

Gravitational Waves: The challenges of the detection

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- **How do ground-based interferometers work?**
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 - How to measure the GW strain $h(t)$ from this detector?
 - Noises limiting the ITF sensitivity: how to tackle them?
- **Prospectives for interferometers and other detectors**

GW quest: a bit of history

- Joseph Weber invents the bar detector
 - The GW changes the resonance condition of a resonant bar of a few tons
 - First claim for detection in 1969... but contested
 - Triggered large interest, at least 18 bars in 8 countries
- Evolve to cryogenic resonant bars (80-90)
- Bar not enough sensitivity:
 - h : few 10^{-21} $1/\sqrt{\text{Hz}}$ @ 900Hz
- ITF started in the 70's (Germany, Rai Weiss)
 - Broad band instrument
- Few ITF prototypes in the 80's
 - MIT, Glasgow, Garching, Caltech,...
 - ~10m long
 - Not made for detection
- Jump to km scale in early 90
 - LIGO, Virgo, GEO, TAMA
- **First detection in 2015 (GW150914)**



Reminder: effect of a GW on free fall masses

A gravitational wave (GW) modifies the distance between free-fall masses

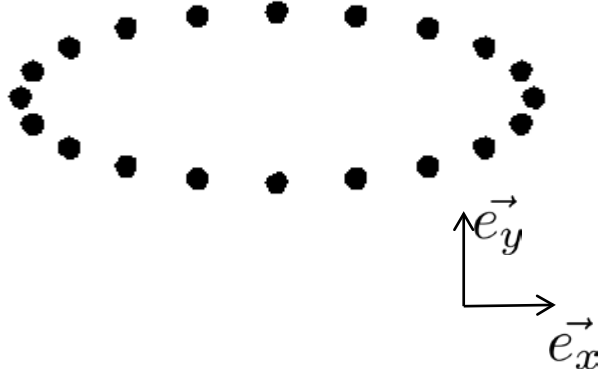


Reminder: effect of a GW on free fall masses

A gravitational wave (GW) modifies the distance between free-fall masses

$$\delta x(t) = -\delta y(t) = \frac{1}{2} h(t) L_0$$

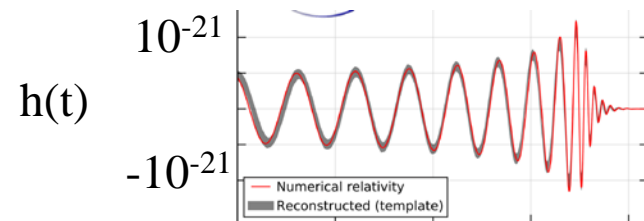
$h(t)$: amplitude of the GW (= strain)



Typical amplitude of a GW crossing the Earth:
 $h \sim 10^{-23}$
(h has no dimension/unit)

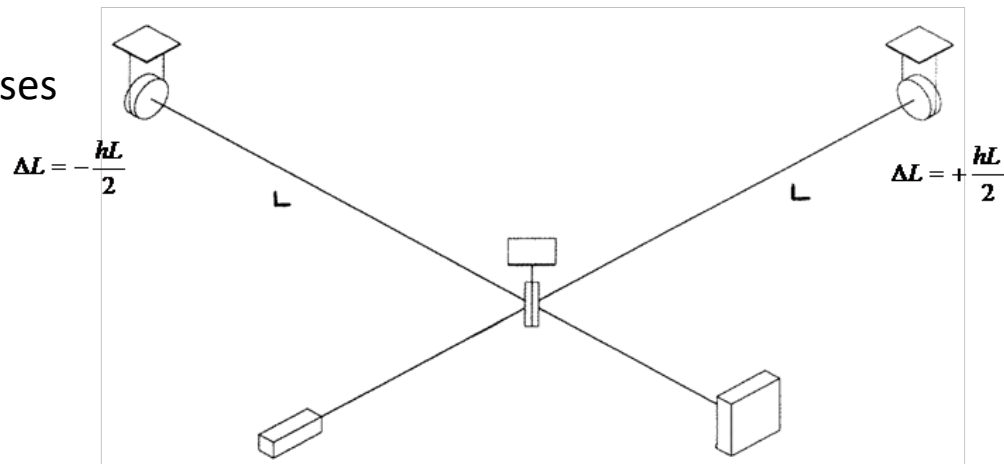
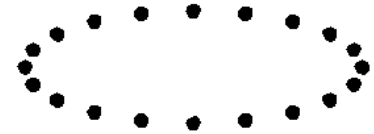
Case of a GW with polarisation + propagating along z

Reconstructed strain of GW150914



Terrestrial GW Interferometer: basic principle

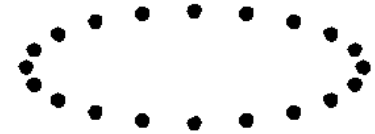
- Measure a variation of distance between masses
 - Measure the light travel time to propagate over this distance
 - Laser interferometry is an appropriate technique
 - Comparative measurement
 - Suspended mirrors = free fall test masses



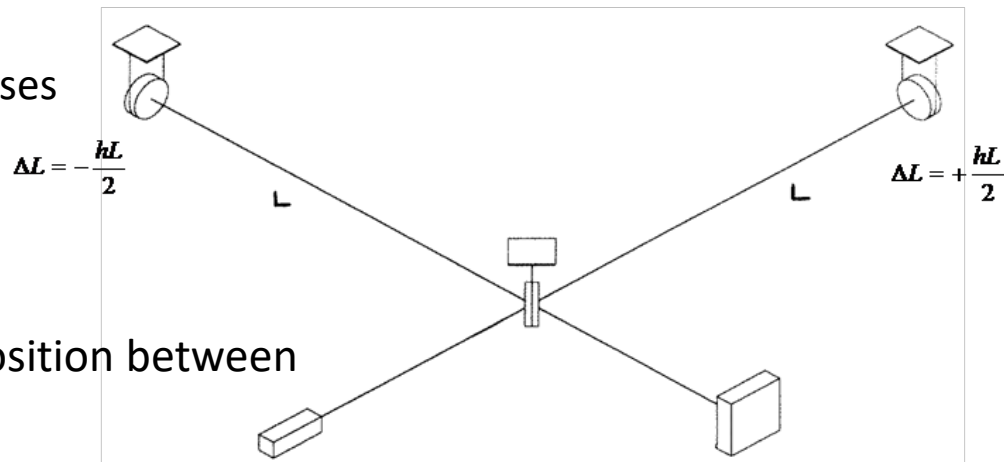
Terrestrial GW Interferometer: basic principle



Terrestrial GW Interferometer: basic principle



- Measure a variation of distance between masses
 - Measure the light travel time to propagate over this distance
 - Laser interferometry is an appropriate technique
 - Comparative measurement
 - Suspended mirrors = free fall test masses



- Michelson interferometer well suited:
 - Effect of a gravitational wave is in opposition between 2 perpendicular axes
 - **Light intensity of interfering beams is related to the difference of optical path length in the 2 arms**

Bandwidth: 10 Hz to few kHz

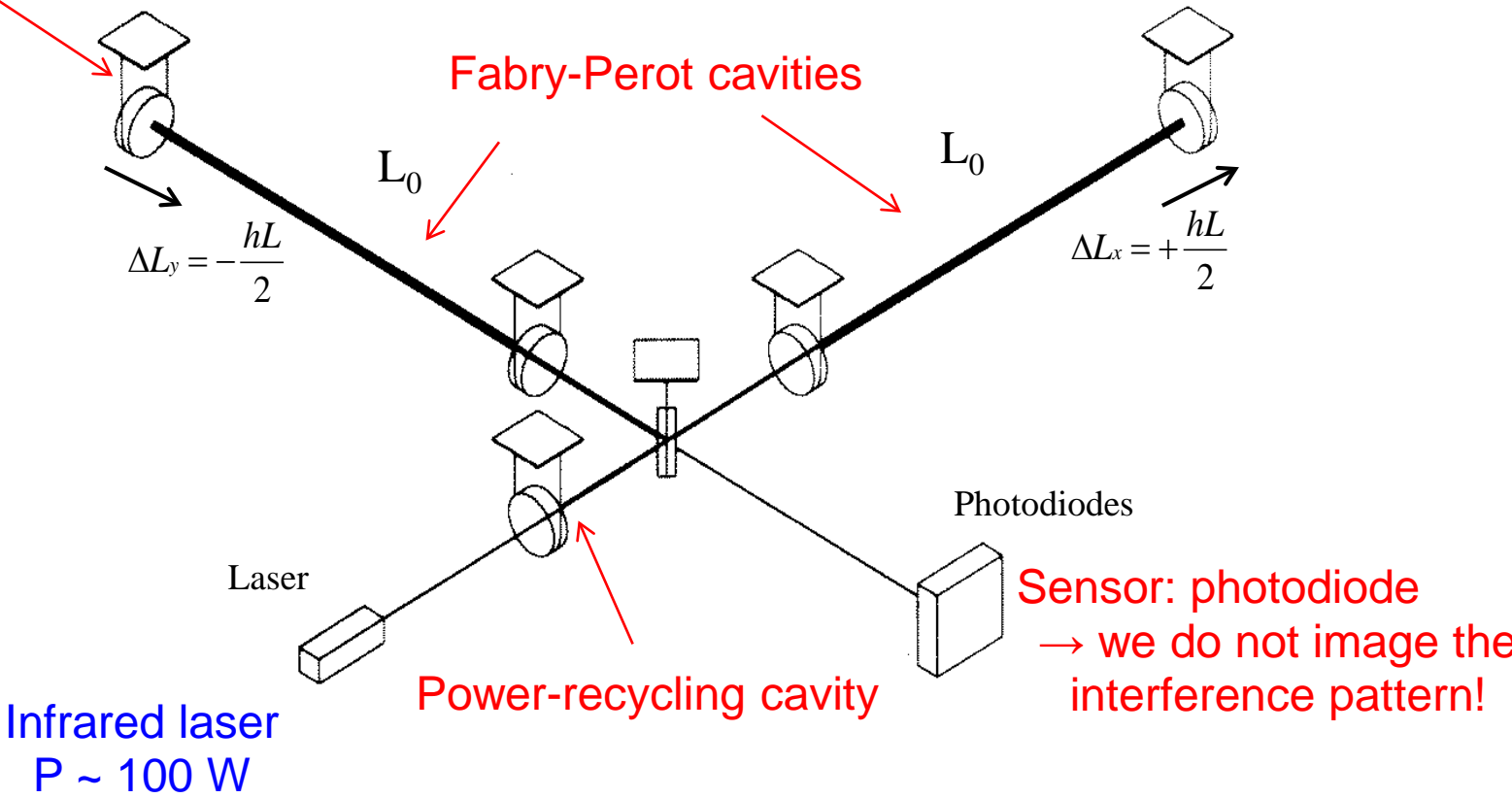
We need a big interferometer:

ΔL proportional to L

➔ need several km arms!

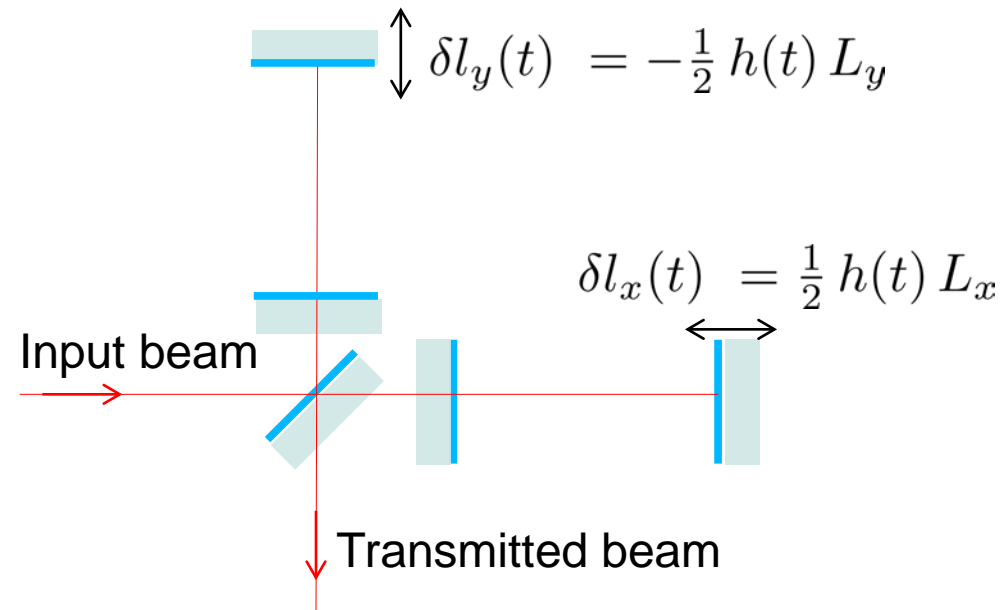
Virgo/LIGO: more complicated interferometers

Suspended mirrors → Mirrors can be considered as free-falling in the ITF plane for frequencies larger than ~10 Hz



WARNING: STILL VERY SIMPLIFIED SCHEME!

Orders of magnitude



Typical amplitude of differential arm length variations when a GW crosses the Earth:

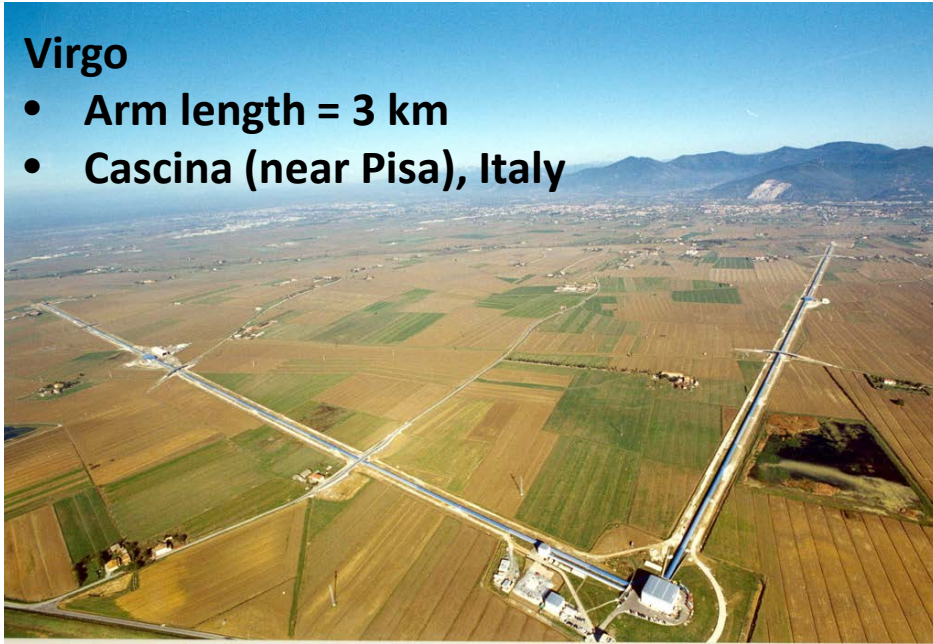
$$\begin{aligned}\delta\Delta L &= \delta l_x(t) - \delta l_y(t) \\ &= h(t) L_0\end{aligned}$$

$$\begin{aligned}h &\sim 10^{-23} & L_0 &= 3 \text{ km} \\ \rightarrow \delta\Delta L &\sim 3 \times 10^{-20} \text{ m} \\ &\sim \frac{\text{size of a proton}}{100000}\end{aligned}$$

Km scale interferometers

Virgo

- Arm length = 3 km
- Cascina (near Pisa), Italy



LIGO Livingston

- Arm length = 4 km
- Louisiana



LIGO Hanford

- Arm length = 4 km
- Washington State



The detector network

Advanced LIGO
Hanford
2015



GEO600 (HF)
2011



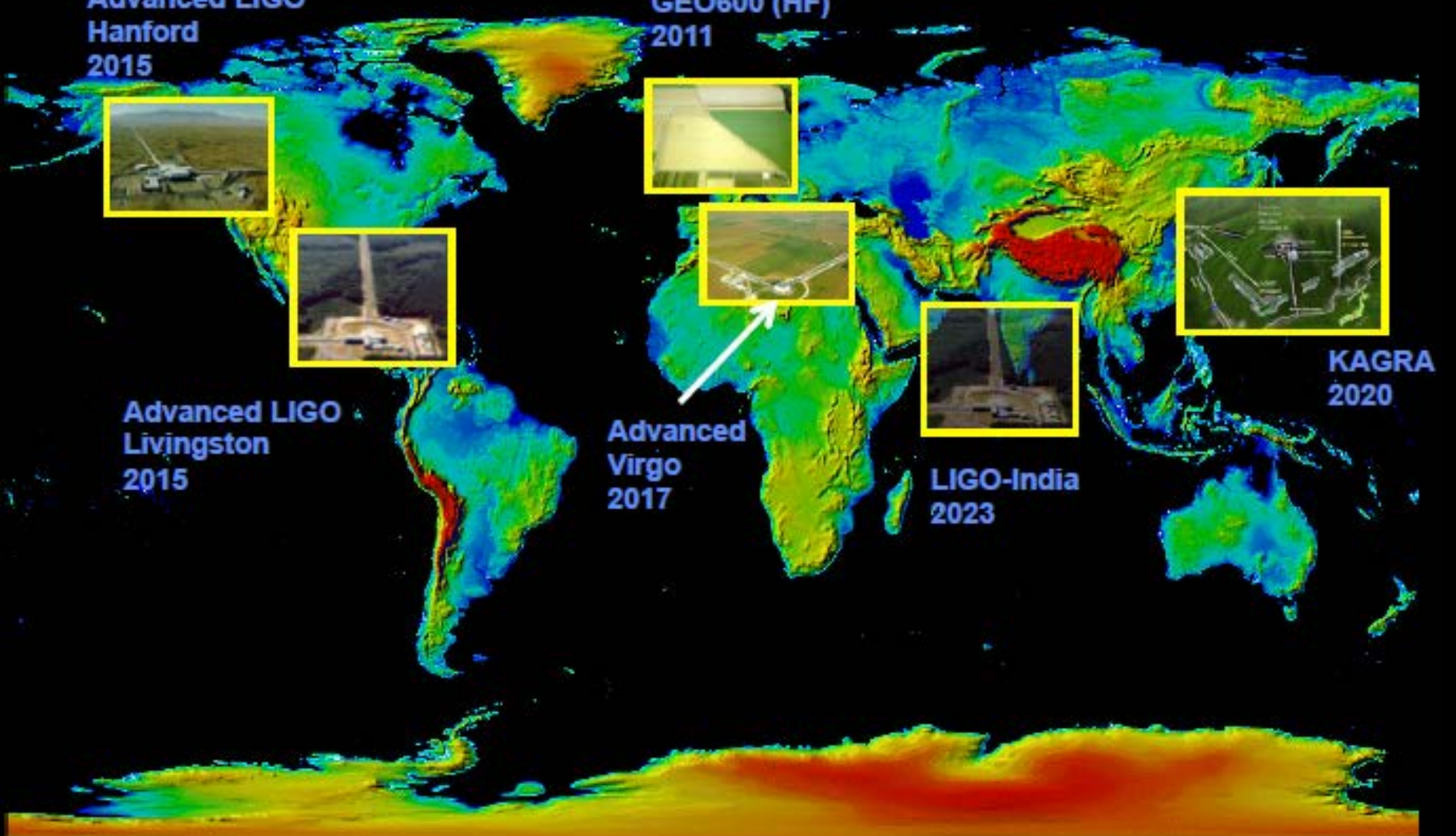
KAGRA
2020

Advanced LIGO
Livingston
2015

Advanced
Virgo
2017



LIGO-India
2023

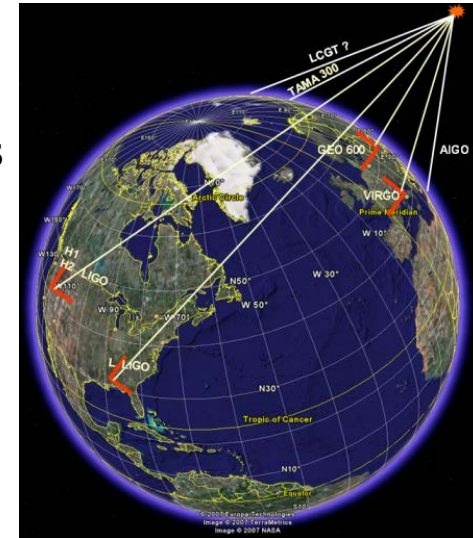
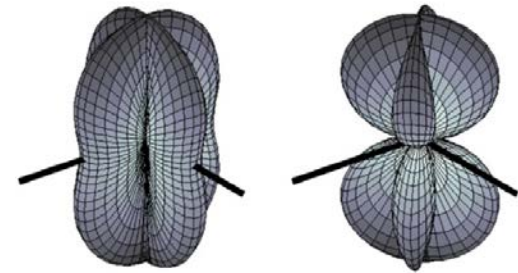


The benefits of the network

- A GW interferometer acts as a wide beam antenna
 - A single detector cannot localize the source
 - Need to compare the signals found in coincidence between several detectors (triangulation):

→ allow to point towards the source position in the sky

→ the telescope is obtained by a network of interferometers



- Looking for rare and transient signals: can be hidden in detector noise
 - requires observation in coincidence between at least 2 detectors
- Since 2007, Virgo and LIGO share their data and analyze them jointly

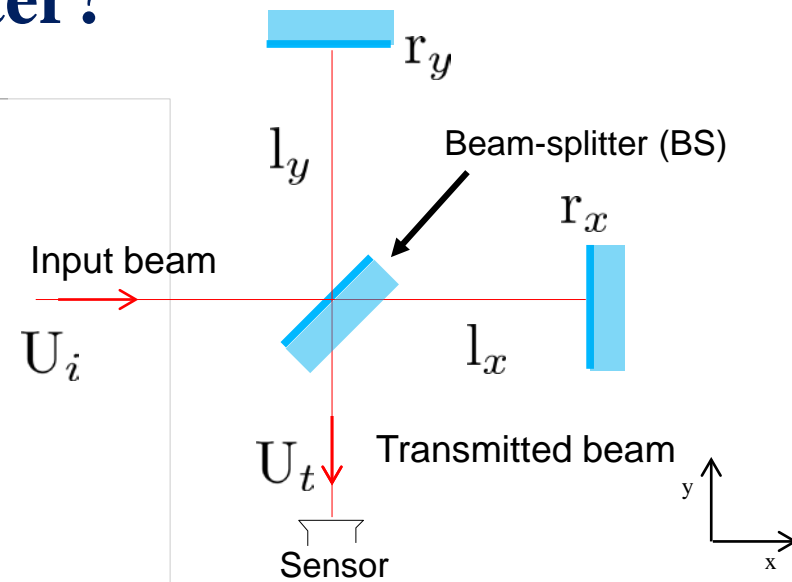
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How do we « observe » ΔL with a Michelson interferometer?

- Input wave $U_i(x, t) = \underline{\mathcal{A}}_i e^{j k x}$
 $= \underline{\mathcal{A}}_i$ on BS
- BS located at (0,0)
- Sensor located at (0,- y_s)
- Amplitude reflection and transmission coefficients: r and t

→ We are interested in the beam transmitted by the interferometer: it is the sum of the two beams (fields) that have propagated along each arm



Around the mirrors:

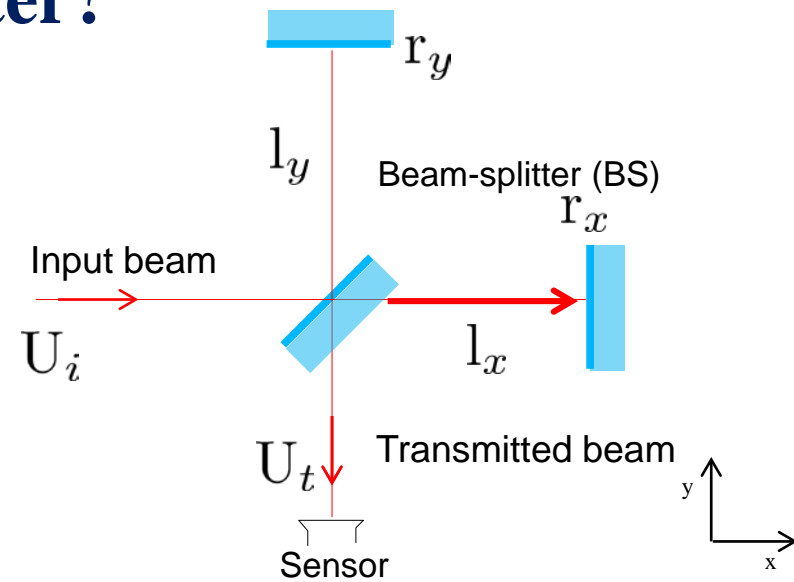
- Radius of curvature of the beam ~ 1400 m
- Size of the beam \sim few cm

→ The beam can be approximated by plane waves

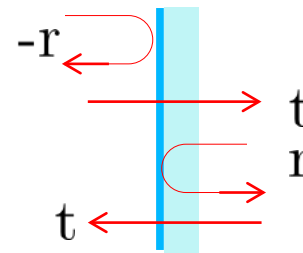
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- Input wave $U_i(x, t) = \underline{\mathcal{A}}_i e^{j k x}$
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- Beam propagating along x-arm:

$$U_{tx} = \underline{\mathcal{A}}_i t_{BS} e^{j k l_x} \dots\dots$$



Sign convention for amplitude reflection and transmission coefficients



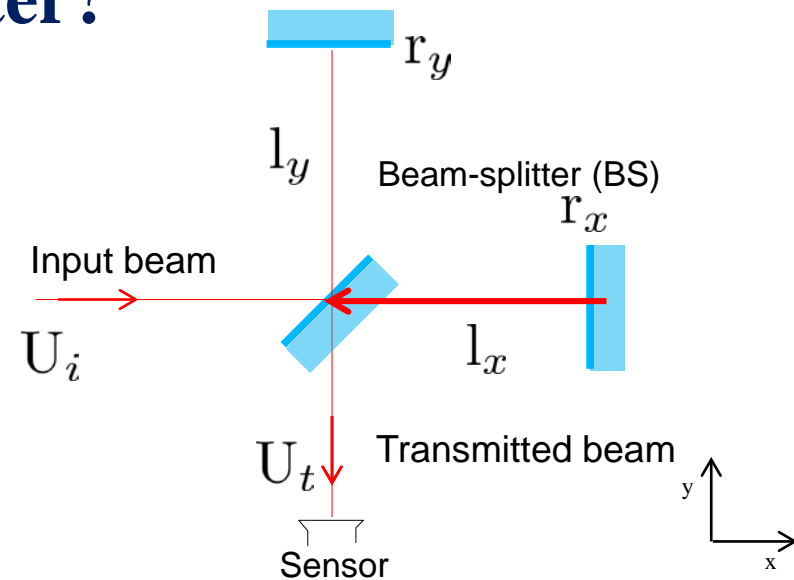
Without losses:
 $t^2 + r^2 = 1$

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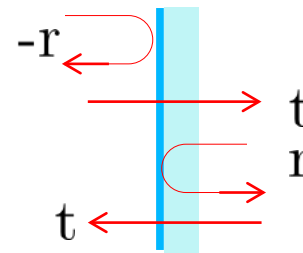
- Beam propagating along x-arm:

$$U_{tx} = \underline{\mathcal{A}}_i t_{BS} e^{j k l_x} \quad (-r_x) e^{j k l_x} \dots\dots$$



Sign convention for amplitude reflection and transmission coefficients

Without losses:
 $t^2 + r^2 = 1$

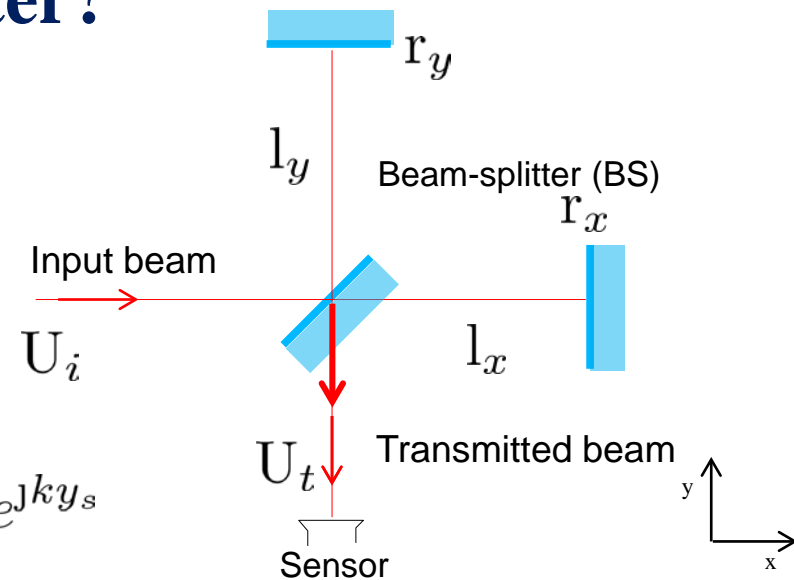


How do we « observe » ΔL with a Michelson interferometer?

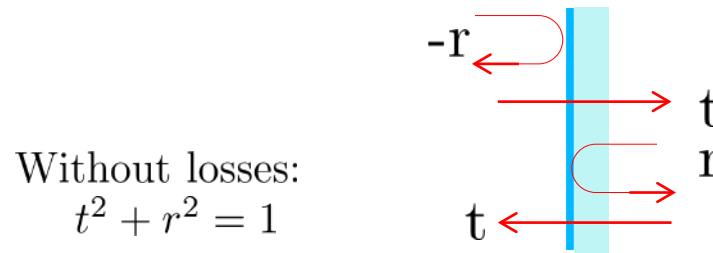
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- Beam propagating along x-arm:

$$U_{tx} = \underline{\mathcal{A}}_i t_{BS} e^{j k l_x} \quad (-r_x) e^{j k l_x} \quad r_{BS} e^{j k y_s}$$



Sign convention for amplitude reflection and transmission coefficients



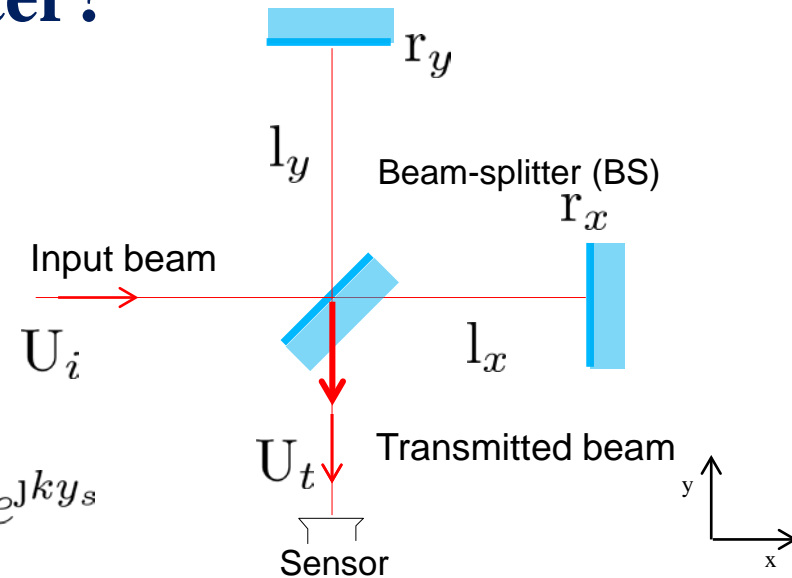
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- Beam propagating along x-arm:

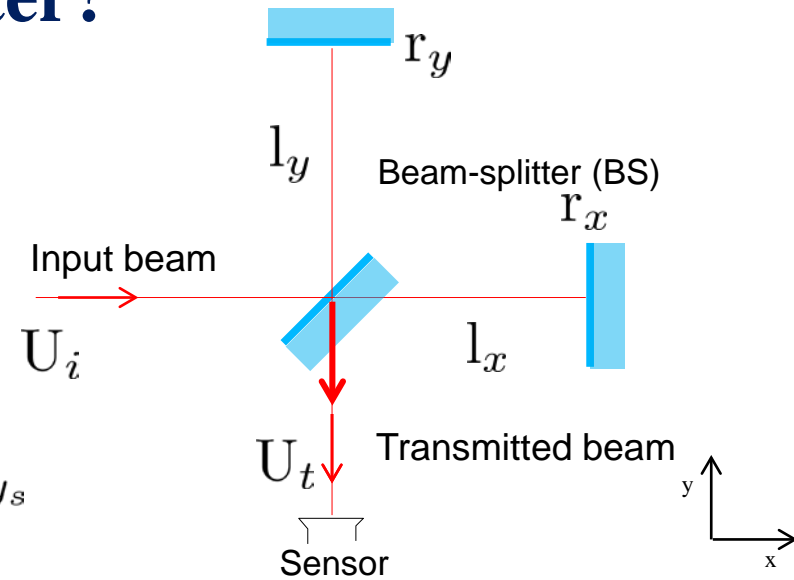
$$\begin{aligned}
 U_{tx} &= \underline{\mathcal{A}}_i t_{BS} e^{j k l_x} \quad (-r_x) e^{j k l_x} \quad r_{BS} e^{j k y_s} \\
 &= \underline{\mathcal{A}}_i t_{BS} r_{BS} (-r_x) e^{2j k l_x} e^{j k y_s} \\
 &= \frac{\underline{\mathcal{A}}_i}{2} \times \underbrace{(-r_x e^{2j k l_x})}_{\text{Complex reflection of the x-arm}} e^{j k y_s} \quad \text{with } t_{BS} = r_{BS} = \frac{1}{\sqrt{2}}
 \end{aligned}$$

Complex reflection of the x-arm



How do we « observe » ΔL with a Michelson interferometer?

Input wave $U_i(x, t) = \underline{\mathcal{A}}_i e^{j k x}$
 $= \underline{\mathcal{A}}_i$ on BS



Beam propagating along x-arm:

$$U_{tx} = \underline{\mathcal{A}}_i t_{BS} e^{j k l_x} \quad (-r_x) e^{j k l_x} \quad r_{BS} e^{j k y_s}$$

$$= \underline{\mathcal{A}}_i t_{BS} r_{BS} (-r_x) e^{2j k l_x} e^{j k y_s}$$

$$= \frac{\mathcal{A}_i}{2} \times \underbrace{(-r_x e^{2j k l_x})}_{\text{Complex reflection of the x-arm}} e^{j k y_s}$$

Beam propagating along y-arm:

$$U_{ty} = -\frac{\mathcal{A}_i}{2} \times \underbrace{(-r_y e^{2j k l_y})}_{\text{Complex reflection of the y-arm}} e^{j k y_s}$$

Transmitted field:

$$U_t = U_{tx} + U_{ty}$$

$$= \frac{\mathcal{A}_i}{2} e^{j k y_s} (r_y e^{2j k l_y} - r_x e^{2j k l_x})$$

Complex reflection of the y-arm

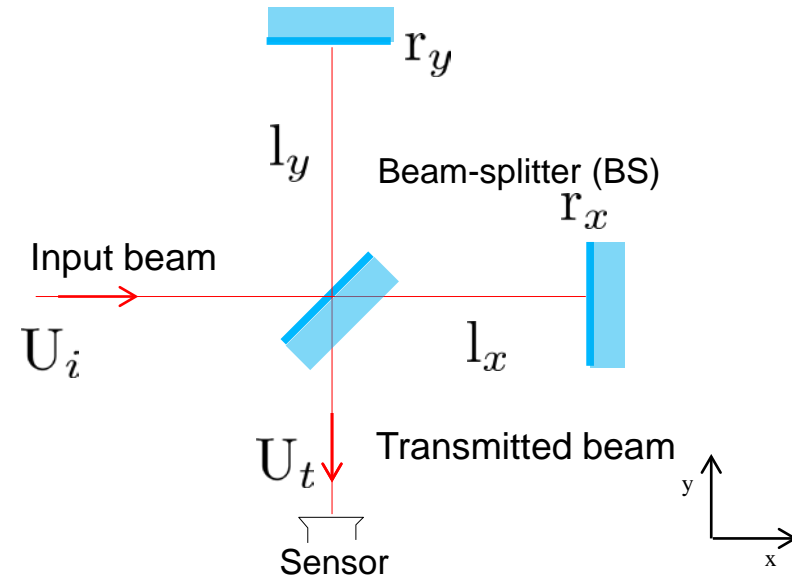
Simple Michelson interferometer: transmitted power

Field transmitted by the interferometer

$$U_t = \frac{A_i}{2} (r_y e^{2jkly} - r_x e^{2jklx})$$

k is the wave number, $k = 2\pi/\lambda$

λ is the laser wavelength ($\lambda=1064$ nm)



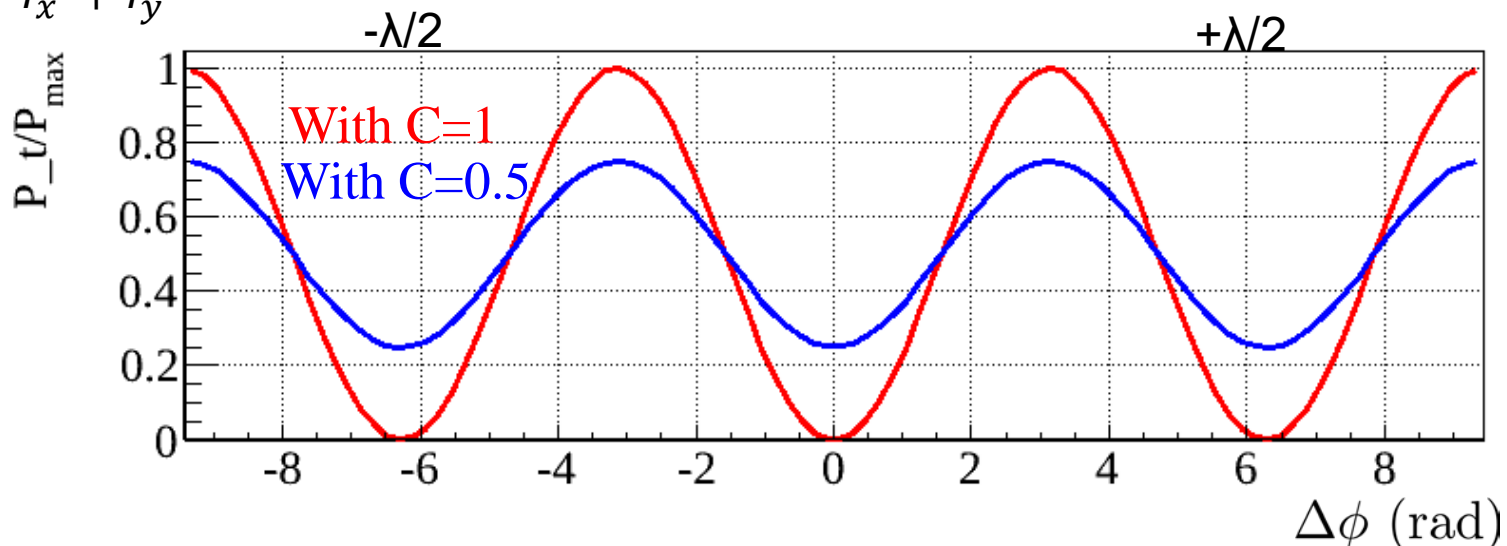
Transmitted power

$$P_t \propto |U_t|^2 = \frac{P_{max}}{2} (1 - C \cos(\Delta\phi))$$

where $\Delta\phi = 2k(l_y - l_x)$

$$\text{ITF contrast: } C = \frac{2r_x r_y}{r_x^2 + r_y^2}$$

$$P_{max} = \frac{P_i}{2} (r_x^2 + r_y^2)$$



What power does Virgo measure?

- In general, the beam is not a plane wave but a spherical wave

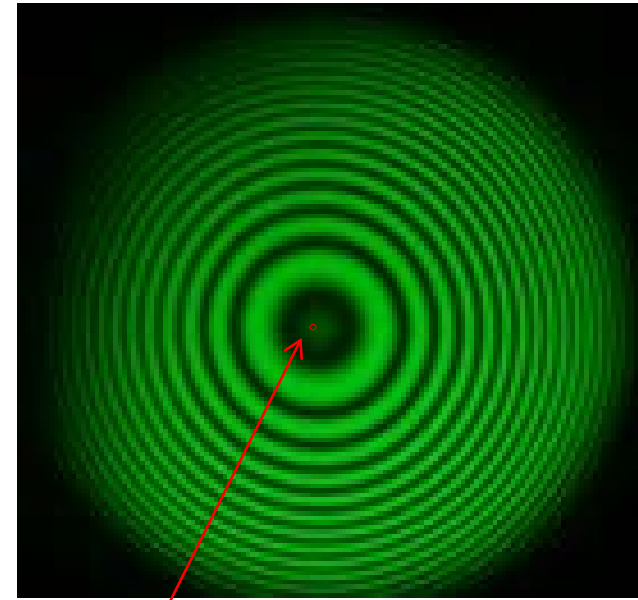
→ interference pattern

(and the complementary pattern in reflection)

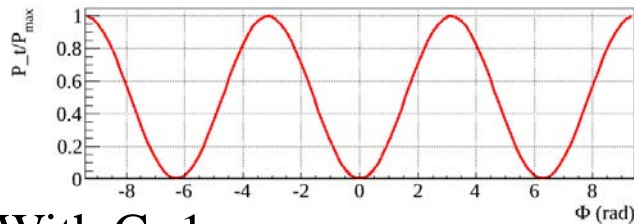
- Virgo interference pattern much larger than the beam size:

~1 m between two consecutive fringes

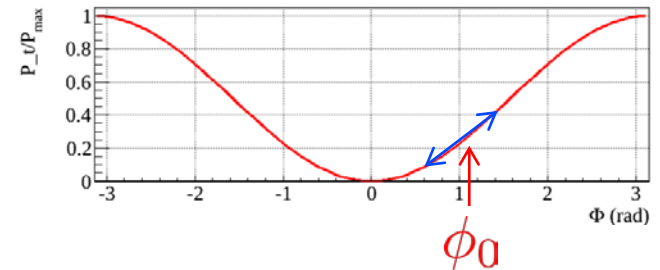
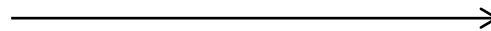
→ we do not study the fringes in nice images !



Equivalent size of Virgo beam



Setting a working point



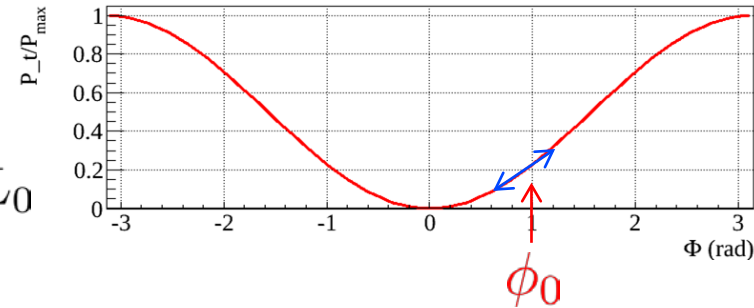
Controlled mirror positions

From the power to the gravitational wave

$$P_t = \frac{P_i}{2} (1 - C \cos(\phi)) \quad \text{where } \phi = 2\frac{2\pi}{\lambda}(l_y - l_x)$$

- Around the working point:

$$\left. \frac{dP_t}{d\phi} \right|_{\phi_0} = \frac{P_i}{2} C \sin(\phi_0) \quad \text{where } \phi_0 = \frac{4\pi}{\lambda} \Delta L_0$$



- Power variations as function of small differential length variations:

$$\delta P_t = \frac{P_i}{2} C \sin(\phi_0) \delta \phi$$

$$\delta P_t = P_i C \frac{2\pi}{\lambda} \sin\left(\frac{4\pi}{\lambda} \Delta L_0\right) \delta \Delta L$$

$$\delta P_t \propto \delta \Delta L = h L_0 \quad \text{around the working point !}$$

From the power to the gravitational wave

- Around the working point:

$$\delta P_t = P_i C \frac{2\pi}{\lambda} \sin\left(\frac{4\pi}{\lambda} \Delta L_0\right) \delta \Delta L$$

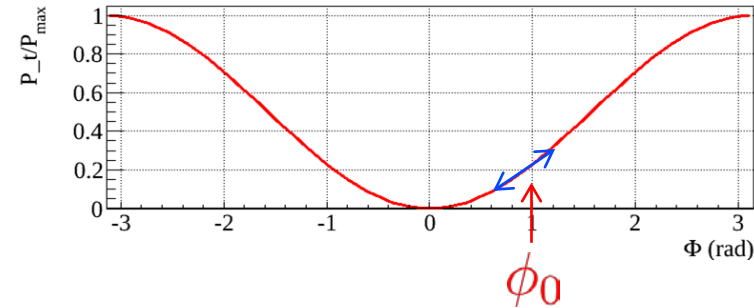
$$\delta P_t = \underbrace{\left(\text{Interferometer response}\right)}_{\text{(W/m)}} \times \delta \Delta L$$



Measurable physical quantity



Physical effect to be detected

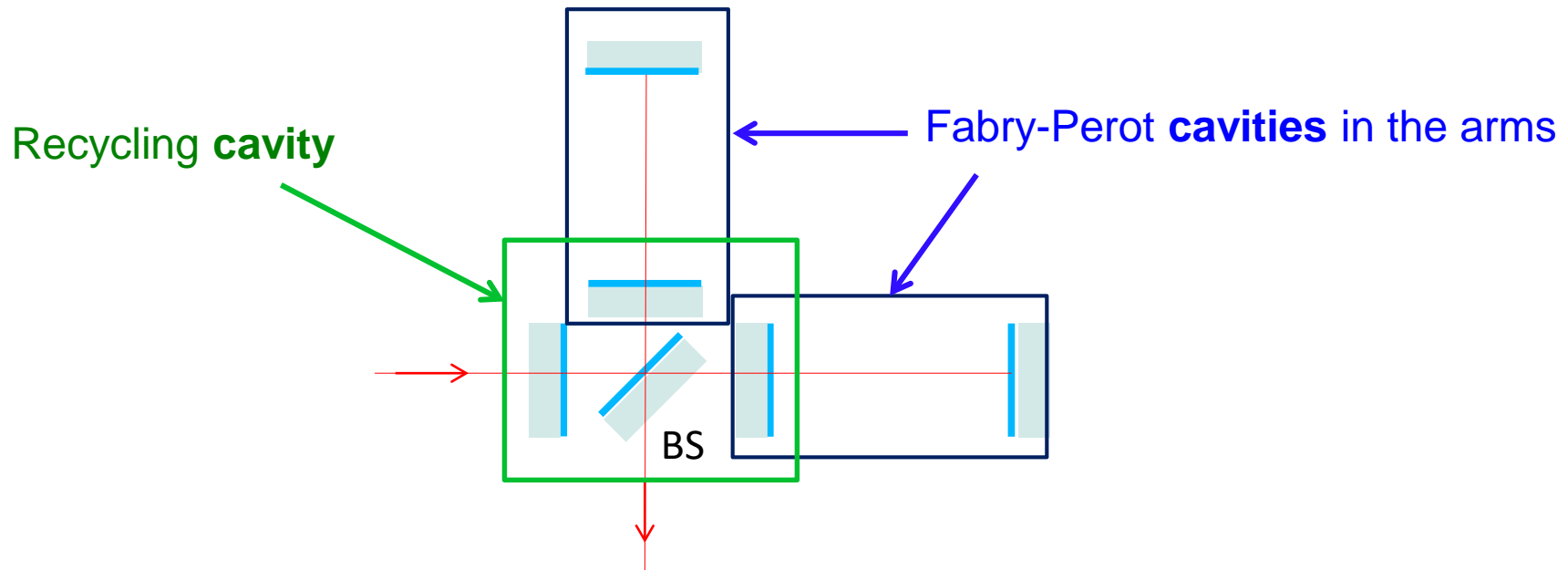


Improving the interferometer sensitivity

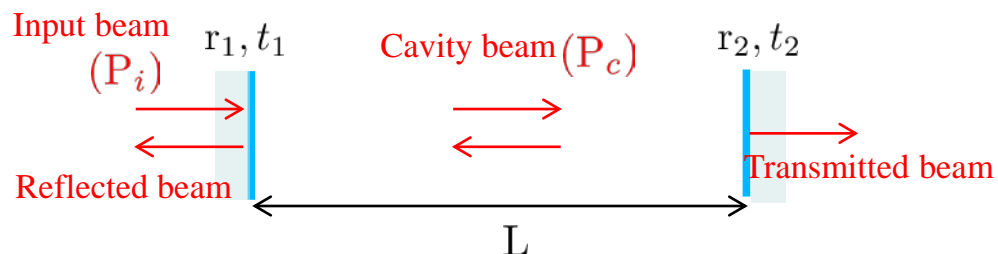
$$\delta P_t = \underbrace{(P_i)}_{\text{Increase the input power on BS}} C \sin\left(\frac{4\pi}{\lambda} \Delta L_0\right) \underbrace{(k \delta \Delta L)}_{\propto \delta \phi}$$

Increase the input power on BS

Increase the phase difference between the arms for a given differential arm length variation



Beam resonant inside the cavities

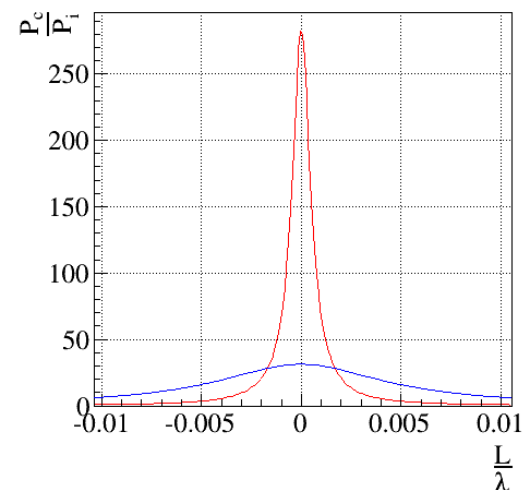
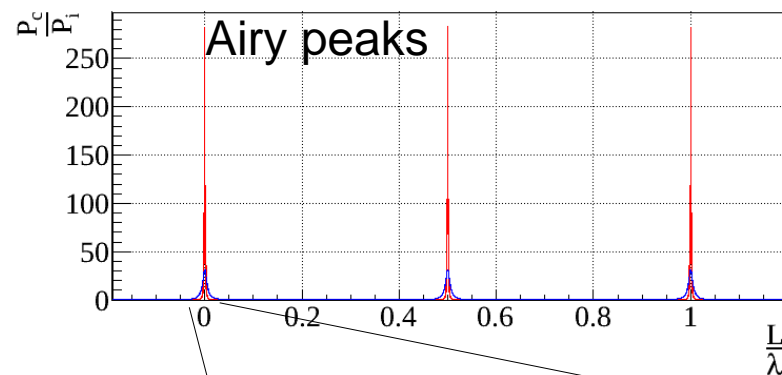


$$P_c = P_i \frac{t_1^2}{(1 - r_1 r_2)^2} \frac{1}{1 + \left(\frac{2\mathcal{F}}{\pi}\right)^2 \sin^2(kL)}$$

$$\text{Finesse } \mathcal{F} = \frac{\pi \sqrt{r_1 r_2}}{1 - r_1 r_2}$$

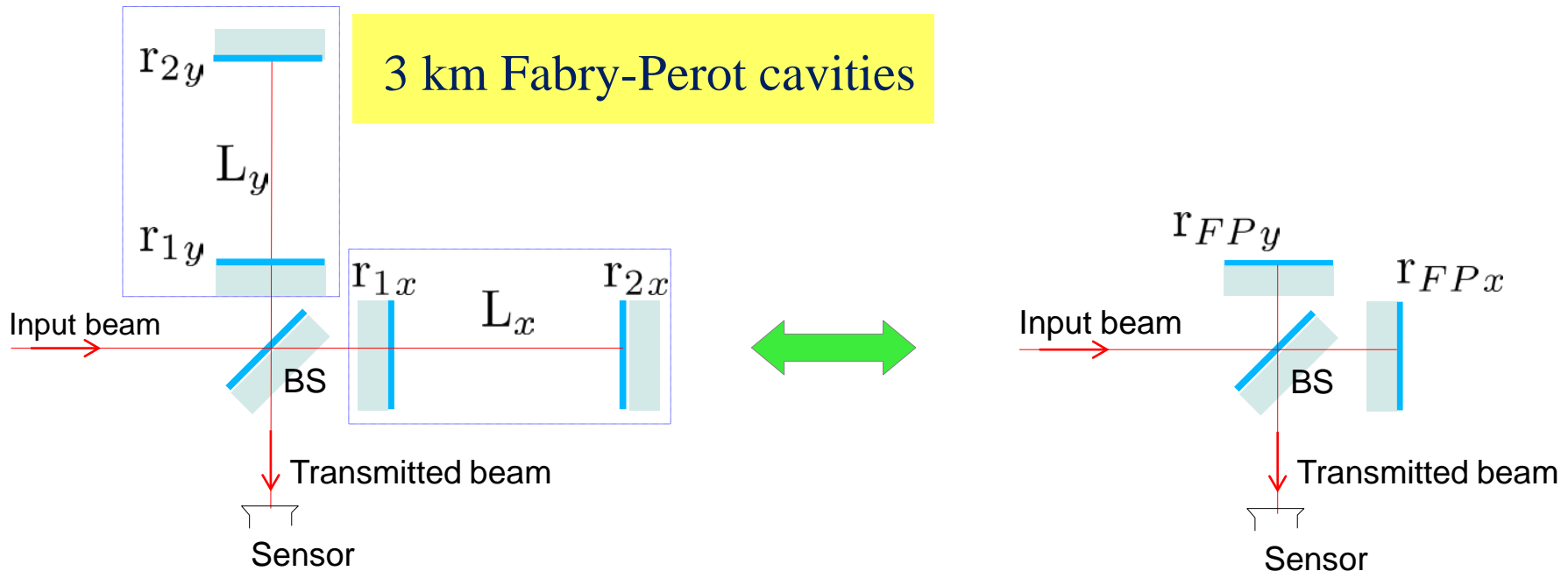
Virgo cavity at resonance: $L = n \frac{\lambda}{2} \quad (n \in \mathbb{N})$

Virgo $\mathcal{F} = 50$
AdVirgo $\mathcal{F} = 443$



Average number of light round-trips in the cavity: $N = \frac{2\mathcal{F}}{\pi}$

How do we amplify the phase offset?



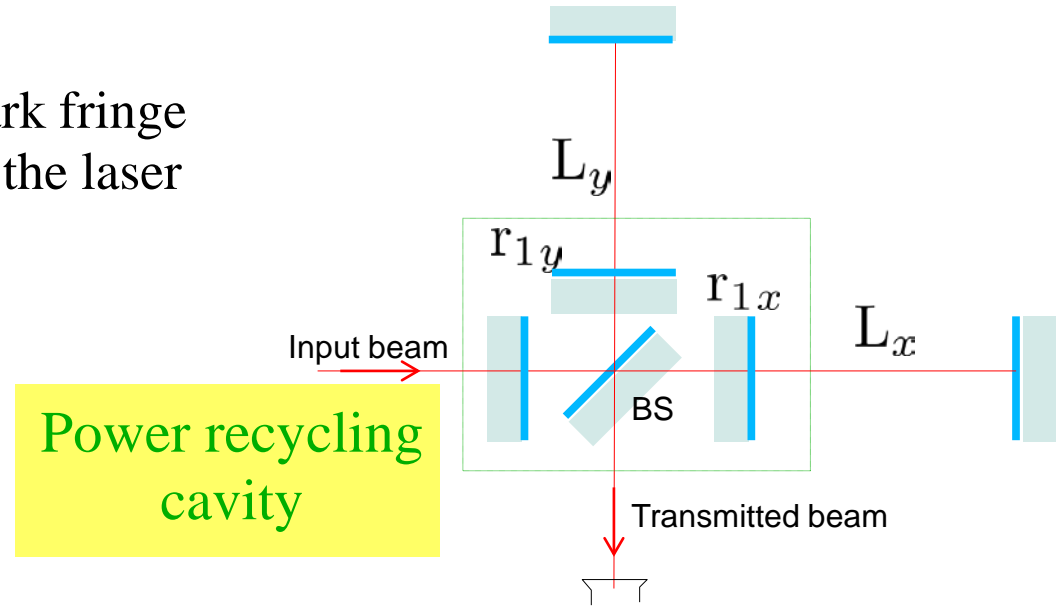
$$r_{FPx} = -1 \times e^{j \frac{2\mathcal{F}}{\pi} 2k \delta L_x}$$

~number of round-trips in the arm
~300 for AdVirgo

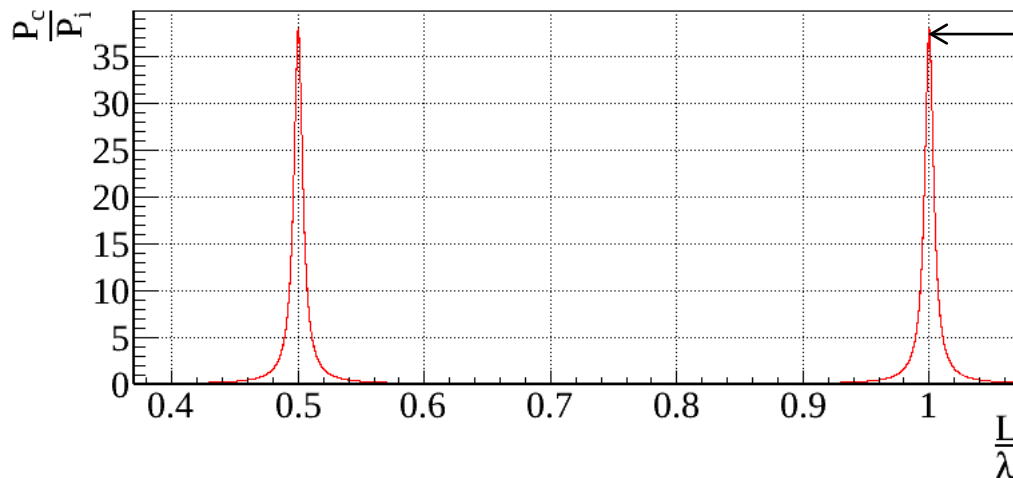
(instead of $r_{armx} = -1 \times e^{j2k(L_x + \delta L_x)}$ in the arm of a simple Michelson)

How do we increase the power on BS?

Detector working point close to a dark fringe
 → most of power go back towards the laser



Resonant power recycling cavity



$$G_{PR} = 38 \quad (r_{PR}^2 = 0.95)$$

→ input power on BS
 increased by a factor 38!

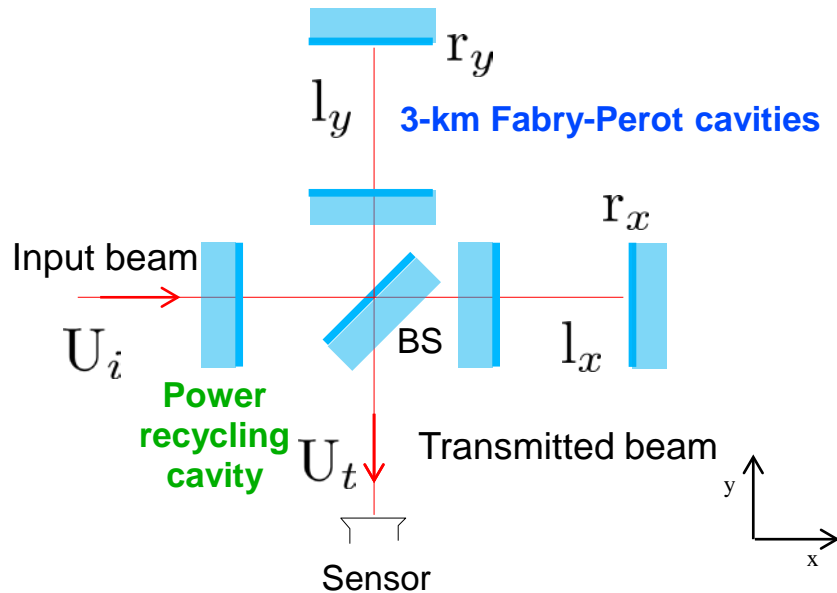
Improved interferometer response

- Response of simple Michelson:

$$\delta P_t = P_i C \frac{2\pi}{\lambda} \sin\left(\frac{4\pi}{\lambda} \Delta L_0\right) \delta \Delta L$$

$$\delta P_t = (\text{Michelson response}) \times \delta \Delta L \quad (\text{W/m})$$

- Response of recycled Michelson with Fabry-Perot cavities:



$$\delta P_t = G_{PR} P_i C \frac{2\pi}{\lambda} \sin\left(\frac{4\pi}{\lambda} \Delta L_0\right) \frac{2\mathcal{F}}{\pi} \delta \Delta L$$

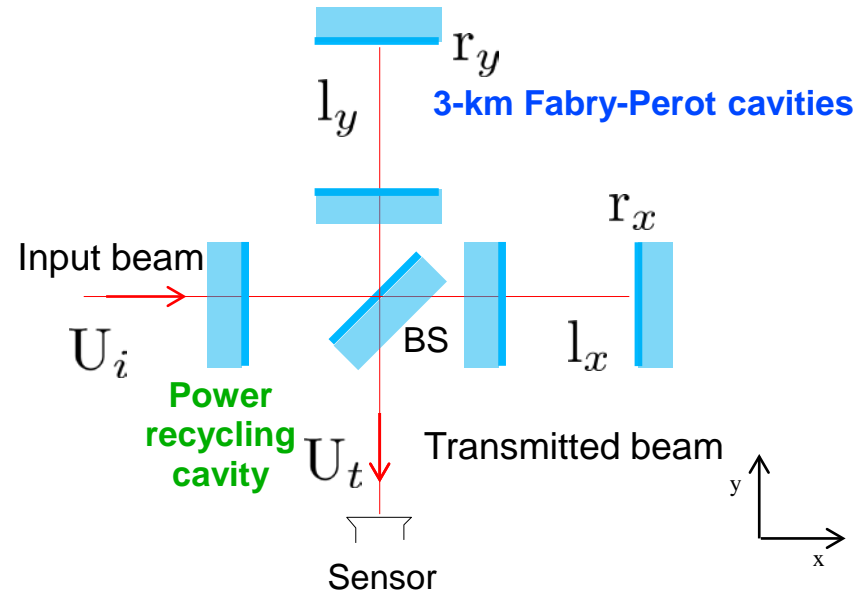
~ 38
 ~ 300

For the same $\delta \Delta L$, δP_t has been increased by a factor ~ 12000

Order of magnitude of the « sensitivity »

$$\delta P_t = G_{PR} P_i C \frac{2\pi}{\lambda} \sin\left(\frac{4\pi}{\lambda} \Delta L_0\right) \frac{2\mathcal{F}}{\pi} \delta \Delta L$$

| | |
|-------------------------|--------------------------------------|
| Laser wavelength | $\lambda = 1064 \text{ nm}$ |
| Input power | $P_i \sim 100 \text{ W}$ |
| Interferometer contrast | $C \sim 1$ |
| Cavity finesse | $\mathcal{F} \sim 450$ |
| Power recycling gain | $G_{PR} \sim 38$ |
| Working point | $\Delta L_0 \sim 10^{-11} \text{ m}$ |



Shot noise due to output power of $\sim 50 \text{ mW}$
 $\rightarrow \delta P_{t,min} \sim 0.1 \text{ nW}$ \longrightarrow

$$\delta \Delta L_{min} \sim 5 \times 10^{-20} \text{ m}$$

$$\rightarrow h_{min} = \frac{\delta \Delta L_{min}}{L} \sim 10^{-23}$$



In reality, the detector response depends on frequency...

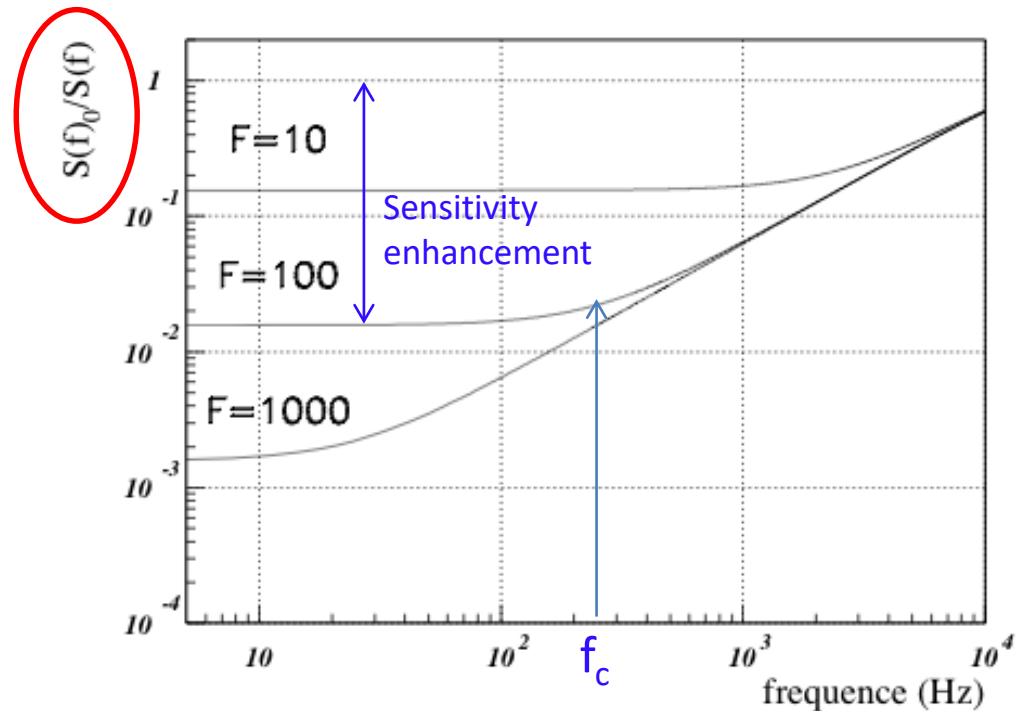


Example of frequency dependency of the ITF response

- Light travel time in the cavities must be taken into account
- Fabry-Perot cavities behave as a low pass filter
- Frequency cut-off:

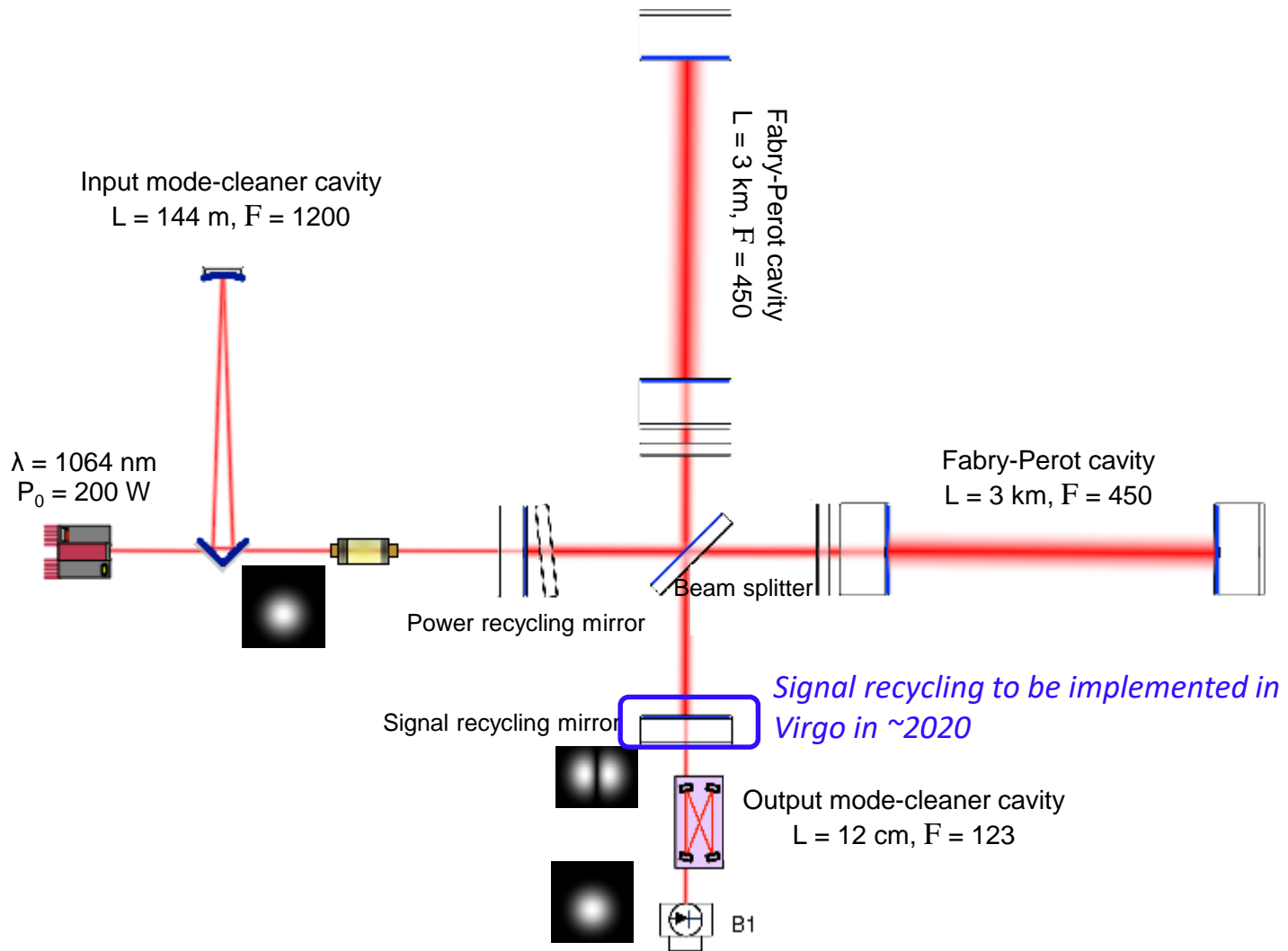
$$f_c = \frac{c}{4FL}$$

Ratio between the sensitivity of an interferometer with Fabry-Perot cavities versus the sensitivity of an interferometer without cavities



- Finesse of Virgo Fabry Perot cavities: $F = 450$, $L = 3$ km $\rightarrow f_c = 55$ Hz

Optical layout of Virgo

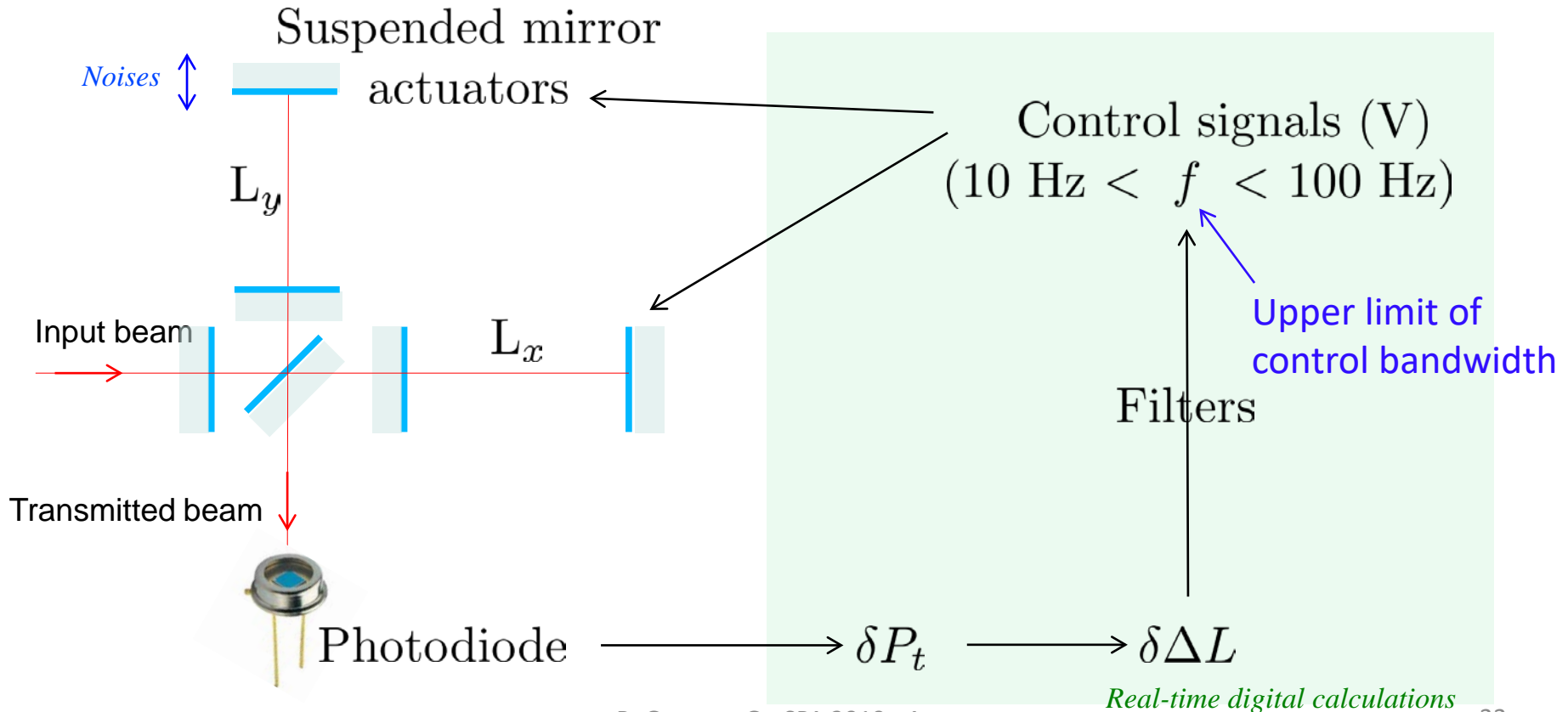


How do we control the working point?



Small offset from a dark fringe: $\Delta L_0 = n \frac{\lambda}{2} + 10^{-11} \text{ m}$

- Controls to reduce the motion up to $\sim 100 \text{ Hz}$
- Precision of the control $\delta \Delta L_{true} \sim 10^{-15} \text{ m}$

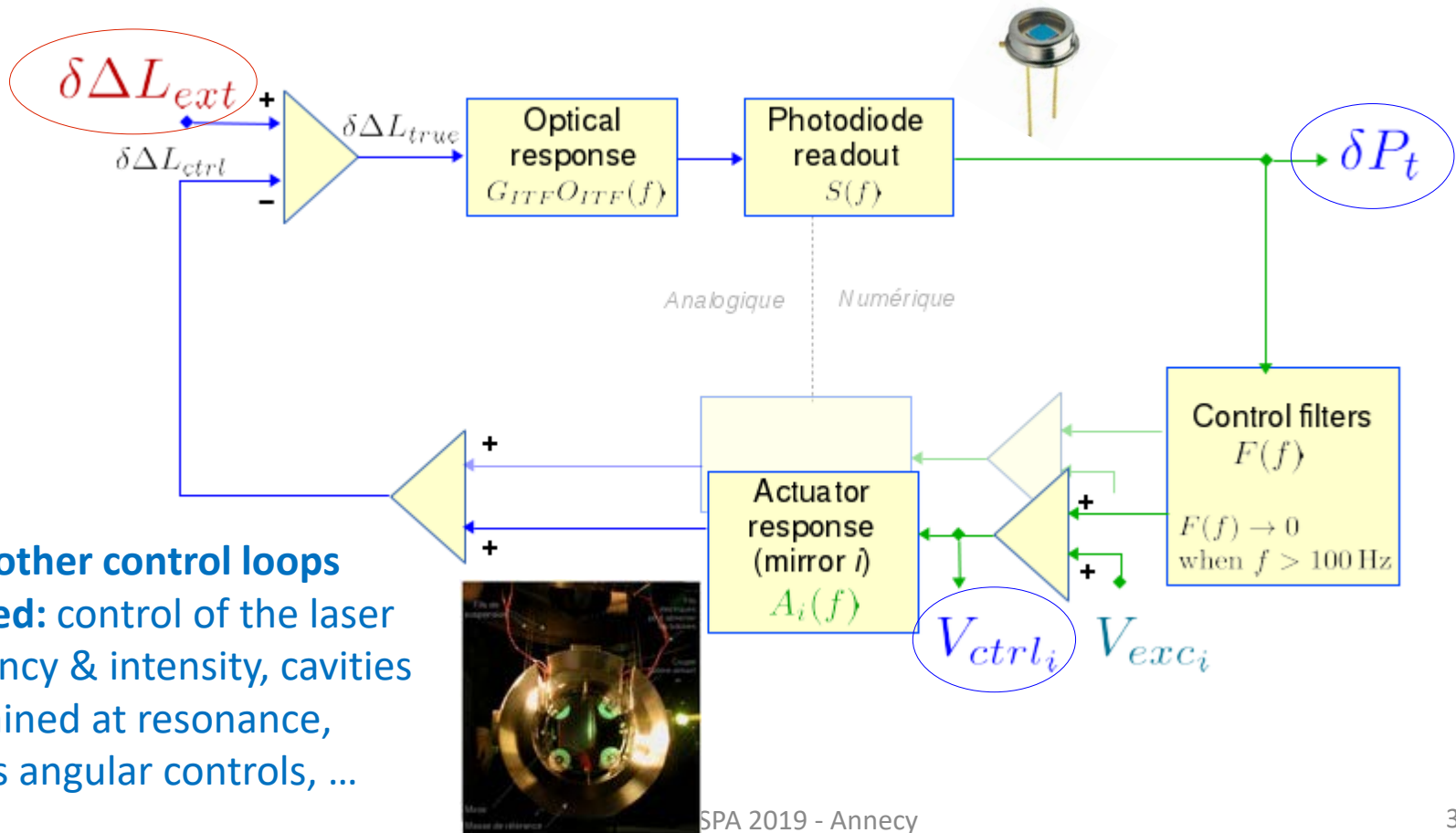


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Small offset from a dark fringe: $\Delta L_0 = n \frac{\lambda}{2} + 10^{-11} \text{ m}$

- Controls to reduce the motion up to $\sim 100 \text{ Hz}$
- Precision of the control $\delta \Delta L_{true} \sim 10^{-15} \text{ m}$

$$\delta \Delta L_{ext} = \delta \Delta L_{noise} + \delta \Delta L_{GW}$$



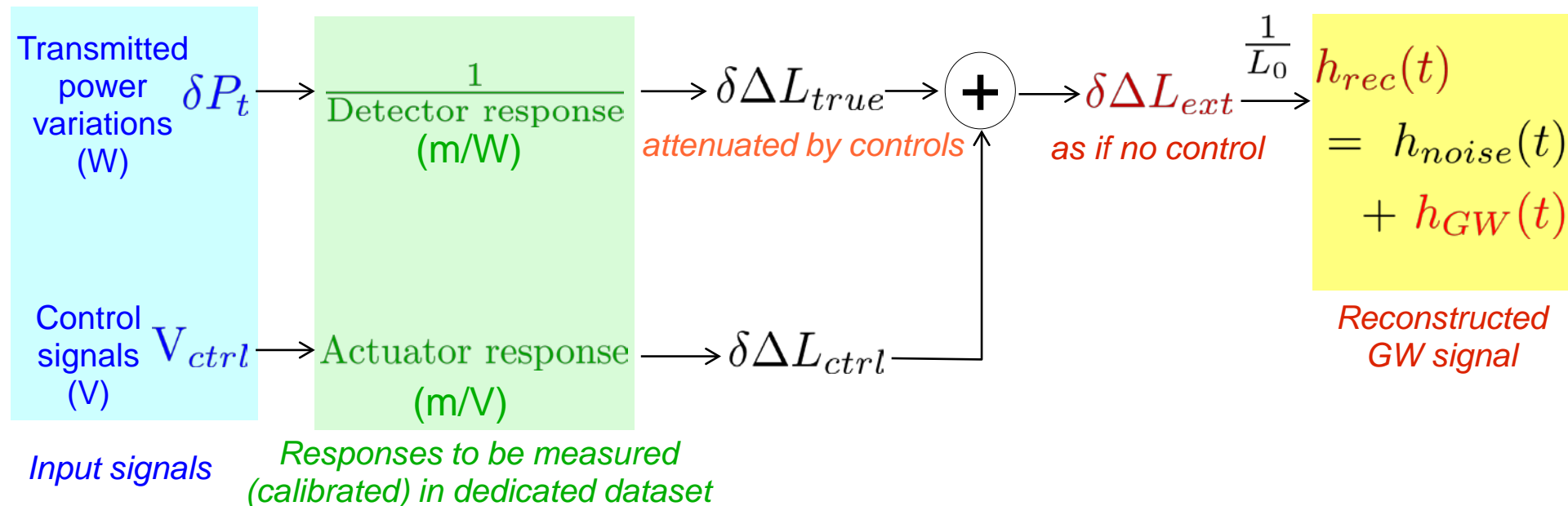
Many other control loops required: control of the laser frequency & intensity, cavities maintained at resonance, mirrors angular controls, ...

From the detector data to the GW strain $h(t)$

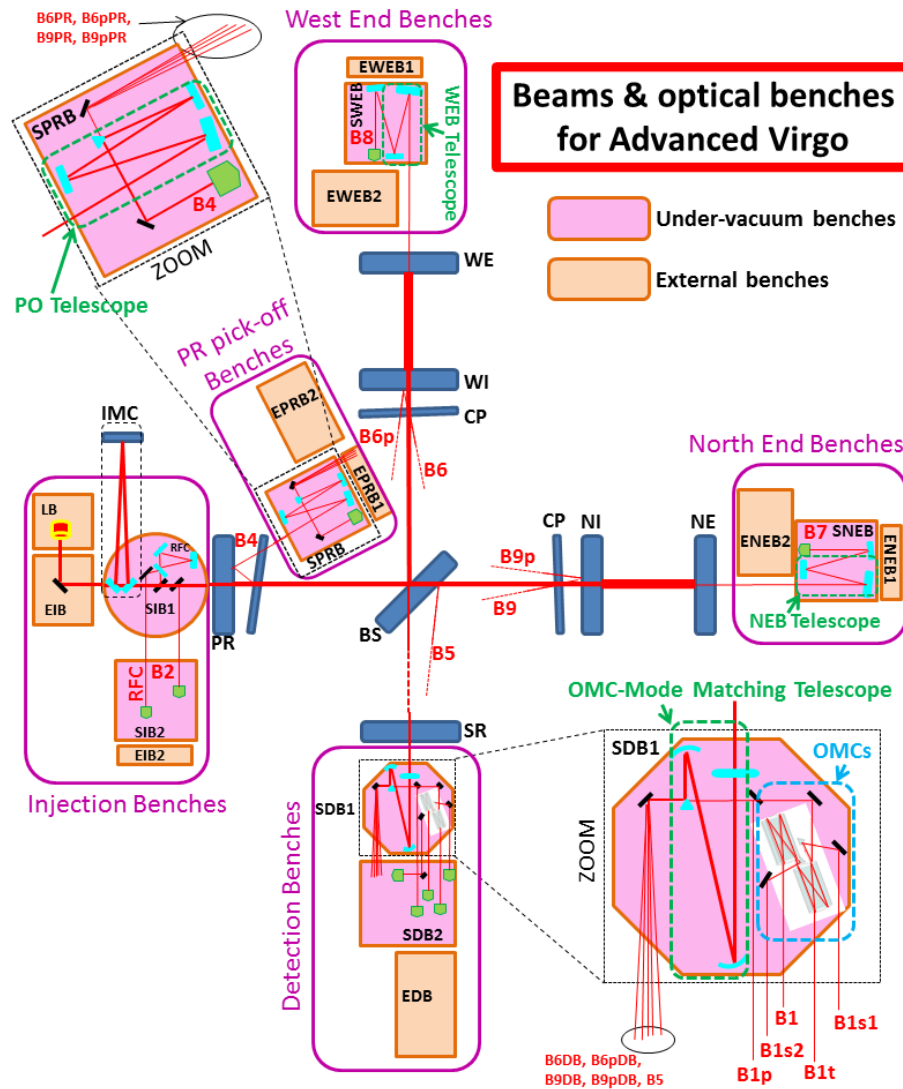
- High frequency (>100 Hz): mirrors behave as free falling masses

$$\rightarrow h(t) = \frac{\delta\Delta L_{true}(t)}{L_0}$$

- Lower frequency: the controls attenuate the noise... but also the GW signal!
 \rightarrow the control signals contain information on $h(t)$



How to extract all error signals? Interferometer optical ports

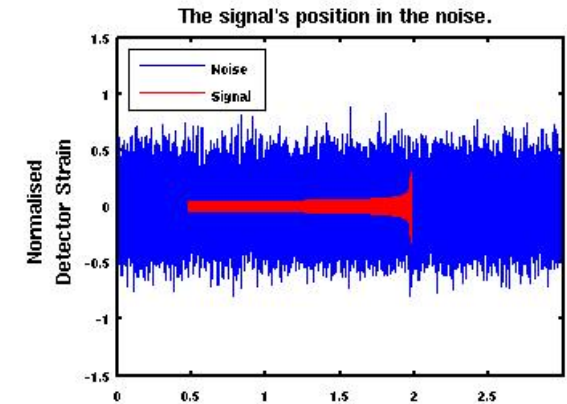
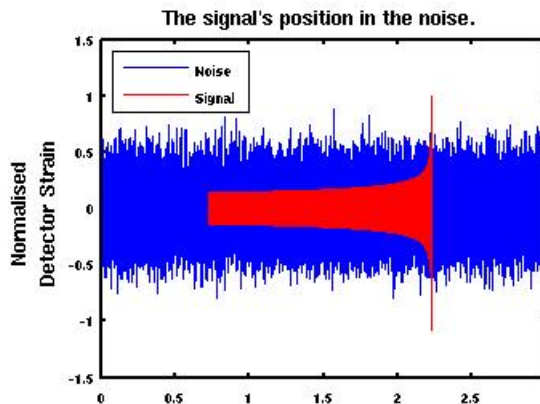
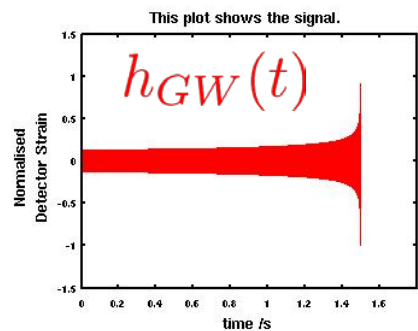
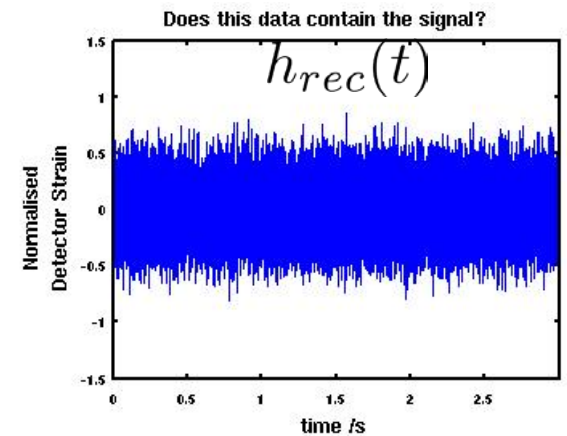
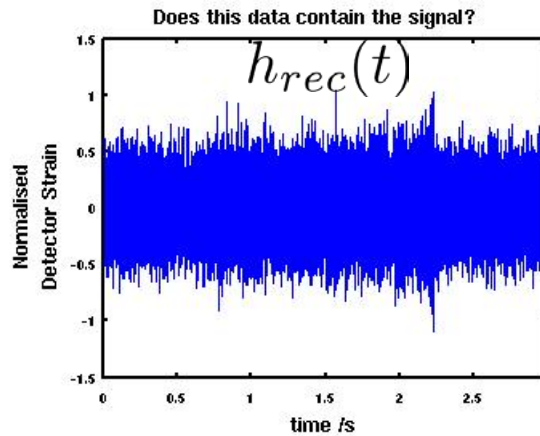
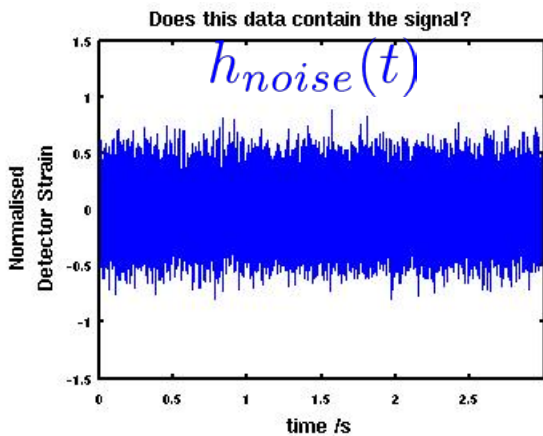


**Noises limiting interferometer
sensitivity:
How to tackle them ?**

Reminder: what is noise in Virgo?

- Stochastic (random) signal that contributes to the signal $h_{rec}(t)$ but does not contain information on the gravitational wave strain $h_{GW}(t)$

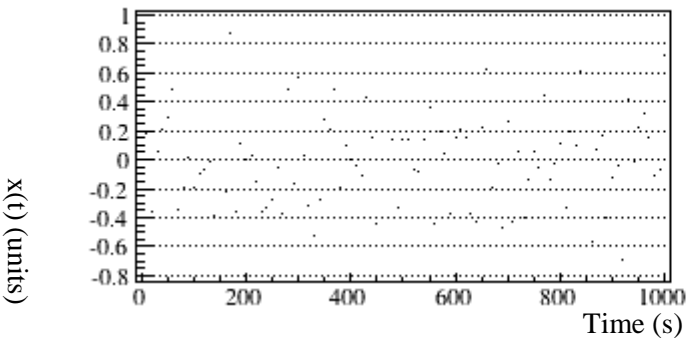
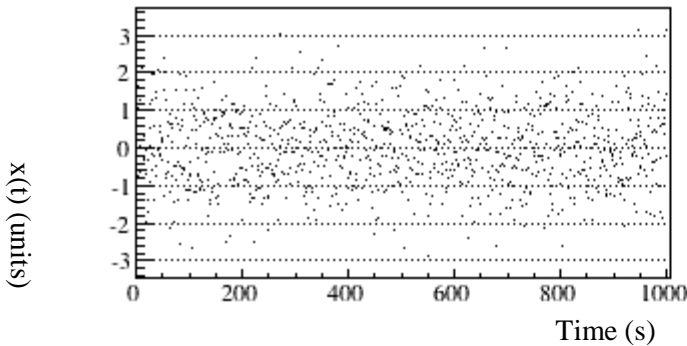
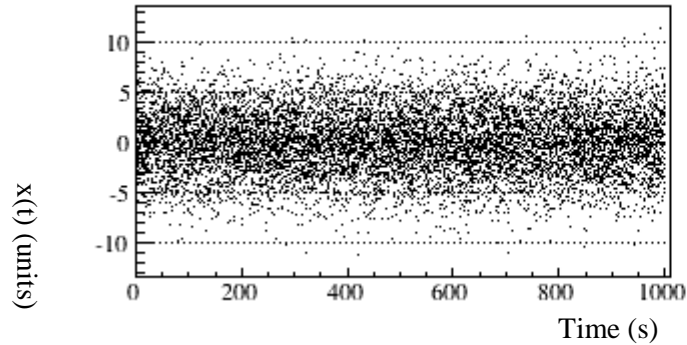
$$h_{rec}(t) = h_{noise}(t) + h_{GW}(t)$$



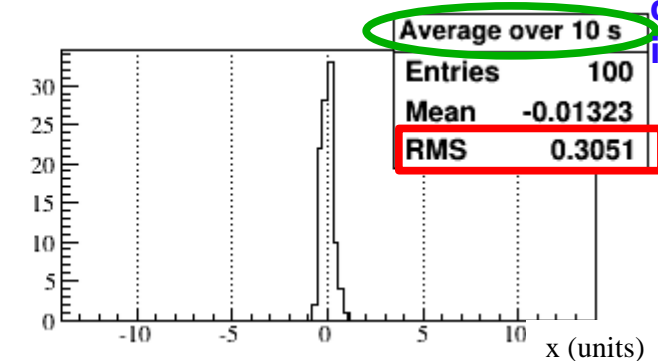
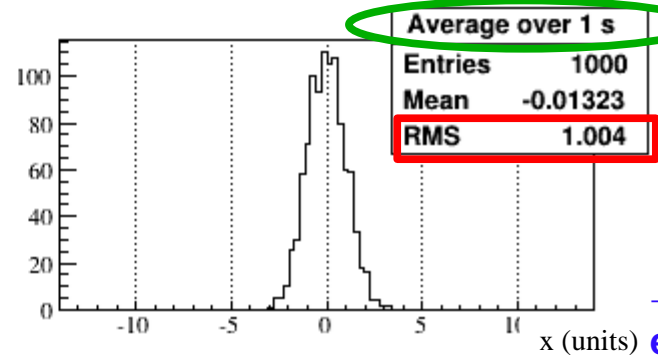
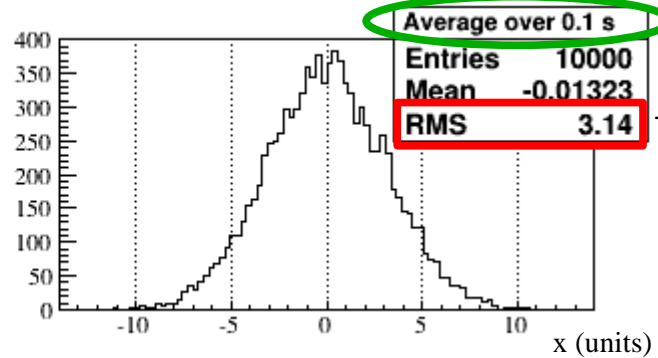
time /s
Extracted from Black Hole Hunter: <http://www.blackholehunter.org/>

How do we characterize noise?

Data points (noise)



Distribution of the data



→ Noise characterised by its standard deviation σ_x

$$\sigma_x = \frac{D}{\sqrt{\text{average duration}}}$$

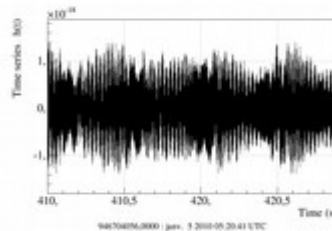
D is in (Data units $\times \sqrt{s}$)
or $\frac{\text{Data units}}{\sqrt{\text{Hz}}}$

→ its absolute value is equal to the standard deviation of the noise when it is averaged over 1 s

From hrec(t) to Virgo sensitivity curve

1/ Reconstruction of h(t)

$$h_{rec}(t) = h_{noise}(t) + h_{GW}(t)$$



2/ Amplitude spectral density of h(t)
(noise standard deviation over 1 s)

$$ASD = \sqrt{PSD} = \sqrt{\frac{|DFT|^2}{T}}$$

Discrete Fourier Transform (DFT)

$\sim 5 \times 10^{-20}$ m/ $\sqrt{\text{Hz}}$ (Advanced Virgo O2, 2017)

$\sim 10^{-20}$ m/ $\sqrt{\text{Hz}}$ (Advanced Virgo nominal)

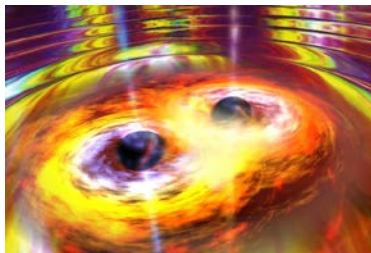
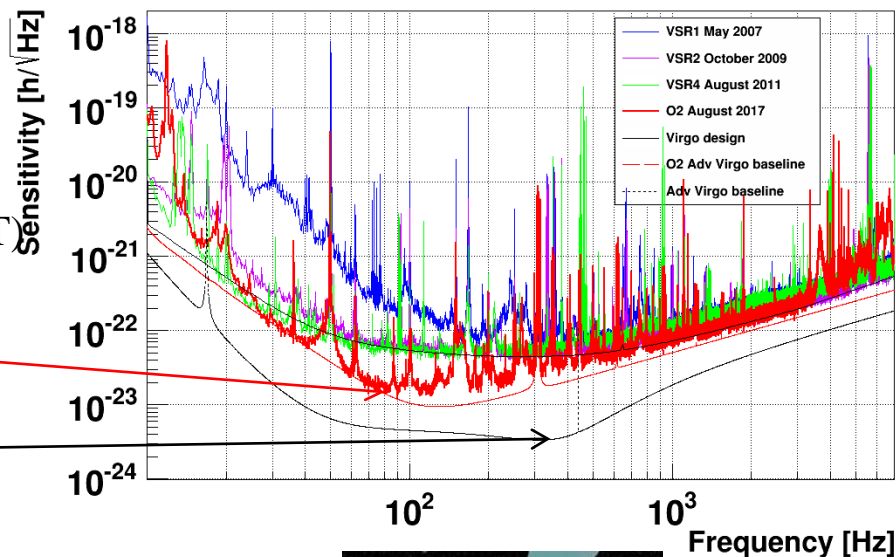


Image: Danna Berry/SkyWorks/NASA

Compact Binary Coalescences

Signal lasts for a few seconds

→ can detect $h \sim 10^{-23}$

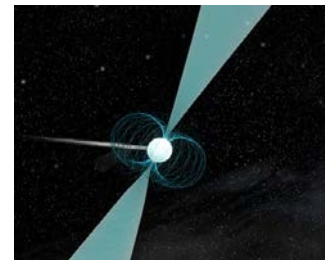


Image: B. Saxton (NRAO/AUI/NSF)

Rotating neutron stars

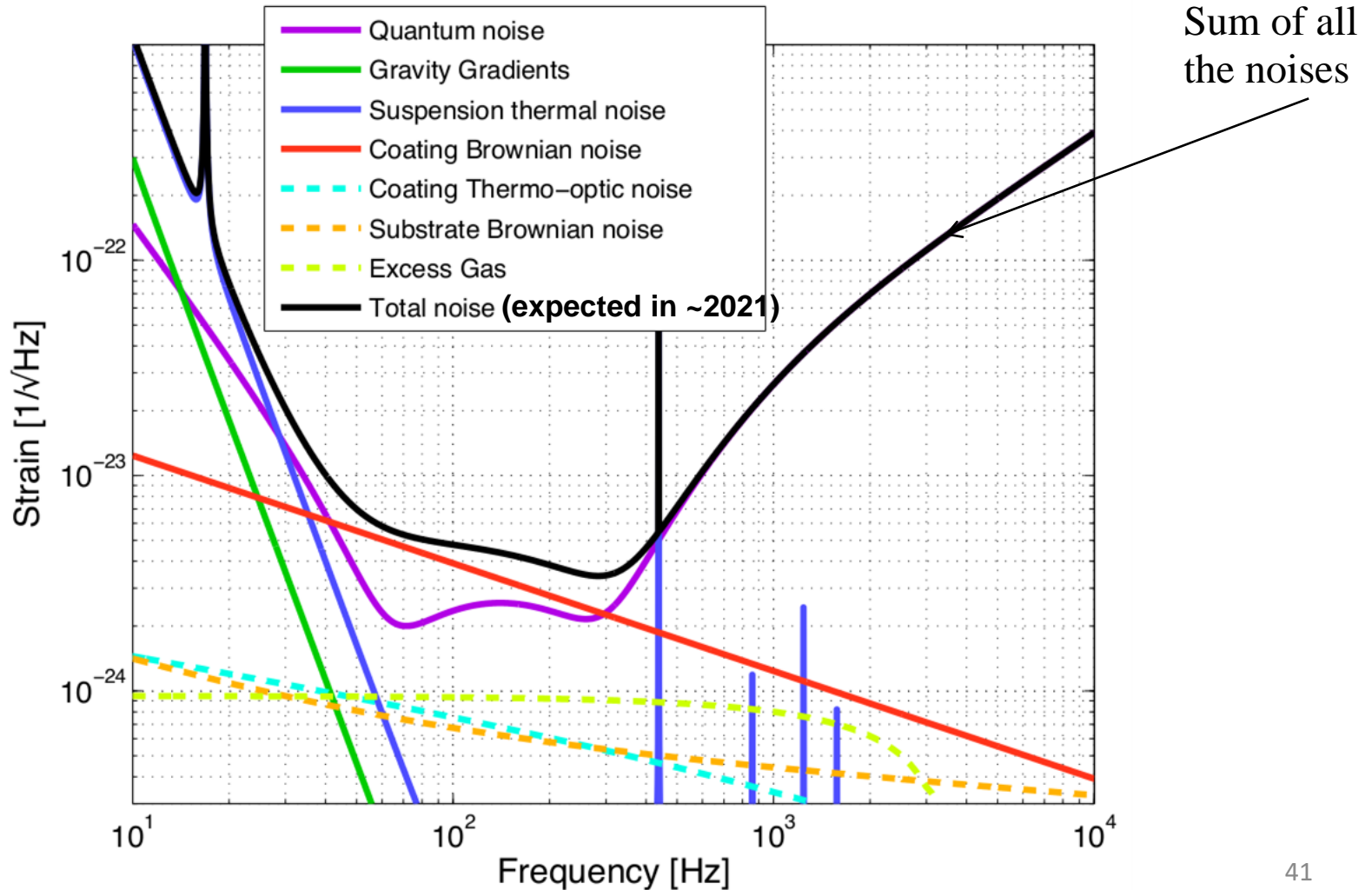
Signal averaged over days ($\sim 10^6$ s)

→ can detect $h \sim 10^{-26}$

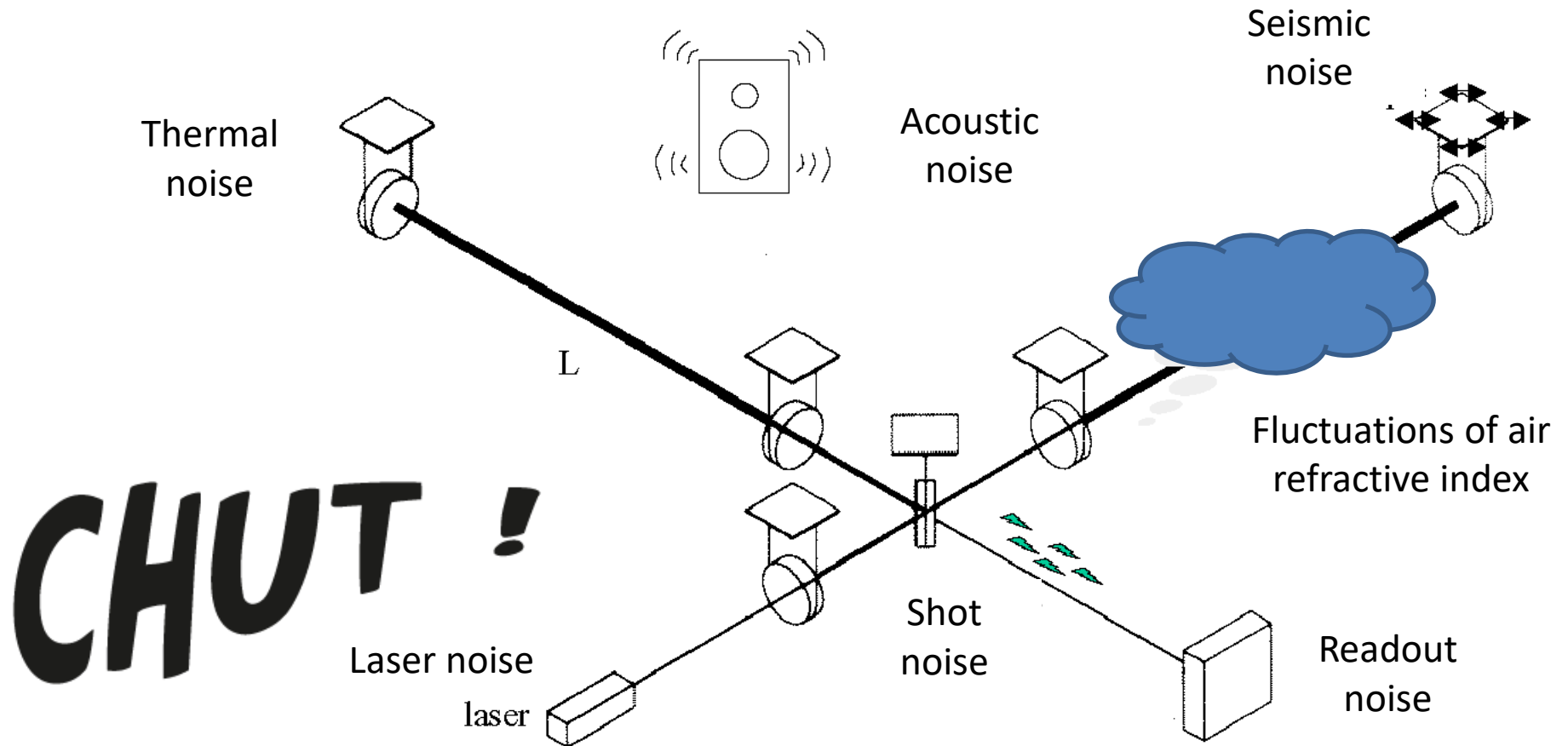
Nominal sensitivity of Advanced Virgo

Fundamental noise only

Possible technical noise not shown



Fundamental noise sources



Under vacuum

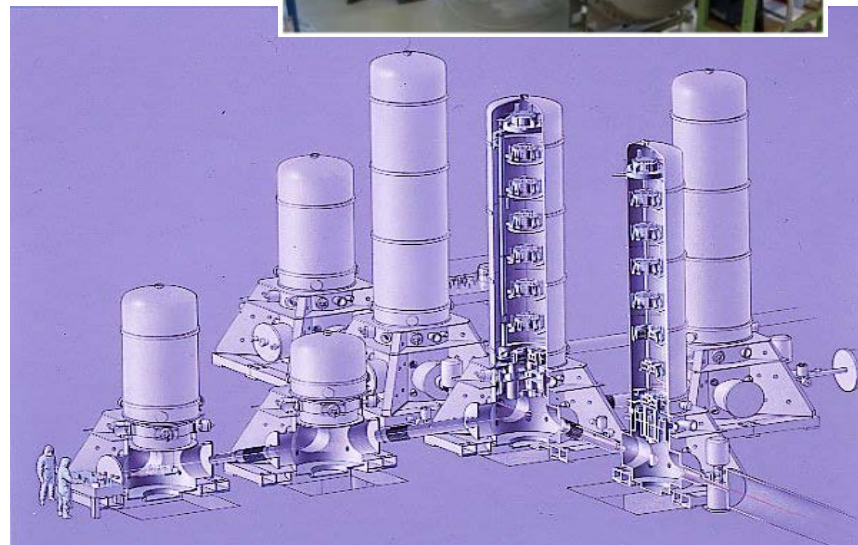


Goals

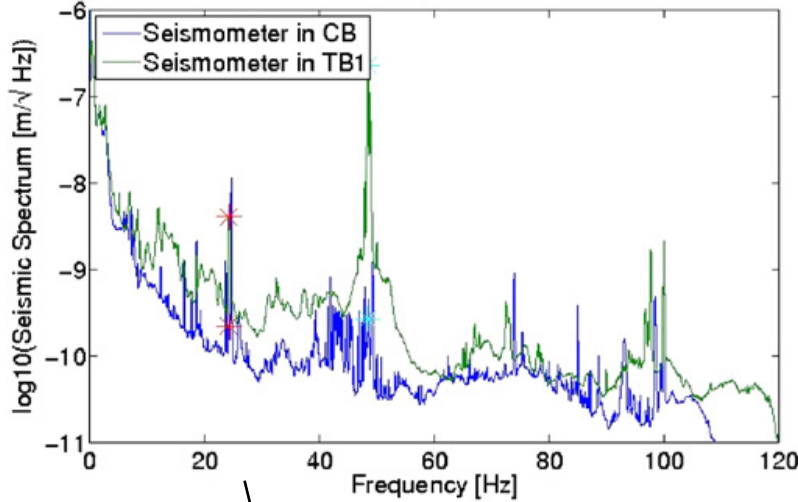
- ❑ Isolation against acoustic noise
- ❑ Avoid measurement noise due to fluctuations of air refractive index
- ❑ Keep mirrors clean

Advanced Virgo vacuum in a few numbers:

- ❑ Volume of vacuum system: 7000 m³
- ❑ Different levels of vacuum:
 - 3 km arms designed for up to 10⁻⁹ mbar (Ultra High Vacuum)
 - ~10⁻⁶ - 10⁻⁷ mbar in mirror vacuum chambers (« towers »)
- ❑ Separation between arms and towers with cryotrap links

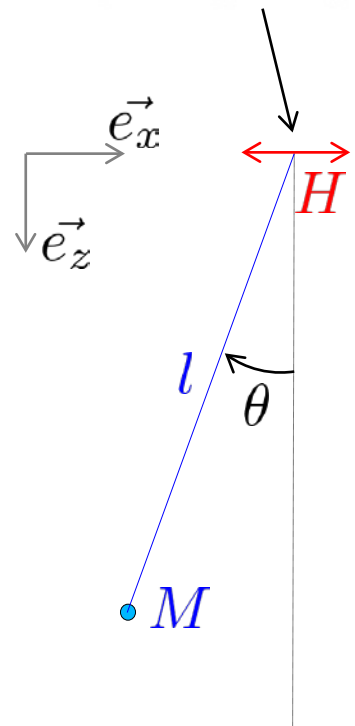


Seismic noise and suspended mirrors



Ground vibrations up to $\sim 1 \mu\text{m}/\sqrt{\text{Hz}}$ at low frequency decreasing down to $\sim 10 \text{ pm}/\sqrt{\text{Hz}}$ at 100 Hz

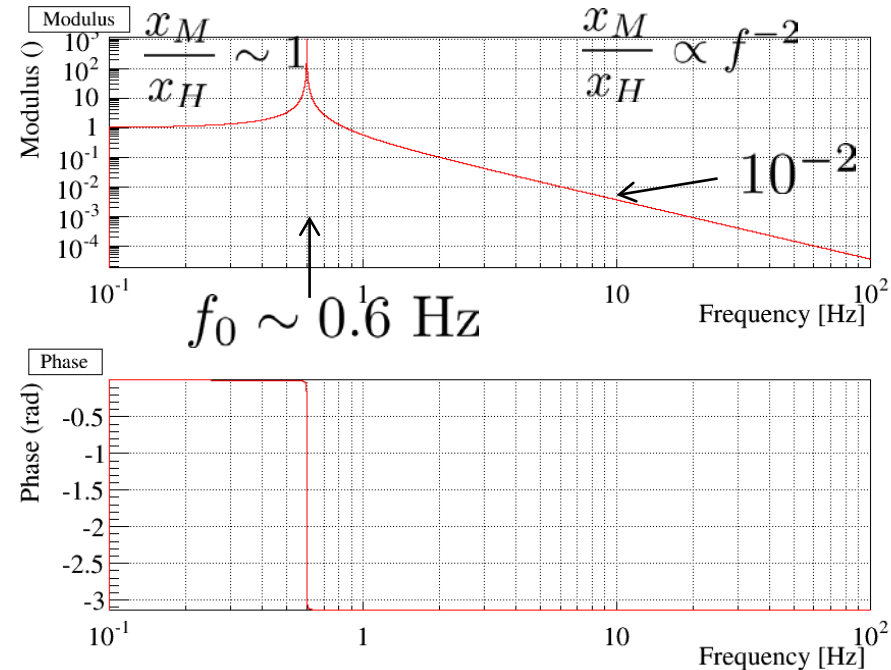
$\gg 10^{-19} \text{ m}/\sqrt{\text{Hz}}$ needed to detect GW !!



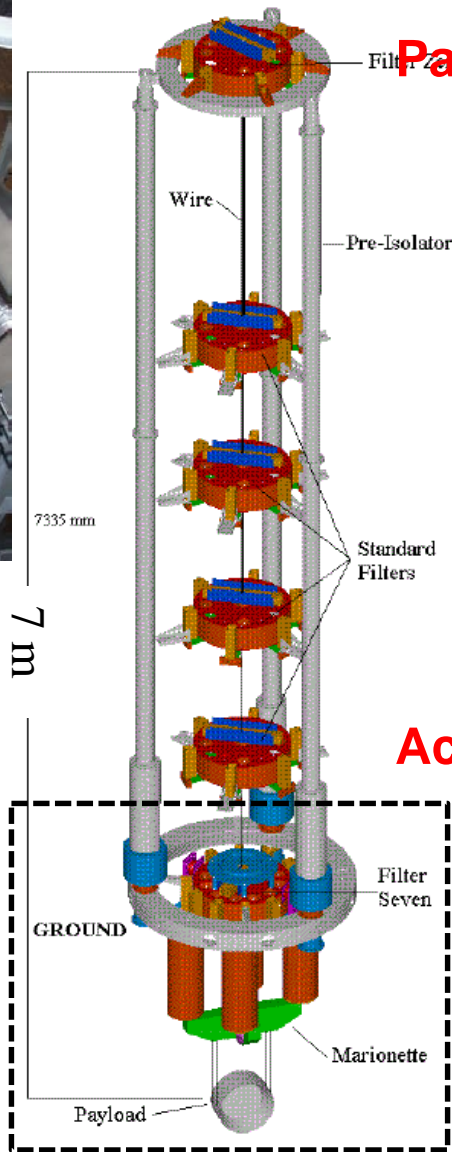
Assuming δx_H small and sinusoidal and θ small:

$$\underline{x}_M = \underline{\mathcal{H}} \times \underline{x}_H$$

Transfer function



Seismic noise: Virgo super-attenuators



Passive attenuation: 7 pendulum in cascade

$$\text{At } 10 \text{ Hz: } \frac{x_{mirror}}{x_{ground}} \sim (10^{-2})^7 = 10^{-14}$$

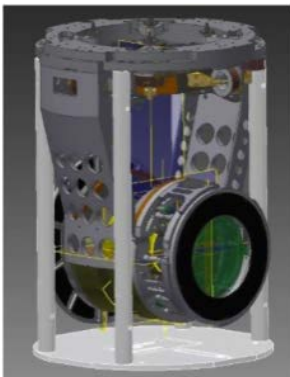
$$x_{ground} \sim 10^{-9} \text{ m}/\sqrt{\text{Hz}}$$

$$\rightarrow x_{mirror} \sim 10^{-23} \text{ m}/\sqrt{\text{Hz}}$$

This noise directly modifies the positions of the mirror surfaces, and thus $\delta\Delta L$ and $h_{rec}(t)$!

Active controls at low frequency

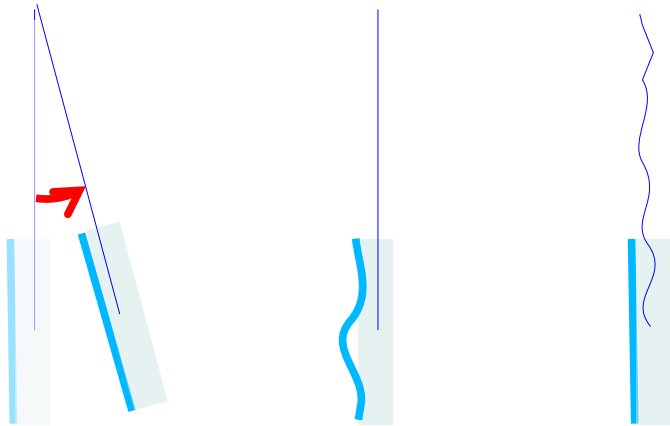
- Accelerometers or interferometer data
- Electromagnetic actuators
- Control loops



Thermal noise (pendulum and coating)

Microscopic thermal fluctuations

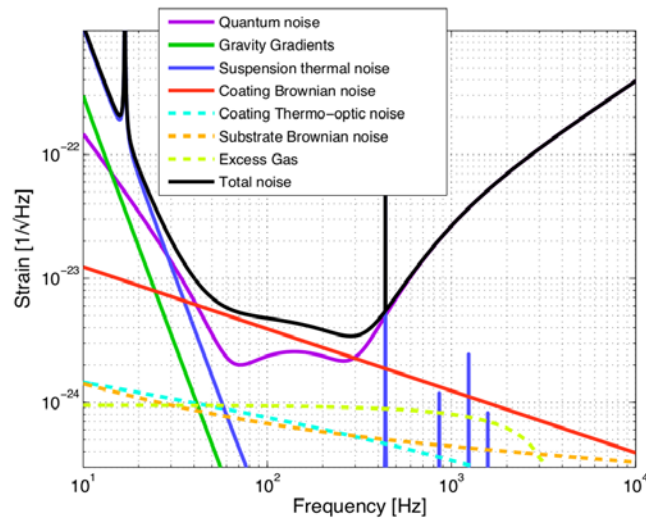
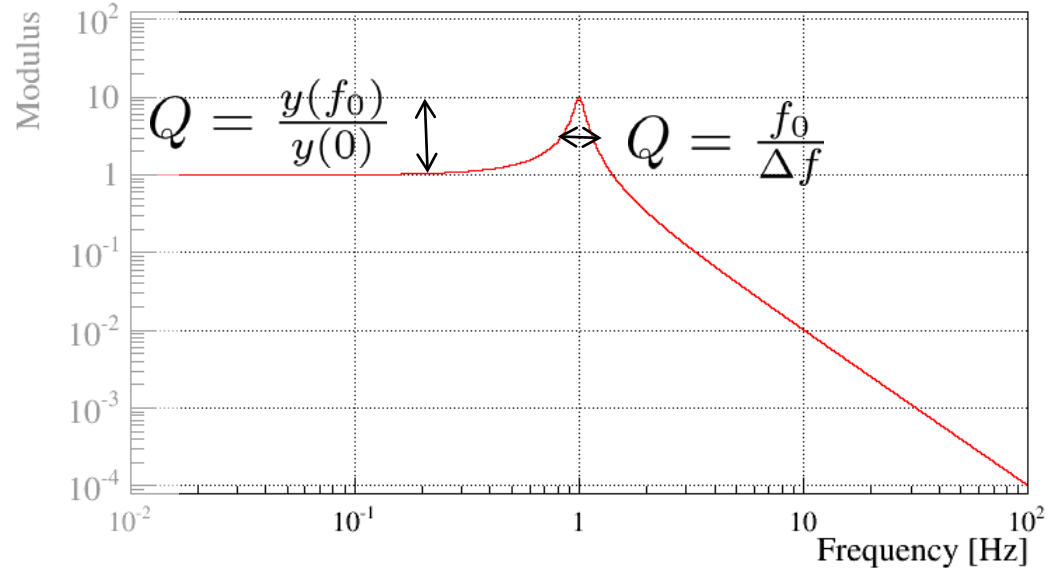
→ dissipation of energy through excitation of the macroscopic modes of the mirror



Pendulum mode
 $f < 40$ Hz

“Mirror” mode
 $f >$ few kHz

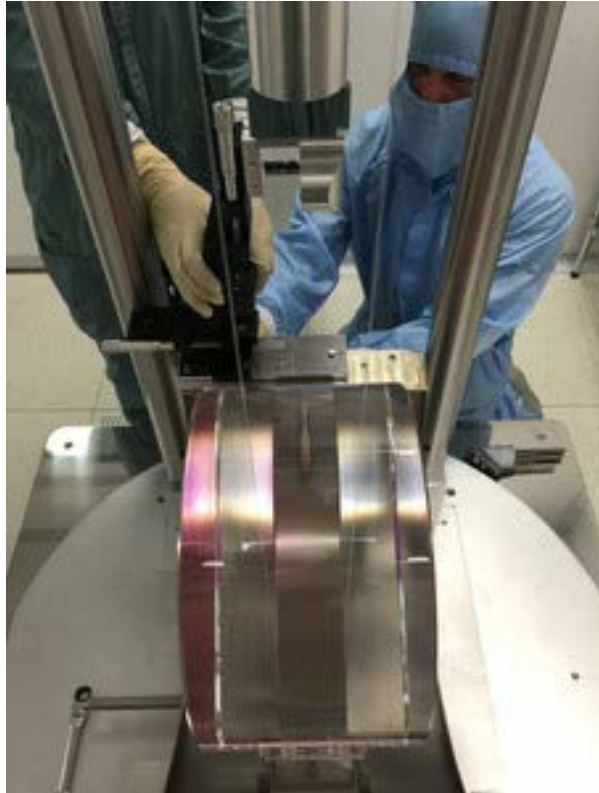
“Violin” modes
 $f > 40$ Hz



This noise directly modifies the positions of the mirror surfaces, and thus $\delta\Delta L$ and $h_{rec}(t)$!

We want high quality factors Q to concentrate all the noise in a small frequency band

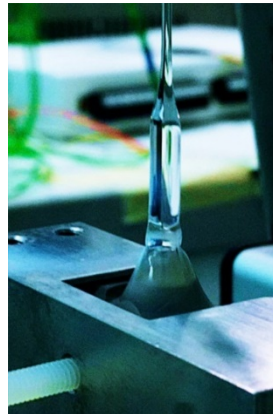
Reduction of thermal noise: monolithic suspensions



Increase the quality factor of the mirrors (wrt to steel wires):

Fused silica

- 400 μm diameter, increasing to ~ 1 mm at both ends
- 0.7 m length
- Load stress: 800 Mpa



Installed in Virgo in 2010

But failures in 2015/2016... (vacuum cleanliness issues)

... now fixed, re-installed beginning 2018

Reduction of thermal noise: mirror coating

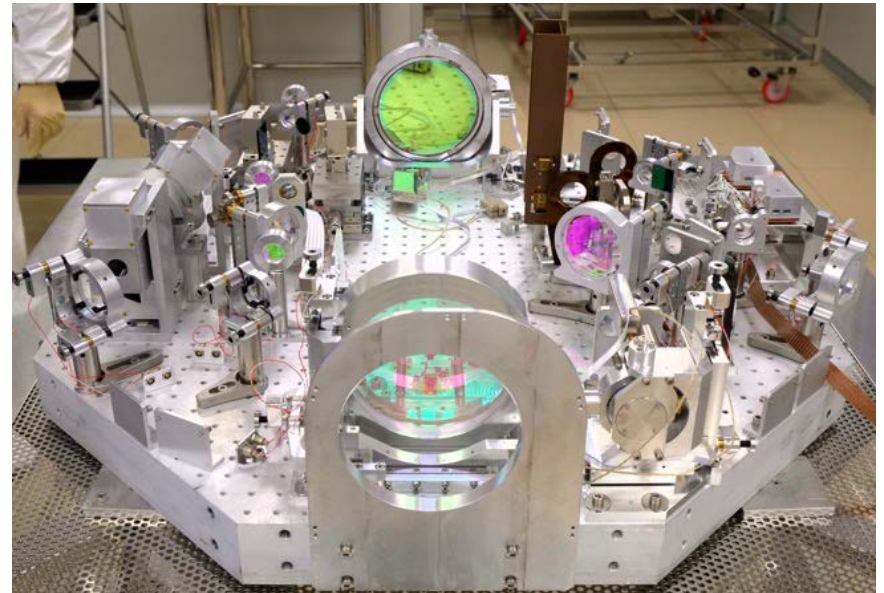
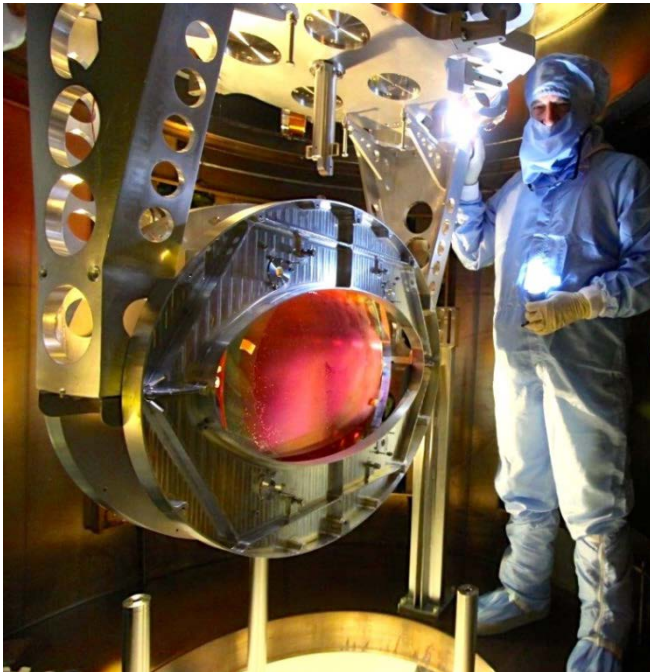
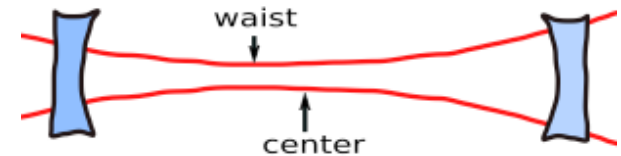


40 kg mirrors of Advanced Virgo
35 cm diameter, 40 cm width
Suprasil fused silica

- Currently the main source of thermal noise
- Very high quality mirror coating developed in a lab close to Lyon (Laboratoire des Matériaux Avancés)
- R&D to improve mechanical properties of coating
- Cryogenics mirrors (at Kagra, future detectors)
 - other substrate
 - other coating
 - other wavelength

Thermal noise: coupling reduction

- Reduce the coupling between the laser beam and the thermal fluctuations
 - **use large beams**: fluctuations averaged over larger surface
 - Thermal Noise $\sim 1/D$, with D = beam diameter
- Impact of large beams:
 - Require large mirrors (and heavier):
 - > Advanced Virgo beam splitter diameter = 55 cm
 - High magnification telescopes to adapt beam size to photodetectors (from $w=50$ mm on mirrors to $w=0.3$ mm on sensors) > require optical benches

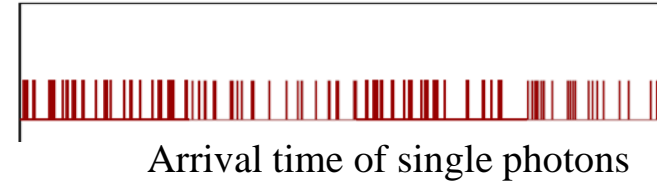


Shot noise

Fluctuations of arrival times of photons (quantum noise)

Power received by the photodiode: P_t

$$\rightarrow N = \frac{P_t}{h\nu} \text{ photons/s on average.}$$



Standard deviation on this number: $\sigma_N = \sqrt{N}$

$$\rightarrow \sigma_{P_t} = \sigma_N \times h\nu = \sqrt{\frac{P_t}{h\nu}} h\nu = \sqrt{P_t h\nu}$$

Virgo laser: $\lambda = 1.064 \mu\text{m} \rightarrow \nu = \frac{c}{\lambda} \sim 2.8 \times 10^{14} \text{ Hz}$

Working point: $P_t \sim 80 \text{ mW} \rightarrow \sigma_{P_t} = 0.1 \text{ nW}/\sqrt{\text{Hz}}$

\rightarrow a variation of power is interpreted as a variation of distance $\delta\Delta L$

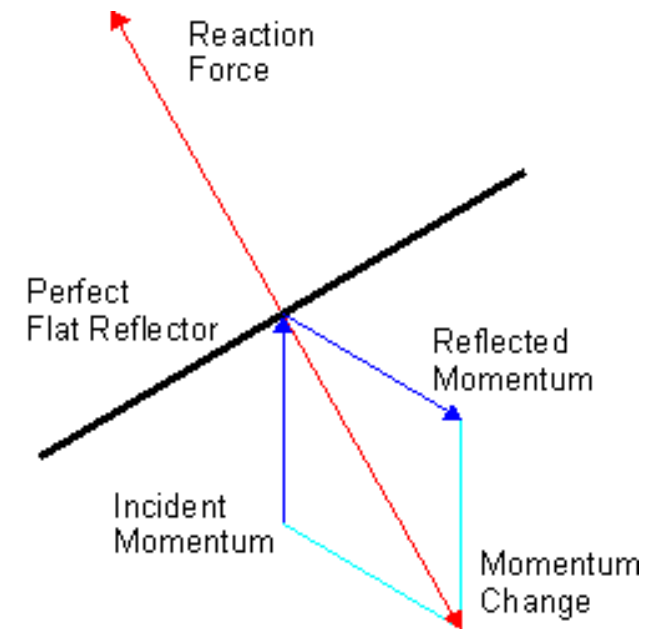
$$\delta P_t = (\text{Virgo response}) \times L_0 \times h \quad h_{\text{equivalent}} = \frac{1}{L_0} \frac{\sigma_{P_t}}{(\text{Virgo response})}$$

(in W/m)

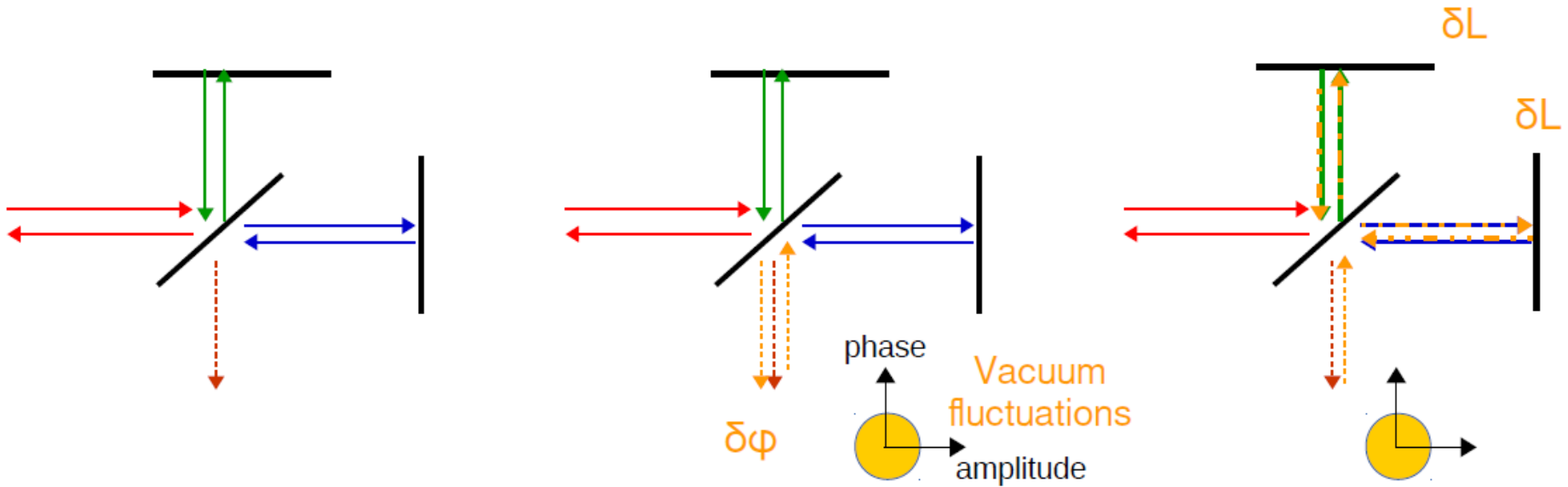
$$\rightarrow \mathbf{h_{\text{equivalent}} \propto 1/\sqrt{P_{\text{in}}}}$$

Radiation pressure noise

- Radiation pressure: transfer of photon's momentum to the reflective surface (recoil force)
- Radiation pressure noise: due to fluctuations of number of photons hitting the mirror surfaces > mirror motion noise
- Radiation pressure noise impact at low frequency:
 - > Mirror motion filtered by pendulum mechanical response



Quantum noise: shot noise and radiation pressure noise



Working point close to a dark fringe
Signal related to phase offset

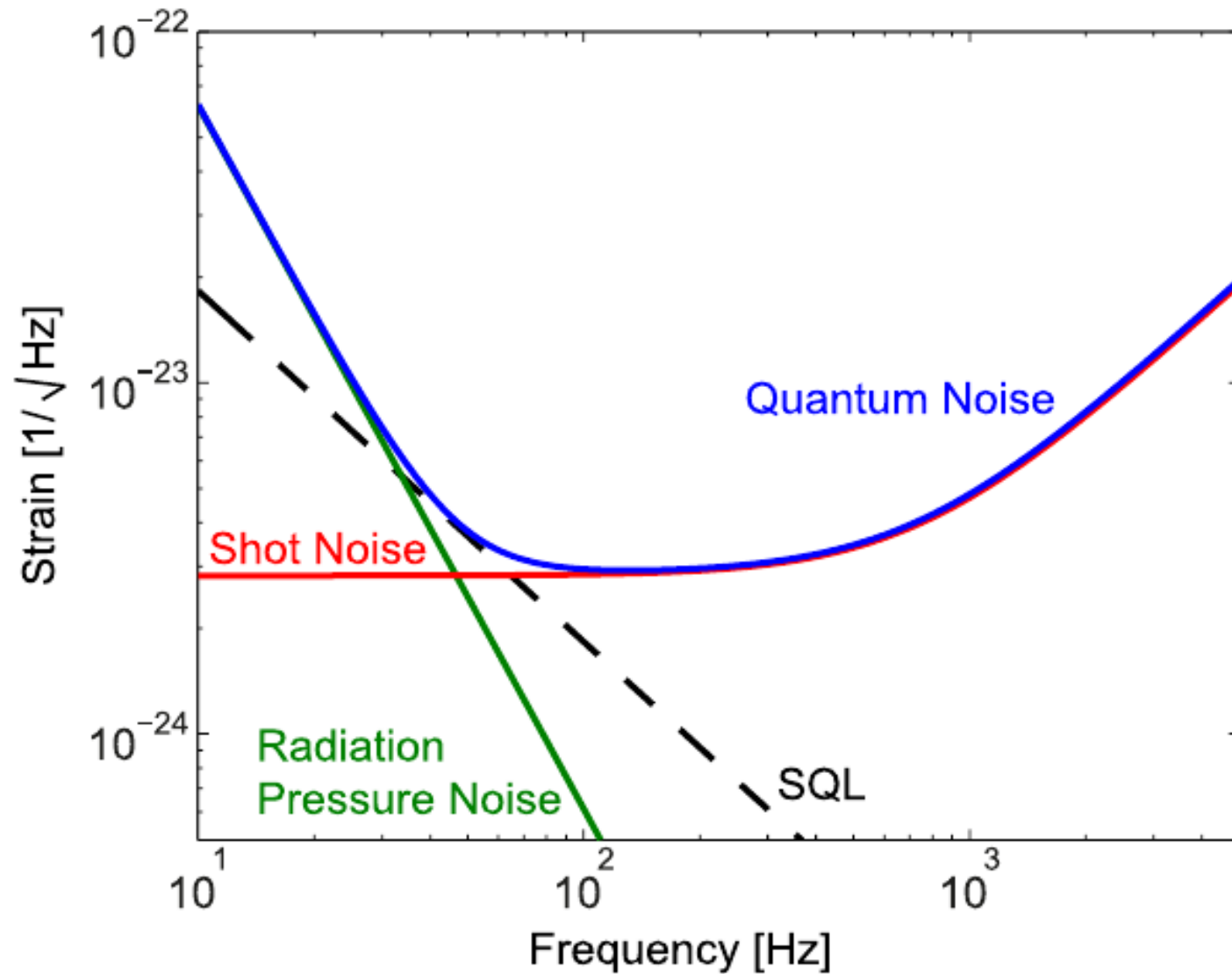
→ fluctuations of the phase
Photon shot noise

$$\propto \frac{\text{Phase fluctuation}}{\text{Laser power}}$$

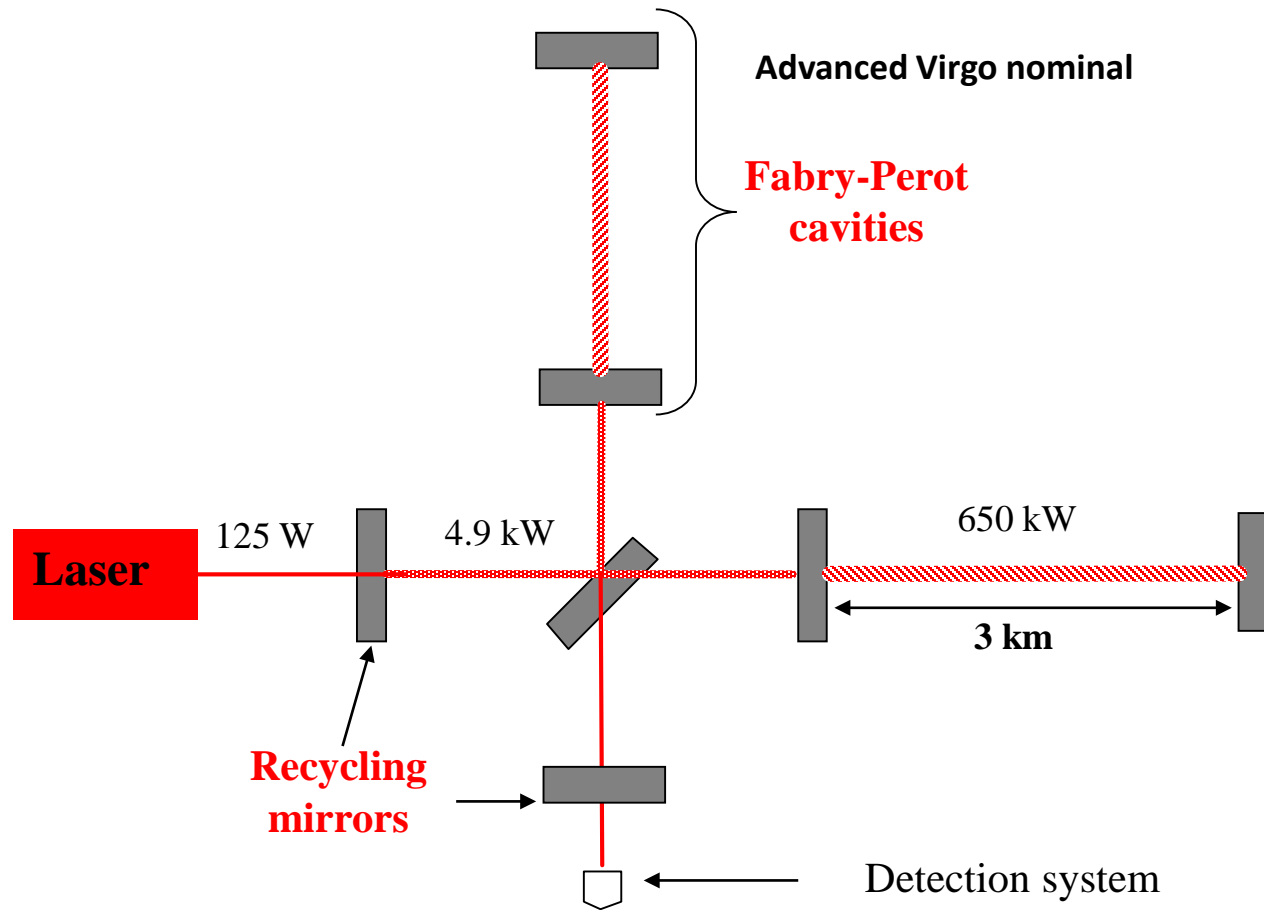
→ fluctuations of the
mirror positions
Radiation pressure noise

$$\propto \text{Amplitude fluctuation} \times \text{Laser power}$$

Quantum noise in the sensitivity



Minimizing shot noise with optical configuration



Reduction of shot noise: high power laser

Goal for AdV (nominal):

- continuous 200 W laser, stable monomode beam (TEM00), 1064 nm

Only 18W currently injected in Advanced Virgo

→ **decrease shot noise contribution**

But limited by side-effects:

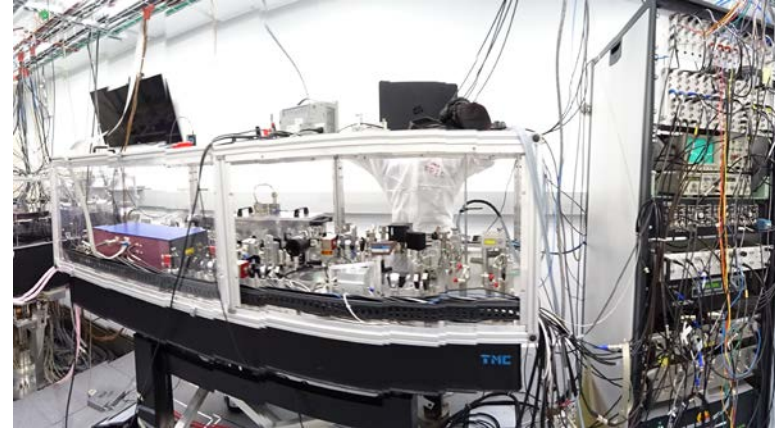
➤ Radiation pressure

- Increase of radiation pressure noise
- Cavities more difficult to control
- Parametric instabilities: coupling of laser high order modes with mirrors mechanical modes

➤ Thermal absorption in the mirrors (optical lensing)

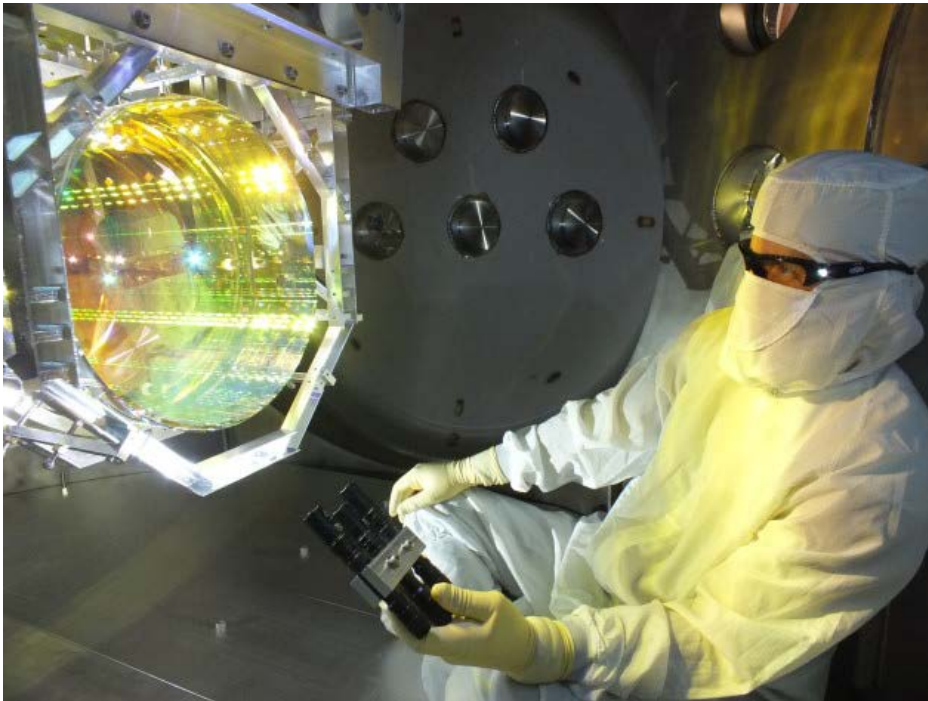
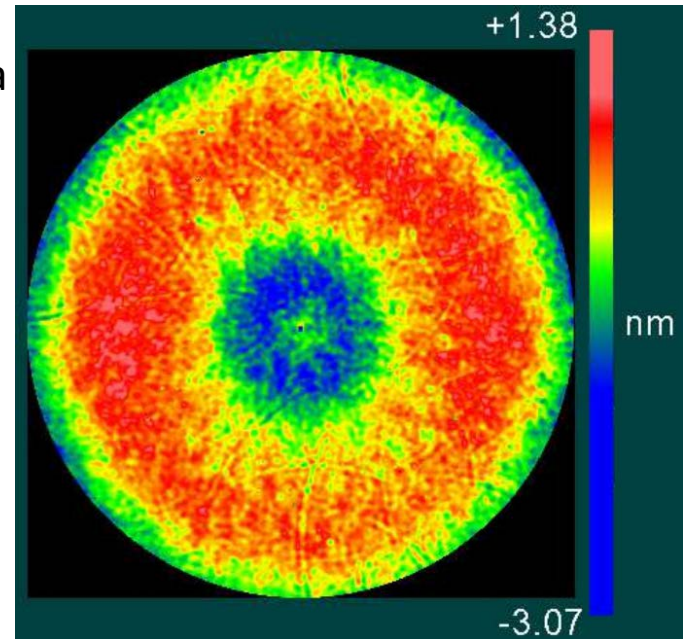
→ Need of thermal compensation system

Avoid optical losses to not spoil high power → high quality mirrors

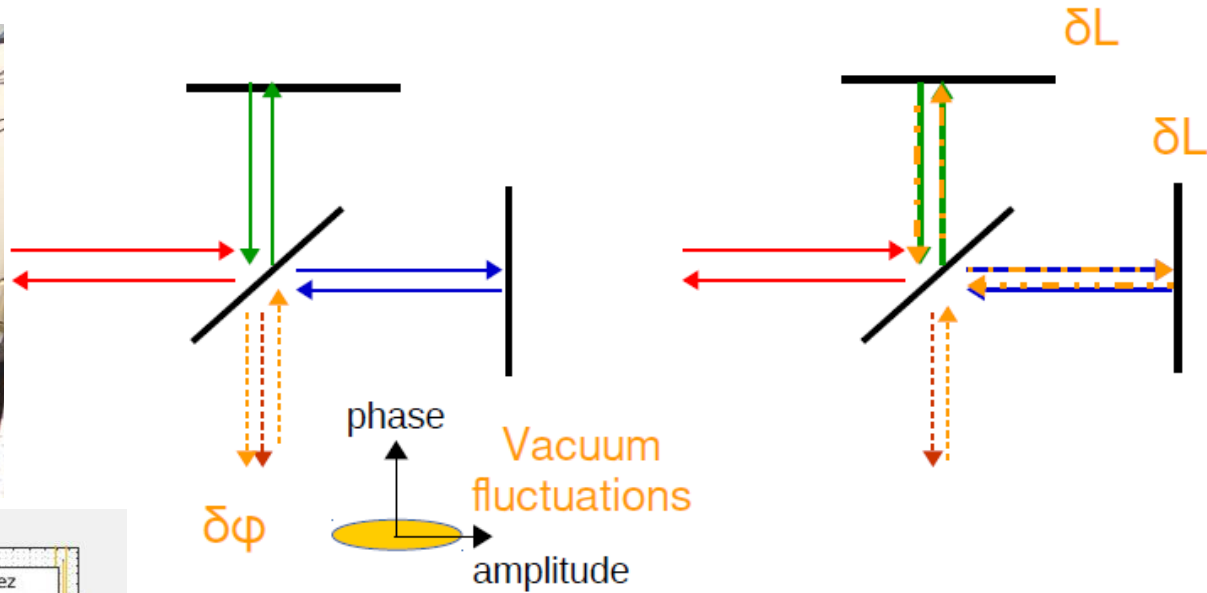


« Perfect » mirrors

- 40 kg, 35 cm diameter, 20 cm thickness in ultra pure silica
- Uniformity of mirrors is unique in the world:
 - a few nanometers peak-to-valley
 - flatness < 0.5 nm RMS (over 150mm diameter)

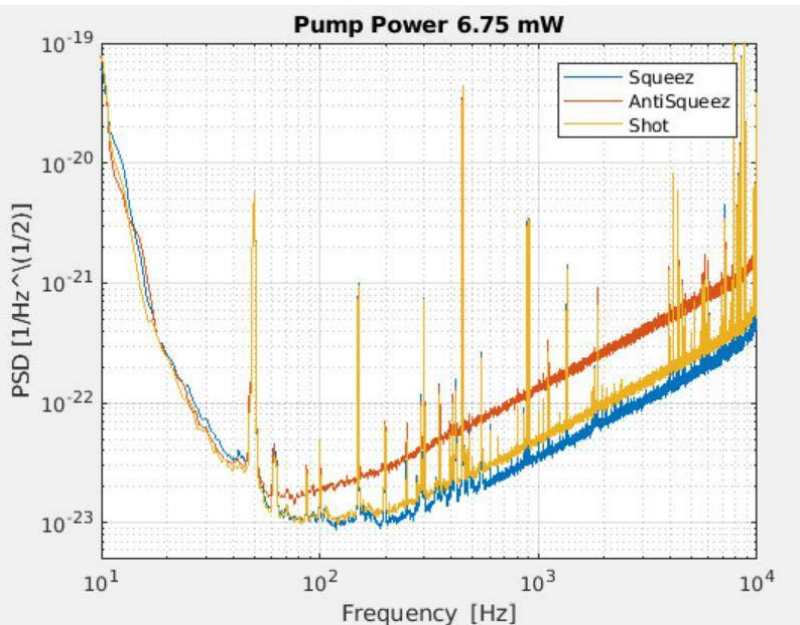


Reduction of shot noise: squeezing

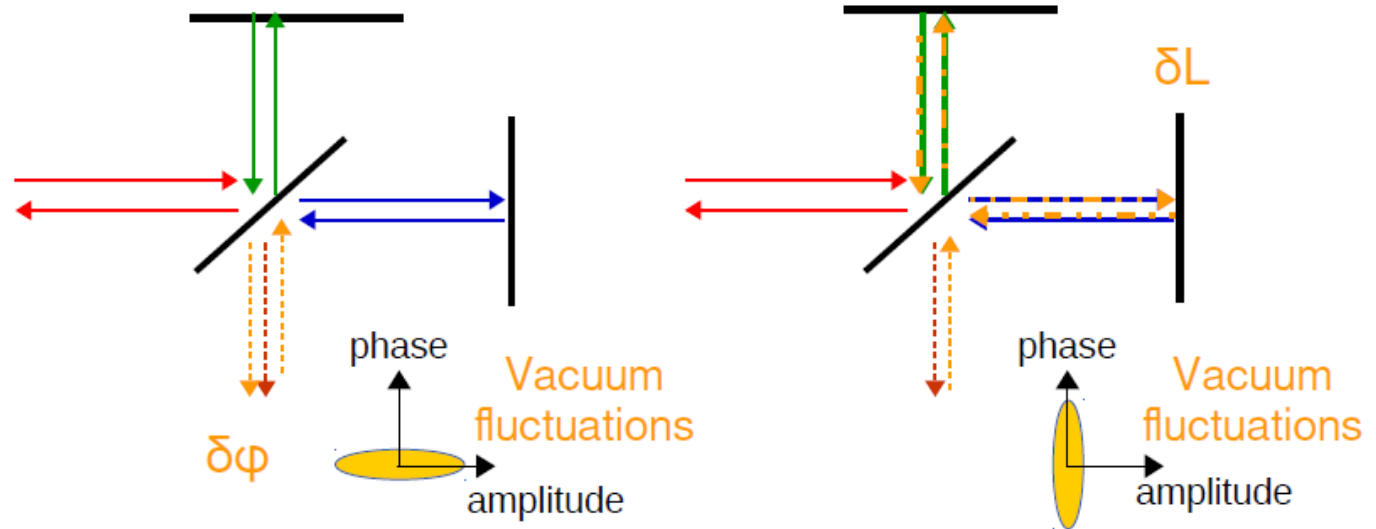


→ Decrease shot noise
 But increase radiation pressure noise

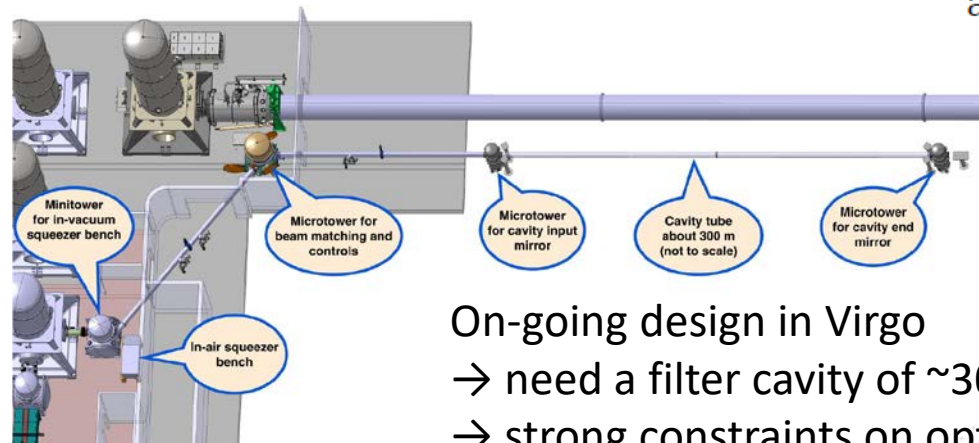
Installed in Virgo and LIGO



Reduction of quantum noise: frequency dependent squeezing



→ **Decrease shot noise
AND radiation pressure noise**



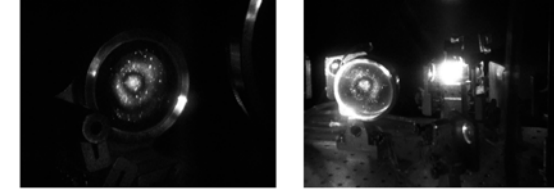
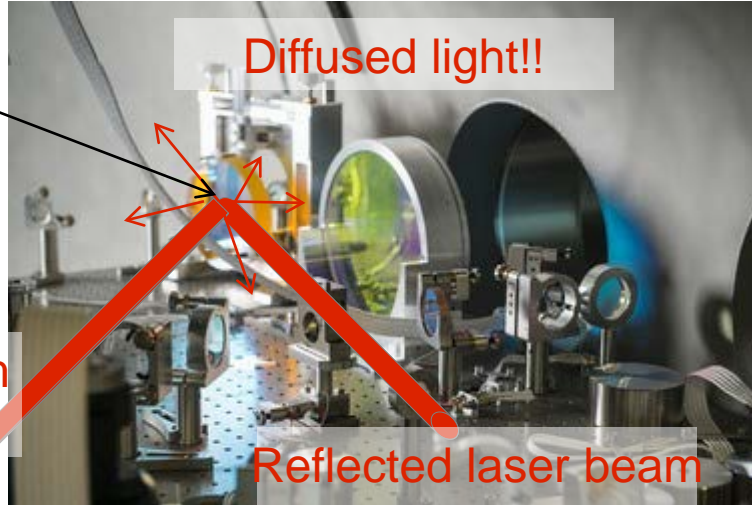
On-going design in Virgo

→ need a filter cavity of ~ 300 m, with finesse ~ 10000

→ strong constraints on optical losses, beam matching and alignment, ...
(suspended in vacuum optical benches)

Example of technical noise: Diffused light

Optical element
(mirror, lens, ...)
vibrating due to
seismic or
acoustic noises

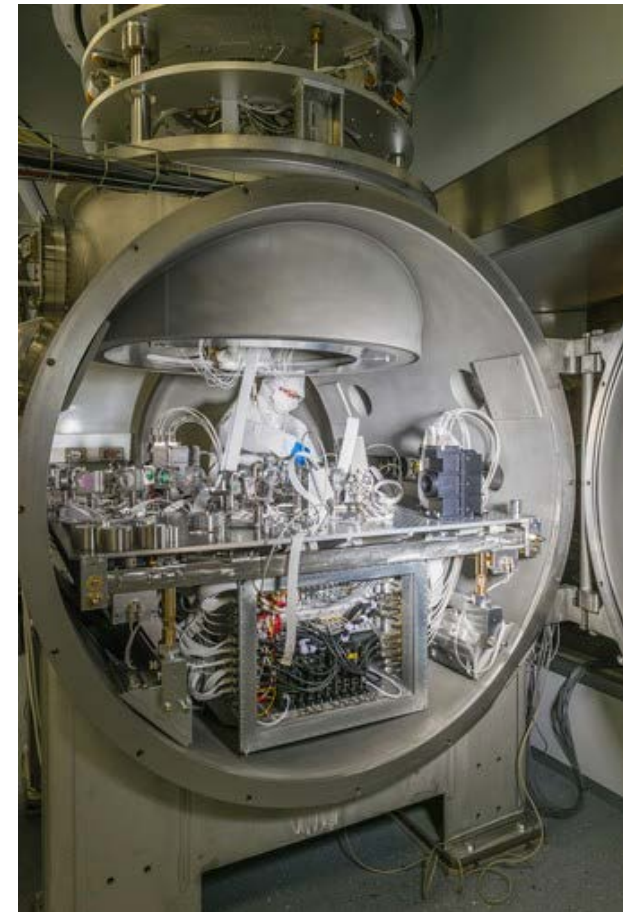


Evolution for AdVirgo: suspend
the optical benches and place
them under vacuum

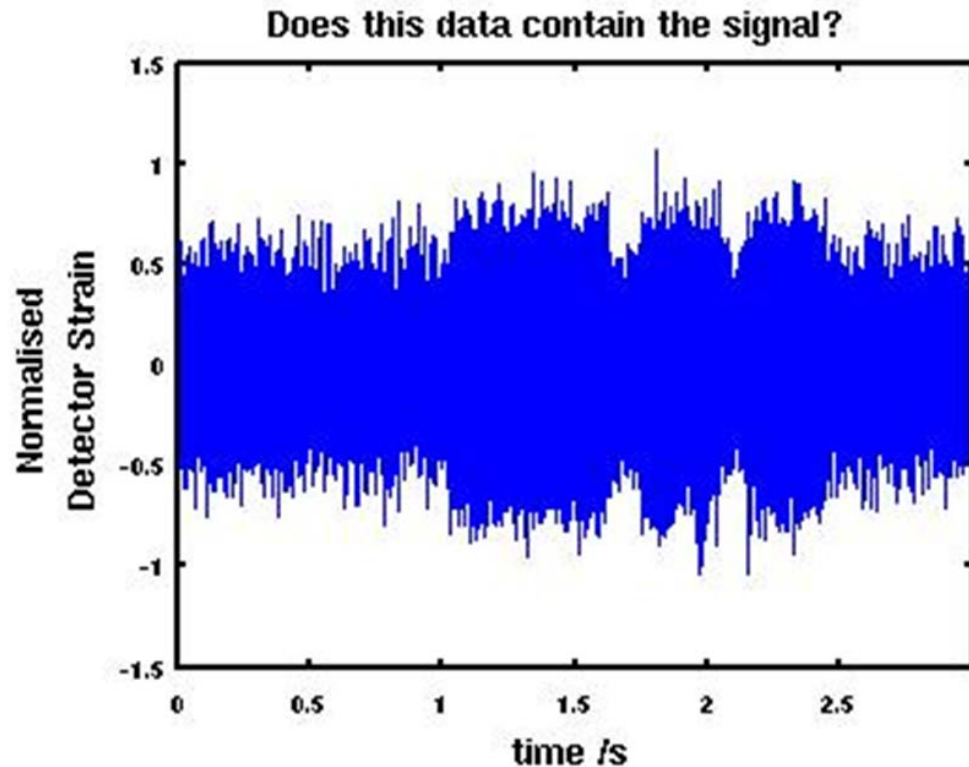
some photons of the diffused
light gets recombined with the
interferometer beam

↓
phase noise

↓
extra power fluctuations
(imprint of the optical element vibrations)



Noises are not always stationary



“Glitches” are impulses of noise.
They might look like a transient GW signal

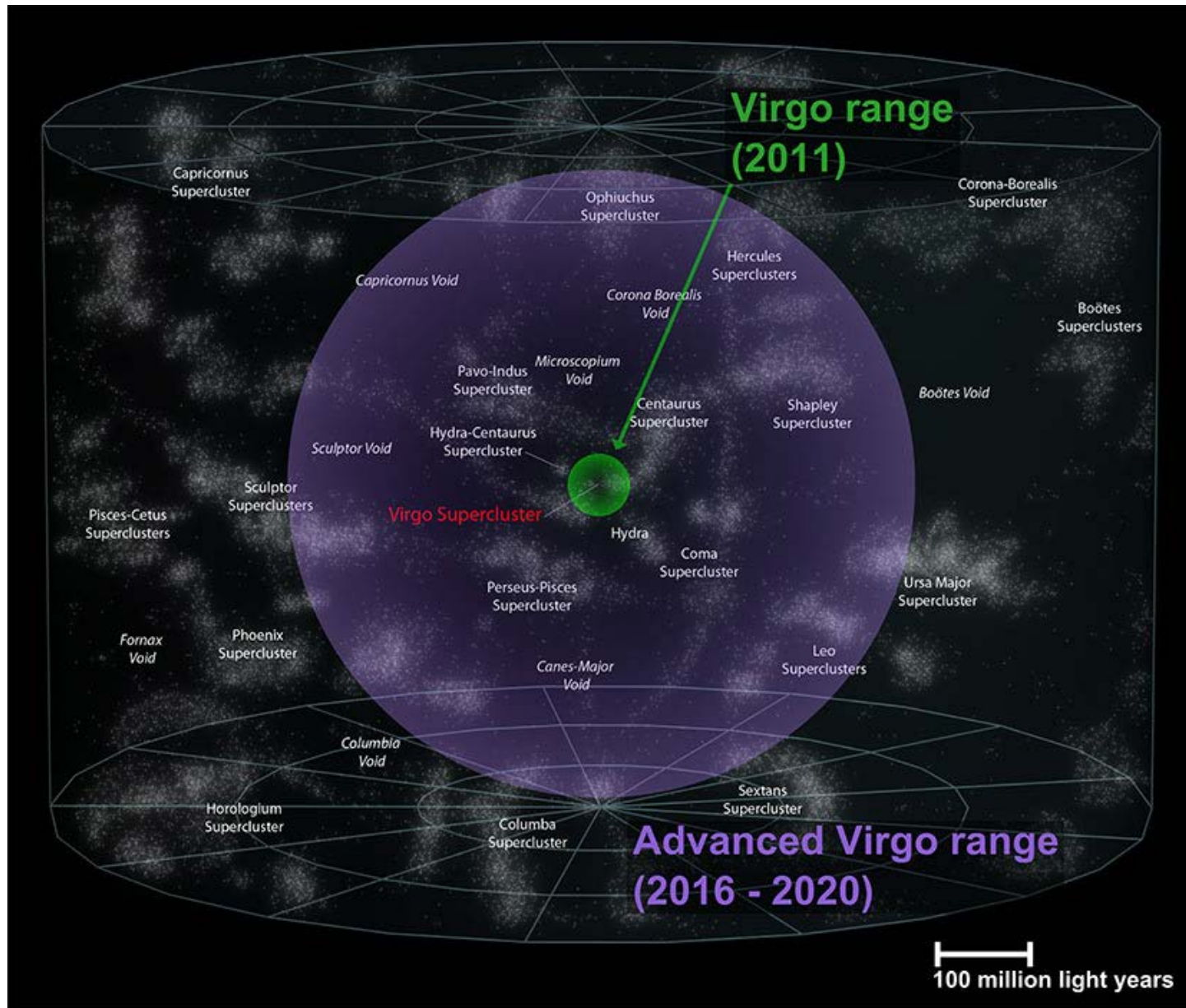


- ❑ environmental disturbances monitored with an array of sensors: seismic activities, magnetic perturbations, acoustic noises, temperature, humidity
→ used to veto false alarm triggers due to instrumental artifacts
- ❑ requires coincidence between 2 detectors to reduce false alarm rate

Table of Contents

- **How can we detect gravitational waves with laser interferometers?**
- **How do ground-based interferometers work?**
 - The Virgo optical configuration or how to measure 10^{-20} m
 - How to maintain the ITF at its working point?
 - How to measure the GW strain $h(t)$ from this detector?
 - Noises limiting the ITF sensitivity: how to tackle them?
- **Prospectives for interferometers and other detectors**

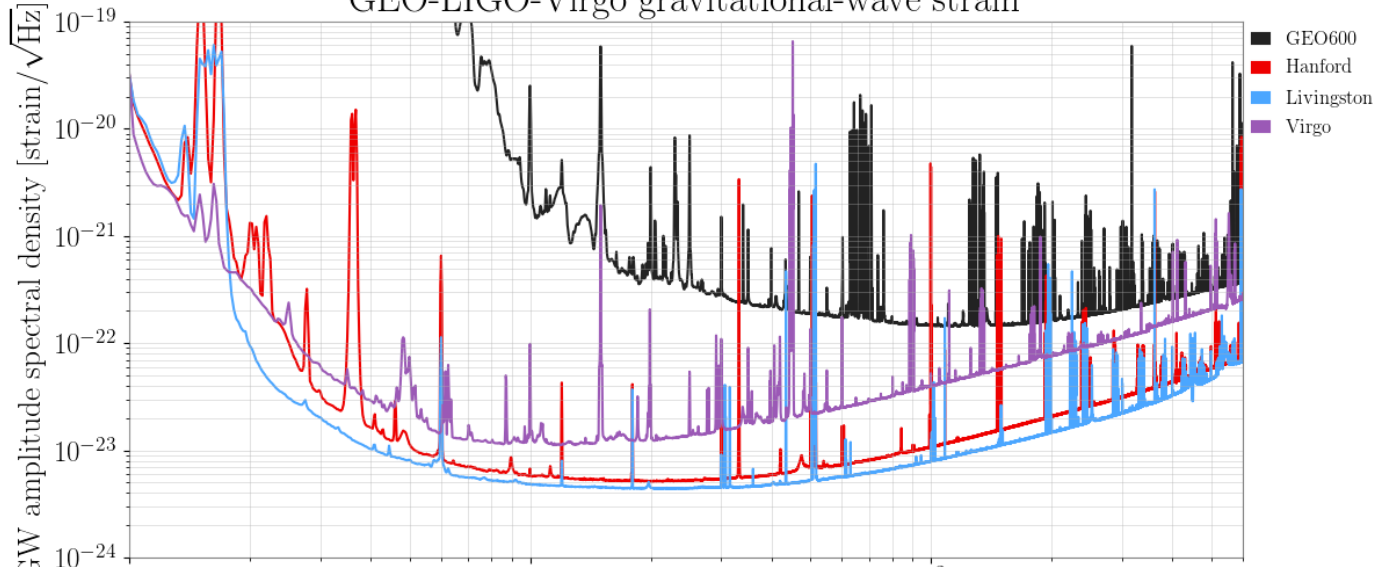
From initial to advanced detectors



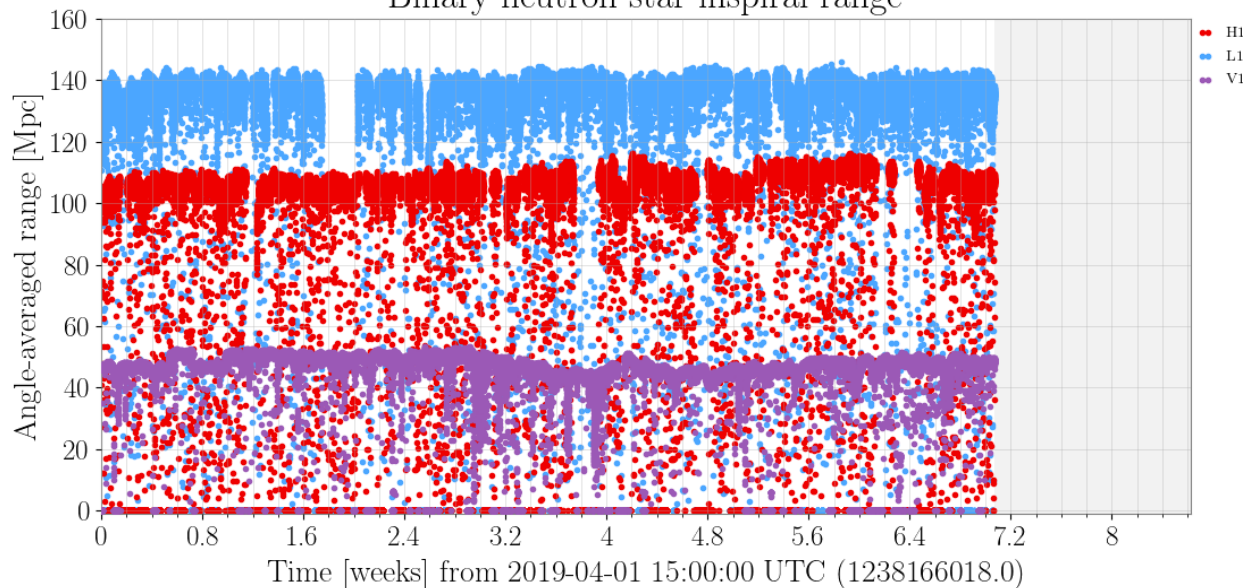
Current interferometers sensitivity

[1239062418-1239148818, state: Locked]

GEO-LIGO-Virgo gravitational-wave strain



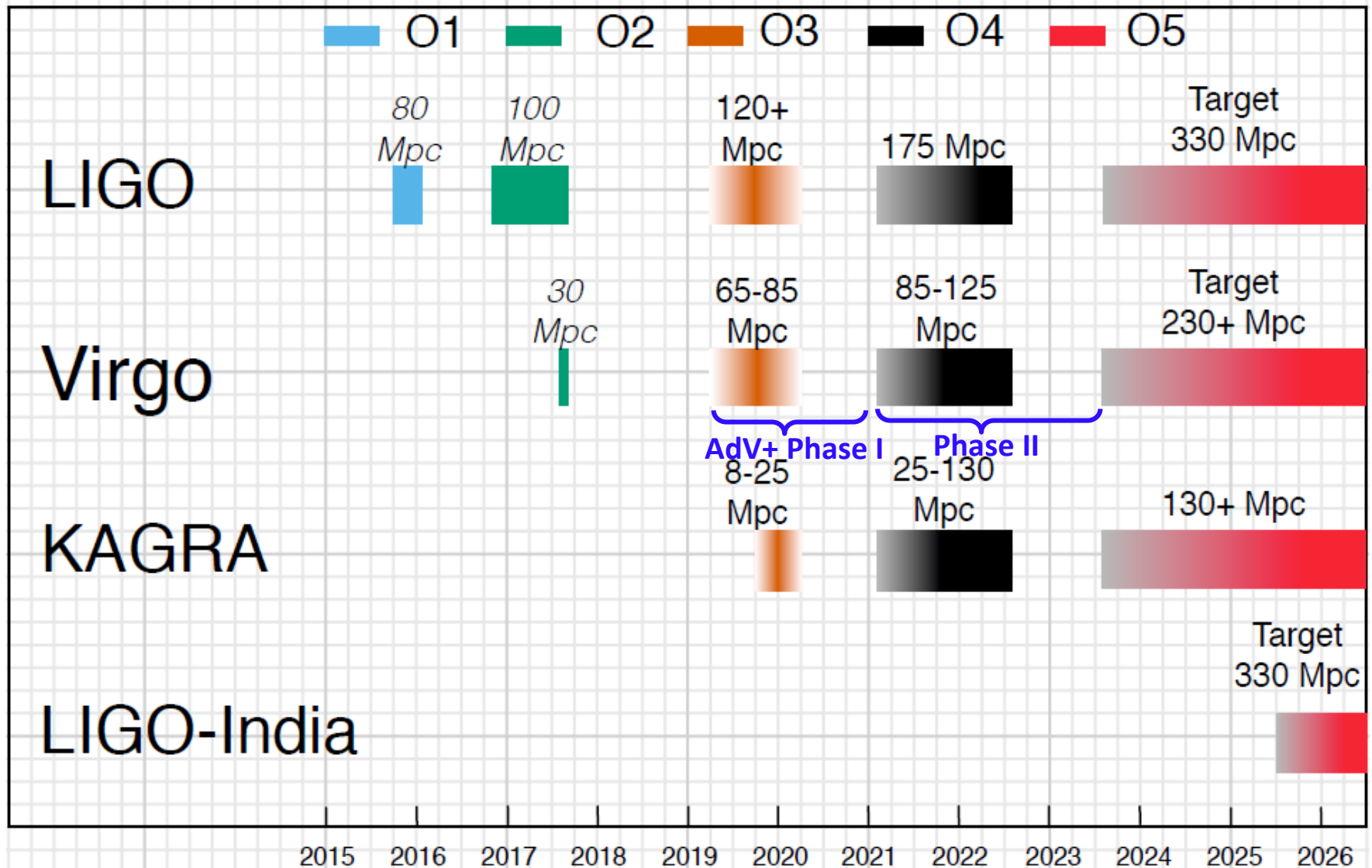
Binary neutron star inspiral range



BNS Range:

Distance at which a neutron star binary coalescence with averaged orientation over the sky can be seen with signal-to-noise ratio of 8

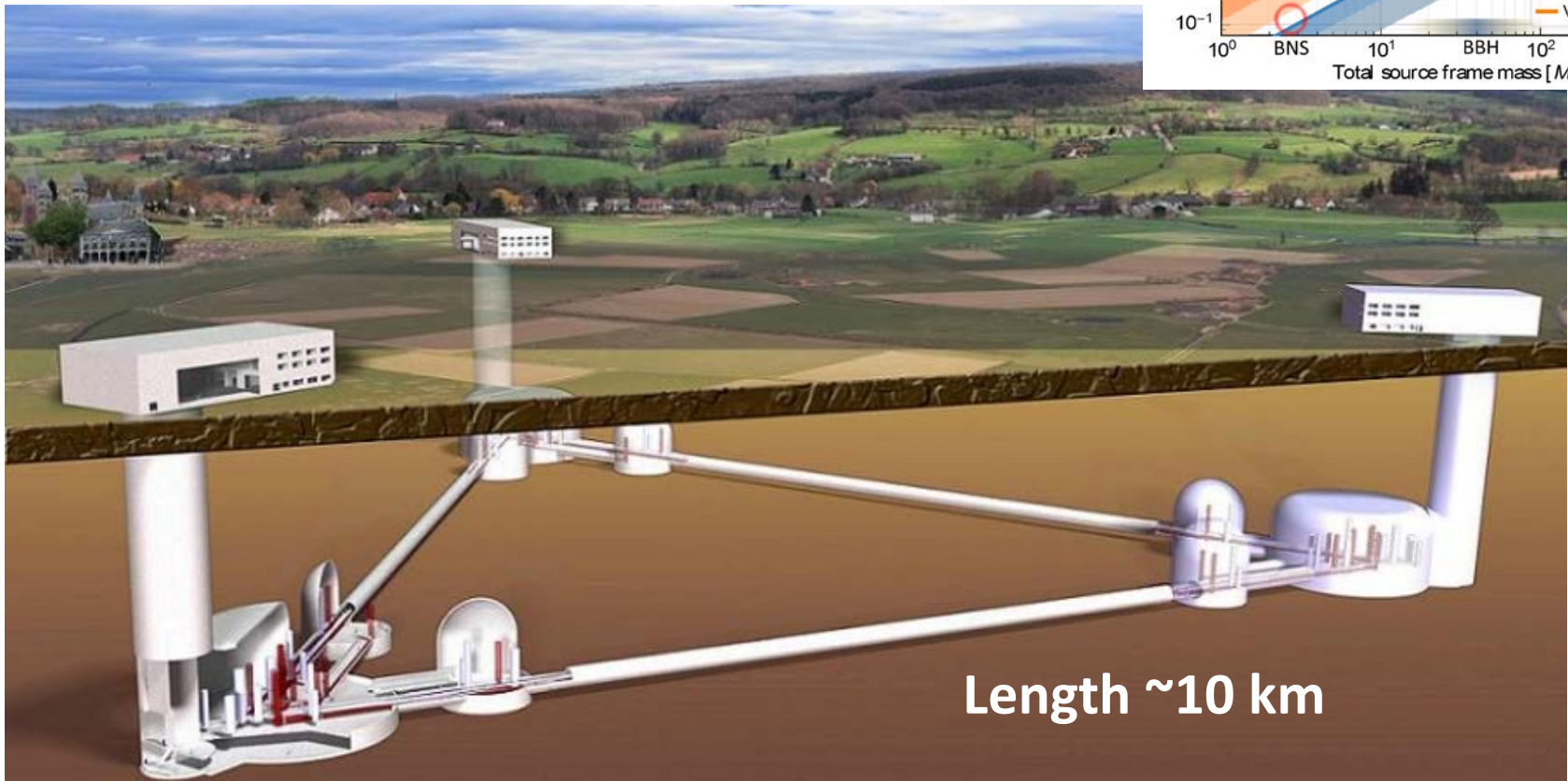
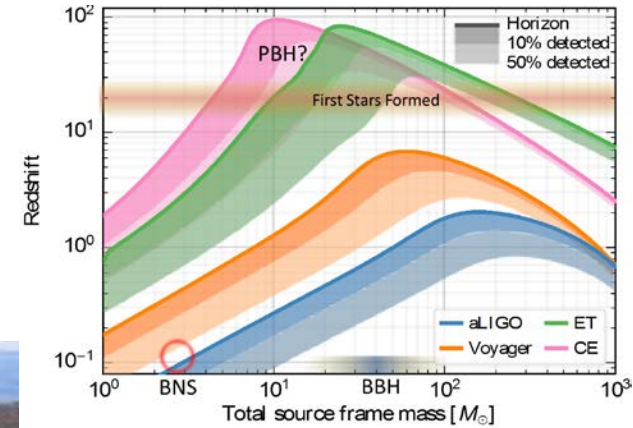
Future observing runs



Einstein Telescope

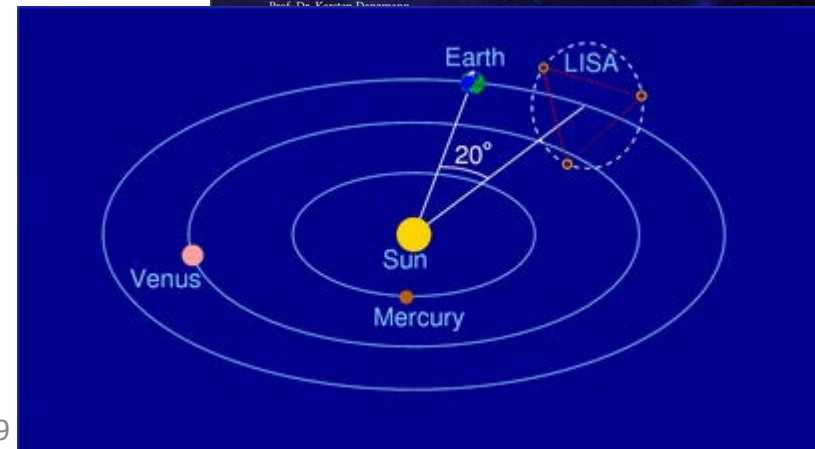
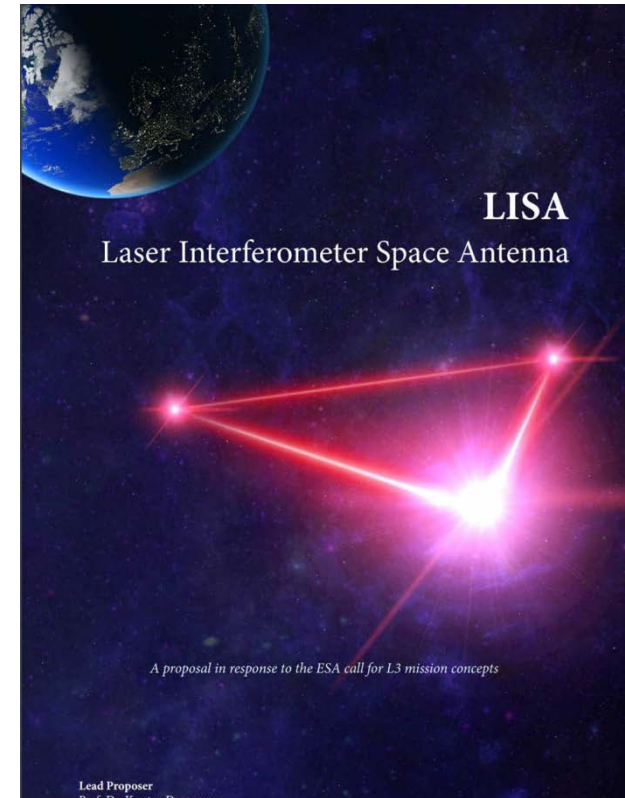
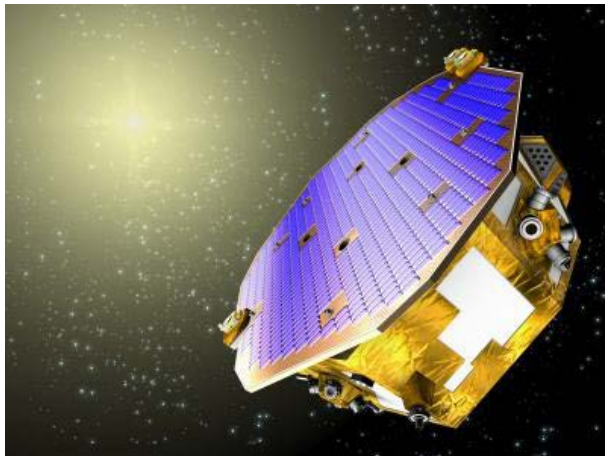
- Third generation interferometer: gain another factor 10 in sensitivity and enlarge bandwidth
- Located underground, ~10 km arms
- Thermal noise reduction with cryogenics
- Xylophone detector?
- In operation after 2030?

Could probe CBC signals from a large fraction of the Universe



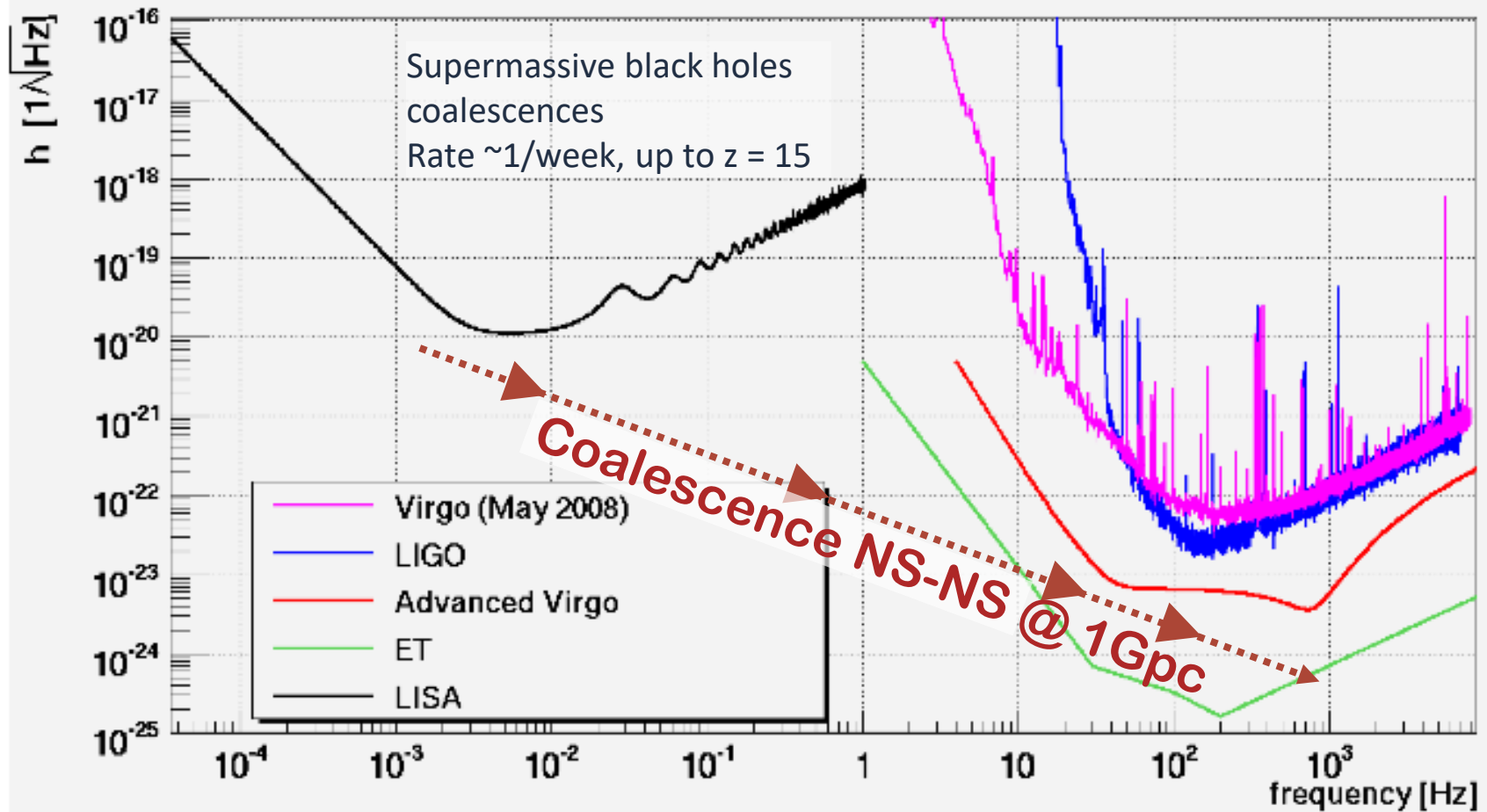
Spatial interferometer: LISA

- **Bandwidth: 0.1 mHz to 1 Hz (2.5 million km arm length)**
- Launch of LISA in the years 2030?
 - operation for 5 to 10 years
- Successful intermediate step: LISA Pathfinder
 - launched end 2015
 - test of free-fall masses
 - validation of differential motion measurements



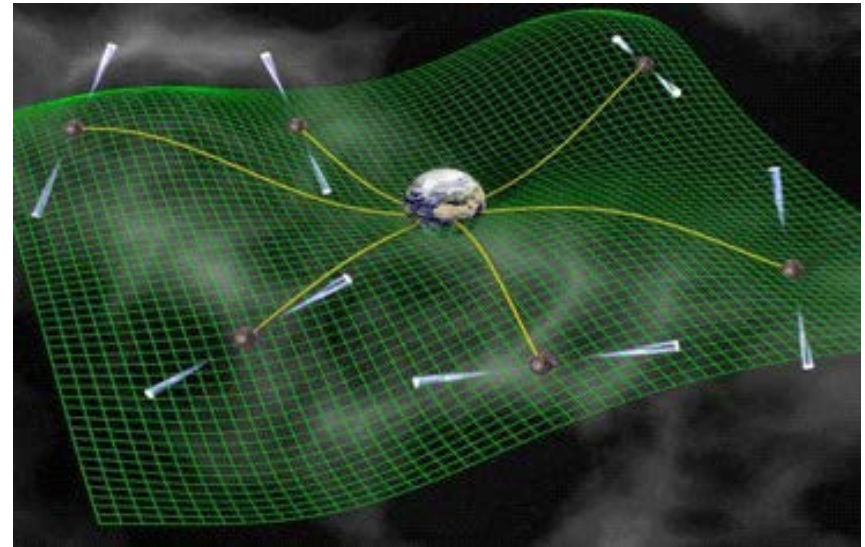
ET and LISA performances

LISA and ground based detectors sensitivities

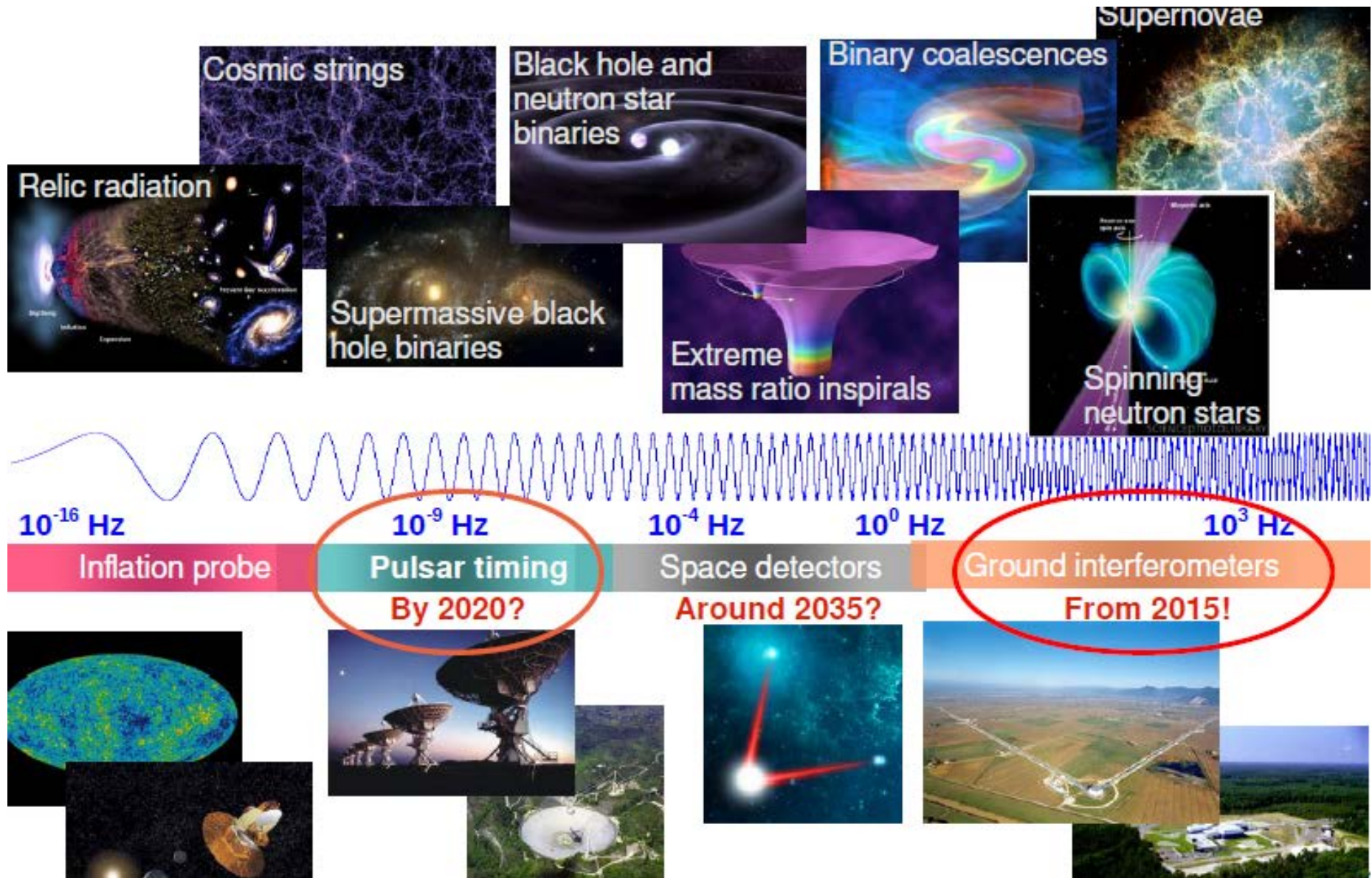


Pulsars timing arrays

- **Bandwidth: 1 nHz to 10 nHz**
- Observation of 20 ms pulsars in radio
 - Residuals of modellisation < 100 ns
 - Weekly sampling over 5 years
- International network
 - Parkes PTA
 - North American NanoHertz Gravitational Wave Observatory
 - European PTA
- **First detections expected in the coming years!**

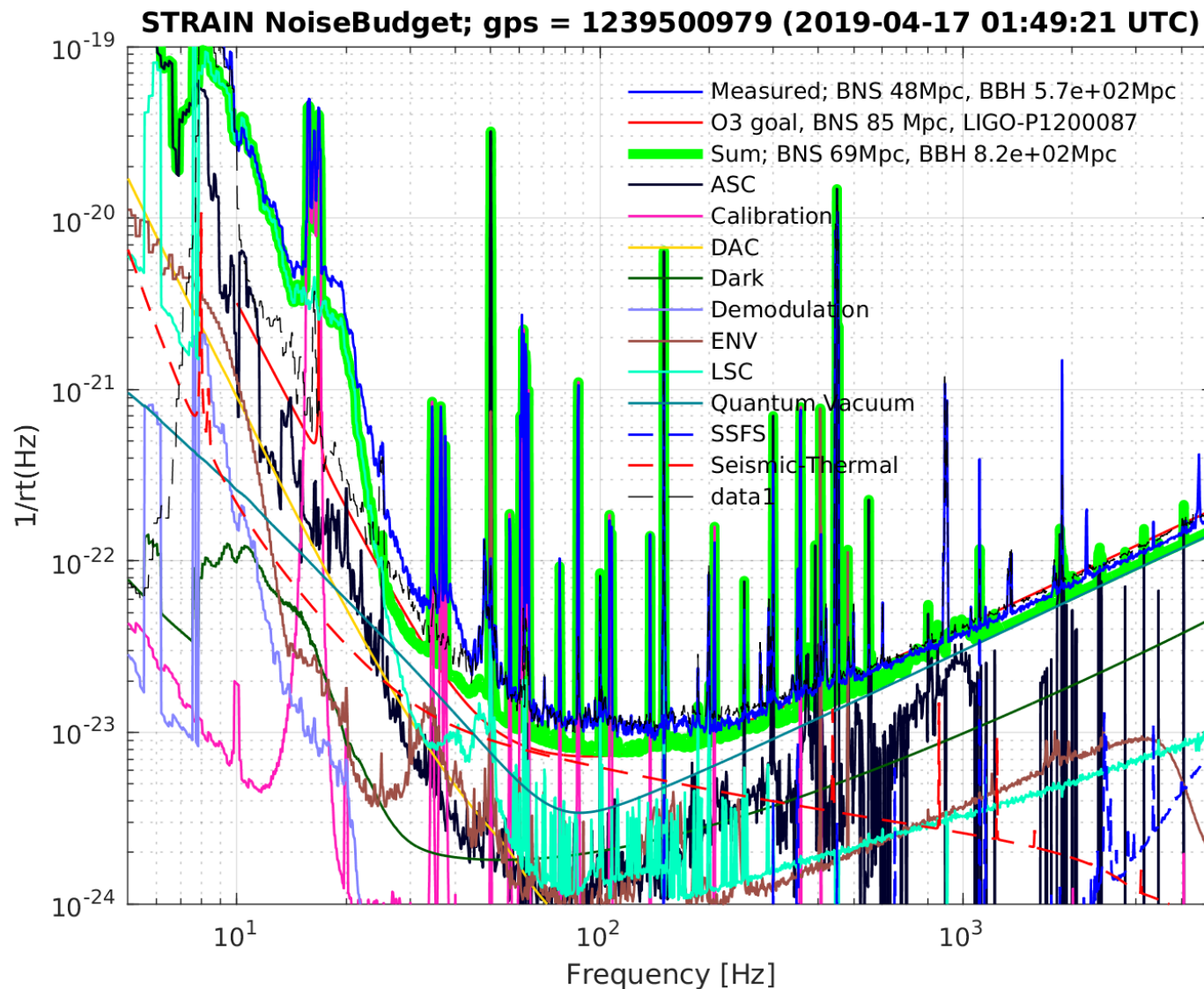


A large GW spectrum to be studied...

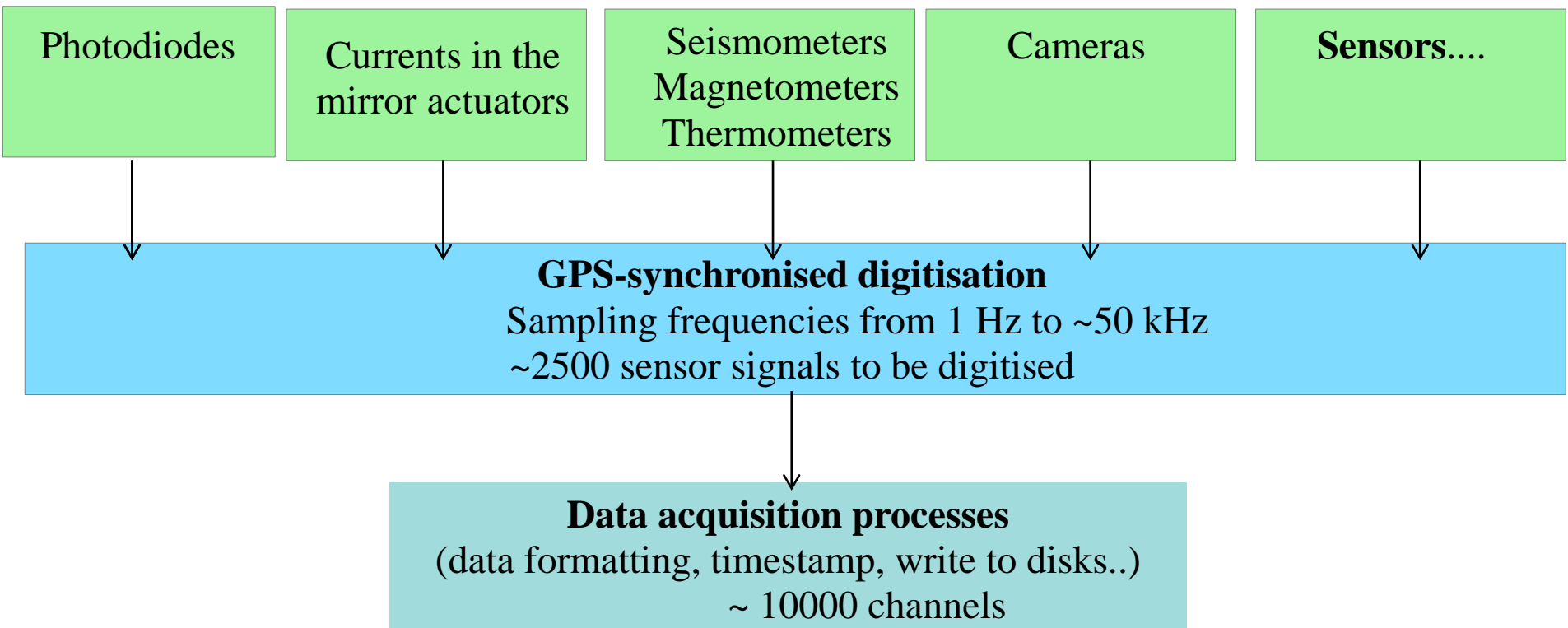


SPARES

Example of Advanced Virgo noise budget (O3 run)



Virgo data acquisition summary



→ { Continuous flow of ~3 TBytes/day (40 to 60 MBytes/s)

Disk space on Virgo site: ~400 TB for 4 months of data

Longer storage: data sent via Ethernet to computing centers (Lyon, Bologna)

Output Mode Cleaner

- 2 bow-tie Fabry Perot cavities:
 - ◆ Get rid of high order modes and controls signals.

Control signals High-order modes

