

Baryon Acoustic Oscillations



Lecturer: Pierros Ntelis

z = 48.40.05 Gyr T = Millennium Simulation 2005 **Credit: Volker Springel** 500 kpc

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Theory <--> **Observations**

Theory

- Current Picture
- Brief Thermal History
- Theoretical Framework
- Smooth Cosmology
- Perturbed Cosmology

Observations

- Observables
- Basic Statistics
- Info-limitations
- Experiments
- Statistical Inference



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Current Picture





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(Some non exhaustive!) Thermal History

- Theoretical Framework
 - **Curvature Matter** • Einstein (1915)
 - Homogeneous Solutions Friedmann (1922)
 - Lemaitre (1931) "Big Bang Paradigm"
- Cosmic Microwave Background (CMB)
 - Alpher Bethe Gamow (1948)
 - Penzias Wilson (1965)
 - Peebles Roll Dicke Wilkinson (1965)
 - Smooth Mather
- Reionization Epoch
 - Gunn Peterson (1965)
- Large Scale Structures (LSS)
 - Hubble
 - Zwicky Rubyn (1937 1970) Dark Matter
 - Riess-Schmidt-Perlmutter (1998) Acceleration
 - SDSS/2dFGRS
 - LIGO/VIRGO

(2005) **BAO Peak**

(1929) Expansion

(2006)

(2015) Gravitational Waves



Temperature Fluctuations



(t, z, T) ~ (380kyr, 1100, 0.3eV)



(t, z, T) ~ (200 Myr, 15, 5 meV)



Density Fluctuations

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Present (t, z, T) ~ (13.8 Gyr, 0, 0.24 meV)

Theoretical Framework



https://hal.archives-ouvertes.fr/tel-01674537/document

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Theoretical Framework: Smooth Cosmology

$$ds^{2} = -c^{2}dt^{2} + a^{2}(t) \left[\frac{1}{1-kr}dr^{2} + r^{2}d\Omega^{2}\right]$$

$$\overset{\text{kest}}{\bigoplus} \qquad \overset{\text{max} \circ 0}{\bigoplus} \qquad \overset{\text{max} \longrightarrow 0}{\bigoplus} \qquad \overset{\text{max} \circ 0}{\bigoplus} \qquad \overset{\text{max} \circ 0}{\bigoplus} \qquad \overset{\text{max} \circ 0}{\bigoplus} \qquad \overset{\text{max} \longrightarrow 0}{\bigoplus} \qquad\overset{\text{max} \longrightarrow 0}{\bigoplus} \qquad\overset{\text{max} \longrightarrow 0}{\bigoplus} \qquad\overset{\text{max} \longrightarrow 0}{\bigoplus} \qquad\overset{\text{m$$

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Theoretical Framework: Perturbed Cosmology

To describe density fluctuations:
$$\rho(t, x) = \bar{\rho}(t) [1 + \delta(t, x)]$$

We need a perturbed metric:
 $ds^2 = -[1 + 2\Psi(\vec{x})] dt^2 + a^2(t) [1 + 2\Phi(t)] d\vec{x}^2$
Perturbed Boltzmann-Einstein Equations:
 $\mathcal{D}_t f_X(\vec{x}, \vec{p}, t) = \mathcal{C}[f_X(\vec{x}, \vec{p}, t)]$
Distribution of Species X: f_x(x,p,t)
Evolution Term Collision Term

Well defined Derivative: $\mathcal{D}_t = \partial_t + a^{-1}(t)\hat{p}^i + \partial_t \Phi(t) + a^{-1}(t)\hat{p}^i\partial_i\Psi(\vec{x})$

8 coupled differential equations, see: Dodelson, 2003



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Theoretical Framework: Perturbed Cosmology

$$\begin{split} & \Psi(\mathbf{n}) \quad \text{Spatial Curvature Field} \\ & \dot{\delta} + ikv = -3\dot{\Phi} \quad \text{continuity eq.} \\ & \dot{v} + \frac{\dot{a}}{a}v = -ik\mu\Psi \quad \text{velocity eq.} \\ & \dot{v} + \frac{\dot{a}}{a}v = -ik\mu\Psi \quad \text{velocity eq.} \\ & \dot{\delta}_{b} + ikv_{b} = -ik\mu\Psi \quad \text{velocity eq.} \\ & \dot{\delta}_{b} + ikv_{b} = -ik\mu\Psi \quad \frac{\dot{\tau}}{R} \left[v_{b} + 3i\Theta_{1} \right] \\ & \dot{b}_{b} + \frac{\dot{a}}{a}v_{b} = -ik\mu\Psi + \frac{\dot{\tau}}{R} \left[v_{b} + 3i\Theta_{1} \right] \\ & \dot{\Theta} + ik\mu\Theta = -\dot{\Phi} - ik\mu\Psi - \dot{\tau} \left[\Theta_{0} - \Theta + \mu v_{b} - \frac{1}{2}L_{2}(\mu)\Pi \right] \\ & \Pi = \Theta_{2} + \Theta_{P2} + \Theta_{P0} \\ & \dot{\Theta}_{\nu} + ik\mu\Theta_{\nu} = -\dot{\Phi} - ik\mu\Psi \quad \text{trivial neutrini extension} \\ \end{split}$$

Ma & Bertschinger arxiv:9506072 citations(1161), Dodelson 2003

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Perturbed Einstein-Boltzmann Equations



P(k): Solutions, i.e. Theoretical Prediction

$$\langle \delta(\vec{k})\delta^*(\vec{k}')\rangle = (2\pi)^3 \delta_D^3(\vec{k} - \vec{k}')P(k)$$

<...>: ensemble average over the whole distribution





CLASS (<u>http://class-code.net/</u>), CAMB (<u>https://camb.info/</u>) software



Power spectrum of the large scale matter density inhomogeneities



Normalized scale independent linear growth-factor: the wavelength-independent growth of matter at late times



CLASS (http://class-code.net/), CAMB (https://camb.info/) software

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Theoretical Framework



https://hal.archives-ouvertes.fr/tel-01674537/document



Theory <--> Observations

Basic aspects of this ACDM model:

- -Initial Conditions: Primordial fluctuations,
- Inflation ?
- Expansion
- -Acceleration
- -Statistical homogeneity and isotropy on large scales

-Baryon Acoustic Oscillations (BAO)

Cosmological Constant Problem

Can these phenomenological aspects, be described in a better way than standard GR, Λ ?



Baryon Acoustic Oscillations (Briefly)

~300,000yr after Big Bang

The universe was hot and dense.

Fout : b, I, γ interact -> high Temperature -> kinetic energy -> outward Pressure

Fin. : Attractive gravitational potential of matter

Counteracting forces create acoustic oscillations to the structures

~360,000yr after Big Bang (Recombination)

The universe cools down at a point were the baryons are combined with the leptons Acoustic oscillations "freeze" at the very large scales

- ~380,000yr after Big Bang (Decoupling) The photons cannot interact anymore with atoms => free stream as CMB Frozen BAO start evolve with time
- ~13Gyr after Big Bang (Today) We observe these frozen BAO in the universe:

Either in the late universe with density fluctuations of the galaxy distributions or. In the early universe with

temperature fluctuations of the total matter distributions

Note: These is a very, very rough description!!



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Baryon Acoustic Oscillations (Briefly)



CREDIT: <u>http://caastro.org/</u> https://www.youtube.com/watch?v=jpXuYc-wzk4





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Observations: What else is out there?

Large Scale Structures (LSS) Galaxy Clustering (GC) strain (10-21 MINUIT 0.25 0.30 0.35 0.40 МСМС 100 Time (s) DR12 CMASS sample $\Delta n/n$ 80 $s^{2}\xi_{0}(s) [h^{-2}Mpc^{2}]$ 60 1703.00052 **SDSS-IV** 40 2.75 20 2.50 2.25 2.00 1.75 0 **BAO** peak positio .50 1.25 1 1.00 0.75 0.50 0.25 0.00 20 120 140 160 40 60 80 100 $s[h^{-1}Mpc]$

Cosmic Microwave Background (CMB)



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Gravitational Waves (GW)





GW speed

GW Damping

GW Dispersion

GW Oscillations

Super Novae Type Ia (SN-Ia) **Standard Candles**







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Observations: What is a structure?





Observations: Observables







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Observations: Observables

1pt Stat: Overdensity $\delta(t;r) = \frac{n(t;r) - \bar{n}(t)}{\bar{n}(t)}$

2pt Stat: 2pt Correlation Function

$$< \xi(t; r_1, r_2) > = < \delta(t; r_1) \delta^{\star}(t; r_1, r_2) >$$

$$= < \xi(t; r_1 - r_2) >$$

$$= < \xi(t; |r_1 - r_2|) >$$

$$= < \xi(t; r) >$$

$$= < \xi(t; r) >$$

$$Due to:$$

$$Homogeneity$$

$$+$$

$$Isotropy$$

2pt Stat: Power Spectrum

Fourier Transform

$$\xi(r) = \int \frac{d^3k}{(2\pi)^3} P(k) e^{-ikr}$$

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Observations: ξ-Observable

Two-Point Correlation Function (2PTCF): ξ(r)

$$dP_{pair}(r) = \bar{n}^2 \left[1 + \xi(r)\right] d^3r$$

ξ-definition: Excess probability to find another galaxy in the neighbourhood of the observed one separated by a given distance r.



Observer



independence ξ(r) = 0 : no Correlation homogeneity

 $\xi(r) < 0$: anti-correlation



Observable: Count-in-Cells

- Select a galaxy as a center
- Create a sphere of radius r
- Compute number of galaxies
- repeat for every galaxy
- compute the mean dd(r)
- repeat for different scales



Randoms: Same Selection function





Observable: ξ-Observable

Estimator of ξ

dd(r): number of data catalog pairs rr(r): number of random catalog pairs

Optimal Estimator (Landy & Szalay 1993)

$$\xi_{ls}(r) = \frac{dd(r) - 2dr(r) + rr(r)}{rr(r)}$$



Observable: Measure Distances





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Observable: Measure Distances



Observed Power Spectrum





Anisotropic Clustering: Alcock Pascynscki Test



Two ingredients are important:

-A way to measure distances of a distribution

-A way to study the distribution



Anisotropic Clustering: Alcock Pascynscki Test



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Anisotropic Clustering: Alcock Pascynscki Test



Figure 5. The measured pre-reconstruction correlation function (left) and power spectrum (middle) in the directions perpendicular and parallel to the line of sight, shown for the NGC only in the redshift range 0.50 < z < 0.75. In each panel, the color scale shows the data and the contours show the prediction of the best-fit model. The anisotropy of the contours seen in both plots reflects a combination of RSD and the AP effect, and holds most of the information used to separately constrain $D_M(z)/r_d$, $H(z)r_d$, and $f\sigma_8$. The BAO ring can be seen in two dimensions on the correlation function plot. To more clearly show the anisotropic BAO ring in the power spectrum, the right panel plots the two-dimensional power-spectrum divided by the best-fit smooth component. The wiggles seen in this panel are analogous to the oscillations seen in the top left panel of Fig 3.

Shadab Alam et. al. 2016

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Observations: only on the 3D past lightcone



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Observations: What we actually measure?



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Observations: Cosmic Bias

Galaxies are biased tracers of matter



 $\delta_{tracer} = b \quad \delta_{matter}$ $\xi_{tracer} = b^2 \quad \xi_{matter}$



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Observations: Redshift Space Distortions



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Experiments: Redshift Surveys a.k.a Galaxy Surveys

Ground Based

- Easy modifications
- Atmospheric noise

Spectroscopic

- Photons transverse sequence of dispersive elements.
- Advantage
 - Excellent $\delta\lambda$ resolution
- Disadvantage
 - Low S/N (since multiple detector element pipeline)
 - Slow imaging. (Need large exposure times.)

Satellites

- Difficult modifications
- No Atmospheric noise

Photometric

- Photons transverse coloured filters
- Advantage:
 - fast imaging
 - good S/N (since one simple detector pipeline)
 - massive data collection
- Disadvantage:
 - Small $\delta\lambda$ resolution



Experiments: Redshift Surveys

Currently Analysing Data

SDSS-IV 2016, 0.2<z<3.5



10,400° 1.5×10^6 CMASS 7.5×10⁵ QSO



WiggleZ 2011, z<1 7,500° 2.4×10⁵ ELG

2dF-GRS₂₀₀₂, z<0.3



1,500° 3.3×10⁵ ELG

Future Projects

Euclid



2023, 0.9<z<1.8 15,000° 10³ x10⁶ Gal

DESI



LSST

2019, 14,000° $30x10^{6}$ Gal z<2 Lya Forest z>2 2020, z<4 18,000° 10³ x10⁶ Gal



Sloan Digital Sky Survey (SDSS)



eBOSS in a nutshell





FLRW-RECONSTRUCTION $\int_{a} \int_{a} \int$



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Euclid Space Mission

- Main project:
 - Sun-Earth L2 point for 6 years
 - 1.2 SiC mirror telescope
- Imaging VIS
 - 550 < λ/nm < 900
- Photometry NISP (Y,J,H)
 - 900 < λ/nm < 2000
- Slitless Spectroscopy NISP :
 - R=380
 - 920 < λ/nm < 1850
 - 30 Million Targets per 4000 sec
- Asurv: 15000 deg²
- First Light 2023
- Objectives:
 - 2.6 Billion Emission Line Galaxies @z < 2.3
 - Nature of Dark Matter (WL) + Dark Energy (GC)
 - Large Scale Structure Science







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Euclid Flagship Simulation

- N-body Simulation
- Fast Multipole Model grav-solver
- Planck 2015 cosmology
- Largest # ~10⁵ particles
- $L_{box} = 3780 h^{-1}Mpc$
- mag-H < 26</p>
- log₁₀ (f_{Hα}) < -16
- 0 < z < 2.3
- > 2.6 Billion Galaxies
- Area 5000 deg²
- Volume 30 (Gpc/h)³







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Experiments: CMB

CMB = Cosmic Microwave Background











Temperature Polarisation E,B Primordial G-Waves!







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Experiments: CMB

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Observations: Statistical Inference

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Fisherology

Cramer-Rao bound theorem

Any unbiased estimator for parameters delivers a Covariance Matrix (C) that is no better than the inverse of the Fisher Matrix (F) Let:

o_b : observable in the bin b

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p_i : parameters

$$C_{ij} = \langle \delta p_i \delta p_j \rangle = (F^{-1})_{ij}$$

Need to model the error(Covariance) from the survey

Observations: Bayesian Approach

Modern observational cosmology relies on Bayes theory

Assuming $\theta = (\phi, n)$, with ϕ interesting and n nuissance, parameter inference is performed as:

$$P(\phi|d,M) \propto \int P(d|\phi,n,M) P(\phi,n|M) dn$$

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Combination:

cnes

 $\begin{array}{l} \chi \ {\rm GC+CMB}^{\,2} = \ \left(\left(\xi(r,\Omega_{m}{}^{\rm F}) - \xi^{\rm Model}(r; \, \alpha_{iso}[\Omega_{m}, \, \Omega_{m}{}^{\rm F}] \, \right) \, \right) / \, \sigma \xi(r,\Omega_{m}{}^{\rm F}) \, \right)^{\,2} + \left(\, \left(\Omega m - 0.4 \, \right) / \, 0.1 \right)^{\,2} \\ \Omega_{m}{}^{\rm Galaxy \ Clustering} + {}^{\rm CMB} = 0.3 + 0.03 & -> \text{small error} \end{array}$

50 500

1000 1500

Multipole moment.

2500

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Parametrizations in LSS + Sn-Ia? + GW?

(Remodified from W.Percival Talk)

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Multi Parameters fit to multi-data

- Given CMB data, other data used to break degeneracies (although CMB does a pretty good job by itself) to understand Dark Energy
- Main Problem: handle what is being constrained and why
 - Difficult to assess systematics
 - Need to be in consistency with all the data
- Always two sets of parameters:
 - Those you fix (part of the prior)
 - Those you vary
- Need to define a prior
 - What set of models?
 - What prior assumptions to make on them (often uniform priors on physically motivated variables)
- Need a sampling method to explore the multi-parameter space

(Remodified from W.Percival Talk)

Conclusions

Thank you for your Attention!

Astronomy 101: Obscuration effects

λ

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Astronomy 101: Obscuration effects

IDEAL Case Clear line identification

λ

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Flux

Astronomy 101: Obscuration effects

Line misidentification: confusion of Hα with N_{IIb}

λ

Due to noisy instrument noisy flux measurement

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Flux

Astronomy 101: Obscuration effects

IDEAL Case Clear line identification

λ

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Flux

Astronomy 101: Obscuration effects

Line misidentification: confusion of Hα with N_{IIb}

λ

Due to noisy instrument noisy flux measurement

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Flux

Astronomy 101: Obscuration effects

Overlapping spectra due to object occultation

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Observations: Alternative Observables

Counts-in-Spheres:
$$N(< r) = \int_0^r dd(s) ds \propto r^{D_2}$$
Fractal Dimension: $D_2(r) = \frac{d \ln N(< r)}{d \ln r}$ Homogeneous
@ large scales $D_2(r) = 3$ Inhomogeneous
@ small scales (clustering) $D_2(r) < 3$

0 0.0 C

Transition to Homogeneity at:

$$D_2(R_H) = 3 @ 1\%$$

(Arbitrary Choice; Independent of survey)

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Observations: Cosmological Principle Tests

P.Ntelis et al. arXiv:1702.02159

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Observable over "time"

