

# Probing SUSY in its most elusive guises

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*RPP*

LPC, January 24, 2019

*based on 1803.03651 [JHEP] + work in progress*

*with Hsin-Chia Cheng, Chris Verhaaren (UC Davis), Lingfeng Li (HKUST)*

# Motivation: naturalness

- Supersymmetry or new strong dynamics are most solid approaches to Higgs naturalness problem
- Very different, but share one crucial feature for phenomenology: top loop is cut off by new colored particles, the “top partners”

$$U^c \sim \begin{pmatrix} u^c \\ \tilde{u}^c \end{pmatrix}$$

↑  
top squark

SUSY commutes with gauge  $SU(3)_c$

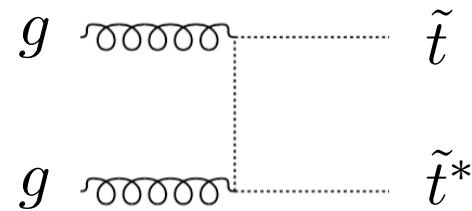
$$\mathcal{L}_{\text{mix}} \sim y u^c \mathcal{O}_u + \text{h.c.}$$

↑  
fermionic operator

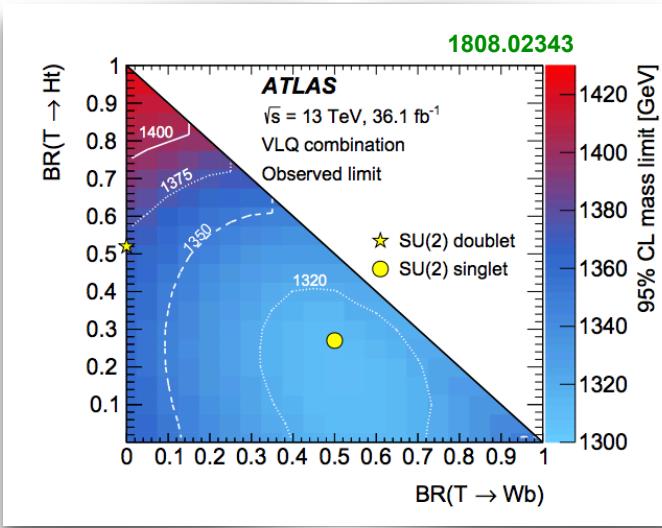
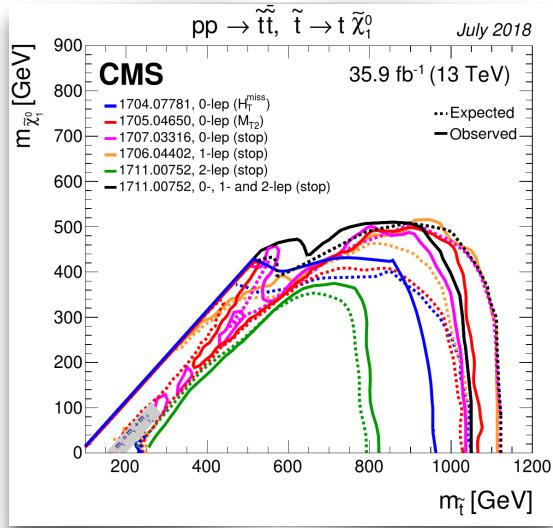
for composite Higgs, partial compositeness forces the strong sector to have color symmetry

# Motivation: naturalness

- But so far, no signs of colored top partners at the LHC



scalars



fermions

- Makes following question very relevant:

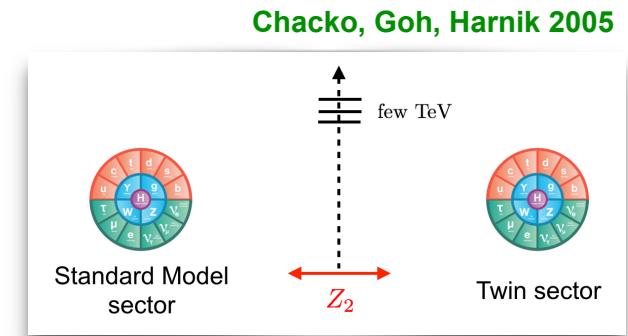
**What if the top partners **do not** have color charge?**

# Neutral Naturalness

- Symmetry-based solutions to little hierarchy problem with **color-neutral top partners**
- Stabilize weak scale up to  $\Lambda \sim 5 - 10$  TeV. Above: SUSY/compositeness/...

- Proof of principle was **Twin Higgs** framework

Top partners are **SM-singlet fermions**



Hidden sector phenomenology is model-dependent (*another talk...*)

But, we have robust indirect probe:

Higgs is pseudo-Goldstone  
with decay constant  $f$



$$\frac{hZZ}{(hZZ)_{\text{SM}}} = \cos \frac{v_A}{f} \simeq 1 - \frac{v^2}{2f^2}$$

# Supersymmetric Neutral Naturalness?

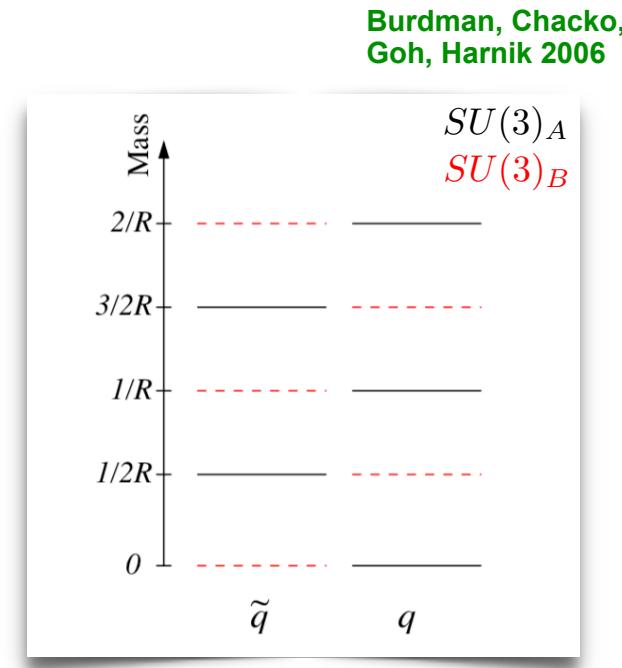
- If top partner is color-singlet, SUSY can only be **accidental**, realized at the level of spectrum

- **Folded SUSY**: orbifold extra dimension with Scherk-Schwarz SUSY breaking

$$SU(3)_A \times \textcolor{red}{SU(3)_B} \times SU(2) \times U(1)$$

$Z_2$

- Contribution of top sector to Higgs mass vanishes *exactly* at 1-loop



# Supersymmetric Neutral Naturalness?

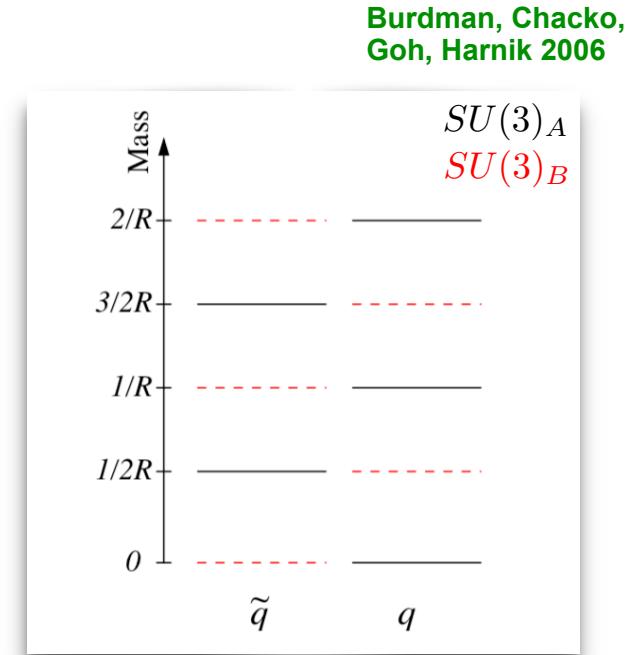
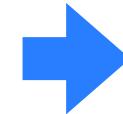
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- In this talk: **accidental SUSY from the bottom-up**
  - New set of exotic signatures at colliders
- In SUSY, Higgs coupling modifications are less robust

Cheng, Li, Salvioni, Verhaaren 1803.03651

# A Tripled Top model

Cheng, Li, Salvioni,  
Verhaaren 1803.03651

- Add **two** copies of the MSSM top sector,

$$SU(3)_A \times SU(3)_B \times SU(3)_C \times SU(2) \times U(1)$$

- Superpotential

$$W = y_t (Q_A H u_A^c + Q_B H u_B^c + Q_C H u_C^c) + M(u'_B u_B^c + u'_C u_C^c)$$

few TeV

$Z_3 \qquad \qquad \qquad Z_2$

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$Z_3$                                      $Z_2$

- Leading soft masses

$$V_s = +\tilde{m}^2 \left( |\tilde{Q}_A|^2 + |\tilde{u}_A^c|^2 \right) - \tilde{m}^2 \left( |\tilde{u}_B^c|^2 + |\tilde{u}_C^c|^2 \right)$$

**raise** SM-colored stops

**lower**  $SU(2)$ -singlet  
hidden stops

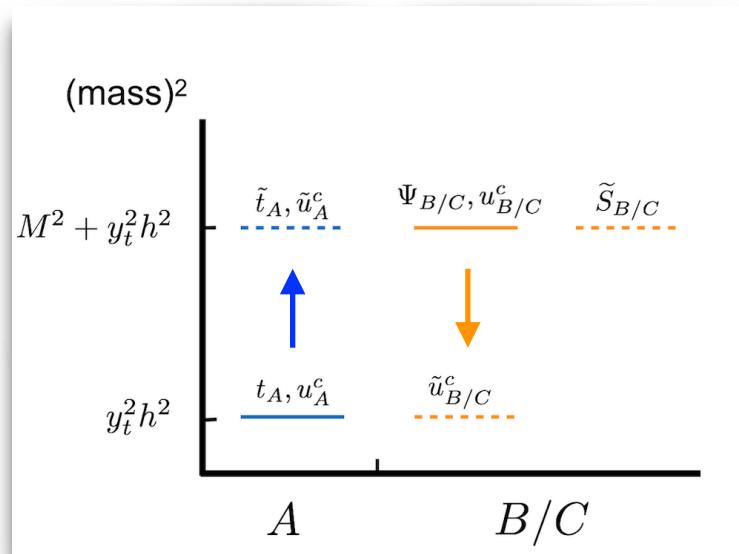
# A Tripled Top model

\* Add two copies of the

## accidental SUSY

for

$$\tilde{m} \rightarrow M$$



Cheng, Li, Salvioni,  
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- Departures from accidental SUSY limit:  $\Delta \equiv \sqrt{M^2 - \tilde{m}^2} \neq 0$   
+ SUSY mass for doublets,  $\omega(Q_B Q'_B{}^c + Q_C Q'_C{}^c) \in W$

**Both OK** as long as  $\Delta, \omega \ll \text{TeV}$ , for example

$$\delta m_H^2 \approx -\frac{N_c y_t^2}{8\pi^2} \omega^2 \ln \frac{M^2}{\omega^2}$$

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- Hypercharge assignments for hidden fields are **free**,  
only requirement is invariance of Yukawas

$$W = y_t (Q_A H u_A^c + Q_B H u_B^c + Q_C H u_C^c)$$



We can choose  $Q_{B,C} \sim \mathbf{2}_{-1/2}$

$$u_{B,C}^c \sim \mathbf{1}_0$$

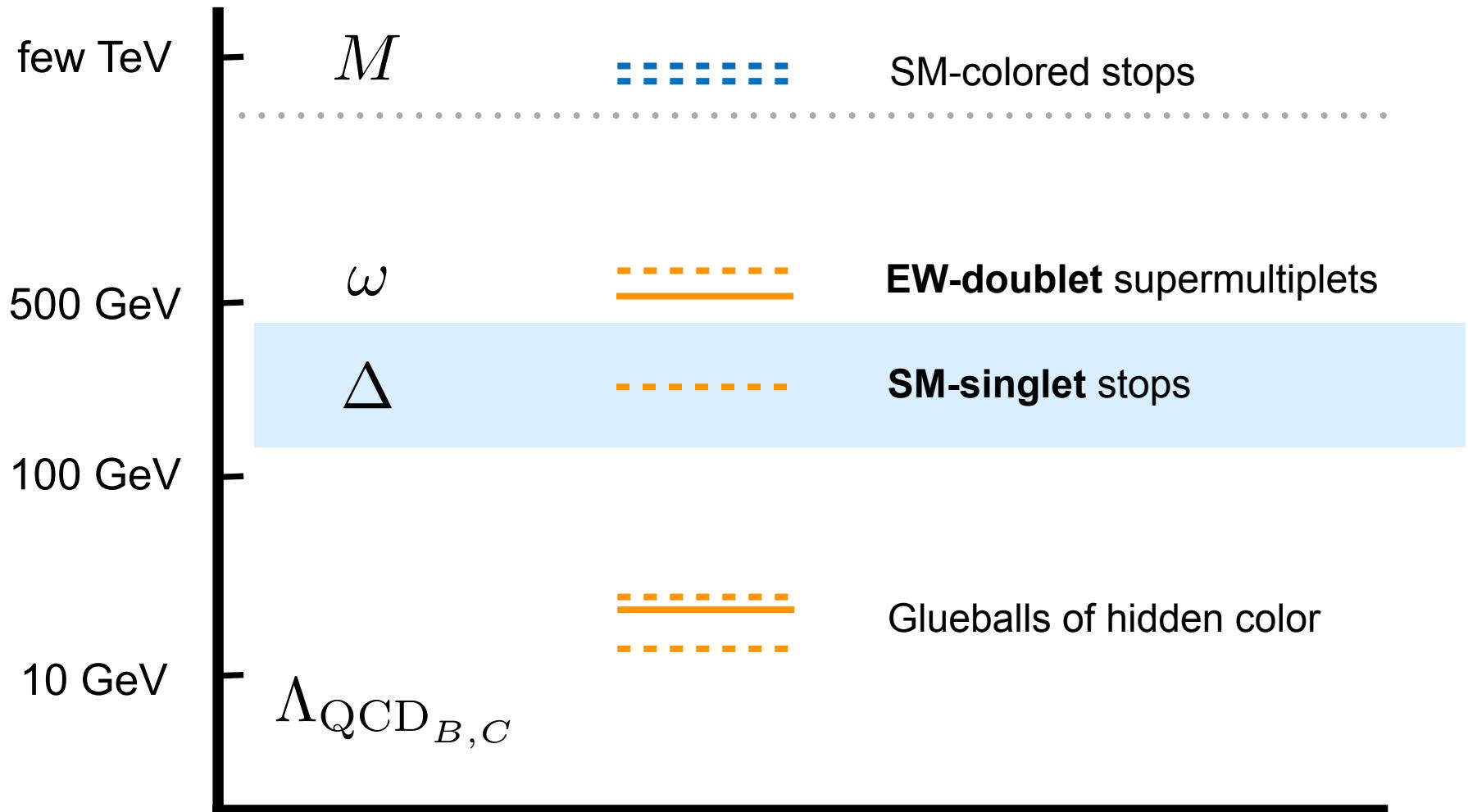
**SM-singlet scalar top partners**

same result, very different model:

Cohen, Craig, Giudice, McCullough 2018

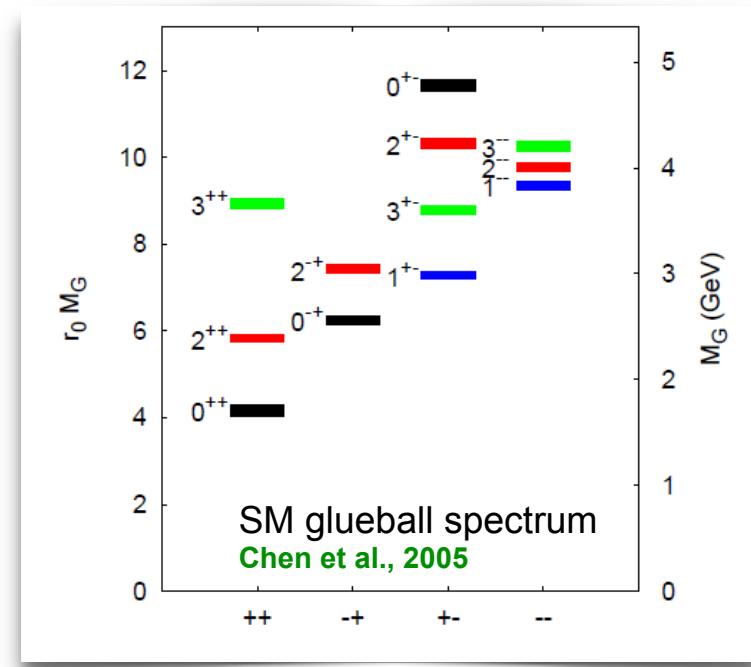
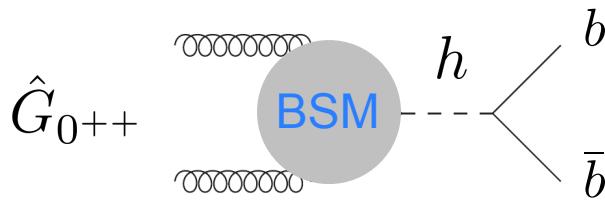
# BSM spectrum

mass



# Hidden sector confinement

- Hidden QCD confines at  $\sim$  few GeV
- No light matter, low-energy spectrum is made of **glueballs**
- Lightest glueball has  $J^{PC} = 0^{++}$ , decays to SM via mixing with the Higgs



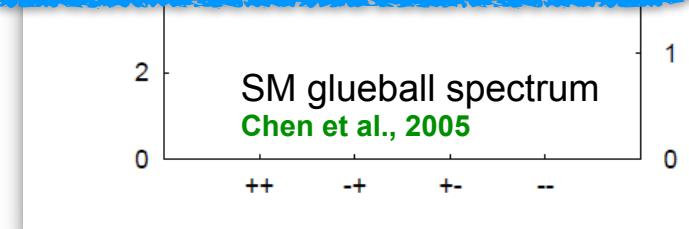
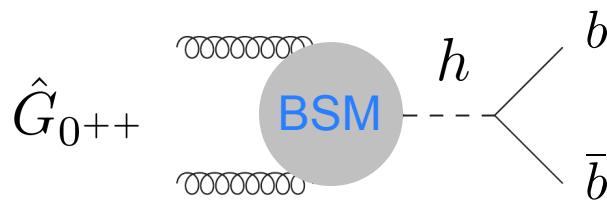
$$c\tau_{0^{++}} \sim 1.2 \text{ m} \left( \frac{5 \text{ GeV}}{\Lambda_{\text{QCD}}_{B,C}} \right)^7 \left( \frac{\omega}{500 \text{ GeV}} \right)^4 \left( \frac{\Delta}{300 \text{ GeV}} \right)^4 \left( \frac{100 \text{ GeV}}{\delta m} \right)^4$$

- Lifetime is much **longer** than e.g. in Folded SUSY ( $\sim$  mm)
- **Large uncertainty** because depends on **subleading soft masses**

# Hidden sector confinement

Assume hidden glueballs escape LHC detectors.

**Look for other, more robust signatures**

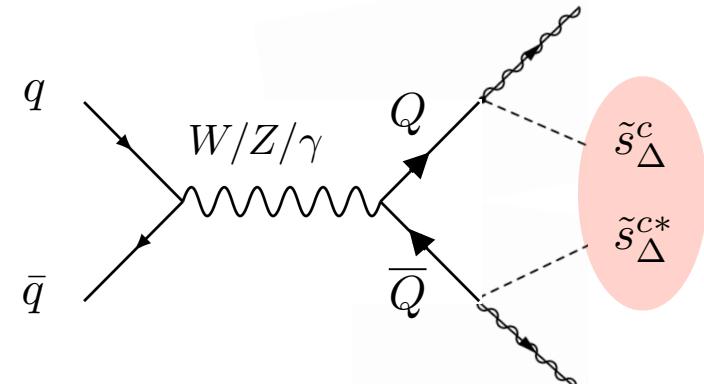


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# Light singlet scalars

- The **singlet scalars** are lightest matter in hidden sectors
- Dominant production from EW-doublets,  
decay down to light scalar  $\tilde{s}_\Delta^c$



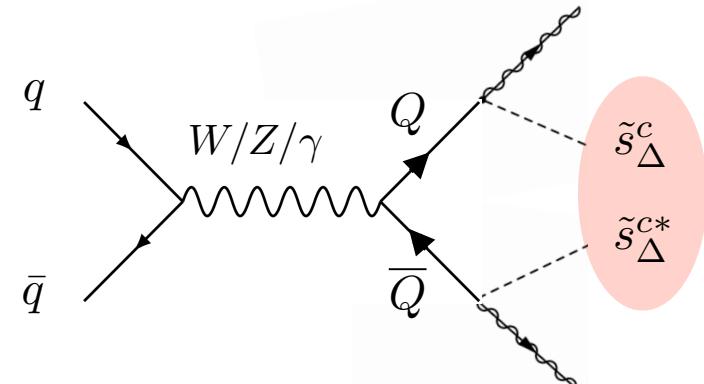
→ typical LHC event results in formation of “squicky” pair

**De-excitation mechanism?**

Kang, Luty 2008

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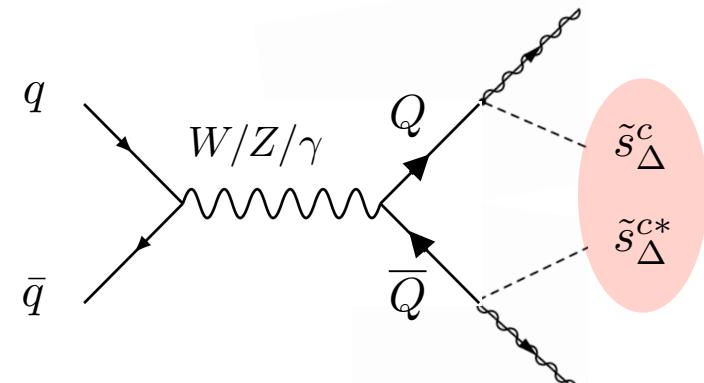
## De-excitation mechanism?

Glueball radiation is prompt, but does not complete de-excitation down to ground state  
Residual kinetic energy

$$K \lesssim m_0 \simeq 7\Lambda_{\text{QCD}_{B,C}} \longleftrightarrow n \sim 10$$

# Light singlet scalars

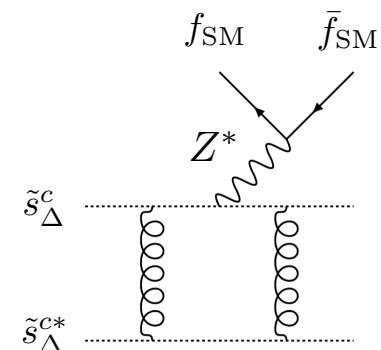
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## De-excitation mechanism?

The Higgs VEV gives **small mass mixing** of singlet and doublet scalars,  $\tilde{s}_\Delta^c$  inherits **coupling to Z**

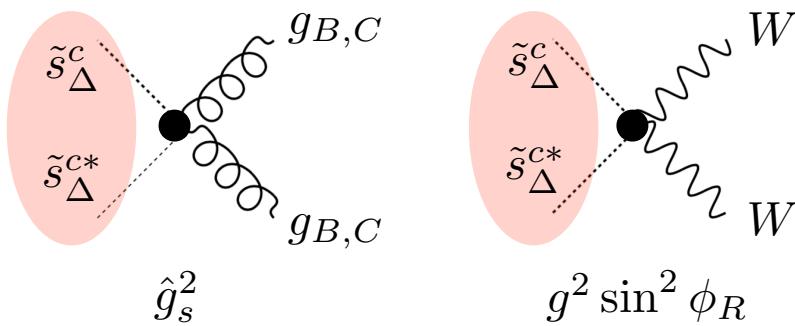


$$t_{\text{de-excite}}^Z \sim \frac{32}{27\pi^4} \frac{\cos^4 \theta_w}{\alpha_W^2 \sin^4 \phi_R N_f} \frac{m_Z^4 m_{\tilde{s}_\Delta^c}^4 m_0^3}{\sigma^6} \sim 4 \cdot 10^{-13} \text{ s} \left( \frac{5 \text{ GeV}}{\Lambda_{\text{QCD}_{B,C}}} \right)^9 \left( \frac{m_{\tilde{s}_\Delta^c}}{300 \text{ GeV}} \right)^4$$

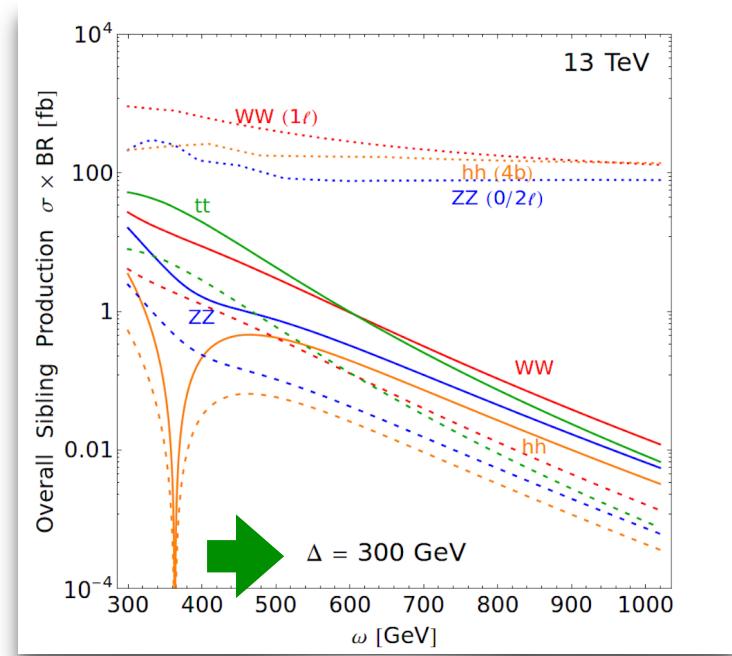
$\sim 0.1 \text{ mm}$ , still prompt

# Light singlet scalars

- Lowest-lying bound state has  $J^{PC} = 0^{++}$
- Annihilates dominantly to invisible glueballs, **BR(SM) ~ % level**



- Resonant signals well below current sensitivity
- **Very light singlets are allowed**



- Extra particles from cascade decays may give further constraints

# Light hidden mesons

- **Switch everywhere**

Cheng, Li, Salvioni,  
Verhaaren, in progress

weak doublets            singlets

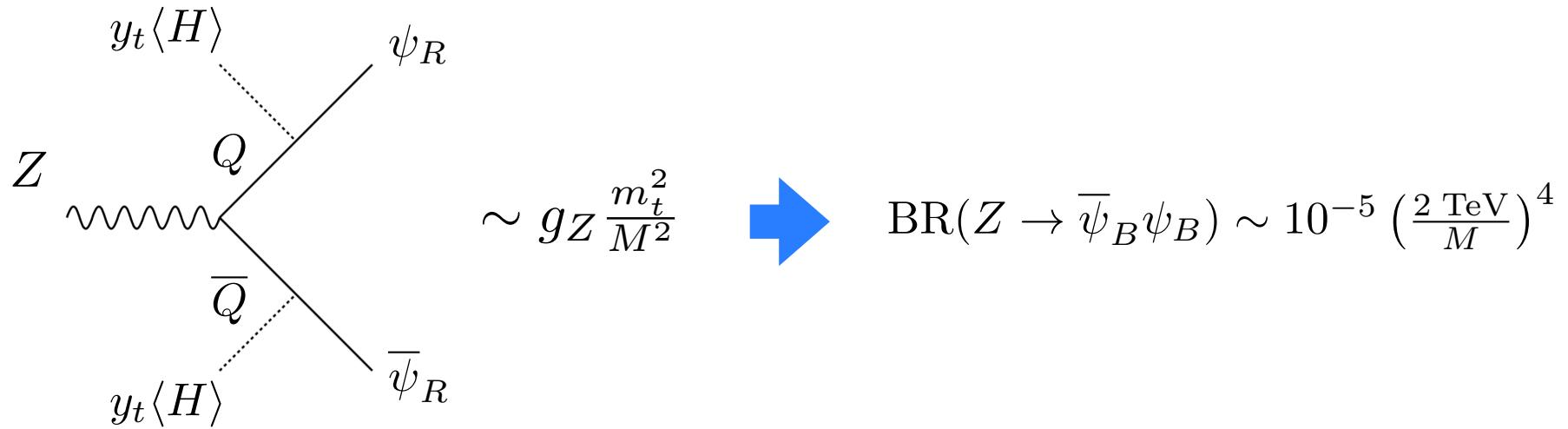
 Higgs potential is **unaffected**

- Top partners are now EW-doublet scalars, Drell-Yan + resonant signals
- $\omega$  is SM-singlet SUSY mass, technically natural to have  $\omega \ll \Lambda_{\text{QCD}_{B,C}}$
- Lightest hidden hadrons are not glueballs, but  $(\bar{\psi}\psi)$  **mesons**

$\hat{\eta}$	$\hat{\Upsilon}$	$\hat{\chi}$	(1-flavor QCD)
$J^{PC} =$	$0^{-+}$	$1^{--}$	$0^{++}$

# Z portal to hidden sector

- Top Yukawa mixes doublets and singlets when Higgs gets VEV

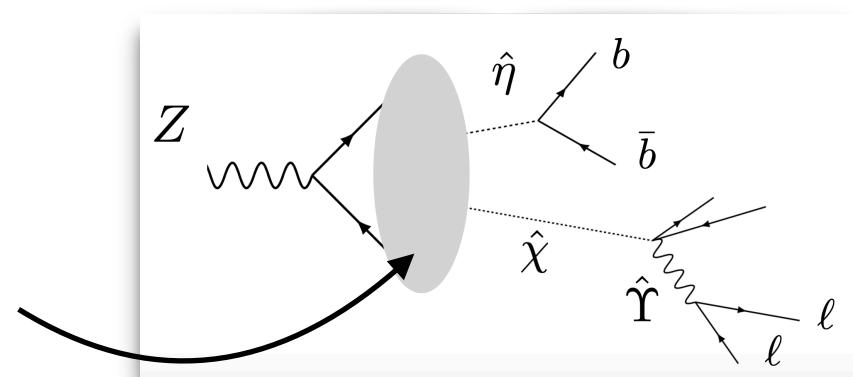


- For meson masses  $\gtrsim 20$  GeV, **decays are prompt**

Most promising signature at LHC:

Cheng, Li, Salvioni,  
Verhaaren, in progress

EFT  $Z_\mu (\hat{\eta} \partial_\mu \hat{\chi} - \partial_\mu \hat{\eta} \hat{\chi})$

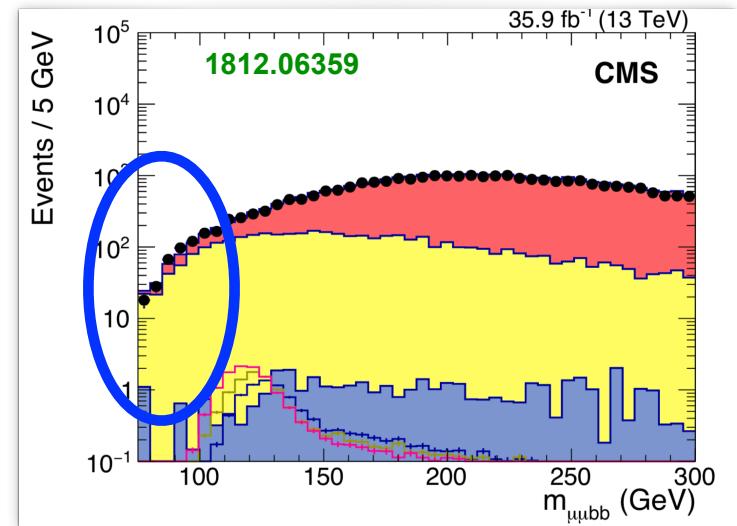


# Z portal to hidden sector

- Recent CMS search for  $h \rightarrow a a \rightarrow b\bar{b} \mu\mu$  has some sensitivity

Compute (suppressed) signal efficiency,  
find  $N_S \approx 16 \left(\frac{2 \text{ TeV}}{M}\right)^4$  signal events

$$\{M_\eta, M_Y, M_\chi\} = \{24, 25, 30\} \text{ GeV}$$

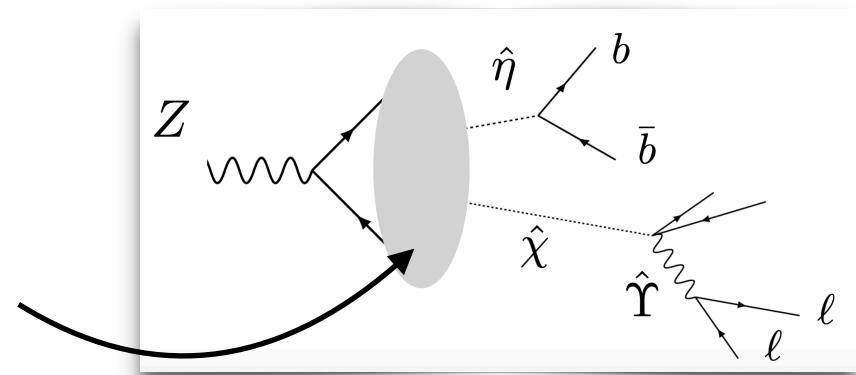


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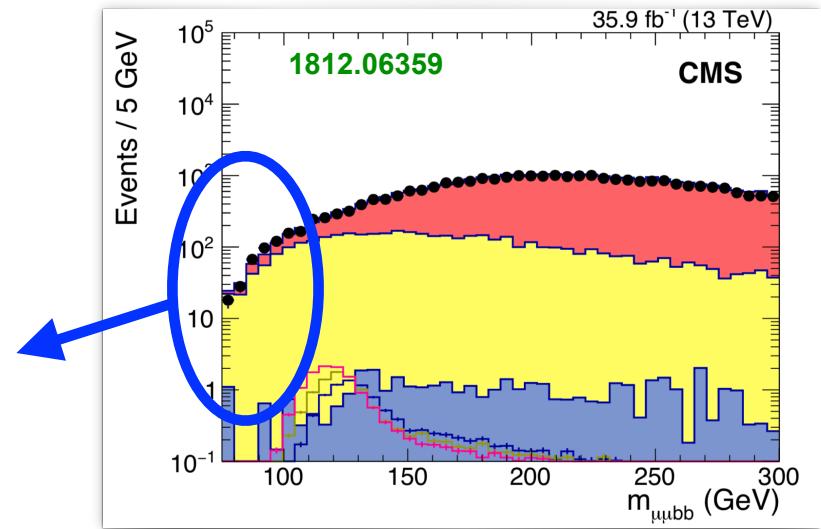
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**preliminary**



$$M \gtrsim 1.9 \text{ TeV}$$

$$\{M_\eta, M_Y, M_\chi\} = \{24, 25, 30\} \text{ GeV}$$

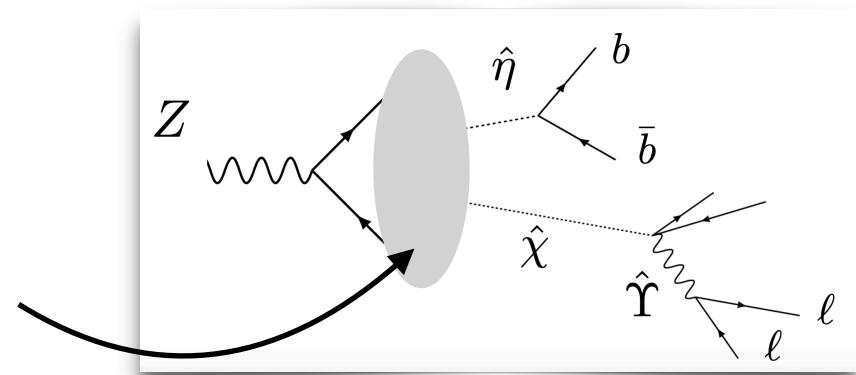


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# Summary

- Connection between naturalness and LHC coverage is so crucial, it **must** be analyzed in all possible guises
- **Neutral naturalness** theories challenge standard assumption that top partners interact via QCD
- “Tripled Top” is new framework, based on **accidental SUSY**
- In one limit, top partners are *singlet scalars*
  - arguably, the most elusive kind
- In other limit, hidden sector accessible via *rare Z decays*
  - At LHC, challenge to keep cuts as soft as possible
  - Reach at future Z factories? *In progress...*

# Backup

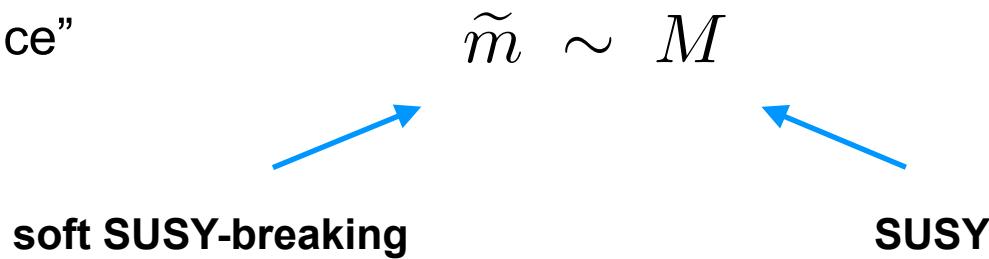
# Necessary ingredients

- A particular structure for the soft masses

$$V_s = +\tilde{m}^2 \left( |\tilde{Q}_A|^2 + |\tilde{u}_A^c|^2 \right) - \tilde{m}^2 \left( |\tilde{u}_B^c|^2 + |\tilde{u}_C^c|^2 \right)$$

Possible origins in next slide

- A “coincidence”



If no mechanism can explain it, **tuning**  $\sim \frac{\Delta^2}{M^2} \sim \text{few \%}$

$$(\Delta = \sqrt{M^2 - \tilde{m}^2})$$

$$M \sim \text{few TeV}$$

$$\Delta \sim \text{few} \times (100 \text{ GeV})$$

# The soft masses?

- Soft masses of equal size and opposite sign?

$$V_s = + \tilde{m}^2 \left( |\tilde{Q}_A|^2 + |\tilde{u}_A^c|^2 \right) - \tilde{m}^2 \left( |\tilde{u}_B^c|^2 + |\tilde{u}_C^c|^2 \right)$$

**1. First guess:**  $D$ -term of extra  $U(1)$ , charges +1 and -1

But then, Yukawas are not invariant  $W \ni y_t (Q_A H u_A^c + Q_B H u_B^c + Q_C H u_C^c)$

Insertions of  $U(1)$ -breaking field spoil the  $Z_3$

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**2. Working model:** exploit properties of strongly coupled SUSY gauge theories

Top fields are **composite mesons**  $P_i \bar{P}_j$  of s-confining SQCD

$$SU(N), \quad F = N + 1$$

Arkani-Hamed, Rattazzi 1998

$$m_{ij}^2 = m_{P_i}^2 + m_{\bar{P}_j}^2 - \frac{2}{b} \sum_k T_{r_k} (m_{P_k}^2 + m_{\bar{P}_k}^2)$$

soft masses of IR composites

soft masses of UV constituents

# The soft masses

$SU(2) \quad F = 3$

Cheng, Li, Salvioni,  
Verhaaren, 1803.03651

$$\begin{array}{c} \tilde{m}_P^2 \quad \tilde{m}_P^2 \quad \tilde{m}_P^2 \\ \tilde{m}_{\bar{P}_2}^2 \quad \left( \begin{array}{c} Q_A \\ \hline \end{array} \right) \\ \tilde{m}_{\bar{P}_2}^2 \\ \tilde{m}_{\bar{P}_1}^2 \end{array}$$

$$\begin{array}{c} \tilde{m}_P^2 \quad \tilde{m}_P^2 \quad \tilde{m}_P^2 \\ \tilde{m}_{\bar{P}_2}^2 \quad \left( \begin{array}{c} u_A^c \\ \hline \end{array} \right) \\ \tilde{m}_{\bar{P}_2}^2 \\ \tilde{m}_{\bar{P}_1}^2 \end{array}$$

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$$m_{ij}^2 = m_{P_i}^2 + m_{\bar{P}_j}^2 - \frac{2}{b} \sum_k T_{r_k} (m_{P_k}^2 + m_{\bar{P}_k}^2)$$



(e.g.:  $m_{\bar{P}_2}^2 > 0$ ,  $m_{\bar{P}_1}^2 = 0$ )

$$(b = 3N - F)$$

$$V_s = +\tilde{m}^2 \left( |\tilde{Q}_A|^2 + |\tilde{u}_A^c|^2 \right) - \tilde{m}^2 \left( |\tilde{u}_B^c|^2 + |\tilde{u}_C^c|^2 \right)$$

- $Z_3$  - symmetric Yukawas

$$W \ni \frac{g_t}{\Lambda_{\text{UV}}^2} P \bar{P} P \bar{P} H \longrightarrow y_t \sim g_t \frac{\Lambda_G^2}{\Lambda_{\text{UV}}^2}$$

# Soft masses of composite mesons

- s-confinement = smooth confinement without chiral symmetry breaking and with non-vanishing confining superpotential

- In the UV, from  $P \rightarrow \sqrt{Z} P$

Arkani-Hamed, Rattazzi  
hep-th/9804068

$$\frac{1}{4} \int d^2\theta S(\mu_{\text{UV}}) W^2 + \text{h.c.} + \int d^4\theta Z F \left( S(\mu_{\text{UV}}) + S^\dagger(\mu_{\text{UV}}) - \frac{T}{4\pi^2} \ln Z \right) P^\dagger e^V P$$

- Anomalous  $U(1)$  symmetry  $Z \rightarrow Z\chi\chi^\dagger$ ,  $P \rightarrow P/\chi$ ,  $S(\mu_{\text{UV}}) \rightarrow S(\mu_{\text{UV}}) + \frac{T}{4\pi^2} \ln \chi$   
 $Z$  is promoted to background vector superfield

- Only invariant object is  $I = \Lambda_h^\dagger Z^{2T/b} \Lambda_h$  ( $\Lambda_h = \mu_{\text{UV}} e^{-8\pi^2 S/b}$ )

and in the UV  $m_P^2(\mu_{\text{UV}}) = -[\ln Z]_{\theta^2\bar{\theta}^2} - [\ln F(\mu_{\text{UV}})]_{\theta^2\bar{\theta}^2} \xrightarrow{\mu_{\text{UV}} \rightarrow \infty} -[\ln Z]_{\theta^2\bar{\theta}^2}$

- In the IR, effective Kähler potential for mesons starts with

$$K \supset c_{M_{ij}} \frac{M_{ij}^\dagger Z_i Z_{\bar{j}} M_{ij}}{I} + \dots \quad \xrightarrow{\hspace{1cm}} \quad m_{M_{ij}}^2 = - \left[ \ln \frac{Z_i Z_{\bar{j}}}{I} \right]_{\theta^2\bar{\theta}^2} \underset{\mu_{\text{IR}} \rightarrow 0}{\Bigg|} = -[\ln Z_i]_{\theta^2\bar{\theta}^2} - [\ln Z_{\bar{j}}]_{\theta^2\bar{\theta}^2} + [\ln I]_{\theta^2\bar{\theta}^2} \\ = m_{P_i}^2 + m_{\bar{P}_j}^2 - \frac{2}{b} \sum_k T_{r_k} \left( m_{P_k}^2 + m_{\bar{P}_k}^2 \right)$$

# Higgs quartic and $T$ parameter

- Higgs quartic: for example  $\lambda \simeq \frac{N_c y_t^4}{16\pi^2} \left( \frac{3}{2} + \log \frac{\omega^2}{m_t^2} \right) + \frac{m_Z^2}{2v^2} \cos^2(2\beta)$

contribution of unmixed  
MSSM stops with mass  $\omega$

$$(\Delta \ll \omega)$$

Numerically,

$$M = 2 \text{ TeV}, \quad \Delta = 300 \text{ GeV}, \quad \omega = 500 \text{ GeV} \quad \rightarrow \quad \lambda \lesssim 0.14$$

but, 2-loop corrections important...

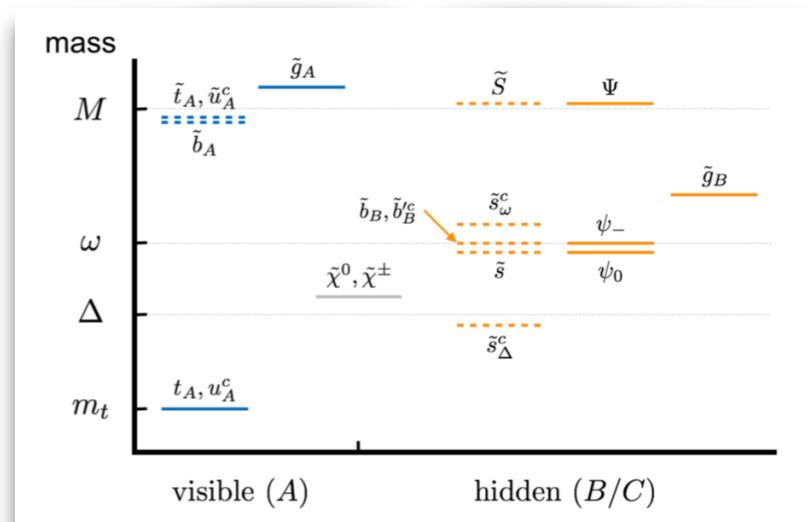
- $T$  parameter: leading contribution comes from light scalars,

$$\hat{T}_{s^c, B+C} \approx + \frac{N_c y_t^2}{48\pi^2} \frac{m_t^2}{\omega^2}$$

$$\omega = 500 \text{ GeV}, \quad \Delta = 300 \text{ GeV}$$

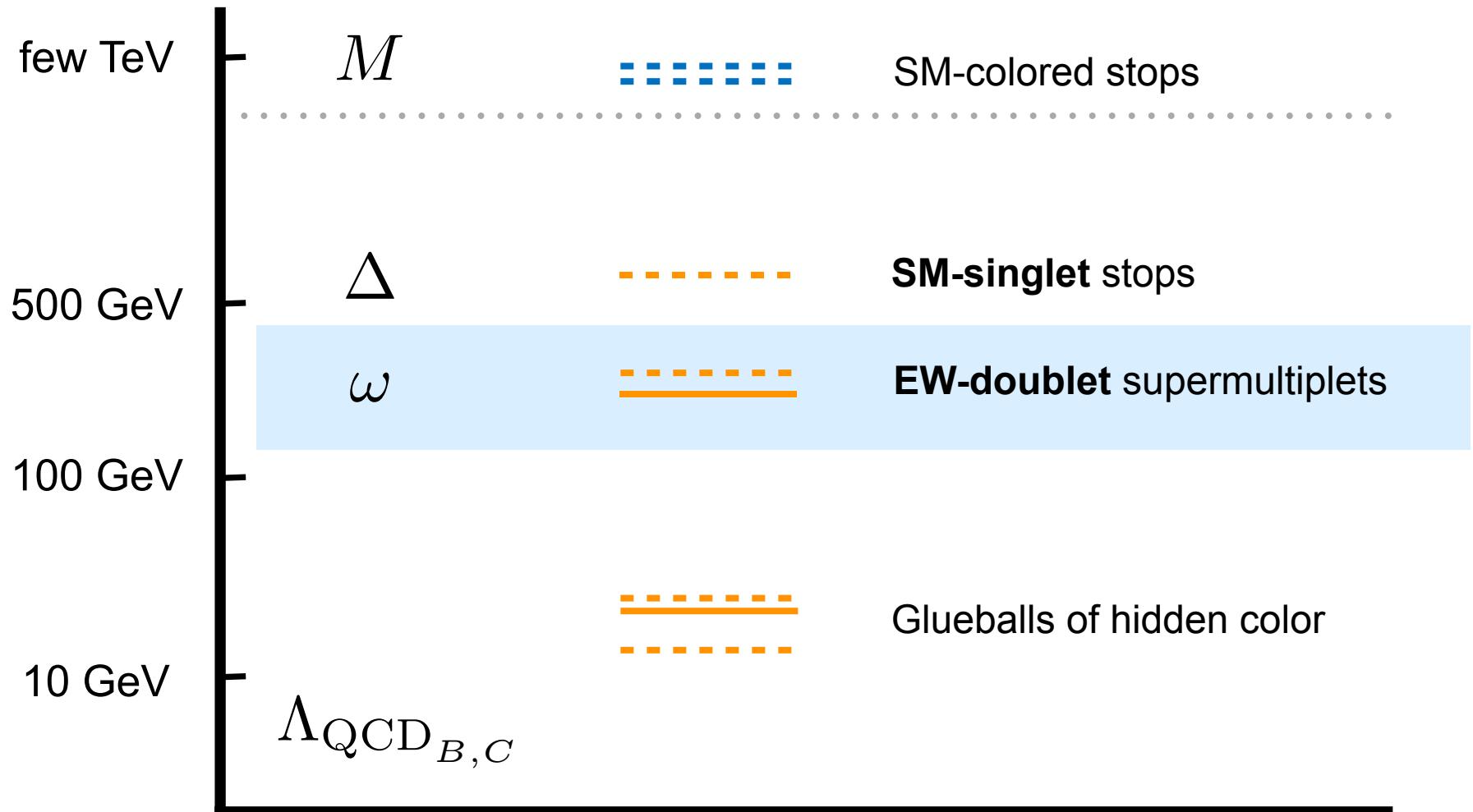
$$\rightarrow \hat{T}_{s^c, B+C} \approx + 4 \times 10^{-4}$$

under control



# Spectrum of BSM states: $\Delta > \omega$

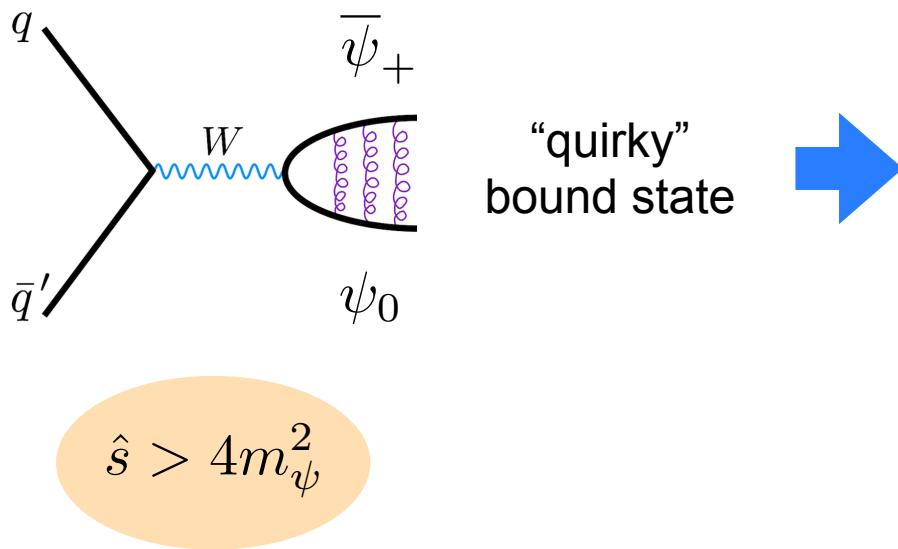
mass



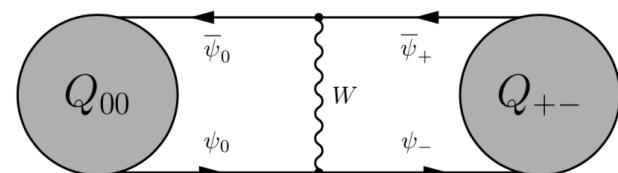
# $\Delta > \omega$ : quirk phenomenology

- If  $\Delta > \omega$ , then target are the EW-doublet supermultiplets with mass  $\sim \omega$
- Fermions have larger Drell-Yan production than scalars,

$$Q_{B,C} \sim \mathbf{2}_{-1/2} \sim \begin{pmatrix} \psi_0 \\ \psi_- \end{pmatrix}$$



de-excites down to ground state  
via emission of **soft photons**

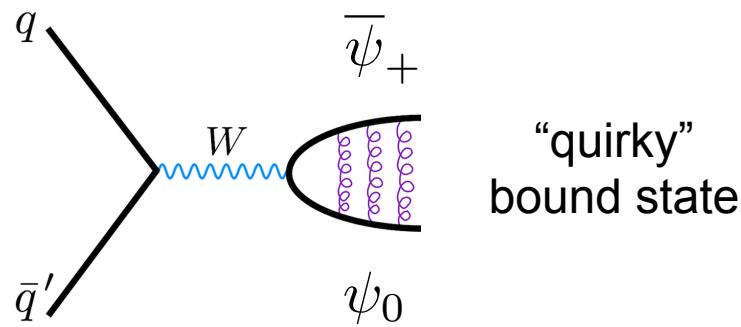


*(electrically-neutral pairs too,  
via mass mixing)*

# $\Delta > \omega$ : quirk phenomenology

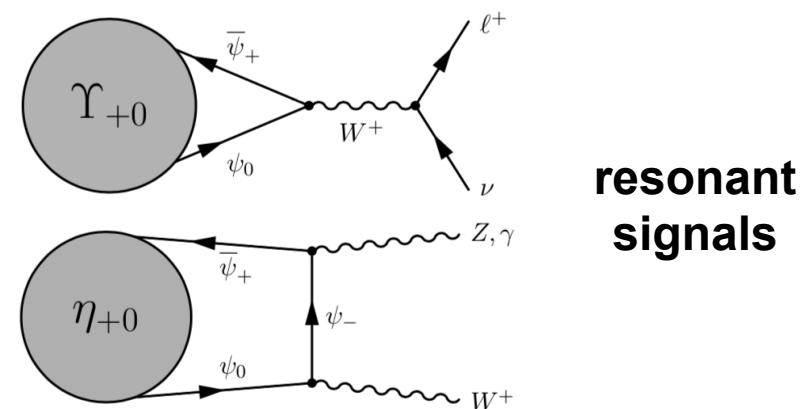
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de-excites down to ground state via emission of **soft photons**

annihilation of  $n = 1$  states

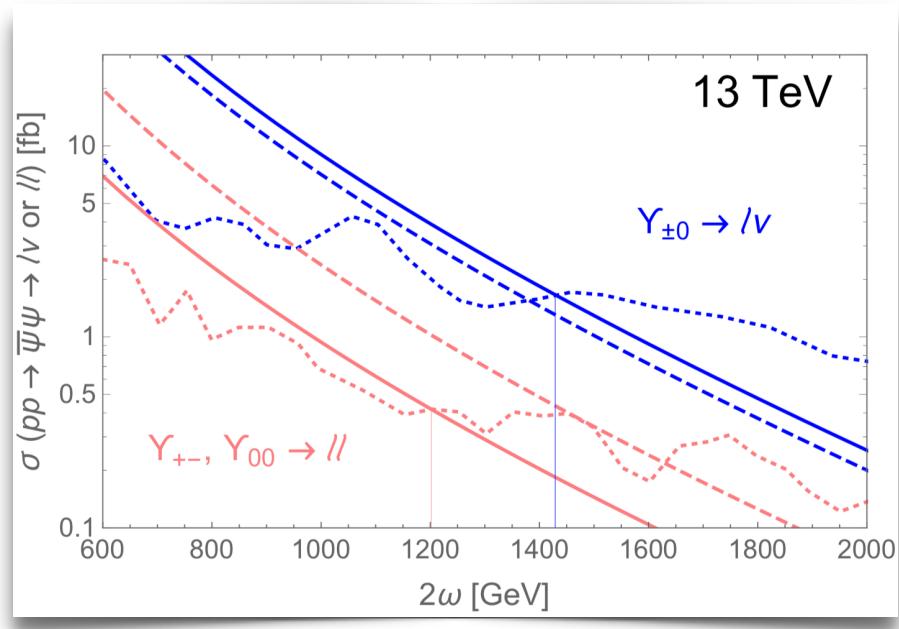


# $\Delta > \omega$ : quirk phenomenology

- Strongest bounds come from **charged channel**  
(decays to pure hidden gluons forbidden)

$\omega \gtrsim 700$  GeV

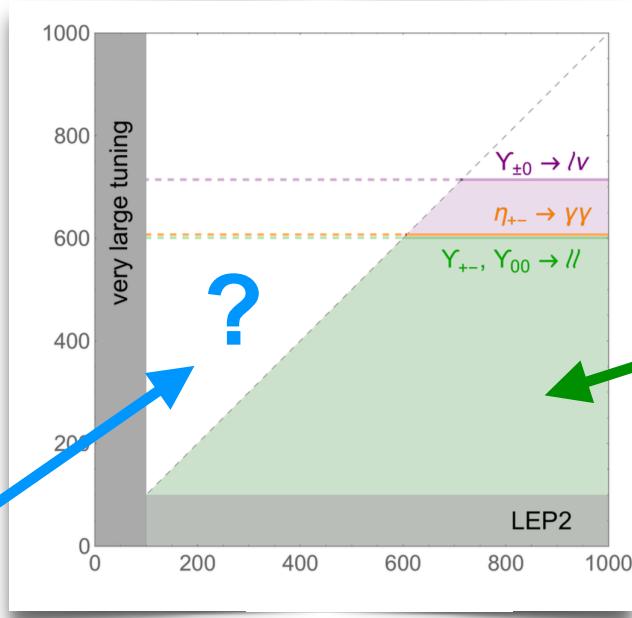
from  $\Upsilon_{+0} \rightarrow \ell\nu$



- Neutral channels give  $\omega \gtrsim 600$  GeV from  $\eta_{+-} \rightarrow \gamma\gamma$   
 $\Upsilon_{+-,00} \rightarrow ll$

# Tripled Top parameter space

$\omega$  [GeV]  
(EW-charged  
supermultiplets)

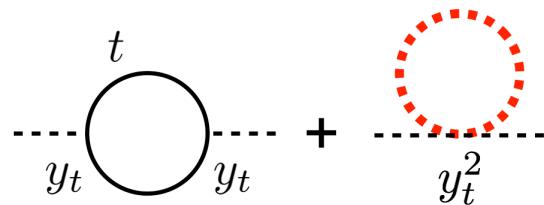


**cascade decays  
to light singlets**  
 $\Delta$  [GeV]  
(singlet scalar top partners)

**Drell-Yan  
+  
quirk  
resonant signals**

# More neutral naturalness

- The top partner zoo



$$\mathcal{L}_{\text{SUSY}} \sim y_t q H u^c + y_t^2 |\tilde{q} H|^2 + y_t^2 |\tilde{u}^c|^2 |H|^2$$

	scalar	fermion
QCD	SUSY	Composite Higgs
EW	Folded SUSY	Quirky Little Higgs
singlet	?	Twin Higgs

Can give stops hidden color, but they still **carry SM electroweak charges**

# More neutral naturalness

- The top partner zoo

	<i>scalar</i>	<i>fermion</i>
QCD	SUSY	Composite Higgs
<i>EW</i>	Folded SUSY	Quirky Little Higgs
<i>singlet</i>	?	Twin Higgs

$$\mathcal{L}_{\text{SUSY}} \sim y_t q H u^c + y_t^2 |\tilde{q} H|^2 + y_t^2 |\tilde{u}^c|^2 |H|^2$$

For **complete-singlet** top partners, need **both** stops coupled in this way

# The Hyperbolic Higgs

Cohen, Craig, Giudice,  
McCullough 2018

- Tree-level potential with flat direction

$$V = \lambda (|H_{\mathcal{H}}|^2 - |H|^2 - f^2)^2$$

Accidentally  $U(2,2)$  symmetric [not a symmetry of full theory]

- Each Higgs charged under its own  $SU(2) \times U(1)$

One massless mode,

$$h_{\text{SM}} = \cos \theta h + \sin \theta h_{\mathcal{H}} \quad \tan \theta = \frac{v}{v_{\mathcal{H}}}$$

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$$V = \lambda (|H_{\mathcal{H}}|^2 - |H|^2 - f^2)^2$$

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- Couplings to matter

$$\mathcal{L} = (y_t H \psi_Q \psi_{U^c} + \text{h.c.}) + y_t^2 \left( |H_{\mathcal{H}} \cdot \tilde{Q}_{\mathcal{H}}|^2 + |H_{\mathcal{H}}|^2 |\tilde{U}_{\mathcal{H}}^c|^2 \right)$$

$\mathbb{Z}_2$  symmetry

quadratic 1-loop correction



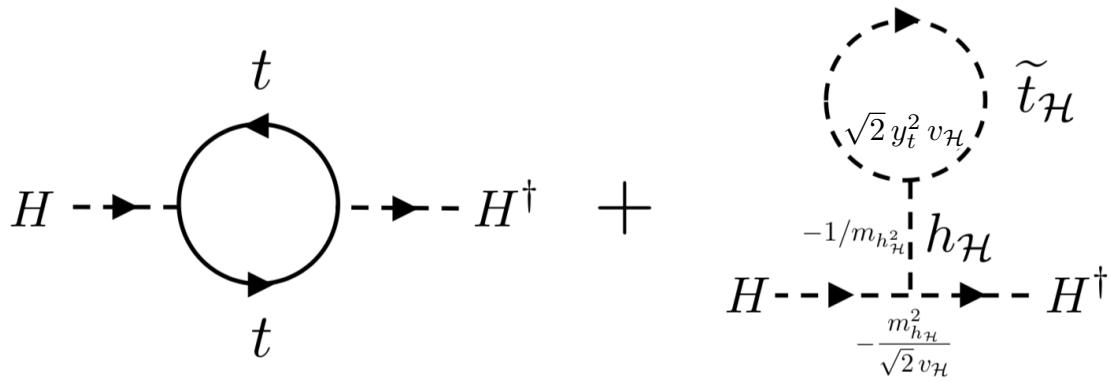
$$\delta V \sim \frac{N_c y_t^2}{16\pi^2} \Lambda^2 (|H_{\mathcal{H}}|^2 - |H|^2)$$

respects  $U(2,2)$

# The Hyperbolic Higgs

Cohen, Craig, Giudice,  
McCullough 2018

- Diagrammatic cancellation

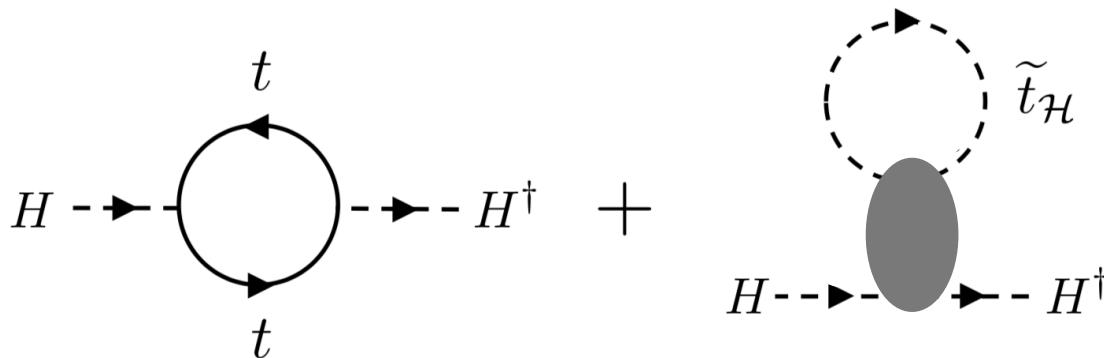


$$\mathcal{L} = (y_t H \psi_Q \psi_{U^c} + \text{h.c.}) + y_t^2 \left( |H_{\mathcal{H}} \cdot \tilde{Q}_{\mathcal{H}}|^2 + |H_{\mathcal{H}}|^2 |\tilde{U}_{\mathcal{H}}^c|^2 \right)$$

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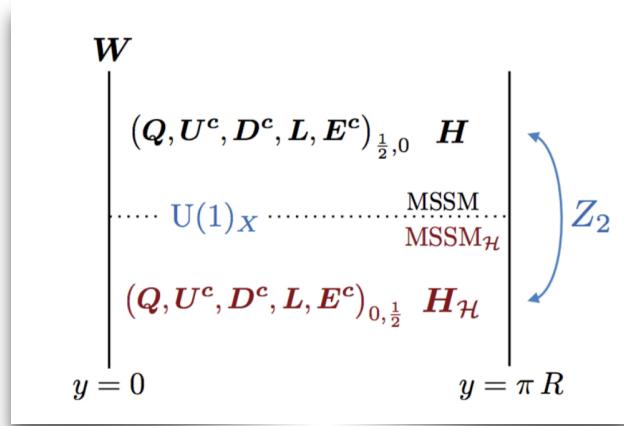


Integrate out heavy radial mode

$$\mathcal{L}_{\text{eff}} = (y_t H \psi_Q \psi_{U^c} + \text{h.c.}) + y_t^2 |H|^2 (|\tilde{t}_{\mathcal{H}}^L|^2 + |\tilde{t}_{\mathcal{H}}^R|^2)$$

$SU(2)_{\mathcal{H}}$  broken below  $v_{\mathcal{H}}$

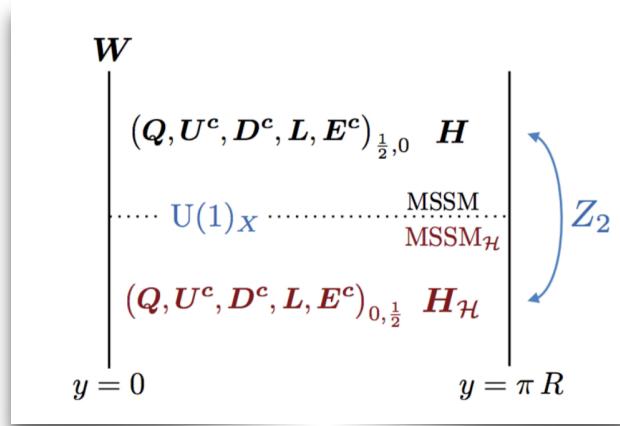
# A 5D SUSY completion



$$\Lambda \sim 1/R$$

- $U(1)_X$   $D$ -term potential  $V_X = \frac{g_X^2}{2} \xi (|H_{\mathcal{H}}|^2 - |H|^2 - f_X^2)^2$

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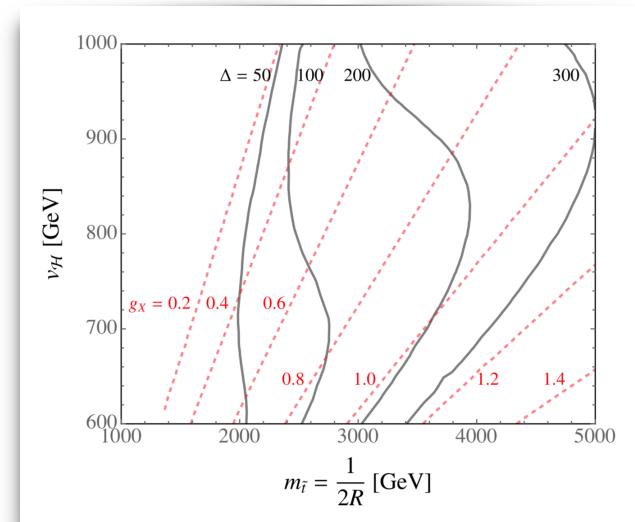
- SUSY breaking gives at 1-loop

$$V_{U(2,2)} \sim \frac{g_X^2 M_X^2}{16\pi^2} (|H|^2 + |H_{\mathcal{H}}|^2)$$

$T$  parameter



$$\frac{M_X}{g_X} \gtrsim 8.6 \text{ TeV}$$



# Phenomenology

- SM and hyperbolic Higgses mix, **universal coupling modification**

$$\frac{y_{hPP}}{y_{hPP}^{\text{SM}}} = \cos \theta \simeq 1 - 1.5\% \rho^2 \left( \frac{\text{TeV}}{v_{\mathcal{H}}} \right)^2$$

+ non-universal correction for the top

$$m_t(H) = \frac{1}{\pi R} \arctan(\pi R y_t |H|) \quad \rightarrow \quad -\pi^2 R^2 y_t^2 v^2 \simeq -1.2\% \left( \frac{5 \text{ TeV}}{1/R} \right)^2$$

- Higgs decays to hyperbolic glue,

$$\text{BR}(h_{\text{SM}} \rightarrow g_{\mathcal{H}} g_{\mathcal{H}}) \sim 2 \times 10^{-5} \rho^2 \left( \frac{\text{TeV}}{v_{\mathcal{H}}} \right)^4$$

# Spontaneous breaking of hidden color?

Cohen, Craig, Giudice,  
McCullough 2018

- What if the hyperbolic stops get VEVs?  $\langle \tilde{t}_{\mathcal{H}}^{L,R} \rangle \neq 0$ 
  - 8 dofs eaten by massive  $SU(3)_{\mathcal{H}}$  gluons
  - radial modes mix with the Higgs
    - *Higgs is partly its own top partner*
- No hidden confinement, **collider pheno strongly altered**

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- For Tripled Top: only **one** light singlet stop in each sector, expect

$$SU(3)_B \xrightarrow{\langle \tilde{u}_B^c \rangle} SU(2)_B$$

depending on VEV size,  $SU(2)$  glueballs  
may still be at bottom of the spectrum