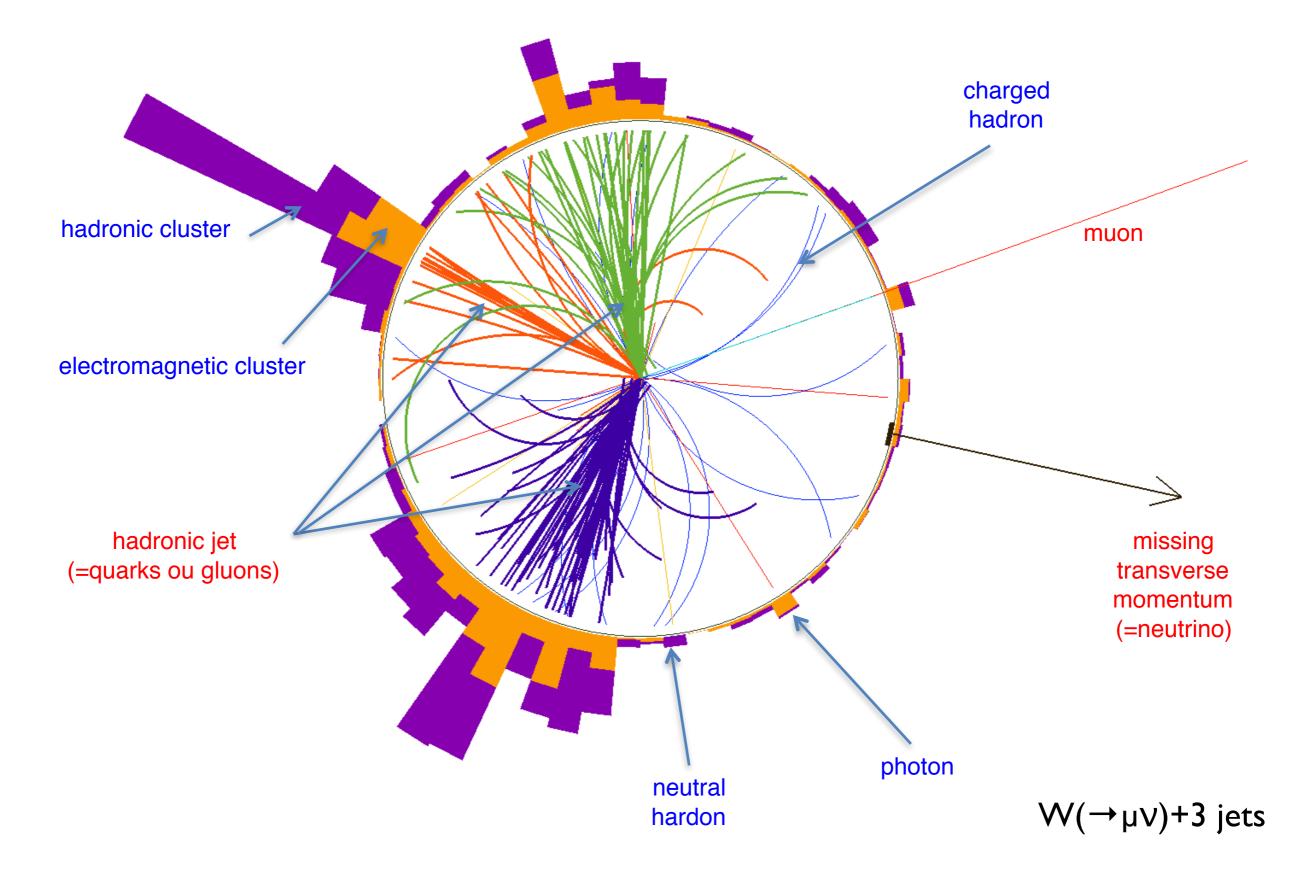
- at 14 TeV : σ_{tot} = 10⁸ nb, σ_H = 0.05 nb Instantaneous luminosity LHC : ℒ = 1×10³⁴ cm⁻²s⁻¹
- 1 billion inelastic collisions per second
- 1 Higgs boson every 2 seconds







"Object" Reconstruction



A Dantesque Environment

Integrated luminosity expressed in inverse-femtobarn (fb⁻¹) ➡ at 14 TeV : 1 fb⁻¹ corresponds to one hundred thousand billion proton collisions

pile-up (PU) = number of inelastic interactions per bunch crossing (every 25 ns)

Ldt=146.9 fb ⁻¹

50

Mean Number of Interactions per Crossing

60

70

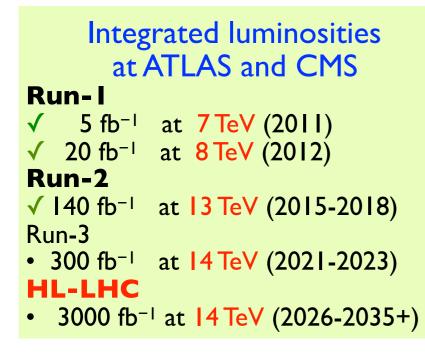
80

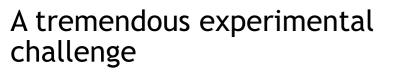
2015: <µ> = 13.4 2016: <µ> = 25.1

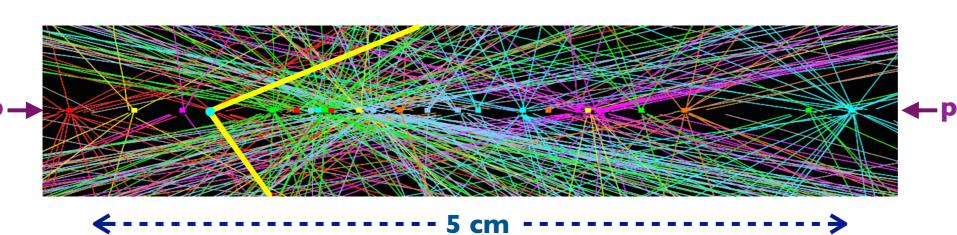
2017: <u> = 37.8

2018: <µ> = 36.1 Total: $<\mu> = 33.7$

ATLAS Online, 13 TeV







600 -

500

400

300

200

100

0

10

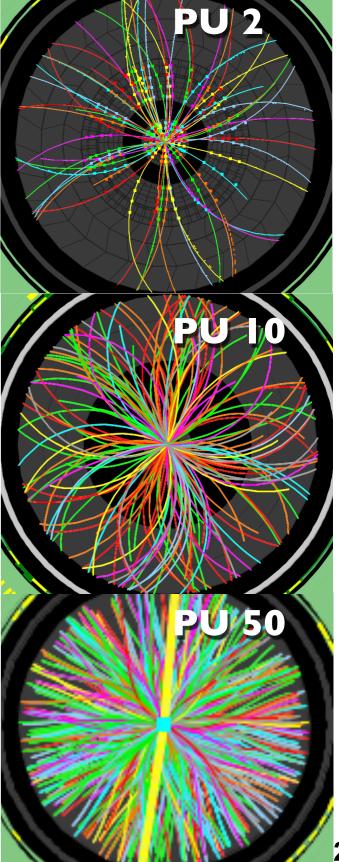
20

30

PU at HL-LHC: 200

40

Recorded Luminosity [pb ⁻¹/0.1]



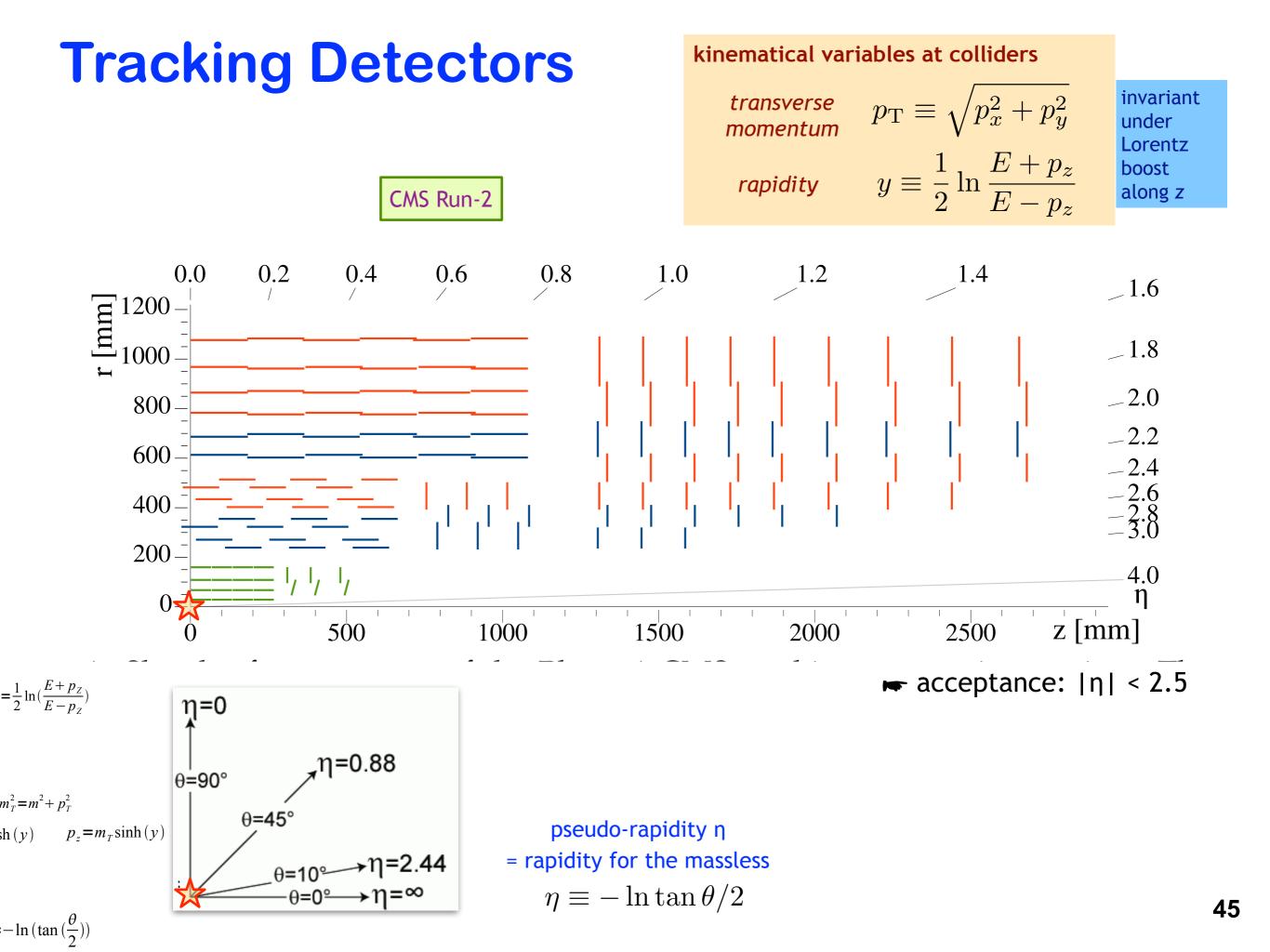


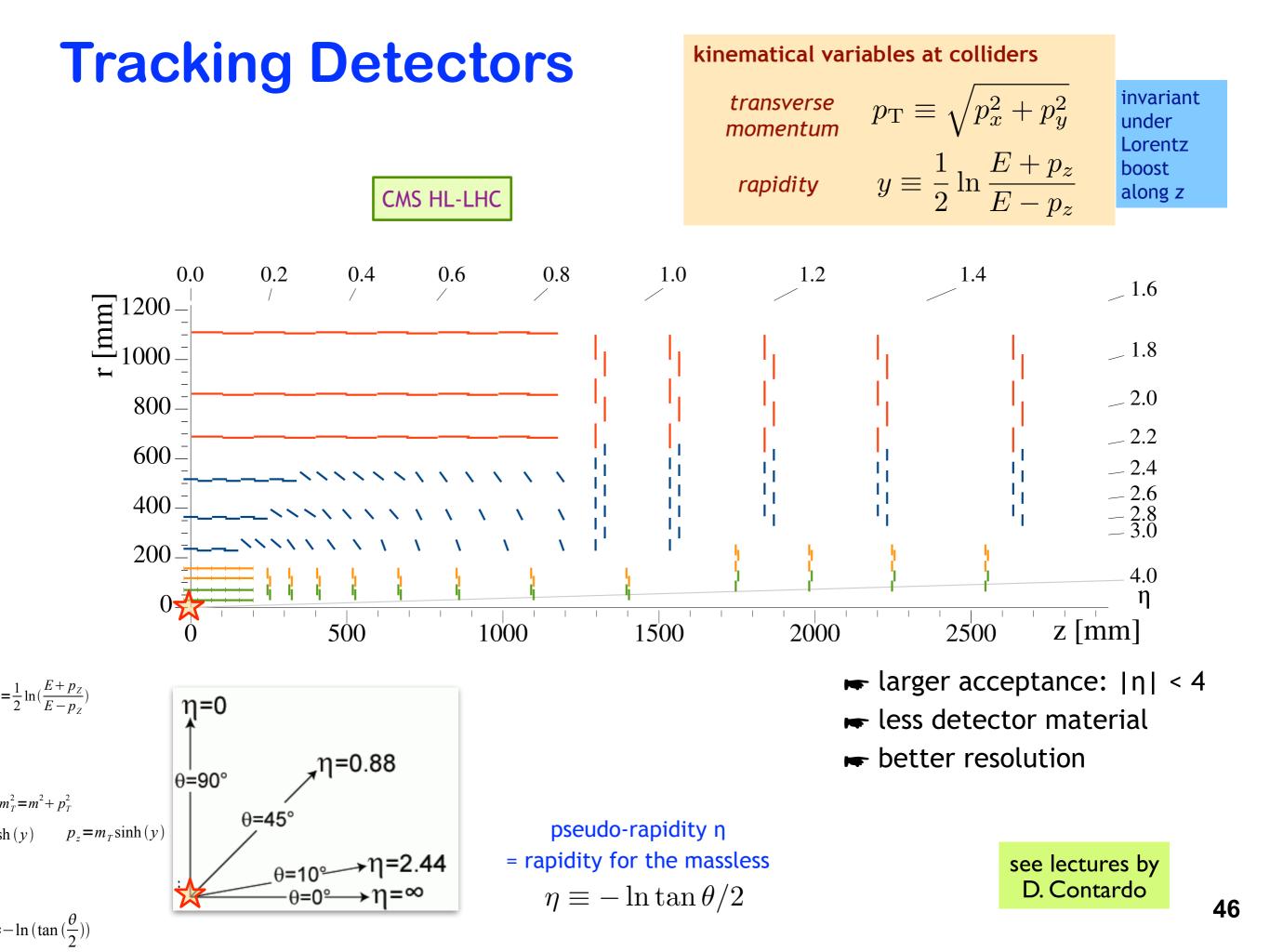
CMS Experiment at LHC. CERN Data recorded: Pri Oct 26 09:06:57 2018 CEST Run/Event: 325309 / 244518 Lumi section: 1 Orbit/Crossing: 121529 / 1650

> 136 pile-up event BX (CMS, October 2018)

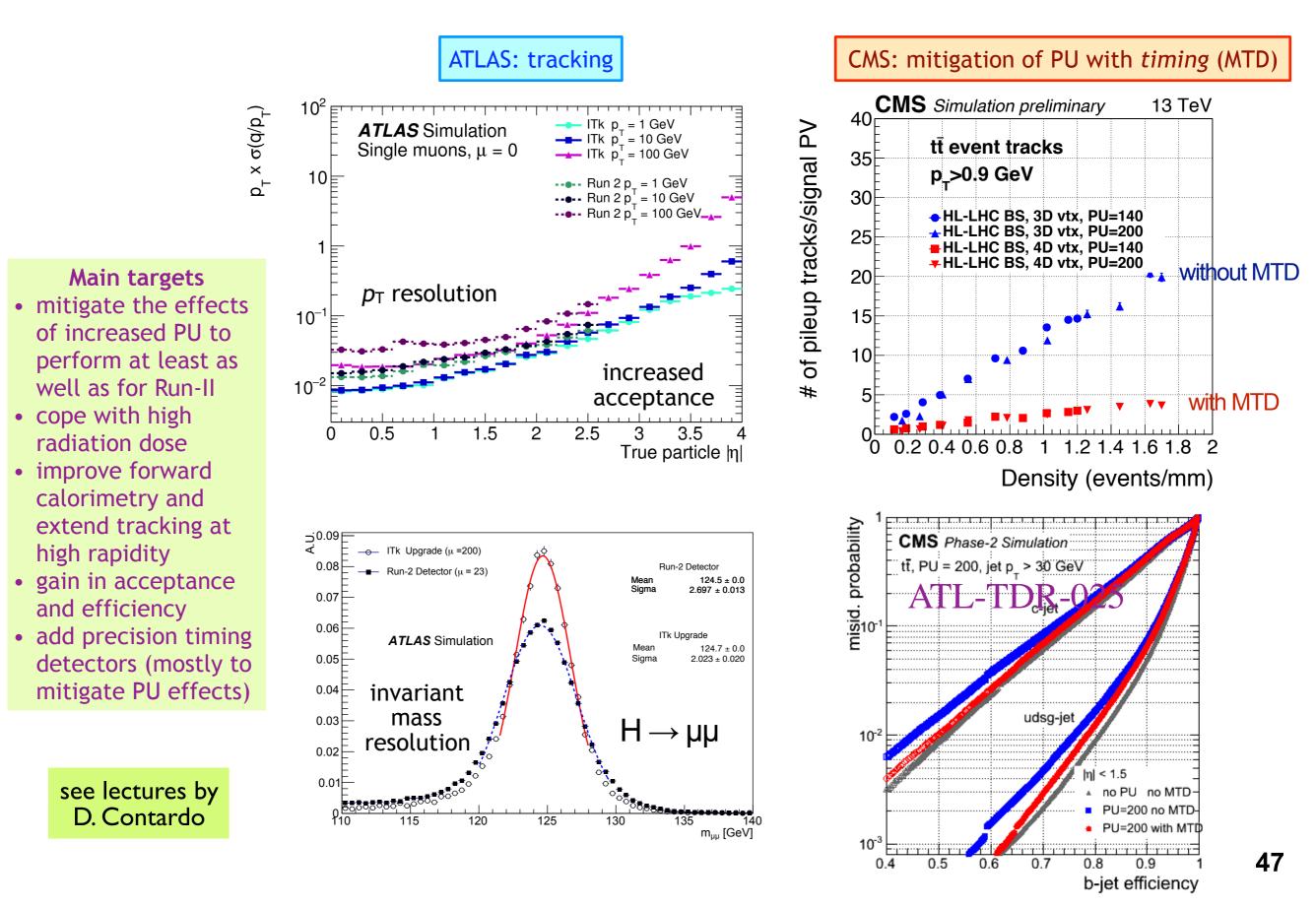
LHC Phase 2 Detector Upgrades







Improved Performance



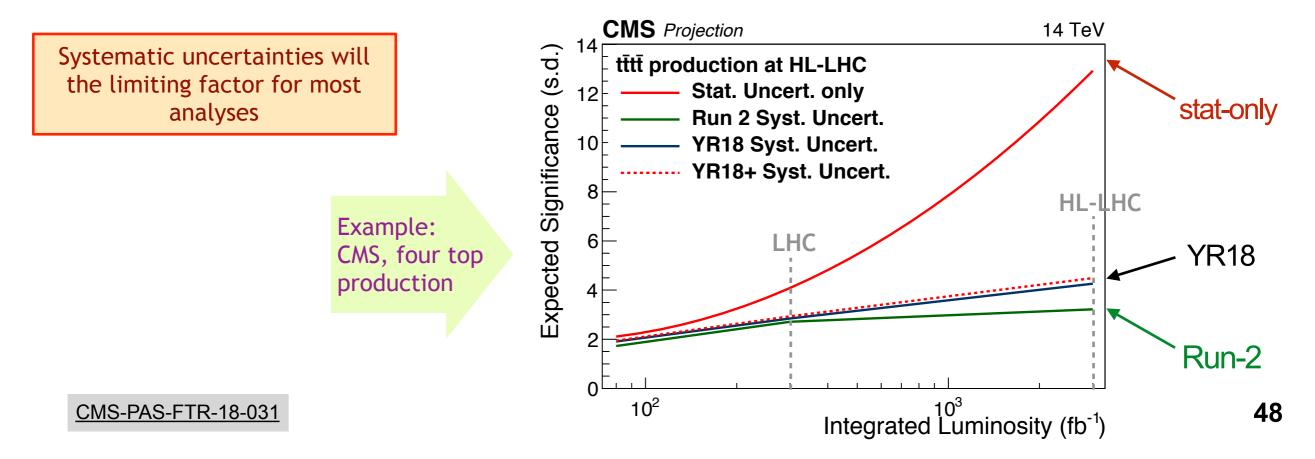
Projected Uncertainties at HL-LHC



🖛 Run-2 scenario (S1)

conservative

- systematic uncertainties as for Run-2
- **Baseline scenario YR18 (S2)** *more realistic*
- uncertainties on methods as of latest Run 2 published results
- for each physics object:
 - detector: unchanged or revised from TDR studies
 - systematic uncertainty: scale as $1/\sqrt{\mathscr{L}}$ up to some agree-upon *floor*
- MC statistics uncertainty: neglected, luminosity uncertainty: 1%
- theory uncertainty: factor 2 in reduction (normalisation & modelling)



Common ATLAS/CMS strategy

3. **BSM**

HL-LHC and HE-LHC Yellow Report 2018

1. Standard Model

4. Flavour Physics

5. High-density QCD

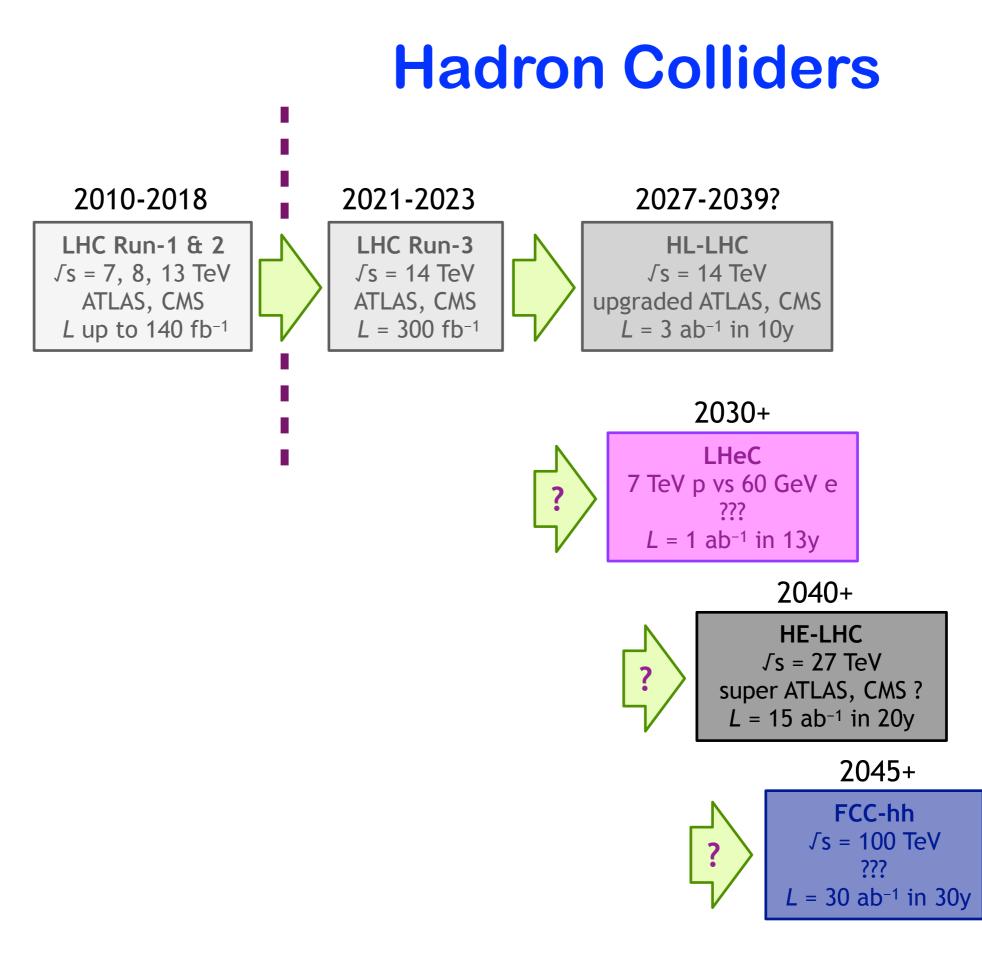
2. Higgs Physics

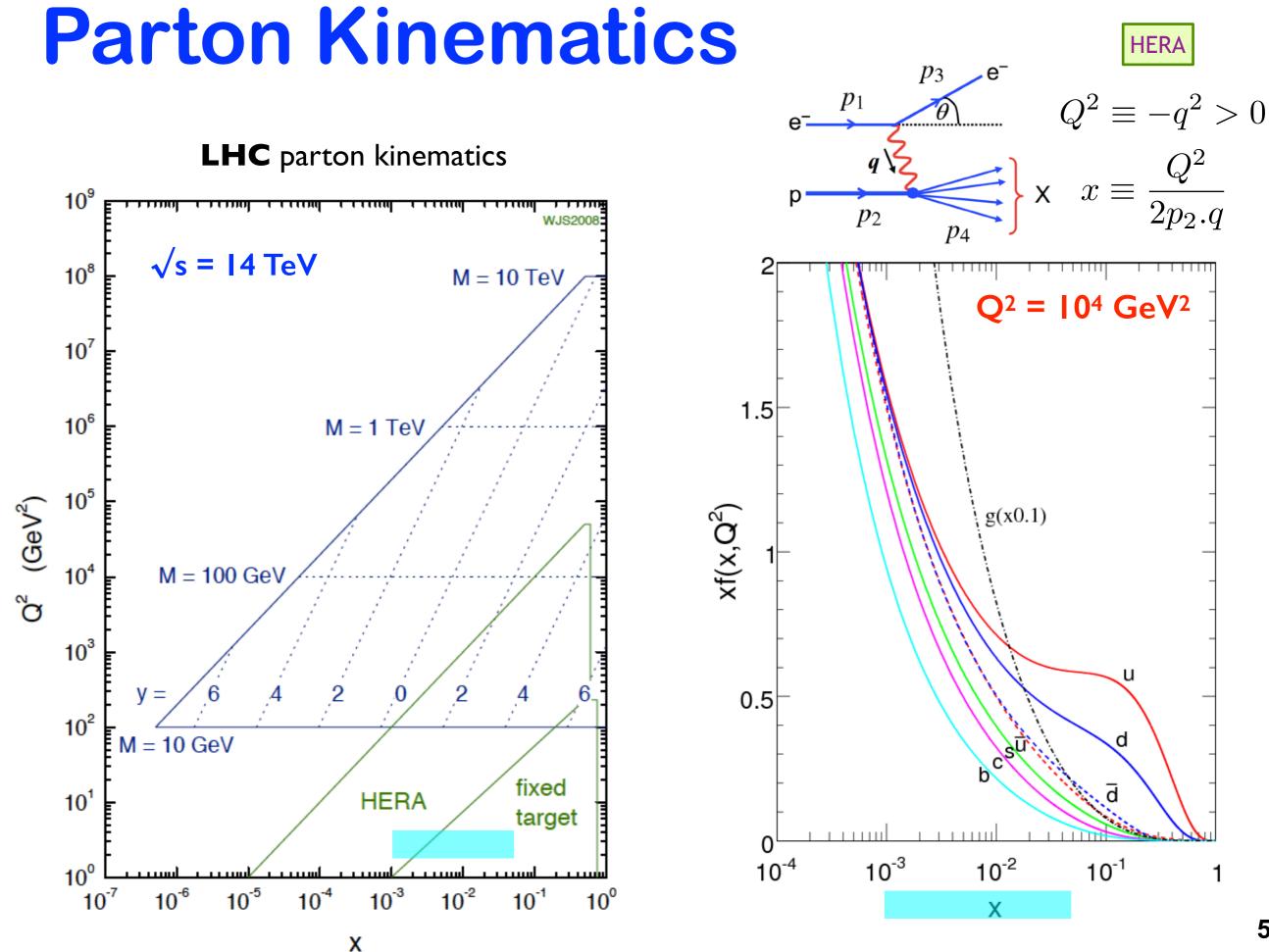
S2 Experimental Systematics

Example of systematic *floors* used in S2 (here: ATLAS)

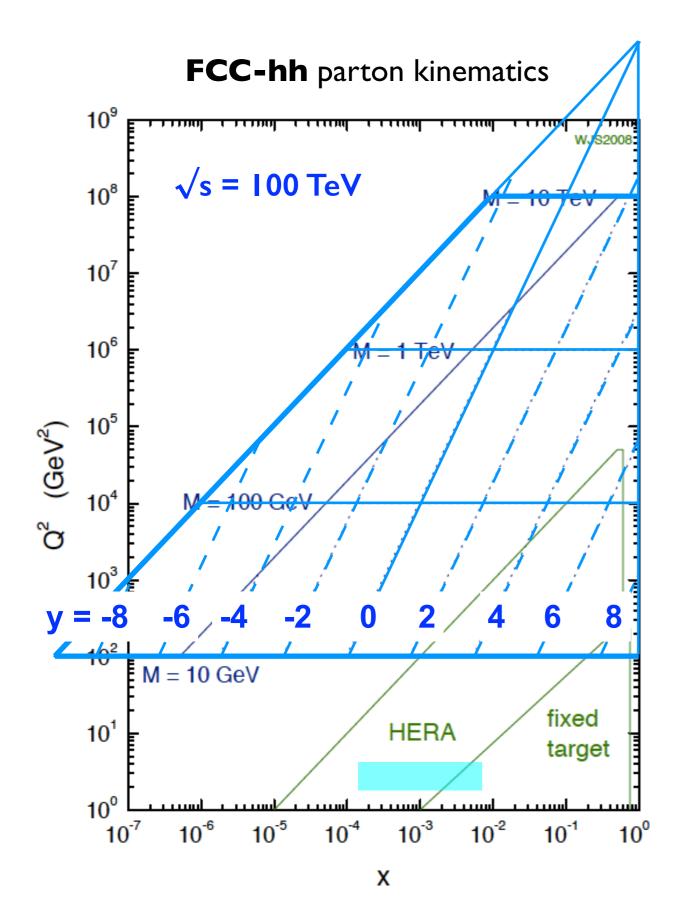
| Source | Component | Run 2 unc. | Projection minimum unc. |
|--|-----------------------|--------------------------------|-------------------------|
| Muon ID | | 1-2% | 0.5% |
| Electron ID | | 1-2% | 0.5% |
| Photon ID | | 0.5 - 2% | 0.25 - 1% |
| Hadronic τ ID | | 6% | Same as Run 2 |
| Jet energy scale | Absolute | 0.5% | 0.1 – 0.2% |
| | Relative | 0.1 - 3% | 0.1 – 0.5% |
| | Pileup | 0-2% | Same as Run 2 |
| | Method and sample | 0.5 - 5% | No limit |
| | Jet flavour | 1.5% | 0.75% |
| | Time stability | 0.2% | No limit |
| Jet energy res. | | Varies with p_T and η | Half of Run 2 |
| $\vec{p}_{\mathrm{T}}^{\mathrm{miss}}$ scale | | Varies with analysis selection | Half of Run 2 |
| b-Tagging | b-/c-jets (syst.) | Varies with p_T and η | Same as Run 2 |
| | light mis-tag (syst.) | Varies with p_T and η | Same as Run 2 |
| | b-/c-jets (stat.) | Varies with p_T and η | No limit |
| | light mis-tag (stat.) | Varies with p_T and η | No limit |
| Integrated lumi. | | 2.5% | 1% |

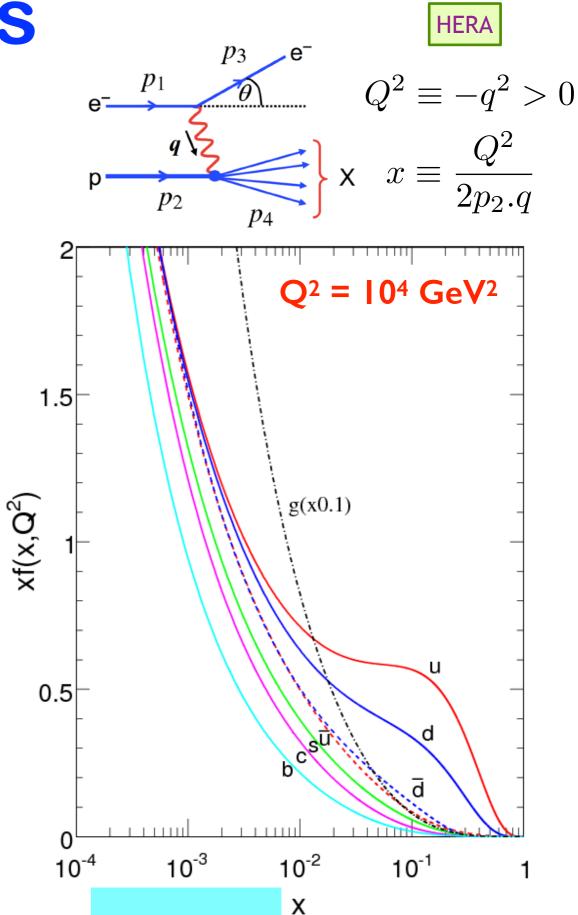
Theory ¹/₂





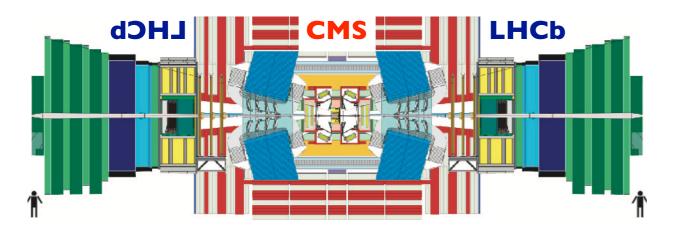
Parton Kinematics





FCC-hh Reference Detector

Starting point

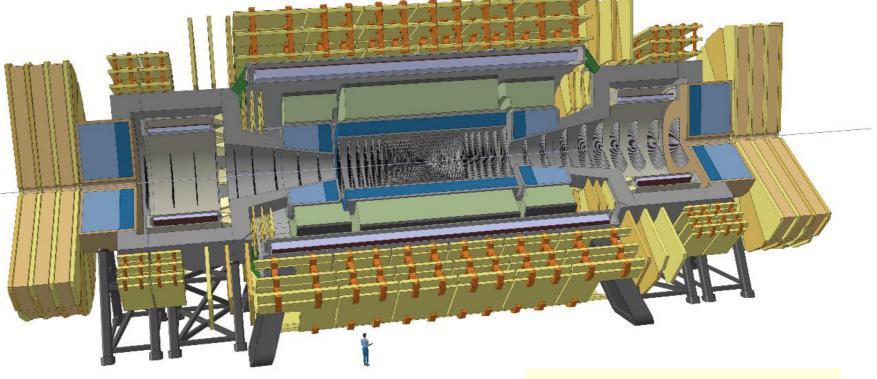


Main features

- 4T solenoid, 10-m bore solenoid
- Two forward 4T, 5-m bore solenoids
- no shielding
- ~I4 GJ stored energy
- EM and H calorimetry up to $\eta = 6$
- high granularity (×4 ATLAS or CMS)
- trigger includes muon system

Some of the challenges

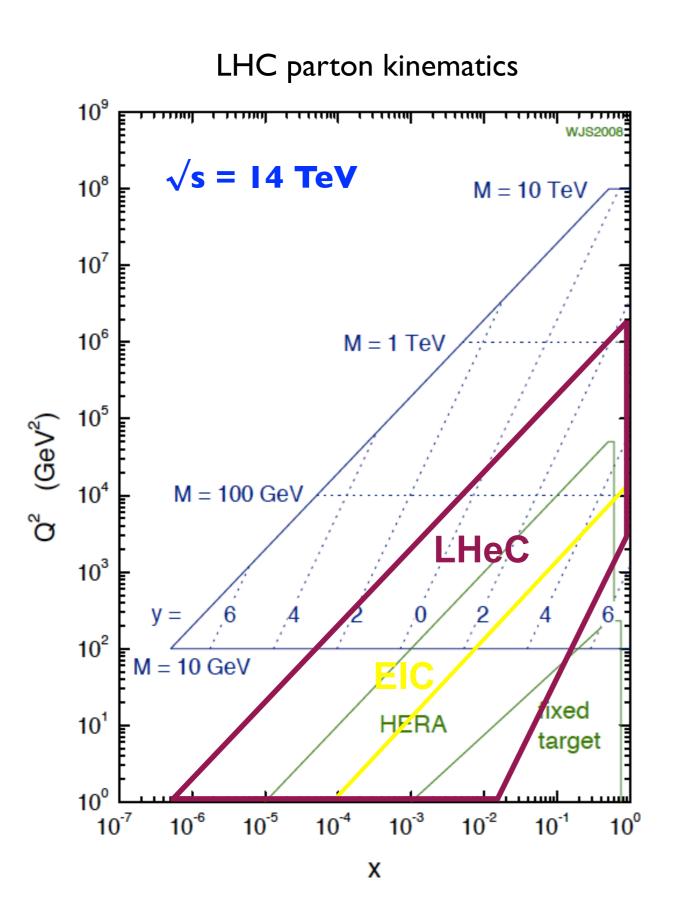
- pileup = 1000 (×10 / HL-LHC)
- radiation = 10¹⁸ part (IMeV)/cm2 (×100 / HL-LHC)
- forward SM physics
- high-p⊤ jets and leptons
- I-I.5 PB/s



one billion € project

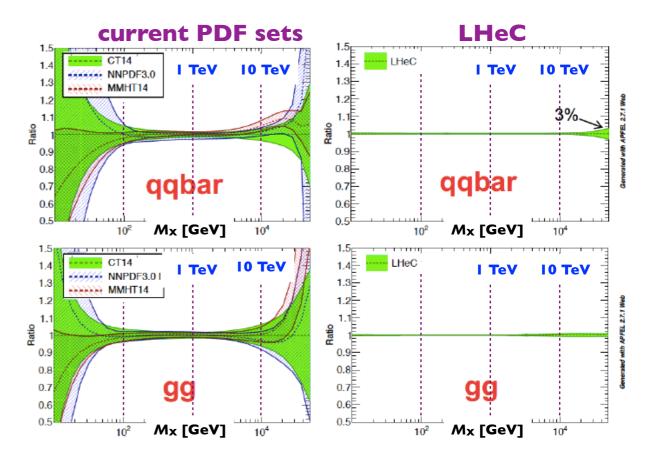


LHeC: e[±]p at HL-LHC

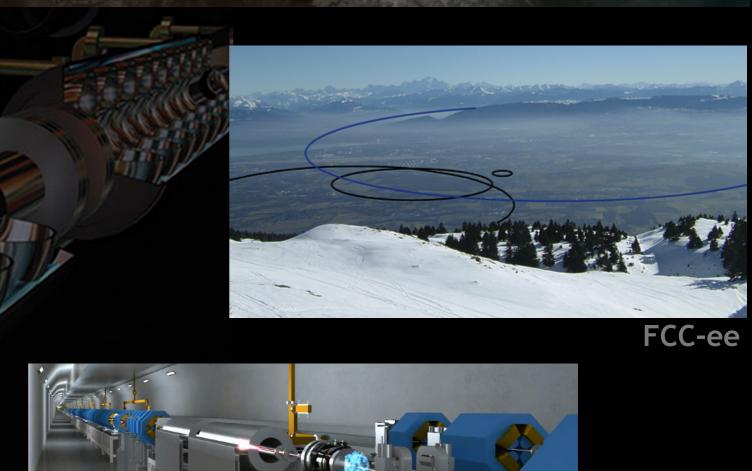


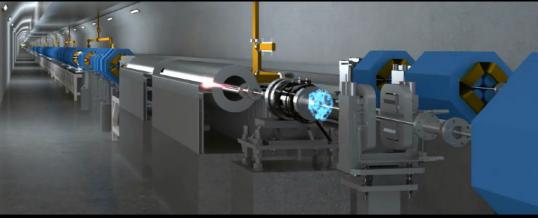
Electrons for the LHC

- Energy Recovery Linac (ERL) <100 MW
- 10-60 GeV e⁻ vs 1-7 TeV p
 - → √s = 200 GeV-1.3 TeV
- concurrent ep and pp (LS4-LS6): 225 fb⁻¹
- dedicated e[±]p (4 years): +650 fb⁻¹



Reduction of theory uncertainties by large factors at the (HE-)(HL-)LHC and FCC-hh

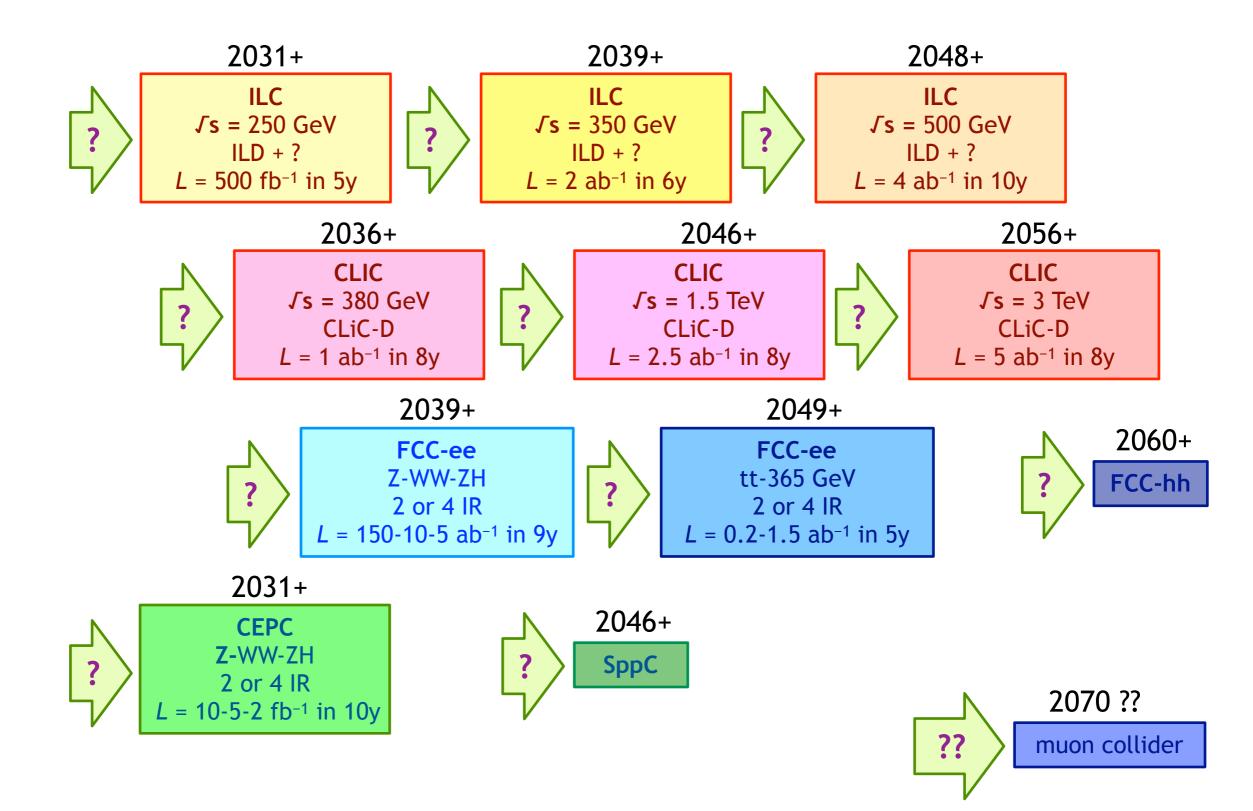




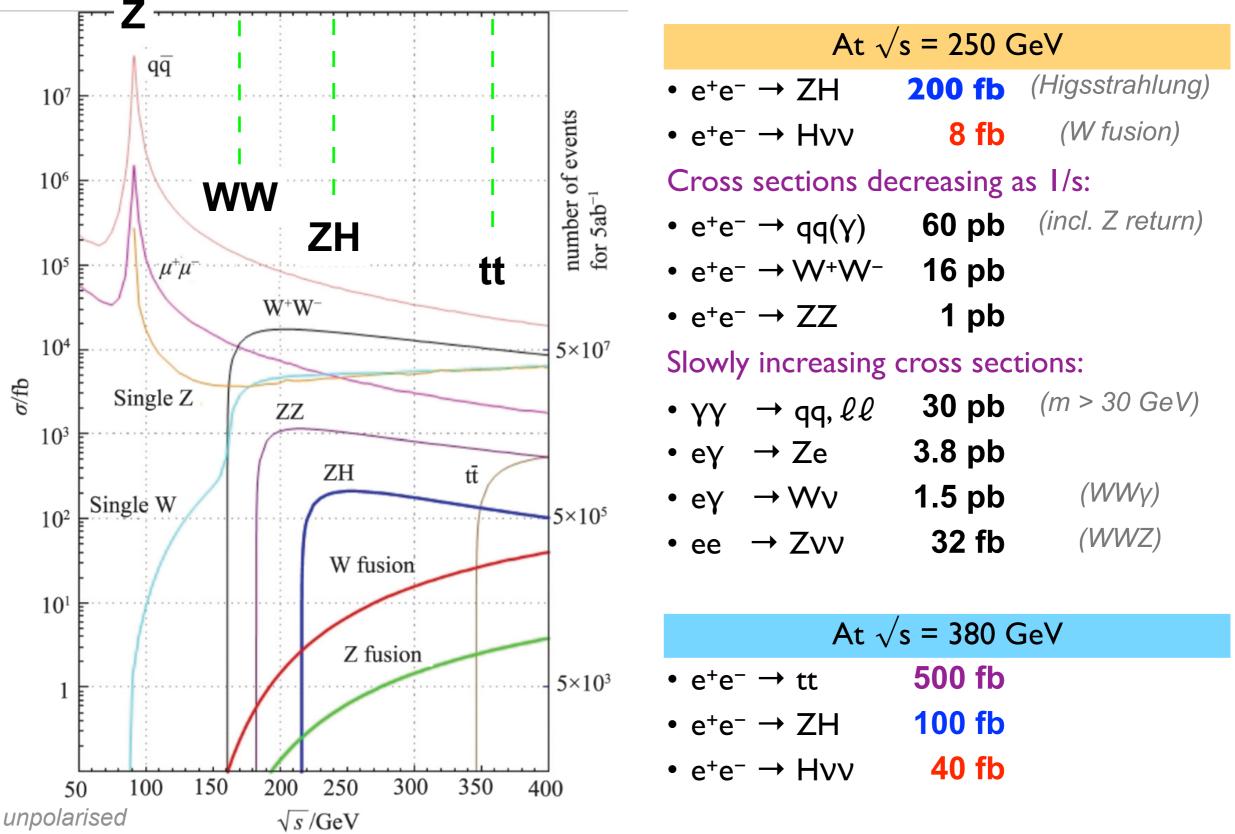
ILC



Lepton Colliders



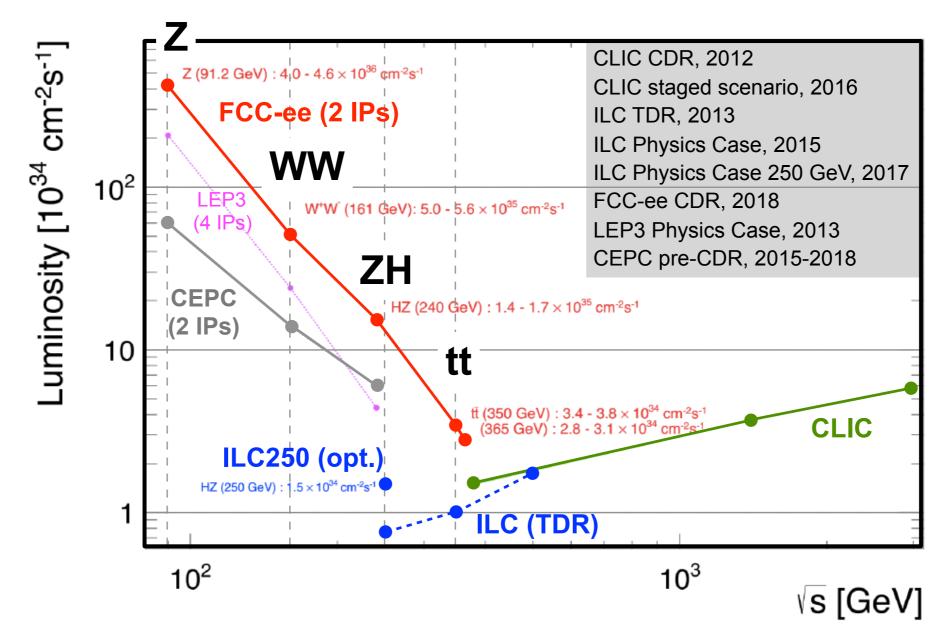
SM Cross Sections at e+e- Colliders



SM Physics at e⁺e⁻ Colliders

| √s | Processes | Physics Goals | Observables |
|----------|--|---|---|
| 91 GeV | • e+e- → Z | ultra-precision EW physics | sin²θ _{eff} Mz, Γz, Nv α, αs |
| 125 GeV | • $e^+e^- \rightarrow H$ | limit on s-channel H production? | Уе |
| 160 GeV | • $e^+e^- \rightarrow W^+W^-$ | ultra-precision W mass | $M_{\rm W}, \Gamma_{\rm W}$ |
| >160 GeV | • $e^+e^- \rightarrow W^+W^-$ • $e^+e^- \rightarrow qq$, $\ell\ell (\gamma)$ | precision W mass and couplings precision EW (incl. Z return) | <i>M</i> w, aTGC <i>N</i> v |
| 250 GeV | • $e^+e^- \rightarrow ZH$ | ultra-precision Higgs mass precision Higgs couplings | <i>М</i> н к∨, к _f , Гн |
| 360 GeV | • e+e- → tt | ultra-precision top mass | mt |
| >360 GeV | • $e^+e^- \rightarrow tt$ • $e^+e^- \rightarrow ZH$ • $e^+e^- \rightarrow Hvv$ | precision top couplings precision Higgs couplings | |
| 500+ GeV | • $e^+e^- \rightarrow ttH$ • $e^+e^- \rightarrow ZHH$ • $e^+e^- \rightarrow Z' \rightarrow ff$ • $e^+e^- \rightarrow \chi\chi$ • $e^+e^- \rightarrow AH, H^+H^-$ | Higgs coupling to top Higgs self-coupling search for heavy Z' bosons search for Supersymmetry search for new Higgs bosons | Уtop λннн |

Luminosity of e⁺e⁻ Colliders



Circular colliders

high-luminosity from Z peak to top pair threshold Linear colliders

extendability at high energy and beam L-polarisation

Linear or Circular? Pros & Cons

| | Circular Colliders (FCC-ee) | | Linear Colliders (ILC) | | |
|--------------------|--|--|--|---|--|
| | pros | cons | pros | cons | |
| √s | | limited by synchrotron radiation (SR), which increases as E⁴_{beam}/R 100 km → 365 GeV max | extendable in energy large potential √s reach 250→500→1000 GeV (access to ttH, ZHH, Hee) | running at √s smaller than 250 GeV would require optimisation | |
| beam- strahlung | | strong: affects beam lifetime (typically 30 min.) top-up injection needed to compensate for fast <i>L</i> burn-off | | strong due to beam size at interaction point (IP) increasing with energy | |
| energy spread | small energy spread (<0.1% at 240 GeV) with top-up injection: mean <i>L</i> = 95% of peak | | | larger energy spread (86% within 1% of nominal at 250 GeV) | |
| lumi | high-lumi obtained with large number of bunches increasing at lower √s due to less SR (spare RF used to accelerate more bunches) crab waist scheme several interaction regions possible | limited by SR power at higher energies | high-lumi obtained with nanometer-size beams increasing naturally with energy thanks to beam dynamics at IP luminosity upgrade (1312 → 2625 bunches) | low repetition rate only one interaction region (ILD and SLD detectors in push-pull) | |
| L-polar | | • no L-polarisation, except perhaps at Z peak | e⁻ beam: ±80% e⁺ beam: ±30% (±60%) | | |
| misc | precise <i>E</i>_{beam} from resonant depolarisation (Z peak and perhaps WW threshold) | | nm-beams at IP allow for very small beam pipe (superior for b/c tagging) | | |

Detector Concepts for ee Colliders

Particle Flow Detectors

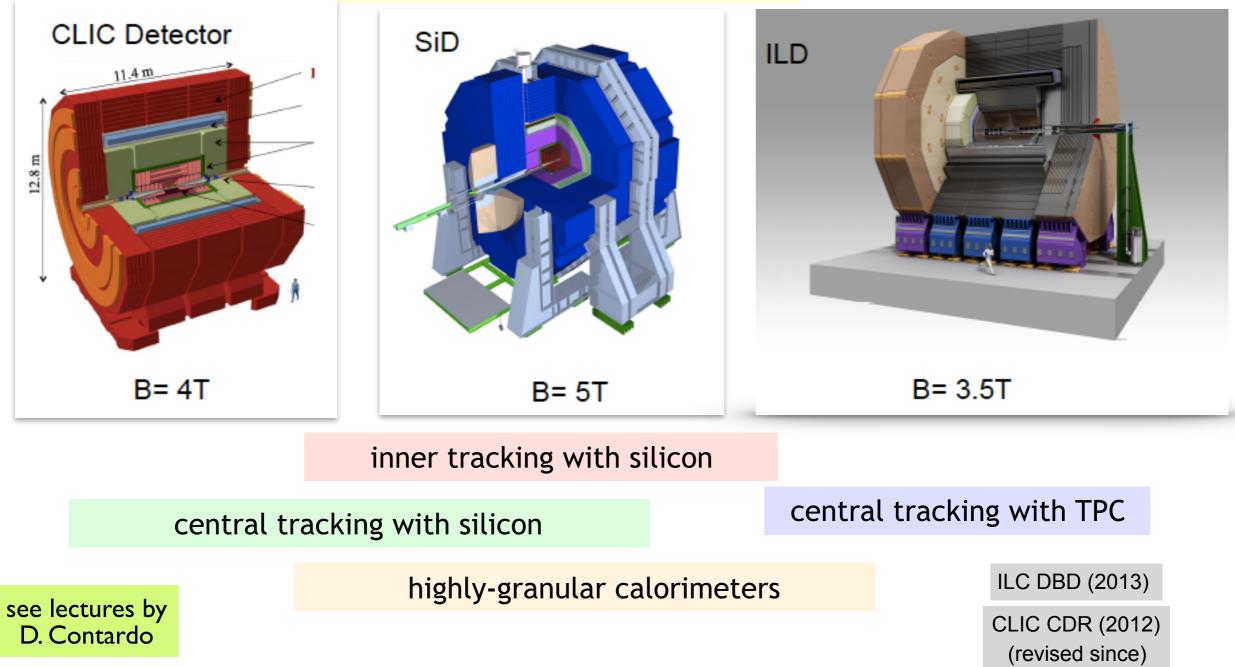
- high hermiticity
- high granularity
- momentum resolution
- high separation power

FCC-ee 2 detector concepts

- CLD: inspired from CLIC detector
- IDEA: from present state-ofthe-art

CEPC 2.5 detector concepts

- baseline: ILD/SiD concept (3T)
- IDEA concept (2T)







"Discoveries make the front pages of the newspapers, while precise measurements of known particle don't, but scientifically they are just as important."

Selected References

CERN

- Machine parameters and project luminosity performance of proposed future colliders at CERN, CERN/SPC/1114
- European Particle Physics Strategy Update

HL-LHC and HE-LHC

• Yellow Book, Report on the physics at HL-LHC and perspectives for HE-LHC

FCC

- Future Circular Collider Study, Conceptual Design Report, 2019, Volume 1, Physics Opportunities
- Physics at a 100 TeV pp collider: Beyond the Standard Model phenomena, <u>arxiv:1606.00947</u>
- Physics at a 100 TeV pp collider: Higgs and EW symmetry breaking studies, <u>arxiv:1606.09408</u>
- Physics at a 100 TeV pp collider: Standard Model processes, <u>arxiv:1607.01831</u>

LHeC

 A Large Hadron Electron Collider at CERN: Report on the Physics and Design Concepts for Machine and Detector, <u>arxiv:1206.2913</u>

CLIC

• Updated baseline for a staged Compact Linear Collider, <u>arxiv:1608.07537</u>

ILC

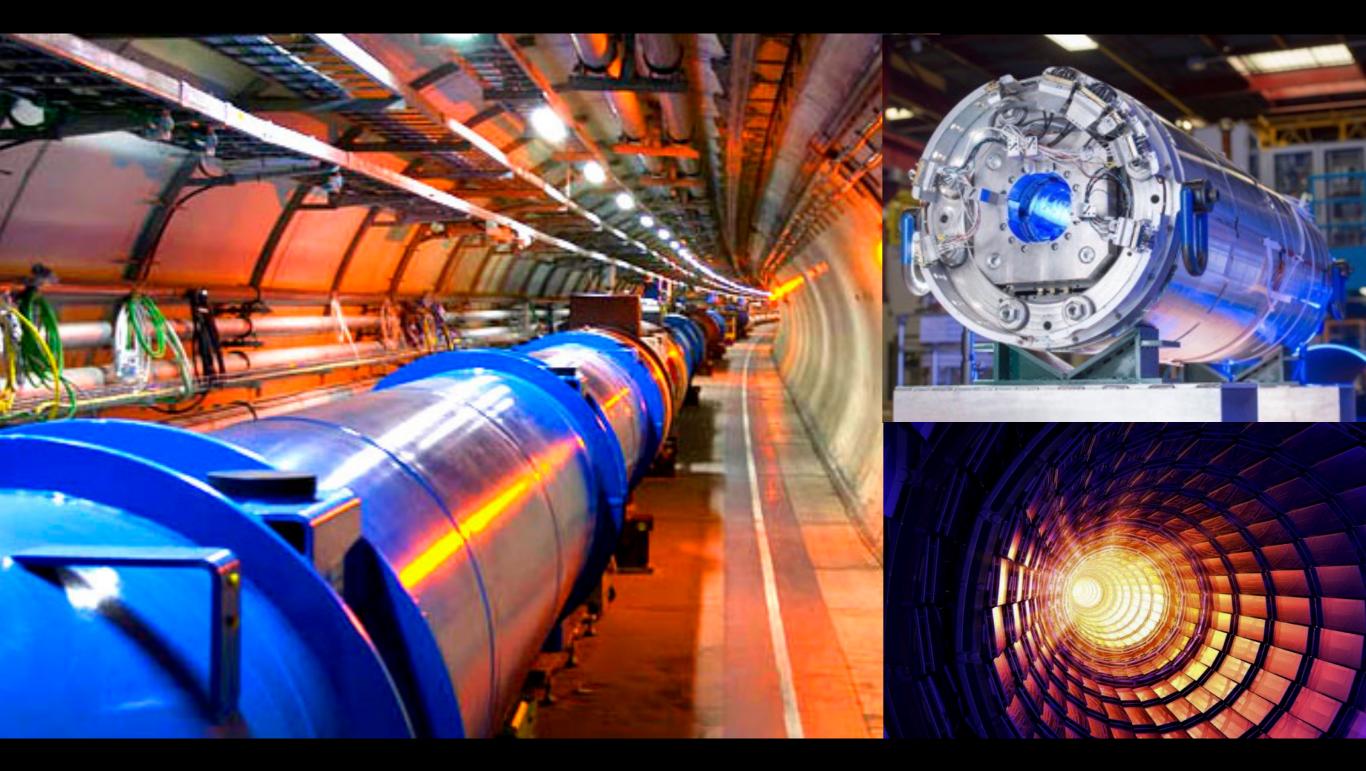
- The International Linear Collider Technical Design Report Volume 1: Executive Summary, <u>arxiv:</u> <u>1306.6327</u>
- Physics Case for the 250 GeV Stage of the International Linear Collider, <u>arxiv:1710.07621</u>

CEPC

• Conceptual Design Report, Volume 2 – Physics and Detector, IHEP-CEPC-DR-2018-02







Gautier Hamel de Monchenault

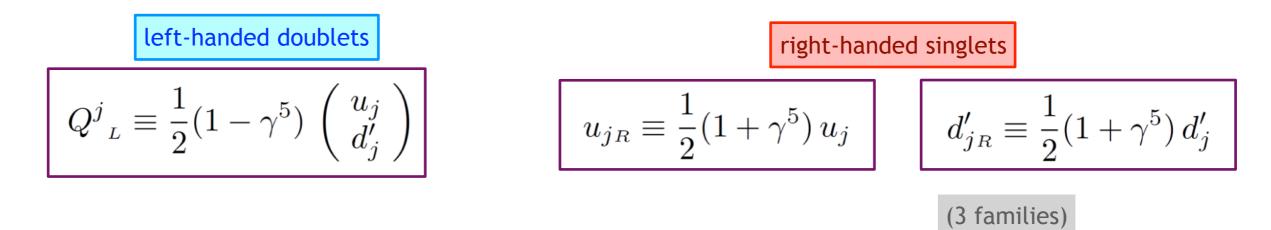
Gauge Sector

$$\begin{split} \mathcal{L}_{\text{gauge}} &= -\frac{1}{4} \, \mathbf{W}_{\mu\nu} \mathbf{W}^{\mu\nu} - \frac{1}{4} \, B_{\mu\nu} B^{\mu\nu} & \text{gauge kinetic terms} \\ &= -\frac{1}{2} \, W^{-}{}_{\mu\nu} W^{+\mu\nu} - \frac{1}{4} \, Z_{\mu\nu} Z^{\mu\nu} - \frac{1}{4} \, F_{\mu\nu} F^{\mu\nu} & \text{vector boson kinetic terms} \\ &+ ig \, \cos \theta_{W} \, \left[\left(\, W^{-}{}_{\mu\nu} W^{+\mu} - W^{+}{}_{\mu\nu} W^{-\mu} \right) Z^{\nu} \, + \, Z_{\mu\nu} W^{+\mu} W^{-\nu} \, \right] & \text{ZWW} \\ &+ ig \, \sin \theta_{W} \, \left[\left(\, W^{-}{}_{\mu\nu} W^{+\mu} - W^{+}{}_{\mu\nu} W^{-\mu} \right) A^{\nu} \, + \, F_{\mu\nu} W^{+\mu} W^{-\nu} \, \right] & \text{YWW} \\ &+ g^{2} \, \cos^{2} \theta_{W} \left[\, Z_{\mu} Z_{\nu} \, W^{-\mu} W^{+\nu} - Z_{\mu} Z^{\mu} \, W^{-}{}_{\nu} W^{+\nu} \, \right] & \text{ZZWW} \\ &+ g^{2} \, \sin^{2} \theta_{W} \left[\, A_{\mu} A_{\nu} \, W^{-\mu} W^{+\nu} - A_{\mu} A^{\mu} \, W^{-}{}_{\nu} W^{+\nu} \, \right] & \text{YYWW} \\ &+ g^{2} \, \cos \theta_{W} \sin \theta_{W} \left[\left(\, Z_{\mu} A_{\nu} + Z_{\nu} A_{\mu} \, \right) W^{-\mu} W^{+\nu} - 2 \, Z_{\mu} A^{\mu} \, W^{-}{}_{\nu} W^{+\nu} \, \right] & \text{YZWW} \\ &+ \frac{g^{2}}{2} \, W^{-}{}_{\mu} W^{+}{}_{\nu} \left[\, W^{-\mu} W^{+\nu} - W^{-\nu} W^{+\mu} \, \right] & \text{WWWW} \end{split}$$

EWSB Sector

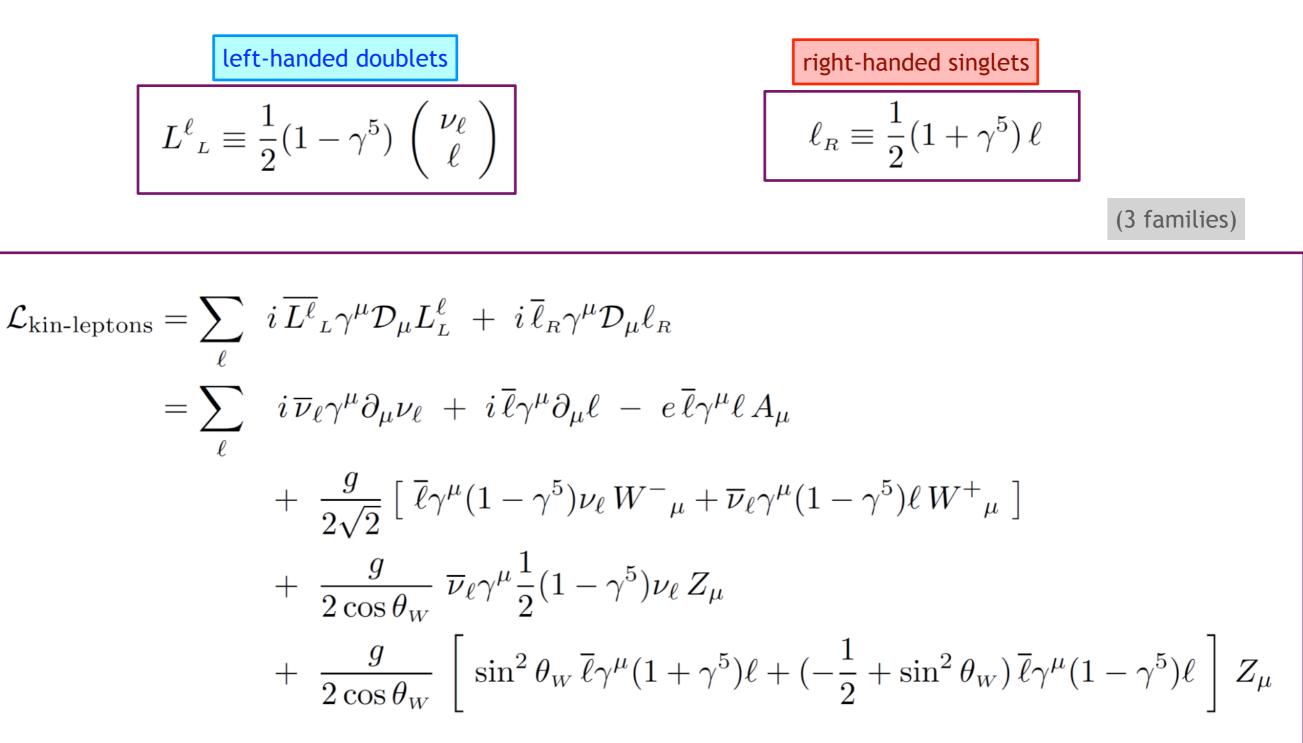
$$\begin{split} \mathcal{L}_{\text{EWSB}} &= \left(\mathcal{D}_{\mu}\phi\right)^{\dagger}\left(\mathcal{D}^{\mu}\phi\right) - \lambda\left[\left(\phi^{\dagger}\phi\right)^{2} - v^{2}\phi^{\dagger}\phi\right] \\ &= \frac{1}{2}\partial_{\mu}h\,\partial^{\mu}h - \frac{1}{2}m_{H}^{2}h^{2} \quad \text{Higgs boson kinetic and mass terms} \\ &+ m_{W}^{2}W^{-}{}_{\mu}W^{+\mu} + \frac{1}{2}m_{Z}^{2}Z_{\mu}Z^{\mu} \quad \text{electroweak boson mass terms} \\ &+ \frac{2m_{W}^{2}}{v}W^{-}{}_{\mu}W^{+\mu}h + \frac{m_{Z}^{2}}{v}Z_{\mu}Z^{\mu}h + \frac{m_{W}^{2}}{v^{2}}W^{-}{}_{\mu}W^{+\mu}h^{2} + \frac{m_{Z}^{2}}{2v^{2}}Z_{\mu}Z^{\mu}h^{2} \\ &- \frac{m_{H}^{2}}{2v}h^{3} - \frac{m_{H}^{2}}{8v^{2}}h^{4} + \left(\text{Cte} = \frac{m_{H}^{2}v^{2}}{8}\right) \quad \begin{array}{c} \text{coupings to bosons} \\ \text{and self-couplings} \\ \text{of the Higgs boson} \end{array}$$

Quark Sector



$$\begin{split} \mathcal{L}_{\text{kin-quarks}} &= \sum_{j} i \overline{Q^{j}}_{L} \gamma^{\mu} \mathcal{D}_{\mu} Q^{j}_{L} + i \overline{u}_{jR} \gamma^{\mu} \mathcal{D}_{\mu} u_{jR} + i \overline{d}_{jR} \gamma^{\mu} \mathcal{D}_{\mu} d_{jR} \\ &= i \overline{\mathbf{u}} \gamma^{\mu} \partial_{\mu} \mathbf{u} + i \overline{\mathbf{d}} \gamma^{\mu} \partial_{\mu} \mathbf{d} + \frac{2}{3} e \overline{\mathbf{u}} \gamma^{\mu} \mathbf{u} A_{\mu} - i \frac{1}{3} e \overline{\mathbf{d}} \gamma^{\mu} \mathbf{d} A_{\mu} \\ &+ \frac{g}{2\sqrt{2}} \left[\overline{\mathbf{d}} \mathbf{V}_{\text{CKM}}^{\dagger} \gamma^{\mu} (1 - \gamma^{5}) \mathbf{u} W^{-}_{\mu} + \overline{\mathbf{u}} \gamma^{\mu} (1 - \gamma^{5}) \mathbf{V}_{\text{CKM}} \mathbf{d} W^{+}_{\mu} \right] \\ &+ \frac{g}{2 \cos \theta_{W}} \left[-\frac{2}{3} \sin^{2} \theta_{W} \overline{\mathbf{u}} \gamma^{\mu} (1 + \gamma^{5}) \mathbf{u} + (+\frac{1}{2} - \frac{2}{3} \sin^{2} \theta_{W}) \overline{\mathbf{u}} \gamma^{\mu} (1 - \gamma^{5}) \mathbf{u} \right] Z_{\mu} \\ &+ \frac{g}{2 \cos \theta_{W}} \left[-\frac{1}{3} \sin^{2} \theta_{W} \overline{\mathbf{d}} \gamma^{\mu} (1 + \gamma^{5}) \mathbf{d} + (-\frac{1}{2} + \frac{1}{3} \sin^{2} \theta_{W}) \overline{\mathbf{d}} \gamma^{\mu} (1 - \gamma^{5}) \mathbf{d} \right] Z_{\mu} \end{split}$$

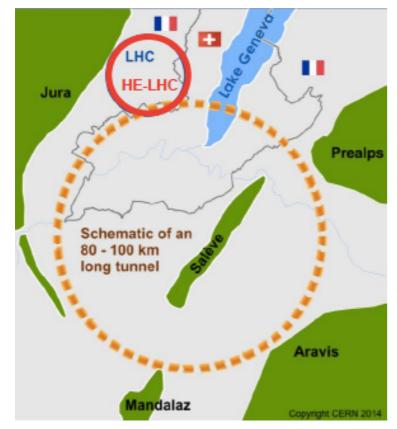
Lepton Sector



neutrinos are massless in the SM

Yukawa Sector

FCC: Future Circular Colliders



100-km tunnel in Geneva area

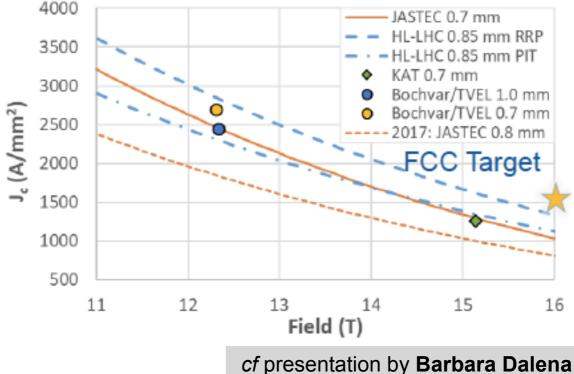
| | \sqrt{s} | L (ab⁻+) | years |
|--------|------------|----------|-------|
| HE-LHC | 27 TeV | 12 | 20 |
| FCC-hh | 100 TeV | 30 | 25 |

Major focus at CERN:

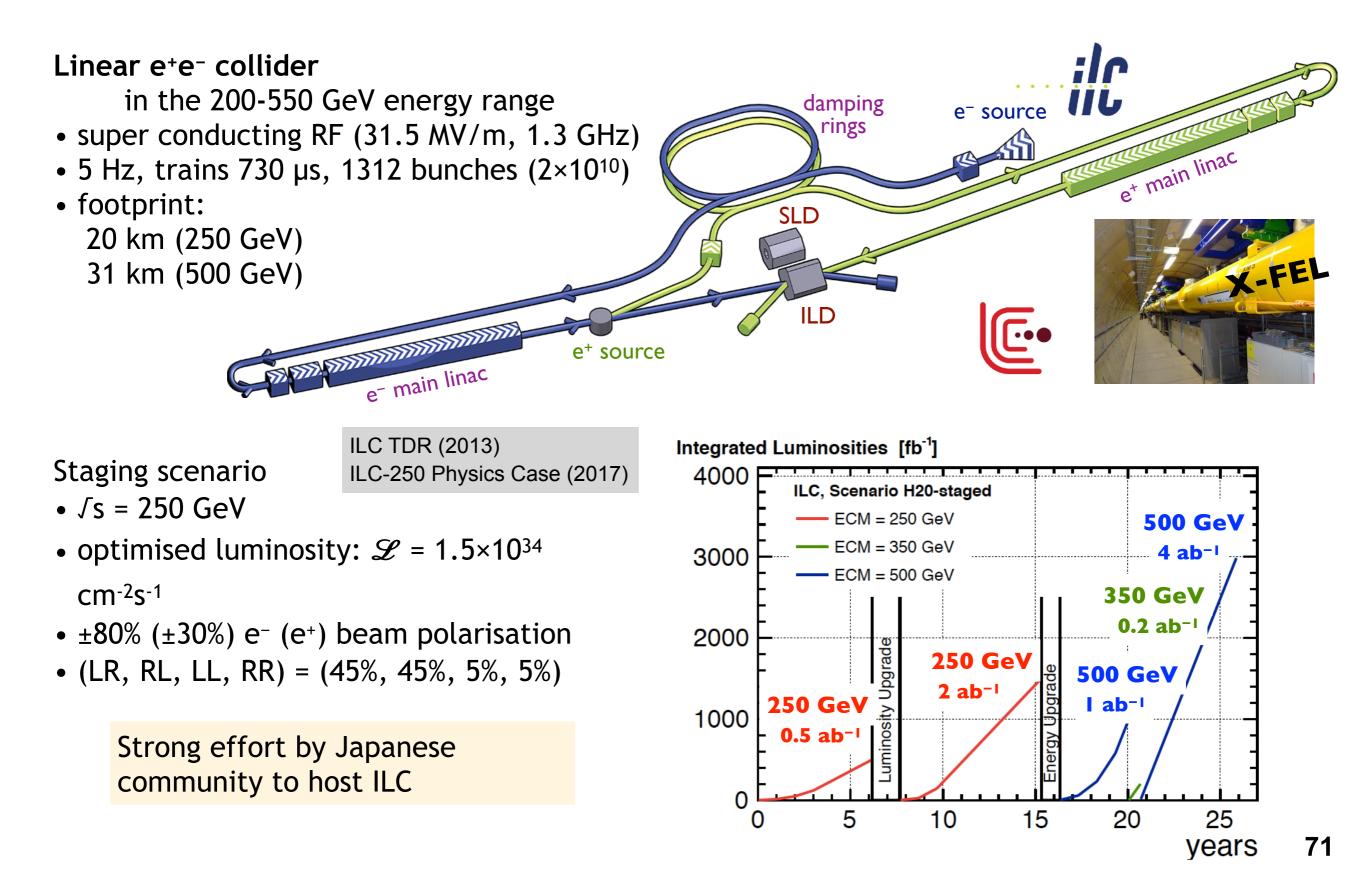
development of 16-T Nb₃Sb SC magnets

- on-going R&D on SC high-field magnets
- prepare industrialisation

| | FC hh ee | | | CERN |
|--------|-------------|---|------------------------------|--------|
| | \sqrt{s} | \mathscr{L} (cm ⁻² s ⁻¹) | first beams (technically) | tunnel |
| HE-LHC | 27 TeV | 1.6×10 ³⁵ | 2040 | LHC |
| FCC-ee | 90-365 GeV | 200-1.5×10 ³⁴ | 2039 | |
| FCC-eh | 3.5 TeV | 1.5×10 ³⁴ | 2043 | 100-km |
| FCC-hh | 100 TeV | 3×10 ³⁵ | 2043 | |
| | 4000 | | | |



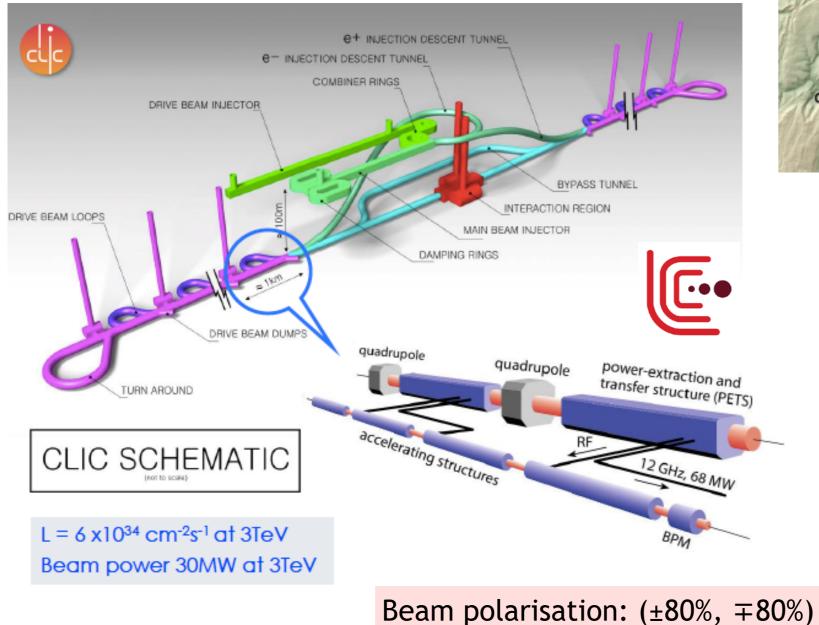
ILC: International Linear Collider



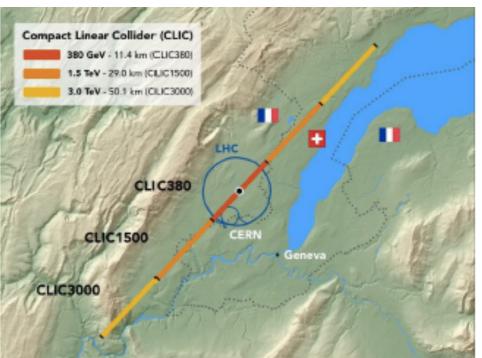
CLIC: Compact Linear Collider

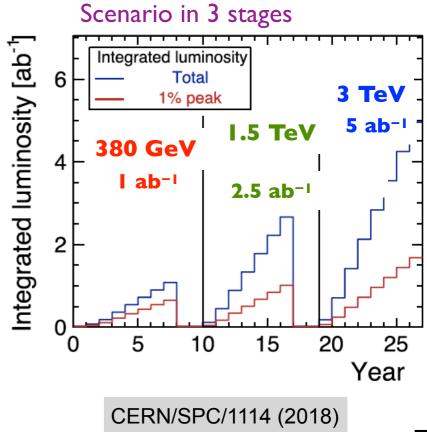
Linear e⁺e⁻ collider at CERN

- in the up-to multi-TeV energy range
- normal conducting high-frequency RF (X-band, 12 GHz)
- e⁻ drive beam for RF power generation

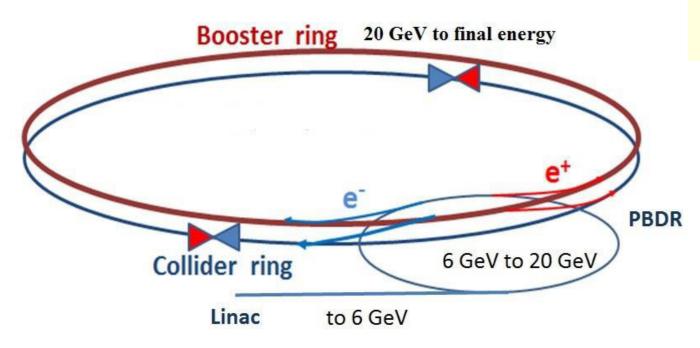


LR / RL = 50% / 50%





FCC-ee: e⁺e⁻ Circular Collider



RF system: high-current \rightarrow high gradient 3 sets of RF cavities

| | V _{rf} [GV] | #bunches | I _{beam} [mA] |
|-----|------------------------------------|----------|------------------------|
| Ζ | 0, 1 | I 6640 | 1390 |
| WW | 0,44 | 2000 | 147 |
| ZH | 2,0 | 393 | 29 |
| top | 10,9 | 48 | 5,4 |

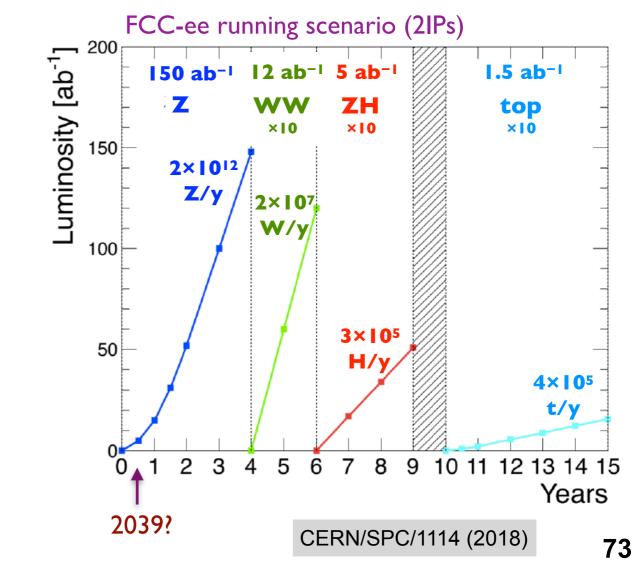
Asymmetric optics with beam crossing angle of 30 mrad

FCC-ee CDR fall 2018

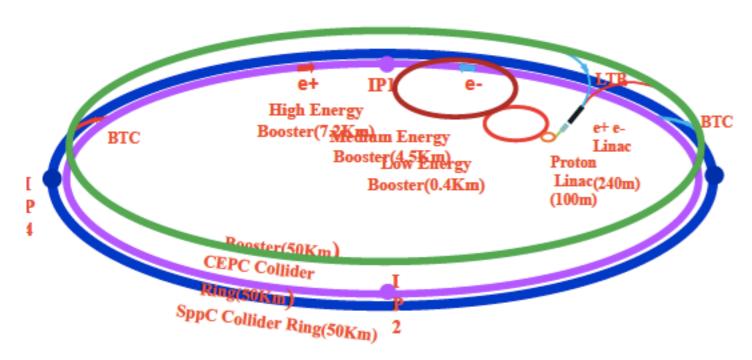
First-phase machine in the **100-km tunnel** built to host eventually FCC-hh

Luminosity limited by SR

- top-up injection (once per minute)
- 50 MW power/beam
- 2 interaction points



CEPC: Chinese e+e- Collider



Project similar to FCC-ee in China

- two colliding rings and a booster
- √s = 90-240 GeV
 - Hosted in a 100-km tunnel which could eventually host a 70-TeV pp collider
 - several possible sites

Peak luminosity (2 IPs) (CDR parameters)

- at the Z: 1.7×10³⁵ cms⁻²s⁻¹ (3T)
- at the W: 1.0×10³⁵ cms⁻²s⁻¹
- at the H: 3×10³⁴ cms⁻²s⁻¹

Physics goals:

- >3×10¹¹ Z bosons (8 ab⁻¹)
- 2×10⁷ W pairs (2.6 ab⁻¹)
- 10⁶ Higgs bosons (5.6 ab⁻¹)

| Тi | m | ١e | li | in | e |
|----|---|----|-------|----|---|
| | | IC | . L I | | |

| 2013-2015 | pre-studies | • |
|-----------|------------------------------|---|
| 2016-2022 | R&D Engineering Design | • |
| 2022-2030 | Construction | |
| 2030-2040 | data taking | |

- Starts before the end of the HL-LHC
- possibly concurrent with the ILC