

# Interplay between $\Delta M_s$ and flavour anomalies



Matthew Kirk

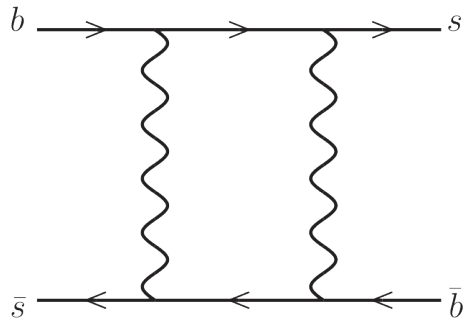
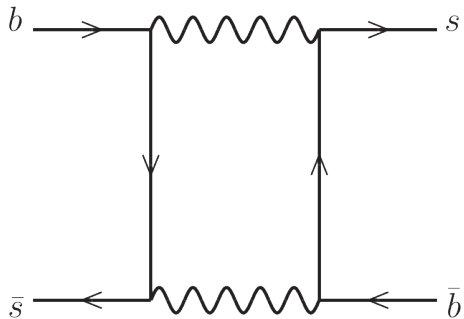


SAPIENZA  
UNIVERSITÀ DI ROMA

(based on 1909.xxxxx – Di Luzio, MK, Lenz, Rauh)

bsll 2019 – Lyon

# Overview of $\Delta M_s$



$$\frac{\partial}{\partial t} \begin{pmatrix} B_s \\ \bar{B}_s \end{pmatrix} = \left( \hat{M} - \frac{i}{2} \hat{\Gamma} \right) \begin{pmatrix} B_s \\ \bar{B}_s \end{pmatrix}$$

# Overview of $\Delta M_S$

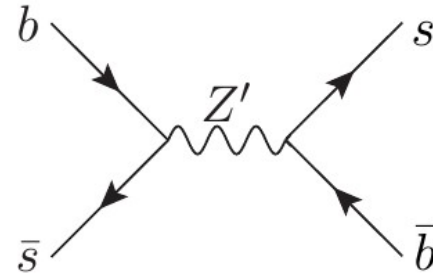
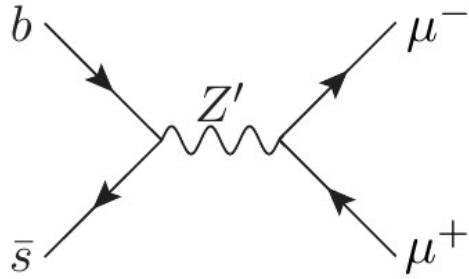
- $\Delta M_S \equiv M_{B_H} - M_{B_L}$
- Calculated as  $2|M_{12}|$
- $M_{12}^q = \frac{G_F^2}{16\pi^2} \lambda_t^2 M_W^2 S_0(x_t) \hat{\eta}_B \frac{\langle \bar{B}_q | Q_1 | B_q \rangle}{2M_{B_q}}$
- The matrix element  $\langle \bar{B}_q | Q_1 | B_q \rangle$  is generally parameterised as  $f_B^2 B_Q$ , and this is the largest uncertainty.

# Linking $R_{K^*}$ and $\Delta M_s$

- There is a generic connection between the two observables for explanations of  $R_{K^*}$  (e.g.  $Z'$ , LQs)
- $Z'$ : two insertions of  $bs$  coupling
- LQ: 1-loop box diagram

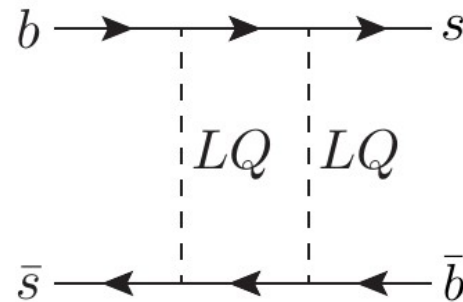
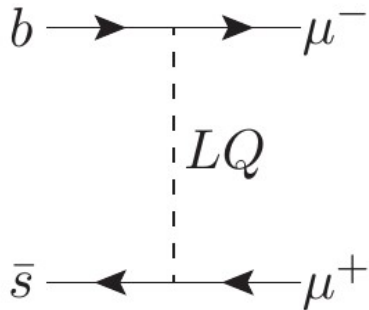
# Linking $R_{K^*}$ and $\Delta M_S$

- The observed  $R_{K^*}$



two  
is of

- $Z'$ :



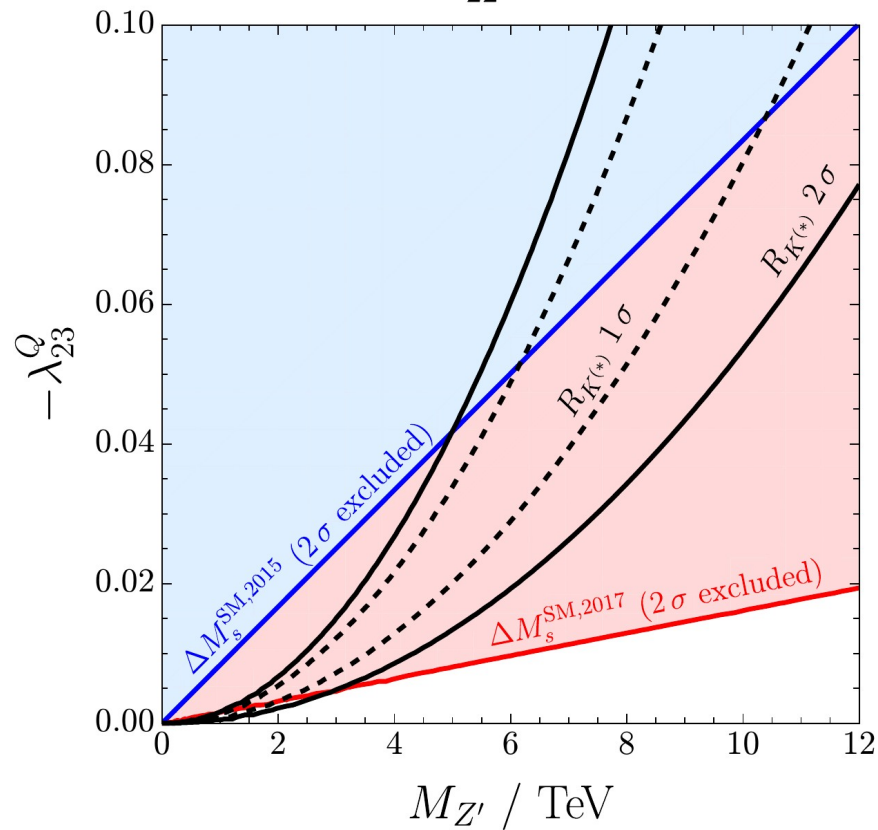
- LC

# Status of $\Delta M_s$

- Exp:  $(17.757 \pm 0.021) \text{ps}^{-1}$
- SM (FLAG '13):  $(18.3 \pm 2.7) \text{ps}^{-1}$  (from 1511.09466)
- SM (FNAL/MILC):  $(20.01 \pm 1.25) \text{ps}^{-1}$
- Discussion in "One Constraint to Kill Them All"  
(1712.06572)

# Status of $\Delta M_S$

$$\lambda_{22}^L = 1$$



# What has happened since?

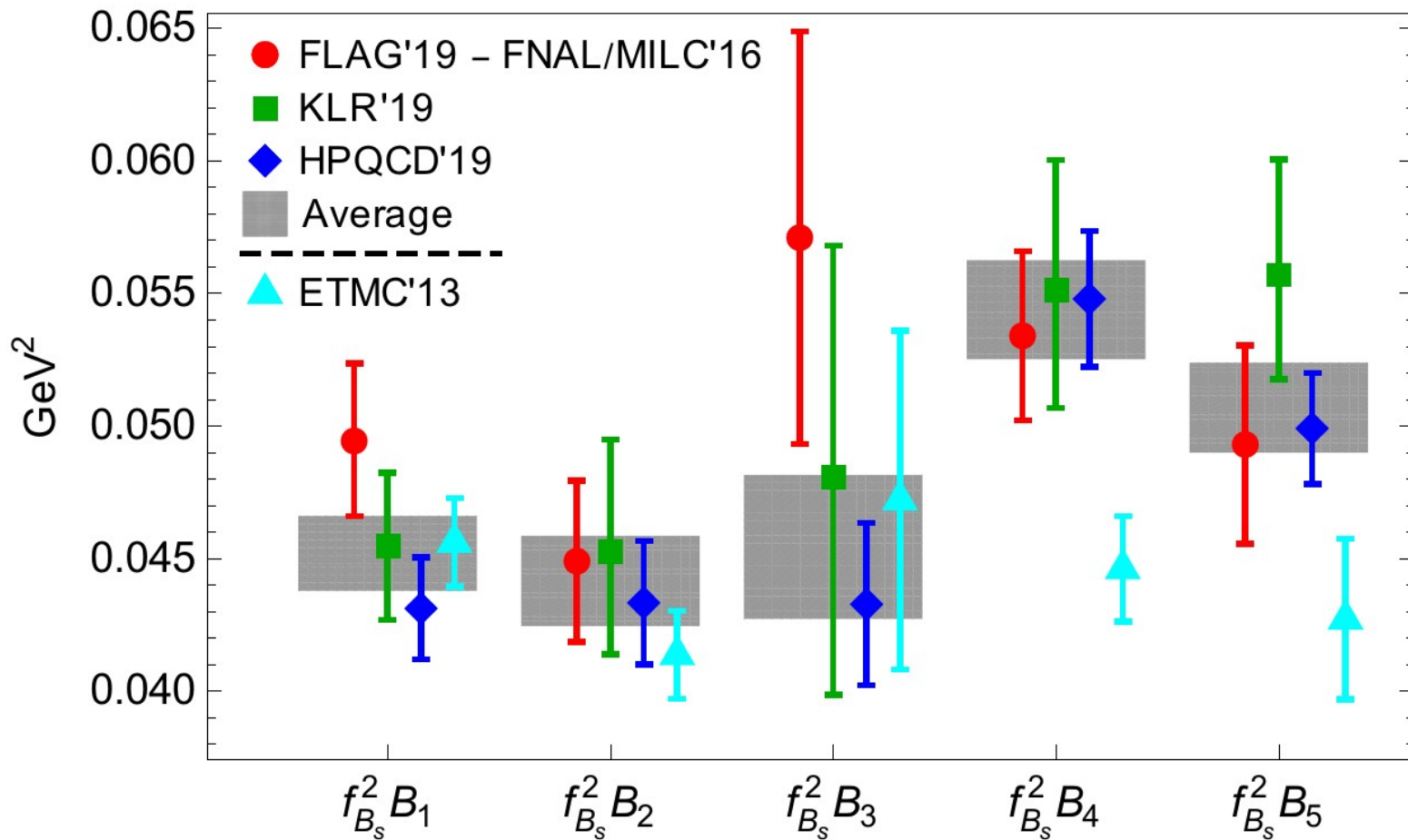
- Moriond 2019:  $R_K: 0.75 \pm 0.12 \rightarrow 0.85 \pm 0.06$
- Still  $\sim 2.5 \sigma$
- Currently  $R_{K^*} < R_K < 1$
- Favours RH quark currents



# New for $\Delta M_s$

- Sum rules calculation of  $B_s$  bag parameters (1904.00940 – King, Lenz, Rauh) – based on 1711.02100 (MK, Lenz, Rauh) and 1606.06054 (Seigen)
- HPQCD calculation of  $B_s$  bag parameters (1907.01025)

# New for $\Delta M_s$



# New for $\Delta M_s$

- Also slight updates to CKM fits
  - Between CKMfitter 2016 and 2018 results, error on  $V_{cb}$  roughly doubled

# Update of $\Delta M_s$

- Using FLAG '19 ( $\approx$  FNAL/MILC)

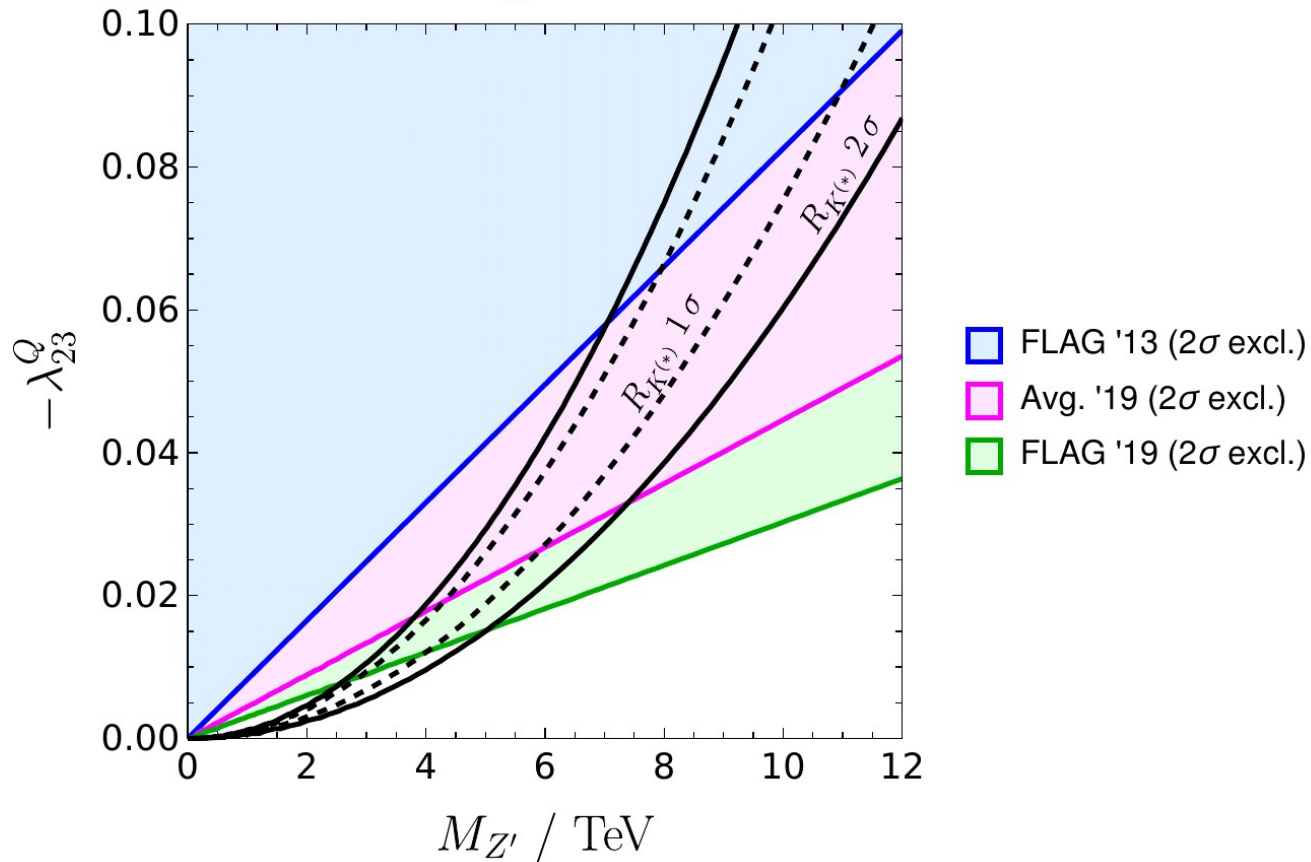
- $\Delta M_s^{\text{FLAG '19}} = (20.1_{-1.6}^{+1.2}) \text{ps}^{-1}$

- Using average of FNAL/MILC, HPQCD, KLR SR

- $\Delta M_s^{\text{Avg. '19}} = (18.4_{-1.2}^{+0.7}) \text{ps}^{-1}$

# Update of $\Delta M_S$

$$\lambda_{22}^L = 1$$



# Bounds on $Z'$ mass

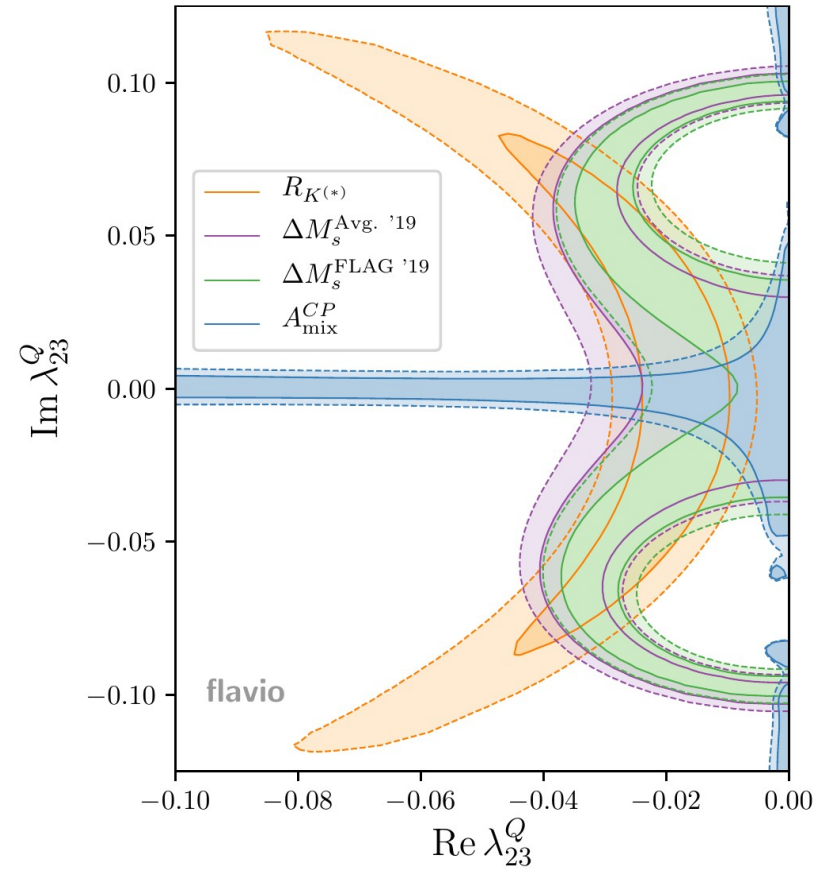
- $\Delta M_s$  rules out (at  $2\sigma$ )  $Z'$  above 5 TeV in the simplest case (only LH quark and lepton coupling, no new phases, lepton coupling = 1)
- What if we relax these restrictions?

# Complex coupling

- $\Delta M_s \sim \Delta M_s^{\text{SM}} \left| 1 + g_{\text{NP}}^2 \right|$
- So new CP violating phases allow for negative contribution

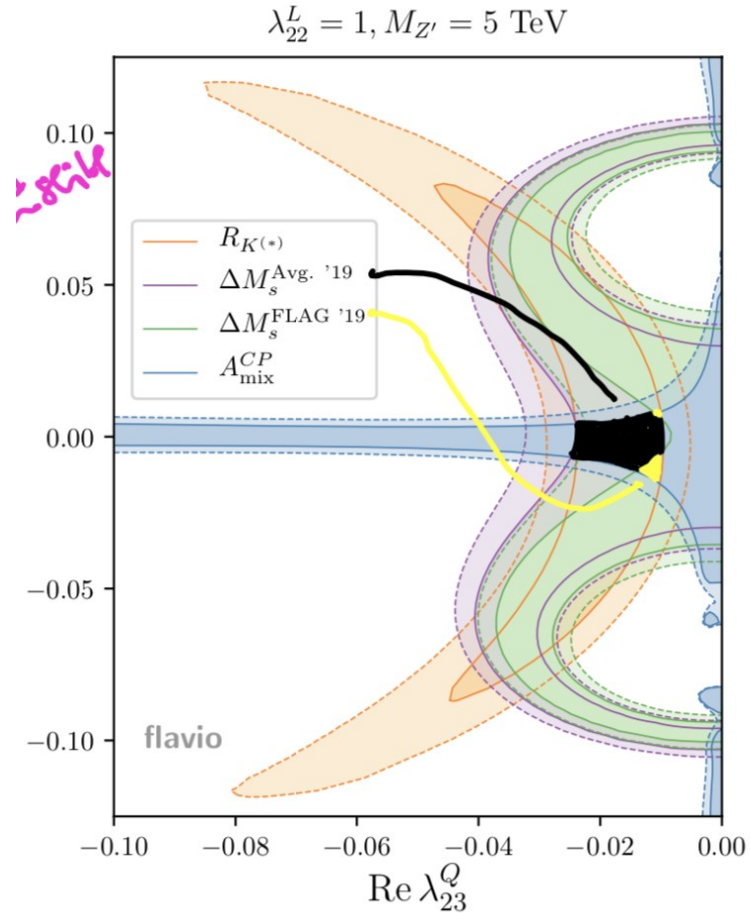
# Complex coupling

$$\lambda_{22}^L = 1, M_{Z'} = 5 \text{ TeV}$$





# Complex coupling



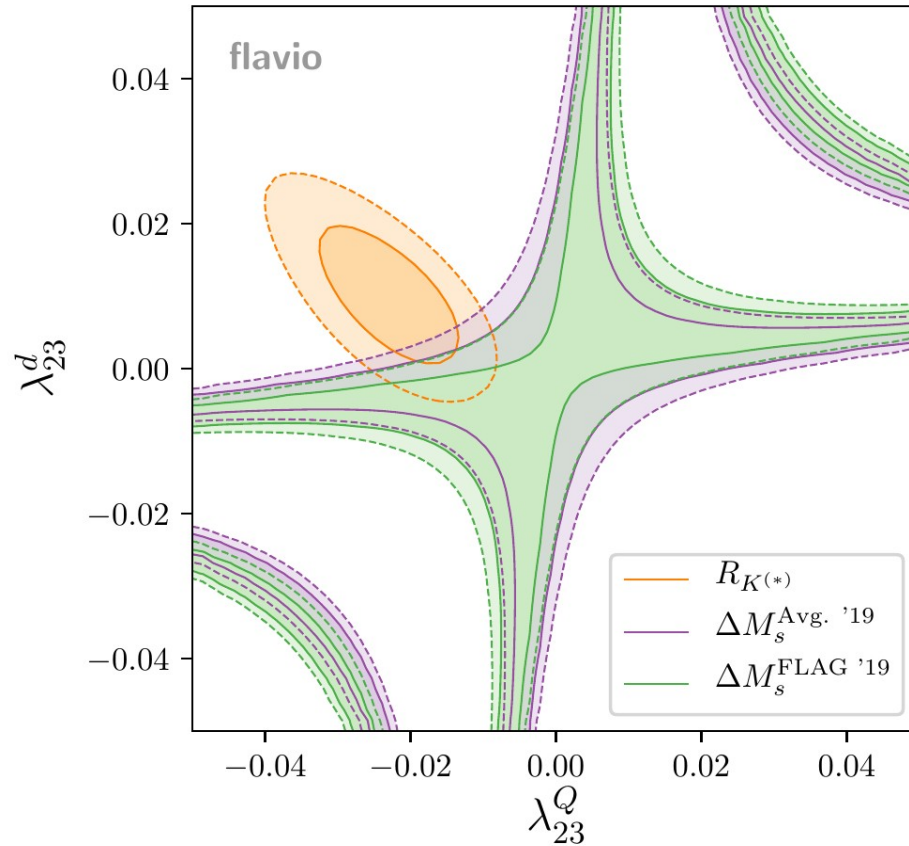
# RH quark coupling

- Get interference term with opposite sign

$$\frac{\Delta M_s^{\text{SM+NP}}}{\Delta M_s^{\text{SM}}} \approx \left| 1 + 200 \left( \frac{5 \text{ TeV}}{M_{Z'}} \right)^2 \left[ (\lambda_{23}^Q)^2 + (\lambda_{23}^d)^2 - 9\lambda_{23}^Q \lambda_{23}^d \right] \right|$$

# RH quark coupling

$$\lambda_{22}^L = 1, M_{Z'} = 5 \text{ TeV}$$



# Look to the future

- By 2025, LHCb expects to have much better precision on  $R_K$  (down to 0.025) and  $R_{K^*}$  (down to 0.031)
- Implies  $6\sigma$  in  $R_K$ ,  $10\sigma$  in  $R_{K^*}$

# World of 2025

- What will  $\Delta M_s$  look like?
- Take matrix element forecasts from LHCb Upgrade II report (1808.08865)
  - Lattice error on matrix element down to 3%
  - We also assume a similar improvement in sum rules
  - Combination at 2%

# World of 2025

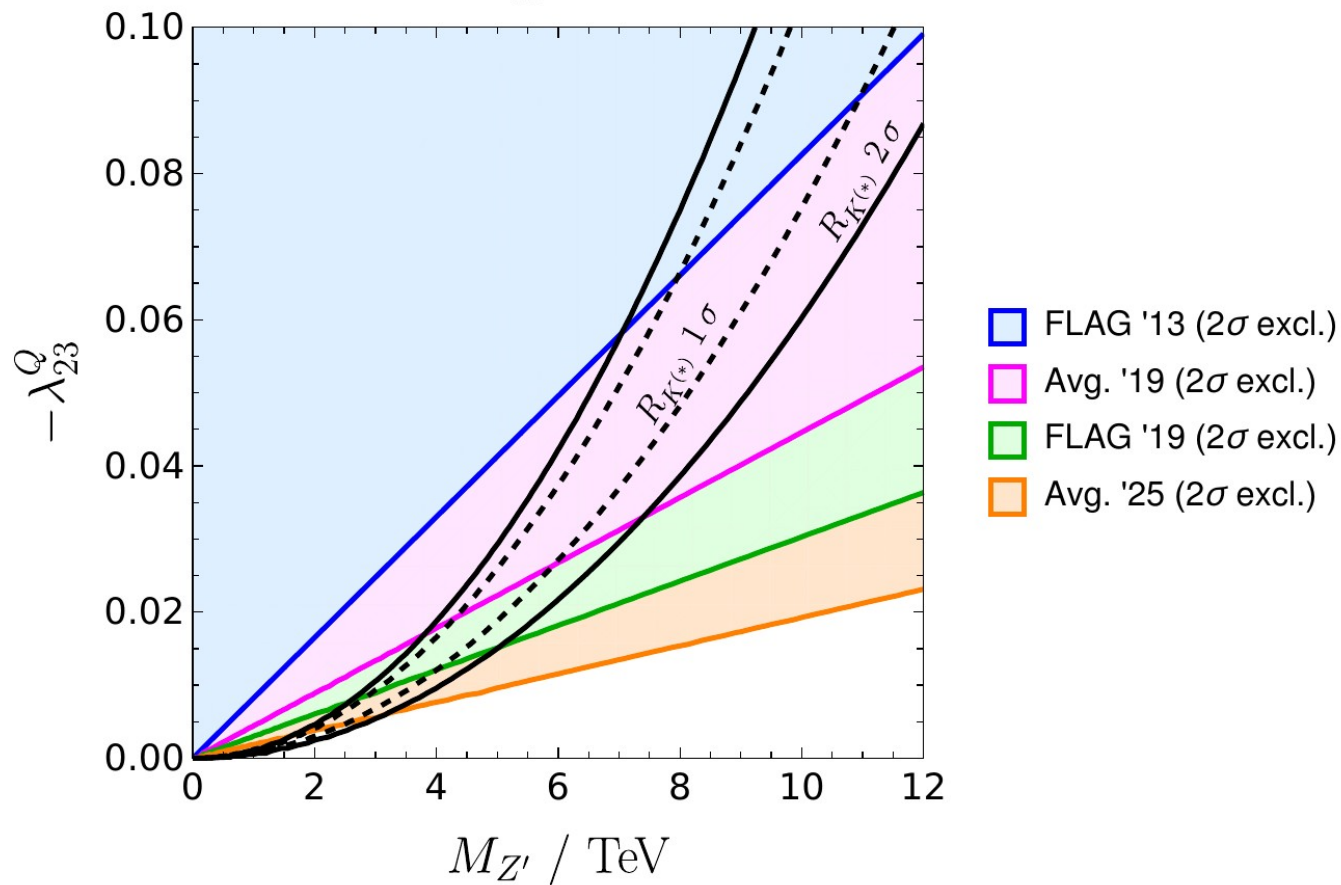
- What will  $\Delta M_s$  look like?
- Take  $V_{cb}$  from Belle II physics book (1808.10567)
- 1% uncertainty (vs ~3% today)
- Everything else the same

# World of 2025

- What will  $\Delta M_s$  look like?
- We expect that the error on  $\Delta M_s$  can be reduced to  $\pm 0.5 \text{ ps}^{-1}$

# World of 2025

$$\lambda_{22}^L = 1$$





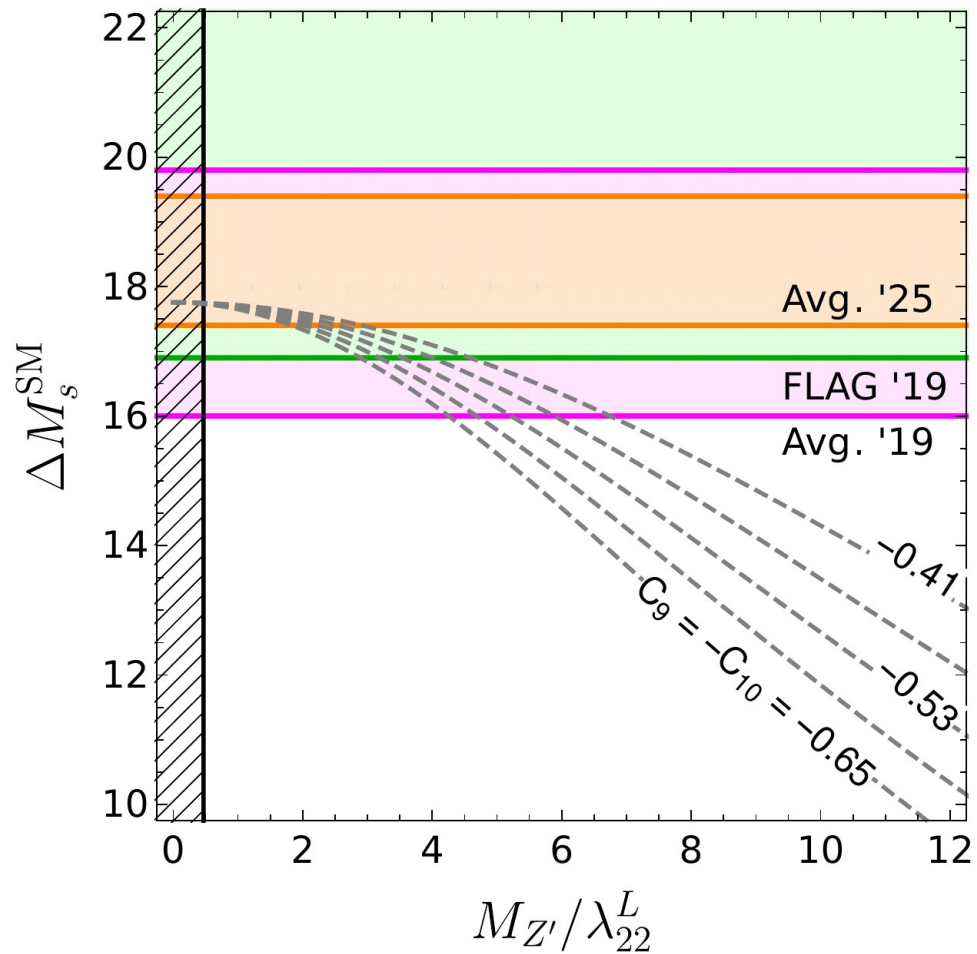
# World of 2025

- Lower central value corresponding to current average, with higher precision, is MORE constraining than the FNAL/MILC result is now.
- Entering the age of precision for  $\Delta M_s$
- And precision is what kills you (/ your models)

# Linking $R_{K^*}$ and $\Delta M_s$

- LHCb expects their data on  $R_{K^*}$  alone will be enough to fit  $C_9$  with uncertainty  $\sim 0.12$
- So what  $\Delta M_s$  value is compatible with a  $Z'$  explanation?

# Linking $R_{K^*}$ and $\Delta M_S$



# Summary

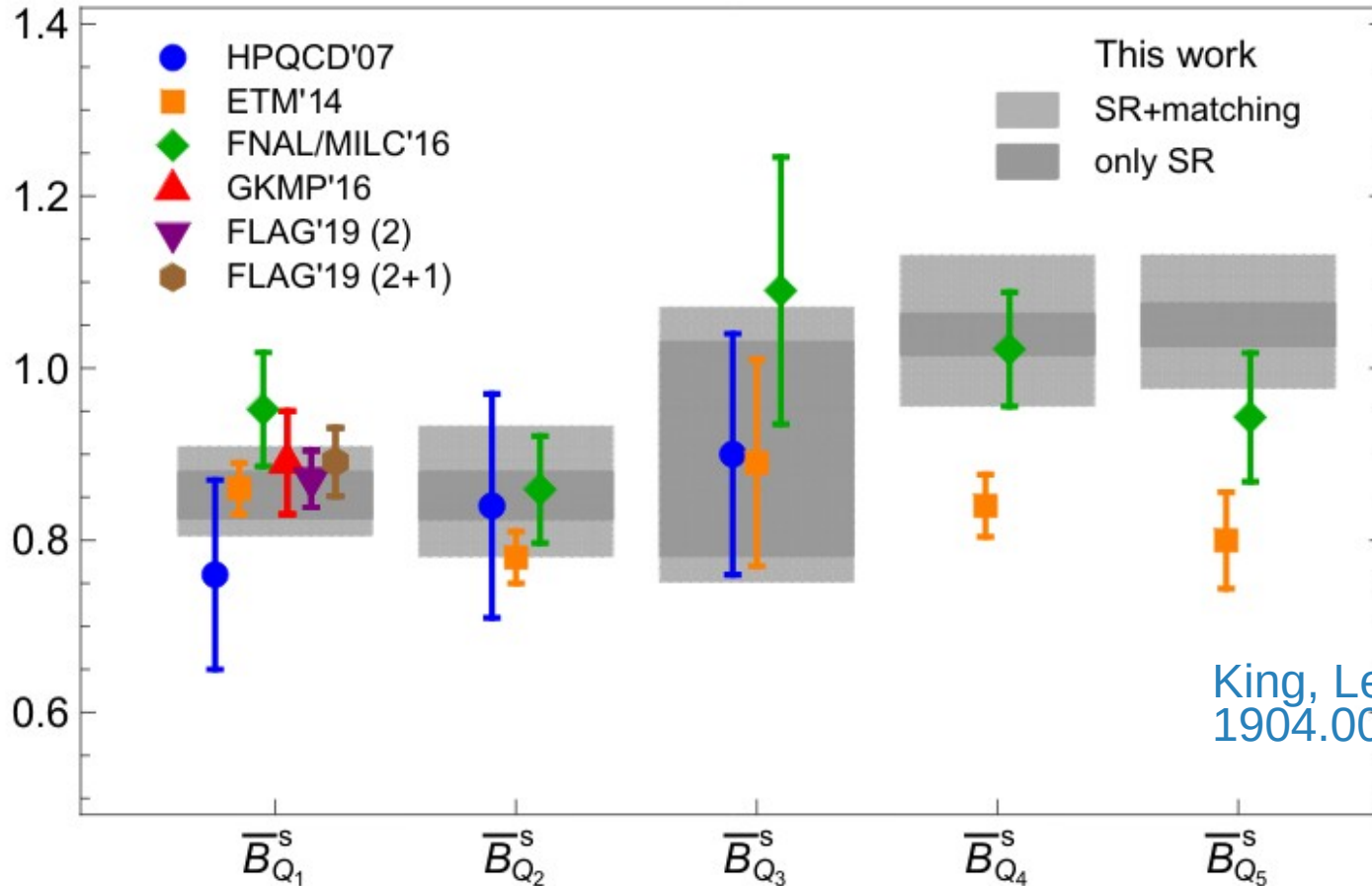
- New determinations of  $B_s$  mixing matrix elements bring us towards precision era of  $B_s$  mixing
- CP violating, or right handed quark coupling loopholes don't give a great improvement
- By 2025 precision will be good enough to exceed strong FNAL/MILC constraints from mixing

EXTRAS

# CKM inputs

- CKMfitter Summer 2018:
  - $V_{cb} = (42.40 + 0.30 - 1.15) * 10^{-3}$
- CKMfitter tree-only Summer 2018:
  - $V_{cb} = (42.41 + 0.40 - 1.50) * 10^{-3}$
- CKMlive (excluding  $\Delta M_s$  and  $\Delta M_d$  from the fit):
  - $V_{cb} = (42.40 + 0.40 - 1.17) * 10^{-3}$

# SR improvement



King, Lenz, Rauh  
1904.00940

# Neutrino trident

- $\nu \rightarrow \nu \mu^+ \mu^-$
- Assumes SU(2)<sub>L</sub> invariance of our NP, so muon coupling implies neutrino coupling too
- CCFR data on cross-section can be used to bound Z' mass / lepton coupling
- Don't expect much better from DUNE



# Linking $R_{K^*}$ and $\Delta M_s$

- $R_{K^*}$  (and other  $b \rightarrow sll$ ) anomalies require  $(\bar{s} b)(\bar{l} l)$  effective coupling.
- So even at the EFT level, expect  $(\bar{s} b)(\bar{s} b)$  coupling via lepton loop
- (But actually this is totally negligible)