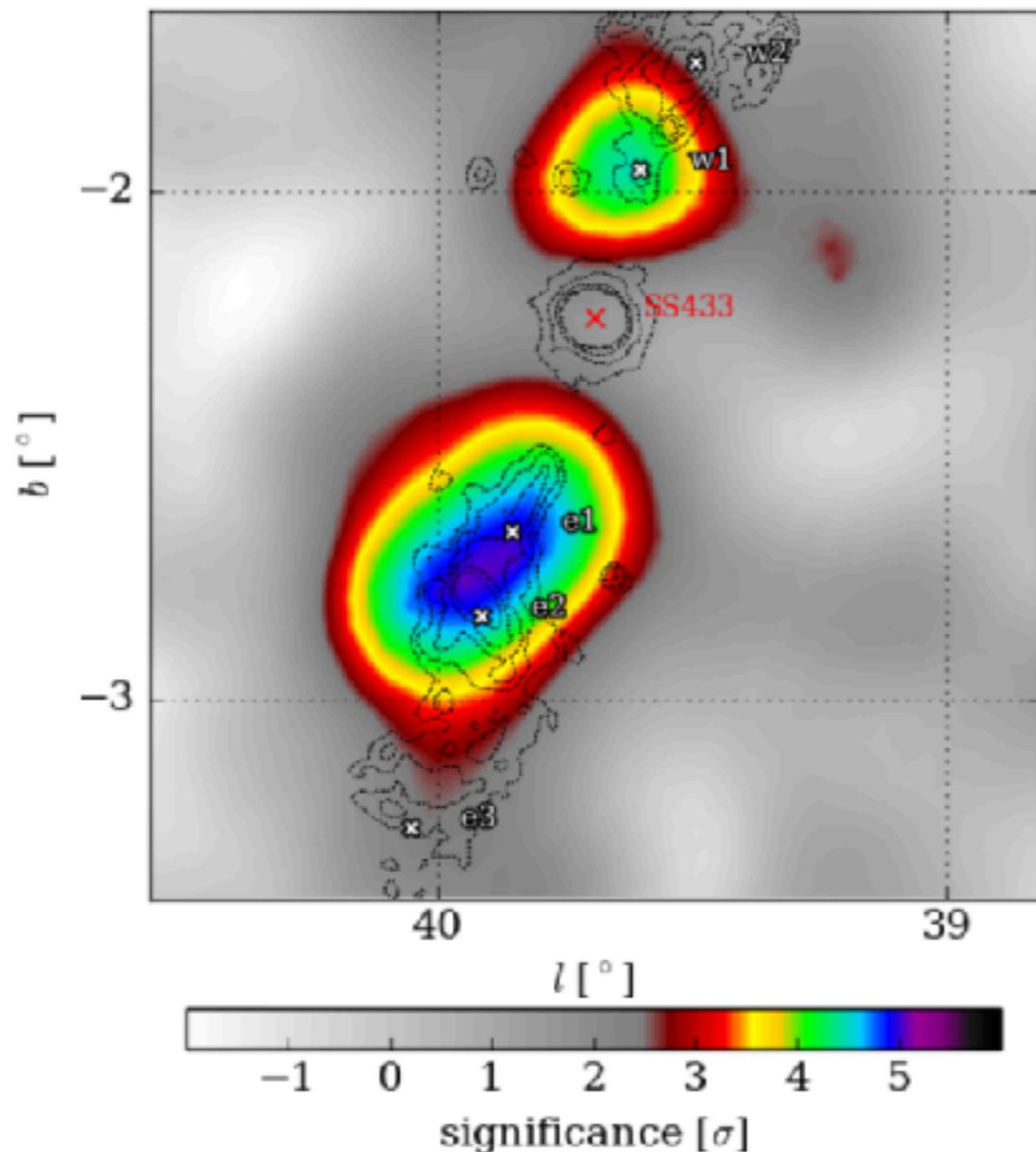


Cosmic Ray Anisotropy and the Galactic-Extragalactic Transition Regime

Ke Fang
Einstein Fellow, Stanford University

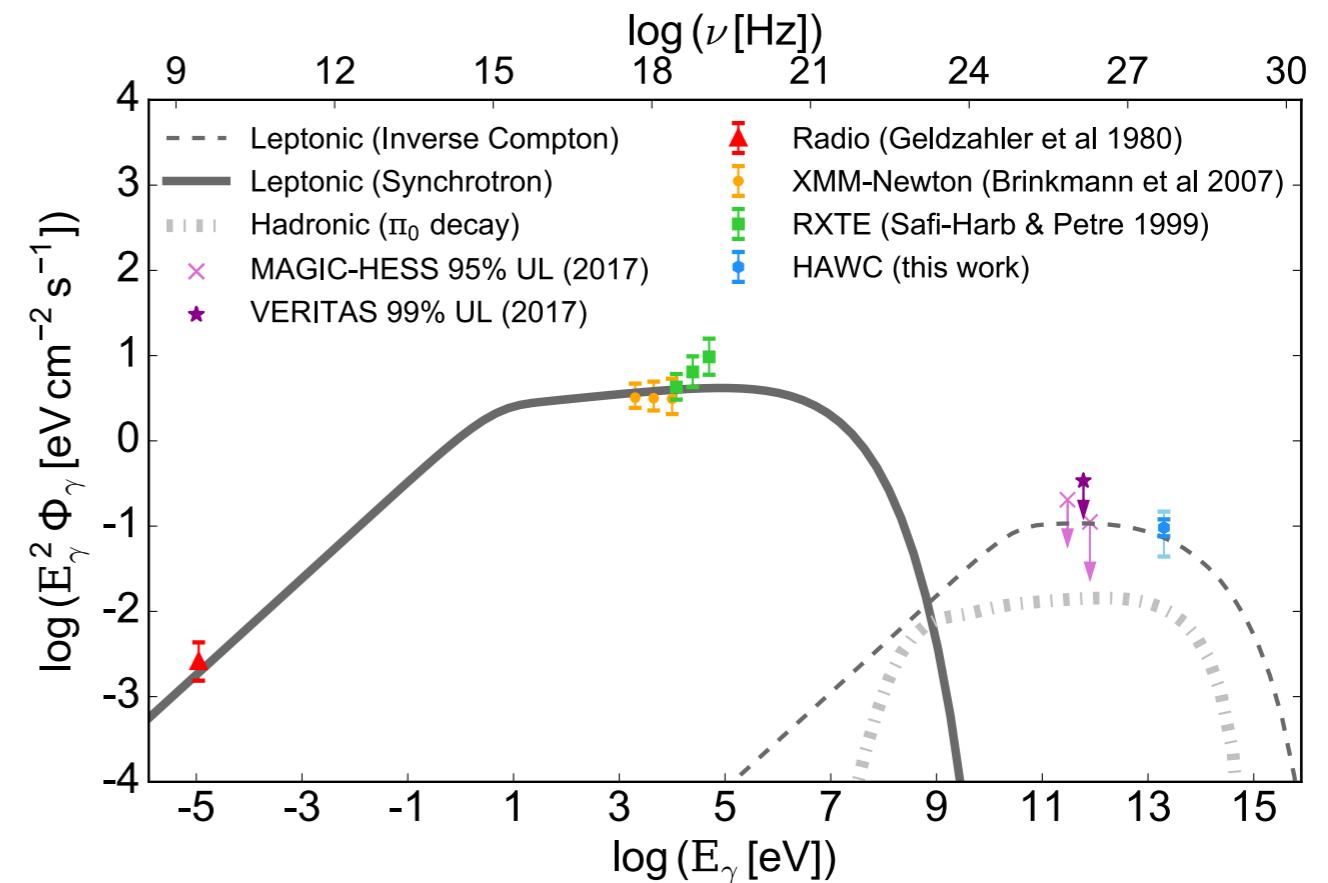
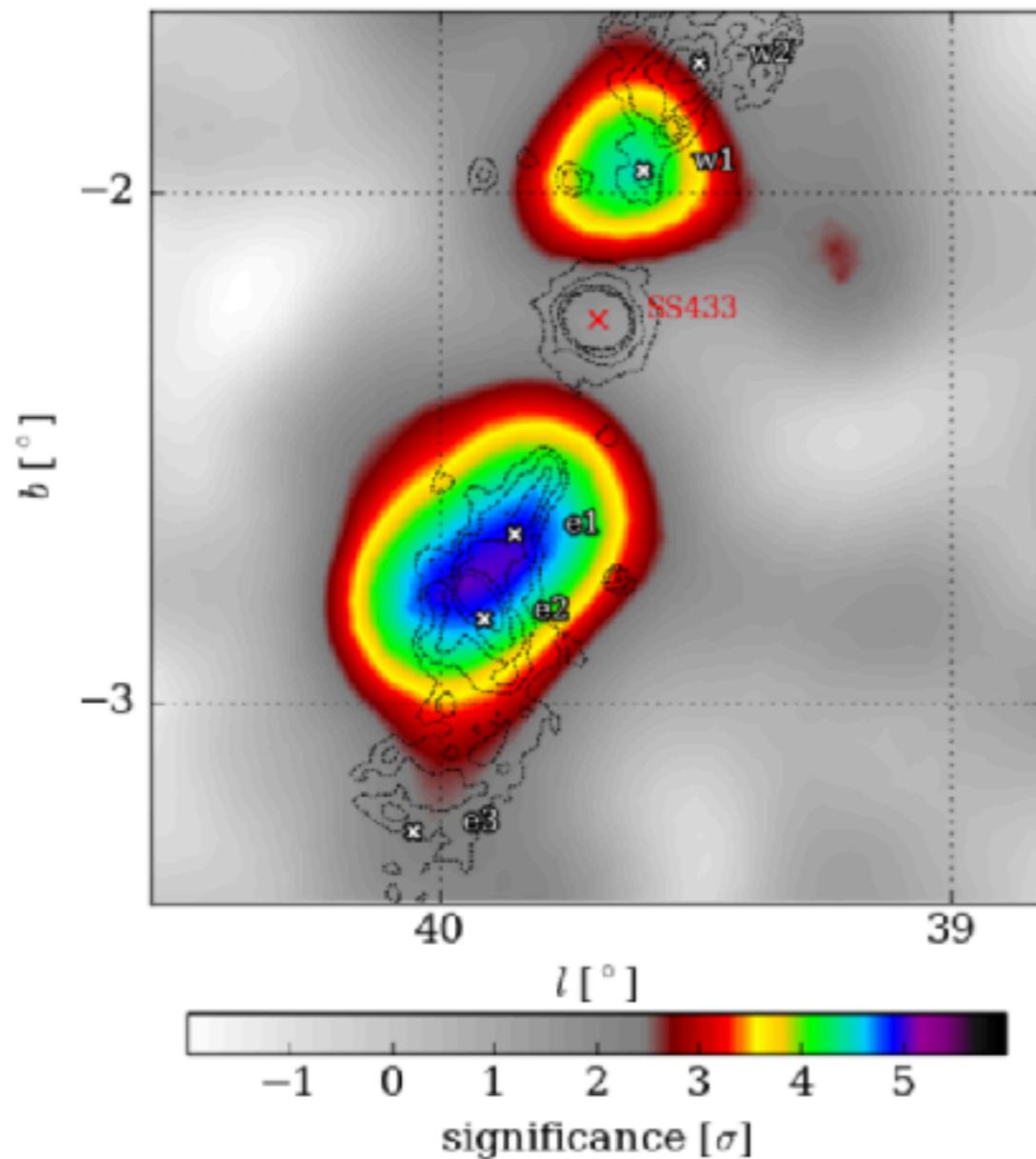
GRAND Collaboration Meeting, Dunhuang, China
Apr 25, 2019

Very-high-energy Gamma-ray Sources could be nearby



HAWC Collaboration, Nature (2018)
Main authors: BenZvi, Brenda, KF, Rho, Zhang, Zhou

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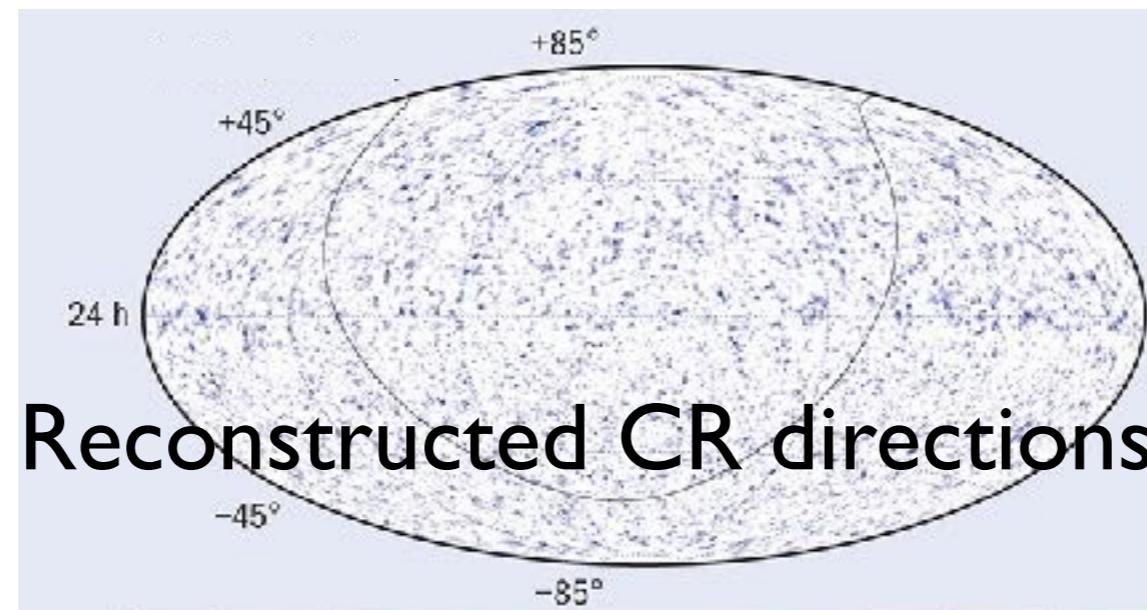


Very-high-energy gamma rays are observed from the lobes of SS 433. Such objects could be **promising gamma-ray sources for GRAND**

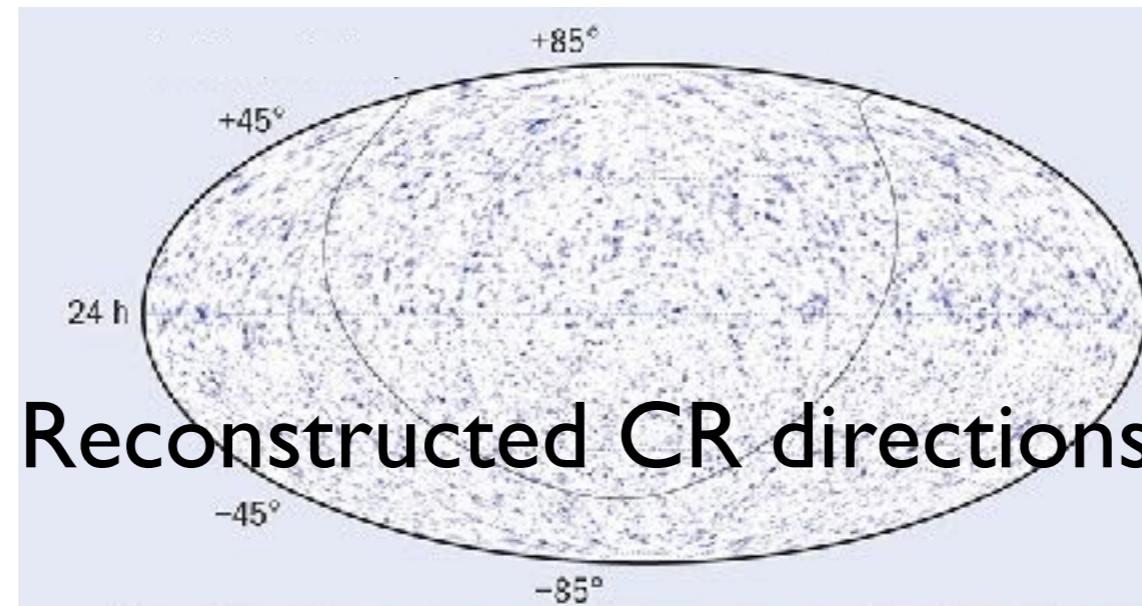
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Cosmic Ray Anisotropy

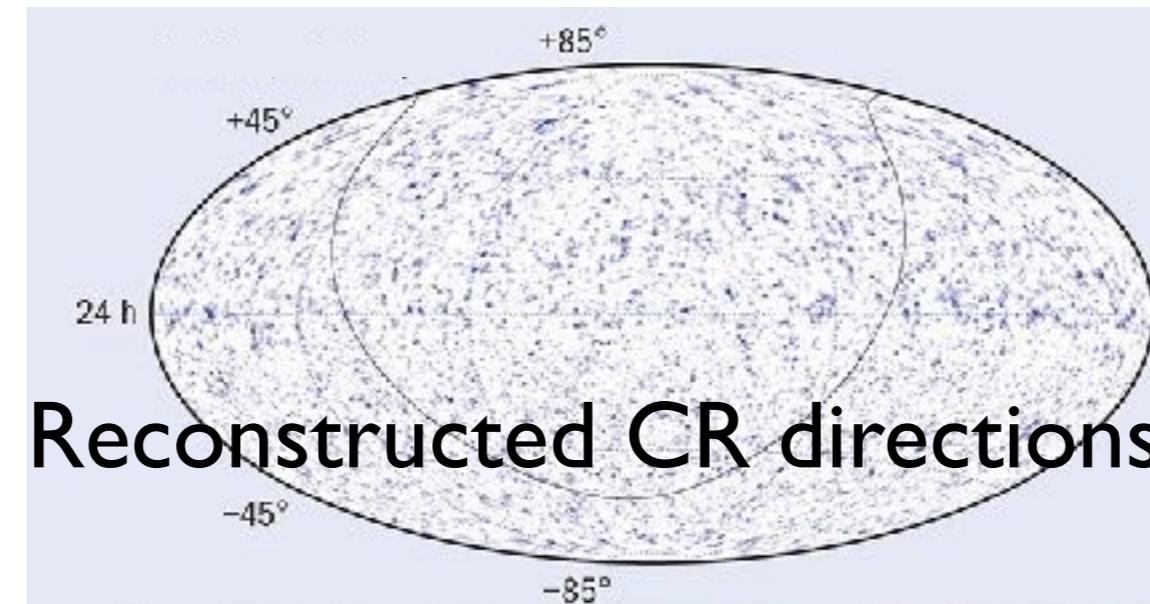


Cosmic Ray Anisotropy

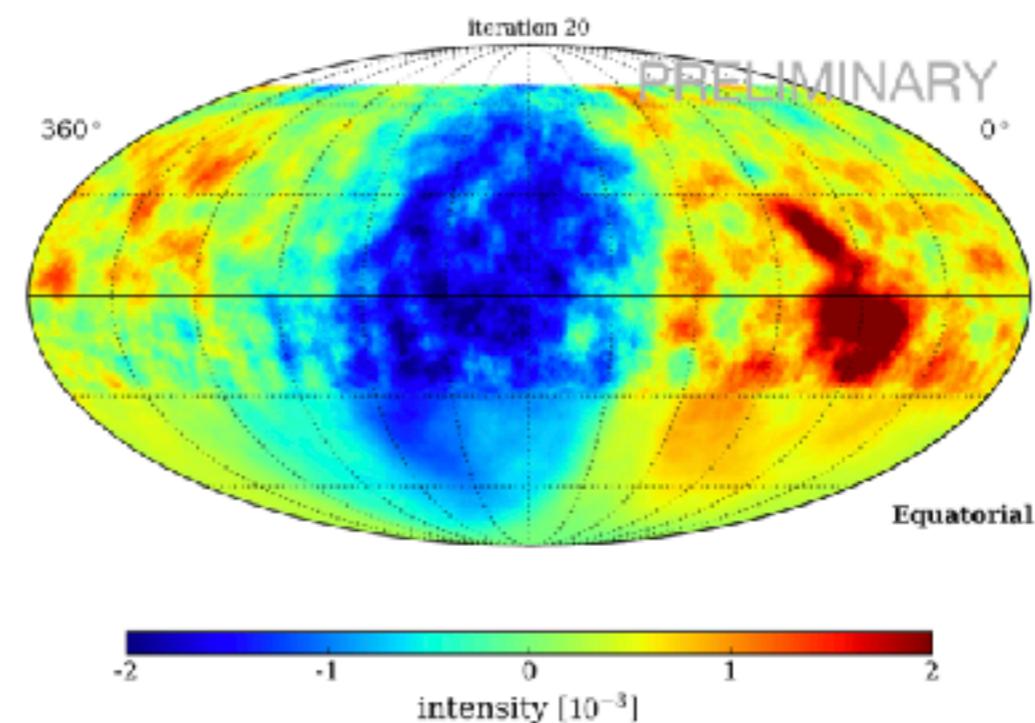


Remove the isotropic term to obtain
relative intensity distribution

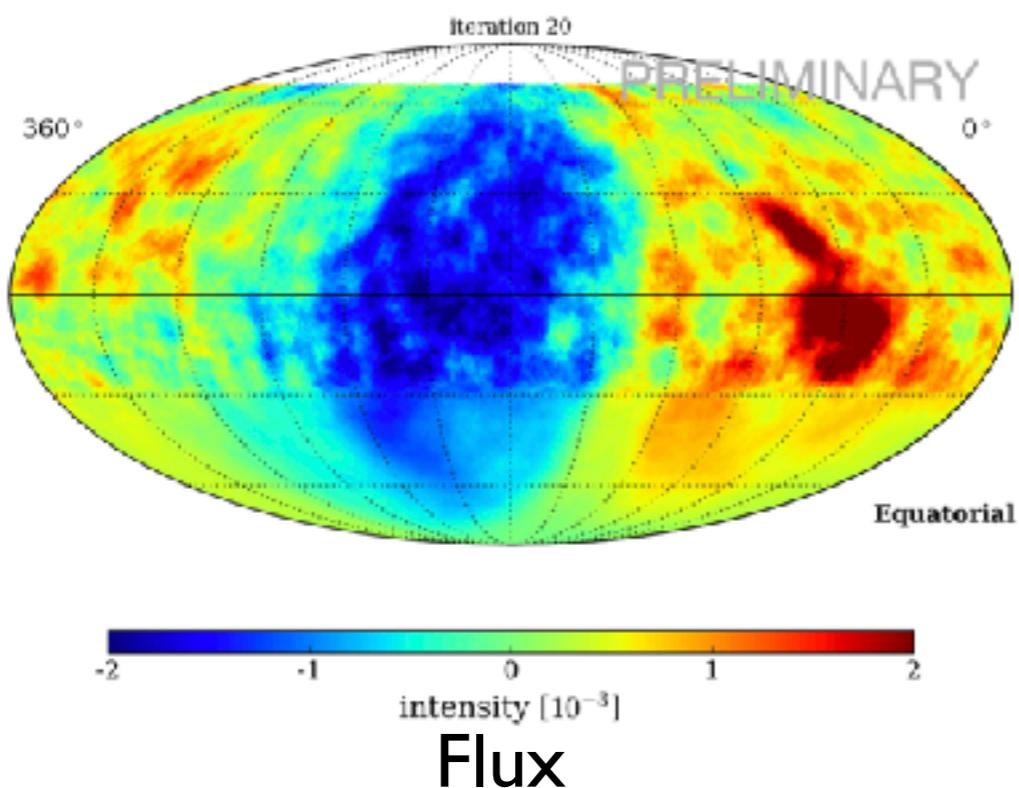
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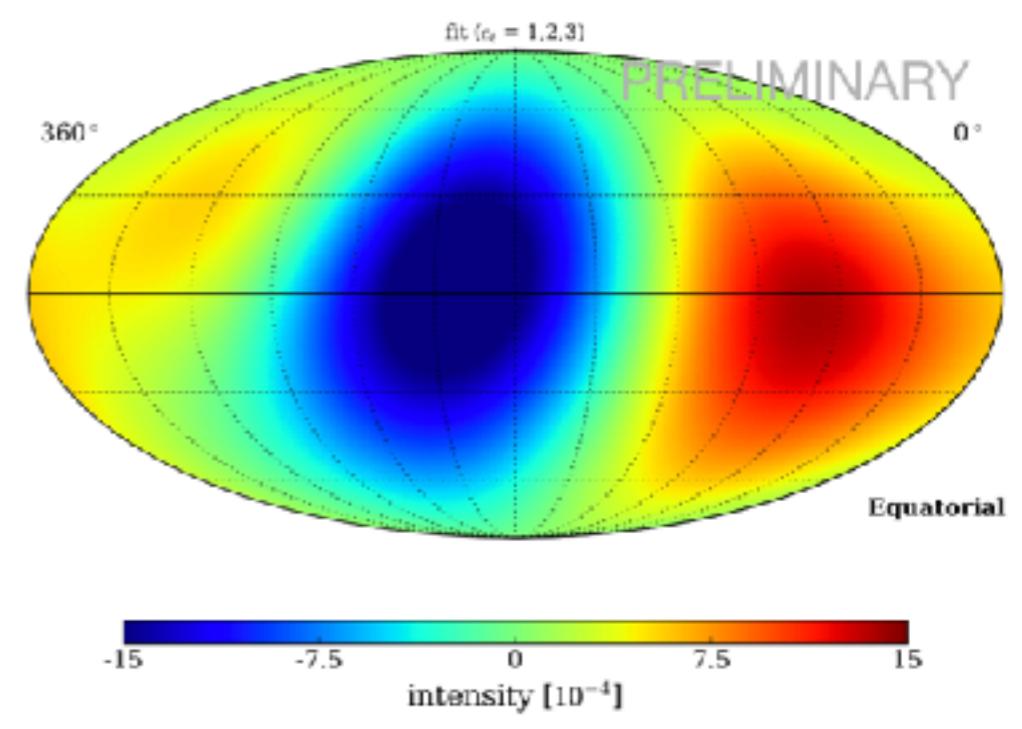
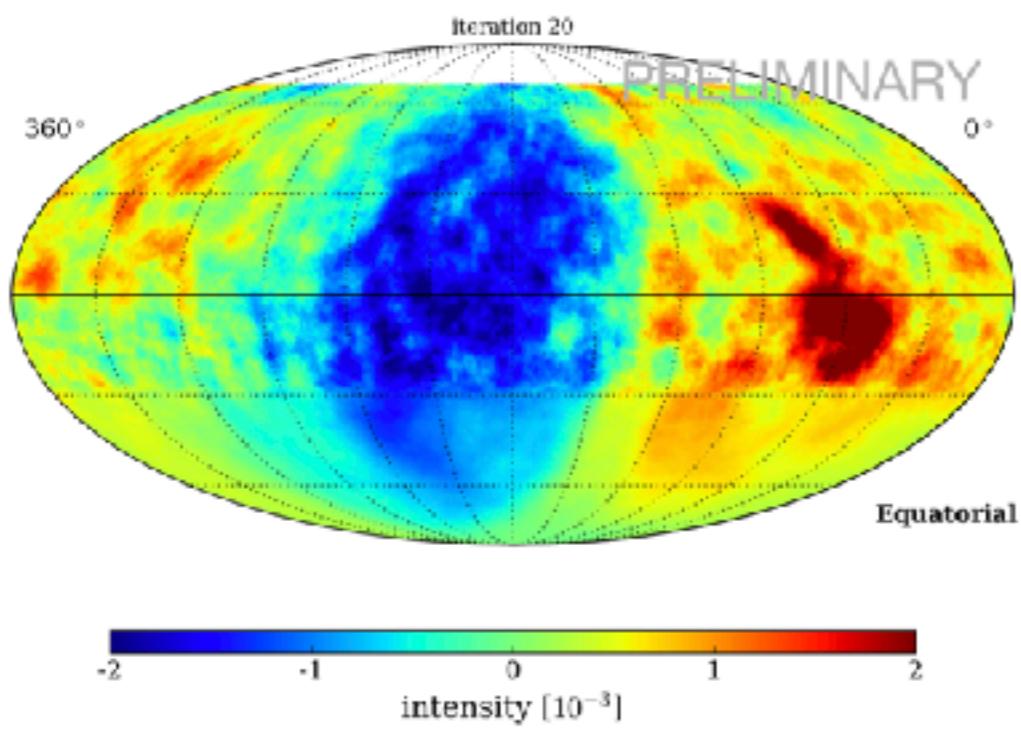
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Large and Small-Scale Anisotropies

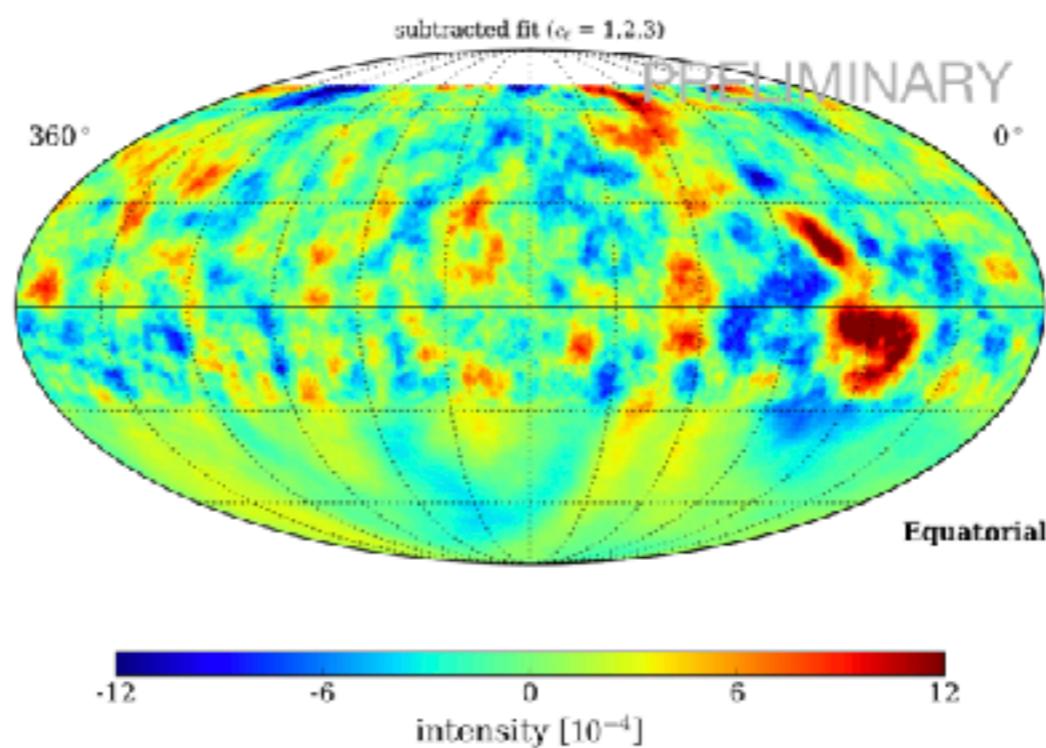
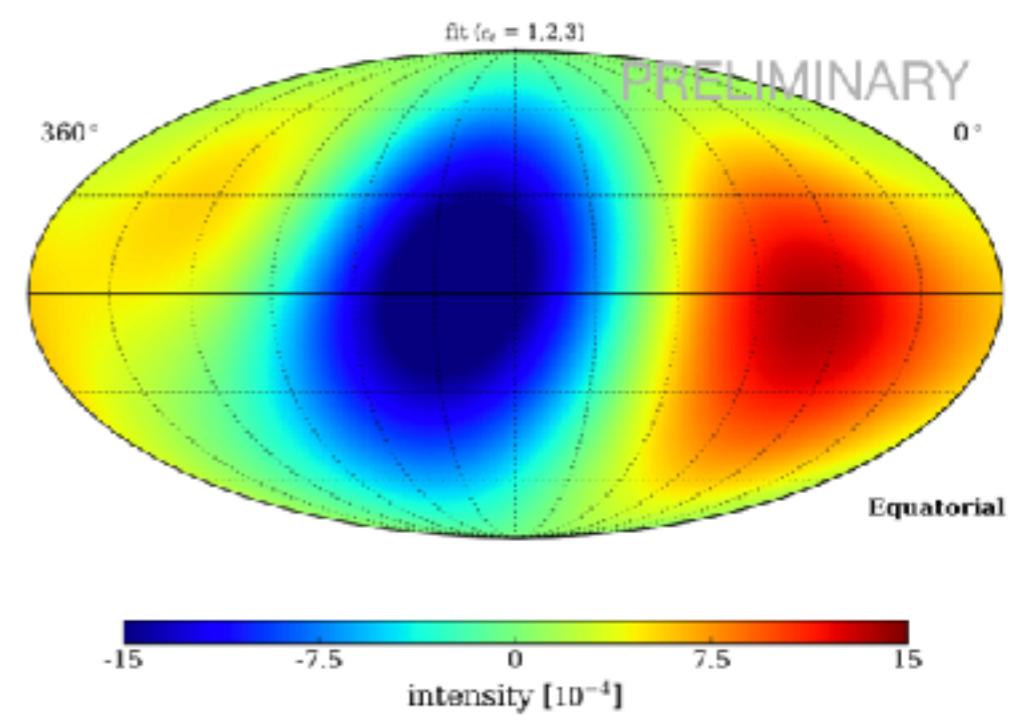
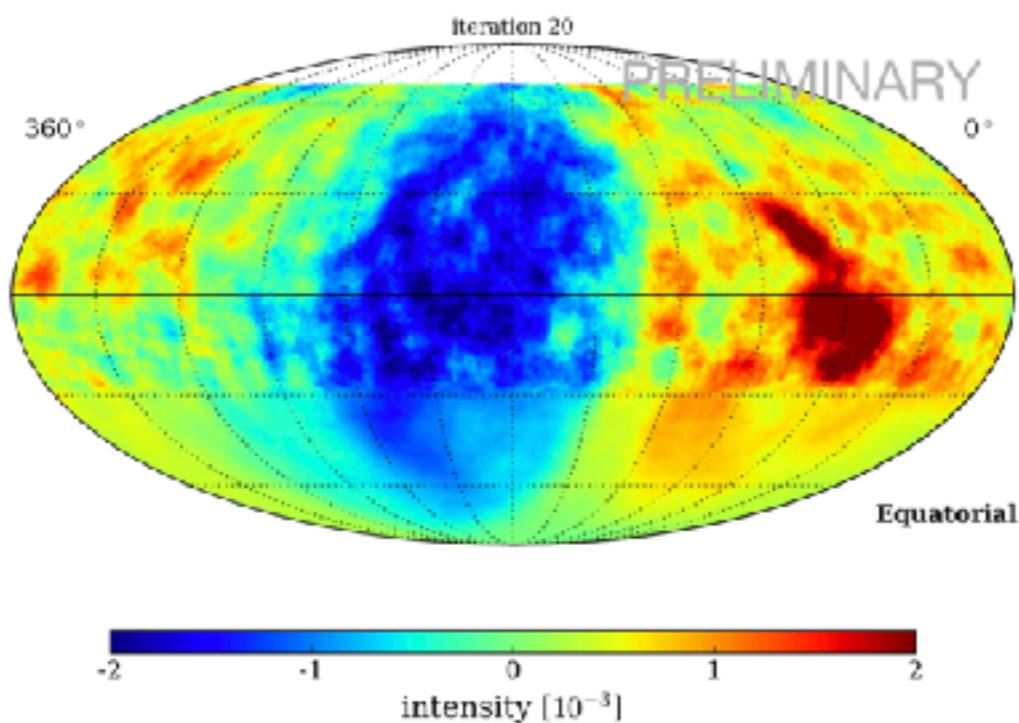


Large and Small-Scale Anisotropies



$\ell=1, 2, 3$ model

Large and Small-Scale Anisotropies



Analysis Algorithm

Analysis Algorithm

Assume that flux in given direction can be written as an isotropic flux times a relative factor

$$\phi(\alpha, \delta) = \phi^{\text{iso}} I(\alpha, \delta)$$

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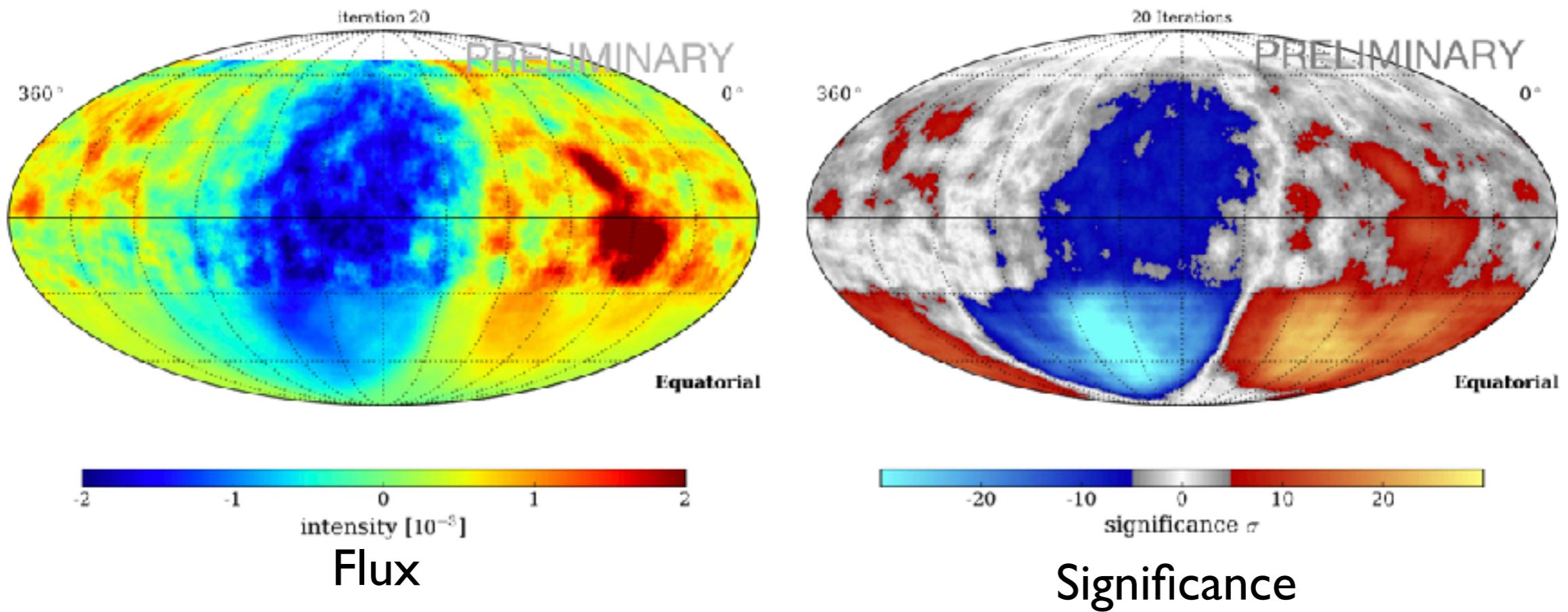
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Maximize this likelihood with respect to the null hypothesis ($I = 1$) gives the best-fit relative intensity and isotropic flux

$$\lambda = \frac{\mathcal{L}(n|I, \mathcal{N}, \mathcal{A})}{\mathcal{L}(n|I^{(0)}, \mathcal{N}^{(0)}, \mathcal{A}^{(0)})}$$

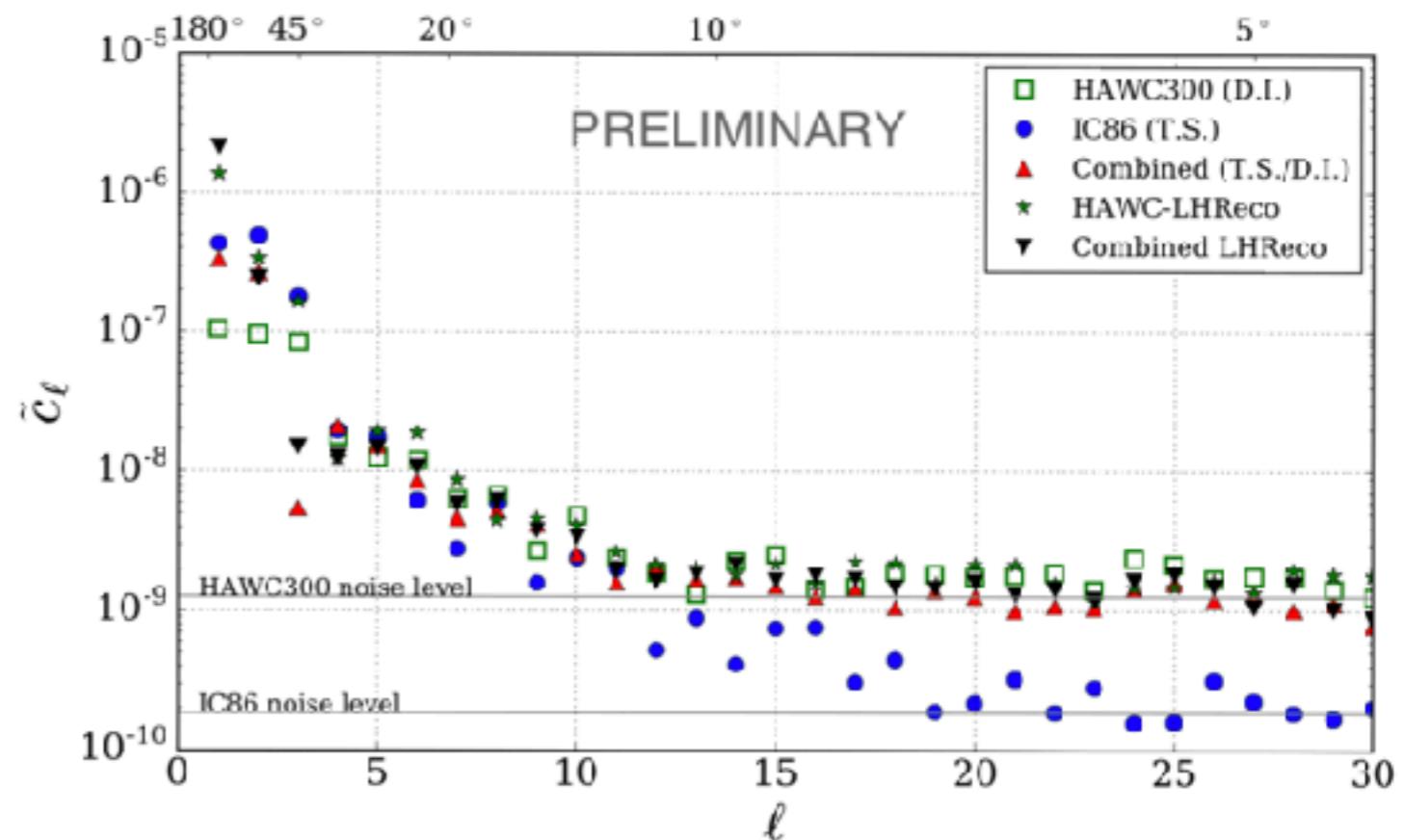
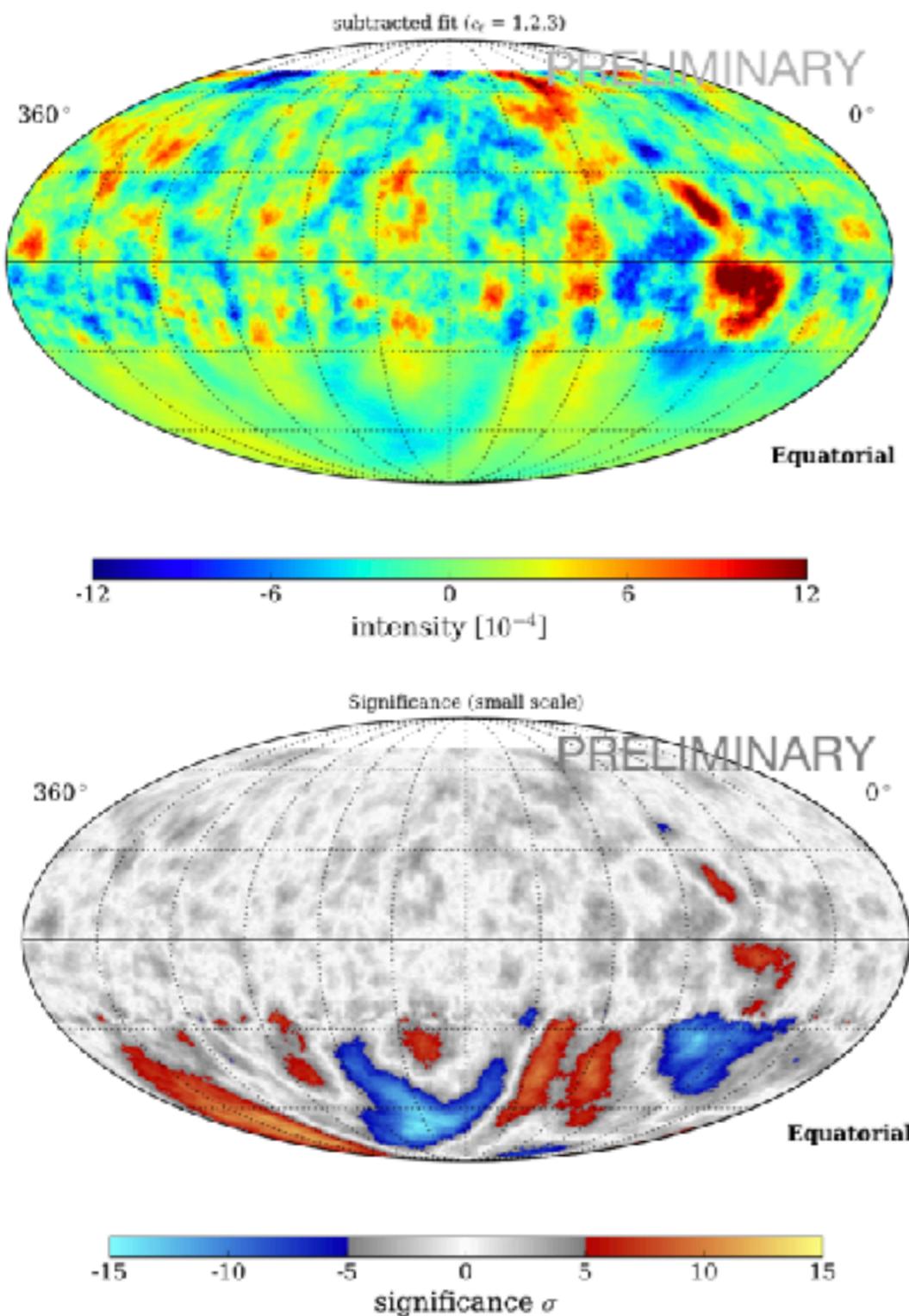
Cosmic Ray Anisotropy at Tens of TeVs - large scale

Cosmic Ray Anisotropy at Tens of TeVs - large scale



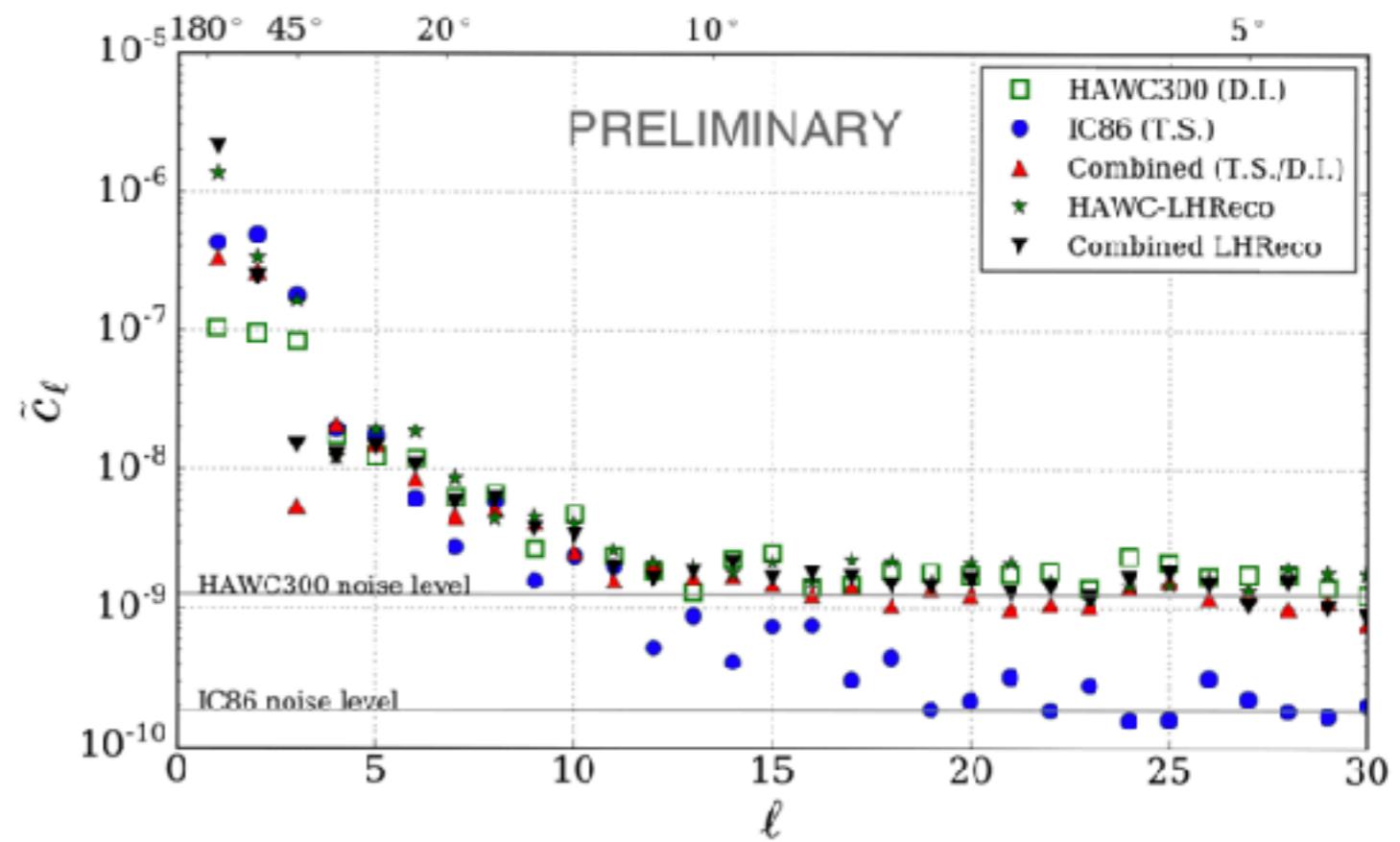
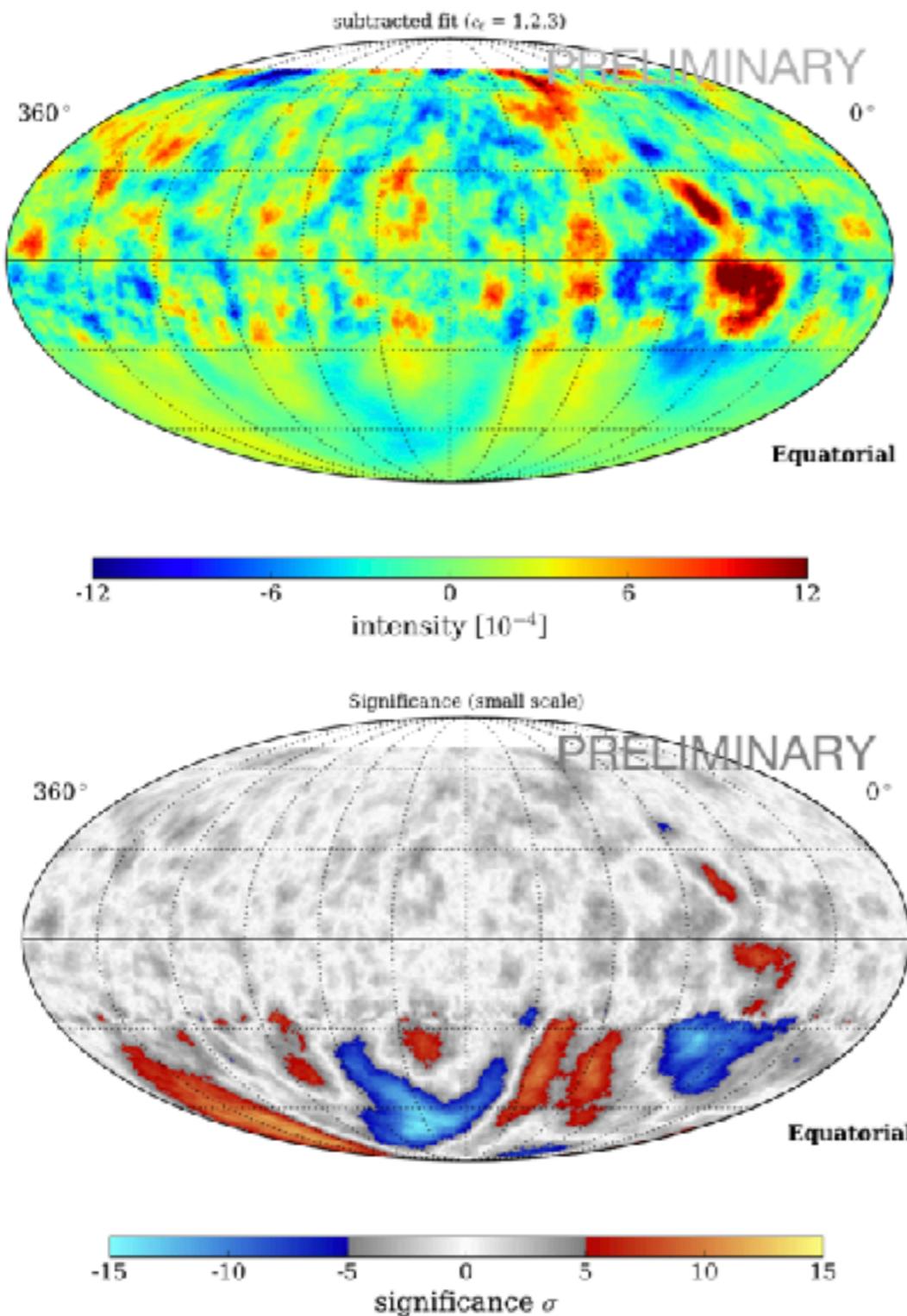
Large-scale anisotropy is at the level of 10^{-3} at ~ 10 TeV

Cosmic Ray Anisotropy at Tens of TeVs



HAWC & IceCube, ICRC 1708.03005

Cosmic Ray Anisotropy at Tens of TeVs



Combined analysis of the HAWC-1yr and IceCube-5yr data finds significant level of anisotropy up to $\ell \sim 10$

HAWC & IceCube, ICRC 1708.03005

Cosmic Ray Anisotropy at > EeV

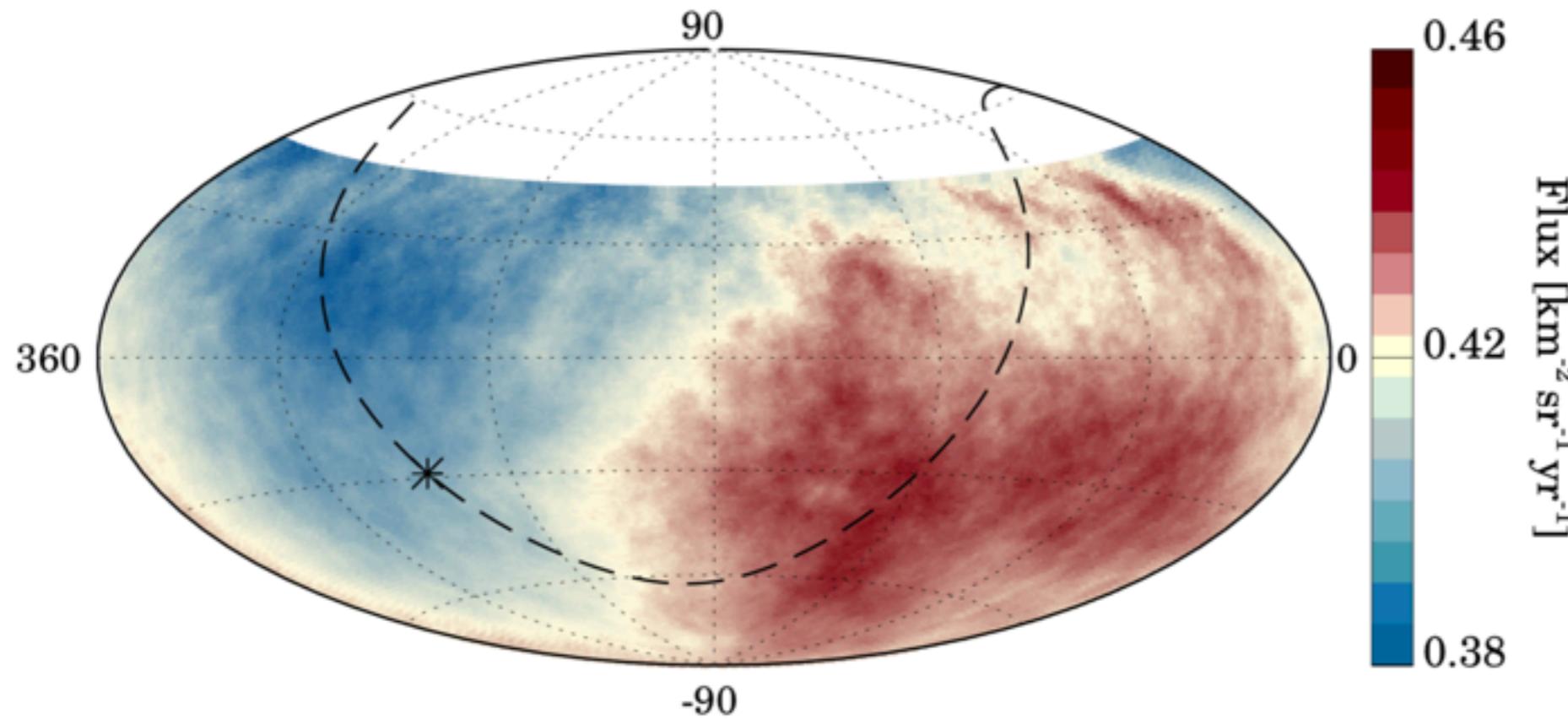


Table 3. Results of the first-harmonic analysis in right ascension in the three bins above 8 EeV.

Energy [EeV]	events	a_1^α	b_1^α	r_1^α	φ_1^α [°]	$P(\geq r_1^\alpha)$
8 - 16	24,070	-0.011 ± 0.009	0.044 ± 0.009	0.046	104 ± 11	3.7×10^{-6}
16 - 32	6,604	0.007 ± 0.017	0.050 ± 0.017	0.051	82 ± 20	0.014
≥ 32	1,513	-0.03 ± 0.04	0.05 ± 0.04	0.06	115 ± 35	0.26

Cosmic Ray Anisotropy at > EeV

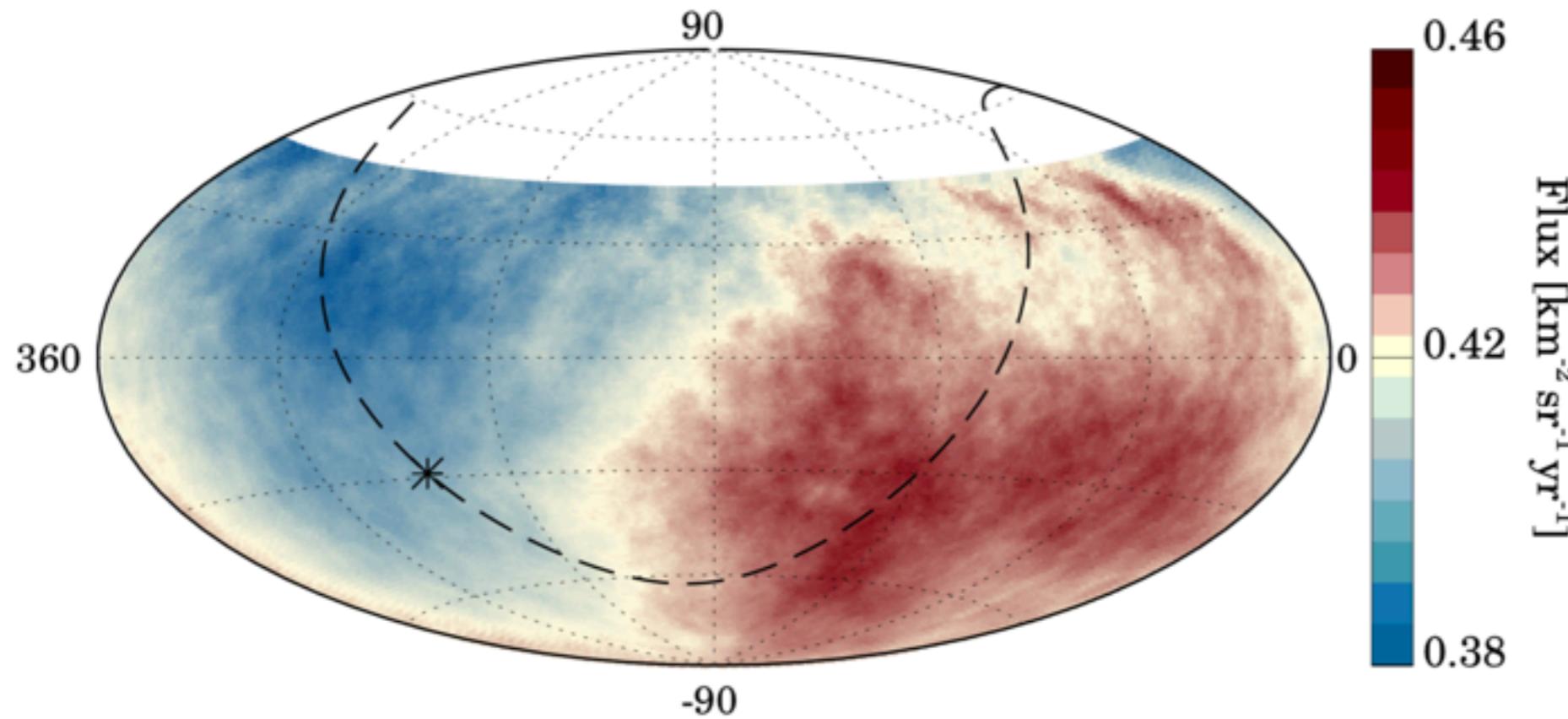
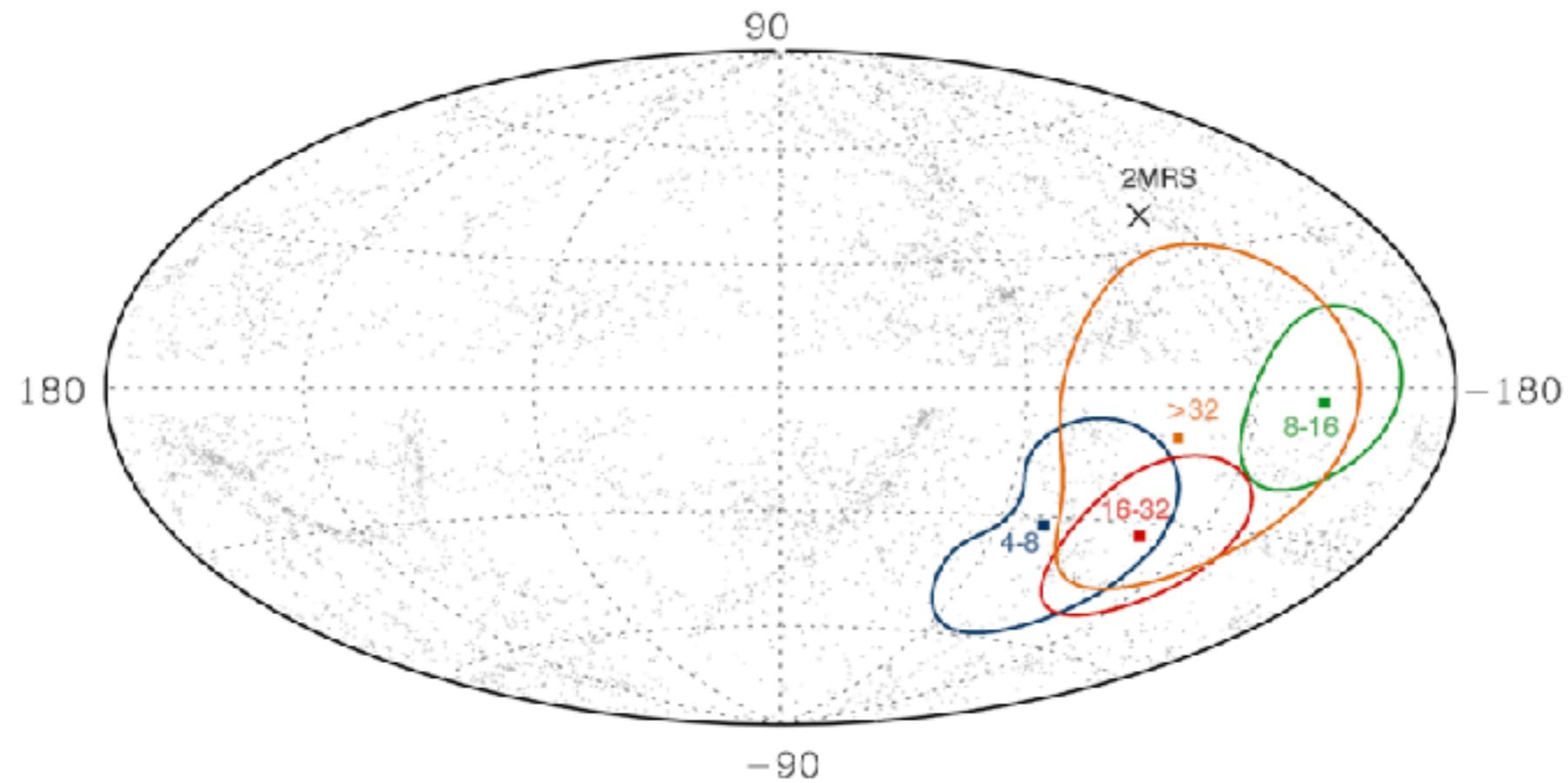


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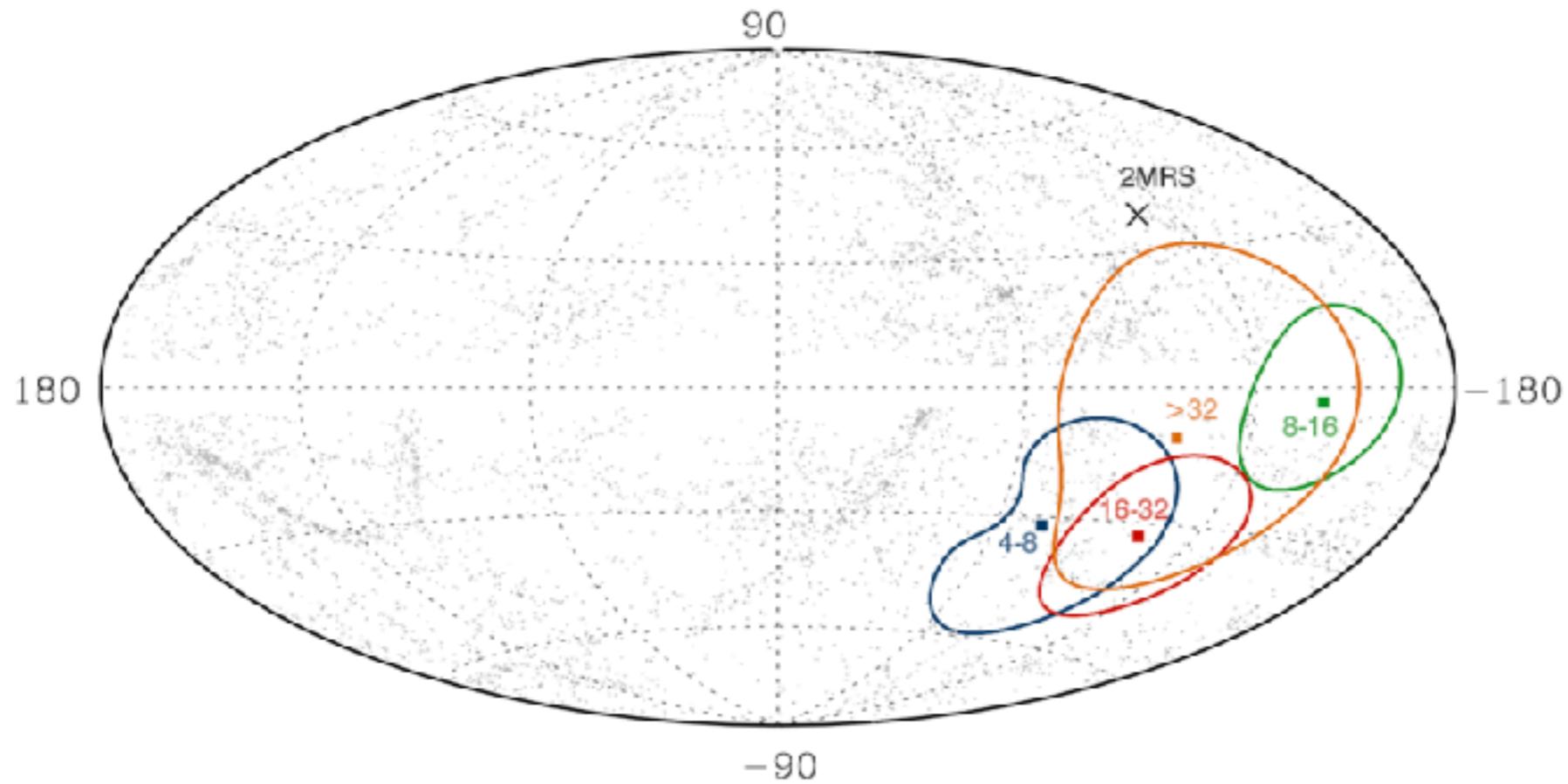
>5 sigma Dipole found above 8 EeV

Hints to Cosmic Ray Origins



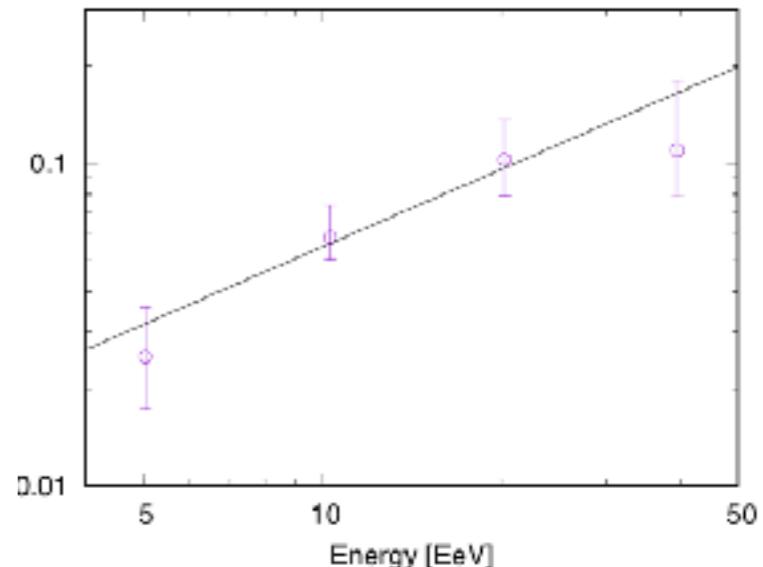
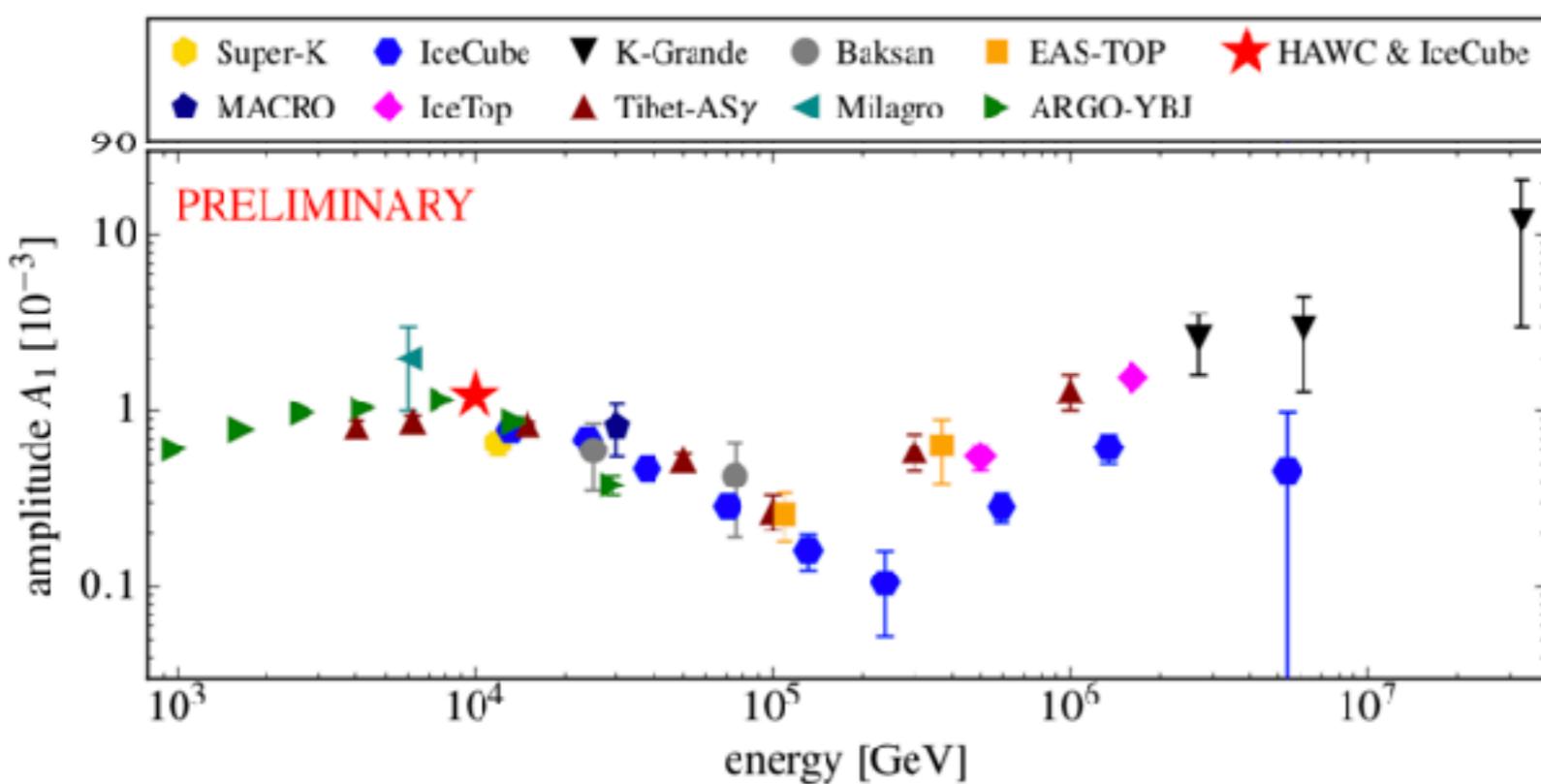
Auger Collaboration ApJ (2018)

Hints to Cosmic Ray Origins

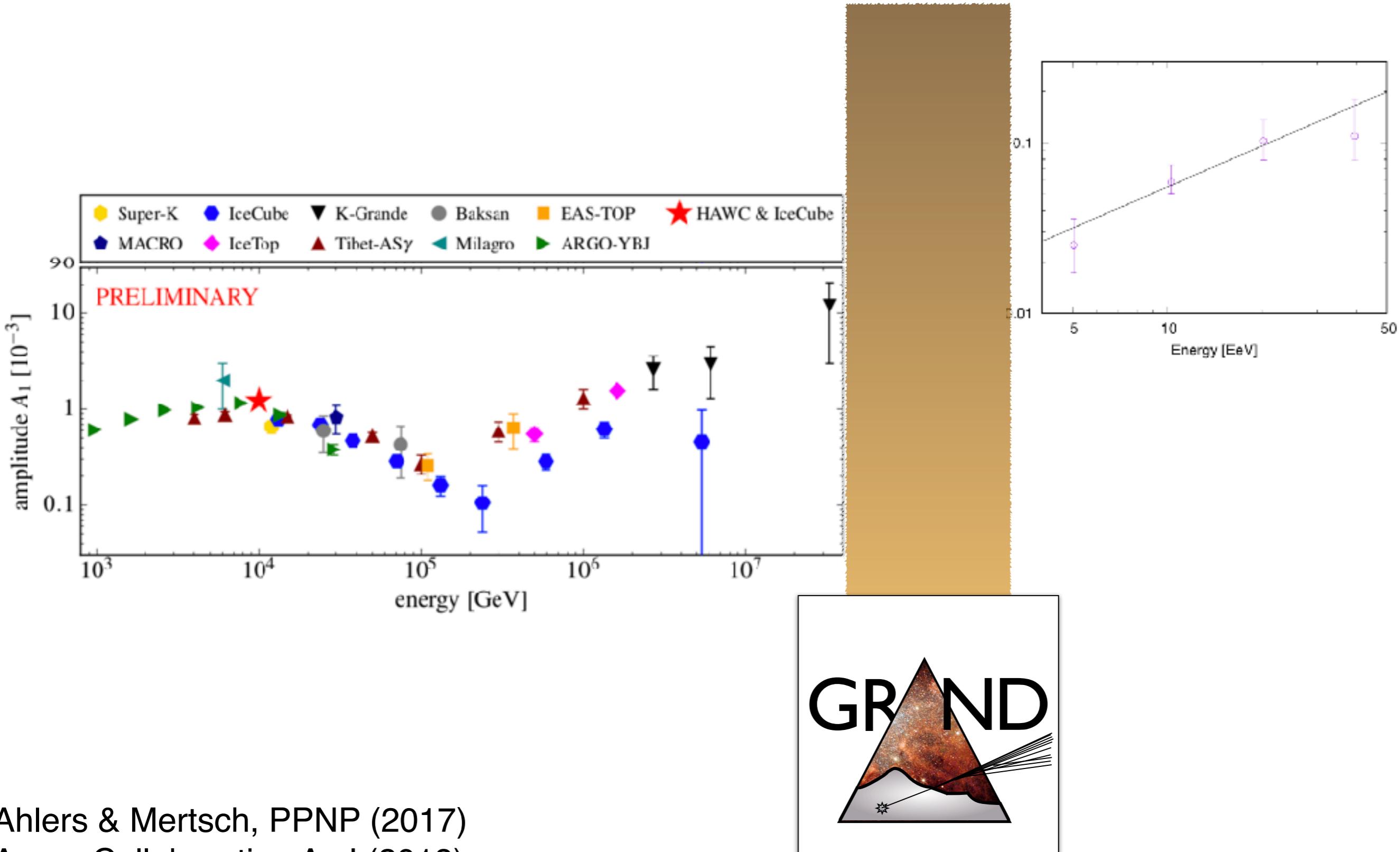


Dipole directions as function of energy, comparing with that from galaxies in the 2MRS catalog

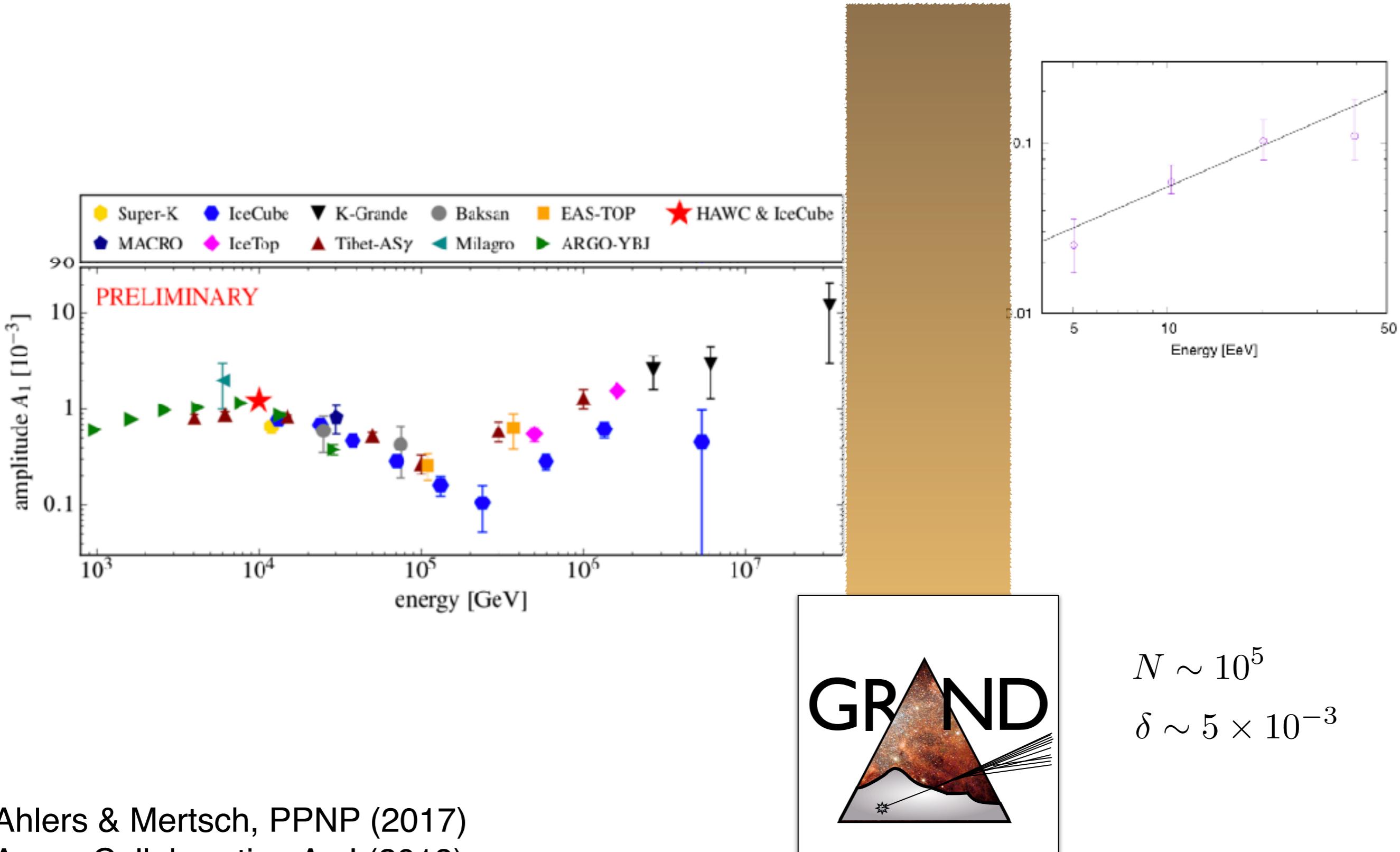
Dipole Amplitude Over Energy

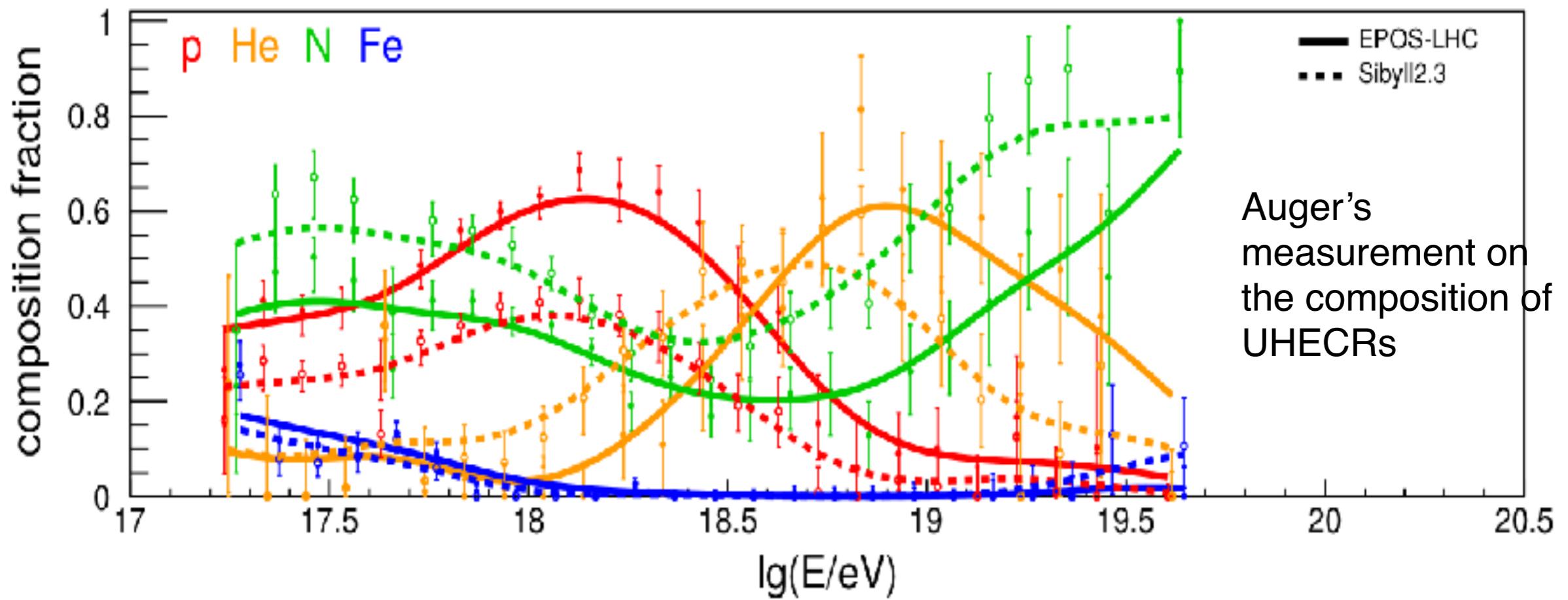


Dipole Amplitude Over Energy



Dipole Amplitude Over Energy

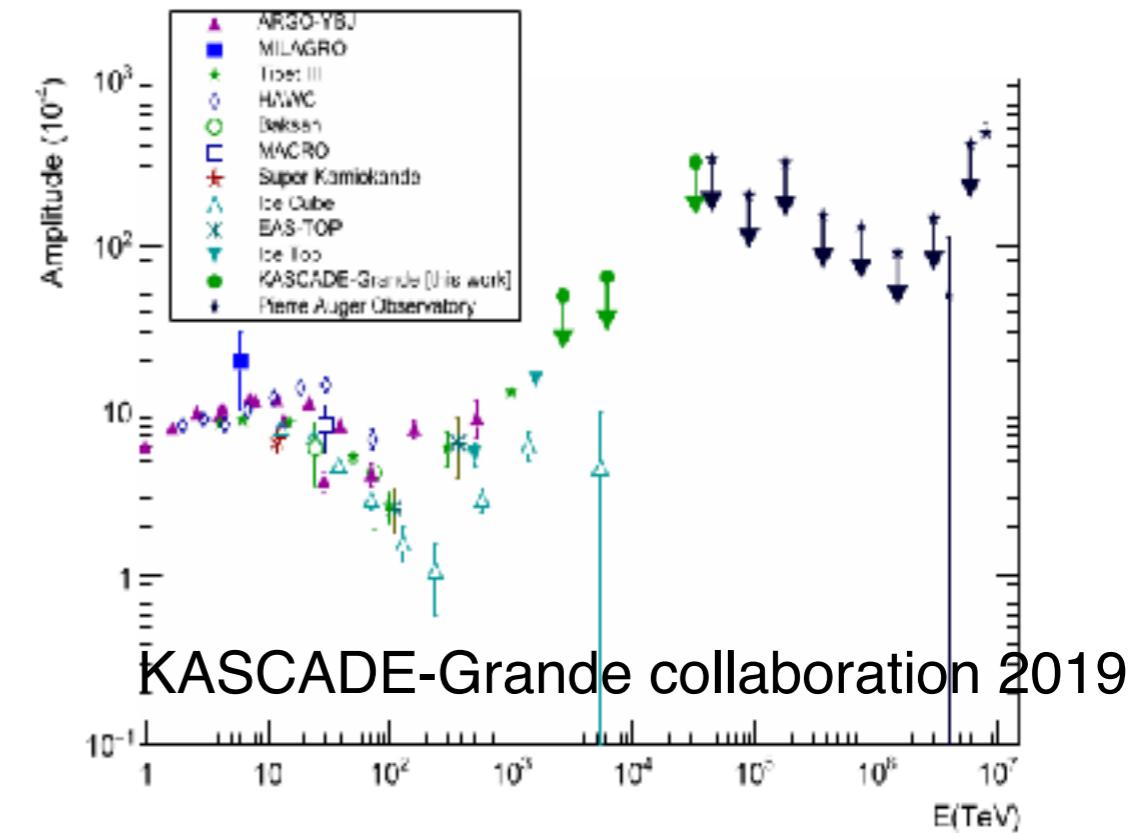




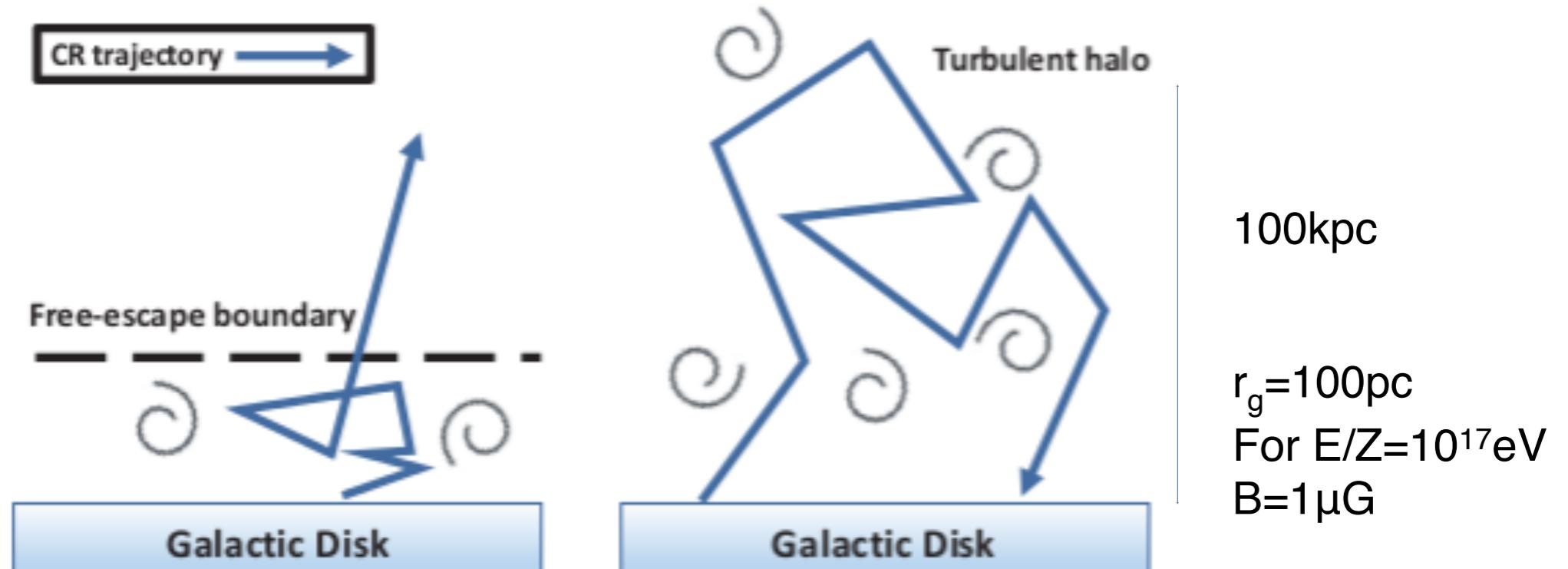
Large-scale anisotropy:
Dipolar component

$$\vec{\Delta} = 3D \frac{\vec{\nabla} n}{n}$$

Possible contribution from GP300:
origin of intermediate-mass nuclei at sub-ankle
Constraint on the properties of local magnetic field (D)



Galactic CRs



Liu et al. 2019

Ex-Galactic CRs

$$D_{\text{diff}}(E < E_*) \sim \left(\frac{c\ell_{\text{coh}}}{H_0}\right)^{1/2} \left(\frac{E}{E_*}\right)^{1/2}$$
$$\simeq 55 \ell_0^{1/2} h^{-1/2} \left(\frac{E}{E_*}\right)^{1/2} \text{ Mpc}$$

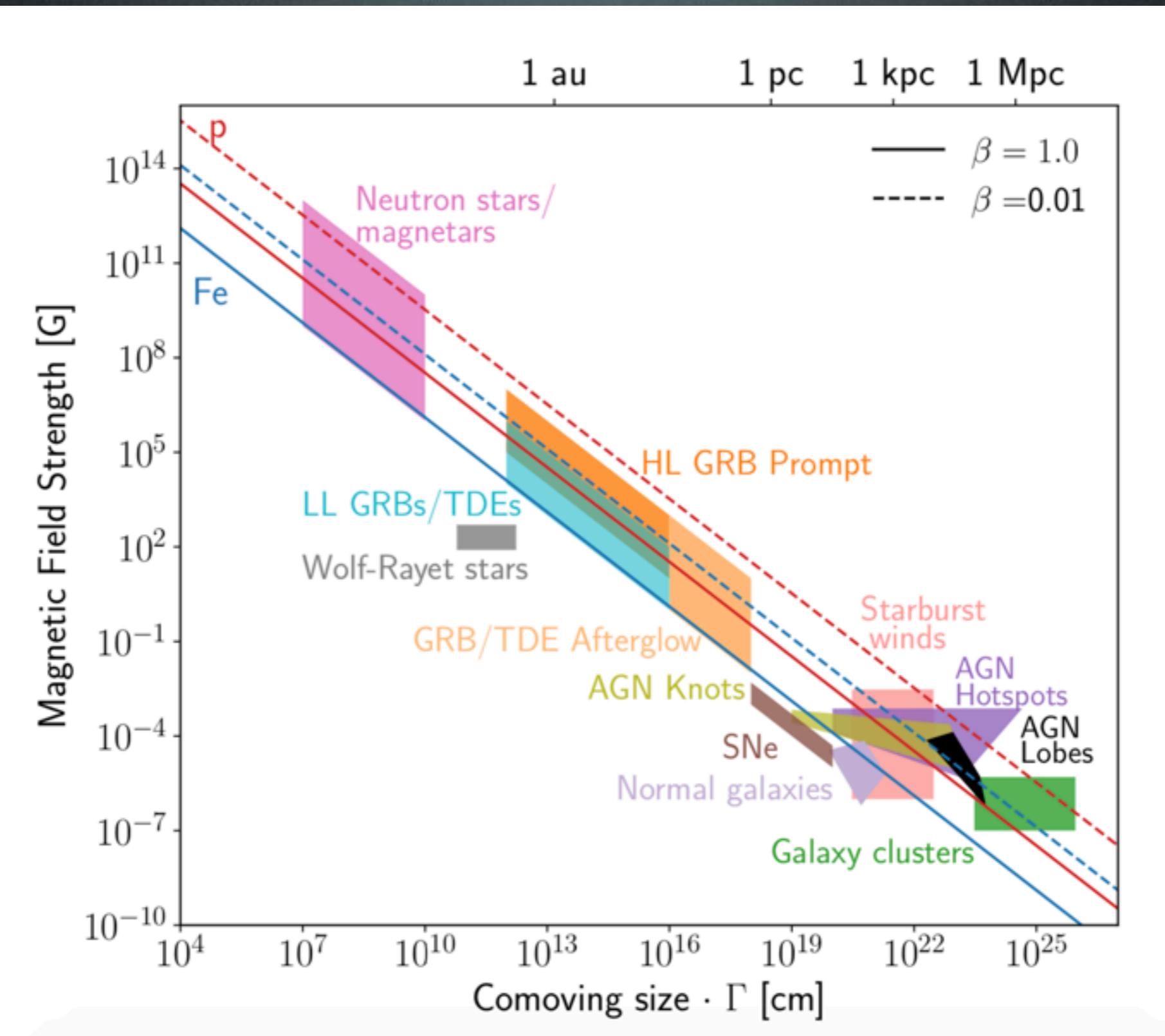
$$\ell_0 = \ell_{\text{coh}}/(1 \text{ Mpc})$$

$$E_* \equiv Z e B_r \ell_{\text{coh}} \simeq 9.2 \times 10^{17} Z B_{-9} \ell_0 \text{ eV}$$

Magnetic horizon for $E < E^*$
(CRs trapped by intergalactic magnetic field
Diffuse slow and cannot reach Earth within the
age of the Universe)

Achterberg et al. 1999

Pulsars as Sources of UHECRs

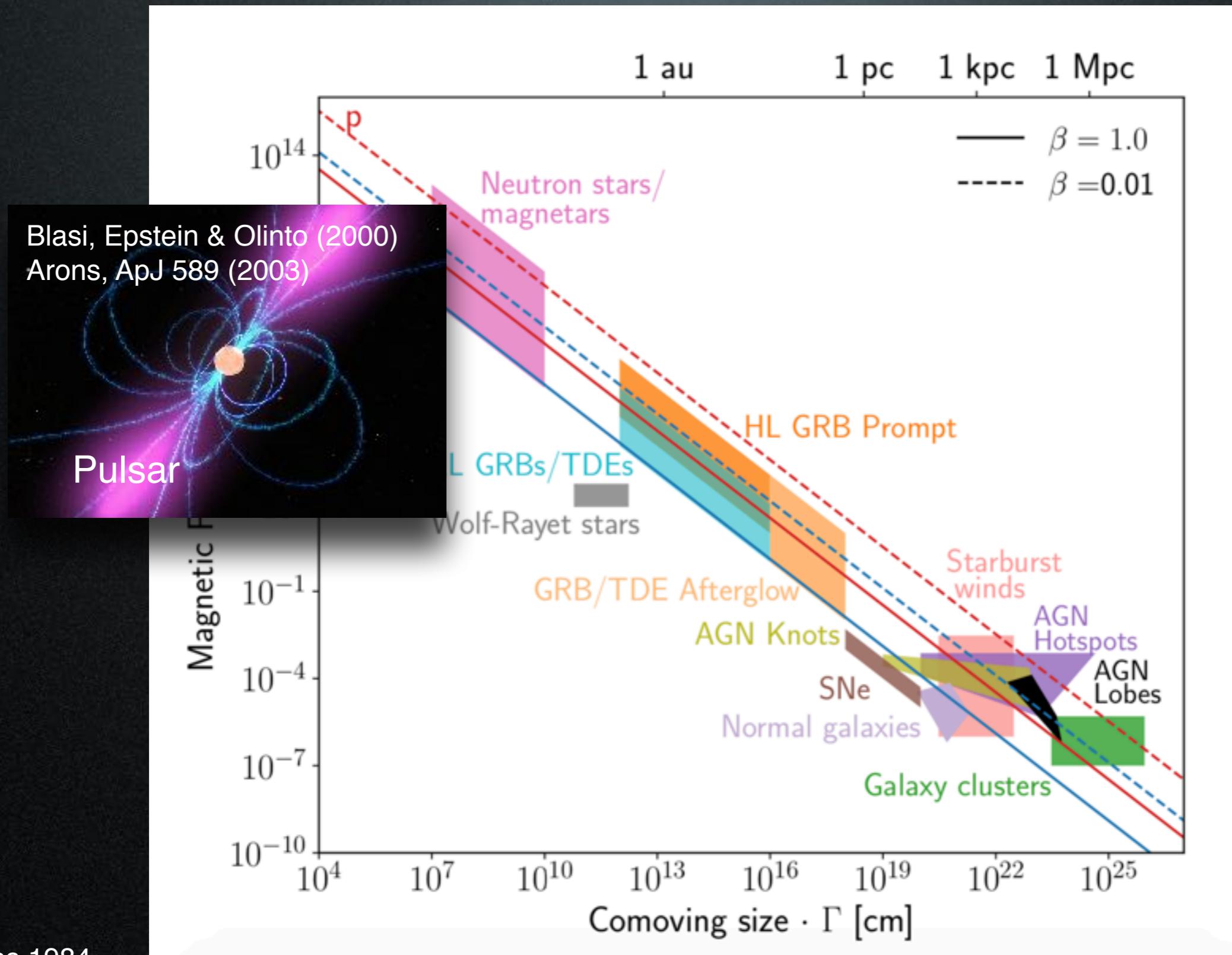


Hillas 1984

Kotera & Olinto 1101.4256

Alves Batista, Biteau, Bustamante et al, 1903.06714

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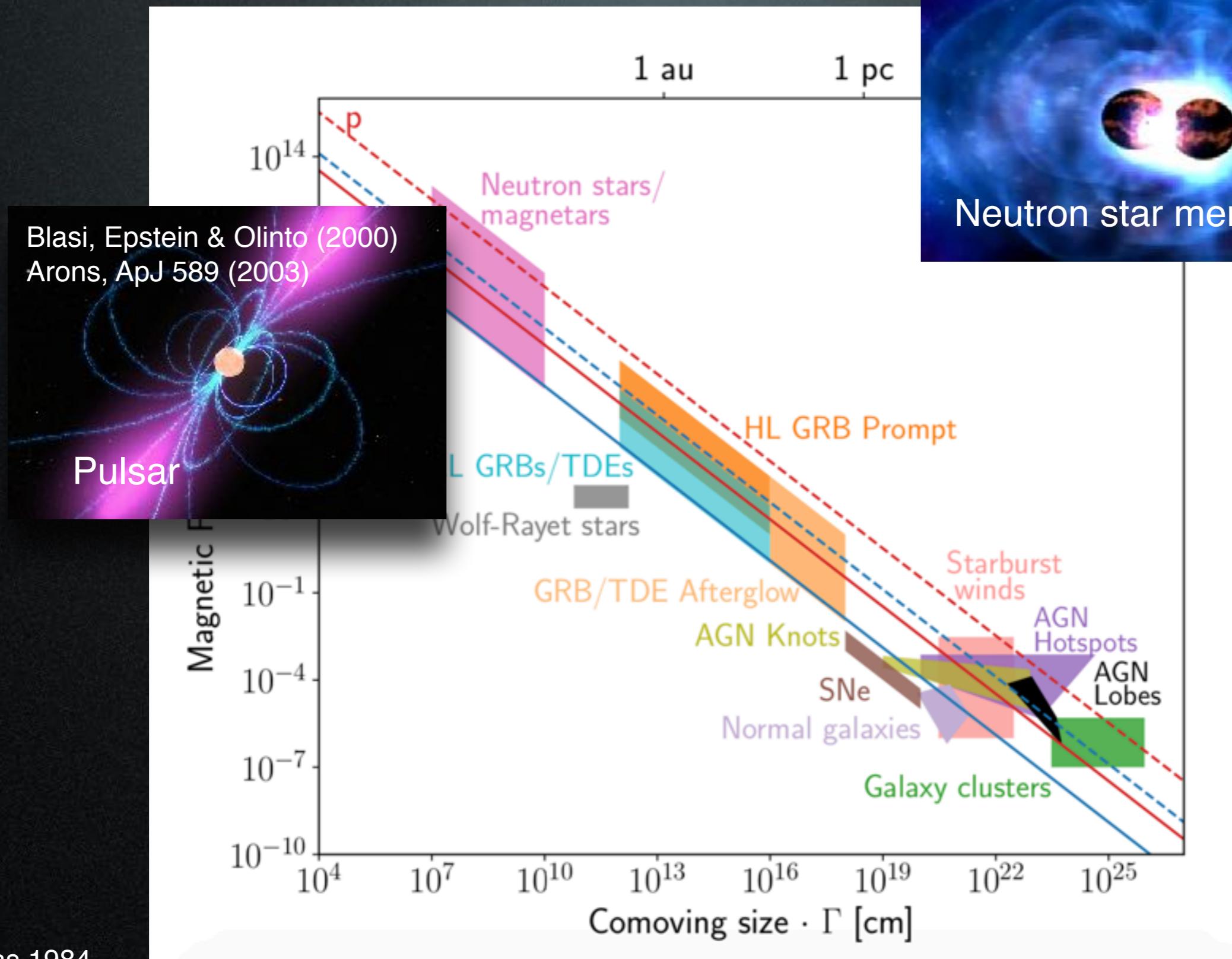


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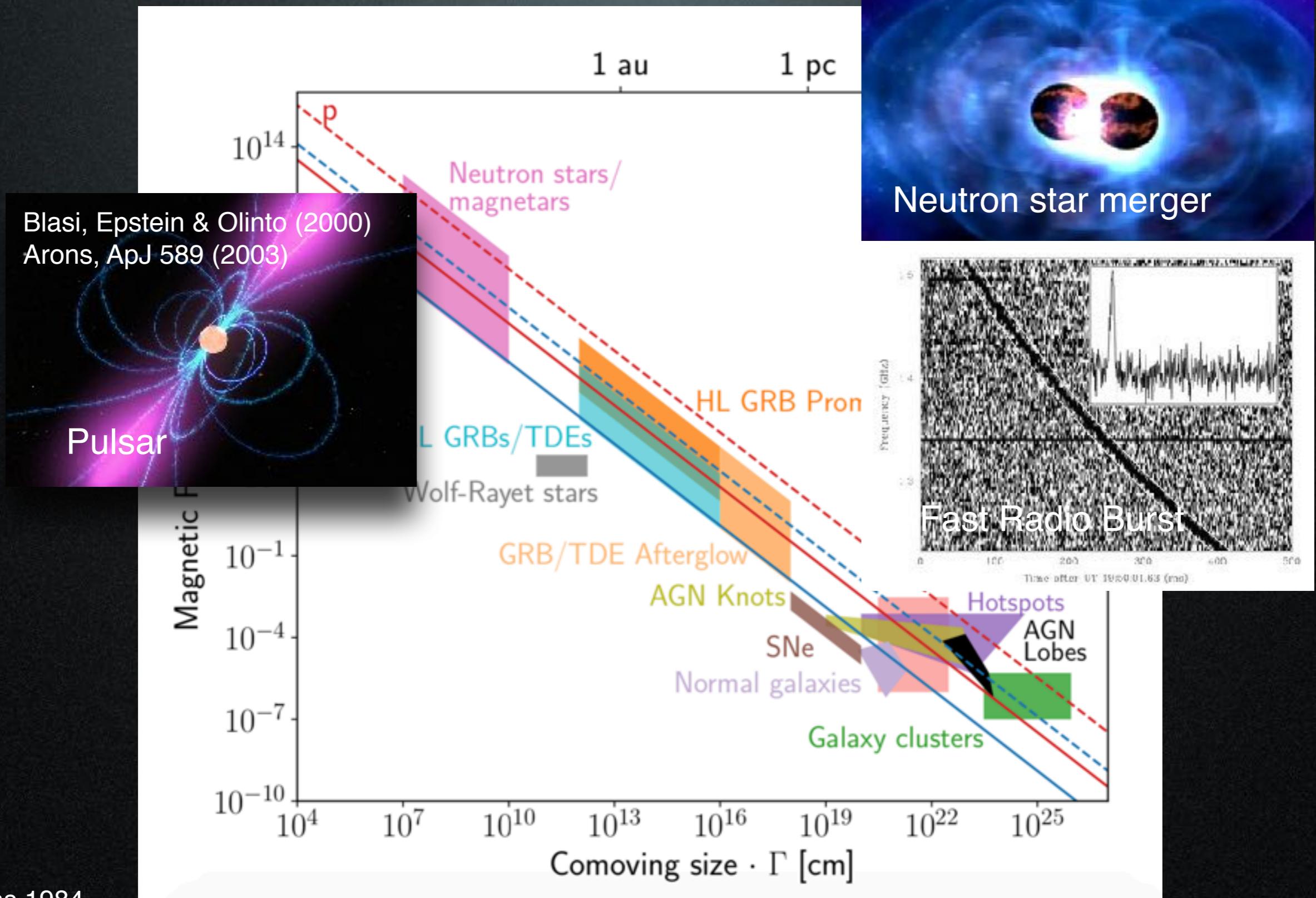


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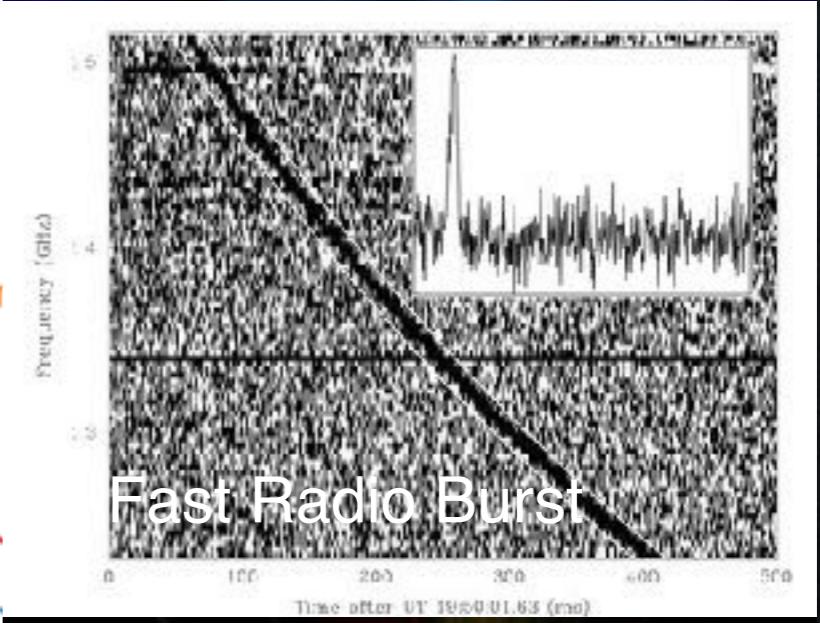
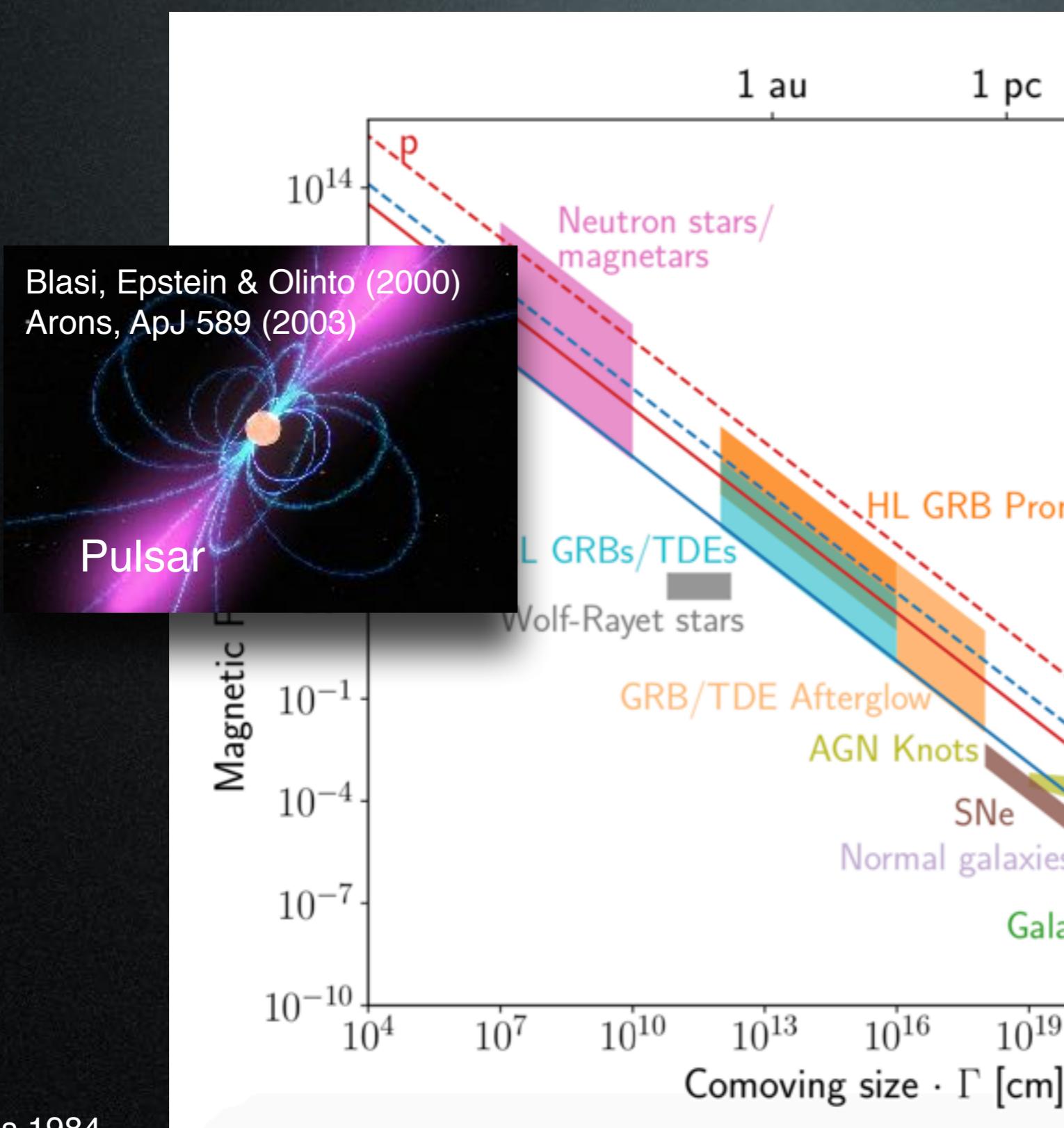


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Cosmic Ray Acceleration

e.g.
Kirk & Lyubarsky (2001)
Arons, ApJ 589 (2003)

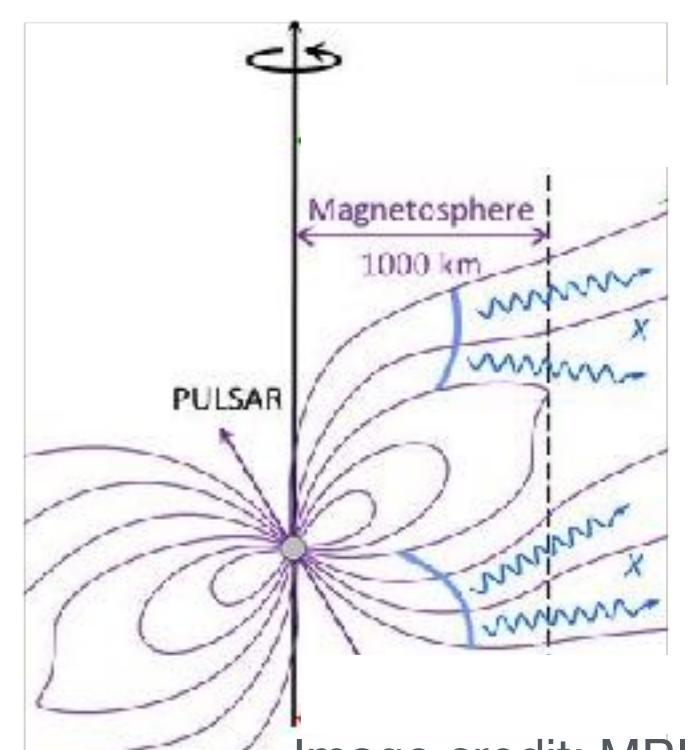


Image credit: MPIK

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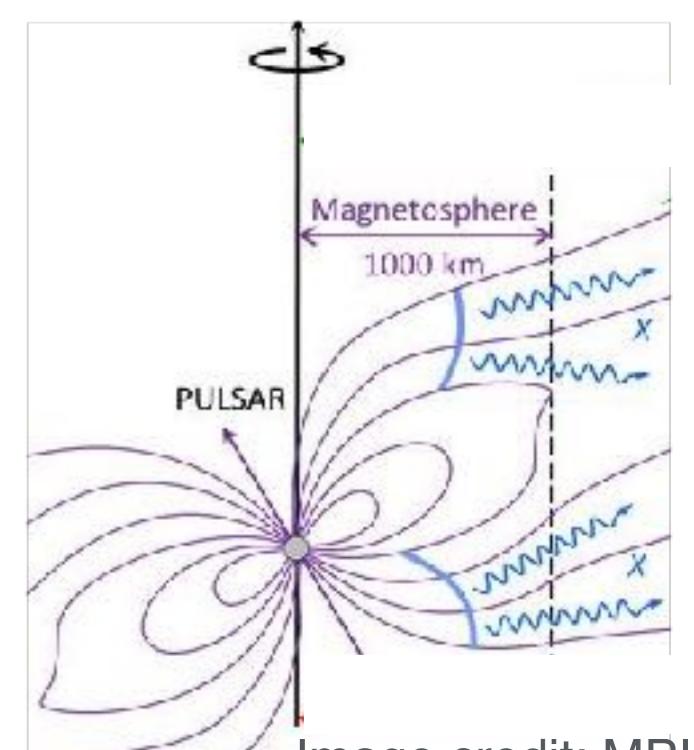


Image credit: MPIK

Particle energy

$$E_{\text{CR}} = 10^{18} A \left(\frac{B}{10^{13} \text{ G}} \right) \left(\frac{P_i}{1 \text{ ms}} \right)^{-2} \left(\frac{\eta}{0.3} \right) \left(\frac{\kappa}{10^4} \right)^{-1} \left(1 + \frac{t}{\tau_{\text{sd}}} \right)^{-1} \text{ eV}$$

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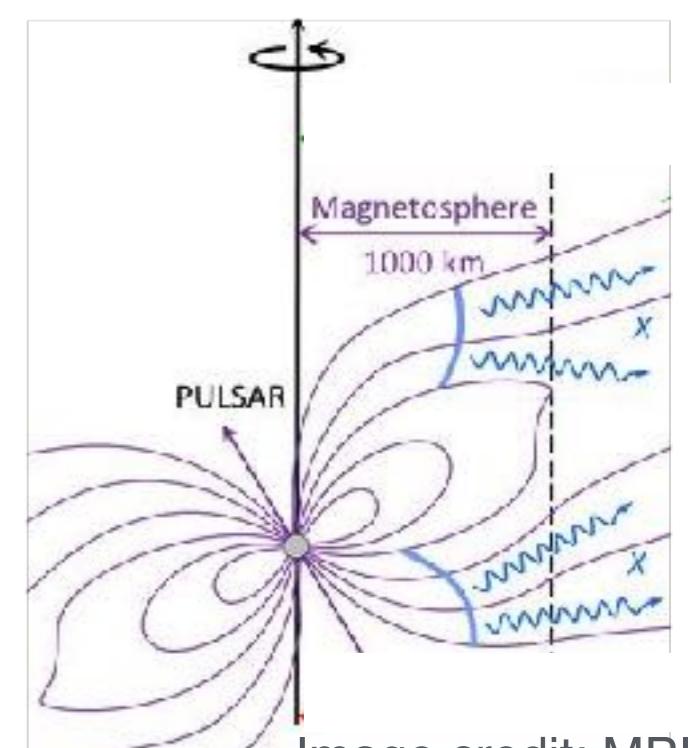


Image credit: MPIK

Particle energy

Magnetic Field

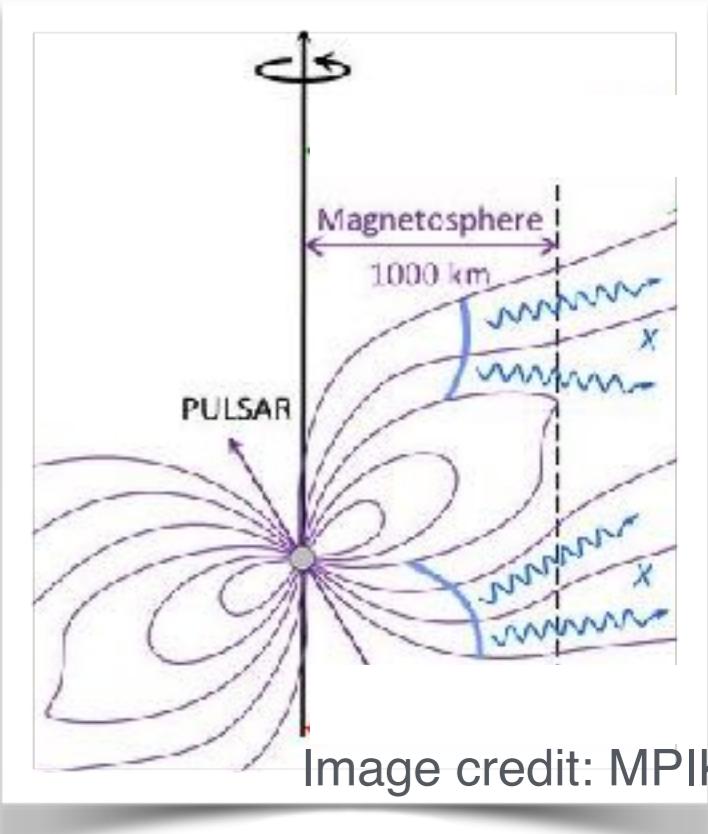
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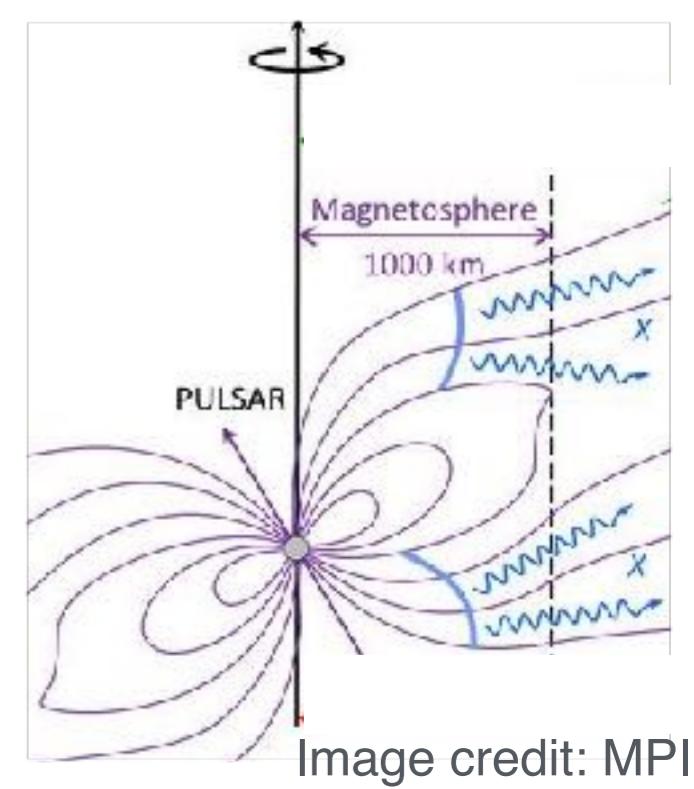
Particle energy initial spin period Magnetic Field

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Cosmic Ray Acceleration

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Arons, ApJ 589 (2003)



Particle energy

initial spin period

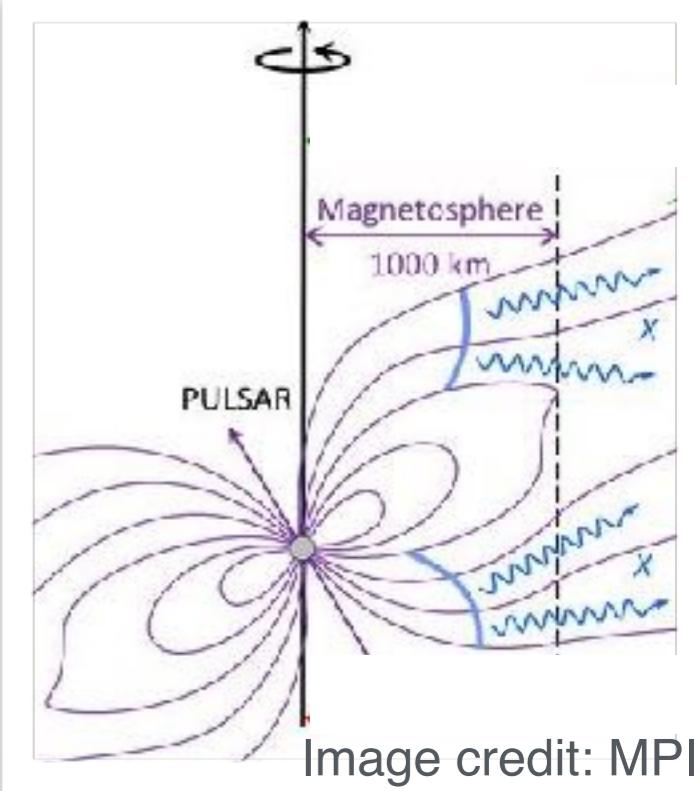
Magnetic Field

Wind efficiency

$$E_{\text{CR}} = 10^{18} A \left(\frac{B}{10^{13} \text{ G}} \right) \left(\frac{P_i}{1 \text{ ms}} \right)^{-2} \left(\frac{\eta}{0.3} \right) \left(\frac{\kappa}{10^4} \right)^{-1} \left(1 + \frac{t}{\tau_{\text{sd}}} \right)^{-1} \text{ eV}$$

Cosmic Ray Acceleration

e.g.
Kirk & Lyubarsky (2001)
Arons, ApJ 589 (2003)



Particle energy

initial spin period

Magnetic Field

Wind efficiency

Multiplicity

$$E_{\text{CR}} = 10^{18} A \left(\frac{B}{10^{13} \text{ G}} \right) \left(\frac{P_i}{1 \text{ ms}} \right)^{-2} \left(\frac{\eta}{0.3} \right) \left(\frac{\kappa}{10^4} \right)^{-1} \left(1 + \frac{t}{\tau_{\text{sd}}} \right)^{-1} \text{ eV}$$

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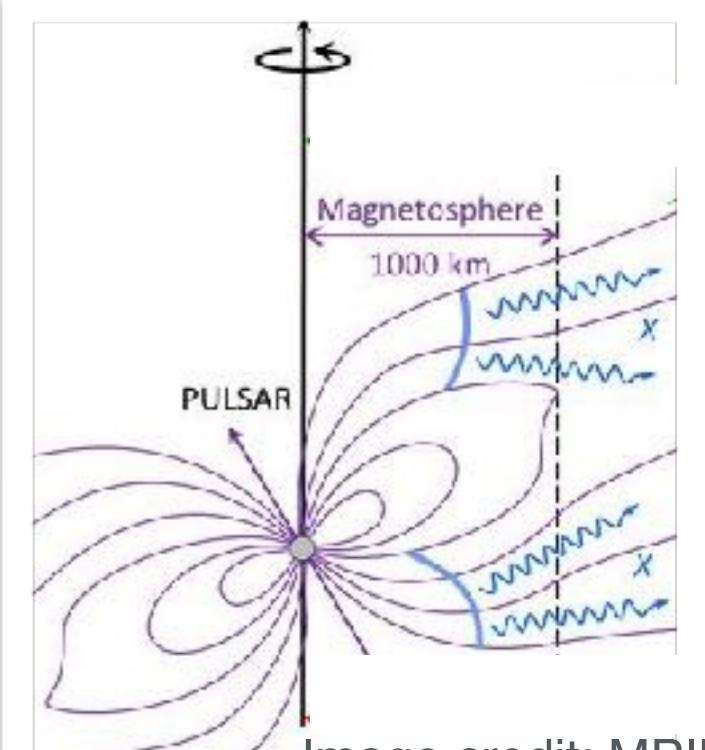


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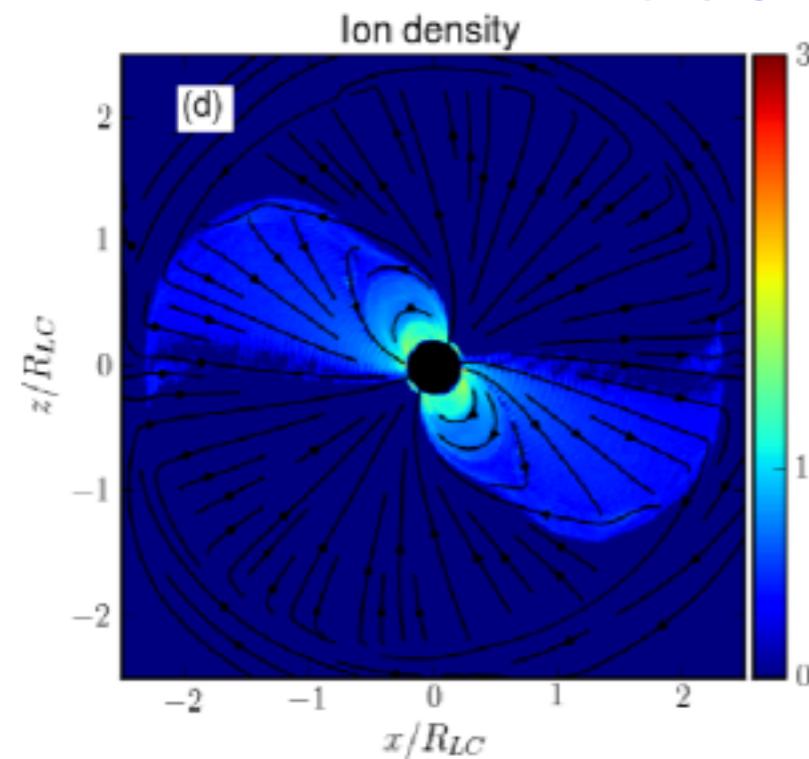
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Cosmic ray injection spectrum

$$\frac{dN_{\text{CR}}}{dE} \propto E^{-1}$$

Cosmic Ray Acceleration



Philippov & Spitkovsky 1707.04323

e.g.
Kirk & Lyubarsky (2001)
Arons, ApJ 589 (2003)

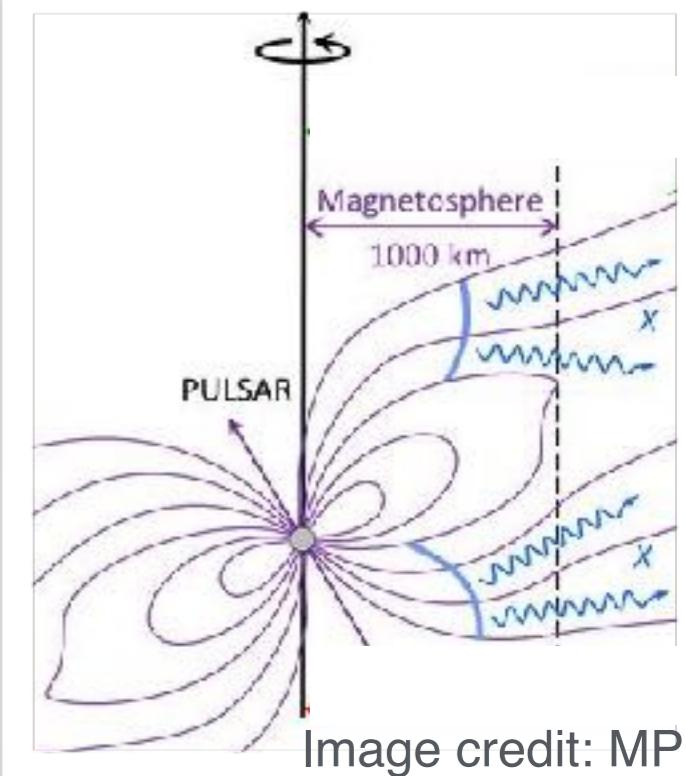


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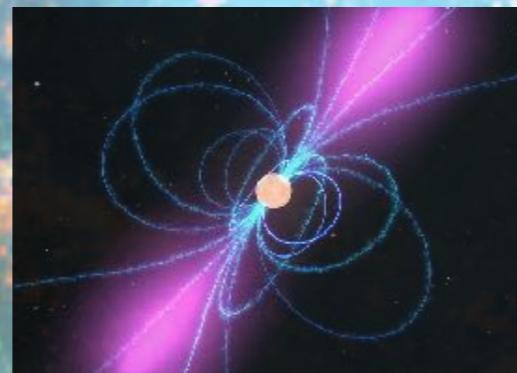
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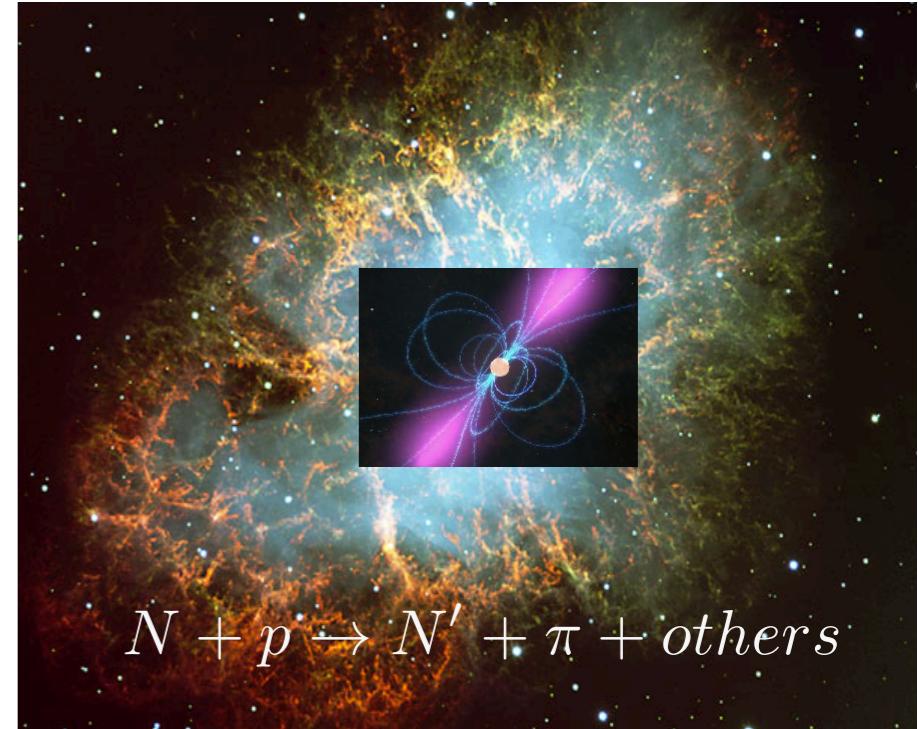
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Cosmic ray particles interacting
with hadronic supernova ejecta



Interaction with Ejecta

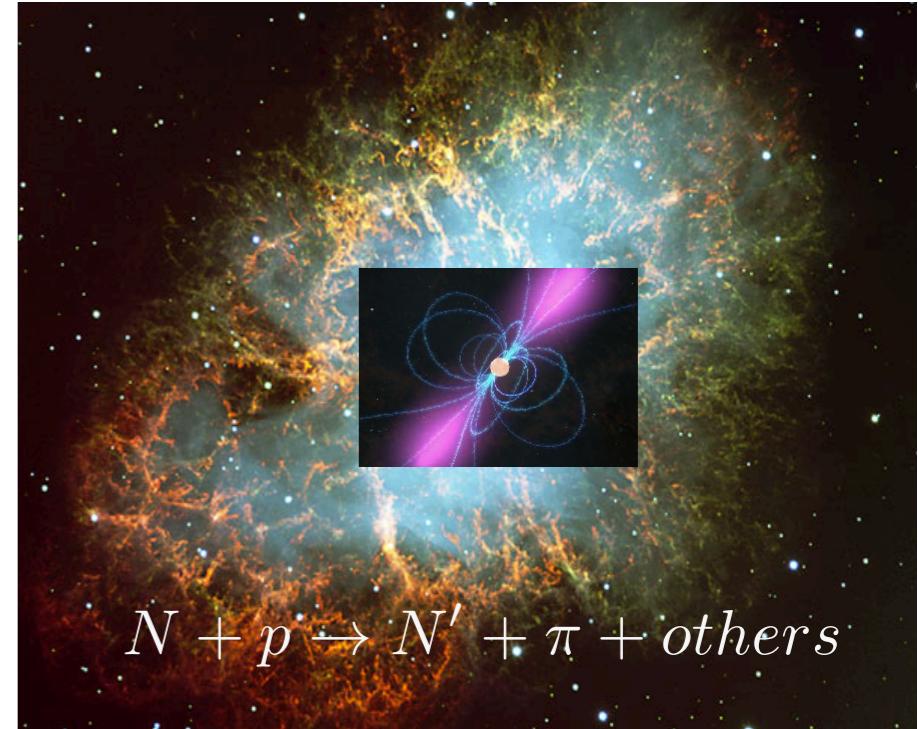
$$\tau_{pp} = 0.2 \left(\frac{M_{\text{ej}}}{10M_{\odot}} \right) \left(\frac{v_{\text{ej}}}{10^4 \text{km/s}} \right)^{-2} \left(\frac{t}{1\text{yr}} \right)^{-2}$$



Interaction with Ejecta

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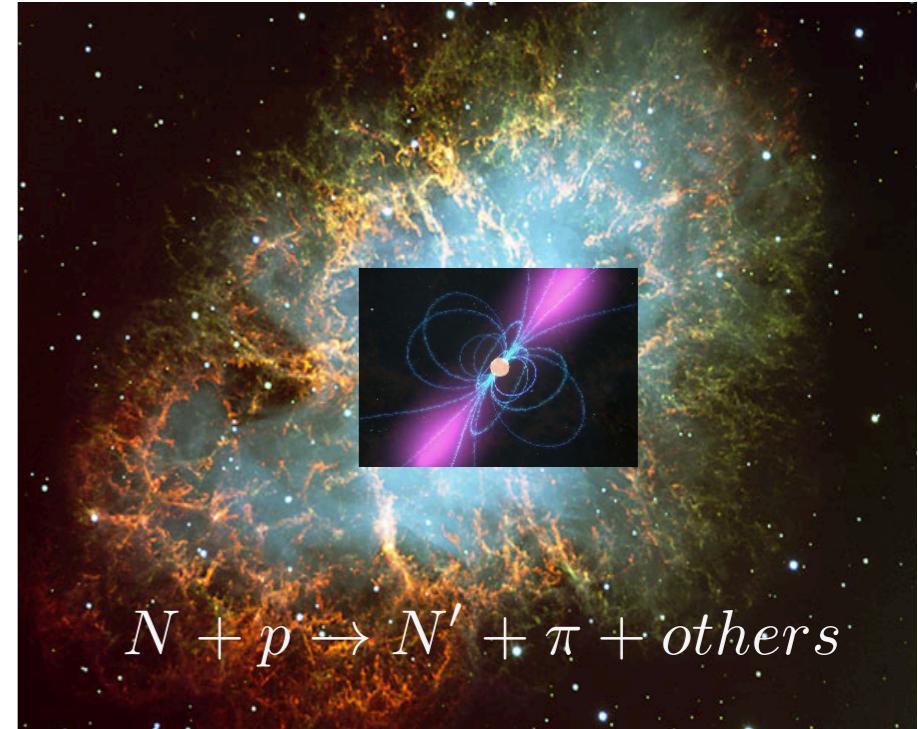
$t \uparrow$



Interaction with Ejecta

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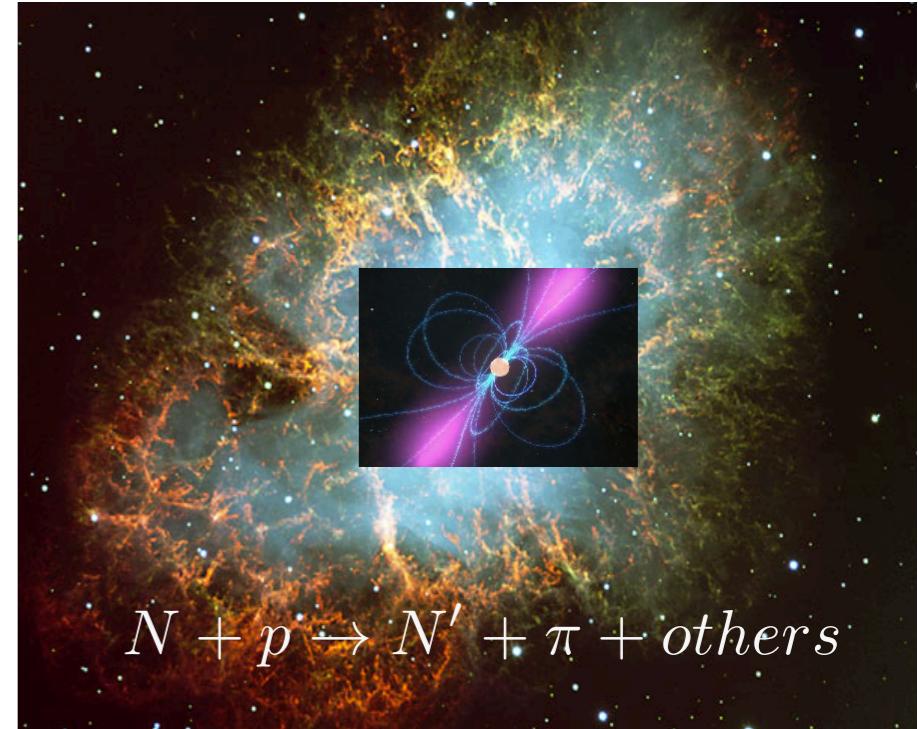
$t \uparrow E_{\text{CR}} \downarrow$



Interaction with Ejecta

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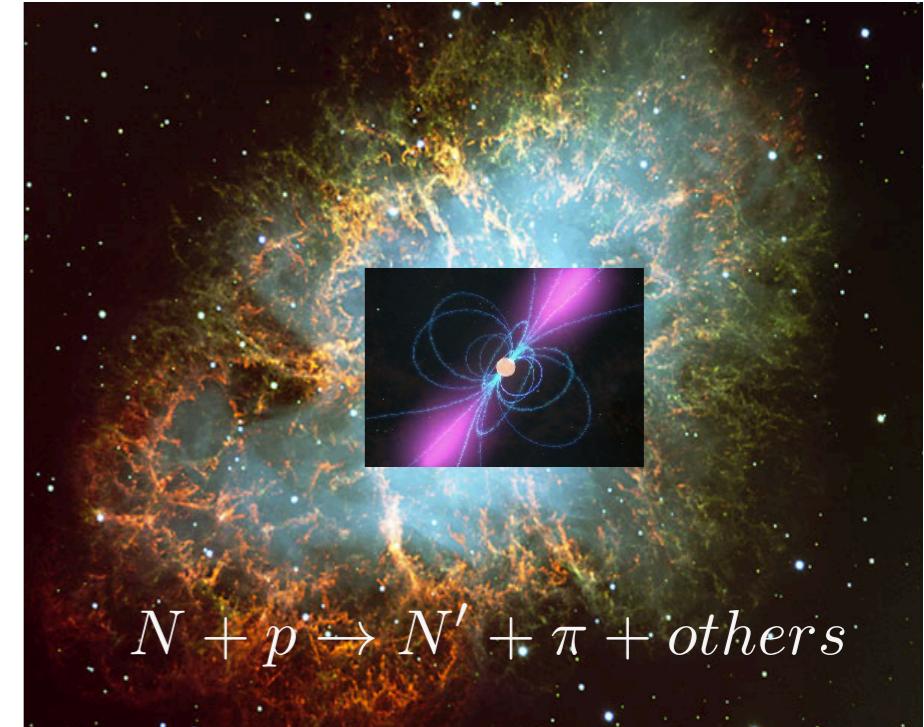


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Monte Carlo simulation tracking particle propagation

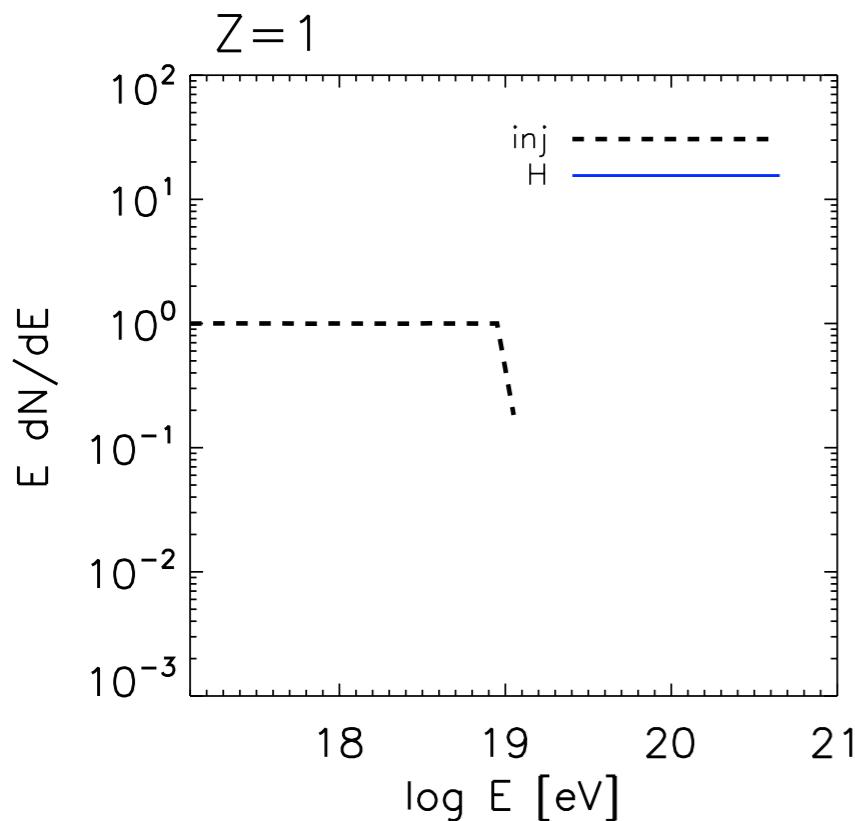
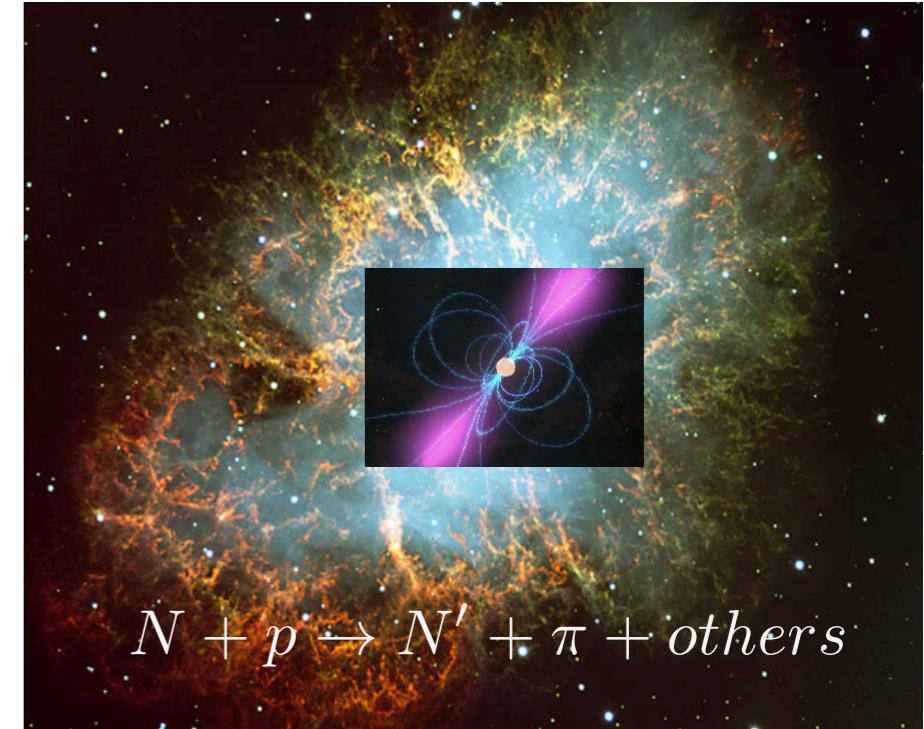


Interaction with Ejecta

$$\tau_{pp} = 0.2 \left(\frac{M_{\text{ej}}}{10M_{\odot}} \right) \left(\frac{v_{\text{ej}}}{10^4 \text{ km/s}} \right)^{-2} \left(\frac{t}{1 \text{ yr}} \right)^{-2}$$

$t \uparrow$ $E_{\text{CR}} \downarrow$ $\tau \downarrow$

Monte Carlo simulation tracking particle propagation



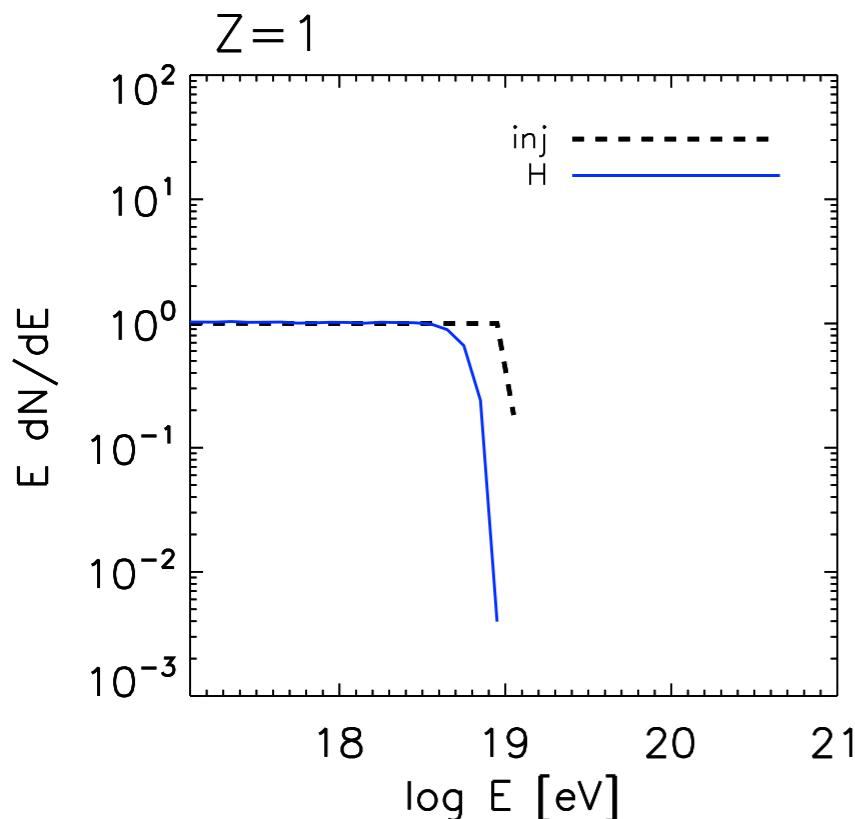
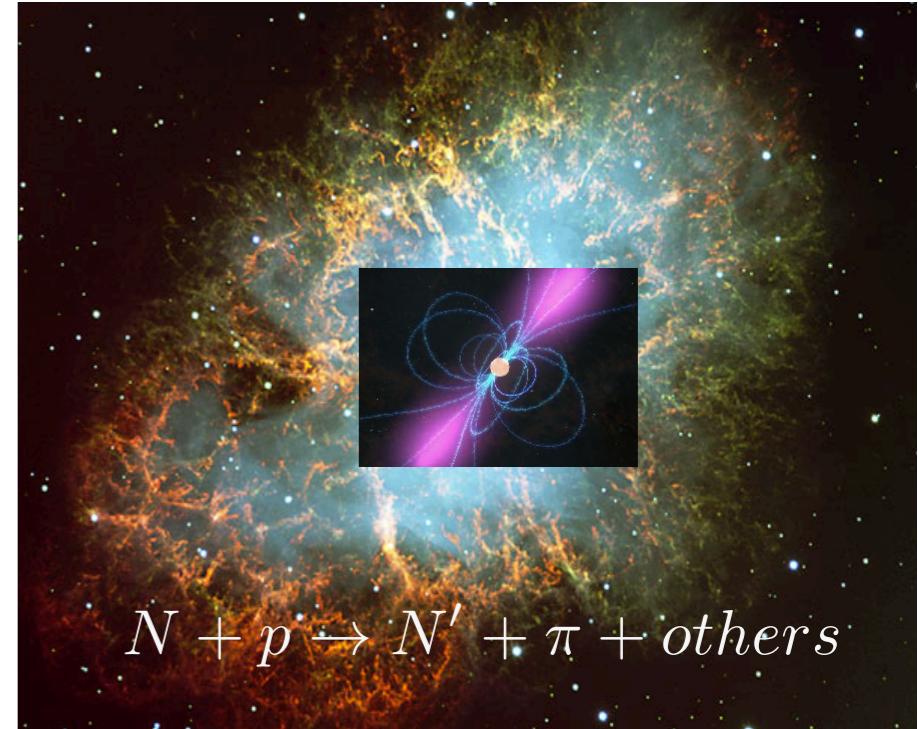
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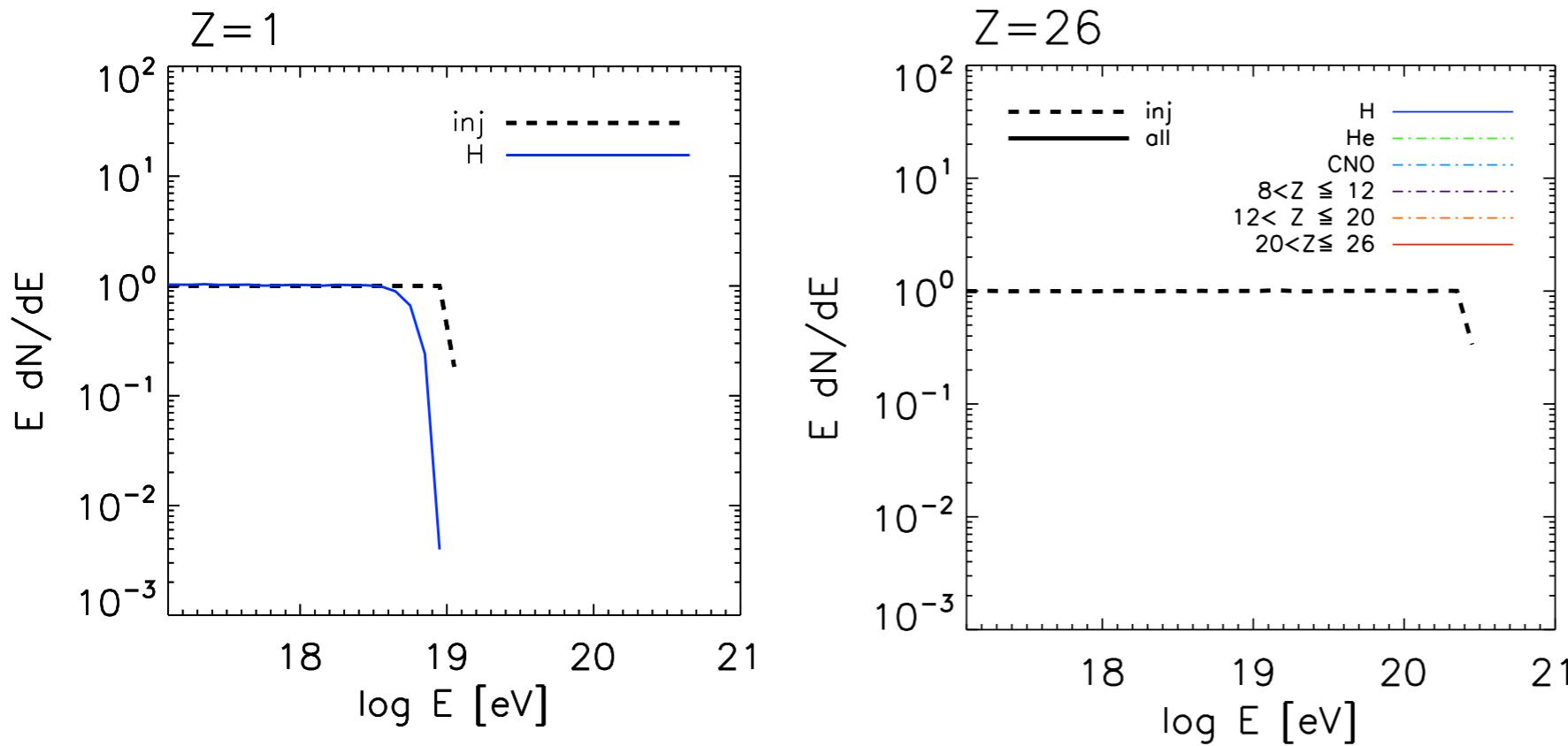
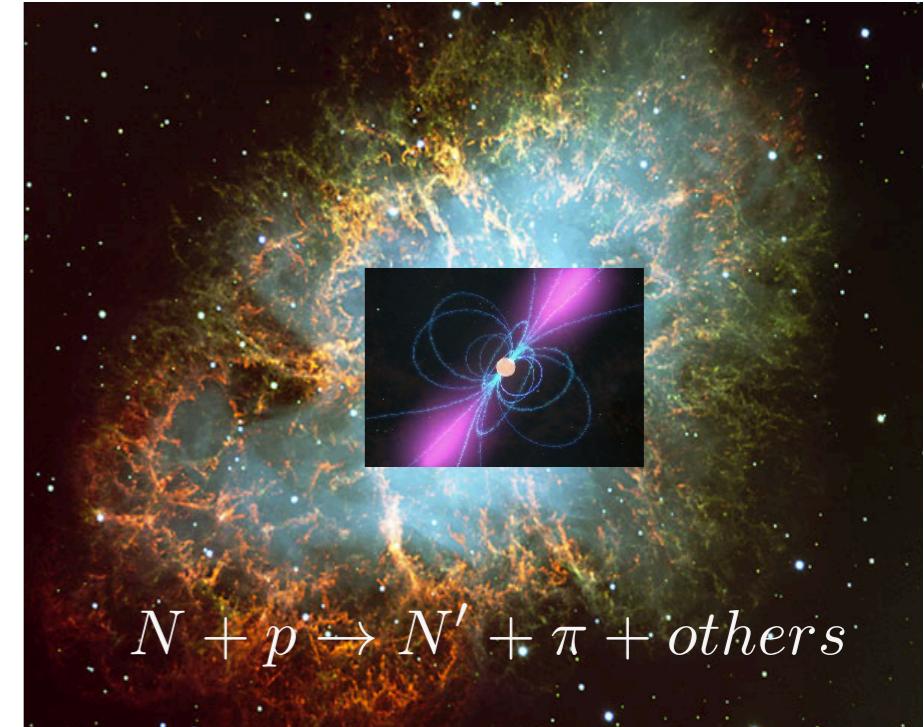
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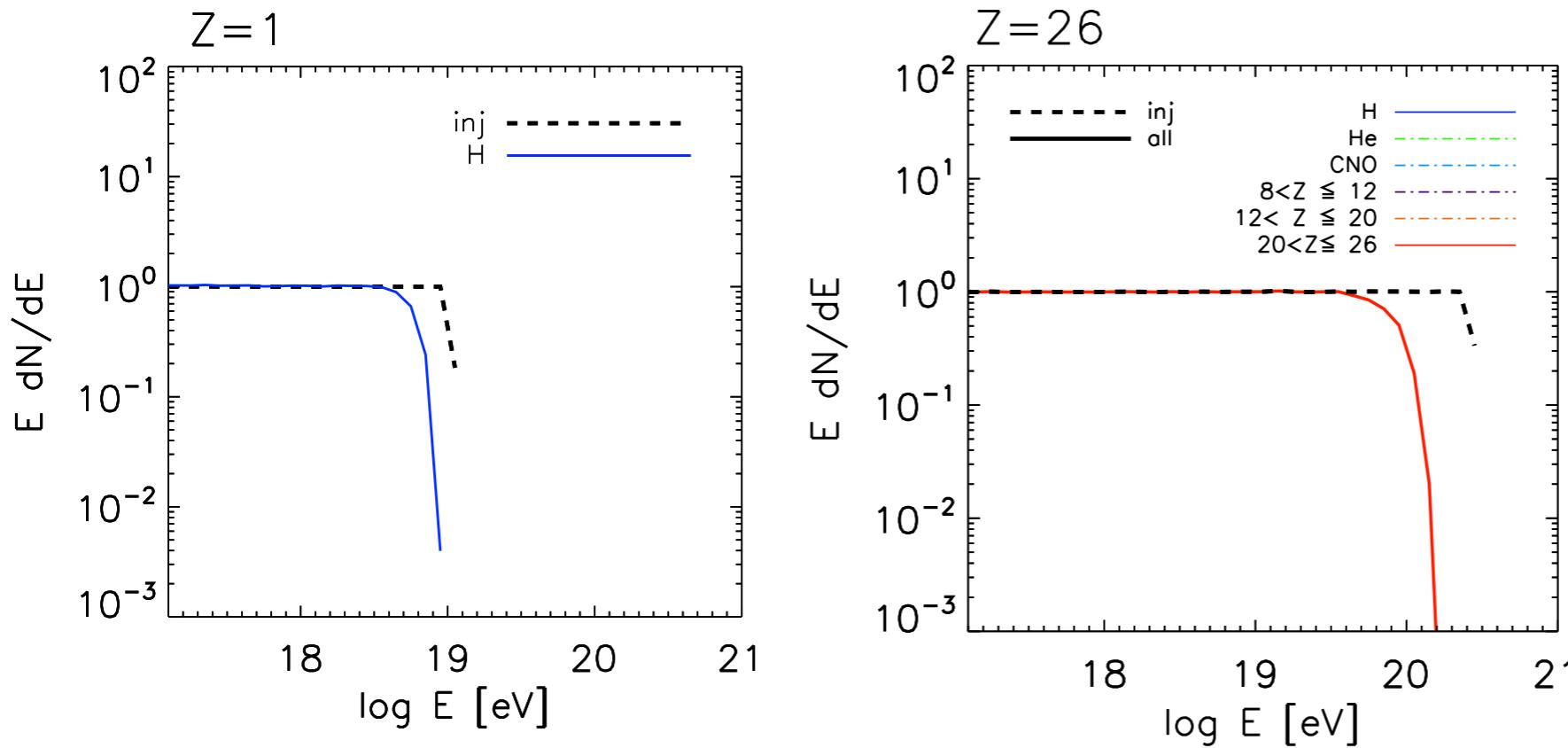
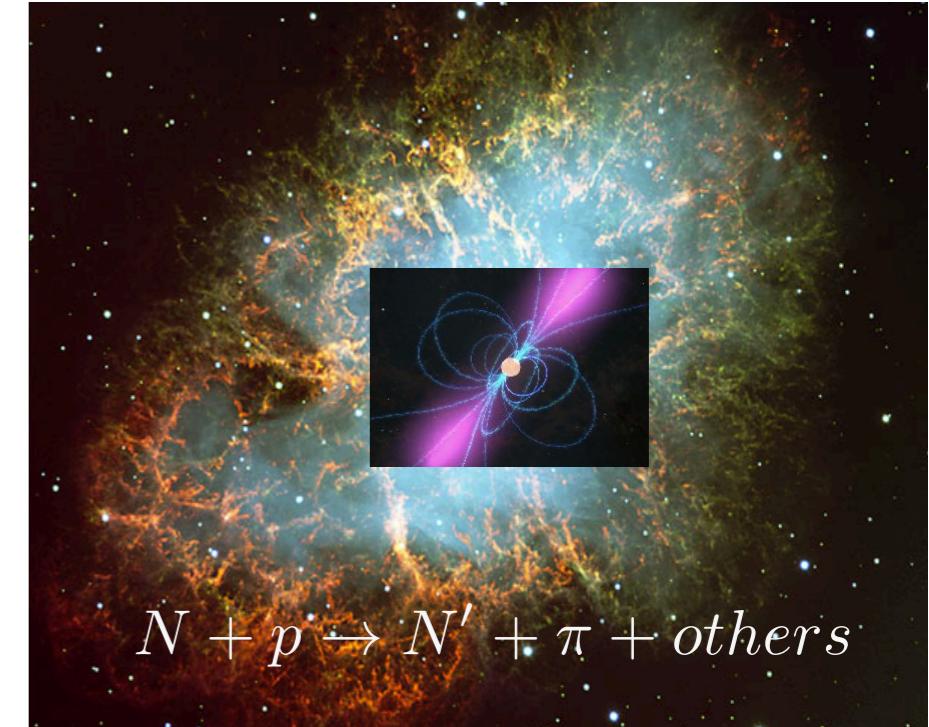
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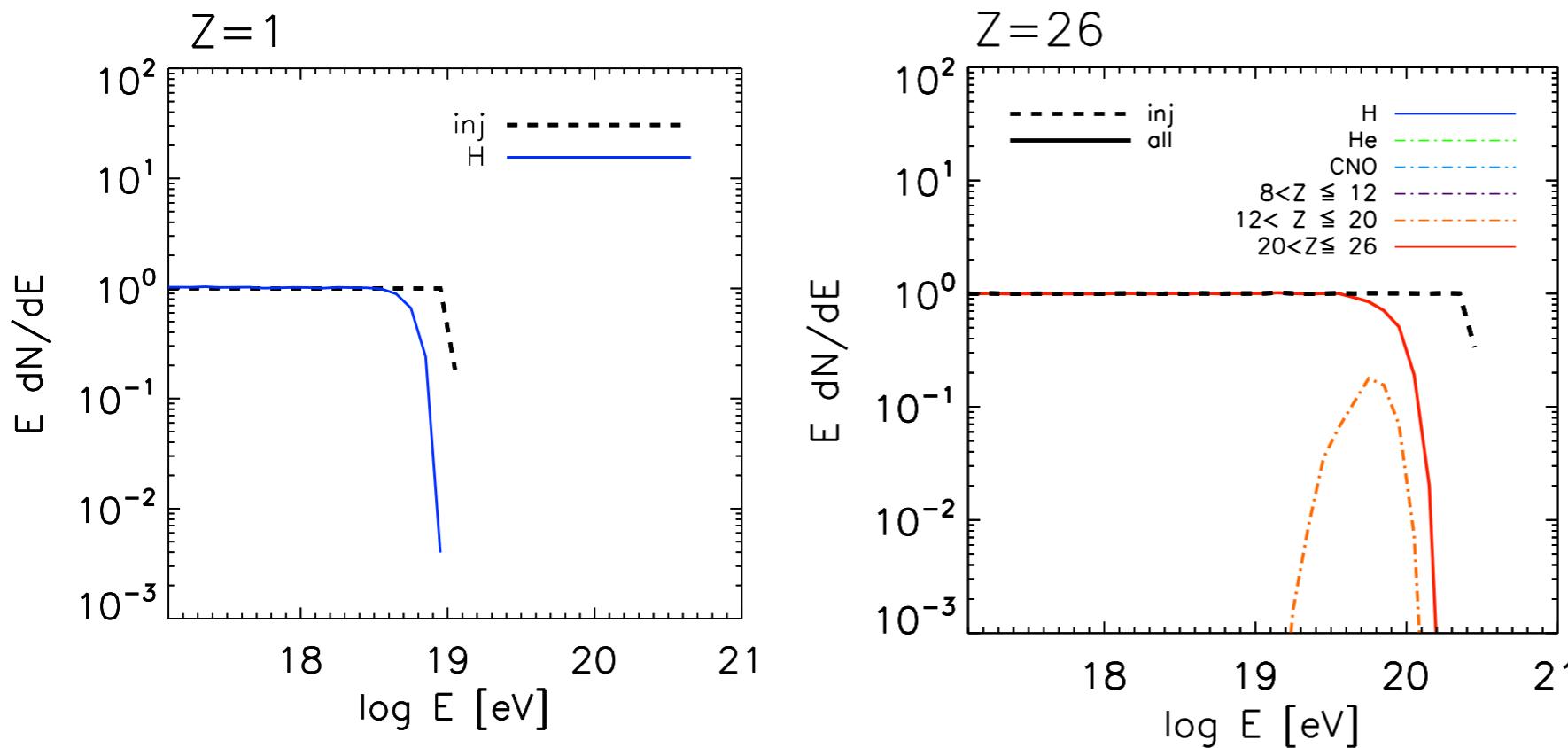
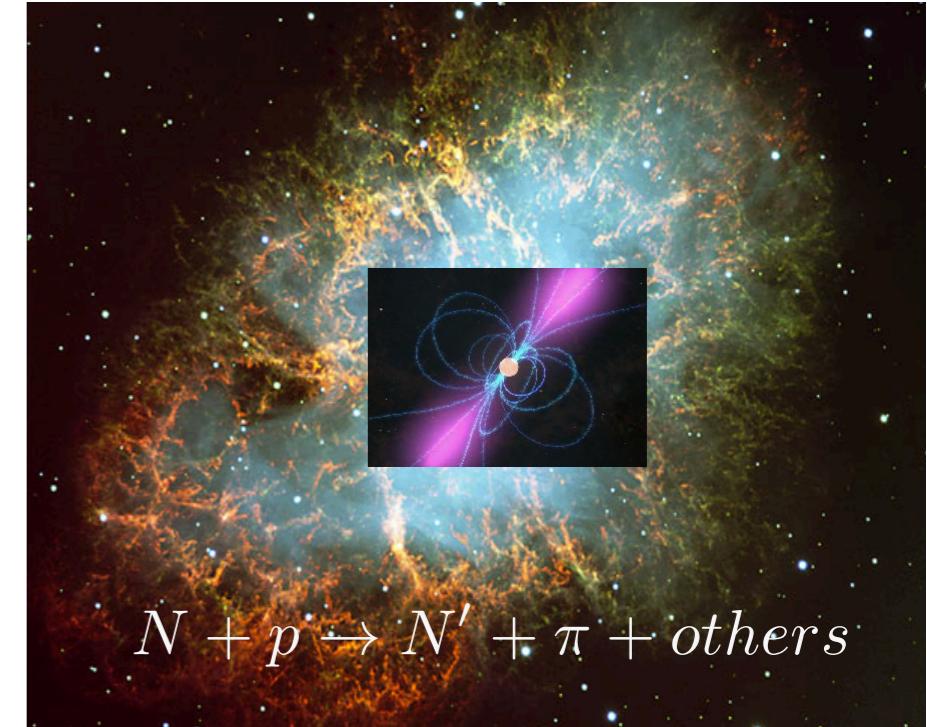
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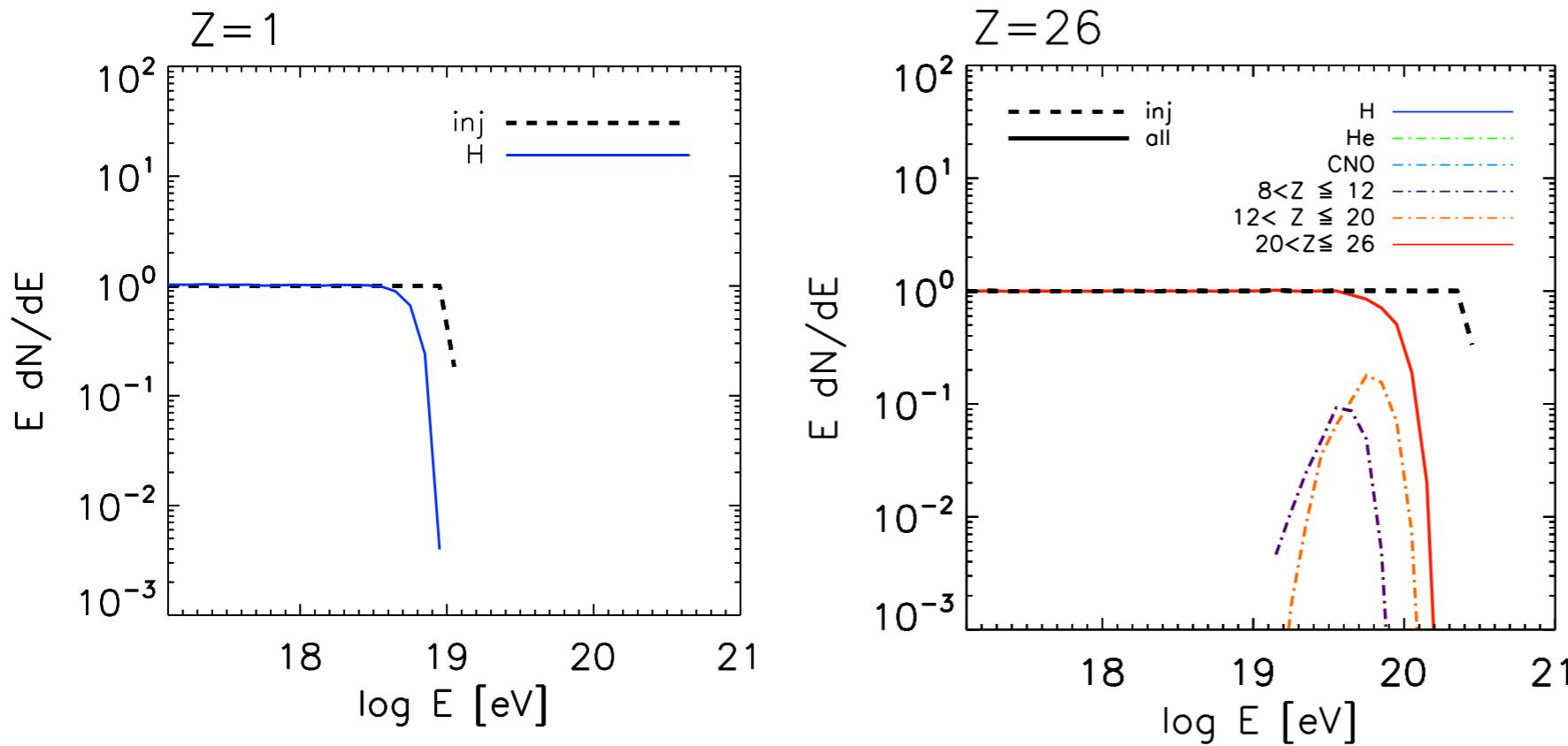
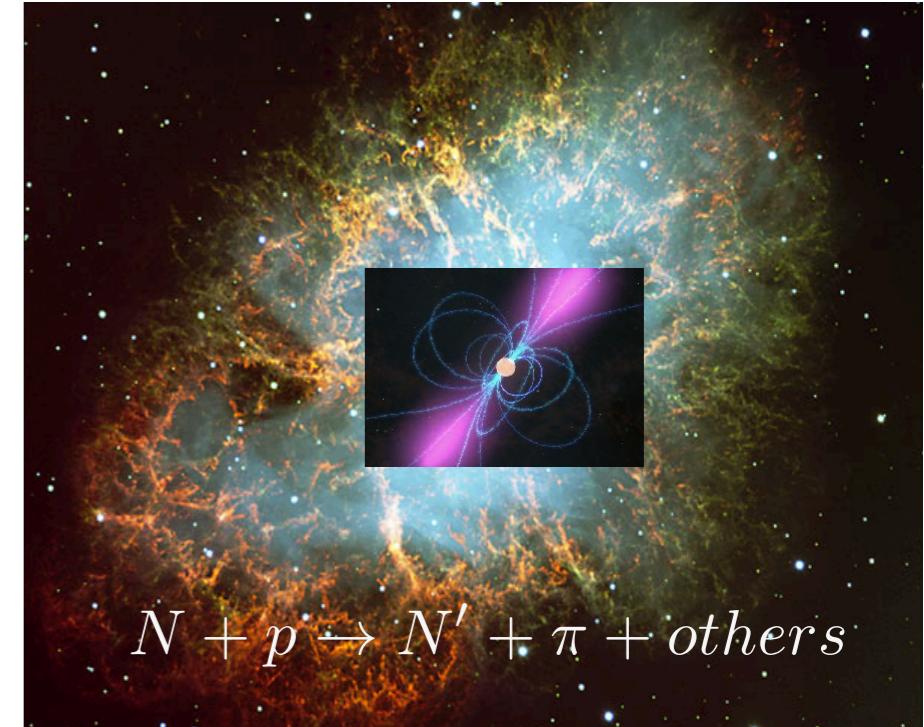
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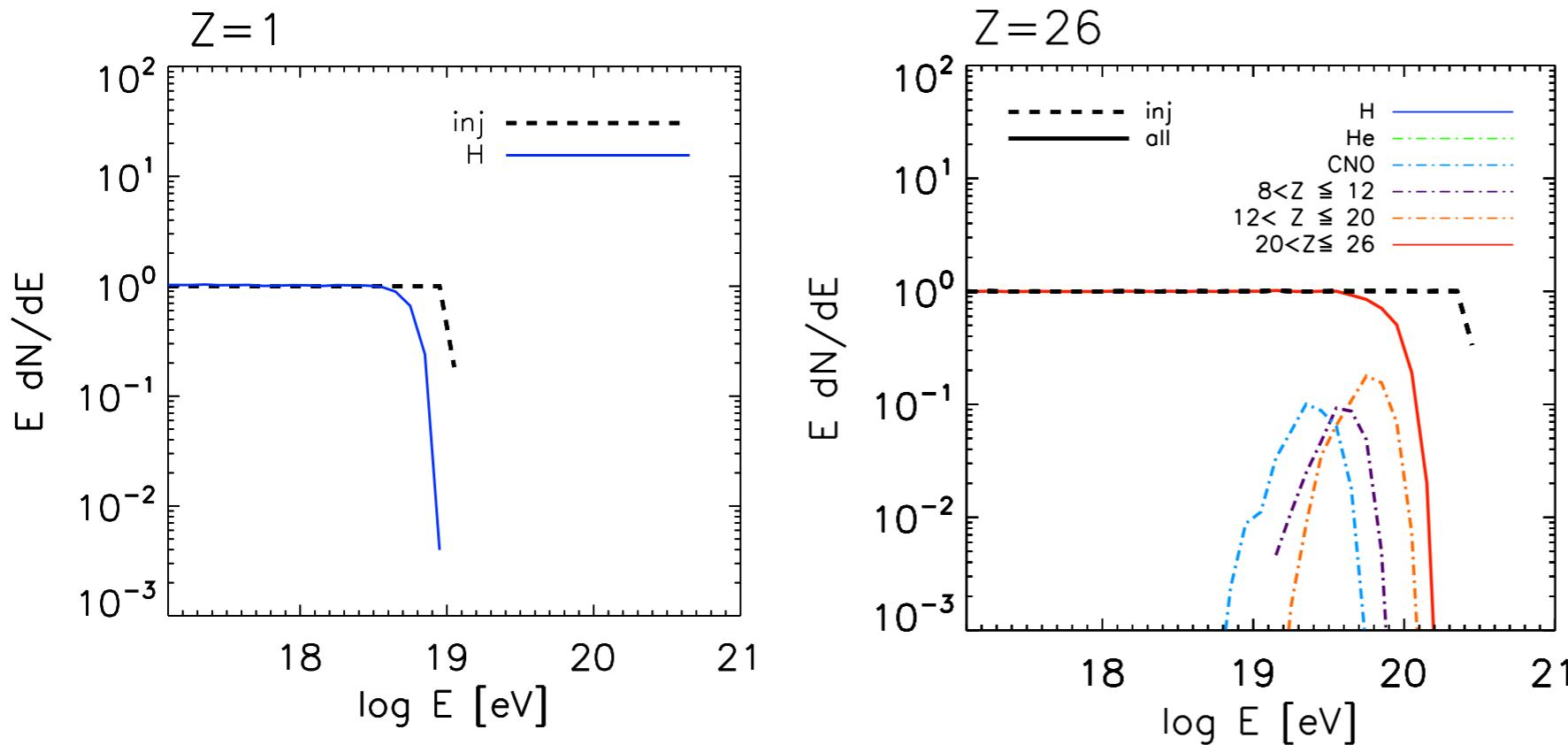
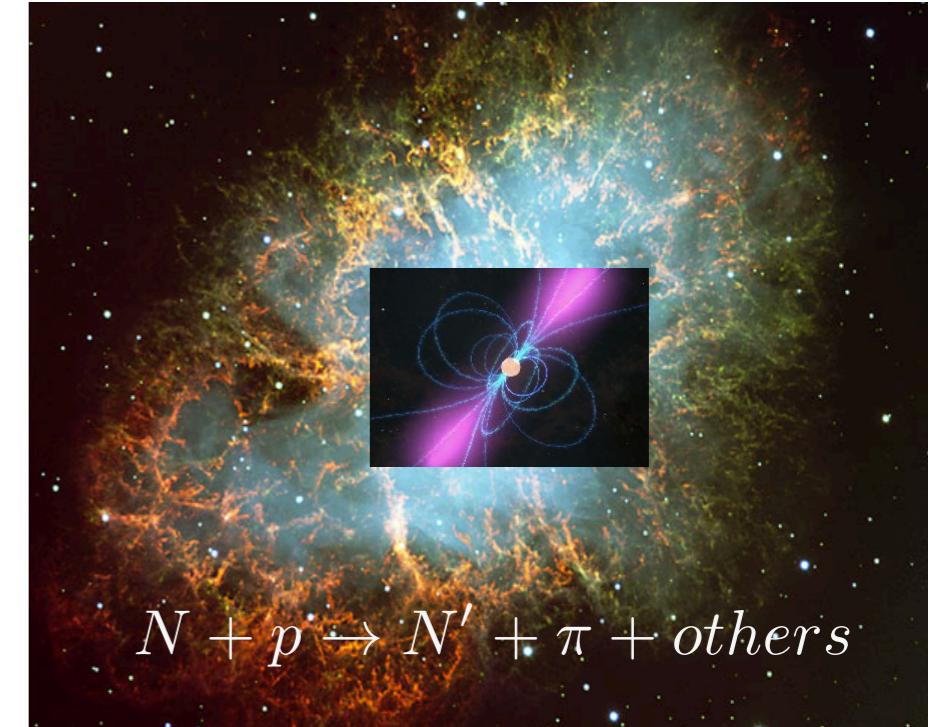
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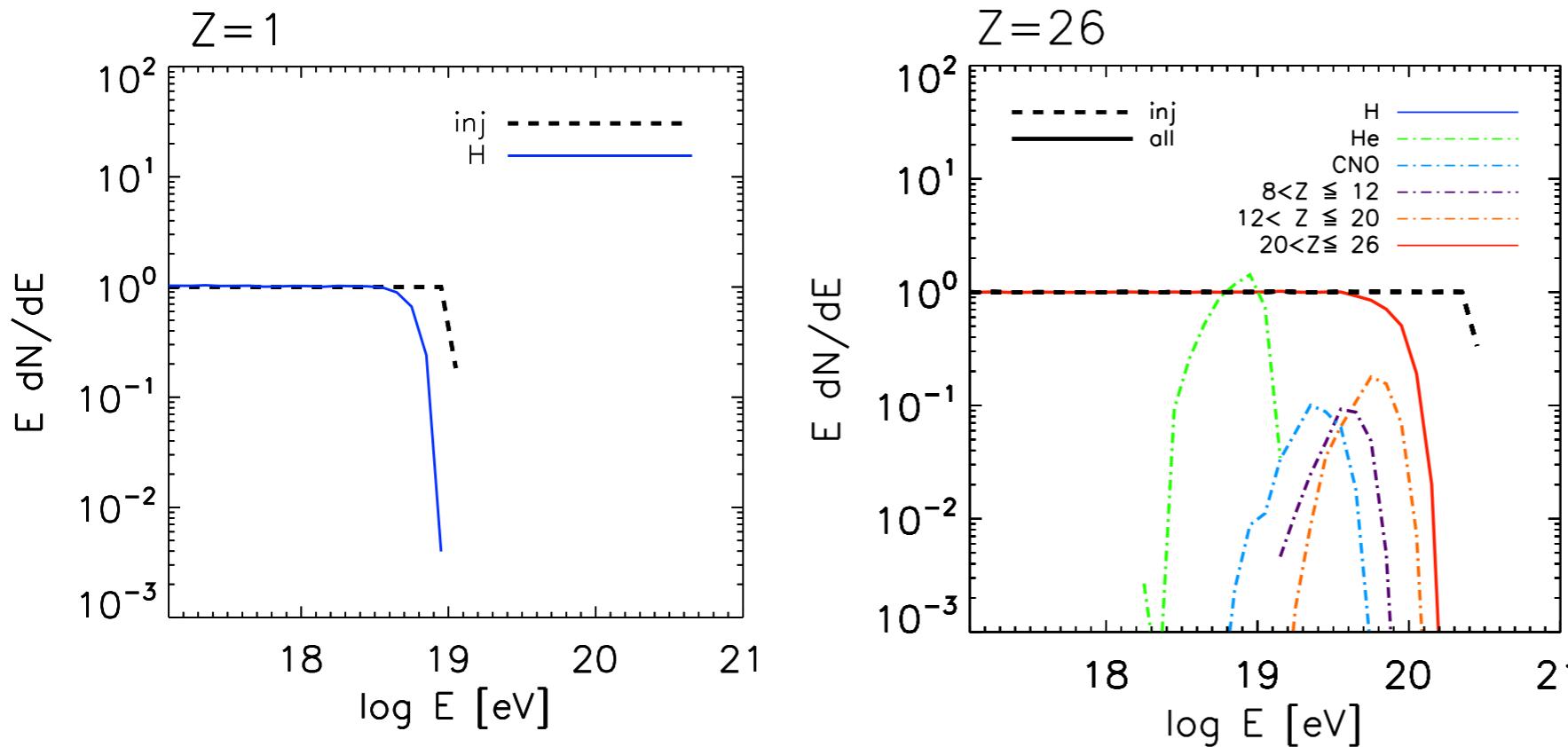
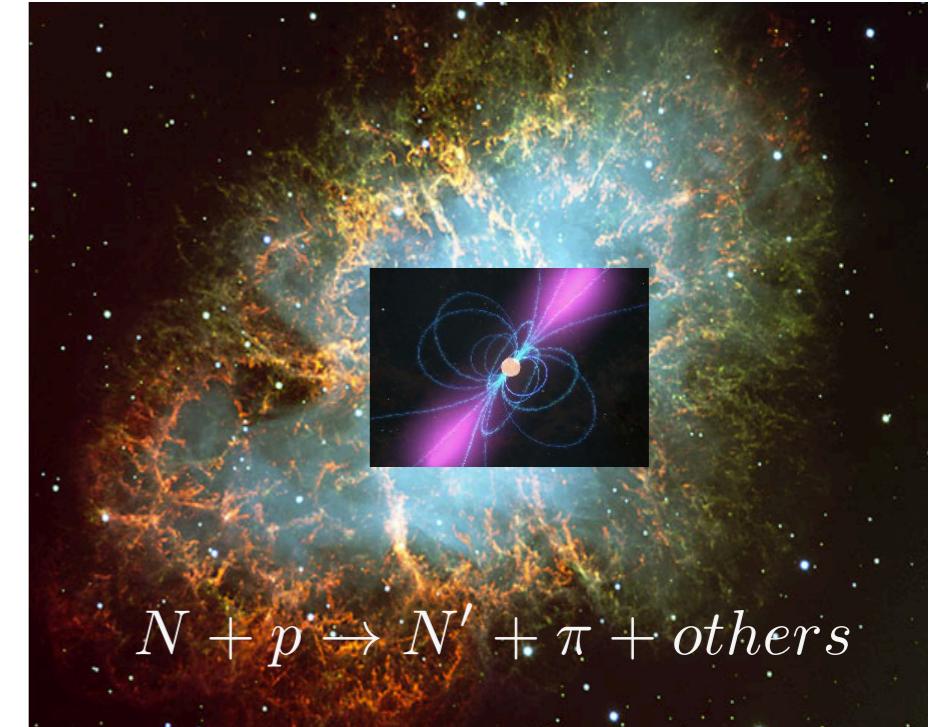
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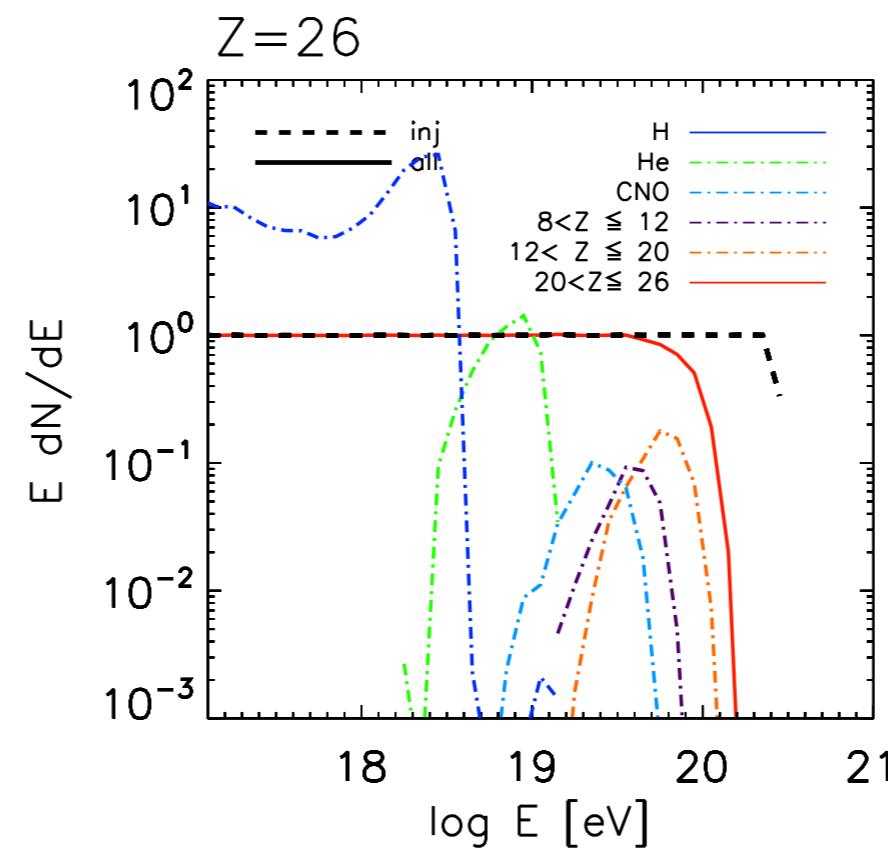
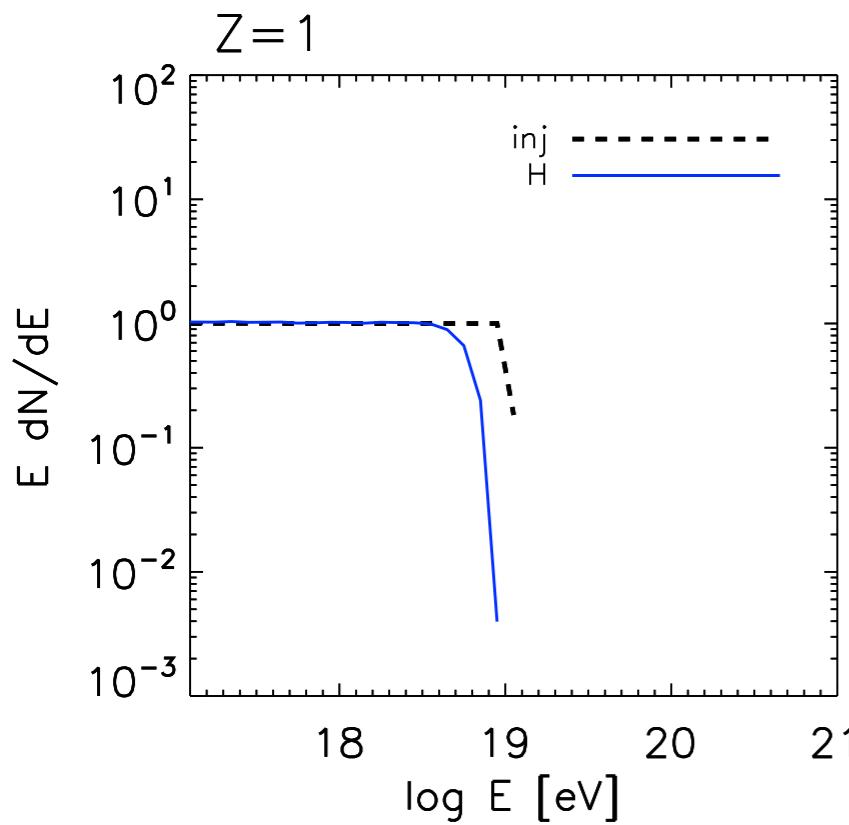
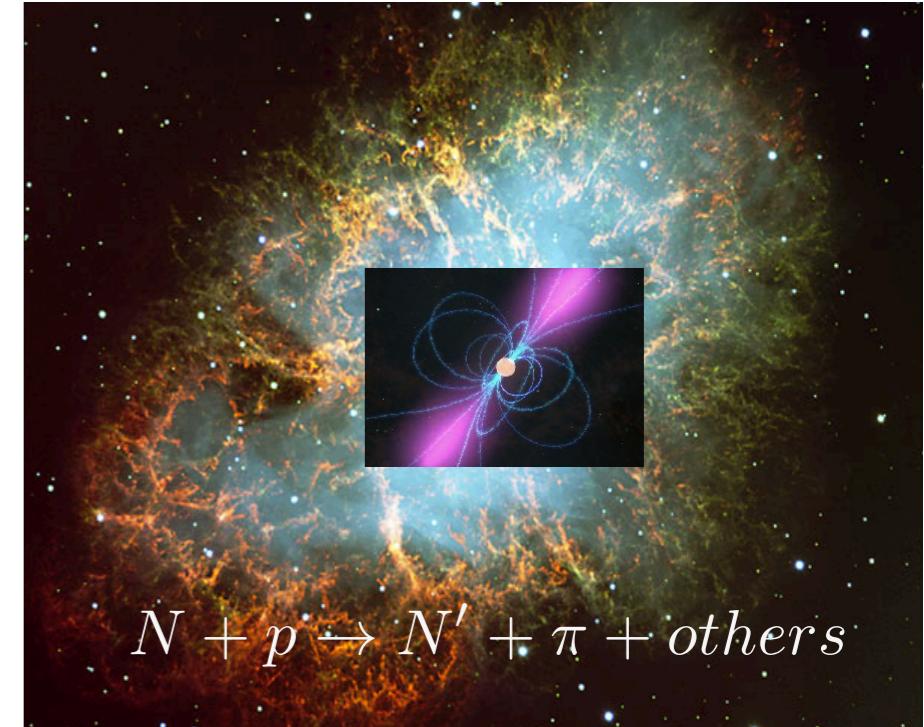
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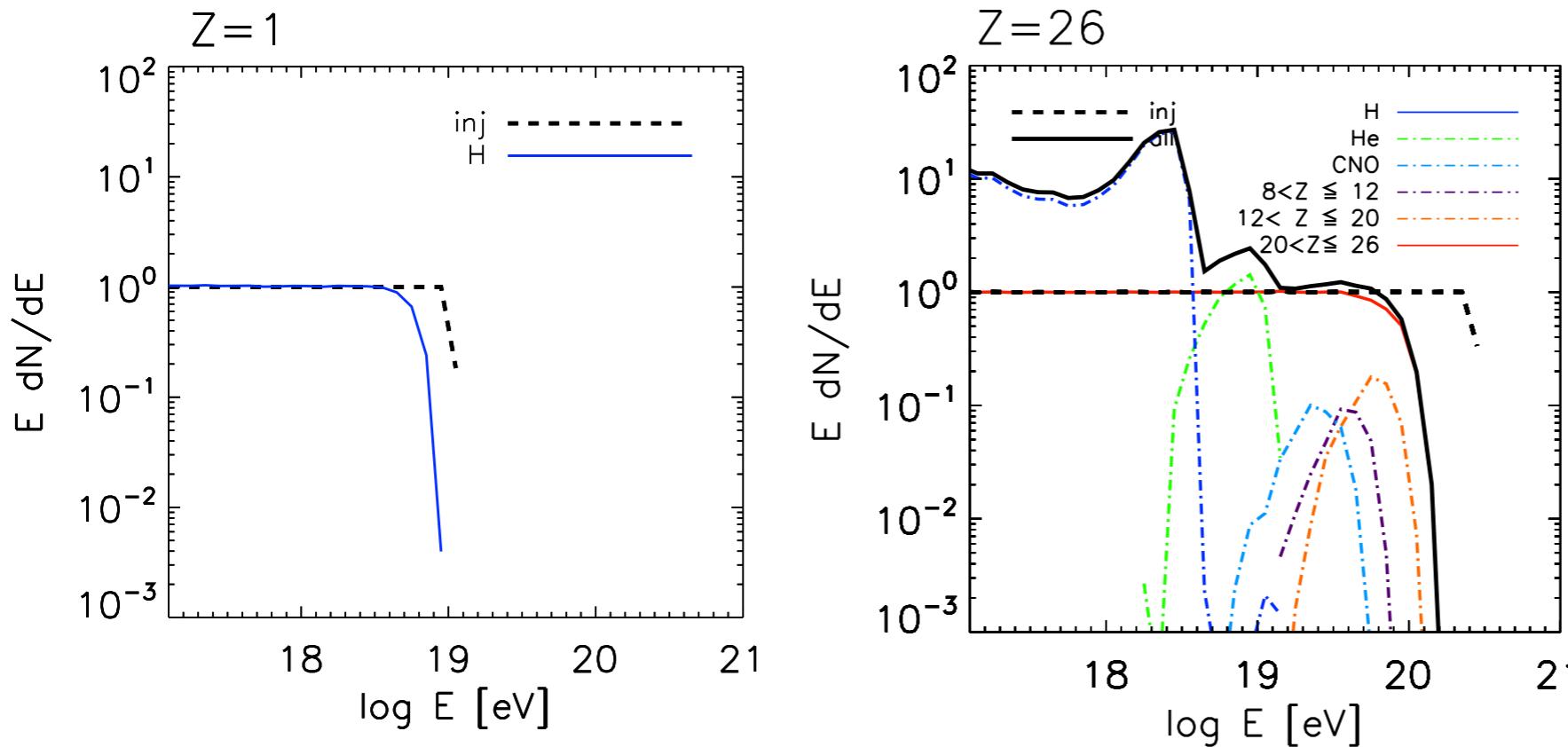
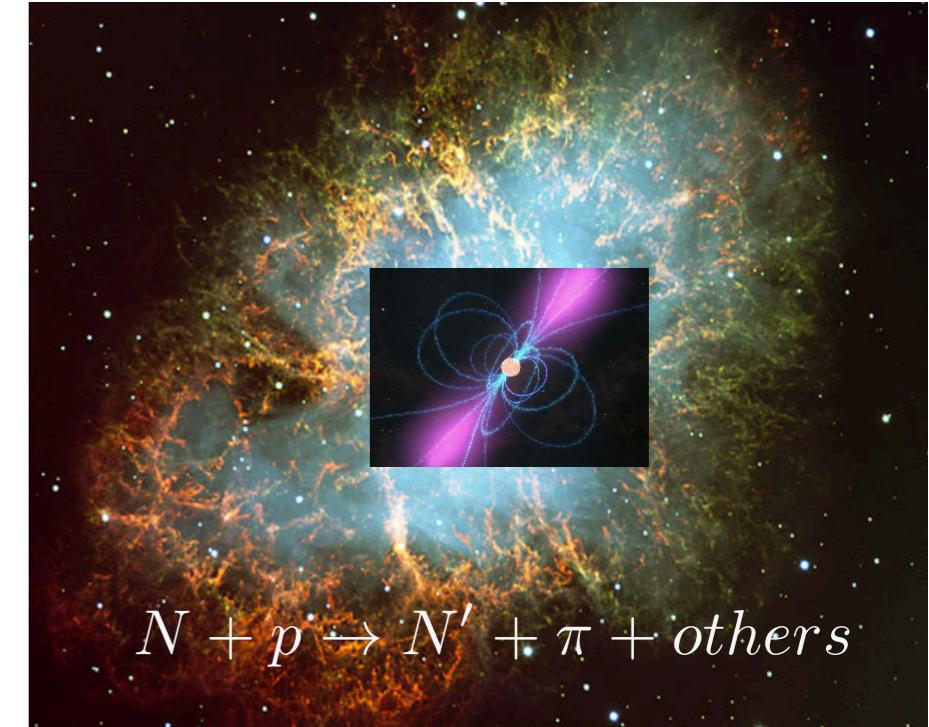
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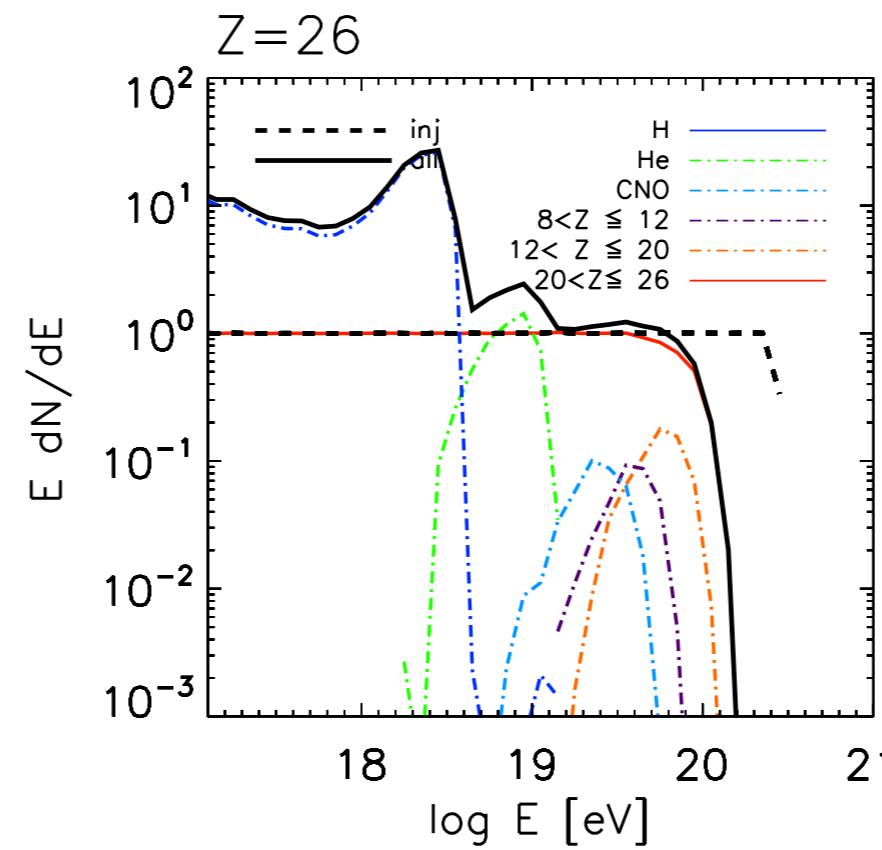
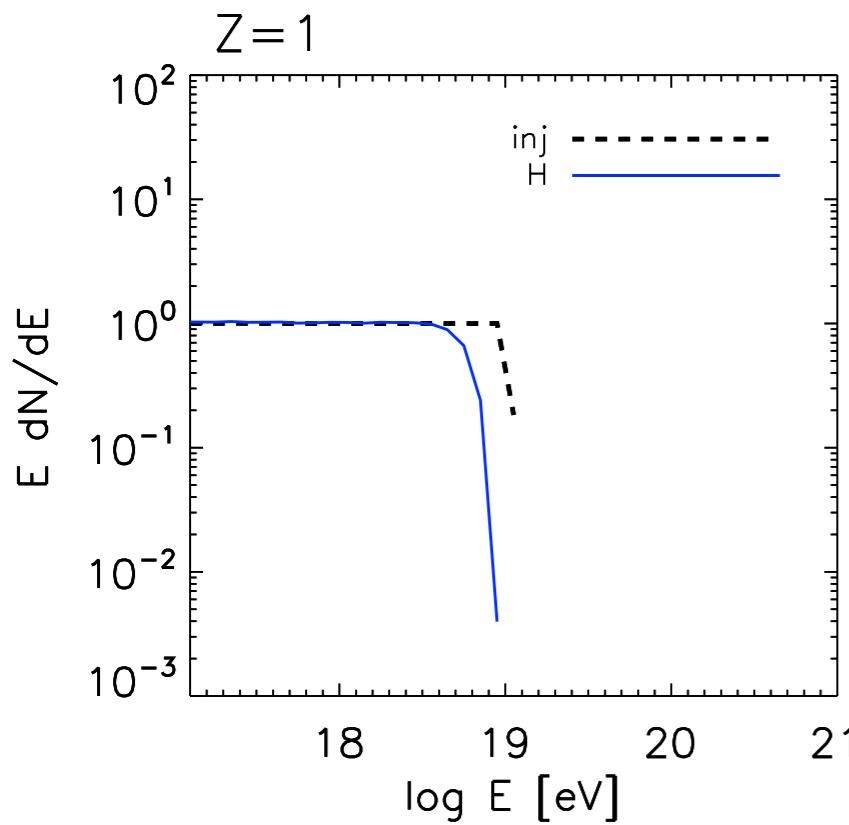
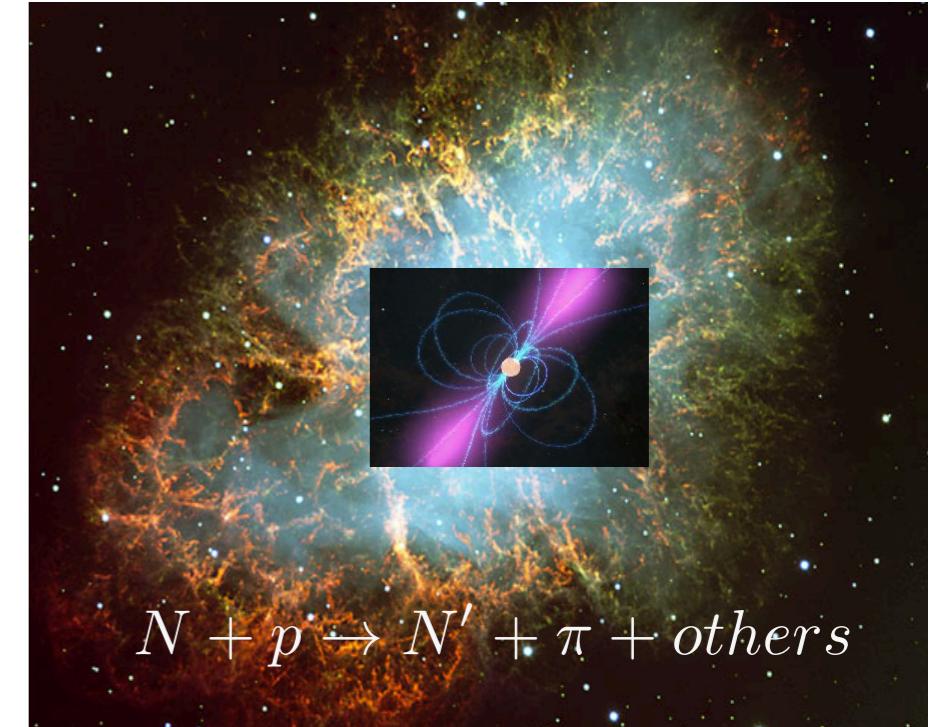
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Interaction with Ejecta

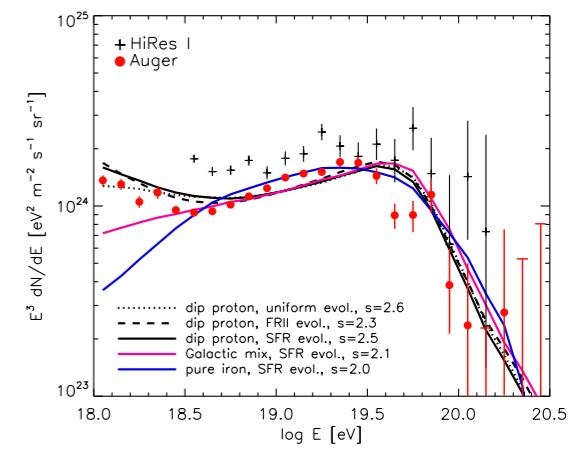
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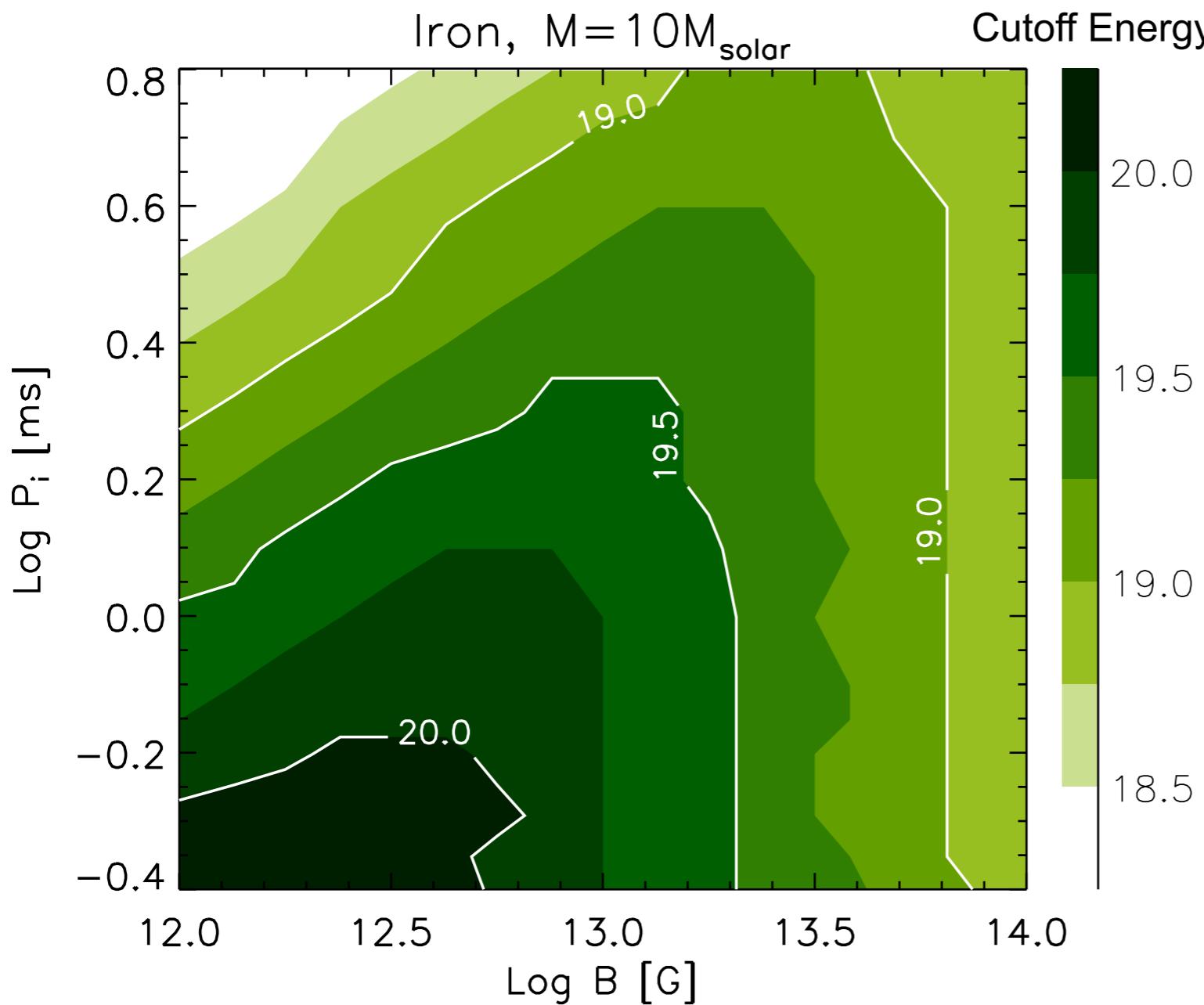
Monte Carlo simulation tracking particle propagation



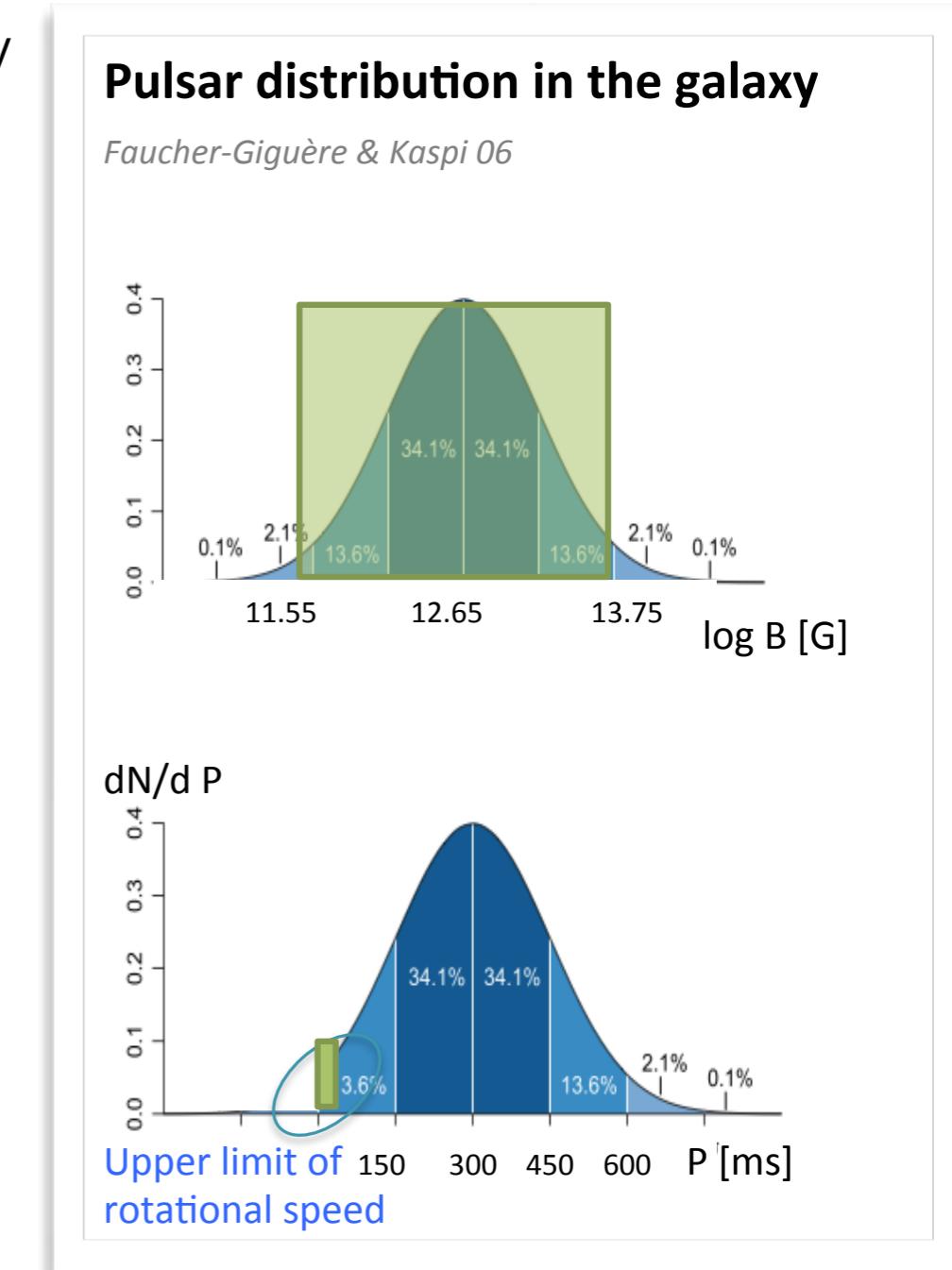
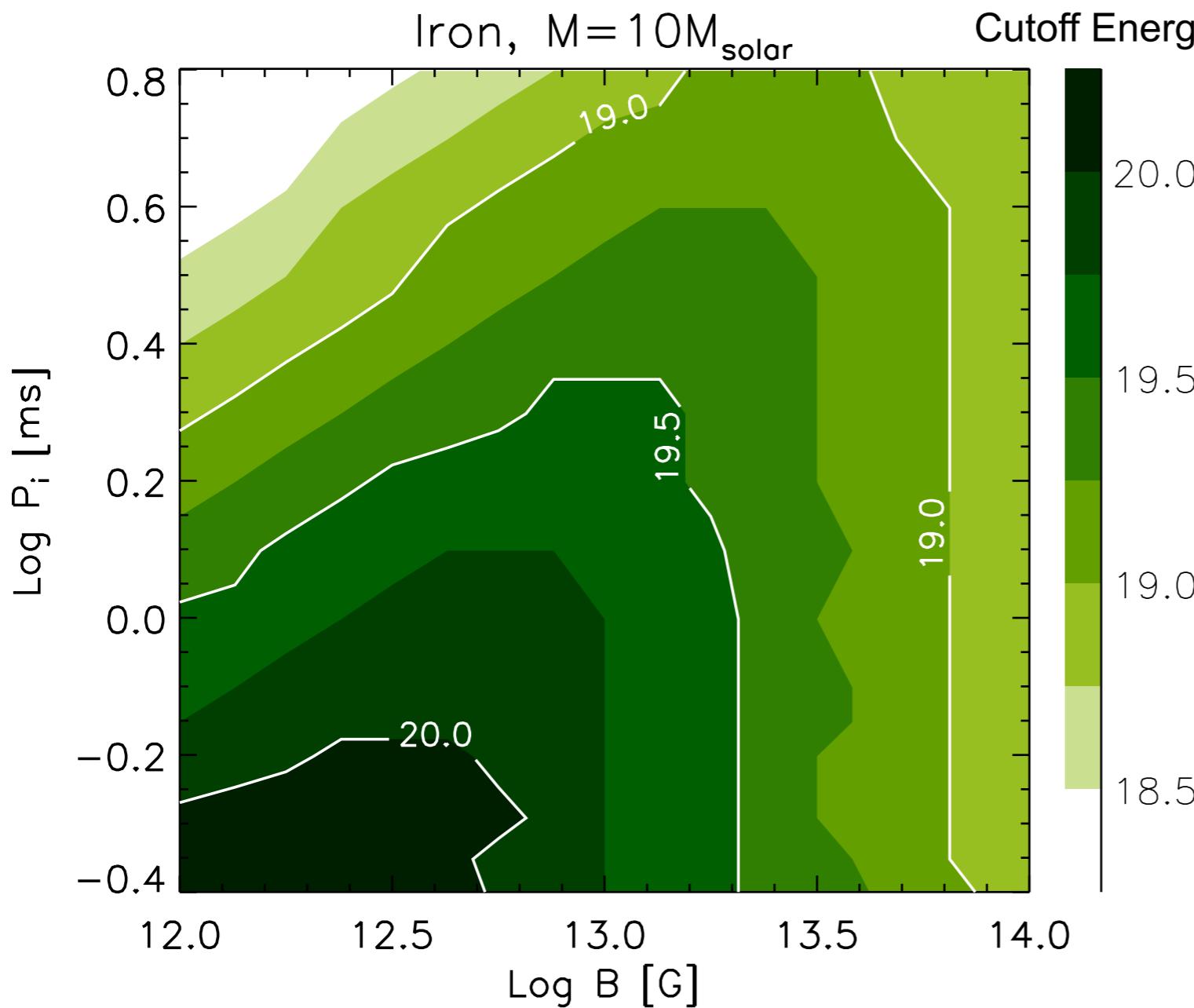
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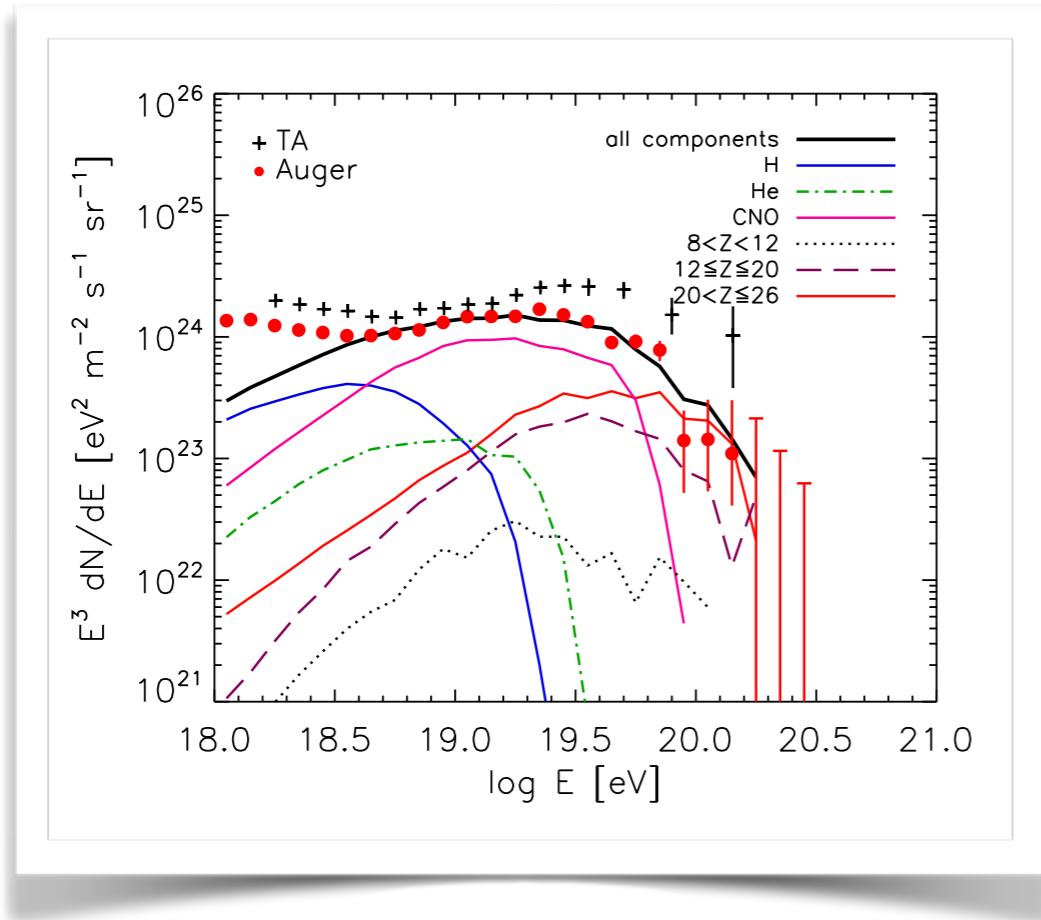
UHE-allowed Pulsars



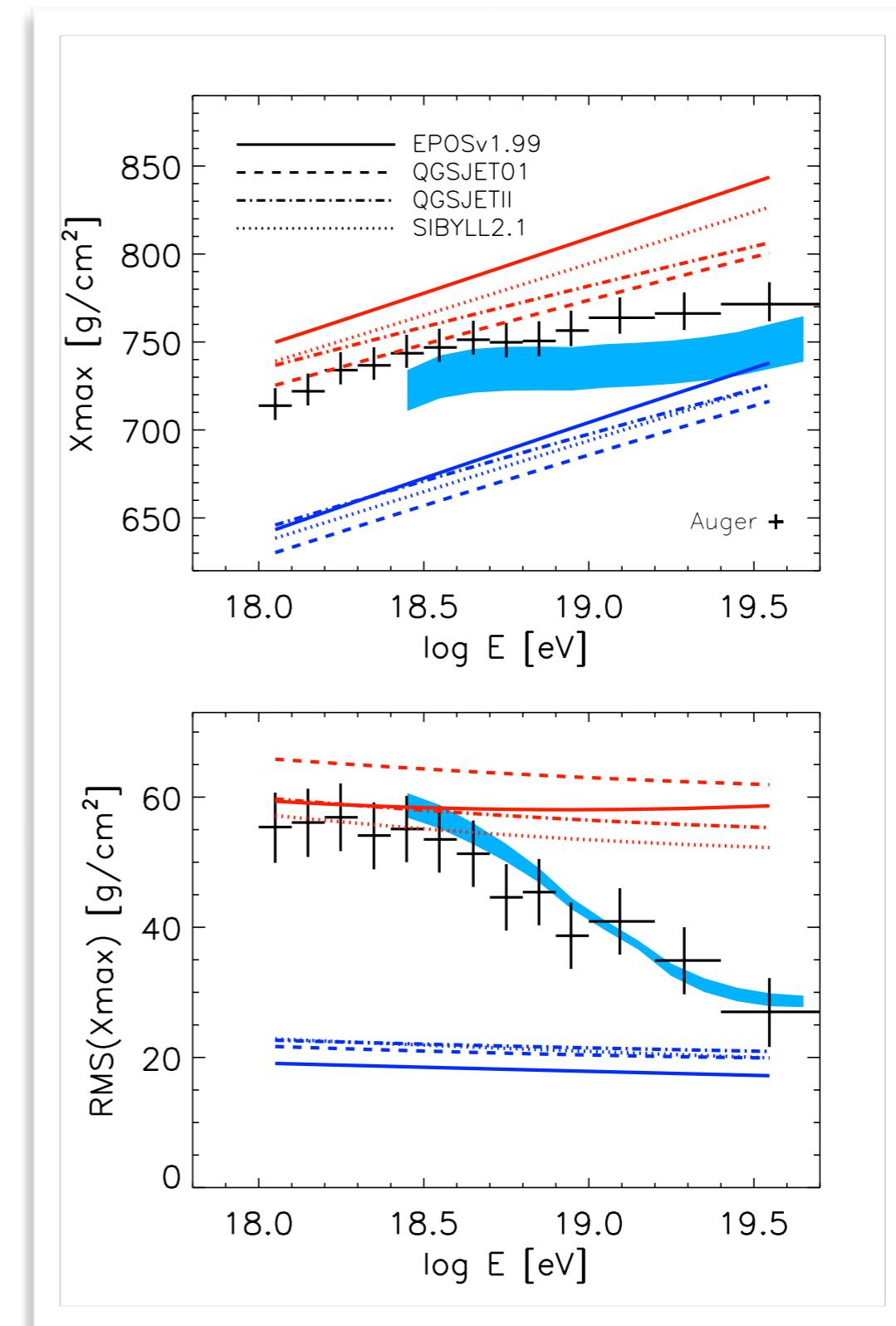
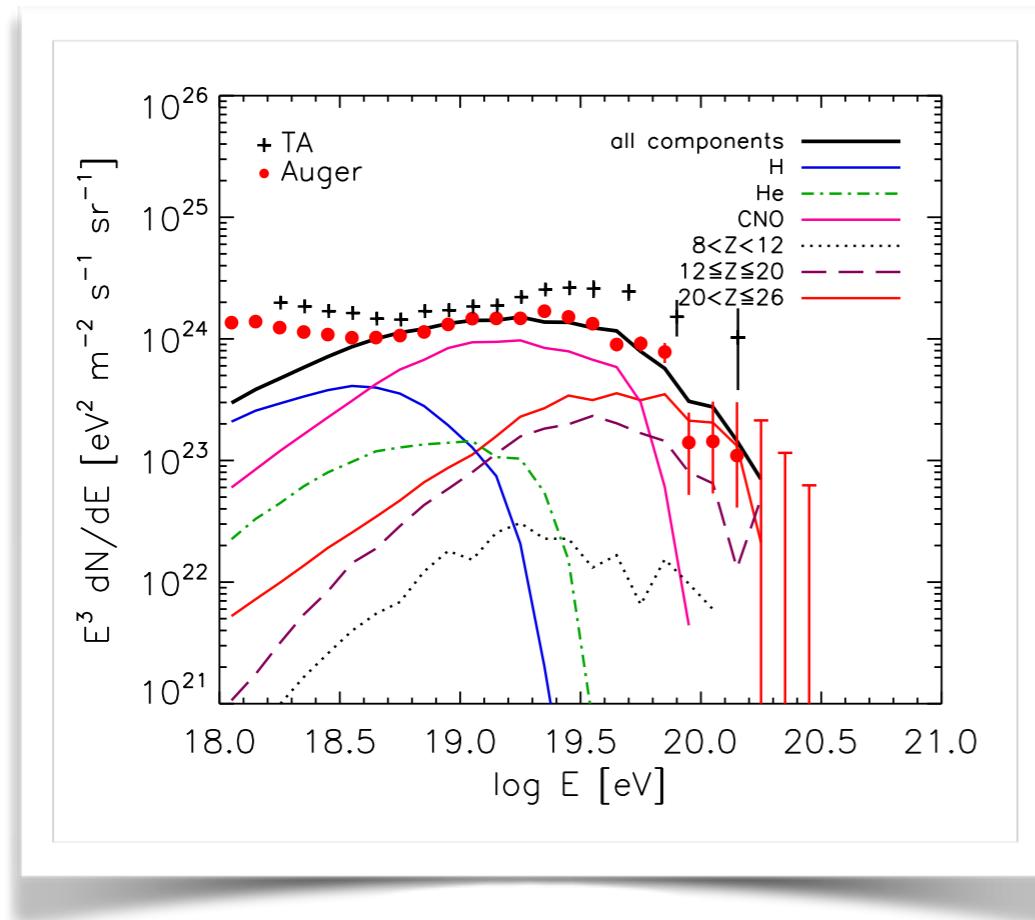
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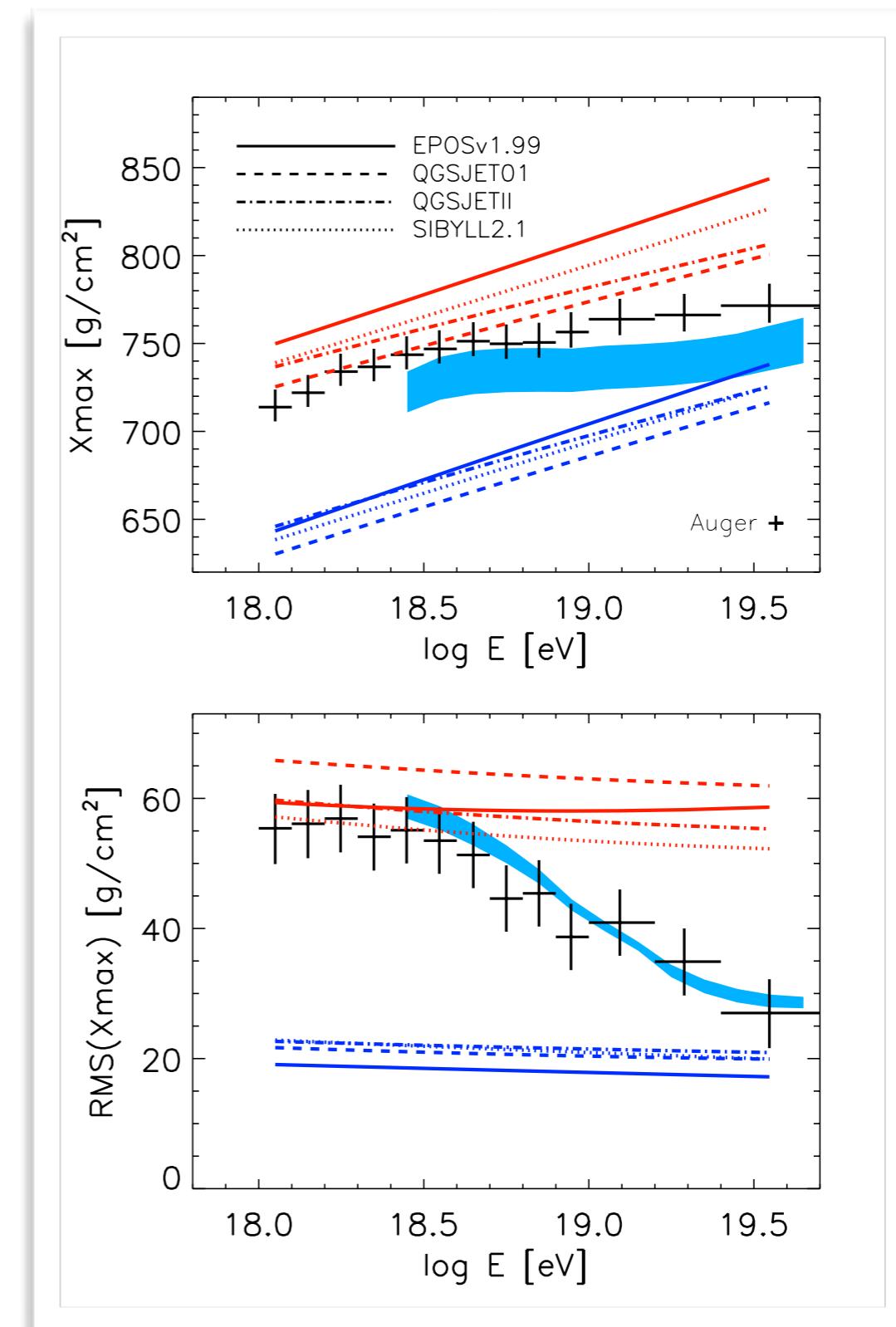
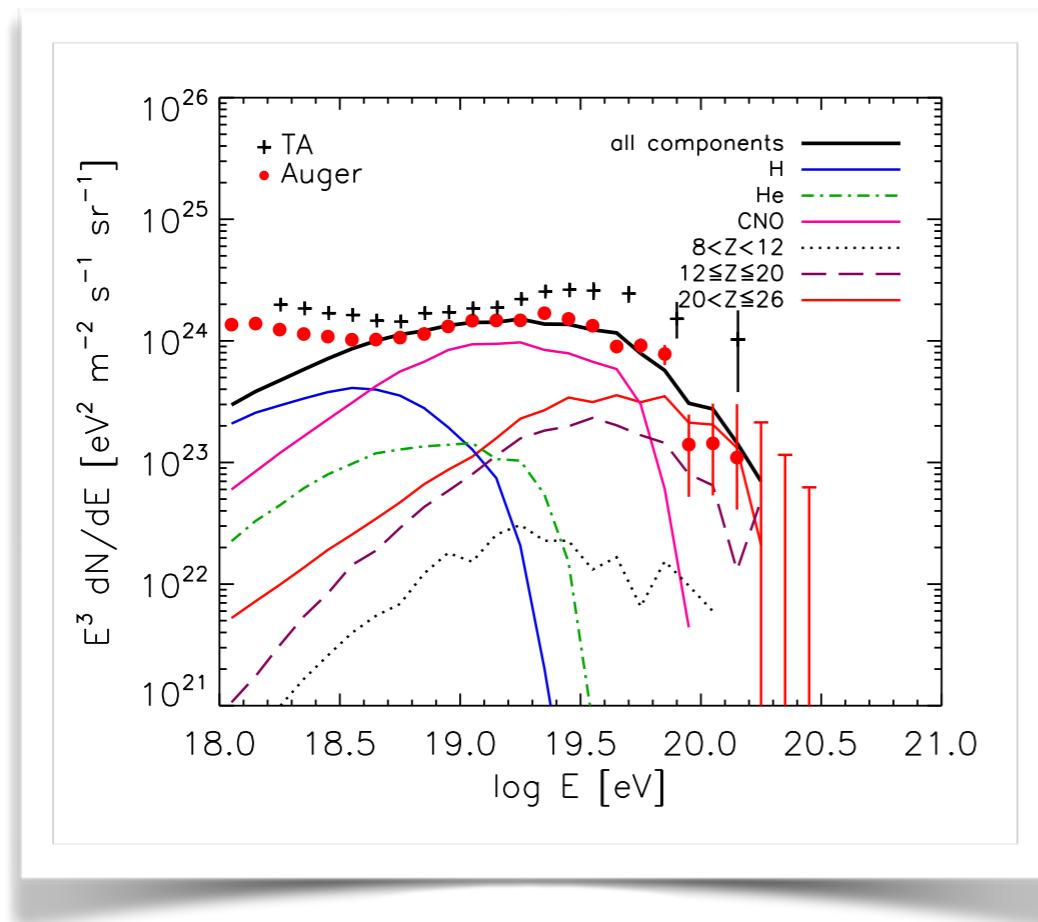
Integrated Extragalactic Pulsars



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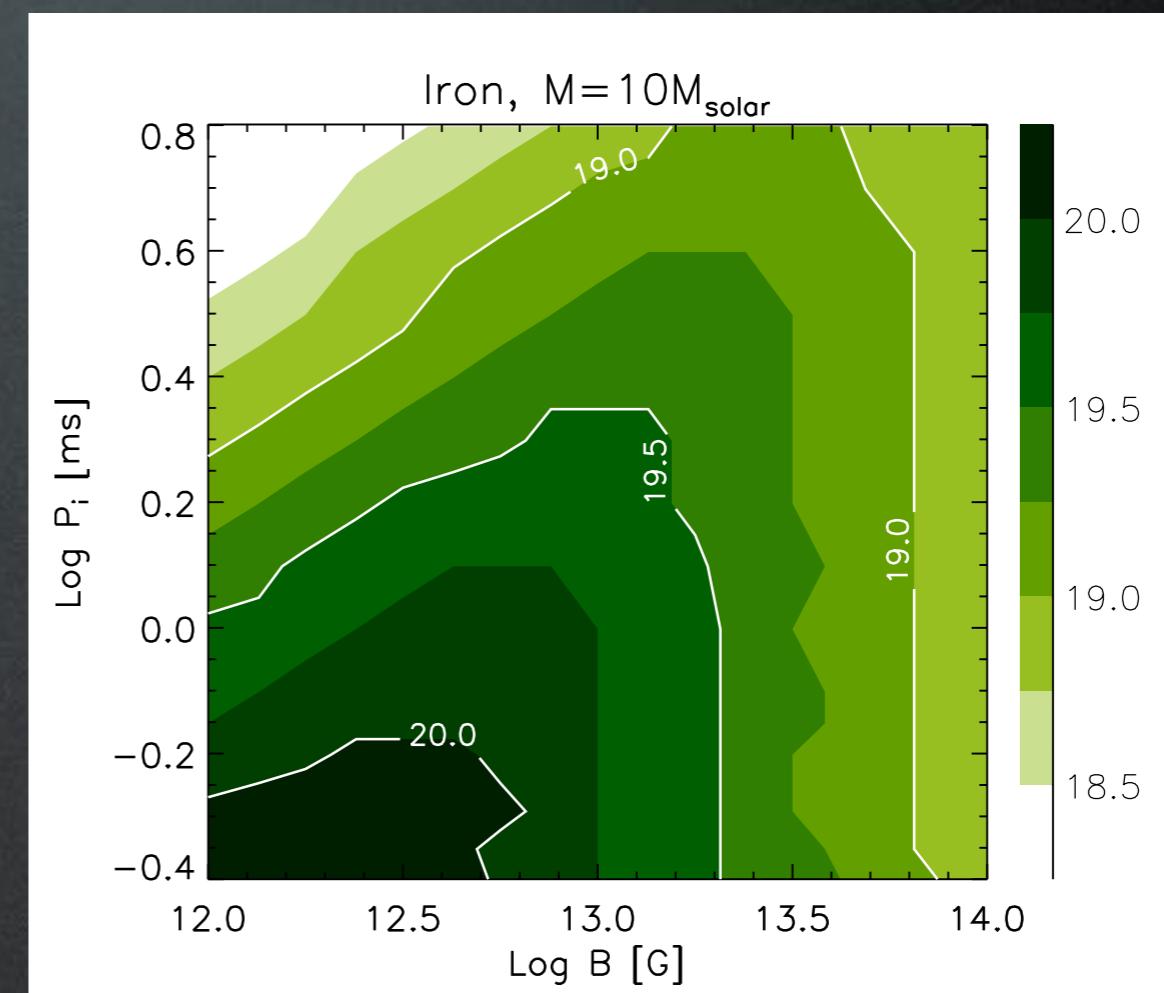
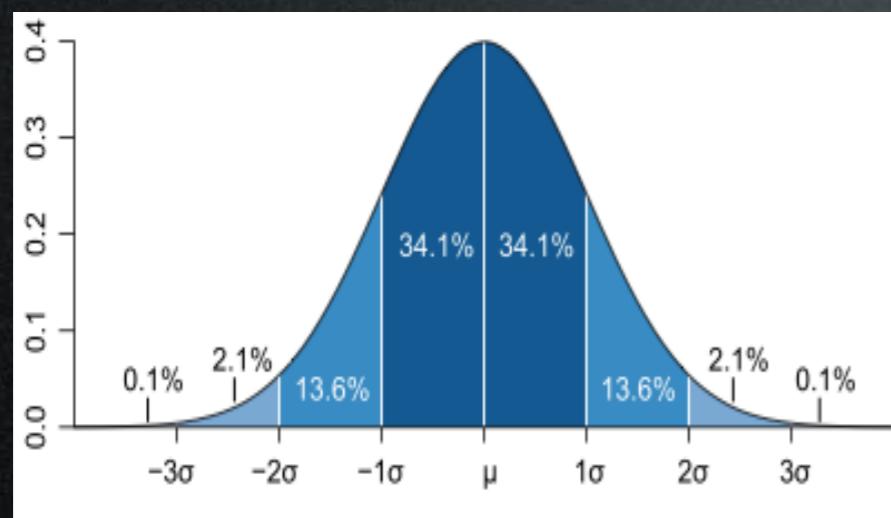


Integrated Extragalactic Pulsars

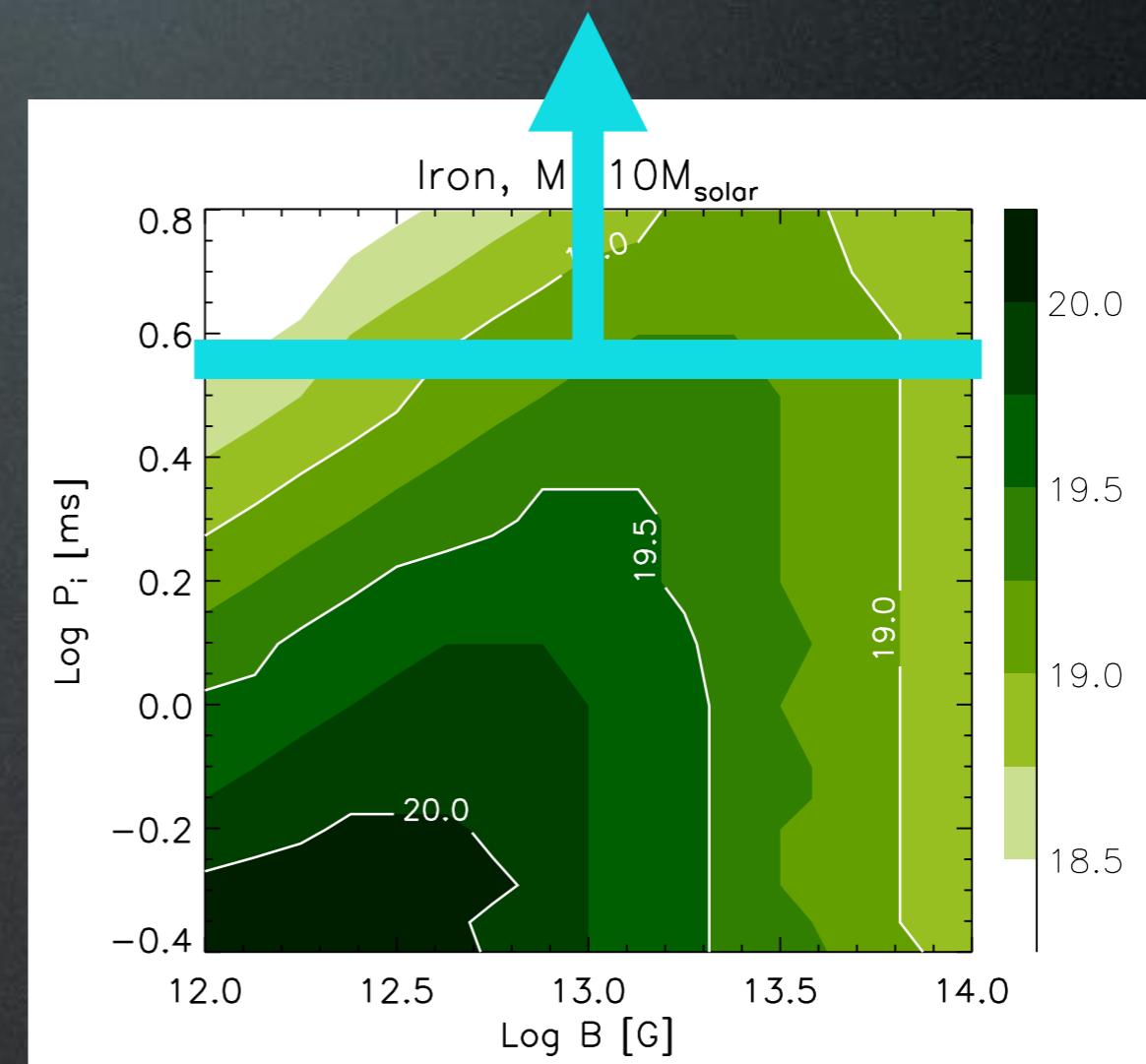
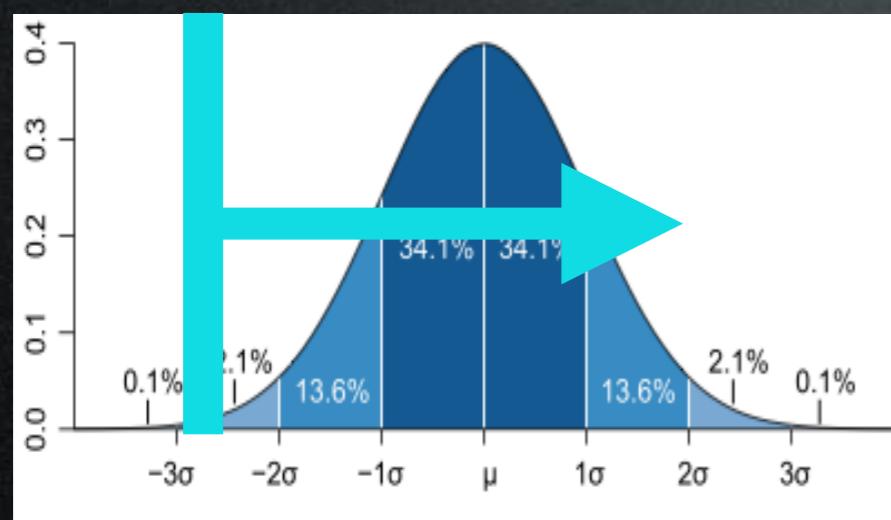


Newborn pulsars can be
successful UHECR accelerators

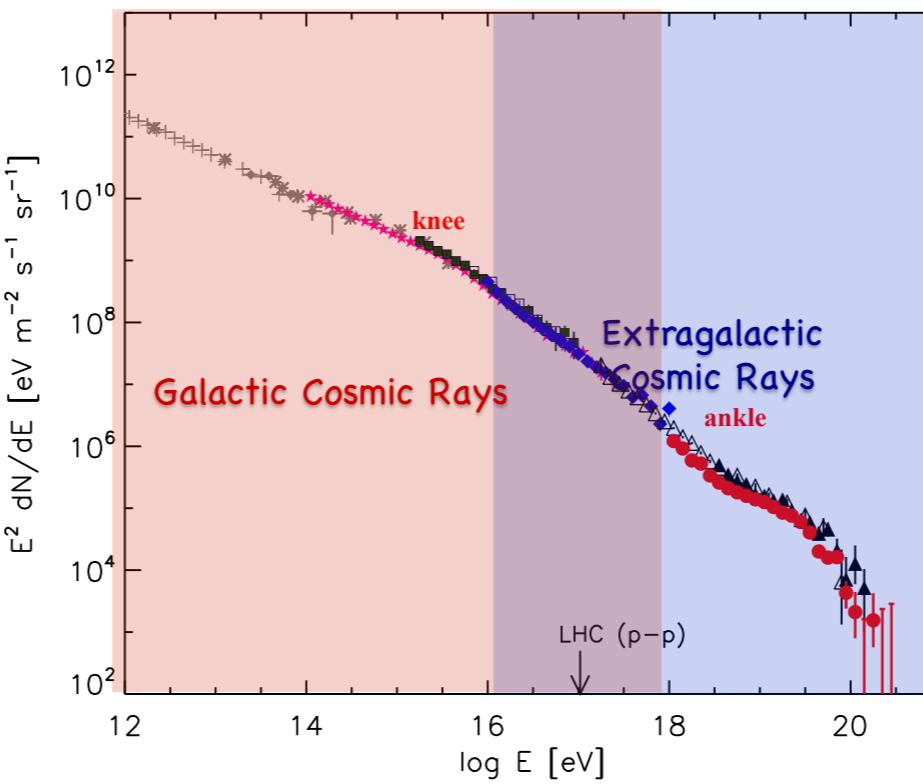
What about their Galactic Counterparts?



What about their Galactic Counterparts?

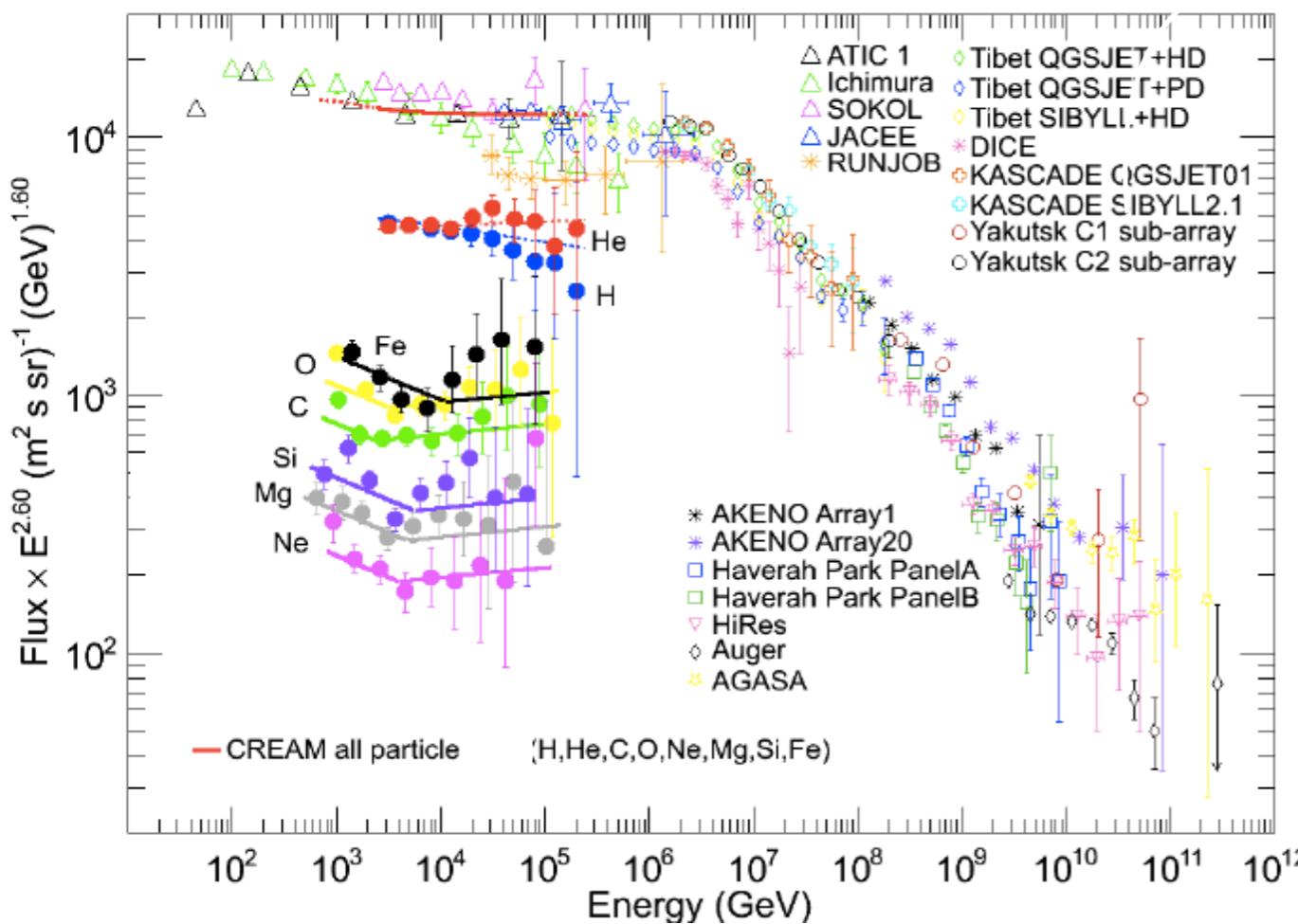
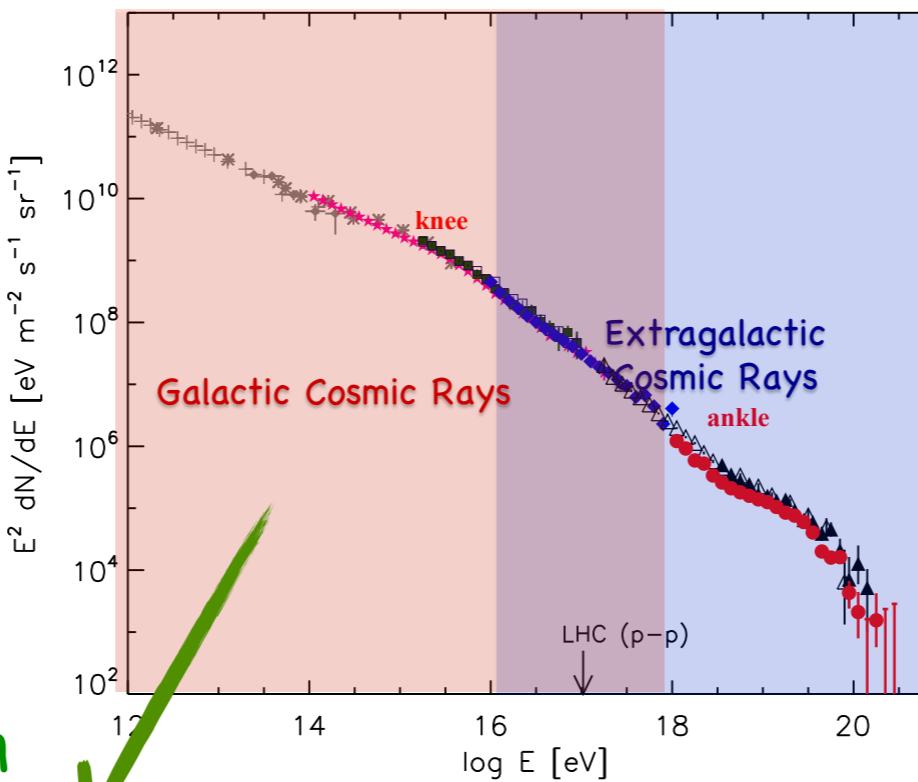


Galactic - Extragalactic Transition



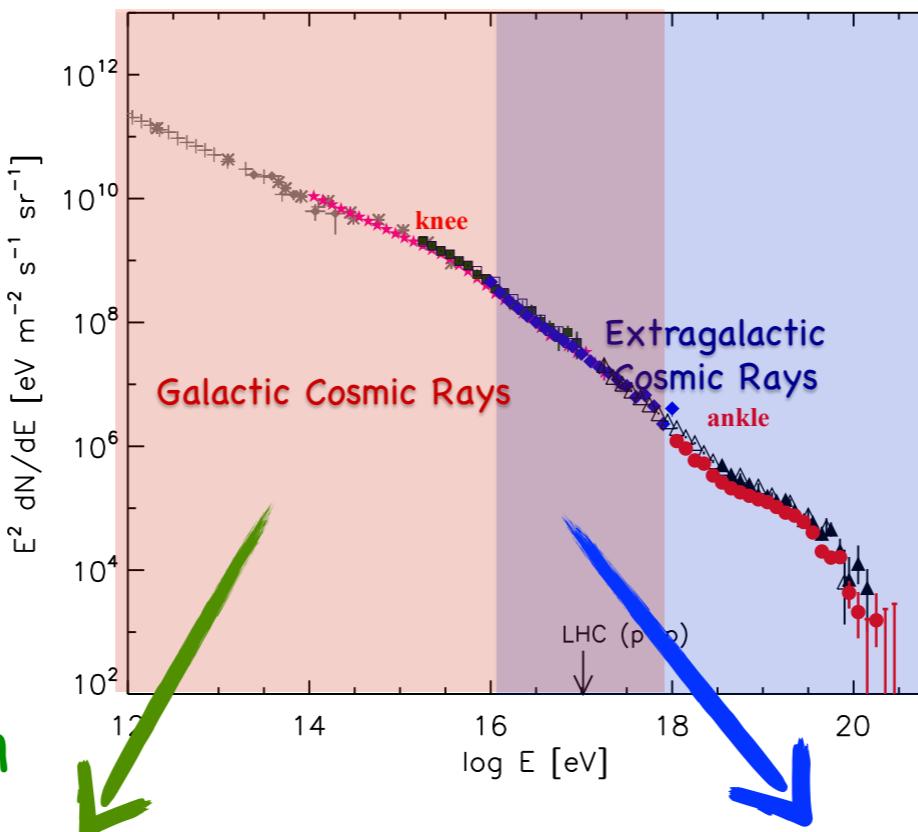
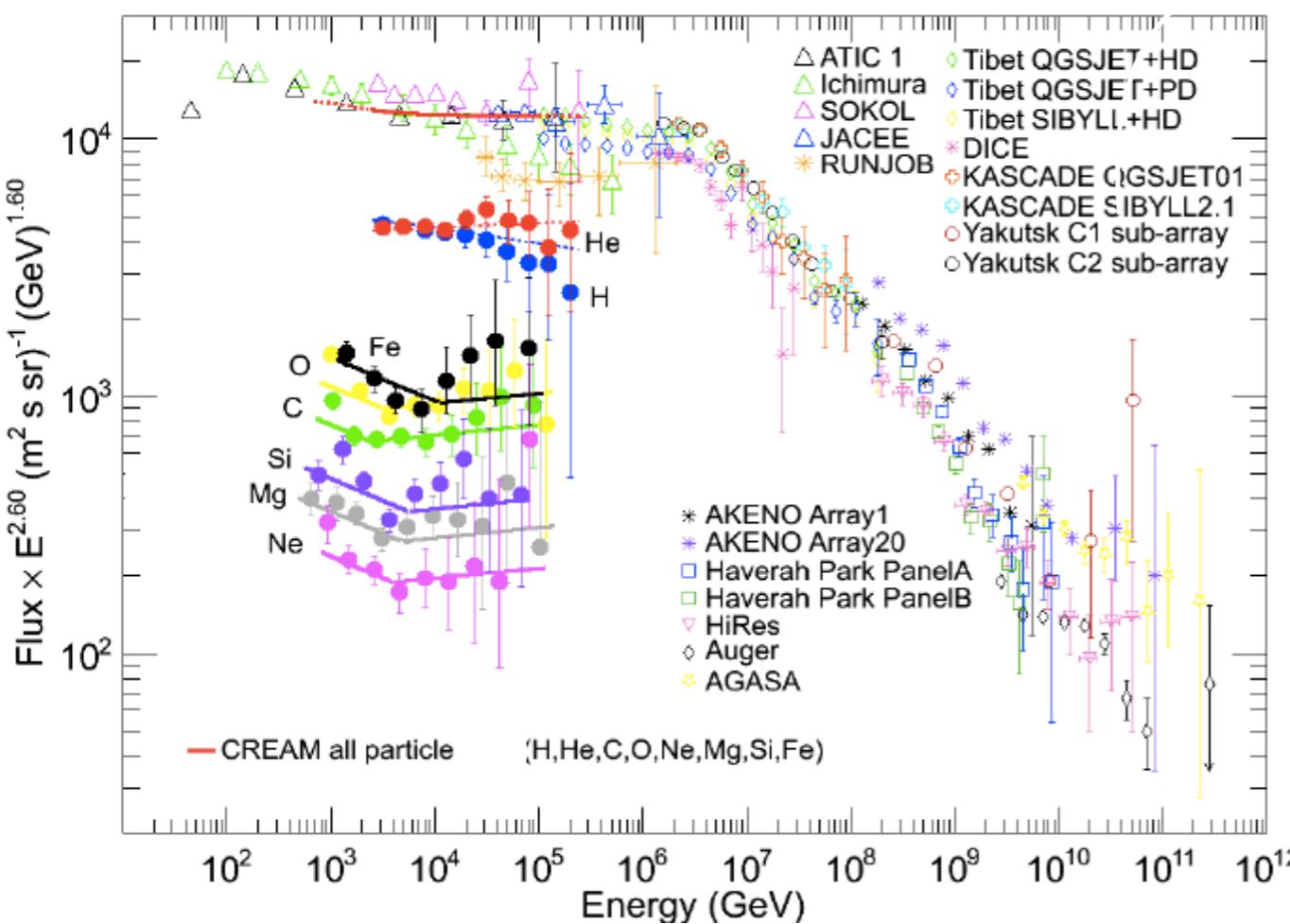
Galactic - Extragalactic Transition

Mostly light composition
below the knee

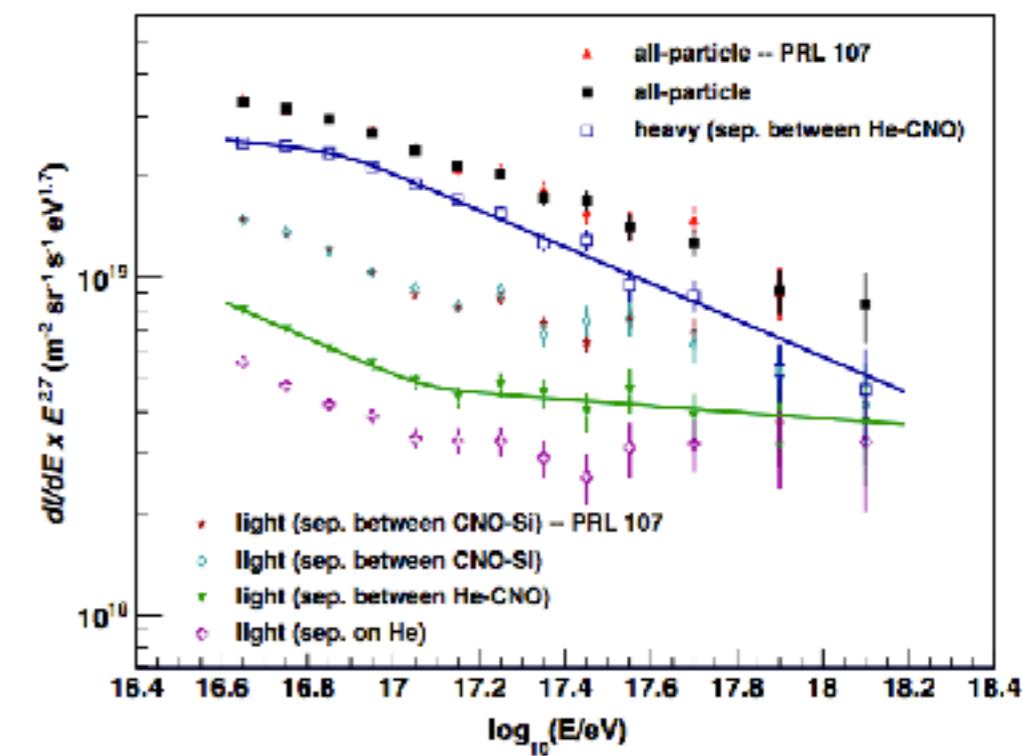


Galactic - Extragalactic Transition

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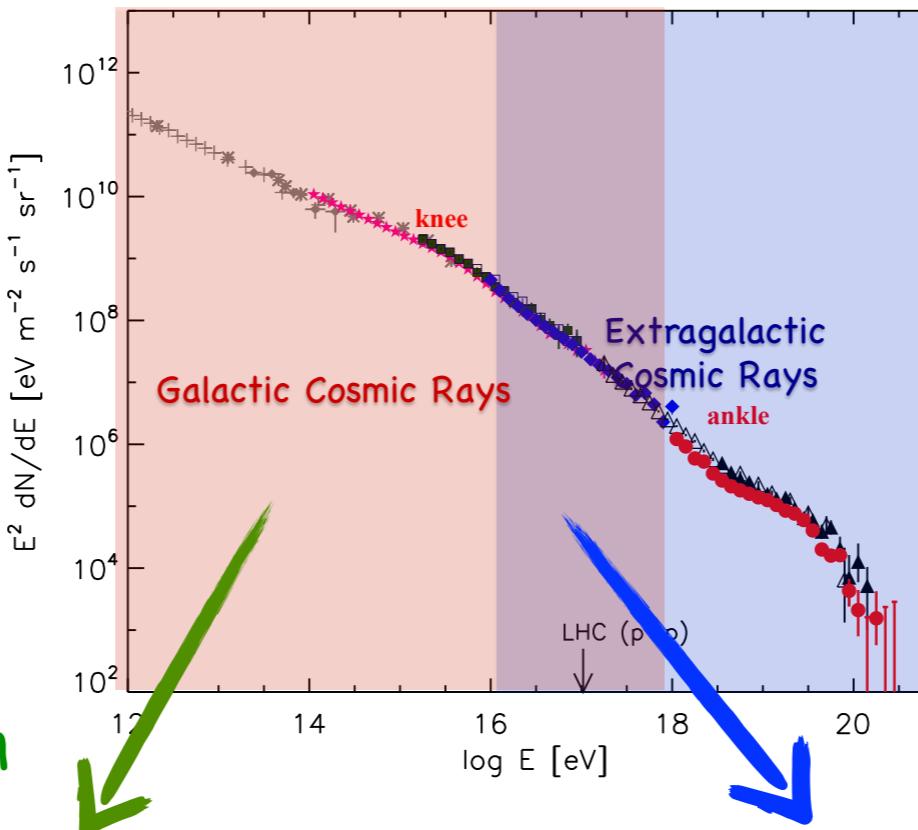
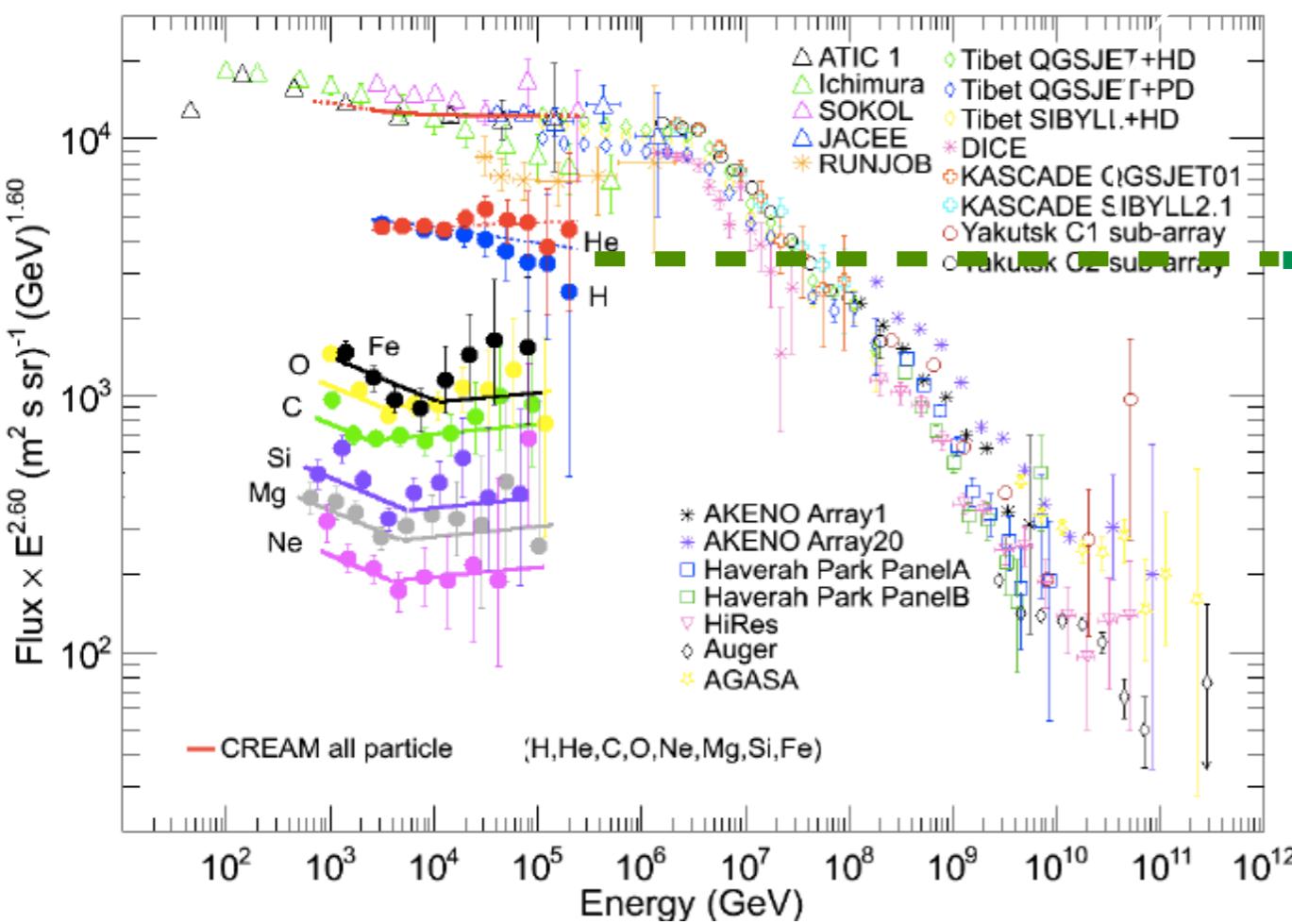
But changed to heavy dominated
at the transition regime



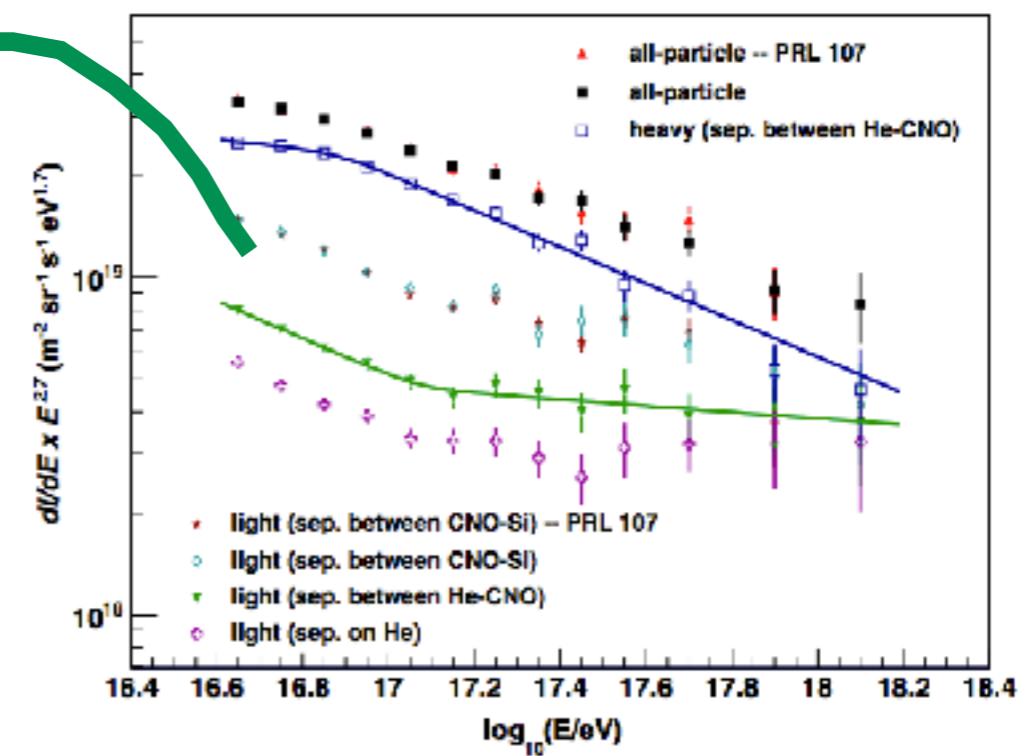
KASCADE,

Galactic - Extragalactic Transition

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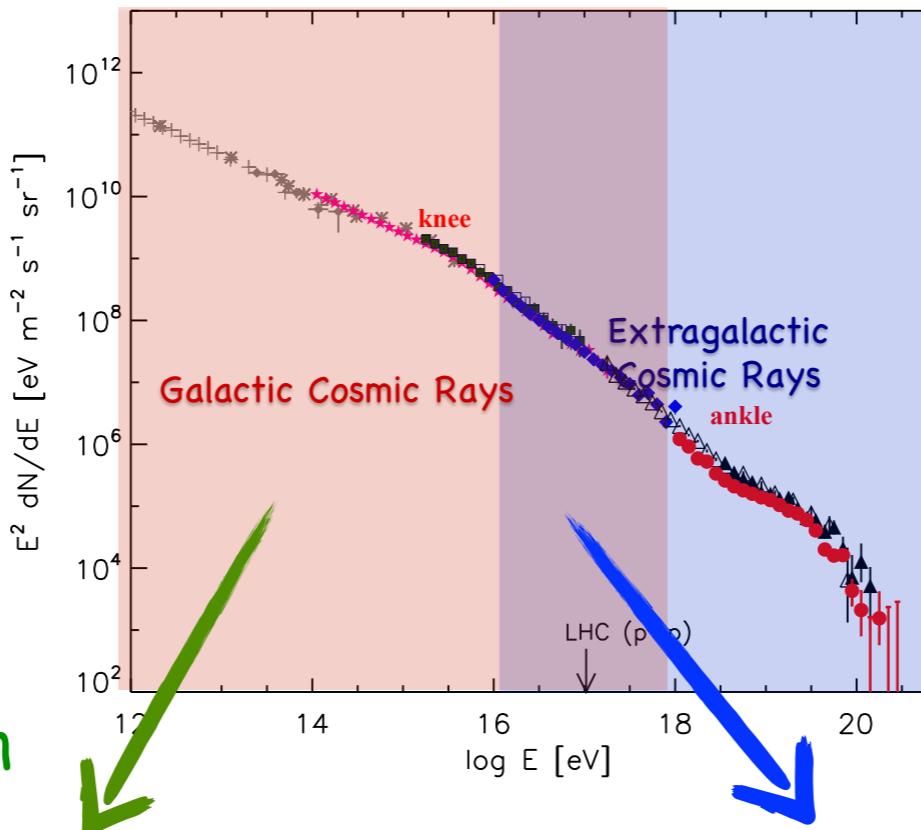
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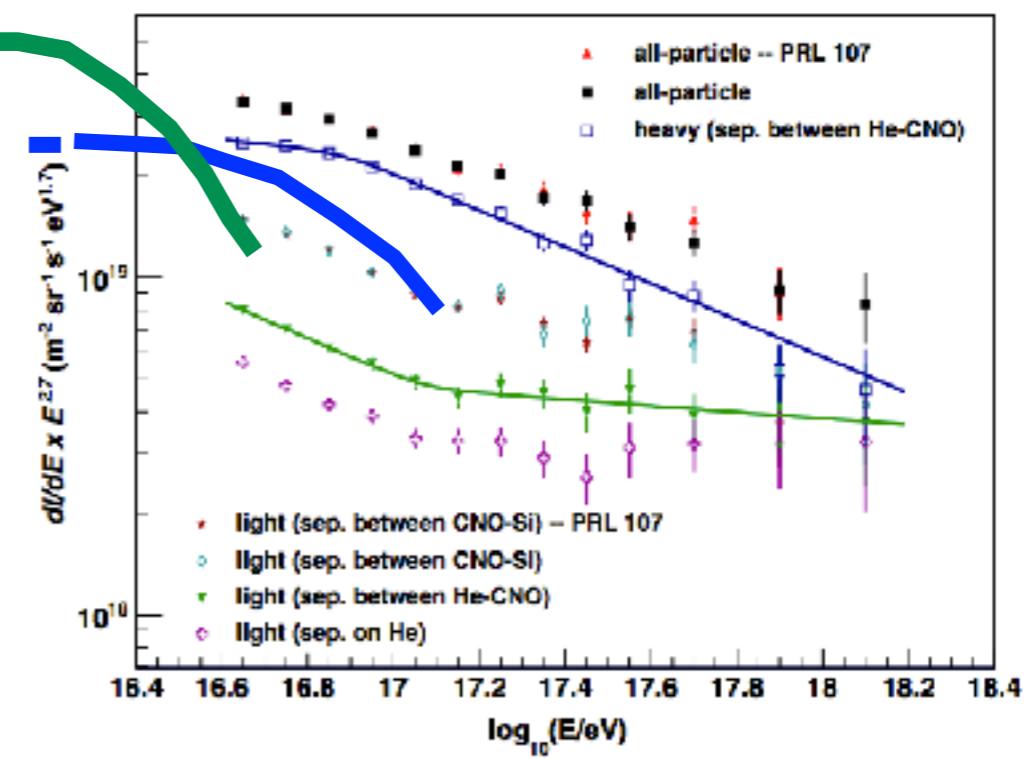
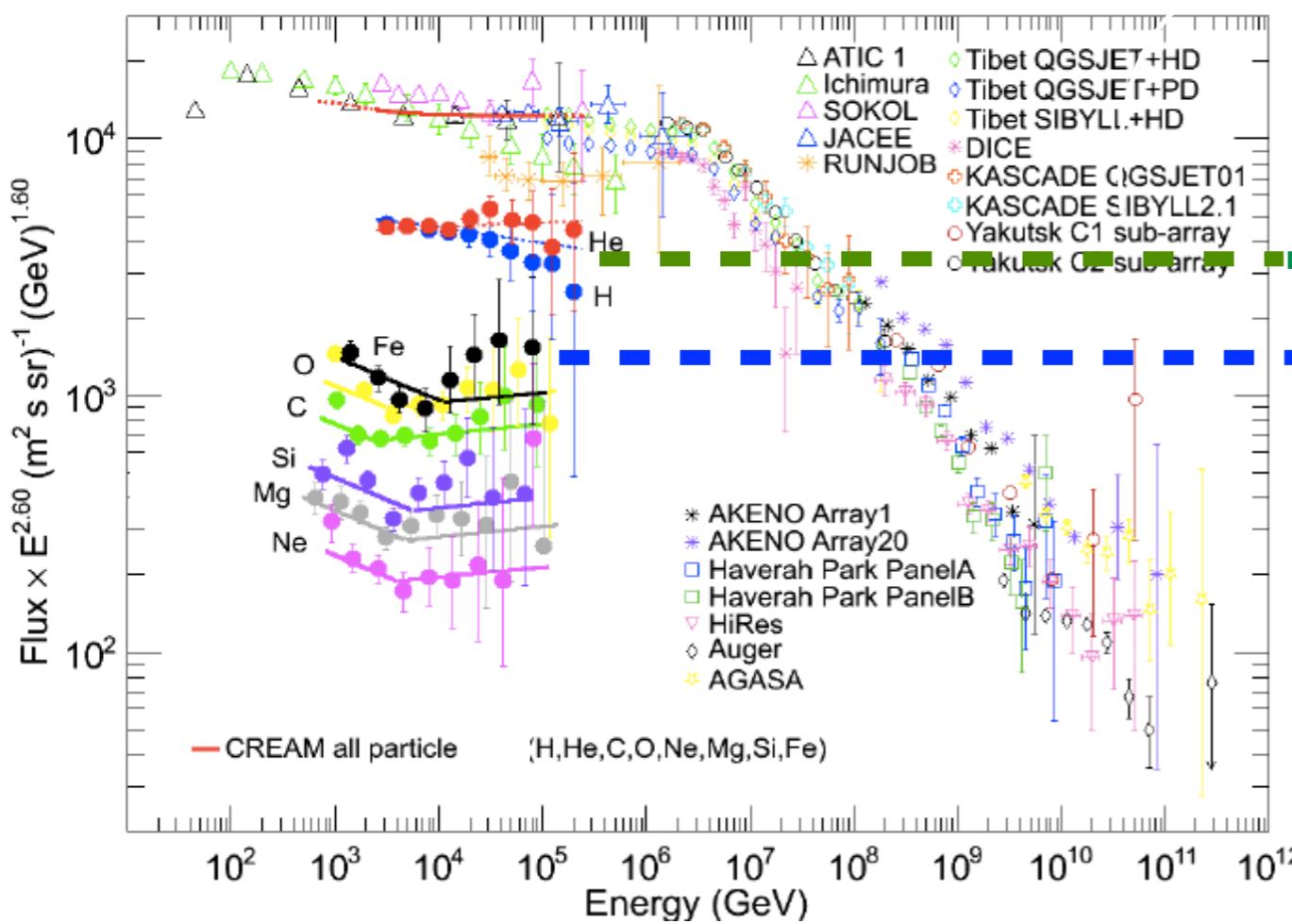
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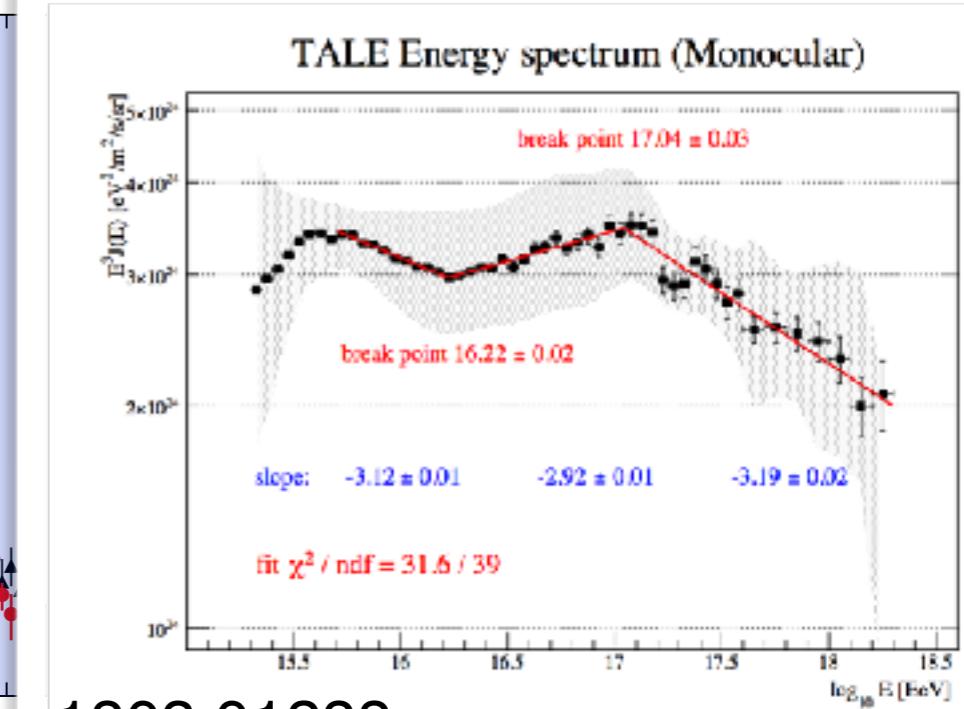
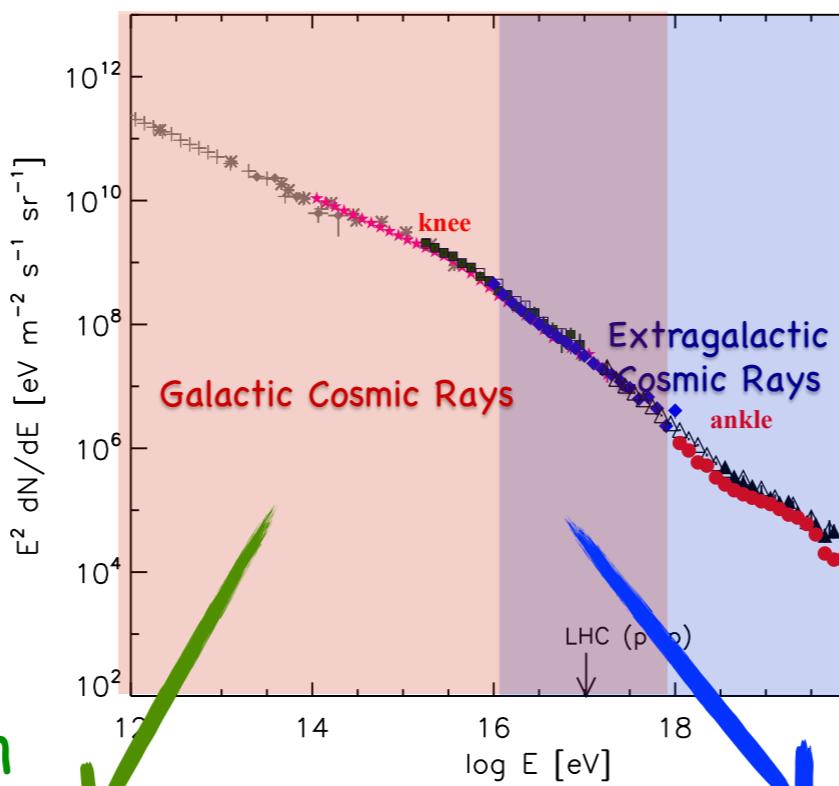
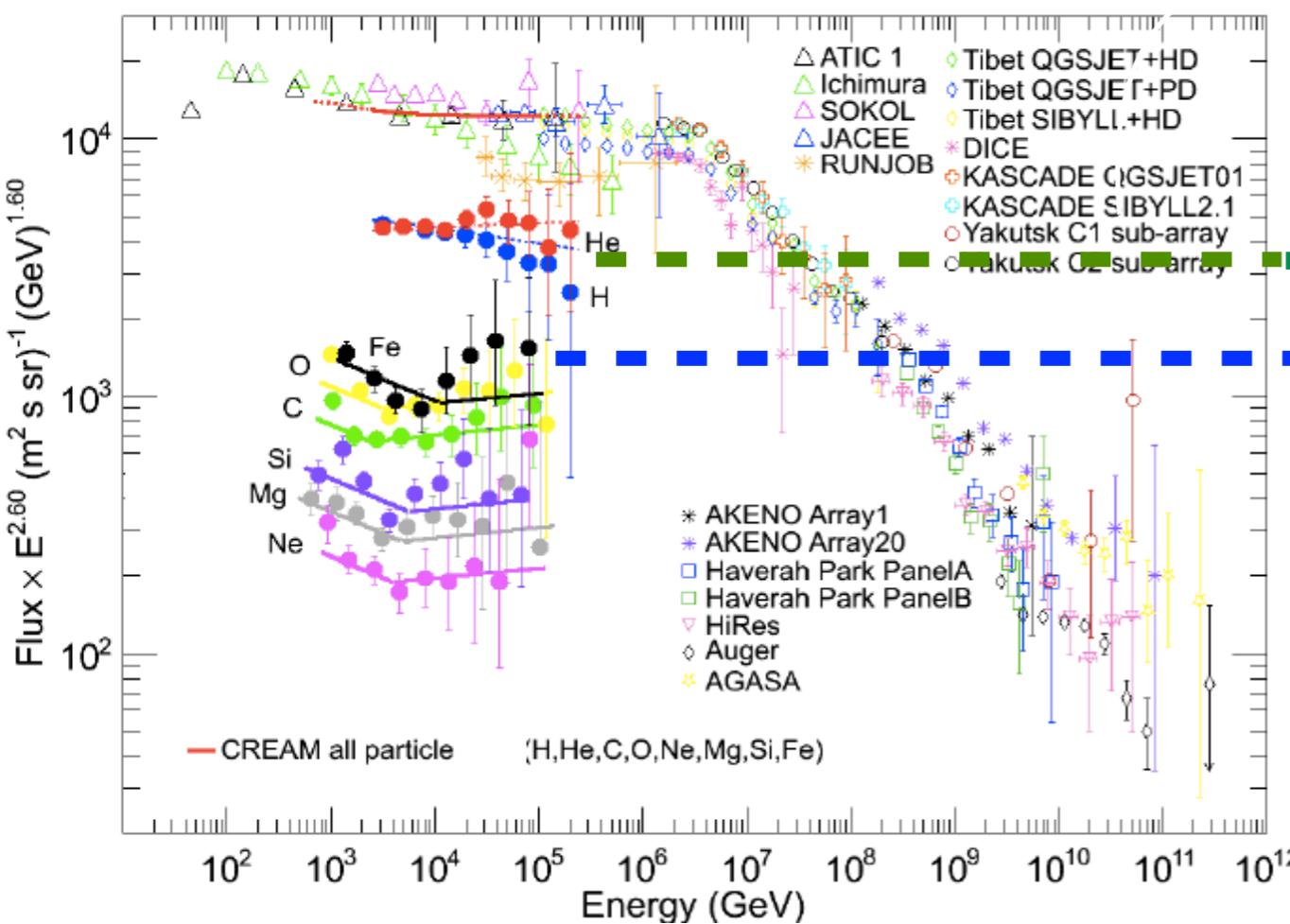
But changed to heavy dominated
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KASCADE,

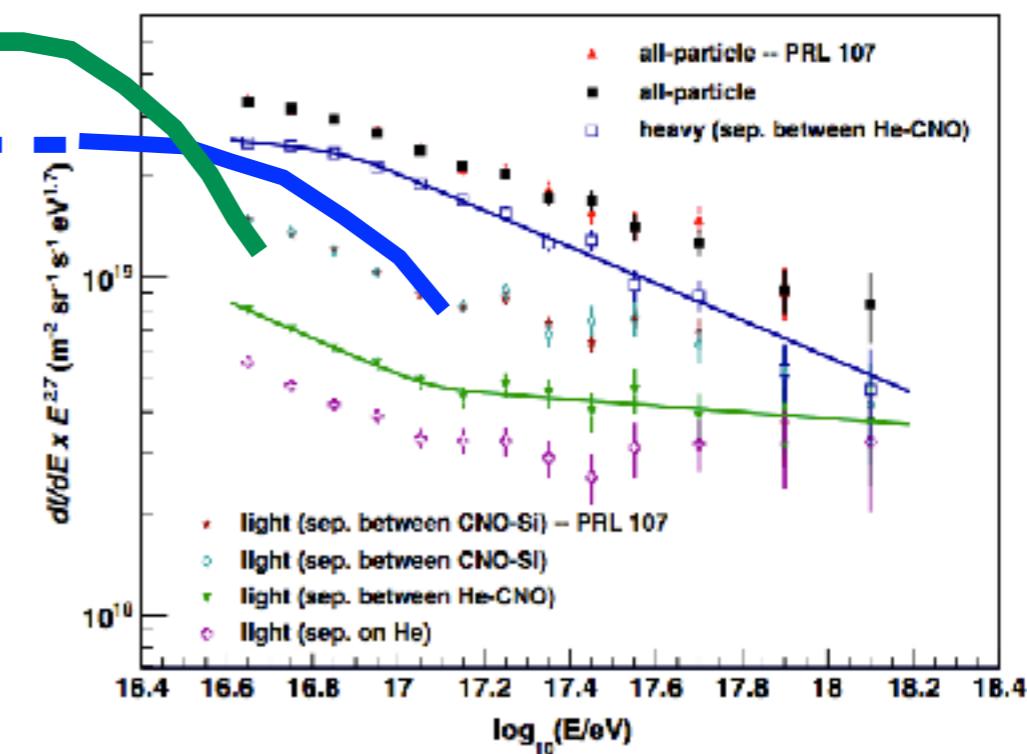
Galactic - Extragalactic Transition

Mostly light composition
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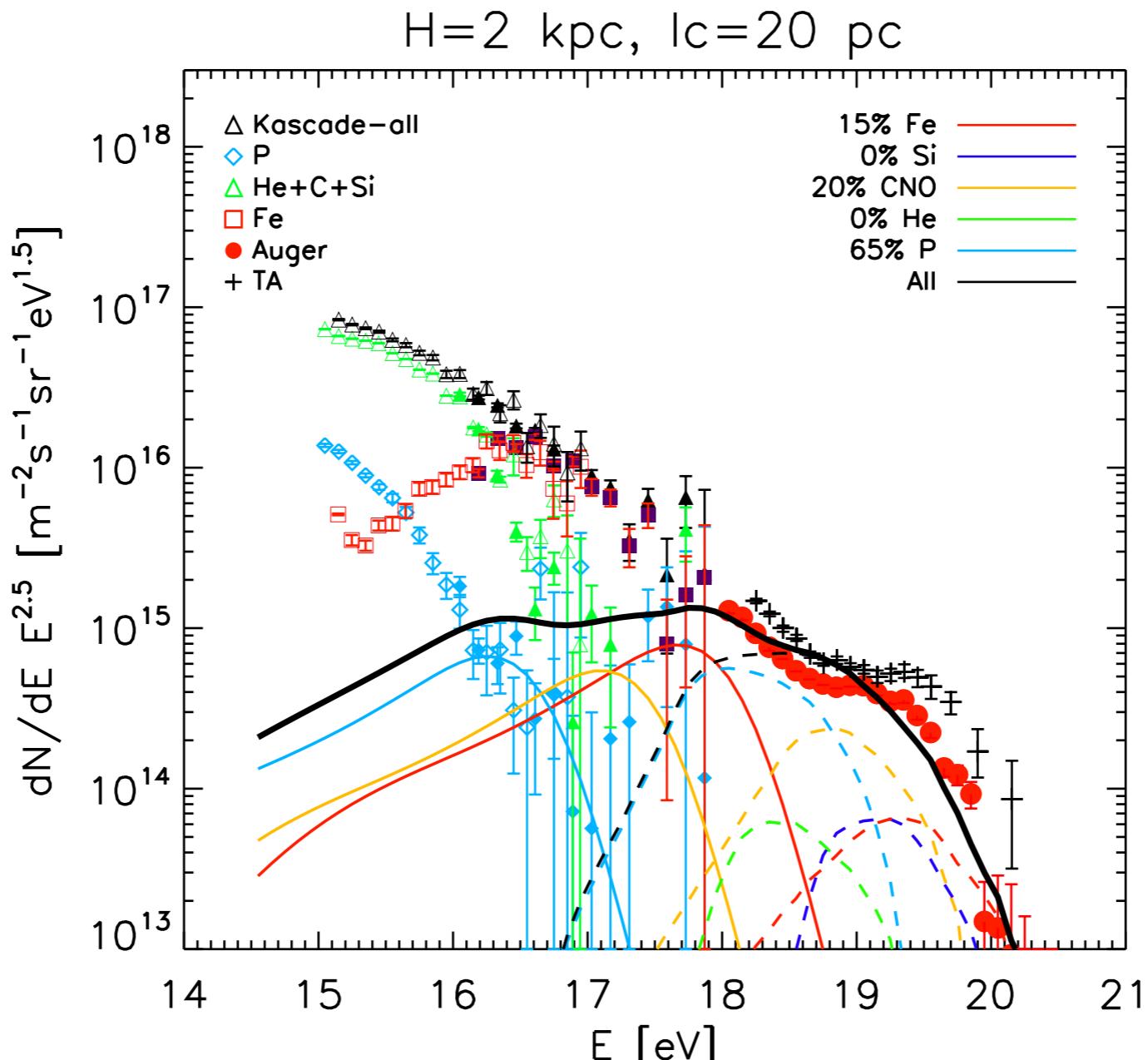
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But changed to heavy dominated
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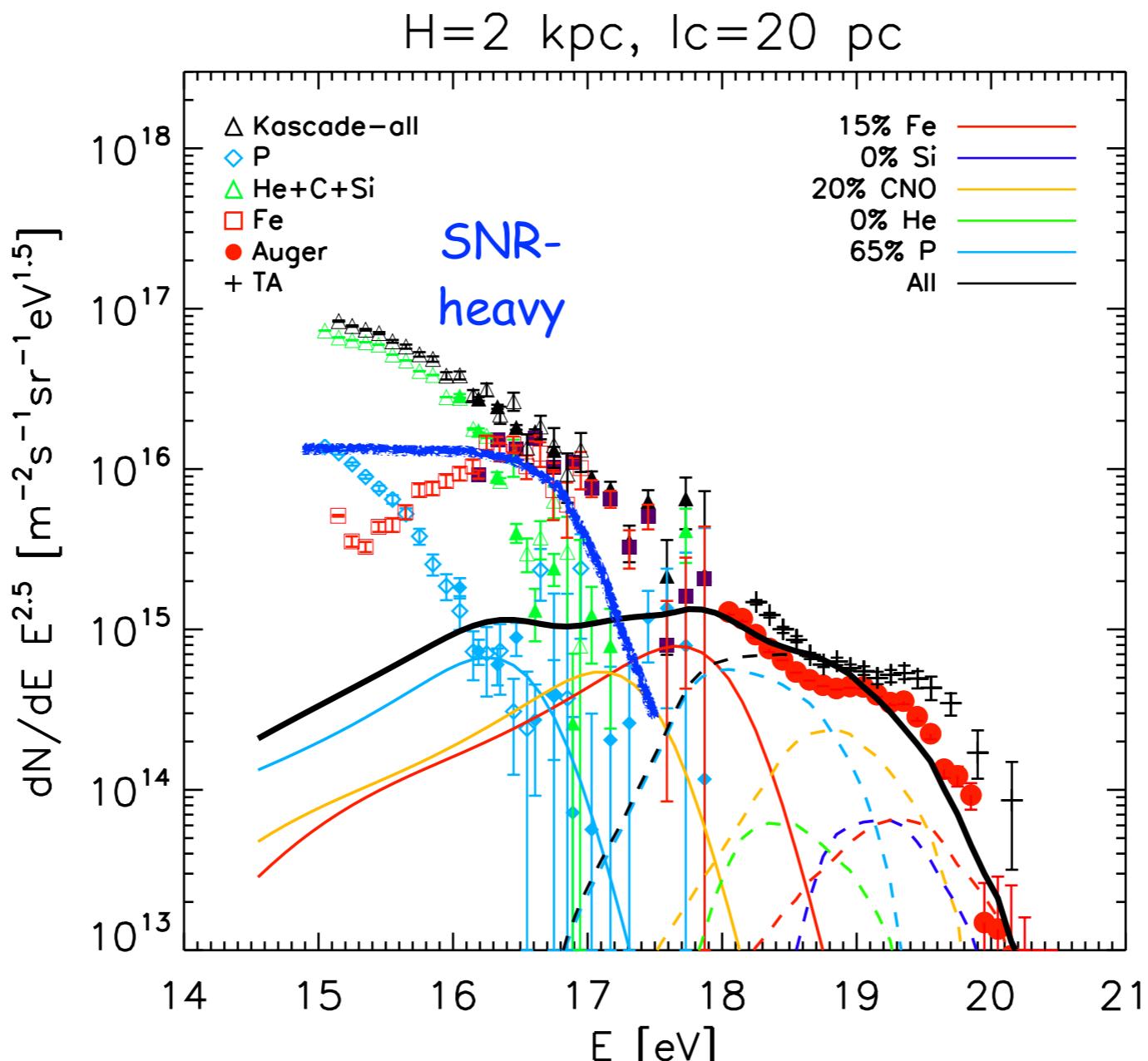
KASCADE,

Contribution from Galactic pulsars - Spectrum



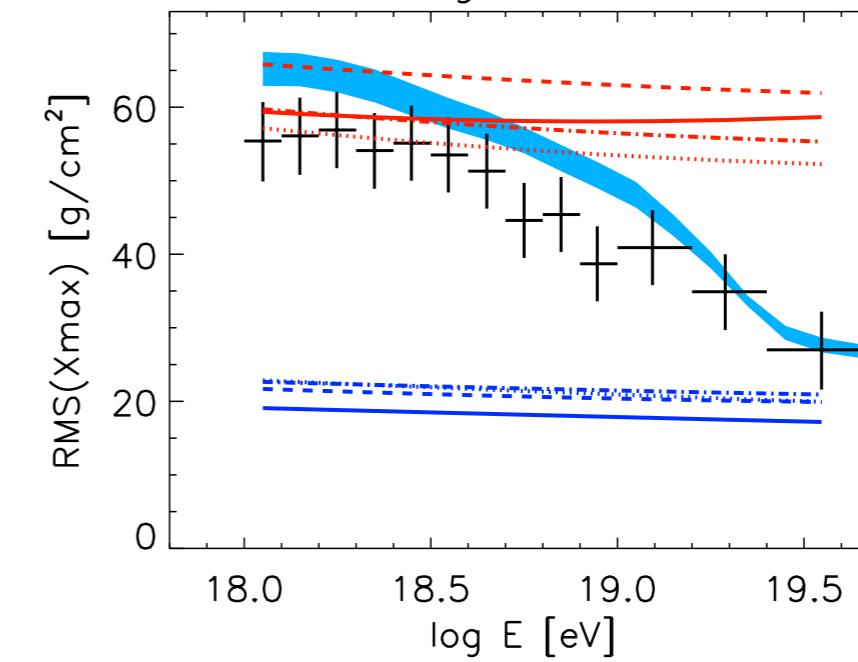
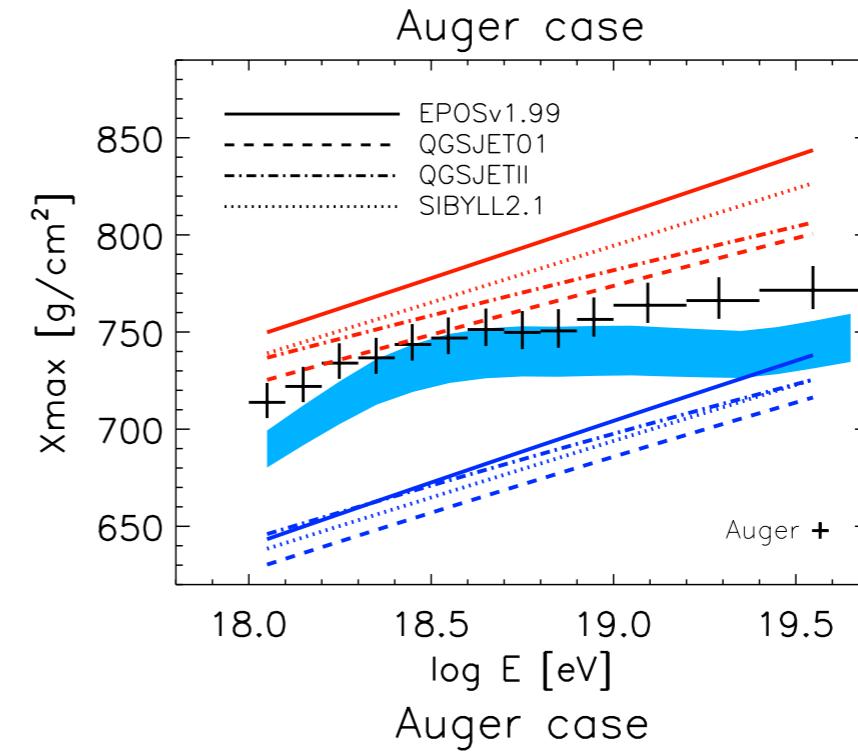
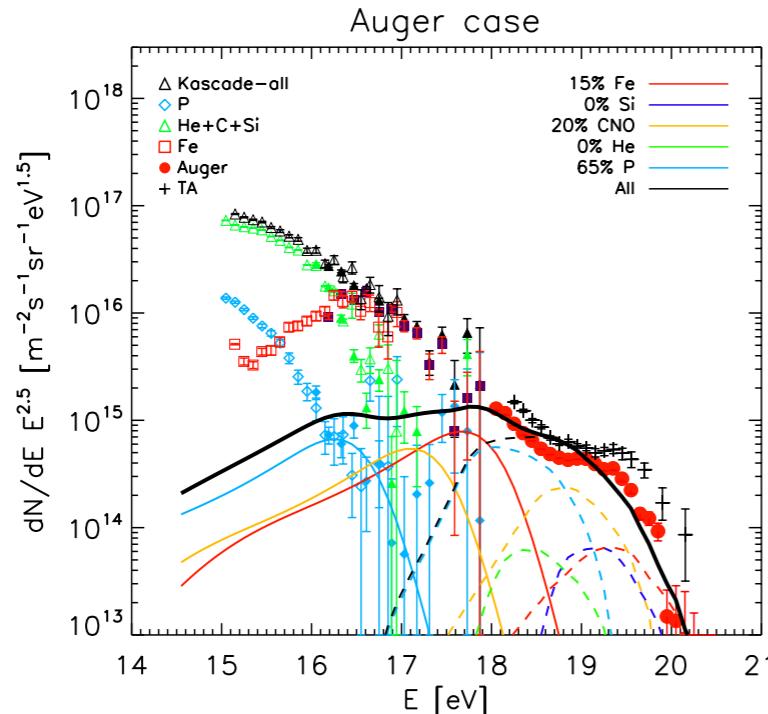
Galactic pulsars can fill the gap

Contribution from Galactic pulsars - Spectrum

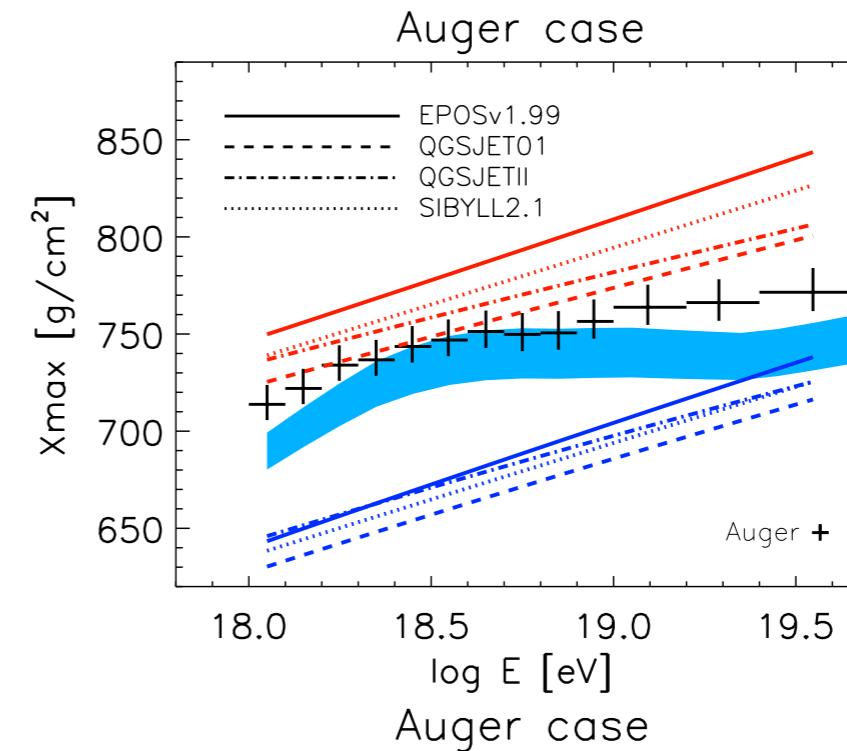
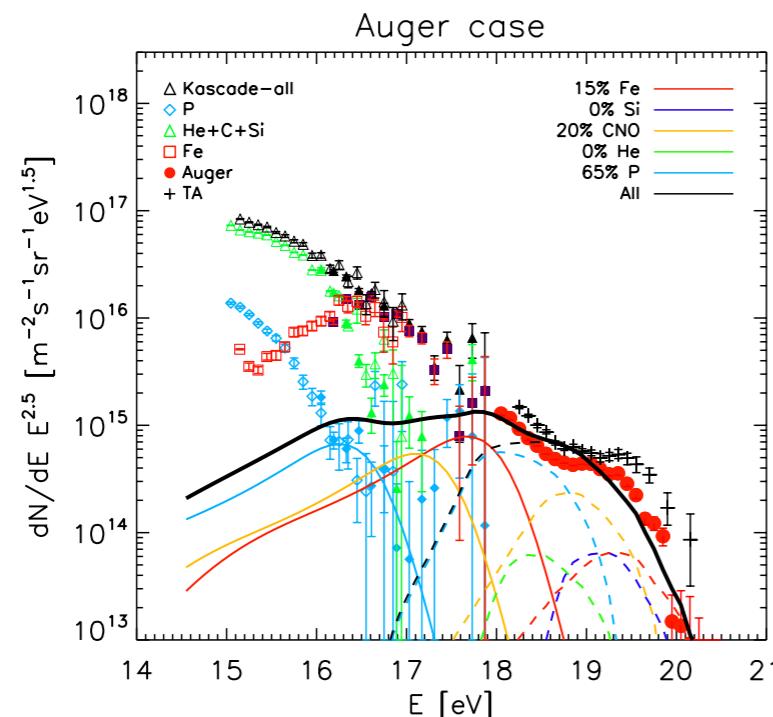


Galactic pulsars can fill the gap

Contribution from Galactic pulsars - Composition



Contribution from Galactic pulsars - Composition



Galactic pulsars can contribute between the knee and the ankle.

GRAND can diagnose the Galactic-extragalactic transition by accurately measuring features in cosmic rays spectrum and composition.

