

# Collider phenomenology of Split-UED

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In collaboration with

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at IPMU

JHEP 0909:078,2009.

arxiv: 0903.1971[hep-th]

# Models beyond the SM

To solve both the fine tuning problem and existence of DM, there are several popular models which give the SM as effective theory.

	Fine tuning problem	Z <sub>2</sub> Parity	Dark matter candidate
SUSY	boson-fermion sym.	R-parity	$\tilde{\chi}_1^0, \tilde{G}$
Little Higgs with T-parity	Global sym.	T-parity (Anomalies; Hill&Hill)	$A_H$
mUED	Lorentz sym in 5dim Low Planck scale	KK-parity	$B_1$

Partners for SM particles.

Parity structure  always produced in pairs at colliders.

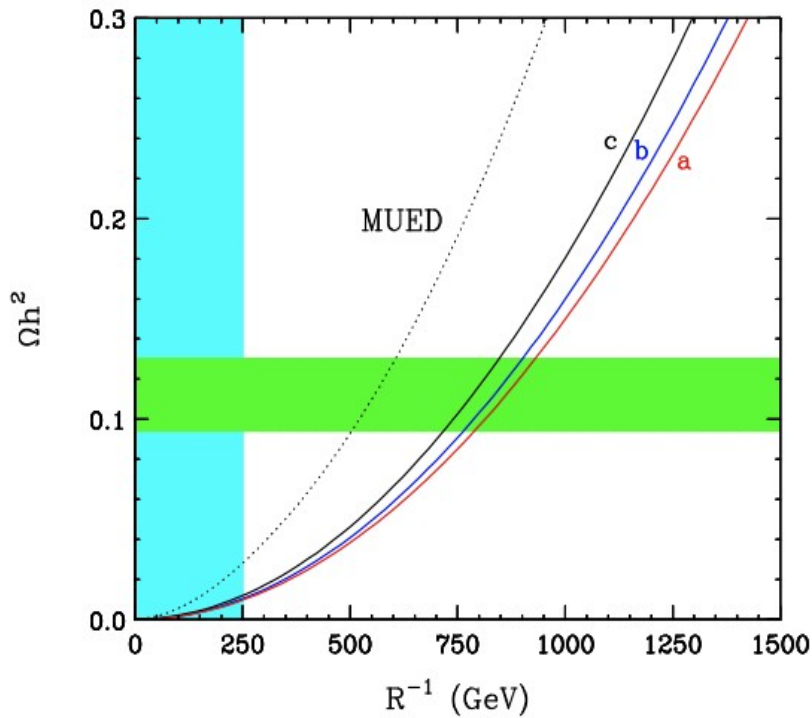
Couplings are given by SM couplings (predictive).

# mUED

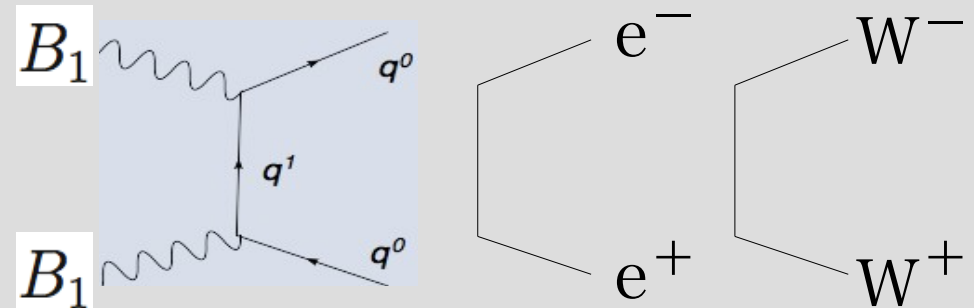
T. Appelquist, H-C. Cheng, B. A. Dobrescu

In mUED, LKP (heavy photon) is DM candidate. G.Servant, T.M.P. Tait

600 ~ 900 GeV LKP DM gives correct DM abundance



K. Kong, K. Matchev, JHEP 0601:038, (2006)

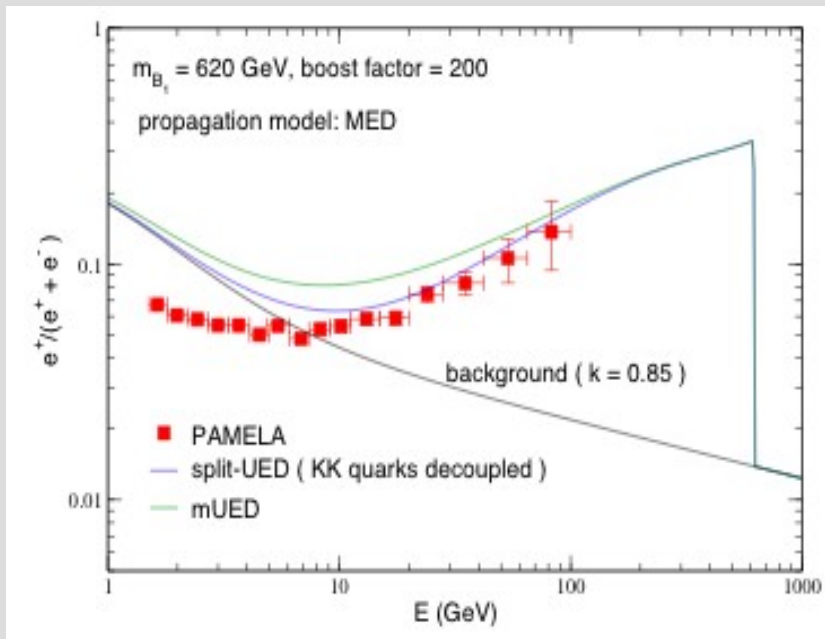


Possible cosmic ray sources

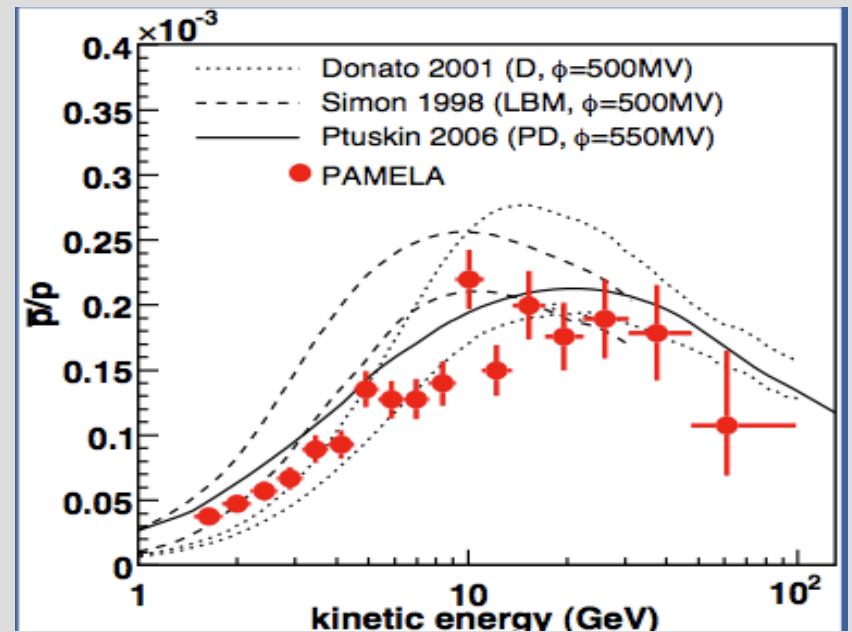
# PAMELA

PAMELA Collaboration (Oscar Adriani et al.)

$e^+/(e^- + e^+)$  flux



anti-p / p flux



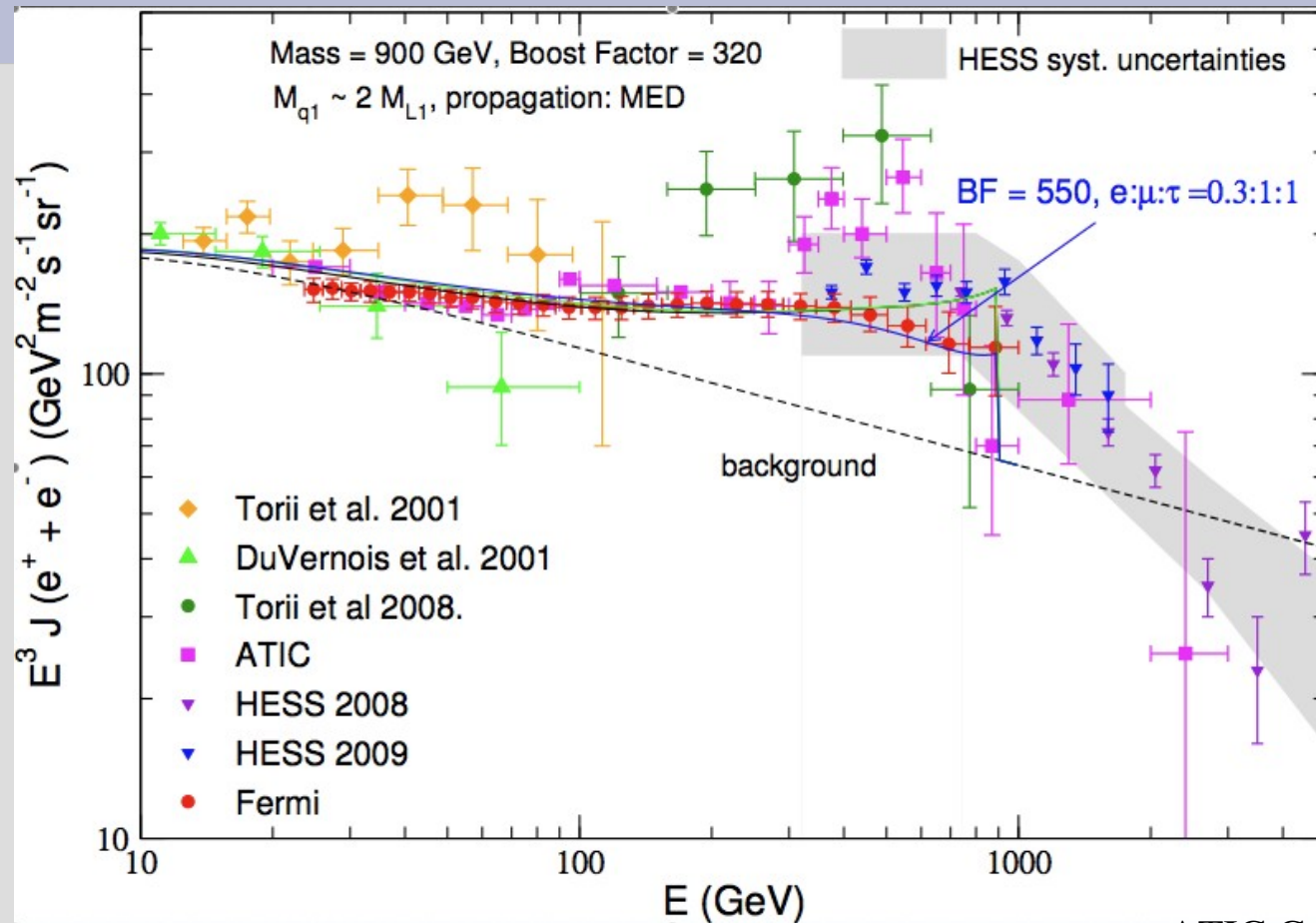
Existence of  $e^+$  sources

with  $> 100\text{GeV}$

(Pulsar ? V. Barger, Y. Gao, Wai Yee Keung,  
D. Marfatia, G. Shaughnessy)

No Excess

# $e^+ + e^-$ flux (FERMI, ATIC)



FERMI

Fermi LAT Collaboration  
 (Aous A. Abdo et al.)

Excess on  $\sim 900$  GeV data ?

ATIC

ATIC Collaboration  
 J. Chang *et al.*

Peak around 600 GeV  
 (Ruled out by Fermi)

# Motivation of Split-UED

DM annihilation  $\stackrel{?}{=}$  source of  $e^+$  flux excess (PAMELA)

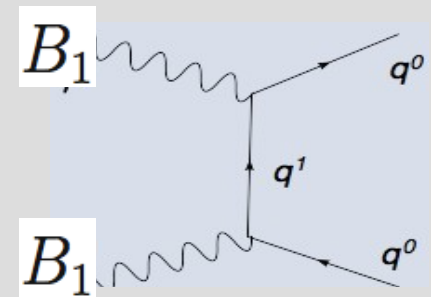
and

ATIC peak with 620 GeV DM (Original motivation)

Fermi excess with 900 GeV DM

On the other hand, hadron modes contribute little. (PAMELA)

Increase the mass of  $q_1$   $\longrightarrow$  suppress



Need mechanism to increase only quark partner mass.

# Plan

- Introduction & Motivation
- Model

Split-UED = mUED + 5D Bulk mass  $\mu$

- Fermionic partners for SM fermions
- Almost degenerate mass spectrum
- Heavy quark partner ( $q_1$ )

- Collider signatures

# mUED model

T. Appelquist, H-C. Cheng, B. A. Dobrescu

All SM fields live in 5D ( $S^1$  compactified).

$$x^M = (x^0 = t, x^1, x^2, x^3, x^5) = (x^\mu, y)$$

→ 
$$\Phi(x, y) = \frac{1}{\sqrt{2\pi R}} \phi^{(0)}(x) + \frac{1}{\sqrt{\pi R}} \sum_{n=1}^{\infty} \left[ \phi^{(+n)}(x) \cos \frac{ny}{R} + \phi^{(-n)}(x) \sin \frac{ny}{R} \right].$$

Zero modes as SM fields

To obtain chiral fermions,

$S^1/Z_2$  orbifolding

$$\Psi'(x') = \eta_P \gamma^5 \Psi(x) \quad x^M = (x^\mu, y) \rightarrow x'^M = (x^\mu, -y).$$

For the SM, we choose:

$$\eta_P = -1 \quad \text{for Q, L}$$

$$\Psi_L(x^\mu, y) = \frac{1}{\sqrt{2\pi R}} \Psi_L^{(0)}(x^\mu) + \sum_{n=1}^{\infty} \frac{1}{\sqrt{\pi R}} \Psi_{L+}^{(n)}(x^\mu) \cos \frac{ny}{R}$$

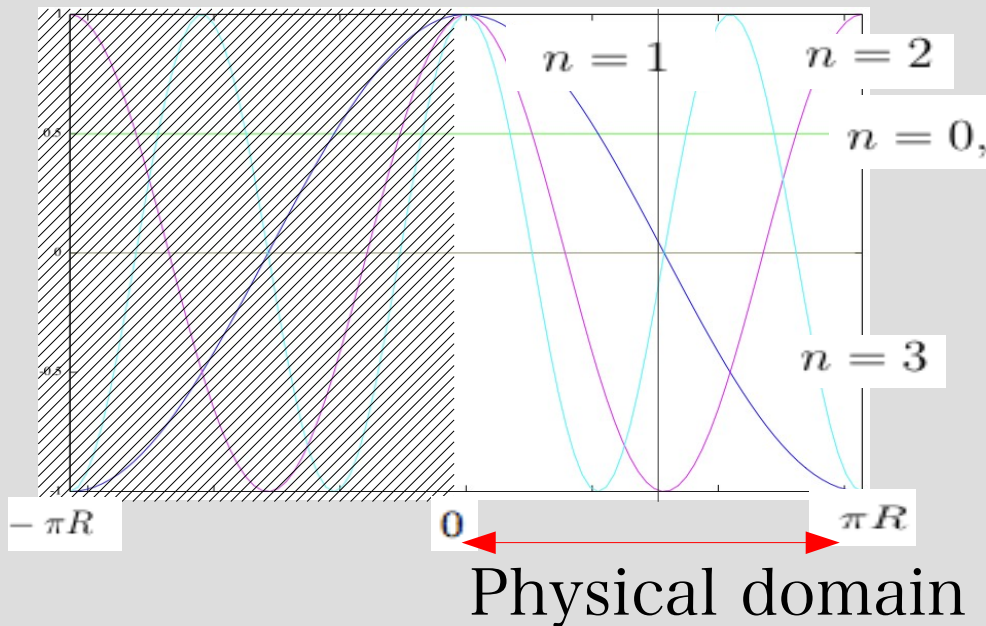
$$\Psi_R(x^\mu, y) = \sum_{n=1}^{\infty} \frac{1}{\sqrt{\pi R}} \Psi_{R-}^{(n)}(x^\mu) \sin \frac{ny}{R}.$$

$$\eta_P = +1 \quad \text{for U, D, E, N}$$



# KK parity

Physical domain is  $0 < y < \pi R$ . 4D eff. Lagrangian obtained by  $y$ -integration.  
 Only terms even under the reflection symmetry survive.



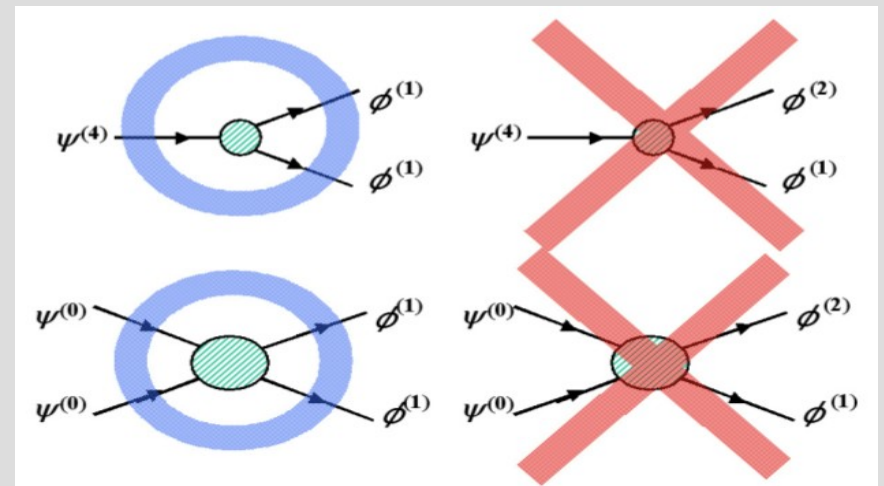
$$\Psi_L(x^\mu, y) = \frac{1}{\sqrt{2\pi R}} \Psi_L^{(0)}(x^\mu) + \sum_{n=1}^{\infty} \frac{1}{\sqrt{\pi R}} \Psi_{L+}^{(n)}(x^\mu) \cos \frac{ny}{R}$$

Symmetry as KK-parity of fields.

Even  $\Psi_L^{(0)}, \Psi_L^{(2)}, \Psi_L^{(4)}, \dots$

Odd  $\Psi_L^{(1)}, \Psi_L^{(3)}, \dots$

Each vertex conserves KK-parity.



# Split-UED model

- mUED + bulk mass  $\mu$

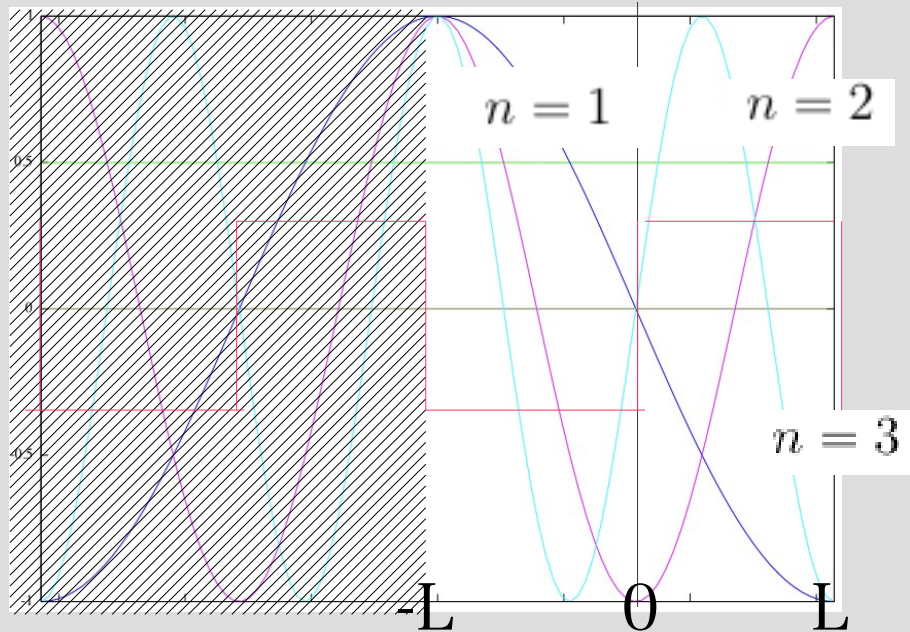
If we introduce normal vector-like mass term  $M(\bar{\Psi}_L \Psi_R + \bar{\Psi}_R \Psi_L)$

after y-integration, it gives KK parity violating terms,  $m(\bar{\Psi}_L^{(0)} \Psi_R^{(1)} + \bar{\Psi}_R^{(1)} \Psi_L^{(0)})$

Instead, we introduce mass term  $M\epsilon(y)(\bar{\Psi}_L \Psi_R + \bar{\Psi}_R \Psi_L)$  S.C. Park, J. Shu

$$S_{\text{split-UED}} = \int d^4x \int_{-L}^L dy \left[ \mathcal{L}_{\text{mUED}} - M\epsilon(y) \bar{\Psi}_q(x, y) \Psi_q(x, y) \right]$$

$$\epsilon(y) = \begin{cases} +1 & (0 < y < L) \\ -1 & (-L < y < 0) \end{cases}$$



After y-integration, terms like

$$m(\bar{\Psi}_L^{(0)} \Psi_R^{(2)} + \bar{\Psi}_R^{(2)} \Psi_L^{(0)}) \text{ remain.}$$

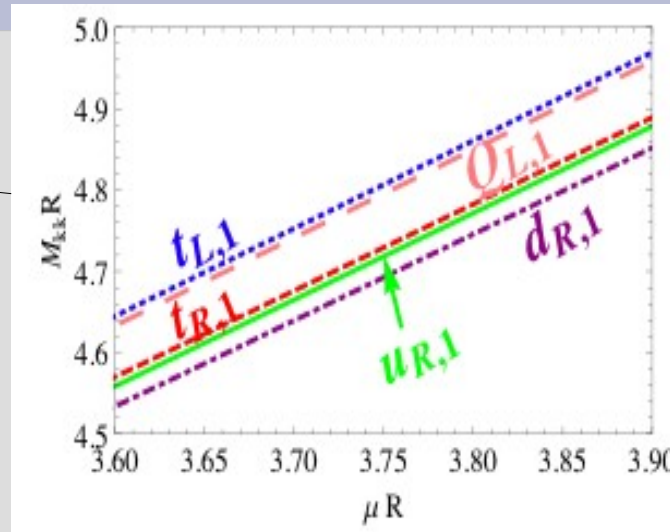
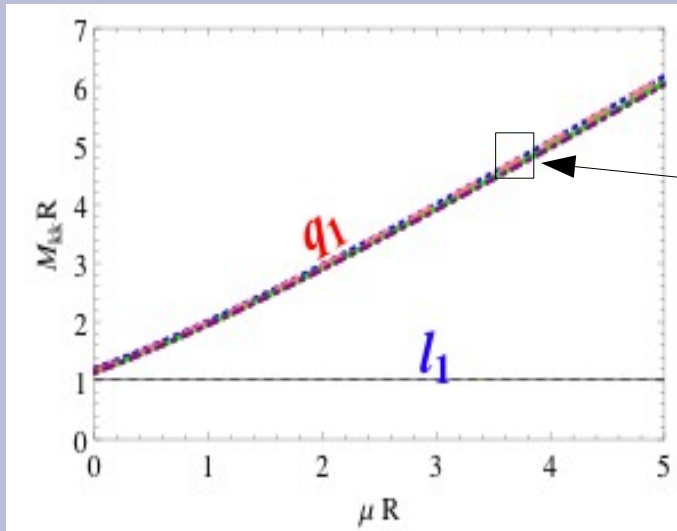
These terms give mixing among

$$\Psi_L^{(0)}, \Psi^{(2)}, \Psi^{(4)}, \dots \quad \text{and} \quad \Psi^{(1)}, \Psi^{(3)}, \dots$$

KK parity conserving

# Spectrum

Split-UED REF

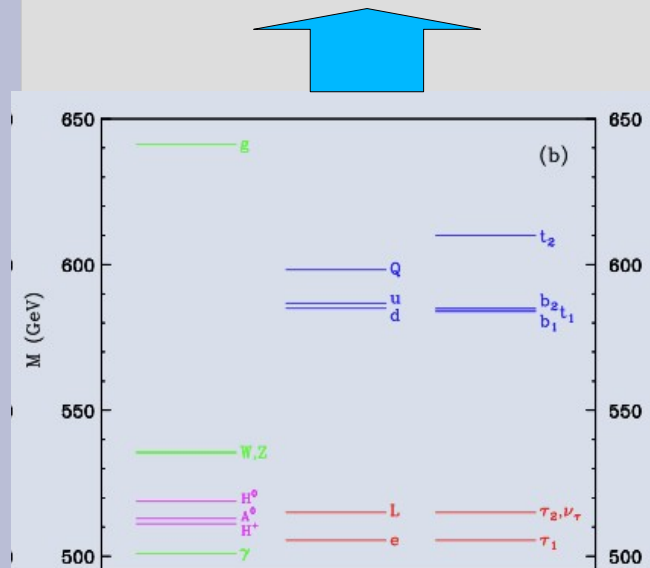


$$m_{q_n}^{\text{tree}} = \sqrt{\mu^2 + k_n^2},$$

$$m_{l_n}^{\text{tree}} = n/R,$$

$$k_{n-} = -|\mu| \tan k_n L,$$

$$k_{n+} = n/R.$$

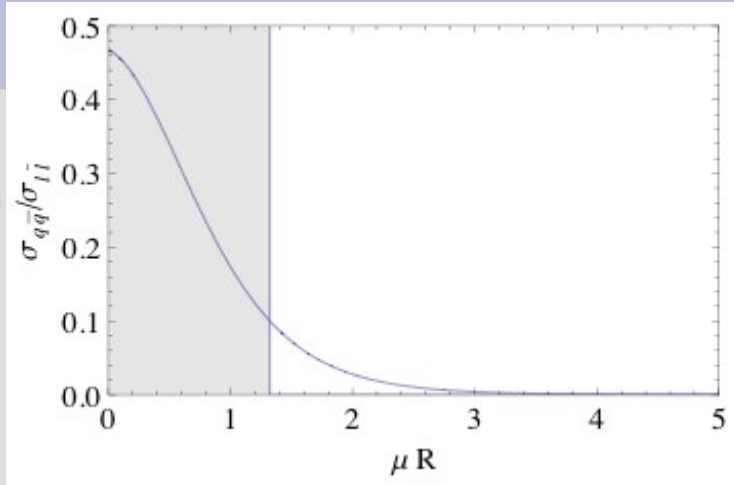


mUED : All masses of the first excited states are degenerate within  $\sim 100$  GeV

Mass differences between quark partners and others becomes  $\sim \mu$

# Fit data

With split-UED, we can reproduce data

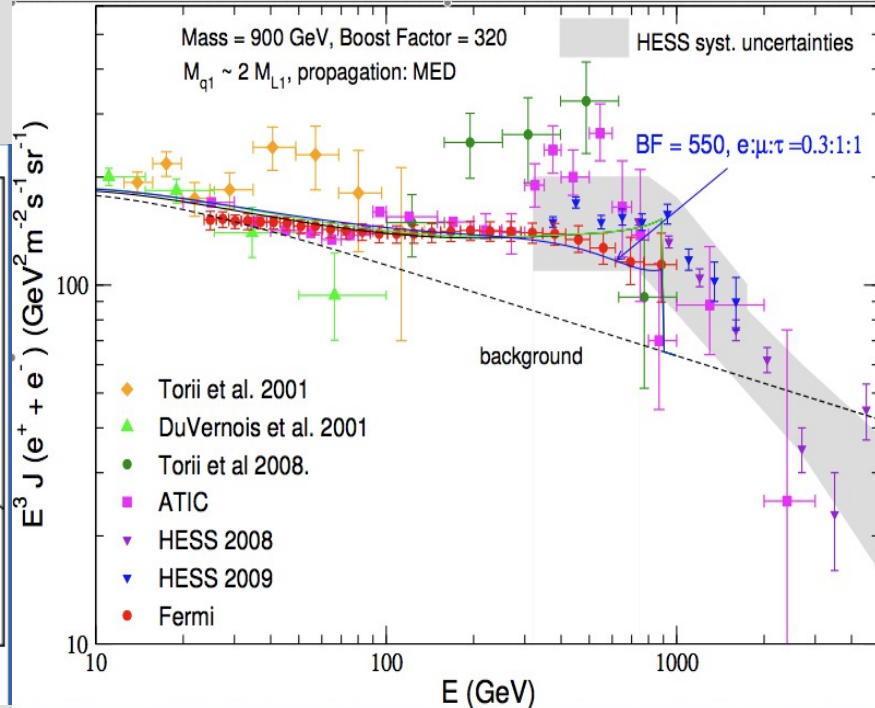
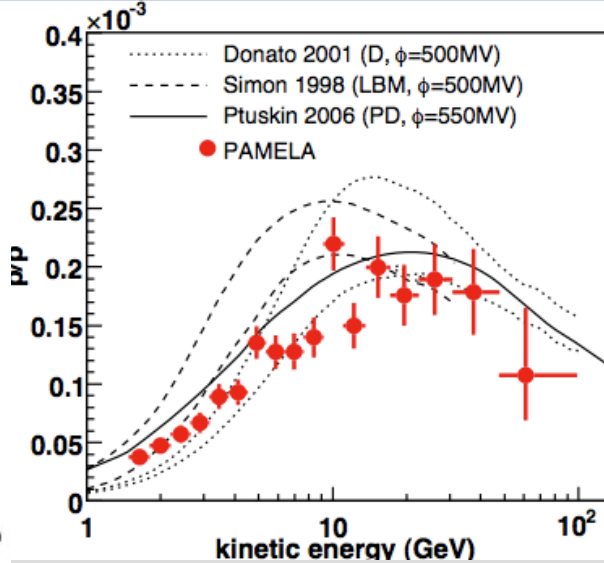
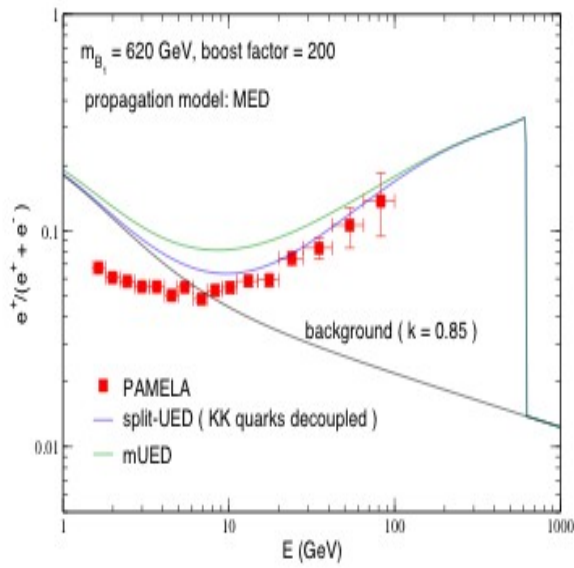


$$\mu \gtrsim \frac{1}{R} \quad \text{for p mode suppression}$$

$e^+/(e^- + e^+)$  flux

anti-p / p flux

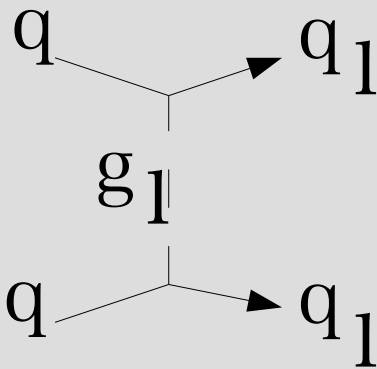
$e^+$  &  $e^-$  flux



# Collider signatures

# $q_1 q_1$ signal

- Large production cross section



Fermionic quark partner

$$\mathcal{M} \sim \frac{1}{t} \bar{u}_4 \gamma^\mu u_2 \bar{u}_3 \gamma_\mu u_1$$

Unlike SUSY (scalar)

$$\mathcal{M} \sim \frac{1}{t} \bar{v}_2 (\not{p}_3 - \not{p}_1 + m_{\tilde{g}}) u_1$$

M.M. Nojiri, M.T. PRD76:015009,2007

No p-wave suppression

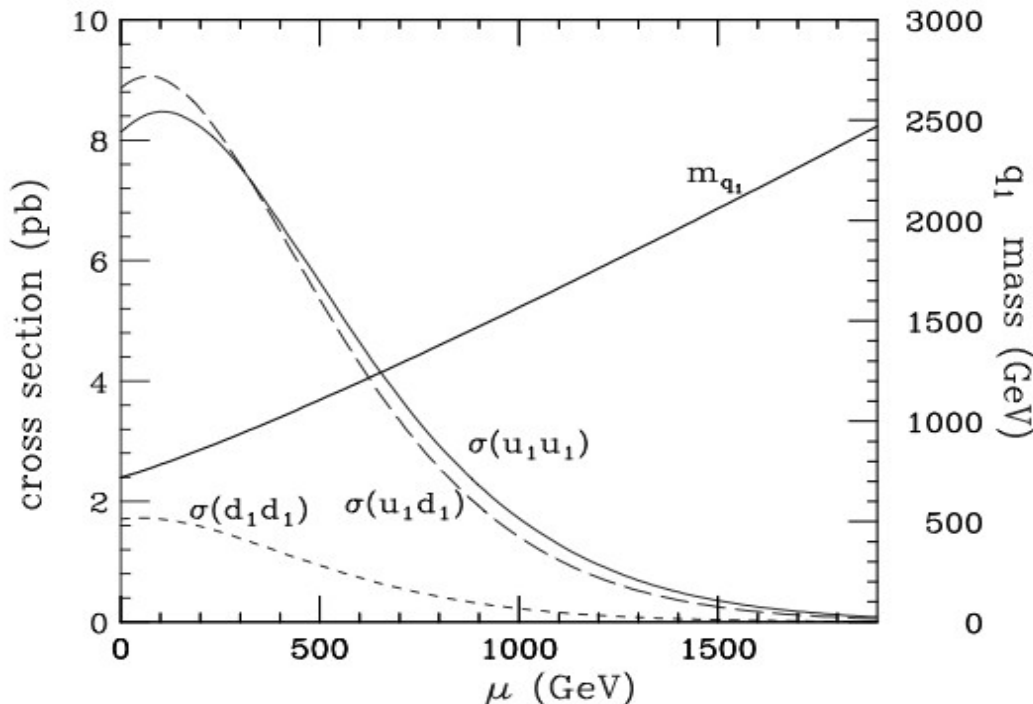
Threshold behavior  $\sim \beta^3 \rightarrow \beta$

$\rightarrow$  10 ~ 100 times larger for the same masses

$q_1 q_1$  7.64 pb

$\tilde{q}\tilde{q}$  125 fb

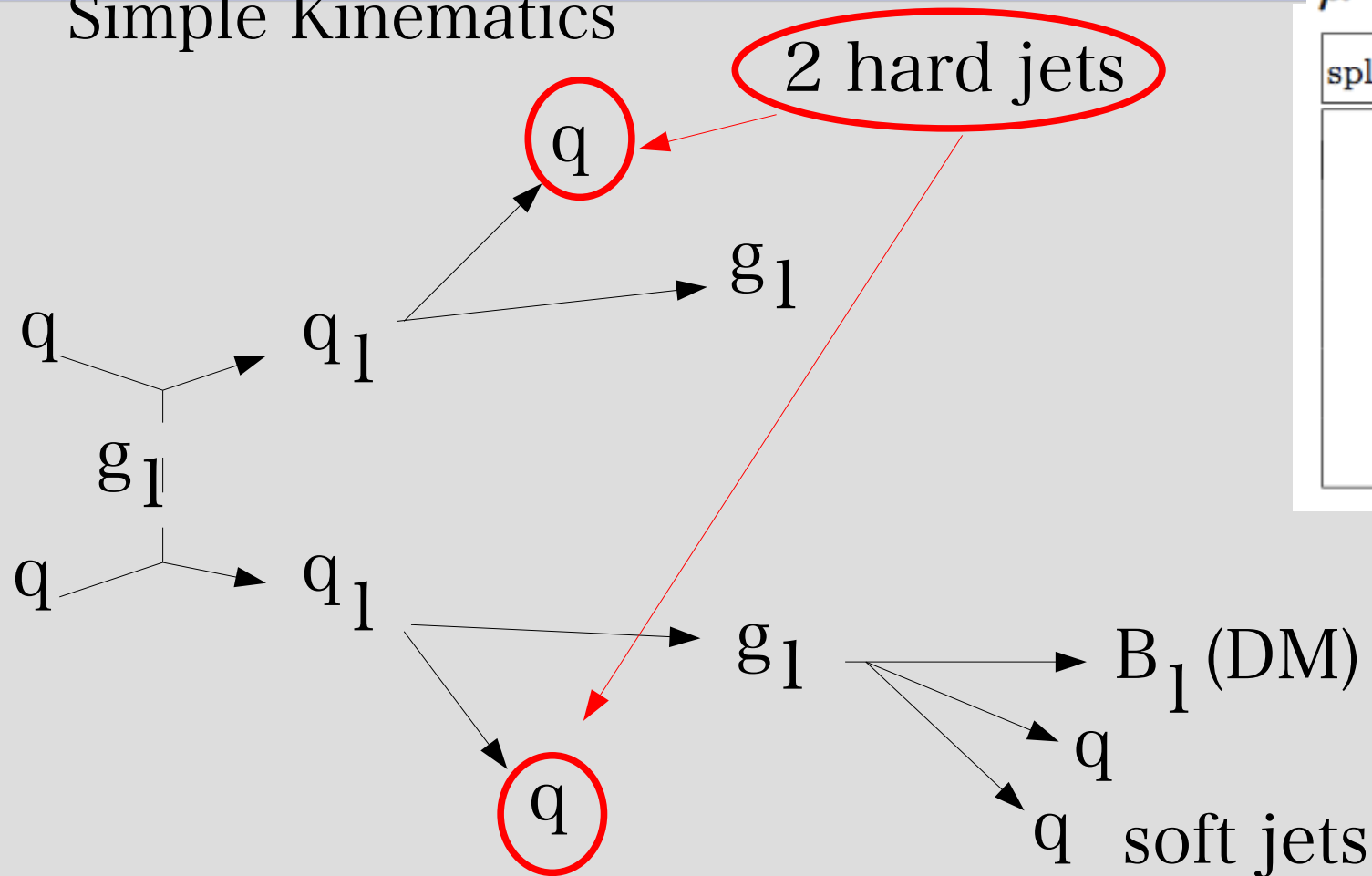
$\rightarrow$  60 times larger



# $q_1 q_1$ signal

- Large mass splitting

Simple Kinematics



$$1/R = 620 \text{ GeV}$$

$$\mu = 700 \text{ GeV}$$

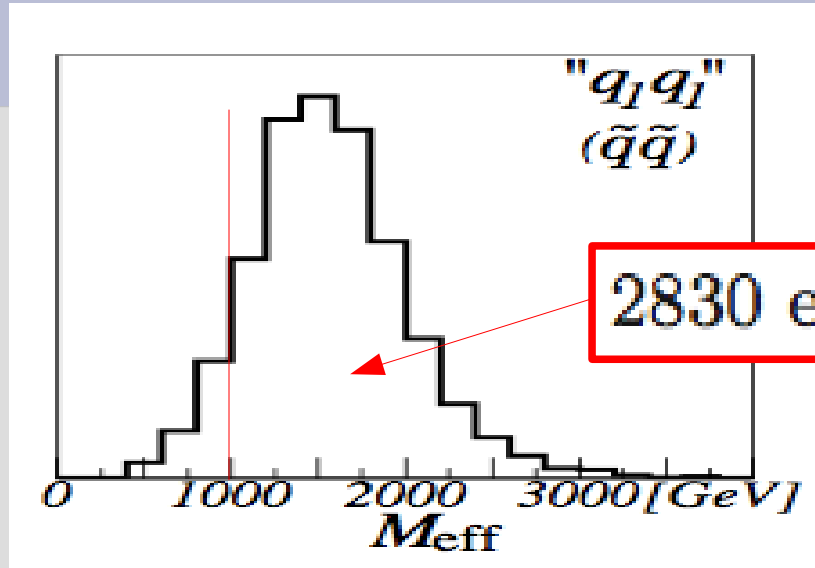
split-UED	mass
$q_{L1}$	1347 GeV
$u_{R1}$	1322 GeV
$d_{R1}$	1318 GeV
$g_1$	794 GeV
$B_1$	621 GeV

Signal is Two hard jets + missing momentum.

# $M_{\text{eff}}$ distribution and SMBG

For  $1 \text{ fb}^{-1}$

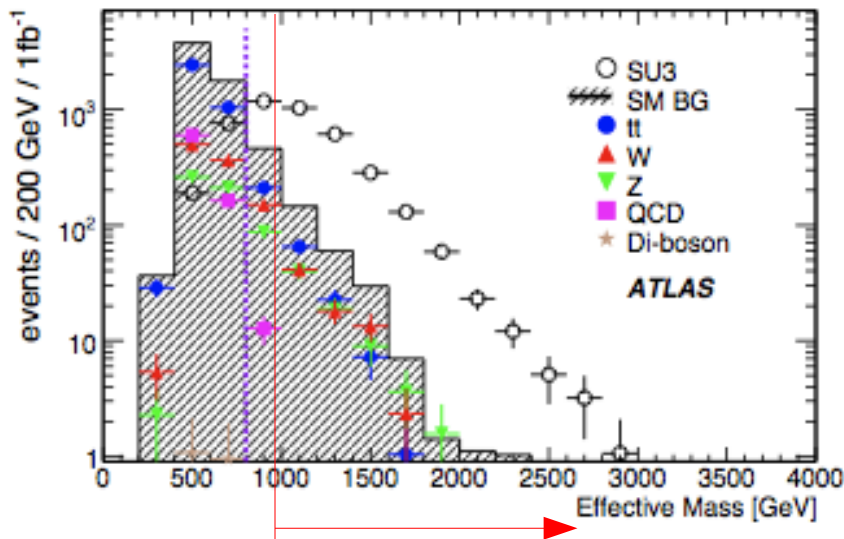
$$M_{\text{eff}} \equiv \sum_{i=1}^4 p_T^{\text{jet},i} + \sum_{i=1} p_T^{\text{lep},i} + E_T^{\text{miss}}$$



	after standard cut	$M_{\text{eff}} > 1 \text{ TeV}$
$q_1 q_1$	0.40	0.37

With lepton veto cuts,  
half of events will remain  
( $\sim 1000$  events)

From ATLAS EP note (0-lepton mode)



$\text{SMBG} < 300/1 \text{ fb}^{-1}$

$\text{Signal} > 1000/1 \text{ fb}^{-1}$

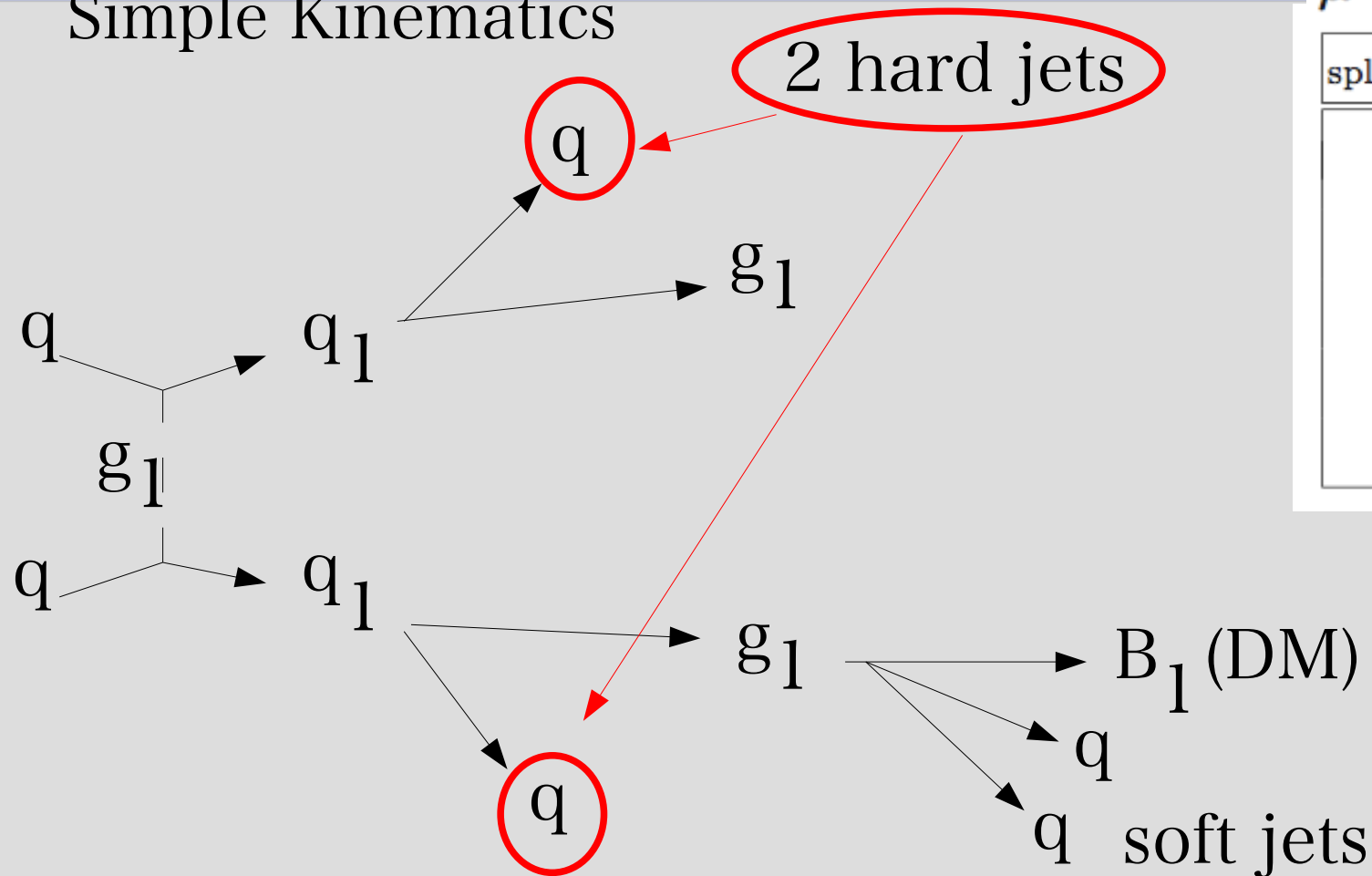
Discovery is easy!



# $q_1 q_1$ signal

- Large mass splitting

Simple Kinematics



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The same Kinematics as  $\tilde{q}_R \tilde{q}_R$  pair production  $\rightarrow$   $M_{T2}$

# M<sub>T2</sub>

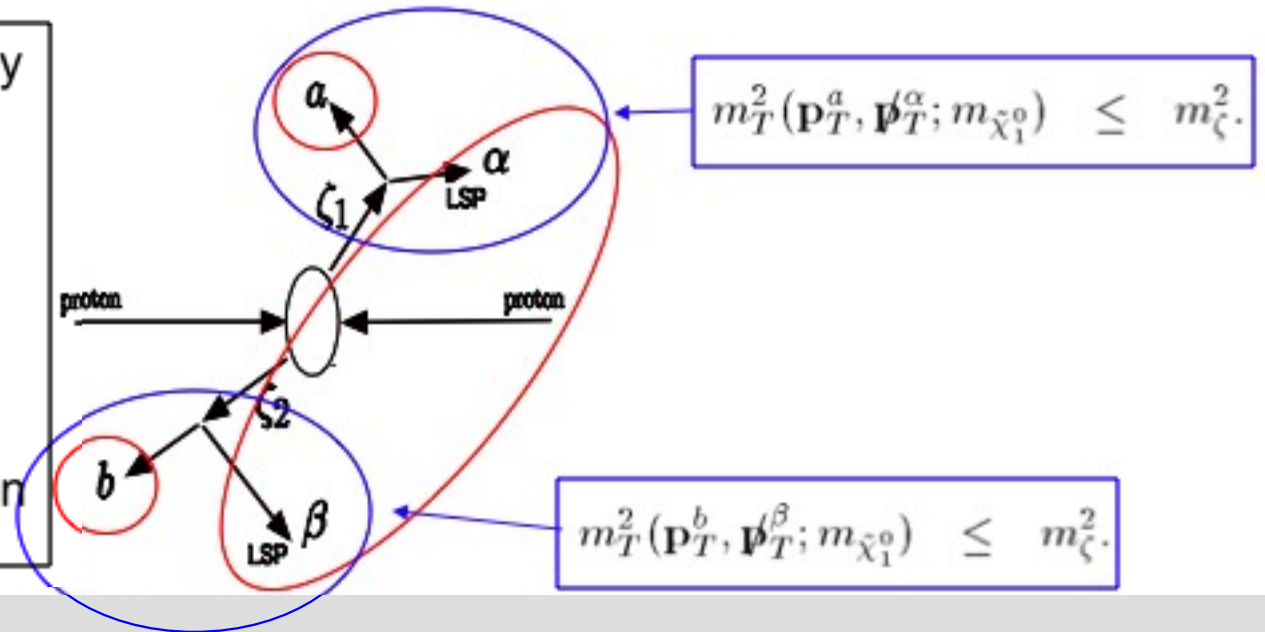
A. Barr, C. Lester, P. Stephens

1. Consider all possible way of separation

$$\mathbf{E}_T = \mathbf{p}_T^{\alpha} + \mathbf{p}_T^{\beta}$$

2. Calculate two  $m_T$  and take larger one

3. Minimize in the separation



$$m_{T2}^2(\mathbf{p}_T^a, \mathbf{p}_T^b, \mathbf{p}_T; m_{\tilde{\chi}_1^0}) \equiv \min_{\mathbf{p}_T^{\alpha} + \mathbf{p}_T^{\beta} = \mathbf{p}_T} \left[ \max \left\{ m_T^2(\mathbf{p}_T^a, \mathbf{p}_T^{\alpha}; m_{\tilde{\chi}_1^0}), m_T^2(\mathbf{p}_T^b, \mathbf{p}_T^{\beta}; m_{\tilde{\chi}_1^0}) \right\} \right] \leq m_{\zeta}^2$$

Defined with two momenta and Missing transverse momentum

The endpoint gives mother particle mass

# M<sub>T2</sub>

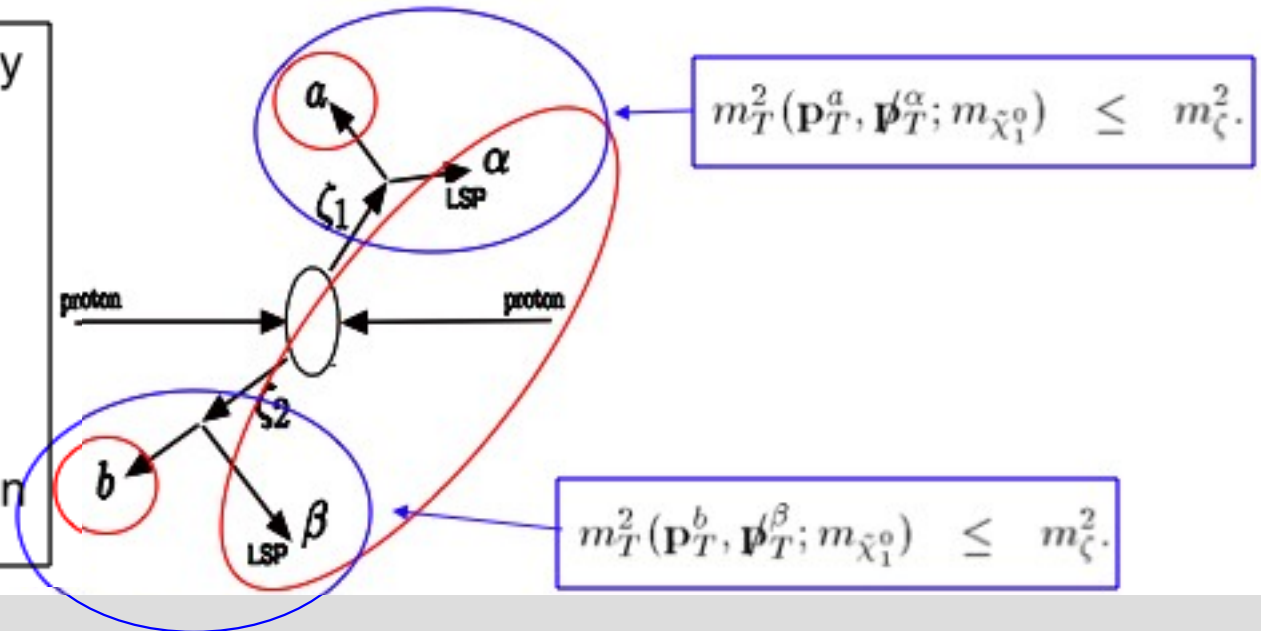
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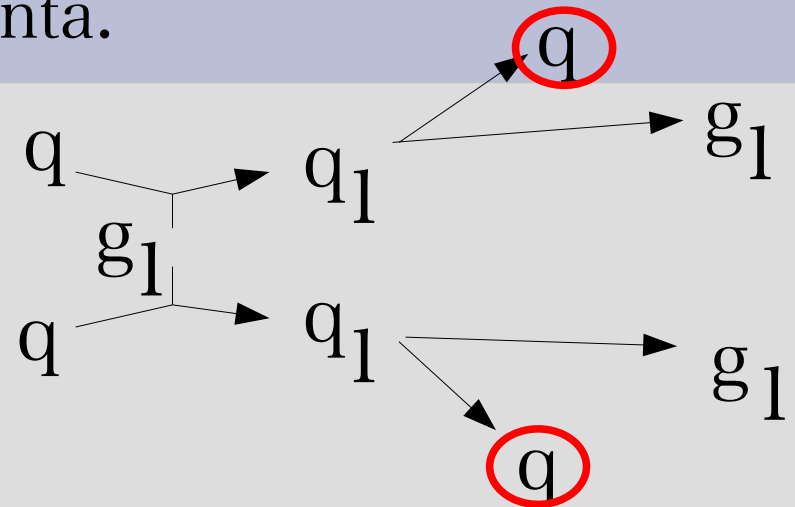
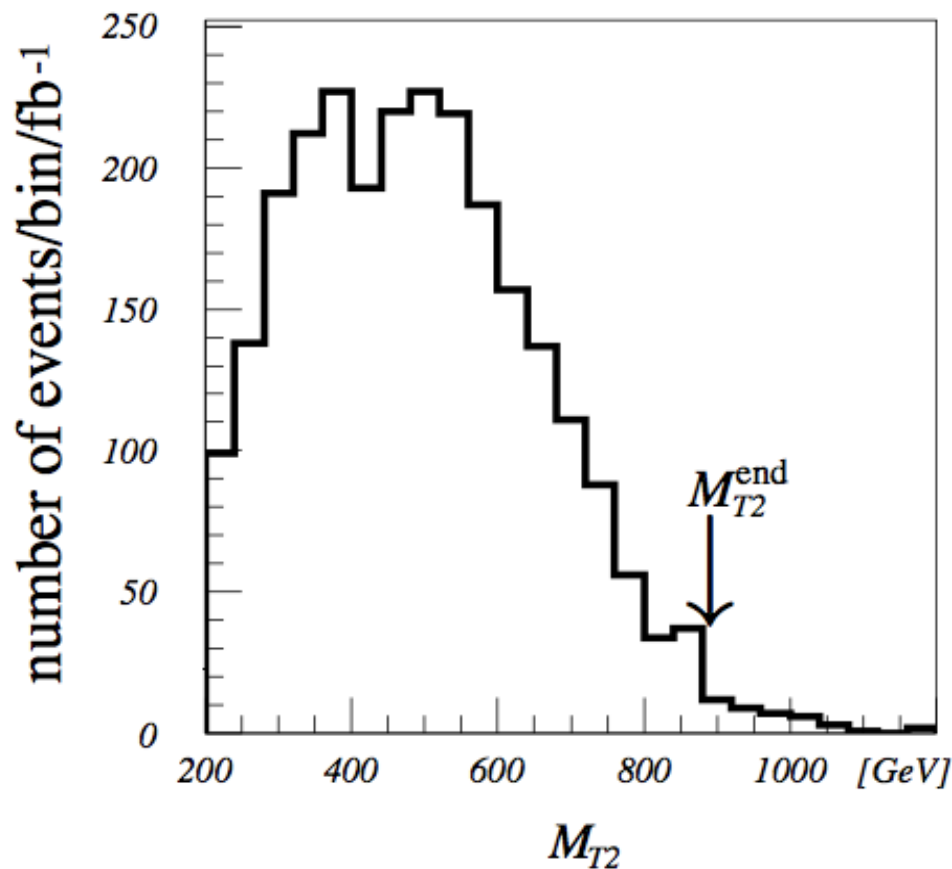
In case DM mass is unknown  
Set test mass to be 0 gives

$$M_{T2}^{\text{end}} = m_A - \frac{m_X^2}{m_A}, \quad (\text{No ISR limit})$$

# $M_{T2}$ distribution

Two highest pt jets for visible momenta.

$$p_{T\text{miss}} = -p_{Tj_1} - p_{Tj_2}$$



$M_{T2}$  endpoint is given by

$$M_{T2}^{\text{end}} = m_A - \frac{m_X^2}{m_A},$$

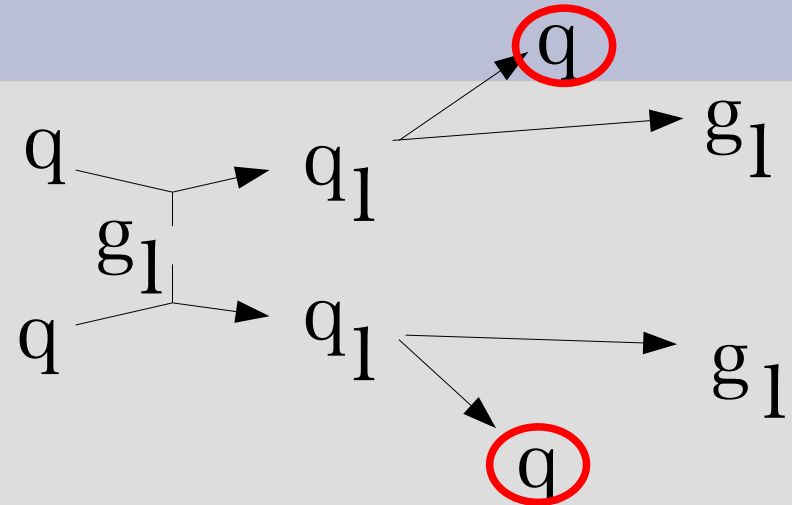
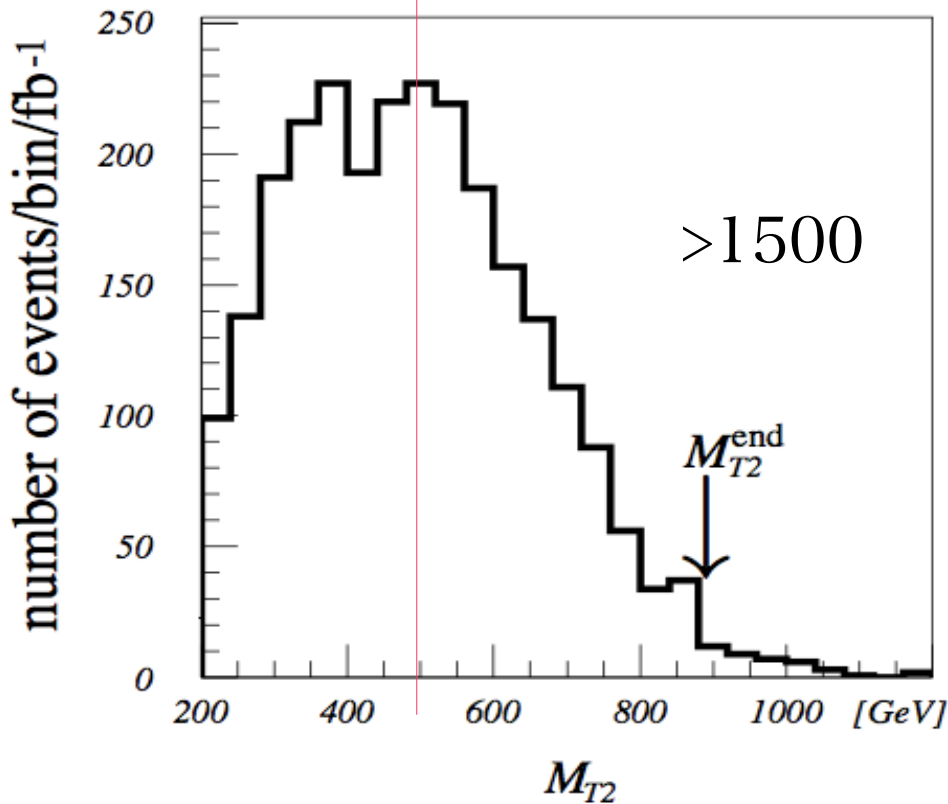
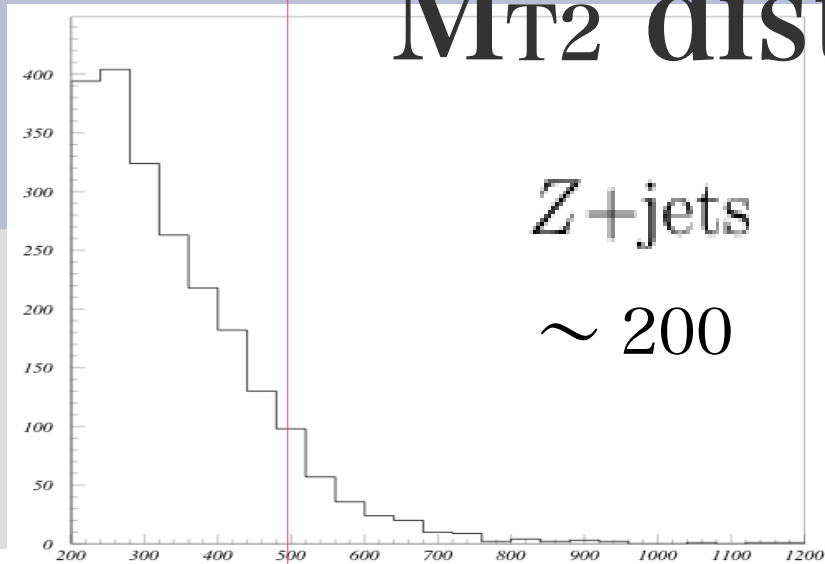
which is

$$m_{q_1} - \frac{m_{g_1}^2}{m_{q_1}} \simeq 880 \text{ GeV}.$$

# Summary

- $e^+ e^-$  flux observations
  - ➔ DM annihilation dominated by leptonic modes
  - ➔ Split-UED with heavy quark partner
- Large cross section (fermion partner)
- Easy to detect because of simple decay kinematics
- $q_1$  mass measurement using  $M_{T2}$

# $M_{T2}$ distribution



$M_{T2}$  endpoint is given by

$$M_{T2}^{\text{end}} = m_A - \frac{m_X^2}{m_A},$$

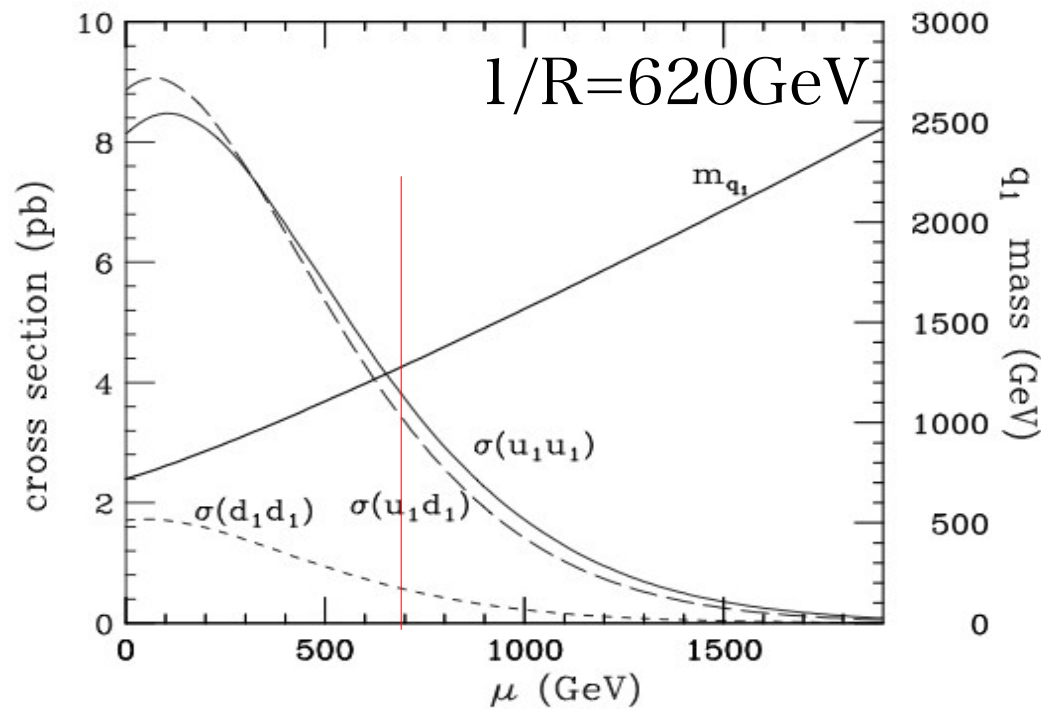
which is

$$m_{q1} - \frac{m_{g1}^2}{m_{q1}} \simeq 880 \text{ GeV.}$$

SM back ground:

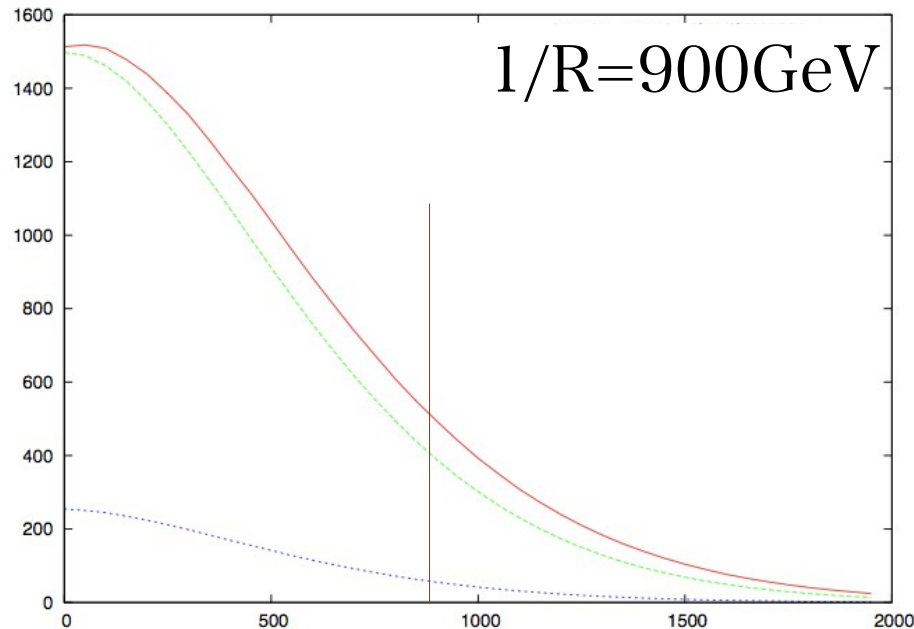
Z+jets events give smaller  $M_{T2}$

# Effects by increasing masses



SMBG  $< 300/1 \text{ fb}^{-1}$

Signal  $> 1000/1 \text{ fb}^{-1}$



Cross section becomes  $\sim 1/10$   
for  $\mu = 900 \text{ GeV}$  (mass  $\sim 2 \text{ TeV}$ )

Signal  $\sim 100/1 \text{ fb}^{-1}$

Even detectable and MT2 endpoint  
will be measurable.

# $S^1/Z_2$ Orbifolding

Consider the parity transformation in  $y$ :  $x^M = (x^\mu, y) \rightarrow x'^M = (x^\mu, -y)$ .

The parity transformation for the fermion fields is defined as

$$\Psi'(x') = \eta_P \gamma^5 \Psi(x) \quad (\text{We can choose } \eta_P \text{ for each field.})$$

If we choose  $\eta_P = +1$



We obtain zero mode only for R field.

$$\Psi(x^\mu, y) = \Psi_L(x^\mu, y) + \Psi_R(x^\mu, y)$$

$$= \left\{ \frac{1}{\sqrt{2\pi R}} \cancel{\Psi_L^{(0)}(x^\mu)} + \sum_{n=1}^{\infty} \frac{1}{\sqrt{\pi R}} \cancel{\Psi_{L+}^{(n)}(x^\mu) \cos \frac{ny}{R}} + \sum_{n=1}^{\infty} \frac{1}{\sqrt{\pi R}} \Psi_{L-}^{(n)}(x^\mu) \sin \frac{ny}{R} \right\} \\ + \left\{ \frac{1}{\sqrt{2\pi R}} \Psi_R^{(0)}(x^\mu) + \sum_{n=1}^{\infty} \frac{1}{\sqrt{\pi R}} \Psi_{R+}^{(n)}(x^\mu) \cos \frac{ny}{R} + \sum_{n=1}^{\infty} \frac{1}{\sqrt{\pi R}} \cancel{\Psi_{R-}^{(n)}(x^\mu) \sin \frac{ny}{R}} \right\}$$



# $S^1/Z_2$ Orbifolding

Consider the parity transformation in  $y$ :  $x^M = (x^\mu, y) \rightarrow x'^M = (x^\mu, -y)$ .

For the fermion fields, the parity transformation is

$$\Psi'(x') = \eta_P \gamma^5 \Psi(x) \quad (\text{We can choose } \eta_P \text{ for each field.})$$

If we choose  $\eta_P = +1$



We obtain zero mode only for R field.

$$\Psi(x^\mu, y) = \Psi_L(x^\mu, y) + \Psi_R(x^\mu, y)$$

$$= \left\{ \begin{aligned} & \frac{1}{\sqrt{2\pi R}} \Psi_L^{(0)}(x^\mu) \\ & + \sum_{n=1}^{\infty} \frac{1}{\sqrt{\pi R}} \Psi_{L+}^{(n)}(x^\mu) \cos \frac{ny}{R} + \sum_{n=1}^{\infty} \frac{1}{\sqrt{\pi R}} \Psi_{L-}^{(n)}(x^\mu) \sin \frac{ny}{R} \end{aligned} \right\}$$

$$+ \left\{ \begin{aligned} & \frac{1}{\sqrt{2\pi R}} \Psi_R^{(0)}(x^\mu) \\ & + \sum_{n=1}^{\infty} \frac{1}{\sqrt{\pi R}} \Psi_{R+}^{(n)}(x^\mu) \cos \frac{ny}{R} + \sum_{n=1}^{\infty} \frac{1}{\sqrt{\pi R}} \Psi_{R-}^{(n)}(x^\mu) \sin \frac{ny}{R} \end{aligned} \right\}$$

With  $\eta_P = -1$ , we obtain zero mode only for L field.

For the SM, we choose:

$$\eta_P = +1 \quad \text{for U, D, E, N}$$

$$\eta_P = -1 \quad \text{for Q, L}$$

# LHC Physics

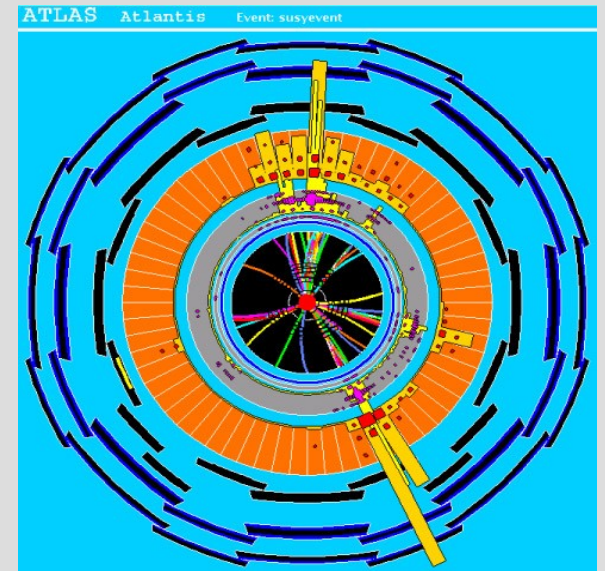
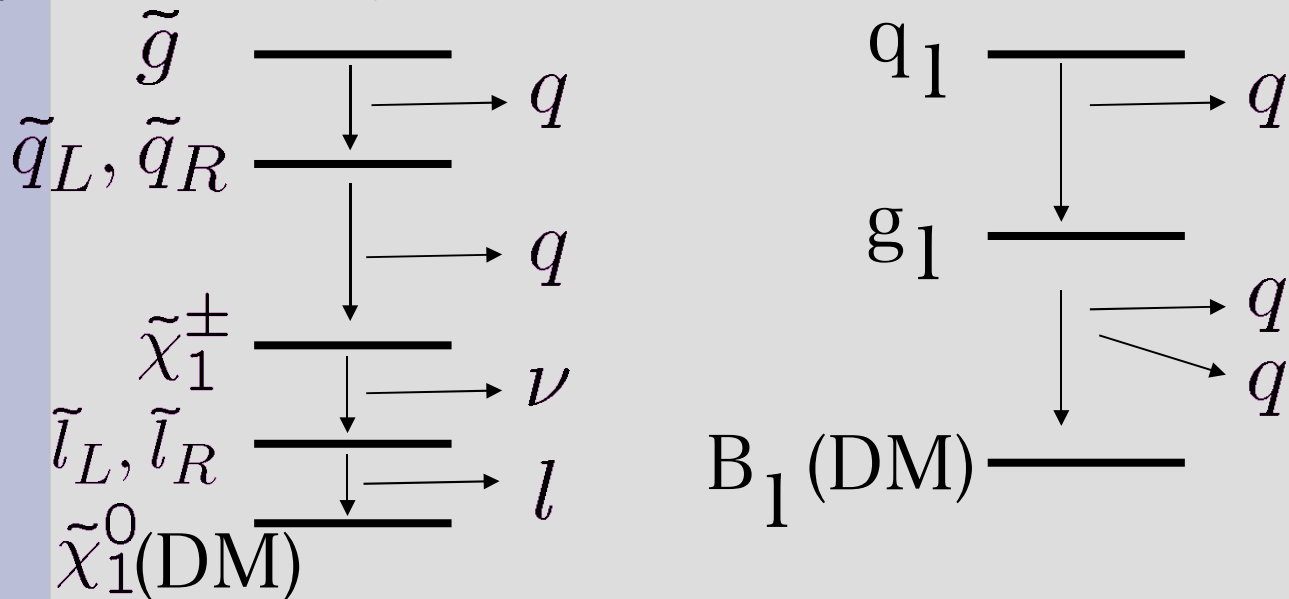
LHC: proton – proton collider ( $\sqrt{s}=14\text{TeV}$ )

Proton: mixture of u, d, g, and sea quarks

➡ Colored particles are copiously produced. (SM events also are)

Z2 parity odd particles are produced in pair.

Each decays in cascade



Large missing momentum  $\cancel{E}_T \equiv \left| \sum_{\text{visible}} p_T \right|$

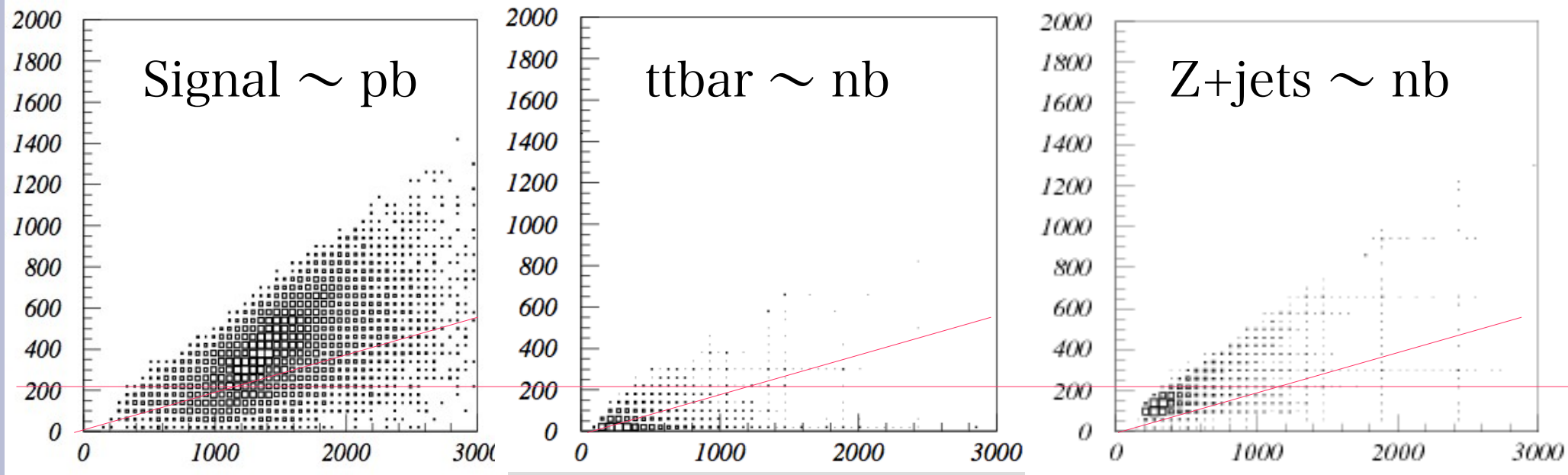
Many hard jets, hard leptons ➡ Large

$$M_{\text{eff}} = \cancel{E}_T + p_{T,1} + p_{T,2} + p_{T,3} + p_{T,4}$$

# SM background

Using missing momentum and effective mass,

We separate Signal from SM background (ttbar, W,Z+jets, QCD)



$E_{\text{miss}} > \max(200, 0.2M_{\text{eff}})$  is commonly used cut to reduce SM events.

Large missing momentum  $E_T \equiv \left| \sum_{\text{visible}} p_T \right|$

Many hard jets, hard leptons  $\rightarrow$  Large

$$M_{\text{eff}} = E_T + p_{T,1} + p_{T,2} + p_{T,3} + p_{T,4}$$

# Event simulation and selection cuts

split-UED	mass	SUSY	mass
$q_{L1}$	1347 GeV	$\tilde{u}_L, \tilde{d}_L$	1355, 1358 GeV
$u_{R1}$	1322 GeV	$\tilde{u}_R$	1304 GeV
$d_{R1}$	1318 GeV	$\tilde{d}_R$	1263 GeV
$g_1$	794 GeV	$\tilde{g}$	799 GeV
$B_1$	621 GeV	$\tilde{\chi}_1^0$	622 GeV

Mimic Split-UED using MSSM point and generate events using HERWIG. (Kinematics is almost the same)

- Selection cuts are from ATLAS EP note (0-lepton mode)

1. At least four jets with  $p_T > 50$  GeV at least one of which must have  $p_T > 100$  GeV; and  $E_T^{\text{miss}} > 100$  GeV.
2.  $E_T^{\text{miss}} > 0.2M_{\text{eff}}$ .
3. Transverse sphericity,  $S_T > 0.2$ .
4.  $\Delta\phi(\text{jet}_1 - E_T^{\text{miss}}) > 0.2, \Delta\phi(\text{jet}_2 - E_T^{\text{miss}}) > 0.2, \Delta\phi(\text{jet}_3 - E_T^{\text{miss}}) > 0.2$ .
5. Reject events with an  $e$  or a  $\mu$ .