

3D Nucleon Imaging

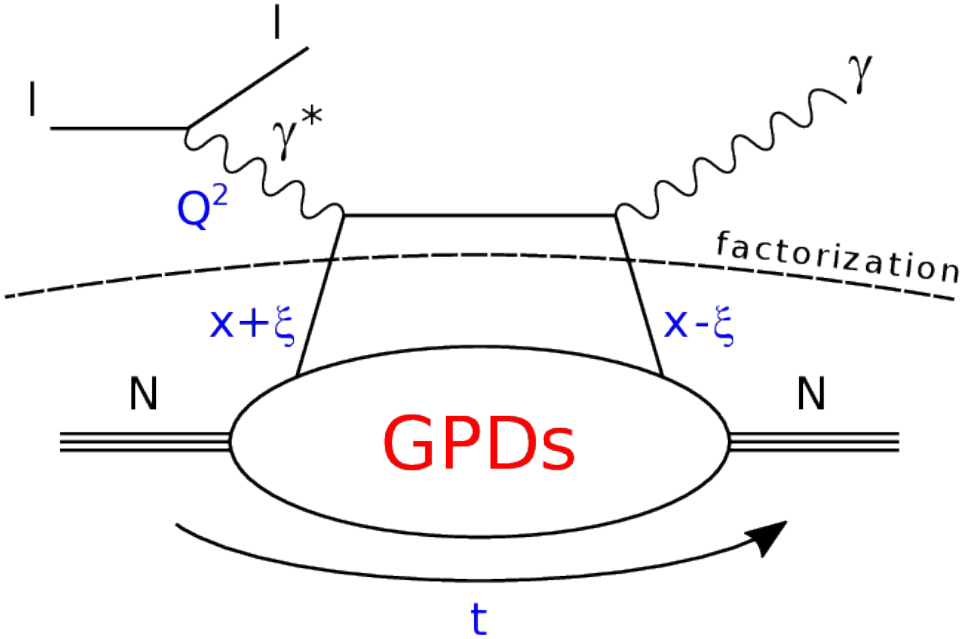
Paweł Sznajder
National Centre for Nuclear Research, Poland



EICUG meeting, Paris, July 22, 2019

- Introduction
- Experimental campaign
- Global analysis of DVCS data - “classic” and ANN approaches
- Summary

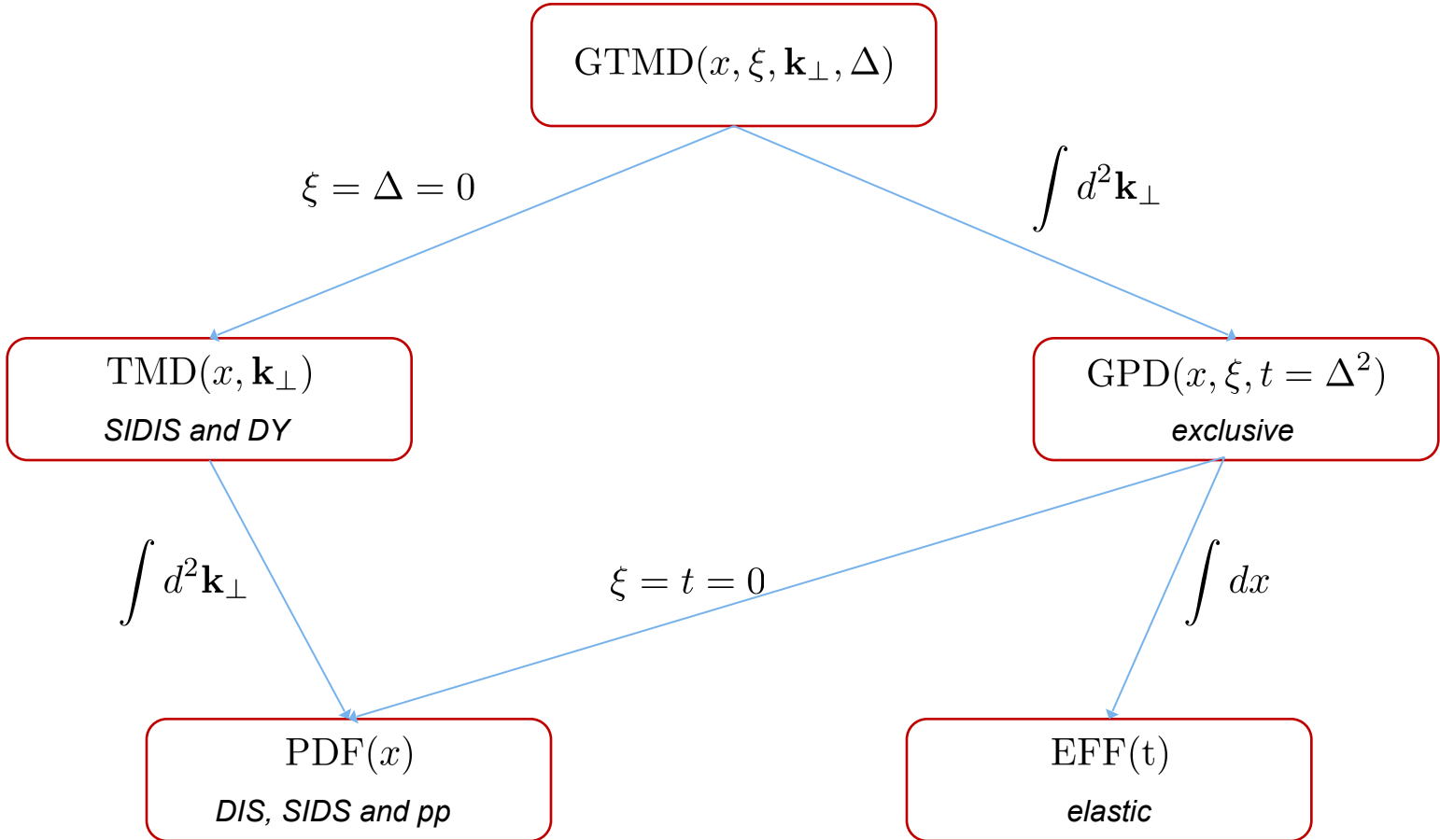
Deeply Virtual Compton Scattering (DVCS)



factorization for $|t|/Q^2 \ll 1$

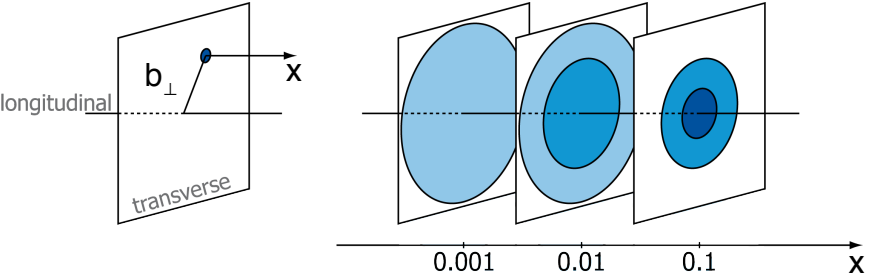
Chiral-even GPDs:
(helicity of parton conserved)

$H^{q,g}(x, \xi, t)$	$E^{q,g}(x, \xi, t)$	for sum over parton helicities
$\tilde{H}^{q,g}(x, \xi, t)$	$\tilde{E}^{q,g}(x, \xi, t)$	for difference over parton helicities
nucleon helicity conserved	nucleon helicity changed	



Nucleon tomography

$$q(x, \mathbf{b}_\perp) = \int \frac{d^2 \Delta}{4\pi^2} e^{-i\mathbf{b}_\perp \cdot \Delta} H^q(x, 0, t = -\Delta^2)$$



Total angular momentum

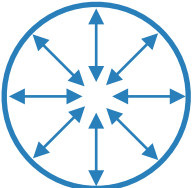
$$\frac{A^q(0) + B^q(0)}{\text{EMT form factors}} = \int_{-1}^1 x [H^q(x, \xi, 0) + E^q(x, \xi, 0)] \underset{\text{Ji's sum rule}}{=} 2J^q$$



“Mechanical” forces acting on quarks, e.g. pressure in nucleon center

$$p(0) = \frac{1}{6\pi^2 M} \int_{-\infty}^0 dt \sqrt{-tt} \underline{C}(t)$$

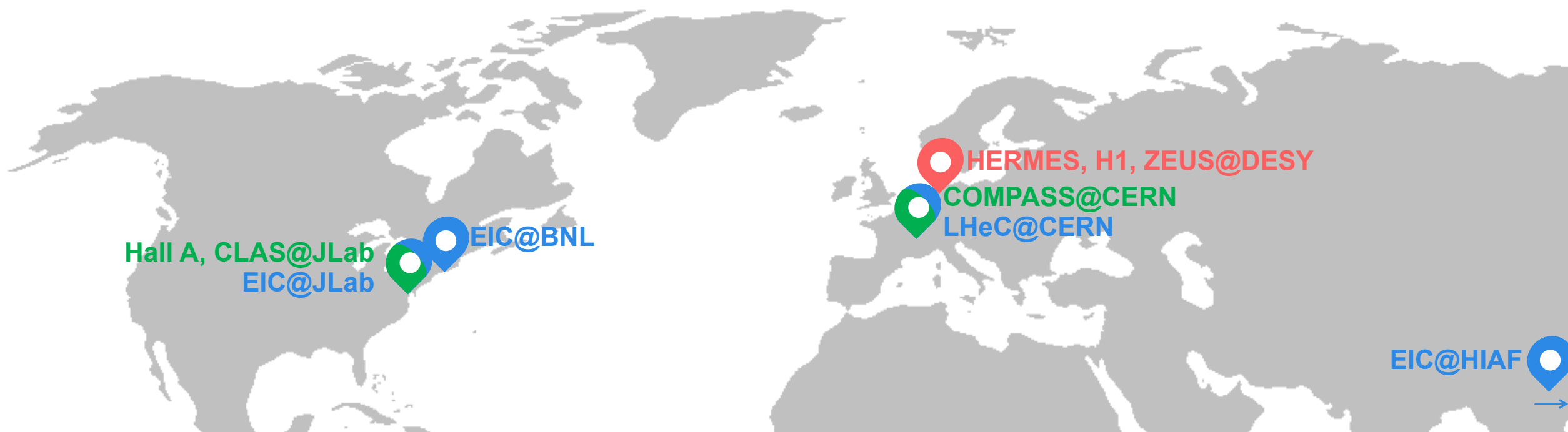
Nucleon mass *EMT form factor*



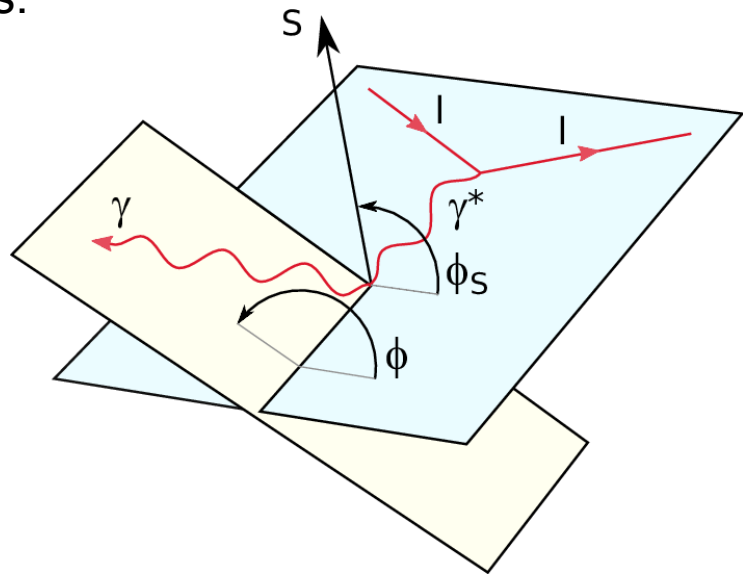
GPDs studied in various laboratories
→ need to cover a broad kinematic range

experiments

closed active planned



Angles:



Kinematic cuts used in presented analyses:

$$Q^2 > 1.5 \text{ GeV}^2$$

$$-t/Q^2 < 0.2$$

No.	Collab.	Year	Observable	Kinematic dependence	No. of points used / all
1	HERMES	2001	A_{LU}^+	ϕ	10 / 10
2		2006	$A_C^{\cos i\phi}$	t	4 / 4
3		2008	$A_C^{\cos i\phi}$	x_{Bj}	18 / 24
			$A_{UT,DVCS}^{\sin(\phi-\phi_S) \cos i\phi}$	$i = 0$	
			$A_{UT,I}^{\sin(\phi-\phi_S) \cos i\phi}$	$i = 0, 1$	
			$A_{UT,I}^{\cos(\phi-\phi_S) \sin i\phi}$	$i = 1$	
4		2009	$A_{LU,I}^{\sin i\phi}$	x_{Bj}	35 / 42
			$A_{LU,DVCS}^{\sin i\phi}$	$i = 1$	
			$A_C^{\cos i\phi}$	$i = 0, 1, 2, 3$	
5		2010	$A_{UL}^{+, \sin i\phi}$	x_{Bj}	18 / 24
			$A_{LL}^{+, \cos i\phi}$	$i = 0, 1, 2$	
6		2011	$A_{LT,DVCS}^{\cos(\phi-\phi_S) \cos i\phi}$	x_{Bj}	24 / 32
			$A_{LT,DVCS}^{\sin(\phi-\phi_S) \sin i\phi}$	$i = 1$	
			$A_{LT,I}^{\cos(\phi-\phi_S) \cos i\phi}$	$i = 0, 1, 2$	
			$A_{LT,I}^{\sin(\phi-\phi_S) \sin i\phi}$	$i = 1, 2$	
7		2012	$A_{LU,I}^{\sin i\phi}$	x_{Bj}	35 / 42
			$A_{LU,DVCS}^{\sin i\phi}$	$i = 1$	
			$A_C^{\cos i\phi}$	$i = 0, 1, 2, 3$	
8	CLAS	2001	$A_{LU}^{-, \sin i\phi}$	—	0 / 2
9		2006	$A_{UL}^{-, \sin i\phi}$	—	2 / 2
10		2008	A_{LU}^-	ϕ	283 / 737
11		2009	A_{LU}^-	ϕ	22 / 33
12		2015	$A_{LU}^-, A_{UL}^-, A_{LL}^-$	ϕ	311 / 497
13		2015	$d^4\sigma_{UU}^-$	ϕ	1333 / 1933
14	Hall A	2015	$\Delta d^4\sigma_{LU}^-$	ϕ	228 / 228
15		2017	$\Delta d^4\sigma_{LU}^-$	ϕ	276 / 358
16	COMPASS	2018	$d^3\sigma_{UU}^\pm$	t	2 / 4
17	ZEUS	2009	$d^3\sigma_{UU}^+$	t	4 / 4
18	H1	2005	$d^3\sigma_{UU}^+$	t	7 / 8
19		2009	$d^3\sigma_{UU}^\pm$	t	12 / 12
SUM:					2624 / 3996

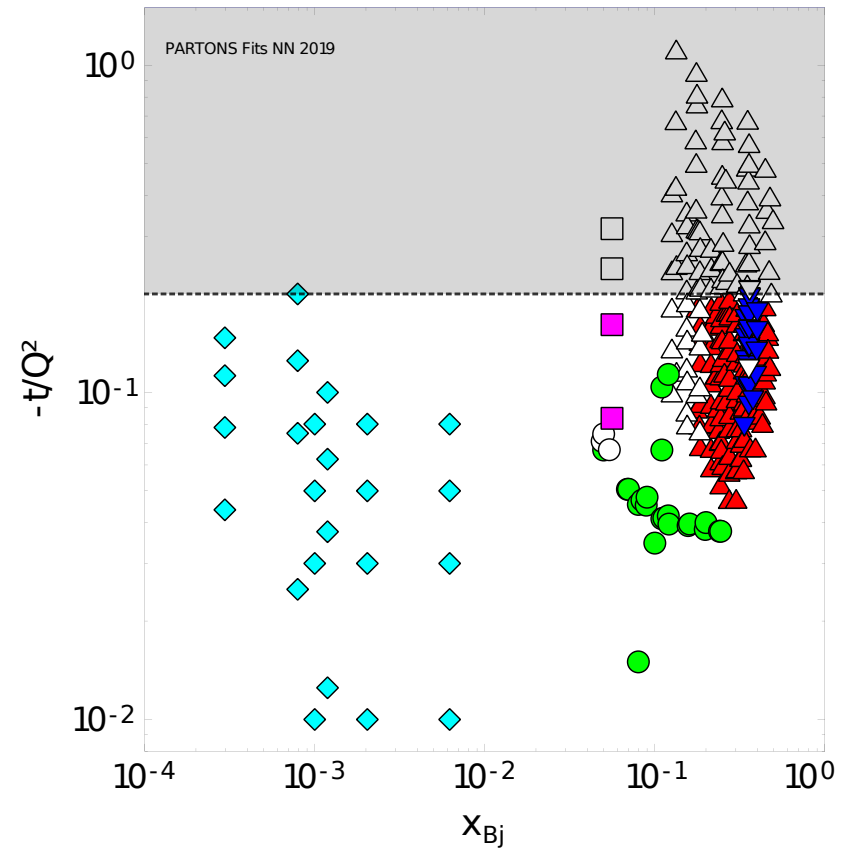
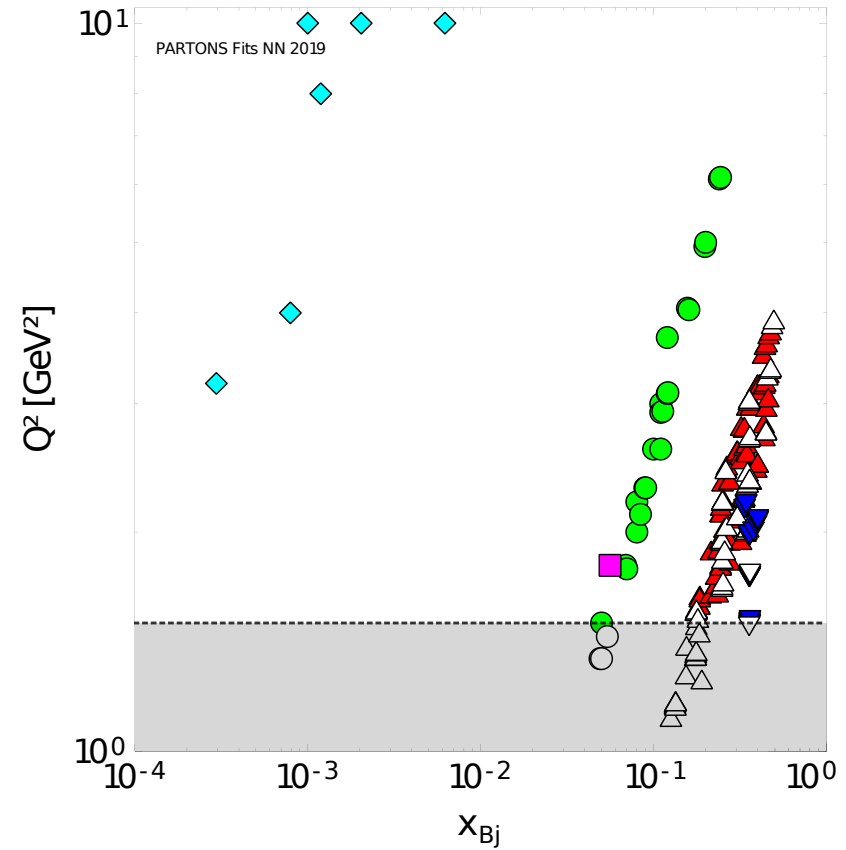
- ▼ HALLA
- ▲ CLAS
- HERMES
- COMPASS
- ◆ H1 and ZEUS

Kinematic cuts used in presented analyses:

$$Q^2 > 1.5 \text{ GeV}^2$$

$$-t/Q^2 < 0.2$$

(exclusion denoted by open symbols and grey areas)



PARTONS - modern platform to study GPDs

- Open source project to support effort of whole GPD community
- For theoreticians, experimentalists and phenomenologists
- Come with number of available physics developments implemented
- Addition of new developments as easy as possible

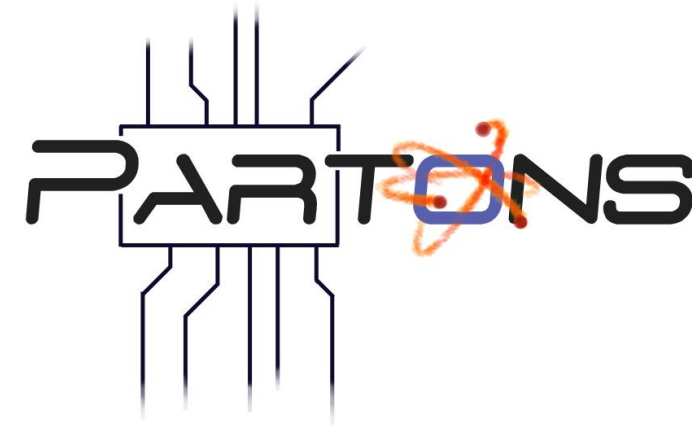
To download and for tutorials, useful information, reference documentation see:

<http://partons.cea.fr>

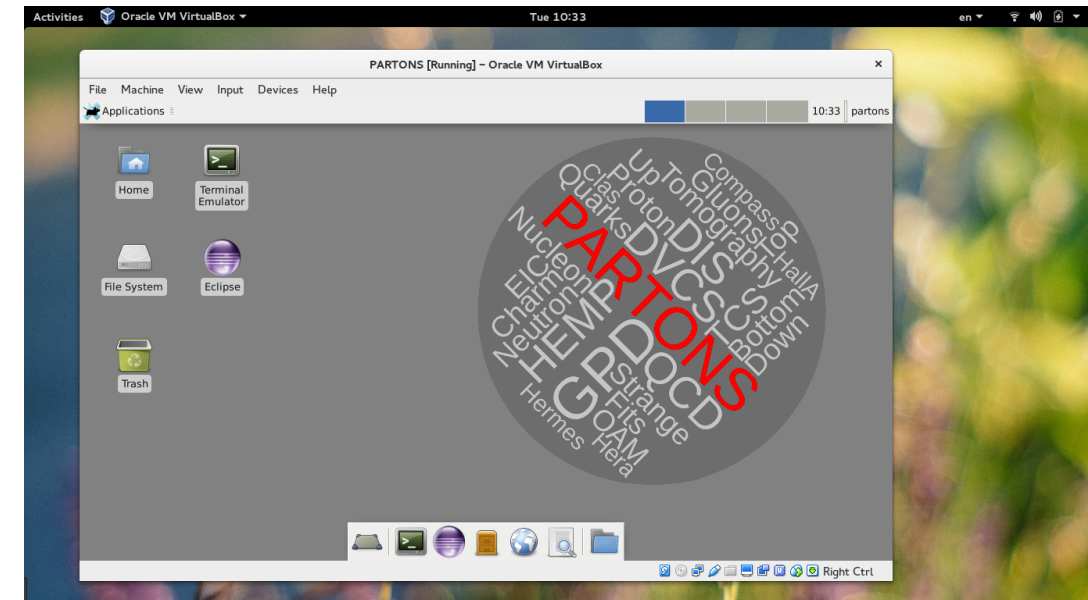
For detail description of architecture see:

[Eur. Phys. J. C78 \(2018\) 6, 478](#)

Logo of the project:



*PARTONS virtual machine
(example of dissemination method):*



H. Moutarde, P. S., J. Wagner "*Border and skewness functions from a leading order fit to DVCS data*"
Eur. Phys. J. C78 (2018) 11, 890

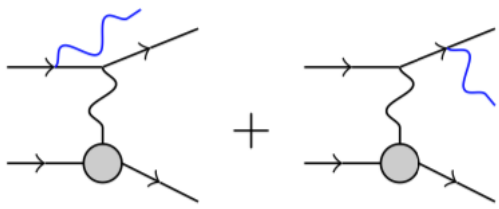
Goal: global extraction of Compton Form Factors (CFFs) from DVCS data using LO/LT formalism

Analysis done within **PARTONS** project

Cross-section for single photon production ($l + N \rightarrow l + N + \gamma$):

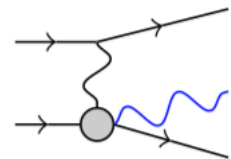
$$\sigma \propto |\mathcal{A}|^2 = |\mathcal{A}_{BH} + \mathcal{A}_{DVCS}|^2 = |\mathcal{A}_{BH}|^2 + |\mathcal{A}_{DVCS}|^2 + \mathcal{I}$$

Bethe-Heitler process



calculable within QED

DVCS



parametrised by CFFs

■ imaginary part

$$\text{Im}\mathcal{G}(\xi, t) = \pi G^{(+)}(\xi, \xi, t) = \pi \sum_q e_q^2 G^{q(+)}(\xi, \xi, t)$$

$$G^{q(+)}(x, \xi, t) = G^q(x, \xi, t) \mp G^q(-x, \xi, t)$$

$$G^{q(+)}(\xi, \xi, t) = G^{q_{\text{val}}}(\xi, \xi, t) + 2G^{q_{\text{sea}}}(\xi, \xi, t)$$

"-" for $G \in \{H, E\}$
 "+" for $G \in \{\tilde{H}, \tilde{E}\}$

■ real part

$$\text{Re}\mathcal{G}(\xi, t) = \text{P.V.} \int_0^1 G^{(+)}(x, \xi, t) \left(\frac{1}{\xi - x} \mp \frac{1}{\xi + x} \right) dx$$

$$\text{Re}\mathcal{G}(\xi, t) = \text{P.V.} \int_0^1 G^{(+)}(x, x, t) \left(\frac{1}{\xi - x} \mp \frac{1}{\xi + x} \right) dx + C_G(t)$$

$$C_H(t) = -C_E(t) \quad C_{\tilde{H}}(t) = C_{\tilde{E}}(t) = 0$$

connected to EMT FF

Relation between subtraction constant and D-term:

$$C_G^q(t) = 2 \int_{-1}^1 \frac{D^q(z, t)}{1 - z} dz \equiv 4D^q(t)$$

where

$$z = \frac{x}{\xi}$$

Decomposition into Gegenbauer polynomials:

$$D^q(z, t) = (1 - z^2) \sum_{i=0}^{\infty} d_i^q(t) C_{2i+1}^{3/2}(z)$$

Connection to EMT FF:

$$D^q(t) = \sum_{\substack{i=1 \\ \text{odd}}}^{\infty} d_i^q(t)$$

$$d_1^q(t) = 5C^q(t)$$

$$C_G^q(t) = 2 \int_{(0)}^1 \left(G^{q(+)}(x, x, t) - G^{q(+)}(x, 0, t) \right) \frac{1}{x} dx$$

- subtraction constant as analytic continuation of Mellin moments to $j = -1$

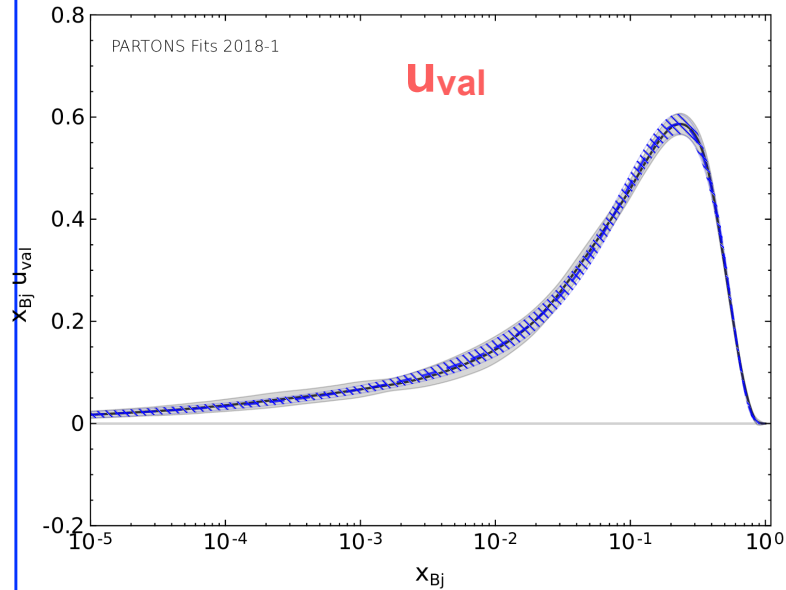
$$G^q(x, 0, t) = \text{pdf}_G^q(x) \exp(f_G^q(x)t) \qquad f_G^q(x) = A_G^q \log(1/x) + B_G^q(1-x)^2 + C_G^q(1-x)x$$

- reduction to PDFs and correspondence to EFFs
- modify "classical" $\log(1/x)$ term by $B_G^q(1-x)^2$ in low- x and by $C_G^q(1-x)x$ in high- x regions
- polynomials found in analysis of EFF data \rightarrow good description of data
- allow to use the analytic regularisation prescription
- finite proton size at $x \rightarrow 1$

$$G^q(x, x, t) = G^q(x, 0, t) g_G^q(x, x, t) \qquad g_G^q(x, x, t) = \frac{a_G^q}{(1-x^2)^2} (1 + t(1-x)(b_G^q + c_G^q \log(1+x)))$$

- at $x \rightarrow 0$ constant skewness effect
- at $x \rightarrow 1$ reproduce power behaviour predicted for GPDs in Phys. Rev. D69, 051501 (2004)
- t -dependence similar to DD-models with $(1-x)$ to avoid any t -dep. at $x = 1$

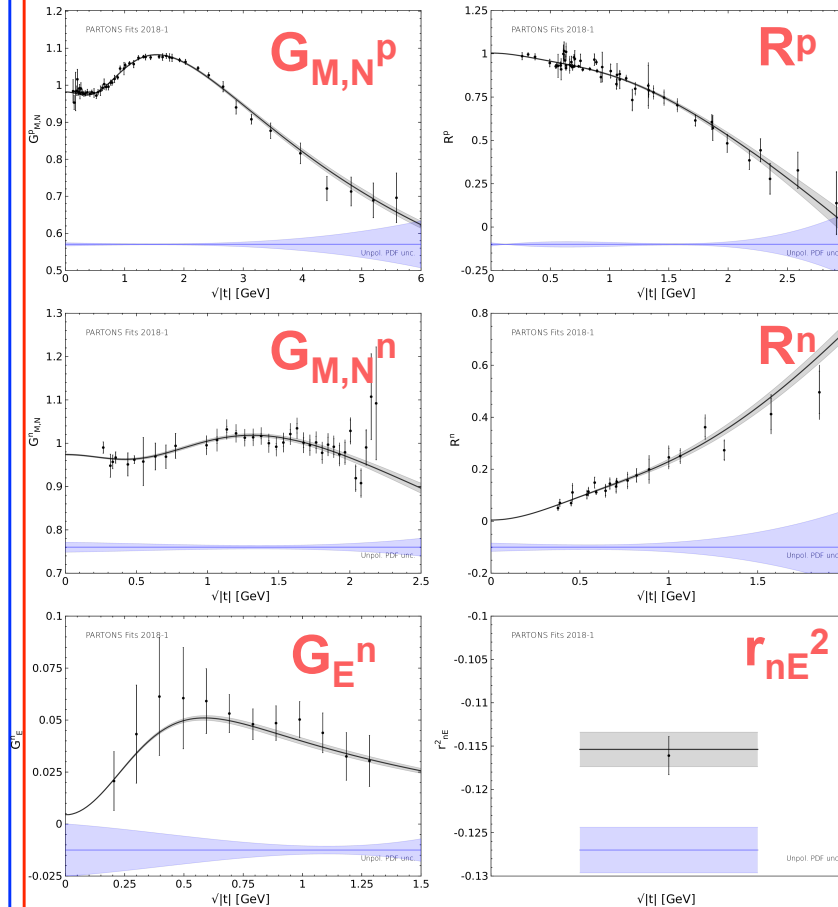
1. Analysis of PDF parameterisations



$$\text{pdf}(x, Q^2) = x^{-g(\delta_p, \delta_q, Q^2)} (1-x)^\alpha \times \sum_{i=0}^4 g(p_i, q_i, Q^2) x^i$$

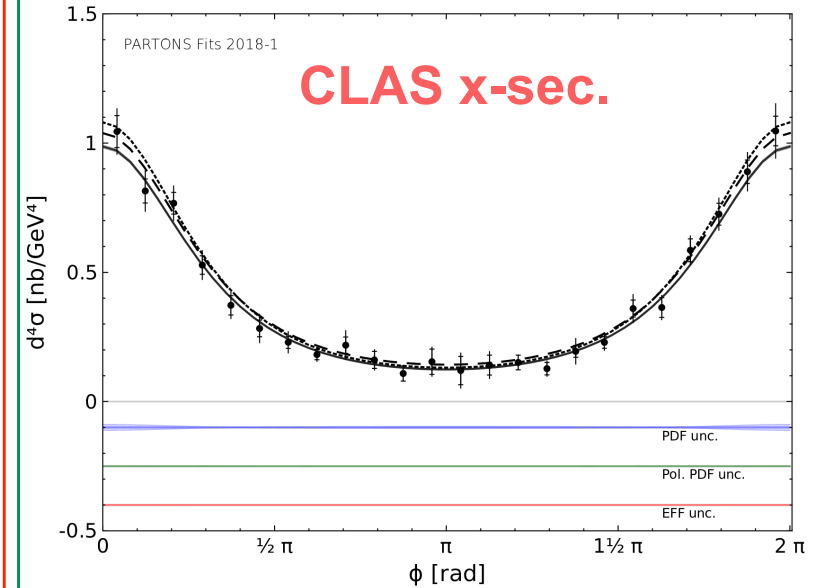
$$g(p, q, Q^2) = p + q \log \frac{Q^2}{Q_0^2}$$

2. Analysis of Elastic Form Factor data



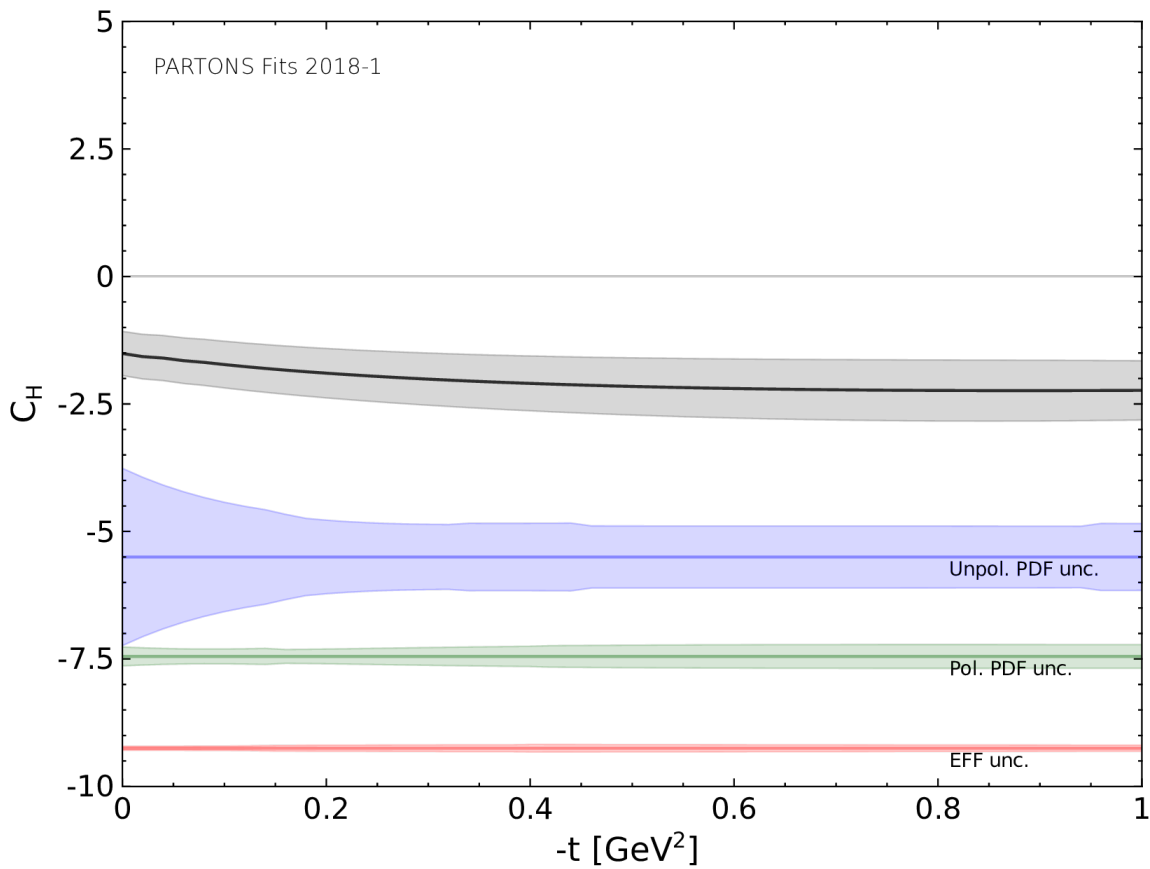
$$\chi^2/\text{ndf} = 129.6/(178 - 9) \approx 0.77$$

3. Analysis of DVCS data

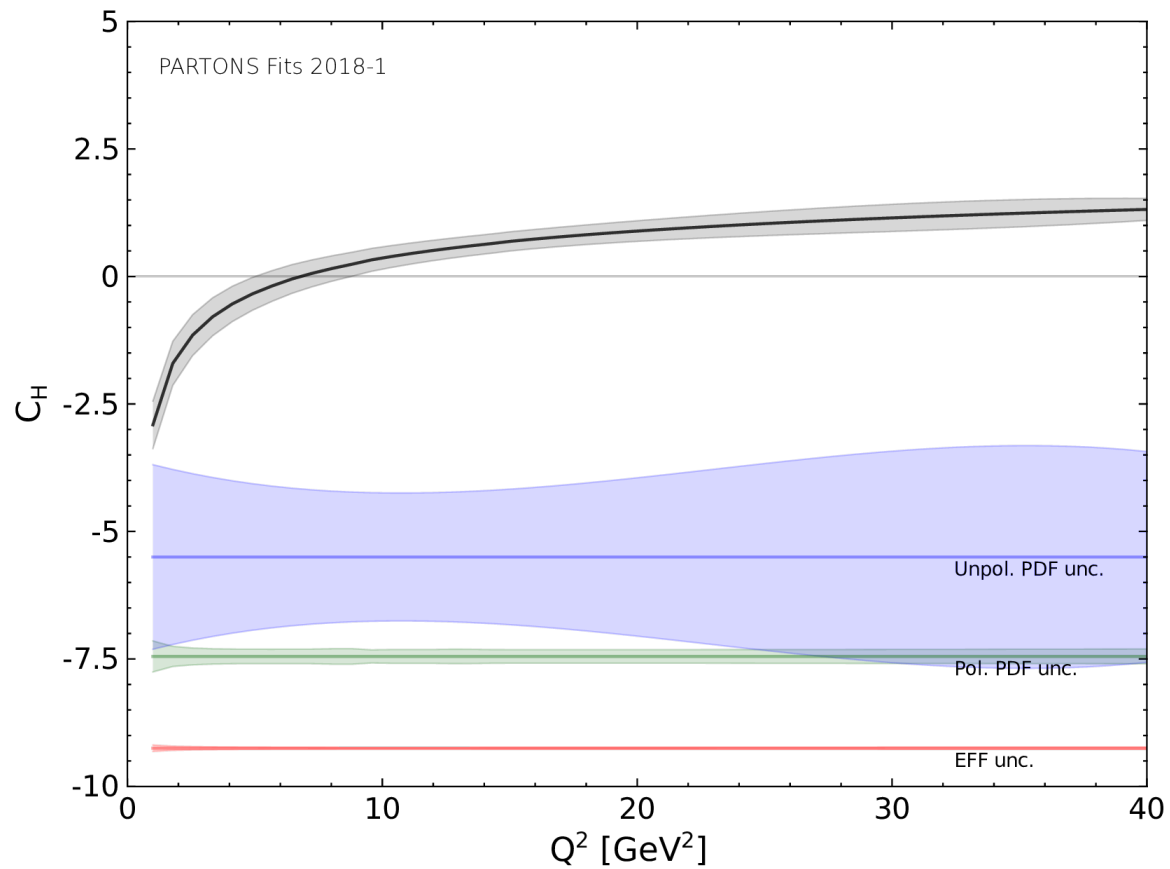


$$\chi^2/\text{ndf} = 2346.3/(2600 - 13) \approx 0.91$$

Subtraction constant:

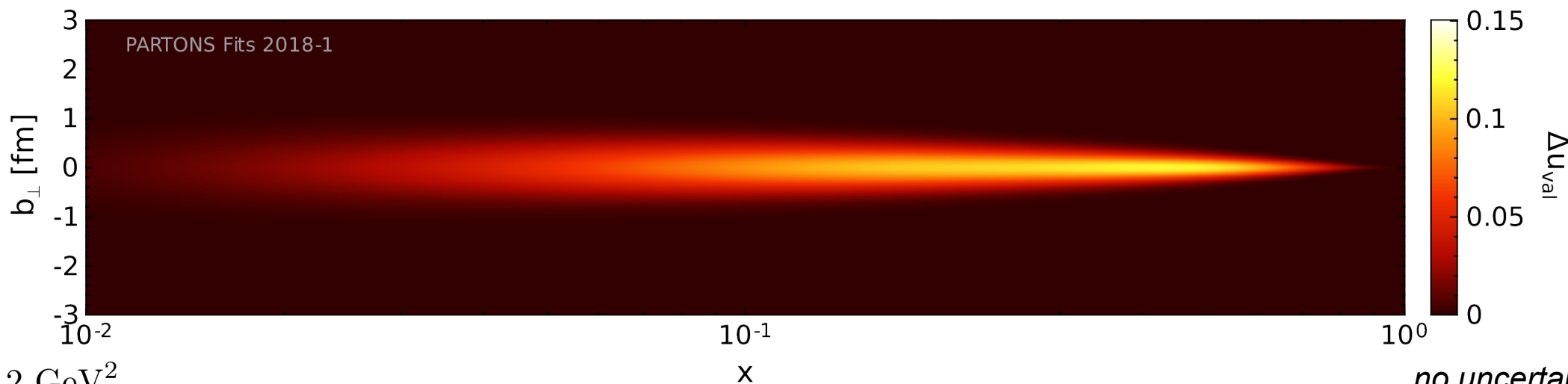
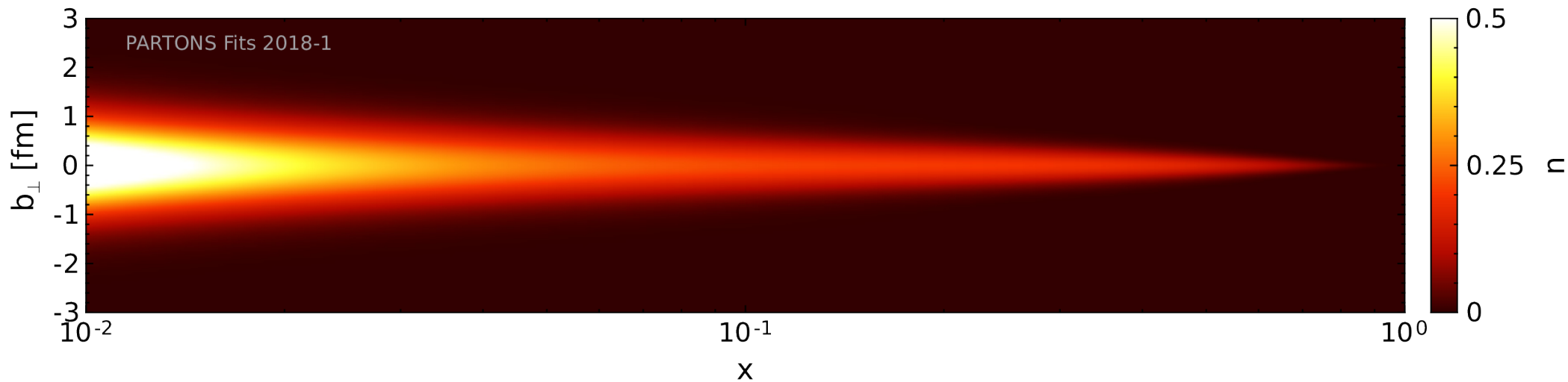


$Q^2 = 2 \text{ GeV}^2$



$t = 0$

Nucleon tomography:

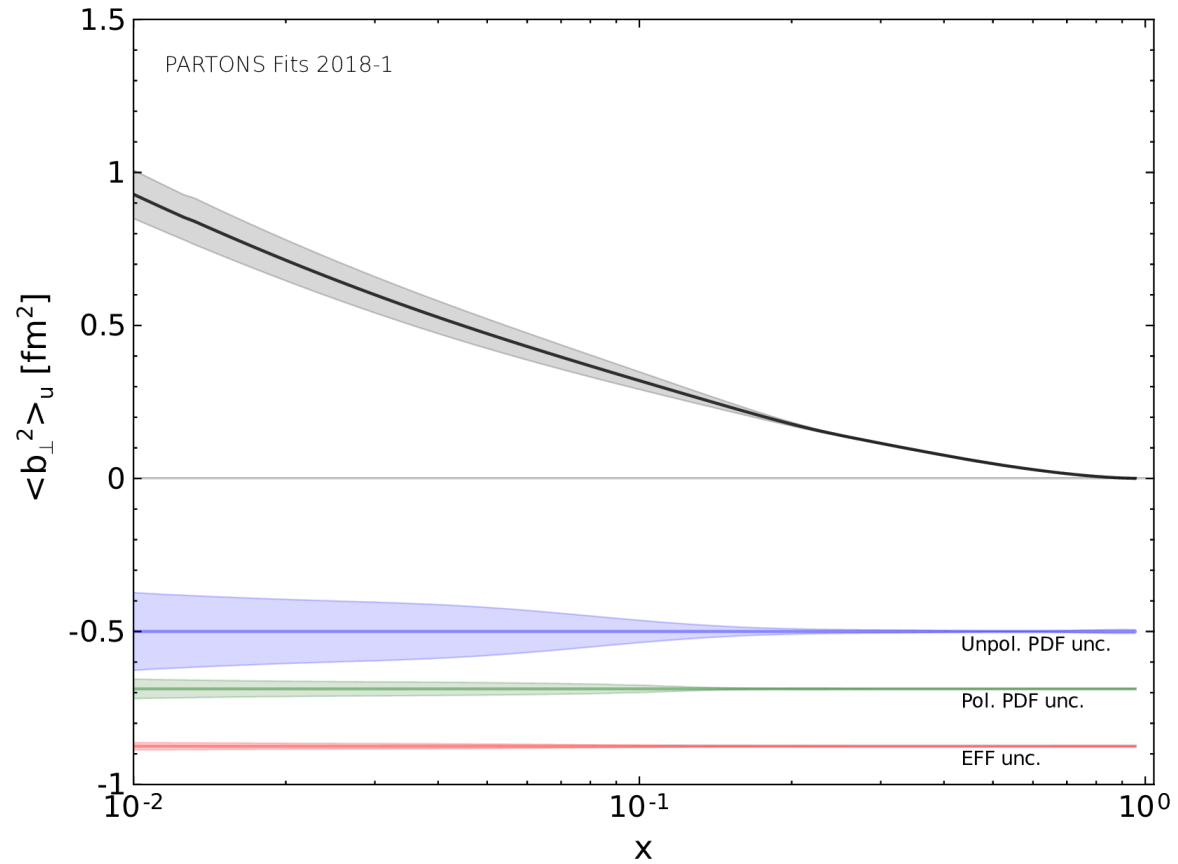


$Q^2 = 2 \text{ GeV}^2$

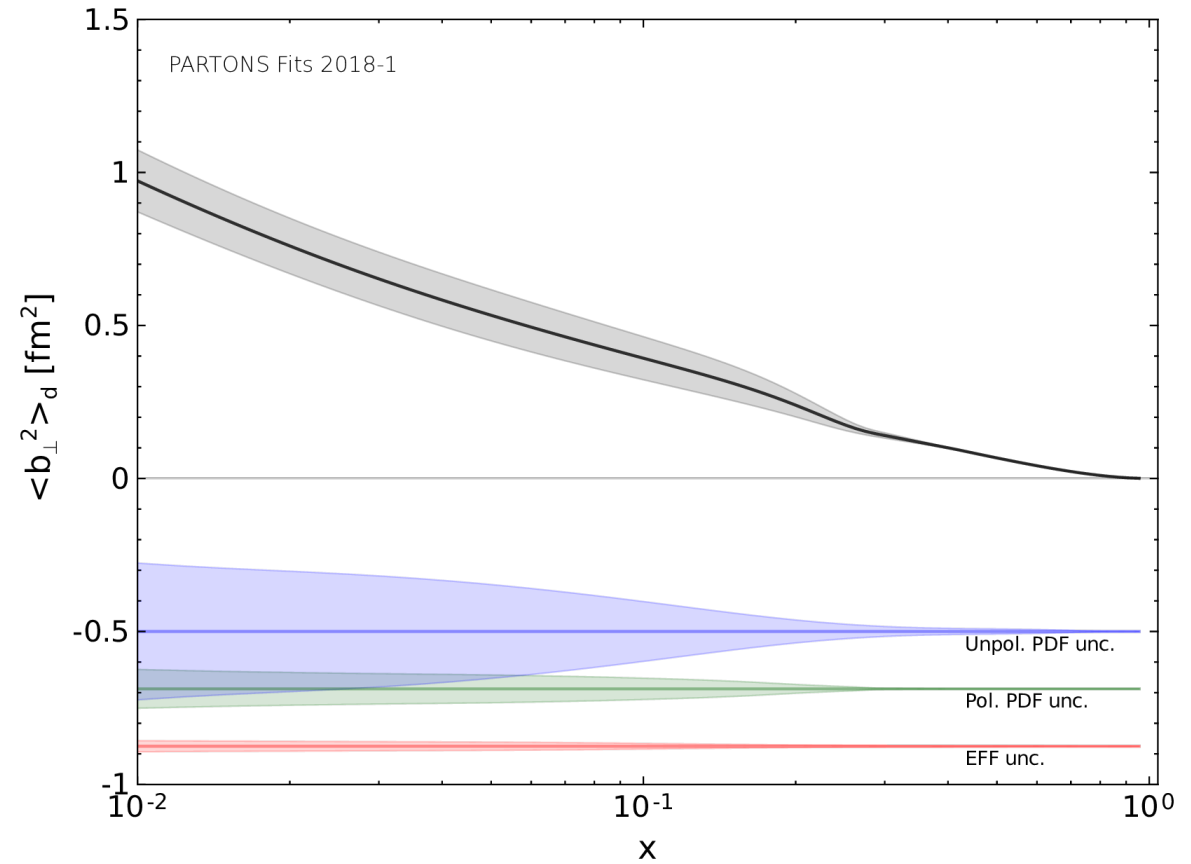
no uncertainties!

Nucleon tomography:

$$\langle b_{\perp}^2 \rangle_q(x) = \frac{\int d^2 \mathbf{b}_{\perp} \mathbf{b}_{\perp}^2 q(x, \mathbf{b}_{\perp})}{\int d^2 \mathbf{b}_{\perp} q(x, \mathbf{b}_{\perp})}$$



$Q^2 = 2 \text{ GeV}^2$



H. Moutarde, P. S., J. Wagner “*Unbiased determination of Compton Form Factors*”
accepted by Eur. Phys. J. C, preprint: arXiv: hep-ph/1905.02089

Goal: global extraction of Compton Form Factors (CFFs) from DVCS data using ANN technique

Analysis done within **PARTONS** project

Input data

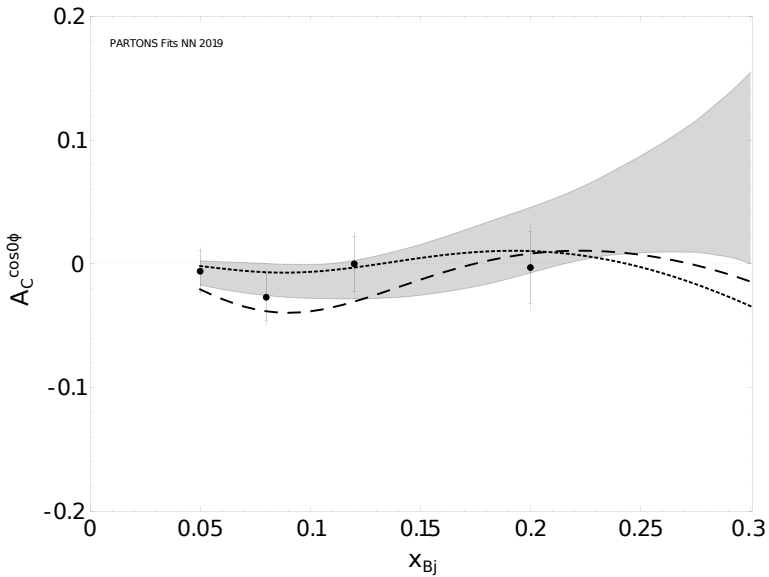
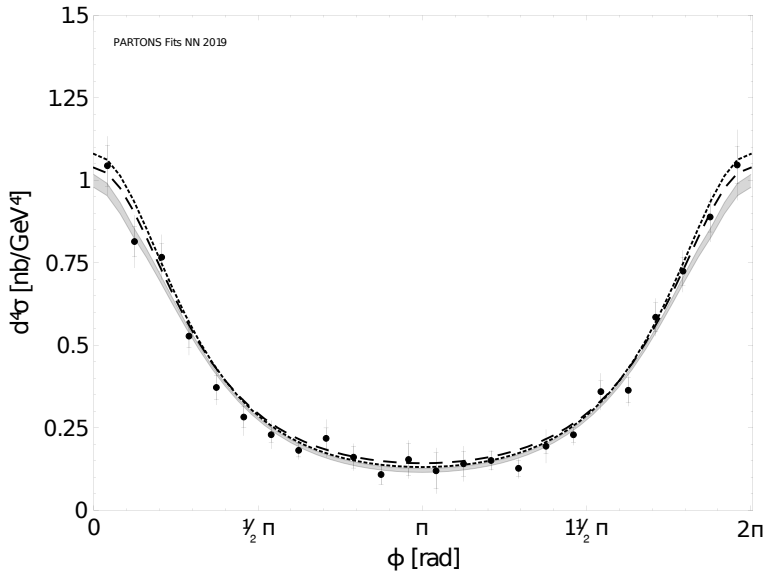
Performance:

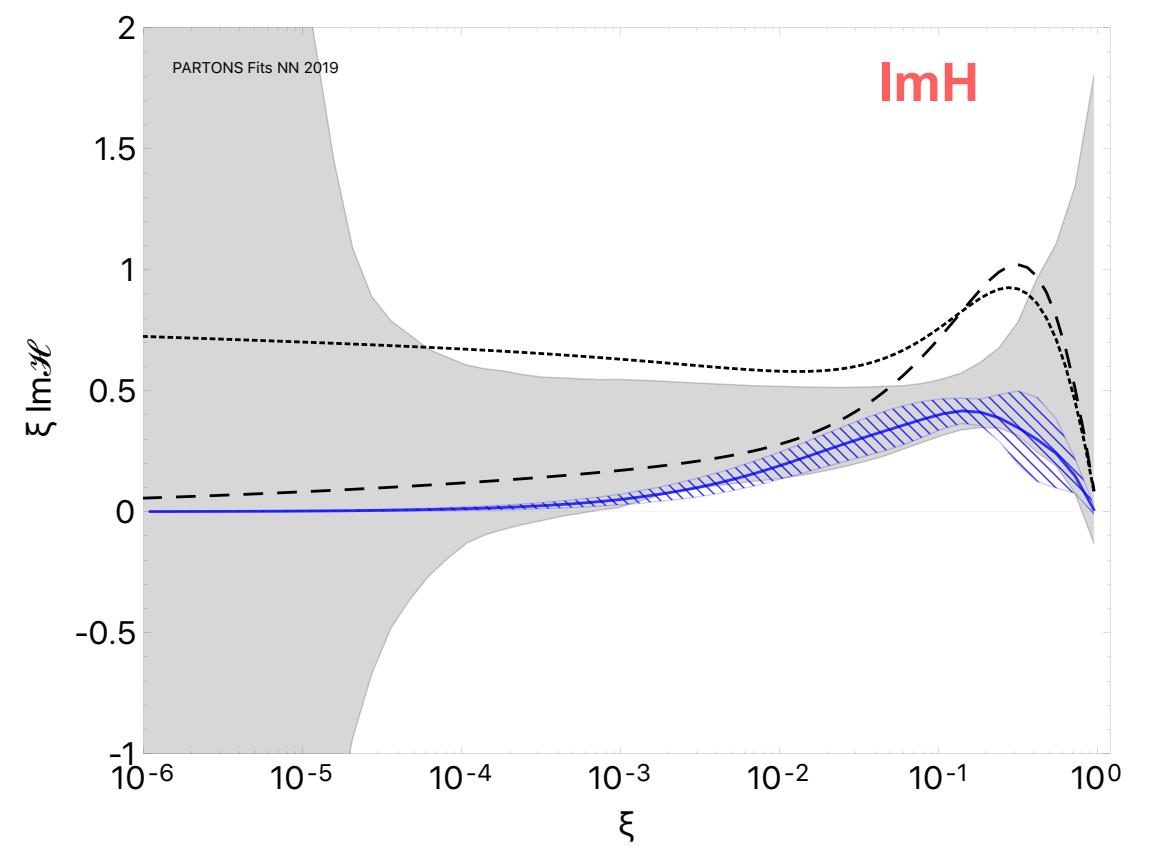
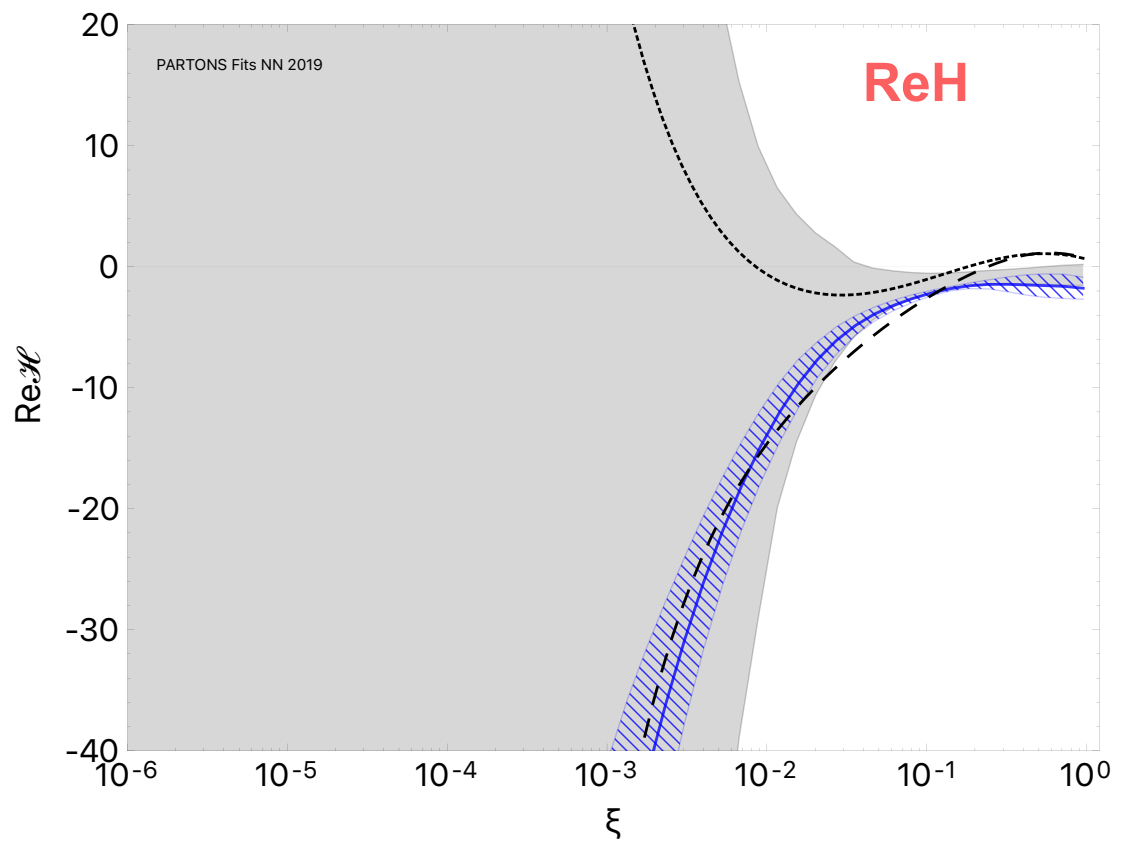
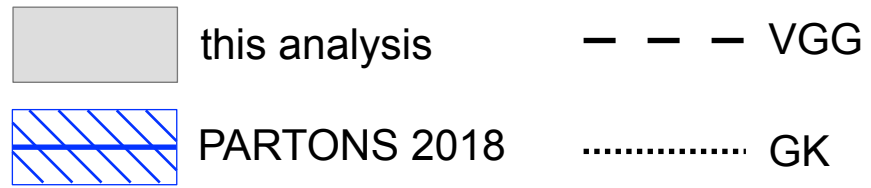
$$\chi^2/nPoints = 2243.5/2624 \approx 0.85$$

No.	Collab.	Year	Ref.	χ^2	n	χ^2/n
1	HERMES	2001	[17]	10.7	10	1.07
2		2006	[18]	5.5	4	1.38
3		2008	[19]	18.5	18	1.03
4		2009	[20]	34.7	35	0.99
5		2010	[21]	40.7	18	2.26
6		2011	[22]	16.7	24	0.70
7		2012	[23]	22.4	35	0.64
8	CLAS	2001	[24]	—	0	—
9		2006	[25]	1.0	2	0.52
10		2008	[26]	376.4	283	1.33
11		2009	[27]	28.3	22	1.29
12		2015	[28]	306.6	311	0.99
13		2015	[29]	884.7	1333	0.66
14	Hall A	2015	[15]	231.8	228	1.02
15		2017	[16]	211.4	276	0.77
16	COMPASS	2018	[30]	3.0	2	1.50
17	ZEUS	2009	[31]	5.49	4	1.38
18	H1	2005	[32]	22.2	7	3.17
19		2009	[33]	23.4	12	1.95

Replication of experimental data to propagate corresponding uncertainties:

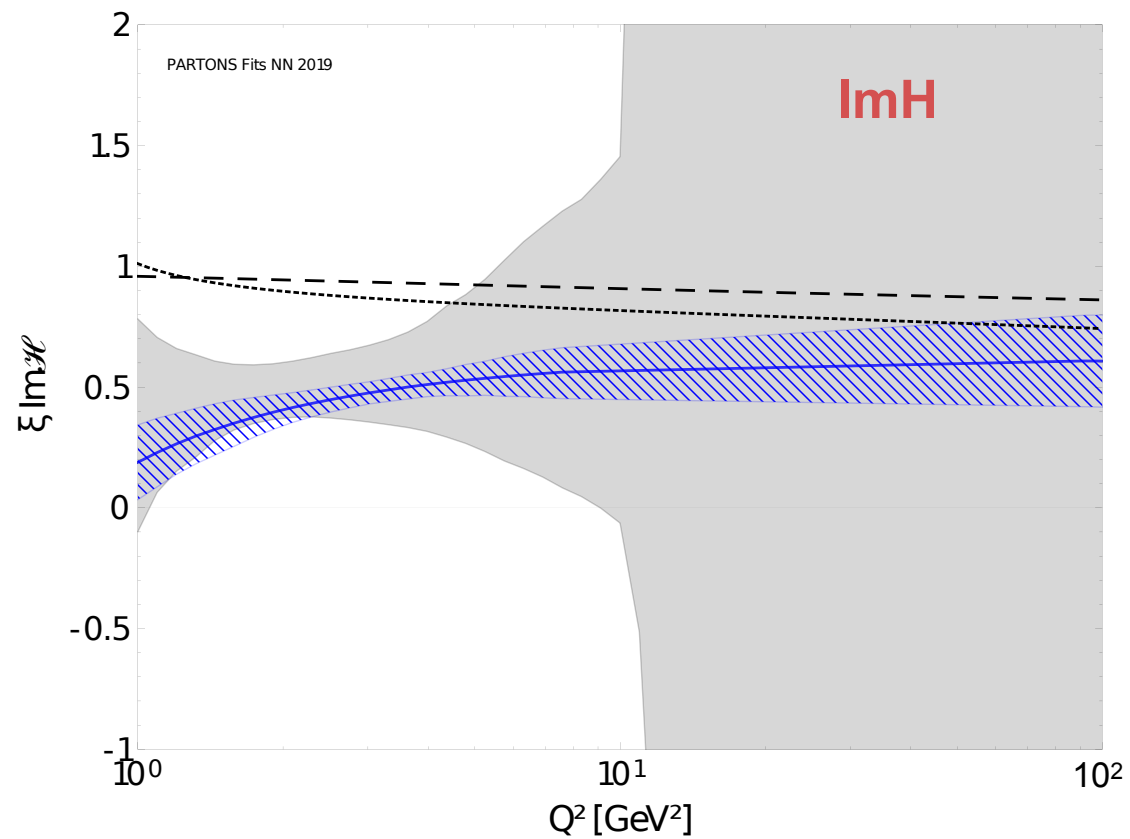
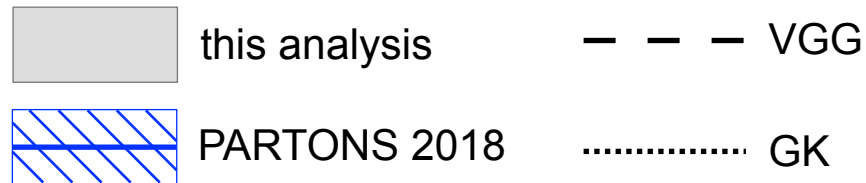
$$v_i \pm \Delta_i^{\text{tot}} \xrightarrow{\text{replica } j} (\text{rnd}_j(v_i, \Delta_i^{\text{tot}}) \pm \Delta_i^{\text{tot}}) \times \text{rnd}_j(1, \Delta_i^{\text{norm}}) \quad \Delta_i^{\text{tot}} = \sqrt{(\Delta_i^{\text{stat}})^2 + (\Delta_i^{\text{sys}})^2}$$



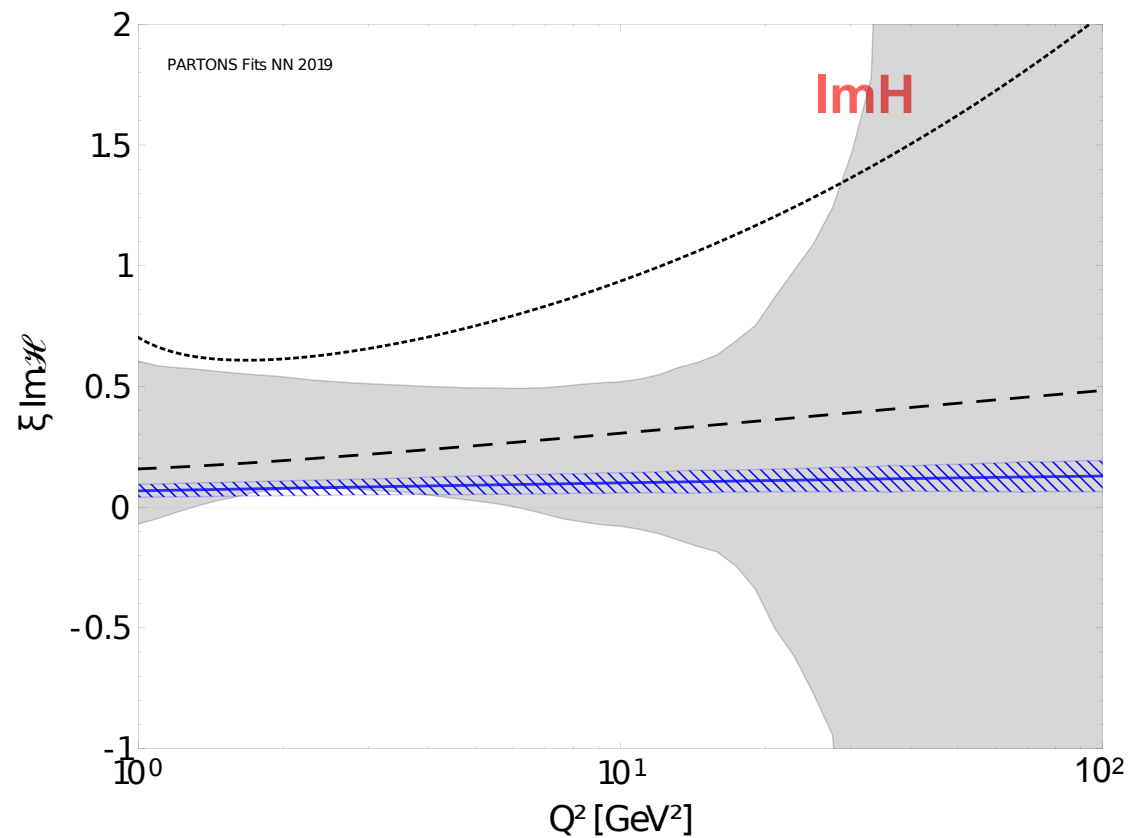


@ $t = -0.3 \text{ GeV}^2, Q^2 = 2 \text{ GeV}^2$

$$\xi \approx \frac{x_B}{2 - x_B}$$

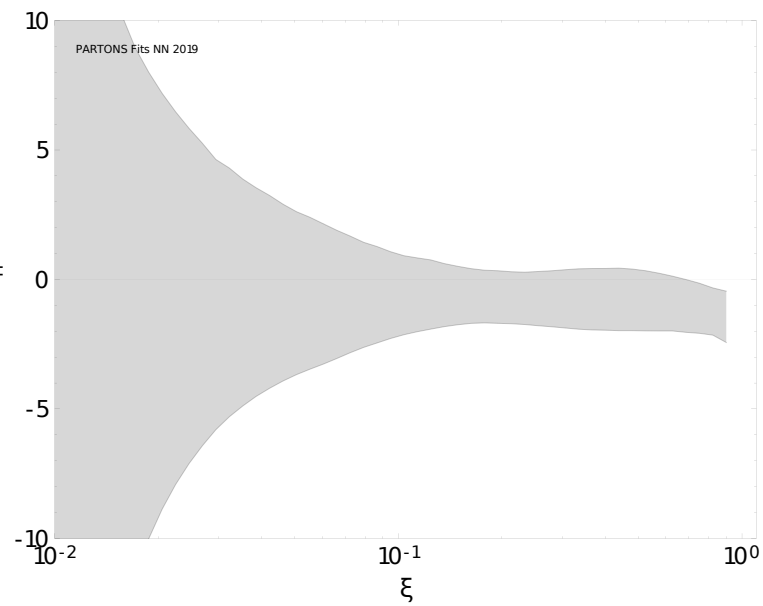


@ $\xi = 0.2, t = -0.3 \text{ GeV}^2$

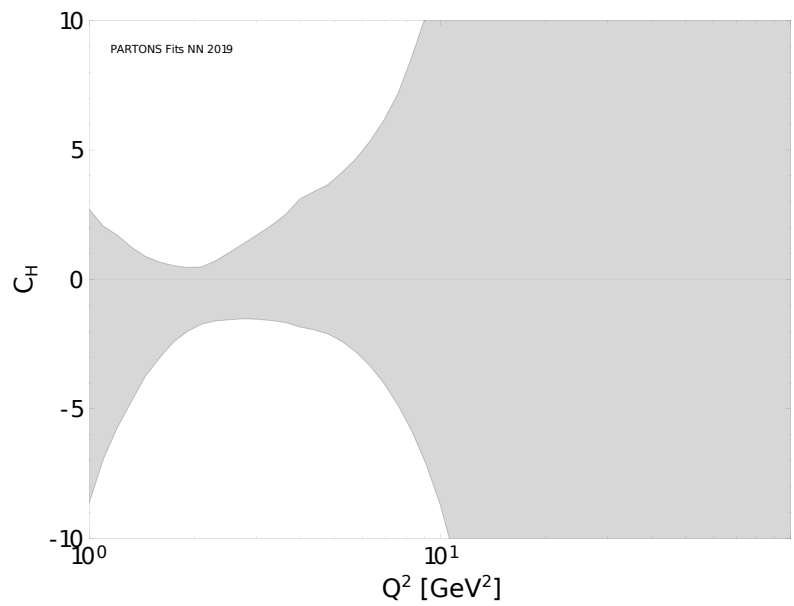


@ $\xi = 0.002, t = -0.3 \text{ GeV}^2$

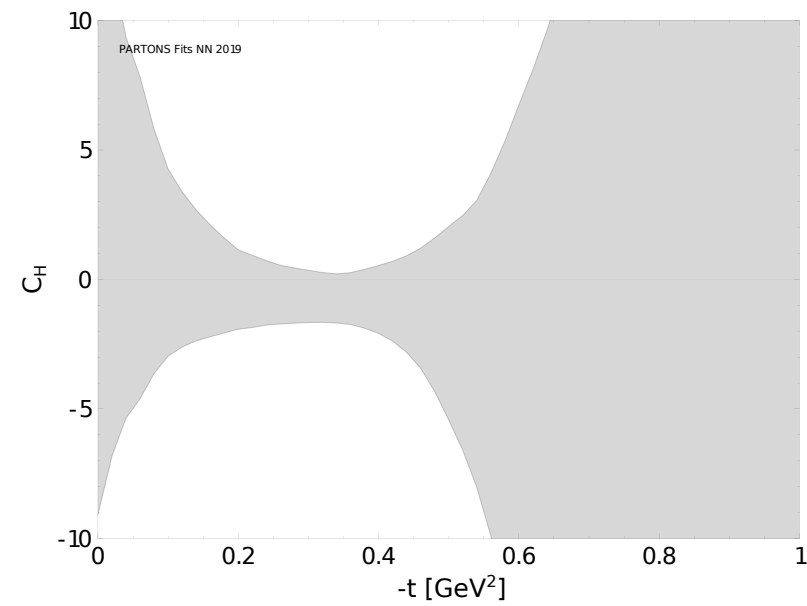
as function of ξ
@ $|t| = 0.3 \text{ GeV}^2, Q^2 = 2 \text{ GeV}^2$



as function of Q^2
@ $\xi = 0.2, |t| = 0.3 \text{ GeV}^2$



as function of $|t|$
@ $\xi = 0.2, Q^2 = 2 \text{ GeV}^2$



- Direct extraction of subtraction constant → encouraging precision
- As expected, no ξ behaviour observed
- Strong, model independent constraints on modeling of this quantity

Generalised Parton Distributions

- novel way to describe partonic structure of nucleon
- allows to study (highlights):
 - nucleon tomography
 - total angular momentum of partons
 - “mechanical” properties of parton distributions

Global analysis of DVCS data

- complementary approaches → classic Ansatz and ANN
- done with PARTONS framework -
- allows to access (highlights):
 - nucleon tomography
 - “mechanical” properties of parton distributions

Clear need to have EIC!