

Angular distributions, correlation and linear polarization in tracking arrays

- Status now
- Ang cor results with sources
- Ang cor formalism and results in-beam
- Lin pol sources with no source calibration
- Lin pol in-beam with no source calibration
- Angular distribution, new idea?
- Conclusions

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Status now, as we see it

method	source	in-beam	need source cal
ang dis	N/A	problem!	yes
ang cor	OK		no
lin-pol			yes

Good examples shown
last time



Lots of discussion...



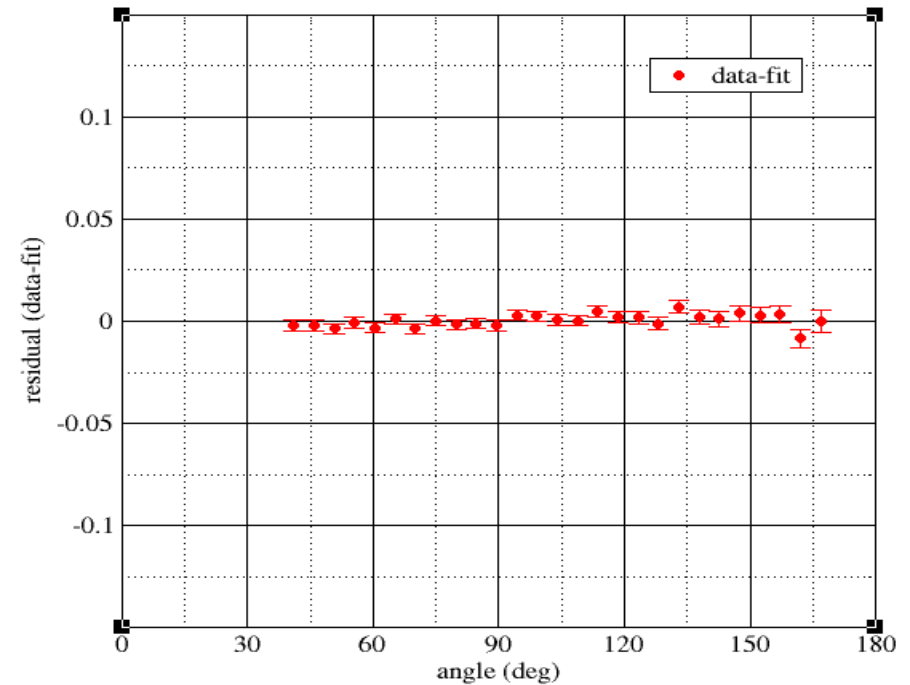
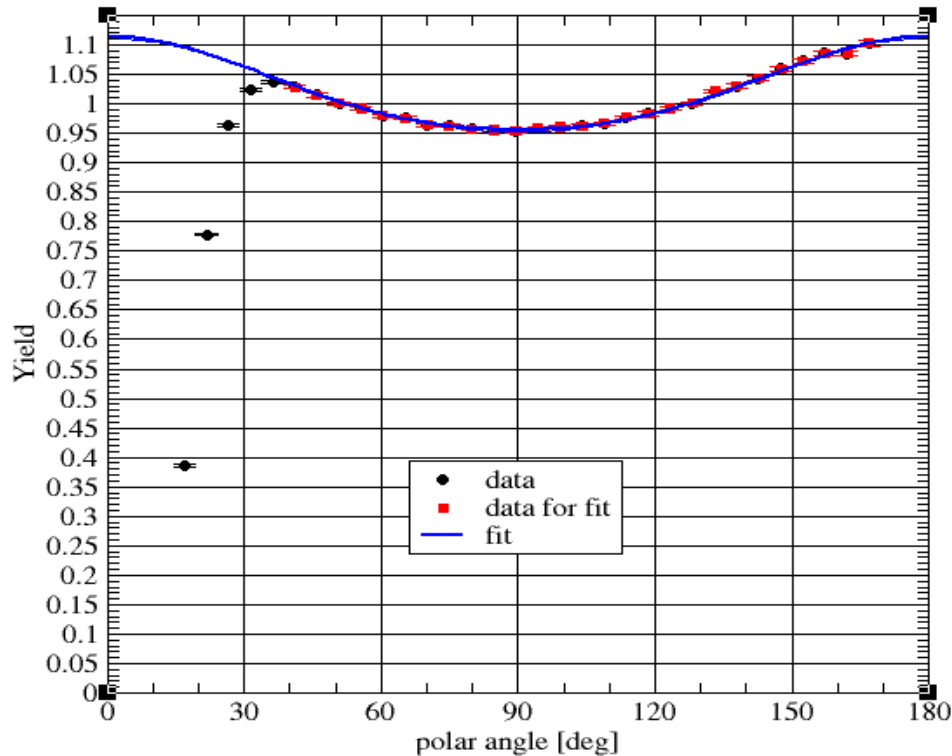
Yikes!



Some source angcor results

(high statistics)

^{60}Co 1173/1333 (classic)



ordinary legfit a0,a2,a4 fit>>>

chi**2: 1.083

a0: 1.000 +/- 0.001

a2: 0.100 +/- 0.002

a4: 0.014 +/- 0.002

----- l_i= 4.0

| L1= 2.0

| L1'= 3.0

| del= 0.000

----- l= 2.0

| L2= 2.0

| L2'= 3.0

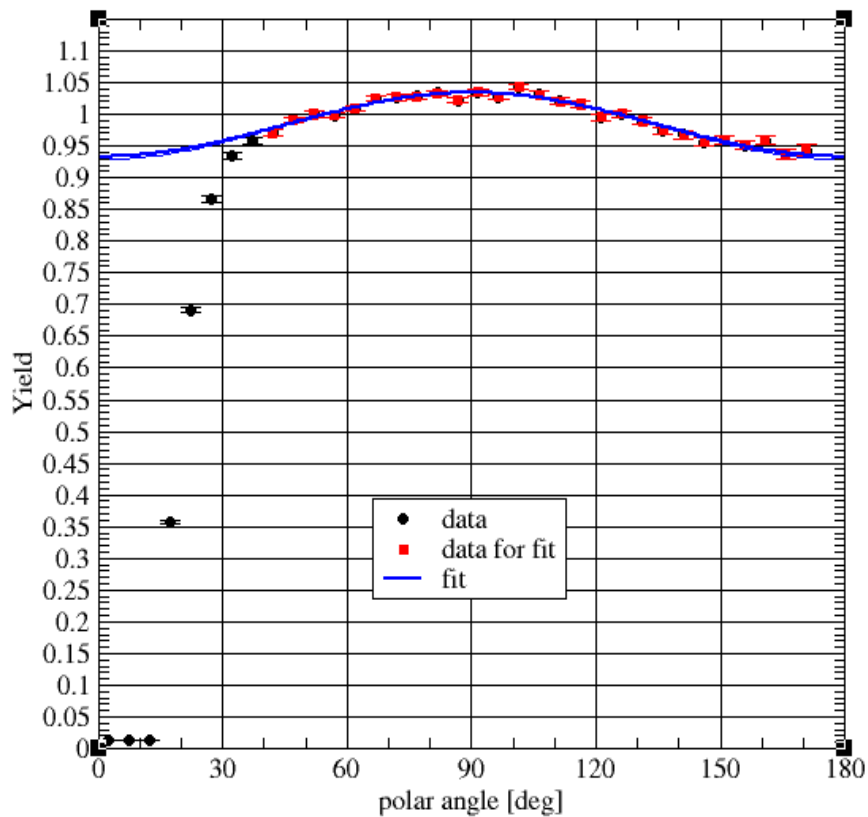
| del= 0.000

----- l_f= 0.0

angular correlation coefficients:

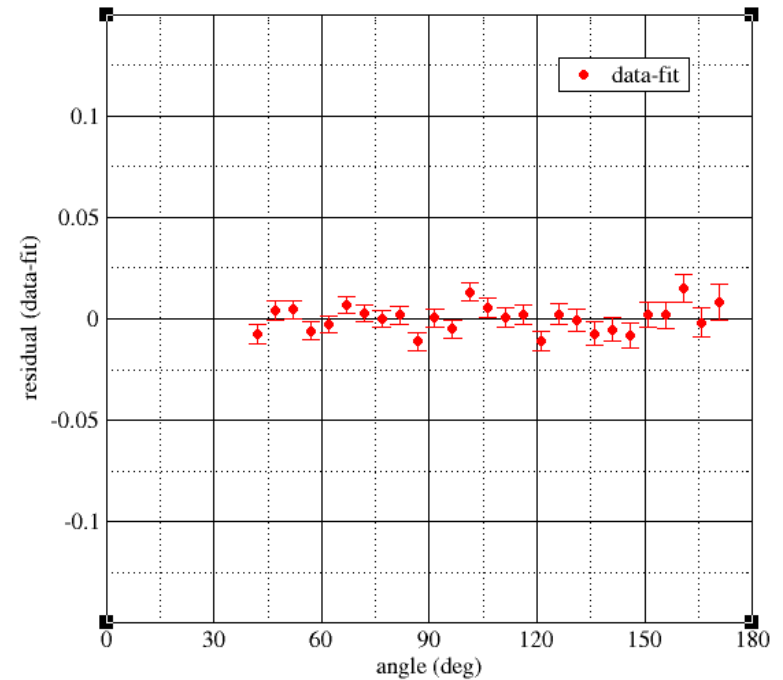
A0 = +1.000000 A2 = +0.102041 A4 = +0.009070 A6 = +0.000000

^{88}Y 898/1836



Fri Sep 20 14:59:44 2019

chi**2: 1.644
a0: 1.000 +/- 0.001
a2: -0.067 +/- 0.002
a4: 0.004 +/- 0.003



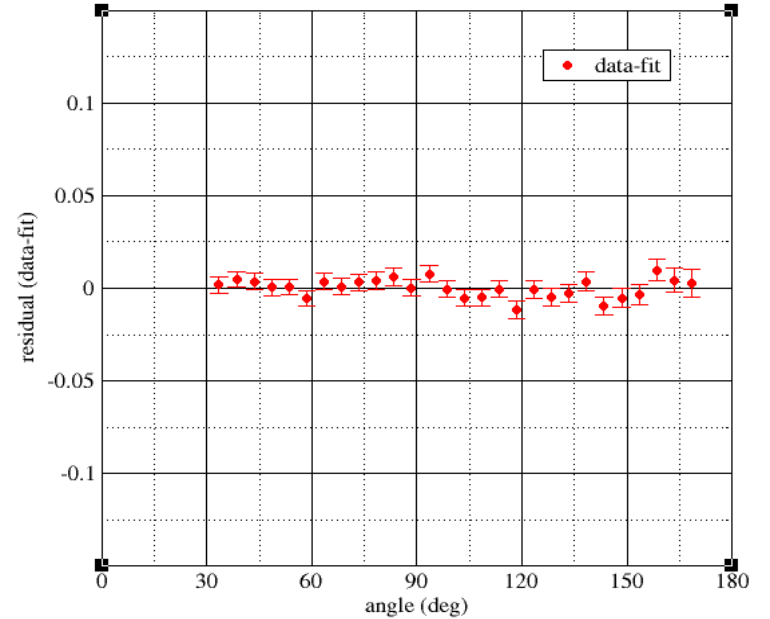
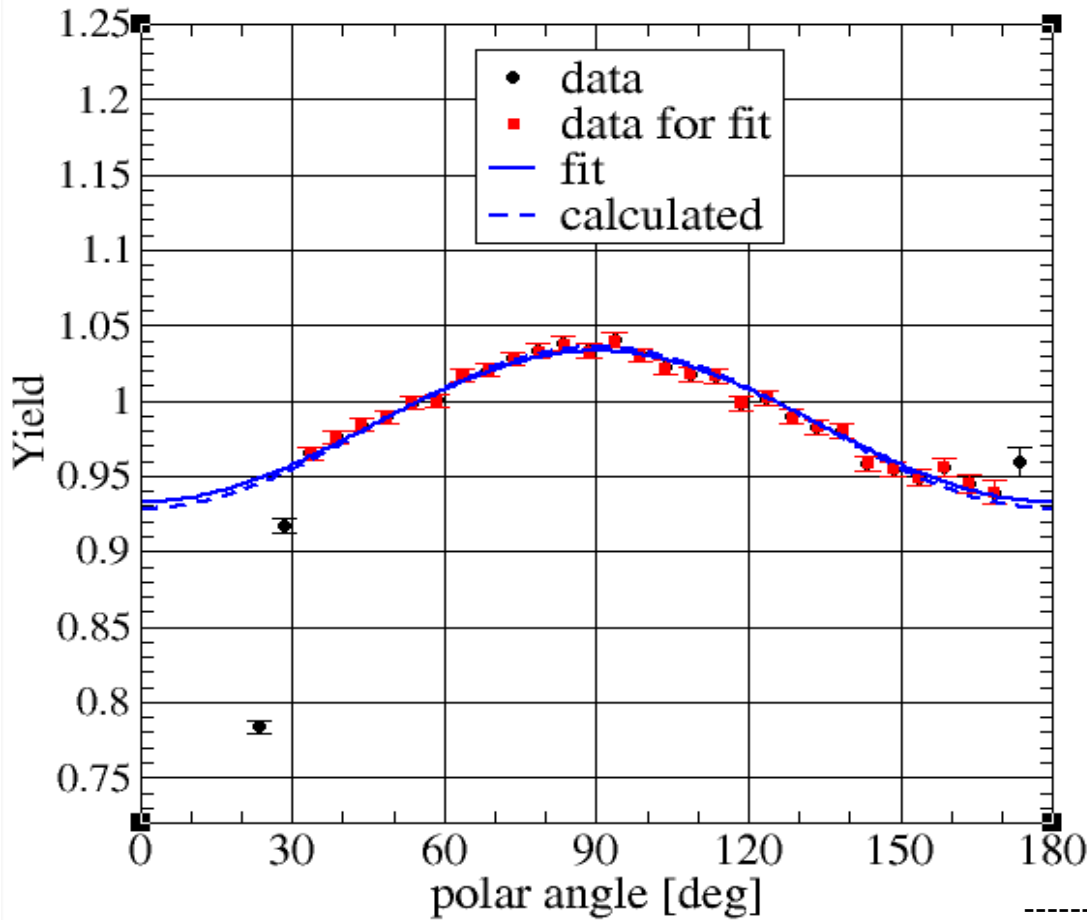
Fri Sep 20 15:00:43 2019

```

----- li= 3.0
| L1= 1.0
| L1'= 2.0
| del= 0.000
----- l= 2.0
| L2= 2.0
| L2'= 3.0
| del= 0.000
----- lf= 0.0
angular correlation coefficients:
A0 = +1.000000 A2 = -0.071429 A4 = -0.000000 A6 = -0.000000

```

^{152}Eu 344/778



ordinary legfit a0,a2,a4 fit>>>

chi**2: 1.033

a0: 1.000 +/- 0.001

a2: -0.066 +/- 0.002

a4: 0.005 +/- 0.003

----- li= 3.0

| L1= 1.0

| L1'= 2.0

| del= 0.000

----- l= 2.0

| L2= 2.0

| L2'= 2.0

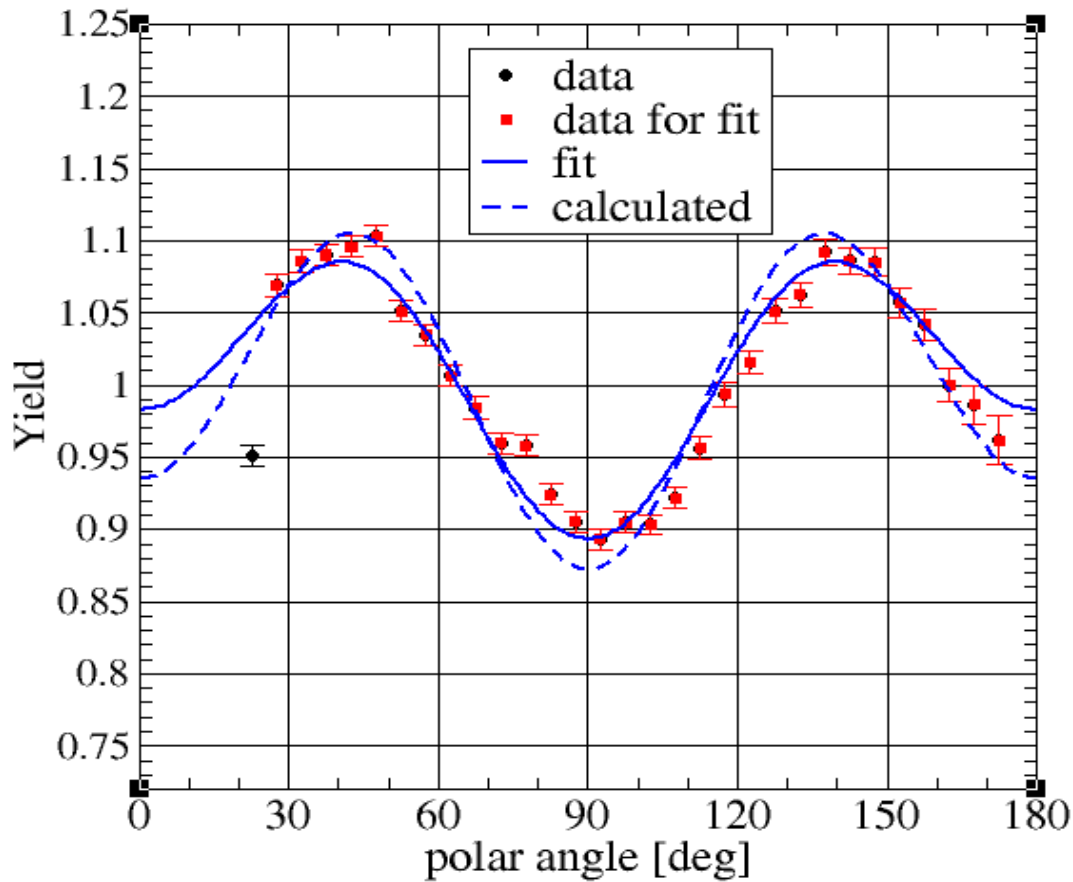
| del= 0.000

----- lf= 0.0

angular correlation coefficients:

A0 = +1.000000 A2 = -0.071429 A4 = -0.000000 A6 = -0.000000

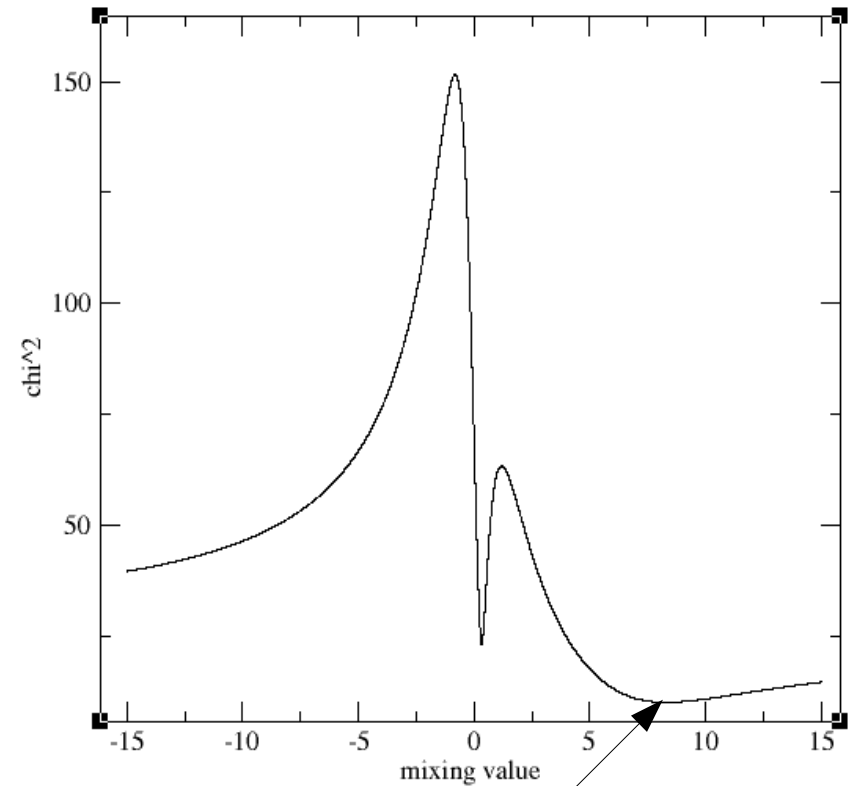
¹⁵²Eu 245/867 Mixed! (interesting!)



χ^2 : 3.890
 a_0 : 1.000 +/- 0.001
 a_2 : 0.114 +/- 0.004
 a_4 : -0.131 +/- 0.005

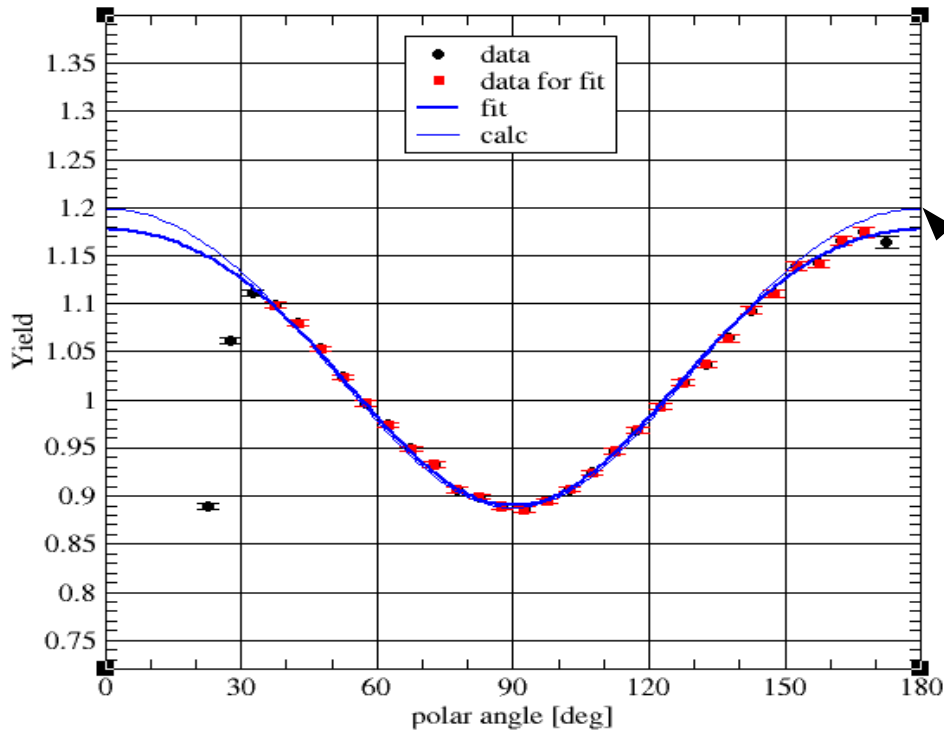
best fit, with $\chi^2 = 9.937729$, is:
 $A_0 = 1.000000$ $A_2 = 0.117791$ $A_4 = -0.182638$ $A_6 = -0.000000$
 for $\delta_2 = 8.294 \pm 1.713$ (== griffin -8.294 ± 1.713)

Mixing fit:



ENSDF says -9.3 (no error)
 (sign conversions...)
 Assumed no attenuation

207Bi; 570/1064 (use for lin pol later)



Calculated curve

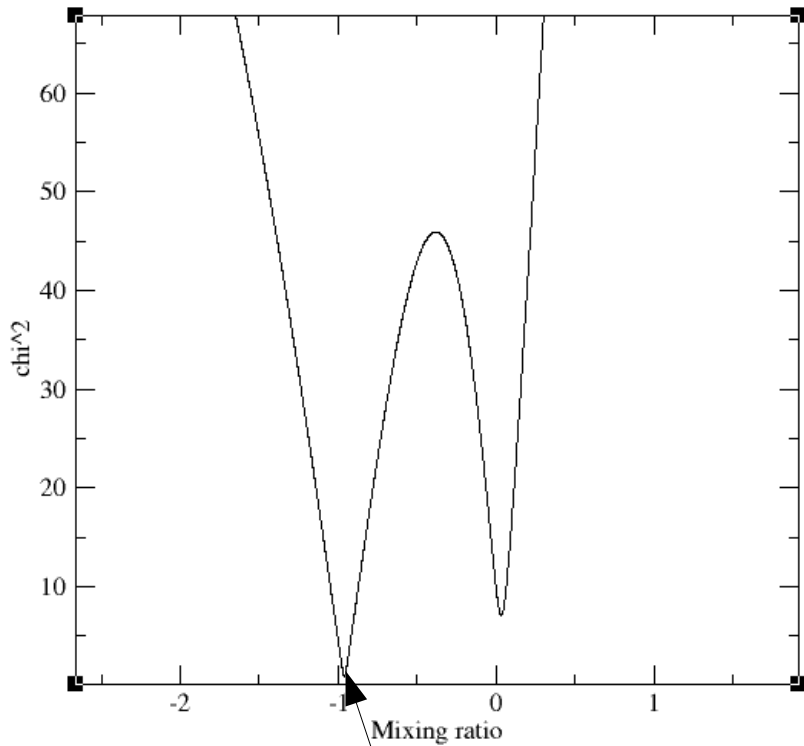
chi**2: 2.281
a0: 1.000 +/- 0.001
a2: 0.202 +/- 0.002
a4: -0.025 +/- 0.002

```

calc_a0a2a4 calc 6.5 2.5 0.5 4 5 0.02 2 3 0
----- li= 6.5
1064 M4+E5 | L1= 4.0
              | L1'= 5.0
              | del= 0.020
----- l= 2.5
570 E2      | L2= 2.0
              | L2'= 3.0
              | del= 0.000
----- lf= 0.5
angular correlation coefficients:
A0 = +1.000000 A2 = +0.213305 A4 = -0.014544
    
```

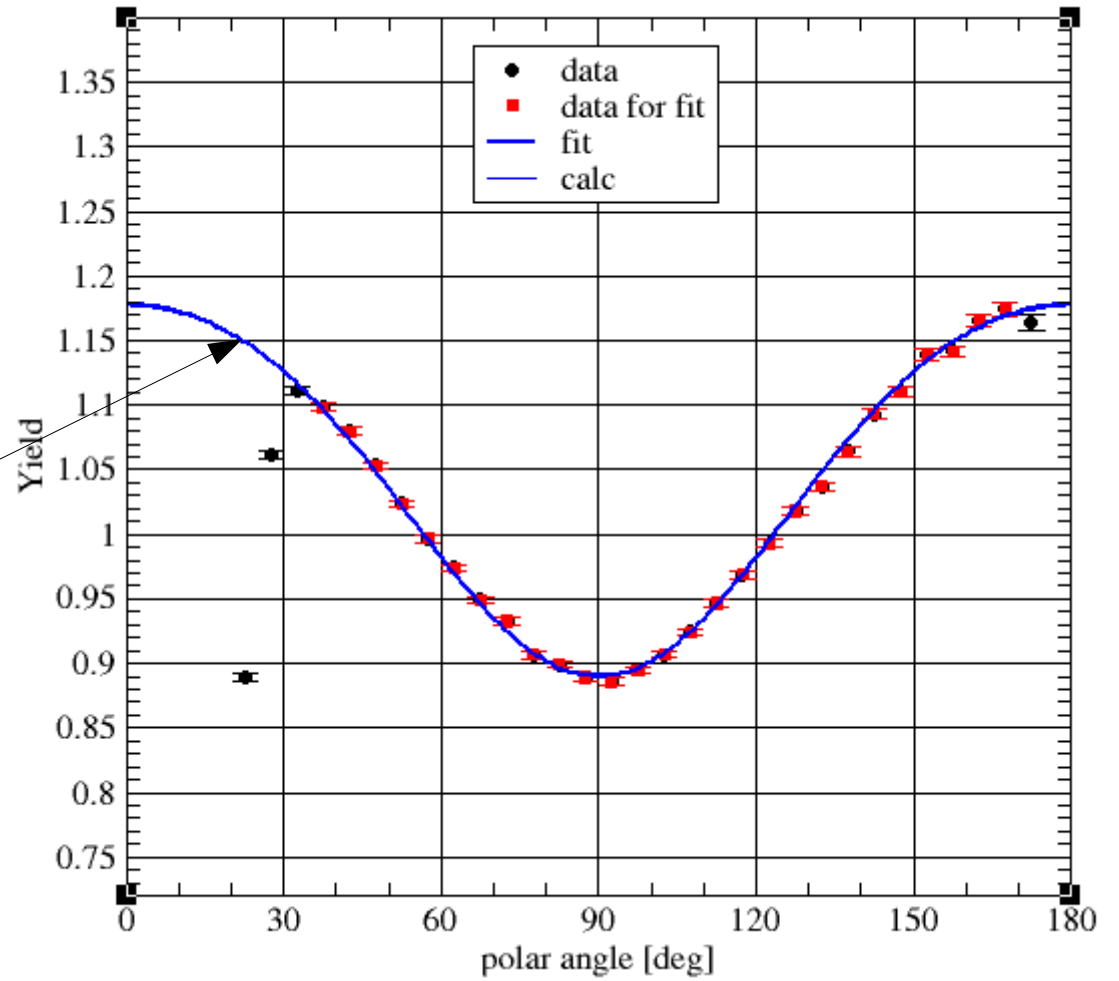
What ENSDF says

Could ENSDF be wrong? Fit...



Looks better

best fit, with $\chi^2 = 0.876589$, is:
 $A_0 = 1.000000$ $A_2 = 0.202619$ $A_4 = -0.023360$ $A_6 = -0.000000$
for $\delta_1 = -0.960 \pm 0.016$ (== griffin 0.960 ± 0.016)



Perfect fit with mixing ratio of $-0.96(2)$

In-beam angular correlations:

DCO (Directional Correlation from Oriented nuclei)

Need to use a different angle

First state is no longer random in m-distribution

The formalism is quite complicated

**DIRECTIONAL CORRELATIONS OF GAMMA RADIATIONS
EMITTED FROM NUCLEAR STATES ORIENTED BY
NUCLEAR REACTIONS OR CRYOGENIC METHODS**

K. S. KRANE
R. M. STEFFEN and R. M. WHEELER

Use this angle for
the angular
distribution rather
than angle
between the
gamma rays as we
do for sources

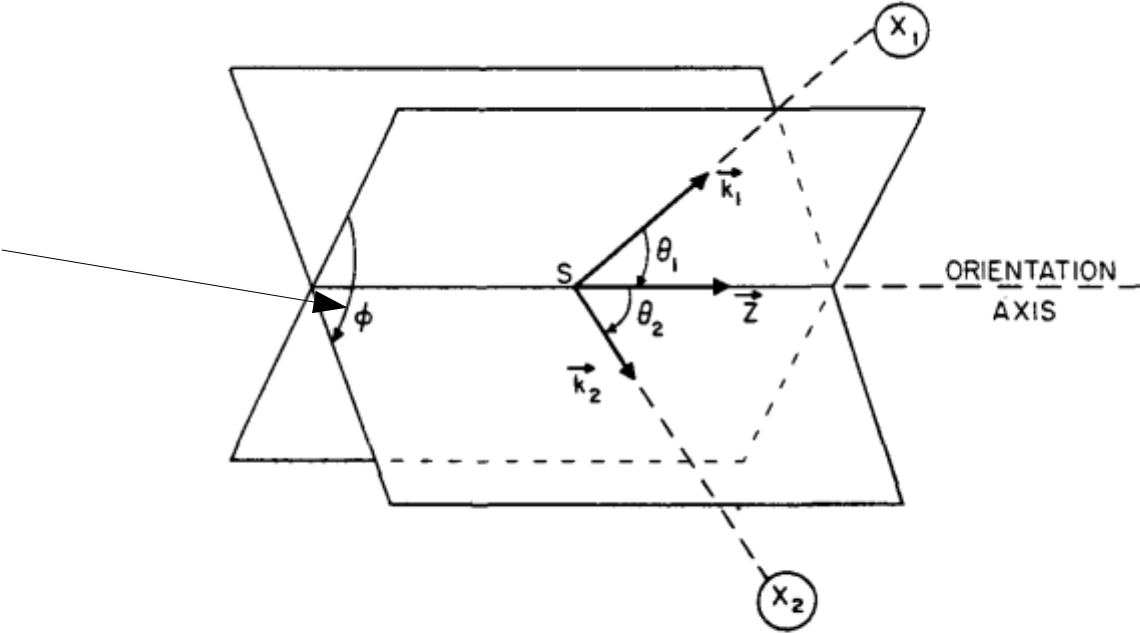


Fig. 2. The angles in a directional correlation of two successive radiations X_1 and X_2 emitted from an axial symmetric oriented source S (DCO)

Taste of the formulas (from Krane)

$$W(\theta_1, \theta_2, \Phi)$$

$$= \sum_{\lambda_1 \lambda_2} B_{\lambda_1}(I_1) A_{\lambda_1}^{\lambda_2 \lambda_1}(X_1) A_{\lambda_2}(X_2) H_{\lambda_1 \lambda_2}(\theta_1, \theta_2, \Phi).$$

Beam alignment
related

Radiation distribution
coefficients

$$H_{\lambda_1 \lambda_2}(\theta_1, \theta_2, \Phi)$$

$$= \sum_{q=-\lambda'}^{\lambda'} \frac{4\pi}{2\lambda_2 + 1} \langle \lambda_1 0 \lambda q | \lambda_2 q \rangle Y_{\lambda q}(\theta_1, 0) Y_{\lambda_2 q}^*(\theta_2, \Phi).$$

Spherical harmonics

We don't observe K_1 and K_2 directions
i.e., $\Lambda = 0$

Breaks down to usual Legendre
polynomials
and only even terms

For 'discrete' array

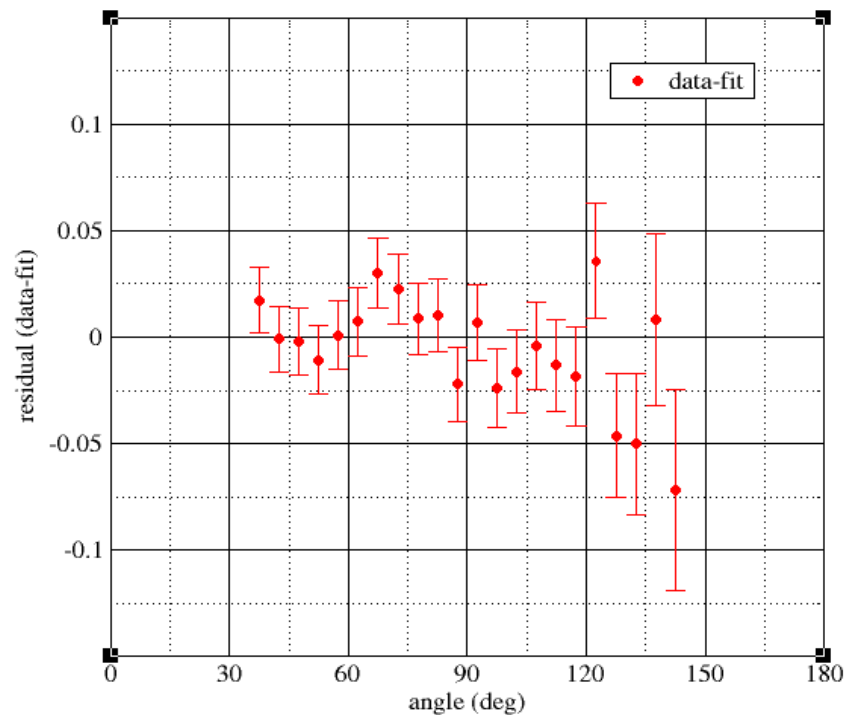
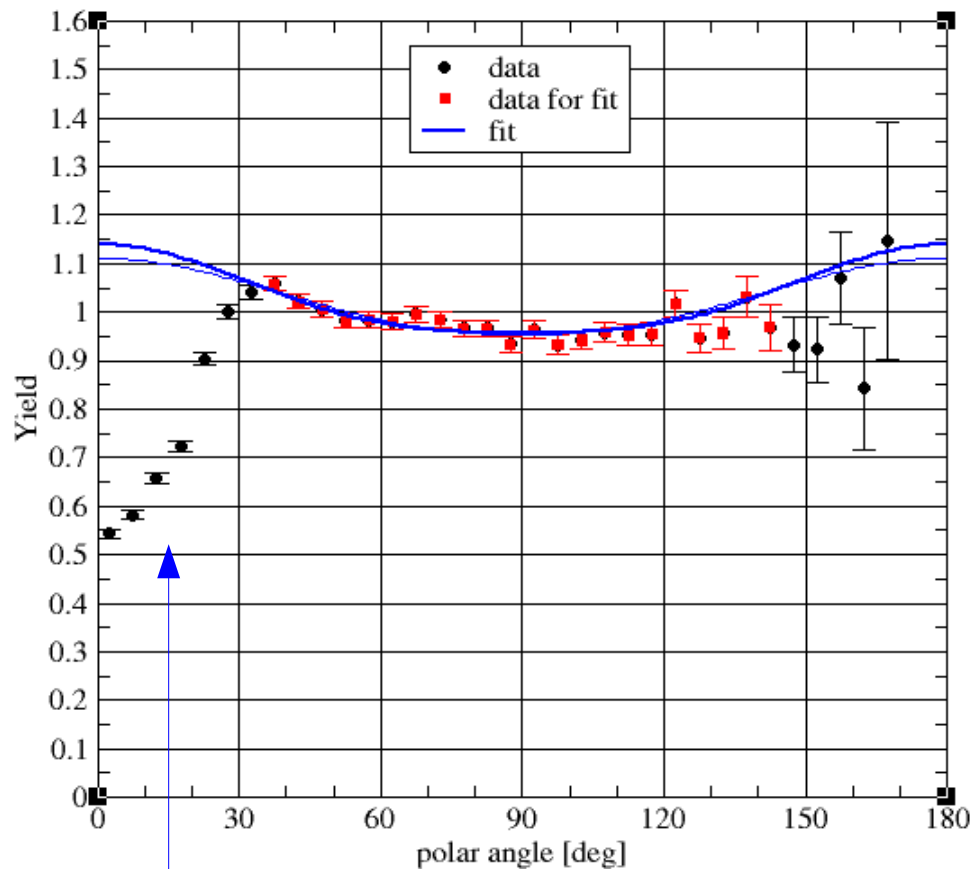
- Use full expression for each pair of gamma detectors
- Reduce number for identical pairs. For Eurogam-II about 83 pairs (E.S. Paul)
- Use full treatment for each of these pairs, where k_1 and k_2 specify the two detector directions

For 'continuous' arrays

- Since we don't observe the directions of the individual gamma rays, the standard formula works, we just have to **use the plane angles** rather than the angle between the gamma rays (*need rigorous proof...*)
- Calculating the coefficients might involve some weighted averages over the k_1 and k_2 directions that depends on the particular configuration
- We have:
$$\omega(\theta) = a_0 + \alpha_2 a_2 P_2(\cos\Phi) + \alpha_4 a_4 P_4(\cos\Phi) + \dots$$

Plane angle
NOT
Angle bt gammas

^{158}Er in-beam; 8(2)6(2)4, using plane angle



Notice: 'cluster hole' is different

chi**2: 1.101
a0: 1.000 +/- 0.007
a2: 0.110 +/- 0.025
a4: 0.030 +/- 0.027

← ?

----- li= 8.0

| L1= 2.0
| L1'= 3.0
| del= 0.000

----- l= 6.0

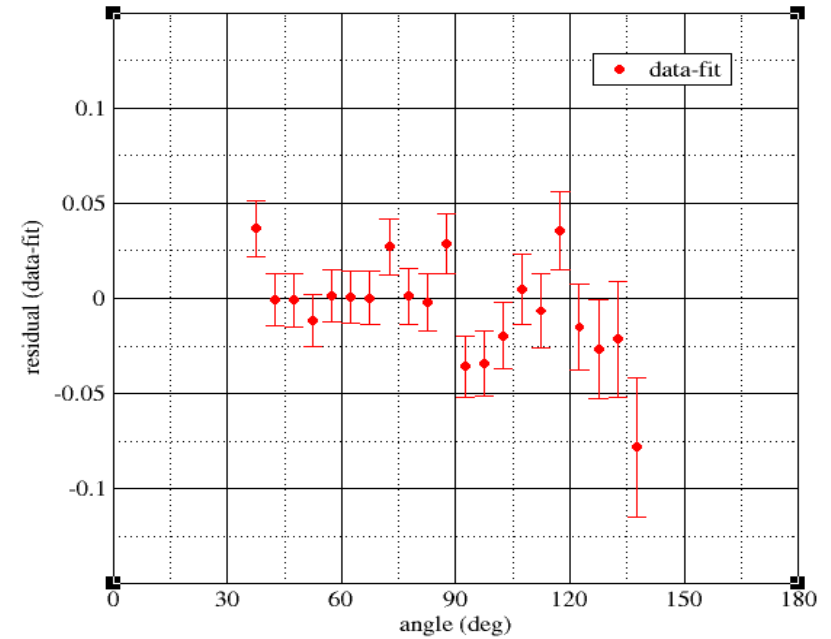
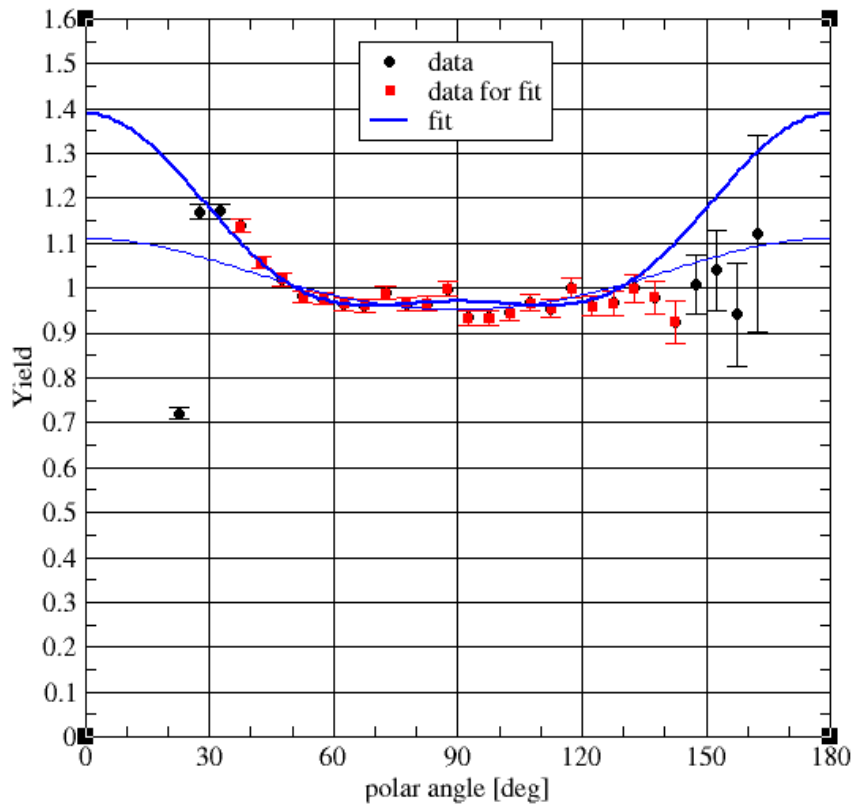
| L2= 2.0
| L2'= 3.0
| del= 0.000

----- lf= 4.0

angular correlation coefficients:

A0 = +1.000000 A2 = +0.102041 A4 = +0.009070 A6 = +0.000000

^{158}Er in-beam; 8(2)6(2)4, using angle bt gammas wrong way!



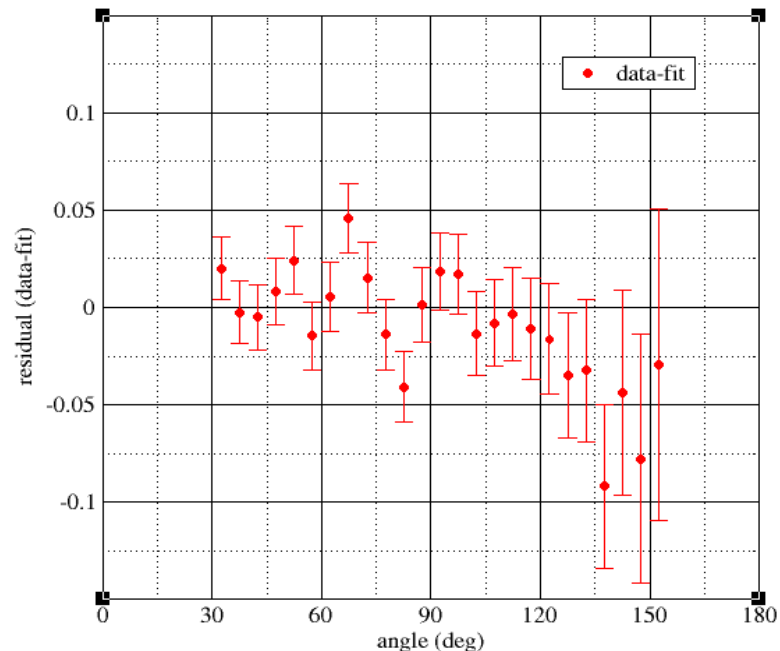
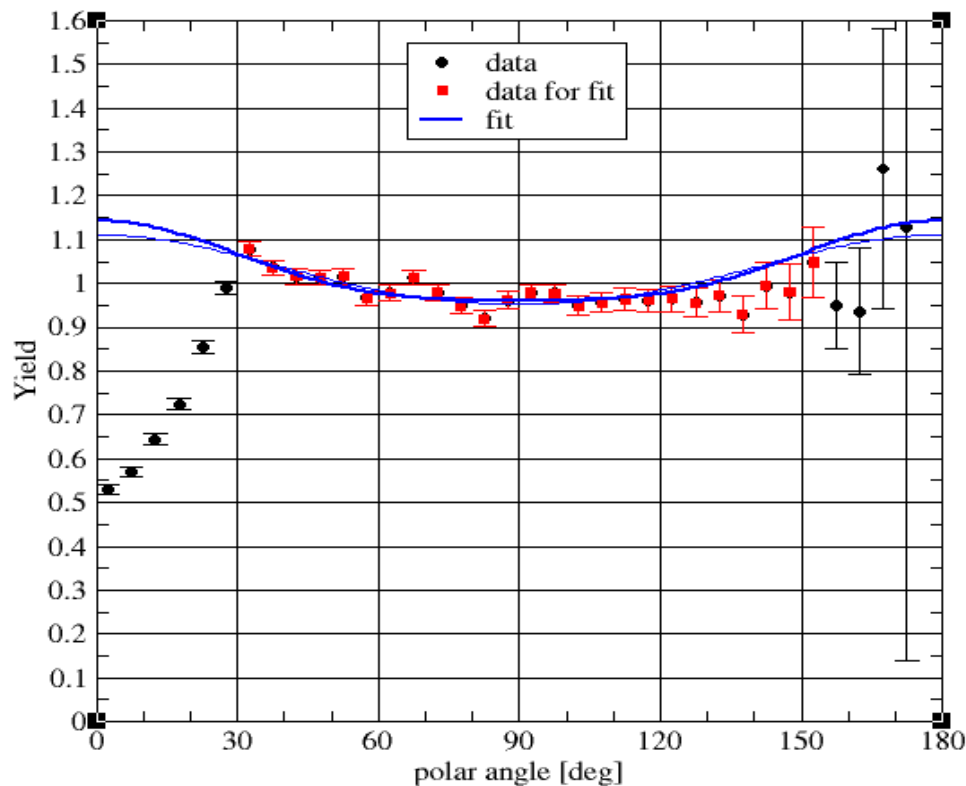
chi**2: 2.375
 a0: 1.034 +/- 0.006
 a2: 0.226 +/- 0.022
 a4: 0.129 +/- 0.023

----- li= 8.0
 | L1= 2.0
 | L1'= 3.0
 | del= 0.000
 ----- l= 6.0
 | L2= 2.0
 | L2'= 3.0
 | del= 0.000
 ----- lf= 4.0

angular correlation coefficients:

A0 = +1.000000 A2 = +0.102041 A4 = +0.009070 A6 = +0.000000

^{158}Er in-beam; 10(2)8(2)6, using plane angle



χ^2 : 1.262
 a_0 : 1.000 +/- 0.005
 a_2 : 0.107 +/- 0.017
 a_4 : 0.036 +/- 0.022

calc_a0a2a4 calc 10 8 6 2 3 0 2 3 0

----- $l_i = 10.0$

| $L_1 = 2.0$
 | $L_1' = 3.0$
 | $\text{del} = 0.000$

----- $l = 8.0$

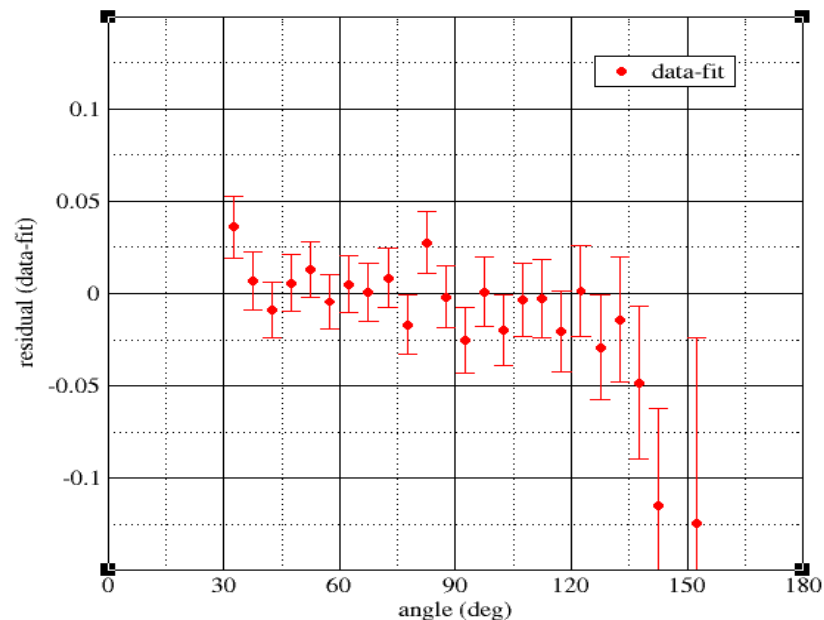
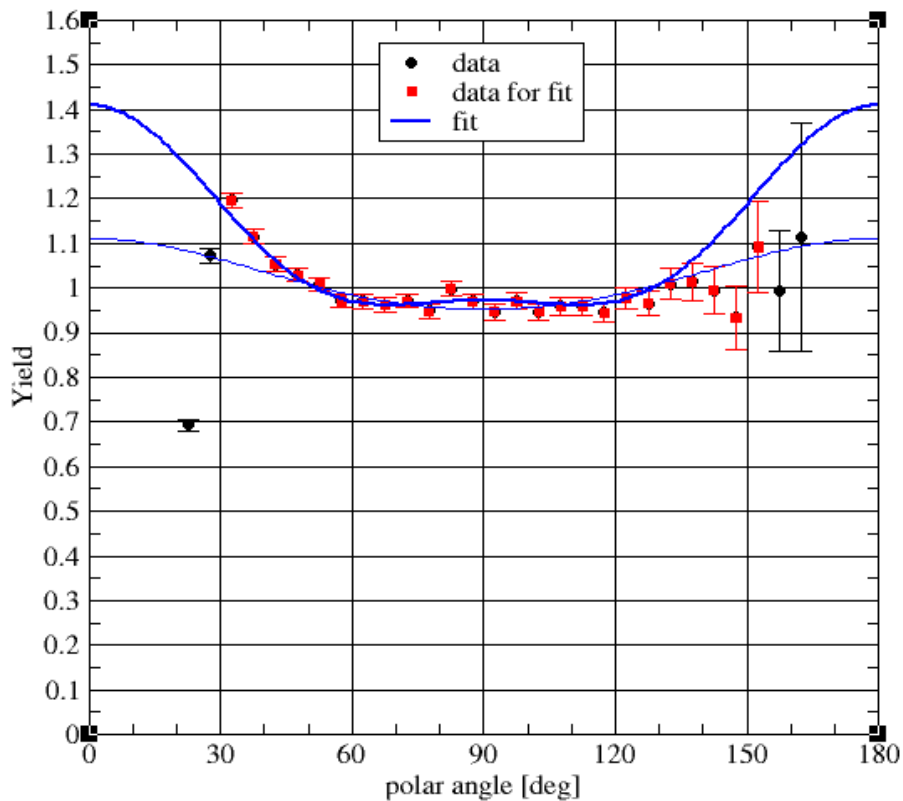
| $L_2 = 2.0$
 | $L_2' = 3.0$
 | $\text{del} = 0.000$

----- $l_f = 6.0$

angular correlation coefficients:

$A_0 = +1.000000$ $A_2 = +0.102041$ $A_4 = +0.009070$ $A_6 = +0.000000$

^{158}Er in-beam; 10(2)8(2)6, using angle bt gammas wrong way!



chi**2: 1.449
a0: 1.039 +/- 0.005
a2: 0.235 +/- 0.016
a4: 0.137 +/- 0.020

calc_a0a2a4 calc 10 8 6 2 3 0 2 3 0

----- li= 10.0

| L1= 2.0
| L1'= 3.0
| del= 0.000

----- l= 8.0

| L2= 2.0
| L2'= 3.0
| del= 0.000

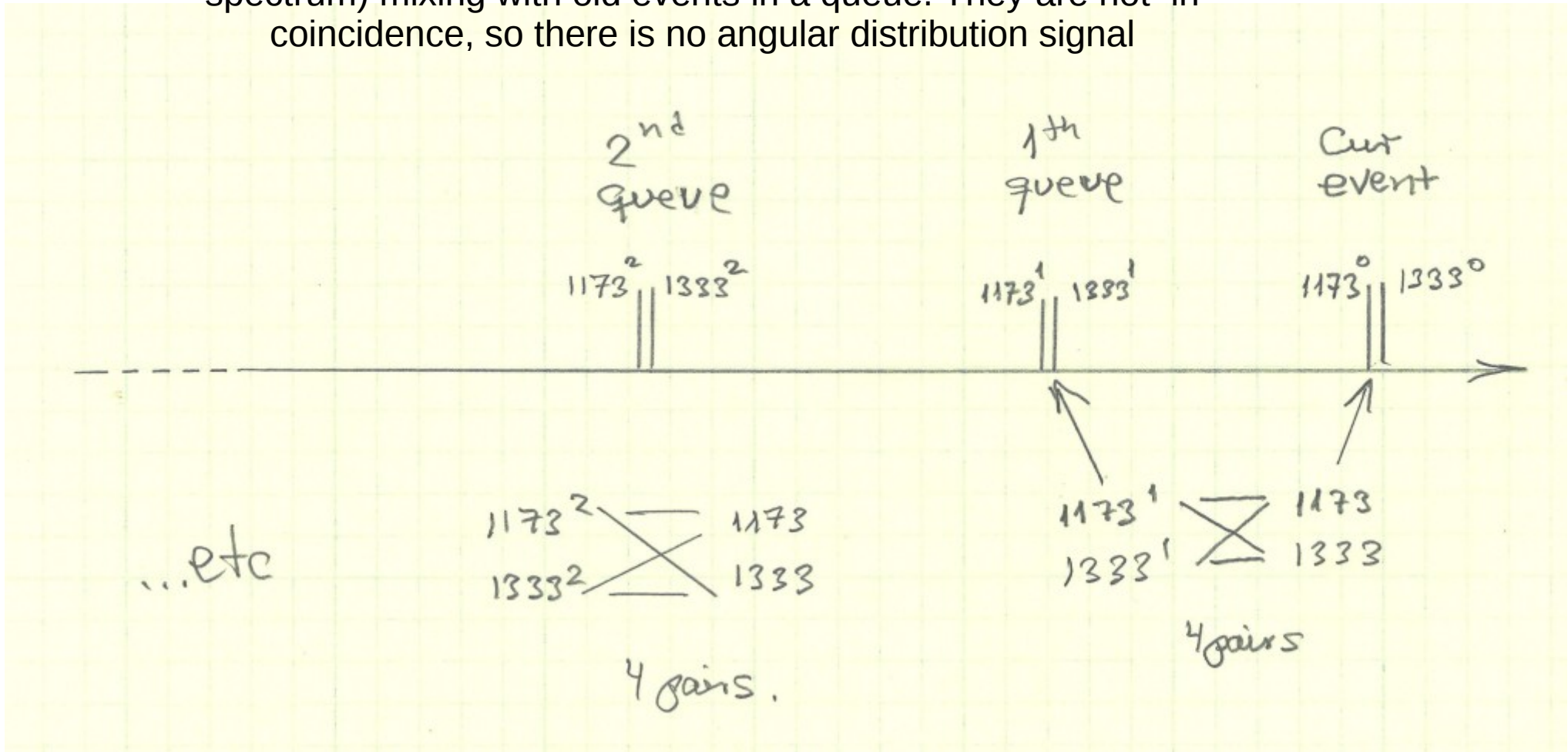
----- lf= 6.0

angular correlation coefficients:

A0 = +1.000000 A2 = +0.102041 A4 = +0.009070 A6 = +0.000000

Normalization, response function

Create response function (reference angular correlation spectrum) mixing with old events in a queue. They are not in coincidence, so there is no angular distribution signal



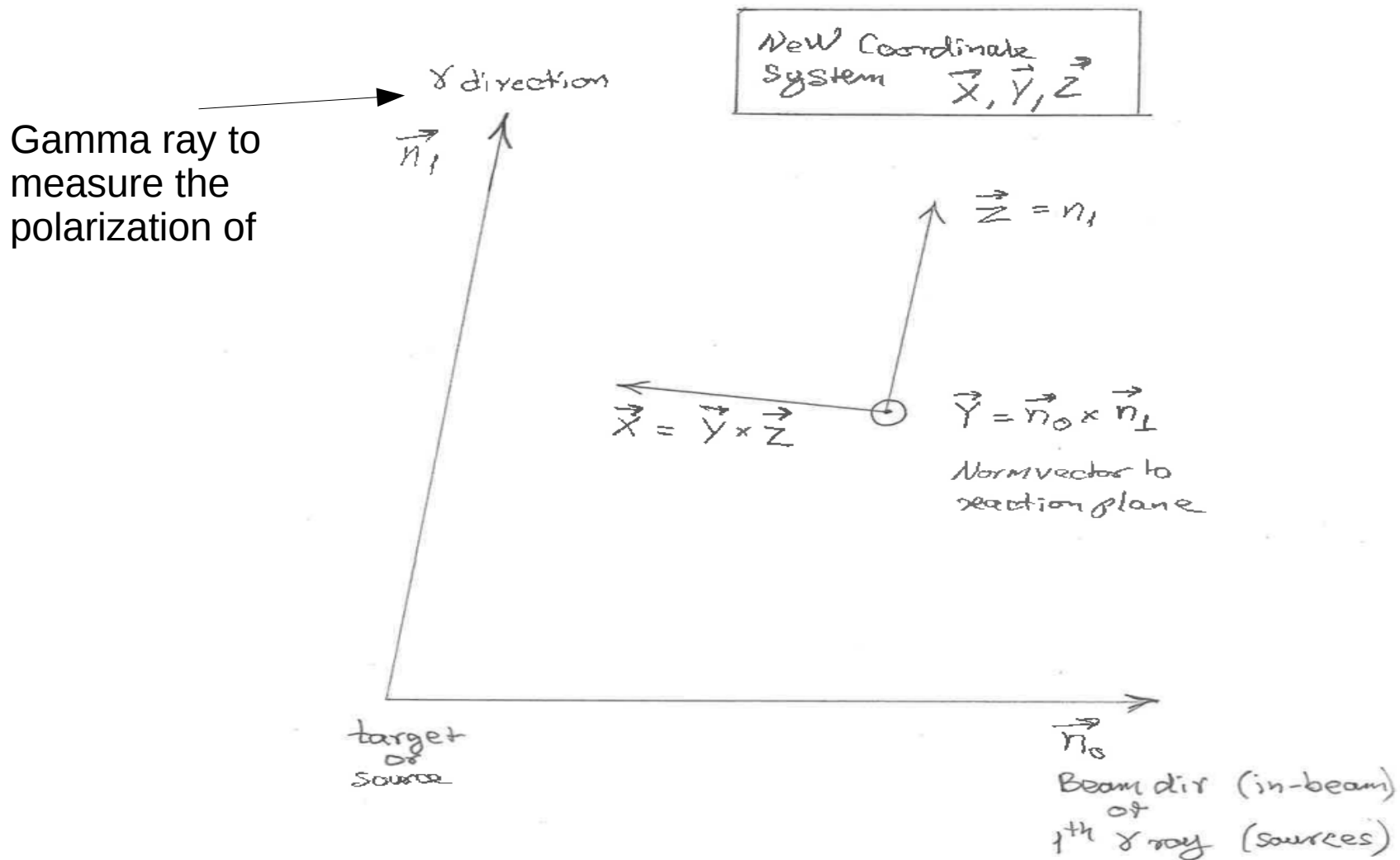
After use, update the old event queue with the current at the 1st place and forget the last one

Linear polarization: sources

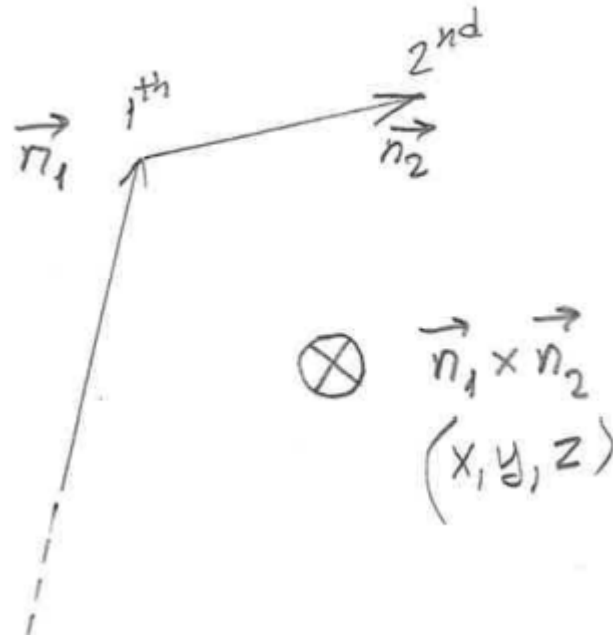
- For coincidences, we use one gamma ray to polarize the other.
- *We used to have to normalize with a source*
- **We will try to convince you that we can use the data itself for the normalization**

Our geometry for linear polarization

1: define a new coordinate system based on the reaction plane



2: find normal vector for the scattering plane



3: find the x', y', z' coordinates of x, y, z in the new X, Y, Z coordinate system

4: the linear polarization AZIMUTH angle is now found as

$$\text{atan2}(y'/x')$$

Range: -180 ... +180 degrees

Taste of formalism (sources, in-beam)

$$\omega(\theta, \gamma) = w(\theta) + P \cos(2\gamma) + (A_2(L_1, L'_1, I_i, I) \mathfrak{R}_2(L_2, L'_2, I_f, I) P_2^2(\cos\theta) + A_4(L_1, L'_1, I_i, I) \mathfrak{R}_4(L_2, L'_2, I_f, I) P_4^2(\cos\theta))$$

E: P=-1
M: P=+1

Angle we just defined

'Usual' A_k coefficients
Use $\alpha_k * B_k$ for in-beam

Like A_k coefficients but has some extra 'K_k coefficients'

Associated Legendre polynomials

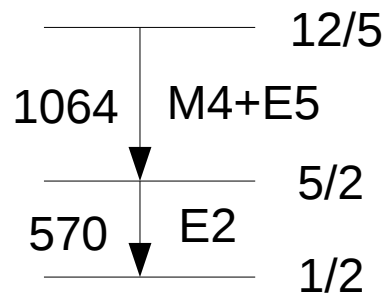
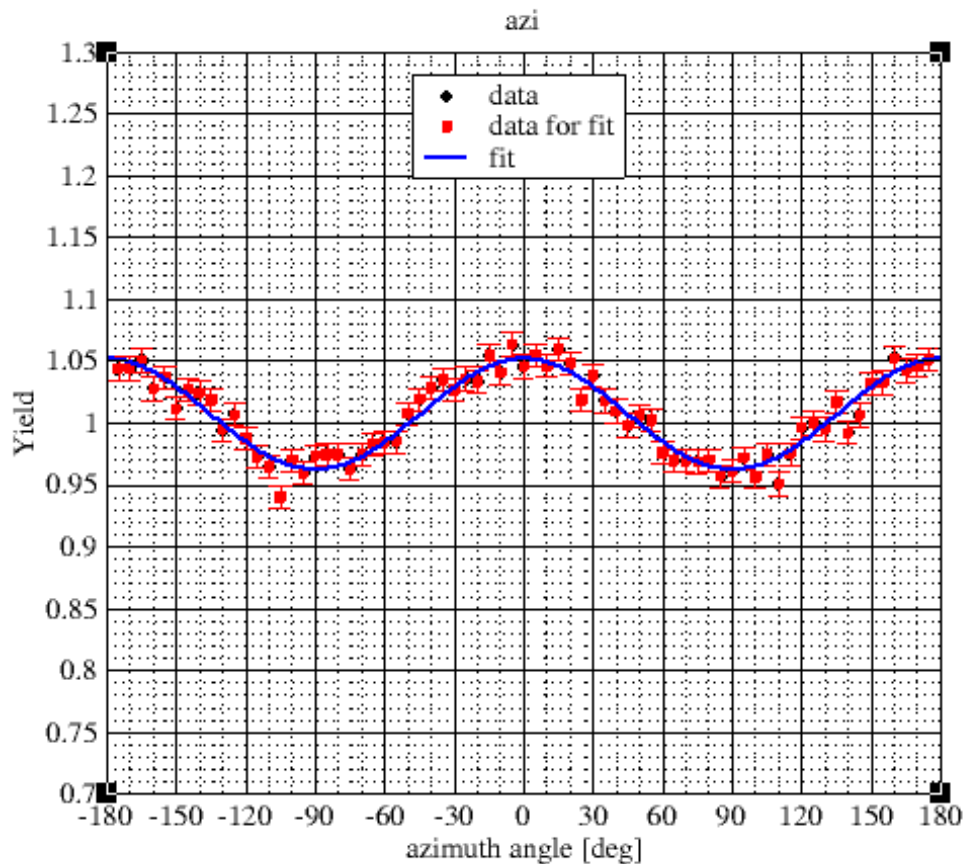
Angle between gamma rays for sources. **Use plane angle for in-beam cases**

Sign of wiggle: $P^*(\dots)$, not just P

(new) Response function

- For sources: replace n_0 vector with a number of old n_0 vectors from a queue of previous ones to produce a response function. The old queue is then updated for every event (FIFO).
-
- For in-beam, the beam axis is replaced with random directions in 3D to produce a response function.

^{207}Bi source; 570 E2 line



Polarization spectrum for the 570 keV E2 when polarized by the 1064 keV M4+E5

13/2(4)5/2(2)1/2

```
calc_a0a2a4 linpol 6.5 2.5 0.5 4 5 -0.96 2 3 0 E 70 110
```

```
----- li= 6.5
```

```
| L1= 4.0
| L1'= 5.0
| del= -0.960
```

```
----- l= 2.5
```

```
| L2= 2.0
| L2'= 3.0
| del= 0.000
```

```
----- lf= 0.5
```

angular correlation coefficients:

A0 = +1.000000 A2 = +0.202619 A4 = -0.023360 A6 = -0.000000

w plot in "w.xy"; try xmgrace w.xy -par w.par

linear polarization coefficients:

C2 = +0.101309 C4 = +0.001947 C6 = -0.000000

linpol plot in "w_pol.xy"; try xmgrace w_pol.xy -par wlinpol.par

cos(2*azi) factor is +0.266040 (in 4pi)

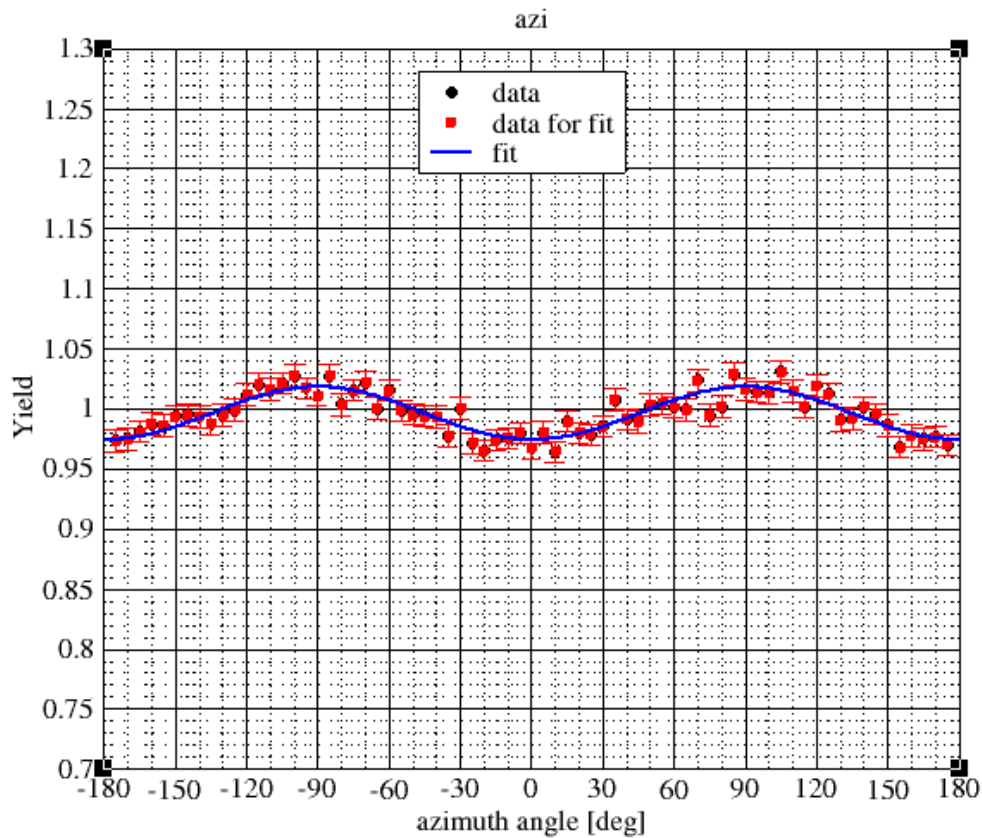
chi**2: 1.105

a0: 1.007 +/- 0.001

a2: 0.045 +/- 0.002

↖ No angle integration yet

^{207}Bi source; 1064 M4 line



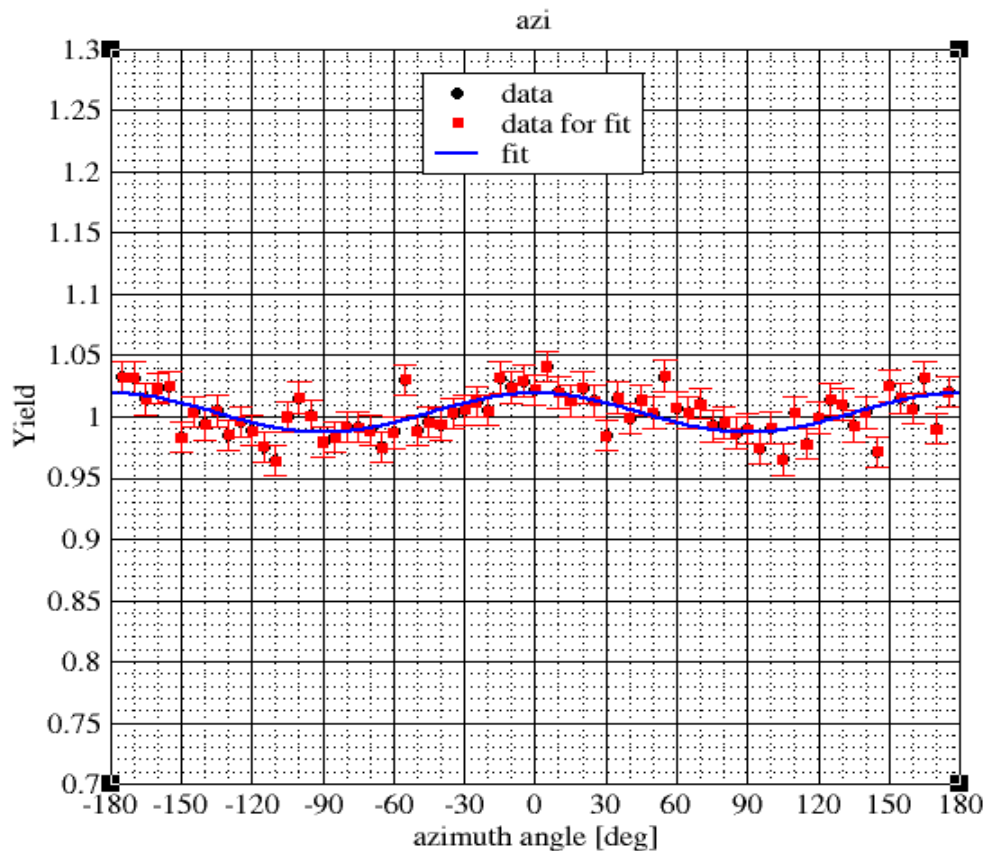
Polarization spectrum
for the 1064 keV
M4+E5 when polarized
by the 570 keV E2

$1/2(2)5/2(4)13/2$
(backwards)

```
calc_a0a2a4 linpol 0.5 2.5 6.5  2 3 0  4 5 -0.96  M 70 110
----- li=  0.5
| L1=  2.0
| L1'= 3.0
| del= 0.000
----- l=  2.5
| L2=  4.0
| L2'= 5.0
| del= -0.960
----- lf= 6.5
```

chi**2: 0.845
a0: 0.996 +/- 0.001
a2: -0.022 +/- 0.002

angular correlation coefficients:
A0 = +1.000000 A2 = +0.202619 A4 = -0.023360 A6 = -0.000000
w plot in "w.xy"; try xmgrace w.xy -par w.par
linear polarization coefficients:
C2 = -0.136224 C4 = +0.009237 C6 = +0.000000
linpol plot in "w_pol.xy"; try xmgrace w_pol.xy -par wlinpol.par
cos(2*azi) factor is -0.371947 (in 4pi)



^{60}Co

1333 polarized by 1173
4(2)2(2)0

calc_a0a2a4 linpol 4 2 0 2 3 0 2 3 0 E 70 110

----- li= 4.0

| L1= 2.0
| L1'= 3.0
| del= 0.000

----- l= 2.0

| L2= 2.0
| L2'= 3.0
| del= 0.000

----- lf= 0.0

angular correlation coefficients:

A0 = +1.000000 A2 = +0.102041 A4 = +0.009070 A6 = +0.000000

w plot in "w.xy"; try xmgrace w.xy -par w.par

linear polarization coefficients:

C2 = +0.051020 C4 = -0.000756 C6 = +0.000000

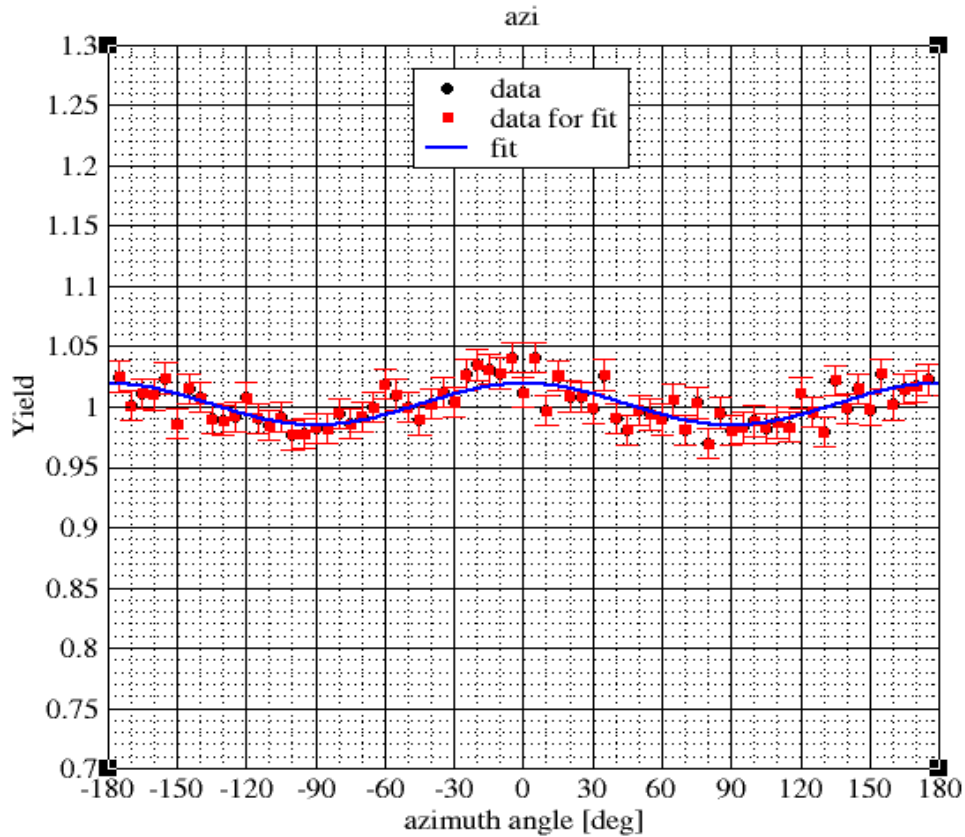
linpol plot in "w_pol.xy"; try xmgrace w_pol.xy -par wlinpol.par

cos(2*azi) factor is +0.136063 (in 4pi)

chi**2: 0.852

a0: 1.002 +/- 0.001

a2: 0.017 +/- 0.002



Mon Sep 23 16:23:05 2019

chi**2: 0.852
a0: 1.002 +/- 0.001
a2: 0.017 +/- 0.002

1173 polarized by 1333
0(2)2(2)4

Backwards calculation...

calc_a0a2a4 linpol 0 2 4 2 3 0 2 3 0 E 70 110

----- li= 0.0

| L1= 2.0
| L1'= 3.0
| del= 0.000

----- l= 2.0

| L2= 2.0
| L2'= 3.0
| del= 0.000

----- lf= 4.0

angular correlation coefficients:

A0 = +1.000000 A2 = +0.102041 A4 = +0.009070 A6 = +0.000000

w plot in "w.xy"; try xmgrace w.xy -par w.par

linear polarization coefficients:

C2 = +0.051020 C4 = -0.000756 C6 = +0.000000

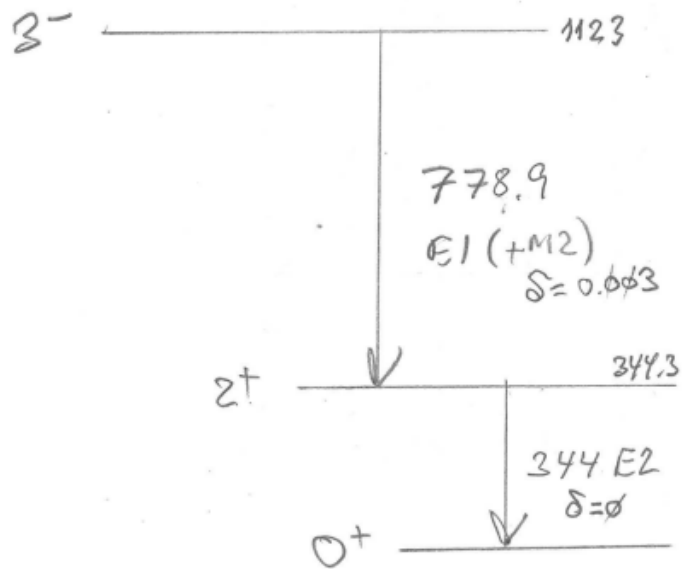
linpol plot in "w_pol.xy"; try xmgrace w_pol.xy -par wlinpol.par

cos(2*azi) factor is +0.136063 (in 4pi)

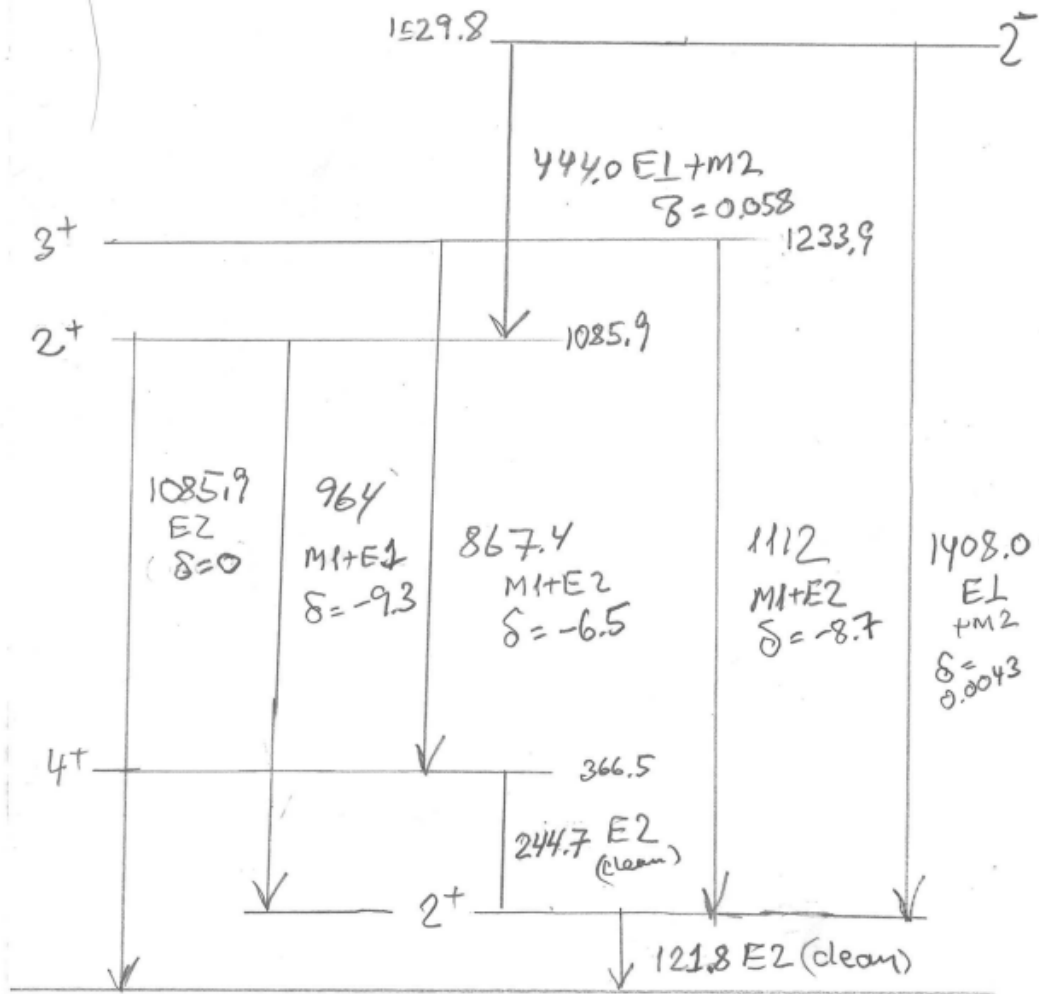
^{152}Eu : great laboratory

$^{152}_{63}\text{EuEC}$

$^{152}_{63}\text{Eu} \beta^- \text{ decay}$



$^{152}_{64}\text{Gd}_{88}$

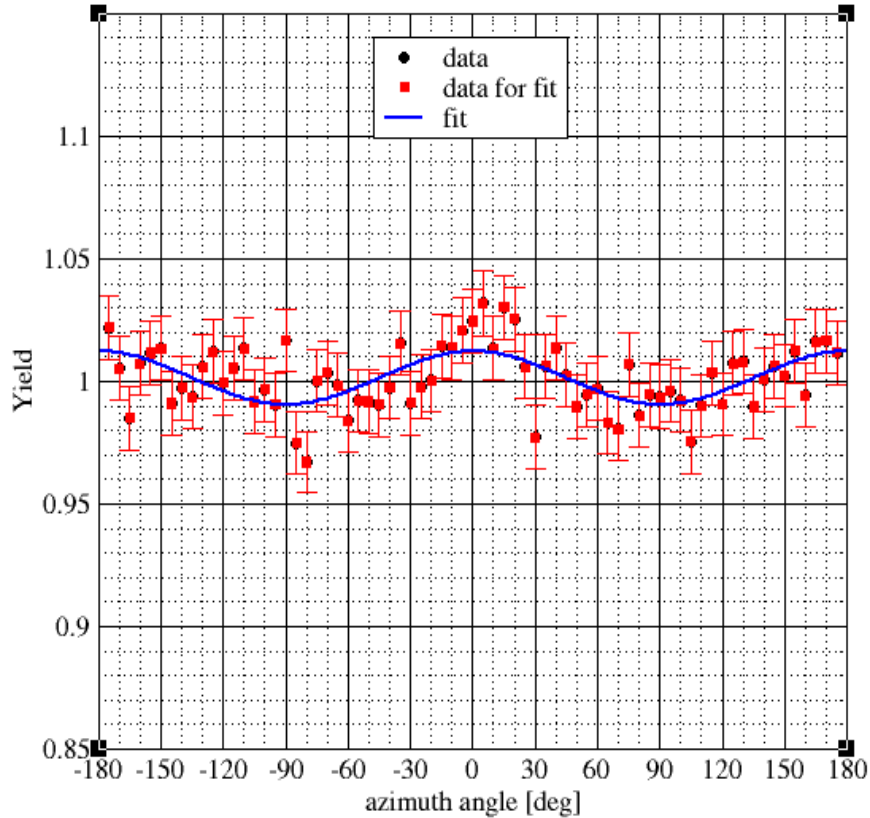


$^{152}_{62}\text{Sm}_{90}$

779 (E1) line polarized by 344 (E2) line

Linear Polarization

azimuth angle bt reaction plane and scatter plane



chi**2: 0.736
a0: 1.001 +/- 0.002
a2: 0.011 +/- 0.002



```
calc_a0a2a4 linpol 0 2 3 2 3 0 1 2 0 E 70 110
----- li= 0.0
| L1= 2.0
| L1'= 3.0
| del= 0.000
----- l= 2.0
| L2= 1.0
| L2'= 2.0
| del= 0.000
----- lf= 3.0
```

angular correlation coefficients:
A0 = +1.000000 A2 = -0.071429 A4 = -0.000000 A6 = -0.000000
w plot in "w.xy"; try xmgrace w.xy -par w.par
linear polarization coefficients:
C2 = +0.035714 C4 = -0.000000 C6 = -0.000000
linpol plot in "w_pol.xy"; try xmgrace w_pol.xy -par wlinpol.par
cos(2*azi) factor is +0.094610 (in 4pi)

1408 (E1) line polarized by 122 (E2) line.

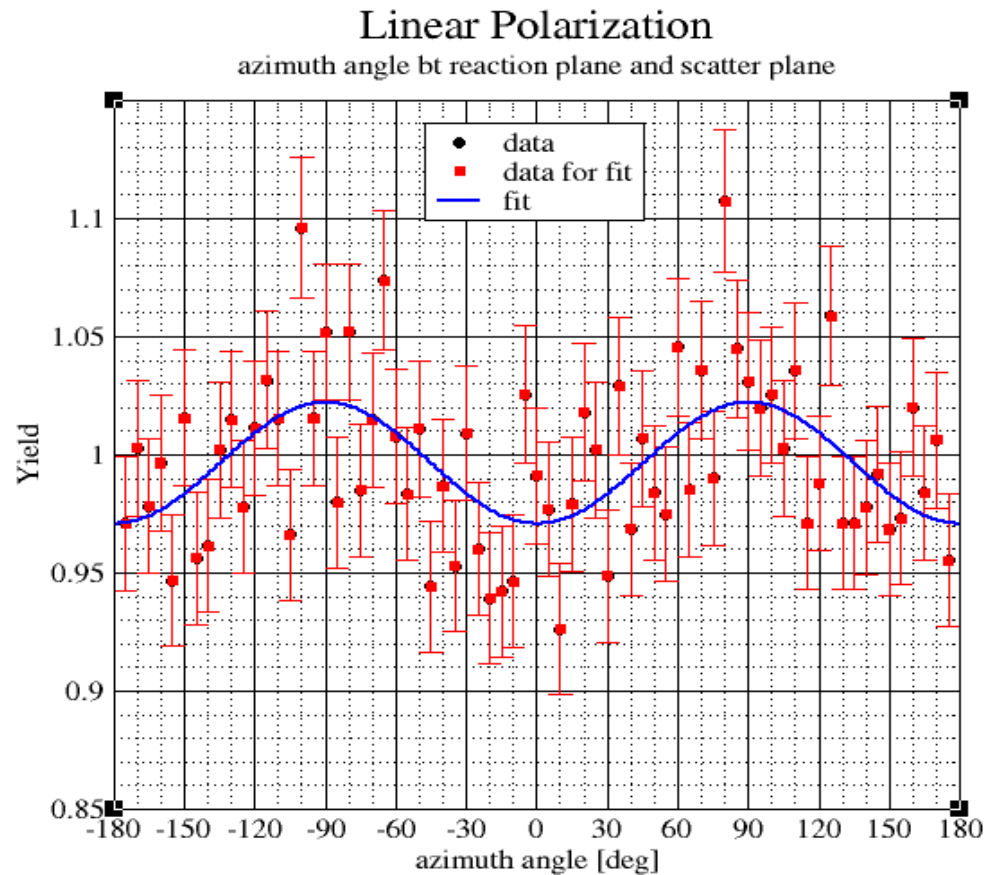
Cautionary tale::

Naively: is E1, so should wiggle up!?

But NO!!

The other coefficients changed sign. We have to be careful for sources. (in-beam easier)

Always calculate!!



chi**2: 1.203
a0: 0.997 +/- 0.003
a2: -0.026 +/- 0.005

```
calc_a0a2a4 linpol 0 2 2 2 3 0 1 2 0 E 70 110
```

```
----- li= 0.0
```

```
| L1= 2.0
```

```
| L1'= 3.0
```

```
| del= 0.000
```

```
----- l= 2.0
```

```
| L2= 1.0
```

```
| L2'= 2.0
```

```
| del= 0.000
```

```
----- lf= 2.0
```

angular correlation coefficients:

A0 = +1.000000 A2 = +0.250000 A4 = +0.000000 A6 = +0.000000

w plot in "w.xy"; try xmgrace w.xy -par w.par

linear polarization coefficients:

C2 = -0.125000 C4 = +0.000000 C6 = +0.000000

linpol plot in "w_pol.xy"; try xmgrace w_pol.xy -par wlinpol.par

cos(2*azi) factor is -0.331133 (in 4pi)



~Incomplete survey of coincidence in ^{152}Eu

Don't expect
much signal
here

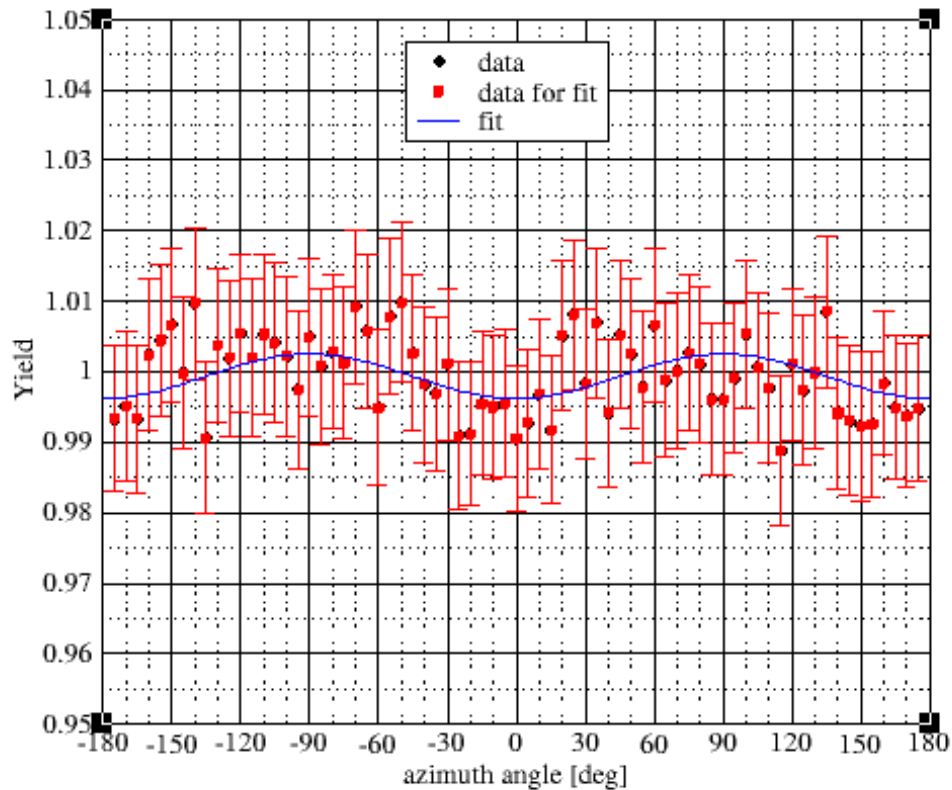
	+--- polarization of		+--- polarize by		sign	
[122 E2]	[1112 M1+E2]	obs=NEG		calc=NEG		
[122 E2]	[1408 E1]	(no signal)				
[122 E2]	[245 E2]	obs=POS		calc=POS	+0.013(6)	
[122 E2]	[964 M1+E2]	obs=		calc=		
[245 E2]	[122 E2]	obs=POS		calc=POS		
[245 E2]	[867 M1+E2]	obs=POS		calc=POS	+0.009(6)	
[344 E2]	[779 E1]	obs=NEG		calc=NEG	-0.059(8)	
[444 E1]	[1086 E2]	obs=		calc=		
[444 E1]	[964 M1+E2]	obs=		calc=		
[779 E1]	[344 E2]	obs=POS		calc=POS	+0.011(2)	
[867 M1+E2]	[245 E2]	obs=NEG		calc=NEG		
[964 M1+E2]	[122 E2] weak	obs=NEG		calc=NEG		
[964 M1+E2]	[444 E1]	obs=		calc=		
[964 M1+E2]	[444 E1]	obs=		calc=		
[1086 E2]	[444 E1]	obs=POS		calc=POS	+0.028(10)	
[1112 M1+E2]	[122 E2]	obs=		calc=		
[1408 E1]	[122 E2]	obs=NEG		calc=NEG	-0.026(5)	

In all cases I have looked at, the measured sign agrees with the calculated sign (amplitudes will come later)

In-Beam linear pol

- Goes a little like the source data processing; but n_0 is now the beam axis
- But we need to *change the uncorrelated first direction in the response spectrum to use random directions in 3D. The 'old' queue has random direction.*

158 Er in-beam, 740 keV 22+ \rightarrow 20+



chi**2: 0.216
a0: 0.999 +/- 0.001
a2: -0.003 +/- 0.002

```
calc_angdis lnpol 22 20 2 3 0 4.0 E 70 110
alpha: _0 = +1.000000 _2 = +0.008672 _4 = +0.000000
----- li= 22.0
| L1= 2.0
| L1'= 3.0
| del= 0.000
----- lf= 20.0
```

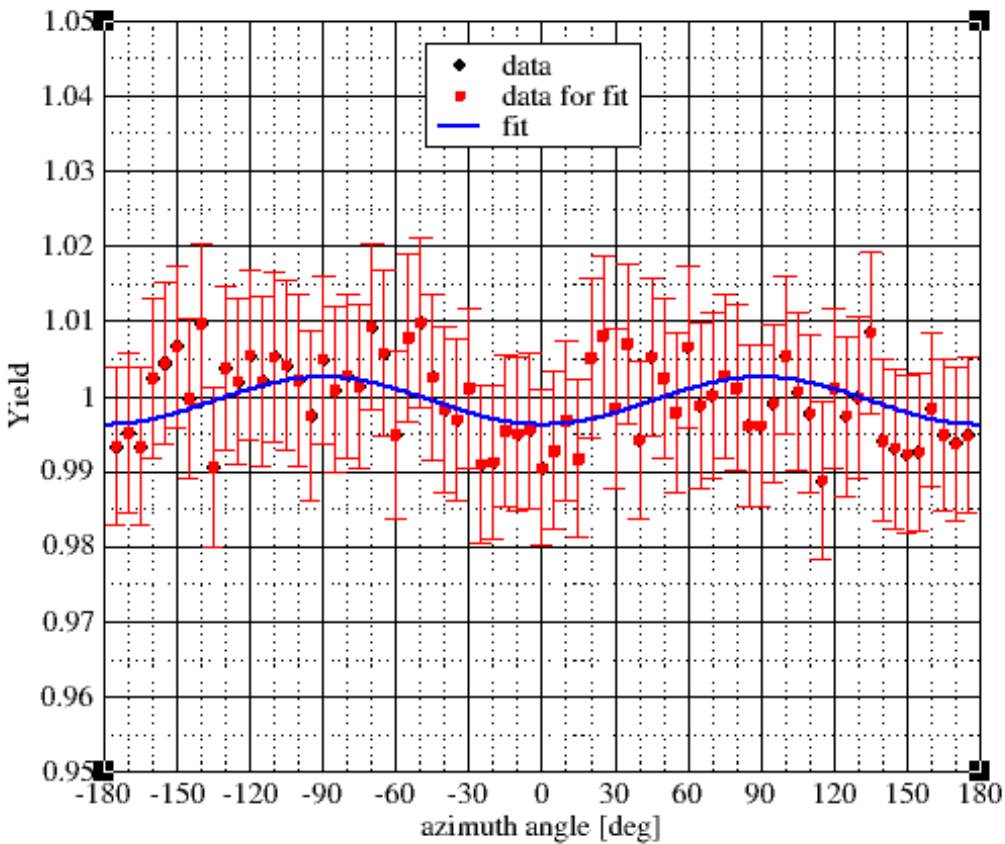
angular distribution coefficients:
A0 = +1.000000 A2 = +0.382060 A4 = -0.134187
[^^^ unattenuated]
A0 = +1.000000 A2 = +0.003313 A4 = -0.000000
[^^^ attenuated]

w plot in "w.xy"; try xmgrace w.xy -par w.par
linear polarization coefficients:

C2 = -0.001657 C4 = -0.000000

lnpol plot in "w_pol.xy"; try xmgrace w_pol.xy -par wlnpol.par
cos(2*azi) factor is -0.004389 (in 4pi)

158Er 334 keV 4+ \rightarrow 2+



chi**2: 0.216
a0: 0.999 +/- 0.001
a2: -0.003 +/- 0.002

```
calc_angdis linpol 4 2 2 3 0 4.0 E 70 110
alpha: _0 = +1.000000 _2 = +0.009995 _4 = +0.000000
----- li= 4.0
| L1= 2.0
| L1'= 3.0
| del= 0.000
----- lf= 2.0
```

angular distribution coefficients:

A0 = +1.000000 A2 = +0.510204 A4 = -0.367347
[^^^ unattenuated]

A0 = +1.000000 A2 = +0.005100 A4 = -0.000000
[^^^ attenuated]

w plot in "w.xy"; try xmgrace w.xy -par w.par

linear polarization coefficients:

C2 = -0.002550 C4 = -0.000000

linpol plot in "w_pol.xy"; try xmgrace w_pol.xy -par wlinpol.par
cos(2*azi) factor is -0.006755 (in 4pi)

Status now (as we see it)

method	source	in-beam	need source cal
ang dis	N/A	problem!	yes
ang cor	OK	OK ^a	no
lin-pol	OK ^b	OK ^c	no

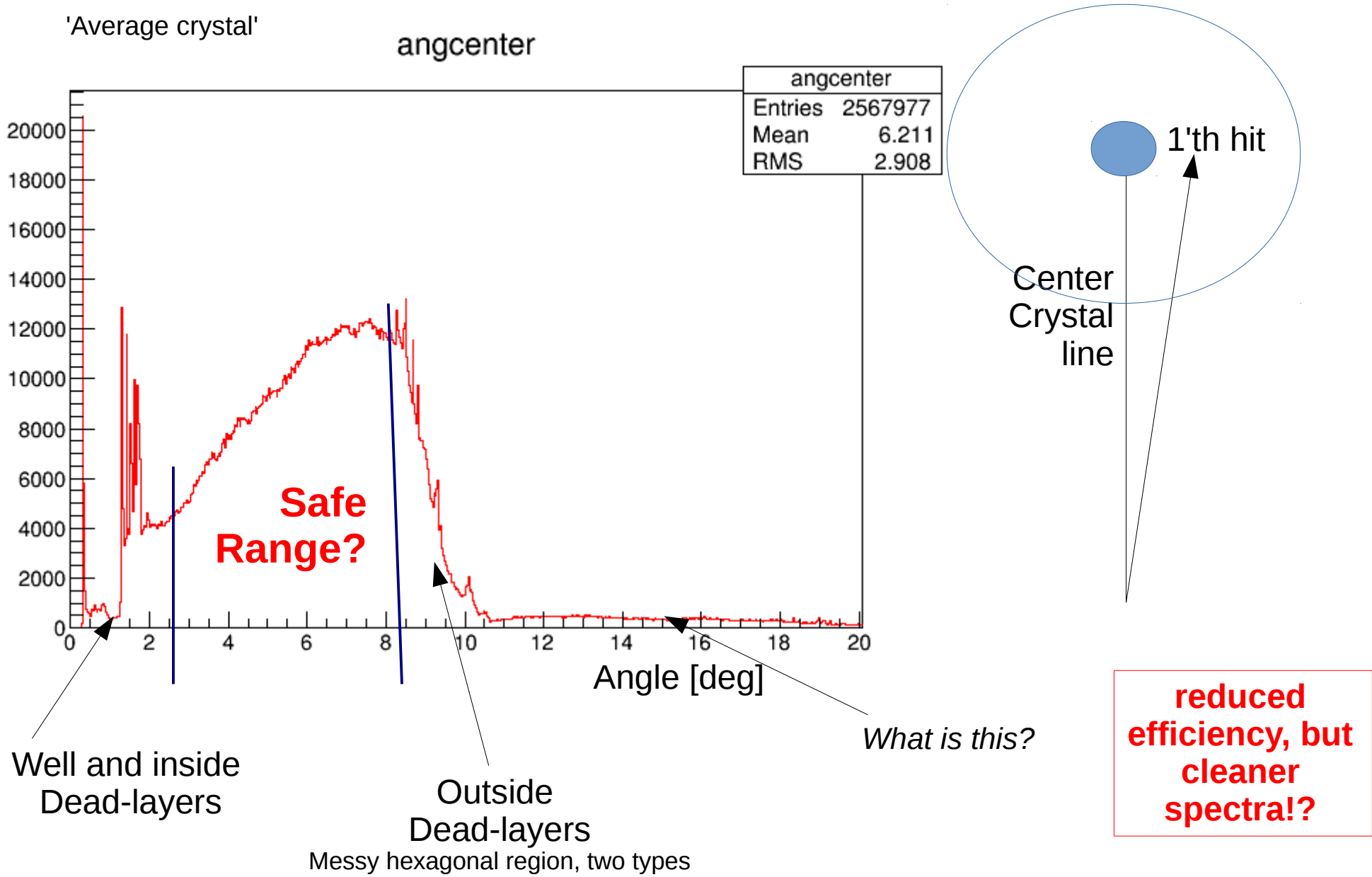
- ^a Using the new plane angle looks promising, but we need to verify.
- ^b Sign always seems right; but we need to work on calculating the amplitudes properly
- ^c Normalization seems to work: sign seems OK, but amplitudes are smaller than *expected* (why?)

Comment on in-beam ang dist

- As shown last time, the problem is that the interactions 'sees' the spaces between the crystals, the well in the crystals and the dead layers on the side
- The interaction in the dead layers and front&well *depends on the energies in a complicated way* making it difficult to produce a good response spectrum with a source.
- We suggest **making masks in azimuth and polar angles that blocks out the dead layers (and other areas)** might solve the problem.
- **Simply find the angle of the first-hit direction to the center of the crystal it hit. Impose min angle to exclude the well and max angle to exclude the surface of the crystal**

↑
Already coded; but not yet tested

First hit angle-to-center analysis



Conclusions

- We still have problems with the in-beam **angular distribution**; but we have some ideas
- For the source and in-beam **angular correlations**, we have things under control
- For the source and in-beam **linear polarizations**, **we can now normalize with the data itself**. The signs are always understood, but understanding and calculating the amplitudes needs more work (always 'calculate' at least for sources)
- We need to work on AGATA data too
- **Need to understand background subtraction better**

This presentation was produced the old fashioned way without the use of AI or ML

Thank you to **Shoufei** and **Dirk** for producing the high statistics GRETINA datasets we used

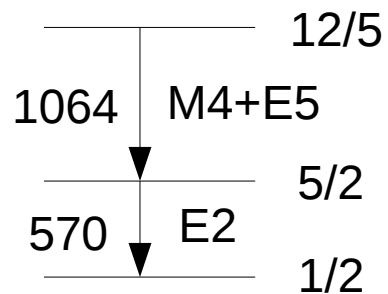
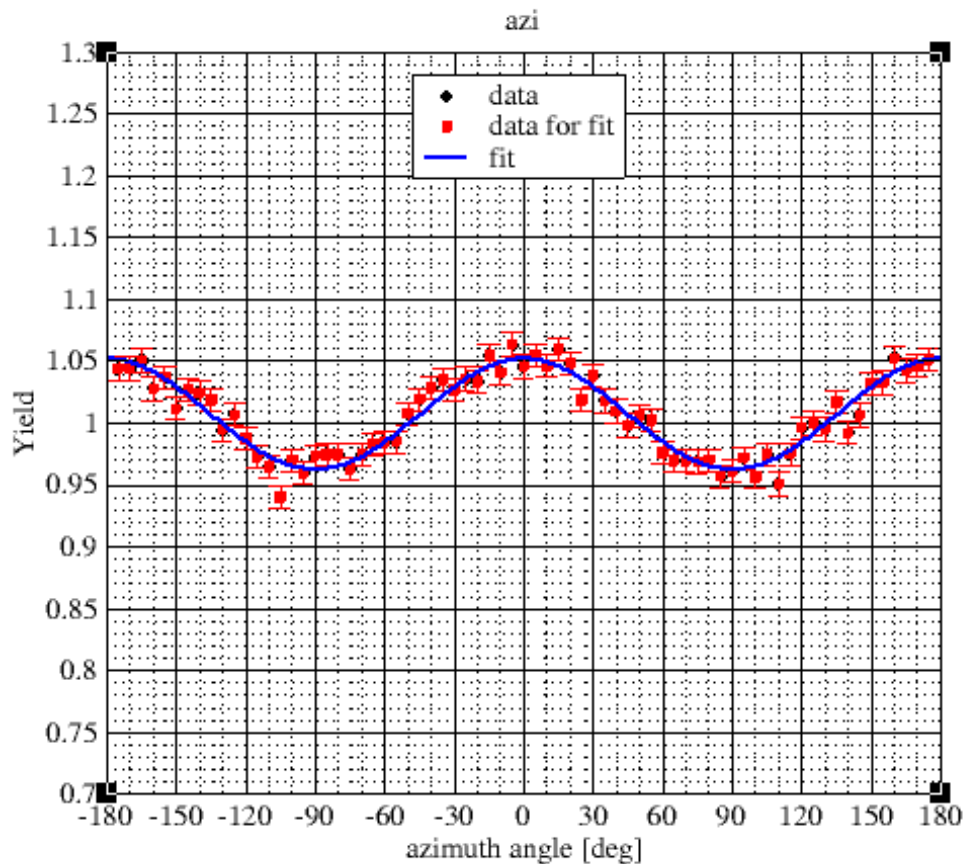
Note added after presentation

- Preliminary investigations show that **the gating on the 'pristine ge', avoiding the dead-layers and the well, does not really help!**
- **That fact** indicates that **the dead-layers, and their possible energy dependence, cannot explain the problem with the angular distributions.**
- **That realization is progress in itself**
- Further investigations are ongoing before the final conclusion

extras

²⁰⁷Bi source; 570 E2 line

In case ENSDF is right and we are wrong about the delta2



Polarization spectrum for the 570 keV E2 when polarized by the 1064 keV M4+E5

13/2(4)5/2(2)1/2

calc_a0a2a4 linpol 6.5 2.5 0.5 4 5 0.02 2 3 0 E 70 110

----- li= 6.5

| L1= 4.0
| L1'= 5.0
| del= 0.020

----- l= 2.5

| L2= 2.0
| L2'= 3.0
| del= 0.000

----- lf= 0.5

angular correlation coefficients:

A0 = +1.000000 A2 = +0.213305 A4 = -0.014544 A6 = +0.000000

w plot in "w.xy"; try xmgrace w.xy -par w.par

linear polarization coefficients:

C2 = +0.106653 C4 = +0.001212 C6 = +0.000000

linpol plot in "w_pol.xy"; try xmgrace w_pol.xy -par wlinpol.par

cos(2*azi) factor is +0.281076 (in 4pi)

chi**2: 1.105
a0: 1.007 +/- 0.001
a2: 0.045 +/- 0.002

Still same sign!